

# Coulomb Excitation Studies at TRIUMF and FRIB



SSNET 2024

Orsay, France

11/5/2024

Daniel Rhodes



# Outline

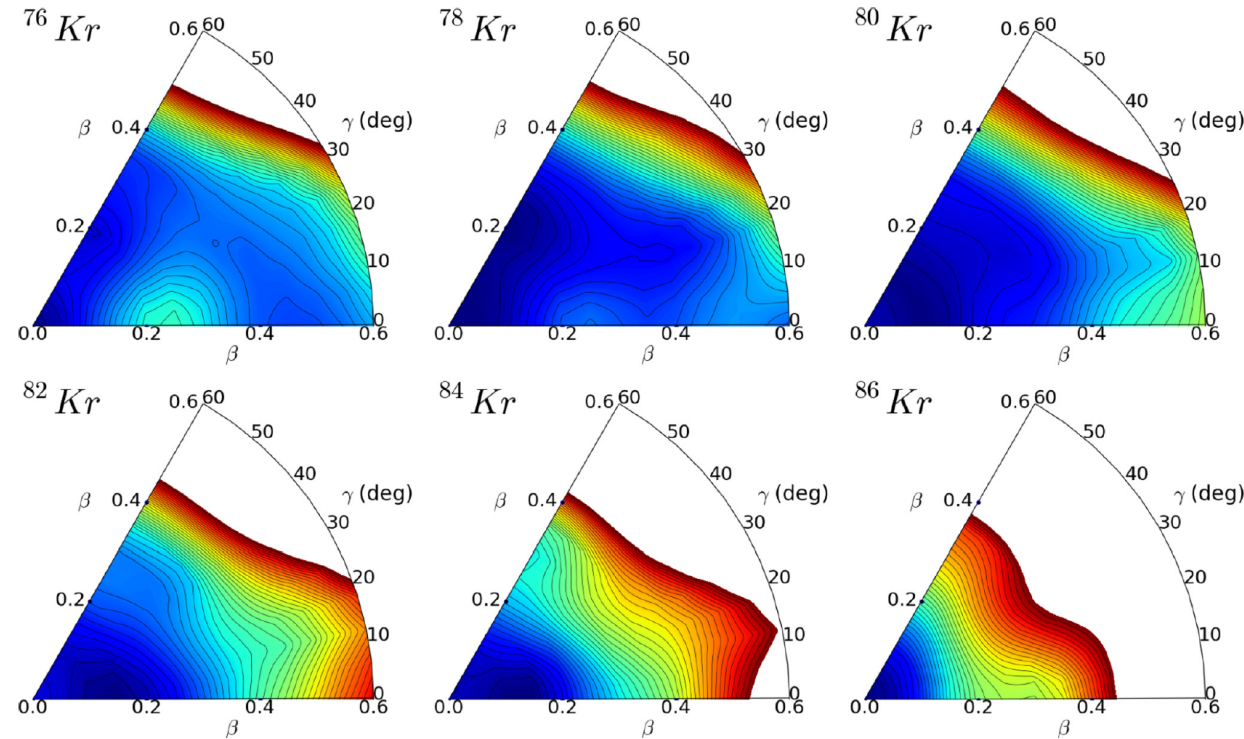
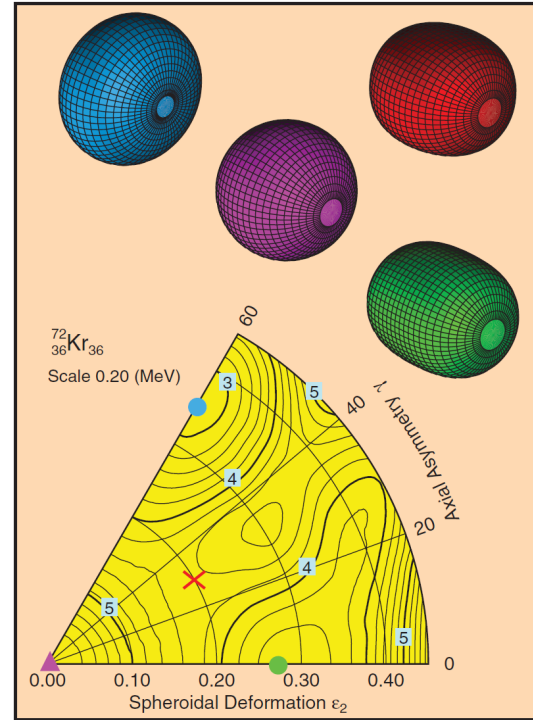
- Coulomb Excitation of  $^{78}\text{Kr}$  (TRIUMF)
  - Motivation
  - Experiment
  - Data Analysis
  - Results and Outlook
- Coulomb Excitation at FRIB (brief)
  - Current status
  - Future plans

# Coulomb Excitation of $^{78}\text{Kr}$



# Nuclear Structure in the Krypton Isotopes

- Shape coexistence in neutron-deficient isotopes
  - Isomerism in  $N=Z=36$   $^{72}\text{Kr}$
- Shape changes along the isotopic chain
  - Evolution between various symmetries
  - $^{82}\text{Kr}$  suggested as E(5) CPS

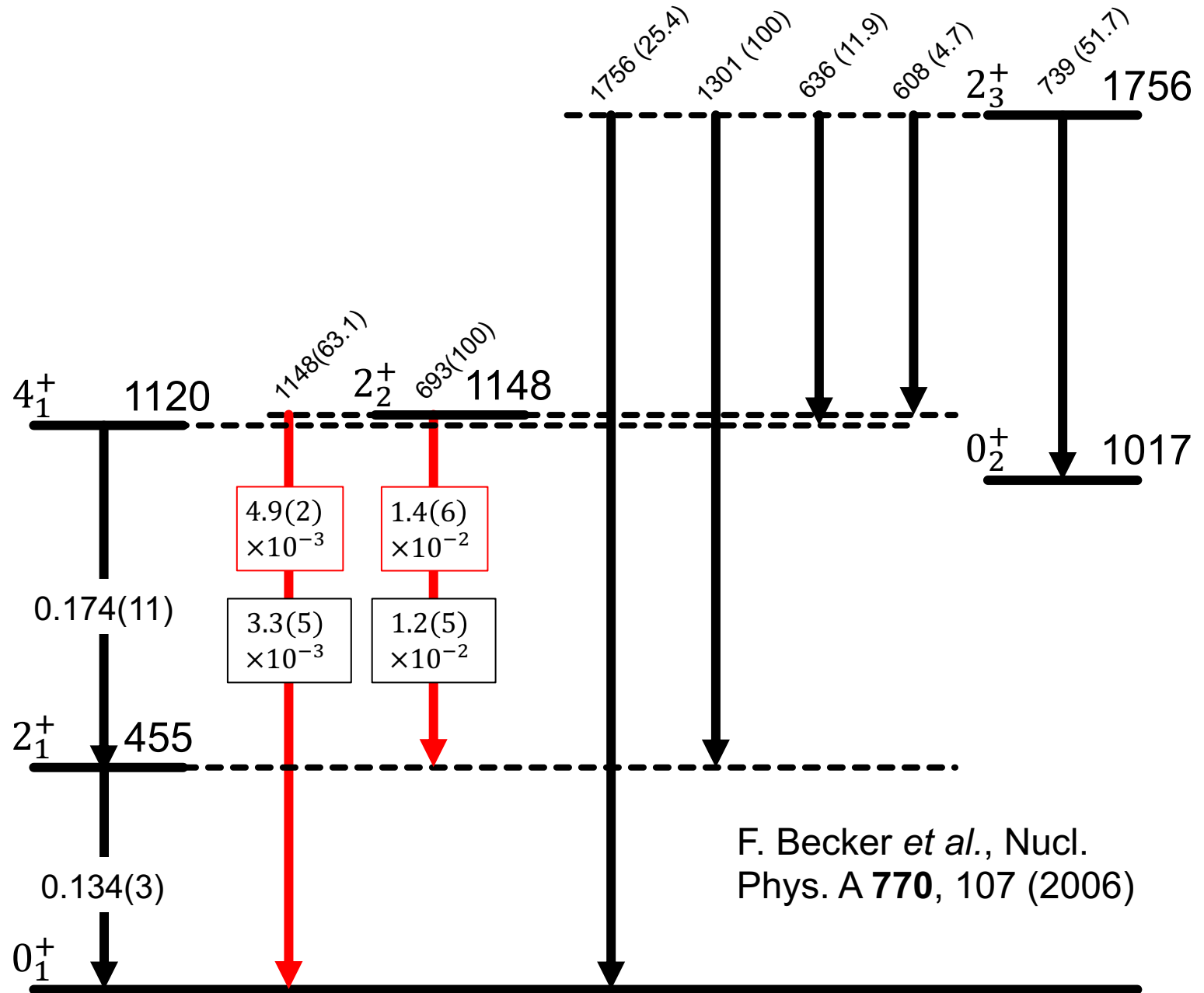


P. Moller *et al.*,  
Phys. Rev. Lett. **103**, 212501 (2009)

K. E. Karakatsanis and K. Nomura, Phys.  
Rev. C **105**, 064310 (2022)

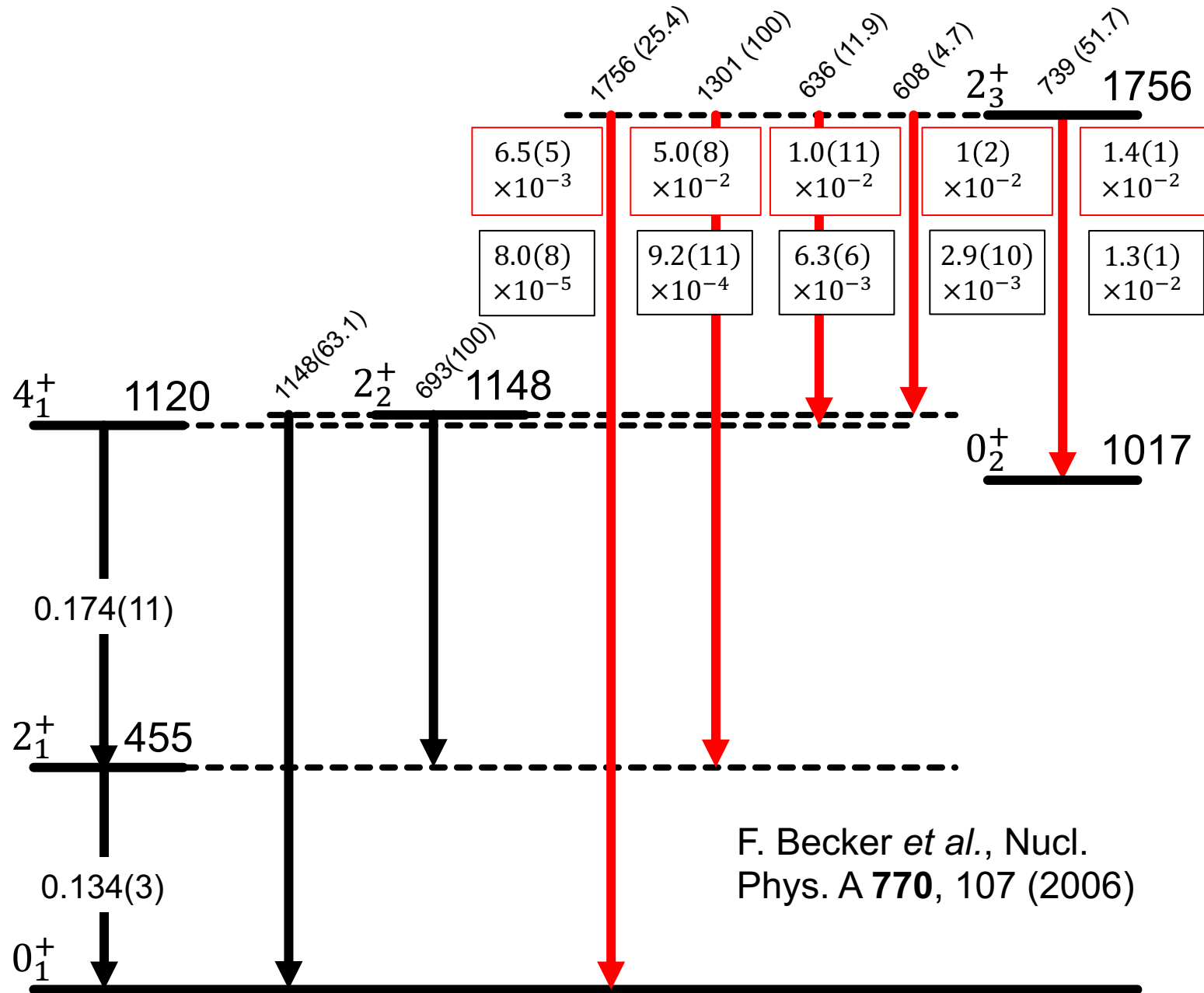
# Motivation for $^{78}\text{Kr}$

- CoulEx measurement by **Becker *et al*** inconsistent with decay data
  - Measured Q moments for first time



# Motivation for $^{78}\text{Kr}$

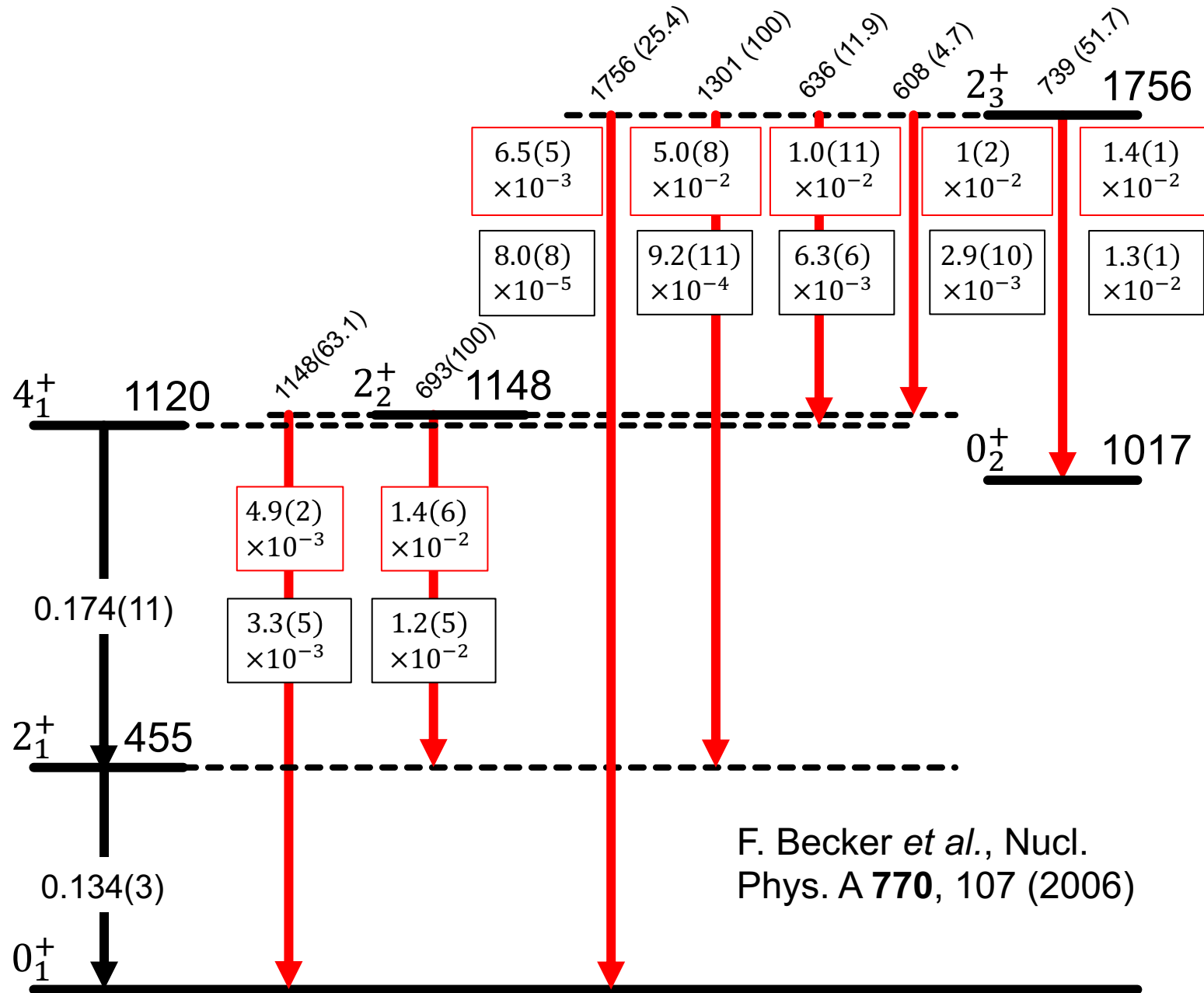
- CoulEx measurement by **Becker *et al*** inconsistent with decay data
  - Measured Q moments for first time
- $2_3^+$  state highly discrepant
  - Lifetime and branching ratios in doubt





# Motivation for $^{78}\text{Kr}$

- CoulEx measurement by **Becker *et al*** inconsistent with decay data
  - Measured Q moments for first time
- $2_3^+$  state highly discrepant
  - Lifetime and branching ratios in doubt
- Proposed band structure based on these results
- Relevant for intrinsic shape parameters



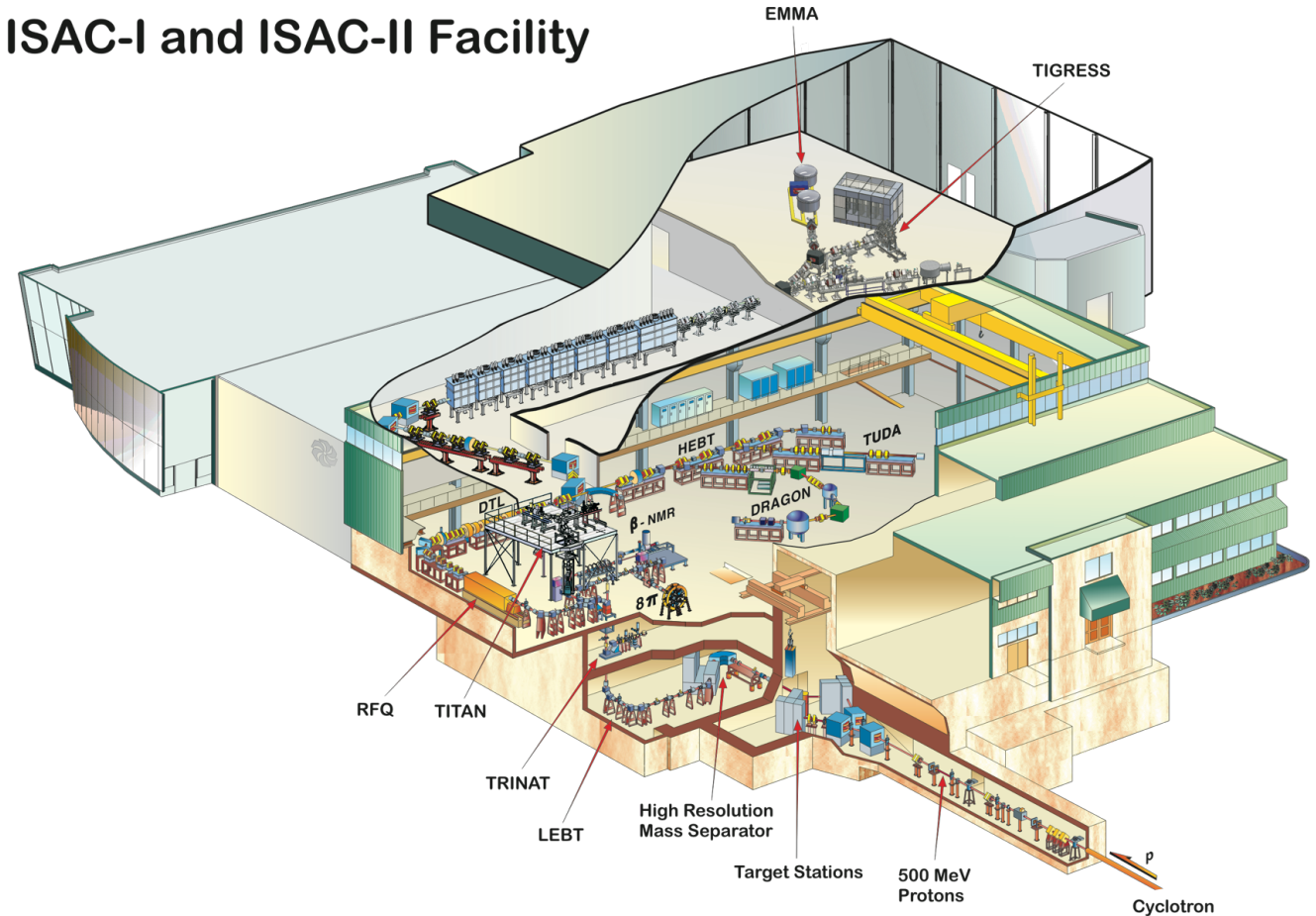
# Experimental Details



# Experiment Overview

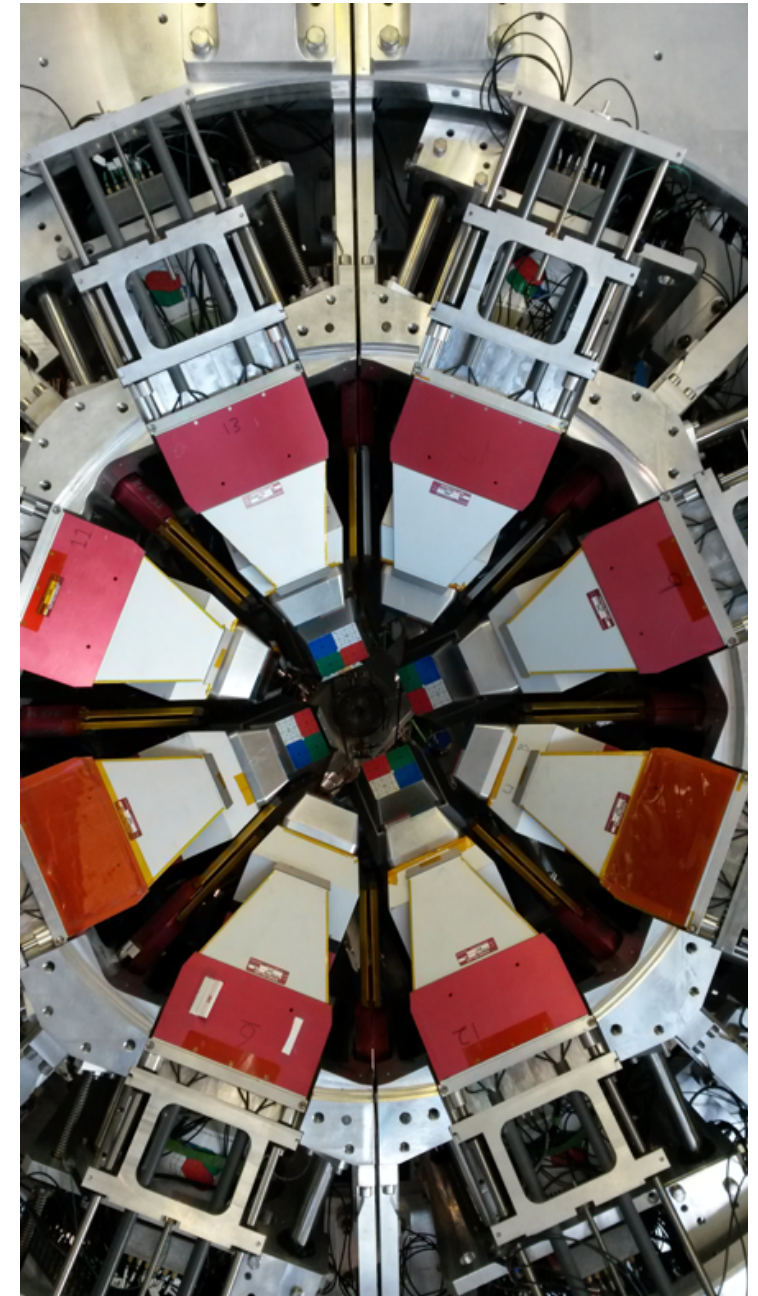
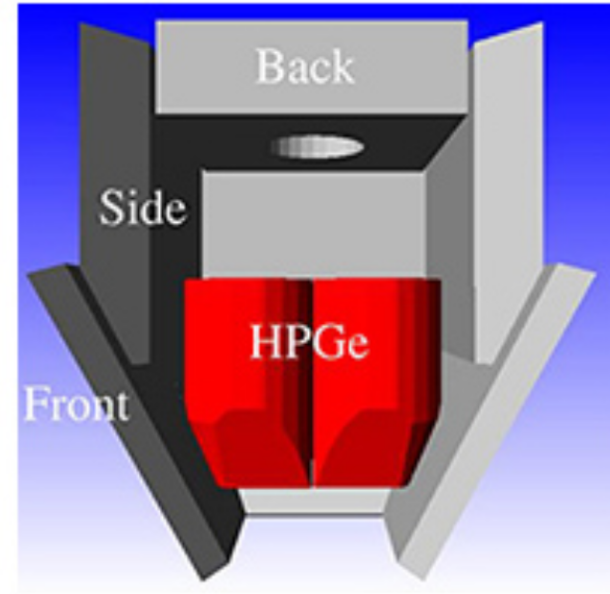
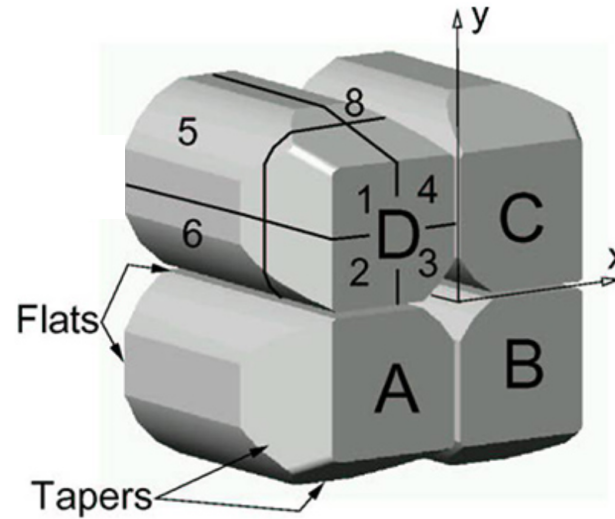
- Experiment was performed at the ISAC-II facility of TRIUMF August 2023
  - Located in Vancouver, BC
  - ISOL RIB Facility
- $^{78,84,86}\text{Kr}$  Off-line ion-source beams
  - Cyclotron not used for stable Kr
- $^{78}\text{Kr}$  delivered to experimental setup at 4.25 MeV/u
  - $^{194,196}\text{Pt}$  and  $^{208}\text{Pb}$  reaction targets

## ISAC-I and ISAC-II Facility



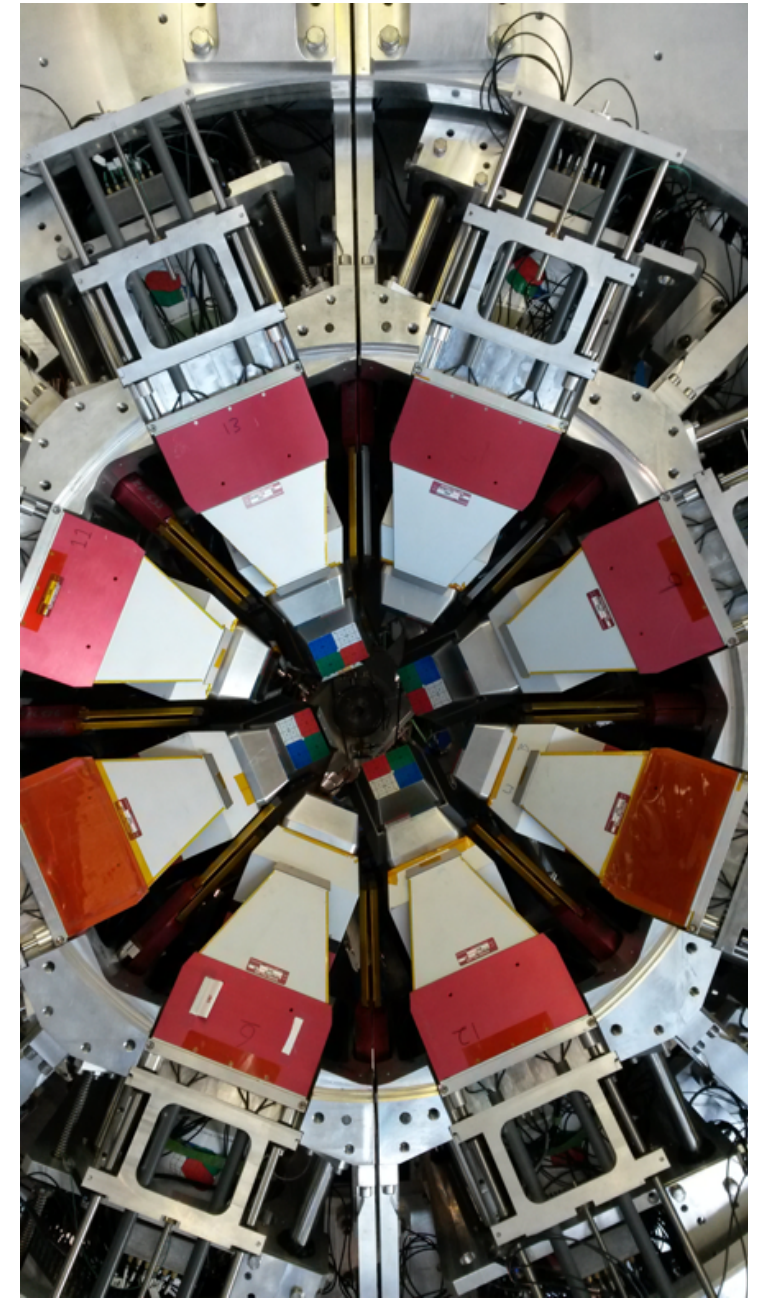
# Experimental Setup

- TRIUMF-ISAC Gamma-ray Escape Suppressed Spectrometer (TIGRESS)
  - 16 Compton-suppressed clovers
  - Four 8-fold segmented crystals per clover
  - Two array configurations



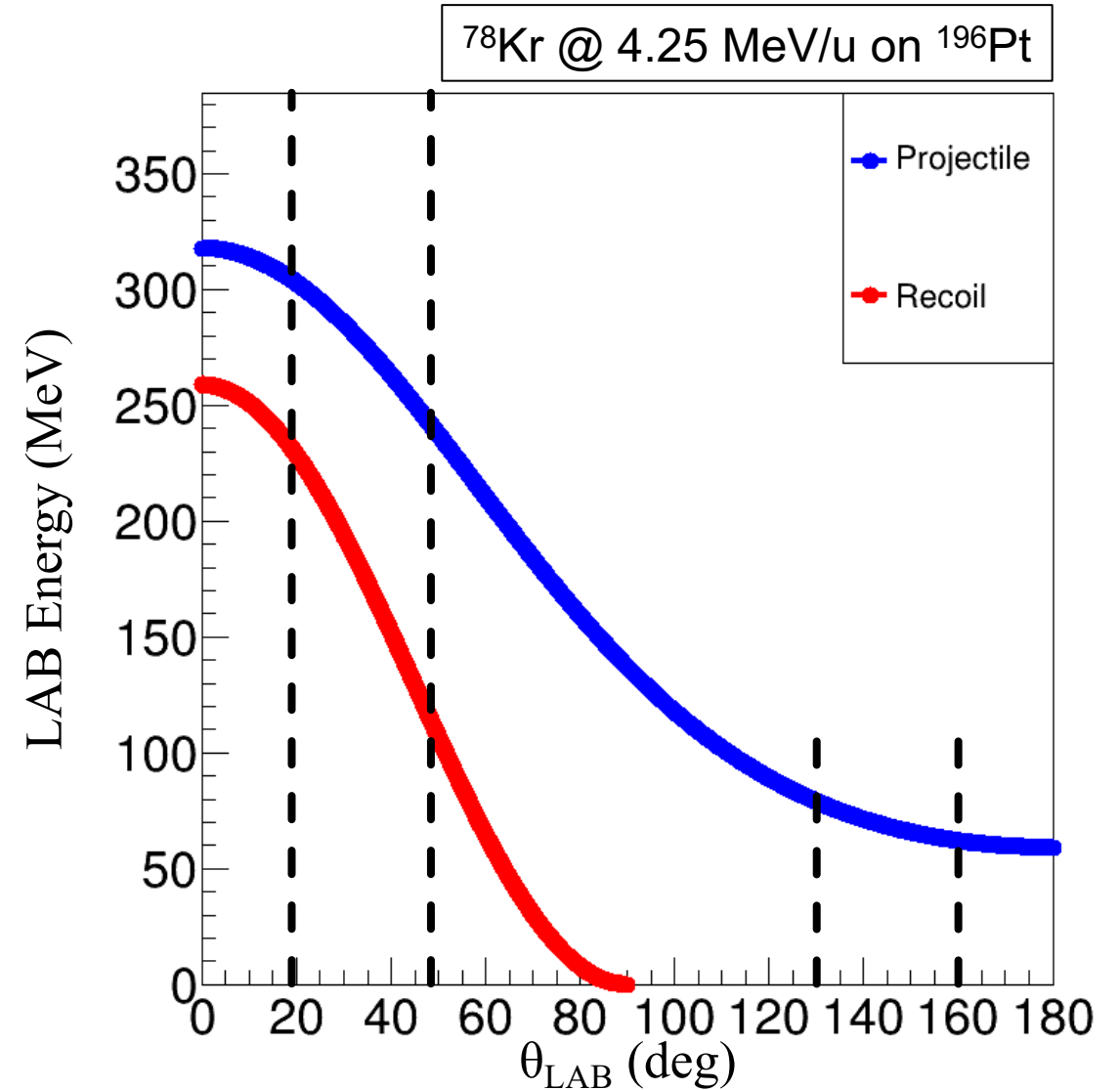
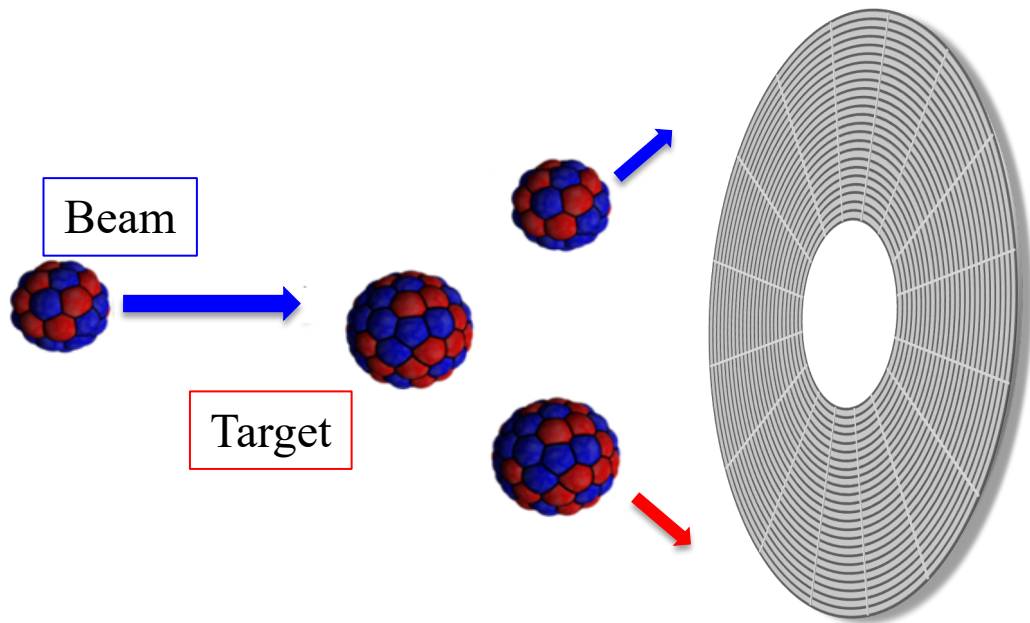
# Experimental Setup

- TIGRESS
  - 16 Compton-suppressed clovers
  - Four 8-fold segmented crystals per clover
  - Two array configurations
- Bambino
  - Two S3 detectors, each 3 cm from target
  - 4 target positions
- Position information from detector segmentation
  - Doppler correction
  - CoulEx analysis



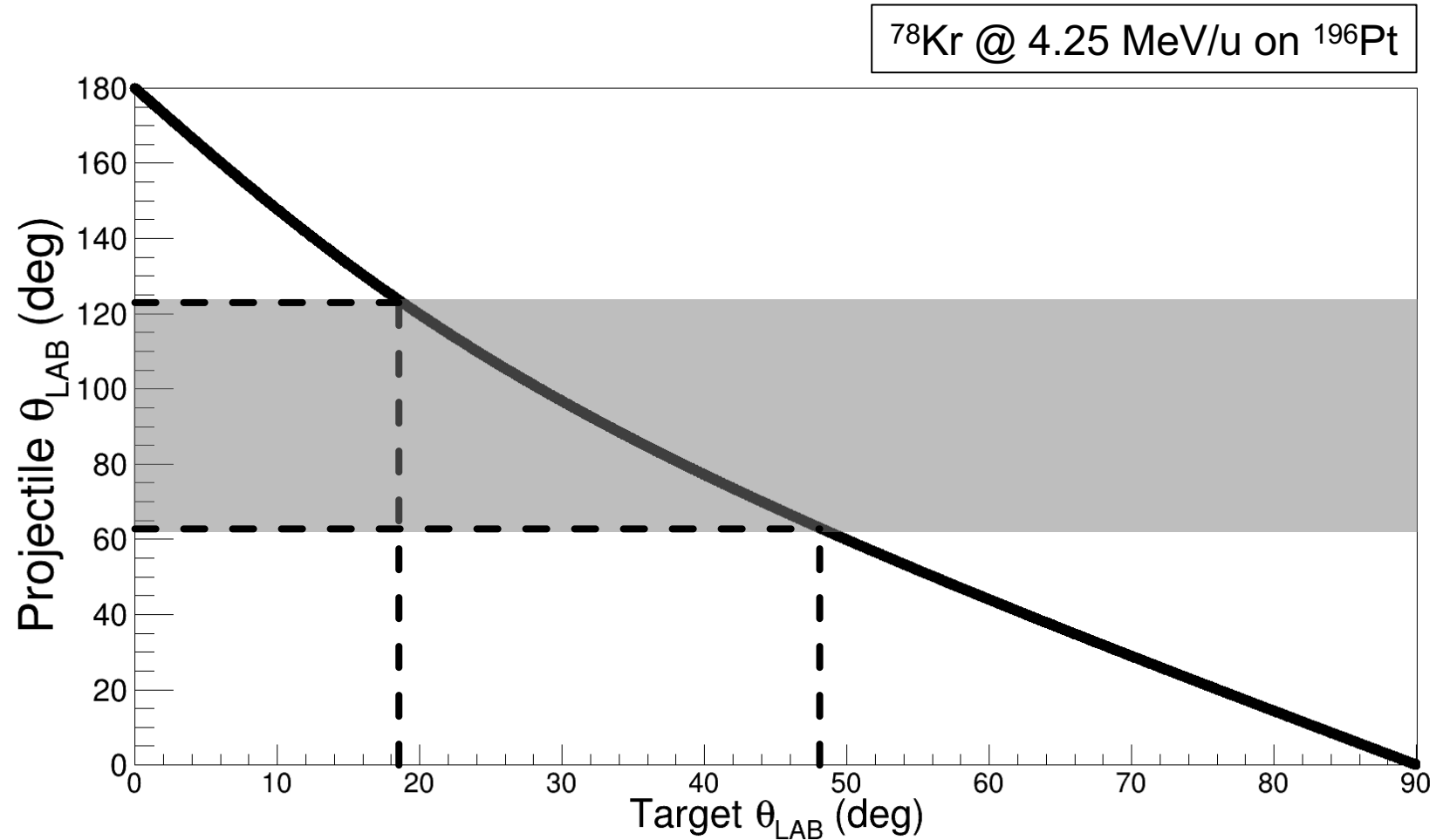
# Particle Detection Scheme

- Kinematic curves provide particle discrimination
  - Forward detector only
- Only 30% of  $4\pi$  physically covered



# Kinematic Reconstruction

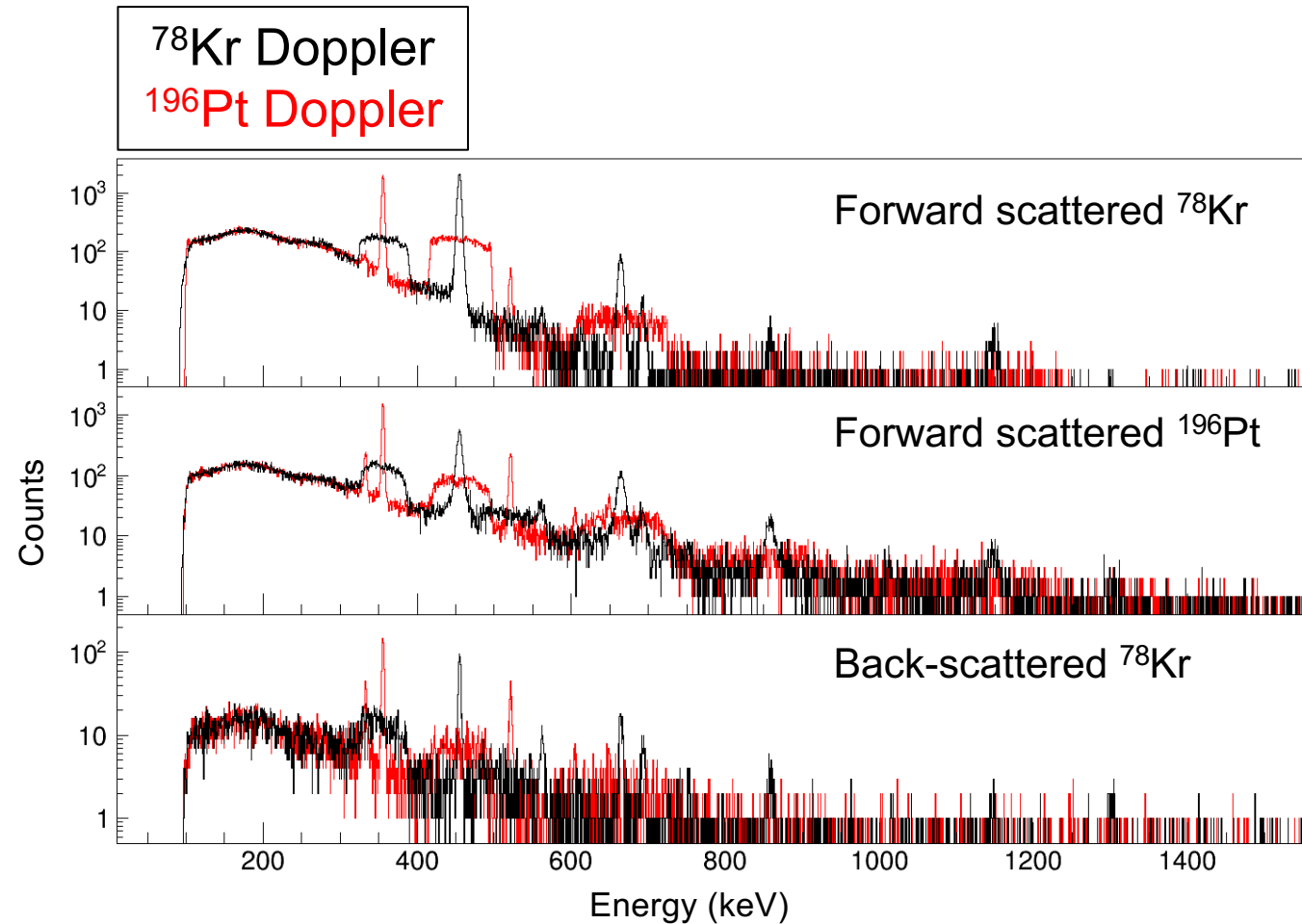
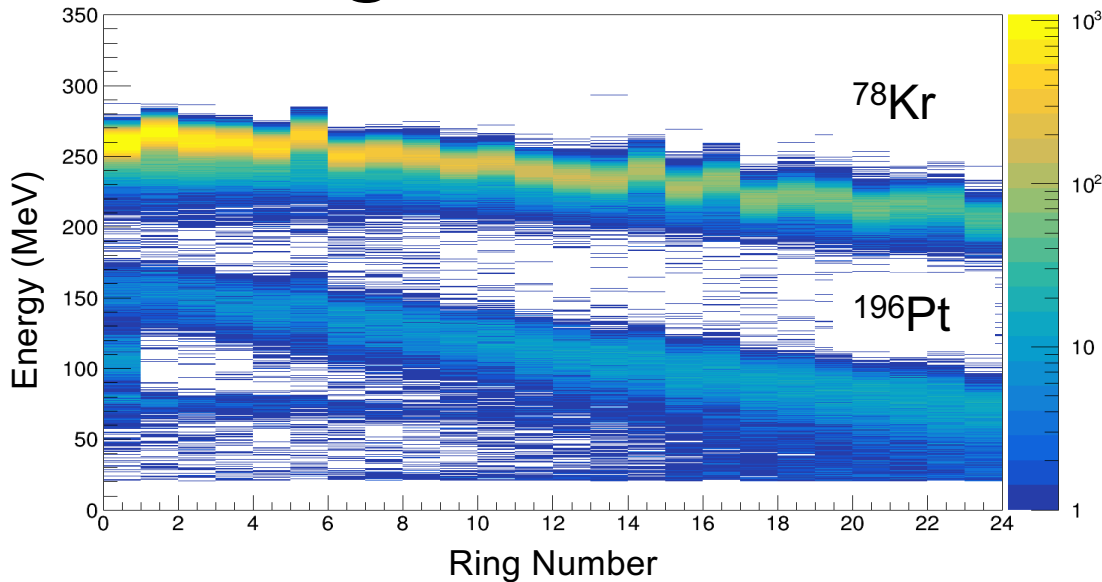
- Reconstruct undetected projectiles scattered near  $90^\circ$  from detected target
- Gain coverage from  $62^\circ - 123^\circ$   
– 51% of  $4\pi$
- 30%  $\rightarrow$  81% of  $4\pi$



# Experimental Spectra I

- $^{194,196}\text{Pt}$  to measure  $B(E2; 2_1^+ \rightarrow 0_1^+)$ 
  - Normalize to target excitations
  - Reduces systematics

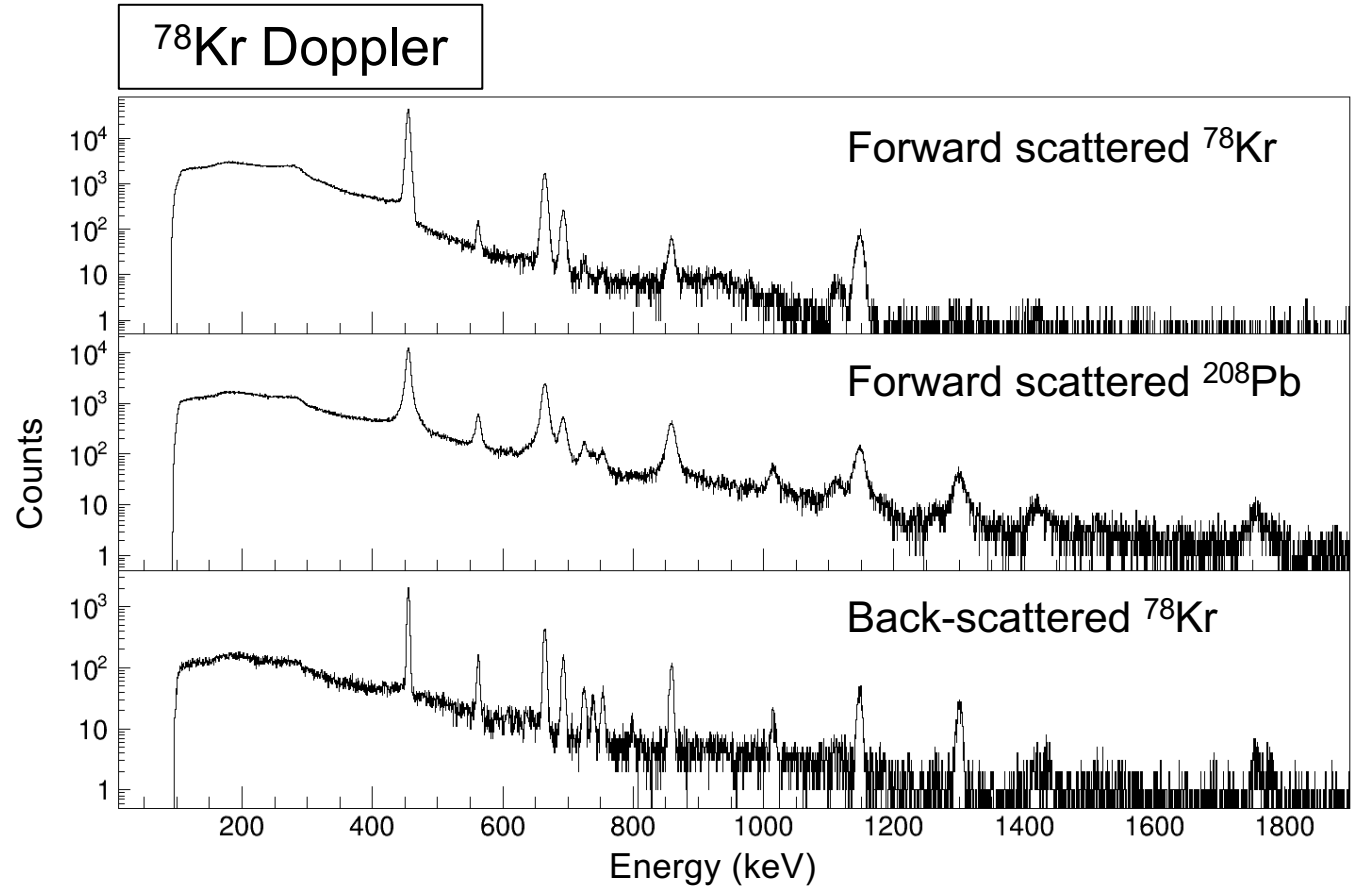
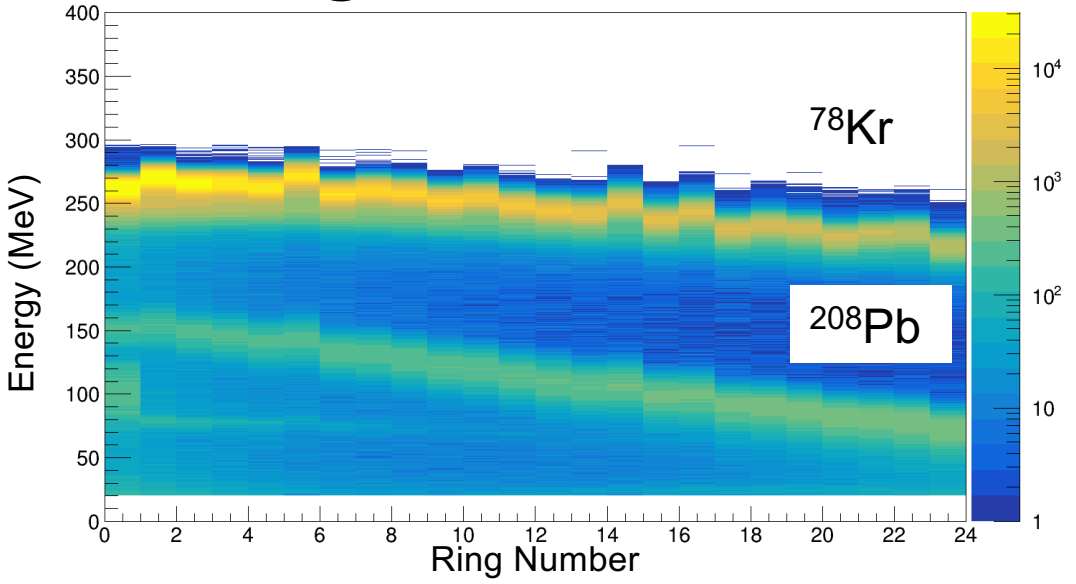
$^{78}\text{Kr}$  @ 4.25 MeV/u on  $^{196}\text{Pt}$



# Experimental Spectra II

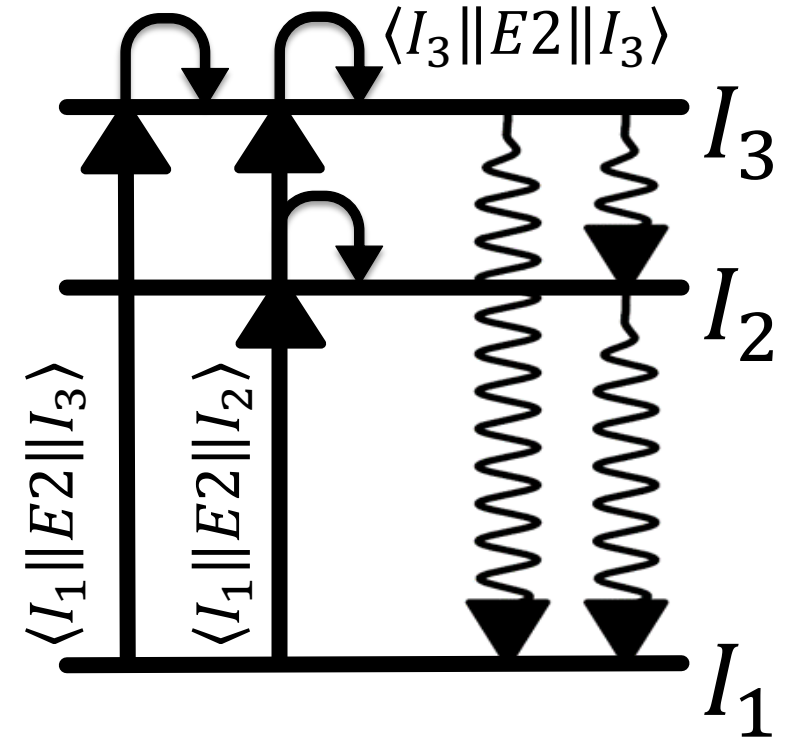
- $^{208}\text{Pb}$  target provides exceptionally clean spectra
  - No target excitations
  - Higher statistics (more time)

$^{78}\text{Kr}$  @ 4.25 MeV/u on  $^{208}\text{Pb}$



# Extracting Matrix Elements with GOSIA

- Many excitation and de-excitation pathways
  - Large network of coupled differential equations
- GOSIA Coulomb excitation code was used
  - Calculates excitation and subsequent decay pattern
  - Fits experimental gamma-ray yields
  - Matrix elements used as parameters in a multi-dimensional least-squares search
- Produces set of best-fit matrix elements
  - Statistical error estimation also possible



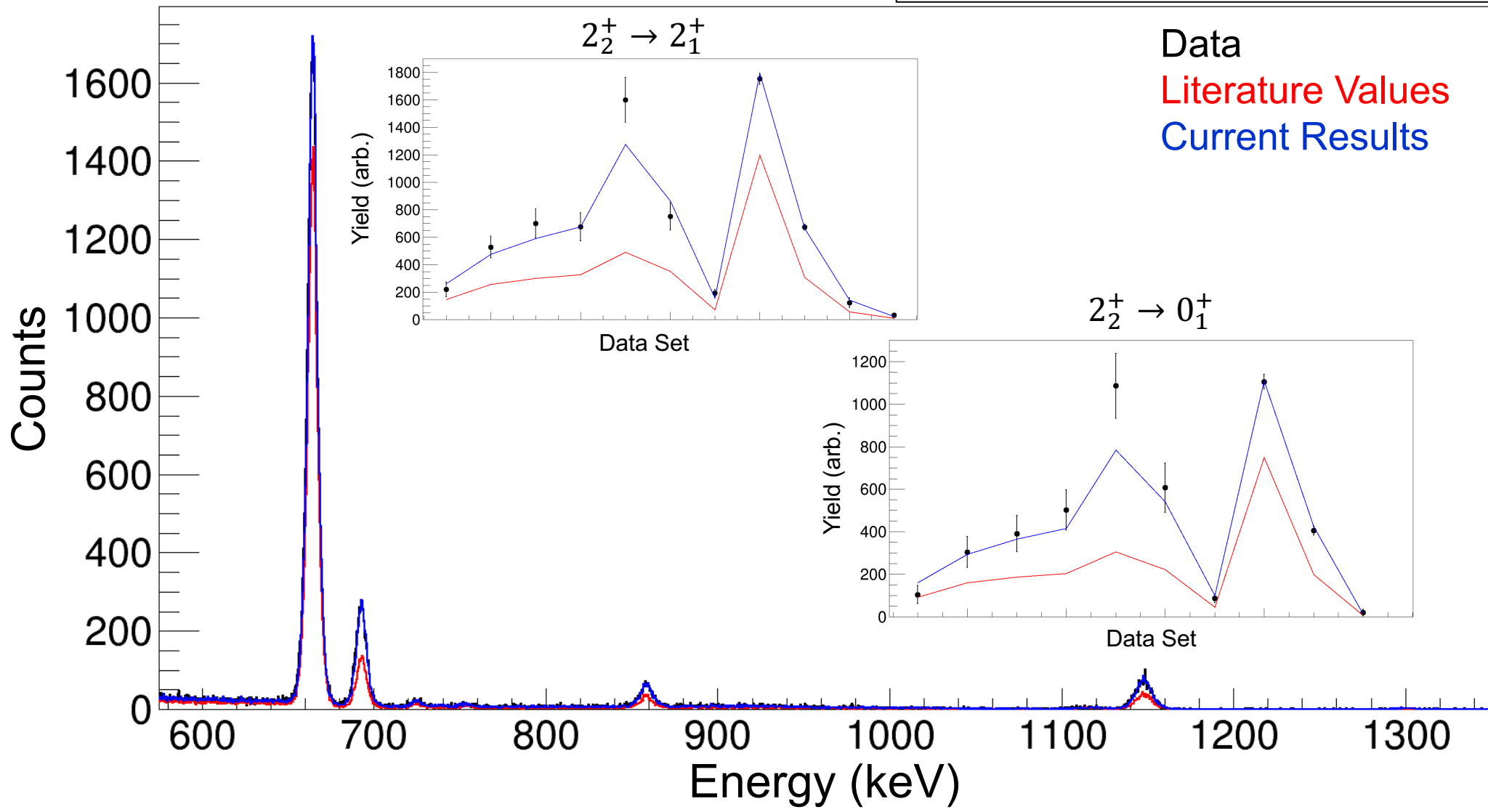
$$i\hbar \frac{d}{dt} a_n(t) = \sum_m \langle n | V(t) | m \rangle \exp [i (E_n - E_m) t / \hbar] a_m(t)$$

$$P_n = a_n a_n^*$$



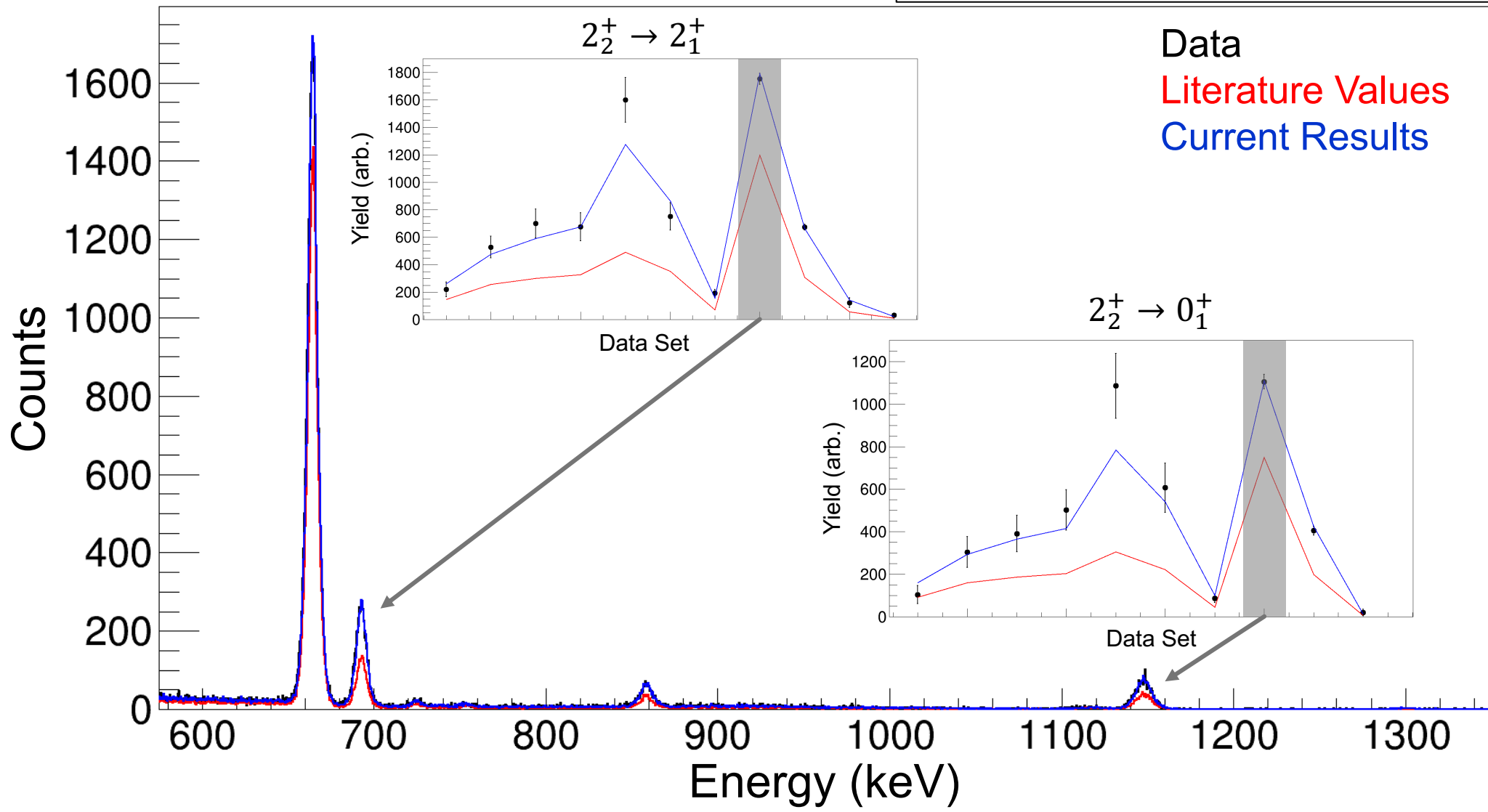
# Yield Reproduction I

$^{78}\text{Kr}$  on  $^{208}\text{Pb}$ ,  $^{78}\text{K}$  Forward Scattered



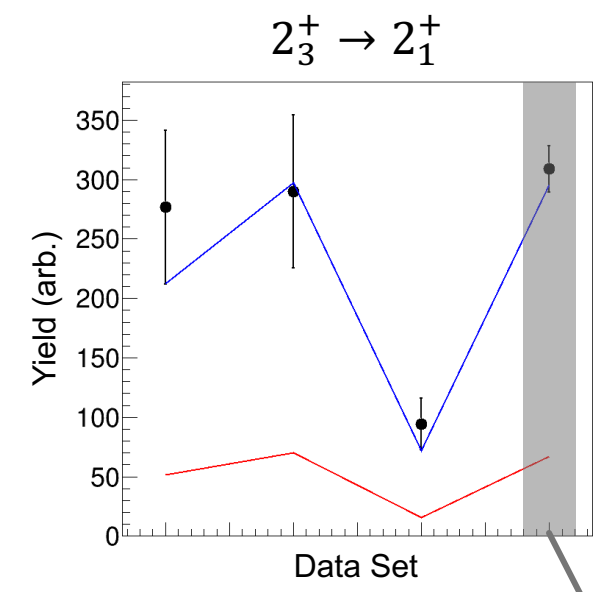
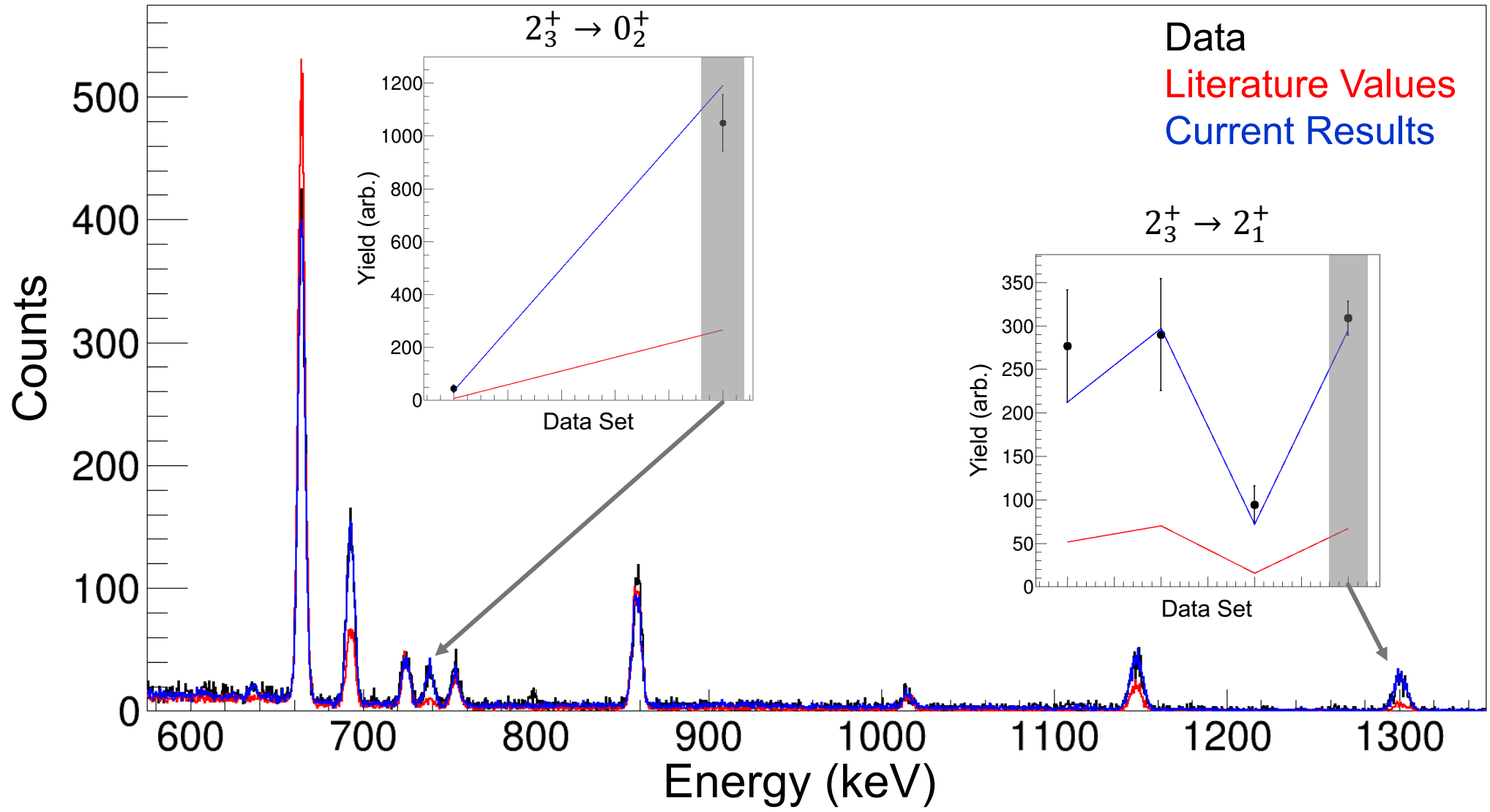
# Yield Reproduction I

$^{78}\text{Kr}$  on  $^{208}\text{Pb}$ ,  $^{78}\text{K}$  Forward Scattered



# Yield Reproduction II

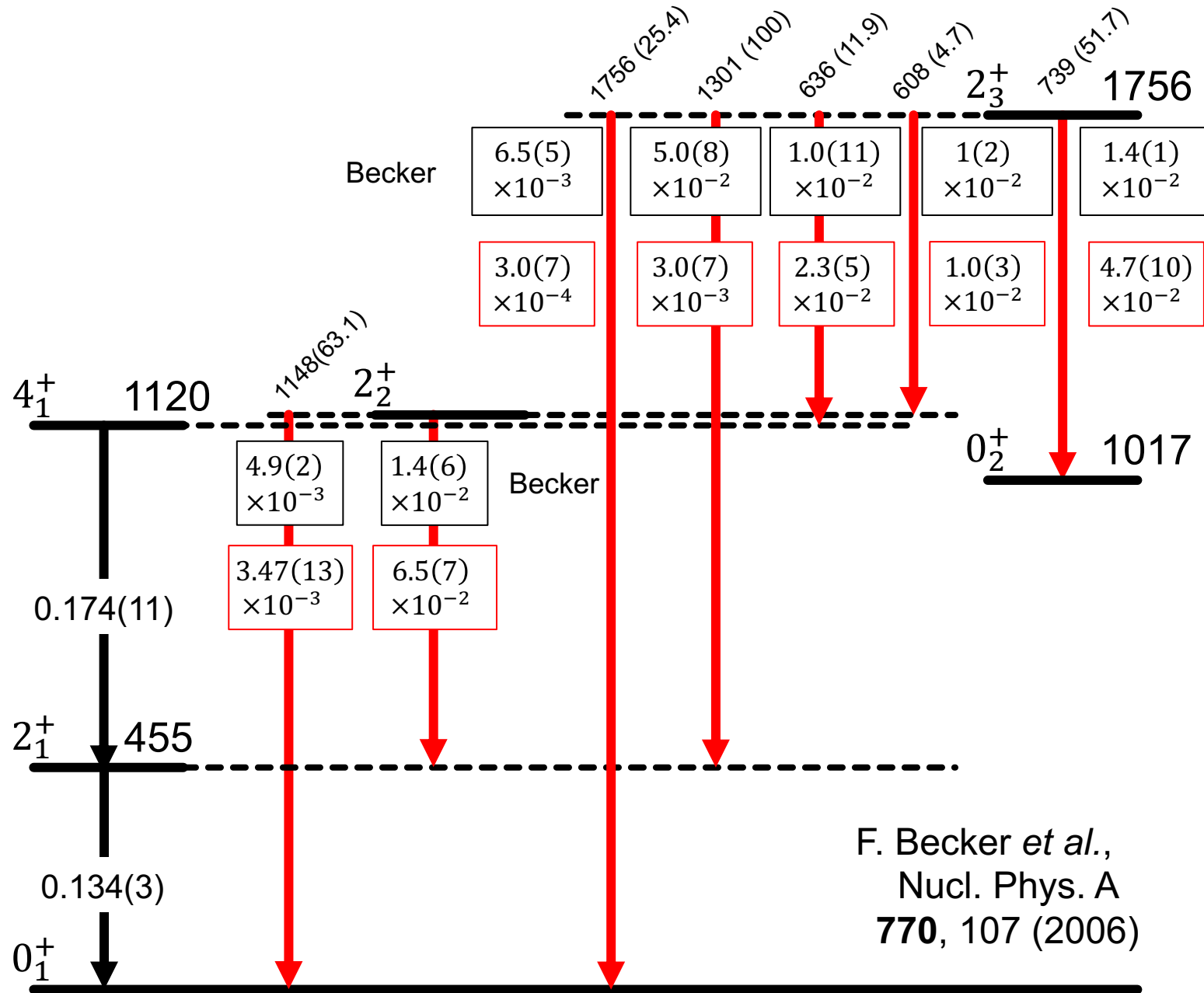
$^{78}\text{Kr}$  on  $^{208}\text{Pb}$ ,  $^{78}\text{K}$  Backscattered



# Results and Outlook

# Results I

- Transition strengths almost all different from Becker et al.
- All branching ratios agree nicely with adopted values (decay data)
- $2_2^+$  lifetime agrees with adopted value
- $2_2^+$  mixing ratio is discrepant —  $0.45(10)$  vs  $4_2^{30}$

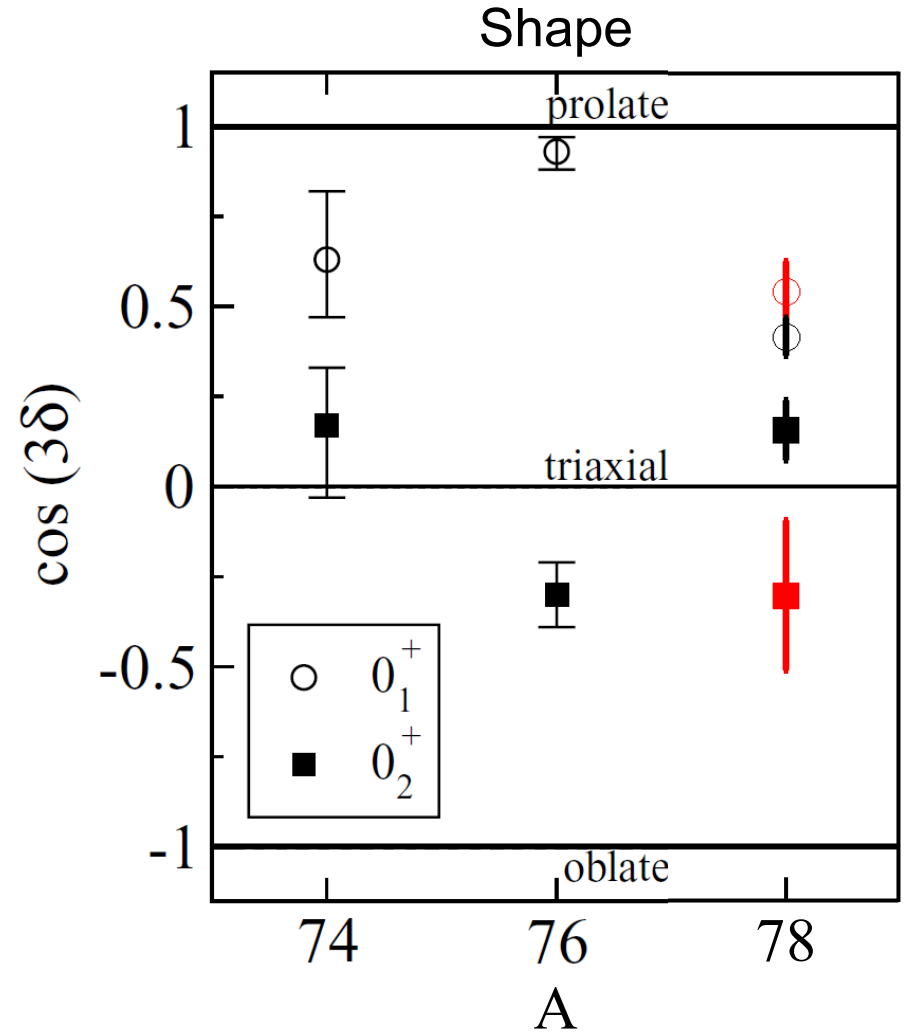
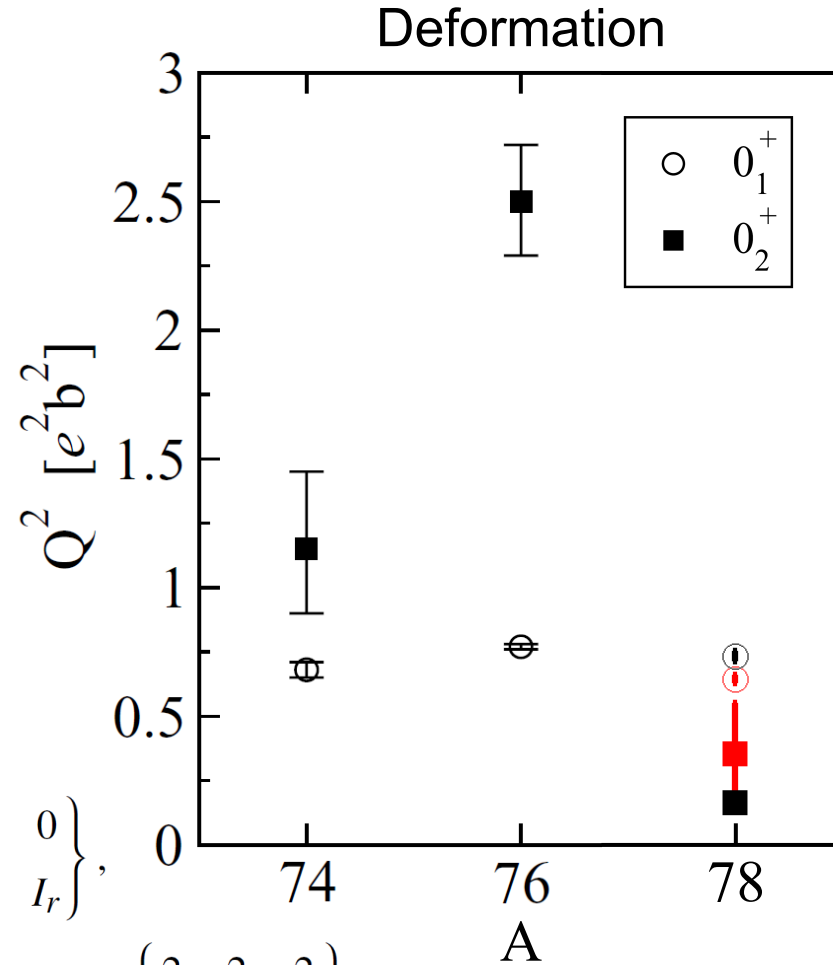


# Shape Parameters

- Shape parameters extracted for  $0^+$  states.
- Small deformations
- Different shapes
  - Largely due to sign of  $2_1^+$  and  $2_3^+$  quadrupole moments

$$\langle Q^2 \rangle = \sqrt{5} \frac{(-1)^{2I_s}}{\sqrt{2I_s+1}} \sum_r M_{sr} M_{rs} \begin{Bmatrix} 2 & 2 & 0 \\ I_s & I_s & I_r \end{Bmatrix},$$

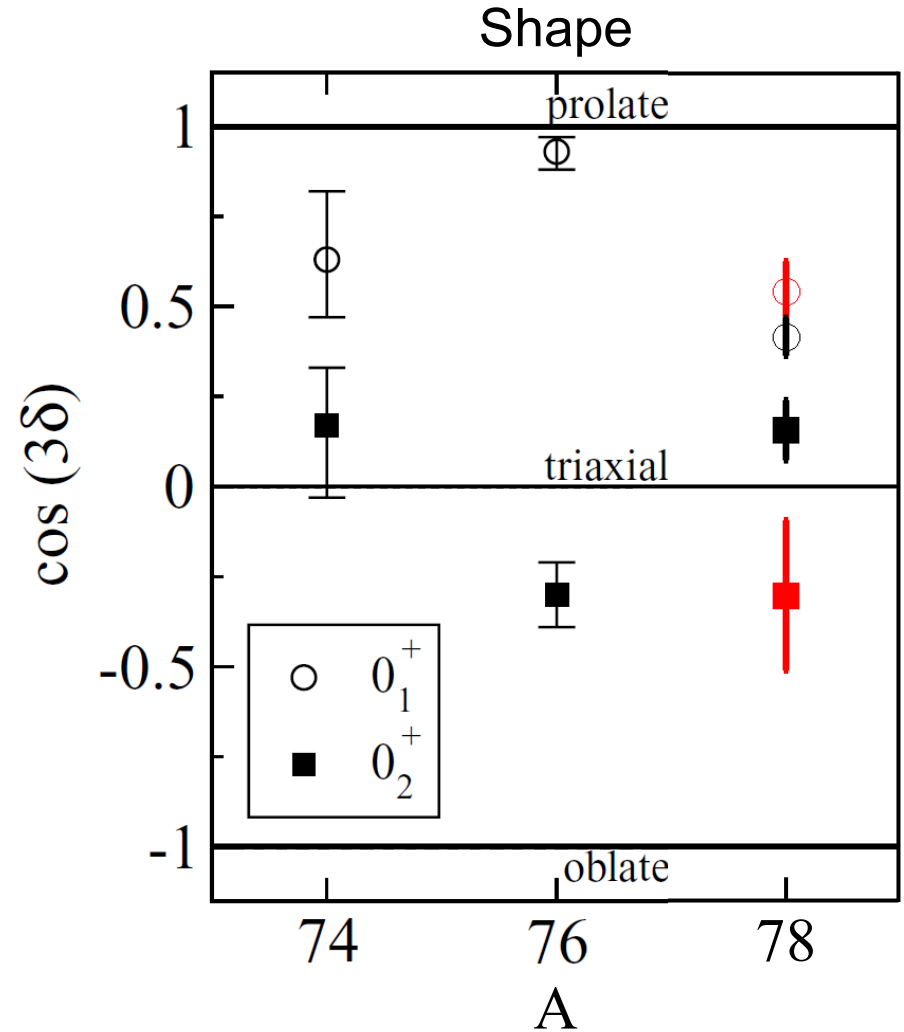
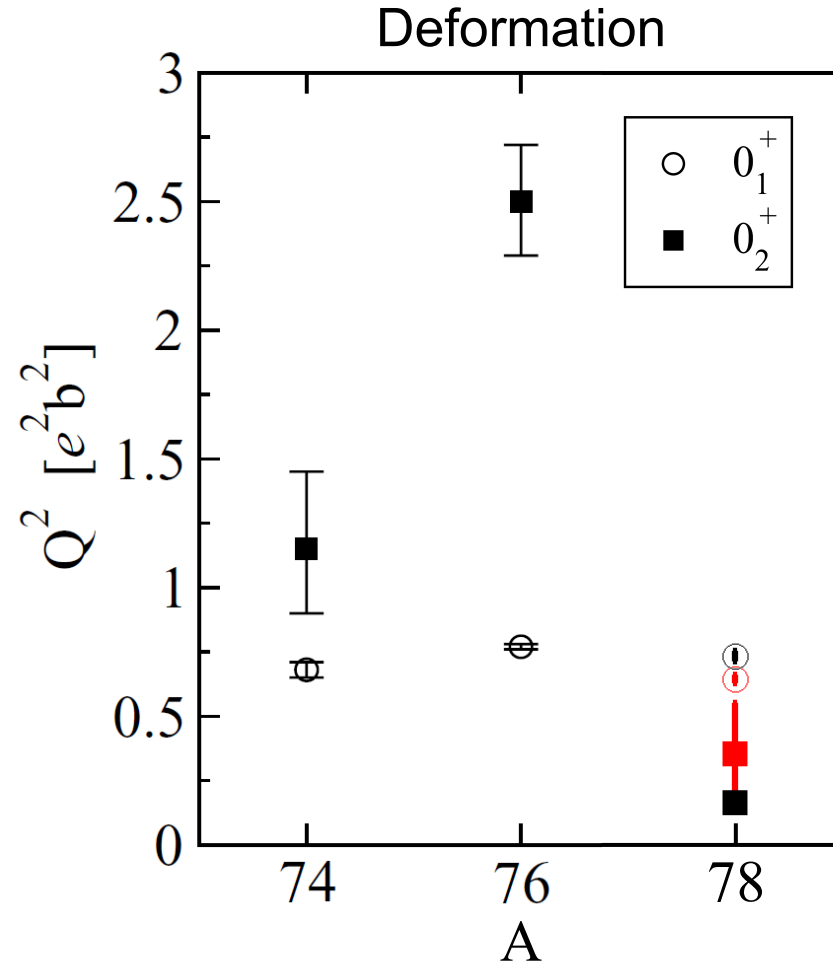
$$\langle Q^3 \cos(3\delta) \rangle = \frac{\sqrt{35}}{\sqrt{2}} \frac{(-1)^{2I_s+1}}{2I_s+1} \sum_{tu} M_{su} M_{ut} M_{ts} \begin{Bmatrix} 2 & 2 & 2 \\ I_s & I_t & I_u \end{Bmatrix}.$$



E. Clement *et al.*, Phys. Rev. C **75**, 054313 (2007)

# Shape Parameters

- Shape parameters extracted for  $0^+$  states.
- Small deformations
- Different shapes
  - Largely due to sign of  $2_1^+$  and  $2_3^+$  quadrupole moments
- Note: No information (yet) on variances of the statistical moments



E. Clement *et al.*, Phys. Rev. C **75**, 054313 (2007)



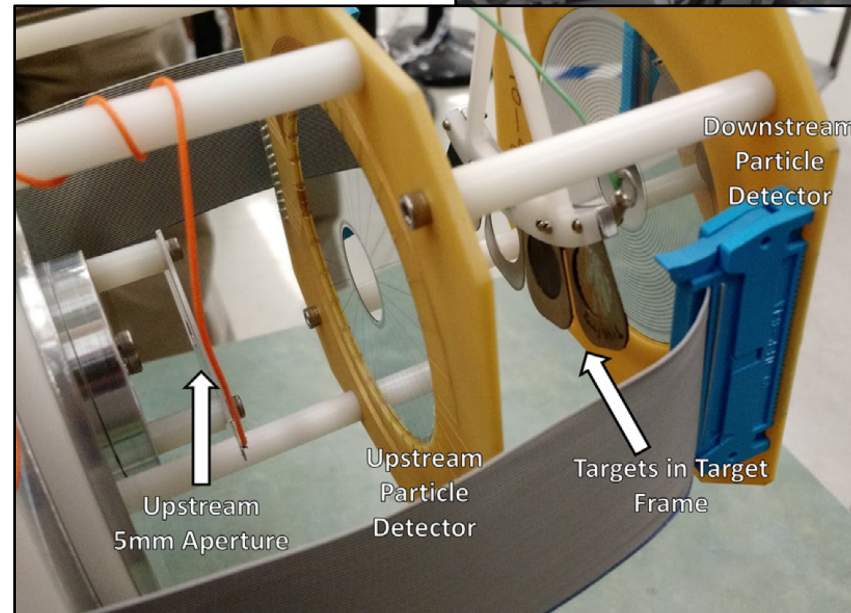
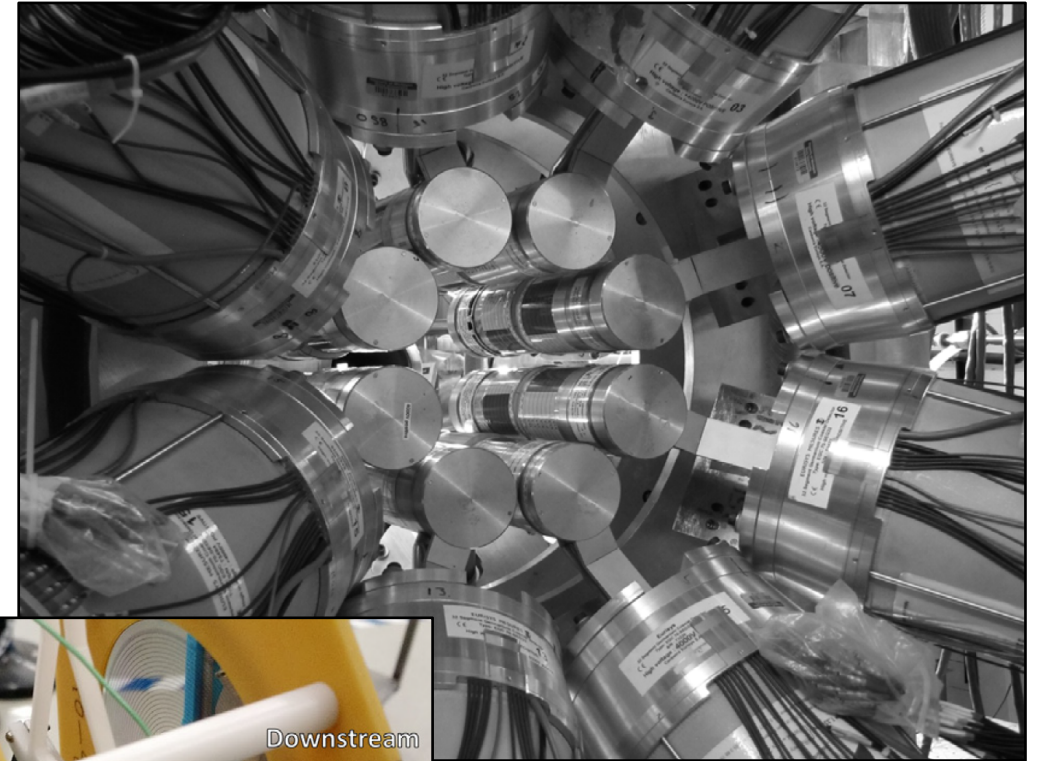
# Experimental Collaboration

- S1937, S1576, and S1866 experimental collaborations
  - TRIUMF, Vancouver, BC V6T 2A3, Canada
  - Department of Physics, University of Surrey, Guildford, United Kingdom
  - Department of Physics, University of York, Heslington, York YO10 5DD, United Kingdom
  - Department of Physics, University of Guelph, Guelph, ON N1G 2W1, Canada
  - Science Technical Center, Simon Fraser University, Burnaby, BC V5A 1S6, Canada
  - Advanced Science Research Center, Japanese Atomic Energy Agency, 2-4 Shirakata Shirane, Tokai, Ibaraki 319-1195 Japan
  - Lawrence Livermore National Laboratory, Livermore, CA 94550, USA



# Coulomb Excitation at FRIB

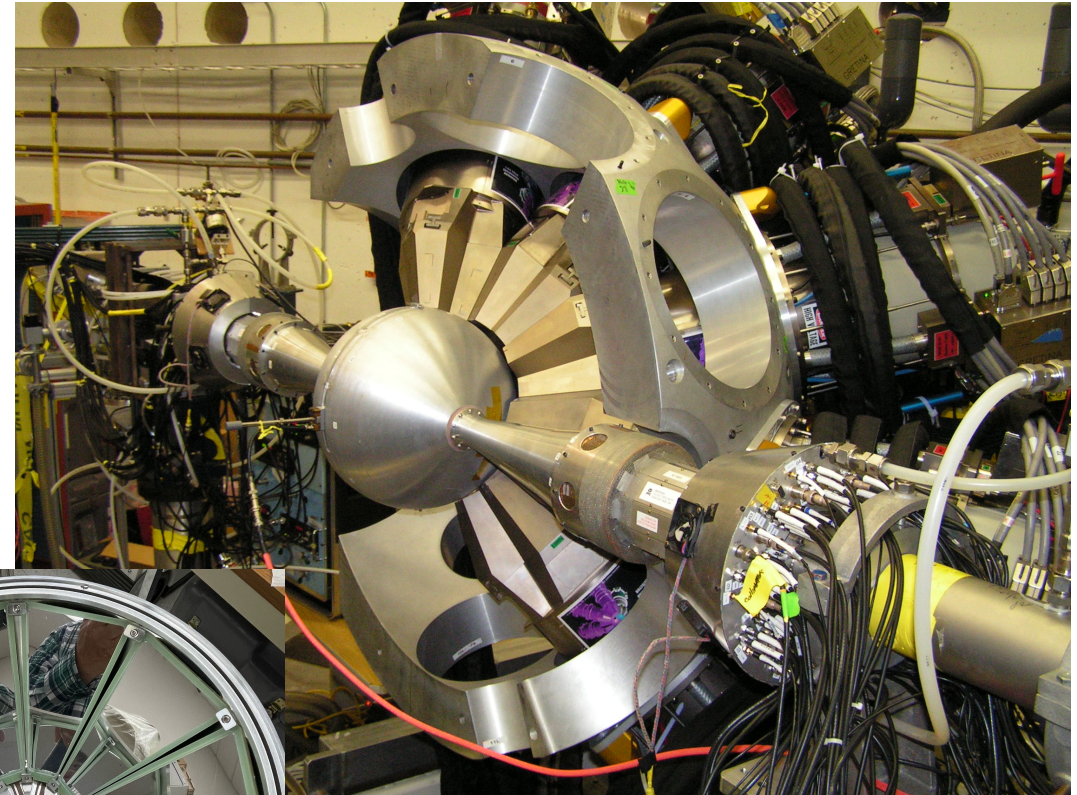
- ReAccelerator (ReA6) Facility provides RIB and stable beams at ~few MeV/u
  - Stop fast RIB in gas cell, extract
  - Ion source for stable beams
  
- Currently employ JANUS setup
  - SeGA with two S3 detectors
  - Many stable and RIB experiments successfully performed
  
- Beam development underway for two approved RIB experiments
  - $^{46}\text{Ar}$  and  $^{44}\text{Ti}$



E. Lunderberg *et al.*,  
NIM A **885**, 30 (2018)

# Future Plans for CouEx at FRIB

- Two complimentary arrays for charged particle detection in anticipation of GRETA @ ReA6
  - CHICOX for  $Z > 20$  nuclei
  - BambinoX for  $Z < 20$  nuclei
- CHICOX is the upgrade of CHICO2 PPAC array
  - Assembly and initial tests completed
  - Will be used first with GRETINA at Argonne next year
- BambinoX houses two S3 detectors similar to JANUS and Bambino
  - Starting manufacturing process
  - Will be ready for GRETA at FRIB



CHICO2 @ Argonne

C. Y. Wu *et al.*, NIM A  
**814**, 6 (2016)

# Thank You!



#### **Disclaimer**

This document was prepared as an account of work sponsored by an agency of the United States government. Neither the United States government nor Lawrence Livermore National Security, LLC, nor any of their employees makes any warranty, expressed or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States government or Lawrence Livermore National Security, LLC. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States government or Lawrence Livermore National Security, LLC, and shall not be used for advertising or product endorsement purposes.

# Extra Slides

# Extracted Matrix Elements I

Matrix Element	This Work	Lunderberg	Becker	Adopted
$\langle 0_1^+    E2    2_1^+ \rangle$	$0.788_5^5$	$0.81_1^1$	$0.82_2^2$	$0.82_1^1$
$\langle 2_1^+    E2    2_1^+ \rangle$	$-0.78_8^8$	$-0.96_{47}^{11}$	$-0.80_4^4$	-
$\langle 2_1^+    E2    4_1^+ \rangle$	$1.38_1^1$	$1.30_2^2$	$1.27_2^5$	$1.25_4^4$
$\langle 4_1^+    E2    4_1^+ \rangle$	$-1.34_{10}^{11}$	$-1.2_{10}^{2.4}$	$-0.73_{14}^{15}$	-
$\langle 4_1^+    E2    6_1^+ \rangle$	$1.87_2^2$	$1.63_7^7$	$1.61_8^6$	$1.56_9^9$
$\langle 6_1^+    E2    6_1^+ \rangle$	$-1.0_2^2$	$-0.8_{13}^{22}$	$-0.87_{12}^{16}$	-
$\langle 6_1^+    E2    8_1^+ \rangle$	$2.26_5^5$	-	$1.80_8^{15}$	$1.82_{14}^{14}$

F. Becker *et al.*, Nucl. Phys. A **770**, 107 (2006)

E. Lunderberg *et al.*, NIM A **885**, 30 (2018)

E. Lunderberg, PhD Thesis, Michigan State University (2017).

# Extracted Matrix Elements II

Matrix Element	This Work	Lunderberg	Becker	Adopted
$\langle 0_1^+    E2    2_2^+ \rangle$	$0.132_3^2$	0.159(5)	0.157(4)	0.13(1)
$\langle 2_1^+    E2    2_2^+ \rangle$	$0.57_3^2$	0.43(3)	0.26(6)	0.24(5)
$\langle 2_2^+    E2    2_2^+ \rangle$	$0.88_{17}^{22}$	$1.0_7^3$	$0.58_8^4$	-
$\langle 0_2^+    E2    2_2^+ \rangle$	$-0.06_{10}^{10}$	-	$-0.03_1^2$	-
$\langle 2_1^+    M1    2_2^+ \rangle$	$0.08_7^7$	0.33(2)	0.38(3)	0.30(3)
$\langle 0_1^+    E2    2_3^+ \rangle$	$0.039_4^5$	0.0384(7)	0.180(8)	0.020(1)
$\langle 2_1^+    E2    2_3^+ \rangle$	$0.123_{16}^{14}$	0.084(5)	$0.50_5^2$	0.068(4)
$\langle 2_2^+    E2    2_3^+ \rangle$	$0.23_{16}^4$	$0.15_{37}^2$	$0.19_5^{32}$	0.12(2)
$\langle 0_2^+    E2    2_3^+ \rangle$	$0.48_5^6$	0.48(1)	0.26(1)	0.25(1)
$\langle 4_1^+    E2    2_3^+ \rangle$	$0.34_4^4$	0.330(6)	$0.22_5^{20}$	0.178(8)
$\langle 2_3^+    E2    2_3^+ \rangle$	$0.7_4^4$	$1.6_5^{18}$	$-0.22_{14}^9$	-
$\langle 2_1^+    M1    2_3^+ \rangle$	$-0.12_3^3$	-0.149(3)	$-0.41_4^{12}$	0.057(4)
$\langle 2_2^+    M1    2_3^+ \rangle$	$0.03_3^3$	0.09(2)	-	$0.016_8^{14}$

F. Becker *et al.*, Nucl. Phys. A **770**, 107 (2006)

E. Lunderberg *et al.*, NIM A **885**, 30 (2018)

E. Lunderberg, PhD Thesis, Michigan State University (2017).

# Extracted Matrix Elements III

Matrix Element	This Work	Lunderberg	Becker	Adopted
$\langle 2_1^+    E2    4_2^+ \rangle$	$0.0542_{13}^{13}$	$0.074_6^5$	$0.073_5^2$	$0.069_5^5$
$\langle 2_2^+    E2    4_2^+ \rangle$	$0.740_{16}^{16}$	$0.89_7^5$	$0.91_4^6$	$0.95_6^6$
$\langle 4_1^+    E2    4_2^+ \rangle$	$0.504_{13}^{13}$	-	$-0.60_3^2$	$0.66_8^8$
$\langle 4_2^+    E2    4_2^+ \rangle$	$1.27_{21}^{23}$	-	-	-
$\langle 4_1^+    M1    4_2^+ \rangle$	$0.10_1^1$	-	$-0.12_7^5$	$0.2_3^3$
$\langle 0_2^+    E2    2_1^+ \rangle$	$0.33_2^2$	$0.243_7^{16}$	$0.30_1^1$	$0.31_1^1$
$\langle 0_1^+    E3    3_1^- \rangle$	$0.22_4^4$	-	-	$0.20_3^3$
$\langle 2_1^+    E3    5_1^- \rangle$	$0.43_2^2$	-	-	-
$\langle 3_1^-    E2    3_1^- \rangle$	$-3.1_{25}^{25}$	-	-	-
$\langle 3_1^-    E2    5_1^- \rangle$	$-0.3_{21}^{21}$	-	-	-

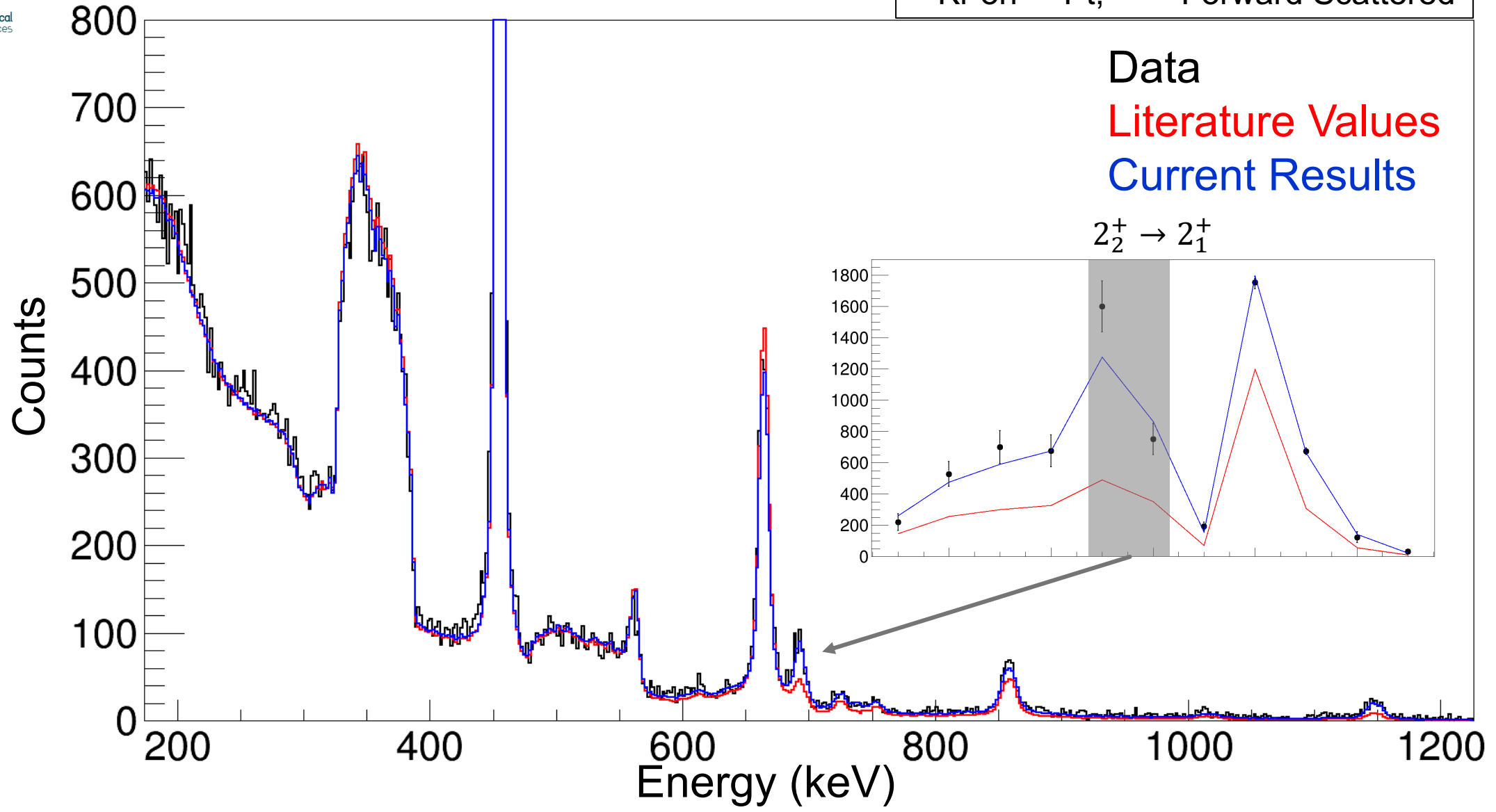
F. Becker *et al.*, Nucl. Phys. A **770**, 107 (2006)

E. Lunderberg *et al.*, NIM A **885**, 30 (2018)

E. Lunderberg, PhD Thesis, Michigan State University (2017).

# Yield Reproduction

$^{78}\text{Kr}$  on  $^{196}\text{Pt}$ ,  $^{196}\text{Pt}$  Forward Scattered



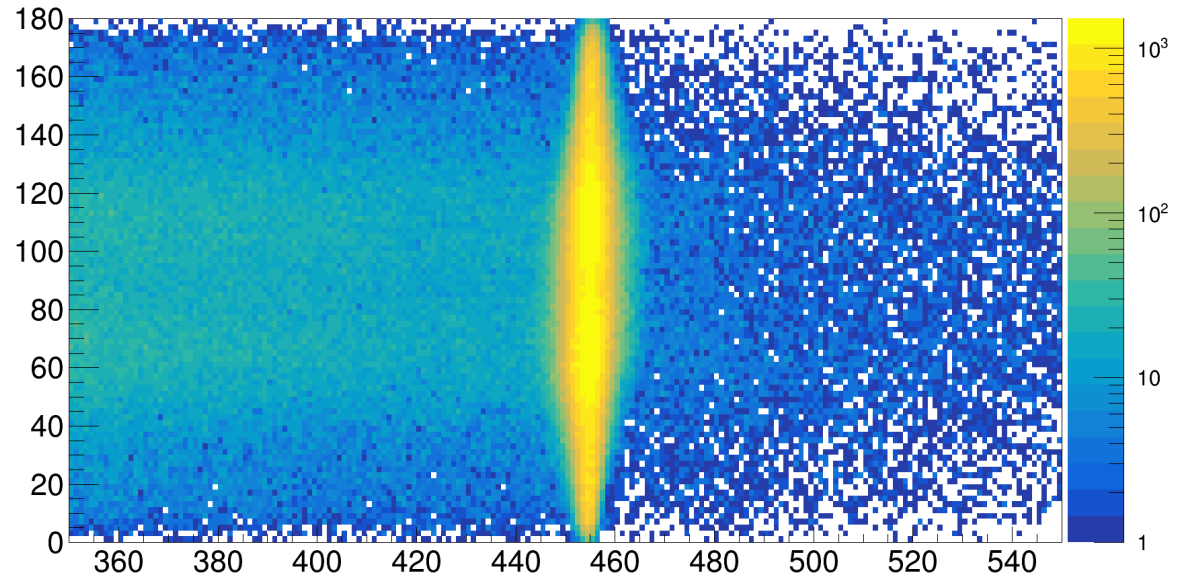
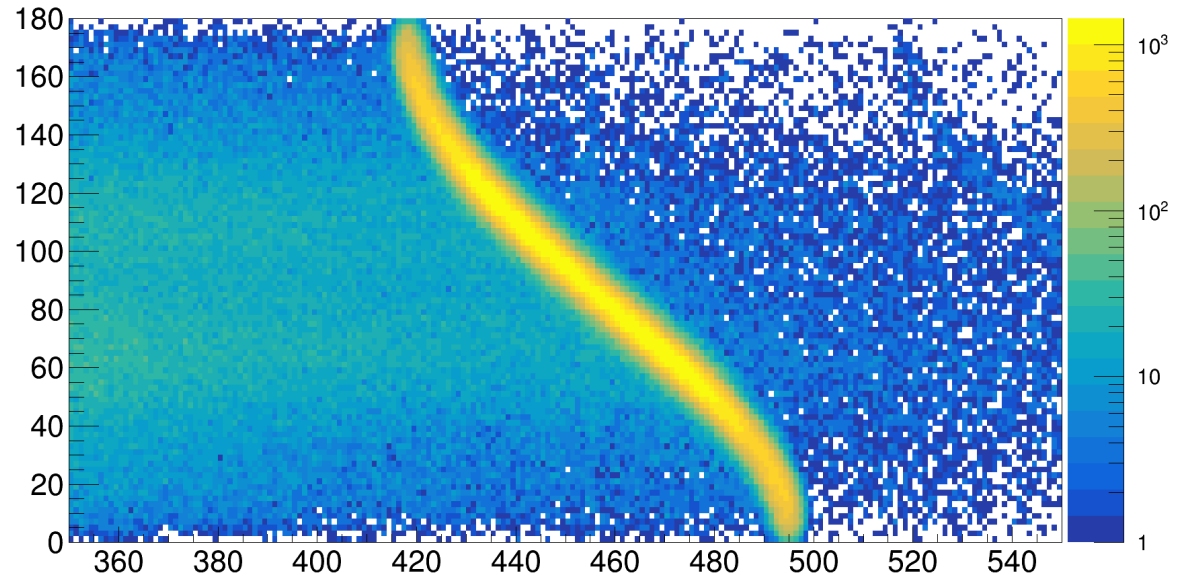
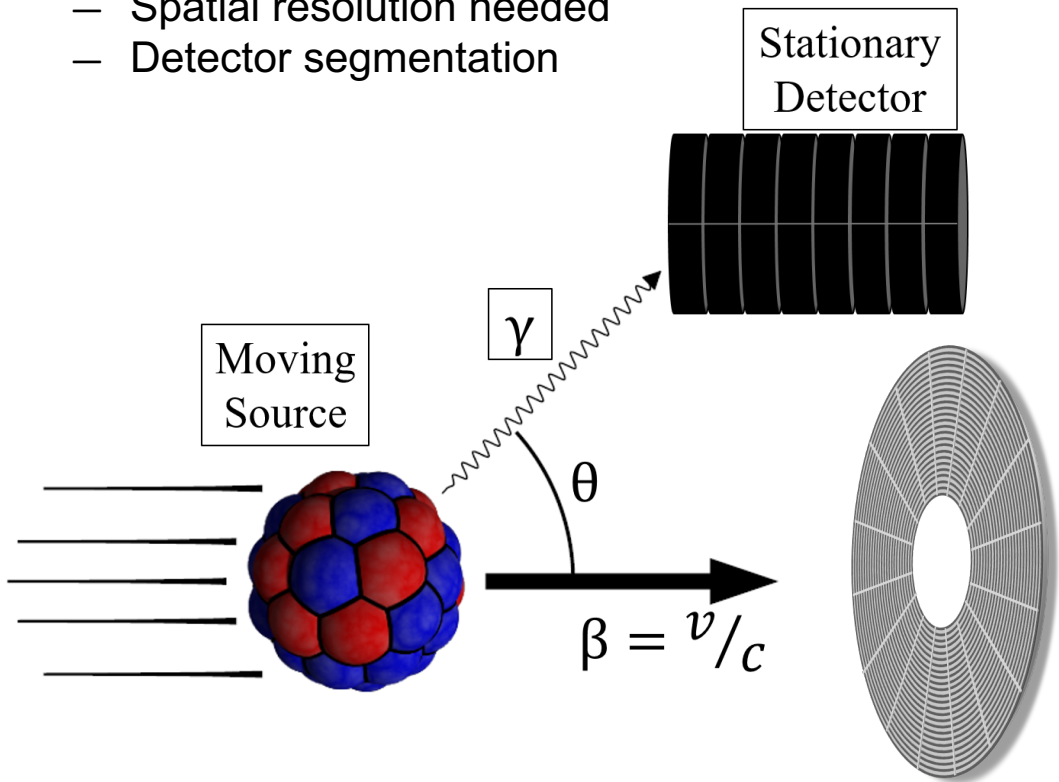




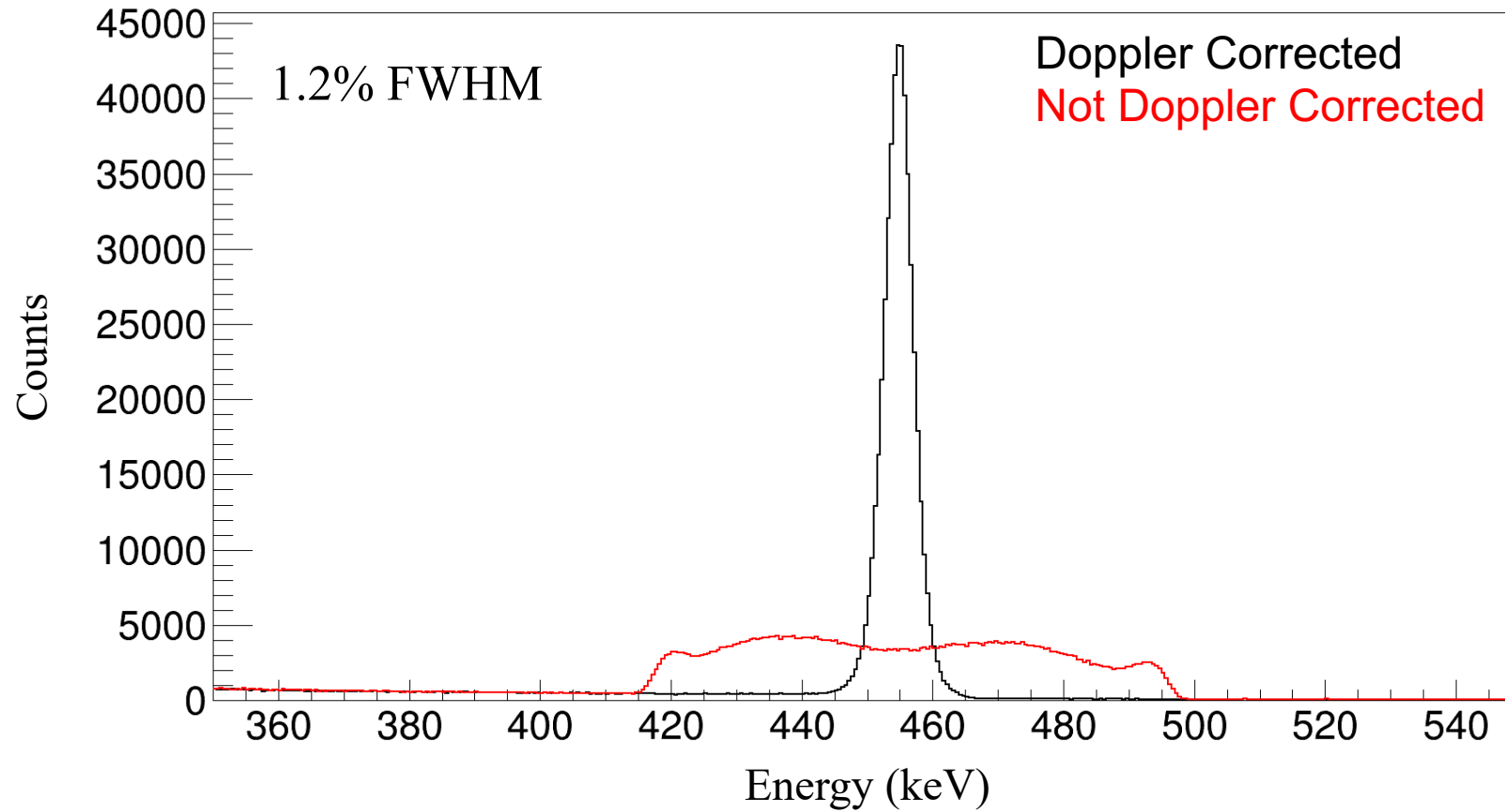
# Doppler Correction

Nuclear & Chemical Sciences

- $E_{LAB} = \frac{E_{REST}}{\gamma(1-\beta \cos \theta)}$
- $\beta = \frac{v}{c}$  depends on scattering angle
  - $\beta$  range: 0.075 to 0.090
  - Spatial resolution needed
  - Detector segmentation



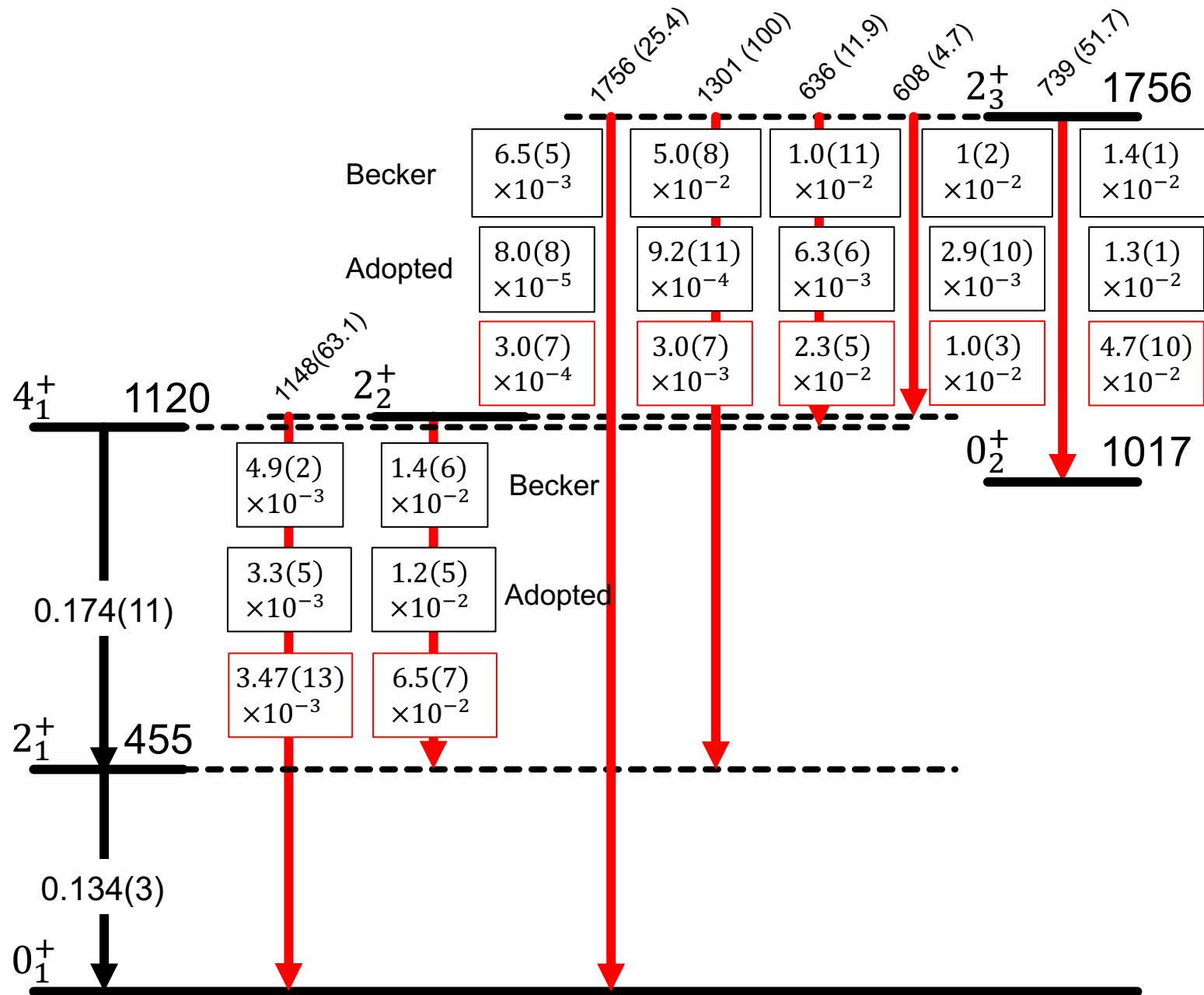
# Doppler Correction





# Results I

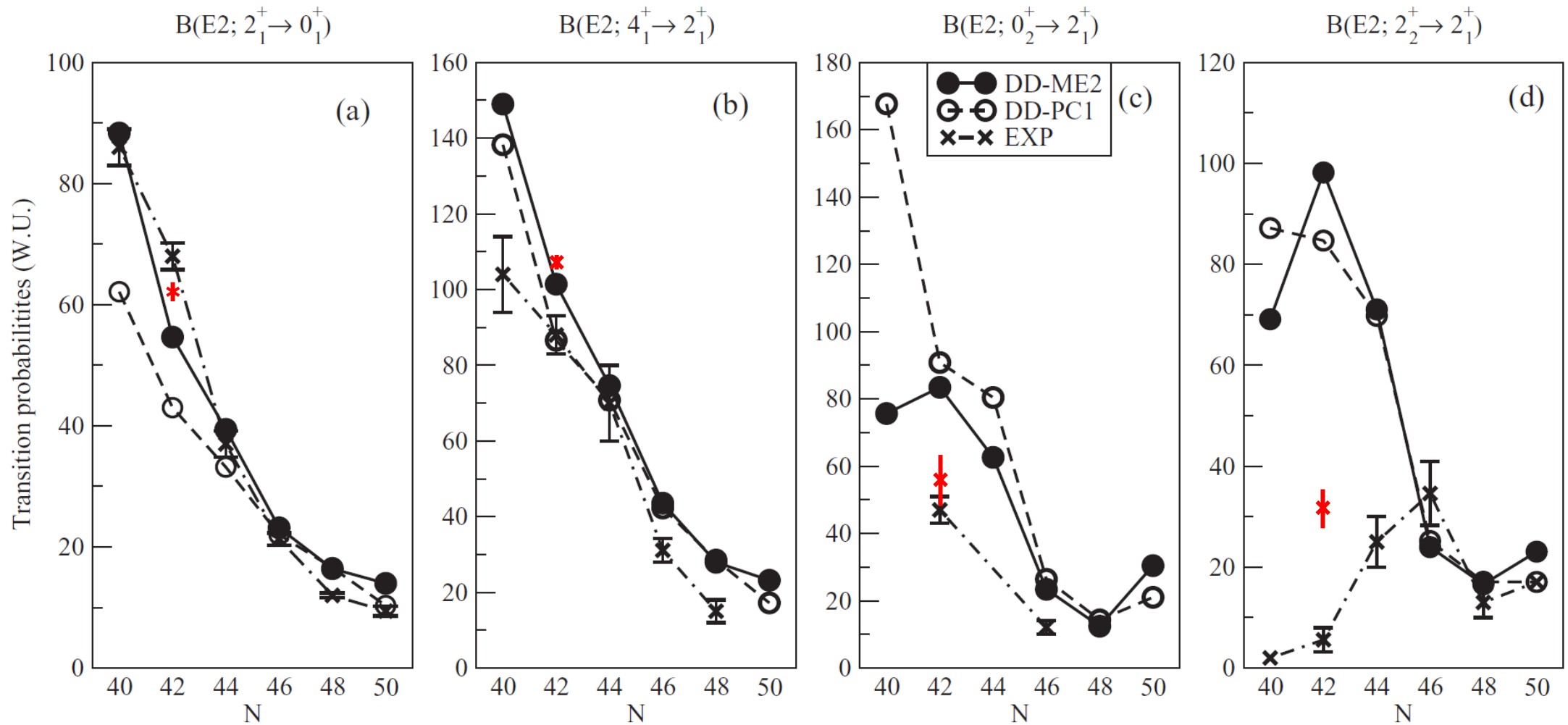
- Transition strengths almost all different from Becker et al.
  - $2_2^+$  lifetime agrees with adopted value
  - All branching ratios agree nicely with adopted values (decay data)
  - $2_2^+$  mixing ratio highly discrepant
    - 0.45(10) vs  $4_2^{30}$





# Results II

Nuclear & Chemical Sciences



K. E. Karakatsanis and K. Nomura, Phys. Rev. C **105**, 064310 (2022)