

Impact of deformation on ultra-relativistic nuclear collisions

Benjamin Bally

SSNET24 - Orsay - 04/11/2024



- Interface between low- and high-energy nuclear physics
- Use of nuclear structure information to better understand heavy-ion collisions
 - Giacone et al.*, PRL 127, 242301 (2021)
 - Bally et al.*, PRL 128, 082301 (2022)
 - Jia et al.*, PRL 131, 022301 (2023)
- Nuclear deformation impacts initial conditions and thus final state observables
- Nuclear structure calculations for ^{16}O and ^{20}Ne using EFT-based interactions

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- **Predictions for $^{16}\text{O} + ^{16}\text{O}$ and $^{16}\text{O} + ^{208}\text{Pb}$ runs at LHC in 2025**

CERN-TH-2024-021

The unexpected uses of a bowling pin: exploiting ^{20}Ne isotopes for precision characterizations of collectivity in small systems

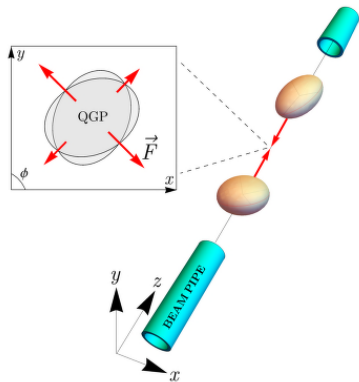
[Giuliano Giacalone](#)^{1,*} [Benjamin Bally](#)² [Govert Nijs](#)³ [Shihang Shen](#)⁴
[Thomas Duguet](#)^{5,6} [Jean-Paul Ebran](#)^{7,8} [Serdar Elhatisari](#)^{9,10} [Mikael Frosini](#)¹¹ [Timo A. Lähde](#)^{12,13}
[Dean Lee](#)¹⁴ [Bing-Nan Lu](#)¹⁵ [Yuan-Zhuo Ma](#)¹⁴ [Ulf-G. Meißner](#)^{10,16,17} [Jacquelyn Noronha-Hostler](#)¹⁸
[Christopher Plumberg](#)¹⁹ [Tomás R. Rodríguez](#)²⁰ [Robert Roth](#)^{21,22} [Wilke van der Schee](#)^{3,23,24} and [Vittorio Somà](#)⁵

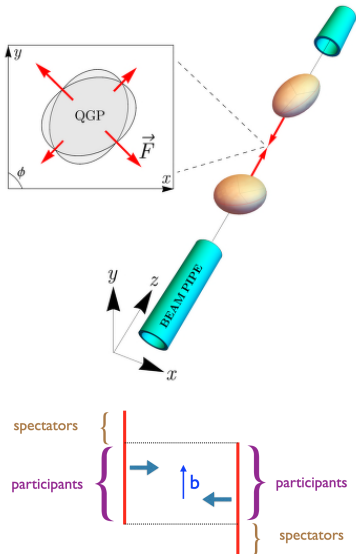
CERN-TH-2024-074

Anisotropic flow in fixed-target $^{208}\text{Pb}+^{20}\text{Ne}$ collisions as a probe of quark-gluon plasma

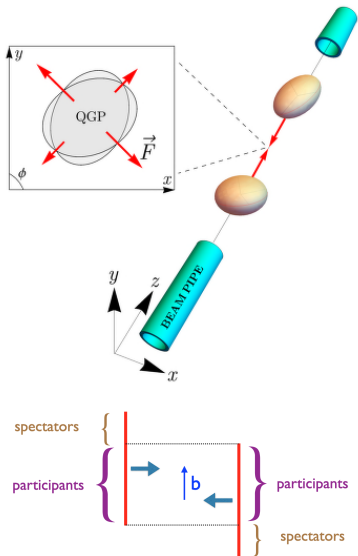
[Giuliano Giacalone](#)^{1,*} [Wenbin Zhao](#)^{2,3,†} [Benjamin Bally](#)⁴ [Shihang Shen](#)⁵
[Thomas Duguet](#)^{6,7} [Jean-Paul Ebran](#)^{8,9} [Serdar Elhatisari](#)¹⁰ [Mikael Frosini](#)¹¹
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[Govert Nijs](#)¹⁸ [Jacquelyn Noronha-Hostler](#)¹⁹ [Christopher Plumberg](#)²⁰ [Tomás R. Rodríguez](#)²¹
[Robert Roth](#)^{22,23} [Wilke van der Schee](#)^{18,24,25} [Björn Schenke](#)^{26,‡} [Chun Shen](#)^{27,28,§} and [Vittorio Somà](#)⁶

- Collaboration between low- and high-energy nuclear physics communities
 - ◇ Heavy-ion collisions
 - ◇ Nuclear structure (PGCM)
 - ◇ Nuclear structure (NLEFT)

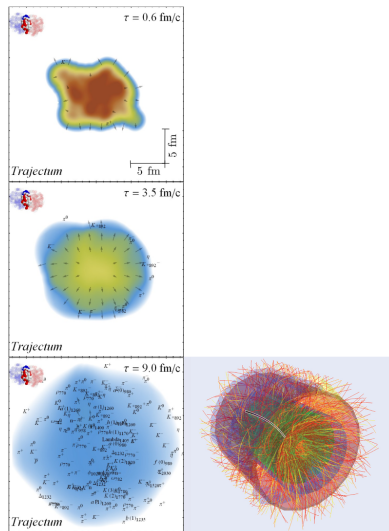




Ollitrault, EPJA 59, 236 (2023)

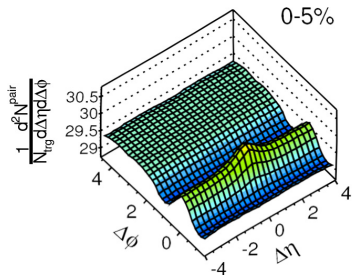


Ollitrault, EPJA 59, 236 (2023)



Giacalone et al., PRL 131, 202302 (2023)

ALICE collaboration

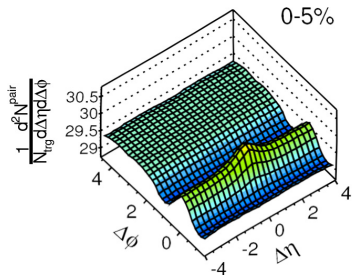


credit: CMS collaboration

- Probability distribution of particle emission

$$P(\phi, \eta) = P(\phi) = \frac{1}{2\pi} \sum_{n=-\infty}^{+\infty} V_n e^{-in\phi}$$

$V_2 \equiv$ elliptic flow, $V_3 \equiv$ triangular flow, ...



credit: CMS collaboration

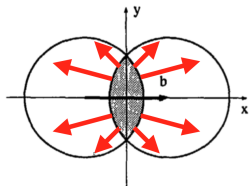
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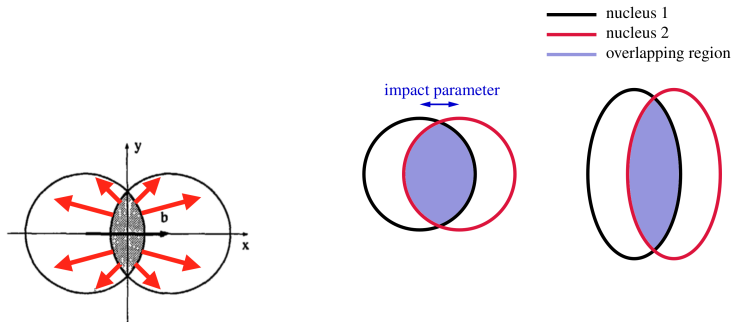
- Average of pair distribution

$$\left\langle \frac{dN_{\text{pair}}}{d\Delta\eta d\Delta\phi} \right\rangle = \langle P(\phi) P(\phi + \Delta\phi) \rangle = \frac{1}{2\pi} \left(1 + 2 \sum_{n=1}^{+\infty} \langle |V_n|^2 \rangle \cos(n\Delta\phi) \right)$$



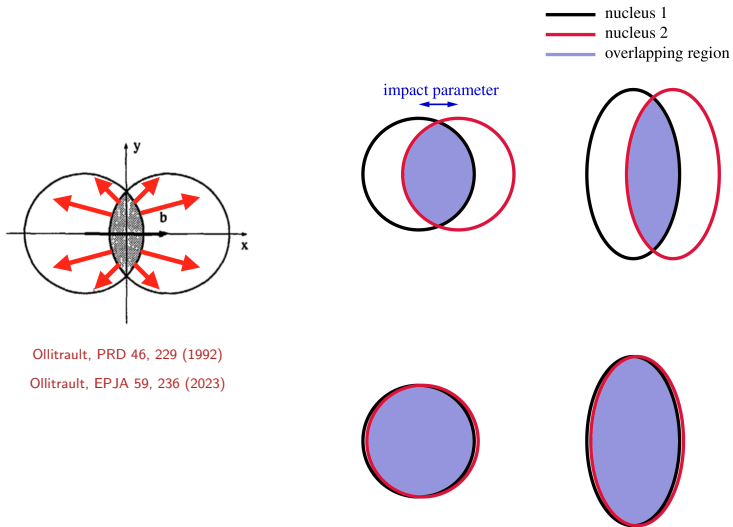
Ollitrault, PRD 46, 229 (1992)

Ollitrault, EPJA 59, 236 (2023)



Ollitrault, PRD 46, 229 (1992)

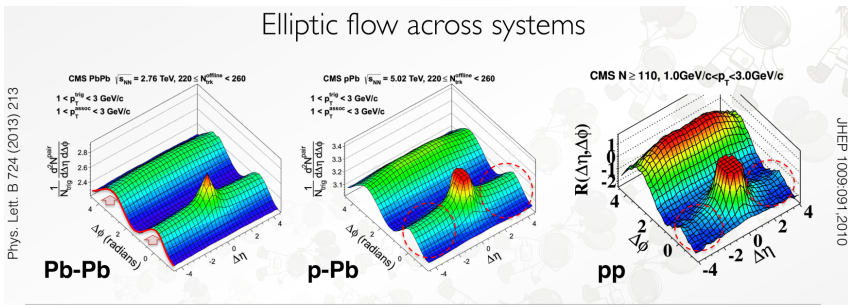
Ollitrault, EPJA 59, 236 (2023)



Ollitrault, PRD 46, 229 (1992)

Ollitrault, EPJA 59, 236 (2023)

Elliptic flow across systems



Chinellato, Quark Matter 2023

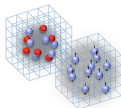
- Collectivity appears in *small systems* (p+p, p+A, d+A, ...)
- Is it the same mechanism? Is hydrodynamic the correct description?

EFT \rightarrow Nuclear structure \rightarrow Relativistic hydrodynamic \rightarrow Hadron transport \rightarrow Nucl-th

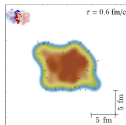
χ EFT
N3LO



PGCM



NLEFT



Trajectum



arXiv:2402.05995

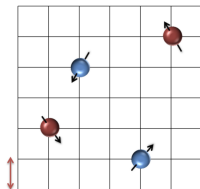
- TAURUS: <https://github.com/project-taurus>
- *Trajectum*: <https://sites.google.com/view/govertnijs/trajectum>
- SMASH: <https://github.com/smash-transport/smash>

- Nuclear Lattice Effective field Theory (NLEFT)

Lee, *Front. in Phys.* 8, 174 (2020)

Lähde and Meißner, *Lectures Notes in Phys.*, Springer (2019)

- Mesh with 8 sites and spacing $a = 1.315$ fm



- Minimal pionless EFT Hamiltonian with $SU(4)$ symmetry

- Pin-hole algorithm \rightarrow nucleon positions

Elhatisari *et al.*, *PRL* 119, 222505 (2017)

- Projected Generator Coordinate Method (PGCM)

$$|\Theta_\epsilon^{\sigma M}\rangle = \sum_{qK} f_\epsilon^{\sigma M}(q, K) P_{MK}^\sigma |\Phi(q)\rangle \quad \text{where } \sigma \equiv Z, N, J, \pi$$

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- Full method: PGCM + Perturbation Theory

Frosini *et al.*, EPJA 58, 62 (2022)

Frosini *et al.*, EPJA 58, 63 (2022)

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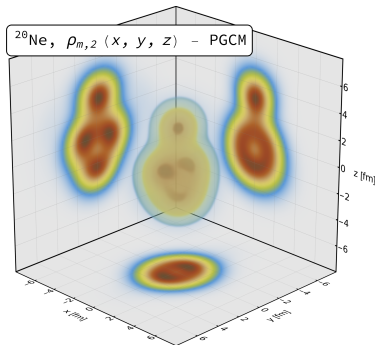
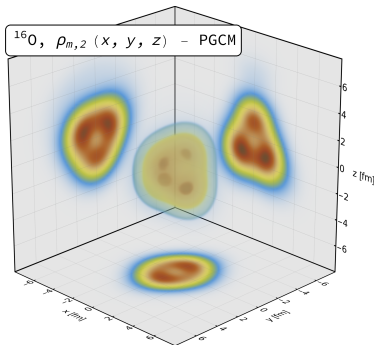
- Model space: $e_{\max} = 6$, $e_{3\max} = 18$, $\hbar\omega = 12$

Hamiltonian: Hütter N3LO

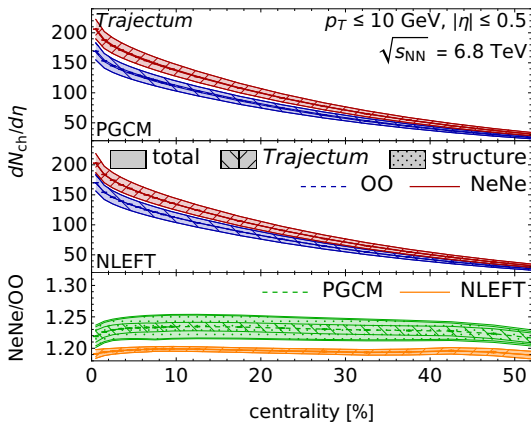
Hütter *et al.*, PLB 808, 135651 (2019)

Reference states $|\Phi\rangle$: real general Bogoliubov (VAPNP minimization)

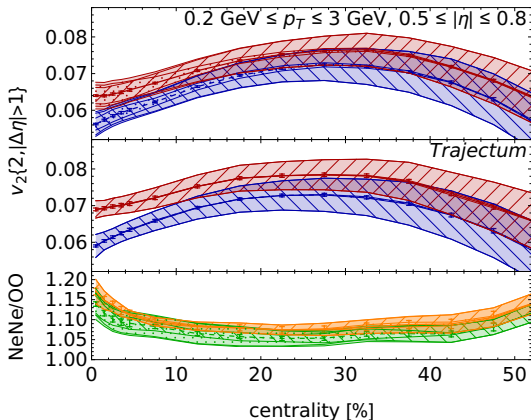
Collective coordinates q : $\beta_{20}, \beta_{22}, \beta_{30}, \beta_{32}$



- Determine average deformation of PGCM ground state: \bar{q}
- One-body density: $\rho_m(x, y, z) = \sum_{st} \frac{\langle \Phi(\bar{q}) | a_{xyzst}^+ a_{xyzst} P^Z P^N | \Phi(\bar{q}) \rangle}{\langle \Phi(\bar{q}) | P^Z P^N | \Phi(\bar{q}) \rangle}$
- Sample directly ρ_m or assuming α clusters



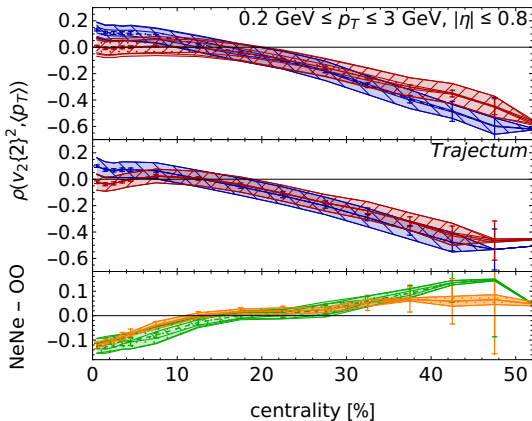
Results: elliptic flow $v_2\{2\}^2$



- In the 0-1% events:

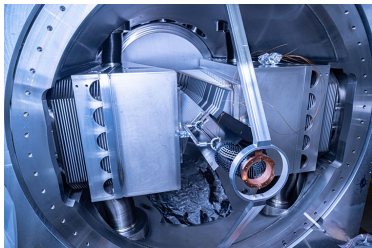
$$\frac{v_2\{2\}_{\text{NeNe}}}{v_2\{2\}_{\text{OO}}} = \begin{cases} 1.170(8)_{\text{stat.}} (30)_{\text{Traj.}}^{\text{str.}} (0)_{\text{syst.}}^{\text{str.}} & \text{(NLEFT)} \\ 1.139(6)_{\text{stat.}} (27)_{\text{Traj.}}^{\text{str.}} (28)_{\text{syst.}}^{\text{str.}} & \text{(PGCM)} \end{cases}$$

Results: Pearson coefficient $\rho(v_2\{2\}^2, \langle p_T \rangle)$

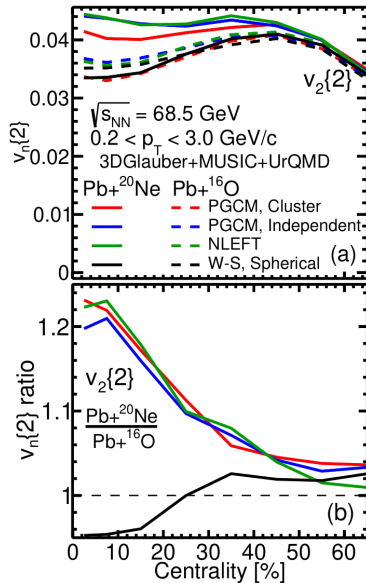


- Negative ρ due to the large deformation of ^{20}Ne

$$\rho_{\text{Ne+Ne}} - \rho_{\text{O+O}} \propto (\beta_{2,16\text{O}}^3 - \beta_{2,20\text{Ne}}^3)$$



credit: CERN



- Collaborative work at the interface between low- and high-energy physics
 - ◇ Make use of the large ground-state deformation of ^{20}Ne
 - ◇ Combines several state-of-the-art frameworks and software
 - ◇ NLEFT and PGCM give consistent results
- We make **predictions** for
 - ◇ $^{16}\text{O} + ^{16}\text{O}$ and $^{16}\text{O} + ^{208}\text{Pb}$ runs at the LHC (2025)
 - ◇ $^{20}\text{Ne} + ^{20}\text{Ne}$ and $^{20}\text{Ne} + ^{208}\text{Pb}$ runs that could be performed in the future