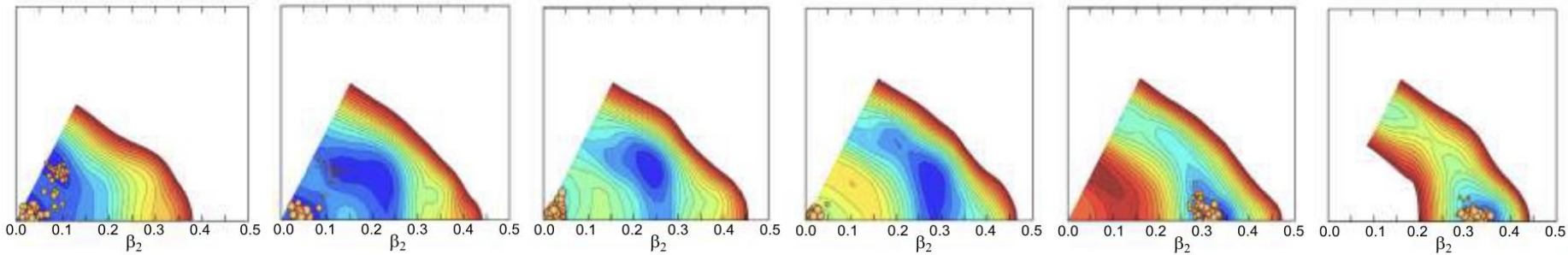
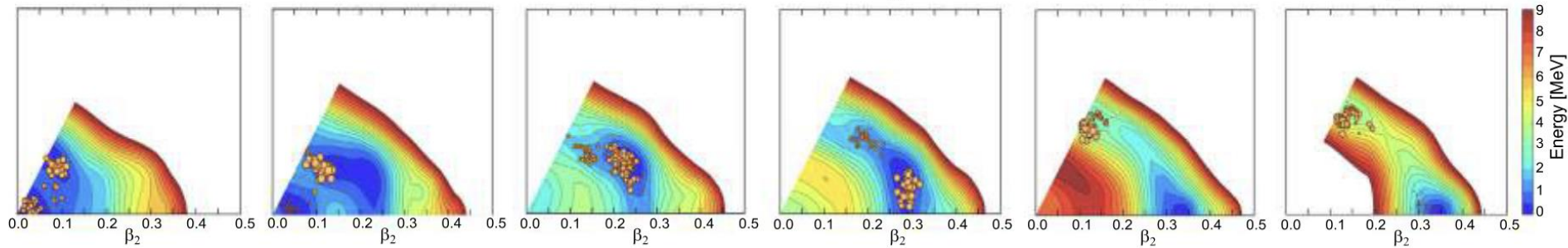




***STUDY OF SHAPE COEXISTENCE
AND COLLECTIVE PROPERTIES IN
⁹⁴⁻⁹⁶ZR ISOTOPES VIA COULOMB
EXCITATION MEASUREMENTS***

Naomi Marchini

ZIRCONIUM ISOTOPES – NUCLEAR STRUCTURE

 ^{92}Zr ^{94}Zr ^{96}Zr ^{98}Zr ^{100}Zr ^{102}Zr MCSM
(0^+_1)
(c)MCSM
(0^+_2)
(d)Type II shell
evolution

ZIRCONIUM ISOTOPES – NUCLEAR STRUCTURE

^{92}Zr

^{94}Zr

^{96}Zr

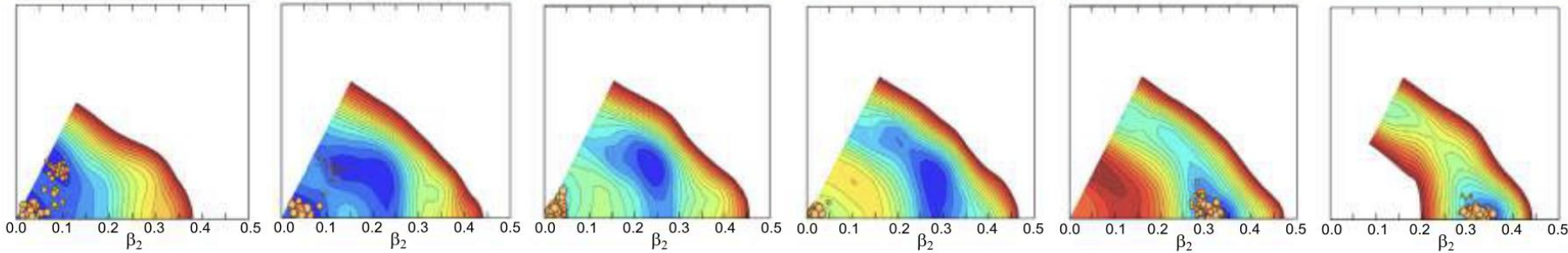
^{98}Zr

^{100}Zr

^{102}Zr

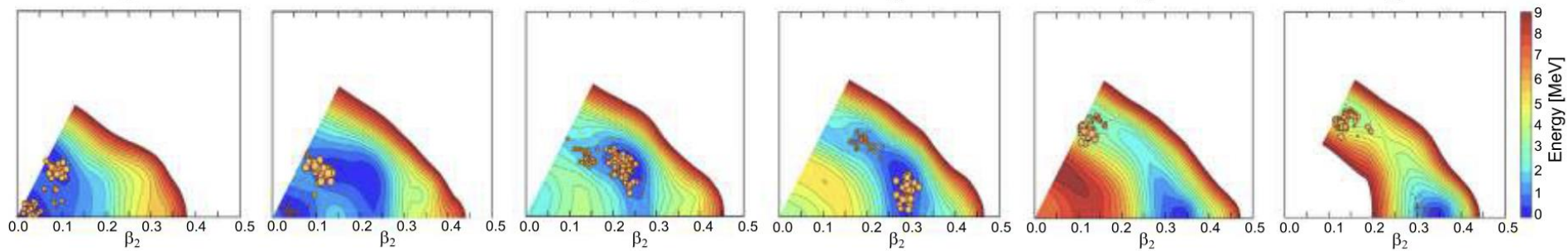
MCSM
(0^+_1)

(c)



MCSM
(0^+_2)

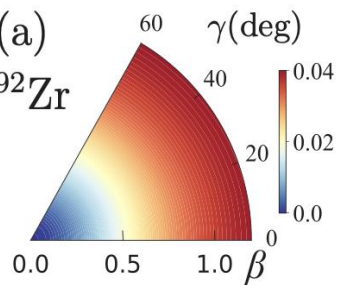
(d)



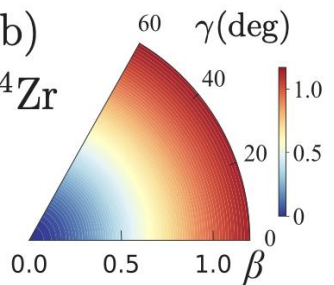
Type II shell evolution

IBM-
CM

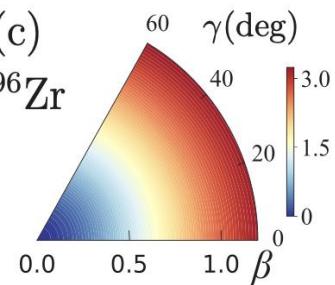
(a) ^{92}Zr



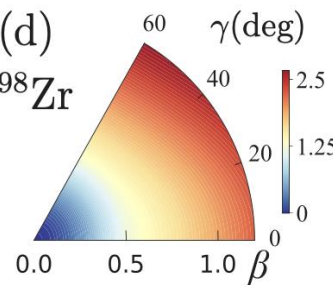
(b) ^{94}Zr



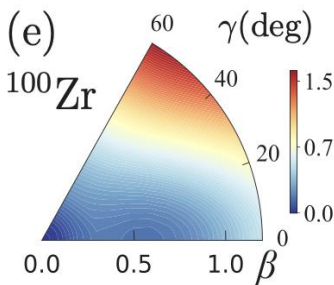
(c) ^{96}Zr



(d) ^{98}Zr

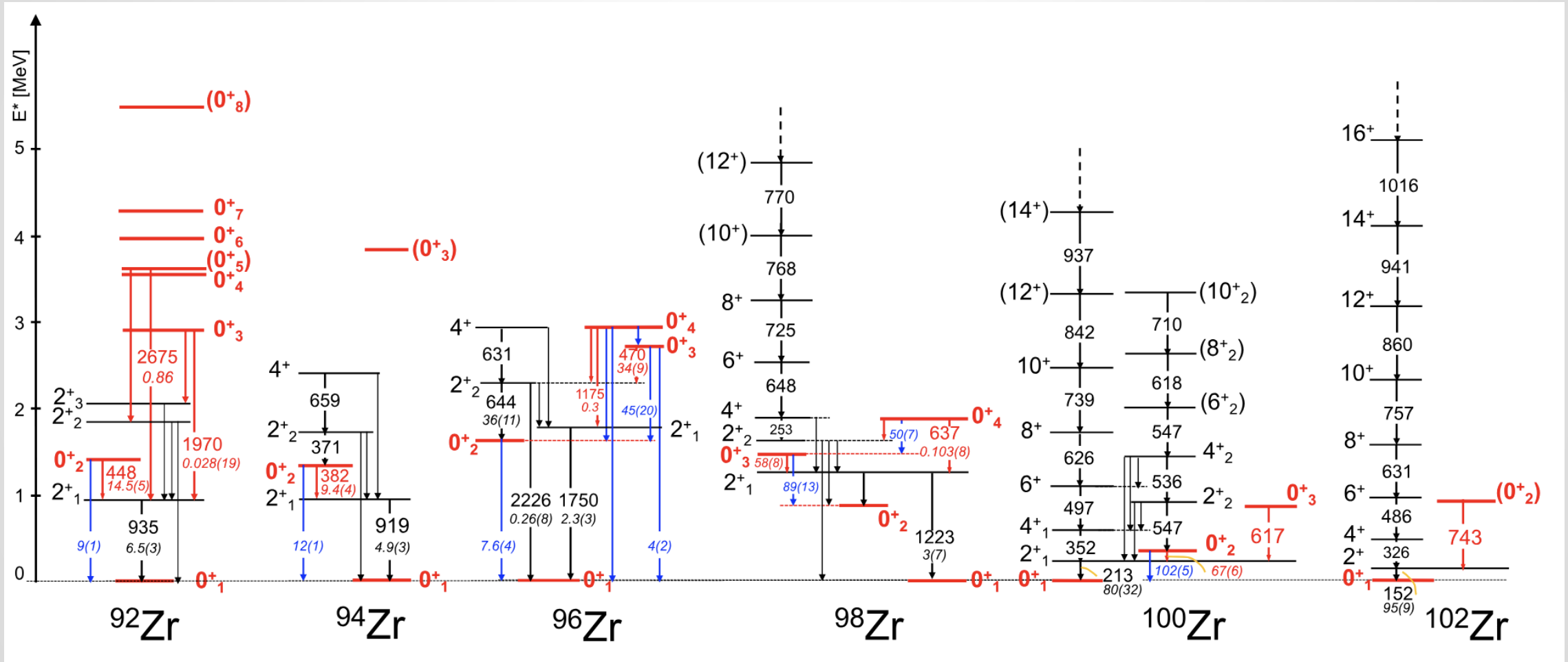


(e) ^{100}Zr

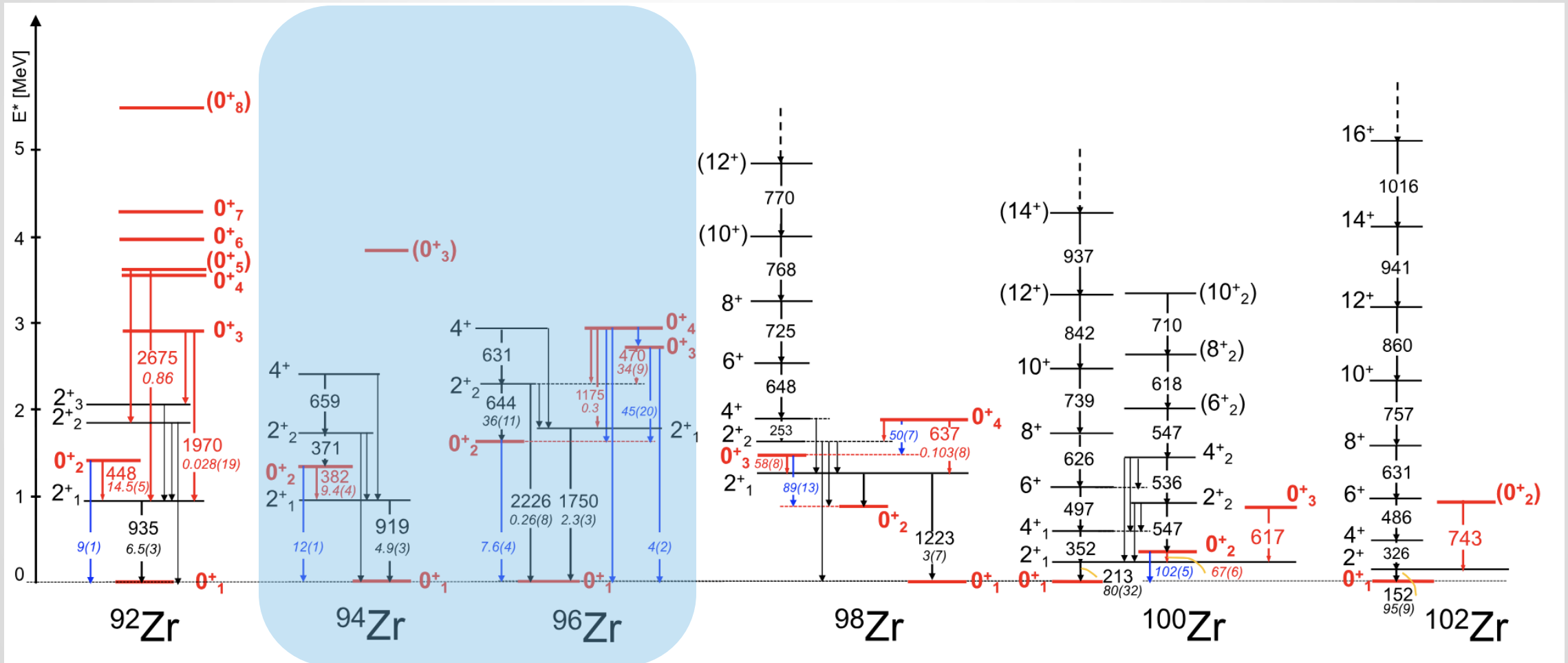


Intertwined
QPT

ZIRCONIUM ISOTOPES – EXPERIMENTAL VALUES



ZIRCONIUM ISOTOPES – EXPERIMENTAL VALUES



^{94}Zr – COULEX EXPERIMENT @LNL

- Beam : ^{94}Zr 370 MeV 0.1 pnA
- Target : self-supporting ^{208}Pb 1mg/cm²



25 HPGe Compton-suppressed detectors

FWHM @1332 keV ~ 0.2%

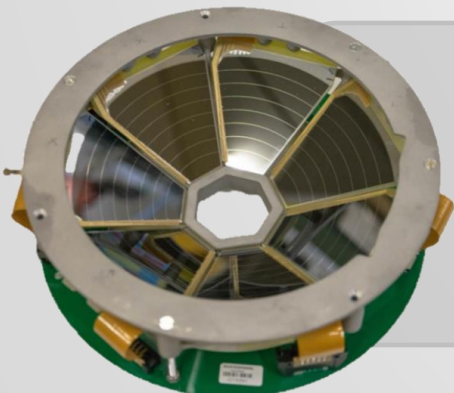
Efficiency @1332 keV ~ 2%



six 3"x3" LaBr3:Ce

FWHM @1332 keV ~ 2%

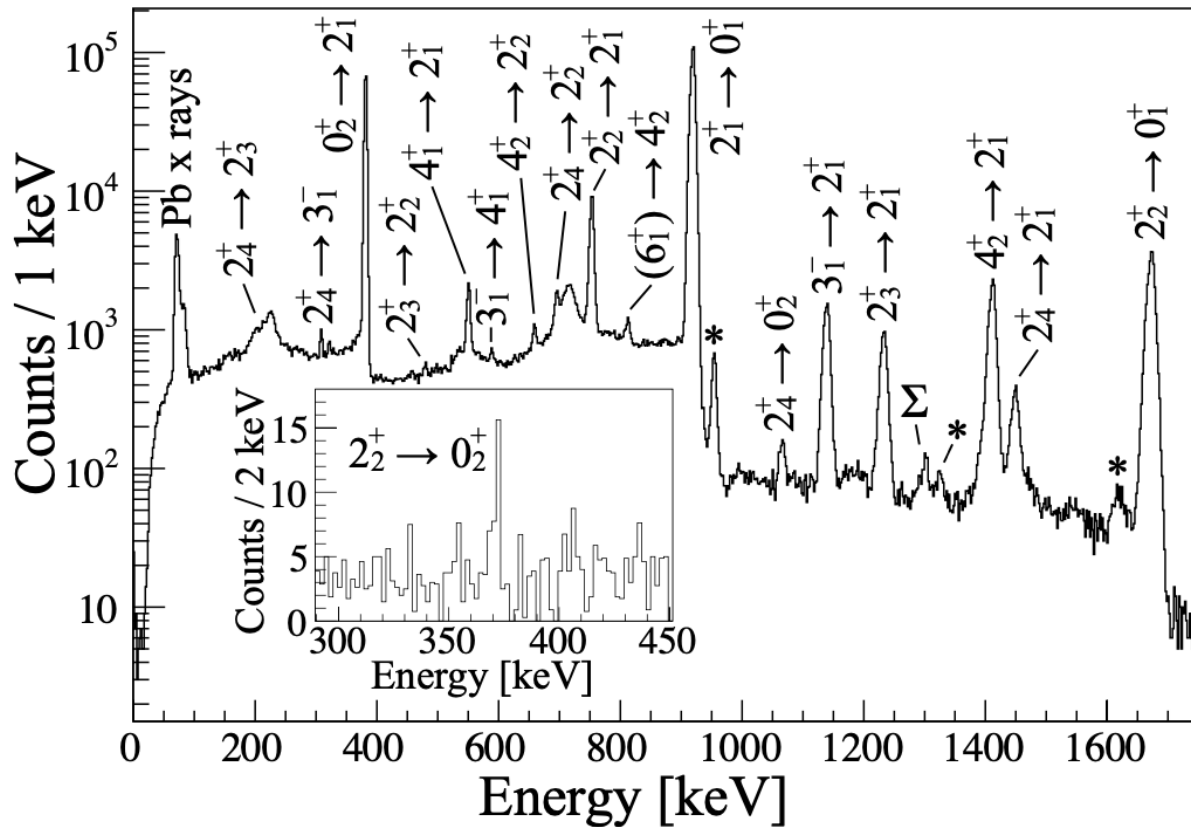
Efficiency @1332 keV ~ 4%



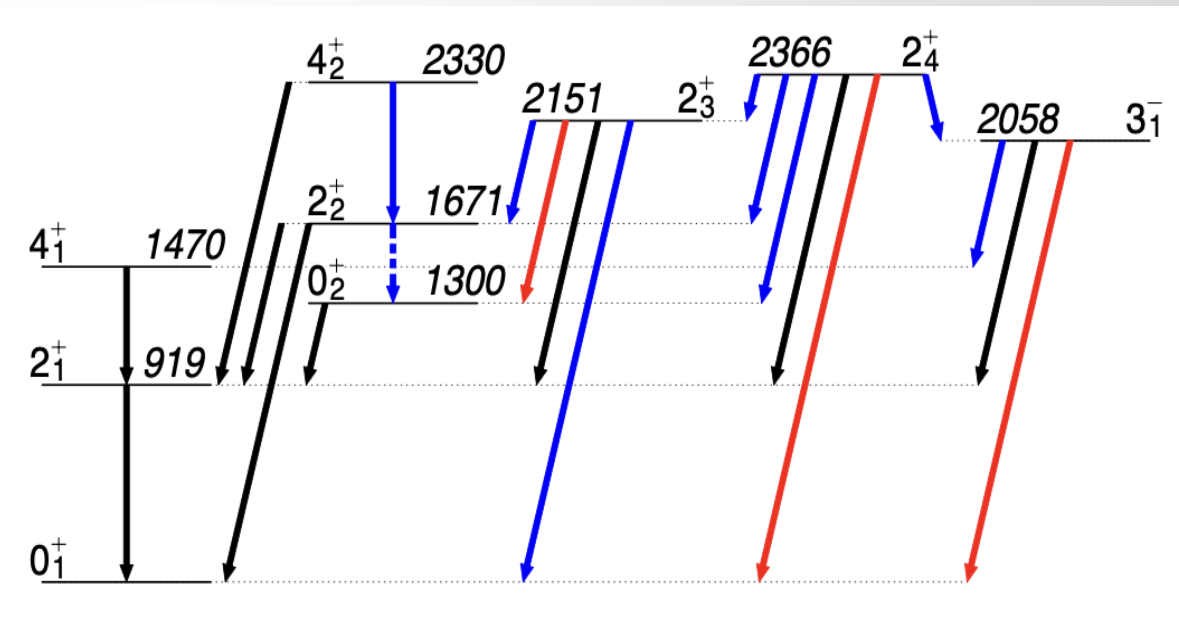
SPIDER modular array of Si detectors segmented into 8 annular strips (junction side).

$\Theta_{\text{Lab}} = 126^\circ - 162^\circ$ (detection of backscattered ^{94}Zr ions)



^{94}Zr – COULEX EXPERIMENT @LNL - RESULTS γ -particle spectrum

Level scheme



^{94}Zr – COULEX EXPERIMENT @LNL – GOSIA ANALYSIS

Using known spectroscopic data (lifetime, mixing and branching ratios):

- **16 B(E2) extracted**

$$\mathbf{B(E3; 3_1^- \rightarrow 0_1^+) = 33(3) \text{ W.u.}}$$

$J_i \rightarrow J_f$	$\langle J_f E2 J_i \rangle$ [eb]	$B(E2; J_i \rightarrow J_f)$ [W.u.]	
	Exp.	Exp.	IBM-CM
$2_1^+ \rightarrow 0_1^+$	+0.250(7) ^{ab}	4.8(2) ^b	2.7
$0_2^+ \rightarrow 2_1^+$	+0.155(4) ^a	9.5(5)	9.3
$4_1^+ \rightarrow 2_1^+$	+0.141(4) ^a	0.87(5)	— ^c
$2_2^+ \rightarrow 0_2^+$	+0.484(12) ^a	18.5(9)	20.2
$2_2^+ \rightarrow 2_1^+$	+0.03(3)	< 0.3	1.49
$2_2^+ \rightarrow 0_1^+$	+0.221(6)	3.9(2)	0.82
$4_2^+ \rightarrow 2_2^+$	+0.96(3) ^a	40(3)	26.6
$4_2^+ \rightarrow 2_1^+$	+0.607(16)	16.1(9)	2.1
$2_3^+ \rightarrow 2_2^+$	+0.249 ^{+0.019} _{-0.040}	4.9 ^{+0.7} _{-1.6}	17.3
$2_3^+ \rightarrow 0_2^+$	< 0.13 ^d	< 1.3	0.07
$2_3^+ \rightarrow 2_1^+$	+0.290 ^{+0.014} _{-0.012} ^a	6.6 ^{+0.6} _{-0.5}	1.2
$2_3^+ \rightarrow 0_1^+$	-0.0182 ^{+0.0016} _{-0.0020}	0.026 ^{+0.005} _{-0.006}	0.001
$2_4^+ \rightarrow 2_3^+$	-0.02 ^{+0.06} _{-0.03}	< 0.2	2.44
$2_4^+ \rightarrow 2_2^+$	±0.073 ^{+0.030} _{-0.018}	0.4 ^{+0.3} _{-0.2}	0.1
$2_4^+ \rightarrow 0_2^+$	±0.177 ^{+0.010} _{-0.005}	2.47 ^{+0.30} _{-0.14}	0.06
$2_4^+ \rightarrow 2_1^+$	+0.092 ^{+0.006} _{-0.004} ^a	0.67 ^{+0.09} _{-0.06}	0.001
$2_4^+ \rightarrow 0_1^+$	-0.001 ^{+0.003} _{-0.006}	< 4 · 10 ⁻³	3 · 10 ⁻⁴

^{94}Zr – COULEX EXPERIMENT @LNL – GOSIA ANALYSIS

Using known spectroscopic data (lifetime, mixing and branching ratios):

- **16 B(E2) extracted**

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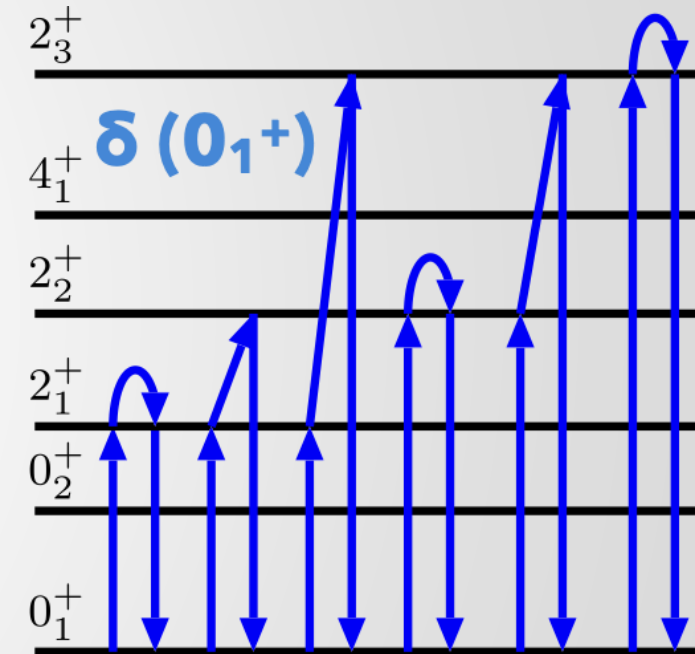
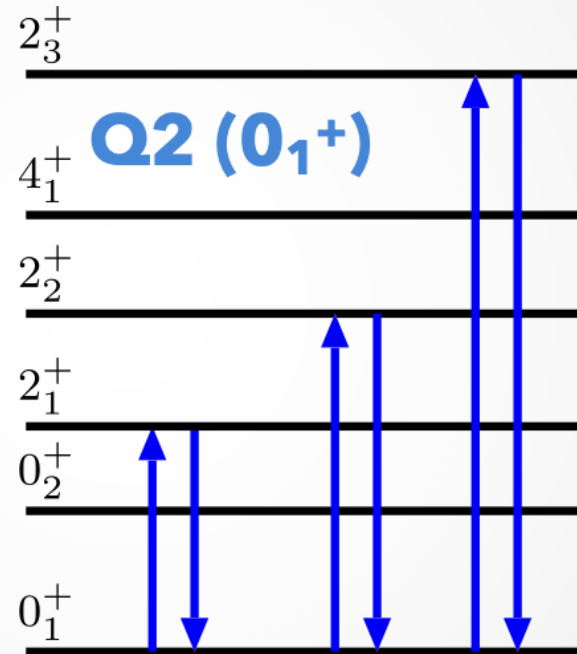
- $Q_s(2_1)$, $Q_s(2_2)$

J_i	$\langle J_i E2 J_i \rangle$ [eb]	$Q_s(J_i)$ [eb]	
	Exp.	Exp.	IBM-CM
2_1^+	$+0.131^{+0.013}_{-0.030}$	$+0.099^{+0.010}_{-0.025}$	+0.066
2_2^+	+0.37(4)	+0.28(3)	+0.31

^{94}Zr – COULEX EXPERIMENT @LNL – GOSIA ANALYSIS

Using known spectroscopic data (lifetime, mixing and branching ratios):

- **16 B(E2) extracted**
 $B(E3; 3_1^- \rightarrow 0_1^+) = 33(3) \text{ W.u.}$
- $Q_s(2_1)$, $Q_s(2_2)$
- **Deformation parameters ($\langle Q^2 \rangle$, $\langle \delta \rangle$) for the 0_1 and 0_2 states using quadrupole sum rules**
 Extracted also the $\langle Q^4 \rangle$ value related to the softness in deformation
 $\sigma(Q^2) = (\langle Q^4 \rangle - (\langle Q^2 \rangle)^2)^{1/2}$



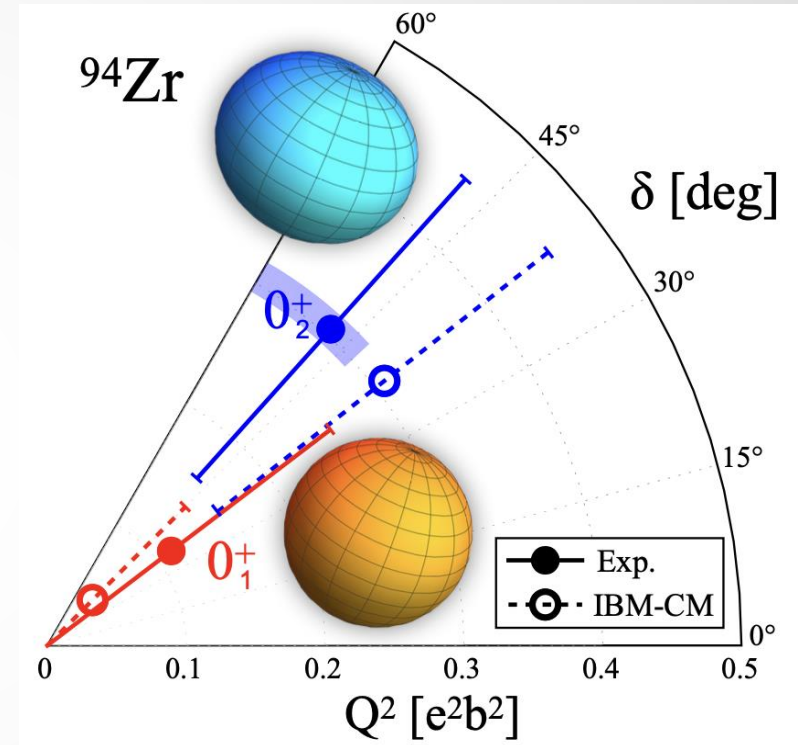
J_i	$\langle Q^2 \rangle [e^2b^2]$		$\sigma(Q^2) [e^2b^2]$		$\langle \cos(3\delta) \rangle$	
	Exp.	Th.	Exp.	Th.	Exp.	Th.
0_1^+	0.112(4)	0.046	0.143(4)	0.094	-0.37(7)	-0.72
0_2^+	0.305(12)	0.308	0.14(3)	0.153	-0.8(2)	-0.4

^{94}Zr – COULEX EXPERIMENT @LNL – GOSIA ANALYSIS

Using known spectroscopic data (lifetime, mixing and branching ratios):

- **16 B(E2) extracted**
 $B(E3; 3_1^- \rightarrow 0_1^+) = 33(3) \text{ W.u.}$
- $Q_s(2_1)$, $Q_s(2_2)$
- **Deformation parameters ($\langle Q^2 \rangle$, $\langle \delta \rangle$)**
 for the 0_1 and 0_2 states using
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 deformation

$$\sigma(Q^2) = (\langle Q^4 \rangle - (\langle Q^2 \rangle)^2)^{1/2}$$



J_i	$\langle Q^2 \rangle [e^2b^2]$		$\sigma(Q^2) [e^2b^2]$		$\langle \cos(3\delta) \rangle$	
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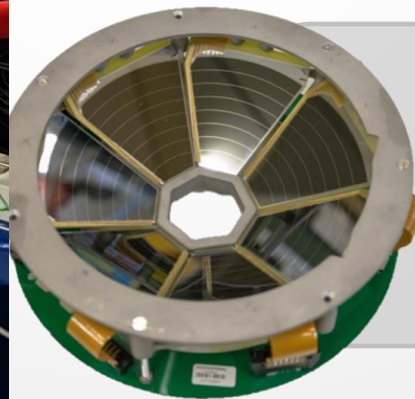
^{96}Zr – COULEX EXPERIMENT @LNL – ANALYSIS ONGOING

Beam : ^{58}Ni 160 MeV 3 pA

Target : self-supporting ^{96}Zr 1mg/cm²



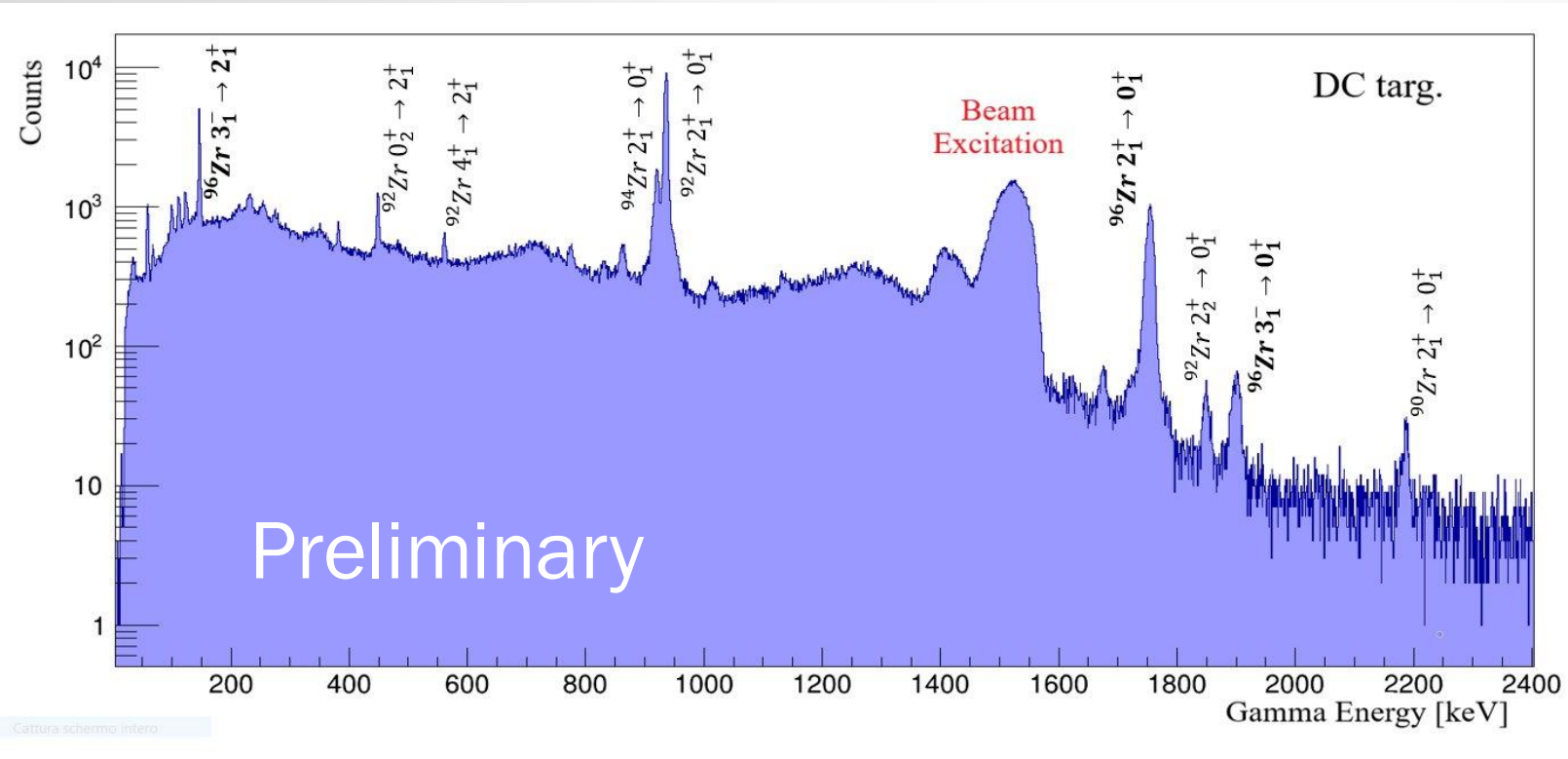
AGATA array (11 ATCs),
close-up position.



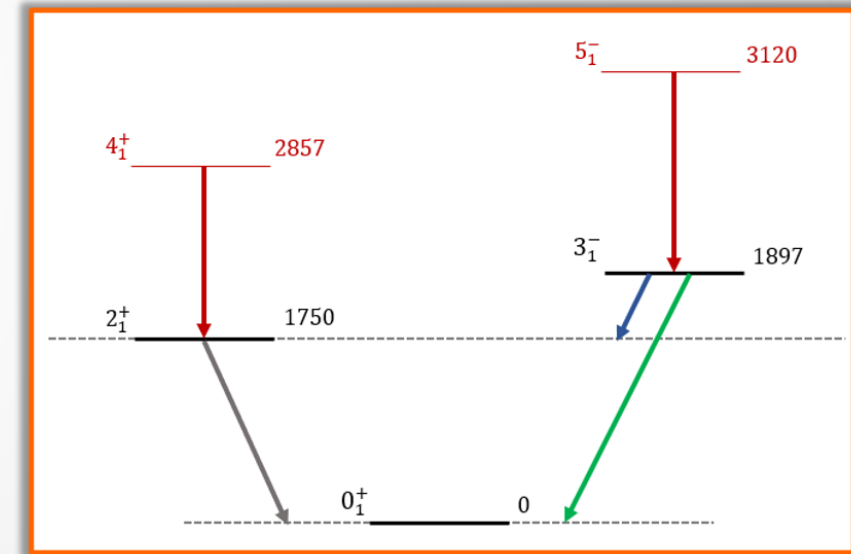
SPIDER modular array of Si detectors
segmented into 8 annular strips (junction
side).

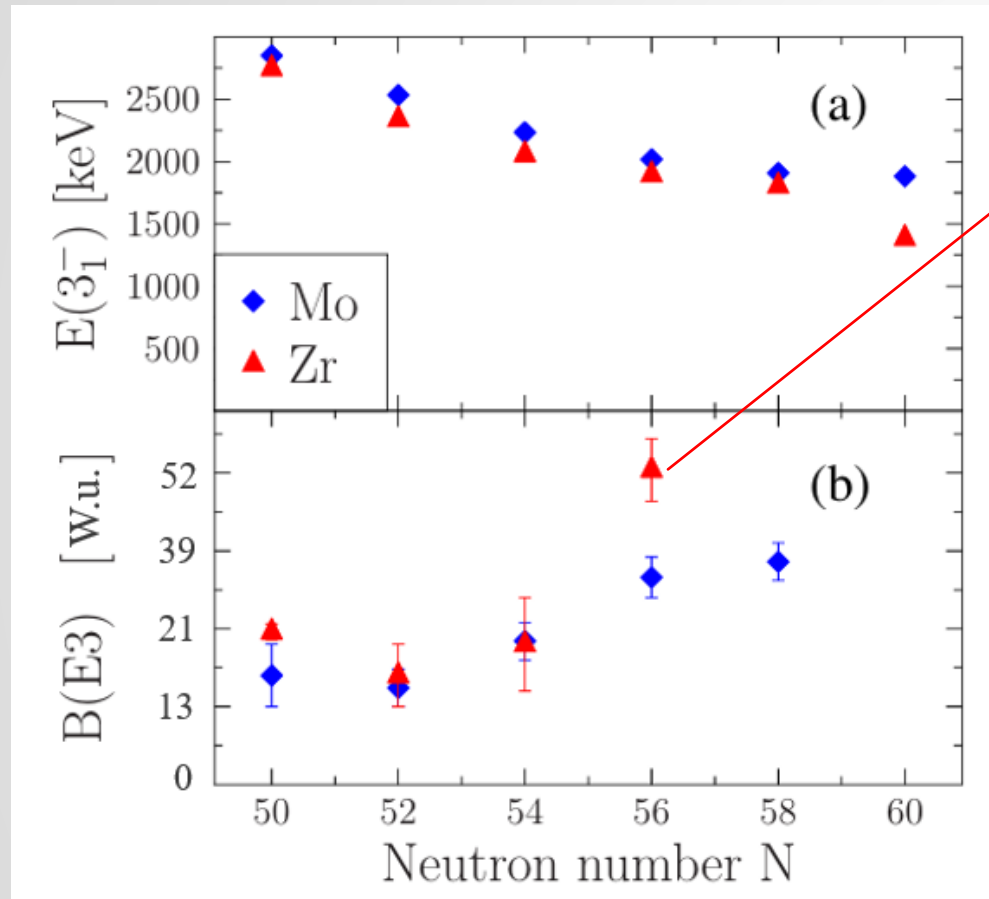
$\Theta_{\text{Lab}} = 126^\circ - 162^\circ$ (detection of
backscattered ^{58}Ni ions)



^{96}Zr – COULEX EXPERIMENT @LNL – ANALYSIS ONGOING γ -particle spectrum

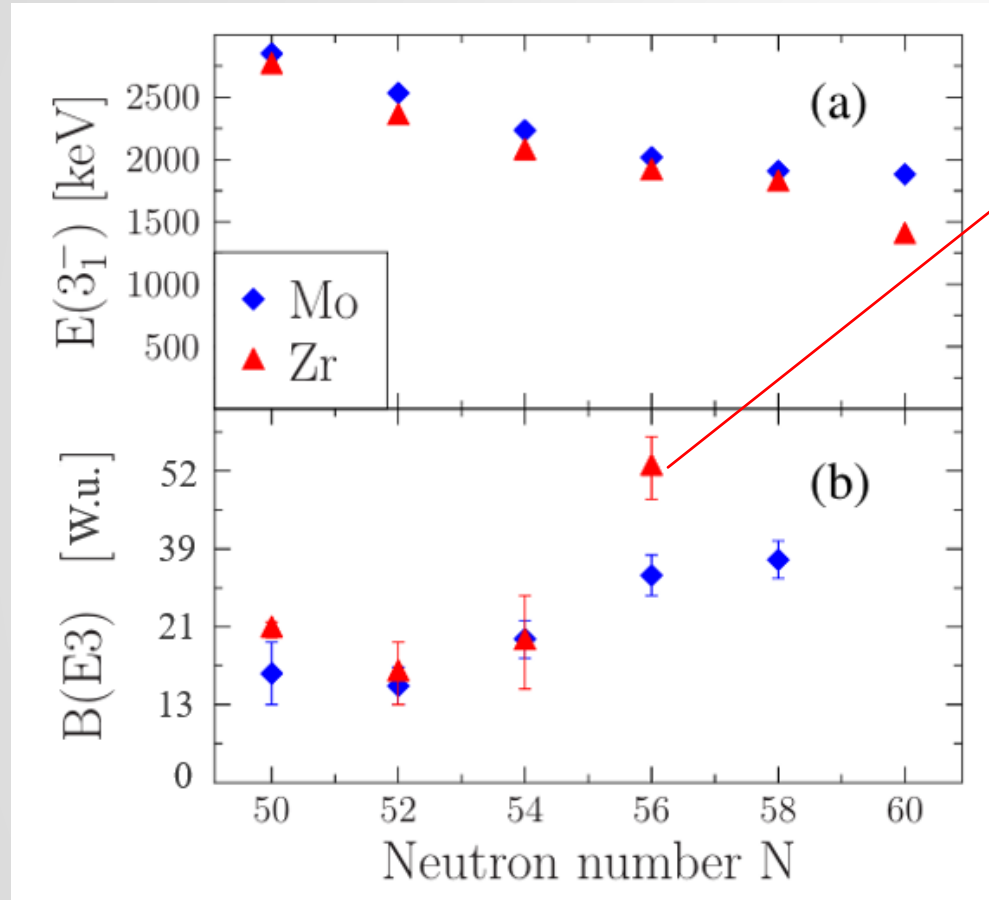
Level scheme



^{96}Zr – COULEX EXPERIMENT @LNL – B(E3)

$B(E3, 3_1^- \rightarrow 0_1^+)$ value in ^{96}Zr strikingly high (evaluated value: 53(6) W.u.), long-standing challenge for theory

The revised value $B(E3) = 42(3)$ W.u. resulting from a new measurement of E1/E3 branching ratio in ^{96}Zr (Ł. Iskra *et al*, Phys. Lett. B 788 (2019)) is in better agreement with the experimental trend

^{96}Zr – COULEX EXPERIMENT @LNL – B(E3) PRELIMINARY RESULTS

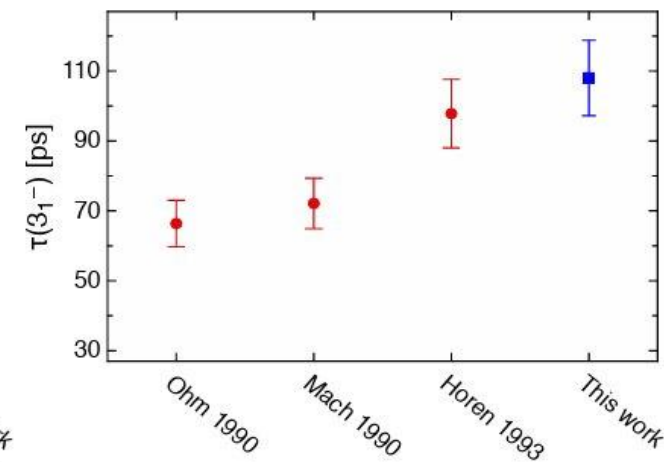
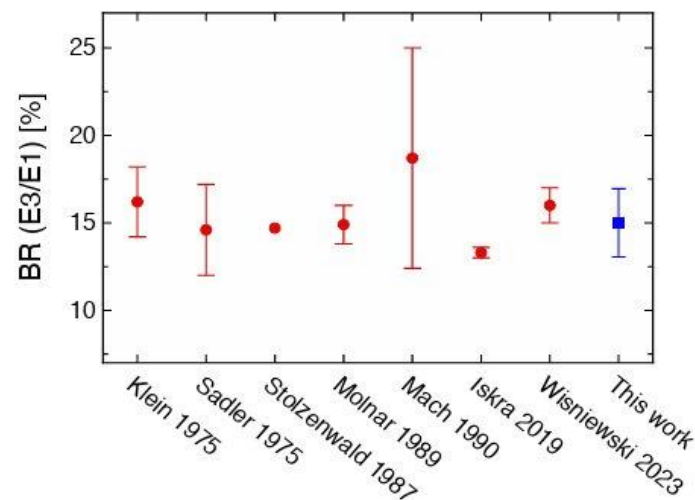
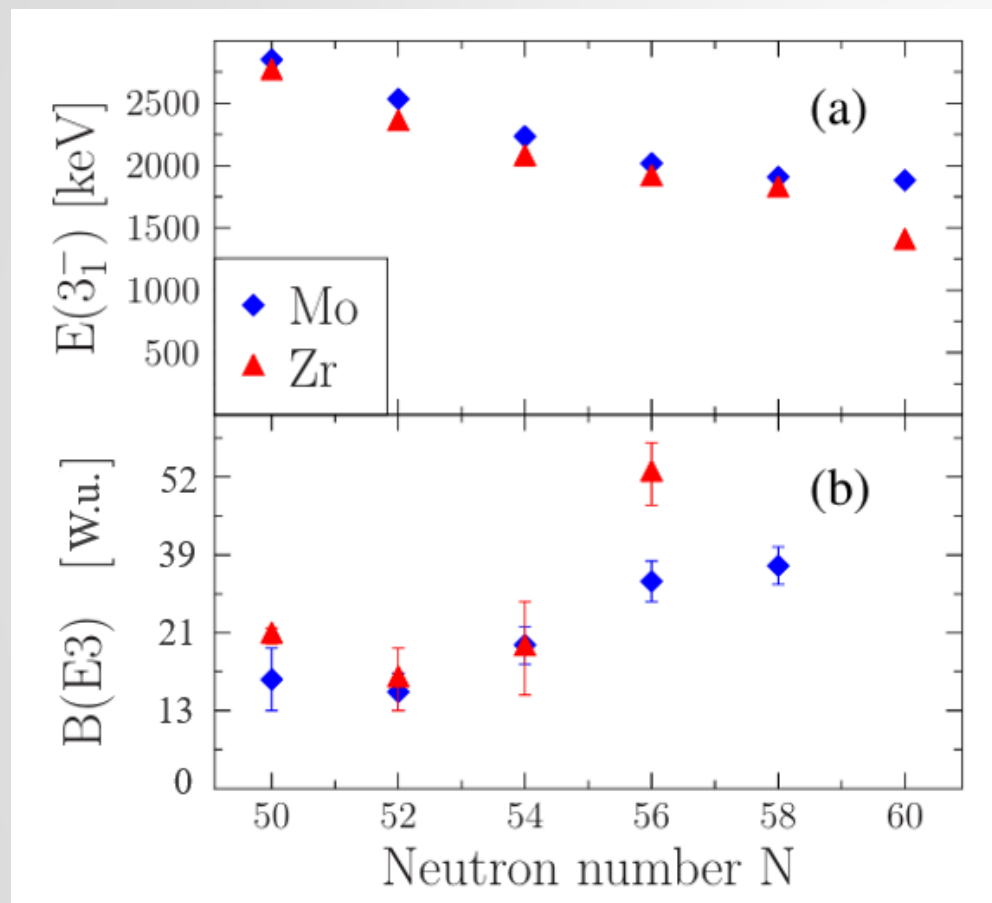
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Our Preliminary results are:

$$B(E1, 3_1^- \rightarrow 2_1^+) = 114(13) \cdot 10^{-4} \text{ W.u.}$$

$$B(E3, 3_1^- \rightarrow 0_1^+) = 41(3) \text{ W.u.}$$

^{96}Zr – COULEX EXPERIMENT @LNL – B(E3) PRELIMINARY RESULTS

Our Preliminary results are:

$$B(E1, 3_1^- \rightarrow 2_1^+) = 114(13) \cdot 10^{-4} W.u.$$

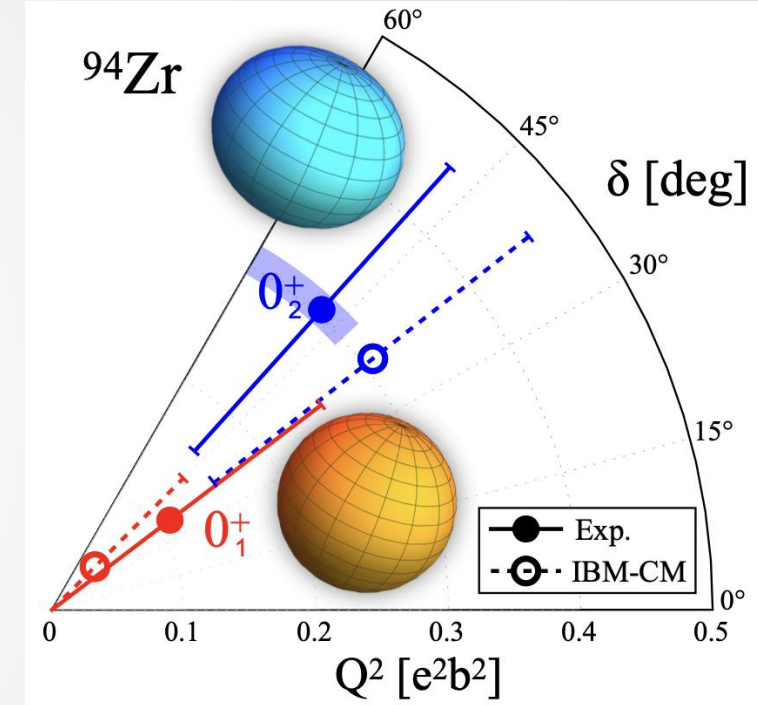
$$B(E3, 3_1^- \rightarrow 0_1^+) = 41(3) W.u.$$

^{96}Zr – COMPLEMENTARY EXPERIMENTS @LNL

- Two-phonon octupole excitation in ^{96}Zr :
 - Measured E3/E1 branching ratio in the 3^- decay.
 - Observation of $6^+ \rightarrow 3^-$ transition
 - SETUP: AGATA + SAURON + PLUNGER
- Combined lifetime and transition-probability measurements in ^{96}Zr via unsafe Coulomb excitation :
 - Investigating the properties of 2^+ and 4^+ band members to provide detailed spectroscopic data on presumed coexisting structures
 - Verify the lifetime of the 6^+ , 3^- states and understanding the puzzling trend in octupole collectivity in Zr isotopes and testing the two-phonon vibration hypothesis
 - SETUP: AGATA + PRISMA + PLUNGER

CONCLUSION

- ^{94}Zr : Spectroscopic quadrupole moments extracted for the first and the second 2^+ states
 Quadrupole invariants extracted for the ground state and the 0_2 state



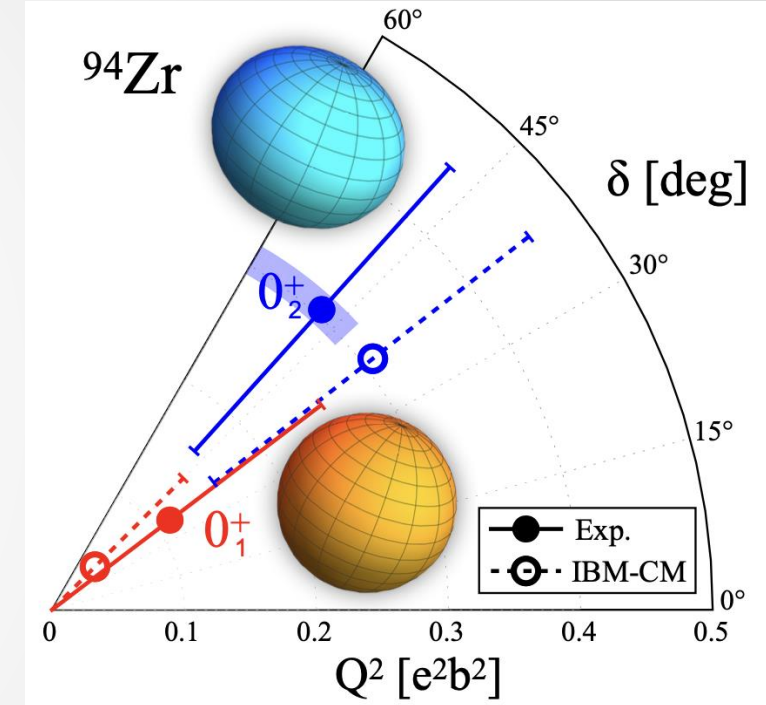
CONCLUSION

- ^{94}Zr : Spectroscopic quadrupole moments extracted for the first and the second 2^+ states

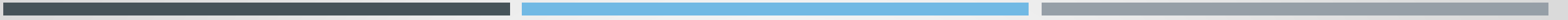
Quadrupole invariants extracted for the ground state and the 0_2 state

- ^{96}Zr : Octupole collectivity under analysis

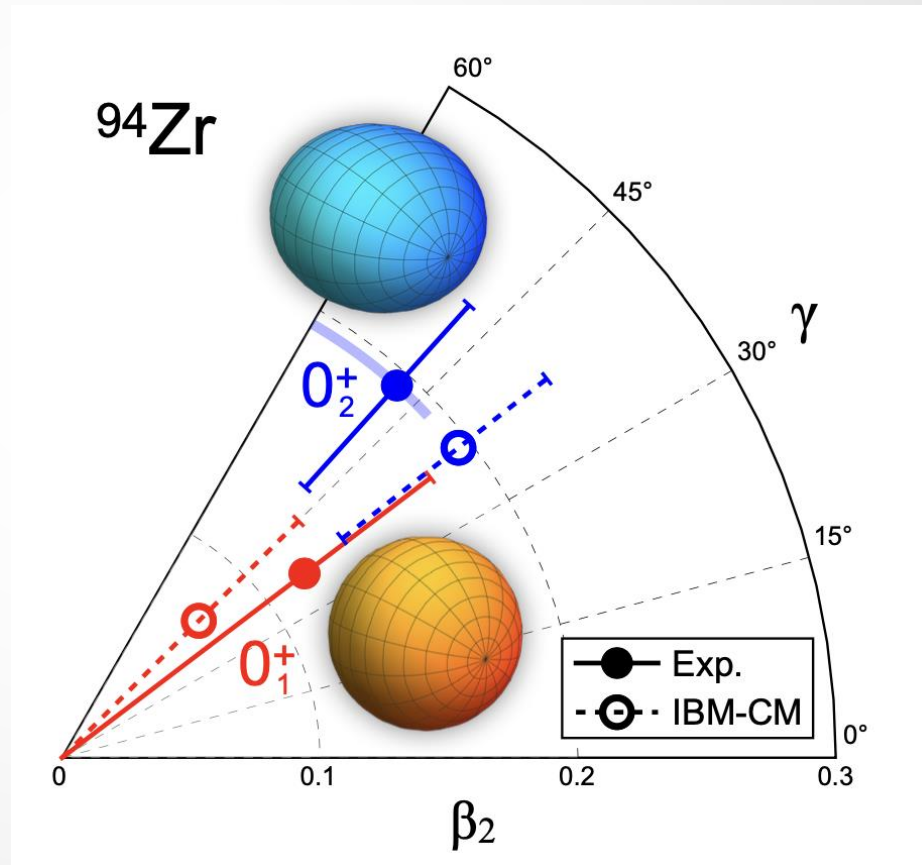
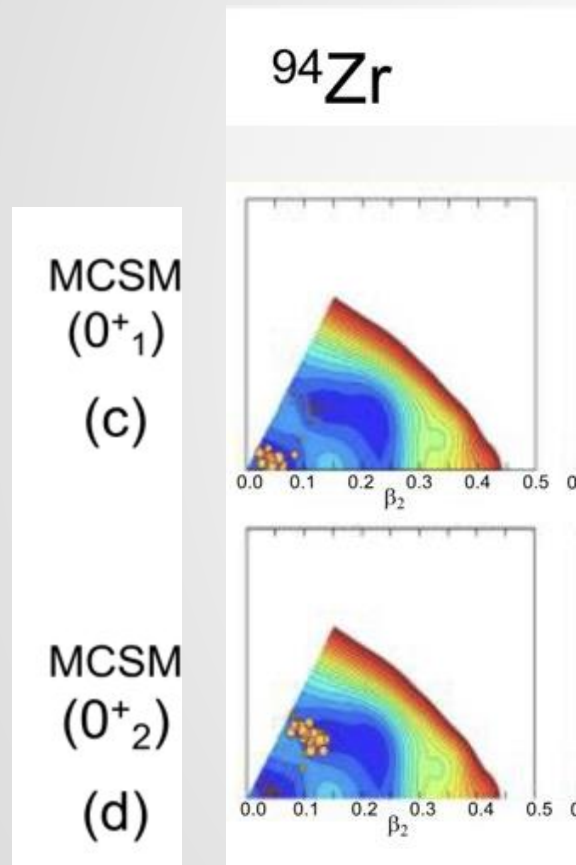
$$B(E3, 3_1^- \rightarrow 0_1^+) = 41(3) W.u.$$

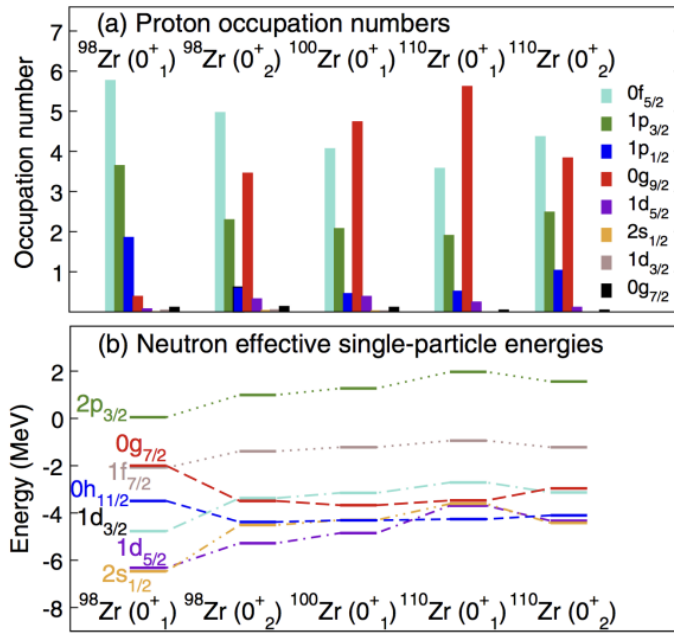


Thank you!



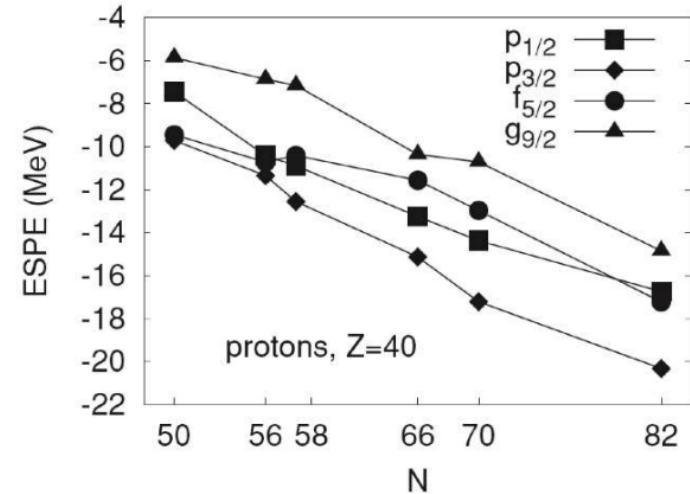
$\langle \beta_2 \rangle = \left(\frac{3}{4\pi} Z R^2 \right)^{-1} \cdot \sqrt{\langle Q^2 \rangle}$, where $R = 1.2 A^{1/3}$ [fm], and $\langle \gamma \rangle = \langle \delta \rangle$ [38]. For ^{94}Zr , $\langle \beta_2 \rangle \approx 0.35 \sqrt{\langle Q^2 \rangle}$.





T. Togashi et al, PRL 117, 172502 (2016)

- p-n tensor interaction reduces the $Z=40$ gap when $\nu g_{7/2}$ is being filled
- 0^+_{2-} states created by 2p-2h (+ 4p-4h...) excitation across $Z=40$
- very different configurations and small mixing of 0^+_{1-} and 0^+_{2-}



K. Sieja et al, PRC 79, 064310 (2009)

