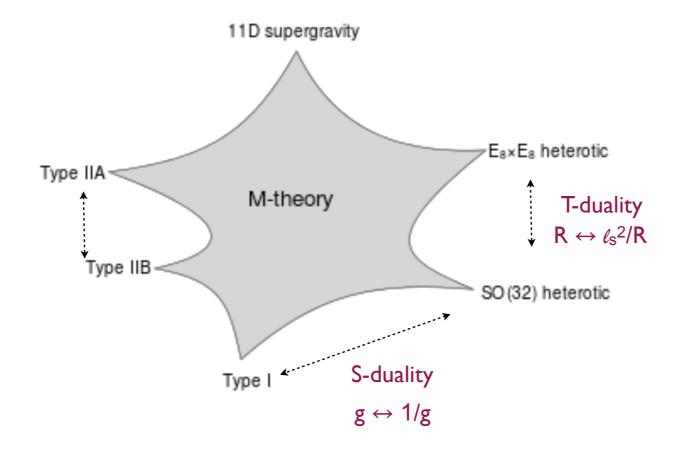
String theory, from the landscape to the swampland

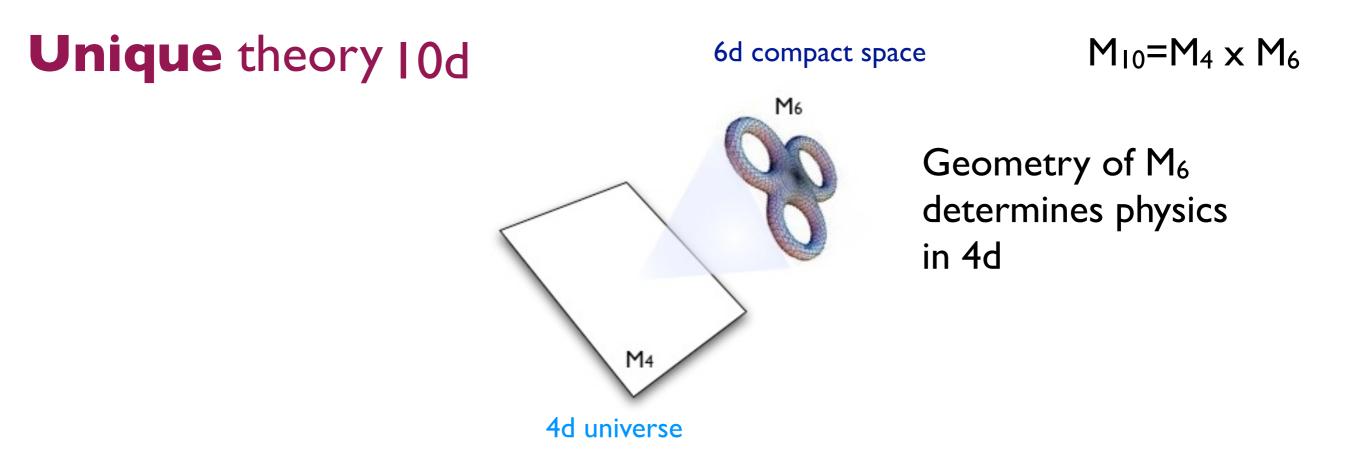
Mariana Graña Institut de Physique Théorique CEA / Université Paris-Saclay France

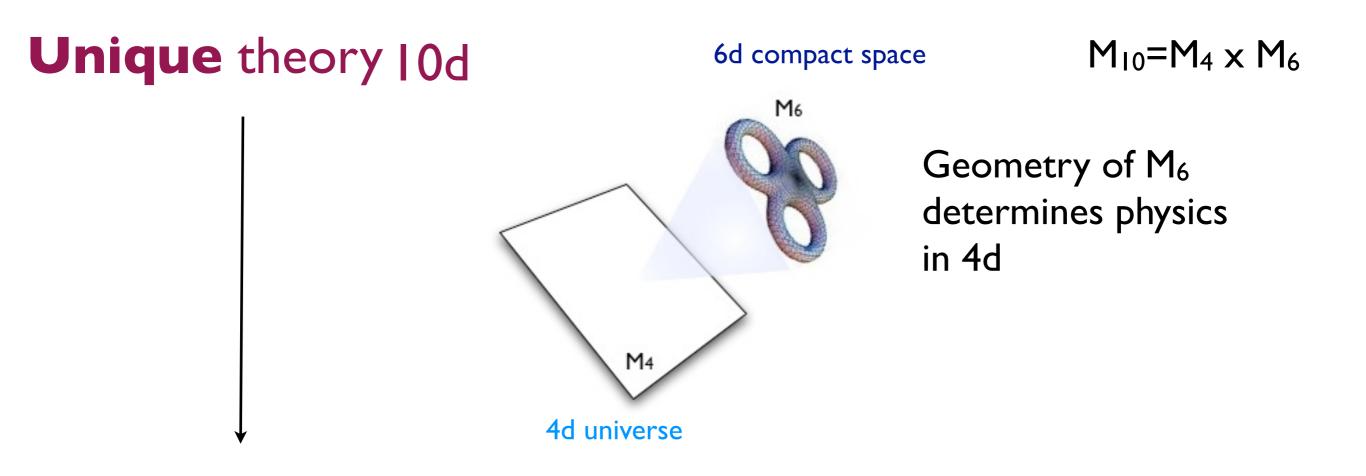
RPP, Jussieu, January 2024

String theory

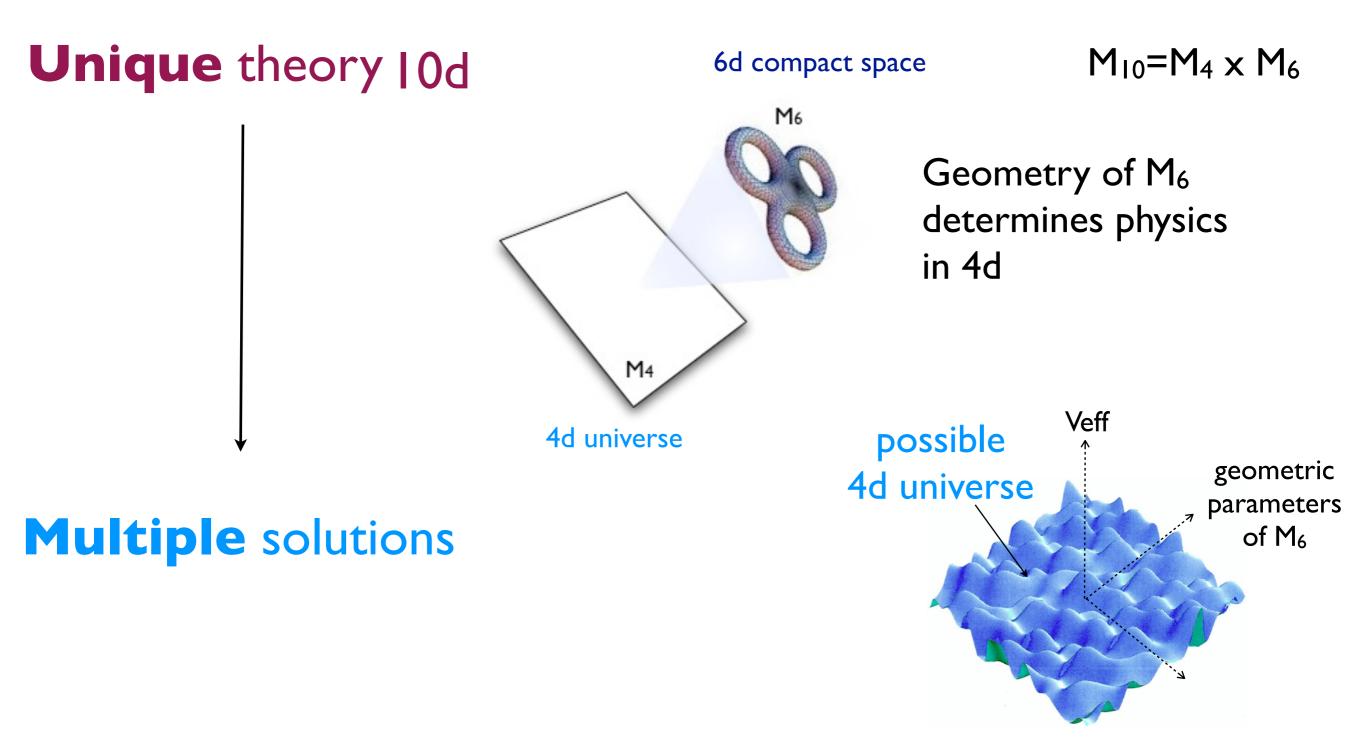
- A remarkable theory of quantum gravity, calculable
- Second superstring revolution ('95): unique theory!

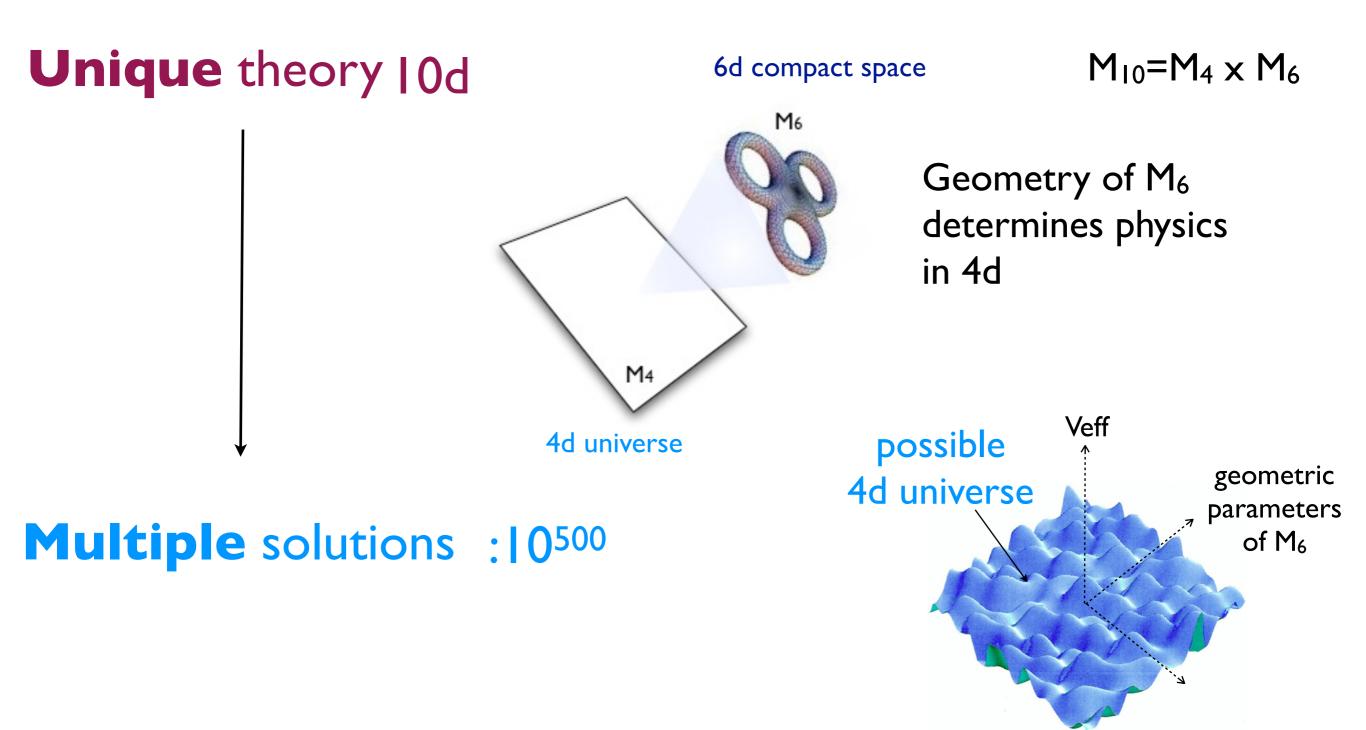


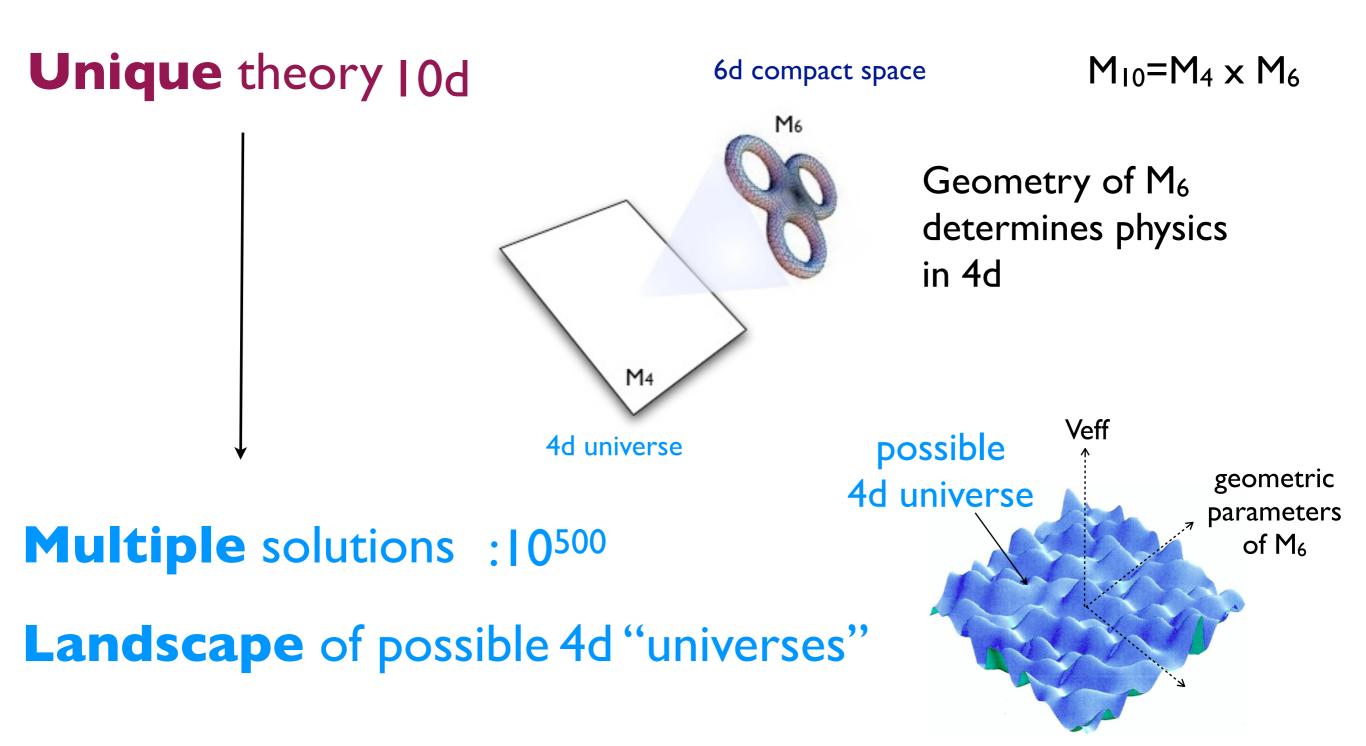


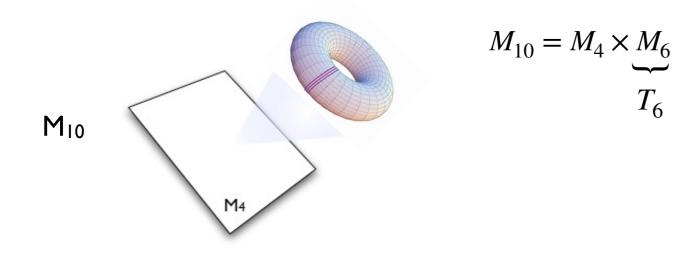


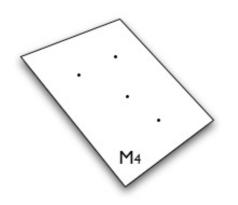
Multiple solutions



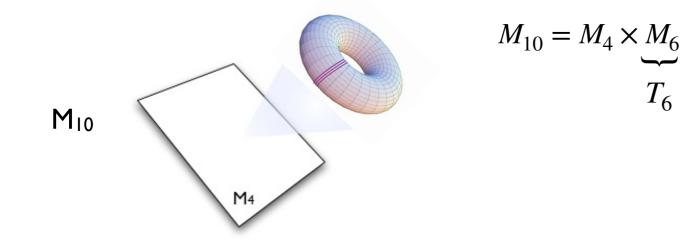


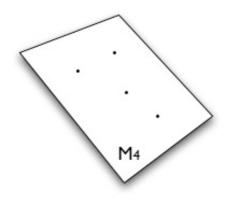




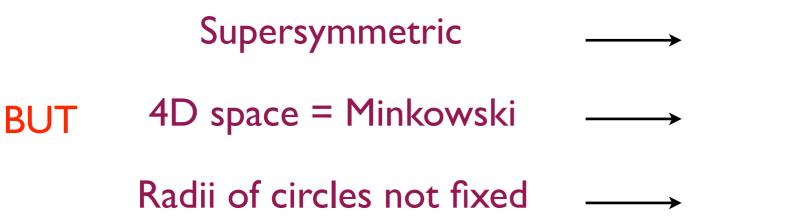


Observable world

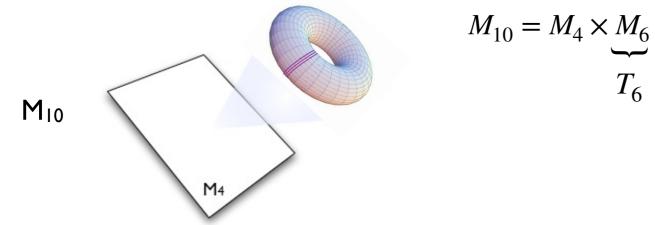


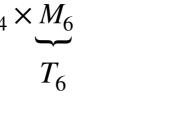


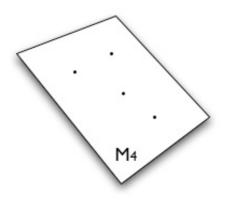
Observable world



- no cosmological constant
- Massless scalars (moduli)





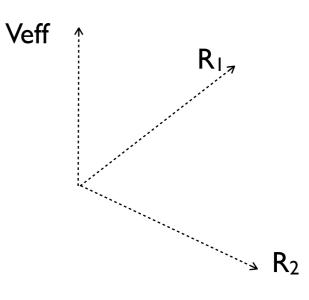


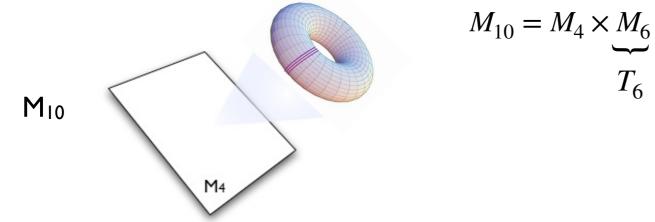


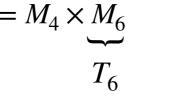


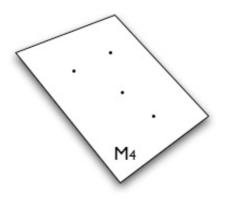
- **BUT** 4D space = Minkowski \longrightarrow
 - Radii of circles not fixed \longrightarrow

- no cosmological constant
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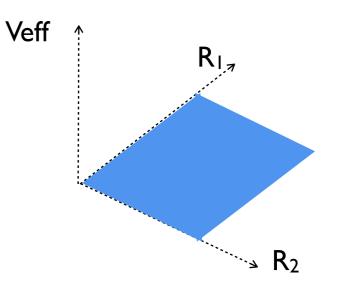


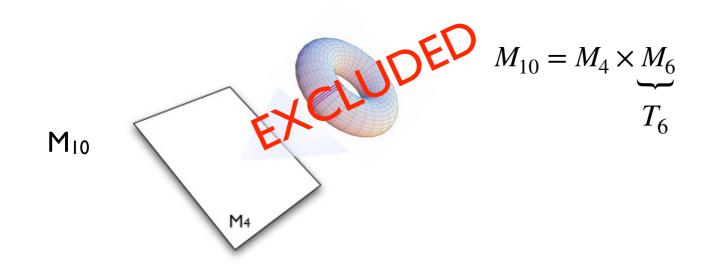


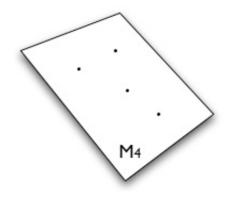
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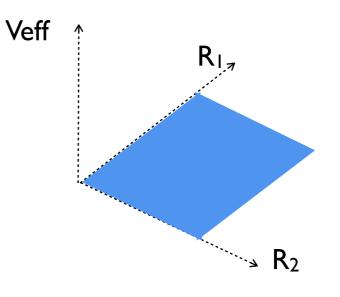


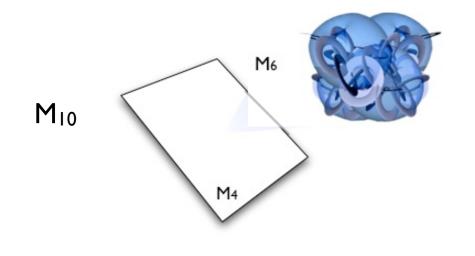




- Supersymmetric _____
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 $M_{10} = M_4 \times M_6$

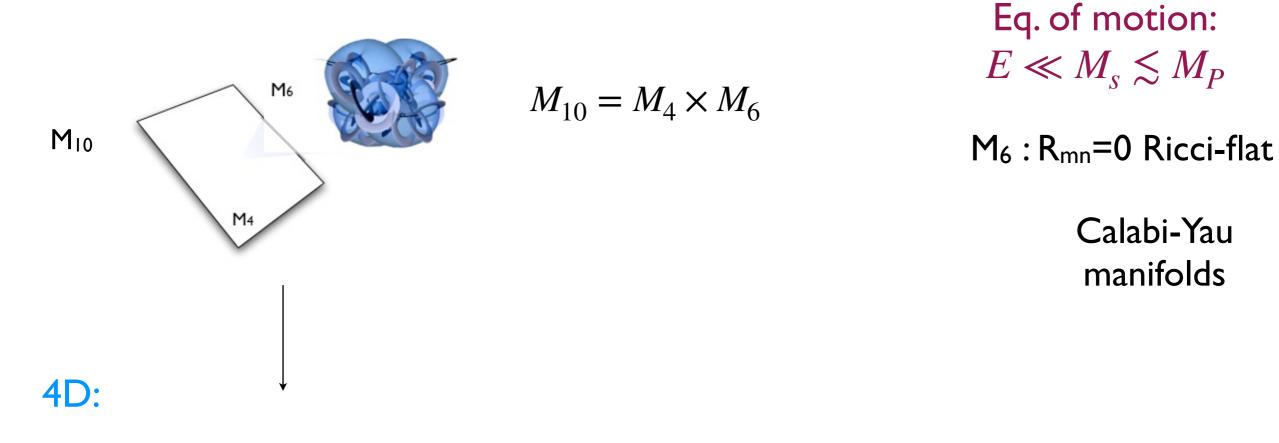
M₁₀

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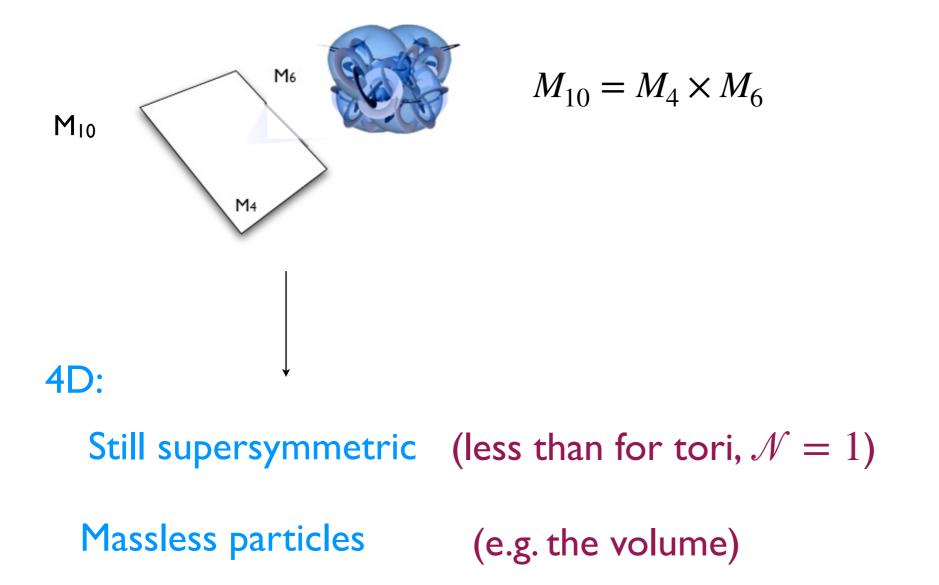
Eq. of motion: $E \ll M_s \lesssim M_P$

M₆ : R_{mn}=0 Ricci-flat

Calabi-Yau manifolds



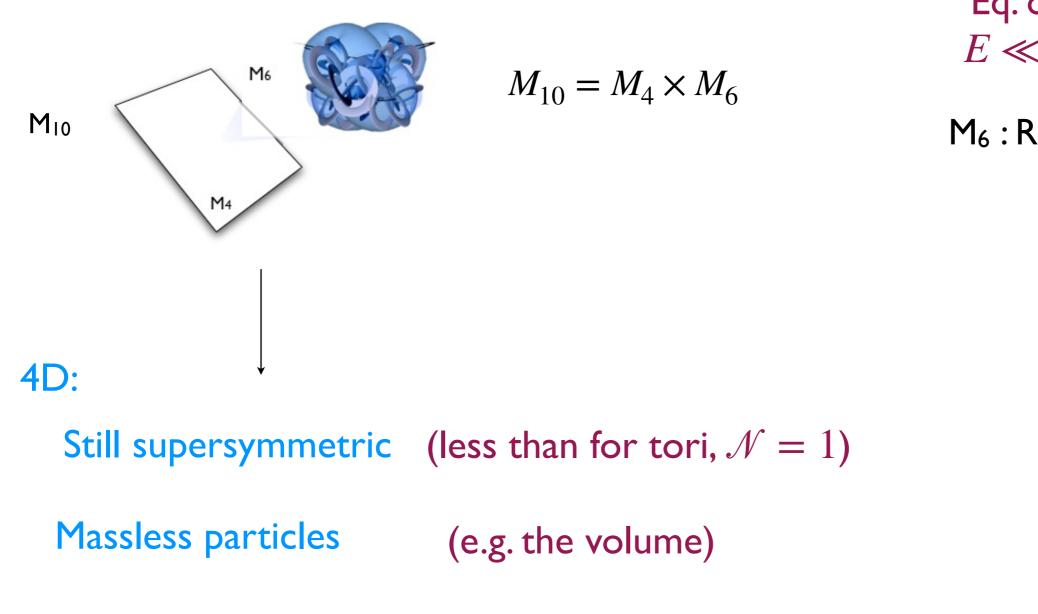
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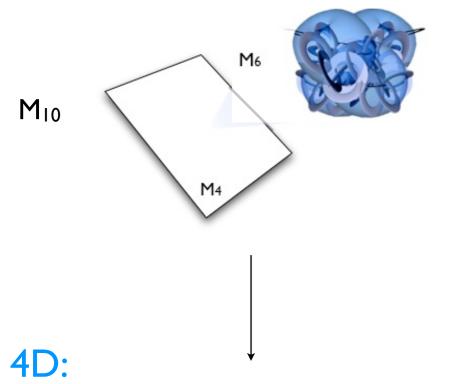


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Richer than tori, can overcome problems

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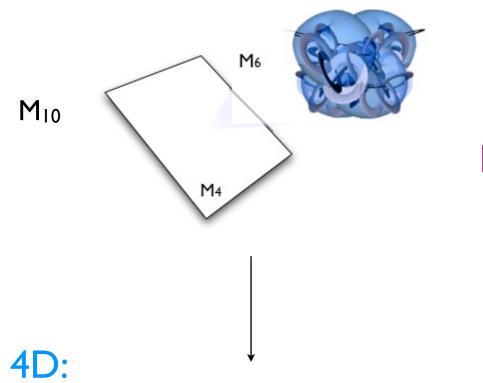
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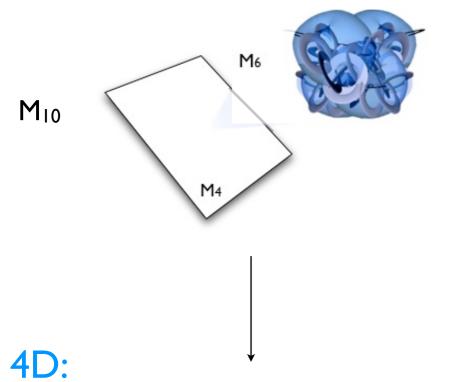
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Landscape of possibles 4d universes

Obtained using Calabi-Yau spaces, and the rest bottom-up, requiring in 4D:

•Standard Model of particles

•Positive cosmological constant (4d de Sitter space)

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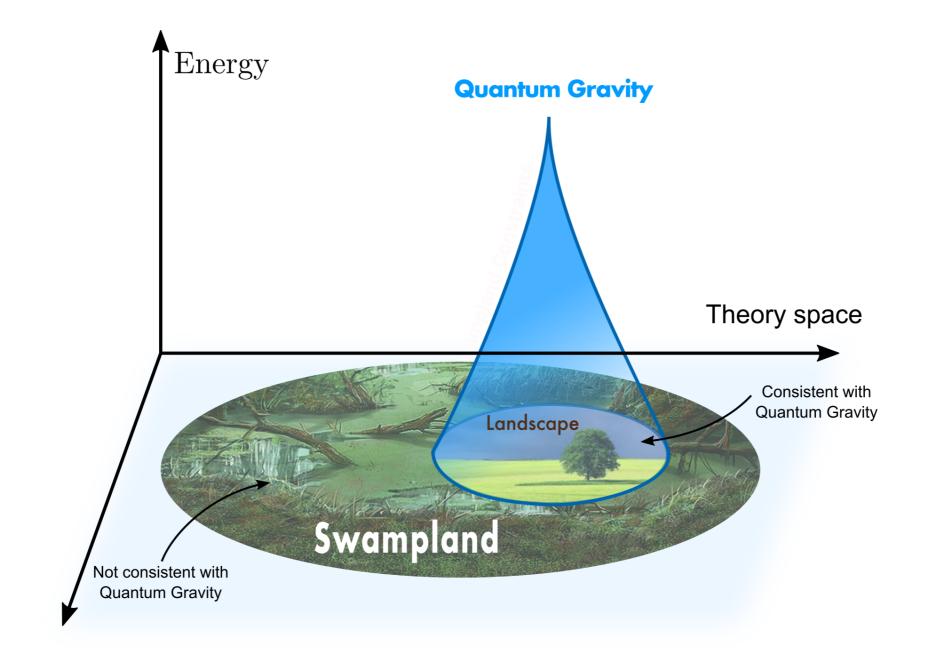
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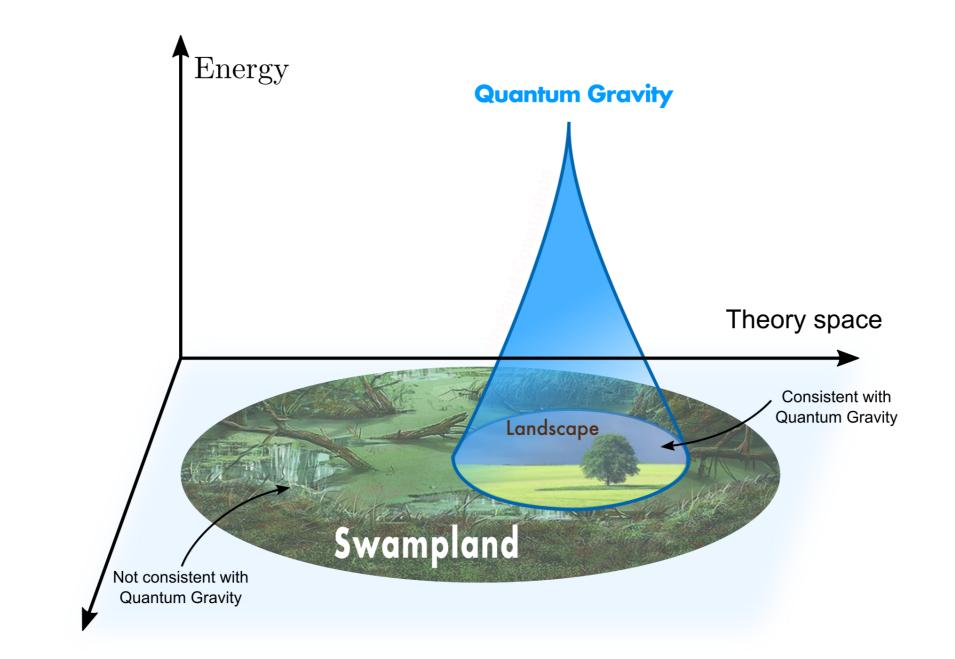
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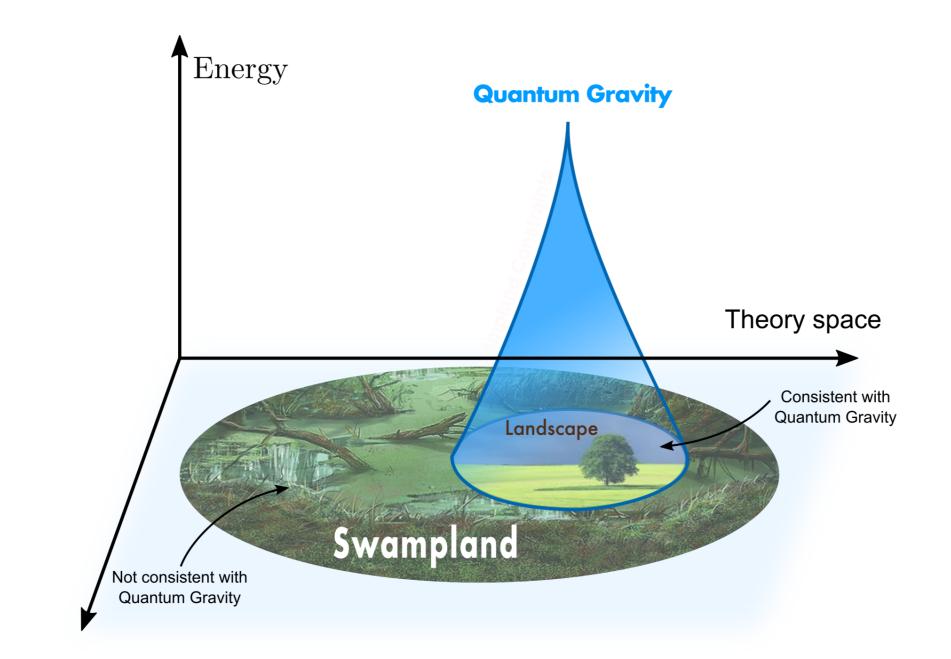
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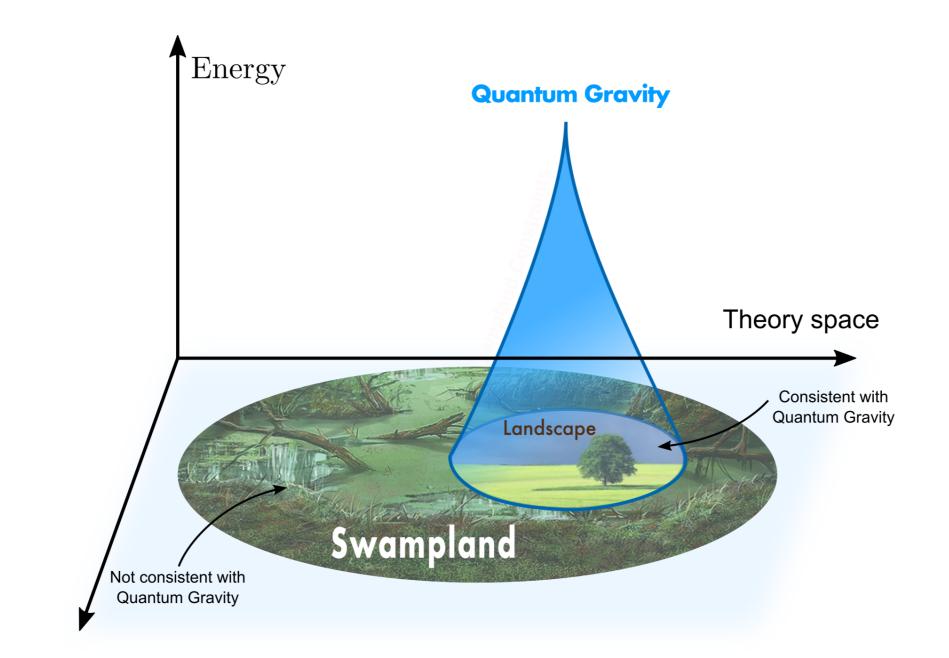




• Series of conjectures on properties of low energy effective Vafa + O(200) people, 2006-on field theories (EFT) to be in the landscape



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An EFT theory is not in the swampland if

(i.e. it is consistent with quantum gravity if it satisfies)

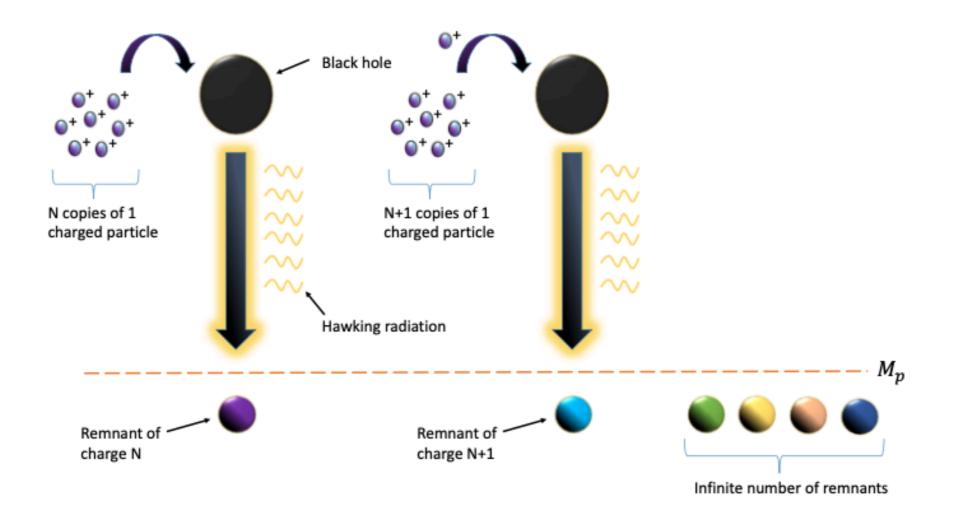
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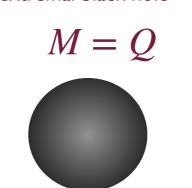


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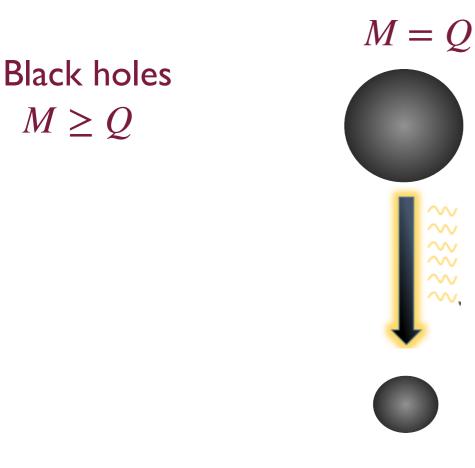
extremal black hole

Black holes $M \ge Q$



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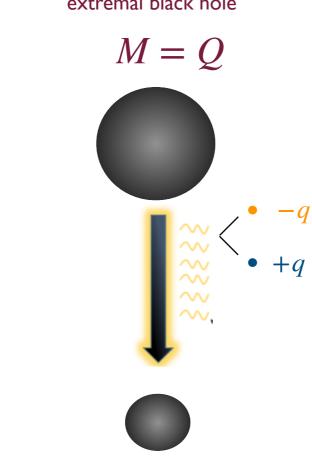
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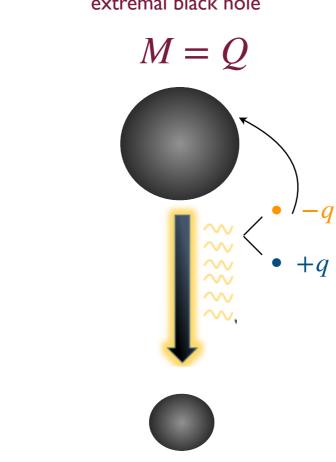


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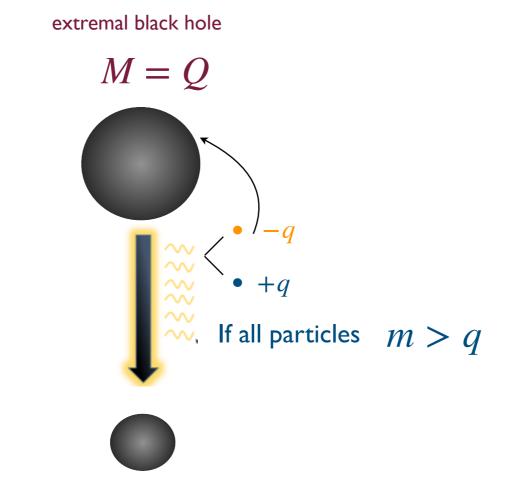


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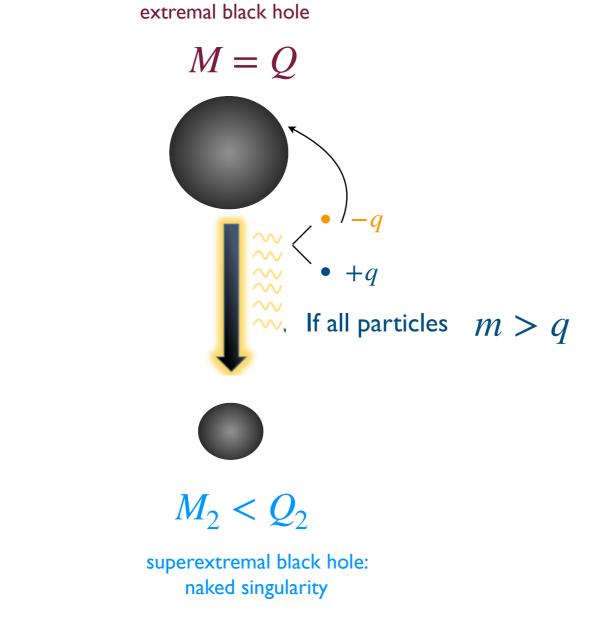
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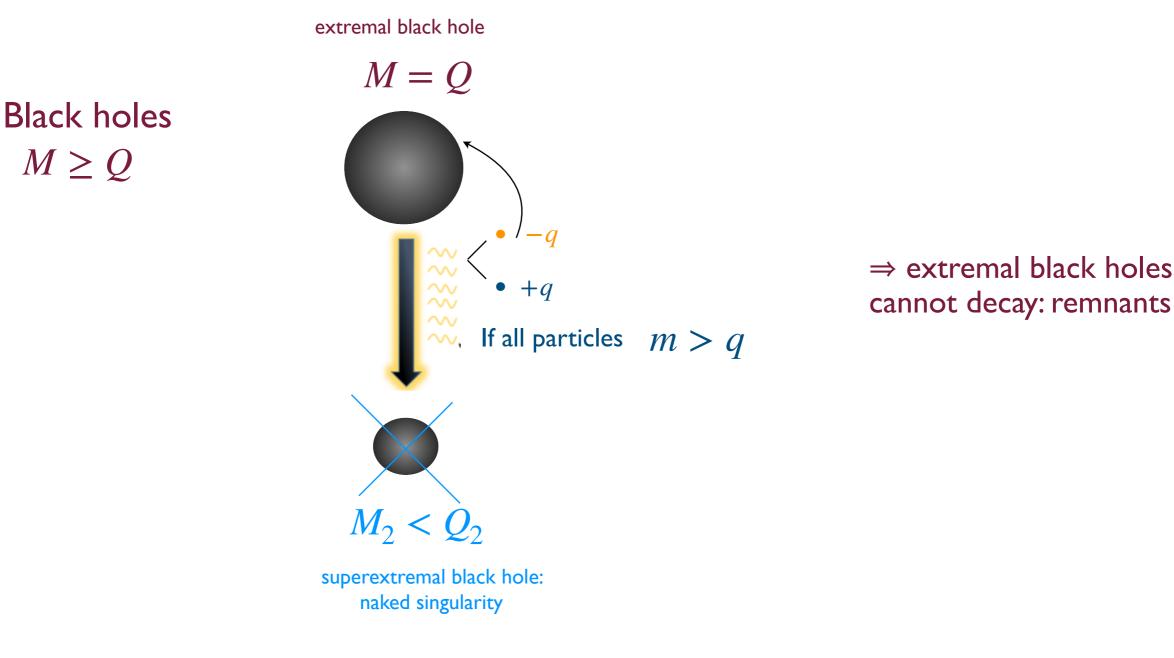


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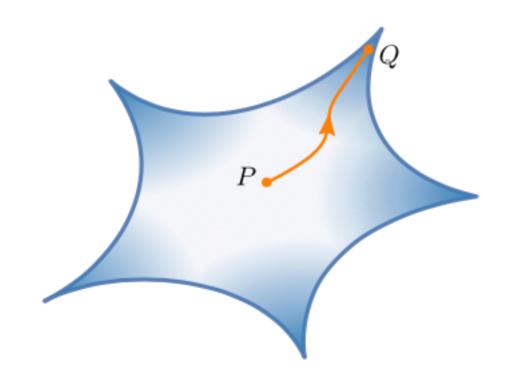
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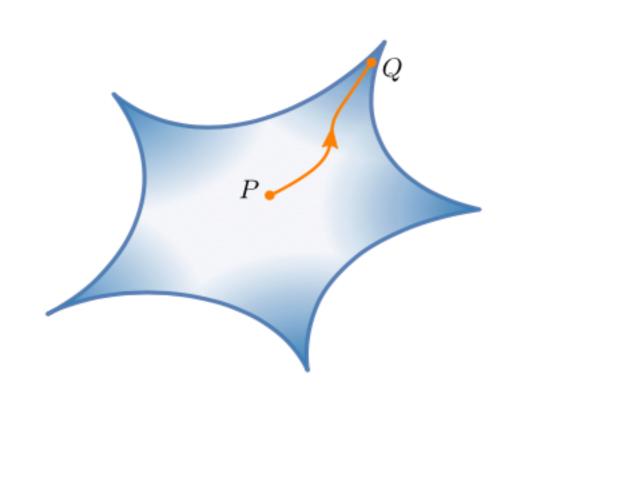




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scalar manifold (moduli space)



ex: compactification on circle Modulus ϕ = R (radius)

$$\mathscr{L}_{10} = \mathscr{R}_{10}$$

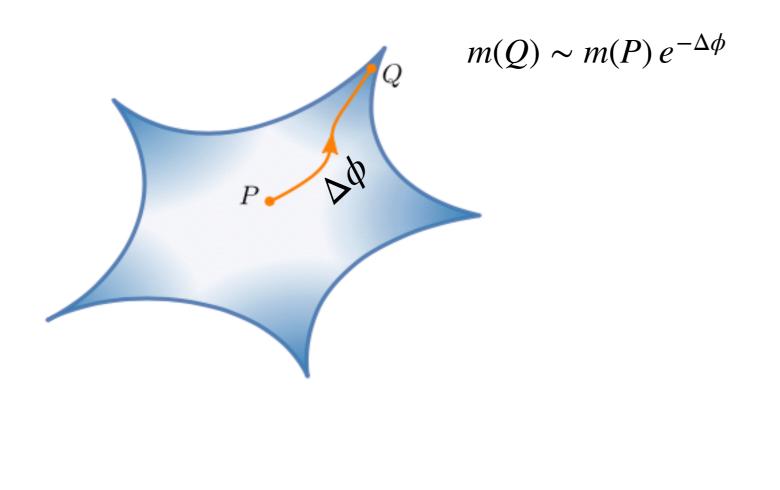
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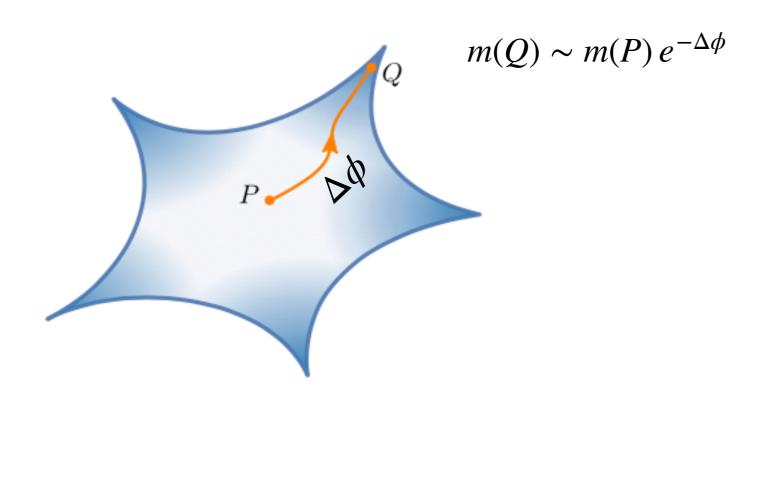
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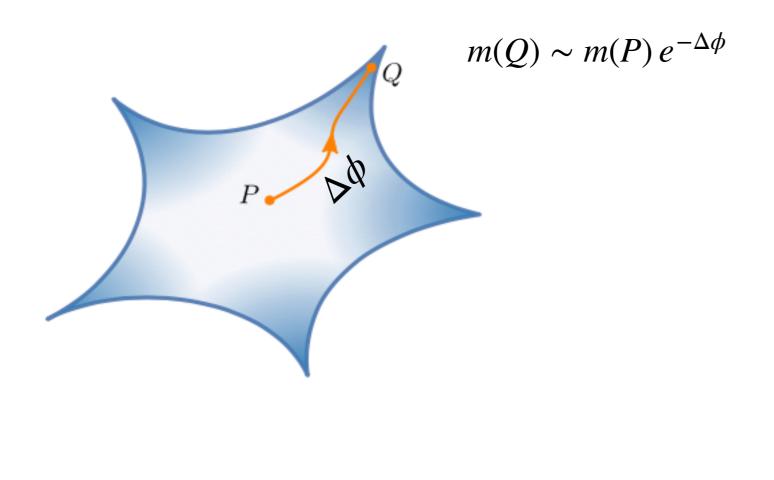
$$\mathscr{L}_{9} = \mathscr{R}_{9} + \frac{1}{R^{2}} \partial_{\mu} R \partial^{\mu} R$$

$$\Delta R = \int_{P}^{Q} \frac{1}{R} dR = \log \left(\frac{R_{Q}}{R_{P}} \right)^{R_{P}}$$

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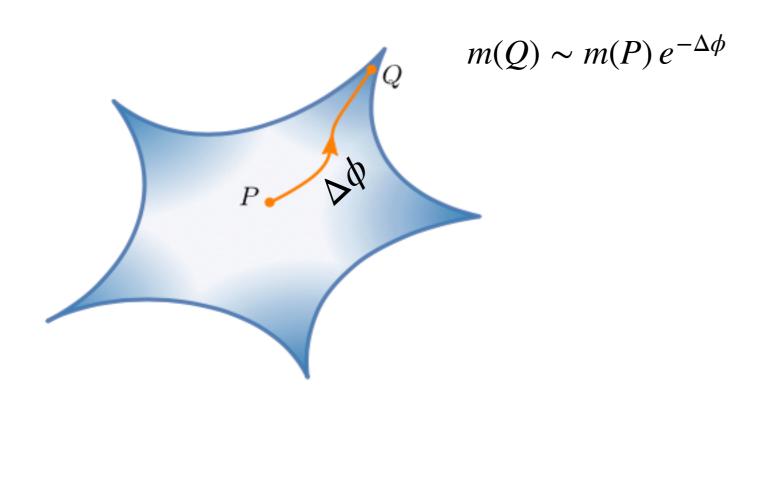
$$m(R) \sim m_{0} e^{-\log R} = \frac{m_{0}}{R}$$

R

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Indeed $m_{KK} = \frac{n}{R}$

• Distance conjecture: an infinite tower of states become exponentially light when approaching boundary of moduli space

 $\mathscr{L} = g_{ij}(\phi) \,\partial_{\mu} \phi^{i} \partial^{\mu} \phi^{j} \qquad \text{scalar manifold (moduli space)}$ $m(Q) \sim m(P) \, e^{-\Delta \phi}$

EFT breaks down when $\Delta \phi \to \infty$

ex: compactification on circle Modulus $\phi = \mathbb{R}$ (radius) $\mathscr{L}_{10} = \mathscr{R}_{10}$ \downarrow $\mathscr{L}_9 = \mathscr{R}_9 + \frac{1}{R^2} \partial_\mu R \partial^\mu R$ $\Delta R = \int_P^Q \frac{1}{R} dR = \log (R_Q/R_P)$

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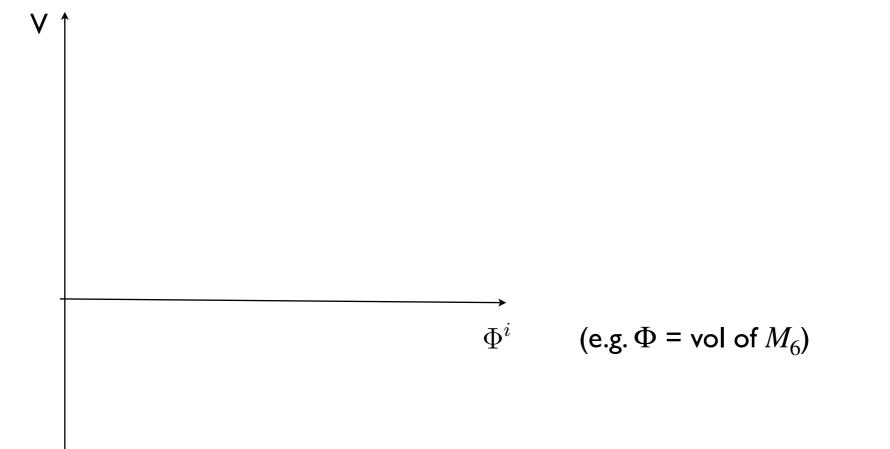
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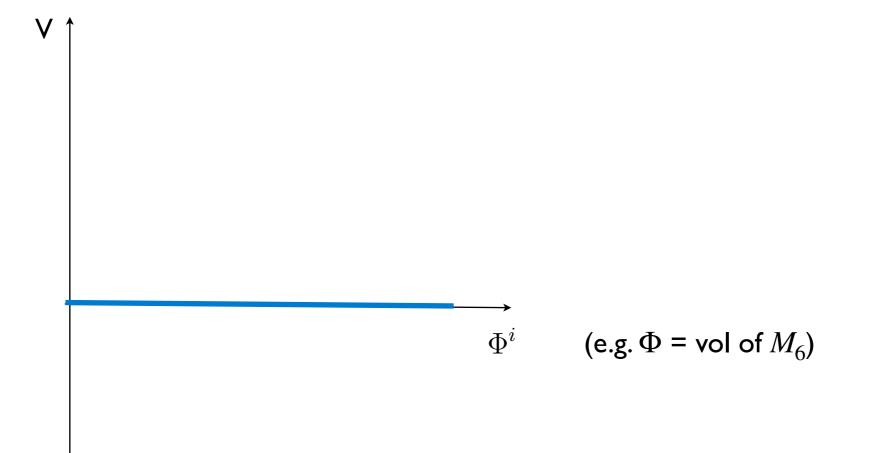
de Sitter space is in the swampland!!

Obied, Ooguri, Spodyneiko, Vafa 18 (OOSV)

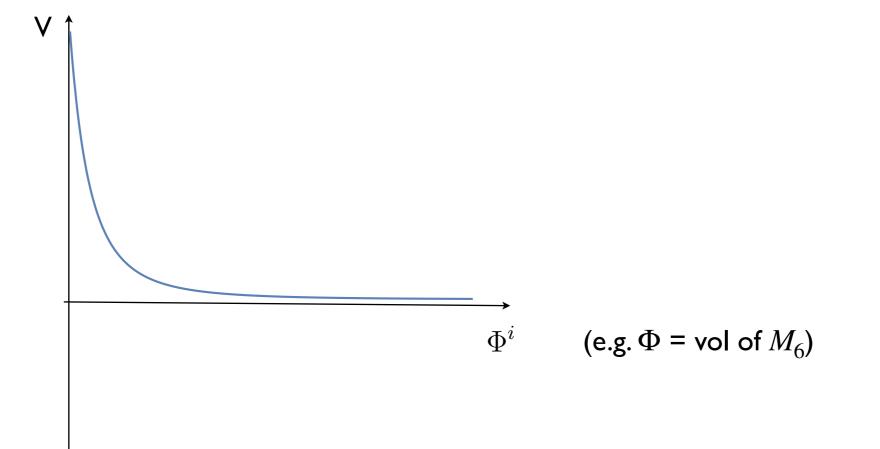
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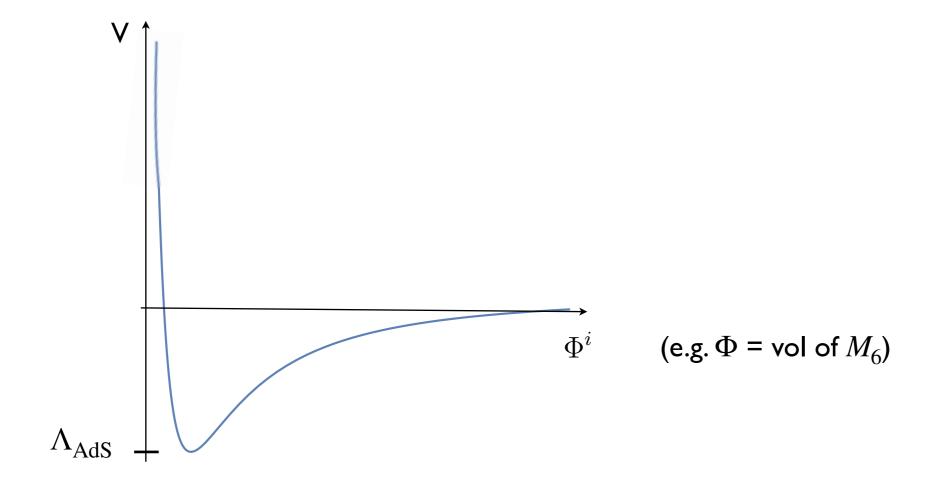
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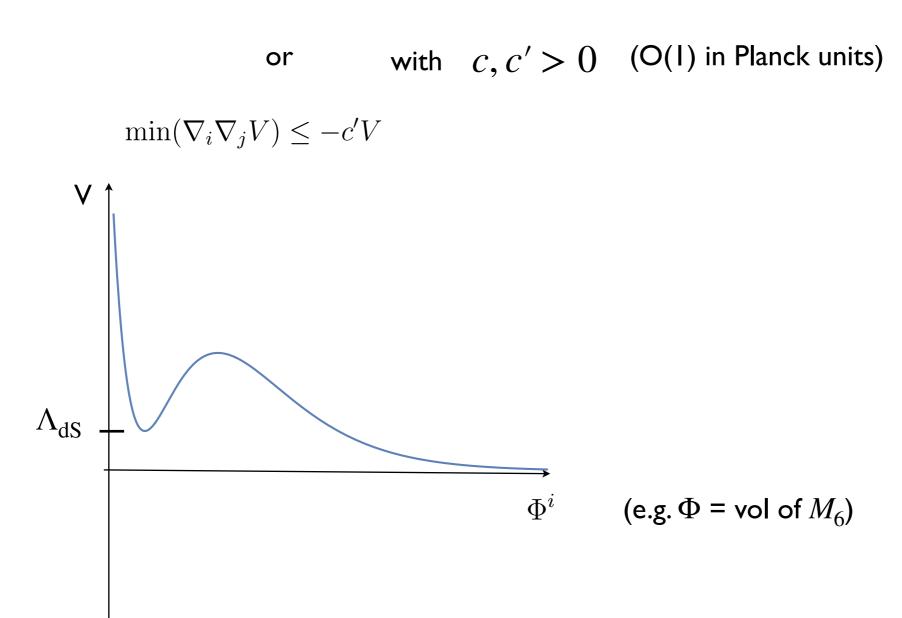


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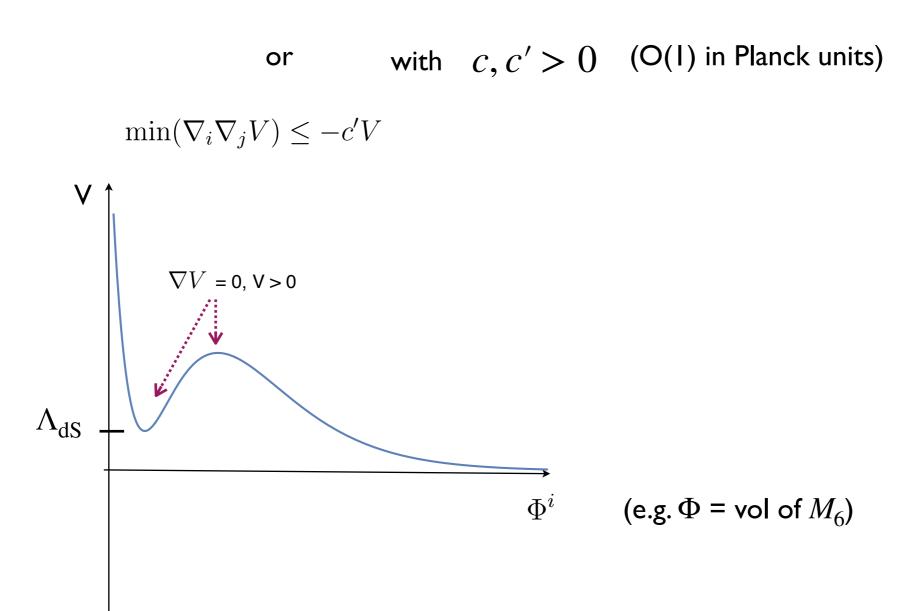
Obied, Ooguri, Spodyneiko, Vafa 18 (OOSV)

In an EFT in the landscape



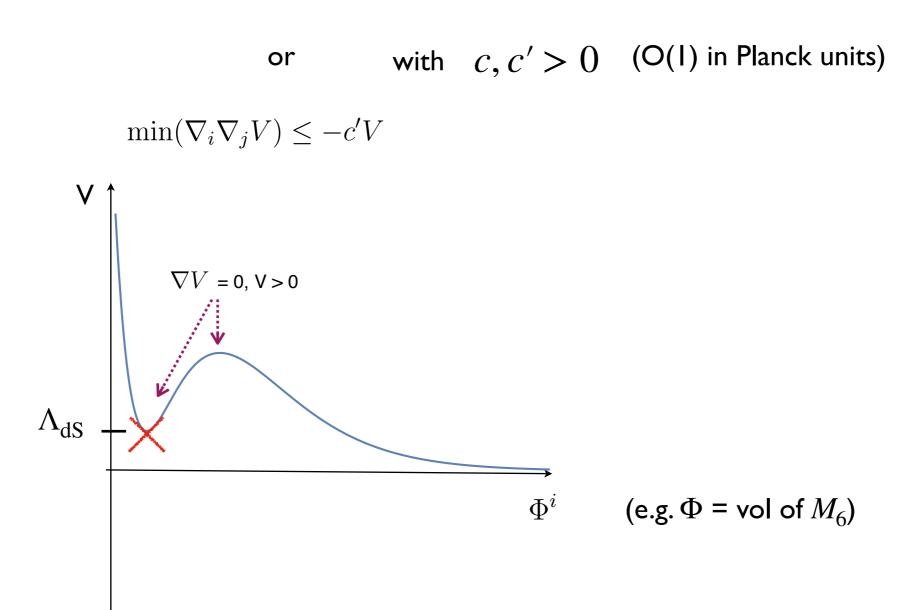
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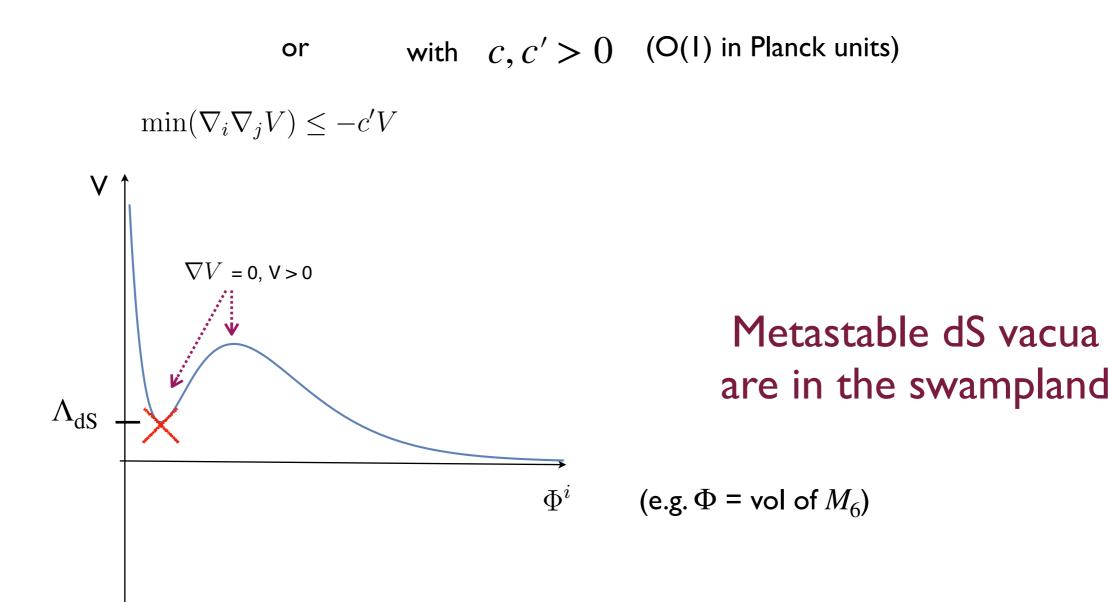
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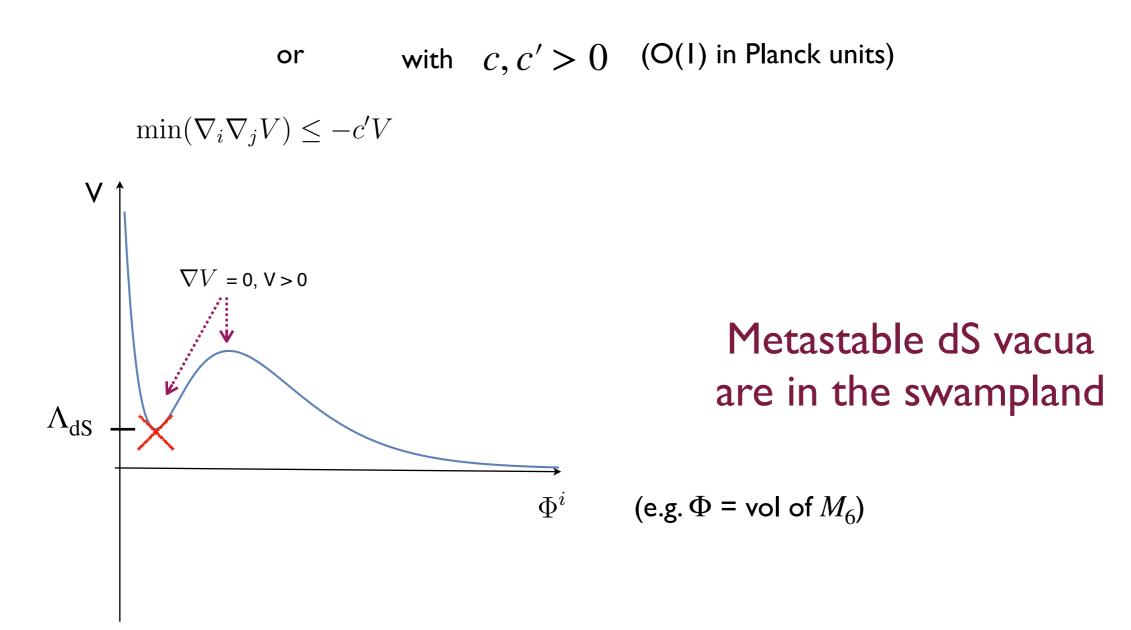
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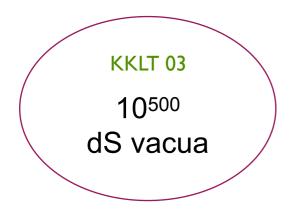
In an EFT in the landscape

The potential satisfies $|\nabla V| \ge cV$



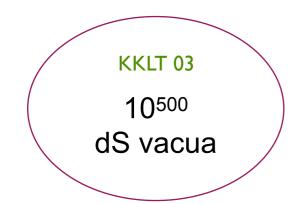
If so, dark energy comes from quintessence field(s)

Back to the landscape: de Sitter vacua in string theory where do we stand?





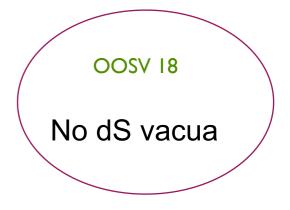
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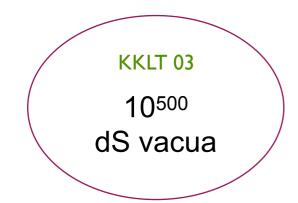
Complicated construction

uses non-perturbative ingredients

Demonstrated to have instabilities with unclear end-points, and other problems



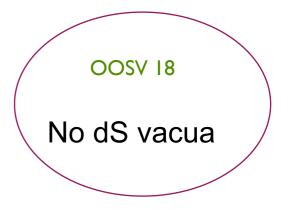
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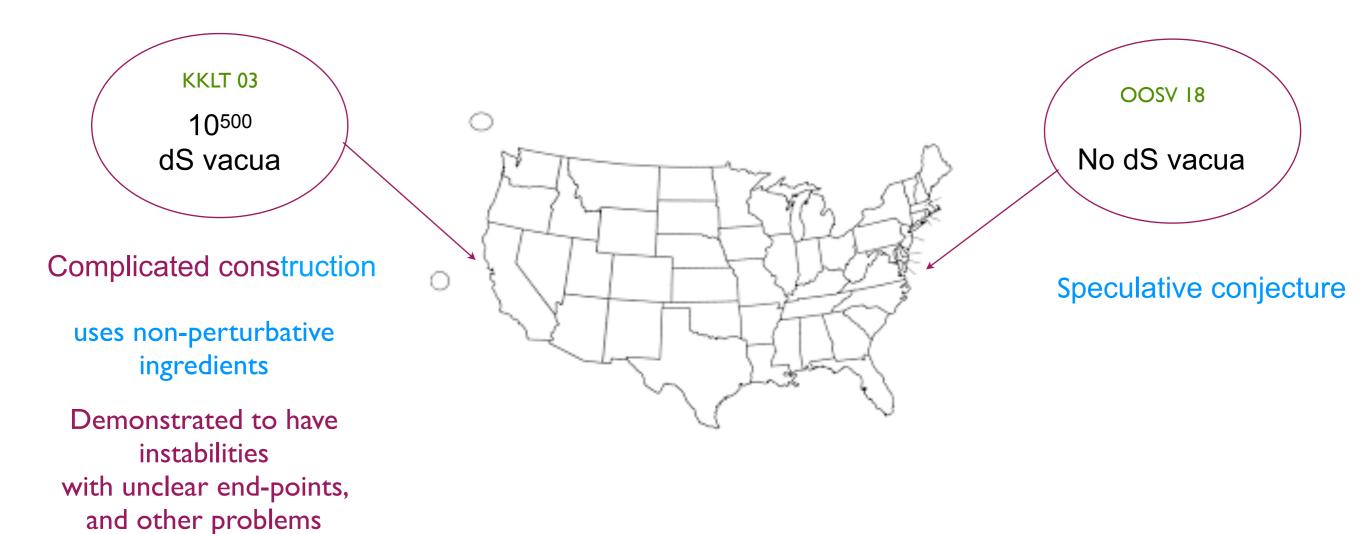
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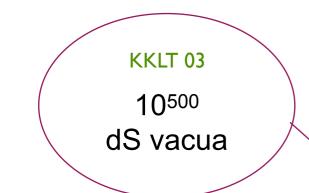
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Speculative conjecture



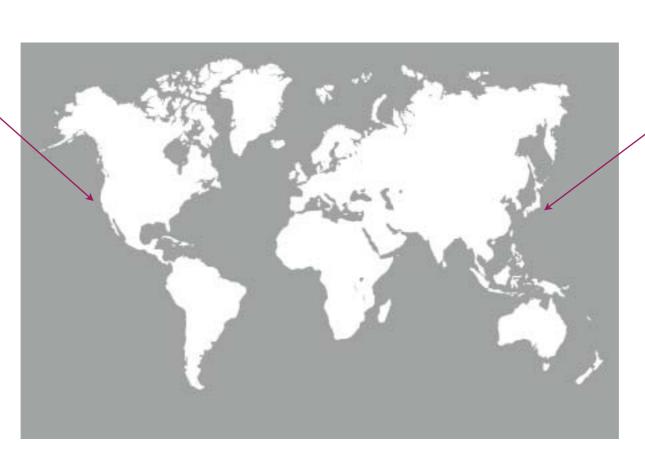


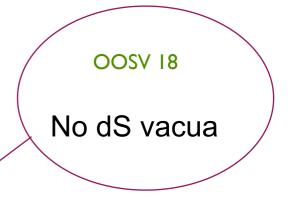


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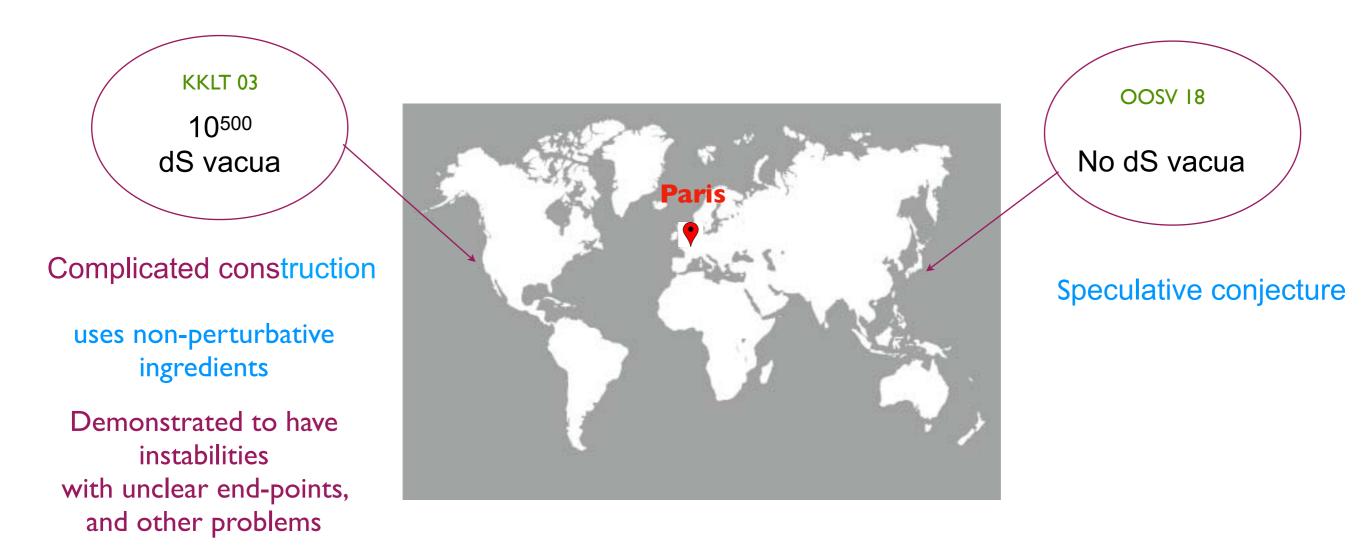
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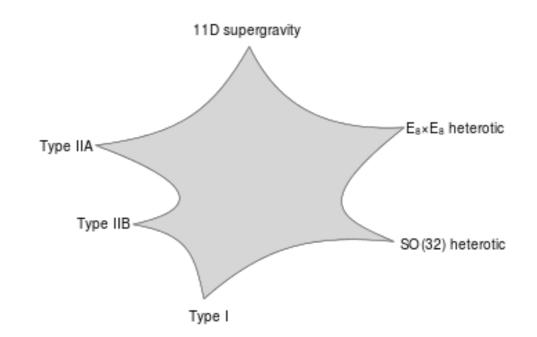
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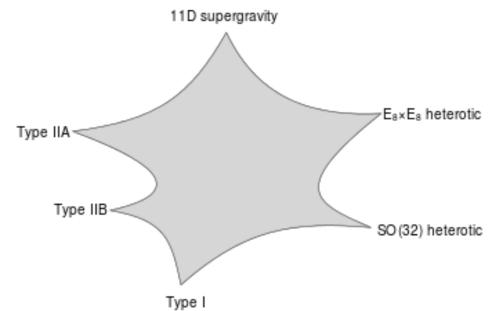
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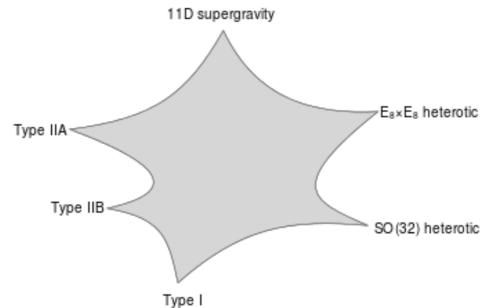


String theory is a remarkable and unique theory of quantum gravity

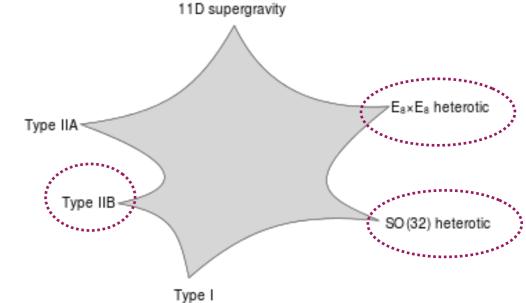
• Unique in 10d, but leads to many 4d effective theories



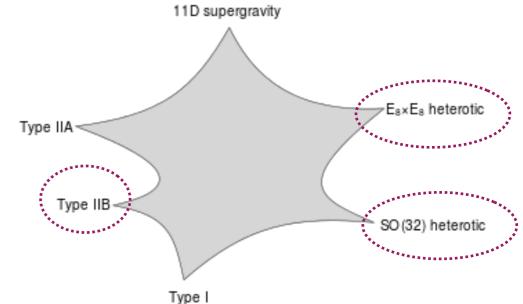
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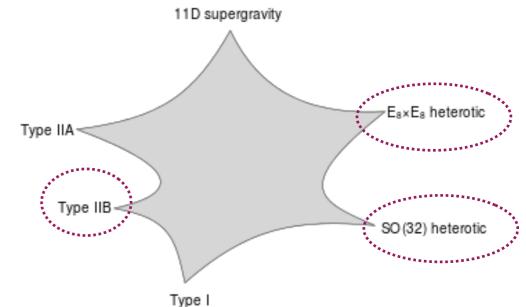
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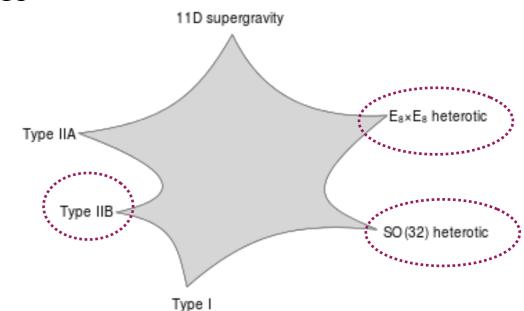
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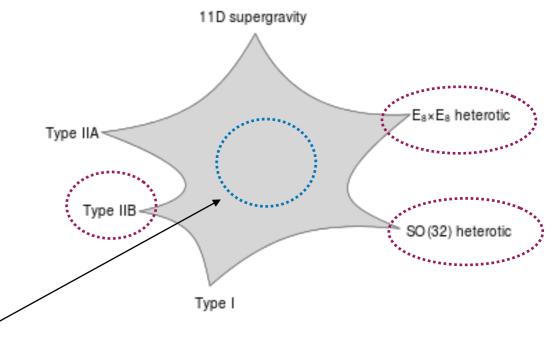


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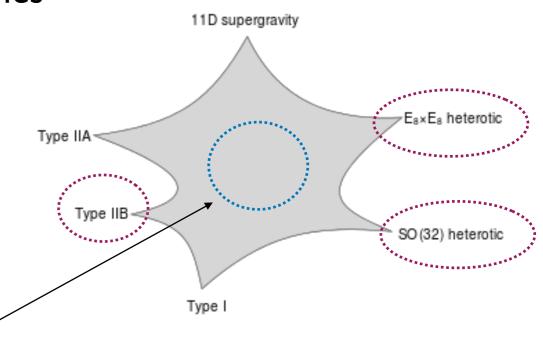


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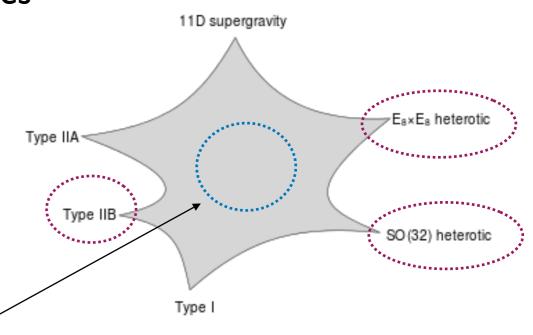
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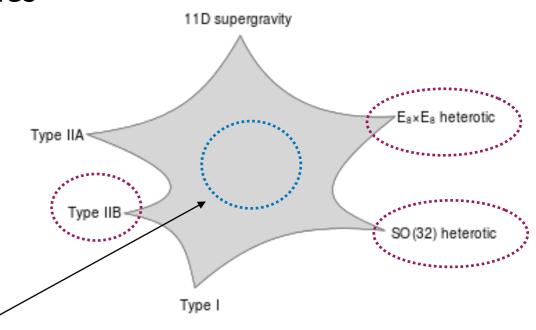
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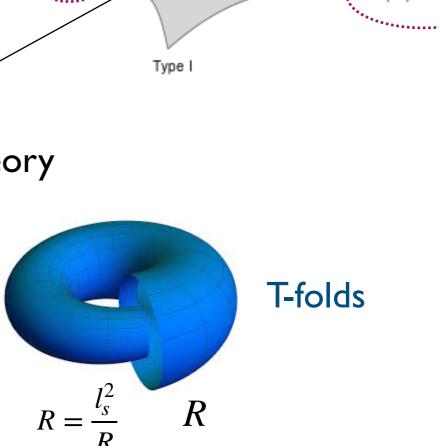
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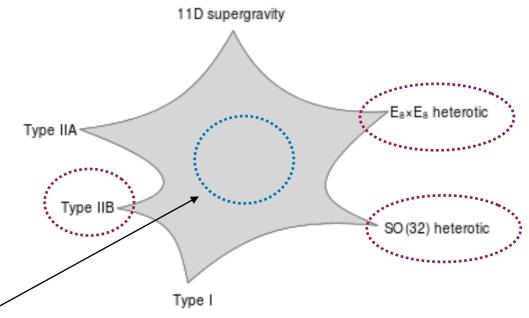


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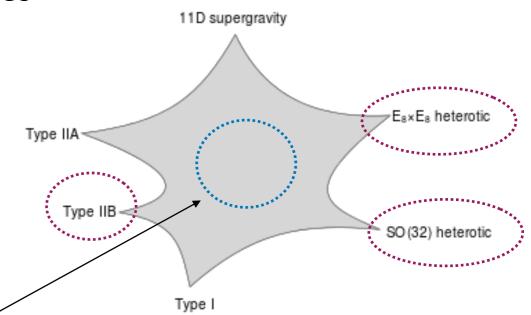


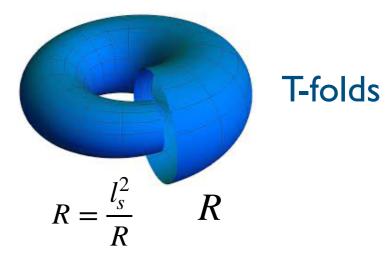
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Beautiful and still largely unexplored landscape

Transplanckian Censorship Conjecture

Bedroya, Vafa 2019

• Sub-Planckian quantum fluctuations should remain quantum (cannot become larger than Hubble radius)

Or equivalently: The expansion of the universe must slow down before all sub-Planckian modes are stretched beyond the Hubble size

Two implications:

- no dS close to boundaries of moduli space, where

$$\frac{|\nabla V|}{V} \ge \frac{2}{\sqrt{(d-1)(d-2)}}$$

- dS can exist inside the bulk, if short lived

$$\tau \le \frac{1}{H} \log \frac{M_P}{H} \sim 60 \, \frac{1}{H}$$