

From towers to cut-offs: Black hole entropies from species

Alvaro Herraez

Max Planck Institute für Physik, München

Based on work with: A. Castellano, **A. Font**, L. E. Ibáñez, D. Lüst, J. Masías, M. Scalisi

MAX-PLANCK-INSTITUT
FÜR PHYSIK



AnLy-Font Meeting

April 11th, 2024









Tuesday 27		
	<u>McAllister</u>	
	<u>Montero</u>	
	<i>Coffee</i>	
	<u>Grimm</u>	
	<u>Herráez</u>	
	<i>Lunch</i>	
	<u>Colloquium by Reece</u>	
	<i>Coffee</i>	
	<u>Martucci</u>	
	<u>Weigand</u>	
	<u>Wiesner</u>	
	<u>Dinner (21:00)</u>	

The Swampland Distance Conjecture and Towers of Tensionless Branes

A. Font¹, A. Herráez² and L.E. Ibáñez²,

¹ *Facultad de Ciencias, Universidad Central de Venezuela, A.P.20513, Caracas 1020-A,
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On scale separation in type II AdS flux vacua

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A Gravitino Distance Conjecture

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A Gravitino Distance Conjecture

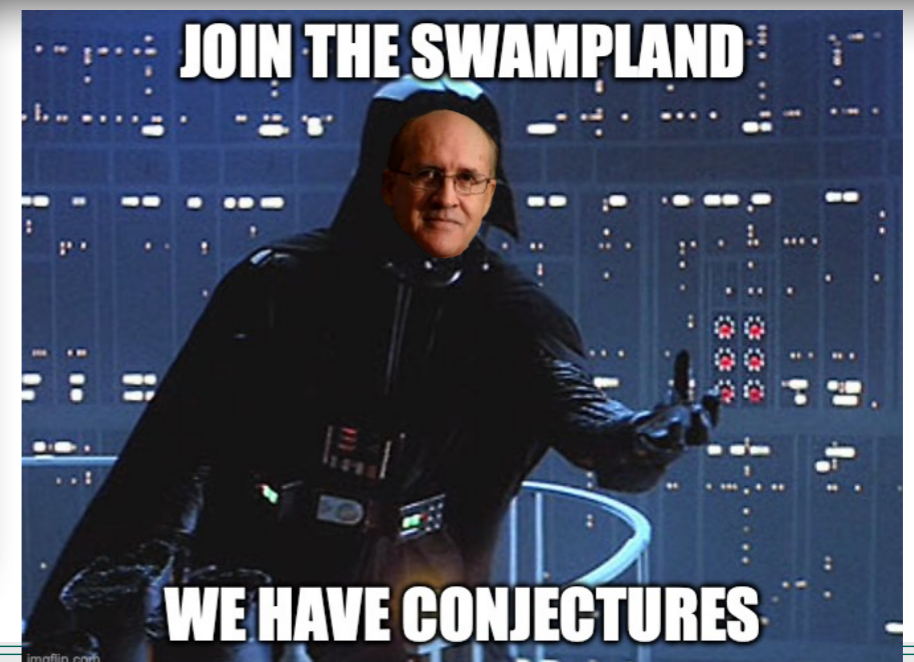
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Outline

1. The Landscape vs. The Swampland

(i) The Swampland Distance Conjecture

(ii) Particles, Strings and Membranes in the infinite Distance Limits

2. The Species Scale and Minimal Black Hole Entropies

(i) The Species Scale

(ii) UV / IR Mixing, the Covariant Entropy Bound and Minimal black holes

(iii) The Black Hole-String Correspondence

(iv) The Black Hole-Species Tower Correspondence

3. Conclusions

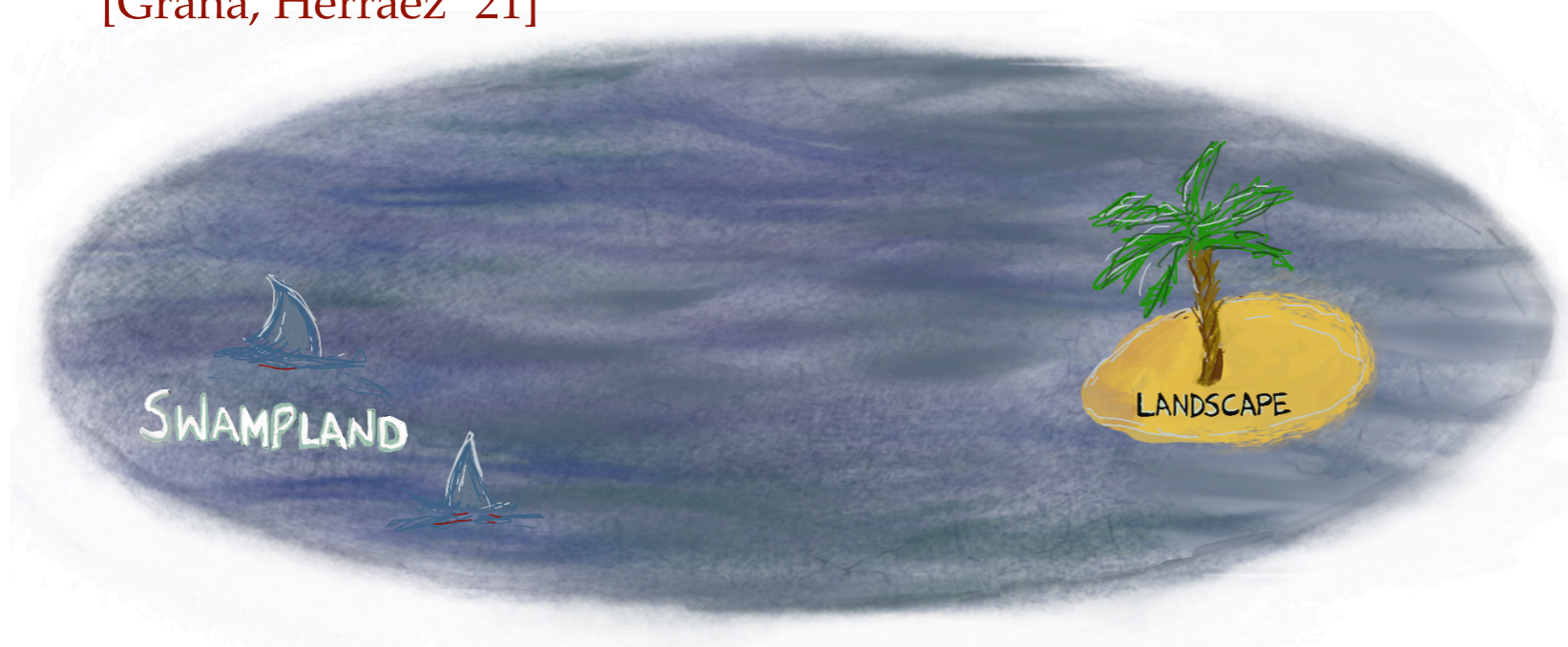
The Landscape vs the Swampland

- **String Landscape** \longrightarrow Naive expectation: Every EFT can be obtained from ST
- **Swampland** \longrightarrow Set of EFT that look consistent BUT cannot be consistently coupled to QG
[Vafa '05]

Reviews: [Brennan, Carta, Vafa '17] [Palti '19]

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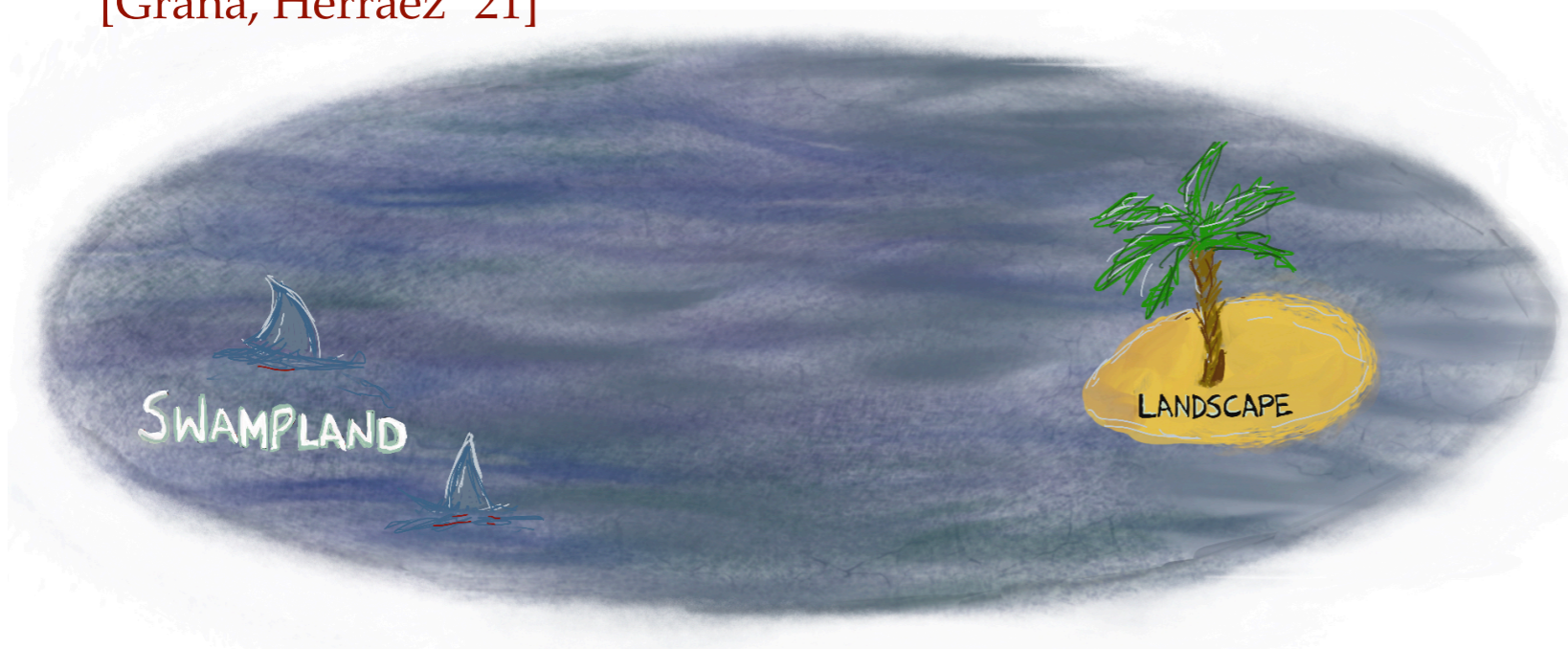
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QUESTION:

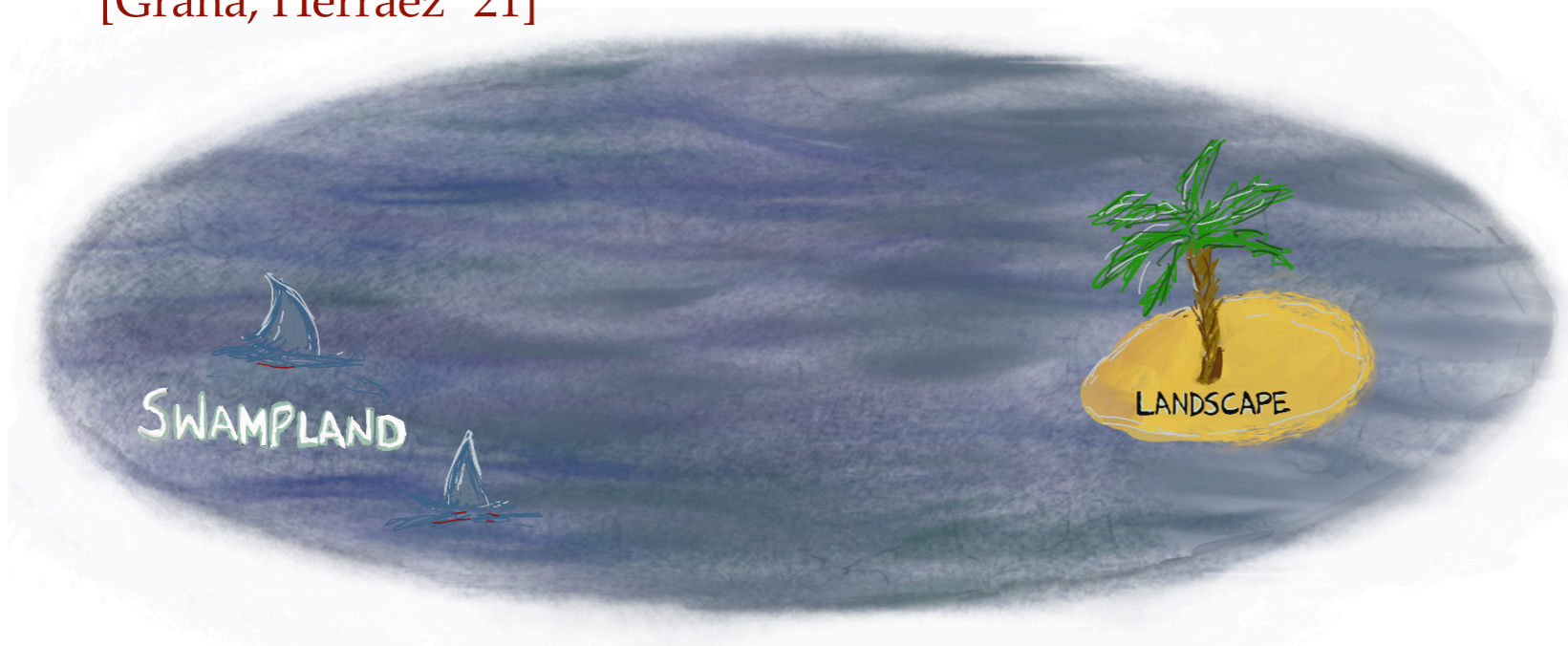
What are the general features of all QG EFT?



The Landscape vs the Swampland

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QUESTION:
What are the general features of all QG EFT?
 \updownarrow
Quantum Gravity Conjectures

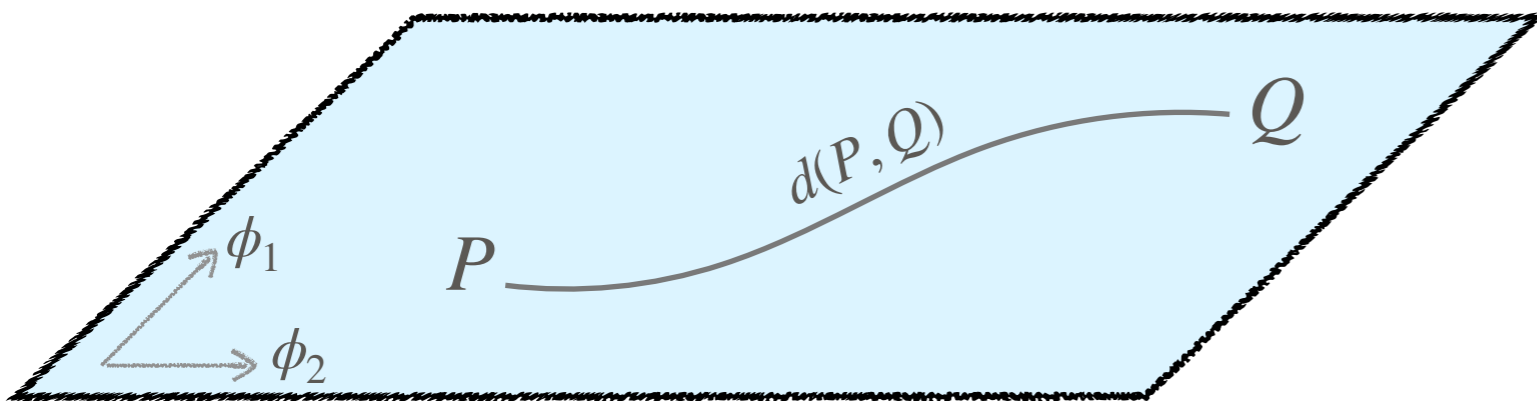
The Distance Conjecture

In a theory of QG, moving in moduli space from a point P to a point Q an infinite distance away, an infinite tower of states become light **exponentially in the geodesic distance**

$$M(Q) \sim M(P) e^{-\alpha \Delta_\phi(P,Q)}$$

[Ooguri, Vafa '06]

Scalar manifold with metric $g_{ij}(\phi_i)$ from kinetic terms



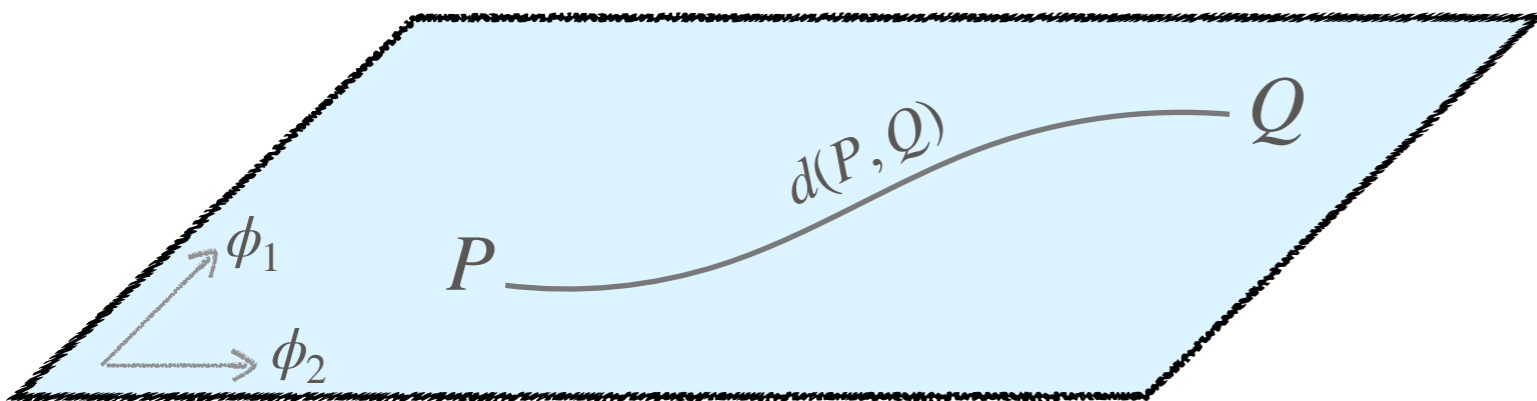
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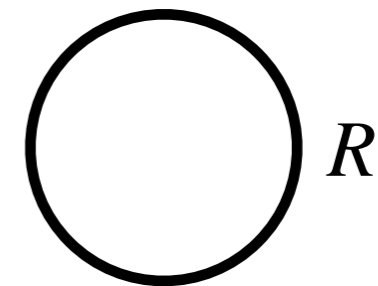
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Scalar manifold with metric $g_{ij}(\phi_i)$ from kinetic terms



- Example: Compactification on a circle of radius



$R \rightarrow \infty$ Kaluza-Klein tower

$R \rightarrow 0$ Winding tower

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- Top-down string constructions

[Andriot, Baume, Blumenhagen, Buratti, Calderón-Infante, Castellano, Cecotti, Corvilain, Etheredge, Font, Gendler, Grimm, Heidenreich, AH, Ibáñez, Joshi, Kaya, Klaewer, Lanza, Lee, Lerche, Li, Lockhart, McNamara, Marchesano, Martucci, Ooguri, Palti, Qiu, Rudelius, Ruiz, Valenzuela, Vafa, Weigand, Wiesner, Wolf, Uranga...]

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- Holography (AdS/CFT)

[Baume, Calderón-Infante'20 '23] [Perlmutter, Rastelli, Vafa, Valenzuela '20]

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[Baume, Calderón-Infante'20 '23] [Perlmutter, Rastelli, Vafa, Valenzuela '20]

- Bottom-up arguments

{Montero, Vafa, Valenzuela '21}[Castellano, AH, Ibáñez '21][Stout '21 '22][Calderón-Infante, Castellano, AH, Ibáñez '23]
{van de Heisteeg, Vafa, Wiesner '23} [Cribiori, Lüst, Montella '23] [Basile, (Cribiori), Lüst, Montella '23 '24]

The Distance Conjecture

[Ooguri, Vafa '06]

- Infinite towers of particles at infinite distance points in IIB CS moduli space \longrightarrow D3-branes wrapping 3-cycles in the internal CY (and mirror in Kähler moduli space in IIA)

[Grimm, Palti, Valenzuela '18]

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- Motivation from preventing the appearance of a global symmetry in QG at the infinite distance point \sim Weak Gravity Conjecture
 - Instantons
 - [Baume, Marchesano, Wiesner '18 '19]
 - Particles
 - Strings
 - [Lee, Lerche, Weigand '18 '19]
 - Membranes
 - [Lanza, Marchesano, Martucci, Valenzuela '20]

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[Font, AH, Ibáñez '19]

IMPORTANT REMARK

- In order for Quantum Gravity conjectures to be meaningful, we need to keep the Planck mass finite.
- The terms “massless / tensionless” = “massless / tensionless in Planck units”.

Tensionless Membranes

[Font, AH, Ibáñez '19]

Type IIA on CY (orientifolds) \longrightarrow Dp-branes wrapping (p-2)-cycles
 $\mathcal{N} = 2$ ($\mathcal{N} = 1$)

$$T_{Dp}(\gamma_{p-2}) = \frac{M_P^3}{\sqrt{4\pi}} 4e^{K/2} \mathcal{V}_{p-2}$$

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Brane	Cycle	Tension (in units of $M_P^3/\sqrt{4\pi}$)
D2	—	$2e^{K/2}$
D4	<i>P.D.</i> $[\tilde{\omega}^a]$	$2e^{K/2} T^a $
D6	<i>P.D.</i> $[\omega_a]$	$2e^{K/2} \left \frac{1}{2} \sum_{b,c} \kappa_{abc} T^b T^c \right $
D8	\mathcal{M}	$2e^{K/2} \left \frac{1}{6} \sum_{a,b,c} \kappa_{abc} T^a T^b T^c \right $
NS5	<i>P.D.</i> $[\beta^K]$	$2e^{K/2} N^K $

$$T_{Dp}(\gamma_{p-2}) = \frac{M_P^3}{\sqrt{4\pi}} 4e^{K/2} \mathcal{V}_{p-2}$$

$$\left(\begin{aligned} \mathcal{V}_2^a &= \int_{\gamma_2^a} J = \int_{\mathcal{M}} J \wedge \tilde{\omega}^a \\ \mathcal{V}_{4,a} &= \frac{1}{2} \int_{\gamma_4^a} J \wedge J = \int_{\mathcal{M}} J \wedge J \wedge \omega_a \\ \mathcal{V}_6 &= \frac{1}{3!} \int_{\mathcal{M}} J \wedge J \wedge J \end{aligned} \right)$$

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Different infinite distance points

\longrightarrow Different moduli diverge

\longrightarrow Always tensionless membranes

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3. Conclusions

The species Scale

- Maximum UV cut-off in QG in the presence of N light species

$$M_{\text{Pl},d} \longrightarrow \Lambda_{\text{QG}} = \frac{M_{\text{Pl},d}}{N^{\frac{1}{d-2}}}$$

[Dvali '07] [Dvali, Reedi '08]
[Dvali, Lüst '10] [Dvali, Gómez '10]

The species Scale

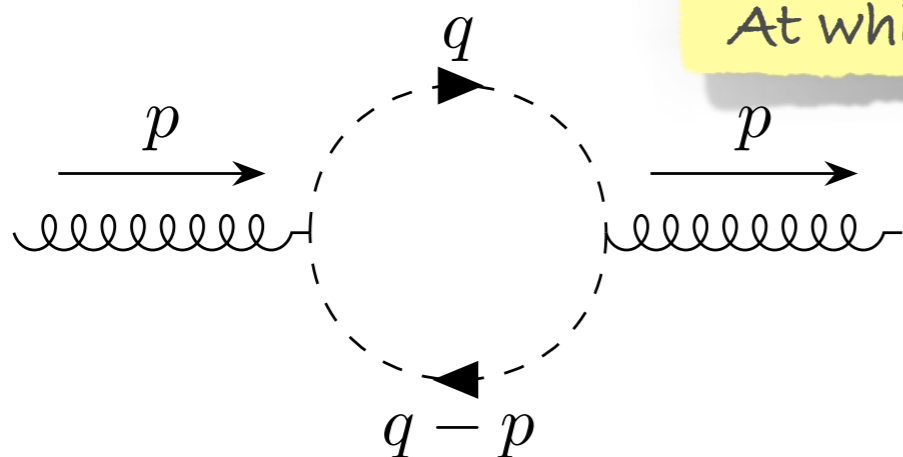
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- Perturbative arguments**

At which scale does the perturbative expansion break down?



$$\pi^{-1}(p^2) = 2p^2 \left(1 - \frac{Np^2}{120\pi M_{\text{pl},4}^2} \ln(-p^2/\mu^2) \right)$$

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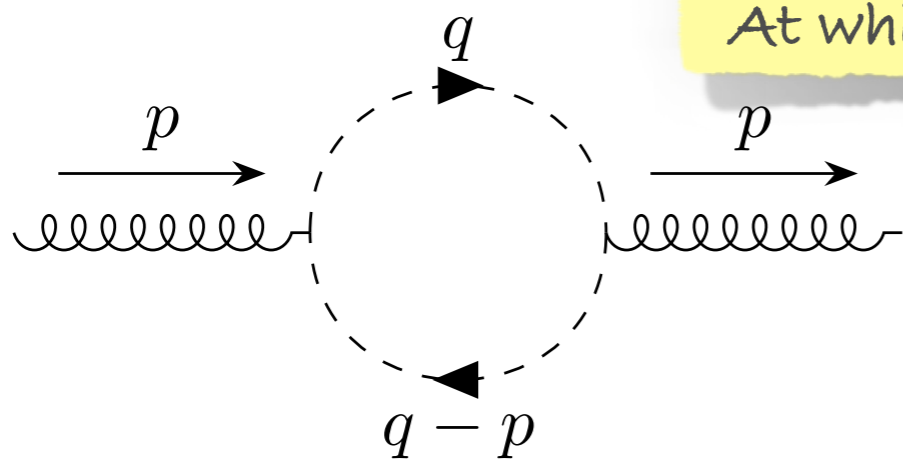
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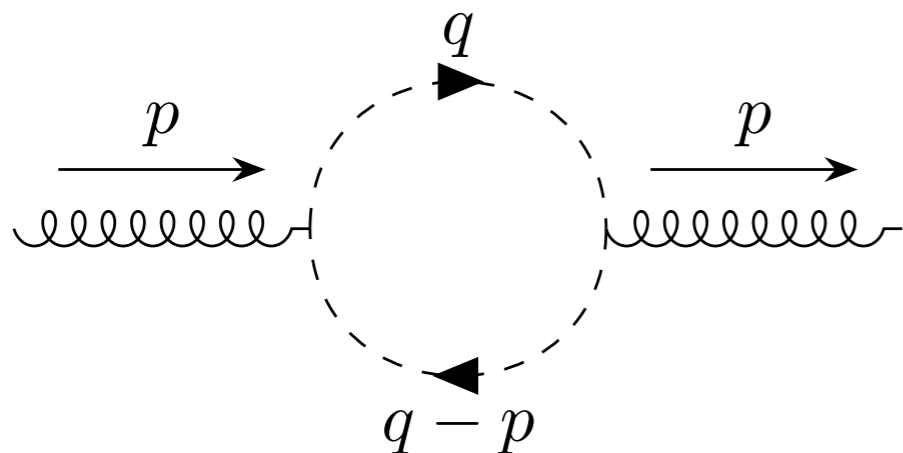
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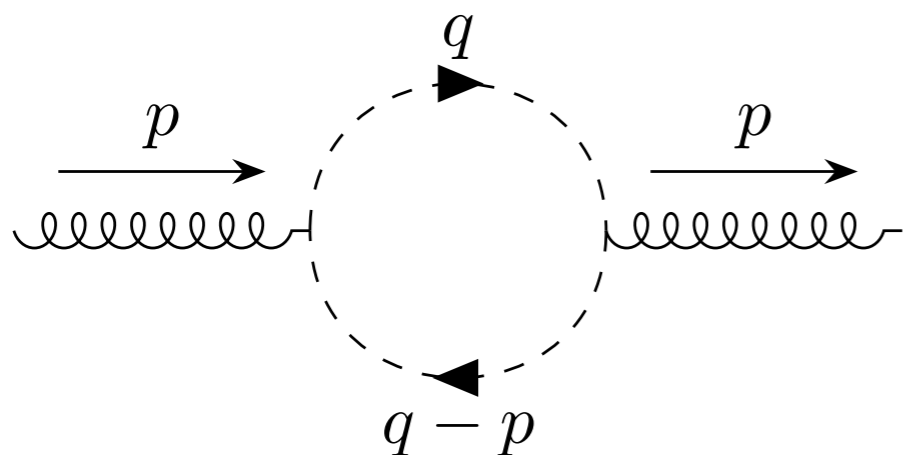
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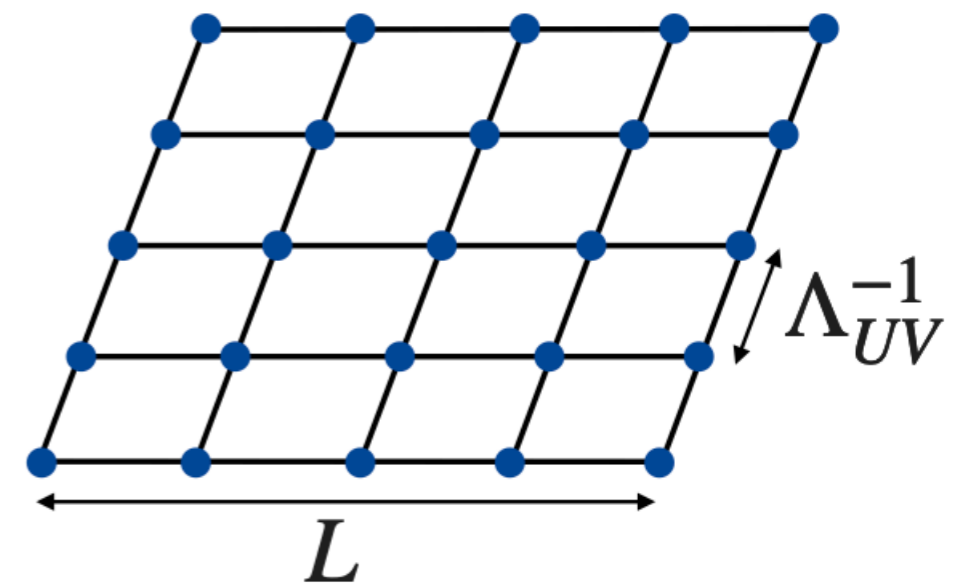
Species Scale of the d -dim EFT = $M_{\text{Pl},d+p}$ (decompactification of p dimensions)
 M_{str} (weakly coupled string limits)

UV/IR Mixing, the Covariant Entropy Bound and Minimal black holes

[Castellano, AH, Ibáñez '21]
[AH, Lüster, Masias, Scalisi (WIP)]

Extensive
Entropy
in QFT

$$S \sim N_{\text{sp}} T^{d-1} \text{vol} \sim N_{\text{sp}} (TL)^{d-1}$$



UV/IR Mixing, the Covariant Entropy Bound and Minimal black holes

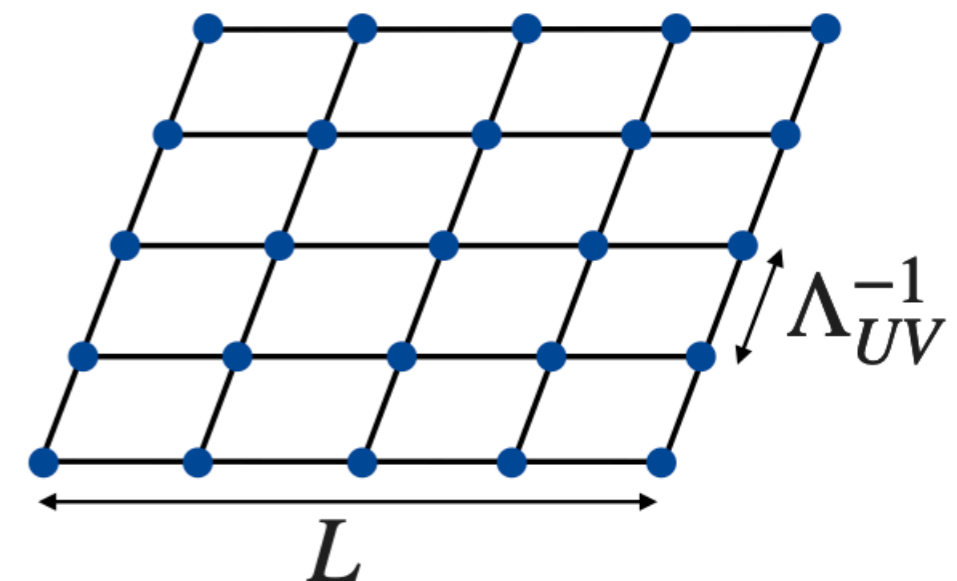
[Castellano, AH, Ibáñez '21]
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$$S \sim N_{\text{sp}} T^{d-1} \text{vol} \sim N_{\text{sp}} (TL)^{d-1}$$
$$T \leq \Lambda_{\text{sp}}$$

Species Scale
(QG cut-off)

$$\Lambda_{\text{sp}} \sim \frac{M_{\text{pl},d}}{N_{\text{sp}}^{\frac{1}{d-2}}}$$



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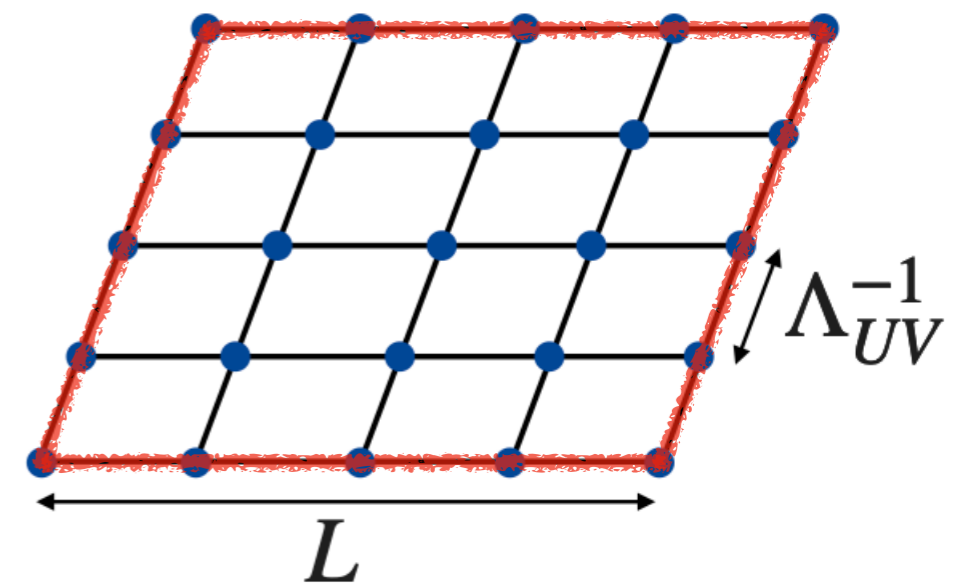
Covariant
Entropy
Bound

[Bousso '99]

$$S \leq \frac{A}{4G_{N,d}} \sim \frac{L^{d-2}}{4G_{N,d}}$$

Species Scale
(QG cut-off)

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UV/IR Mixing, the Covariant Entropy Bound and Minimal black holes

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$$S \leq \frac{A}{4G_{N,d}} \sim \frac{L^{d-2}}{4G_{N,d}}$$

Saturation of the bound at the scale of gravitational collapse

$$S \simeq N_{\text{sp}} \quad T = \frac{1}{L} \simeq \Lambda_{\text{sp}}$$

UV/IR Mixing, the Covariant Entropy Bound and Minimal black holes

[Castellano, AH, Ibáñez '21]
[AH, Lüst, Masias, Scalisi (WIP)]

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Entropy
in QFT

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Species Entropy

[Cribiori, Montella, Lüst '23]

Black Hole-String Correspondence

[Susskind '93]

[Horowitz, Polchinski '96 '97]

[Chen, Maldacena, Witten '21]

[Susskind '21]

[Ceplack, Emparan, Puhm,

Tomasevic '22]

[Bedroya, Vafa, Wang '23]

Black Hole-String Correspondence

[Susskind '93]

[Horowitz, Polchinski '96 '97]

Black Hole

$$\ell_{\text{Pl},d}^{d-2} = g_{s,d}^2 \ell_{\text{str}}^{d-2}$$

$$M_{\text{BH}} \sim \frac{R_{\text{BH}}^{d-3}}{\ell_{\text{Pl},d}^{d-2}} \sim \frac{R_{\text{BH}}^{d-3}}{g_{s,d}^2 \ell_{\text{str}}^{d-2}}$$

$$S_{\text{BH}} \sim (R_{\text{BH}}/\ell_{\text{Pl},d})^{d-2} \sim g_{s,d}^{\frac{2}{d-3}} (M_{\text{BH}} \ell_{\text{str}})^{\frac{d-2}{d-3}}$$

Black Hole-String Correspondence

[Susskind '93]

[Horowitz, Polchinski '96 '97]

Black Hole

(Free) String

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$$M_{\text{str}} \sim \frac{L_{\text{str}}}{\ell_{\text{str}}^2}$$

$$S_{\text{BH}} \sim (R_{\text{BH}}/\ell_{\text{Pl},d})^{d-2} \sim g_{s,d}^{\frac{2}{d-3}} (M_{\text{BH}} \ell_{\text{str}})^{\frac{d-2}{d-3}}$$

$$S_{\text{str}} \sim L_{\text{str}}/\ell_{\text{str}} \sim M_{\text{str}} \ell_{\text{str}}$$

Black Hole-String Correspondence

[Susskind '93]

[Horowitz, Polchinski '96 '97]

Black Hole

(Free) String

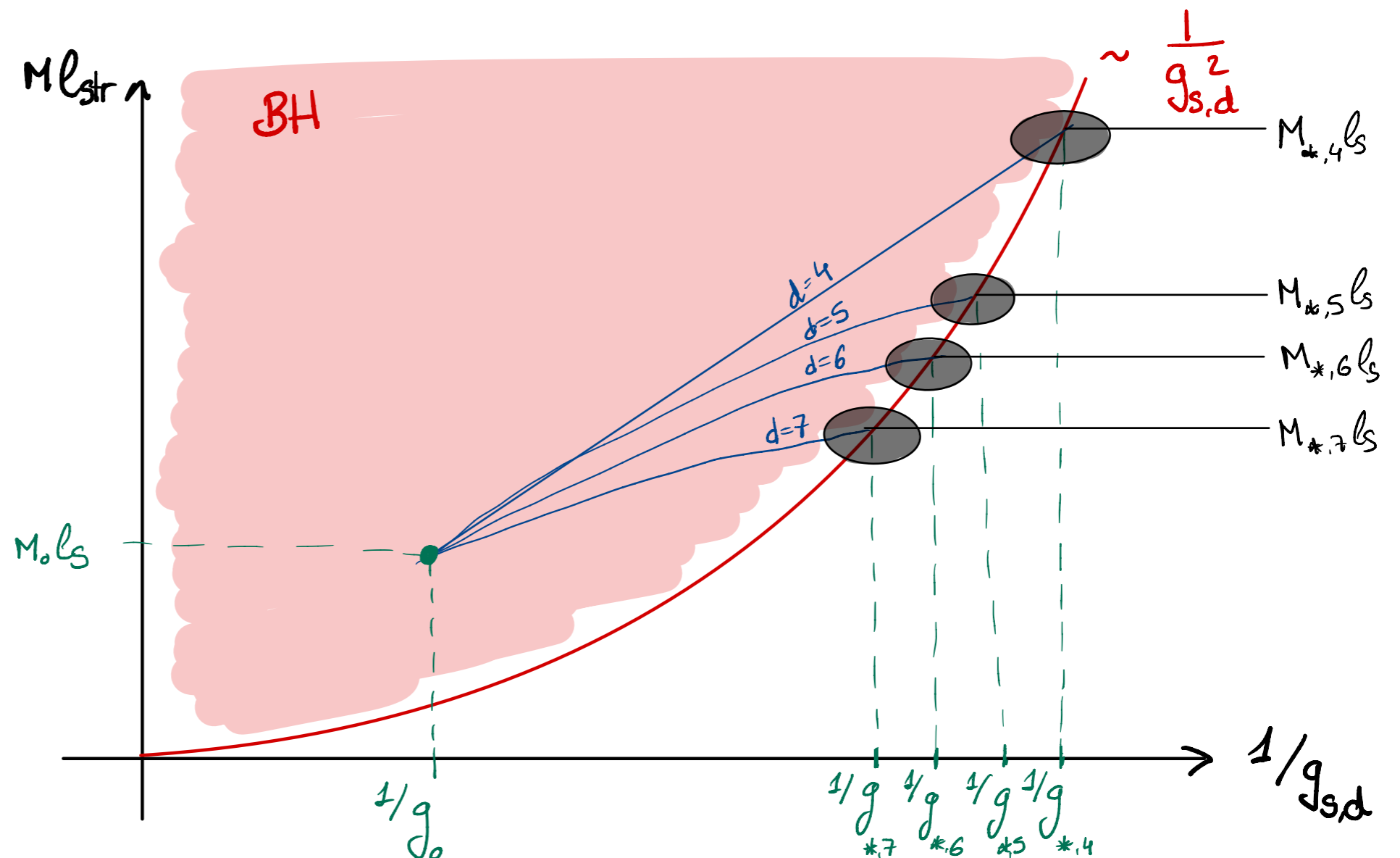
$$\ell_{\text{Pl},d}^{d-2} = g_{s,d}^2 \ell_{\text{str}}^{d-2}$$

$$M_{\text{BH}} \sim \frac{R_{\text{BH}}^{d-3}}{\ell_{\text{Pl},d}^{d-2}} \sim \frac{R_{\text{BH}}^{d-3}}{g_{s,d}^2 \ell_{\text{str}}^{d-2}}$$

$$M_{\text{str}} \sim \frac{L_{\text{str}}}{\ell_{\text{str}}^2}$$

$$S_{\text{BH}} \sim (R_{\text{BH}}/\ell_{\text{Pl},d})^{d-2} \sim g_{s,d}^{\frac{2}{d-3}} (M_{\text{BH}} \ell_{\text{str}})^{\frac{d-2}{d-3}}$$

$$S_{\text{str}} \sim L_{\text{str}}/\ell_{\text{str}} \sim M_{\text{str}} \ell_{\text{str}}$$



[AH, Lüst, Masias, Scalisi (WIP)]

Black Hole-String Correspondence

[Susskind '93]

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Black Hole

(Free) String

$$\ell_{\text{Pl},d}^{d-2} = g_{s,d}^2 \ell_{\text{str}}^{d-2}$$

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$$M_{\text{str}} \sim \frac{L_{\text{str}}}{\ell_{\text{str}}^2}$$

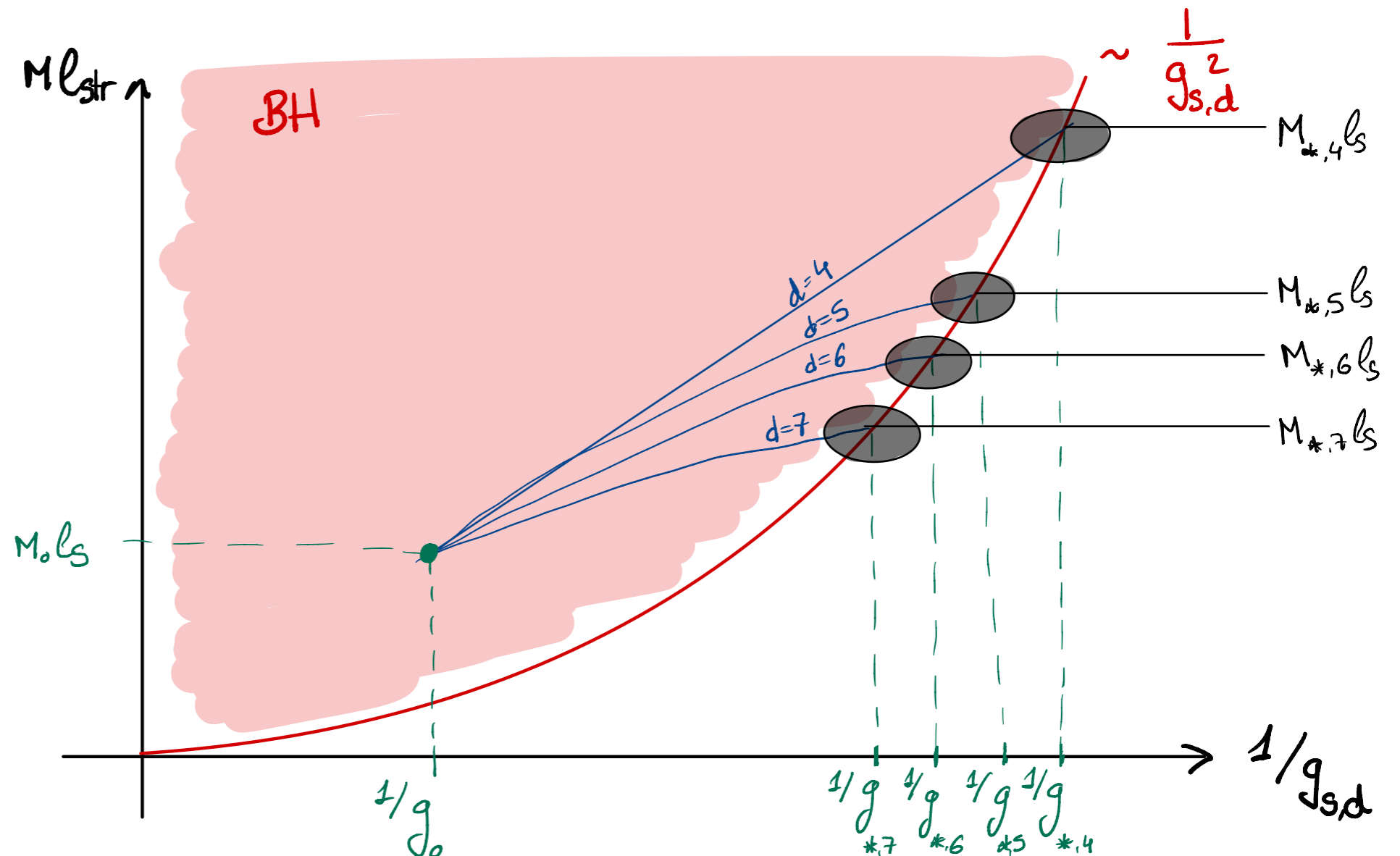
$$S_{\text{BH}} \sim (R_{\text{BH}}/\ell_{\text{Pl},d})^{d-2} \sim g_{s,d}^{\frac{2}{d-3}} (M_{\text{BH}} \ell_{\text{str}})^{\frac{d-2}{d-3}}$$

$$S_{\text{str}} \sim L_{\text{str}}/\ell_{\text{str}} \sim M_{\text{str}} \ell_{\text{str}}$$

Correspondence
point (line)

$$R_{\text{BH}} \sim \ell_{\text{str}}$$

$$S = \frac{1}{g_{s,*}^2} = N_{\text{sp}}$$



[AH, Lüst, Masias, Scalisi (WIP)]

Black Hole-Species Tower Correspondence

$$\ell_{\text{Pl},d}^{d-2} = \frac{\ell_{\text{sp}}^{d-2}}{\mathcal{V}}$$

$$\ell_{\text{str}} \rightarrow \ell_{\text{sp}} = \Lambda_{\text{sp}}^{-1}$$

$$g_s^{-2} \rightarrow \mathcal{V}$$

Black Hole

$$M_{\text{BH}} \sim \frac{R_{\text{BH}}^{d-3}}{\ell_{\text{Pl},d}^{d-2}} \sim \frac{R_{\text{BH}}^{d-3} \mathcal{V}}{\ell_{\text{sp}}^{d-2}}$$

$$S_{\text{BH}} \sim (R_{\text{BH}}/\ell_{\text{Pl},d})^{d-2} \sim \left(\frac{M_{\text{BH}}^{d-2} \ell_{\text{sp}}^{d-2}}{\mathcal{V}} \right)^{\frac{1}{d-3}}$$

Box of (free) species

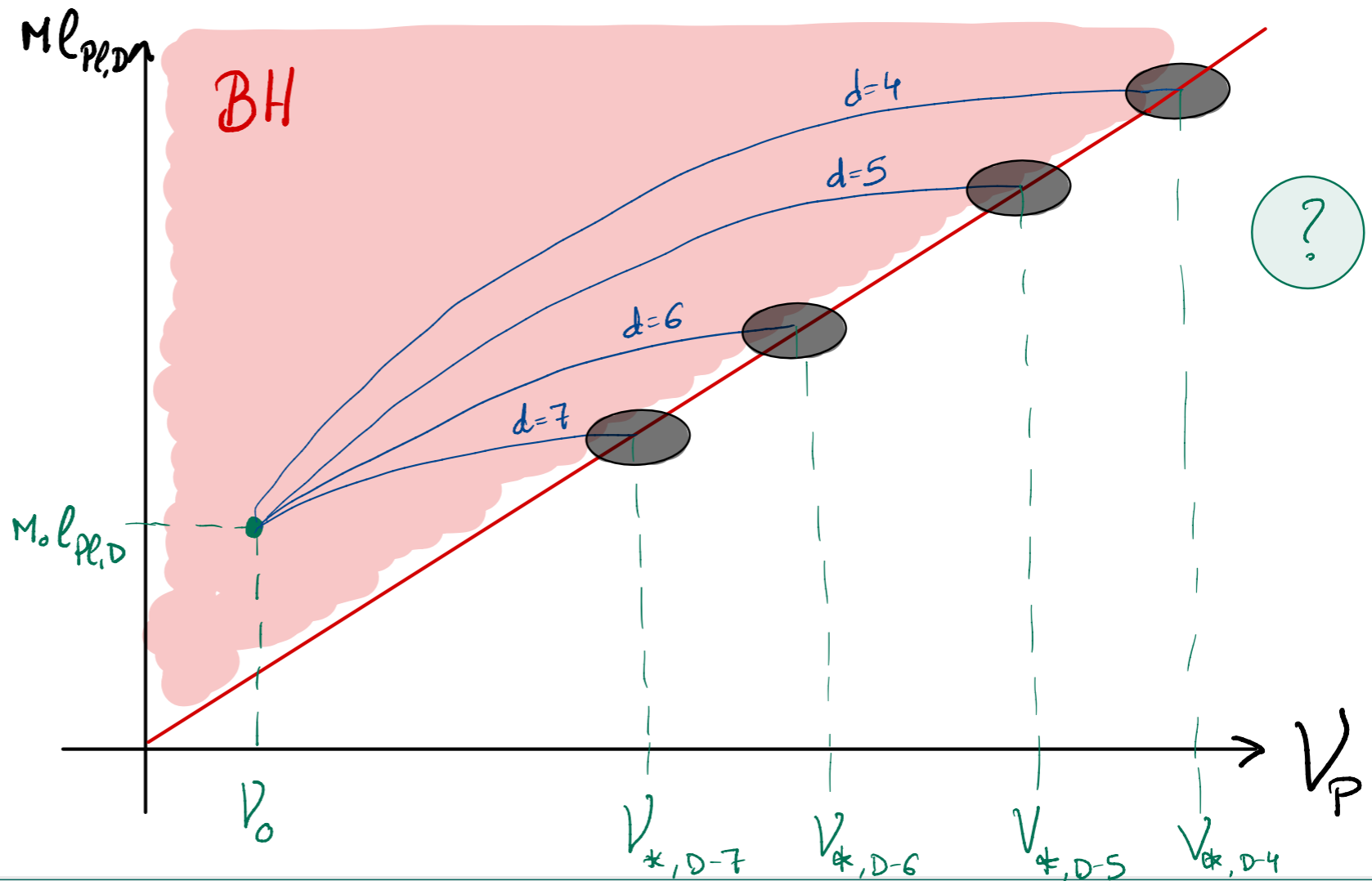
$$L^{-1} = T \leq \Lambda_{\text{sp}}$$

$$S \sim N_T (TL)^{d-1}$$

Correspondence point (line)

$$R_{\text{BH}} \sim \ell_{\text{sp}}$$

$$S = \mathcal{V}_* = N_{\text{sp},*}$$



[AH, Lüst, Masias, Scalisi (WIP)]

Black Hole-Species Tower Correspondence

$$\ell_{\text{Pl},d}^{d-2} = \frac{\ell_{\text{sp}}^{d-2}}{\mathcal{V}}$$

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Black Hole

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Box of (free) species

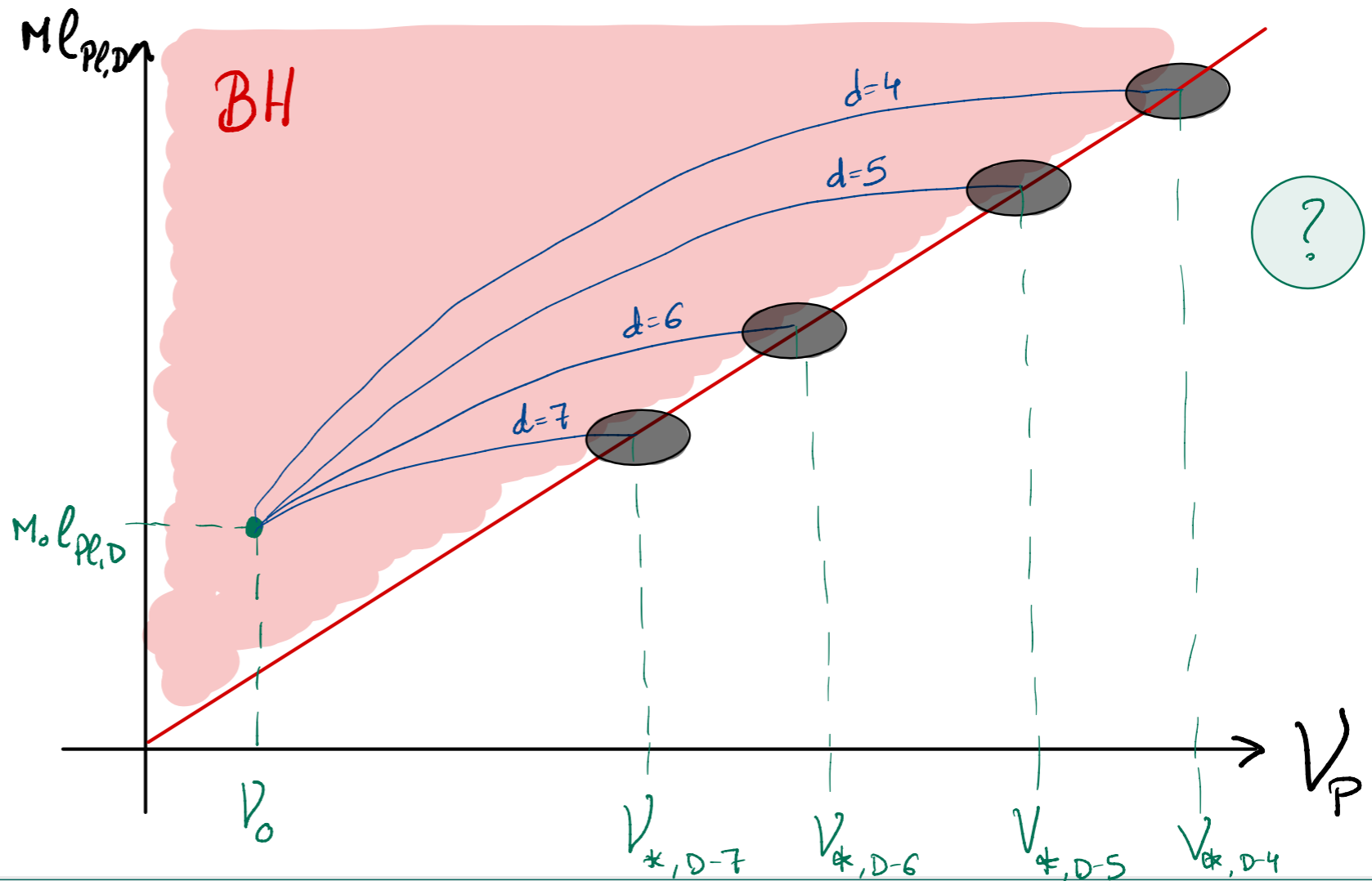
$$L^{-1} = T \leq \Lambda_{\text{sp}}$$

$$S \sim N_T (TL)^{d-1} \sim N_{\text{sp},*}$$

Correspondence point (line)

$$R_{\text{BH}} \sim \ell_{\text{sp}}$$

$$S = \mathcal{V}_* = N_{\text{sp},*}$$



[AH, Lüst, Masias, Scalisi (WIP)]

Summary

- Lots of light towers near infinite distance limits \longrightarrow Particles and extended objects
- Maximum cut-off for gravitational EFTs with such species $\longrightarrow \Lambda_{\text{sp}} = \frac{M_{\text{Pl},d}}{N_{\text{sp}}^{\frac{1}{d-2}}} \geq m_{\text{tower}}$
- Entropy Bounds suggest smallest BH in the EFT has $R_{\text{BH}} \simeq \Lambda_{\text{sp}}^{d-1}$ and
$$M_{\text{BH}} \simeq \Lambda_{\text{sp}}^{3-d} M_{\text{Pl},d}^{d-2}$$
- Can compute the entropy (up to order one-factors, but recover area law) of semiclassical BHs from microstates of a free box of quantum relativistic species at $T = \Lambda_{\text{sp},*}$ yielding $S = N_{\text{sp},*} = N_T (TL)^{d-1}$

Thank you!

Gracias Anamaría!



Y mi más sincera enhorabuena por este merecidísimo premio!