Yukawas at infinite distance

#### Luis Ibáñez

#### Instituto de Física Teórica UAM-CSIC, Madrid





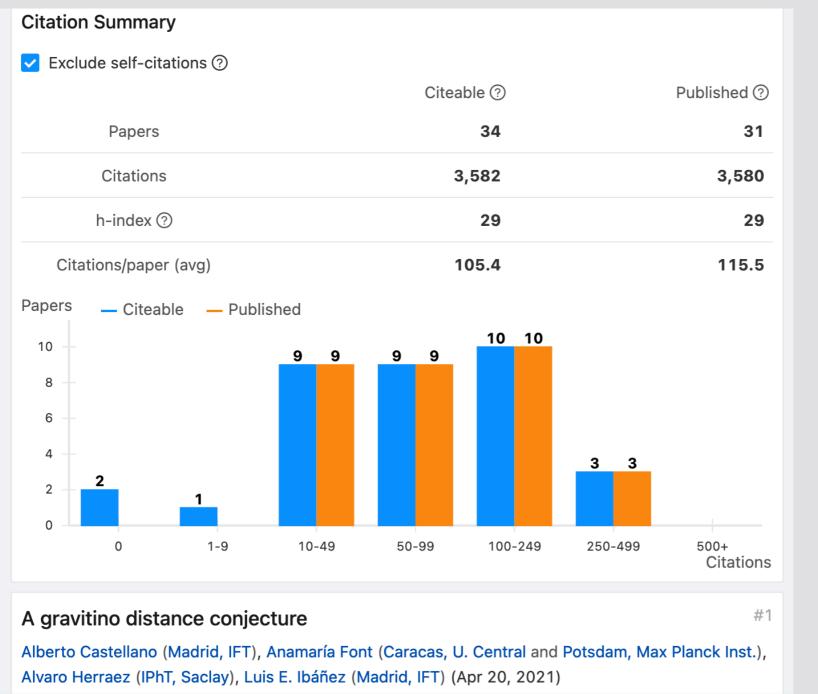


AnLy Meeting in honor of Anamaria Font, Annecy, April 2024

#### My most frequent collaborator!!

1988

2021



Published in: JHEP 08 (2021) 092 • e-Print: 2104.10181 [hep-th]

#### Working with Anamaria is a pleasure, but also a guarantee of quality!!



Physics Letters B Volume 245, Issues 3–4, 16 August 1990, Pages 4

#### Supersymmetry breaking free duality invariant gaugino condensation

<u>A. Font <sup>a</sup>, L.E. Ibáñez <sup>b</sup>, D. Lüst <sup>b</sup>, F. Quevedo <sup>c</sup></u>

M. Cvetič, A. Font, L.E. Ibánez, D. Lüst, F. Quevedo

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string vacua

Nuclear Physics B Volume 361, Issue 1, 26 August 1991, Pages 194-232

Target-space duality, supersymmetry

breaking and the stability of classical



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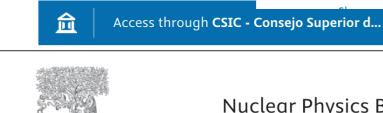
Nuclear Physics B

Volume 345, Issues 2–3, 3 December 1990, Pages 389-430

#### Higher-level Kac-Moody string models and their phenomenolog implications

Anamaría Font, Luis E. Ibáñez, Fernando Quevedo

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Nuclear Physics B Volume 536, Issues 1–2, 21 December 1998, Pages 29-68

D = 4, N = 1, type IIB orientifolds



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Physics Letters B Volume 217, Issue 3, 26 January 1989, Pages 272-276



#### $Z_N \times Z_M$ orbifolds and discrete torsion

A. Font, L.E. Ibáñez, F. Quevedo



Published for SISSA by 🖄 Springer

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# The Swampland Distance Conjecture and towers of tensionless branes

Anamaría Font,<sup>a</sup> Alvaro Herráez<sup>b</sup> and Luis E. Ibáñez<sup>b</sup>



PUBLISHED BY INSTITUTE OF PHYSICS PUBLISHING FOR S. RECEIVED: August 1,

ACCEPTED: August 24, PUBLISHED: September 6,

# Fluxes, moduli fixing and MSSM-like vacua in a simple IIA orientifold

<u>G. Aldazabal</u><sup>a</sup>, <u>A. Font</u><sup>b c</sup>, <u>L.E. Ibáñez</u><sup>d</sup>, <u>G. Violero</u><sup>d</sup>

Pablo G. Cámara, Anamaria Font<sup>\*</sup> and Luis E. Ibáñez

Departemente de Férica Toónica ( YI and Institute de Férica Toónica ( YVI

#### Strong-weak coupling duality and non-perturbative effects in string theory

A. Font<sup>a</sup>, L.E. Ibáñez<sup>b</sup>, D. Lüst<sup>b</sup> and F. Quevedo<sup>c</sup>

<sup>a</sup> Departamento de Fisica, Universita Central de Venezuela, Aptdo 20513, Caracas 1020-A, Venezuela

b CERN, CH-1211 Geneva 23, Switzerland

<sup>c</sup> Theoretical Division LANL, Los Alamos, NM 87545, USA

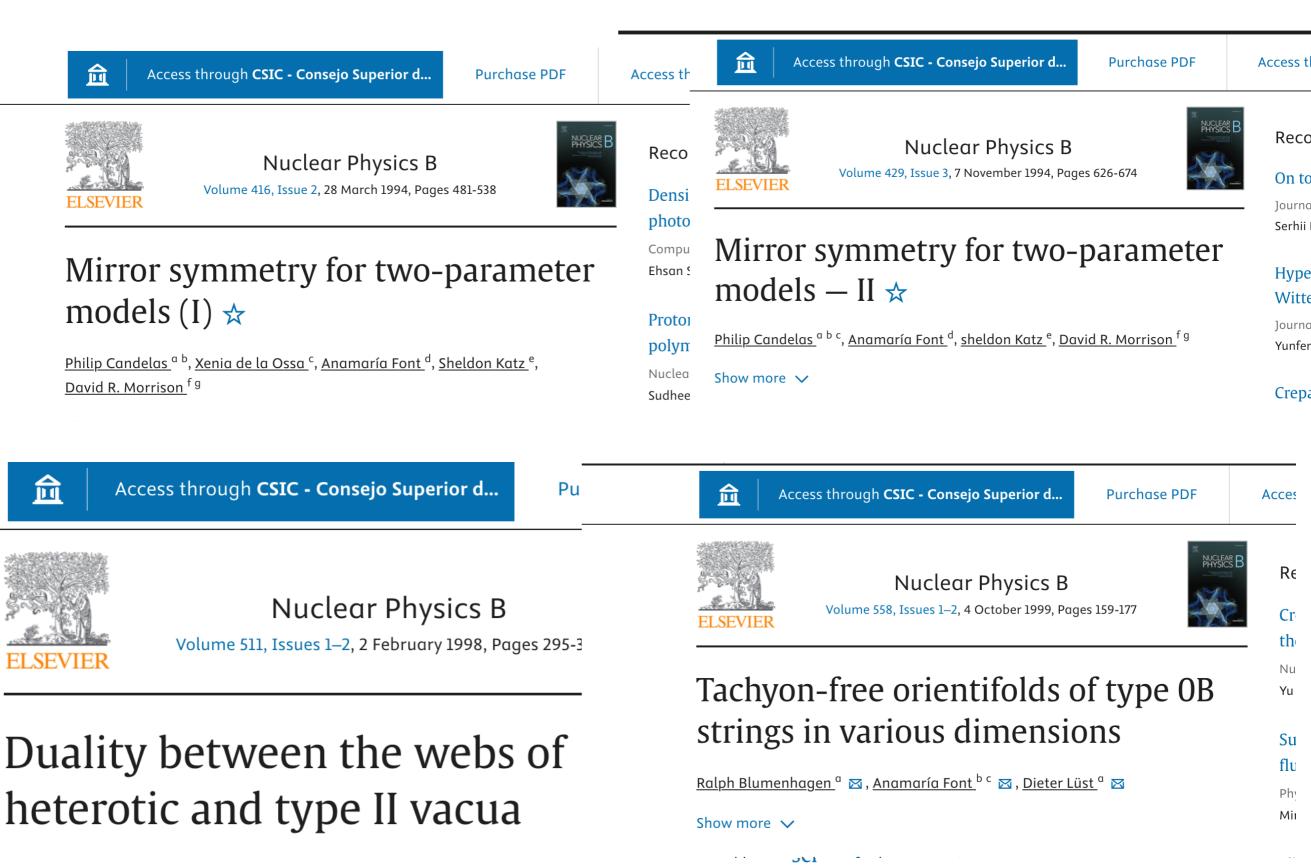
Received 13 July 1990

We conjecture the existence of a new discrete symmetry of the modular type relating weak and strong coupling in string theory. The existence of this symmetry would strongly constrain the non-perturbative behaviour in string partition functions and introduces the notion of a maximal (minimal) coupling constant. An effective lagrangian analysis suggests that the dilaton vacuum expectation value is dynamically fixed to be of order one. In supersymmetric heterotic strings, supersymmetry (as well as this modular symmetry itself) is generically spontaneously broken.



#### ICTP Prize 1998

# S-DUALITY



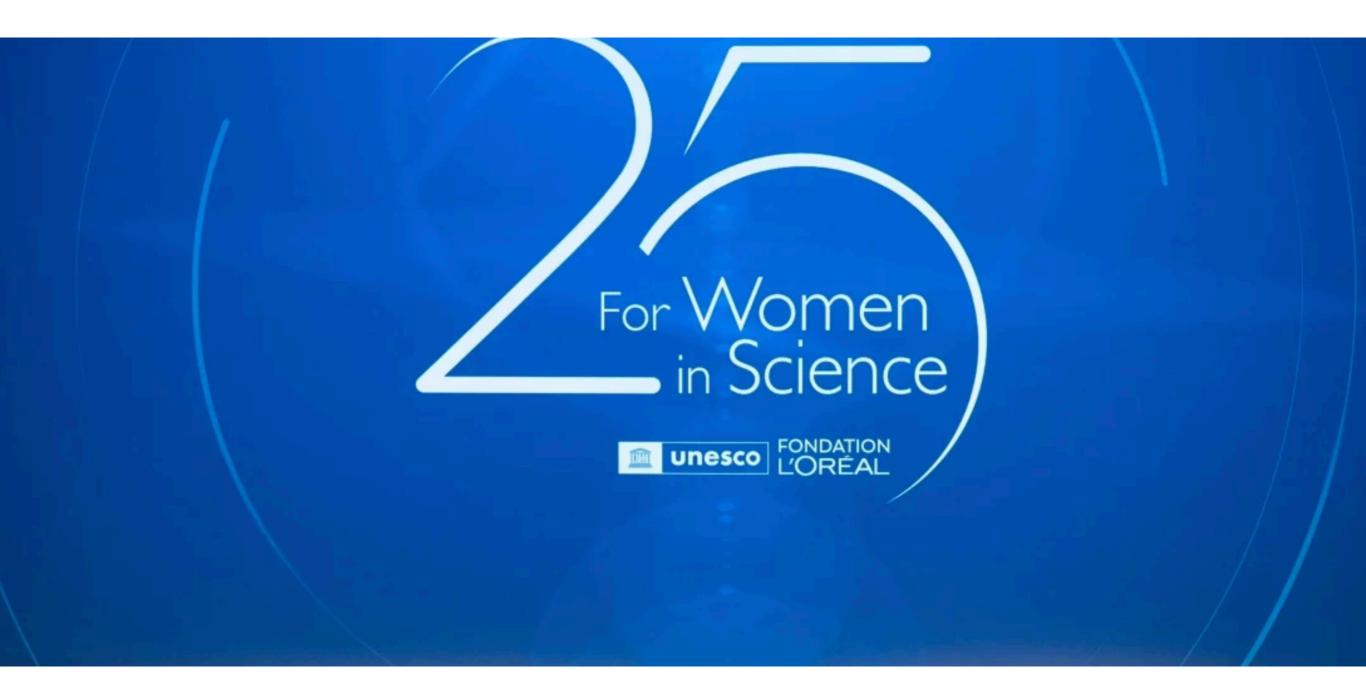
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Philip Candelasía Font 🖂

Etc

2023

# **L'Oreal Prize**



SEARCH

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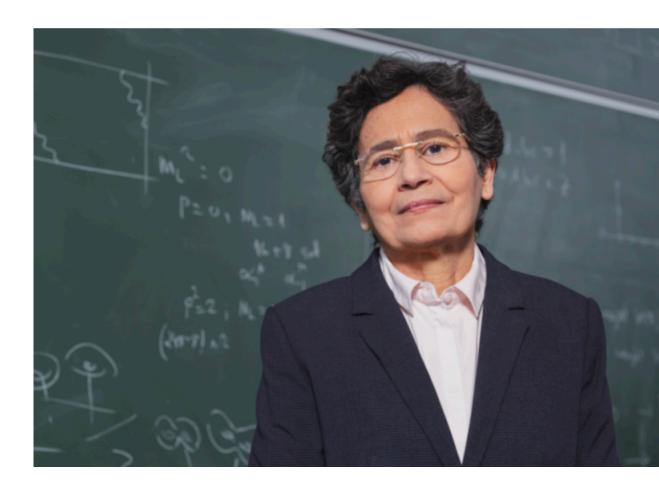
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#### LAUREATE FOR LATIN AMERICA AND THE CARIBBEAN

#### **PROFESSOR ANAMARÍA FONT**

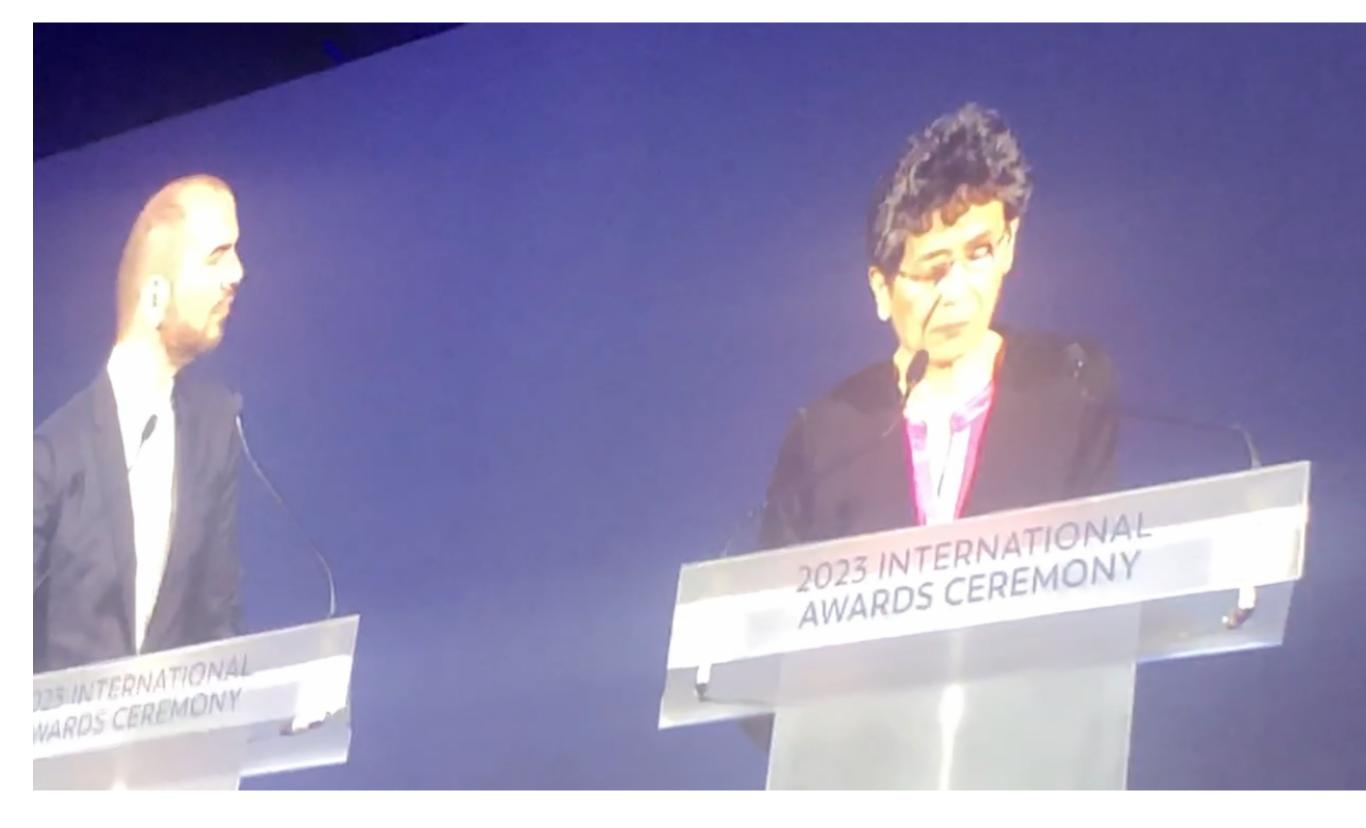
Professor of Physics, Central University of Venezuela.

Prof. Anamaría Font is recognized for her work in theoretical particle physics, with a particular focus on developing the theory of superstrings. This describes, in a unified and consistent way, the elementary particles of nature. Her research has enabled further understanding of the theory's consequences for the structure of matter and quantum gravity, which are also relevant to the description of black holes and the first moments after the big bang.



# Paris, 15-th June 2023



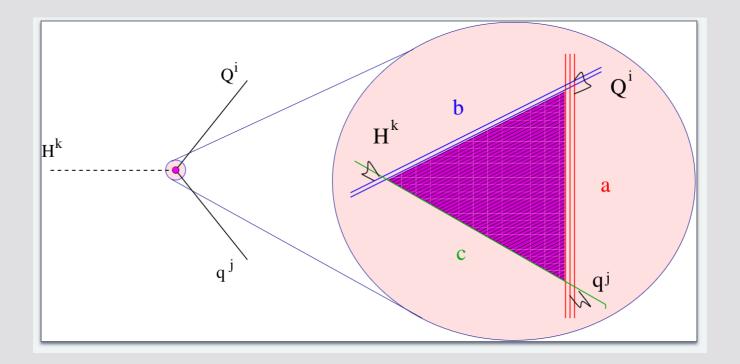


# Congratulations Anamaria !!

# Yukawas at infinite distance

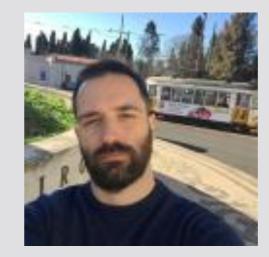


# Yukawas at infinite distance



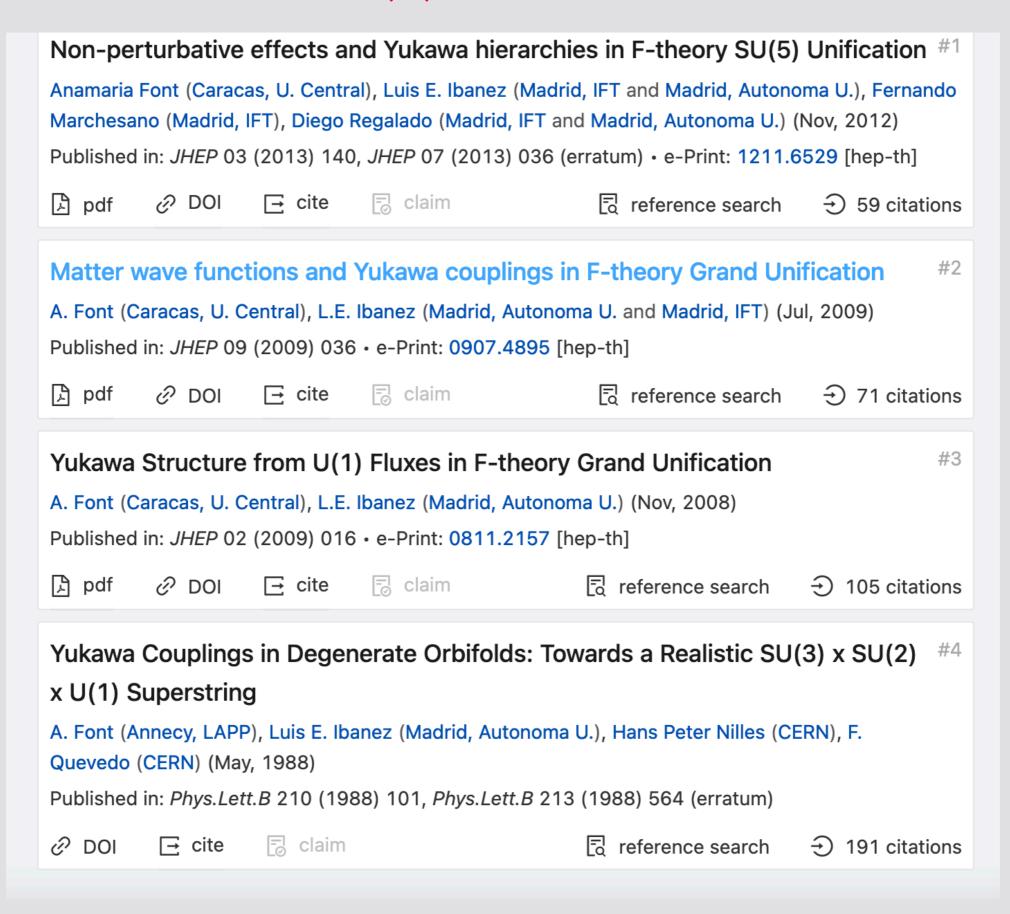
# Work in collaboration with:





G.F. Casas and F. Marchesano arXiv: 2403.09775 and 2404.XXXX to appear

#### I have written several papers on Yukawas with Anamaria:



## Some classical Swampland lore

Vafa 2005, Palti (2019), van Beest et al. (2021), Graña, Herraez (2021)

- U(1) WGC: a particle exists with 
$$~~m~~\leq qgM_p$$

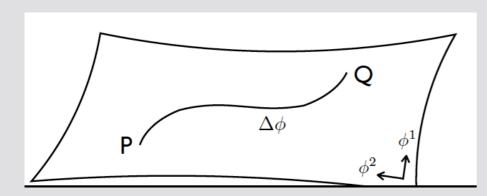
Consistency under dimensional reduction in a circle:
 (sub)Lattice/Tower WGC

$$m_n = nqM_p$$

• The limit  $g \longrightarrow 0$  is singular

A tower of particles should become massless

• Related: as a modulus goes to infinity a tower arises:  $\Delta \phi \to \infty$ 



$$m(Q) \simeq m(P)e^{-\lambda\Delta\phi}$$
  
 $\lambda \sim 1$ 

#### The case of 4D, N=1 and Yukawas

- Not much studied. New features like 4d CHIRALITY
  - Also Yukawa couplings of charged matter fields

 $Y_{abc}(\Phi^a\Phi^b\Phi^c)$ 

• Although less SUSY, results reliable in the perturbative regime

#### **Questions:**

Is  $Y_{abc} \longrightarrow 0$  at infinite distance?

- What goes wrong if at all in that limit ? Are there towers of particles becoming massless?
- If there are towers, what is their structure?
- Are they consistent with the (sub)Lattice WGC?

# Answers we find in this work

- We use Type IIA CY orientifolds with chiral matter at intersecting branes
- $Y_{abc} \rightarrow 0 IS at infinite distance$

• 
$$Y_{abc} \rightarrow 0$$
  
Large volume:  $Y_{abc} \sim \left(\frac{m_{D0}}{M_p}\right)$  decompactification to  $M - th$   
Large C.S.  $Y_{abc} \sim \prod \left(\frac{m_{gon}^a}{M_p}\right)^{1/2}$  and  $p = 2, 4, 6$  large dimensions

Gonions are charged oscillator states localised at intersections, with

$$m_{gon}^2 \simeq n \ \theta \ M_s^2$$

Gonions have all same charge (violate Lattice/Tower WGC) and not extremal

$$m_{gon} \simeq g_*^2 \overline{M_p}$$

• Simplest examples for single large c.s. saxion u go to zero like

$$Y \sim rac{1}{u^r} \qquad \qquad Y \sim g_*^{2r} \qquad \qquad r=1/4, 1/2, 3/4, 1$$
 Explains what goes wrong..

• Application to small Dirac neutrino masses : a dark photon, two large dimensions....but challenging

#### 4d, N=1 Type IIA CY Orientifolds as a laboratory

- CY compactification of IIA with orientifold quotient  $\Omega_{ws}(-1)^{F_L}\mathcal{R}$ ,  $\mathcal{R}(J,\Omega) = (-J,\overline{\Omega})$
- There are O(6) planes and D6-branes wrapping 3-cycles  $~\Pi_{lpha}~and~mirrors~\Pi_{lpha^*}$

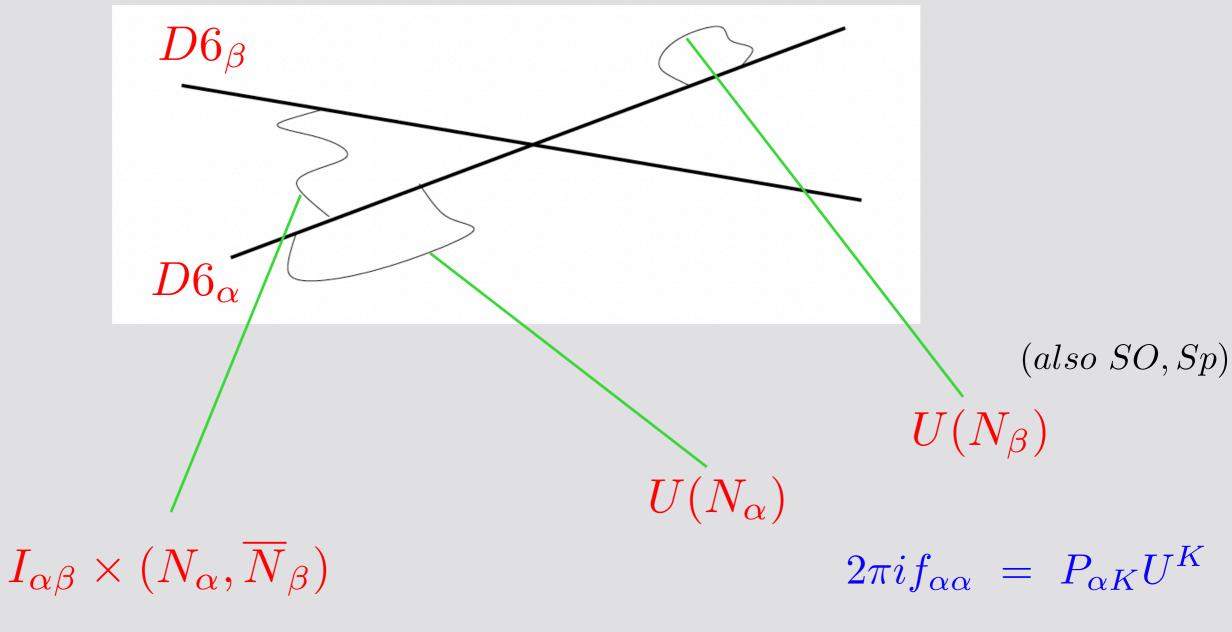
$$[\Pi_{\alpha}] = P_{\alpha J}[\Sigma_{+}^{J}] + Q_{\alpha}^{K}[\Sigma_{K}^{-}] \qquad [\Sigma_{K}^{-}] \cdot [\Sigma_{+}^{J}] = 2\delta_{K}^{J}$$

Closed string moduli:

Kahler:  $T^a = b^a + it^a$ , where  $J_c \equiv B + iJ = (b^a + it^a)\omega_a$  $C.S: U^K = \zeta^K + iu^K$ , where  $\Omega_c \equiv C_3 + ie^{-\phi}Re\Omega = (\zeta^K + iu^K)\alpha_K$ 

• Closed string moduli: (up to w.s. and D2 instantons)

$$K_K \equiv -\log\left(\operatorname{Vol}_{X_6}\right) = -\log\left(\frac{i}{48}\mathcal{K}_{abc}(T^a - \bar{T}^a)(T^b - \bar{T}^b)(T^c - \bar{T}^c)\right)$$
$$K_Q \equiv -2\log\mathcal{H} = -2\log\left(\frac{i}{8\ell_s^6}\int_{X_6}e^{-2\phi}\Omega\wedge\bar{\Omega}\right) = 4\phi_4$$

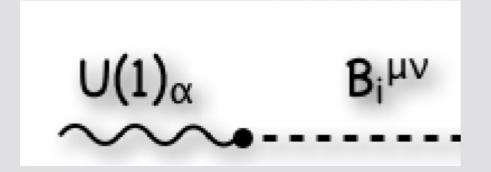


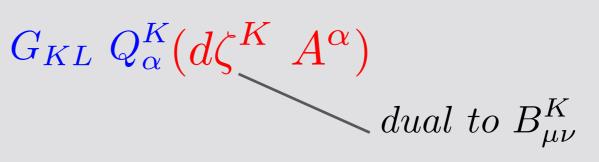
 $chiral \ bi - fundamentals \ at \ intersections$ 

Berkooz, Douglas and Leigh, (1996) Reviews: Blumenhagen et al (2006), Marchesano (2007), Ibañez, Uranga (2012), Marchesano, Schellekns, Weigand (2024)

# U(1)'s

• Some U(1)'s become massive getting Stuckelberg mass mixing with 2-forms:



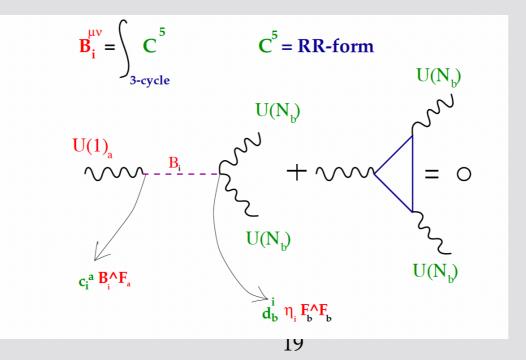


• Stuckelberg masses:

$$M_{\alpha\beta}^2 = 4G_{KL}Q_{\alpha}^K Q_{\beta}^L g_{\alpha}g_{\beta} M_{\rm P}^2$$

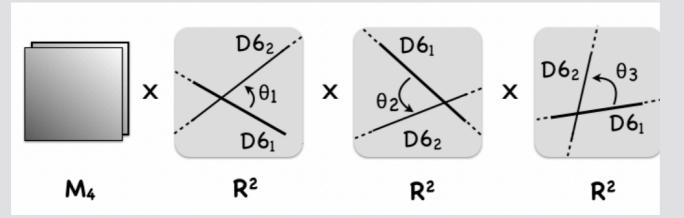
(may have massless eigenvalues, e.g. hypercharge in SM)

• Green-Schwarz cancel some U(1) pure and mixed anomalies



#### Gonions: flavour towers at intersections

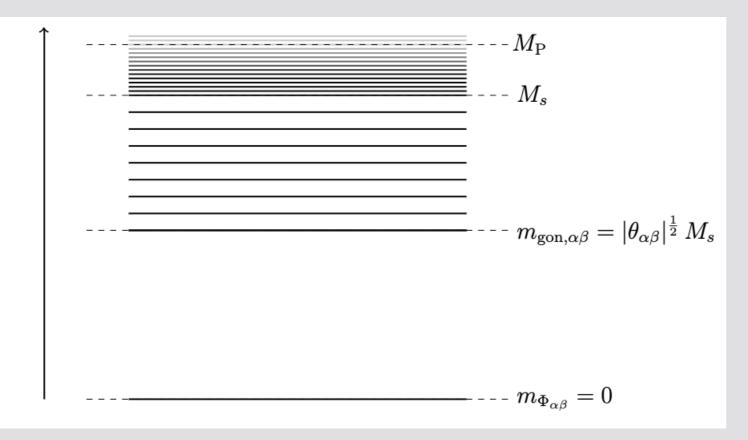
• At an intersection local geometry specified by 3 angles

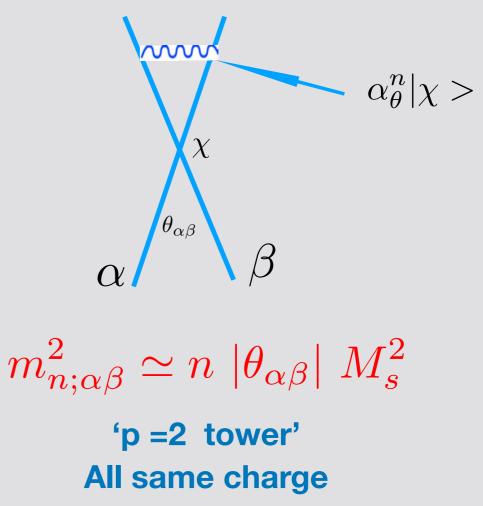


• SUSY preserved at intersection:  $\theta_1 + \theta_2 + \theta_3 \in 2{f Z}$ 

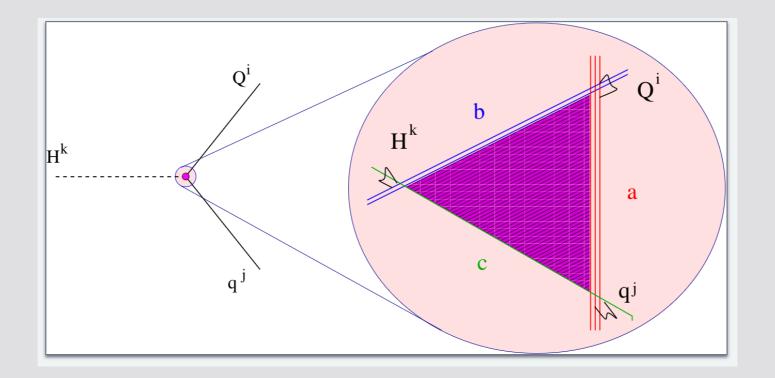
Aldazabal et al (2001)

• In addition to massless chiral bifundamental, a tower of bi-fundamentals: 'Gonions'





#### Yukawas in toroidal and CY orientifolds



Aldazabal et al(2001), Cremades et al(2003), Cvetic et al (2003), Lust et al (2004))

E.g.  $T^2 \times T^2 \times T^2$  orientifolds (or Abelian orbifolds)

$$Y_{ijk} = e^{\phi_4/2} \prod_{r=1}^3 \left( \operatorname{Im} T^r \right)^{-1/2} \left[ \Theta^{(r)} \right]^{1/4} W_{ijk}^{(r)}$$

(ignoring open string moduli)

$$\Theta^{(r)} = 2\pi \frac{\Gamma(1 - |\chi_{ab}^r|)}{\Gamma(|\chi_{ab}^r|)} \frac{\Gamma(1 - |\chi_{bc}^r|)}{\Gamma(|\chi_{bc}^r|)} \frac{\Gamma(1 - |\chi_{ca}^r|)}{\Gamma(|\chi_{ca}^r|)}$$

$$|\chi^r_{lphaeta}| = | heta^r_{lphaeta}| ext{ or } 1 - | heta^r_{lphaeta}|$$

• Essentially depends only on local geometry

• Depends only on local geometry: Expect structure valid for general CY:

$$Y_{ijk} = \frac{e^{\phi_4/2}}{Vol_X^{1/2}} \Theta_{ijk}^{1/4} W_{ijk}$$

• N=1 supergravity: canonically normalized Yukawas given by

$$Y_{ijk} = e^{K/2} \left( K_{i\bar{i}} K_{j\bar{j}} K_{k\bar{k}} \right)^{-1/2} W_{ijk}$$

• Gives information about Kahler metric of chiral matter fields:

$$K_{i\bar{i}}K_{j\bar{j}}K_{k\bar{k}} = e^{3\phi_4}\Theta_{ijk}^{-1/2}$$

#### Kinetic terms of chiral fields

• Thus for the toroidal case, recalling

$$\Theta^{(r)} = 2\pi \frac{\Gamma(1 - |\chi_{ab}^r|)}{\Gamma(|\chi_{ab}^r|)} \frac{\Gamma(1 - |\chi_{bc}^r|)}{\Gamma(|\chi_{bc}^r|)} \frac{\Gamma(1 - |\chi_{ca}^r|)}{\Gamma(|\chi_{ca}^r|)}$$

$$K_{i\bar{i}} = e^{\phi_4} (2\pi)^{-1/2} \prod_{r=1}^3 \left( \frac{\Gamma(|\chi_i^r|)}{\Gamma(1-|\chi_i^r|)} \right)^{1/2}$$

$$|\chi^r_{lphaeta}| = | heta^r_{lphaeta}| ext{ or } 1 - | heta^r_{lphaeta}|$$

 $\mathcal{H} = e^{-2\phi_4}$ 

• For small angles, recalling  $heta^r \simeq (m_{gon}^r/M_s)^2$ 

$$K_{i\bar{i}} \simeq \frac{e^{\phi_4}}{(\theta_{\alpha\beta}^{min})^{1/2}} \simeq e^{2\phi_4} \frac{M_p}{m_{gon,\alpha\beta}^{min}}$$

- Will give rise to a singular behaviour as  $\ m_{gon,\alpha\beta}^{min} 
ightarrow 0$ 

The  $Y \longrightarrow 0$  limit and infinite distance

$$Y_{ijk} = \frac{W_{ijk}}{Vol_X^{1/2}} e^{\phi_4/2} \Theta_{ijk}^{1/4}$$

Infinite distance and Kahler moduli (fixed c.s.)

$$\frac{Y_{ijk}}{Vol_X^{1/2}} \longrightarrow 0 \quad \longrightarrow \quad Vol_X \longrightarrow \infty$$

 $(W_{ijk} \rightarrow 0 \ typically \ requires \ non-generic \ fine-tuning)$ 

• These limits are at infinite distance: SDC a tower of particles should become massles: the D0's

$$m_{D0}^2 \simeq \frac{M_p^2}{Vol_X} \longrightarrow |Y| \simeq \frac{m_{D0}}{M_p}$$

• So this limit is the M-theory limit

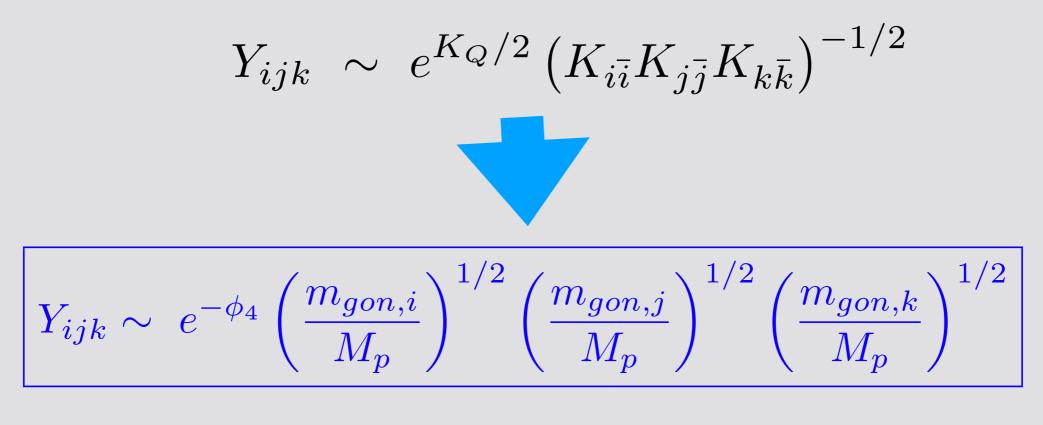
A tower of particles should become massless

#### Small Yukawas and gonion masses

Infinite distance and complex structure (fixed Kahler moduli)

$$Y_{ijk} \simeq B e^{\phi_4/2} \Theta_{ijk}^{1/4}$$

With e.g. at least one small angle per complex plane and SUSY (No N=2 planes)



See also Castellano, Herraez, Ibañez (2023)

• Simple example with a dominant small angle:

$$\mathbf{\dot{k}} \stackrel{\mathbf{i}}{\mathbf{k}} \simeq e^{-\phi_4} \left(\frac{m_{gon,i}}{M_p}\right)^{1/2} \left(\frac{M_s}{M_p}\right)^{1/2} \left(\frac{M_s}{M_p}\right)^{1/2}$$

$$Y_{ijk} \simeq \left(\frac{m_{gon,i}}{M_p}\right)^{1/2}$$

- Small Yukawas imply a tower of light particles with same charge as the massless field
- In EFT gonion masses come from FI-term of U(1) gauge group felt at the intersection

$$m_{gon}^2 \simeq g_*^2 \xi_{FI}^* \simeq g_*^2 \frac{Q_*^u}{u} M_p^2 \simeq \frac{Q_*^u}{u^2} M_p^2$$
  
 $\theta \sim 1/u$   $-\log(U + U^* - Q_*^u V_*)$   $Ref_* \simeq \frac{1}{g_*^2} \simeq u$ 

 $g_*$  is the gauge coupling of the U(1) (sub)group under which the leading gonions transform

### General asymptotic behaviour of Yukawas

• We have considered the infinite c.s. limit in several settings/examples:

• 'STU' Type IIA orientifold models models, dual to magnetized Type I and SO(32) models with U(1) bundles

- 'EFT String Limits of refs.
- Specific toroidal Type IIA orientifolds (e.g. Pati-Salam-like)

Blumenhagen, Honecker, Weigand (2005)

Lanza, Marchesano, Martucci, Valenzuela (2021) Cremades, Ibañez, Marchesano (2002)

• A lot of casuistics......For limits parametrized by a single growing c.s. field u :

$$Y_* \sim \frac{1}{u^r}$$
  $r = \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1$   
(Recall Y~  $e^{\phi_4/2}\Theta_{ijk}^{1/4}$ )

• Consistent with Type IIB results in : Conlon, Cremades, Zuevedo hep-th/0609180 (2006)

• Thus in general one will have

$$Y_* \sim g_*^{2r}$$

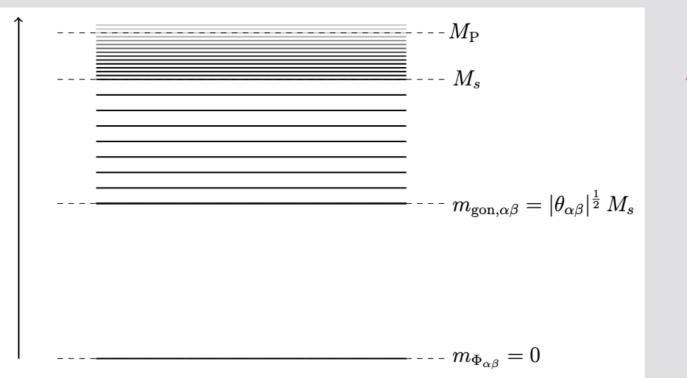
 $g_{*}$  again, is the gauge coupling of the (sub)group under which the leading gonions transform

• Thus in a vanishing Yukawa coupling limit :

$$Y_* \to 0 \longrightarrow g_* \to 0$$

• This explains why this limit is singular: the gauge group would survive as a global symmetry, which is forbidden in QG

## More about the gonion towers



$$m_{n;\alpha\beta}^2 \simeq n |\theta_{\alpha\beta}| M_s^2$$

'p =2 tower'

#### All same charge: not BPS

• Thus e.g. in the simple class of models with a single leading gonion tower (along with two large dimensions) one has

$$m_{
m gon} \sim g_* M_s \sim g_*^2 M_{
m P} \,, \qquad Y_* \sim g_* \,, \qquad g_* \sim e^{\phi_4}$$

The WGC condition  $m \leq \sqrt{2}gM_p$  verified with room to spare

• The (sub)Lattice/Tower WGC not realised here (all gonions have same charge)

# Neutrinos at infinite distance?

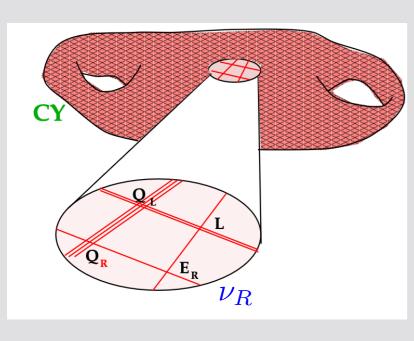
If neutrinos are Dirac tiny Yukawas ~  $10^{-13}$  needed....



#### Dirac neutrinos at infinite distance

how

G. Casas, L. Ibañez, F. Marchesano hep-th/2404.XXXX



The SM at intersecting D6-branes:  $U(3)_a \times Sp(2)_b \times U(1)_c \times U(1)_d$ 

only hypercharge massless after  $B \wedge F$  couplings

 $\nu'_R s$  only charged under

 $Q_{\nu} \equiv (Q_c + Q_d) = 2I_R - L$ 

With a single large c.s. field M:

$$\Lambda d^* \quad Y_{\nu} \simeq \left(\frac{m_{gon}^{\nu}}{M_p}\right)^{1/2} \simeq g_{\nu} \simeq \ 6.9 \times 10^{-13} \ (exp.)$$

• Then all scales fixed since they are determined by  $\,g_{
u}\,$  in rather universal way :

String Scale	KK small dim	SM KK replicas	$ u_R, \tilde{\nu}_R  ext{ tower }$	large dim	Dark vector boson
$M_s$	$M_{KK}, M_{KK/W}(D6)$	$m_{gon}^{SM}$	$m_{gon}^{ u}$	$m_{KK}$	$M_V$
$g_ u M_p$	$\lesssim g_{ u} M_p$	$\lesssim g_{ u} M_p$	$g_ u^2 M_p$	$g_ u^2 M_p$	$g_{ u} ar{H}  - g_{ u}M_s$
$700 { m TeV}$	$\lesssim 700 TeV$	$10-100~{\rm TeV}$	500  eV	500  eV	$5\times 10^{-2}$ - $500~{\rm eV}$

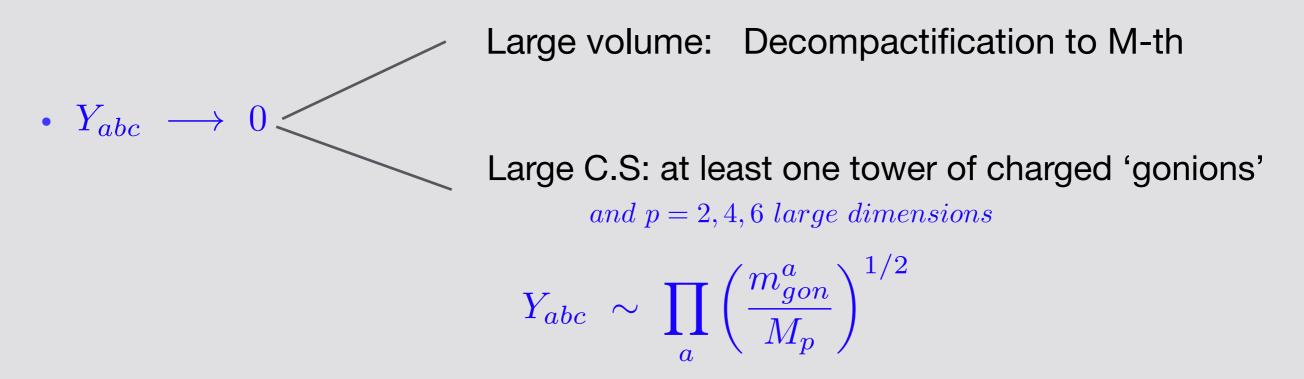
• However: only SUSY, examples with just Hypercharge massless known are the CFT orientifold examples of Schellekens et al (2004) which are non-geometric

• Implementation in a geometric setting challenging

# Conclusions

• Using Type IIA CY N=1 orientifolds as a laboratory:

 $Y_{abc} \longrightarrow 0 IS at infinite distance$ 



• Gonions have all same charge (violate Lattice/Tower WGC) and not extremal, e.g. for a single tower of gonions

 $m_{gon} \simeq g_*^2 M_p \qquad \qquad M_s \simeq g_* M_p$ 

• Simplest examples for single large c.s. saxion u go to zero like



• Also the gauge coupling of (sub)group felt at the intersection



Application to small Dirac neutrino masses: rather unique setting with

$$Y_{\nu} \simeq \left(\frac{m_{gon}^{\nu}}{M_p}\right)^{1/2} \simeq g_{\nu} \simeq 6.9 \times 10^{-13} \ (exp.)$$

e.g. light gauge boson coupling to $(2I_R - L)$  with a mass ~ 5 × 10<sup>-2</sup> eV

• Implementation in a geometric string setting challenging

Thank you !!



# Congratulations Anamaria for your fantastic work!!

Your friendship is a privilege!!



Back-up

#### Consistency with WGC under dimensional reduction

• It has been argued it is required that the WGC comes with a full tower of states with all charges (Lattice/Tower WGC)

- Gonions are a counterexample This is because of the double supression  $m_{gon} \simeq g_*^2 M_p$ 
  - After compactifying the theory on a circle, the 'convex hull' contains the extremal region if we remain in perturbation theory

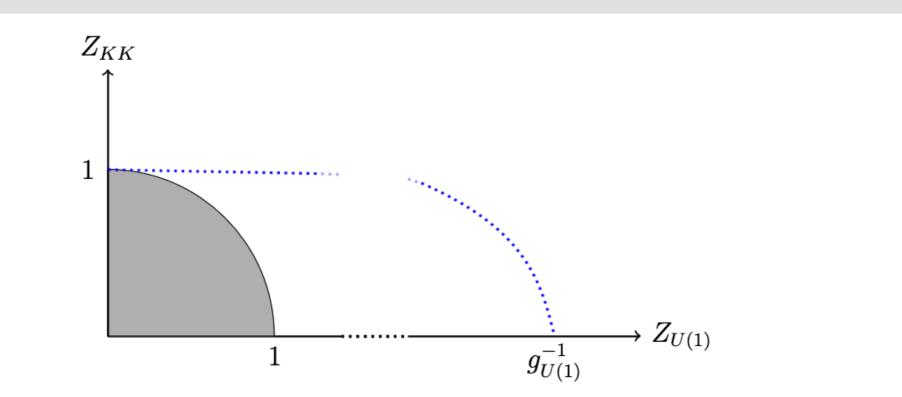


Figure 9: Blue line corresponds to the convex hull of the charge-to-mass ratio  $\vec{Z} = \vec{Q}/m_{\text{gon}}^{\text{KK}}$ , where  $m_{\text{gon}}^{\text{KK}}$  are the gonion Kaluza-Klein replicas. If the radius of the circle compactification satisfies  $R \gtrsim M_{\text{P}}^{-1}$ , the convex hull always contains the extremal region (grey area, see [108, eq.(83)]). Here we stay in a perturbative regime  $g_{U(1)} \ll 1$ .

