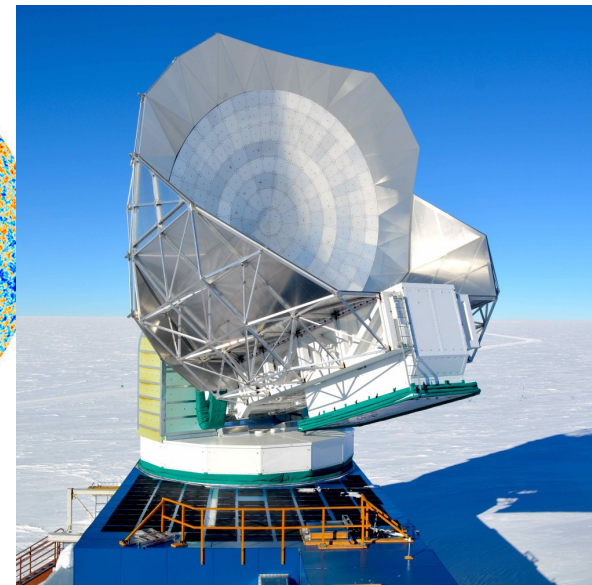
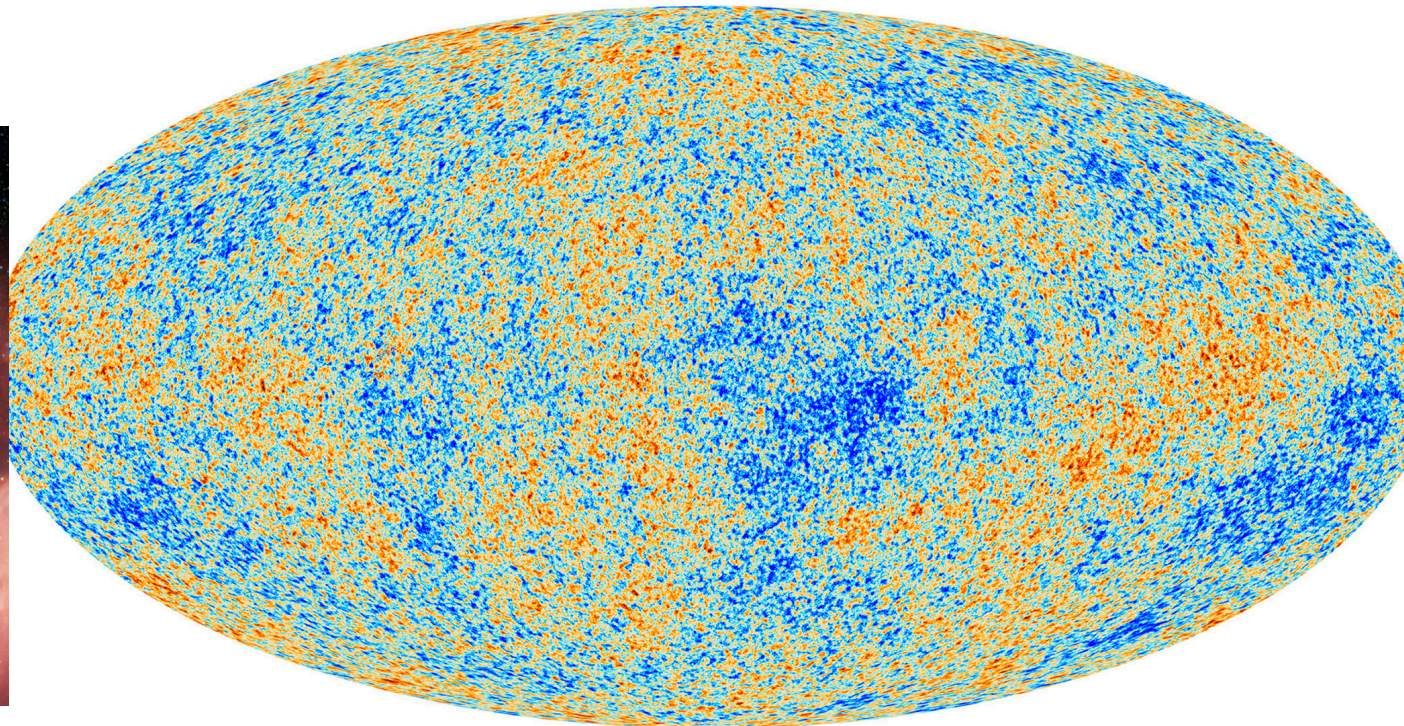
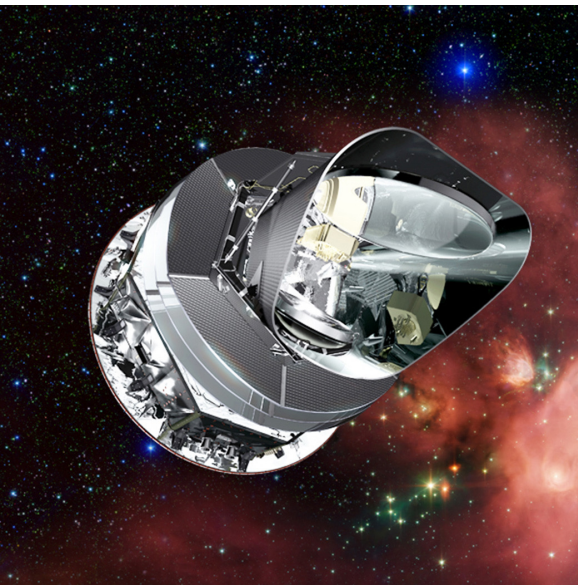


A joint Planck and SPT-SZ measurement of CMB lensing cluster masses

Alexandre Huchet

Supervisor: Jean-Baptiste Melin – CEA / Irfu / DPhP



A joint Planck and SPT-SZ
measurement of

CMB lensing cluster masses

A quick introduction/reminder

A joint Planck and SPT-SZ
measurement of

CMB lensing

cluster masses

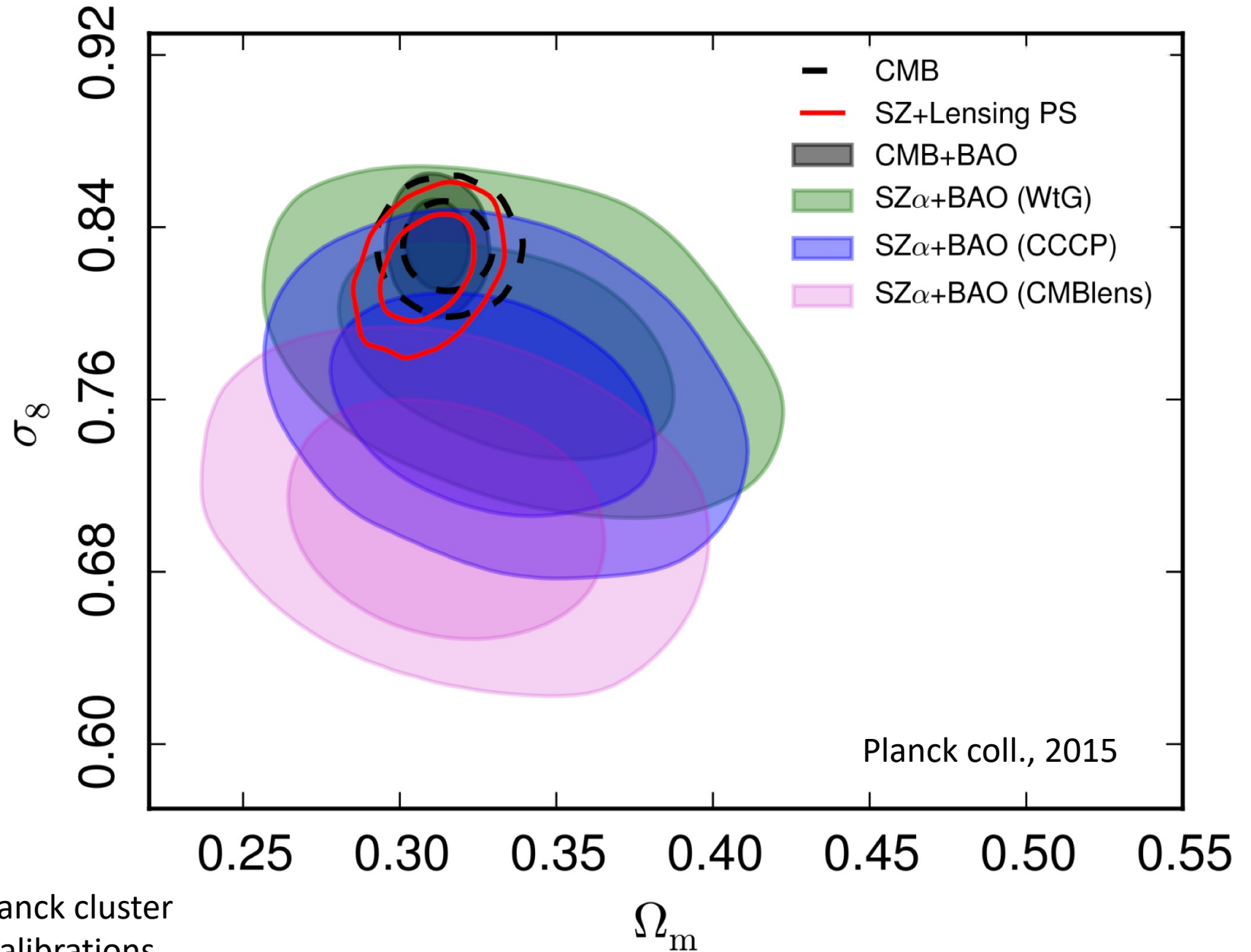
A quick introduction/reminder

Cosmology with clusters

Mass function:

$z, M \leftrightarrow \text{cosmo}$

- Redshift from optical survey
- Mass from?



Constraints on σ_8 and Ω_m from Planck cluster count, based on different mass calibrations

A joint Planck and SPT-SZ
measurement of

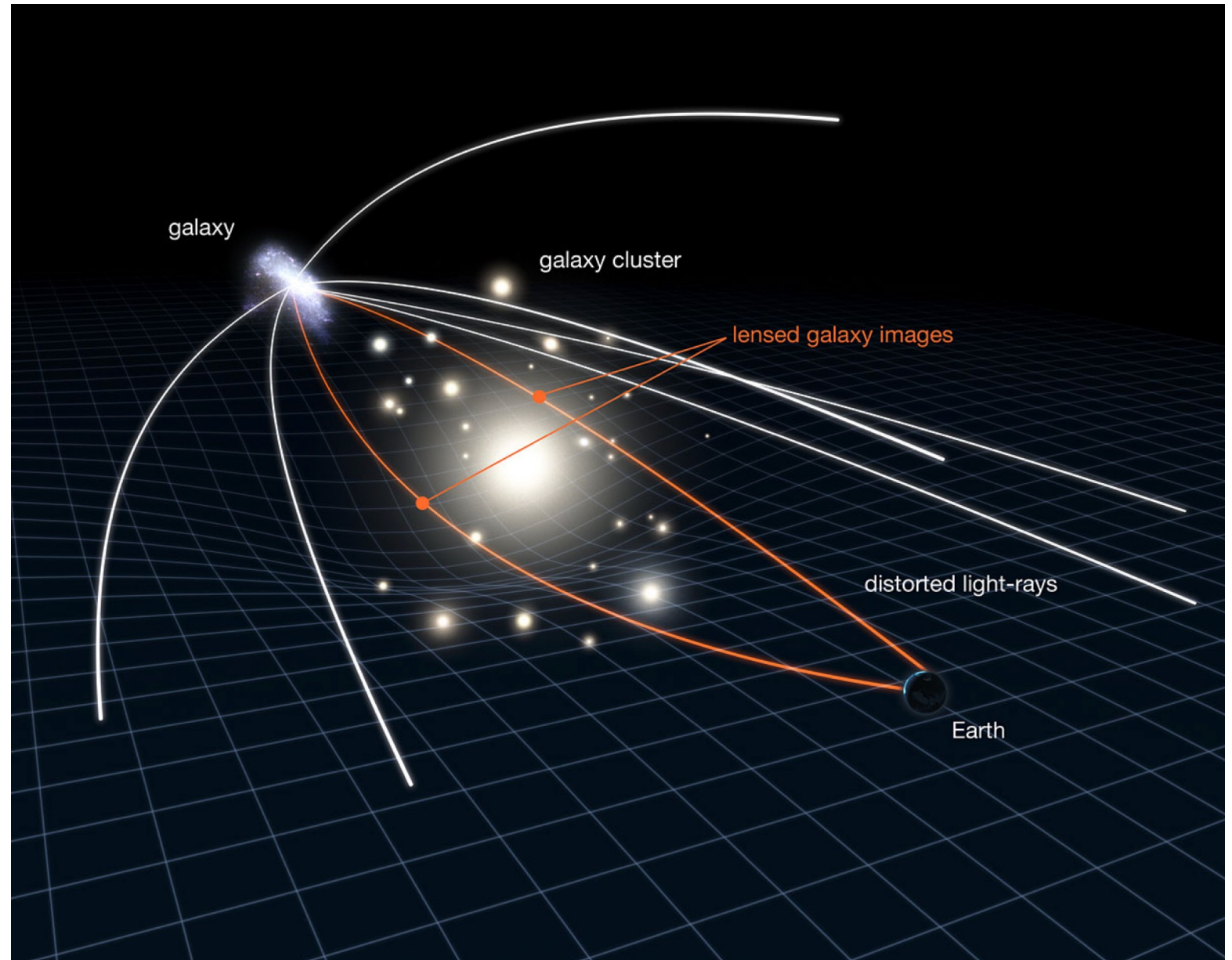
CMB lensing

cluster masses

A quick introduction/reminder

Gravitational lensing

- **Visible light:** galaxies, 3% of total mass
- **X-rays:** hot intracluster gas, 12% of total mass
- **Gravitational lensing:** the above + dark matter (85%)
= 100% of total mass

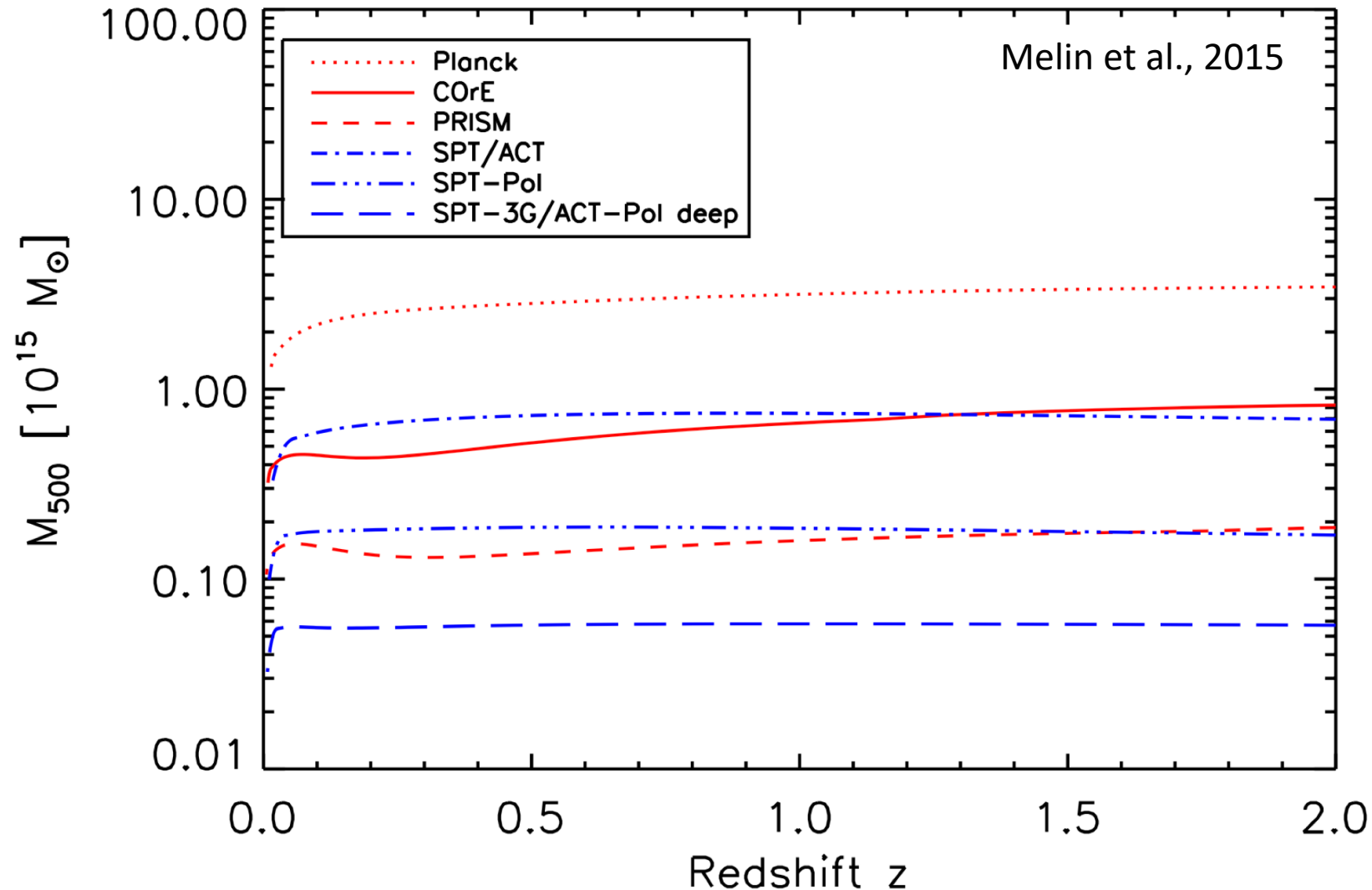


Lensing induced by a cluster on a background galaxy

Which source?

Two different types of sources:

- **Background galaxies:** need to find background galaxies, i.e. up to $z \sim 1$
- **CMB:** the CMB is the source, i.e. up to $z \sim 1100$



Mass measured with a signal to noise ratio of 1 as a function of redshift for CMB lensing

A joint Planck and SPT-SZ

measurement of

CMB lensing

cluster masses

A quick introduction/reminder

Two surveys

Planck/HFI

- In space
- All-sky: 42000 deg²
- 5 arcmin beam
- 6 frequencies: 100, 143, 217, 353, 545, 857 GHz

SPT-SZ

- Ground based
- 2500 deg²
- 1.75 arcmin beam
- 3 frequencies: 95, 150, 220 GHz

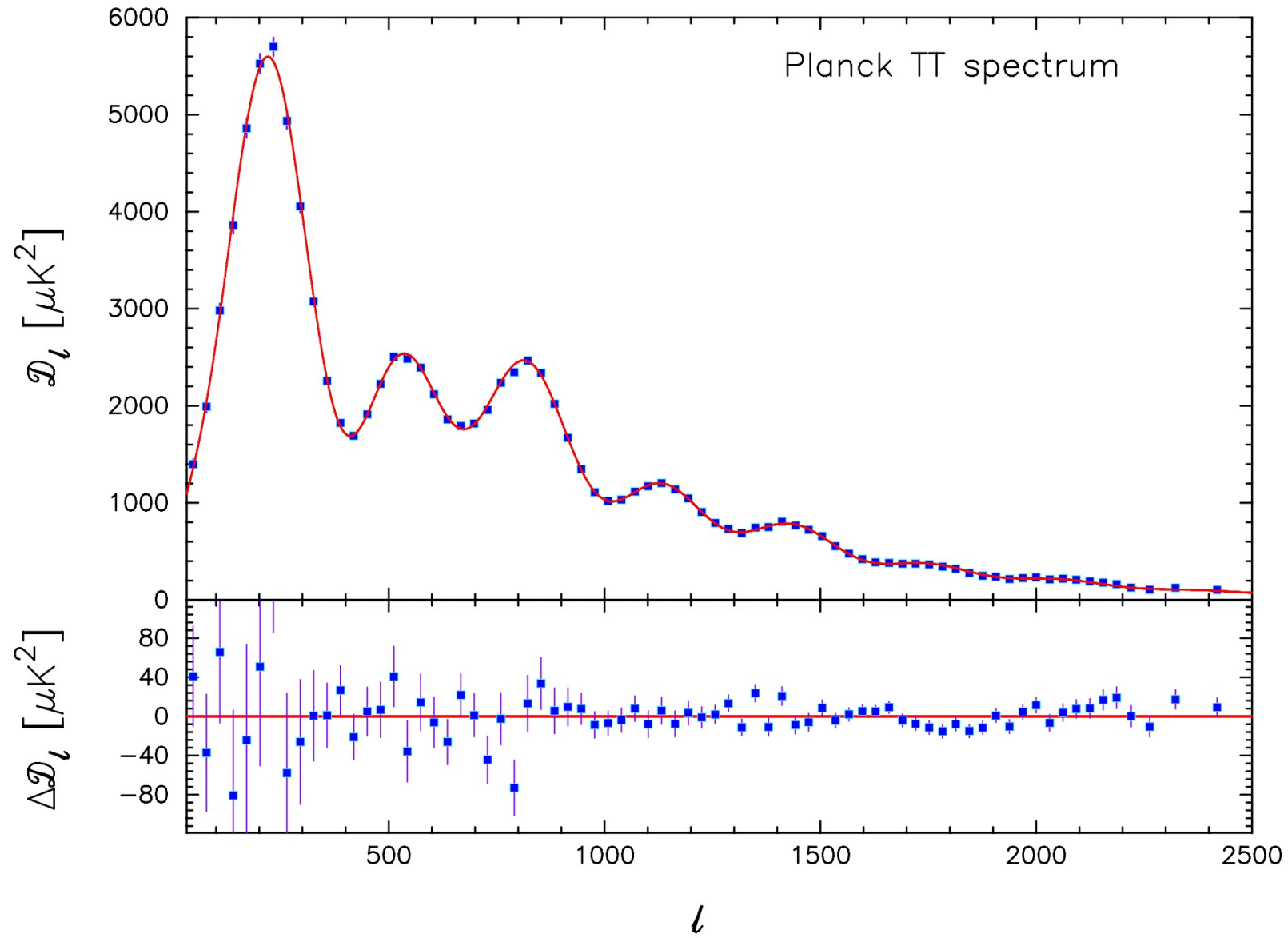
We use a sample of 468 clusters from SPT-SZ (Bocquet et al, 2019)

What to do then?

- We use **Planck** et **SPT-SZ**, two complementary data sets
- First steps: **separated** analysis for each data set
 - Analysis on simulated maps
 - Apply the method to real data
- We then **combine** the Planck and SPT-SZ data sets
 - First simulation
 - Then real data

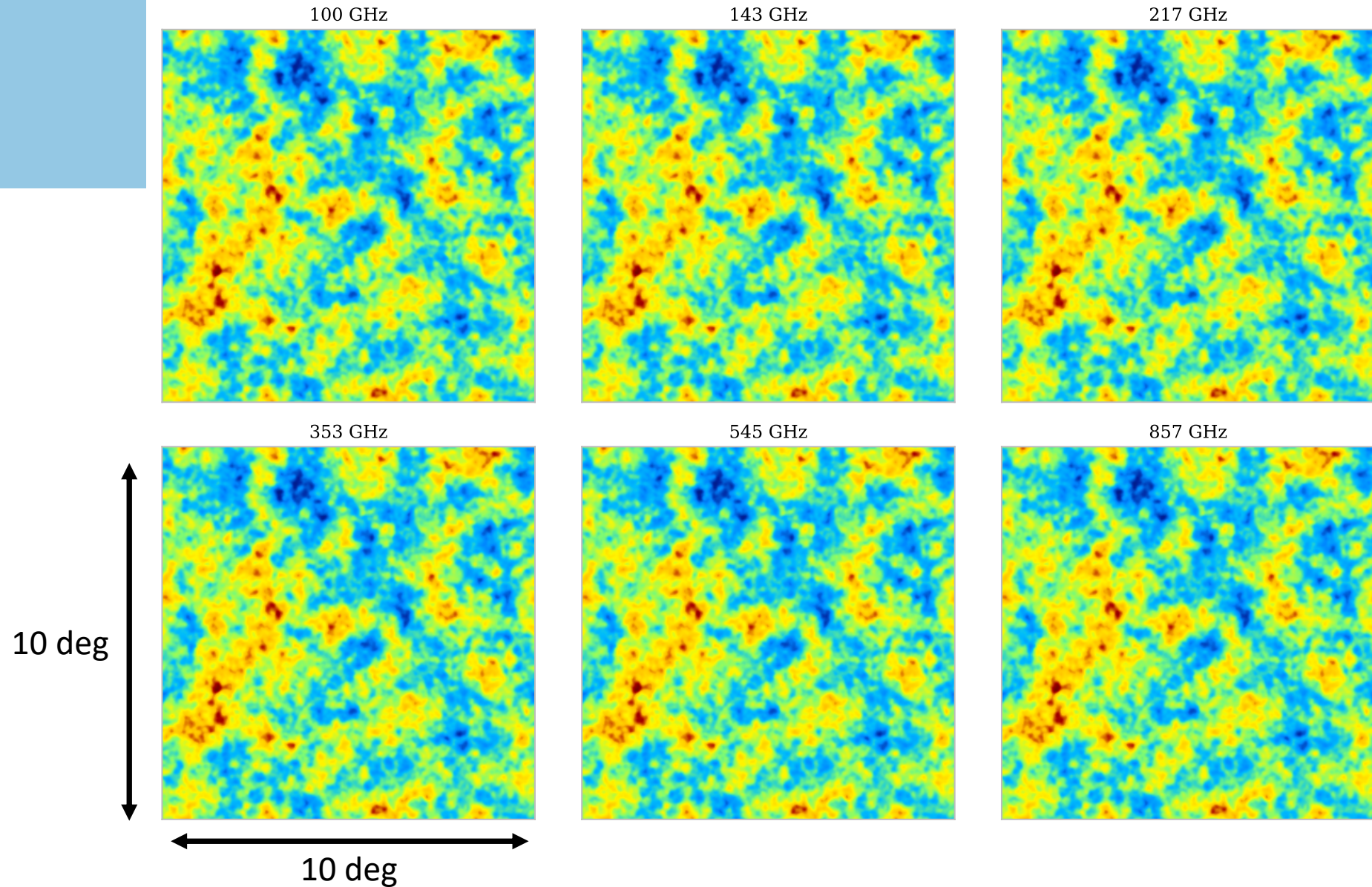
Map simulation

- **CMB:** Gaussian random field from Planck CMB power spectrum
- **Cluster lens:** Navarro-Frenk-White (NFW) density profile
- **SZ effect:** generalized NFW (GNFW) profile (Arnaud et al. 2010)
- **Instrumental point spread function (PSF)**
- **Instrumental noise**



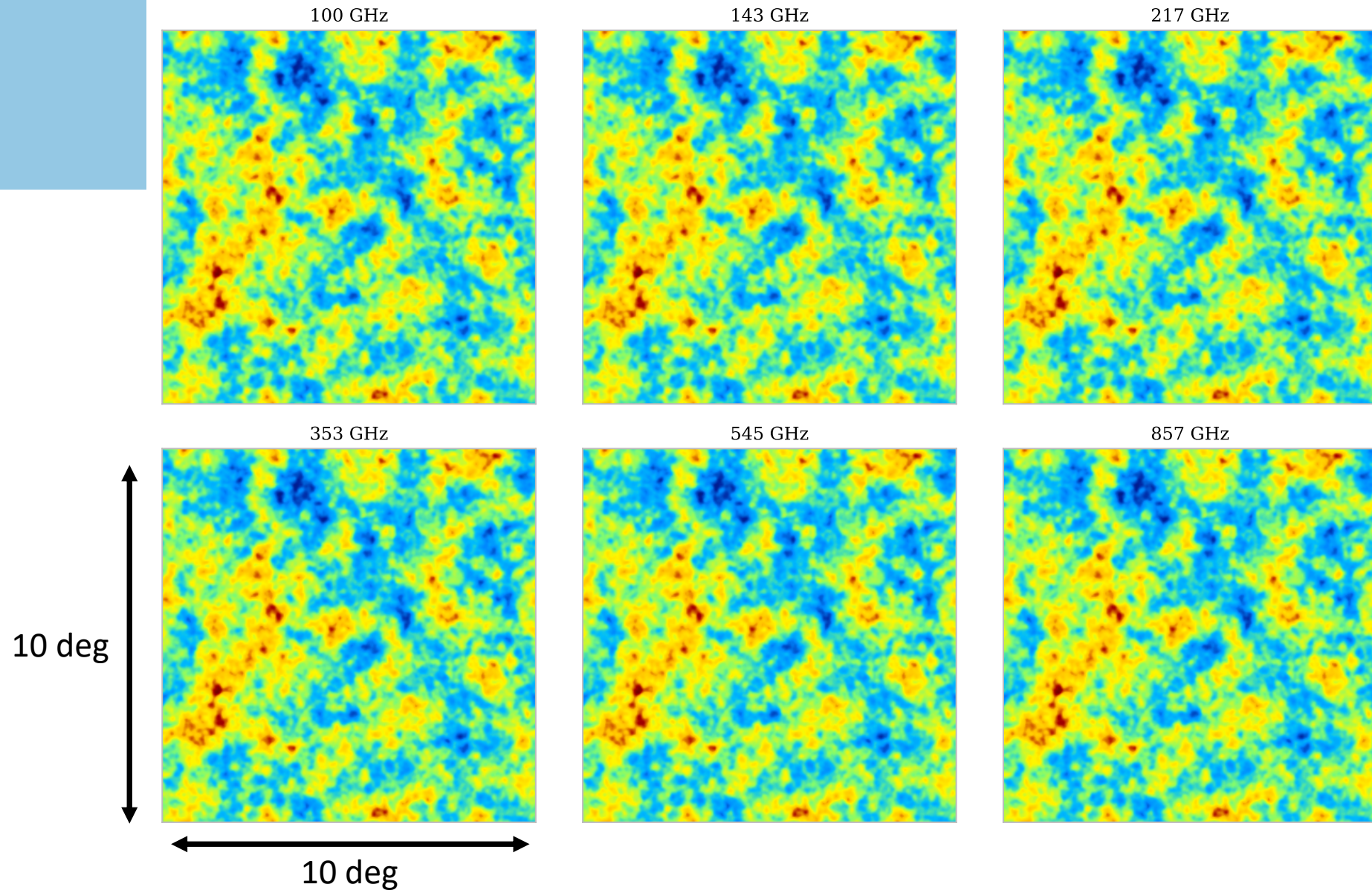
Planck simulation

- CMB



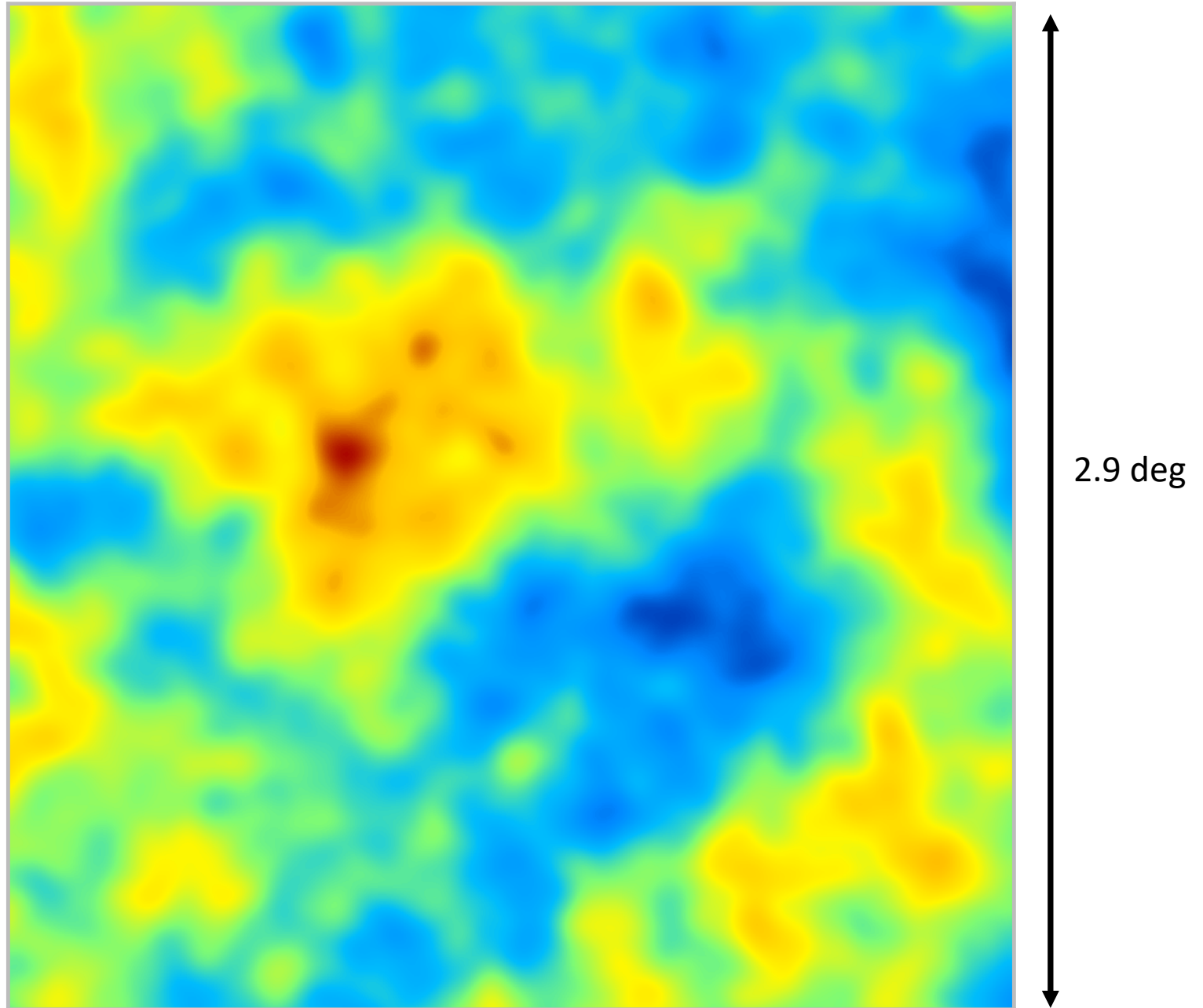
Planck simulation

- CMB
- Cluster lens



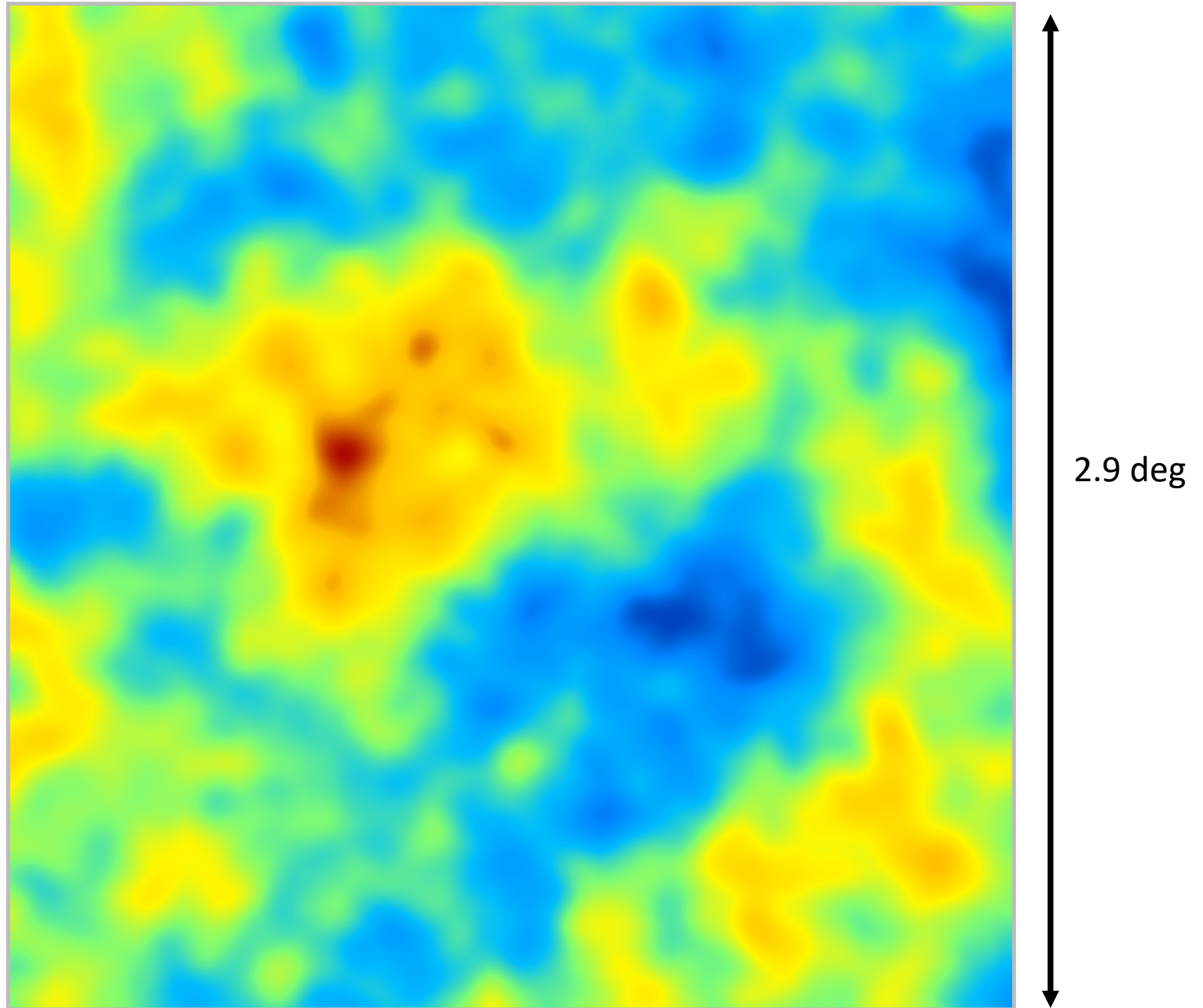
Planck simulation

- CMB
- No lensing



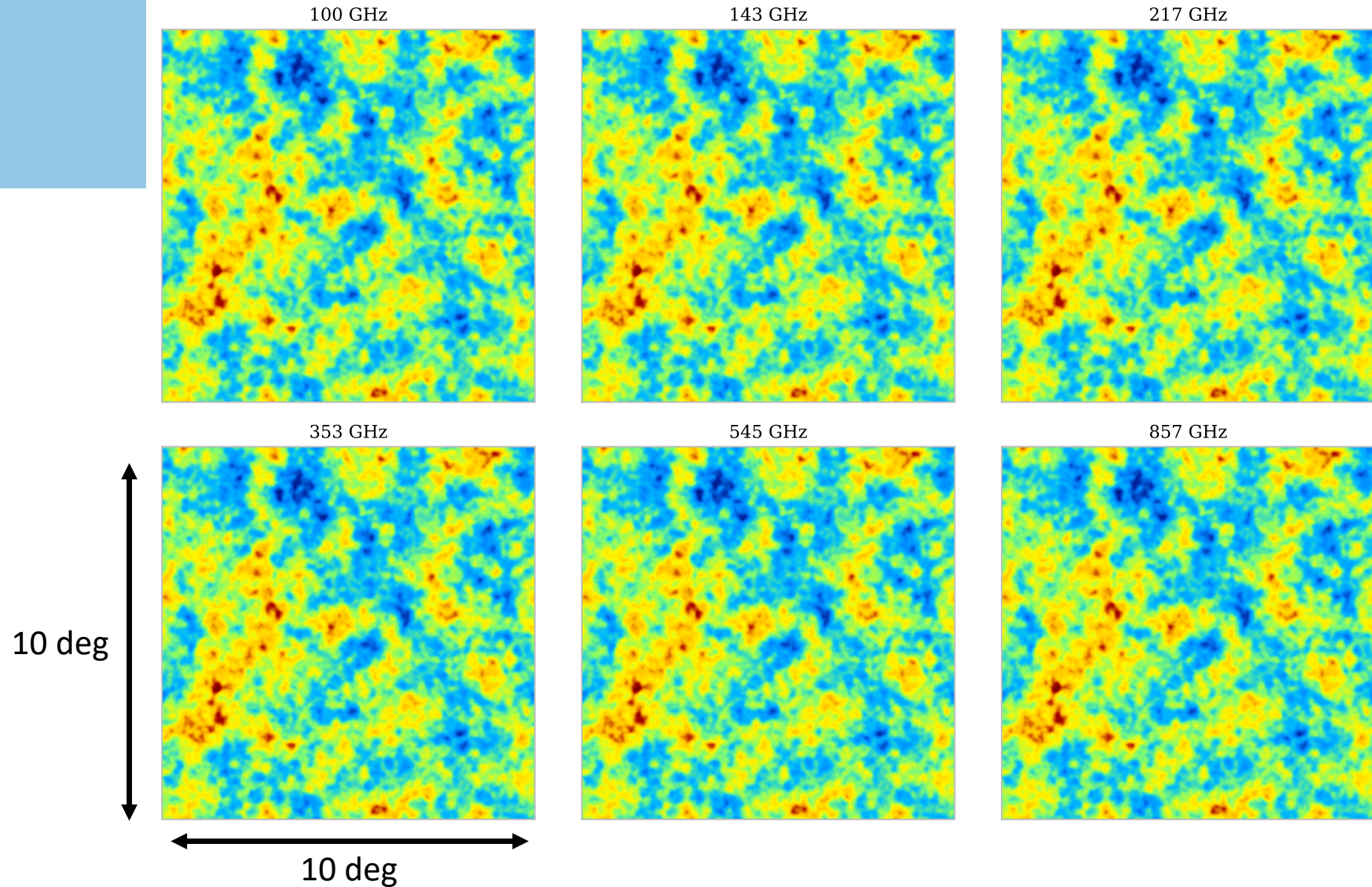
Planck simulation

- CMB
- Lensing



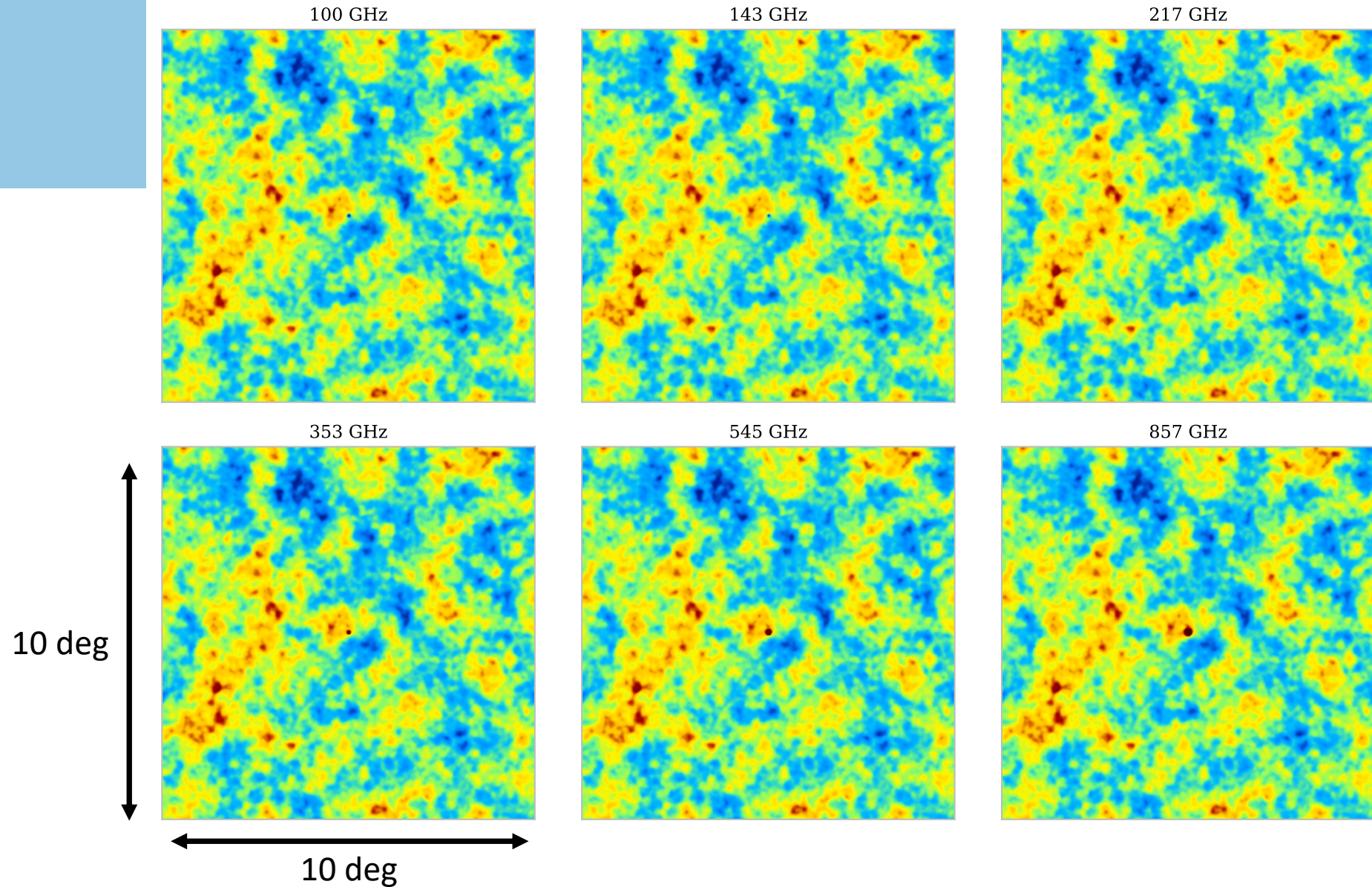
Planck simulation

- CMB
- Cluster lens



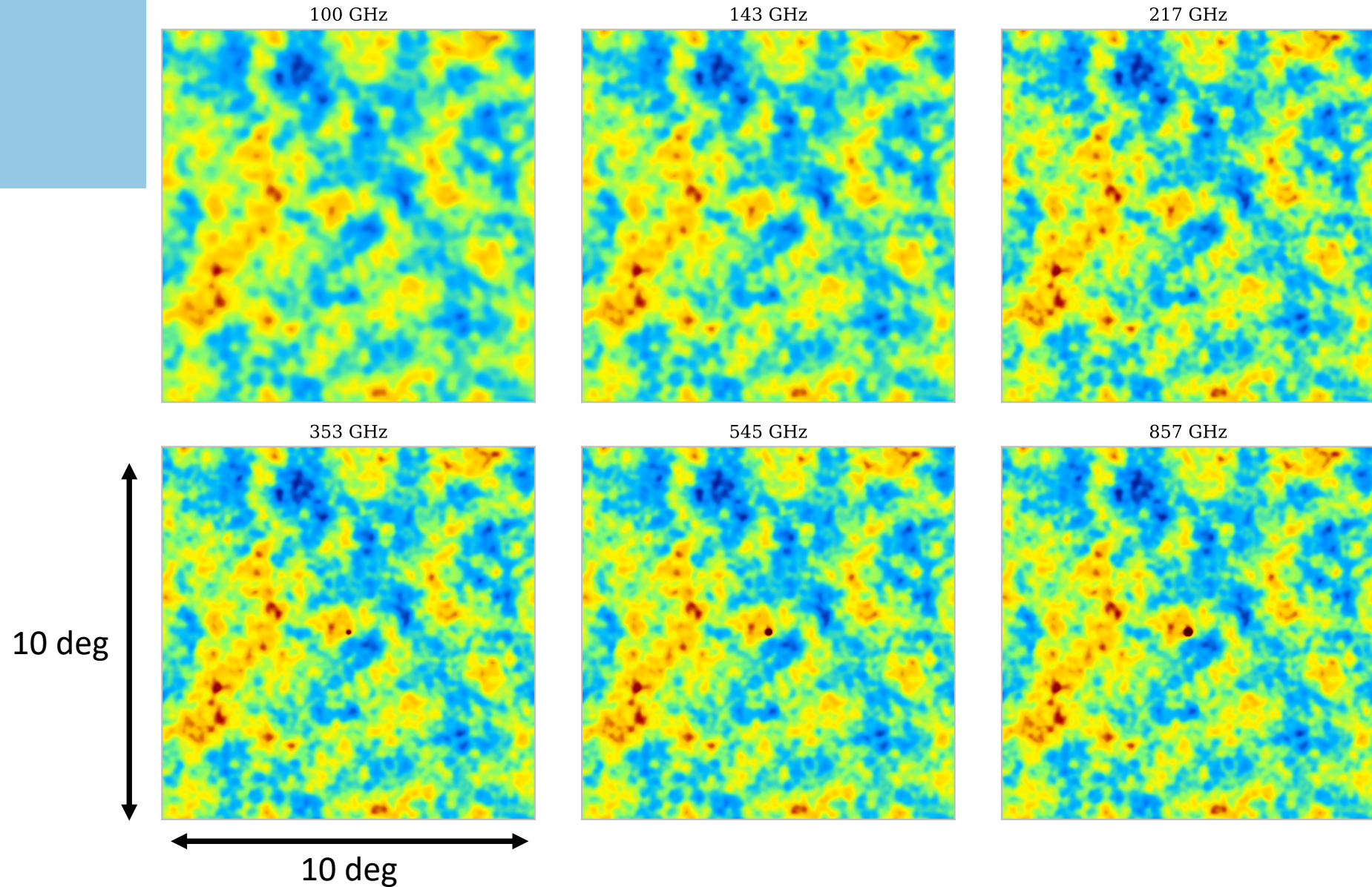
Planck simulation

- CMB
- Cluster lens
- SZ effect



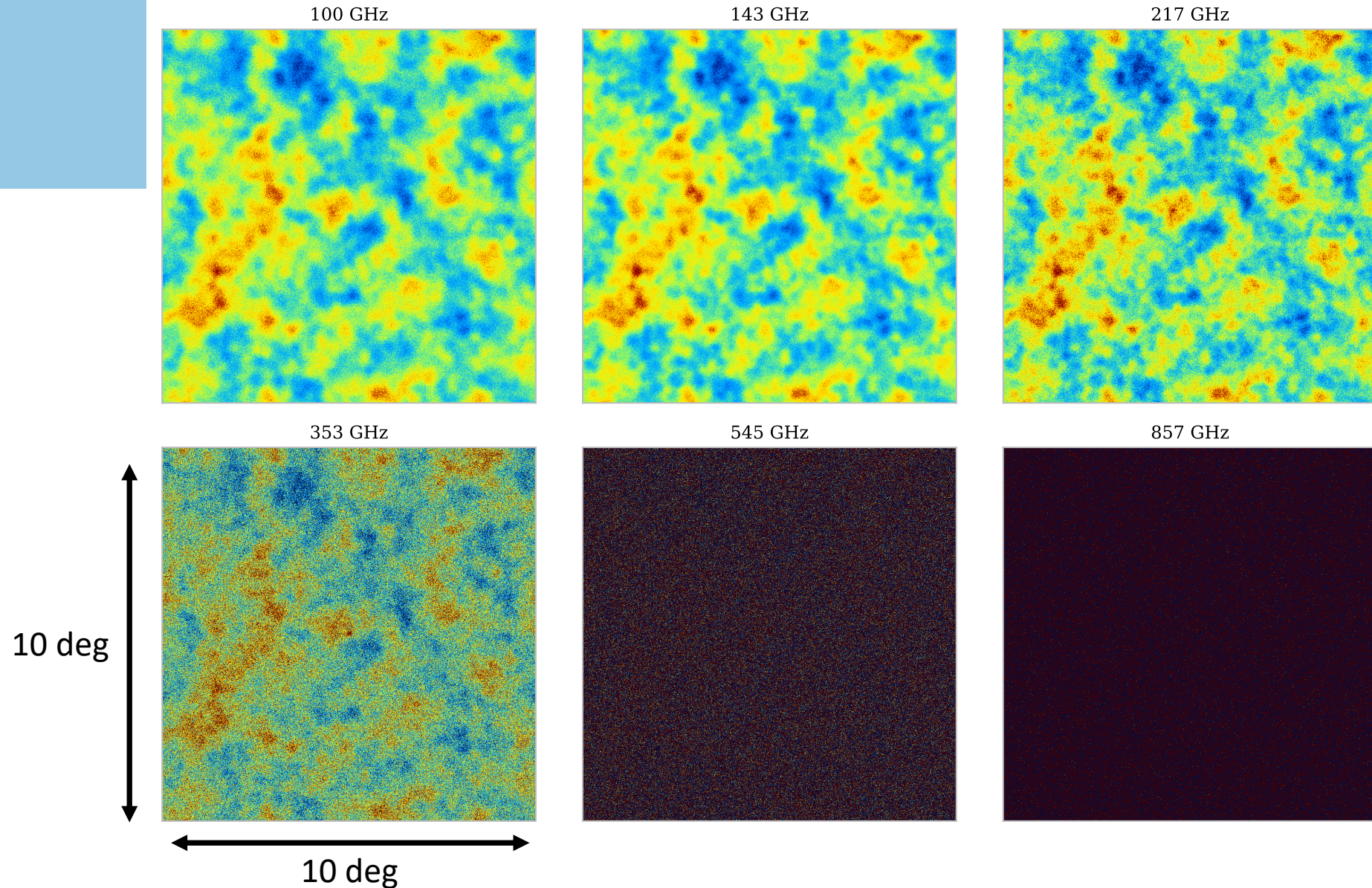
Planck simulation

- CMB
- Cluster lens
- SZ effect
- Instrumental PSF



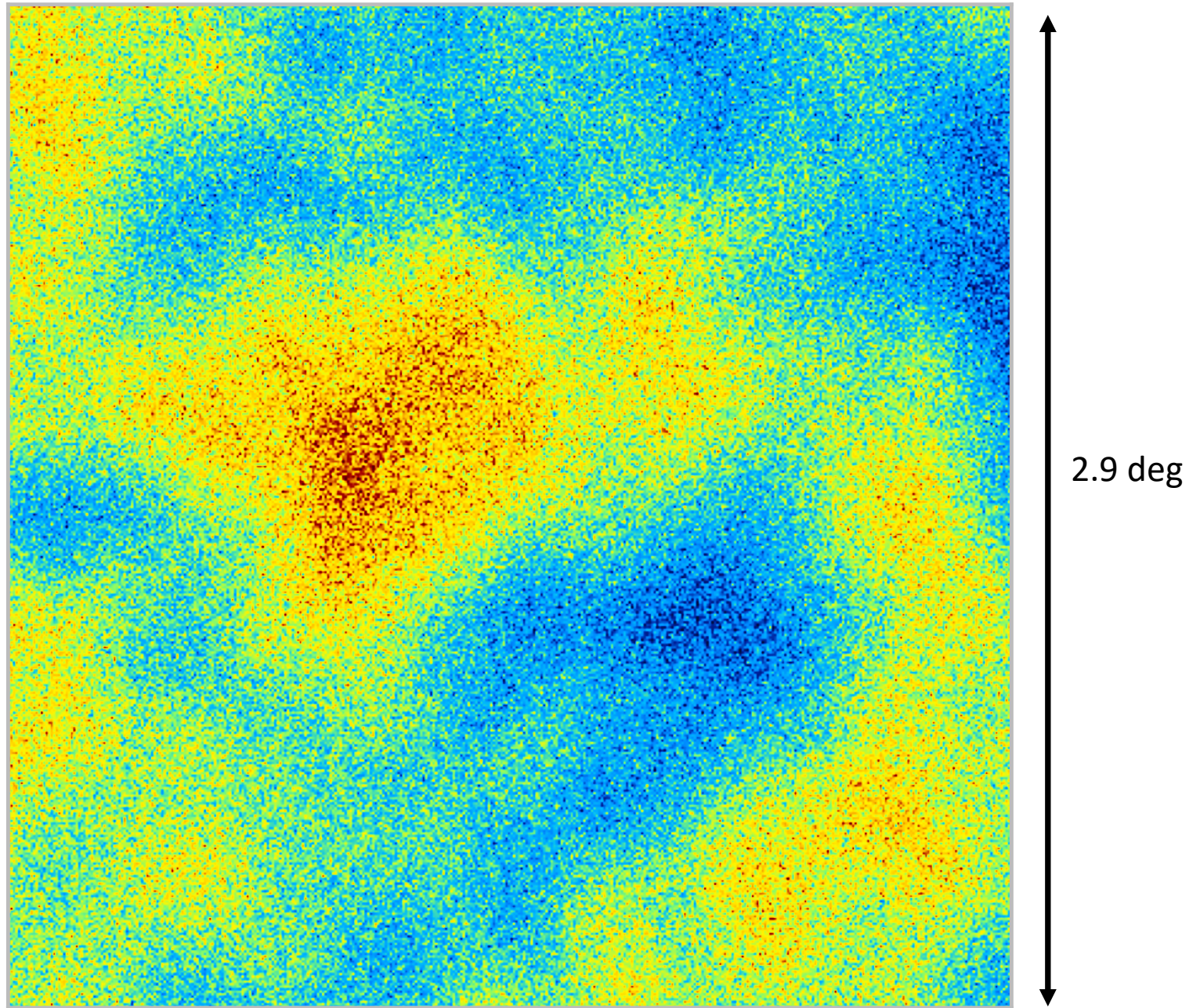
Planck simulation

- CMB
- Cluster lens
- SZ effect
- Instrumental PSF
- Instrumental noise



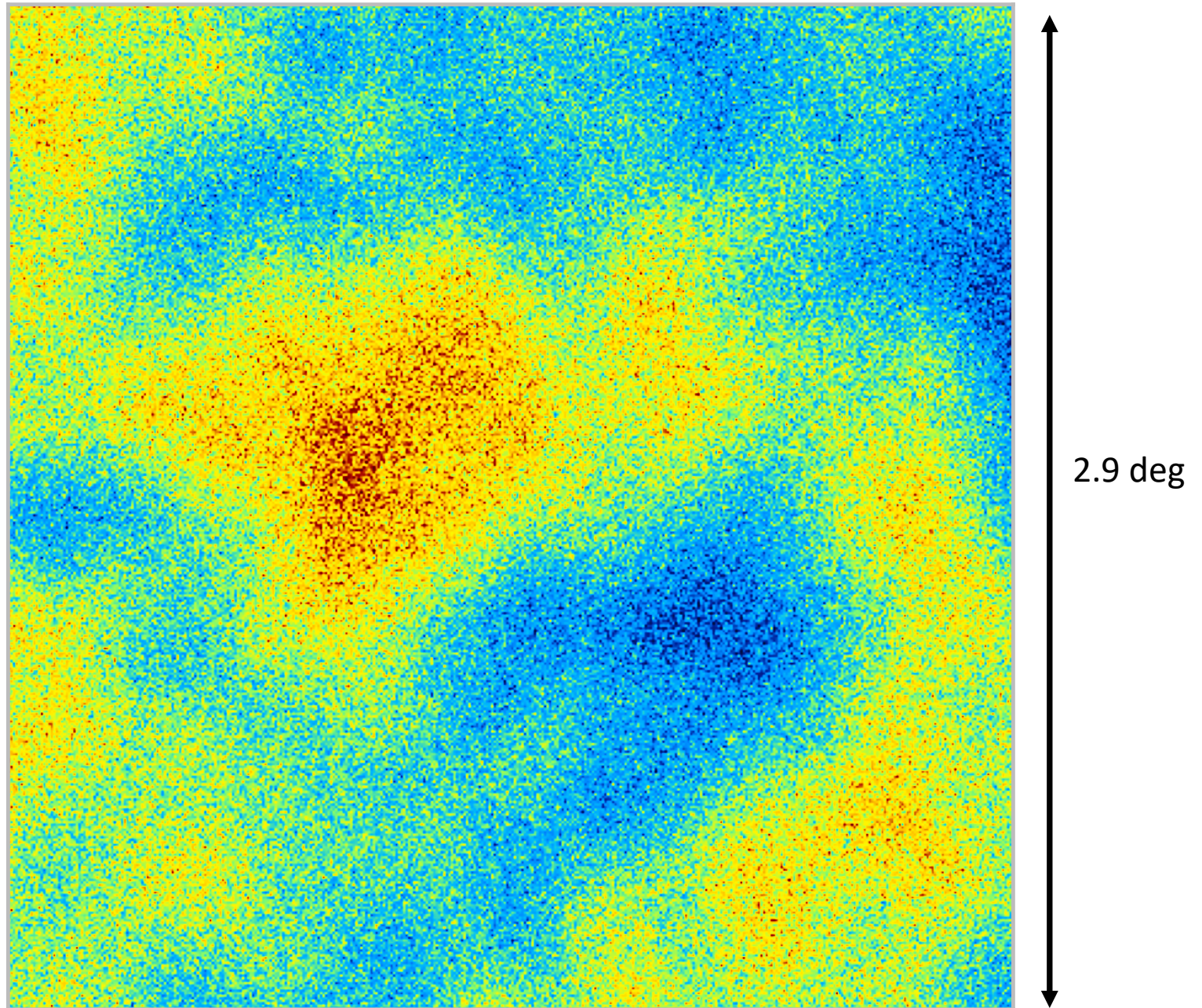
Planck simulation

- 100 GHz map
- No SZ effect
- No lensing



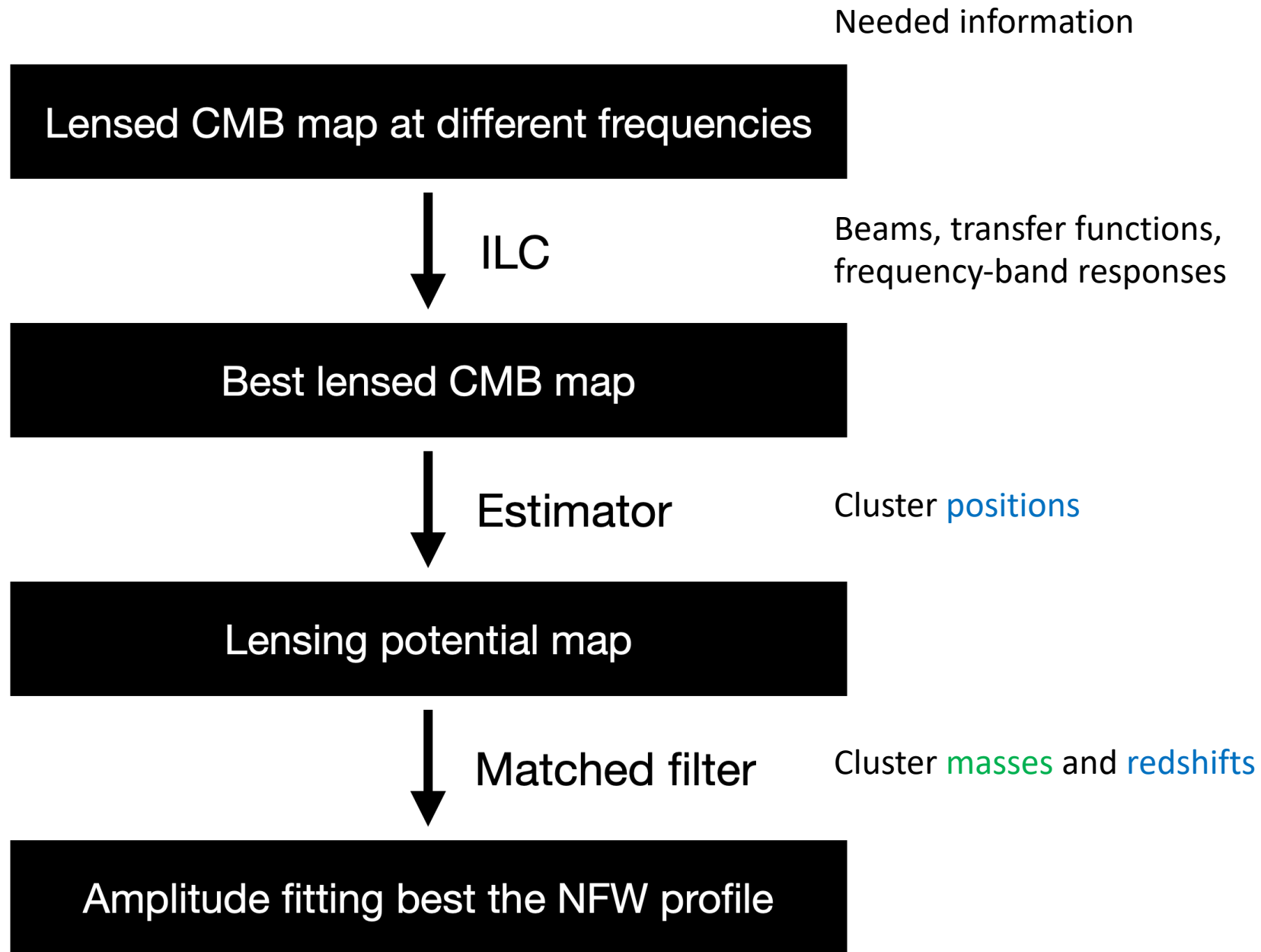
Planck simulation

- 100 GHz map
- No SZ effect
- Lensing



Data analysis

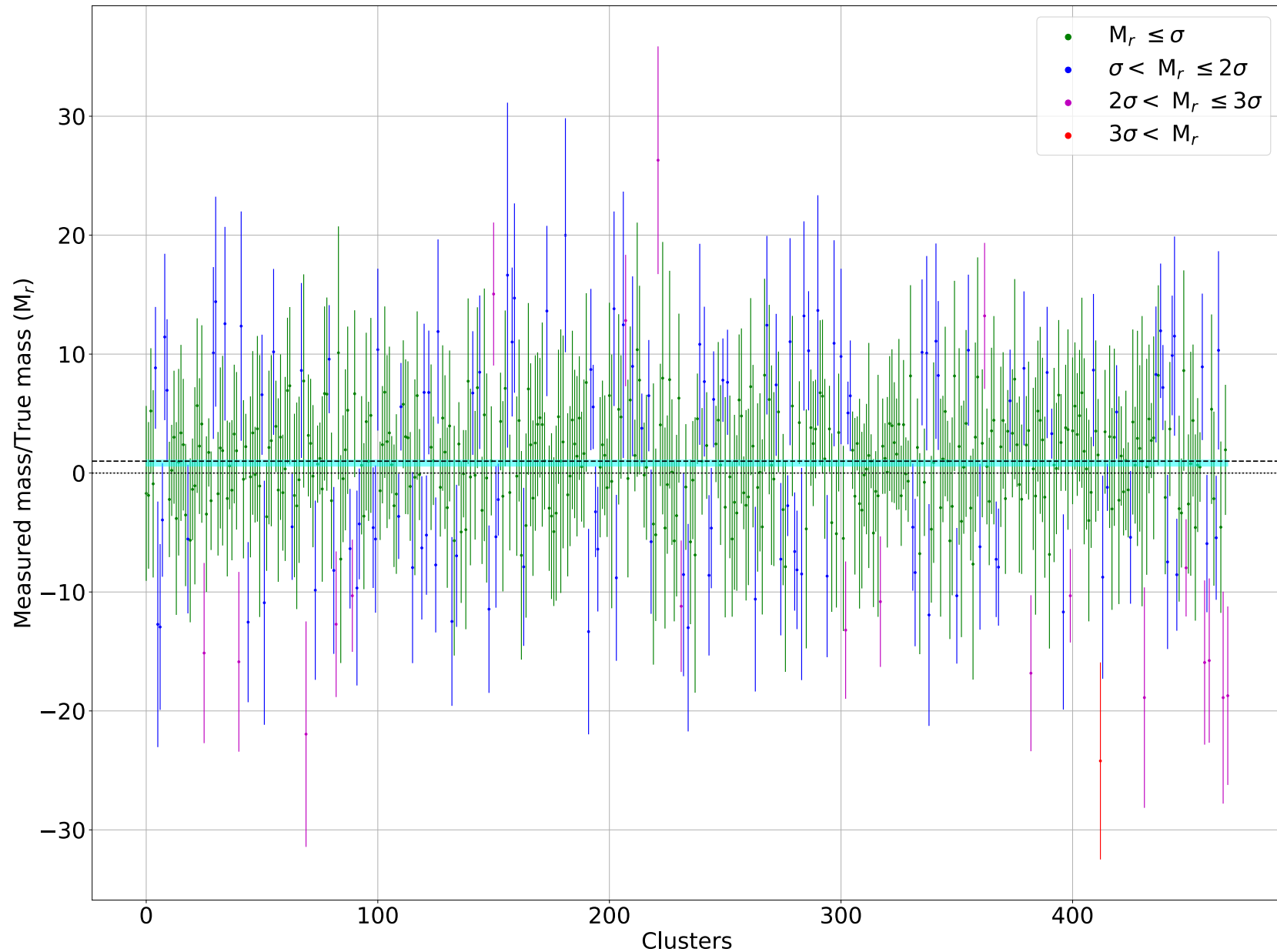
- **Internal Linear Combinations (ILC)**, Remazeilles et al., 2011
- **Lensing estimator**, Hu & Okamoto, 2002
- **Matched filter**, Melin et al., 2015



One Planck simulation

Each point and associated error bar correspond to an **individual cluster mass measurement**, for a total of 468.

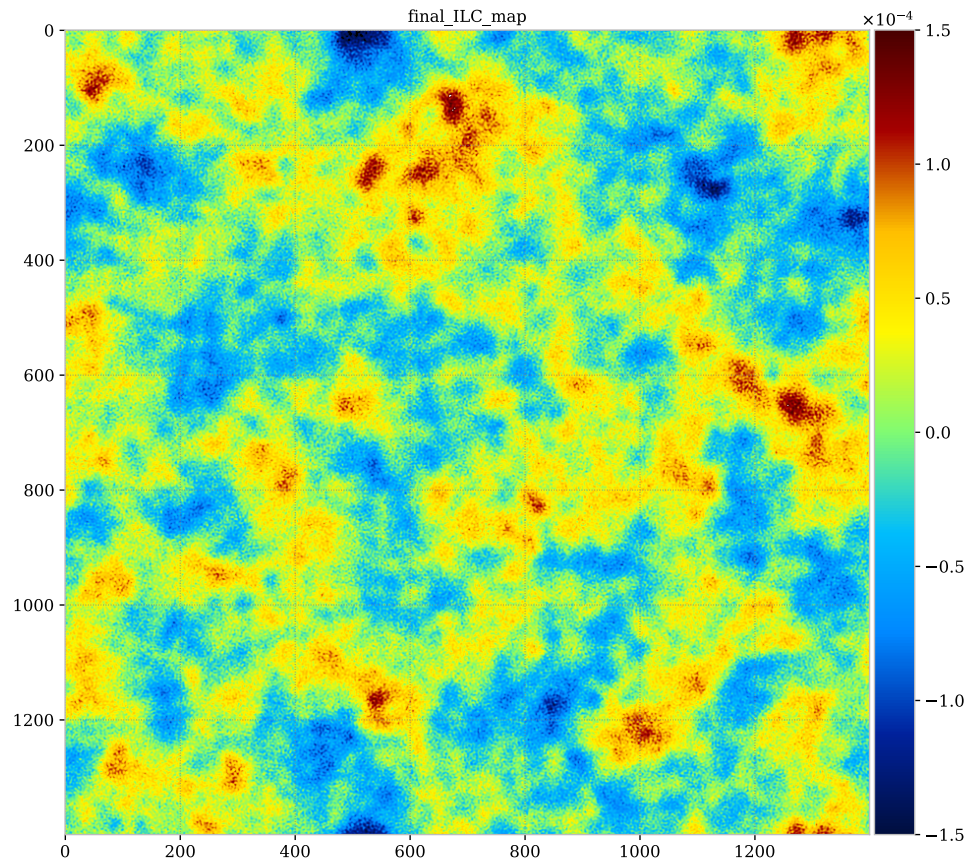
Averaging these measurements provides $\langle M_r \rangle = 0.84 \pm 0.25$, compatible with one



Comparison between Planck and SPT results...

Planck ILC maps: large scales

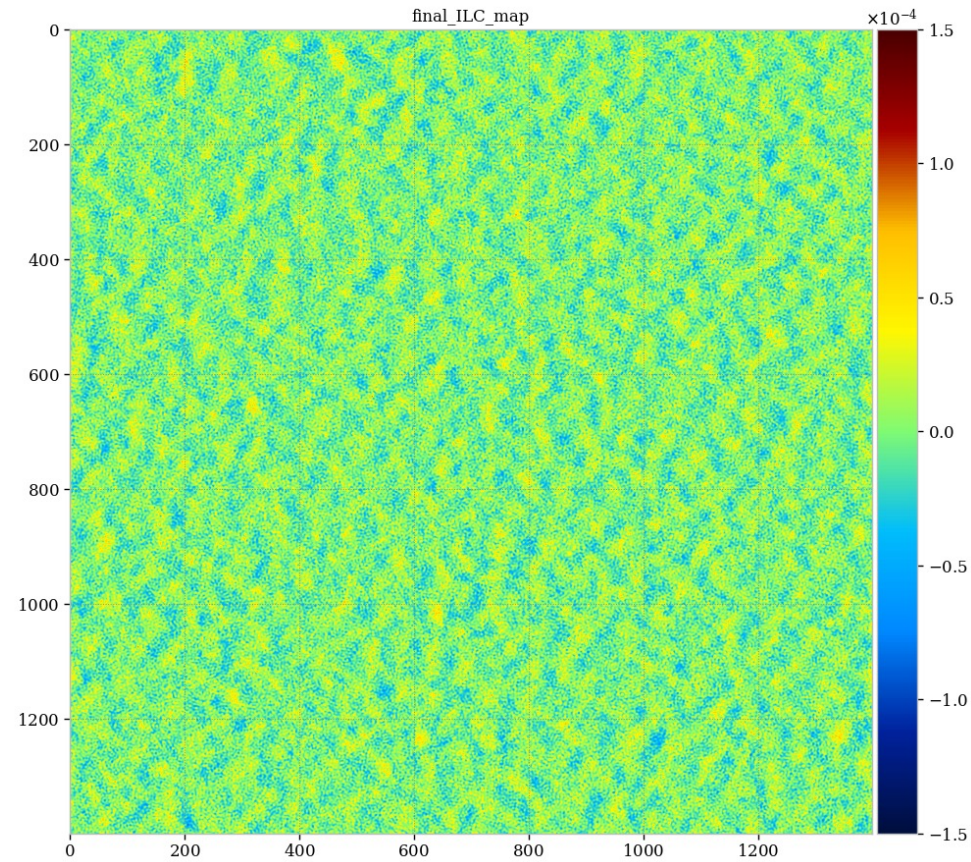
$\langle M_r \rangle = 0.84 \pm 0.25$ (one simulation)



Planck ILC map

SPT ILC maps: small scales

$\langle M_r \rangle = 0.91 \pm 0.22$ (one simulation)



SPT ILC map

Final ILC maps for the same location

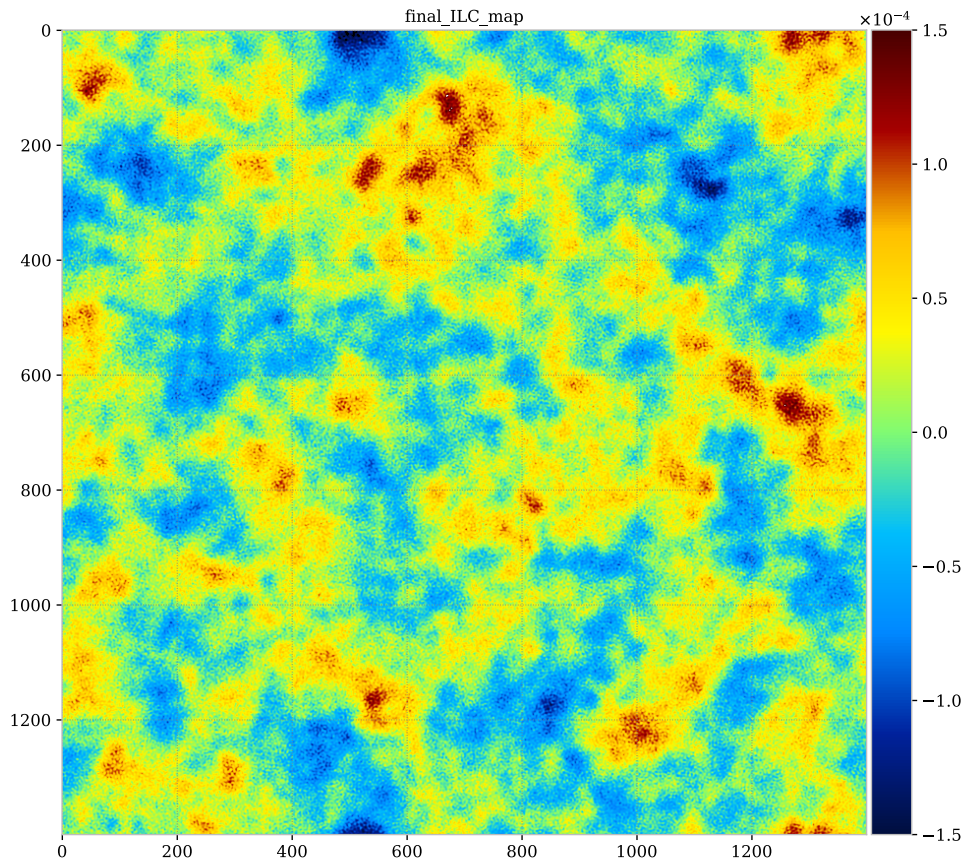
... and the combination of both

Planck: $\langle M_r \rangle = 0.84 \pm 0.25$ (one simulation)

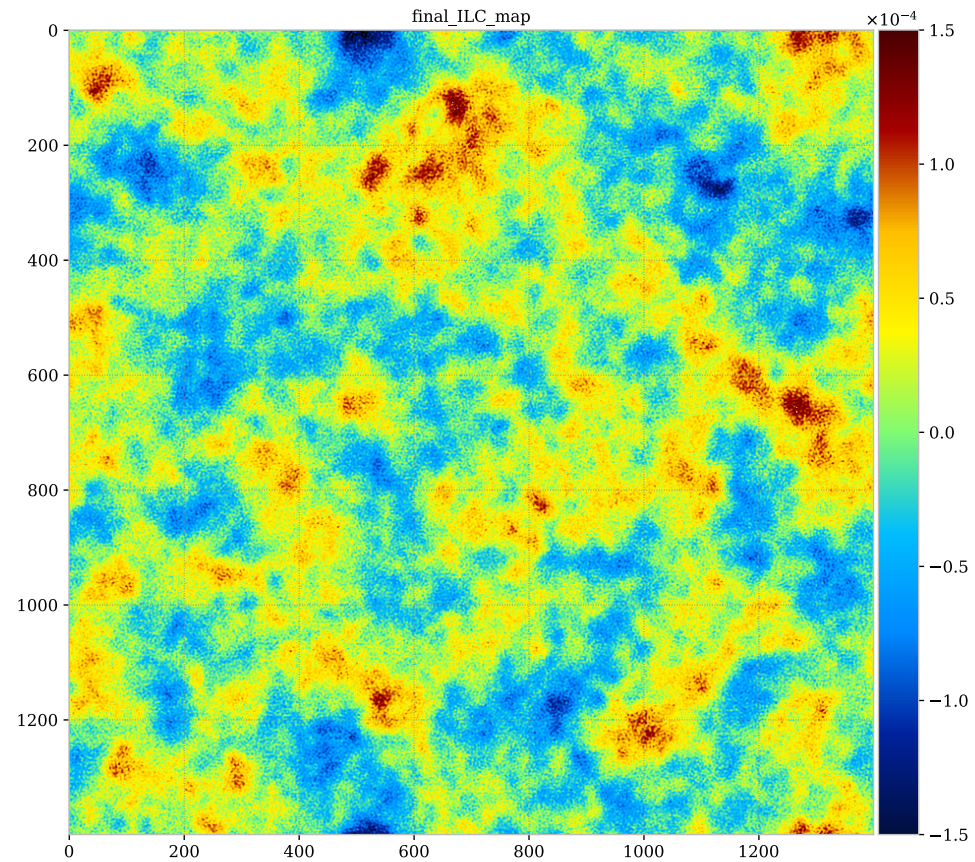
SPT: $\langle M_r \rangle = 0.91 \pm 0.22$

Combination:

$\langle M_r \rangle = 0.88 \pm 0.17$



Planck ILC map



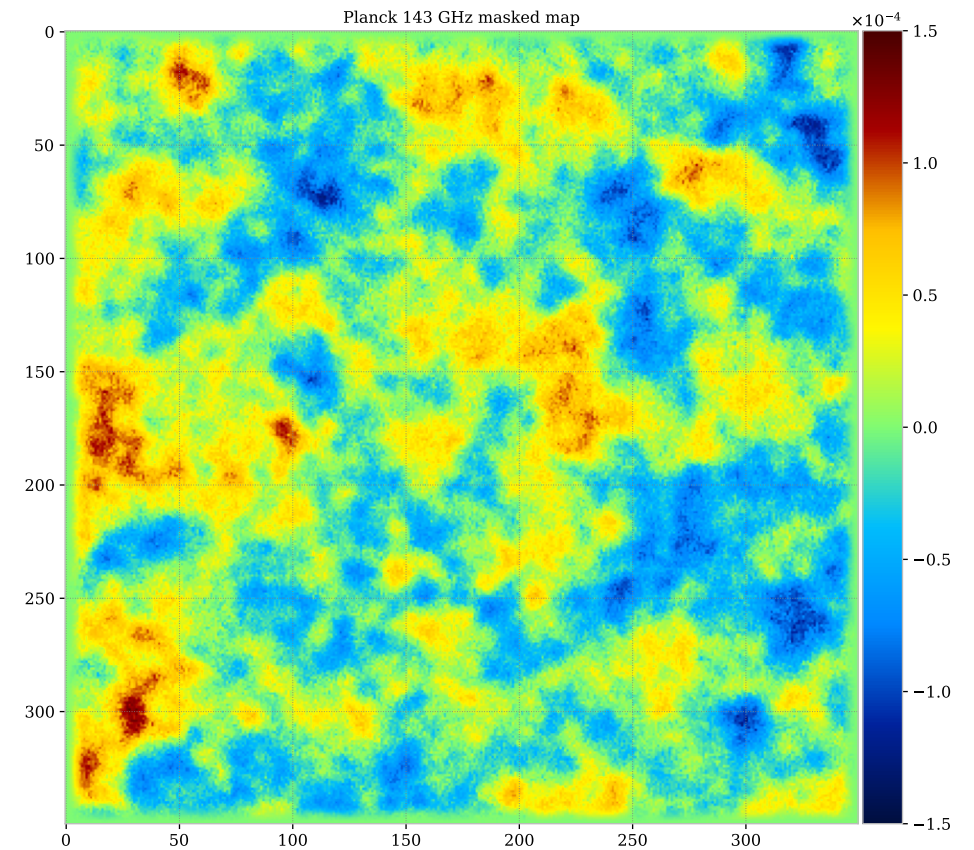
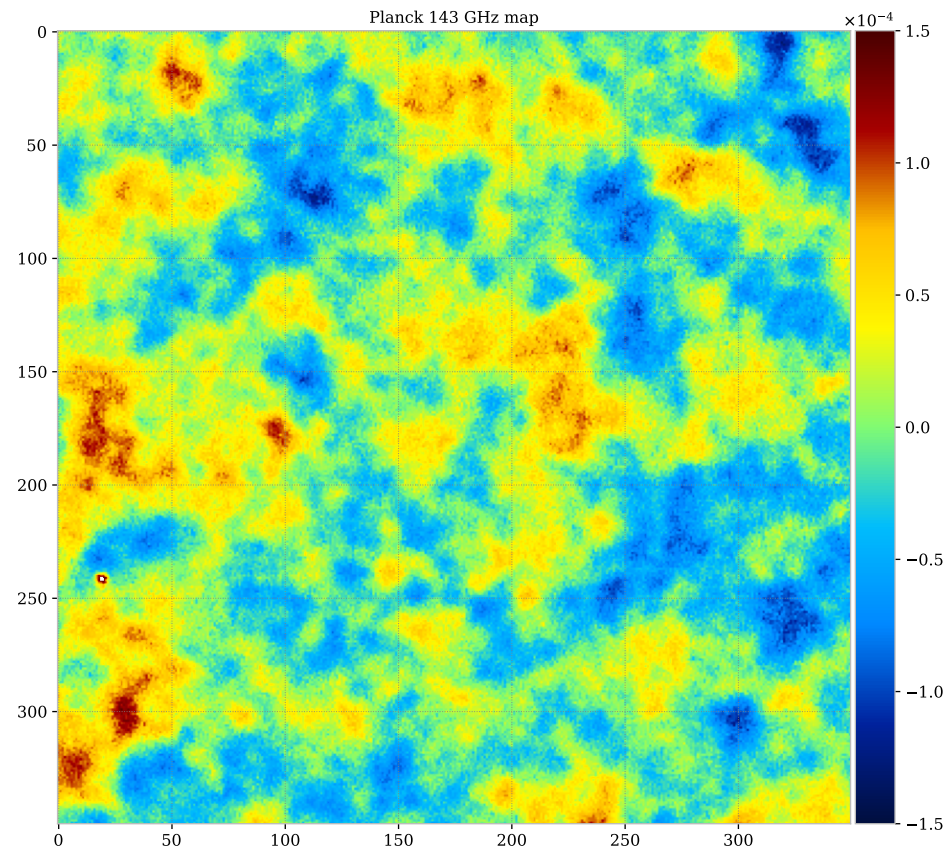
Combi ILC map

Final ILC maps for the same location

Real maps need to be cleaned

Points sources: replaced by gaussian field with CMB properties, continuity with vicinity

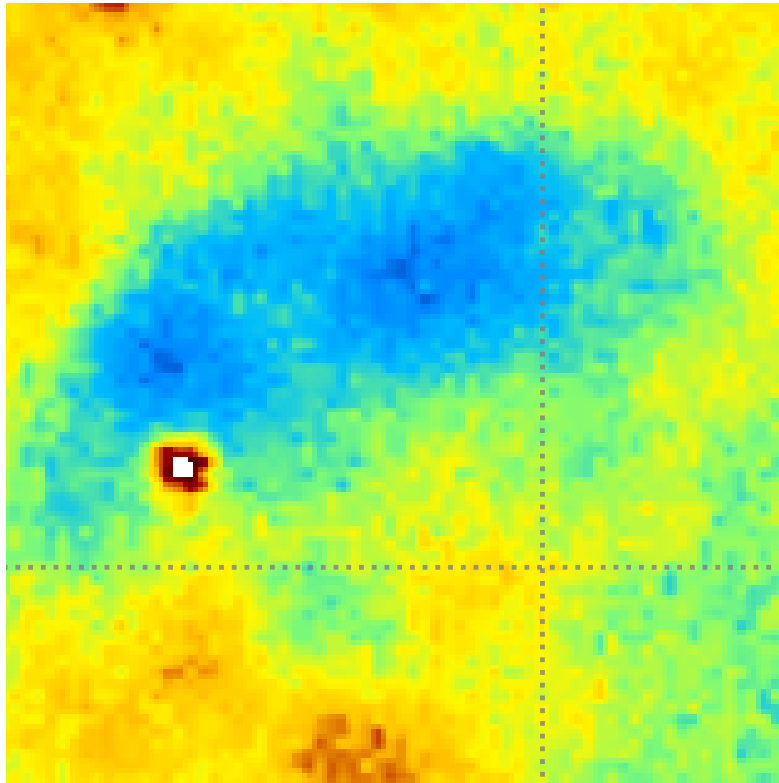
Maps not periodic: apodisation of the maps



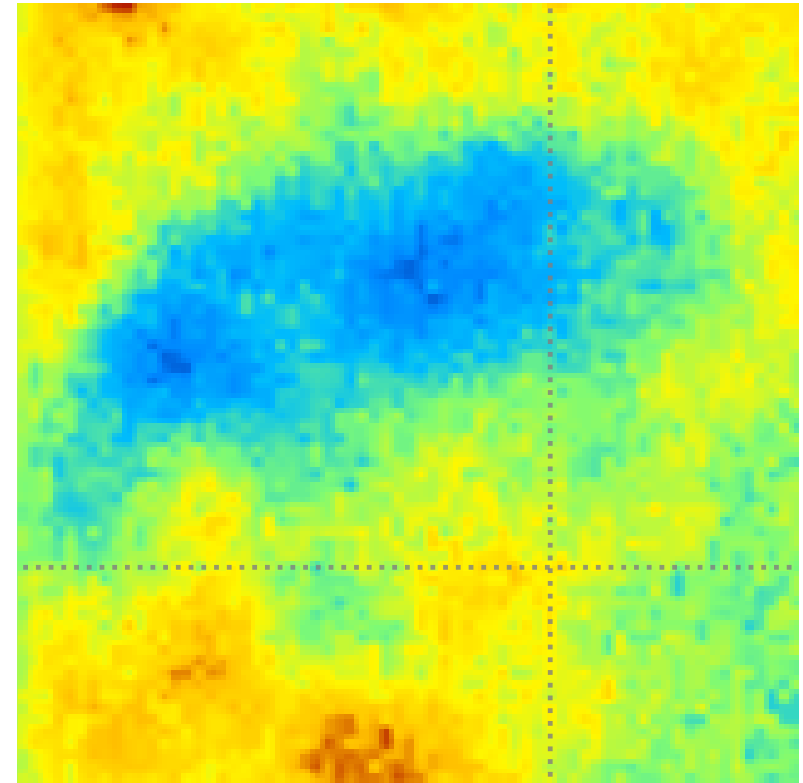
Real maps need to be cleaned

Points sources: replaced by gaussian field with CMB properties, continuity with vicinity

Maps not periodic: apodisation of the maps



Original map (zoom)



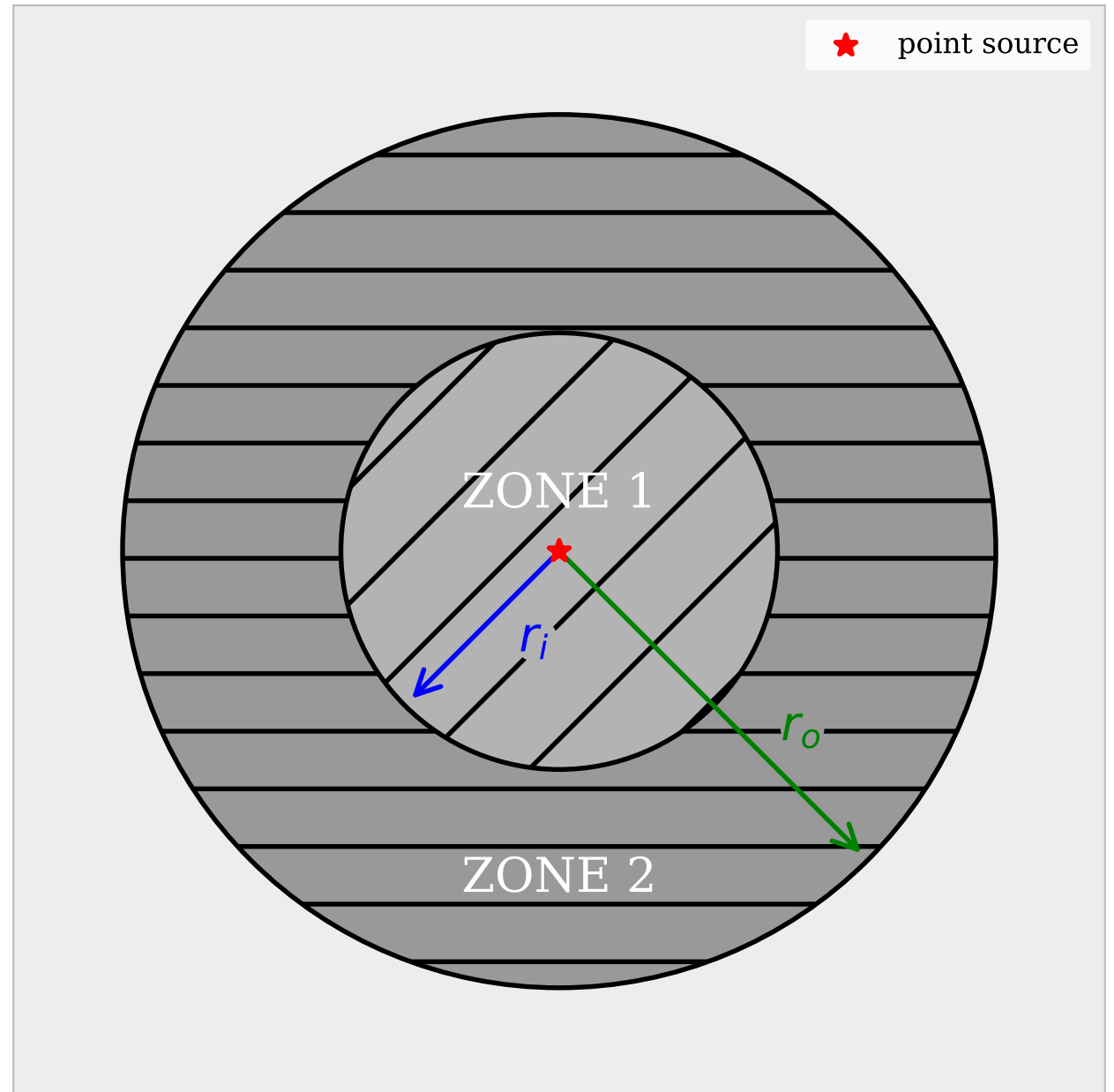
Masked map

Inpainting

To fill ZONE 1 with a realistic CMB compatible with ZONE 2:

- Compute the correlation function / power spectrum of the map
- Create a CMB map with it
- Adapt the new CMB map to ensure continuity

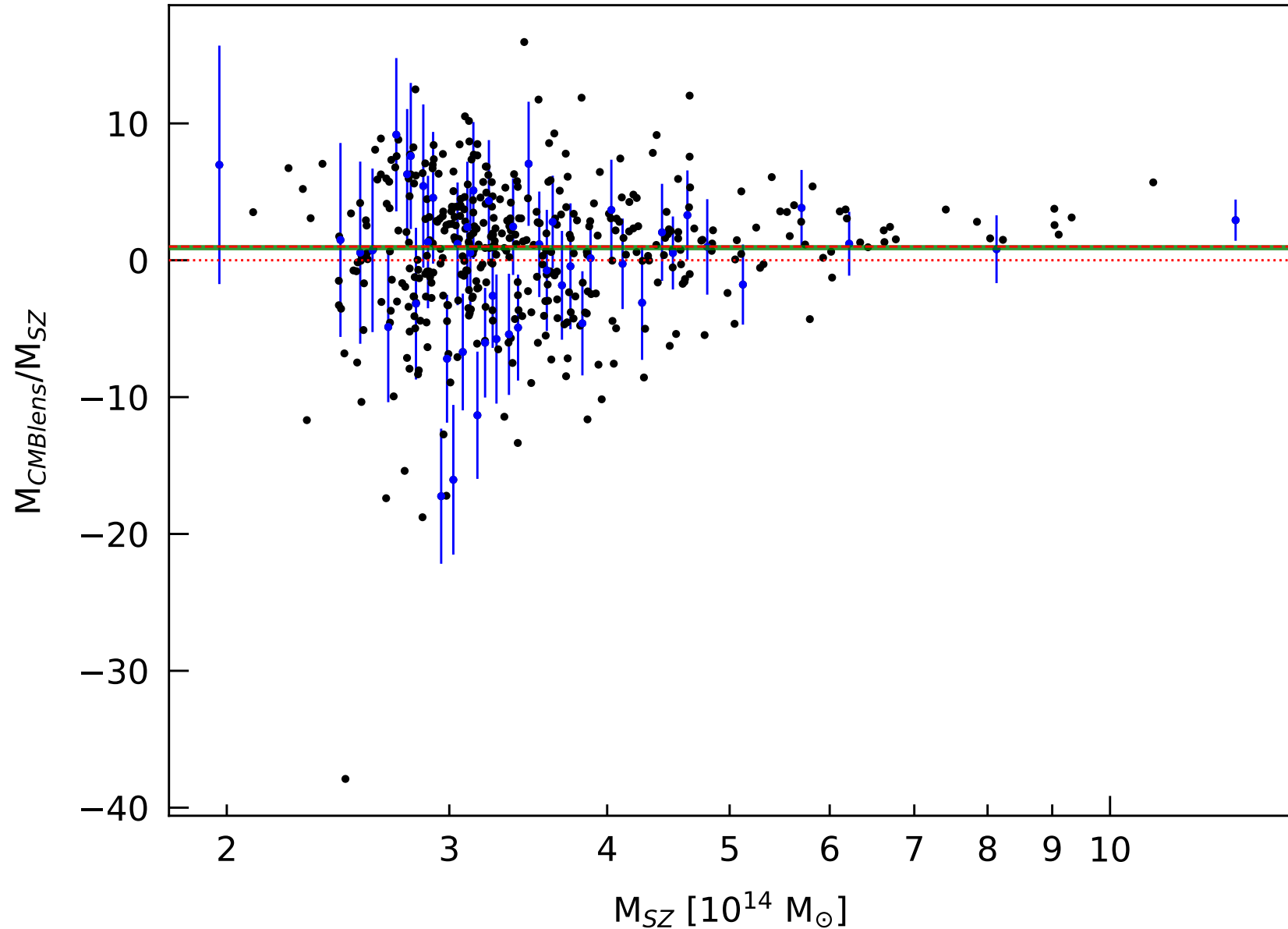
*Hoffman & Ribak 1991,
Benoit-Lévy et al. 2013*



Combined results (real)

- The point sources are masked
- The lensing due to foregrounds is subtracted using “off” measurements

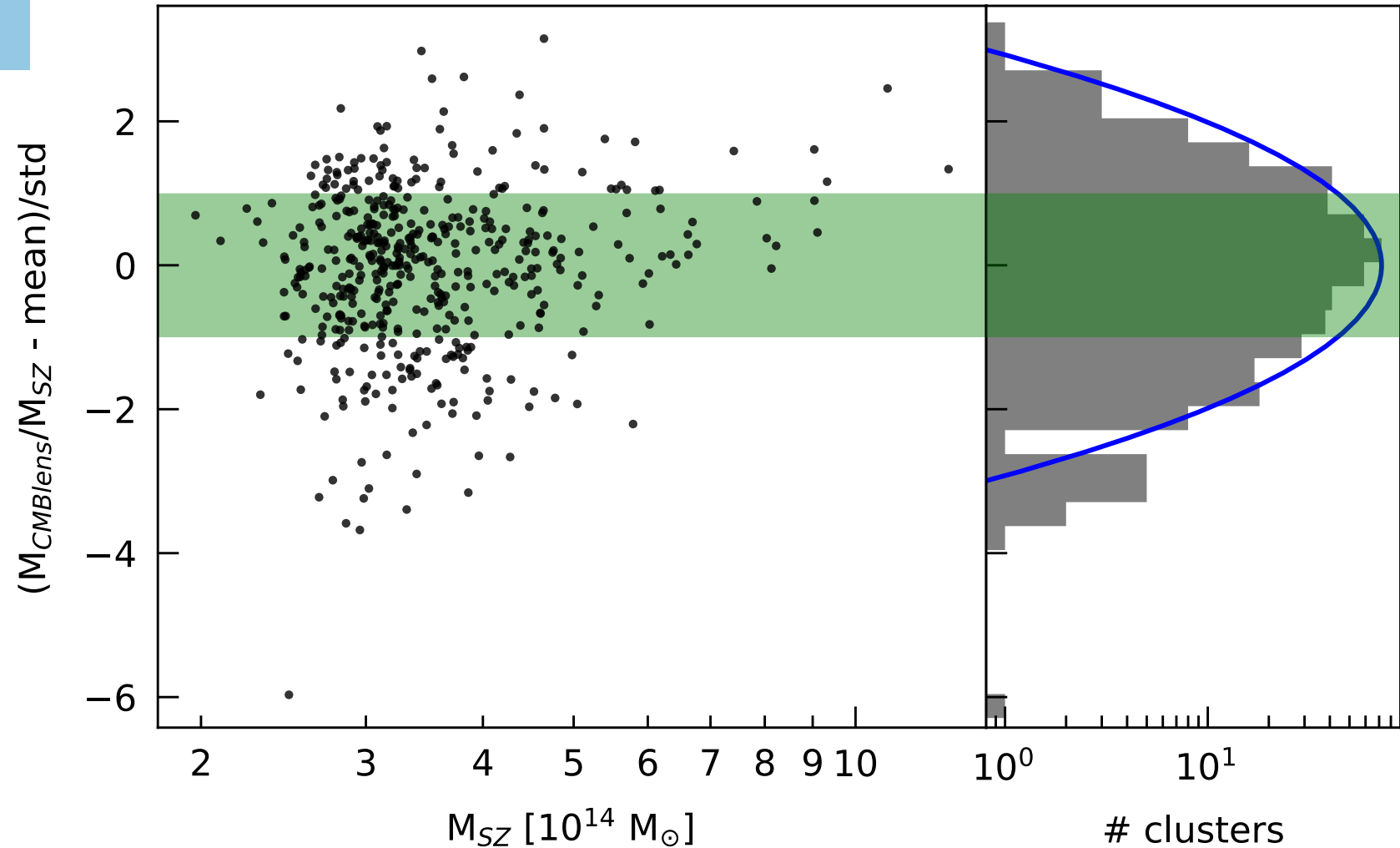
Averaging these measurements provides
 $\langle M_r \rangle = 0.92 \pm 0.19$,
compatible with one



Combined results (real)

- The point sources are masked
- The lensing due to foregrounds is subtracted using “off” measurements

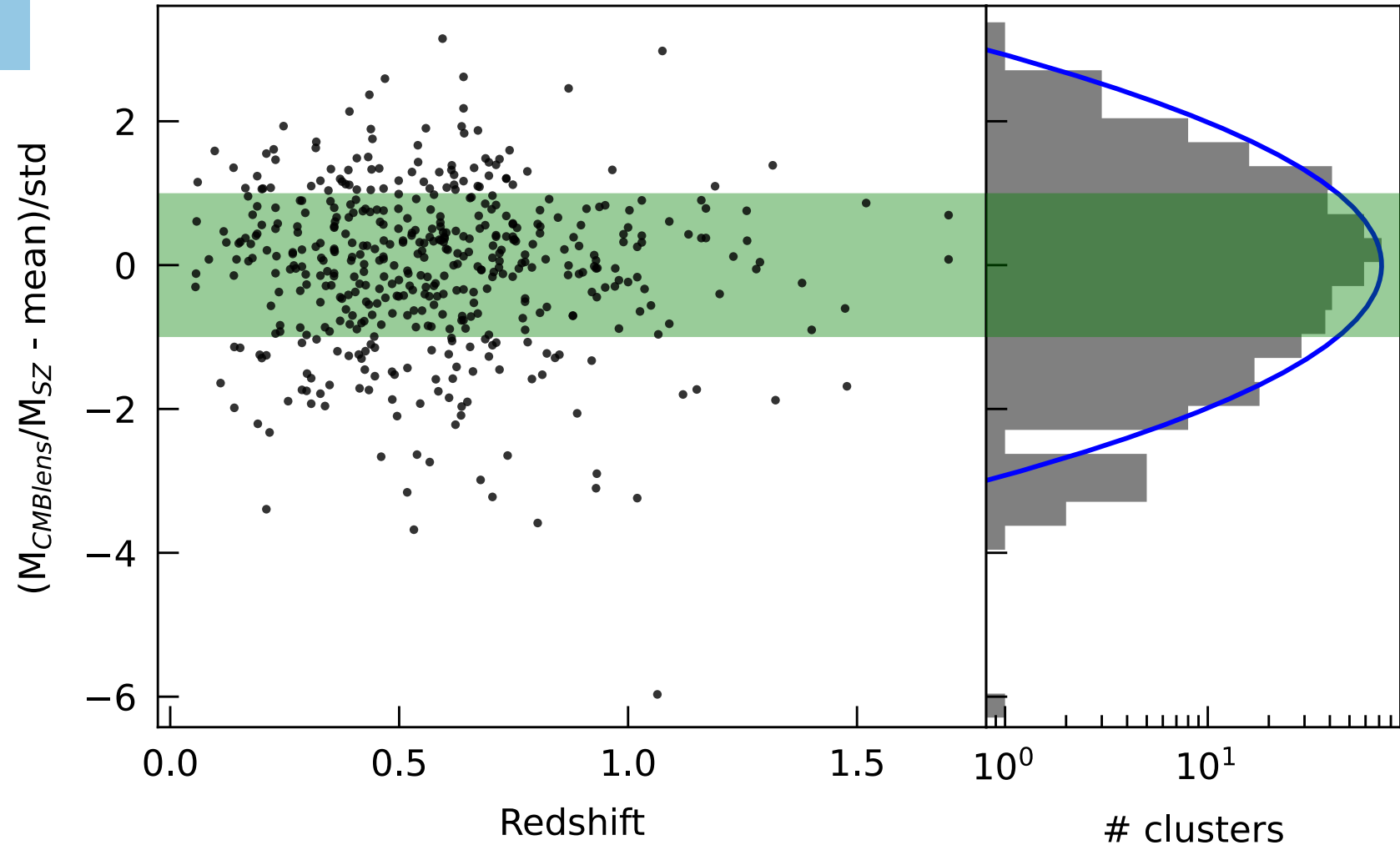
Averaging these measurements provides
 $\langle M_r \rangle = 0.92 \pm 0.19$,
compatible with one



Combined results (real)

- The point sources are masked
- The lensing due to foregrounds is subtracted using “off” measurements

Averaging these measurements provides
 $\langle M_r \rangle = 0.92 \pm 0.19$,
compatible with one

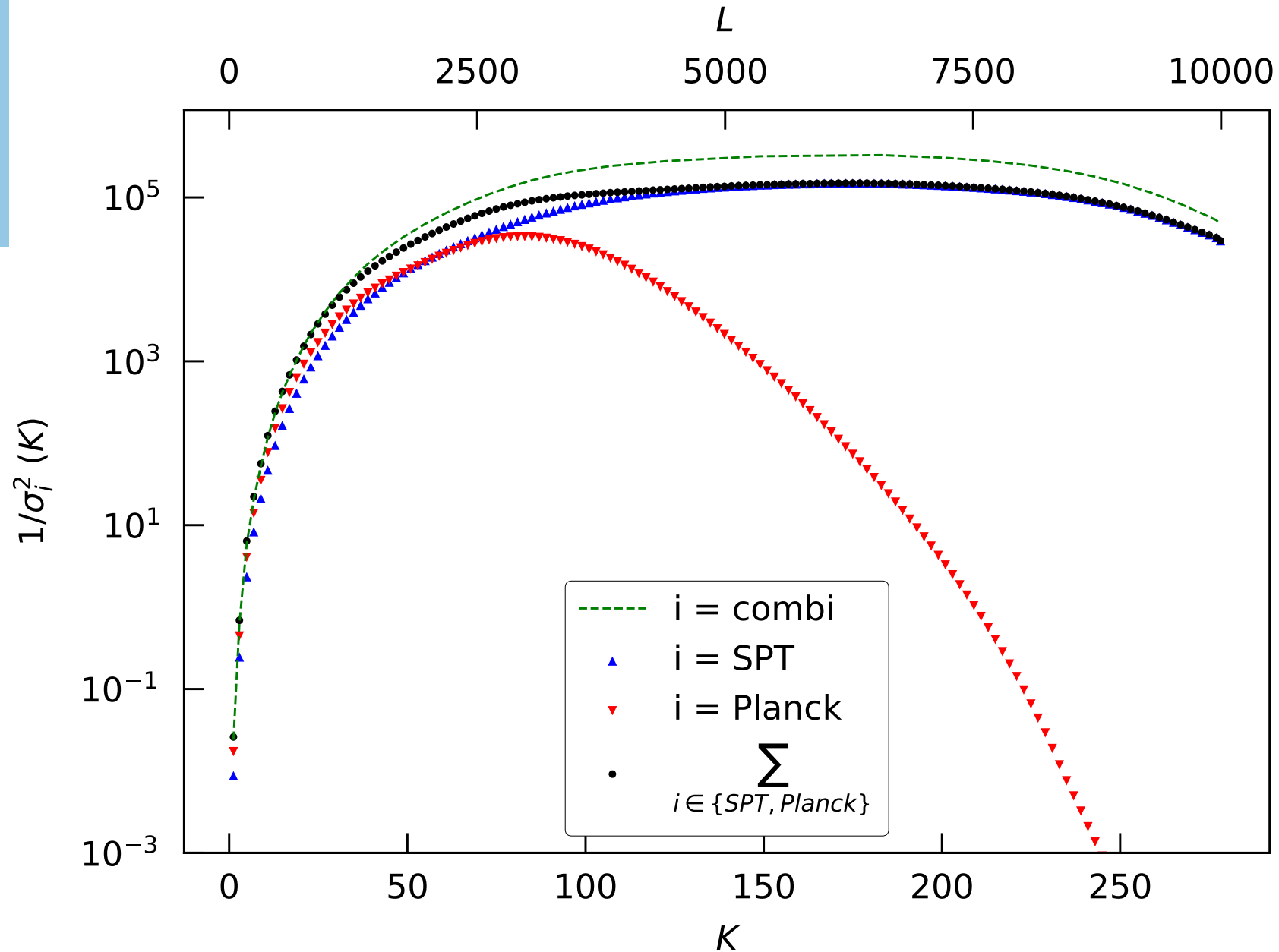


Combined ILC map

- Planck brings most of the information on large scales
- SPT on small scales
- We get a better precision at all scales, not only statistical precision

→ Complementarity

$$\Sigma = \frac{1}{\sigma_{planck}^2} + \frac{1}{\sigma_{SPT}^2} =? \frac{1}{\sigma_{combi}^2}$$

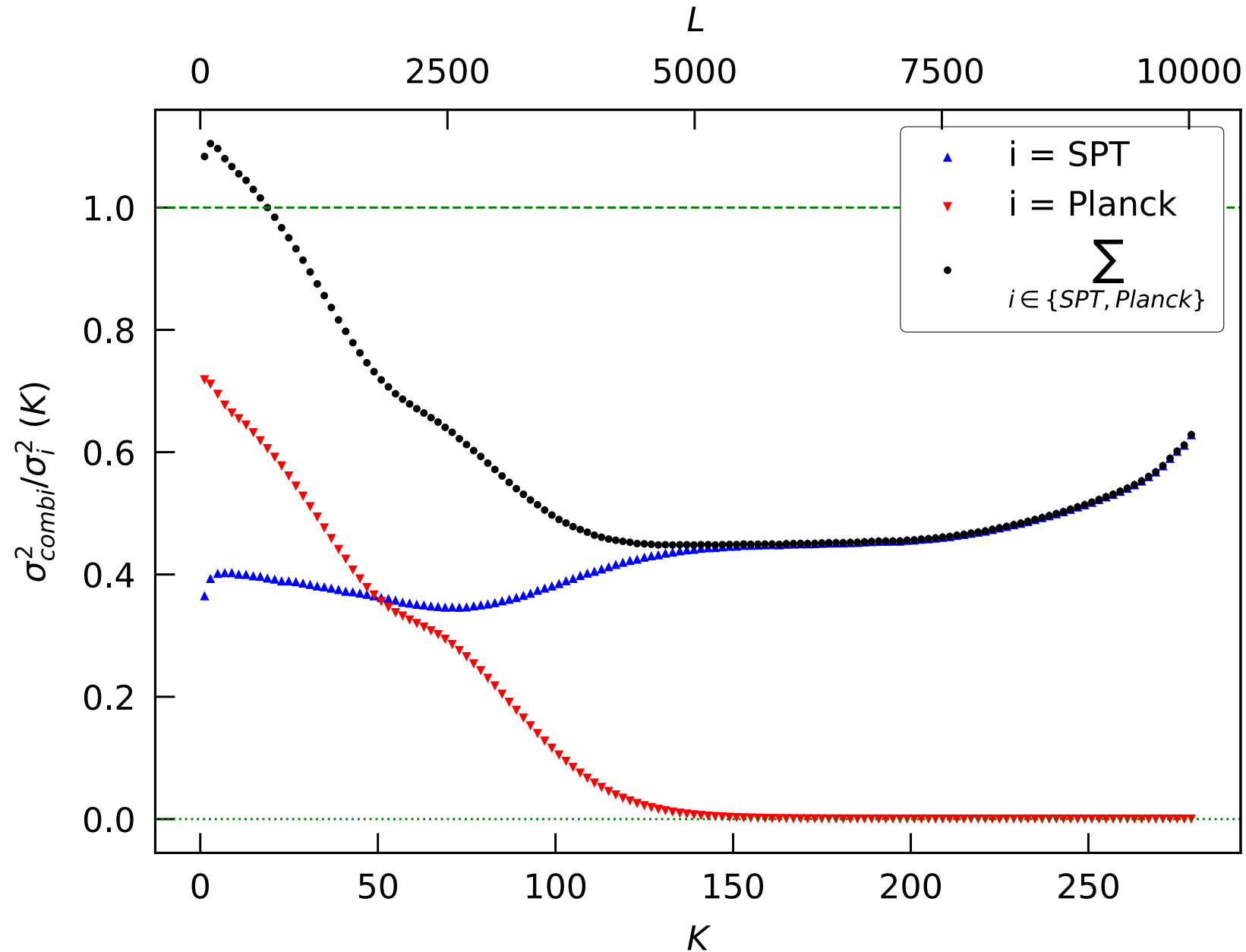


Combined ILC map

- Planck brings most of the information on large scales
- SPT on small scales
- We get a better precision at all scales, not only statistical precision

→ Complementarity

$$\Sigma = \frac{\sigma_{combi}^2}{\sigma_{planck}^2} + \frac{\sigma_{combi}^2}{\sigma_{SPT}^2} =? \frac{\sigma_{combi}^2}{\sigma_{combi}^2}$$



Systematic effects

- The baseline analysis uses a profile up to $5 \times r_{500}$
- The main uncertainty is the assumption on the matter profile

$\langle M_r \rangle = 0.92 \pm 0.19$ (stat.)

Uncertainty	$\Delta \frac{M_{\text{CMB lens}}}{M_{\text{SZ}}}$
Profile up to $3 \times r_{500}$	+0.017
Profile up to $7 \times r_{500}$	-0.019
Miscentering	-0.009
Error on z	± 0.001
Error on M_{500}	± 0.007
Total	± 0.022
No relativistic SZ	-0.012

Summary

- **First** CMB-lensing galaxy cluster mass measurement using a **combination** of **ground** and **space**-based surveys
- Analysis tested on simulations and applied to actual SPT-SZ and Planck data
- We measure the signal at **4.8 sigma** on real data, a significant gain with respect to measurements performed on the two individual datasets
- Small increasing trend from $M_{\text{CMB lens}}$ with respect to M_{SZ} still to be understood
- **Correlations** between the scales observed by SPT-SZ and the scales observed by Planck **improve** the constraints on the lensing potential
- Planck data will remain a key element in CMB-lensing cluster studies for decades to come

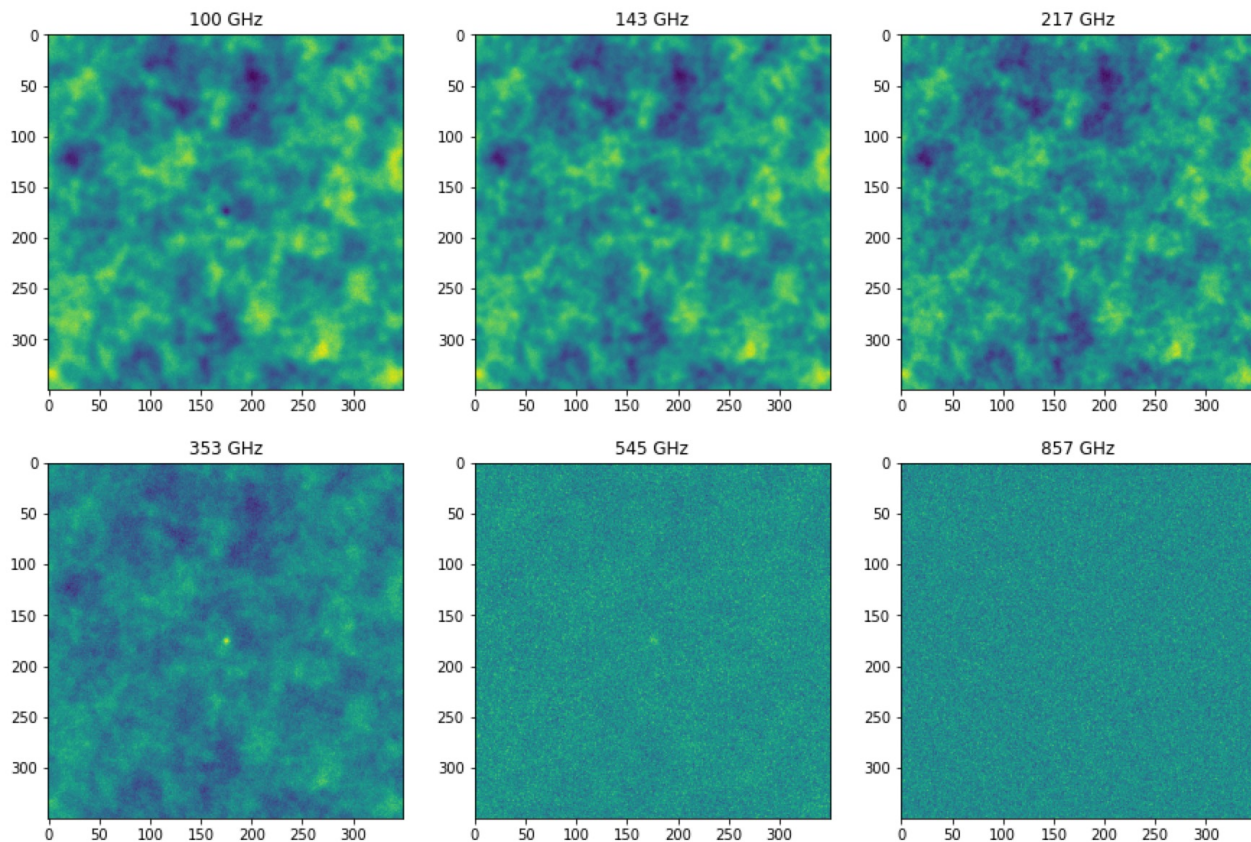
Backup slides

Internal Linear Combinations

- **Contaminants:** SZ effect, foreground
- **Instrumental characteristics:** PSF, noise

Combine the maps at different frequencies to remove contaminants, easier when we know the recipe

→ **Best lensed CMB map**



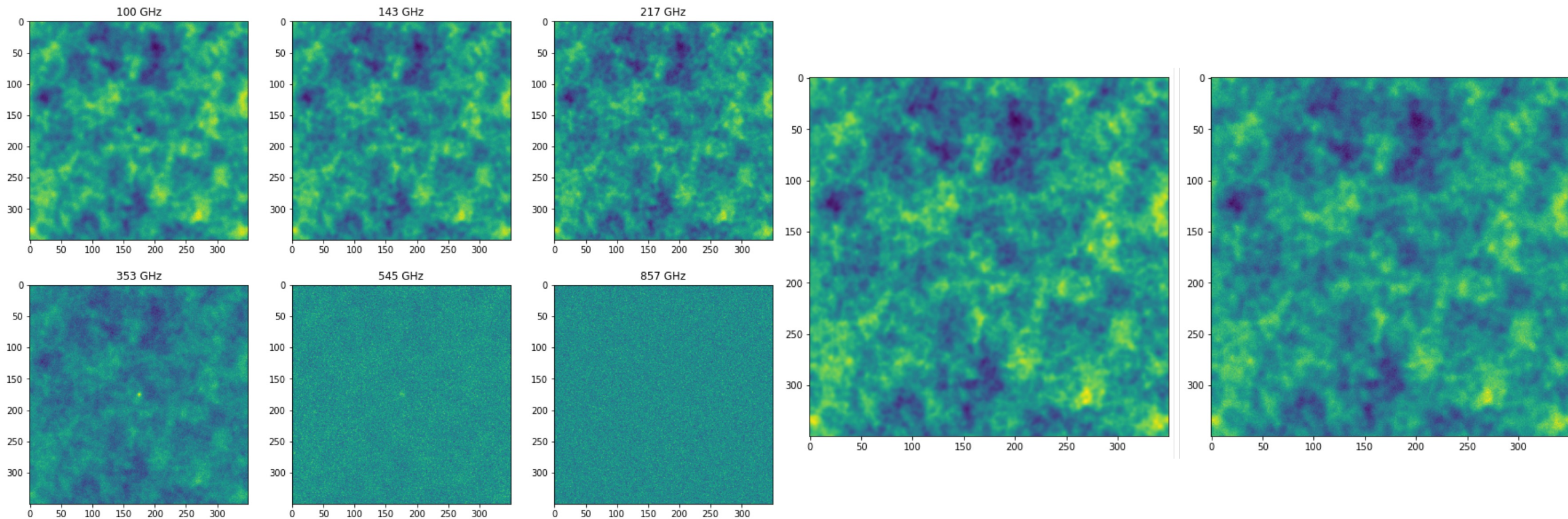
$$\begin{cases} m_{\nu_0}(\mathbf{k}) = \alpha_{\nu_0} s(\mathbf{k}) + \beta_{\nu_0} y_{\nu_0}(\mathbf{k}) + n_{\nu_0}(\mathbf{k}) \\ m_{\nu_1}(\mathbf{k}) = \alpha_{\nu_1} s(\mathbf{k}) + \beta_{\nu_1} y_{\nu_1}(\mathbf{k}) + n_{\nu_1}(\mathbf{k}) \\ \dots \\ m_{\nu_5}(\mathbf{k}) = \alpha_{\nu_5} s(\mathbf{k}) + \beta_{\nu_5} y_{\nu_5}(\mathbf{k}) + n_{\nu_5}(\mathbf{k}) \end{cases}$$

Internal Linear Combinations

- **Contaminants:** SZ effect, foreground
- **Instrumental characteristics:** PSF, noise

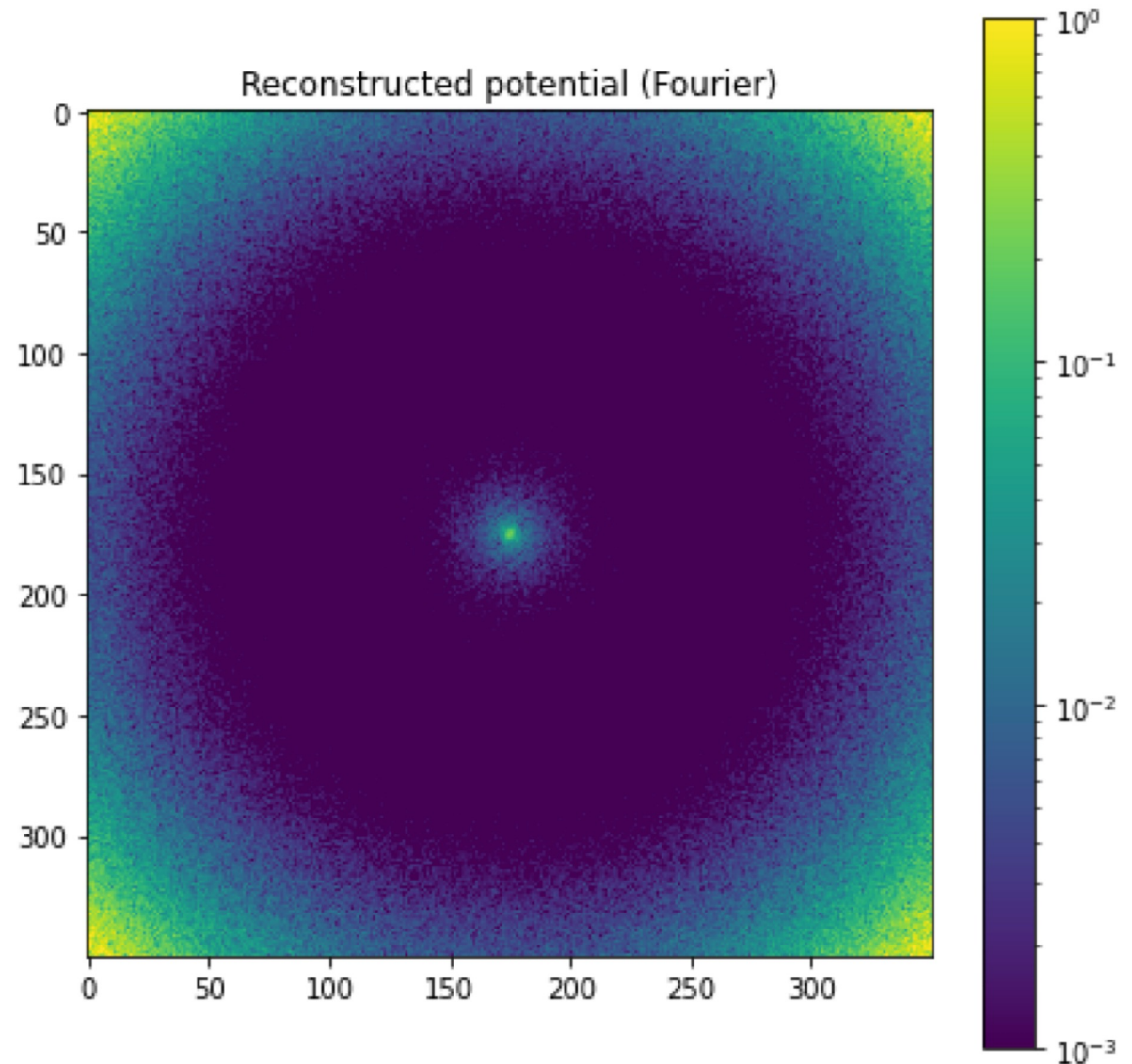
Combine the maps at different frequencies to remove contaminants, easier when we know the recipe

→ **Best lensed CMB map**



Lensing estimator

- The CMB k-modes (spatial frequencies, i.e. the different scales) are uncorrelated
- The CMB on our map is lensed, **inducing spatial correlations**
- Use these correlations to rebuild the lensing potential



2D-Fourier transform of the reconstructed gravitational potential (small k-modes – large scales in the middle)

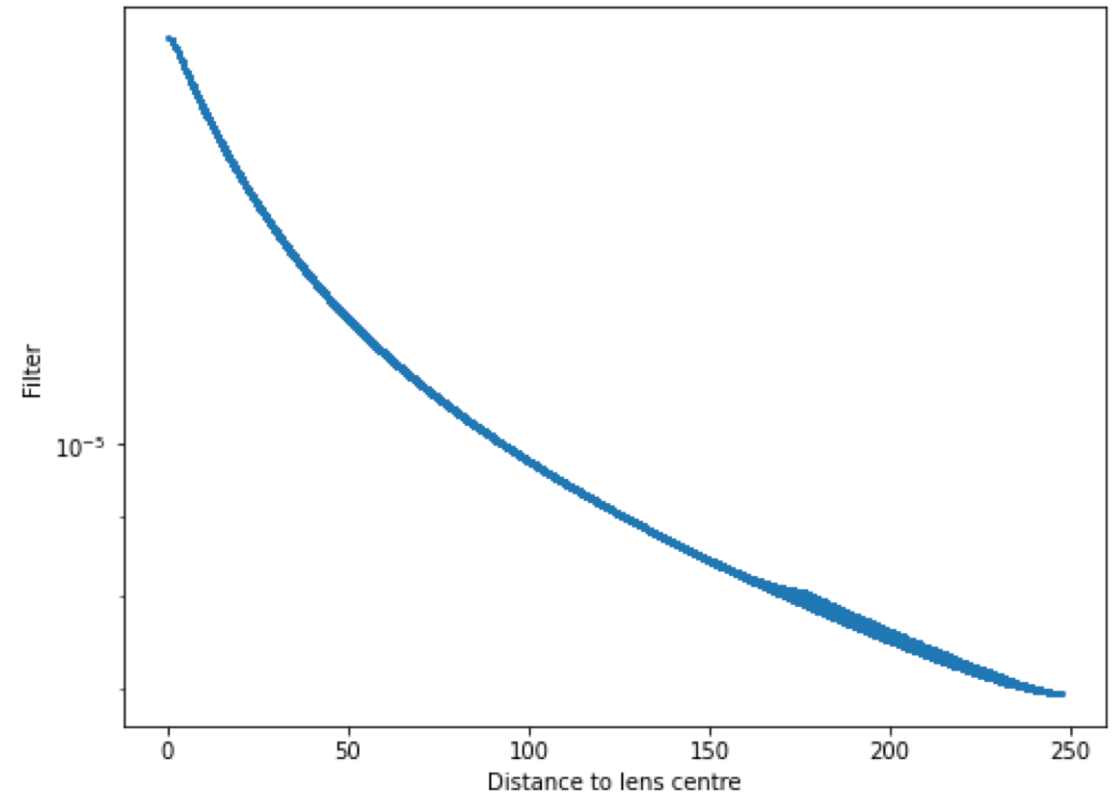
Matched filter

- Compares the obtained lensing potential to a NFW profile for a given mass
- We know the NFW profile used in the simulations
- Returns the estimation of the amplitude fitting best the NFW profile. For simulations, we expect to get, in average:

$$\frac{M_{\text{measurement}}}{M_{\text{true}}} = 1$$

$$\hat{\phi}_0 = \left[\sum_{\mathbf{K}} \frac{|\Phi(\mathbf{K})|^2}{A(\mathbf{K})} \right]^{-1} \sum_{\mathbf{K}} \frac{\Phi^*(\mathbf{K})}{A(\mathbf{K})} \hat{\phi}(\mathbf{K})$$

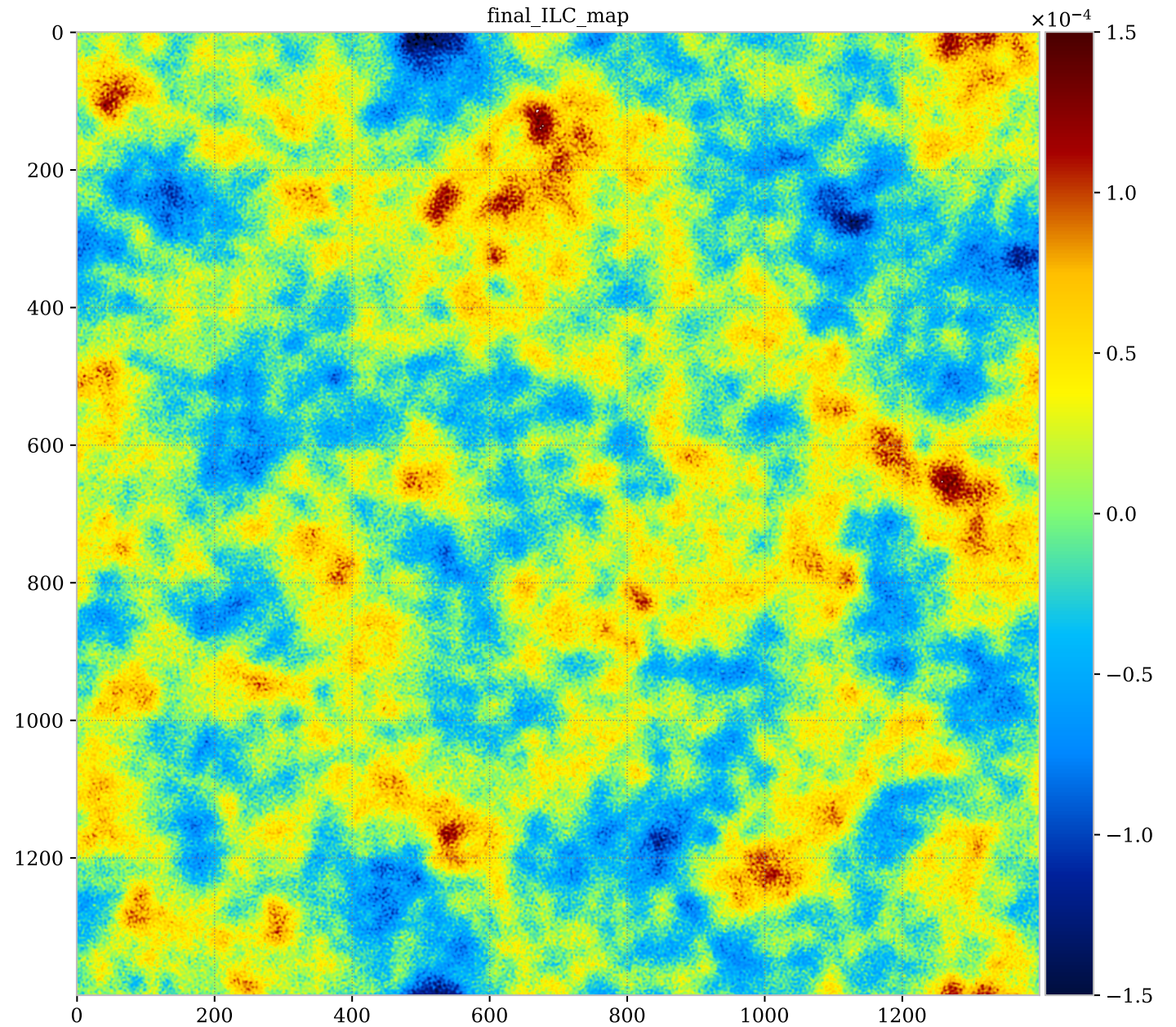
NFW lensing potential
Variance of measure obtained for \mathbf{K}
Obtained lensing potential



Filter NFW lensing profile

Planck ILC map

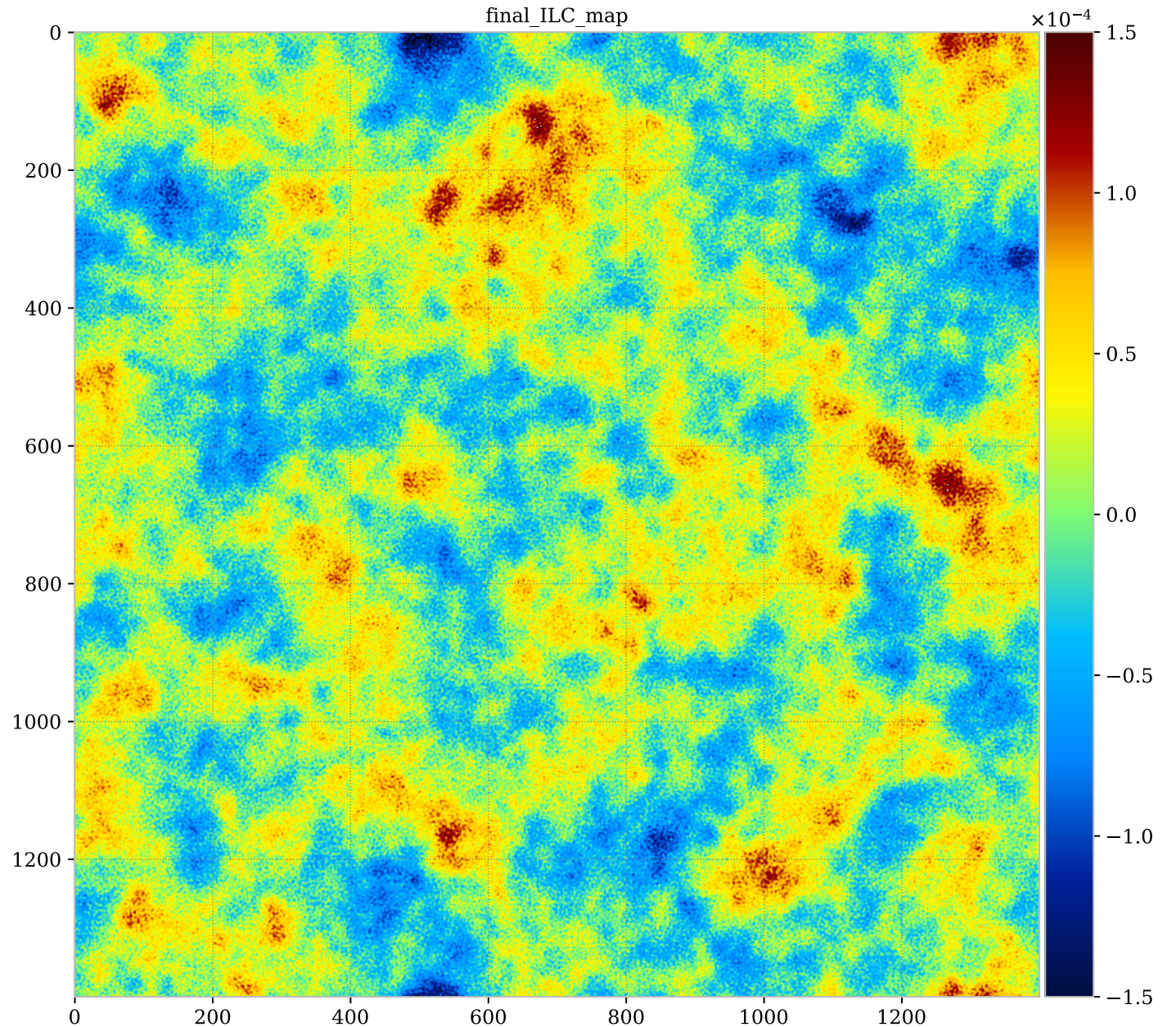
- For one simulated cluster
- No foreground simulated
- The map is periodic



Combined ILC map

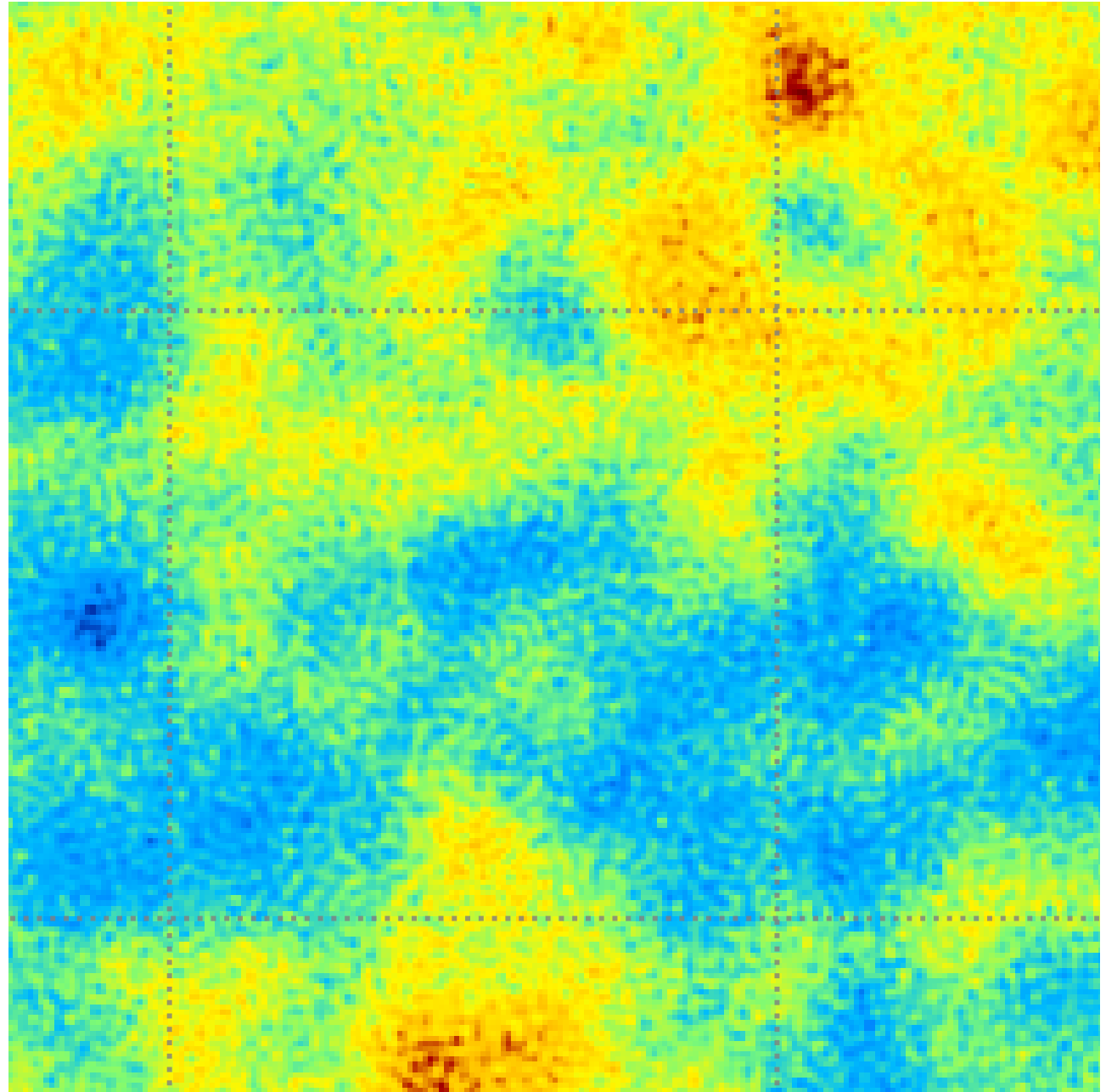
- Better small scales than Planck only
- The surveys really are complementary

$$\bullet \frac{1}{\sigma_{combi}^2} = \frac{1}{\sigma_{planck}^2} + \frac{1}{\sigma_{SPT}^2}$$



Planck ILC map

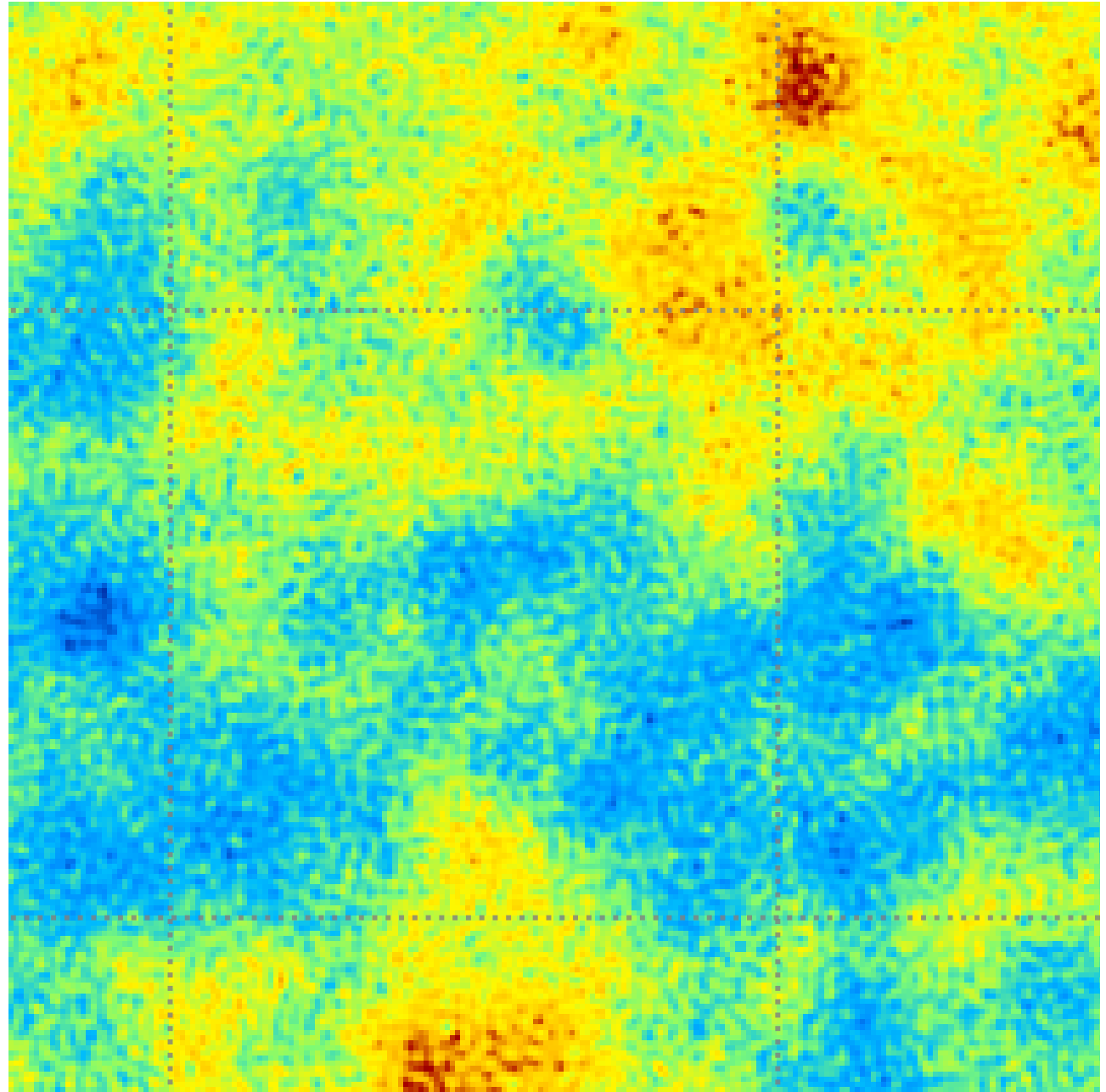
- For one simulated cluster
- No foreground simulated
- The map is periodic



Combined ILC map

- Better small scales than Planck only
- The surveys really are complementary

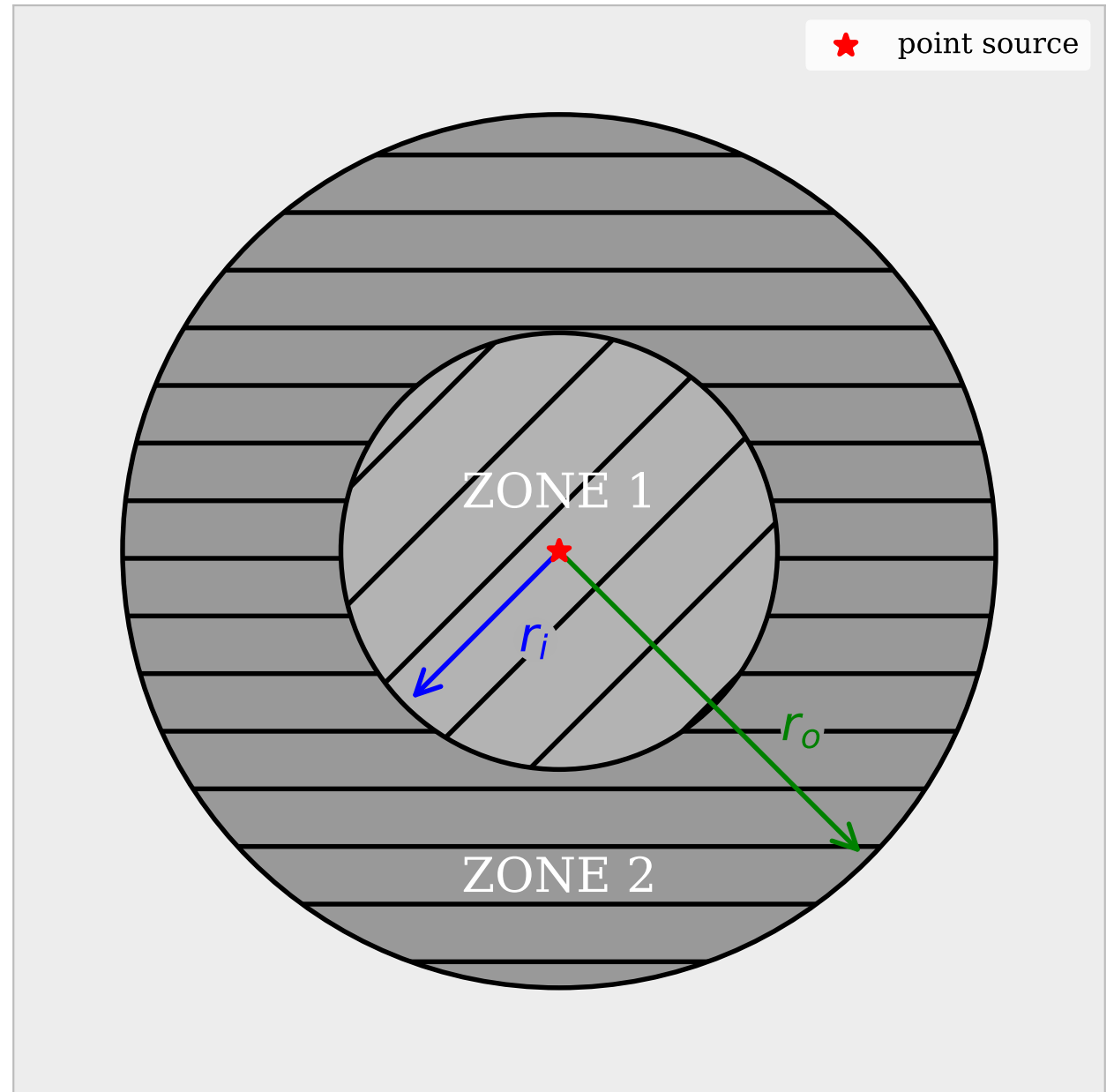
$$\bullet \frac{1}{\sigma_{combi}^2} = \frac{1}{\sigma_{planck}^2} + \frac{1}{\sigma_{SPT}^2}$$



Inpainting

To fill ZONE 1 with a realistic CMB compatible with ZONE 2:

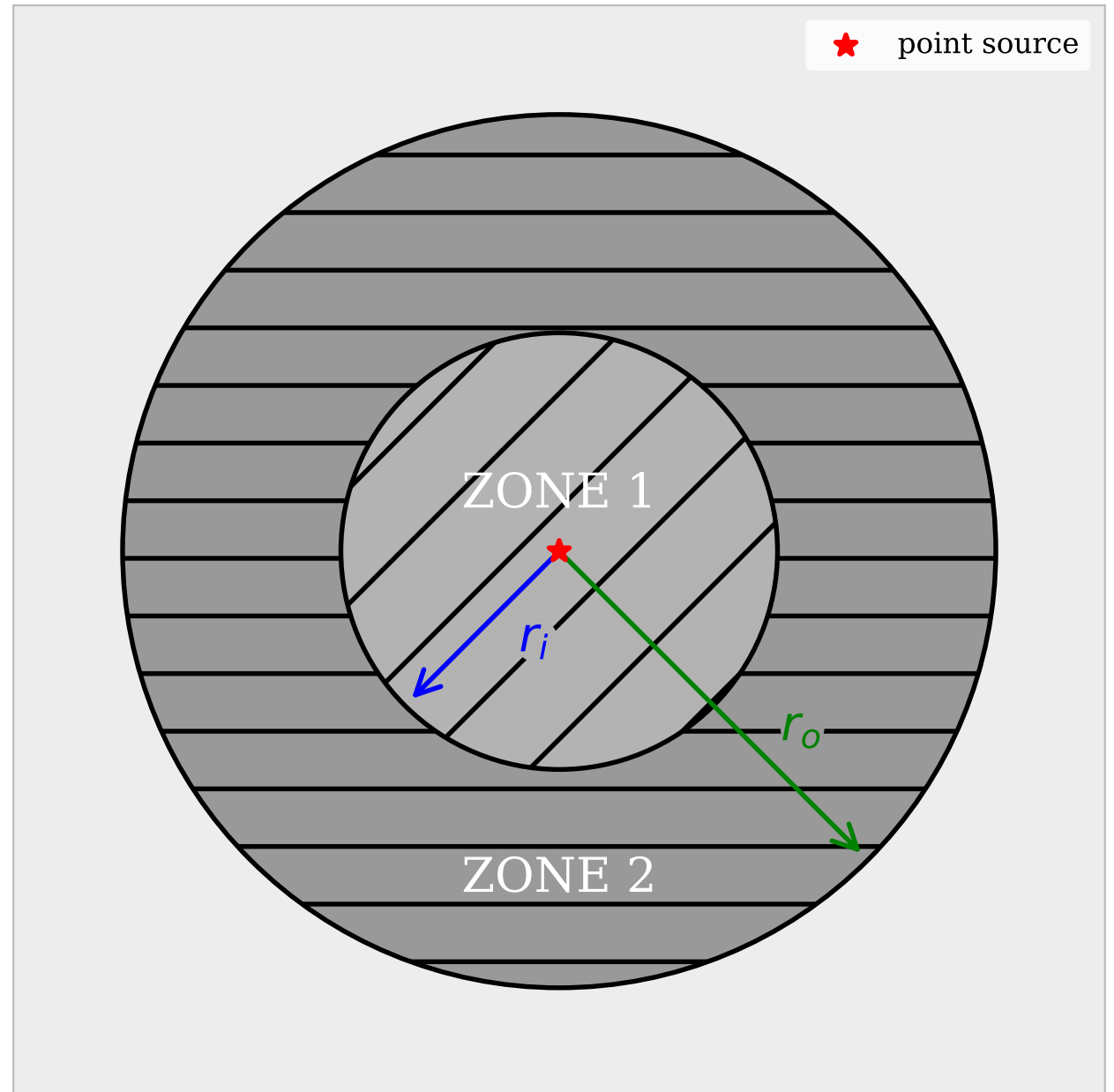
- Compute the correlation function / power spectrum of the map
- Create a CMB map with it
- Adapt the new CMB map to ensure continuity



Inpainting

- We want to fill ZONE 1 with a realistic CMB, compatible with ZONE 2
- We compute the correlation function / power spectrum of the map
- We create a CMB map with it

→ We now have to adapt the new CMB map to ensure continuity

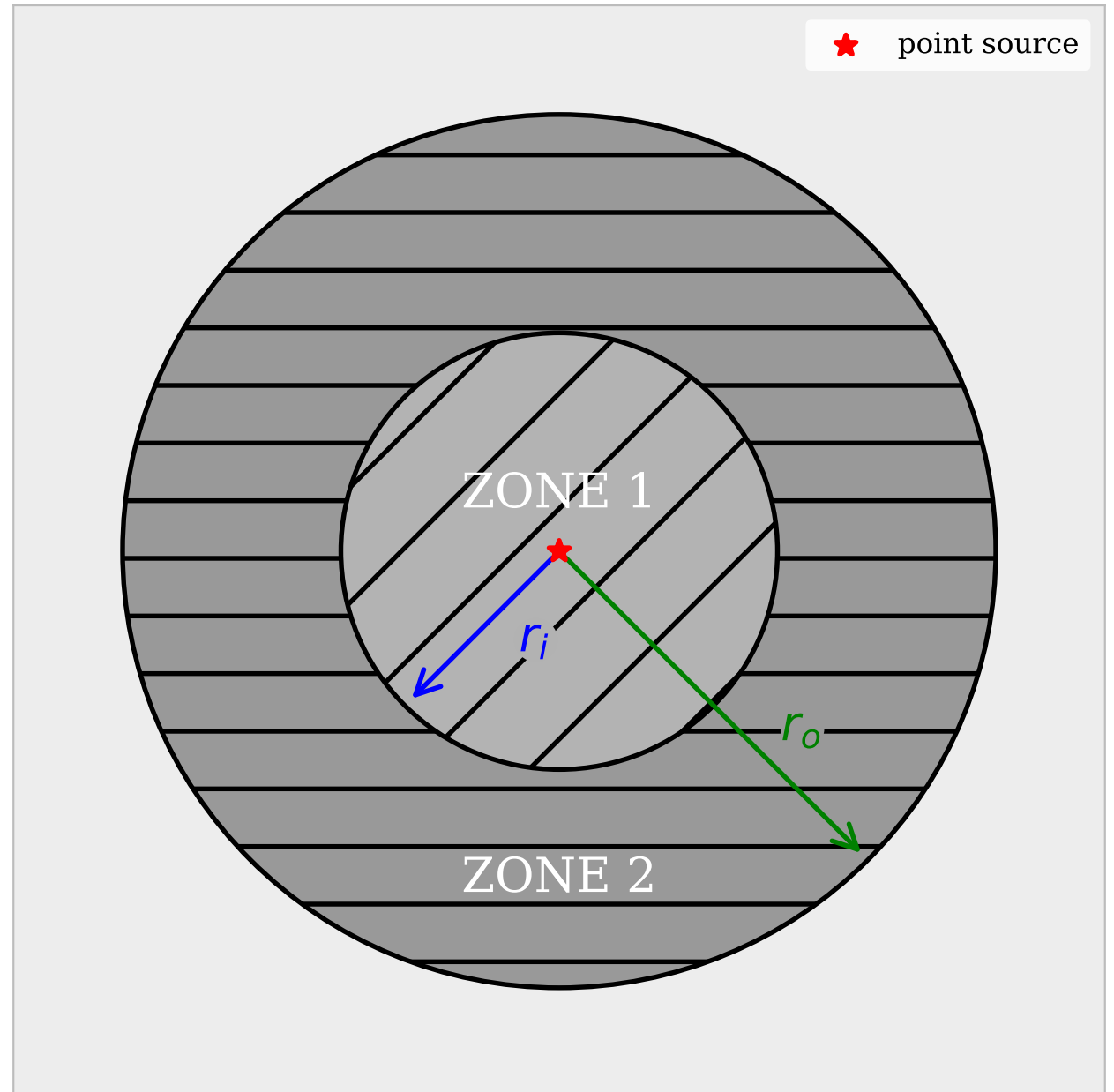


Inpainting

- The conditional probability distribution function of pixels in ZONE 1 constrained by pixels in ZONE 2 is a gaussian

$$\mathcal{P}(p_1|Z_2) = \frac{\mathcal{P}(Z_2|p_1)\mathcal{P}(p_1)}{\mathcal{P}(Z_2)}$$

- We keep the random deviations from the realization but use the mean of the PDF of the real map

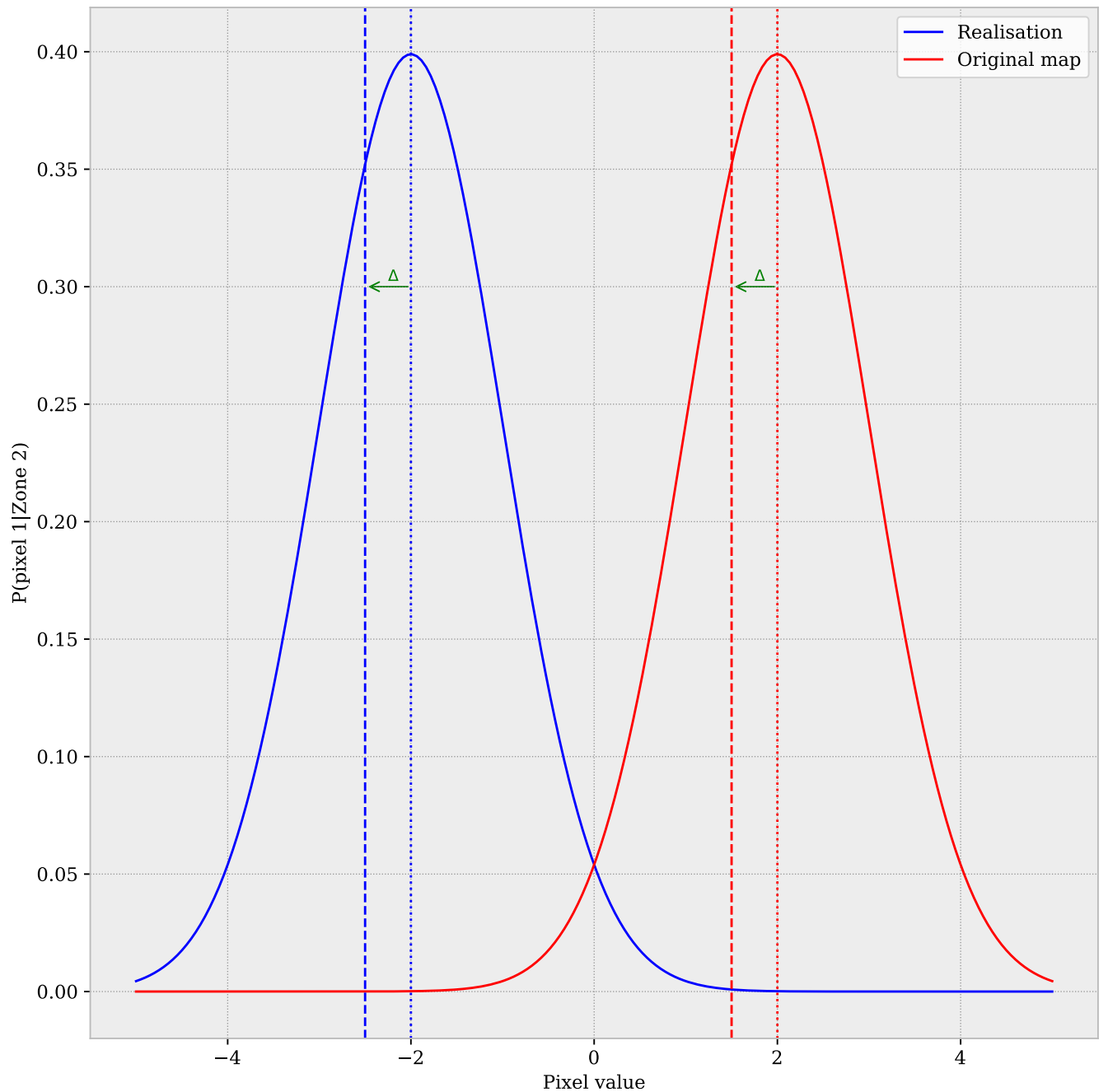


Inpainting

- The conditional probability distribution function of pixels in ZONE 1 constrained by pixels in ZONE 2 is a gaussian

$$\mathcal{P}(p_1|Z_2) = \frac{\mathcal{P}(Z_2|p_1)\mathcal{P}(p_1)}{\mathcal{P}(Z_2)}$$

- We keep the random deviations from the realization but use the mean of the PDF of the real map

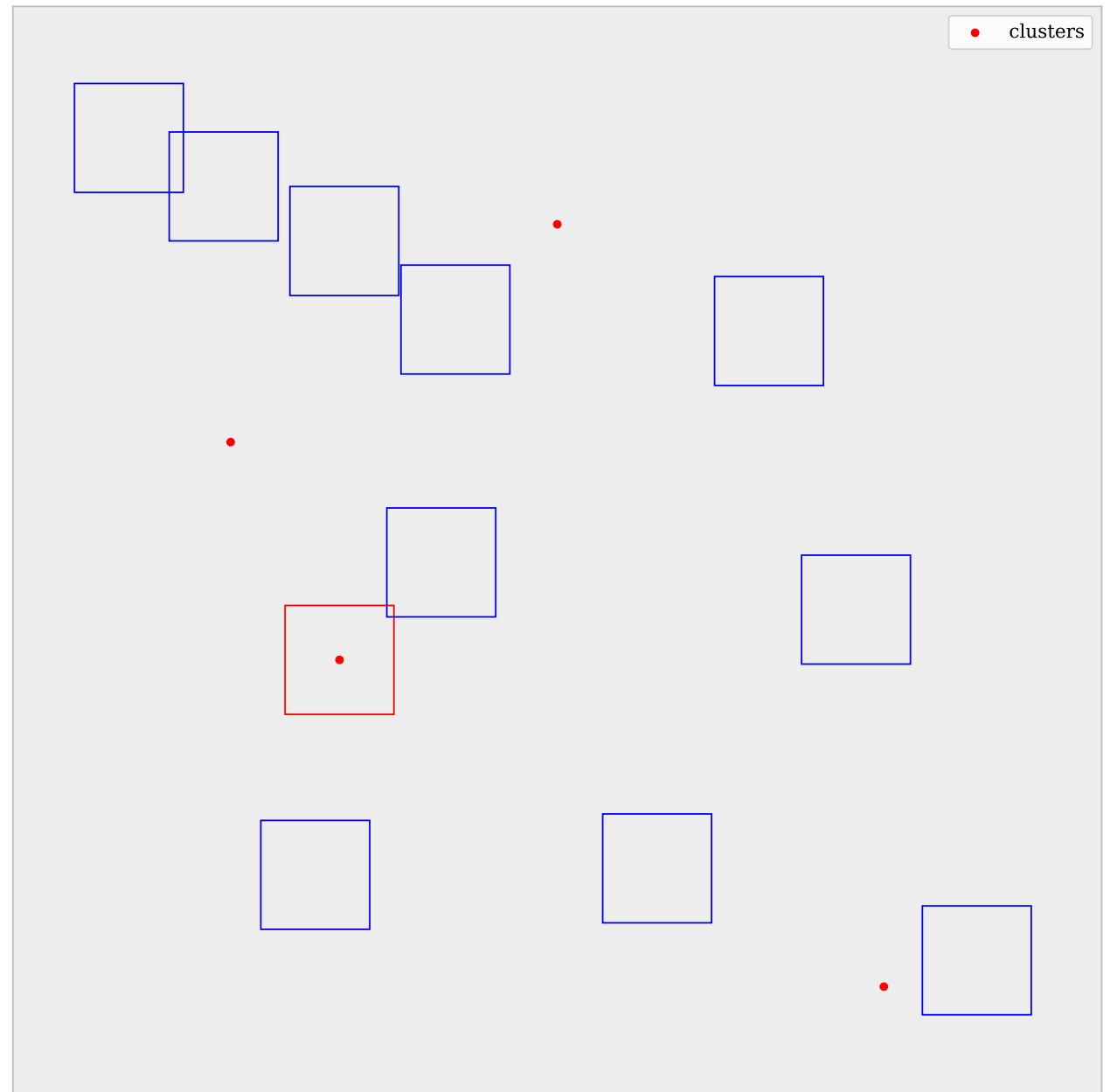


Bias in the lensing!

- Massive **foreground** objects have a lensing effect
- Having **non periodic** maps creates another bias
- These biases **can be corrected** by “off” measurements

→ We draw 10 **random** “off” maps **not centered on a cluster** for each “on” map and run the analysis on them

→ Final result is **on - off**



For one “on” map, we cut 10 “off” maps in the sky map