

# $3^{rd}$ year PhD CPPM seminar

## $\text{LFV } \tau \rightarrow e\ell\ell$ decays at Belle II

Arthur Thaller

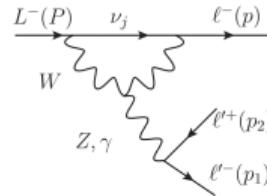
Aix Marseille Univ, CNRS/IN2P3, CPPM

November 27, 2023

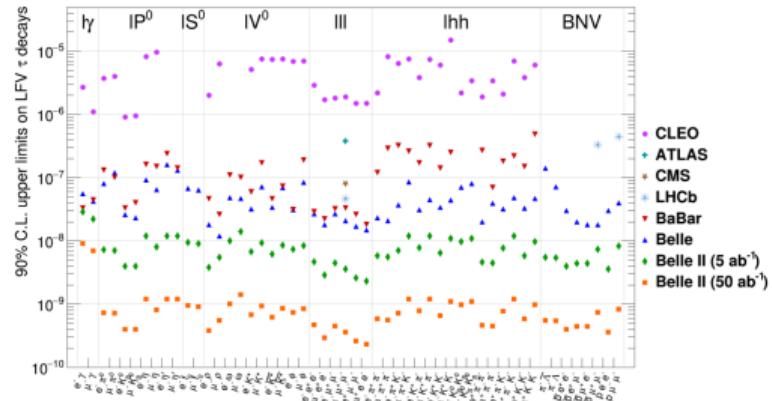


# LFV and $\tau$ decays

- Lepton flavor is conserved in the SM (although "accidentally")
  - ▶ Except for neutrino oscillations
  - ▶ Typically for LFV lepton decays :  
 $\mathcal{B}(LFV) \sim 10^{-50}$
- Anomalies in LFU measurement can imply LFV at detectable levels
- Many new physics models predict LFV  $\tau$  decays around  $10^{-8} - 10^{-10} \rightarrow$  in Belle II's reach !
- $\tau$  decays are a good place to look for LFV, since  $\tau$  is the heaviest lepton

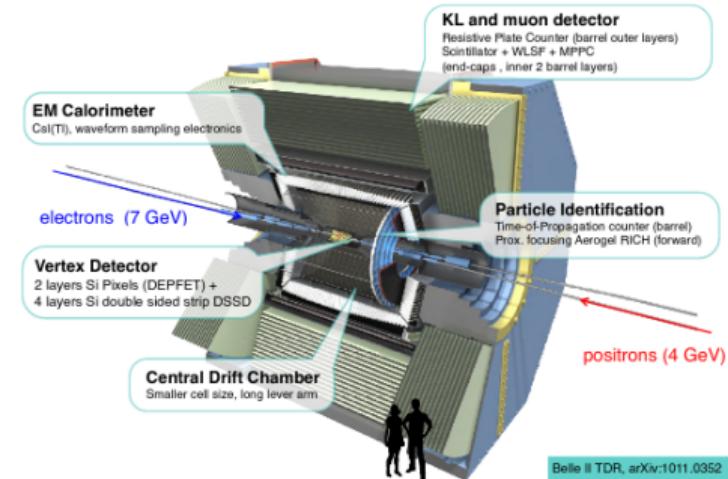


SM diagram for LFV



# Belle II

- $e^+e^-$  collider, 10.58 GeV →  $\Upsilon(4S)$  resonance  
→ B-factory
- Record instantaneous luminosity  
 $4.7 \times 10^{34} cm^{-2}s^{-1}$
- Current dataset :  $424 \text{ fb}^{-1}$  (on-resonance + off-resonance)
- Clean environment, collision energy is well known
- Hermetic detector → good missing energy resolution
- $\tau$  pair production cross section is quite high (0.92 nb) w.r.t B meson production
  - ▶  $\sim 400$  million  $\tau$  pairs already produced  
→  $\tau$ -factory !



# $\tau \rightarrow e\ell\ell$

- $\tau^\pm \rightarrow e^\pm \ell^\mp \ell^\pm + cc, l = e, \mu$
- 5 modes :  $e^+e^-e^+, e^+e^-\mu^+$ ,  
 $e^+\mu^-e^+, \mu^+e^-\mu^+, \mu^+\mu^-e^+$
- $\tau^+ \rightarrow \mu^+\mu^-\mu^+$  : Analysis done by Robin Leboucher
- Using full LS1 dataset :  $424 \text{ fb}^{-1}$ 
  - ▶ Off-resonance  $\tau\bar{\tau}$  production cross section is extremely close to on-resonance :  $\sigma_{\tau\bar{\tau}} = 0.919^* \left(\frac{10.58}{E_{\text{off-res}}}\right)^2 \text{ nb}$

Quantity to be measured :

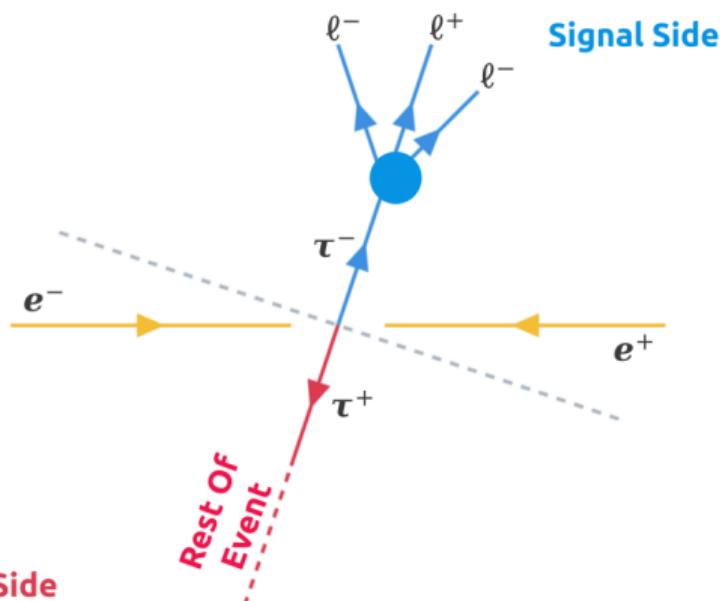
$$\mathcal{B}(\tau \rightarrow e\ell\ell) = \frac{N_{\text{sig}}^{\text{obs}}}{\mathcal{L} \times 2\sigma_{\tau\bar{\tau}} \times \epsilon_{\text{sig}}}$$

Belle results at  $782 \text{ fb}^{-1}$

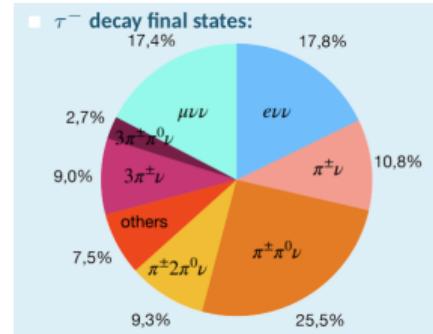
Mode	$\varepsilon$ (%)	$N_{\text{BG}}$	$\sigma_{\text{syst}}$ (%)	$N_{\text{obs}}$	$\mathcal{B} \times 10^{-8}$
$\tau^- \rightarrow e^-e^+e^-$	6.0	$0.21 \pm 0.15$	9.8	0	<2.7
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$\tau^- \rightarrow \mu^+e^-e^-$	11.5	$0.01 \pm 0.01$	7.7	0	<1.5

# Untagged analysis

We perform an untagged analysis : we don't explicitly reconstruct the other  $\tau$ , instead we use information from the Rest of Event (ROE) : energy, clusters, particle content...



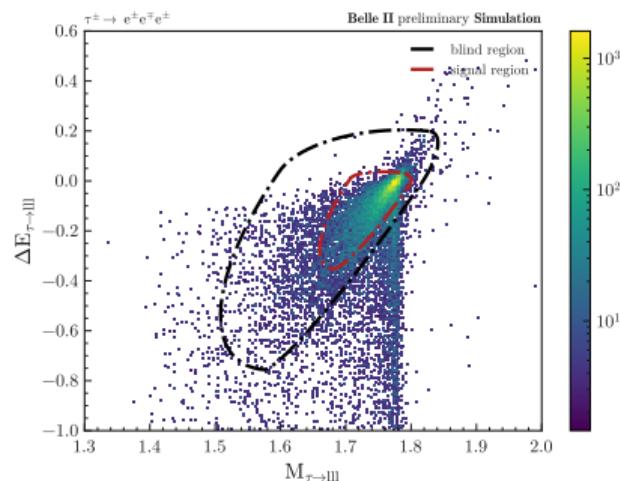
- 1-prong (+ neutrals)  $\tau$  decays :  $\tau \rightarrow \pi\nu$ ,  $\tau \rightarrow \ell\nu\nu \sim 80\%$
- Add 3-prong :  $\tau \rightarrow 3\pi\nu$
- 30% gain in signal efficiency w.r.t. tagged (1-prong tag) analysis (Belle and BaBar)
- More background also reconstructed



# Event selection

- Require that all tracks come from the IP
- Leptons : apply loose selection on the leptons particle identification variables (PID) for each mass hypothesis
  - ▶ muon : muonID > 0.5
  - ▶ electron : electronID > 0.5
- Use thrust to define 2 hemispheres : plane orthogonal to thrust axis separates the events in 2 halves
  - ▶  $T = \max_{n_T} \left( \frac{\sum_i |p_i \cdot n_T|}{\sum_i |p_i|} \right)$
- Require that the 3 leptons are on the same side of the event, and that everything else is on the other side
  - ▶ Additional photons, clusters, tracks...

- Use  $(\Delta E_{3\ell}, M_{3\ell})$  plane to define signal region and reduce background ( $\Delta E = \frac{E_{beam}}{2} - E_{3\ell}$ )
- Get signal region by fitting  $\Delta E_{3\ell}$  and  $M_{3\ell}$  distributions with asymmetric gaussians.



Signal distribution in  $(\Delta E_{3\ell}, M_{3\ell})$  for  $\tau^+ \rightarrow e^+ e^- e^+$

## Background composition

Various background sources after event selection, depending on the mode :

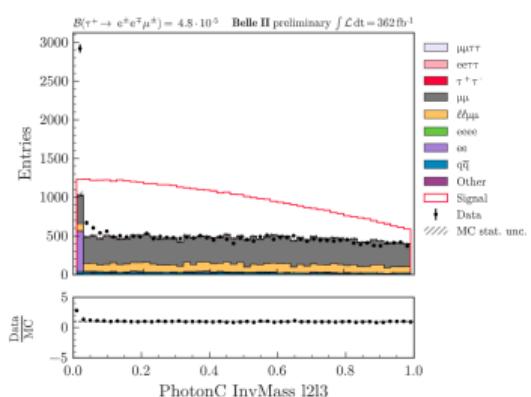
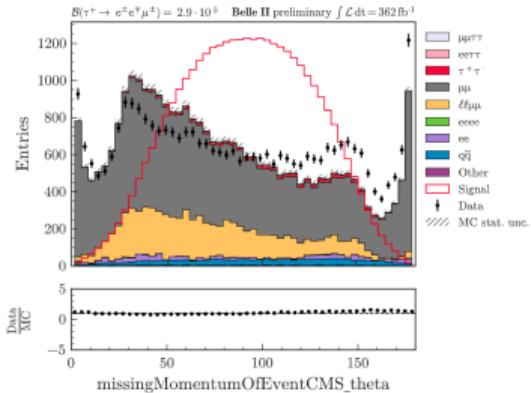
- $q\bar{q}$  : light quark pair ( $q = u,d,c,s$ )
- QED backgrounds :  $2\ell$  and  $4\ell$  events
- Mis-modeled contributions, radiative events with pair conversion and di-photons events

Background rejection is done mode by mode, first applying cut-based selection and further rejecting background using BDT.

- Due to presence of electrons : lot of background from QED processes.
- In principle these background contributions can be removed using physics considerations, mainly from the fact that there is no missing momentum
- However in the end, we achieve better sensitivity by using BDT classifier.

# Background rejection

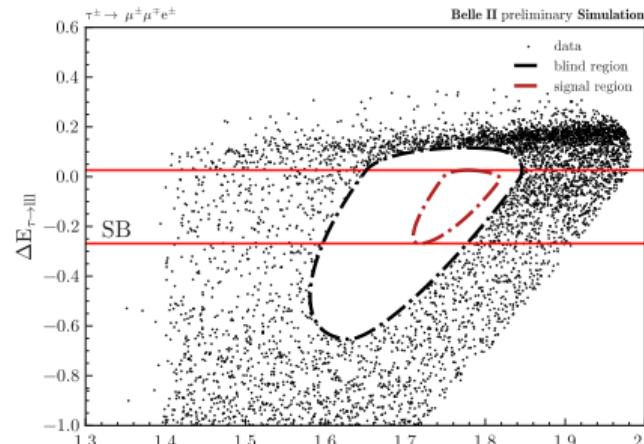
- Cut based preselection : target obvious peaking backgrounds and mismodeled contributions
  - ▶ Missing momentum aligned with the beam axis from di-photons
  - ▶ Low invariant mass of dilepton systems : radiative events with pair conversion
  - ▶ High thrust values : QED background
  - ▶ Refine PID selections : rank the same flavor lepton PID variables and cut tighter on the leading one.  
→ require that one lepton of each flavor is clearly identified
- Remaining background : reject with BDT trained on data



## BDT training

Train a BDT(one per mode) on data, using 2 training samples :

- Upper and lower region : data that survive previous cuts
- In sidebands and blinded ellipse : data that survives previous cuts, but with inverted PID requirements
- More training stat !
- Make sure there is no risk of signal
- We keep sidebands completely independant for final background estimation
- Control that BDT output does not depend on  $M_\tau$
- 31 input variables (kinematics, ROE, missing energy, event shape...)



# BDT cut

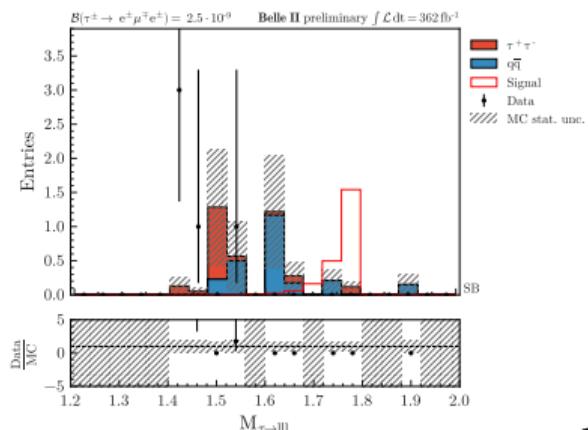
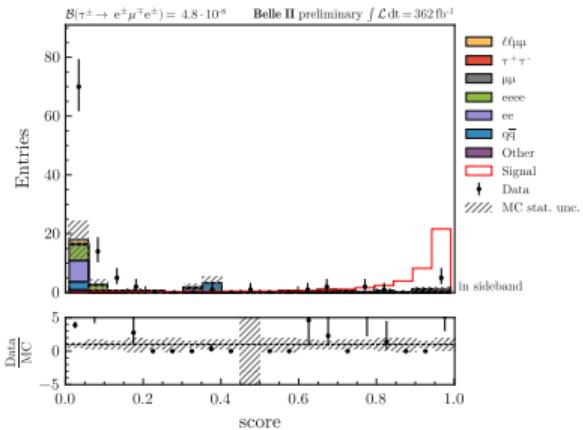
Apply selection on the BDT output in order to maximize the  
punzi f.o.m. :  $\frac{\epsilon_{sig}}{\frac{3}{2} + \sqrt{N_{bg}}}$

- $\epsilon_{sig}, N_{bg}$  Signal efficiency and remaining background after BDT cut

After application of every selection :

	$e^+e^-e^+$	$e^+e^-\mu^+$	$e^+\mu^-\mu^+$	$\mu^+e^-\mu^+$	$\mu^+\mu^-e^+$
$\epsilon_{sig}$	16.5%	18.2%	21.2%	22%	17.1%
$N_{SB}$	2	4	5	2	5

- $\epsilon_{sig}$  : Final signal efficiency in the signal region
- $N_{SB}$  : Number of remaining events in the side bands



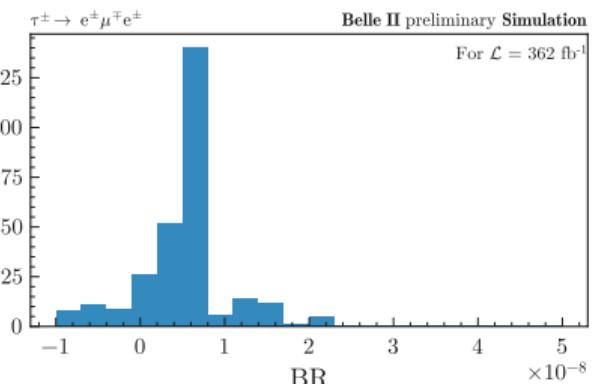
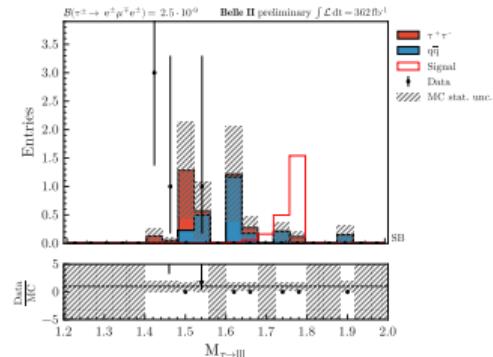
# Background estimation and signal yield extraction

Fit the data in  $M_\tau$  :  $PDF_{tot} = N_{sig} \cdot PDF_{sig} + N_{bg} \cdot PDF_{bg}$

- $PDF_{sig}$  : signal PDF, obtained from MC, most likely gaussian
- $PDF_{bg} = e^{c \cdot M_\tau}$  : background PDF, obtained from data sidebands

Upper limit on the branching ratio can be estimated :

- Generate toys assuming background only
- Fit with  $PDF_{tot}$ , extract  $N_{sig}$   
 $\rightarrow \mathcal{B}(\tau \rightarrow e\ell\ell) = \frac{N_{sig}}{\mathcal{L} \times 2\sigma_{\tau\bar{\tau}} \times \epsilon_{sig}}$
- From preliminary results :  $\mathcal{B}_{UL}(\tau \rightarrow e\ell\ell) \sim 2 \cdot 10^{-8}$



# Conclusion

- $\tau \rightarrow ell$  analysis, untagged method, which allows us to be competitive (better!) with Belle's result despite lower statistics
  - ▶ Also thanks to Belle II overall better performances
- Event selection and background rejection based on geometrical considerations, combination of cuts based approach and BDT
  - ▶ To overcome non simulated contamination, data-driven background rejection
- Signal extraction strategy needs to be finalized, systematics uncertainty need to be evaluated  
→ uncertainty dominated by statistics
  - ▶ Data-driven background estimation
  - ▶ Fitting makes the analysis more robust against statistical fluctuations
- Objective is to be ready for Moriond, March 2024

Thanks for listening !

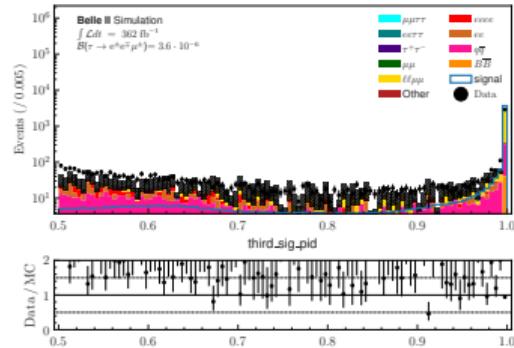
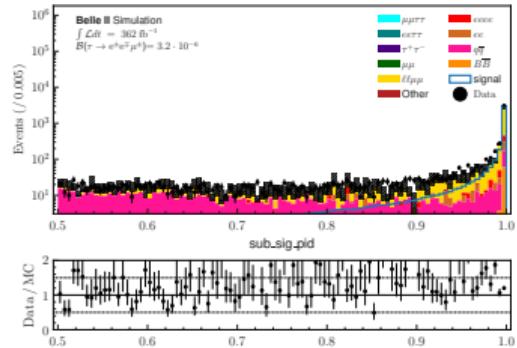
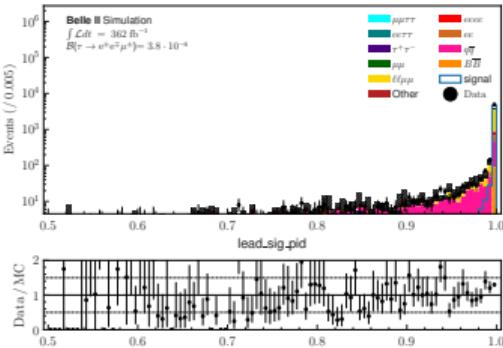
# BACKUP

## Belle numbers

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At  $782 \text{ fb}^{-1}$

# PID variables, $e^+e^-\mu^+$



# Asymmetric error bars

## Asymmetric error bars on data yields (“vanilla case”)

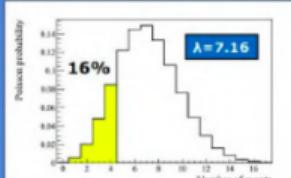
- after discussion at past tau meeting, we assign asymmetric uncertainties to yields in **data and MC**
  - before computed as symmetrical Poisson uncertainties  $\sqrt{N}$ , for  $N$  entries in bin<sub>i</sub>
- adopt frequentist approach and find iteratively  $\lambda_1$ ,  $\lambda_2$  so that  $P(n \leq N_{\text{bin}} | \lambda_1) \leq 0.16$  and  $P(n \geq N_{\text{bin}} | \lambda_2) \leq 0.16$

### Option 6: Frequentist approach

Find values of  $\lambda$  that are on border of being compatible with observed #events

If  $\lambda > 7.16$  then probability to observe  
4 events (**or less**) < 16%

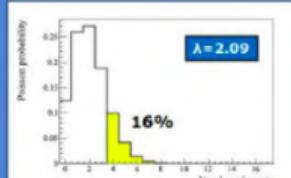
Note: also uses ‘data you didn’t observe’, i.e. a bit like definition of significance



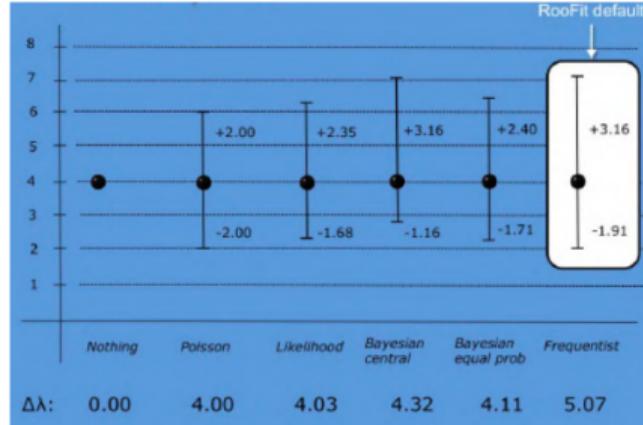
smallest  $\lambda (>n)$  for which  $P(n \leq n_{\text{obs}} | \lambda) \leq 0.159$

+3.16 → smallest  $\lambda (>n)$  for which  $P(n \leq n_{\text{obs}} | \lambda) \leq 0.159$

-1.91 → largest  $\lambda (<n)$  for which  $P(n \geq n_{\text{obs}} | \lambda) \leq 0.159$



L.Zani - Marseille 2023.03.06 - Tau to lepton phi unboxing



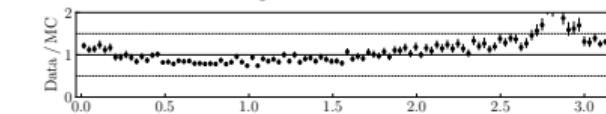
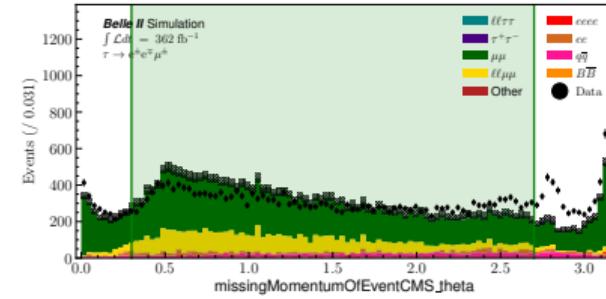
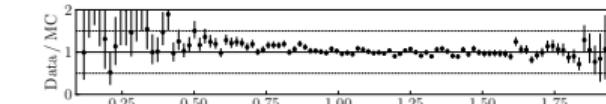
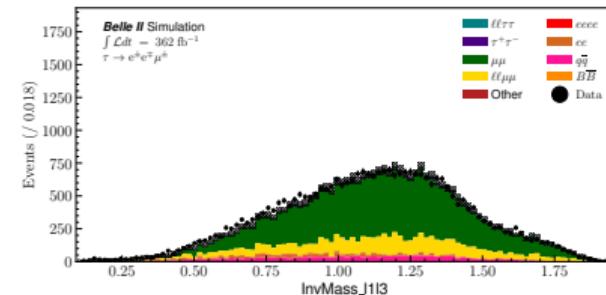
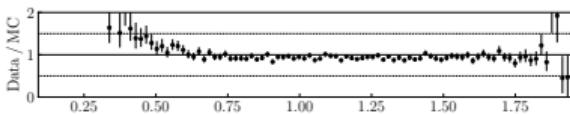
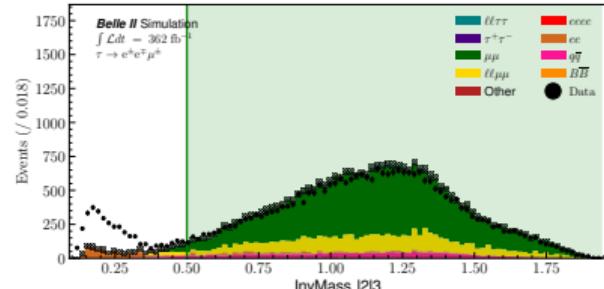
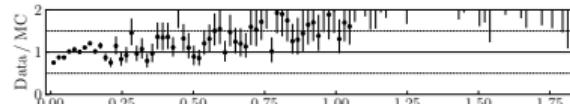
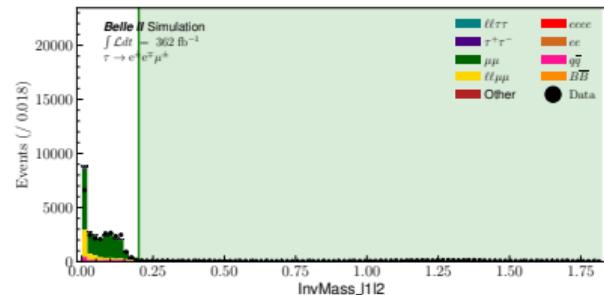
- in each bin error bars are defined as:
  - $\text{err\_stat\_up} = \lambda_1 - N_{\text{bin}}$ ,
  - $\text{err\_stat\_low} = N_{\text{bin}} - \lambda_2$

## BDT variables

```
'thrust', 'tau_flightDistance_overErr',
'L3_sig_angleToMissing', 'tag_side_mode',
'tau_sig_dcosTheta', 'lead_sig_E',
'missingMass20fEvent', 'cleoConeCollision_0',
'InvMass_l2l3', 'tau_sig_cosToThrust0fEvent',
'L3_sig_theta', 'roeEmasktight',
'missingMomentum0fEvent', 'roeNeextramasktight',
'L1_sig_theta', 'nGoodPhotons',
'L1_sig_angleToMissing', 'cleoConeThrust_1',
'L2_sig_angleToMissing', 'InvMass_l1l2',
'roeMmasktight', 'third_sig_E',
'L2_sig_theta', 'cleoConeThrust_2',
'tau_sig_dphi', 'totalPhotonsEnergy0fEvent',
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'missingMomentum0fEventCMS_theta',
'tau_sig_chiProb', 'cleoConeThrust_0',
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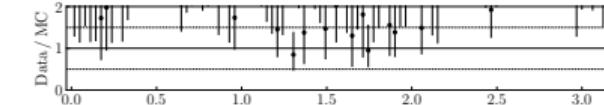
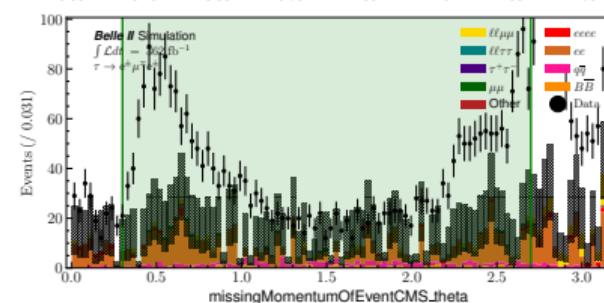
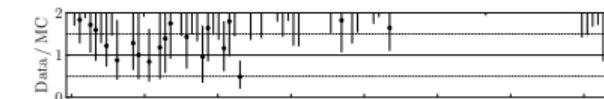
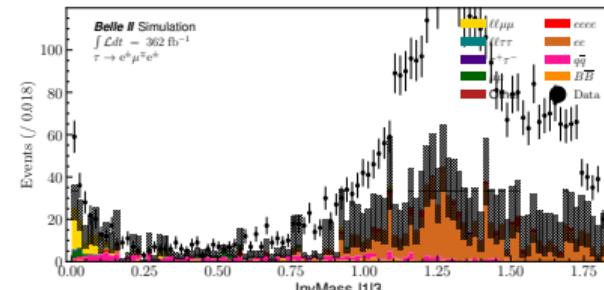
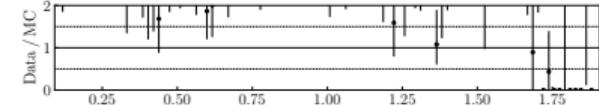
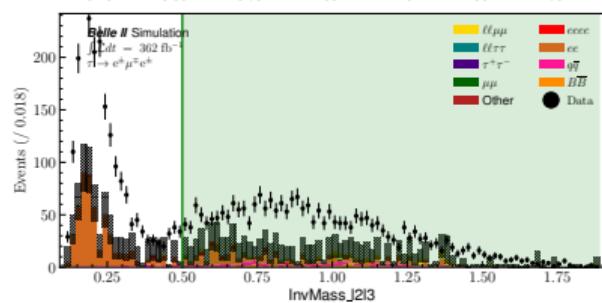
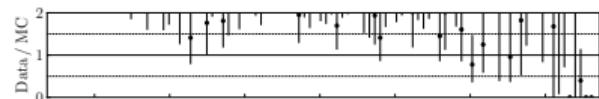
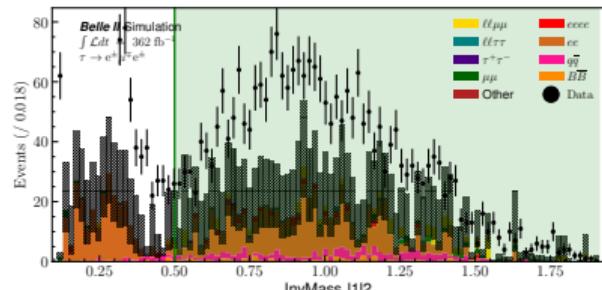
# $e^+e^- \mu^+$ data-driven selection

Right after reconstruction :

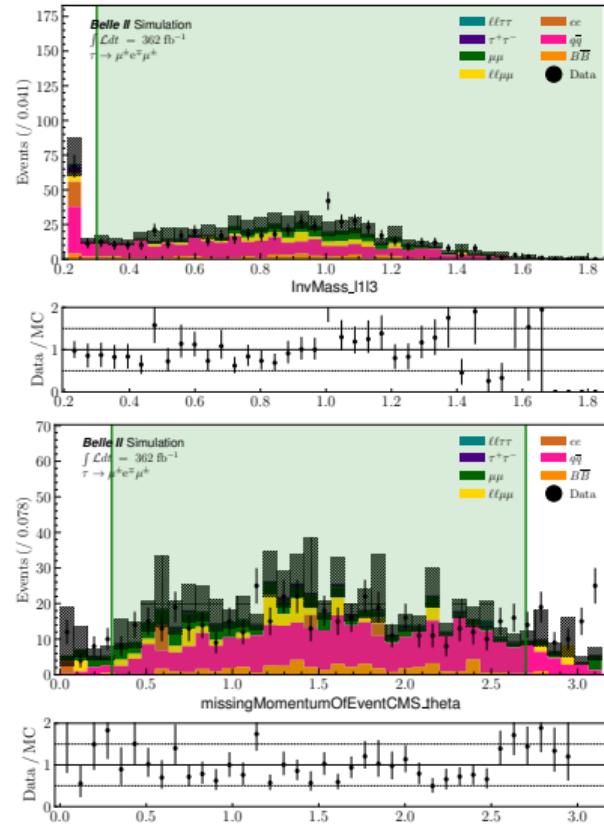
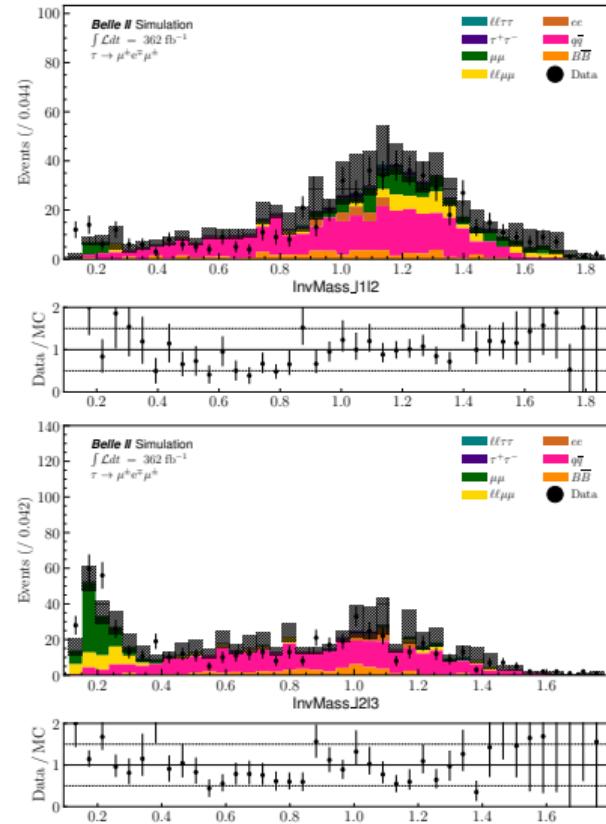


# $e^+ \mu^- e^+$ data-driven selection

Right after reconstruction :



# $\mu^+e^-\mu^++$ data-driven selection



# $\mu^+\mu^-e^+$ data-driven selection

Right after reconstruction :

