



European Research Council  
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**Institut de Ciències del Cosmos**  
**UNIVERSITAT DE BARCELONA**

A vibrant, multi-colored cosmic background featuring a nebula with shades of purple, pink, blue, and green, interspersed with numerous bright stars and light trails.

**A COSMOLOGY REVIEW FOR  
STRING THEORISTS**

# COSMOLOGY PRIMER

- Base assumption: FLRW metric  
(homogeneity & isotropy at leading order on largest scales)

$$ds^2 = -dt^2 + a^2 d\vec{r}^2$$

$$\vec{d} = a\vec{r}$$

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$$ds^2 = -dt^2 + a^2 d\vec{r}^2$$

$$\vec{d} = a\vec{r}$$

- Also: Perturbations of physical size  $k = 1/r_{\text{comoving}}$

# COSMOLOGY PRIMER

- Expansion rate related to energy content

$$H^2 = \frac{8\pi G}{3} \rho = \frac{1}{3} \rho$$

$$H = \frac{\dot{a}}{a}$$
$$\vec{d} = a\vec{r}$$

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$$H = \frac{\dot{a}}{a}$$
$$\vec{d} = a\vec{r}$$

- This also defines a horizon

$$D_H = 1/H$$

(or in comoving space:  $r_H = 1/(aH)$  )

# COSMOLOGY PRIMER

- Energy content:

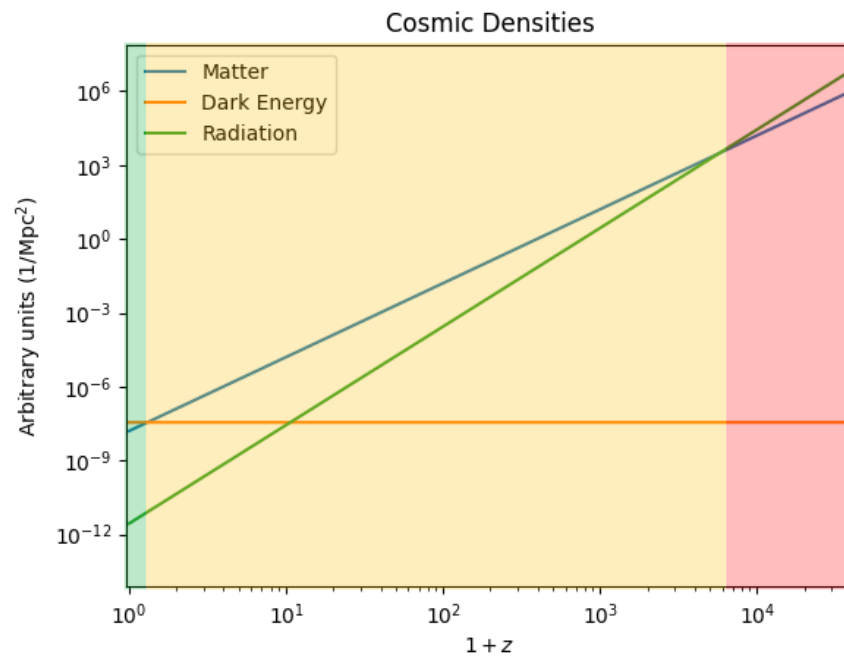
$$\rho_{\text{rad}} \propto \frac{E}{V} \propto \frac{1}{\lambda V} \propto a^{-4}$$

$$\rho_{\text{mat}} \propto \frac{E}{V} \propto \frac{m}{V} \propto a^{-3}$$

$$\rho_{\Lambda} = \text{const.}$$

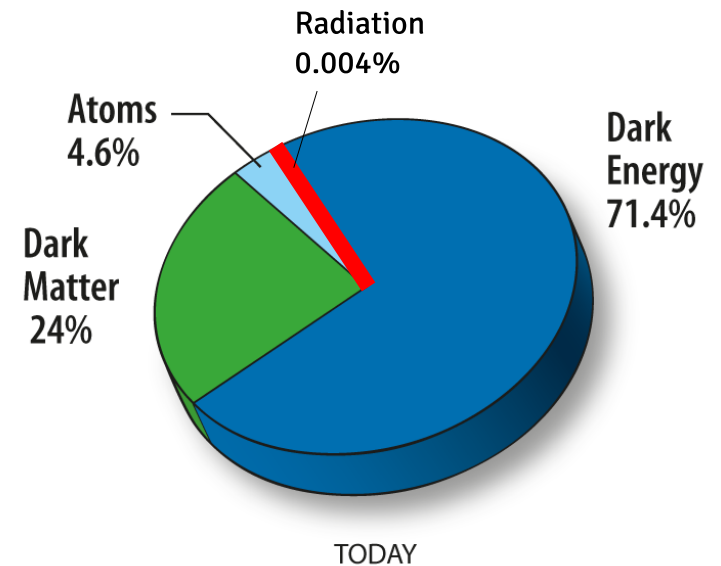
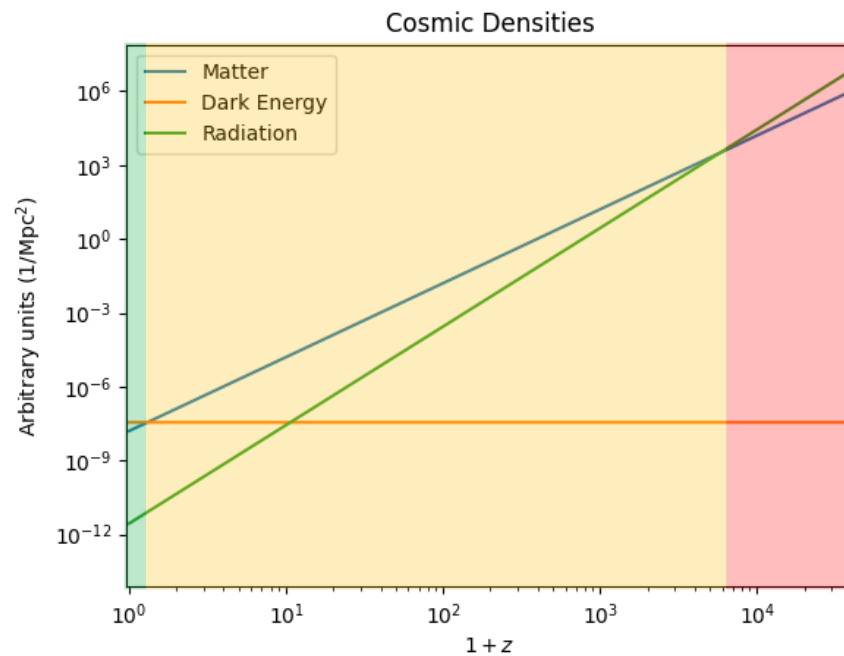
# ENERGY CONTENT

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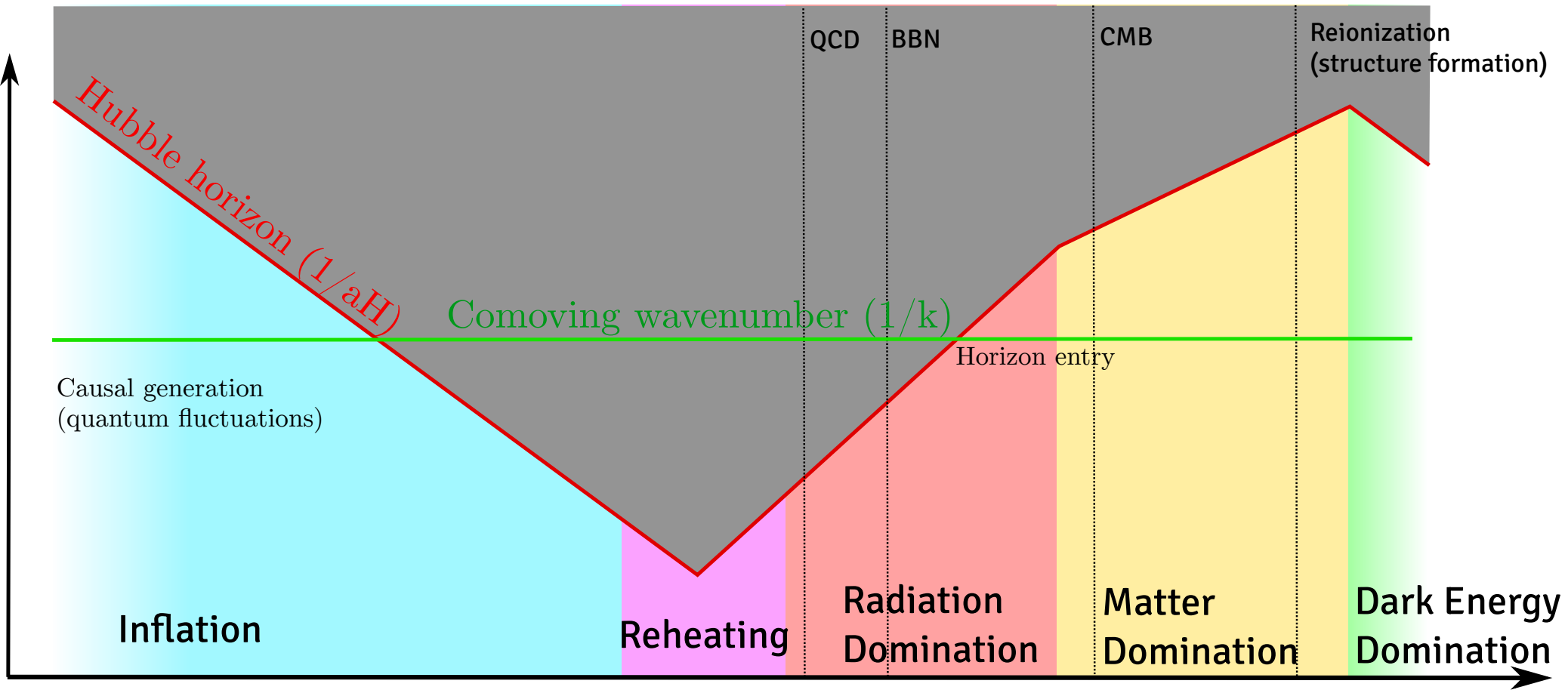
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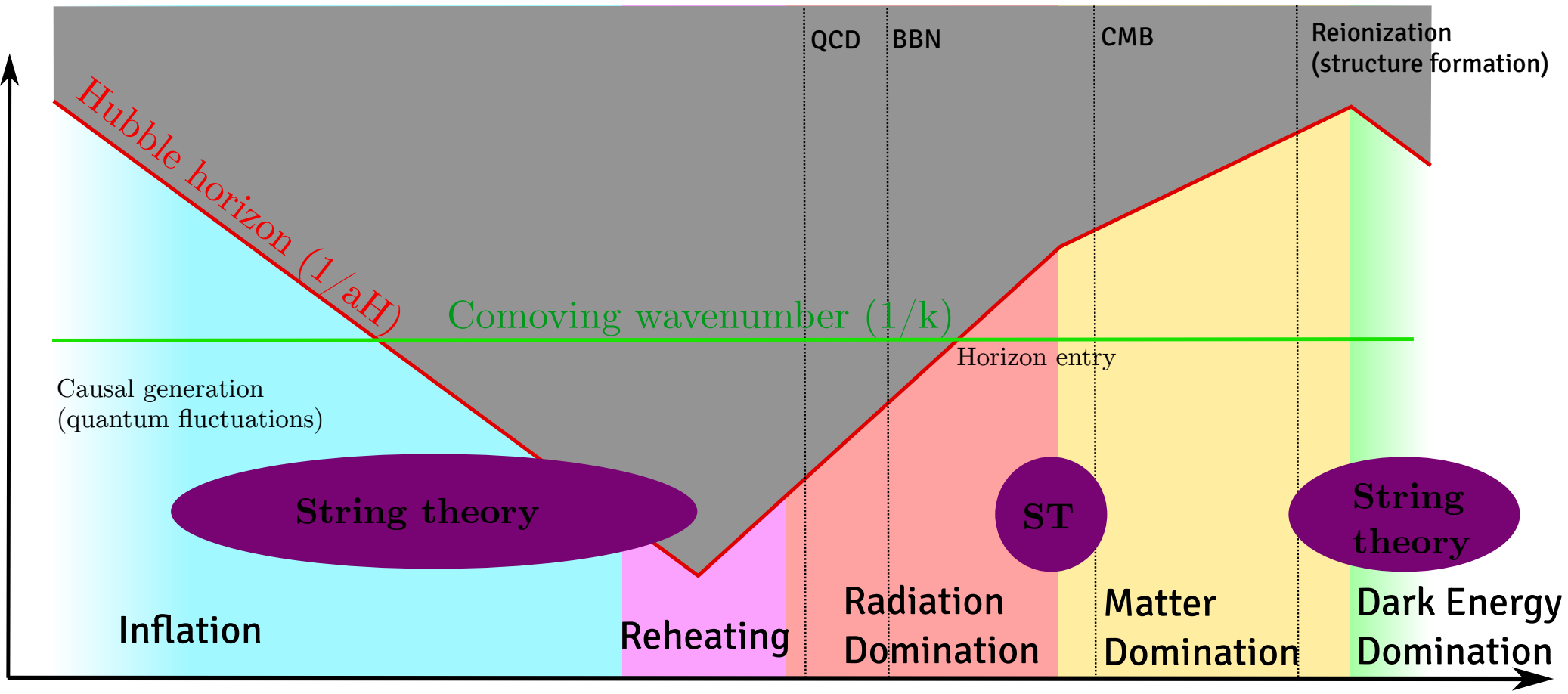




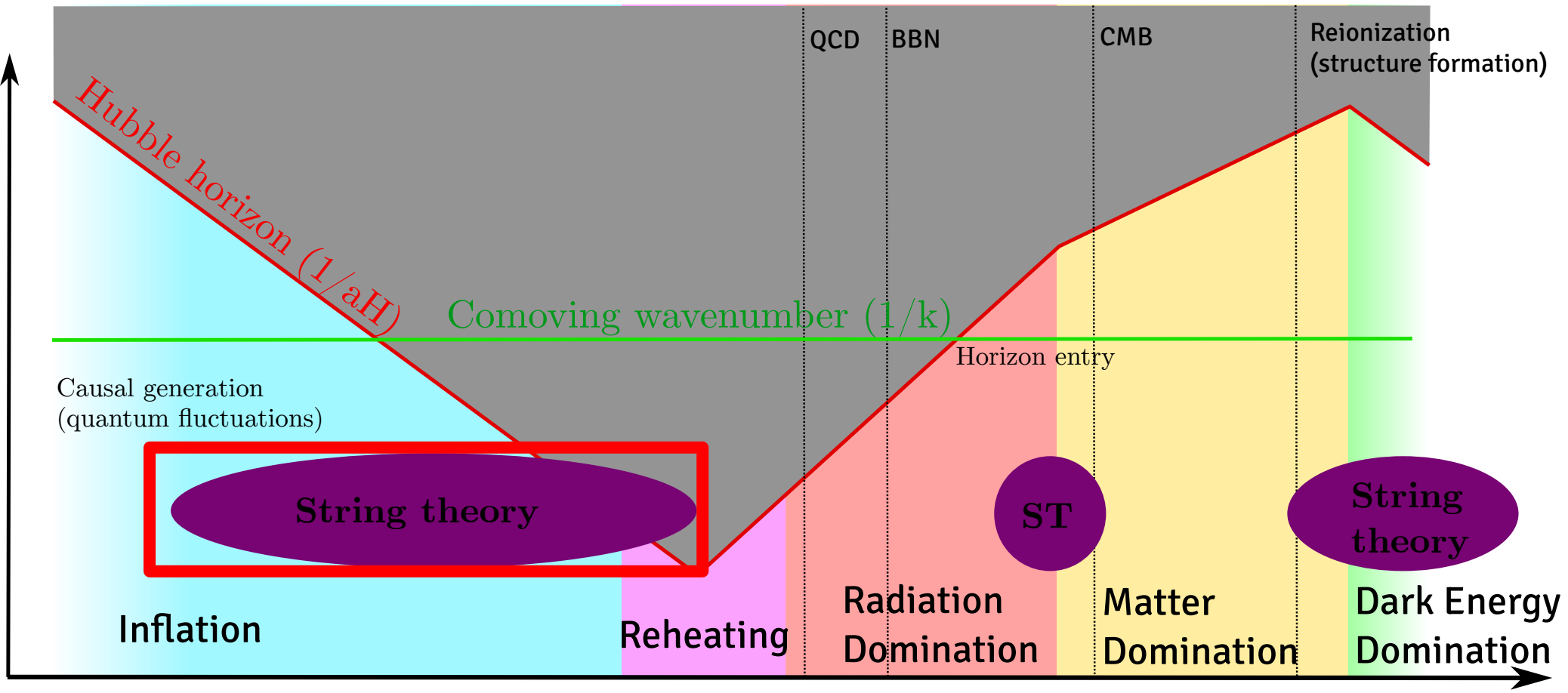
# OUR COSMIC HISTORY (SO FAR)



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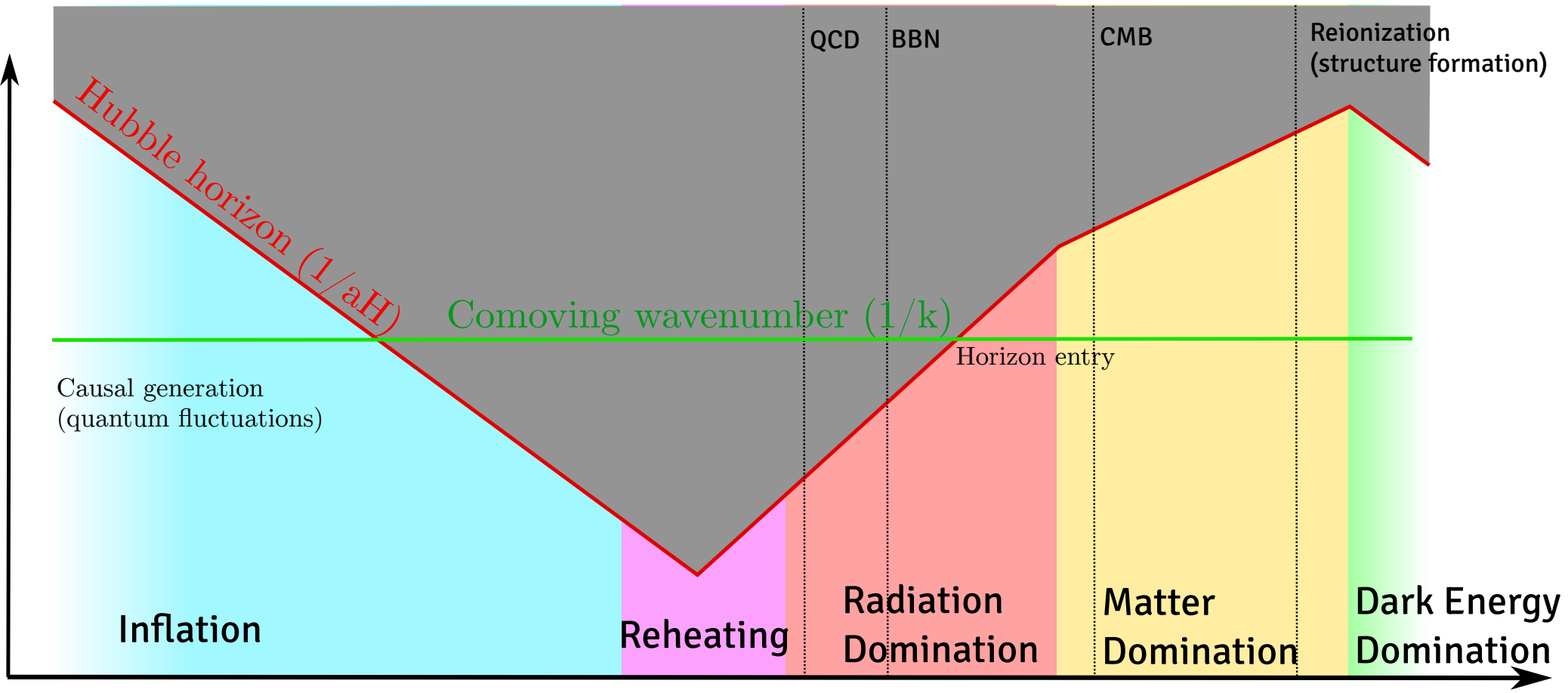
# OUR COSMIC HISTORY (SO FAR)



# INFLATION

- Horizon problem
  - thermal contact before inflation generates isotropy
- Flatness problem
  - inflation expands space, diluting any existing curvature
- Causal perturbations
  - super-horizon perturbations were sourced by sub-horizon quantum fluctuations

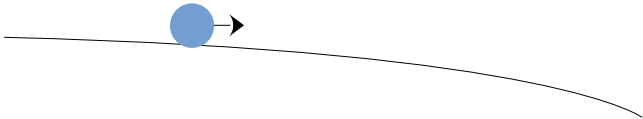
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# INFLATION

Slow roll of scalar field

$$H^2 = \frac{\rho}{3} \approx \frac{1}{3} \left( \frac{\dot{\phi}^2}{2} + V \right) \approx \frac{V}{3}$$



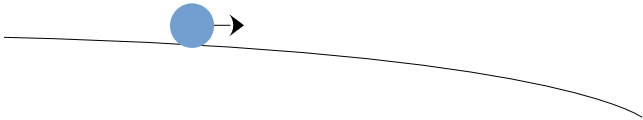
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$$\partial_{\phi} V \ll V$$



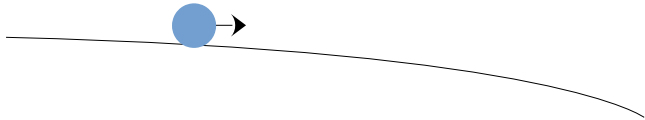
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$$\Rightarrow H^2 \sim V \sim \text{const.}$$

$$\Rightarrow \frac{1}{aH} \propto a^{-1} \text{shrinks}$$

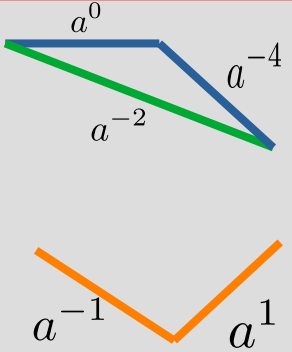


# INFLATION CONDITIONS

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$\rho_K \propto a^{-2}, \rho_{\text{rest}} = \begin{cases} a^0 & \text{inflation} \\ a^{-4} & \text{post-inflation} \end{cases}$

$\frac{1}{aH} = \begin{cases} a^{-1} & \text{inflation} \\ a^{+1} & \text{post-inflation} \end{cases}$

$$\Delta N = \Delta \ln a$$

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(more or less, e.g. reheating, different scales)
- Additional requirement of  $\partial_\phi^2 V \ll V$   
→ Natural result:  $|\Delta\phi| \gg 1$

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- Moduli fields are natural candidates for scalar fields in cosmology
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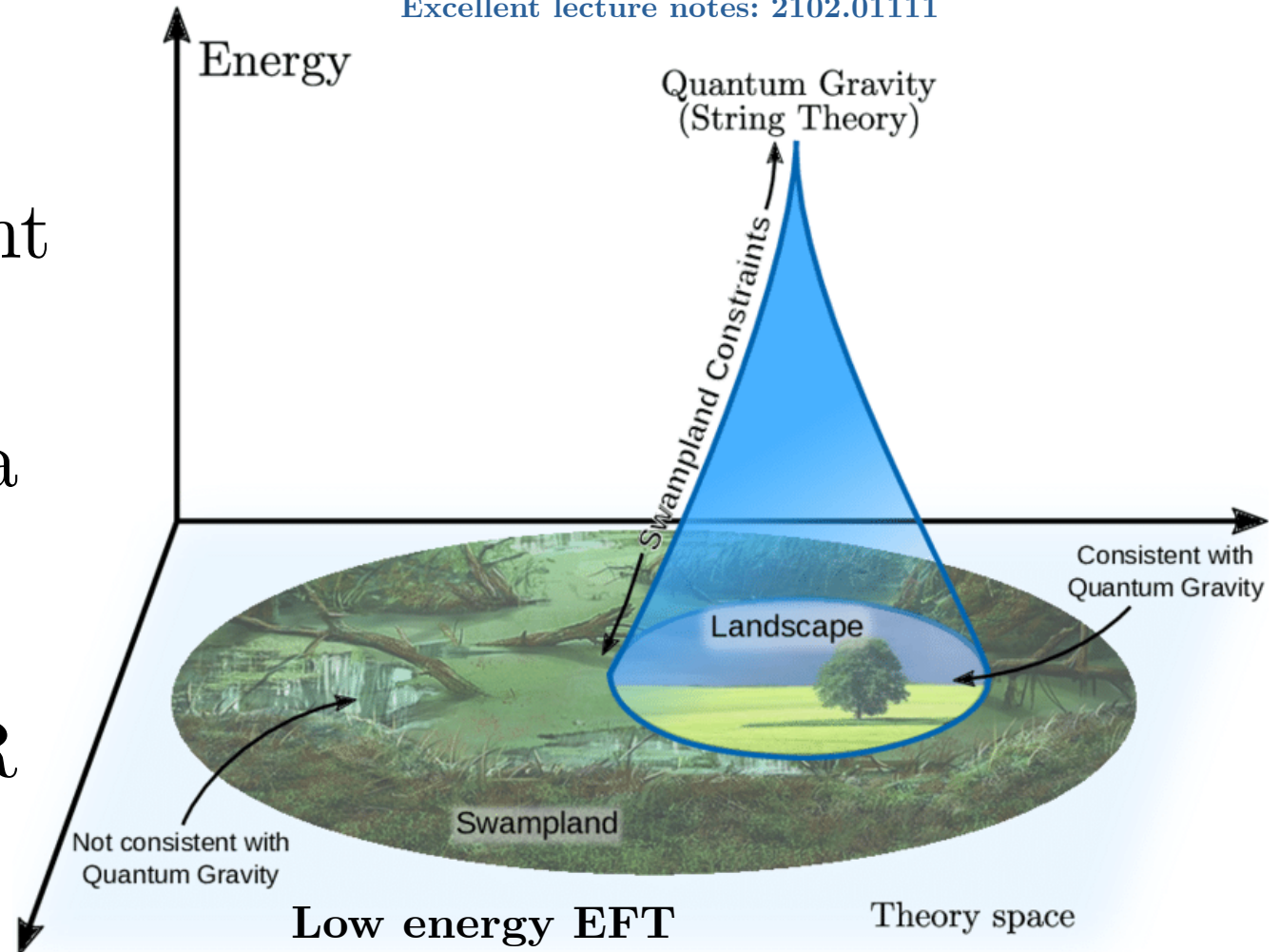
# INFLATION AND STRINGS

- Moduli fields are natural candidates for scalar fields in cosmology
  - Can moduli fields do inflation?
- Many potentials can be realized in string theory
- BUT there might be problems lurking:
  - **Swampland criteria**

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Excellent lecture notes: 2102.01111

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- Define criteria in UV that need to be kept in the IR





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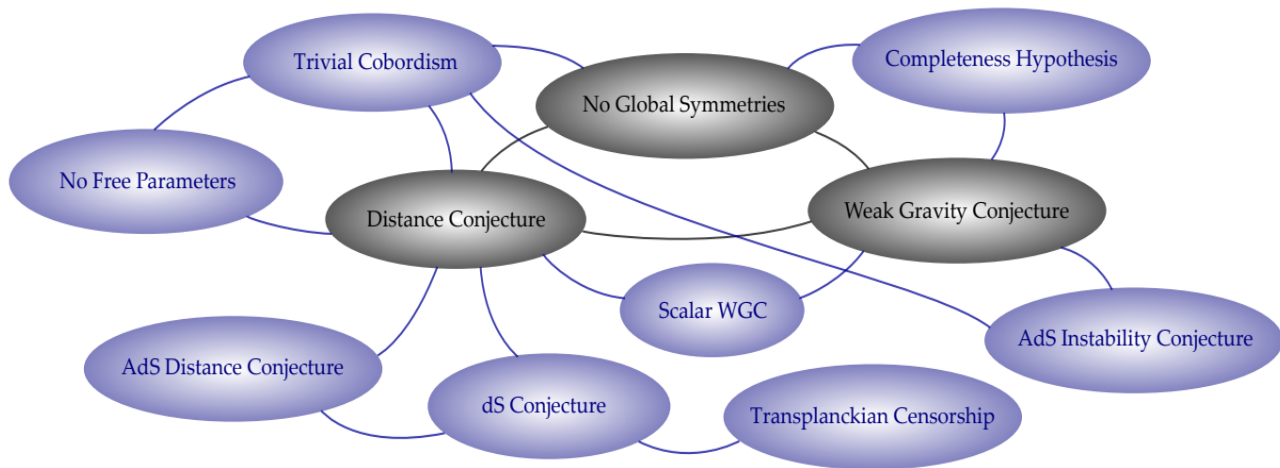


Figure 4: Map of the Swampland conjectures. The conjectures in black are at the core of the Swampland program, and we will discuss them in detail in the following. The conjectures in purple will also be discussed throughout the lectures, but sometimes in less detail.

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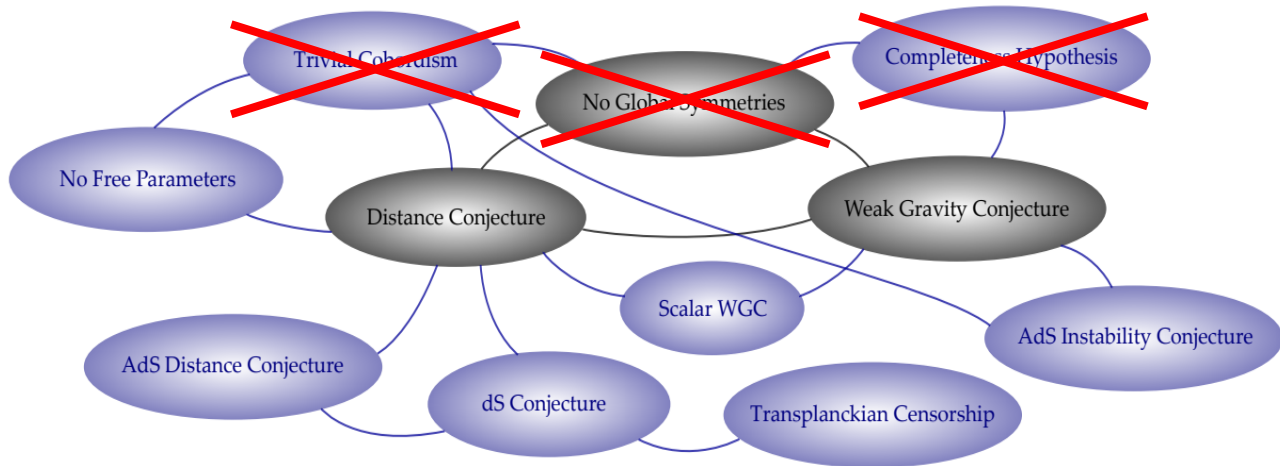


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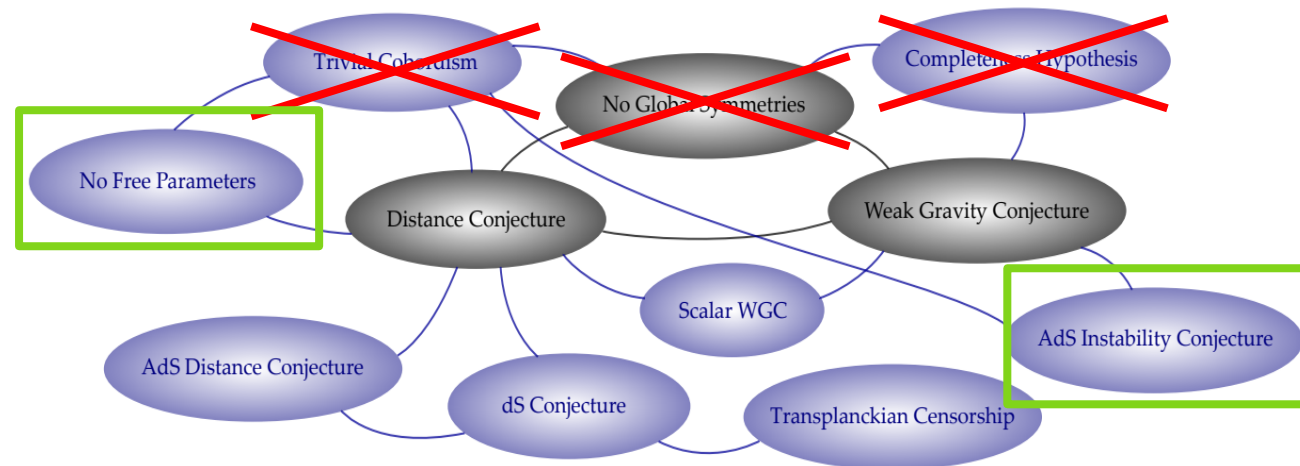


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**Boundary  
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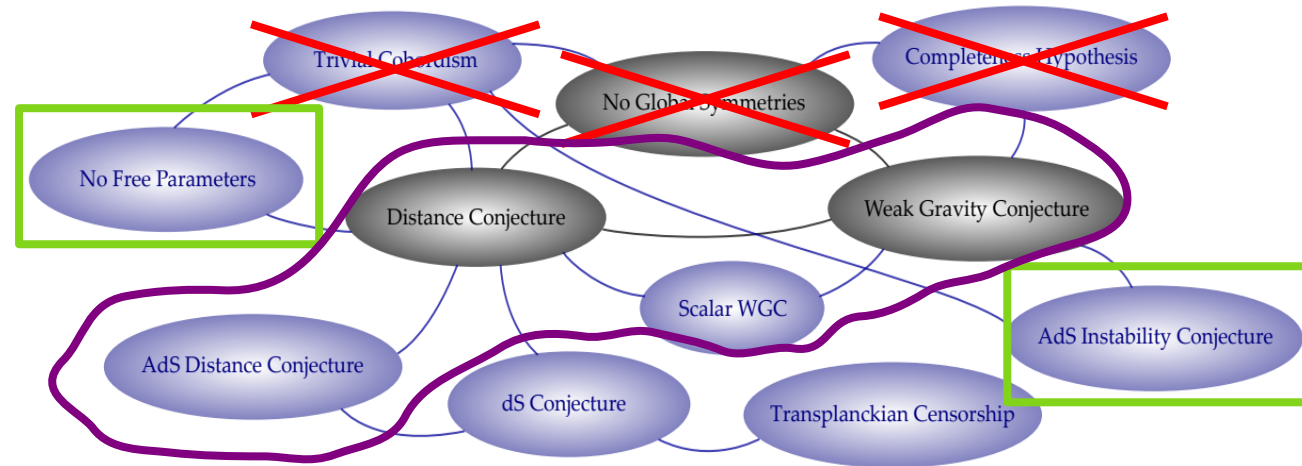


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$$\Delta\phi < \frac{1}{\lambda} \ln \left( \frac{1}{M} \right) \quad \text{Distance conditions} \quad \text{Boundary conditions}$$

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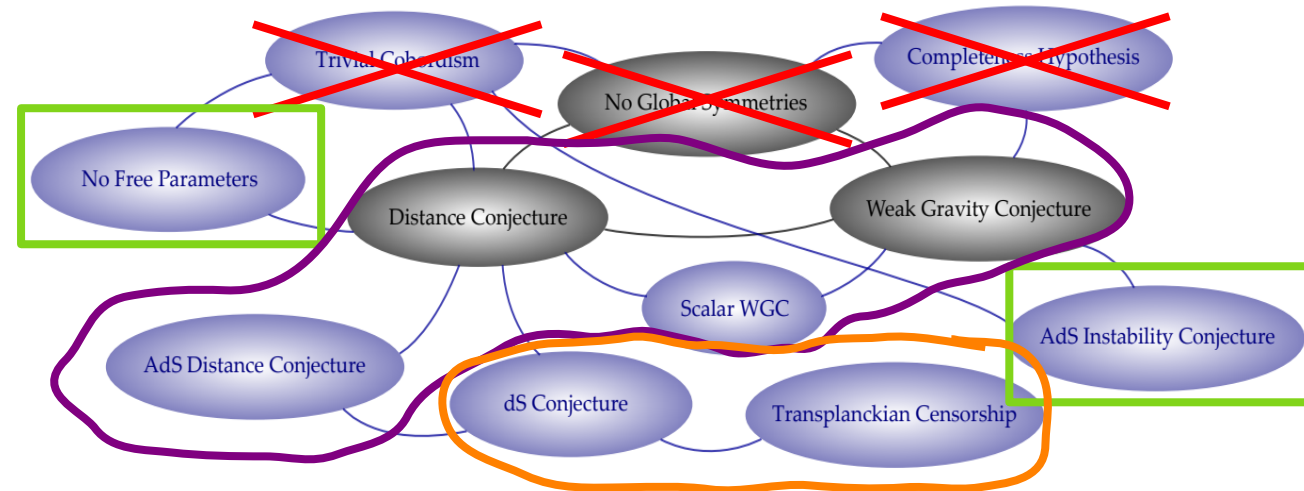


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Distance conditions

Boundary conditions

Potential conditions

$$\partial_\phi V/V > 1$$

## *Simplified* SWAMPLAND

- Field shall not move too much

$$\Delta\phi < \frac{1}{\lambda} \ln \left( \frac{1}{M} \right) \sim \mathcal{O}(1)$$

- Potential should be curved enough

or  $\partial_\phi V/V \gtrsim \mathcal{O}(1)$

$-\partial_\phi^2 V/V \gtrsim \mathcal{O}(1)$



Contested!

# *Simplified* INFLATION

- Slow roll requires  $\partial_\phi V \ll V$
- Long inflation + slow roll requires  $\partial_\phi^2 V \ll V$   
 $|\Delta\phi| \gg 1$

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- Long inflation + slow roll requires  $\partial_\phi^2 V \ll V$   
 $|\Delta\phi| \gg 1$

⇒ Obviously in tension!

$\Delta\phi \lesssim \mathcal{O}(1)$
$\partial_\phi V/V \gtrsim \mathcal{O}(1)$ or $-\partial_\phi^2 V/V \gtrsim \mathcal{O}(1)$

(single-field slow-roll is incompatible)



# WHAT GIVES?

- Swampland:
  - Wrong conjectures
  - Wrong application of conjectures to EFT
- Inflation:
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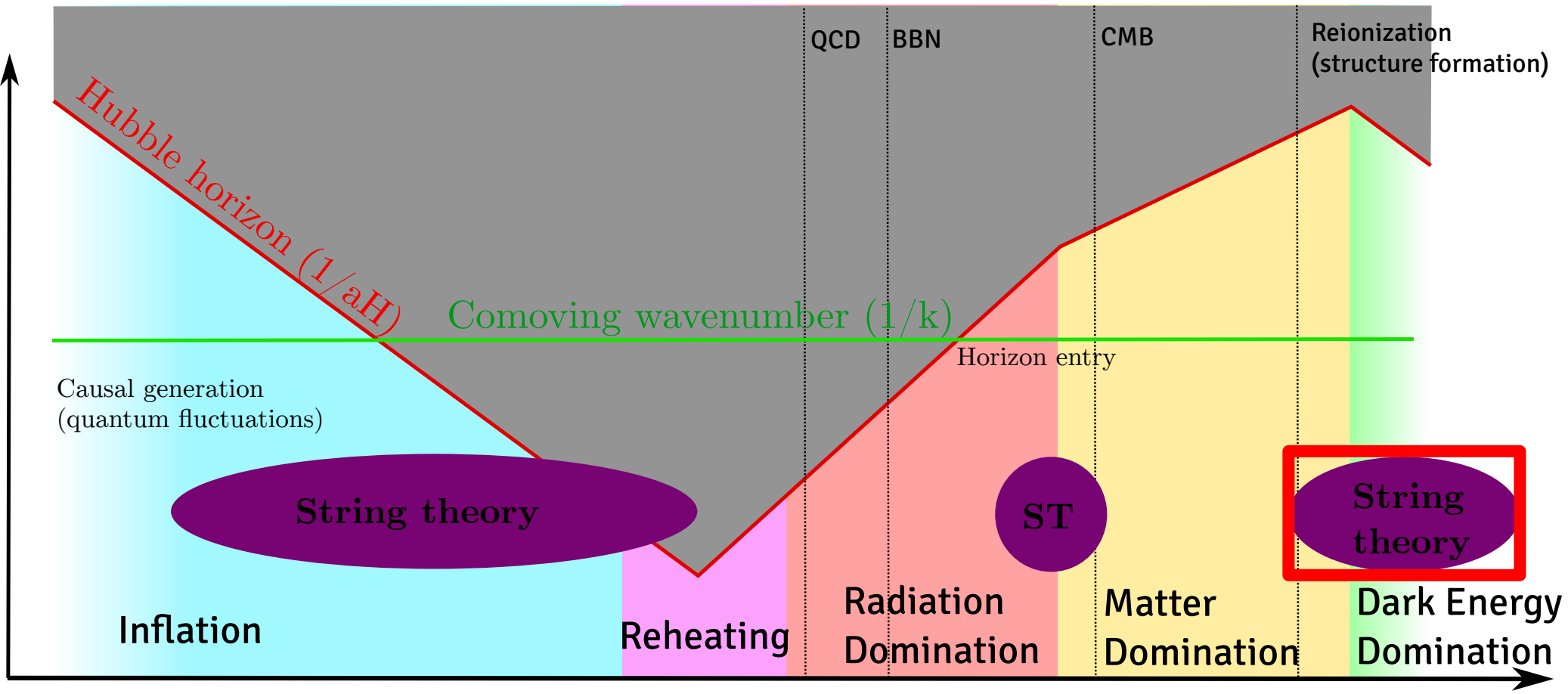
$$\ddot{\phi} + 3H(1 + Q)\dot{\phi} + \partial_{\phi}V = 0$$

e.g. warm  
inflation:  
Dissipative  
equation of  
motion

Multifield, warm, eternal, natural/Starobinsky, modified gravity, ...

1807.04390,	1809.03962,	1807.11938,	1810.06532,	1902.02849,	1809.01277,
1807.05193,	1108.2166,	1811.11698,	2101.08882	1902.03939,	1810.04001,
1807.09698,	1910.06796,	1907.08943,		1905.05654,	2106.03578,
1808.01615,	1911.00323,	1912.00749,		1910.11676,	2002.02941
2204.13794...	2001.10042,			2105.11935,	
	2002.04925,			2108.01448,	
	2101.00638,			2111.15477,	
	2209.06153			2207.09793	

# OUR COSMIC HISTORY (SO FAR)



# STRING THEORY AND DARK ENERGY

- No constants/no free parameter
  - no cosmological constant!
- We need dynamical dark energy!
  - Can we realize it?

⇒ Quintessence

# NEWS FROM THE SWAMPLAND

- **Nils Schöneberg**
- **Léo Vacher**
- **J. D. F. Dias**
- **Martim M. C. D. Carvalho**
- **C. J. A. P. Martins**

**Leo Vacher**



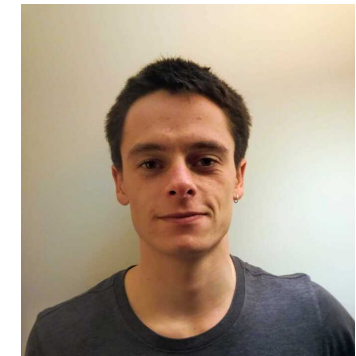
**Carlos Martins**



**João Dias**



**Martim Carvalho**



# QUINTESSENCE 101

- Scalar field Dark Energy

$$\ddot{\phi} + 3H\dot{\phi} + \partial_{\phi}V = 0$$

$$\delta\ddot{\phi} + 3H\delta\dot{\phi} + \dot{h}\dot{\phi}/2 + [k^2/a^2 + \partial_{\phi}^2V]\delta\phi = 0$$

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$$\ddot{a} = -\frac{1}{2}aH^2(1 + 3w_{\text{eff}}) > 0$$

$$w_{\text{eff}} = f_{\phi}w_{\phi} + (1 - f_{\phi})w_{\text{rest}} \approx f_{\phi}w_{\phi} < -\frac{1}{3}$$

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$$\frac{1}{2}\dot{\phi}^2 < V$$

Similar to SR, but less restrictive



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Dynamical system analysis  
(is it at all possible?)

$$x = \frac{\dot{\phi}}{\sqrt{6}H}$$

$$y = \frac{\sqrt{V}}{\sqrt{3}H}$$

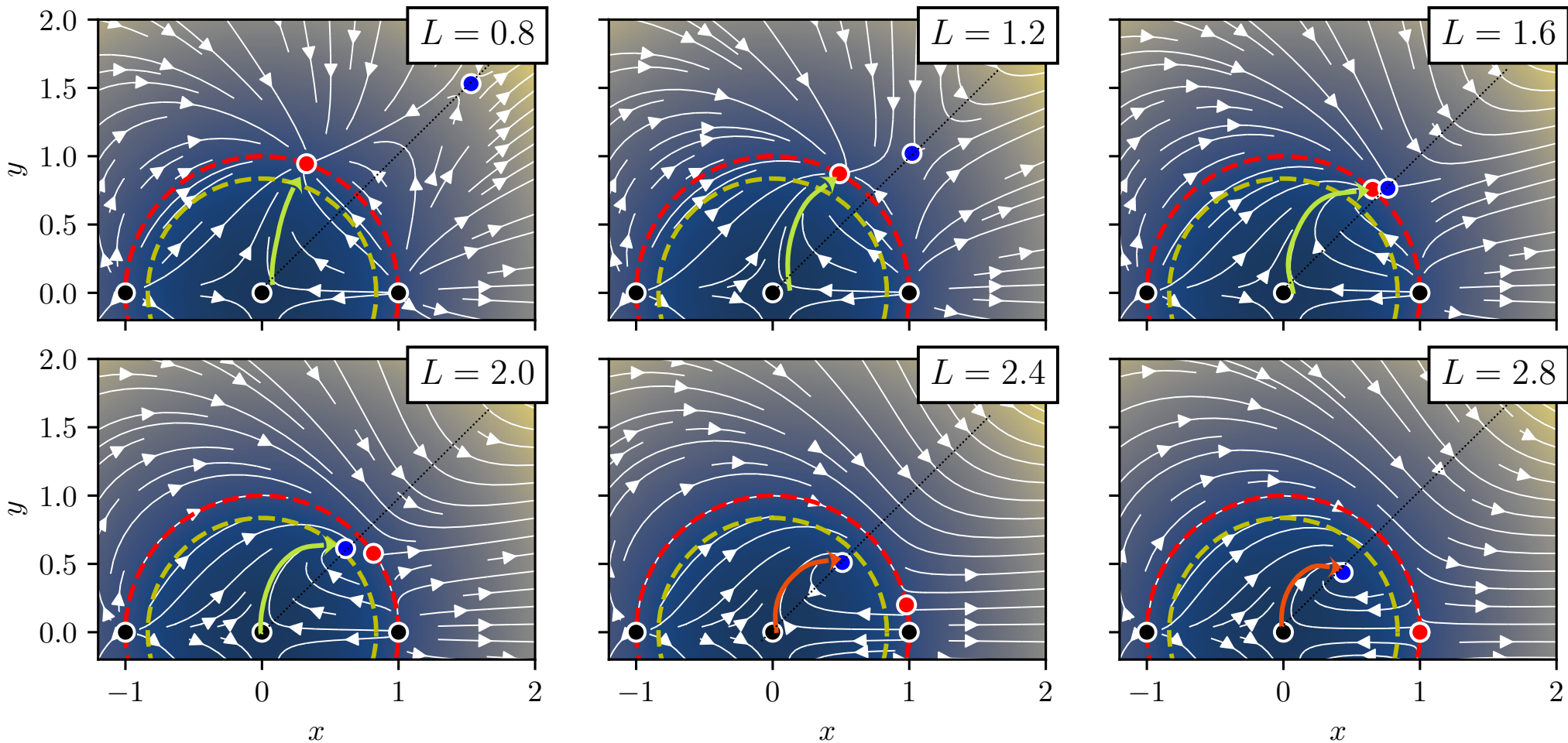
$$f_{\phi} = x^2 + y^2$$

$$\partial_{\ln a} x = -3x + \frac{\sqrt{6}}{2}Ly^2 - x \frac{d \ln H}{d \ln a}$$

$$\partial_{\ln a} y = -\frac{\sqrt{6}}{2}Lxy - y \frac{d \ln H}{d \ln a}$$

$$L = -\partial_{\phi}V/V$$

## DYNAMICAL SYSTEM ANALYSIS



Red circle = dark energy domination

Yellow circle = current observed accel.

Points = critical points

# DYNAMICAL SYSTEM ANALYSIS

- Location of blue attractor:

$$x^2 + y^2 = 3/L^2 \stackrel{!}{=} (1 - \Omega_m) \approx 0.7$$

- Corresponding bound on potential:

$$L = -\partial_\phi V/V \leq 2.1$$

BUT: No need to last long, so maybe

$$\begin{array}{l} |\Delta\phi| \ll 1 \\ -\partial_\phi^2 V \gg V \end{array}$$

are fine

# QUINTESSENCE AND SWAMPLAND

- The equation for  $L$ :

$$\frac{dL}{d \ln a} = \sqrt{6}x(L^2 + g)$$

$$g = -\partial_\phi^2 V/V$$

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$\Rightarrow$  For large  $g$ , we have strong acceleration of  $L$   
(either positive or negative) 

$$\Delta\phi = \int \frac{d\phi}{dt} dt = \sqrt{6} \int x d \ln a \sim 1.2 \Delta \ln a \sim 0.3 \quad \checkmark$$

$x \sim 0.5$

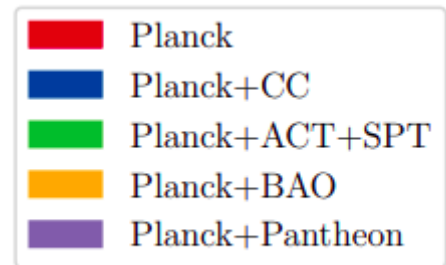
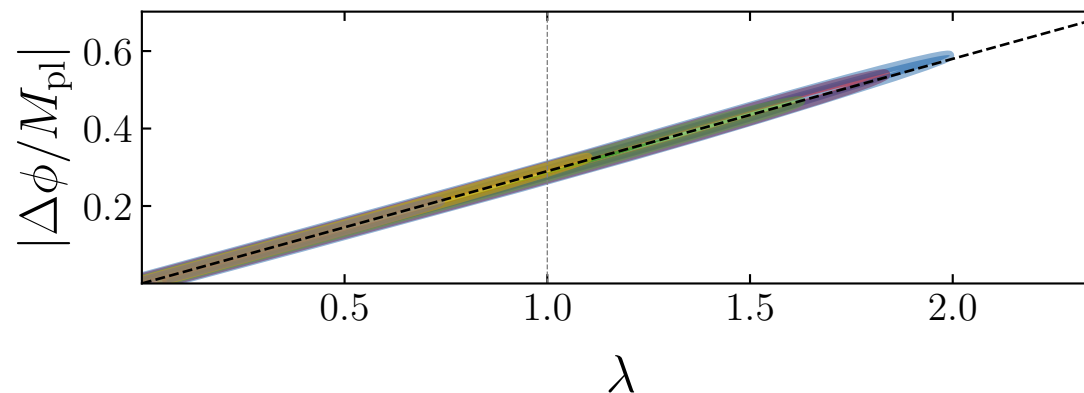
# FROM THEORY TO PRACTICE

- Let's investigate a few models and see what's happening!

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Good news: SDC doesn't seem to be an issue!  
(in any cases)

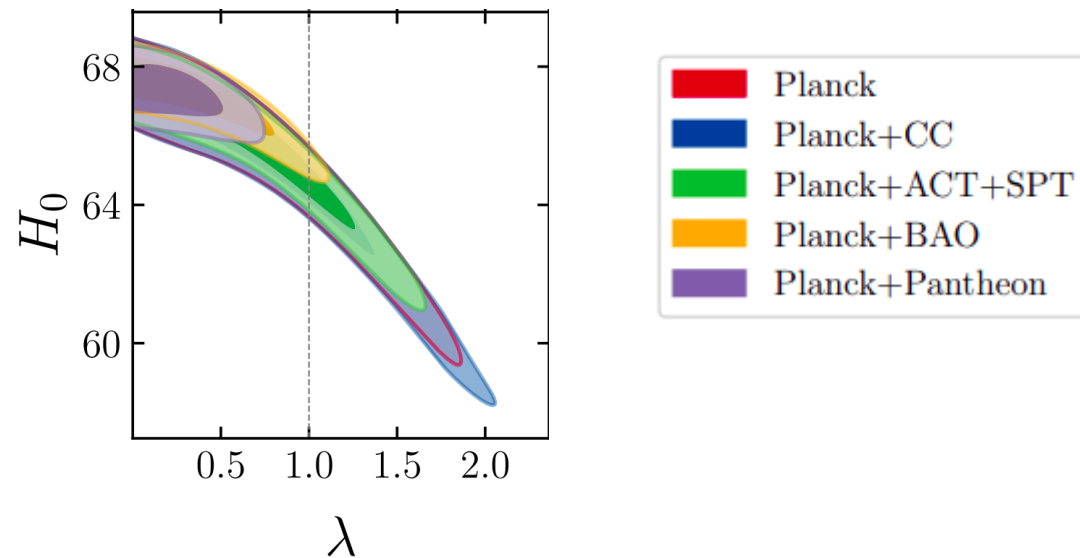




# FROM THEORY TO PRACTICE

- Exponential:

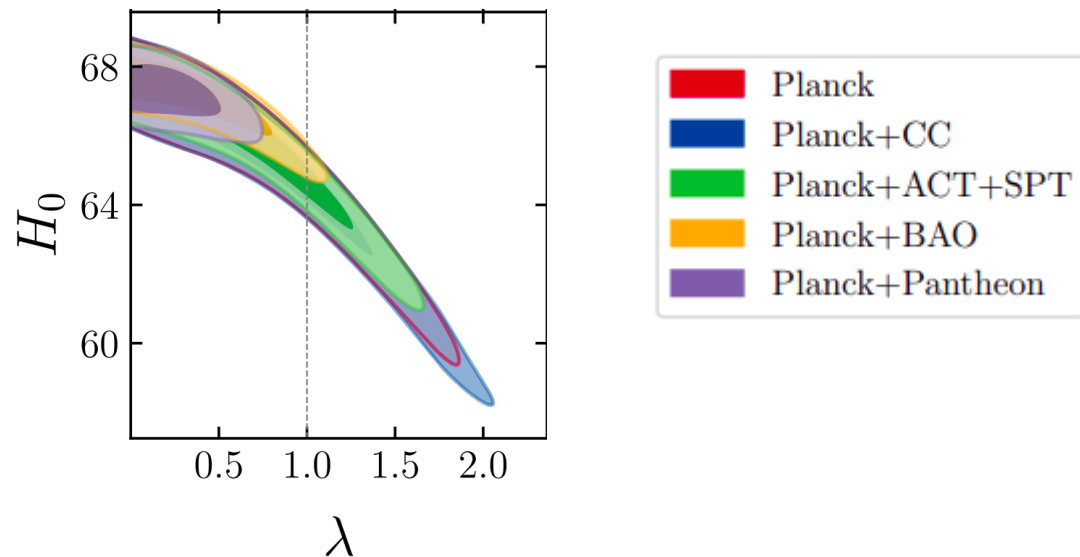
$$V(\phi) = V_0 \exp(-\lambda\phi)$$



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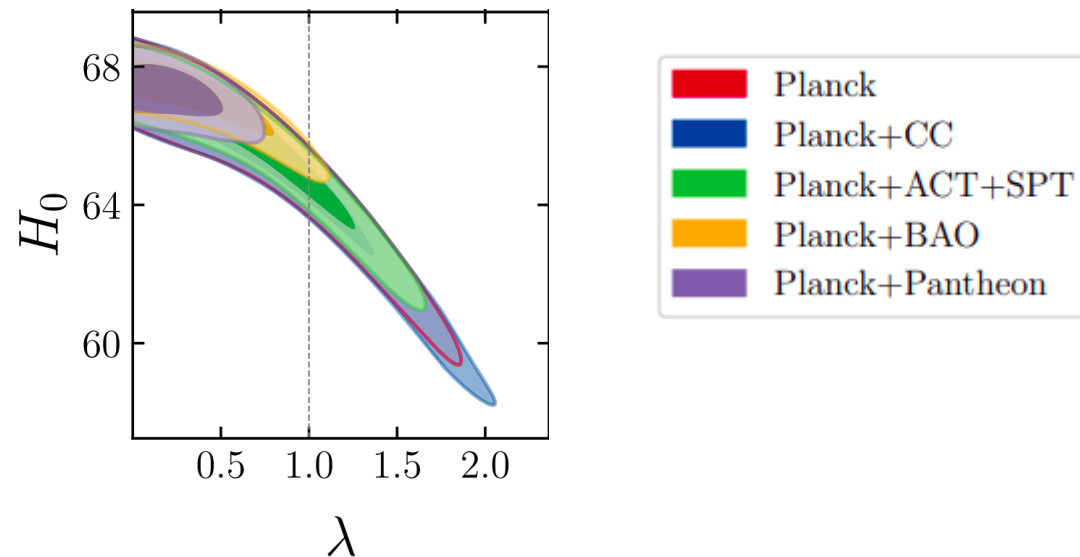


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$$P(\lambda > 1) \approx \begin{cases} 24\% & \text{Planck} \\ 0.24\% & \text{Planck + Pantheon+} \\ < 0.001\% & \text{Planck + Pantheon} \\ < 0.001\% & \text{Planck+H}_0 \end{cases}$$

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$$V(\phi) = A \cos(c\phi) \quad -\partial_\phi^2 V/V = c^2 \gg 1$$

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We even get for free:  $|\partial_\phi V/V| = c \tanh(c\phi) \rightarrow \infty$  for  $c\phi \rightarrow \frac{\pi}{2}$

# FROM THEORY TO PRACTICE

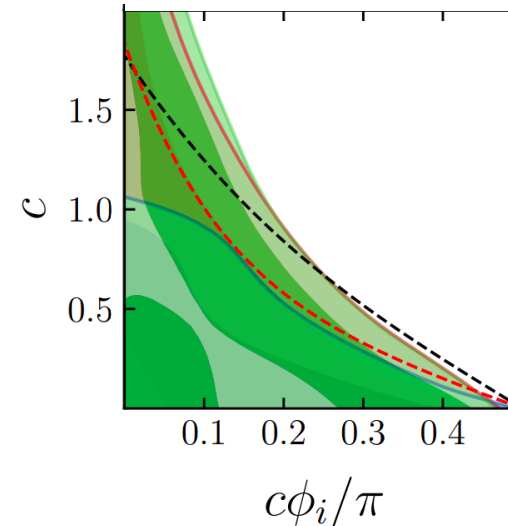
- Cosine potential:

$$V(\phi) = A \cos(c\phi)$$

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$$|\partial_\phi V/V| = c \tan(c\phi) \rightarrow \infty \quad \text{for} \quad c\phi \rightarrow \frac{\pi}{2}$$

- Conclusions:



# FROM THEORY TO PRACTICE

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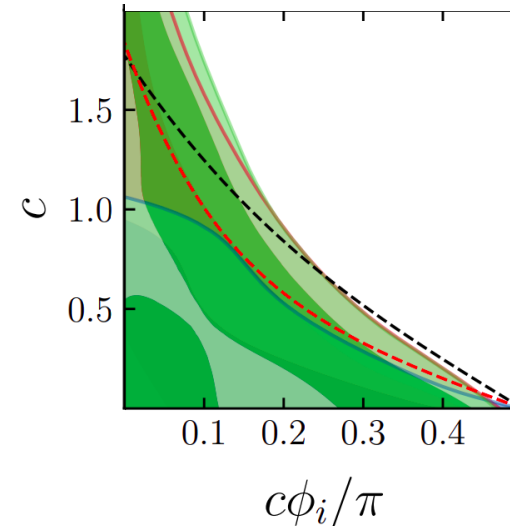
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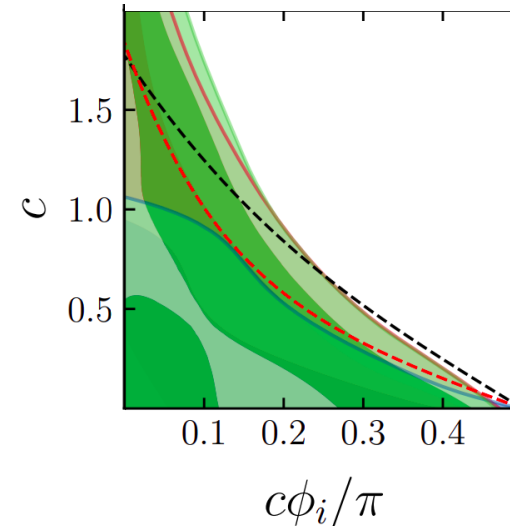
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- Conclusions:

- $c > 1$  is possible! (though disfavored by large  $H_0$ )
- The limit of  $c\phi \rightarrow \frac{\pi}{2}$  is not really reached



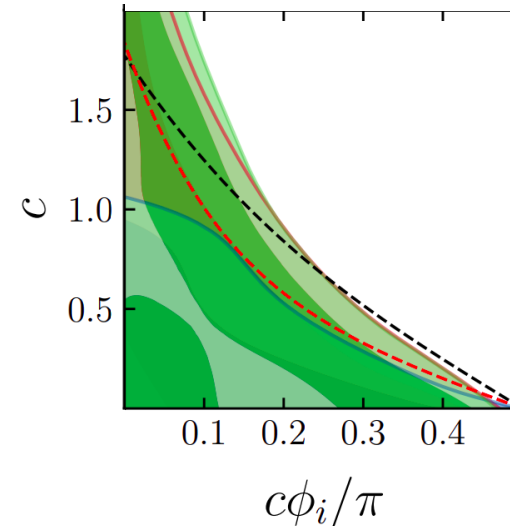
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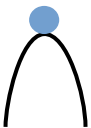
$$V(\phi) = A \cos(c\phi)$$

$$-\partial_\phi^2 V/V = c^2 \gg 1$$

$$|\partial_\phi V/V| = c \tan(c\phi) \rightarrow \infty \quad \text{for} \quad c\phi \rightarrow \frac{\pi}{2}$$

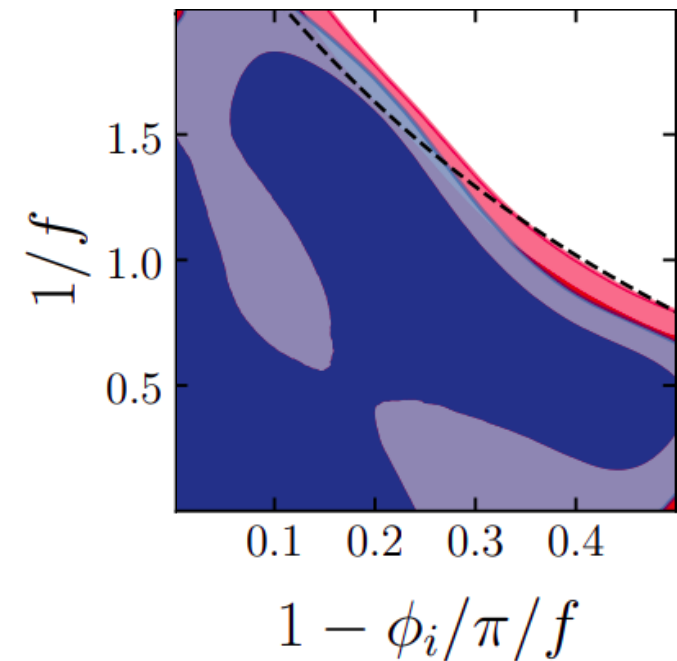


- Conclusions:

- $c > 1$  is possible! (though disfavored by large  $H_0$ )
- The limit of  $c\phi \rightarrow \frac{\pi}{2}$  is not really reached
- Fine tuning  (but only very mildly!)

# OTHER POSSIBILITIES

- Axionic potential  $V(\phi) = m^2 f^2 [1 - \cos(\phi/f)]$ 
  - Similar to cosine potential, just more permissive



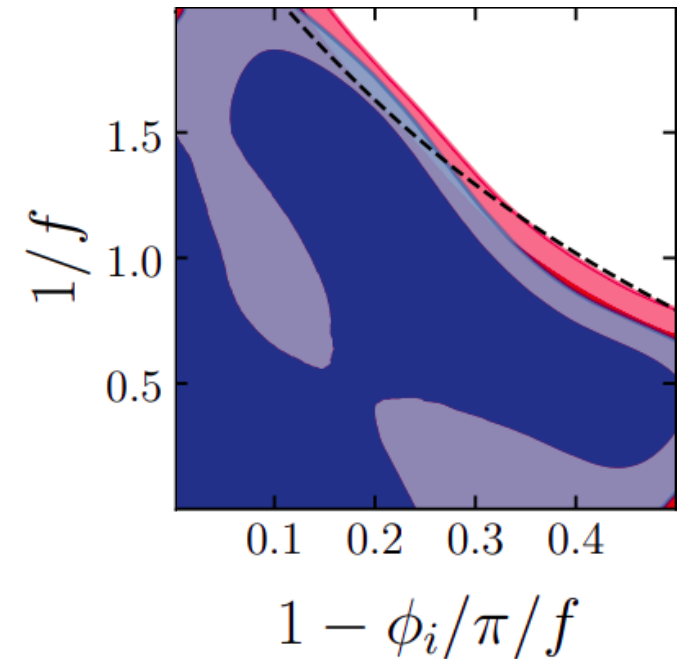
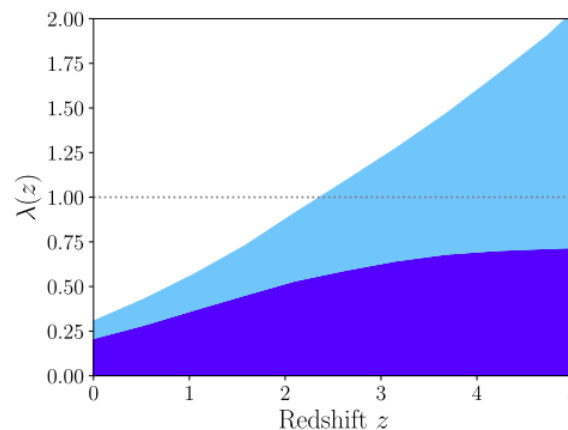
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- Inverse exponential

$$V(\phi) = A \exp(\sigma/\phi)$$

- Not great

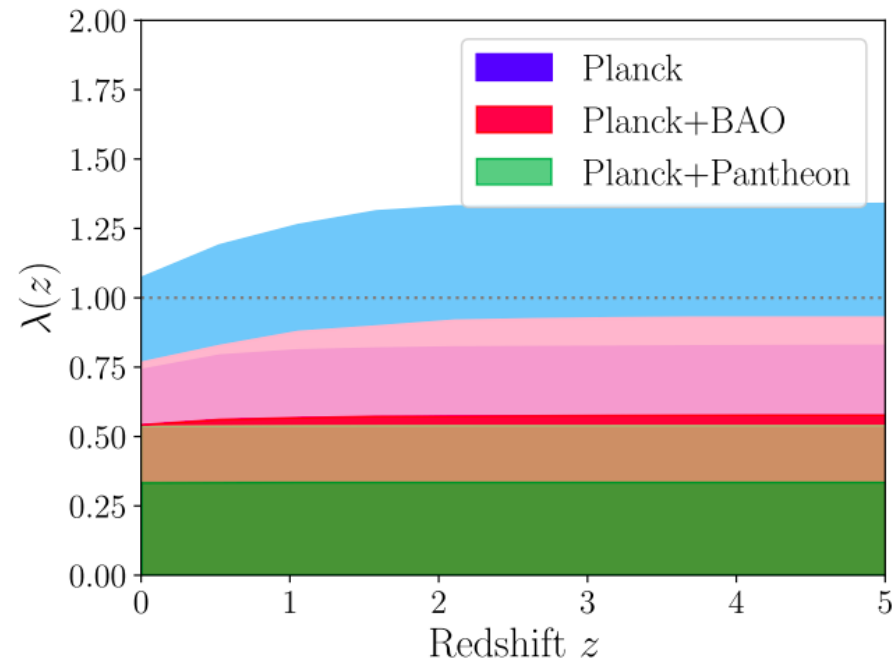


# OTHER POSSIBILITIES

- Double exponential:

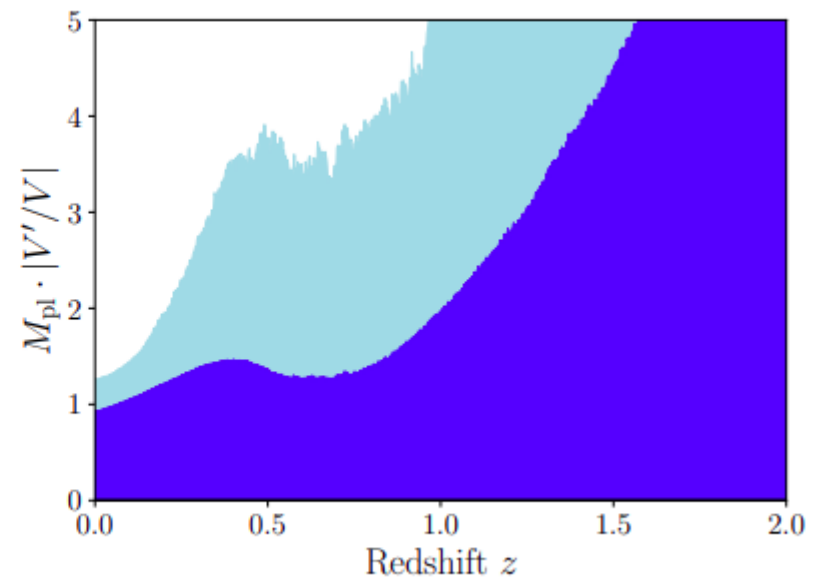
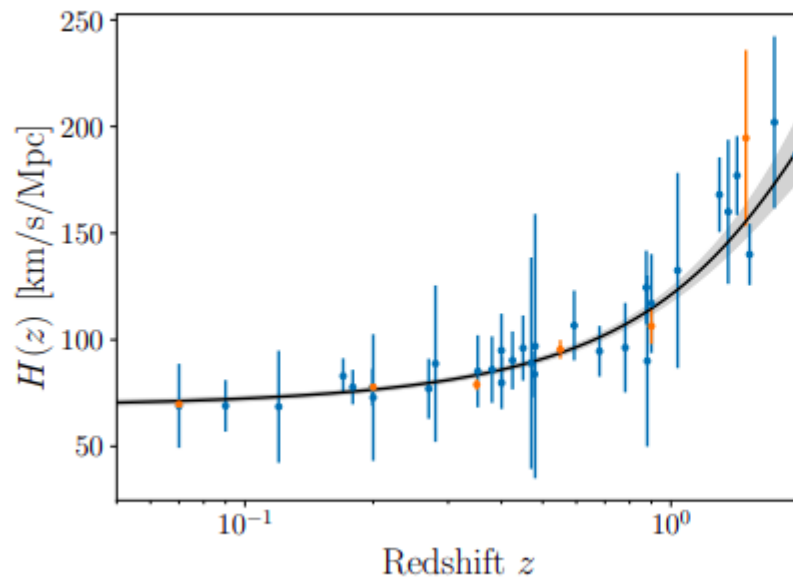
$$V(\phi) = A[\exp(\lambda\phi) + r \exp(\kappa\phi)]$$

- Basically  
the same as  
exponential case



# CAN WE DO BETTER?


- Model-independent construction, right?!  
(e.g. cosmic chronometers + BAO)



# DEVIL IN THE DETAIL

- Have to convert

Data  $\rightarrow H(z) \rightarrow H(z), H'(z) \rightarrow \rho_\phi, d\rho_\phi/dz \rightarrow \dot{\phi}, V(z) \rightarrow V, \partial_\phi V \rightarrow \lambda = |\partial_\phi V/V|$



Except for CC,  
The data  
require other  
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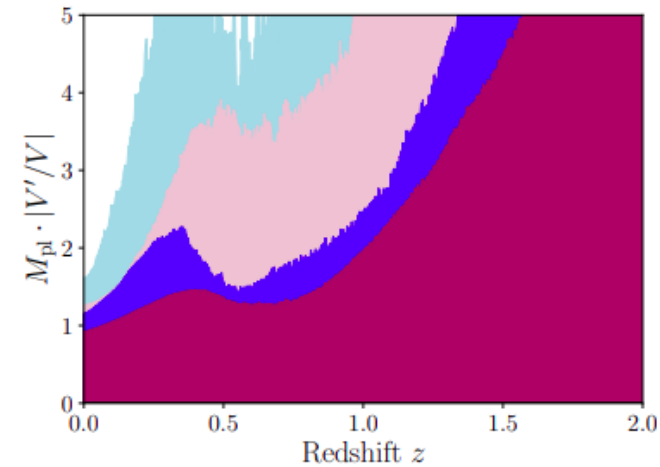
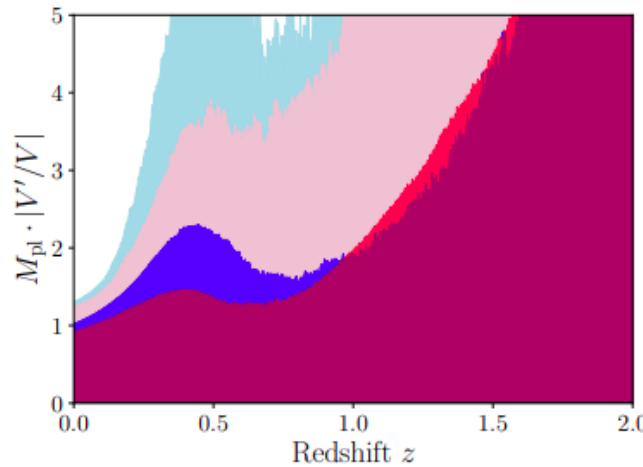
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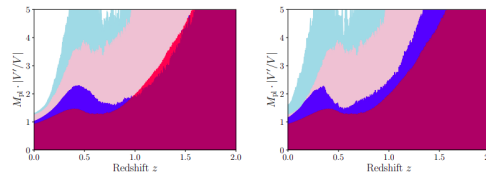
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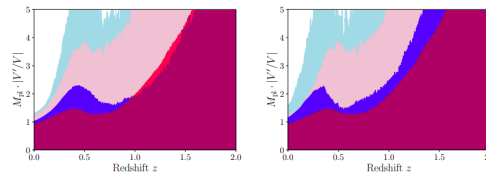
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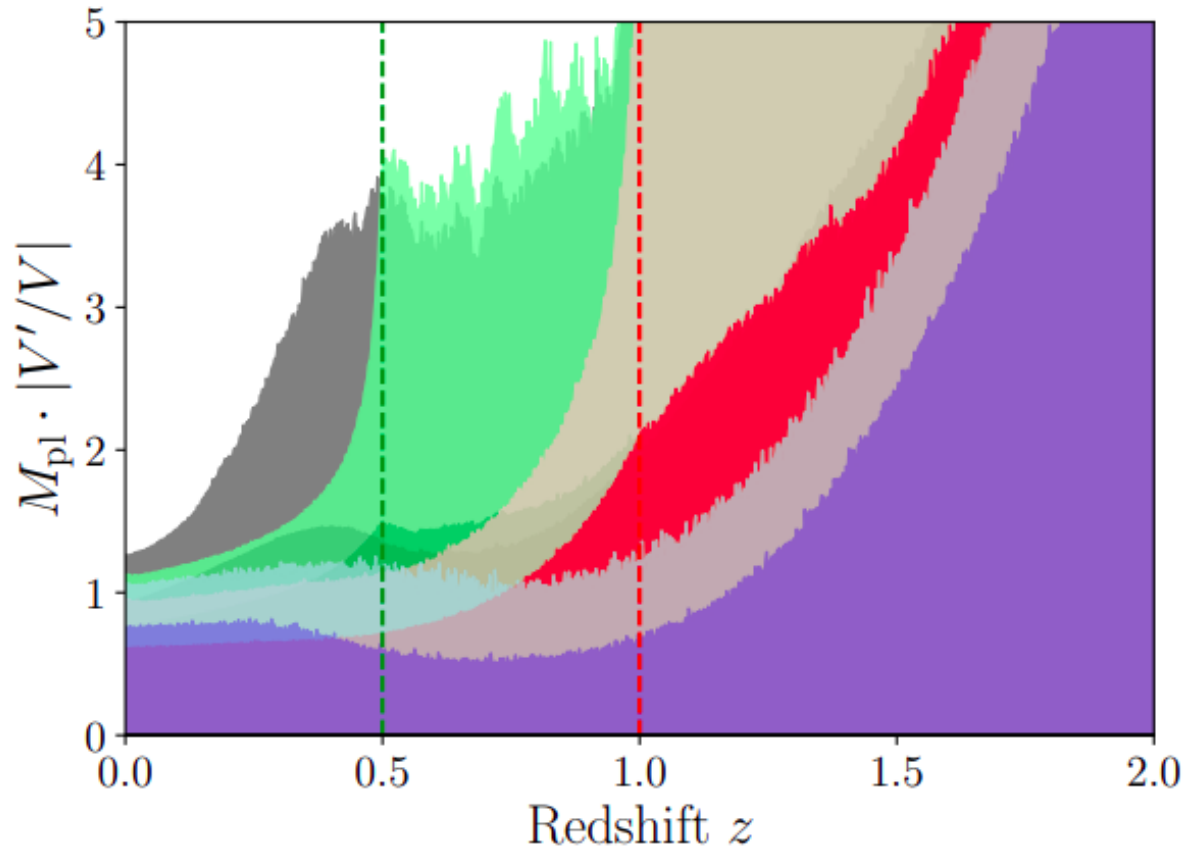
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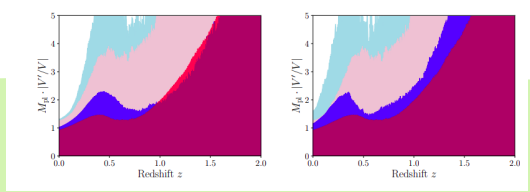


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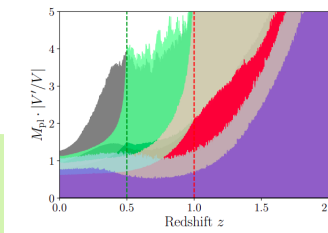
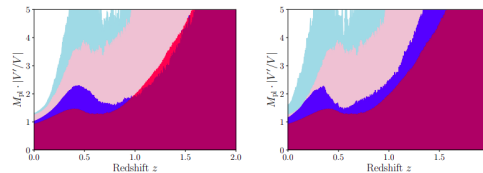
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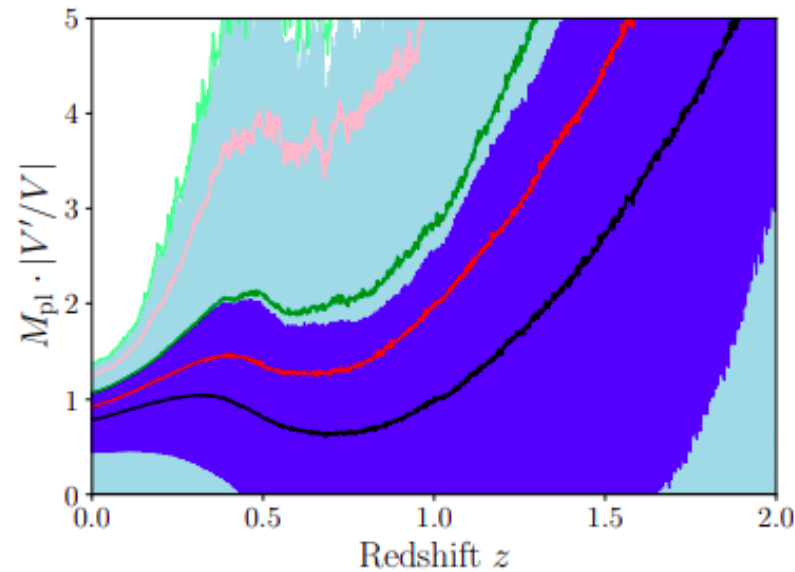
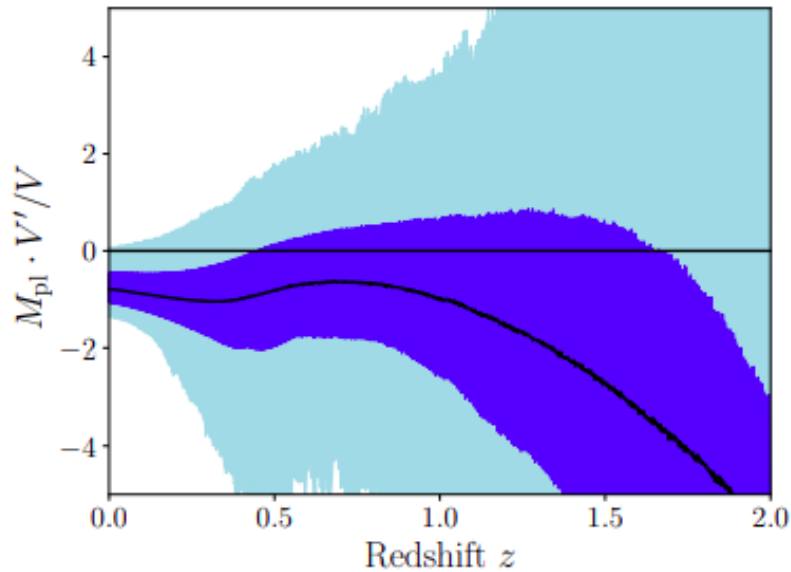
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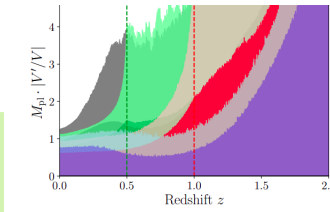
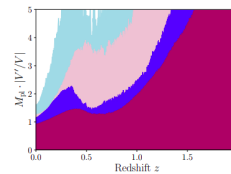
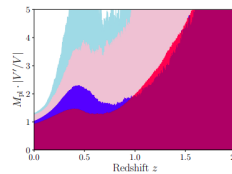
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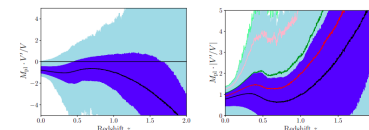
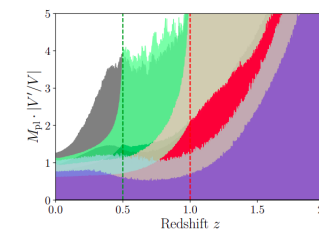
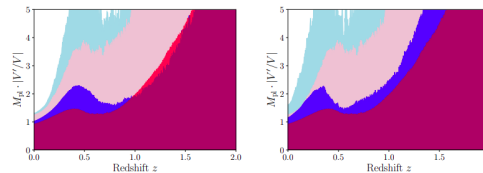
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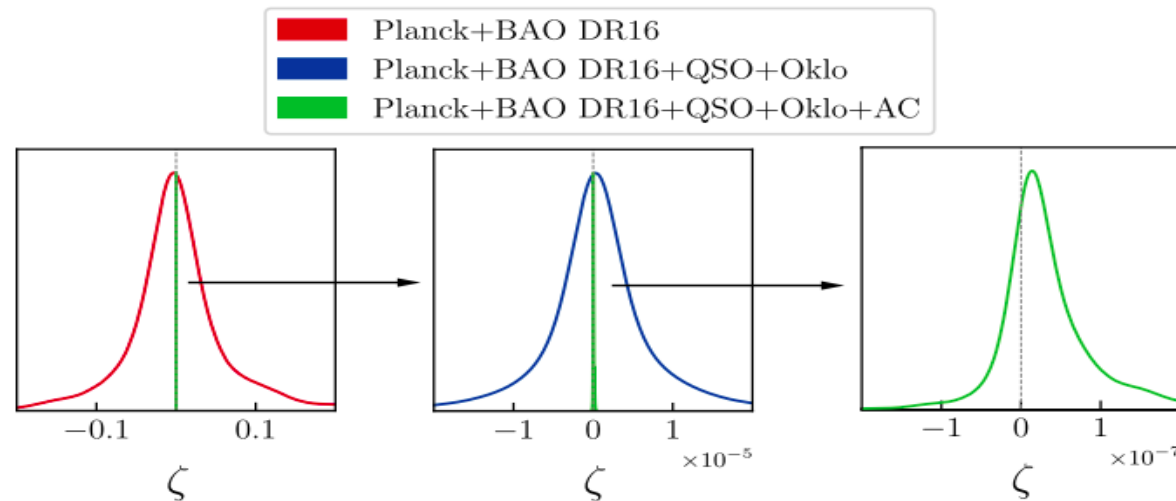
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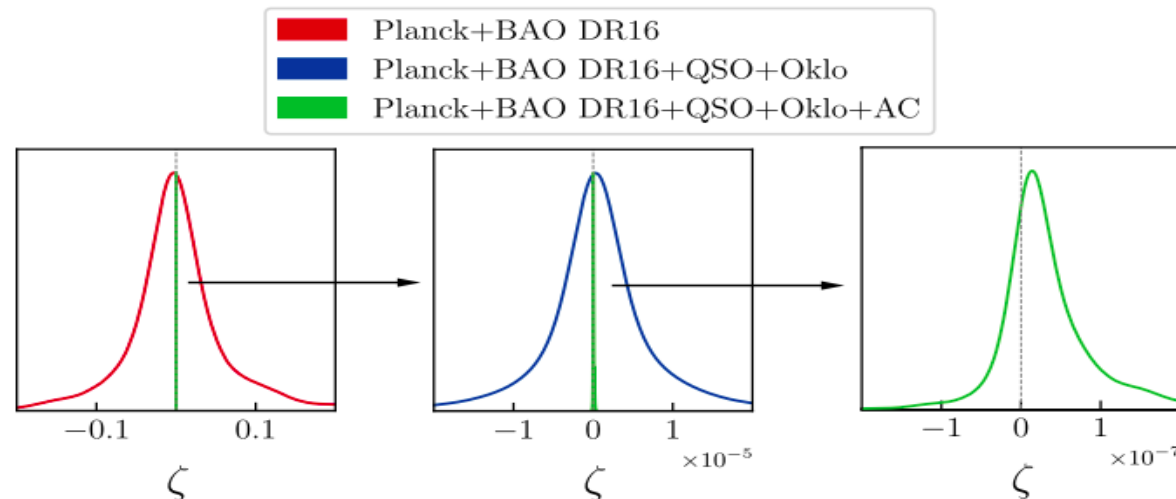
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As such, almost any natural order coupling of the quintessence with electromagnetic fields expected from most unified theories has to face either the large hurdle of constructing a theoretical reason to effectively forbid such a coupling or has to face problems of extreme fine-tuning.

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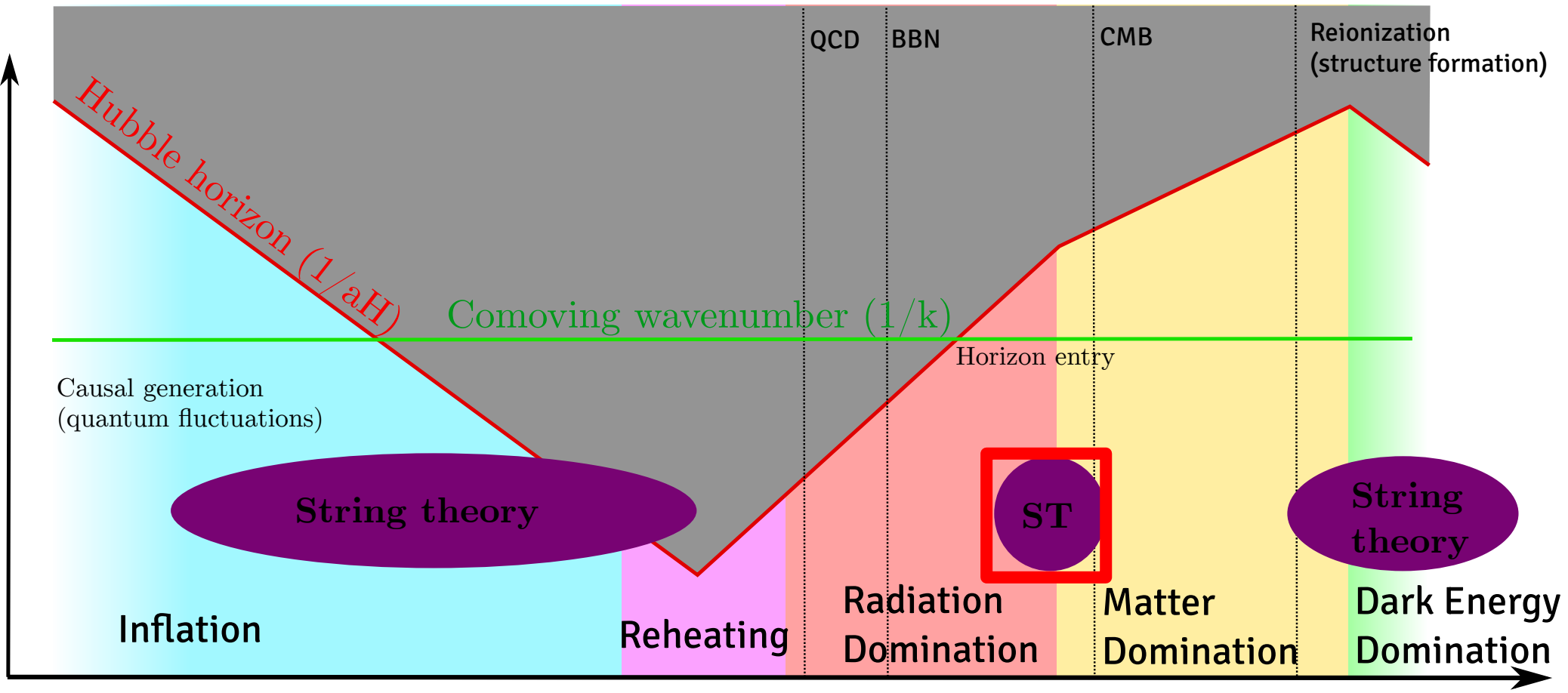
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- Be careful about model-independent reconstructions



# OUR COSMIC HISTORY (SO FAR)



# THINGS I DID NOT TOUCH UPON

- Hubble tension in cosmology:
  - Local data measuring high  $H_0 \sim 73\text{km/s/Mpc}$
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- Model solutions involve recombination-time dynamics
  - Early dark energy can be motivated with a string-motivated axionic potential

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  - modified inflationary models can come to the rescue
- Dynamical dark energy is in peril from swampland criteria
  - currently no better solution than to put DE on an unstable maximum