

Master 2 Internship Oral Presentation

# Development of Monte Carlo tool for Radiation Protection

Under the supervision of  
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20/06/2024



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# I. Introduction



# I. Introduction : Context and Smartium work

Need for **radionuclide** in **medical sector** (production, **manipulation** and storage)



Laboratory front panel [1]

*Lead wall*

*Working stations*

*Measurement system*



Spin-off from IPHC's works  
Created in 2021

**Develops numerical solutions for radiation protection and nuclear measurements**

# I. Introduction : Context and Smartium work

Need for **radionuclide** in **medical sector** (production, **manipulation** and storage)



*Lead wall*

*Working stations*

*Measurement system*

*Laboratory front panel [1]*

Smartium work using **MC simulations**:

- 1) **Relationship** between **probe** and **staff** exposition to define warning threshold.
- 2) Radiological **exposure** as a function of the **position** for better probe placement.

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Need for **radionuclide** in **medical sector** (production, **manipulation** and storage)



Laboratory front panel [1]

Lead wall

Working stations

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Smartium work using **MC simulations**:

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Internship targets :

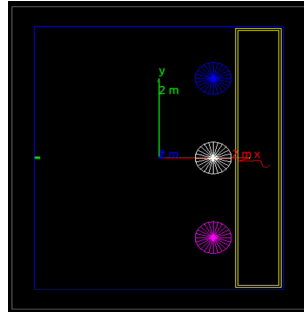
Make a **MC simulation** of a **laboratory front panel**

Find and implement **Variance Reduction Techniques** (VRTs) to **reduce as much as possible** the computation **time** while **limiting the impact** on the **result**

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# II. Materials & Methods



$$x = \bar{x} \pm \sigma_x$$

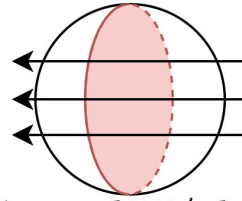
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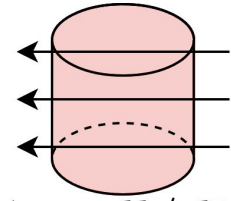
## II. Materials & Methods : Dosimetric quantities

**Physical quantities**  
Measurable

- Fluence (part.m<sup>-2</sup>)



$$\phi = dN/dA$$



$$\phi \approx dl/dV$$

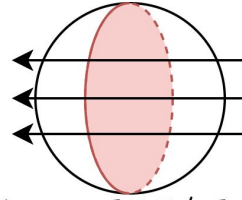
- Absorbed dose (J/Kg or Gy) :  $dE/dm$



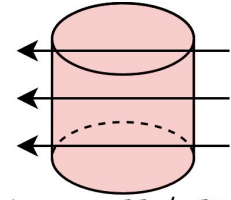
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**Protective quantities**  
Not measurable

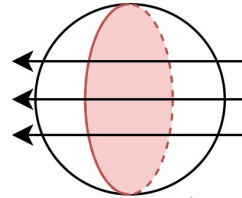
- Equivalent dose for an organ T (Sv) :  $H_T = D_{T,R}W_R$   
Takes into account the effect of a given radiation on tissues.

- Effective dose for the body (Sv) :  $E = \sum H_T W_T$   
Takes into account the organs sensibilities

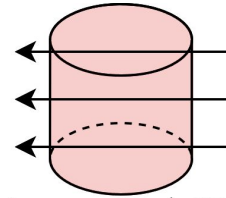
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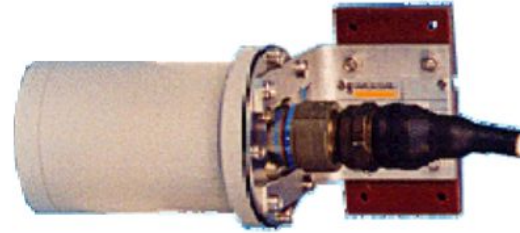
Protective quantities are not measurable : Introduce **operational quantities**  
Measurable **approximations** of protective quantities

## II. Materials & Methods : Dosimetric quantities

**Operational quantity** : Measurable approximations of protective quantities  
Use for calibration of measurement system



*Personal dosimeter*



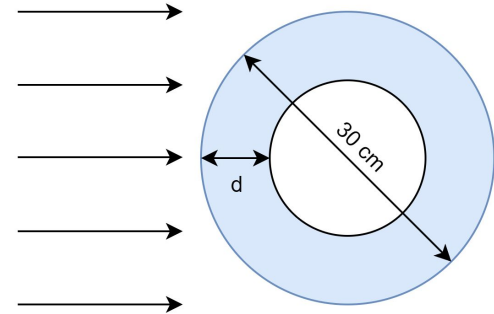
*Probe*

## II. Materials & Methods : Dosimetric quantities

**Operational quantity** : Measurable approximations of protective quantities

The ambient dose equivalent :  $H^*(d)$

Dose equivalent produced by radiation field  
in the ICRU sphere of density  $1 \text{ g/cm}^3$  at a depth  $d$ .



## II. Materials & Methods : Dosimetric quantities

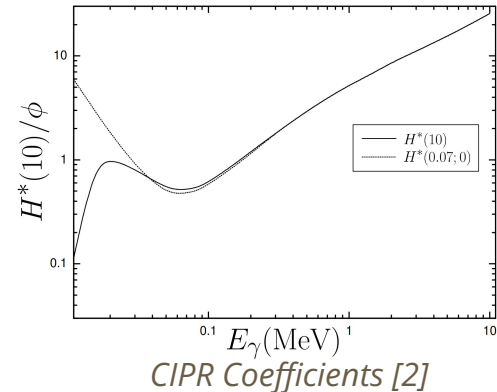
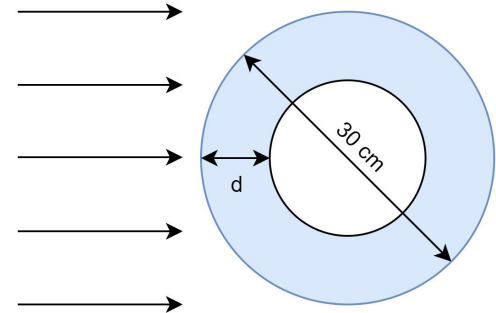
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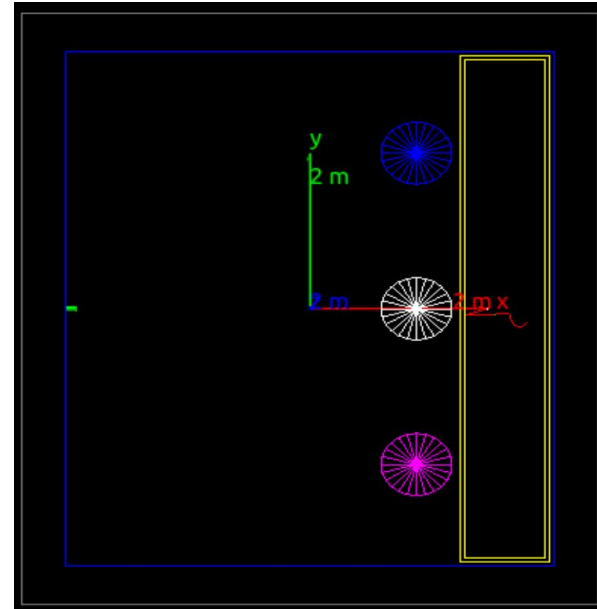
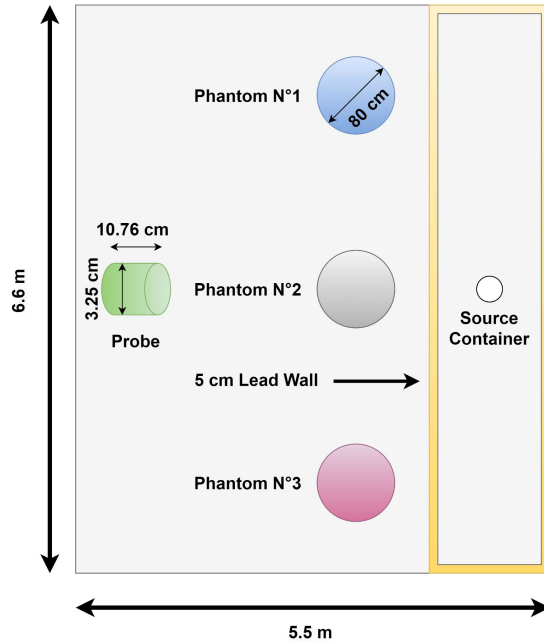
In this work we compute :

$$\dot{H}^*(10) = \dot{\phi} \sum_i CIPR_i I_i$$



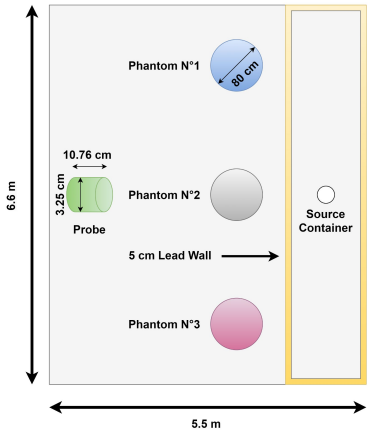
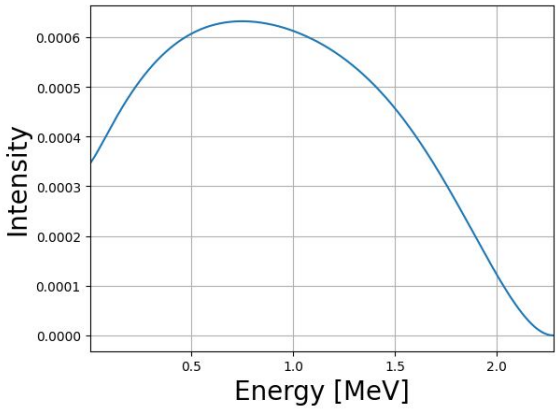
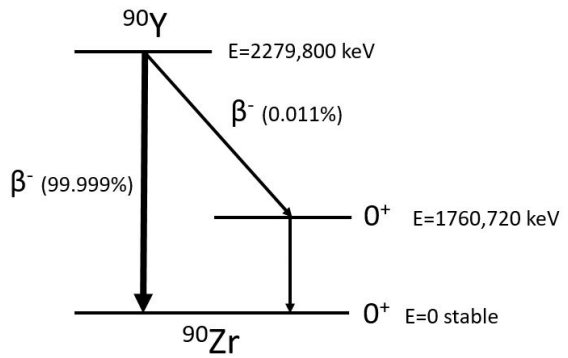
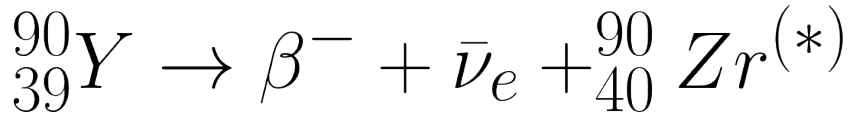
# II. Materials & Methods : Modeling of the laboratory

First work carried out : Learn the GATE software  
Modelisation of the laboratory



# II. Materials & Methods : Modeling of the laboratory

Source :  $^{90}\text{Y}$  of activity  $A = 1110 \text{ GBq}$



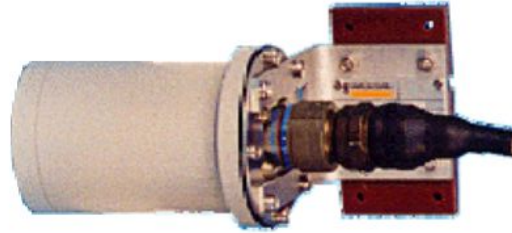
Decay scheme and spectrum data from [3]

$\beta^{-}$  slowed in lead wall  $\rightarrow$  **Bremsstrahlung photon irradiation**

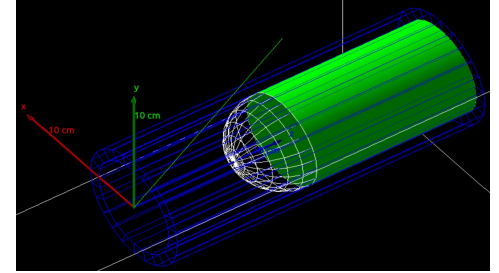
## II. Materials & Methods : Modeling of the laboratory

Probe:

- Cylindrical shape
- Aligned with phantom N°2 and source
- Silicon : semiconductor
- Detection range : [0.01  $\mu\text{Sv/h}$  ; 1000 Sv/h]



*SG/Si 11 probe*



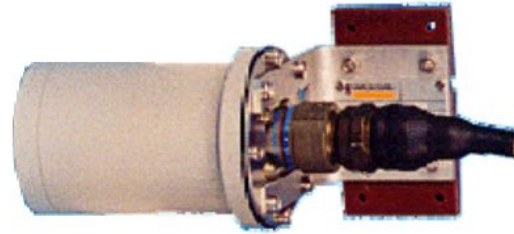
*Probe model*



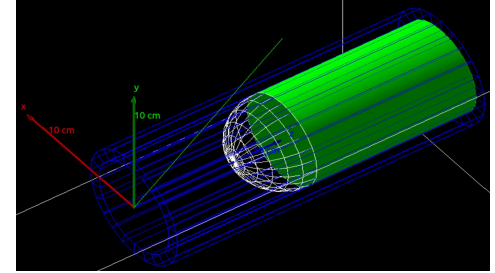
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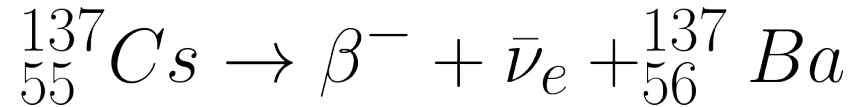


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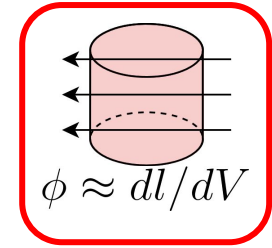
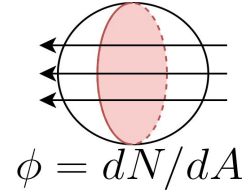
To **ensure** the **accuracy** of the probe Monte Carlo modeling : **comparison** with **experimental** data.



Relative error ~1.5%  
**Validation** of the modeling

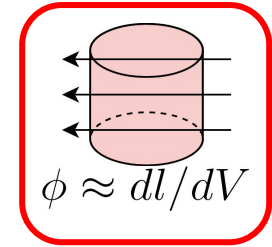
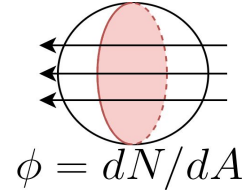
## II. Materials & Methods : Uncertainties calculations

Reminders : Compute  $H^*(10)$  for probe and staff  
Use the **fluence approximation**



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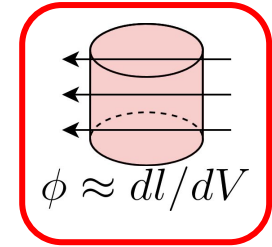
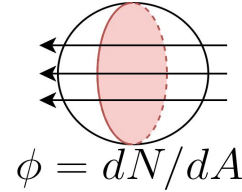


$$\frac{\sigma(\dot{H}^*(10))}{\dot{H}^*(10)} = \sqrt{\frac{\sum_i \sigma_{l_i}^2}{(\sum_i l_i)^2} + \frac{\sum_i (I_i^2 \sigma_{CIPR_i}^2 + CIPR_i^2 I_i)}{(\sum_i CIPR_i I_i)^2}} + \frac{1}{N_{\text{hit}}}$$

**Unknown term !/\**

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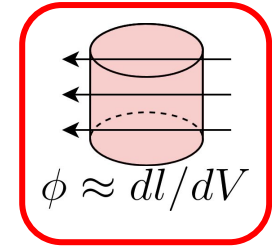
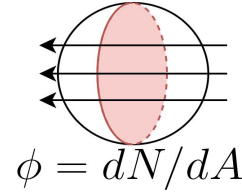
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1) **Compute** the relative uncertainty using the **classical definition**.

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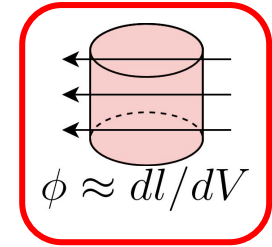
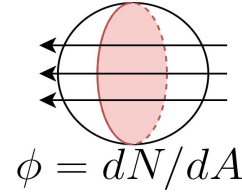
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- 1) **Compute** the relative uncertainty using the **classical definition**.
- 2) **Estimate** the standard deviation of the **approximation** with **several simulations**

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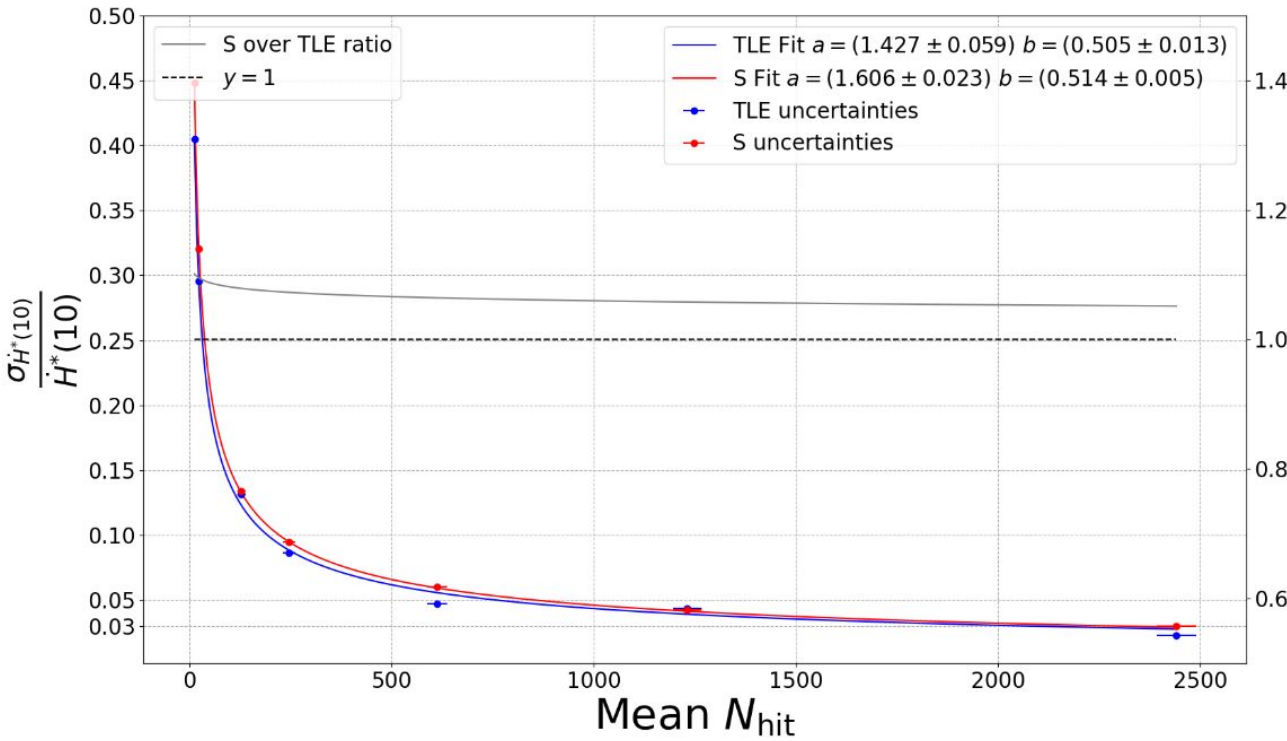


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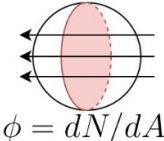
**Unknown term !/!**

- 1) **Compute** the relative uncertainty using the **classical definition**.
- 2) **Estimate** the standard deviation of the **approximation** with **several simulations**
- 3) **Compare** the standard deviation of the approximation to the computed relative uncertainty of the classical definition

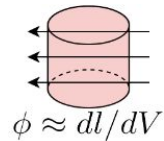
# II. Materials & Methods : Uncertainties calculations



**Red curve** : Surface method, computed.



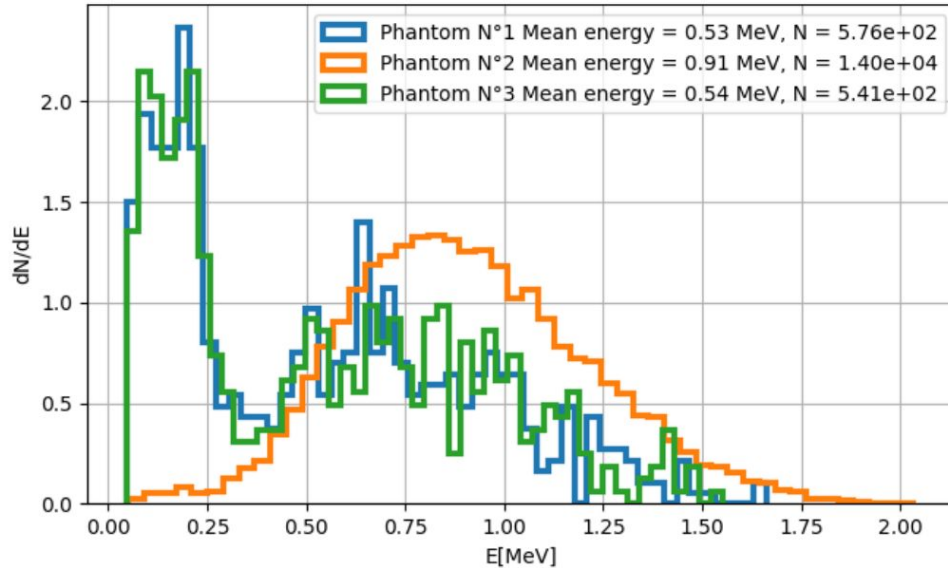
**Blue curve** : Lengths method, estimated with N simulations.



$$\frac{\sigma(\dot{H}^*(10))}{\dot{H}^*(10)} = \frac{a}{N_{hit}^b}$$

## II. Materials & Methods : Modeling of the laboratory

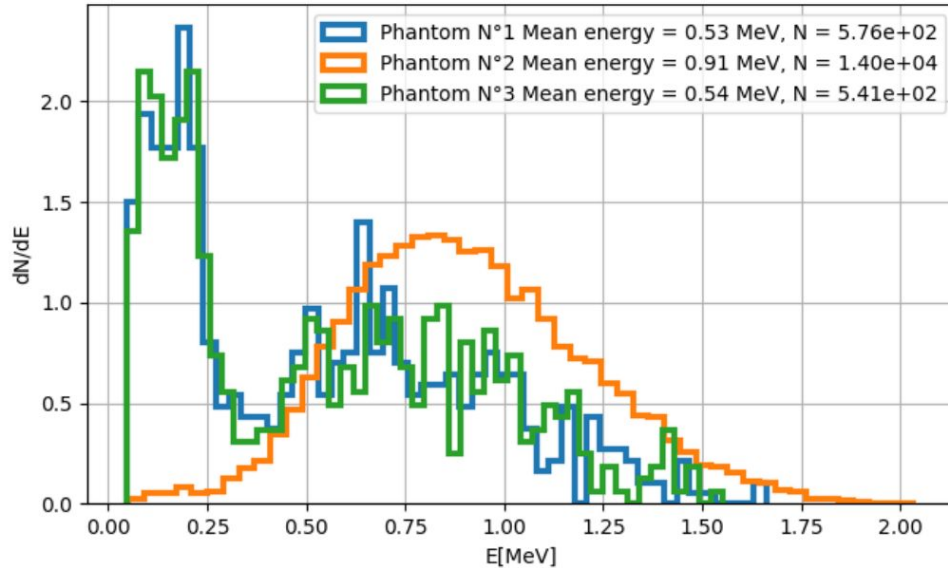
Simulation results :  $N_{\text{sim}} = 10^9$ ,  $\Delta T = 23 \text{ h } 35 \text{ min}$





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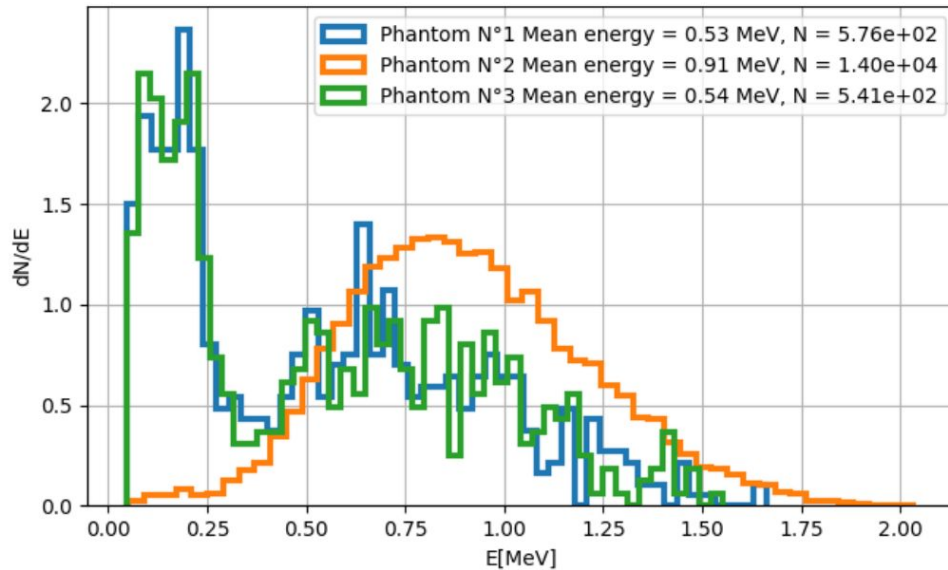


Phantom N°2 : ✓

$$\dot{H}^*(10) = (20.1 \pm 0.30) \mu\text{Sv/h}$$

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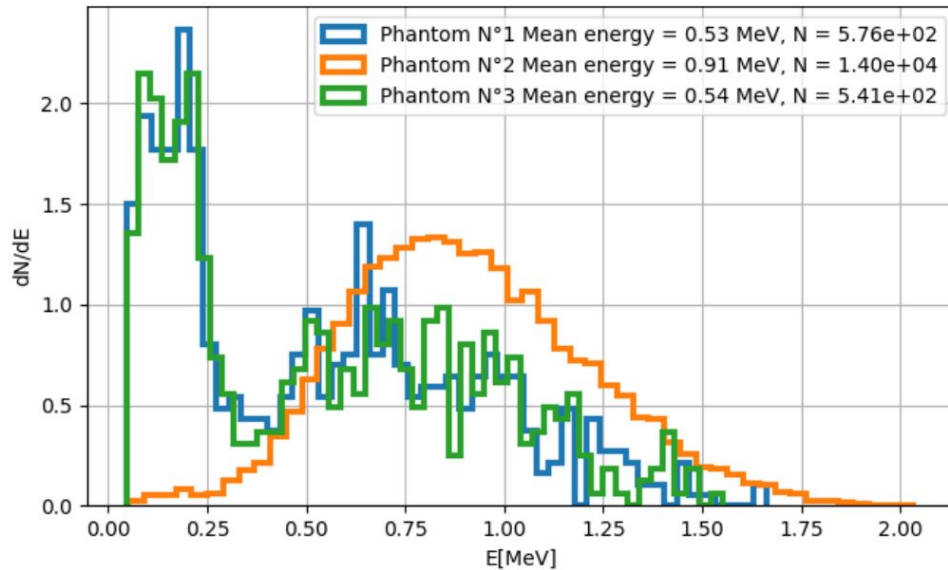
Probe :  
**Only 3 hit !** ✗

$$\dot{H}^*(10) = (1.89 \pm 1.97) 10^{-1} \mu\text{Sv/h}$$

**104% relative uncertainty for the probe : no reference value**

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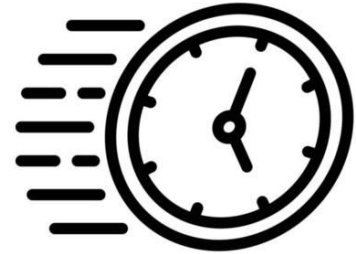
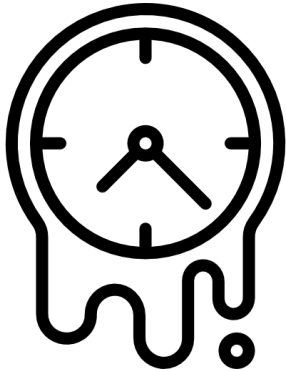
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To have **5% error on the probe** :  $9.65 \times 10^3$  hours or **1 year**, 1 month and 8 days  
/!\ Low  $N_{\text{hit}}$ , only an approximation /!\

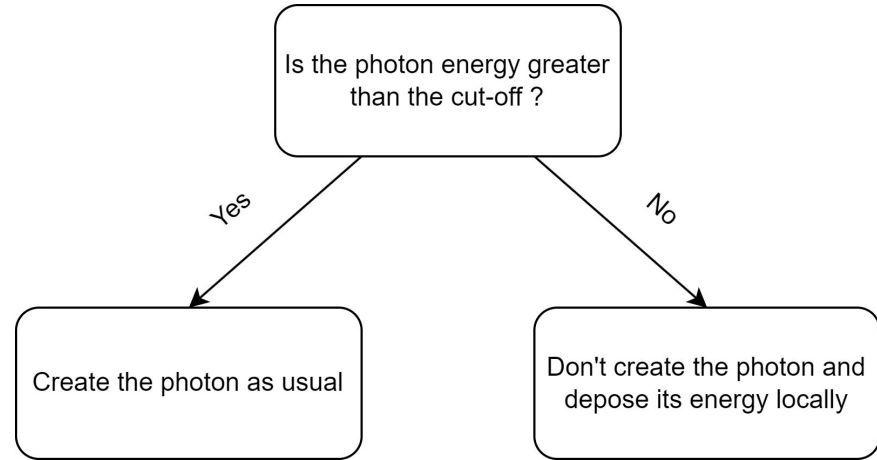
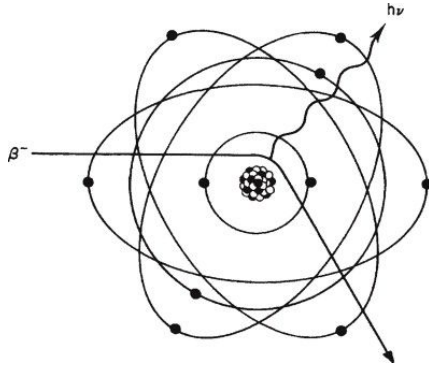
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# III. Variance Reduction Techniques (VRTs)



# III. VRT : Secondary particles Cut-Off



In GEANT4 the cut-off is expressed in **distance** unit which corresponds to the **mean free path**.

**Save time** by **increasing the cut-off** (less particle to simulate)

### III. VRT : Secondary particles Cut-Off

For  $N_{\text{sim}} = 2\text{E}8$

| Electron and Photon cut-off | $\dot{H}^*(10)$ ( $\mu\text{Sv/h}$ ) | $\Delta T$      | Volume    |
|-----------------------------|--------------------------------------|-----------------|-----------|
| 1 mm and 1 mm               | $(2.02 \pm 0.05)10^{+1}$             | 26 h 51 m 36 s  | Phantom 2 |
| 10 mm and 10 mm             | $(1.98 \pm 0.06)10^{+1}$             | 4 h 43 min 12 s | Phantom 2 |
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**Coherent results**

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Coherent results

**Reduction of the computation time**



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**Initially : 10 mm**

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**Results valid to (400, 30) mm**

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Coherent results

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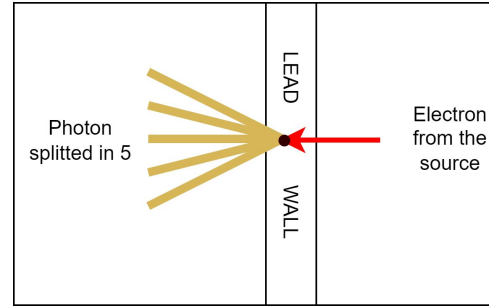
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**Results valid to (400, 30) mm**

**Conclusion : 1.4 times faster, no bias**

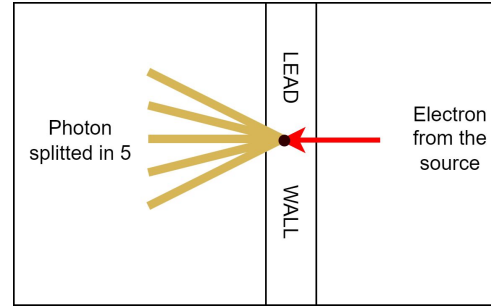
# III. VRT : Uniform Bremsstrahlung Splitting (UBS)

Instead of creating 1 photon, generate  $N_{\text{split}}$  **independent** photons with a statistical weight  $w = 1 / N_{\text{split}}$  to propagate through the results.



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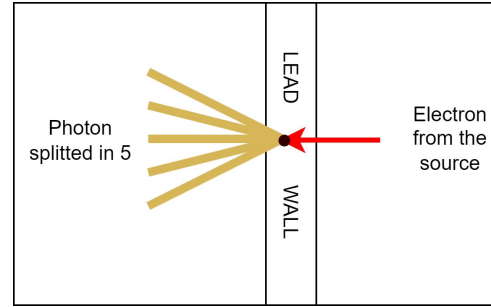


**Theoretical** evolution of the uncertainty :  $R = \frac{\sigma \dot{H}^*(10)}{\dot{H}^*(10)}$   $R \sim 1/\sqrt{N_{\text{hit}}}$

$$R \rightarrow R_{\text{split}} = \frac{R}{\sqrt{N_{\text{split}}}}$$

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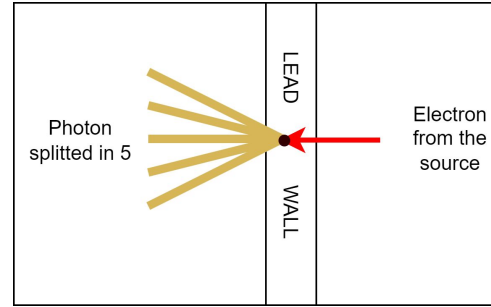
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$$\ln(R_{\text{split}}) = \ln(R) - \frac{1}{2}\ln(N_{\text{split}})$$

# III. VRT : Uniform Bremsstrahlung Splitting (UBS)

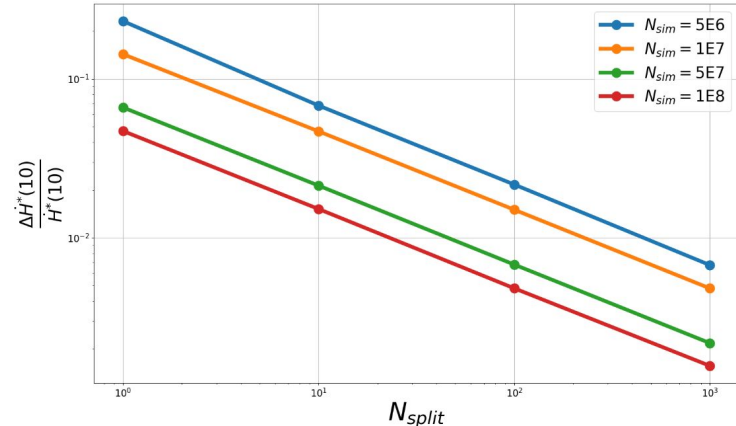
Instead of creating 1 photon, generate  $N_{\text{split}}$  **independent** photons with a statistical weight  $w = 1 / N_{\text{split}}$  to propagate through the results.



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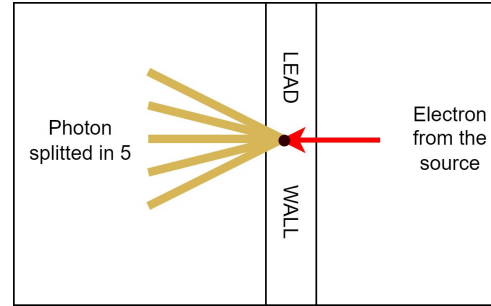
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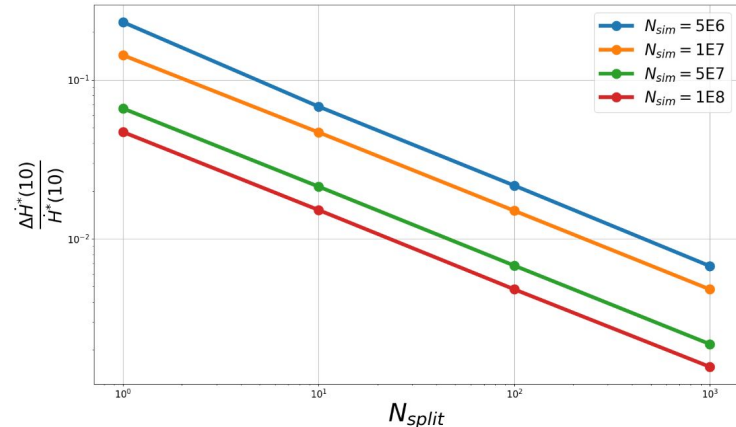


**Theoretical** evolution of the uncertainty :  $R = \frac{\sigma \dot{H}^*(10)}{\dot{H}^*(10)}$   $R \sim 1/\sqrt{N_{\text{hit}}}$

$$R \rightarrow R_{\text{split}} = \frac{R}{\sqrt{N_{\text{split}}}}$$

$$\ln(R_{\text{split}}) = \ln(R) - \frac{1}{2}\ln(N_{\text{split}})$$

Mean leading coefficient :  $0.502 \pm 1.93 \cdot 10^{-3} \%$   
Theoretical uncertainty evolves as expected



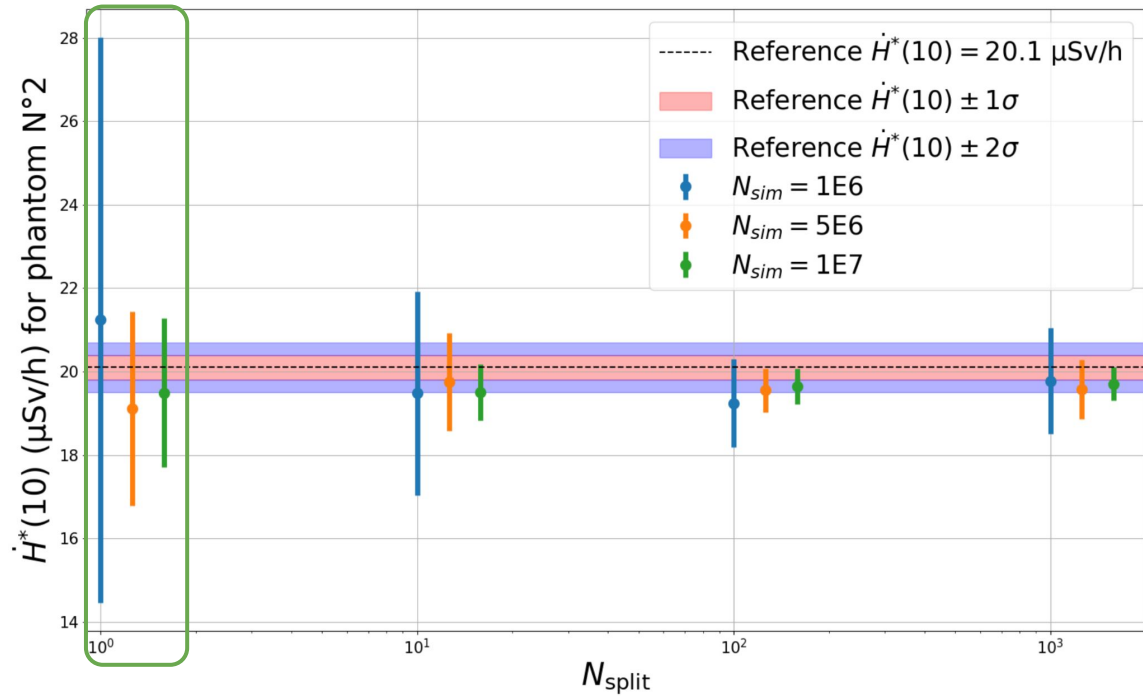


# III. VRT : Uniform Bremsstrahlung Splitting (UBS)

**Bias** study on  $H^*(10)$  and uncertainties

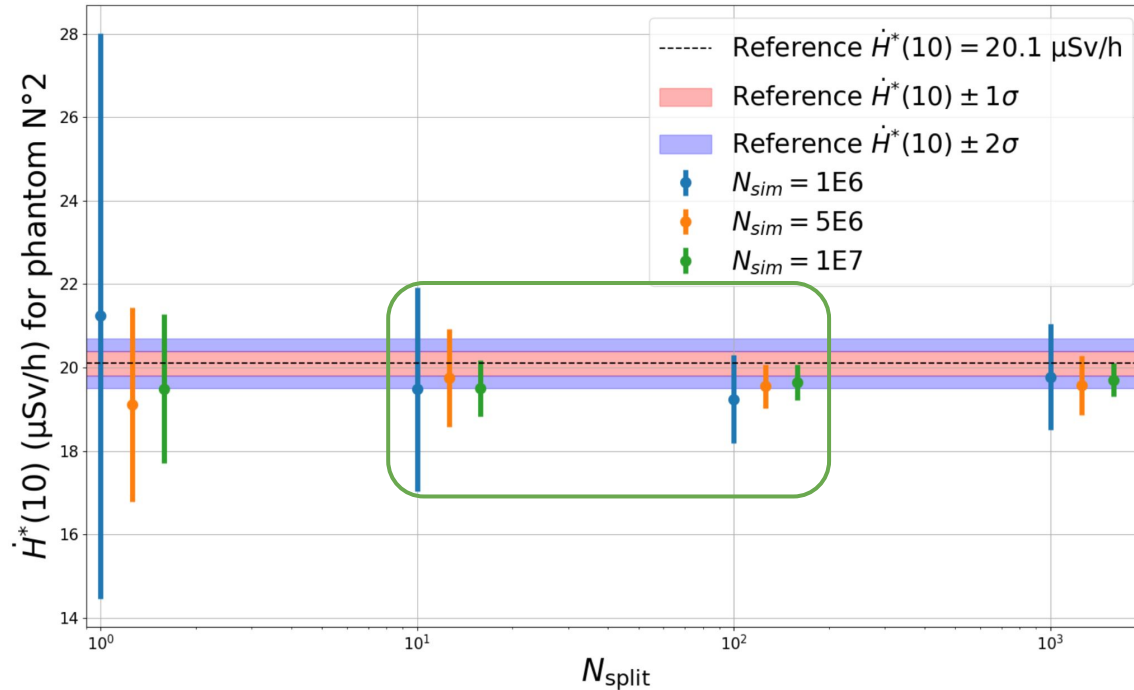
# III. VRT : Uniform Bremsstrahlung Splitting (UBS)

Bias study on  $H^*(10)$  and uncertainties



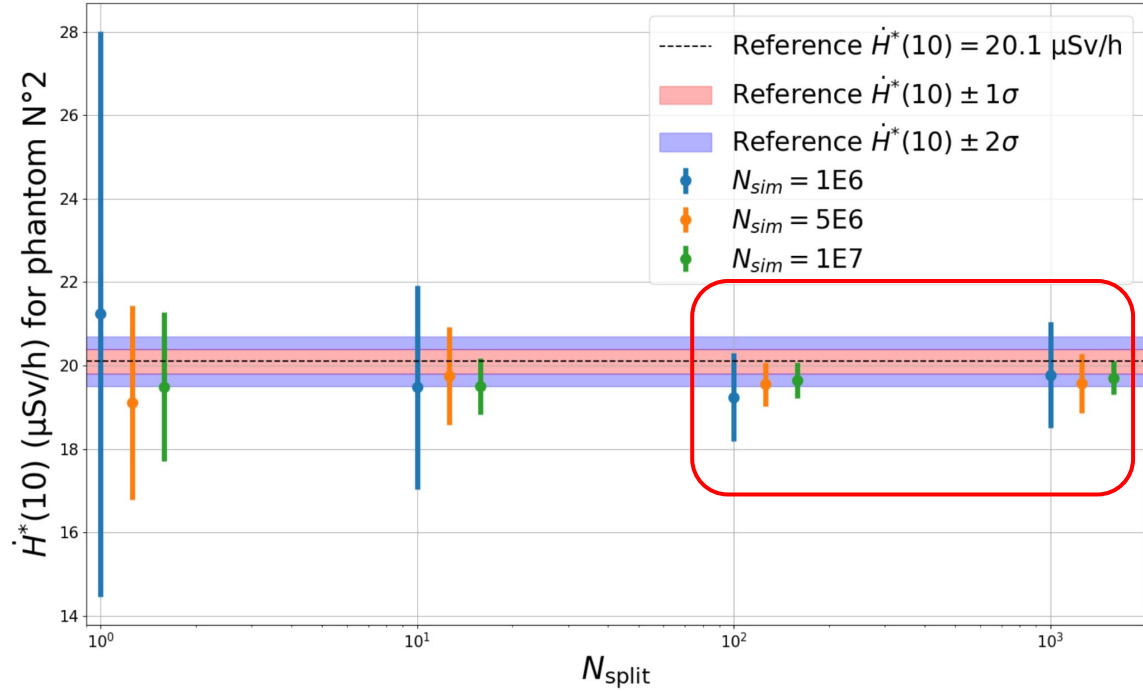
# III. VRT : Uniform Bremsstrahlung Splitting (UBS)

Bias study on  $\dot{H}^*(10)$  and uncertainties



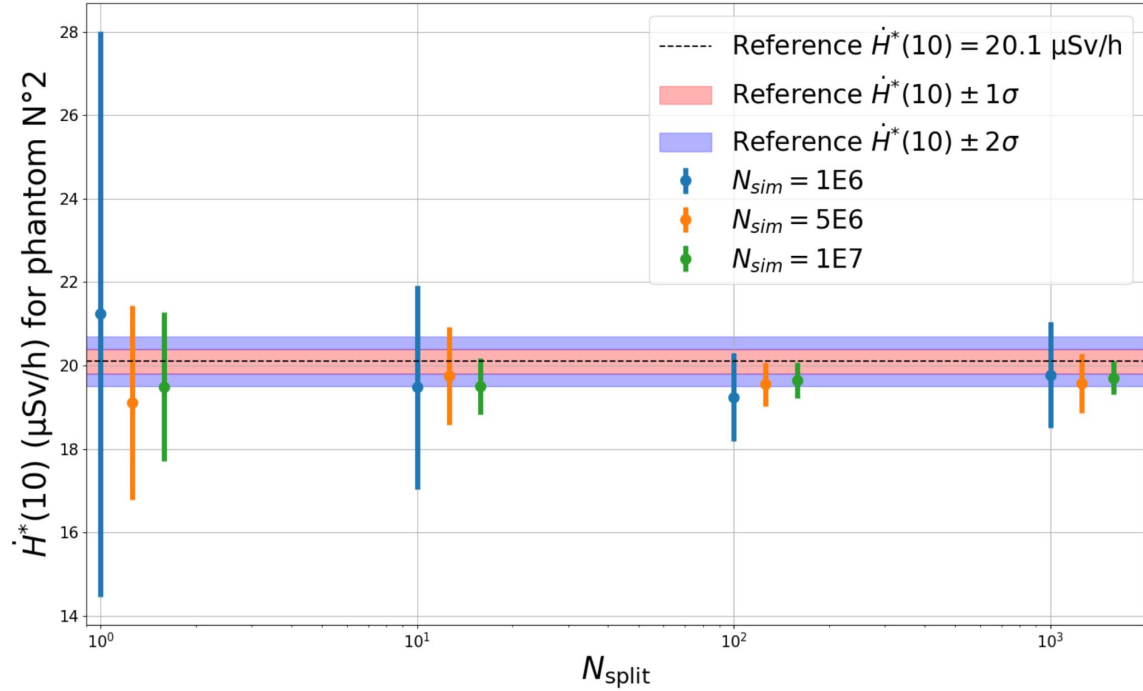
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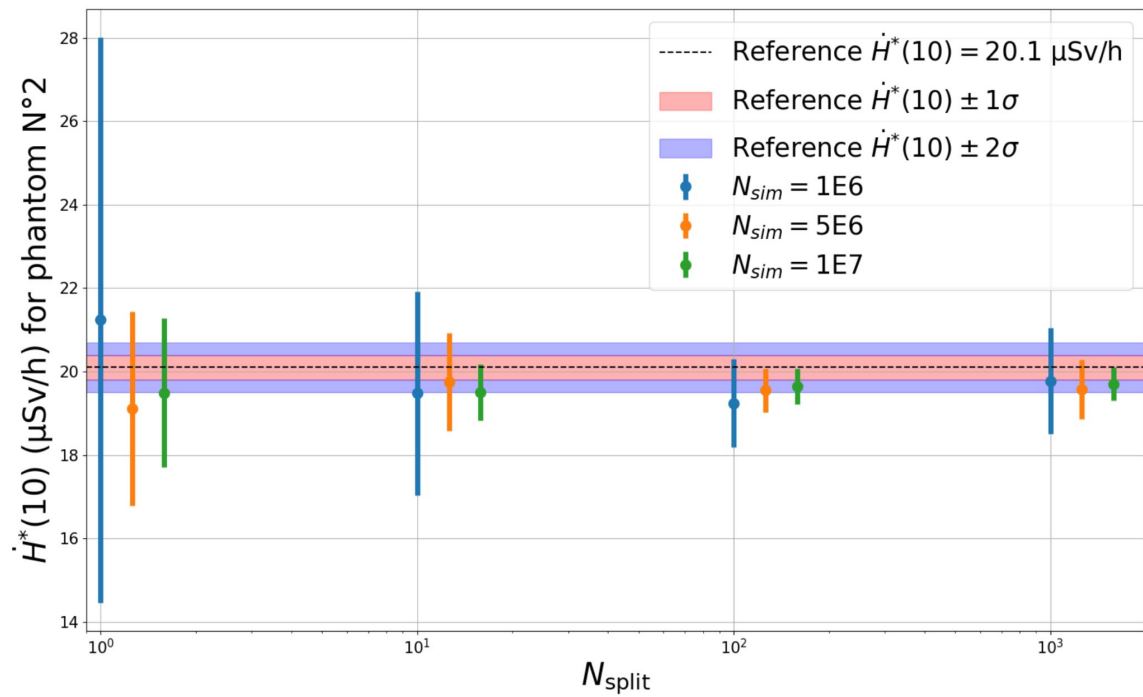
To avoid bias :  $N_{\text{split}} = 100$  when  $N_{\text{sim}} > 10^7$

Increase computation time by 5%.

Multiply number of hit by  $N_{\text{split}}$ .

# III. VRT : Uniform Bremsstrahlung Splitting (UBS)

Bias study on  $H^*(10)$  and uncertainties



To avoid bias :  $N_{split} = 100$  when  $N_{sim} > 10^7$

Increase computation time by 5%.

Multiply number of hit by  $N_{split}$ .

**Conclusion : 100/1.05 times faster, no bias**

### III. VRT : Probe Radius Variation

$$\dot{H}^*(10) = \dot{\phi} \sum_i CIPR_i I_i$$

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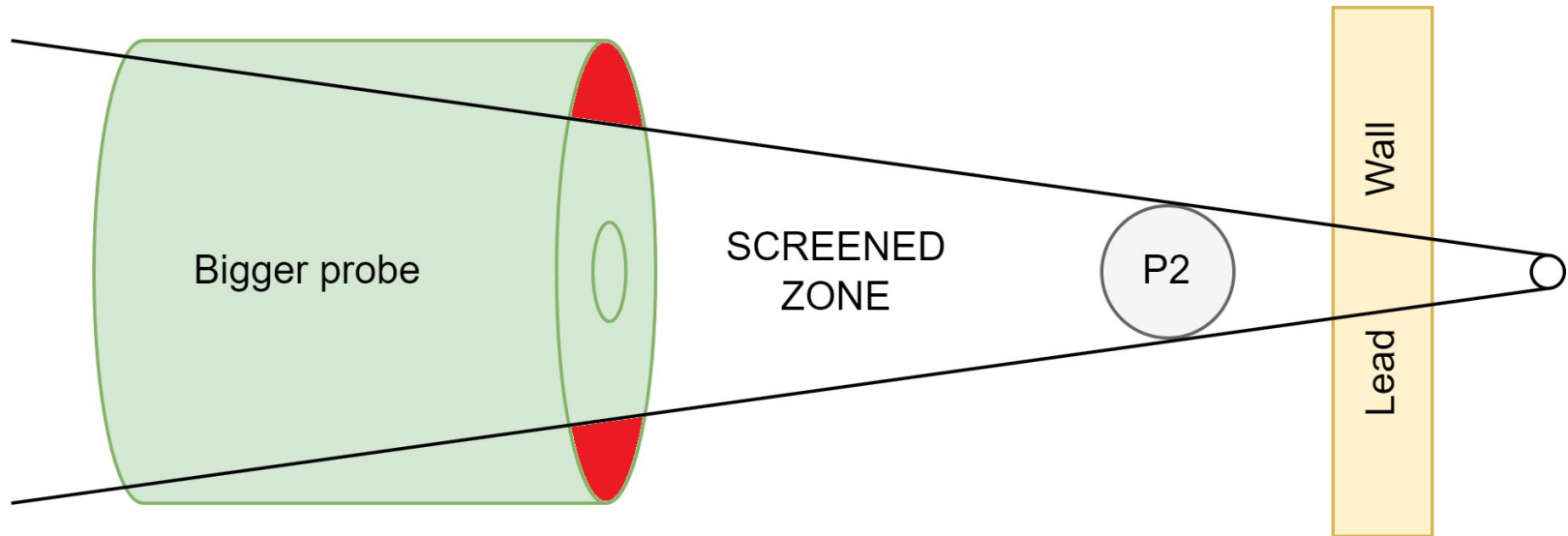
Invariant by the changing the radius **for the probe** under some assumptions :  
**Unidirectional** and **Homogeneous** radiation field, **invariant energy distribution**.



### III. VRT : Probe Radius Variation

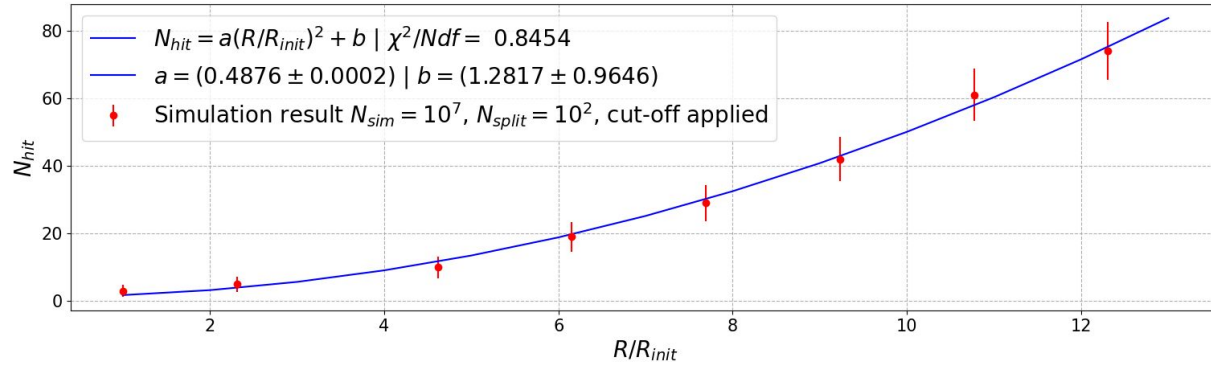
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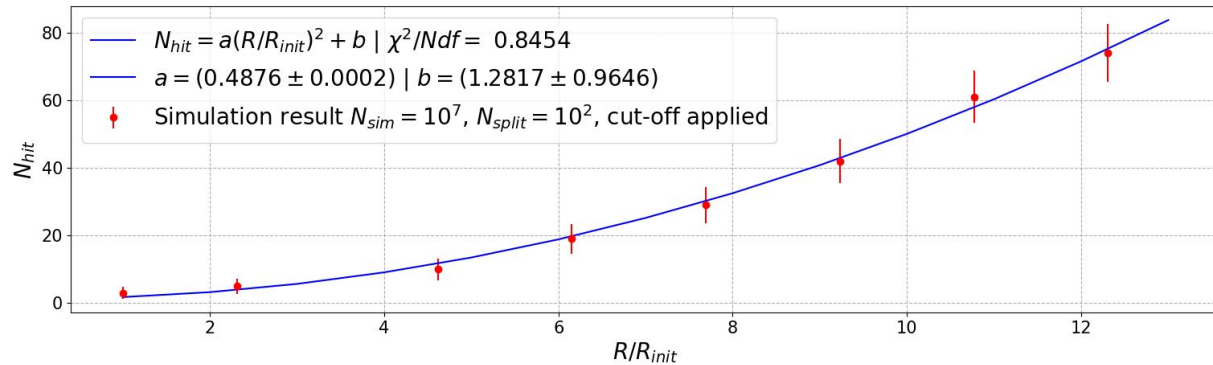
Under these assumptions  $N_{hit}$  should follow a square law.



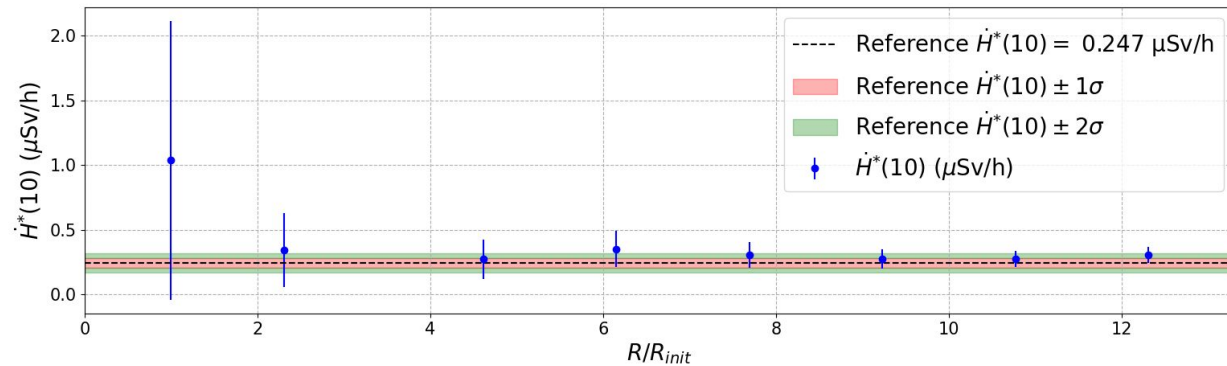
$N_{hit}$  follows a square law,  
**hypothesis validated.**

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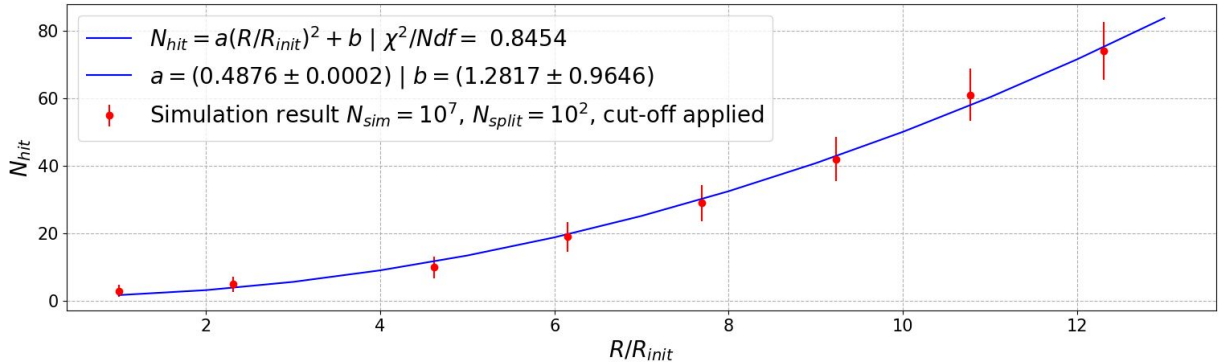
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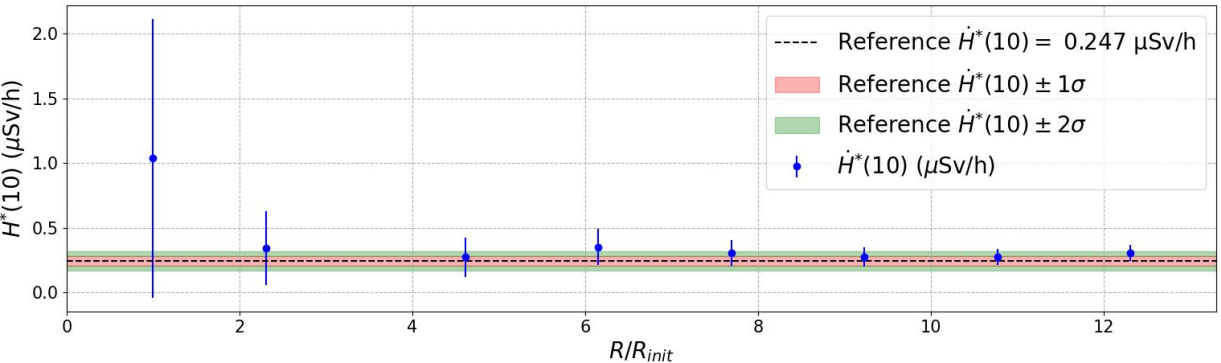
Results **converge to a reference value** obtained with  $N_{sim} = 10^9$ ,  $N_{split} = 100$  and cut-off applied

# III. VRT : Probe Radius Variation

Under these assumptions  $N_{hit}$  should follow a square law.



$N_{hit}$  follows a square law, hypothesis validated.

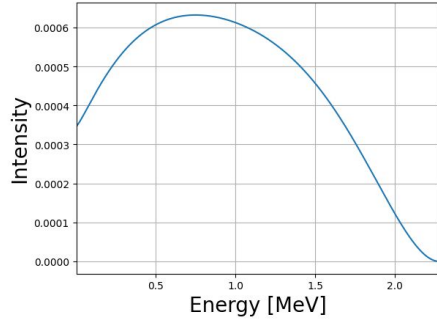


Results converge to a reference value obtained with  $N_{sim} = 10^9$ ,  $N_{split} = 100$  and cut-off applied

**Conclusion : 150 times faster, no bias, radius set to 40 cm**

# III. VRT : Cutting the energy spectrum

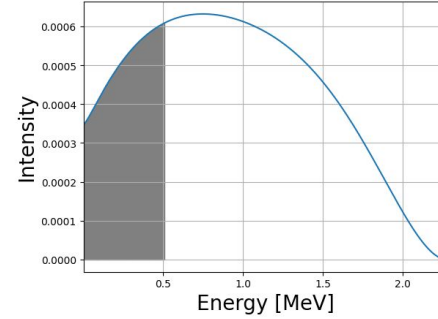
Low energy particles don't cross the lead wall : Simulating useless particles ?



Cut useless part

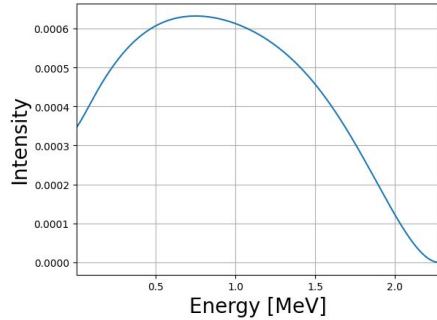


$$P(\text{cross}) < 10^{-7}$$



# III. VRT : Cutting the energy spectrum

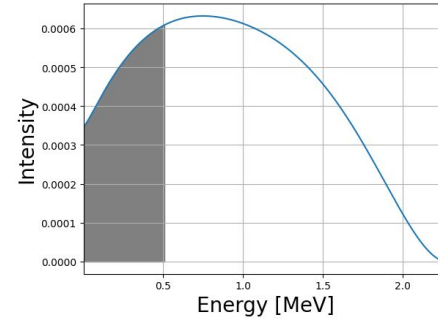
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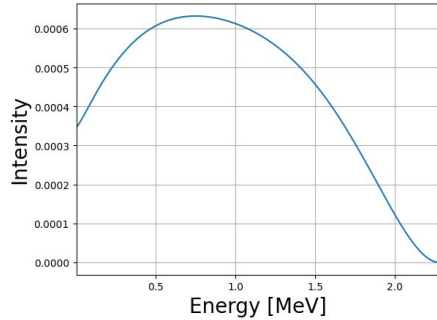
$P(\text{cross}) < 10^{-7}$



Correction on the activity  $A \rightarrow A \frac{\int_{E_{\text{cut}}}^{E_{\text{max}}} \frac{dN}{dE} dE}{\int_0^{E_{\text{max}}} \frac{dN}{dE} dE}$

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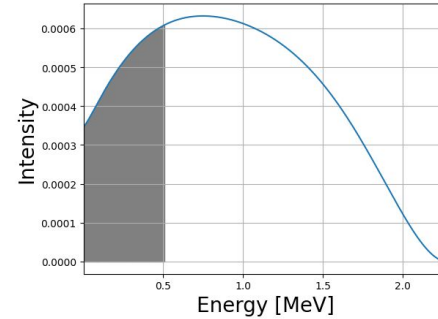
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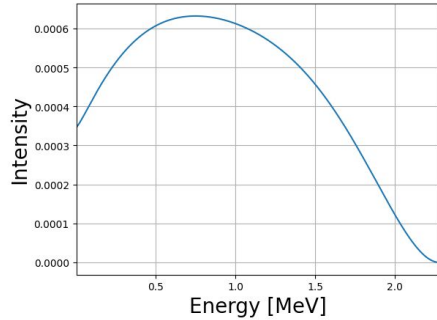


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| Method               | $N_{\text{hit}}$ | $\Delta T$  | $\dot{N}_{\text{hit}}$ (particles.s <sup>-1</sup> ) | $\dot{H}^*(10)$ (μSv/h)  |
|----------------------|------------------|-------------|---|--------------------------|
| Without spectrum cut | 14003            | 23 h 35 min | $(1.65 \pm 0.01)10^{-1}$                            | $(2.01 \pm 0.03)10^{+1}$ |
| With spectrum cut    | 19092            | 26 h 2 min  | $(2.25 \pm 0.02)10^{-1}$                            | $(2.06 \pm 0.03)10^{+1}$ |

# III. VRT : Cutting the energy spectrum

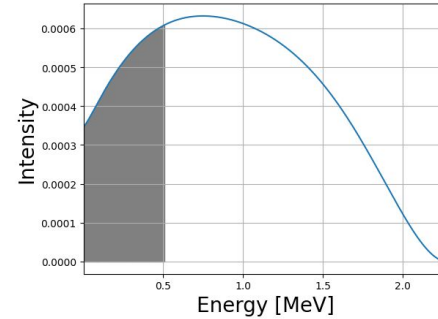
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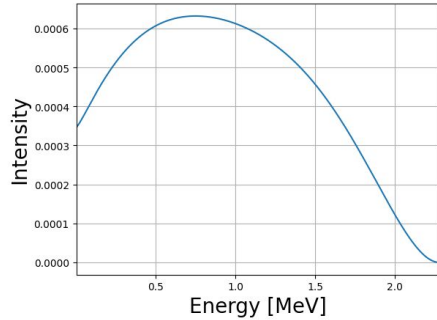
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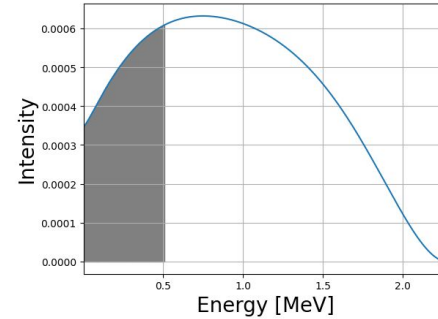
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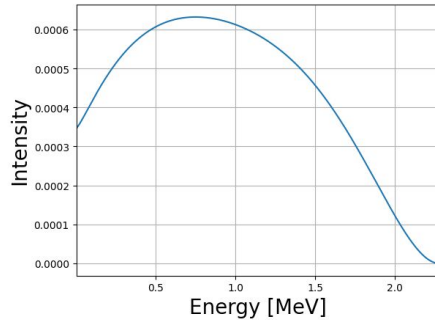


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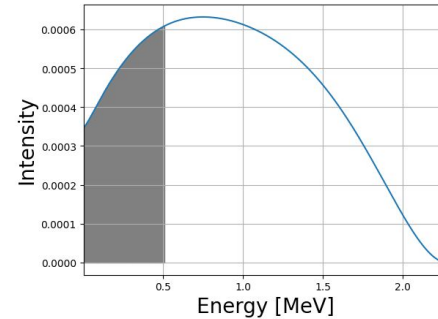
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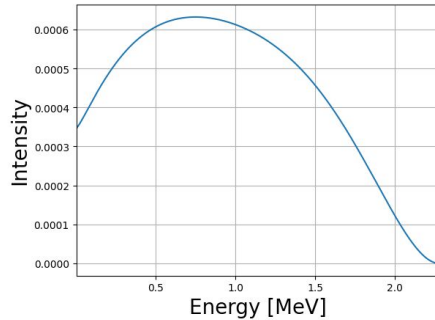
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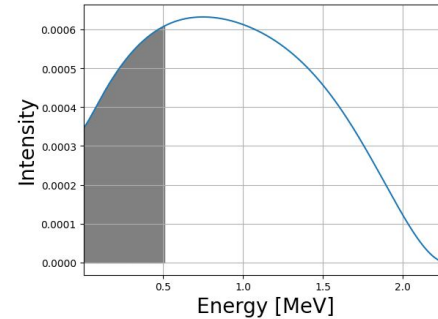
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# III. VRT : Cutting the energy spectrum



Cut useless part  
 →  
 $P(\text{cross}) < 10^{-7}$

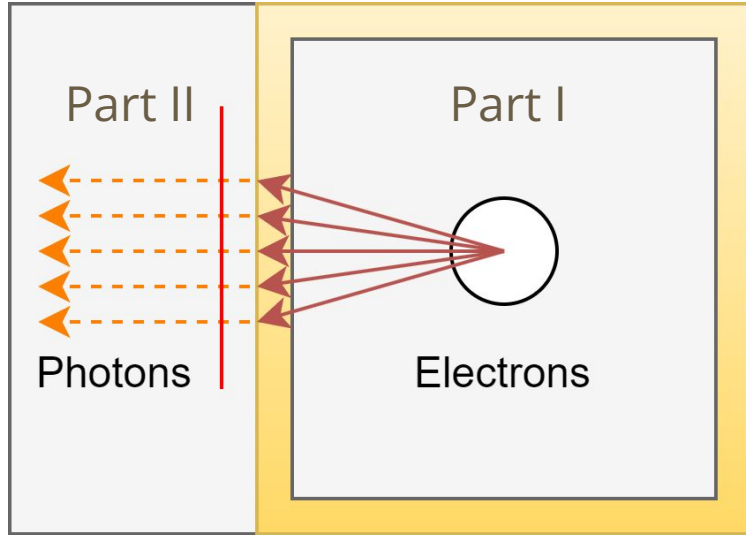


Correction on the activity  $A \rightarrow A \frac{\int_{E_{\text{cut}}}^{E_{\text{max}}} \frac{dN}{dE} dE}{\int_0^{E_{\text{max}}} \frac{dN}{dE} dE}$

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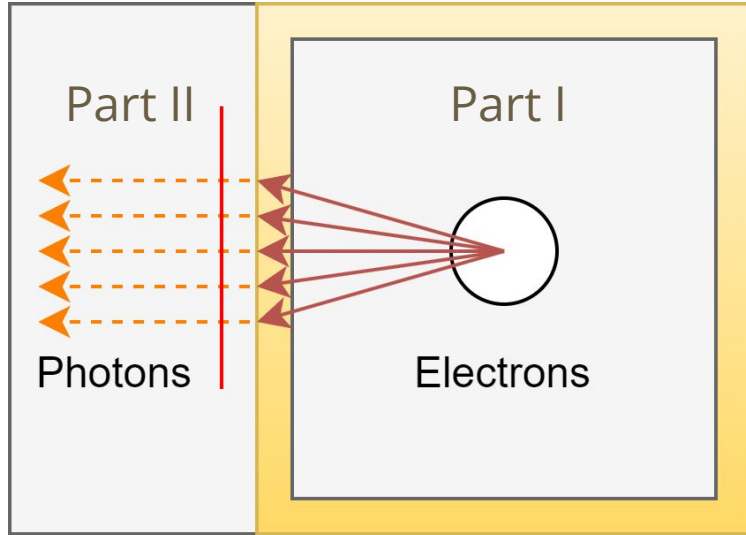
**Conclusion : For same  $N_{\text{hit}}$ ,  $(1.24 \pm 0.01)$  faster, no bias**

# III. Photon Phase Space



Only need to simulate part II for different configurations

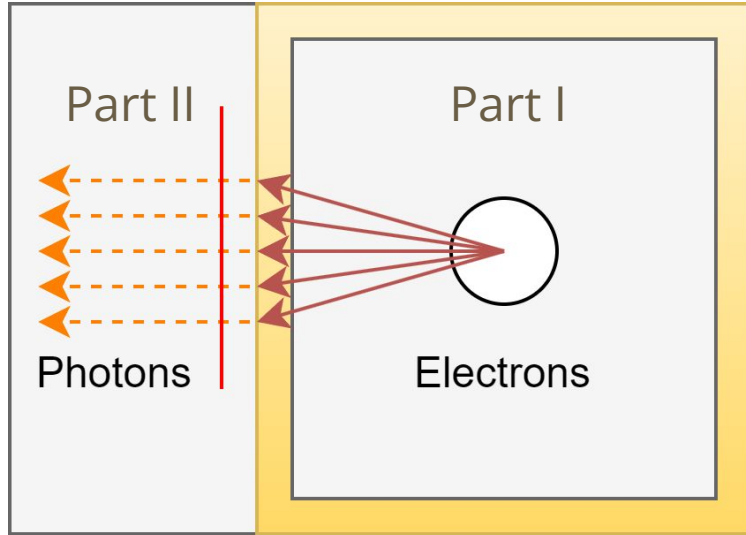
# III. Photon Phase Space



New uncertainty term :

$$\frac{\sigma_{\dot{H}^*(10)}}{\dot{H}^*(10)} = \sqrt{\frac{\sum_i \sigma_{l_i}^2}{(\sum_i l_i)^2} + \frac{\sum_i (I_i^2 \sigma_{CIPR_i}^2 + CIPR_i^2 I_i)}{(\sum_i CIPR_i I_i)^2} + \frac{1}{N_{\text{hit}}} + \frac{2}{N_\gamma}}$$

# III. Photon Phase Space

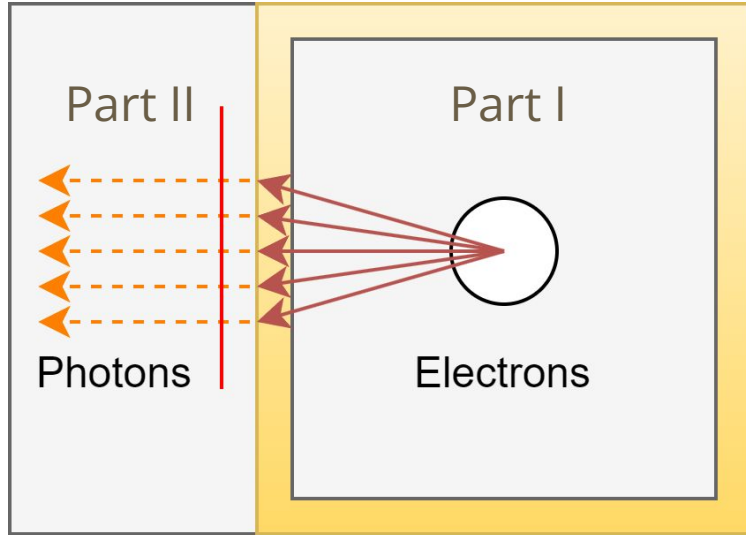


New uncertainty term :

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| Method              | $\dot{H}^*(10)$ ( $\mu\text{Sv/h}$ ) | $\Delta T$  |
|---------------------|--------------------------------------|-------------|
| Without phase space | $(2.47 \pm 0.37) 10^{-1}$            | 24 h 45 min |
| With phase space    | $(2.70 \pm 0.39) 10^{-1}$            | 34 s        |

# III. Photon Phase Space



New uncertainty term :

$$\frac{\sigma_{\dot{H}^*(10)}}{\dot{H}^*(10)} = \sqrt{\frac{\sum_i \sigma_{l_i}^2}{(\sum_i l_i)^2} + \frac{\sum_i (I_i^2 \sigma_{CIPR_i}^2 + CIPR_i^2 I_i)}{(\sum_i CIPR_i I_i)^2}} + \frac{1}{N_{\text{hit}}} + \frac{2}{N_\gamma}$$

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| Without phase space | $(2.47 \pm 0.37) 10^{-1}$            | 24 h 45 min |
| With phase space    | $(2.70 \pm 0.39) 10^{-1}$            | 34 s        |

**Conclusion :  $2.6 \cdot 10^3$  times faster, no visible bias  
Only possible after a first simulation**

### III. VRT : Total time gain

Secondary particles cut-off :  $g(\text{Cut-Off}) = 1.4$



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**Uniform Bremsstrahlung splitting :  $g(\text{UBS}) = 100/1.05$**

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Secondary particles cut-off :  $g(\text{Cut-Off}) = 1.4$

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**Probe radius variation :  $g(\text{Radius}) = 151.48$**

### III. VRT : Total time gain

Secondary particles cut-off :  $g(\text{Cut-Off}) = 1.4$

Uniform Bremsstrahlung splitting :  $g(\text{UBS}) = 100/1.05$

Probe radius variation :  $g(\text{Radius}) = 151.48$

**Energy spectrum cut :  $g(\text{Spectrum}) = 1.24 \pm 0.01$**

### III. VRT : Total time gain

Secondary particles cut-off :  $g(\text{Cut-Off}) = 1.4$

Uniform Bremsstrahlung splitting :  $g(\text{UBS}) = 100/1.05$

Probe radius variation :  $g(\text{Radius}) = 150$

**Energy spectrum cut :  $g(\text{Spectrum}) = 1.24 \pm 0.01$**

$$\text{Total gain : } G = (2.504 \pm 0.020)10^4$$

### III. VRT : Total time gain

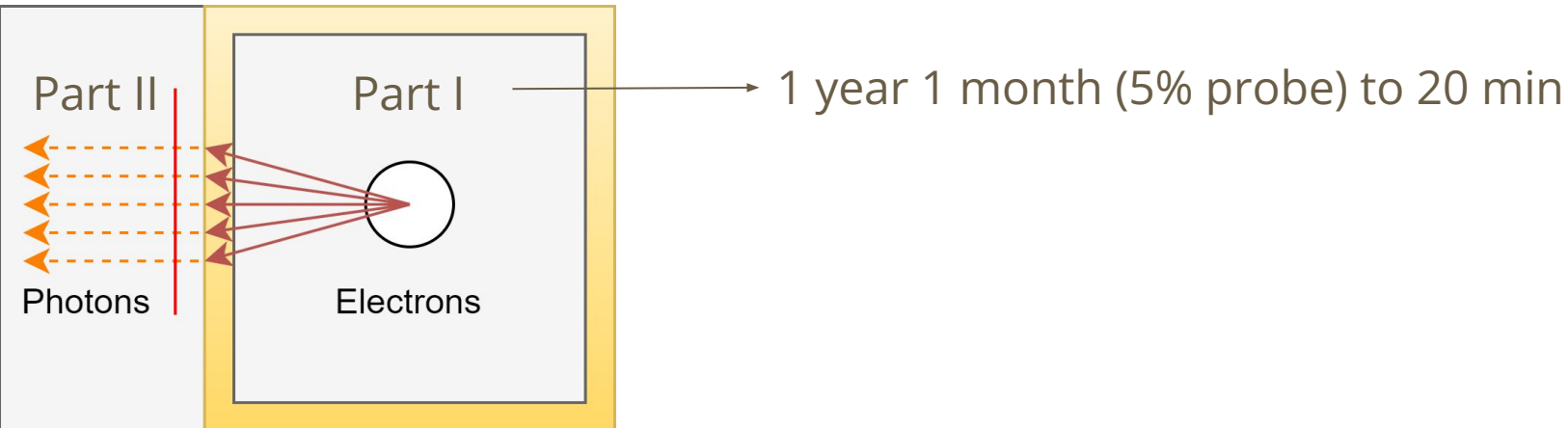
Secondary particles cut-off :  $g(\text{Cut-Off}) = 1.4$

Uniform Bremsstrahlung splitting :  $g(\text{UBS}) = 100/1.05$

Probe radius variation :  $g(\text{Radius}) = 151.48$

**Energy spectrum cut :  $g(\text{Spectrum}) = 1.24 \pm 0.01$**

$$\text{Total gain : } G = (2.504 \pm 0.020)10^4$$



### III. VRT : Total time gain

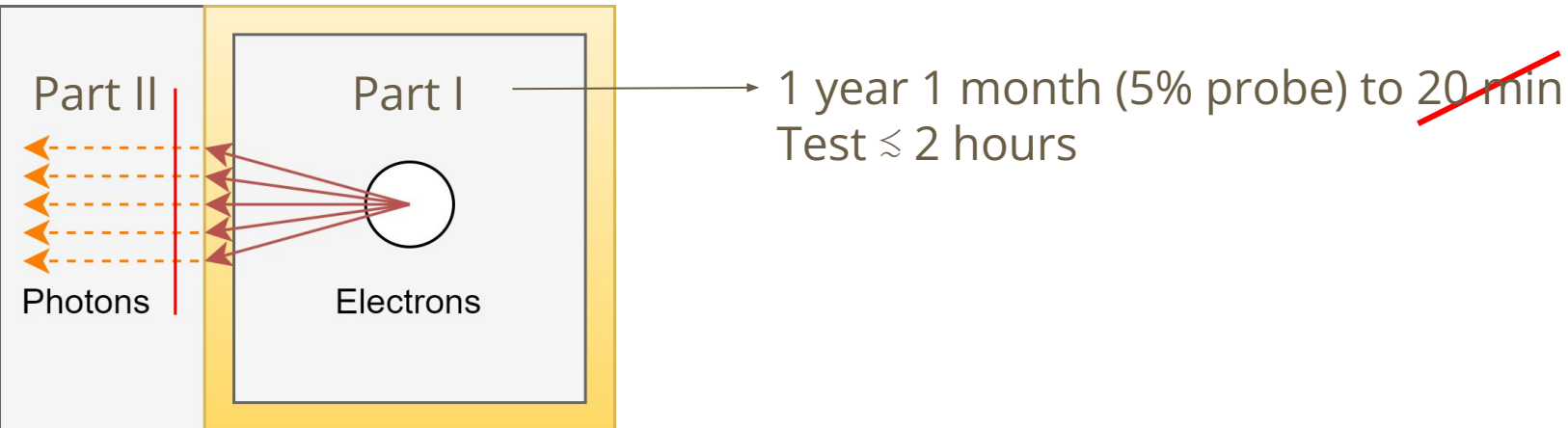
Secondary particles cut-off :  $g(\text{Cut-Off}) = 1.4$

Uniform Bremsstrahlung splitting :  $g(\text{UBS}) = 100/1.05$

Probe radius variation :  $g(\text{Radius}) = 151.48$

**Energy spectrum cut :  $g(\text{Spectrum}) = 1.24 \pm 0.01$**

$$\text{Total gain : } G = (2.504 \pm 0.020)10^4$$



### III. VRT : Total time gain

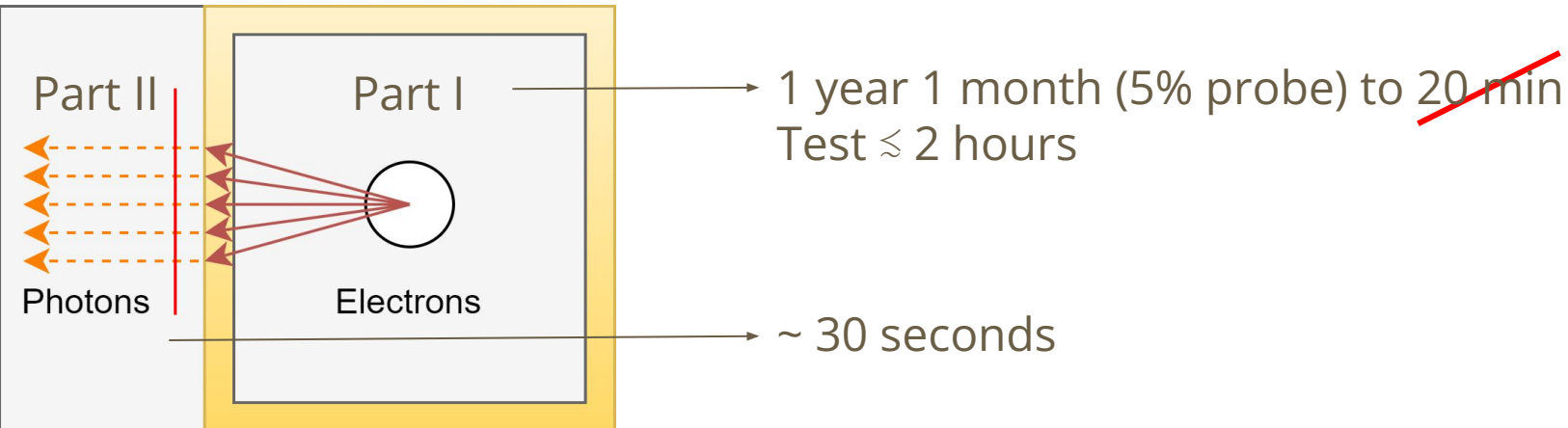
Secondary particles cut-off :  $g(\text{Cut-Off}) = 1.4$

Uniform Bremsstrahlung splitting :  $g(\text{UBS}) = 100/1.05$

Probe radius variation :  $g(\text{Radius}) = 151.48$

**Energy spectrum cut :  $g(\text{Spectrum}) = 1.24 \pm 0.01$**

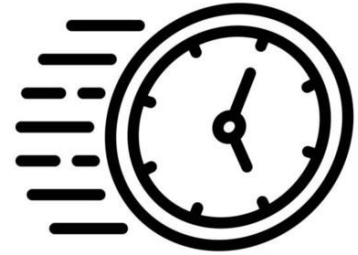
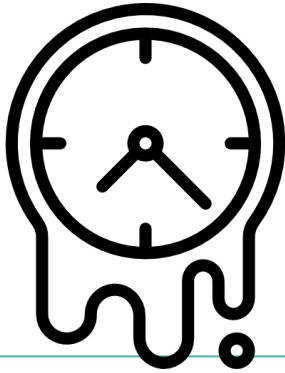
$$\text{Total gain : } G = (2.504 \pm 0.020)10^4$$



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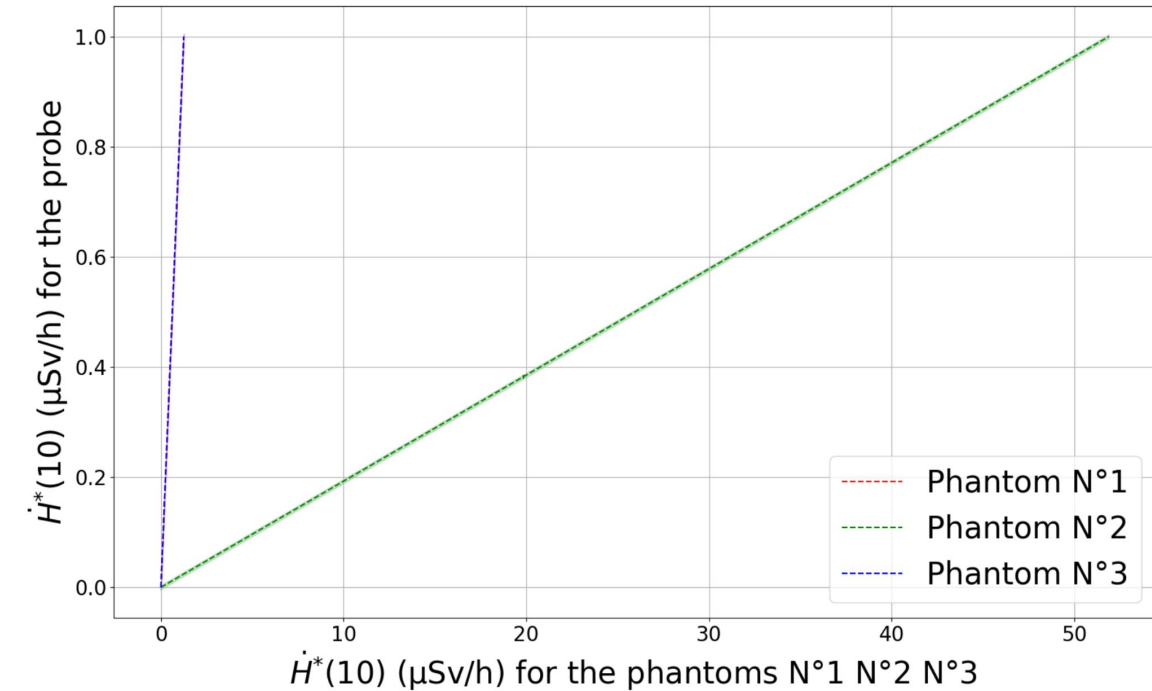
# IV. Application of the methods





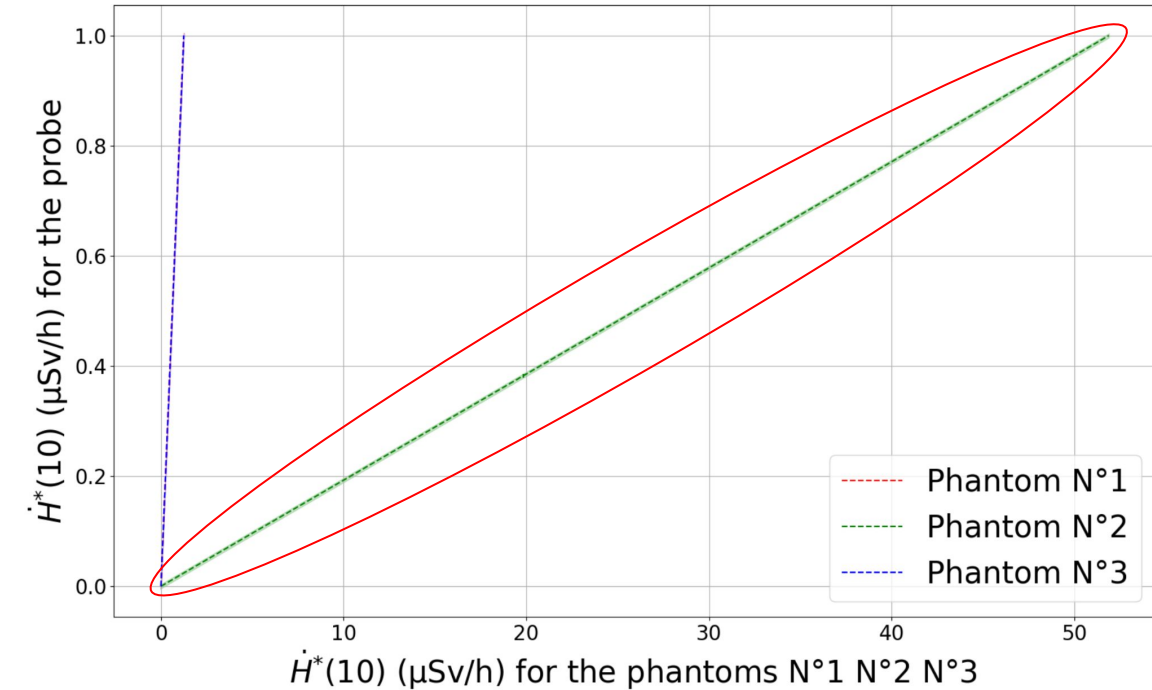
# IV.A Threshold signal

$N_{sim} = 3 \cdot 10^9$ ,  $N_{split} = 10^2$ ,  $R_{probe} = 40$  cm, Cut-Off applied, Energy spectrum cut :



# IV.A Threshold signal

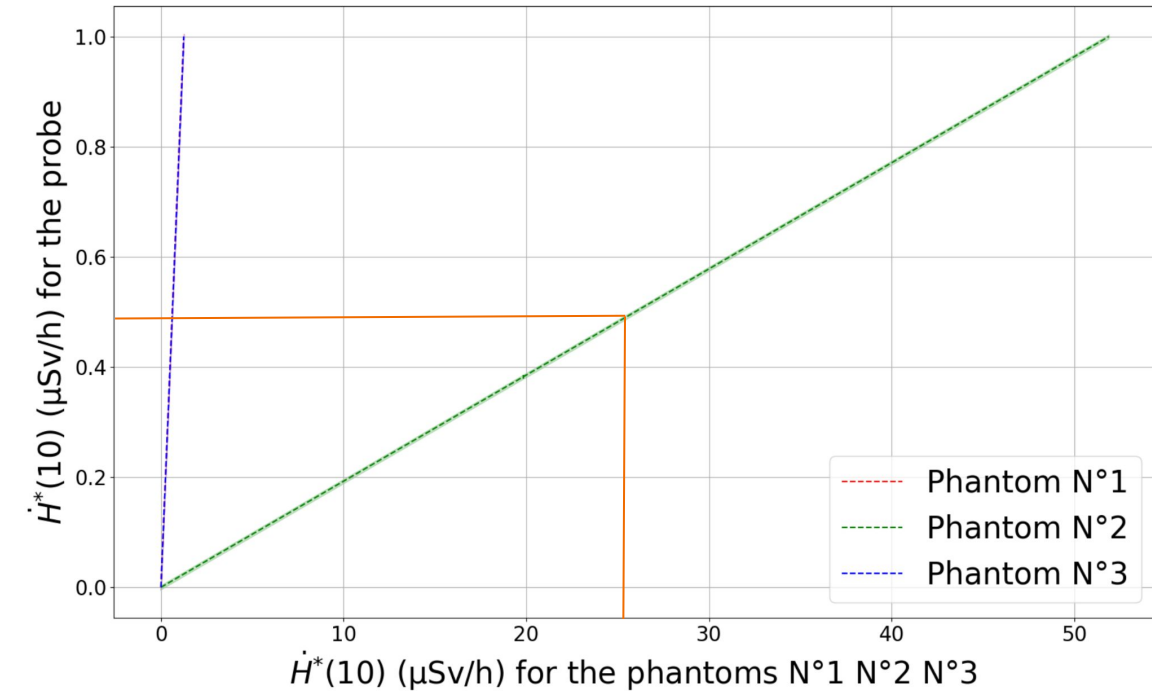
$N_{sim} = 3 \cdot 10^9$ ,  $N_{split} = 10^2$ ,  $R_{probe} = 40$  cm, Cut-Off applied, Energy spectrum cut :



Phantom N°2 : **(51.32 ± 0.53)** times more than the probe.

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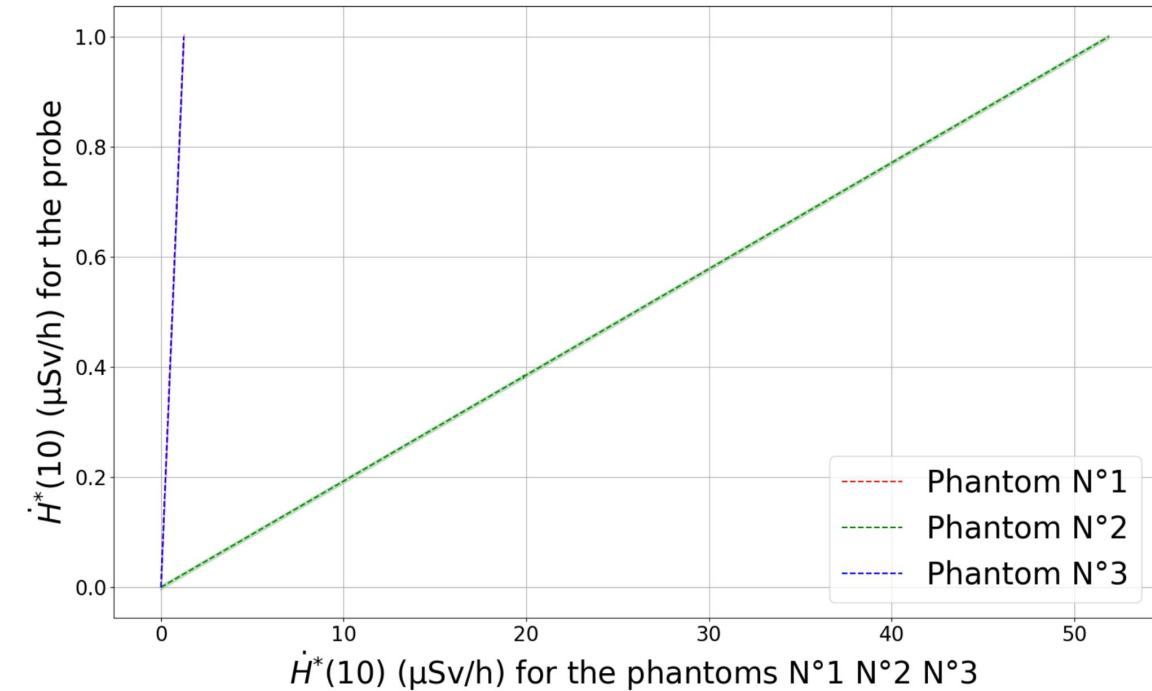


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~ **0.5  $\mu\text{Sv/h}$  threshold** for 25 $\mu\text{Sv/h}$

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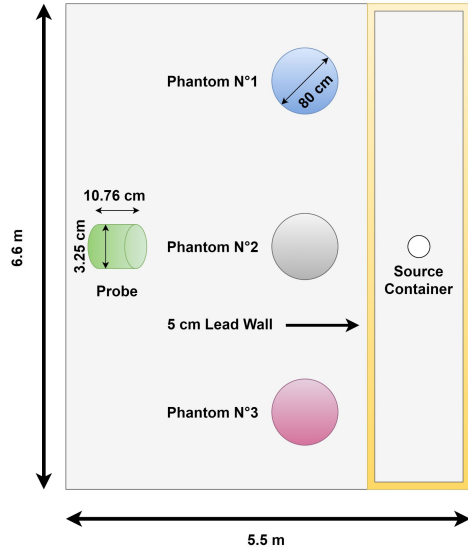
Phantom N°2 : **(51.32 ± 0.53)** times more than the probe.

~ **0.5  $\mu\text{Sv/h}$  threshold** for 25 $\mu\text{Sv/h}$

Variation of 43% for the probe  
**Correlation between individual bias ?**

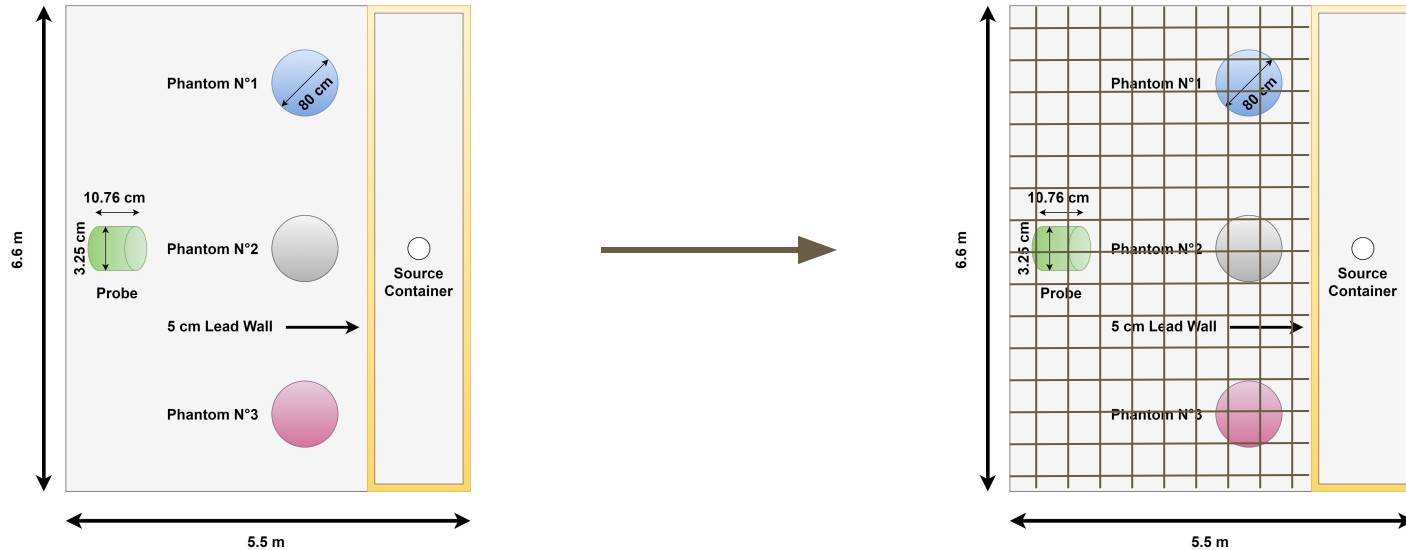
# IV.B Optimization of probe placement

$N_{\text{sim}} = 3 \cdot 10^9$ ,  $N_{\text{split}} = 10^2$ ,  $R_{\text{probe}} = 40 \text{ cm}$ , Cut-Off applied, Energy spectrum cut :



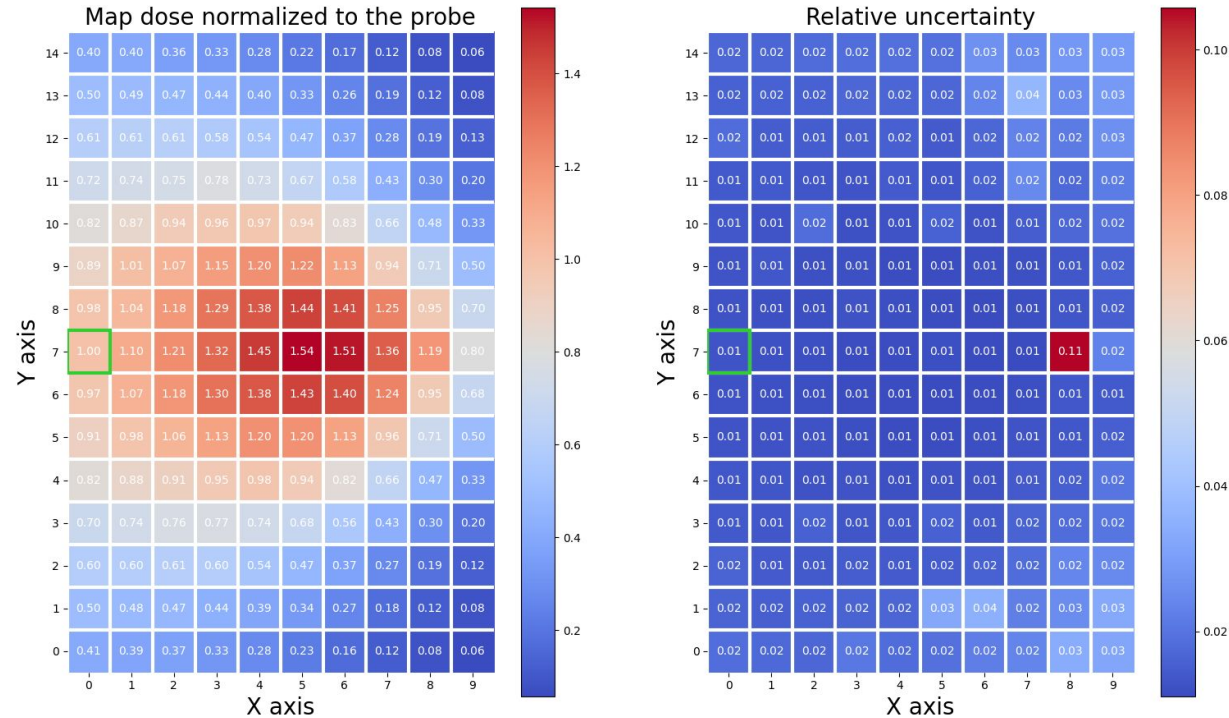
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Possibility to increase the signal by a factor **(1.54 ± 0.02)**

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# V. Conclusion

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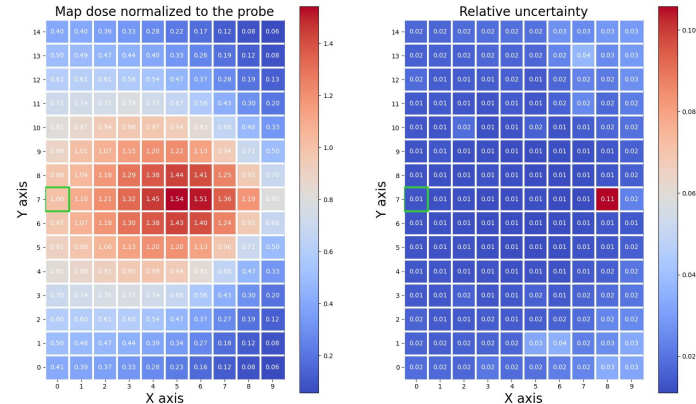
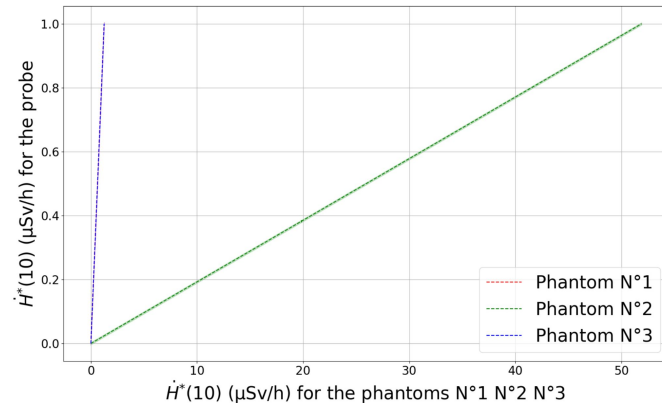
# V. Conclusion

- Simulation of laboratory front panel
- Uncertainty calculation → More than a year for good statistical results
- Introduction VRTs → 2 hours to generate a phase space
- Using phase space → ~ 30 seconds for any configuration

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**Establish radiological exposure as a function of position**



# V. Conclusion

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**Establish relationship between probe and staff exposure**  
**Establish radiological exposure as a function of position**

Openings :

- Investigate single VRT bias correlation
- Obtain experimental reference value for the probe
- Find other VRTs

# Sources

[1] - Arronax Nantes

<https://www.arronax-nantes.fr/chimie-et-radiopharmacie/thematique/radiopharmacie/>

[2] - CIPR Coefficients

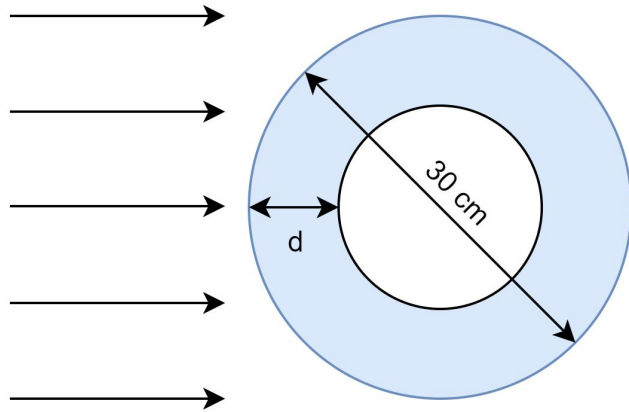
International Commission on Radiological Protection, 1995, Conversion coefficients for use in Radiological Protection Against External Radiation, publication 74

[3] -  $^{90}\text{Y}$  Decay scheme and energy spectrum data

International Atomic Energy Agency

# Backups : ICRU Sphere

ICRU = Internal Commission on Radiation Units & Measurements



76.2 % O, 11.1% C, 10.1% H, 2.6% N

# Backups : Radiation protection factors

$dE/dm$  Absorbed dose (Gy or J/Kg)

Ideal  $dE/dx$  to kill DNA : 100 keV/ $\mu\text{m}$

Even if two types of particles deposited  $dE/dm$  their  $dE/dx$  is different

$$H_T = D_{T,R} W_R$$

Different organs sensibilities (experimental)

$$E = \sum H_T W_T$$

# Backups : Materials & Methods : The GATE software

GATE software developed by the international OpenGATE collaboration

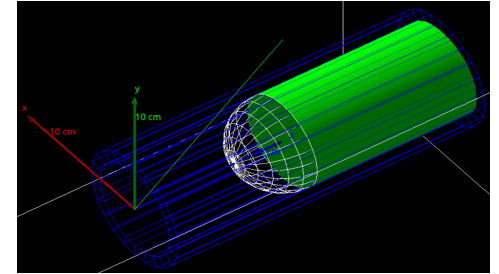
Define volumes and geometries with associated material

Select physical processes : EM type in our case

Photoelectric, Compton, pair production, Bremsstrahlung, Annihilation...

Source : Particles type, energy range, angular distribution.

Attach actors to volumes (TLE Dose Actor, Energy Spectrum, Fluence actor, Phase Space Actor...)

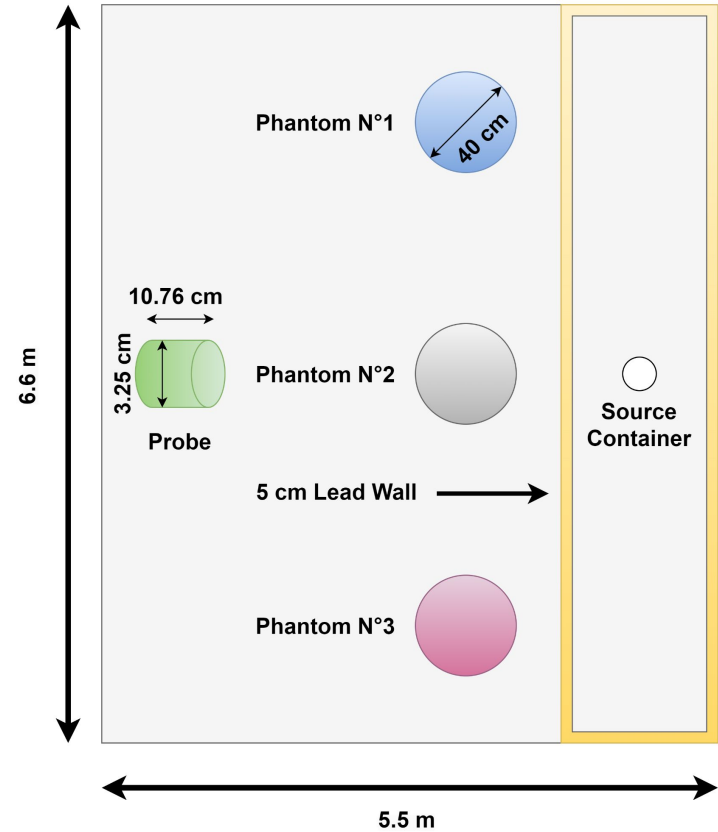


*Cylindrical Si probe*



# Backups : More details about the simulation

Distance Probe - Phantom N°2 : 3.9 m  
Distance Phantom N°2 - Source : 0.8 m  
Distance Probe - Source : 4.7 m

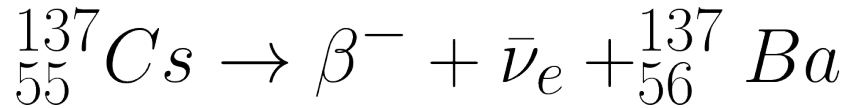




# Backups : Probe modeling validation

|                                      | Theoretical (given) | Measurement (given) | Simulated        |
|--------------------------------------|---------------------|---------------------|------------------|
| $\dot{H}^*(10)$ ( $\mu\text{Sv/h}$ ) | 37.5                | 36.84               | $37.40 \pm 0.03$ |

To **ensure** the **accuracy** of the probe Monte Carlo modeling : **comparison** with **experimental** data.



Relative error  $\sim 1.5 \cdot 10^{-2}$

**Validation** of the modeling

# Backups : $\dot{H}^*$ (10) invariance

Invariant by the changing the radius **for the probe** under some assumptions :  
**Unidirectional** and **Homogeneous** radiation field, **photon spectrum invariant**.

$$\dot{H}^*(10) = \dot{\phi} \sum_i CIPR_i I_i$$

$$\phi(r) = \frac{dl(r)}{dV(r)} = \frac{1}{V(r)} \sum_i l_i(r)$$

$$\phi(R) = \frac{dl(R)}{dV(R)} = \frac{1}{V(R)} \sum_i l_i(R)$$

$$\sum_i l_i(R) = \sum_i l_i(r) \left(\frac{R}{r}\right)^2$$

$$\phi(R) = \frac{1}{V(R)} \sum_i l_i(r) \left(\frac{R}{r}\right)^2$$

$$\phi(R) = \frac{1}{\pi h} \sum_i l_i(r) \frac{1}{r^2}$$

$$\phi(R) = \frac{1}{V(r)} \sum_i l_i(r)$$

$$\phi(R) = \phi(r)$$

# Backups : Radiological zonation

| Zone type   |  | Zone identification | Maximum total effective dose (external plus internal) |
|-------------|--|---------------------|---|
| Unregulated |  | White               | 80 $\mu$ Sv/month                                     |
| Supervised  |  | Blue                | 7.5 $\mu$ Sv/hr                                       |
| Controlled  | Limited                                  | Green               | 25 $\mu$ Sv/hr  |
|             | Specially regulated                      | Yellow              | 2 mSv/hr  |
|             | Forbidden without specific authorization | Orange              | 100 mSv/hr  |
| Red         |  | above 100 mSv/hr    |   |

Cancer risk : 0.5% / 100 mSv

Public limit : 1 mSv/yr  
Worker limit : 20 mSv/yr

*Karlsruhe Institute of Technology*

### III. VRT : Probe Radius Variation

$$\dot{H}^*(10) = \dot{\phi} \sum_i CIPR_i I_i$$

Invariant by the changing the radius **for the probe** under some assumptions :  
**Unidirectional** and **Homogeneous** radiation field, **invariant energy distribution**.

