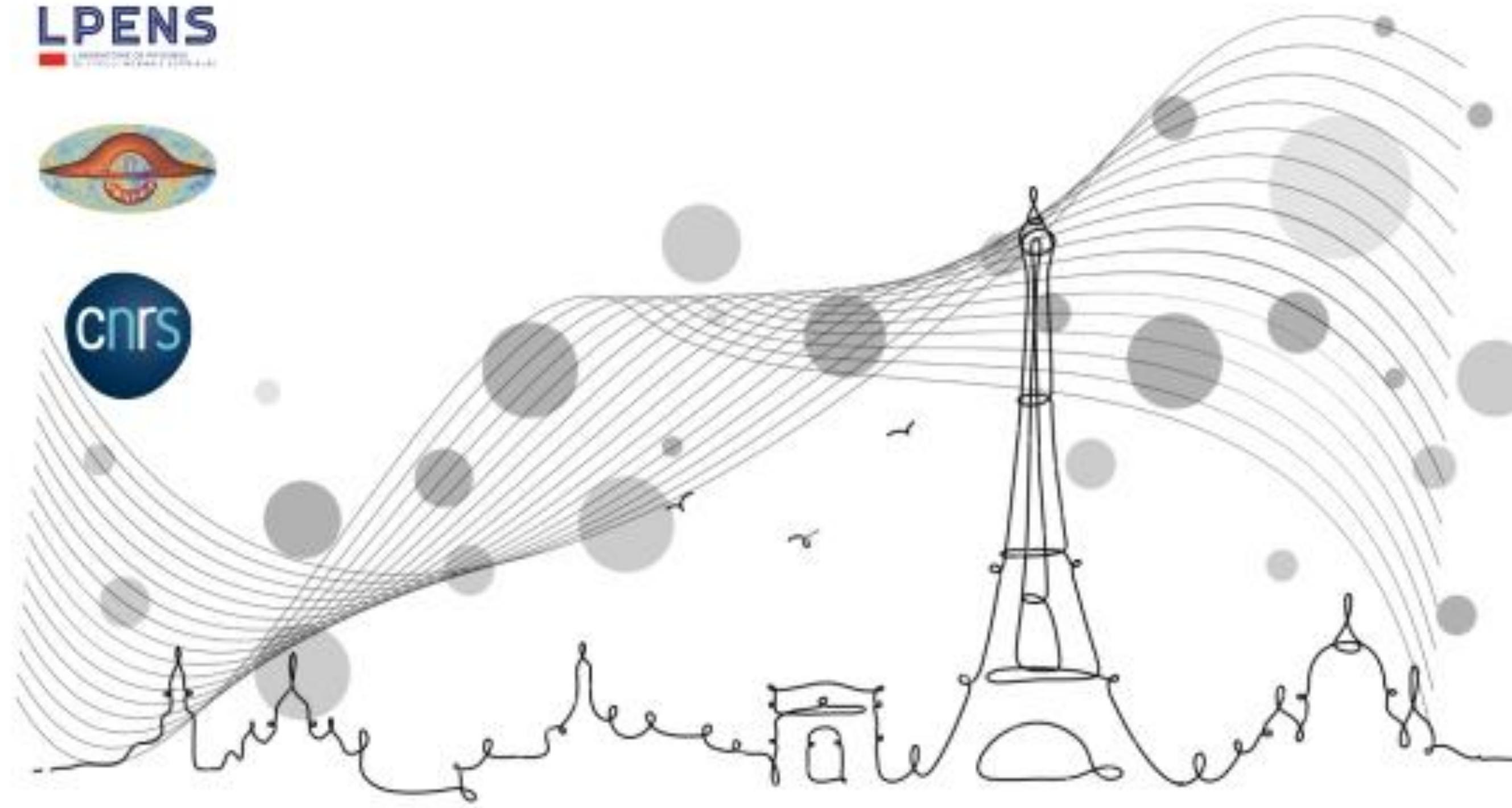


Primordial Black Holes from supercooled phase transitions

Yann Gouttenoire

28th November 2023



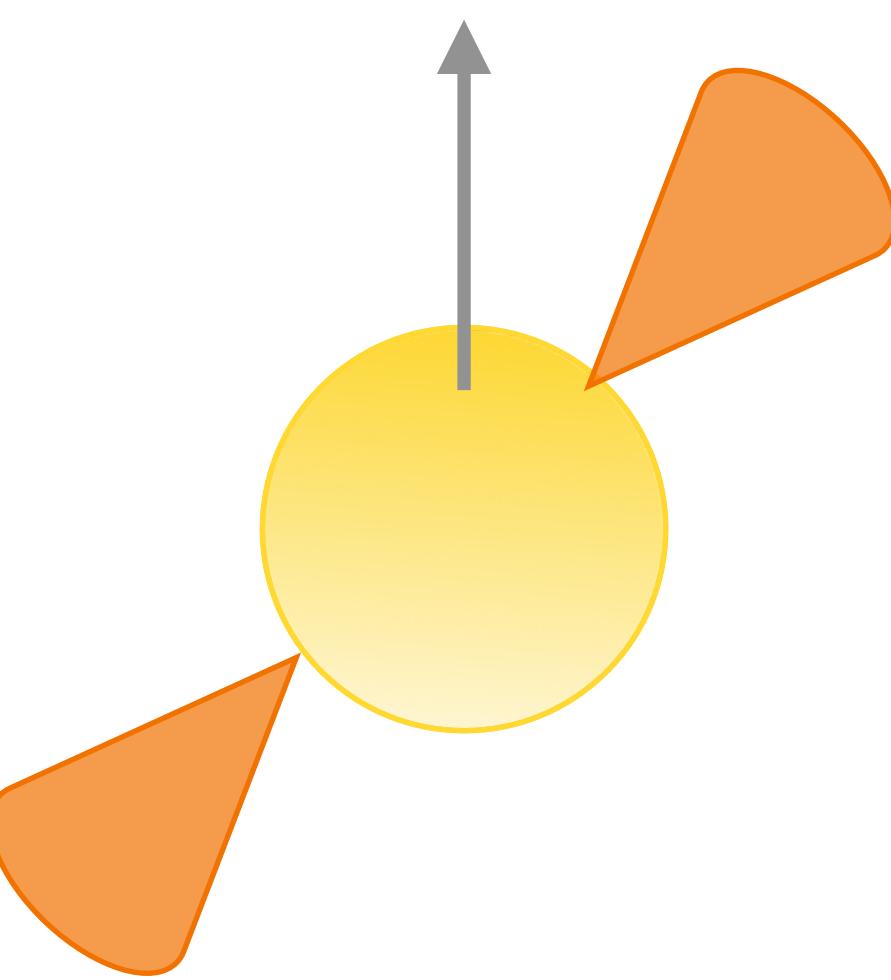
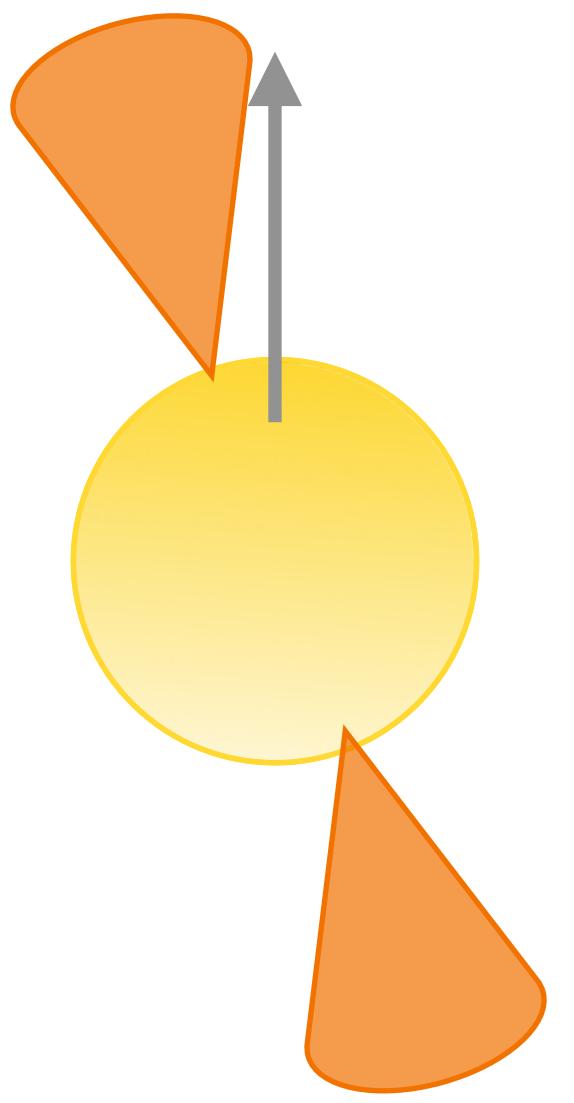
Paris workshop on primordial black holes and gravitational waves

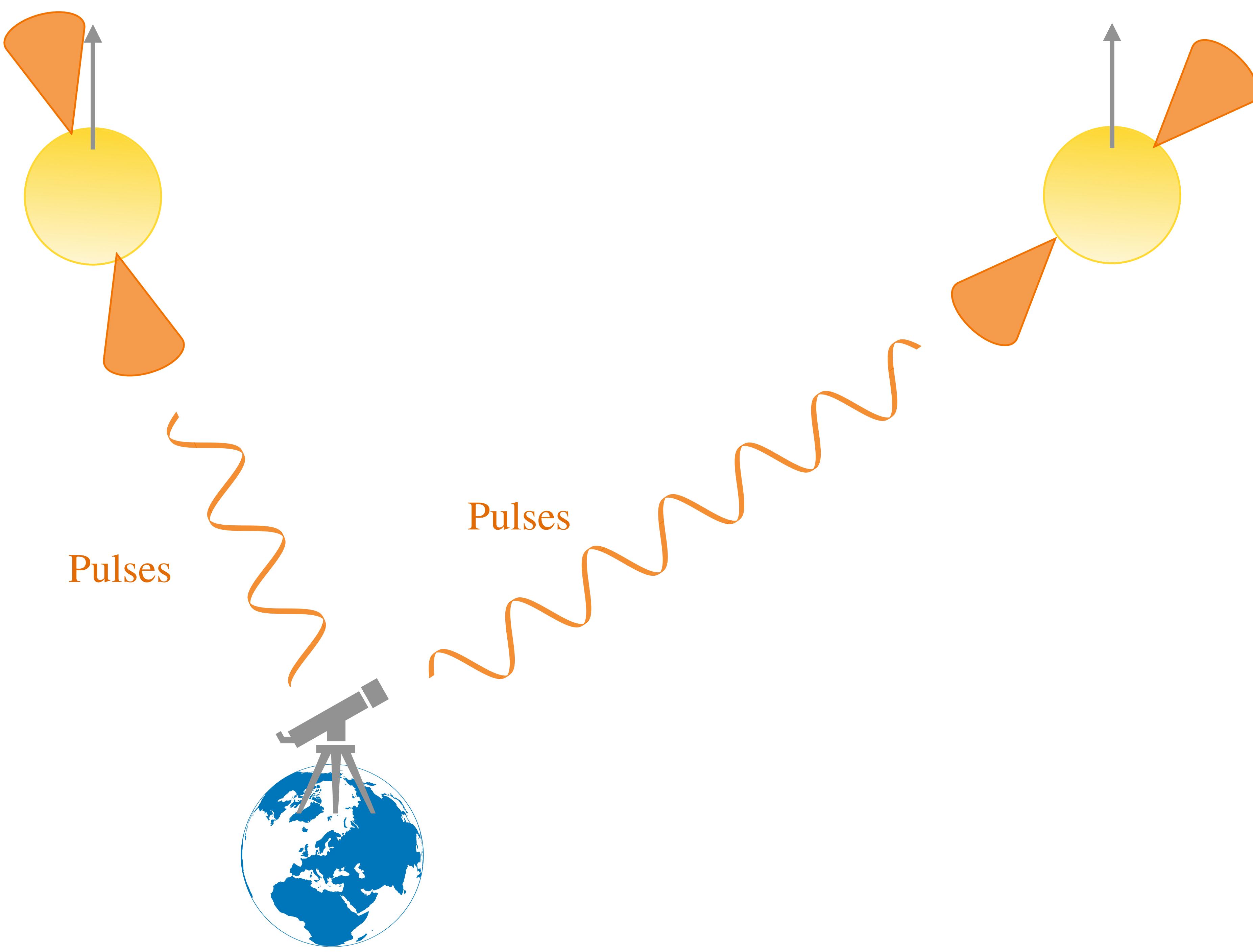
Postdoc in Tel Aviv U.

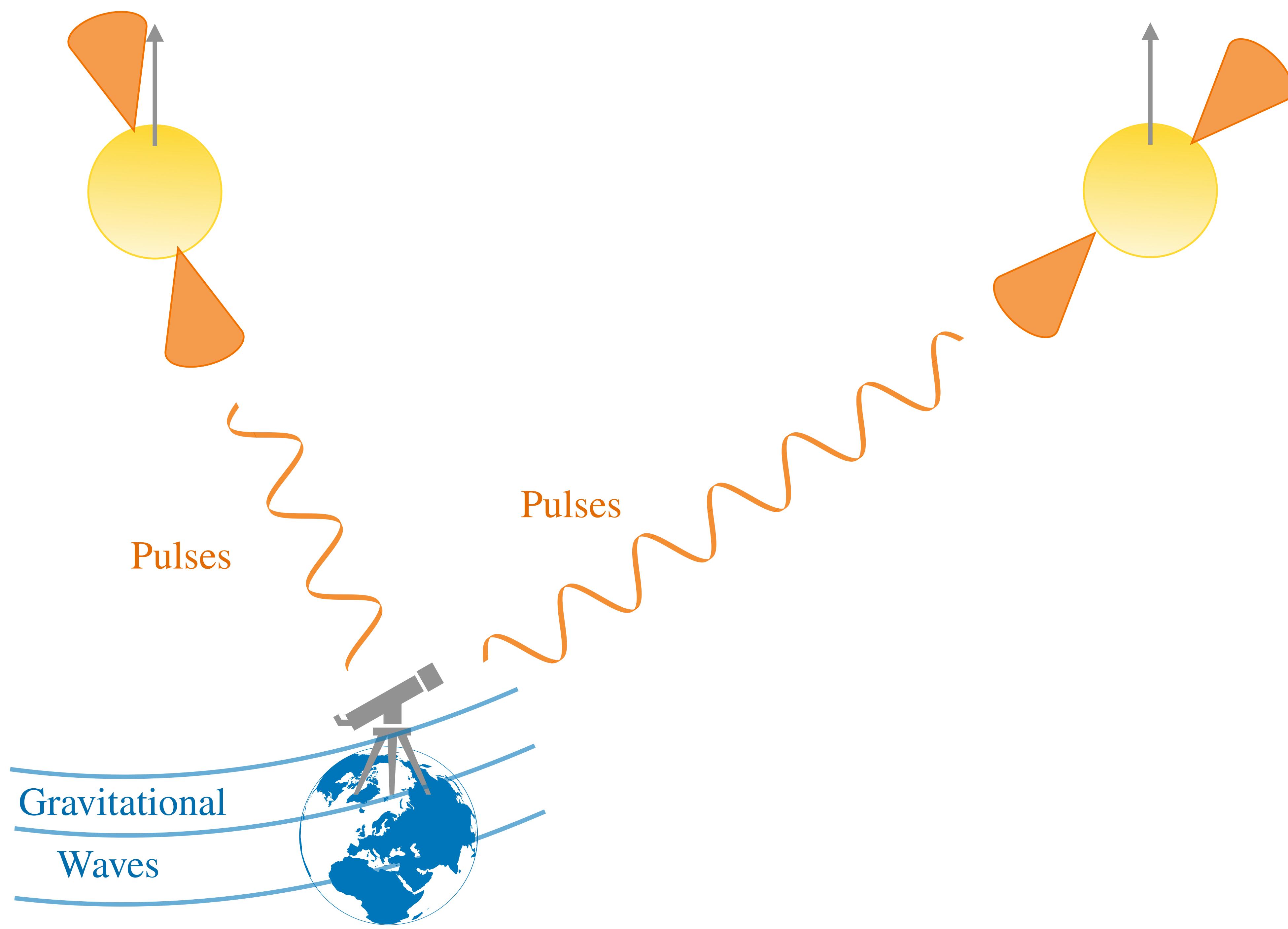
Azrieli International Postdoctoral Fellows

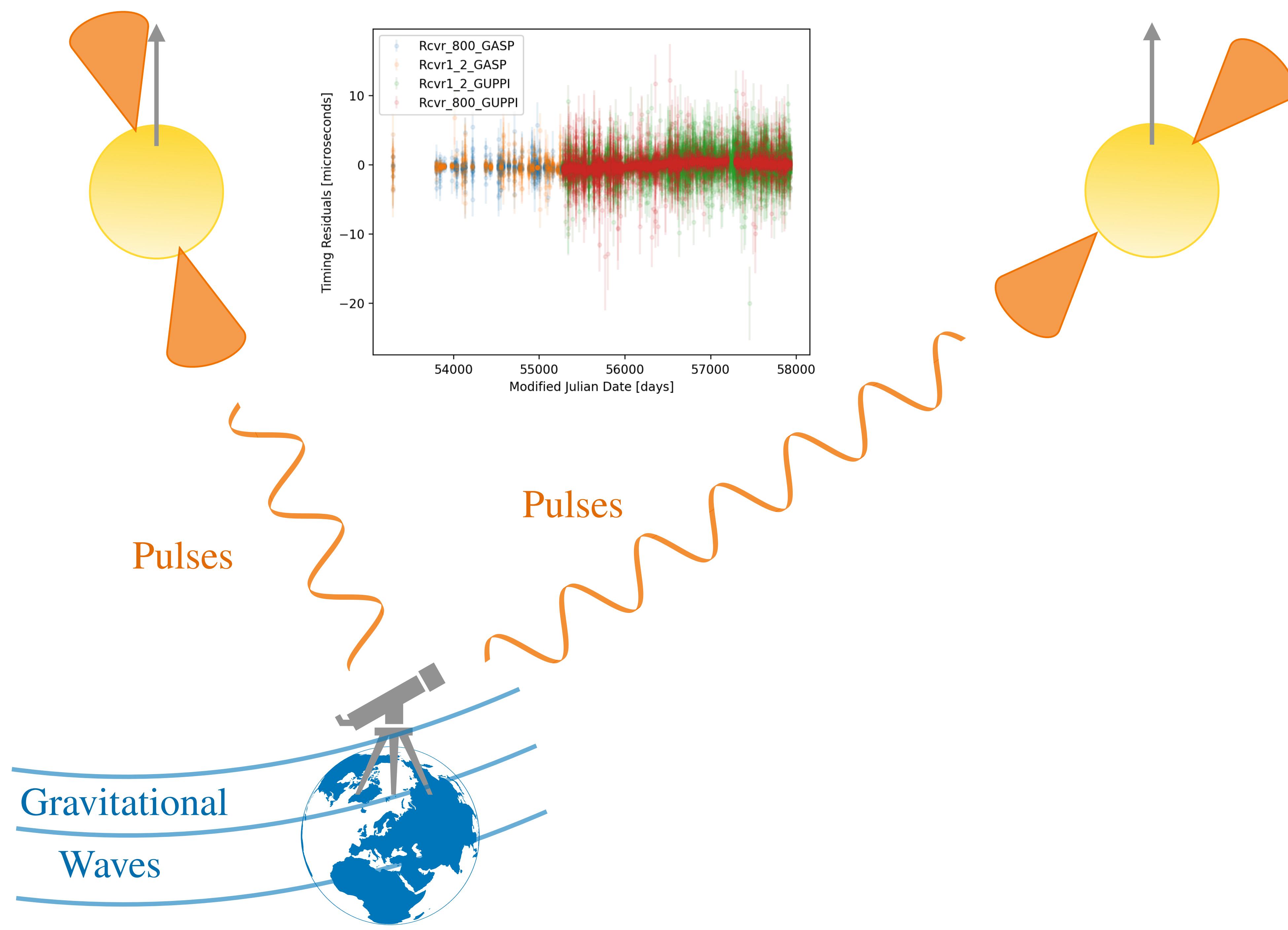
Fondation
Azrieli
Foundation

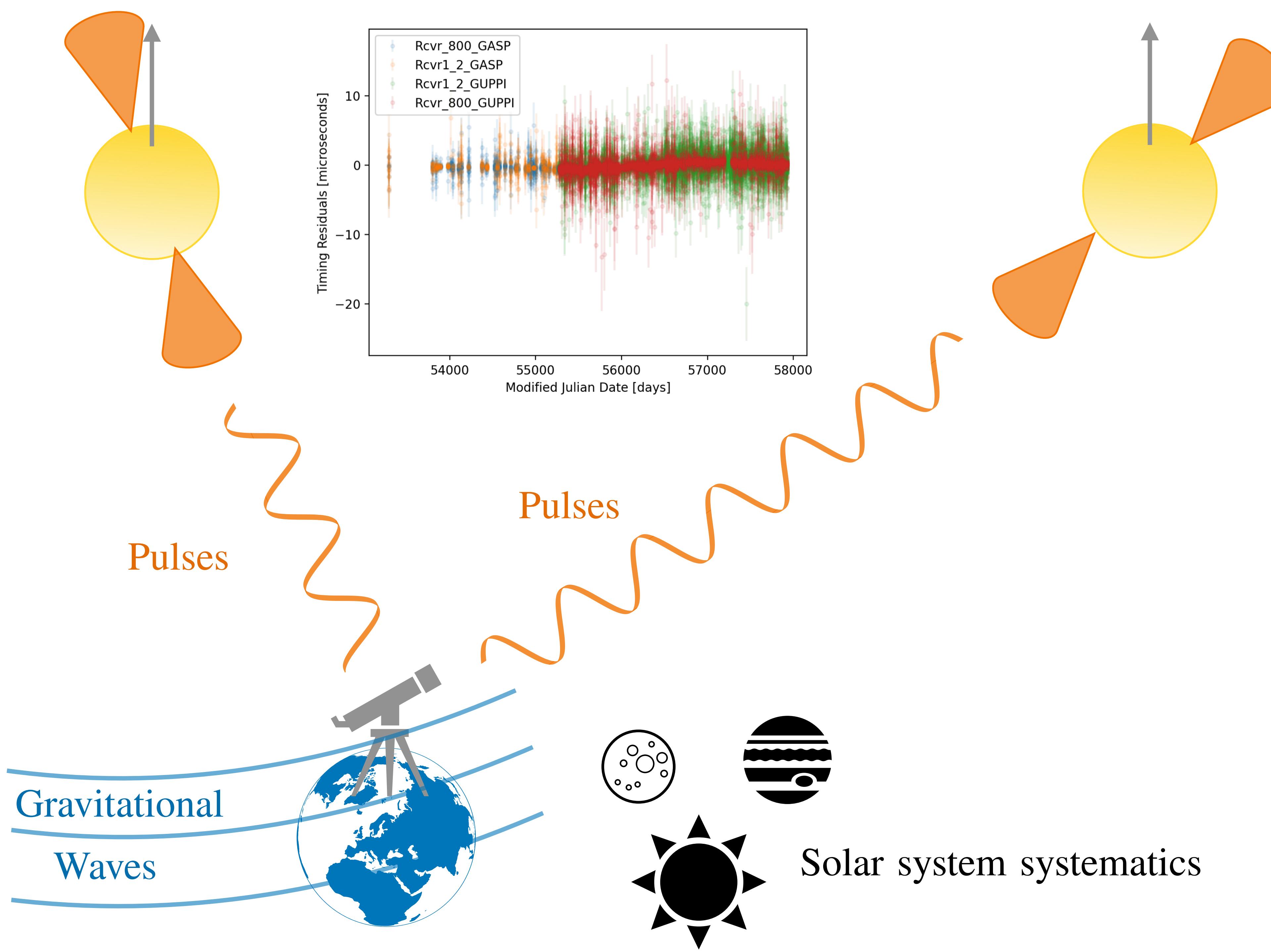


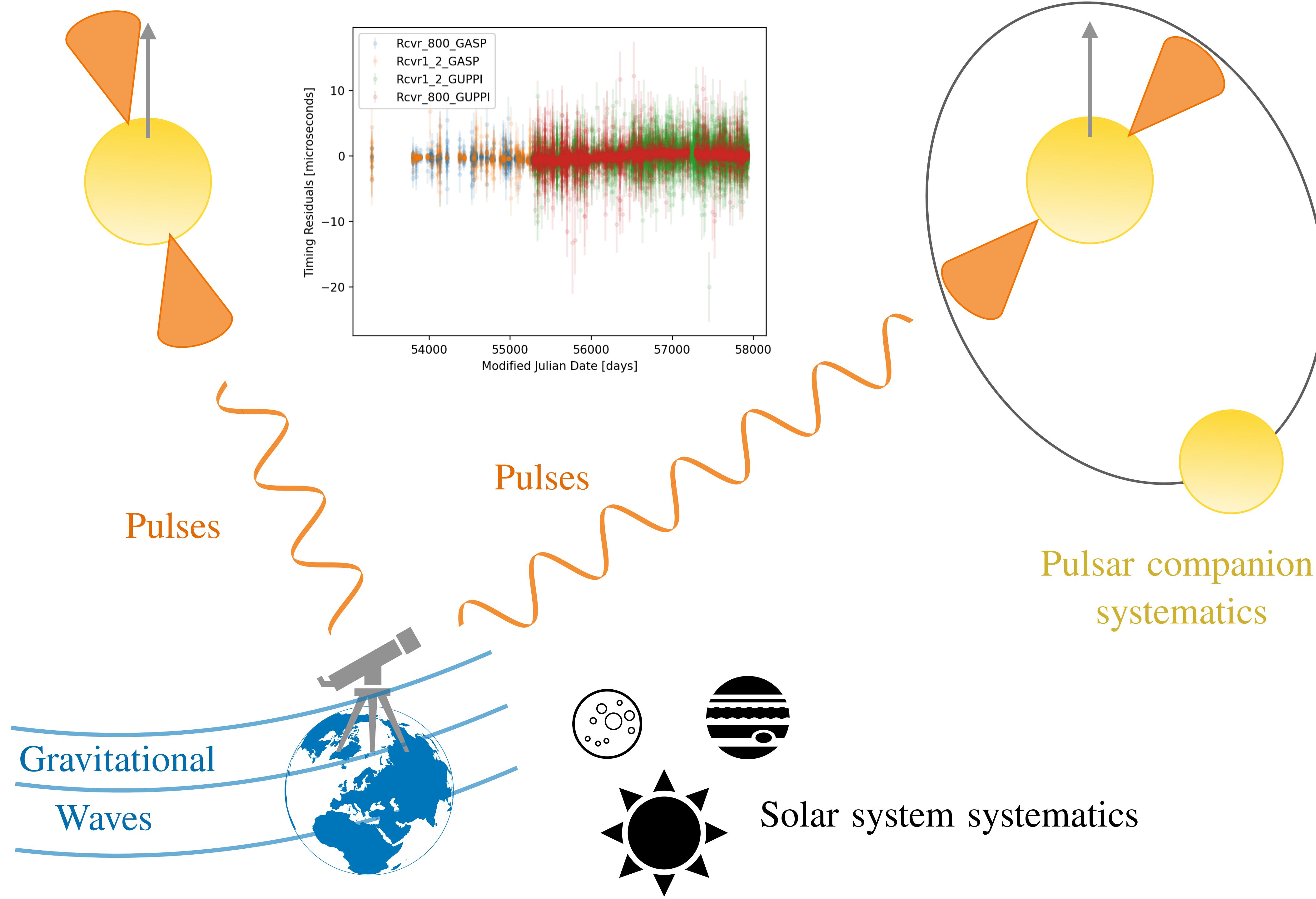


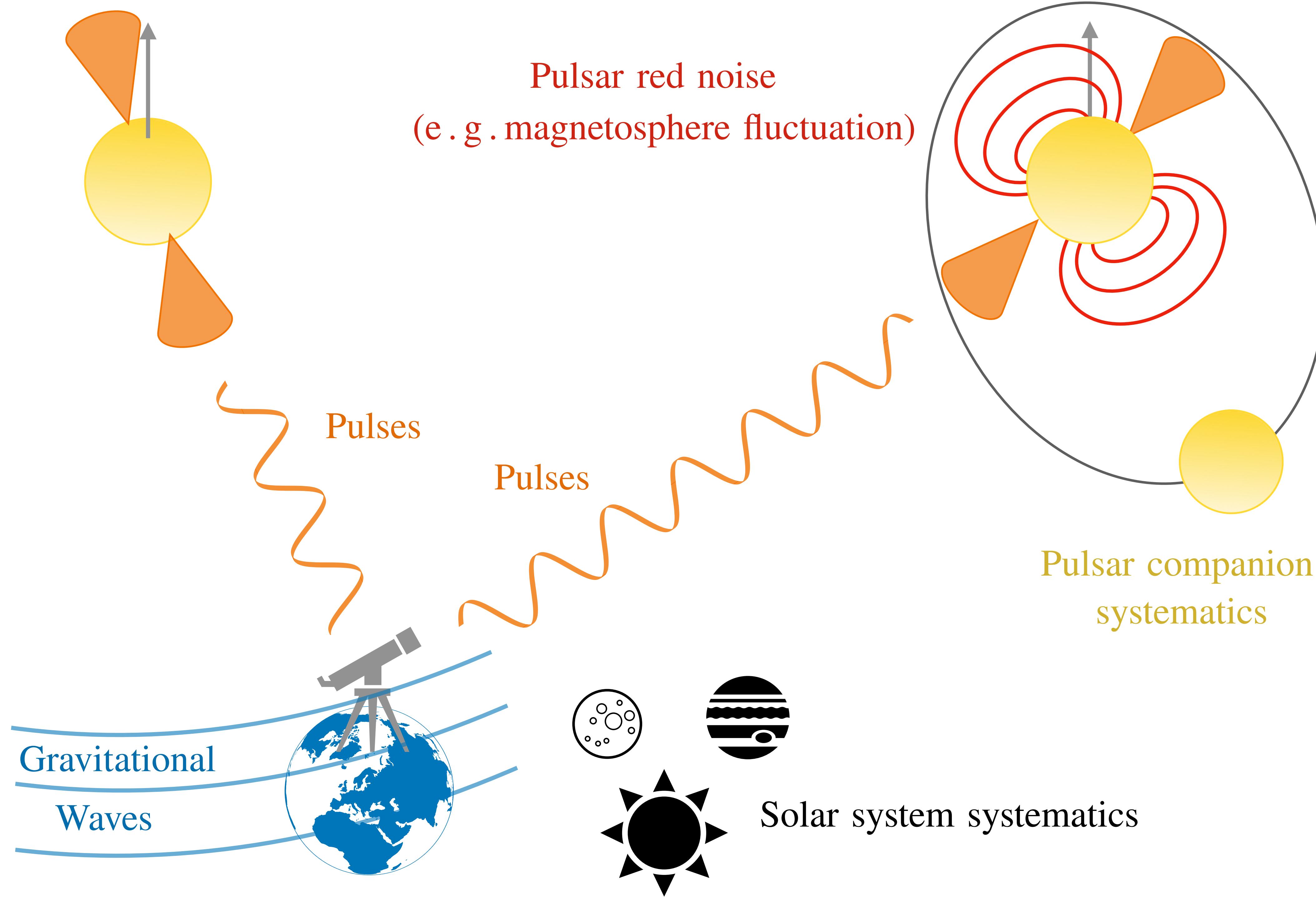


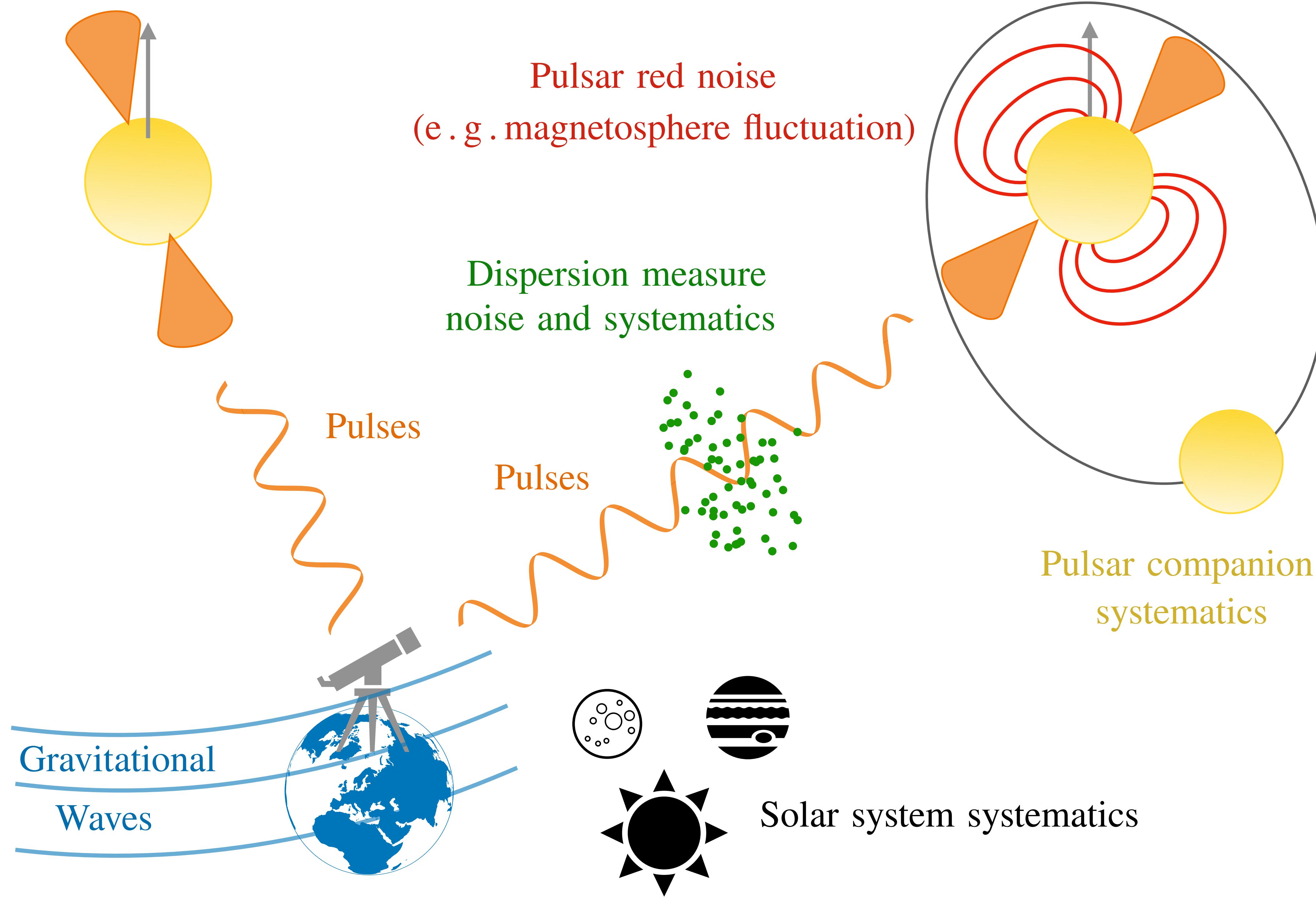


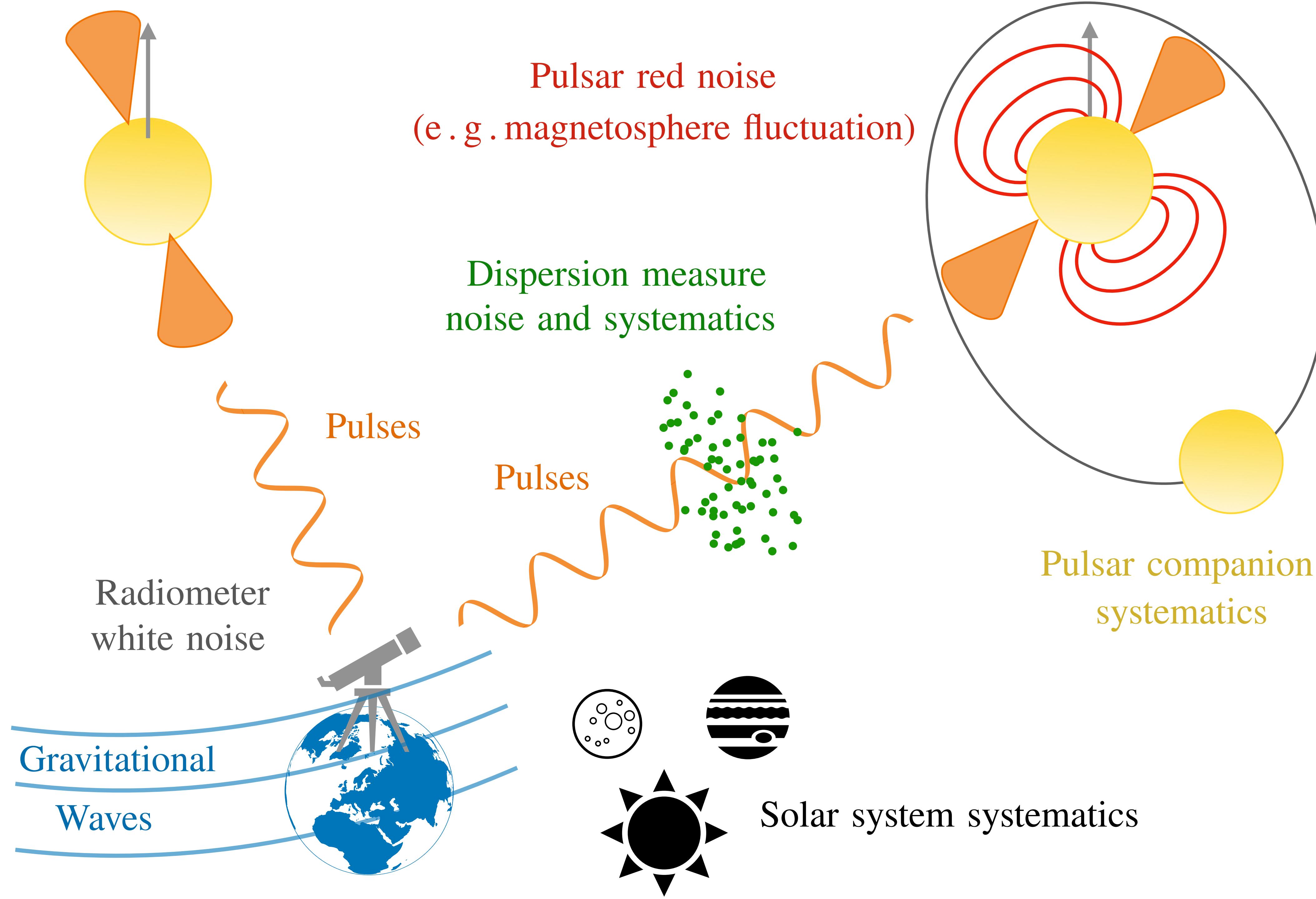


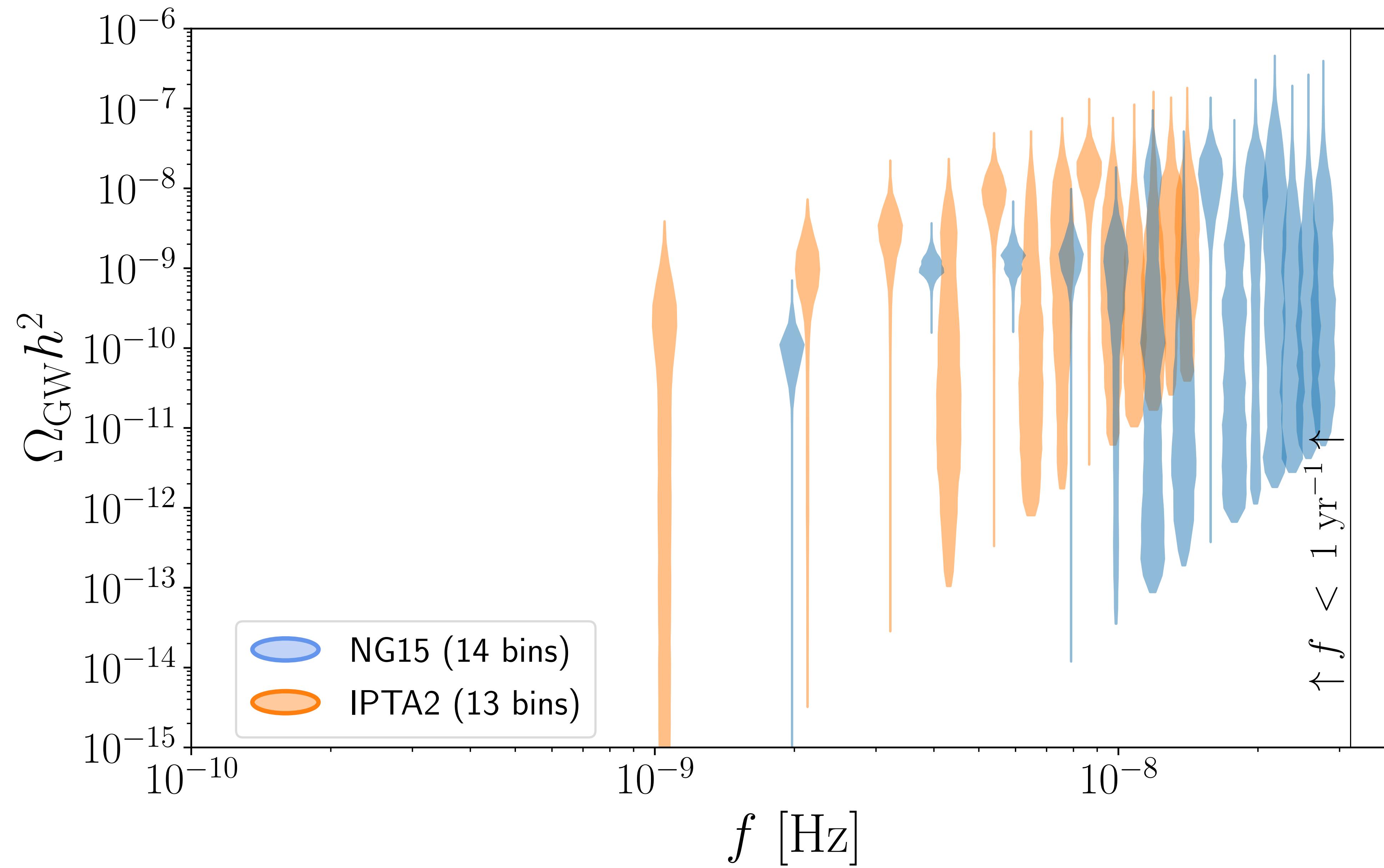




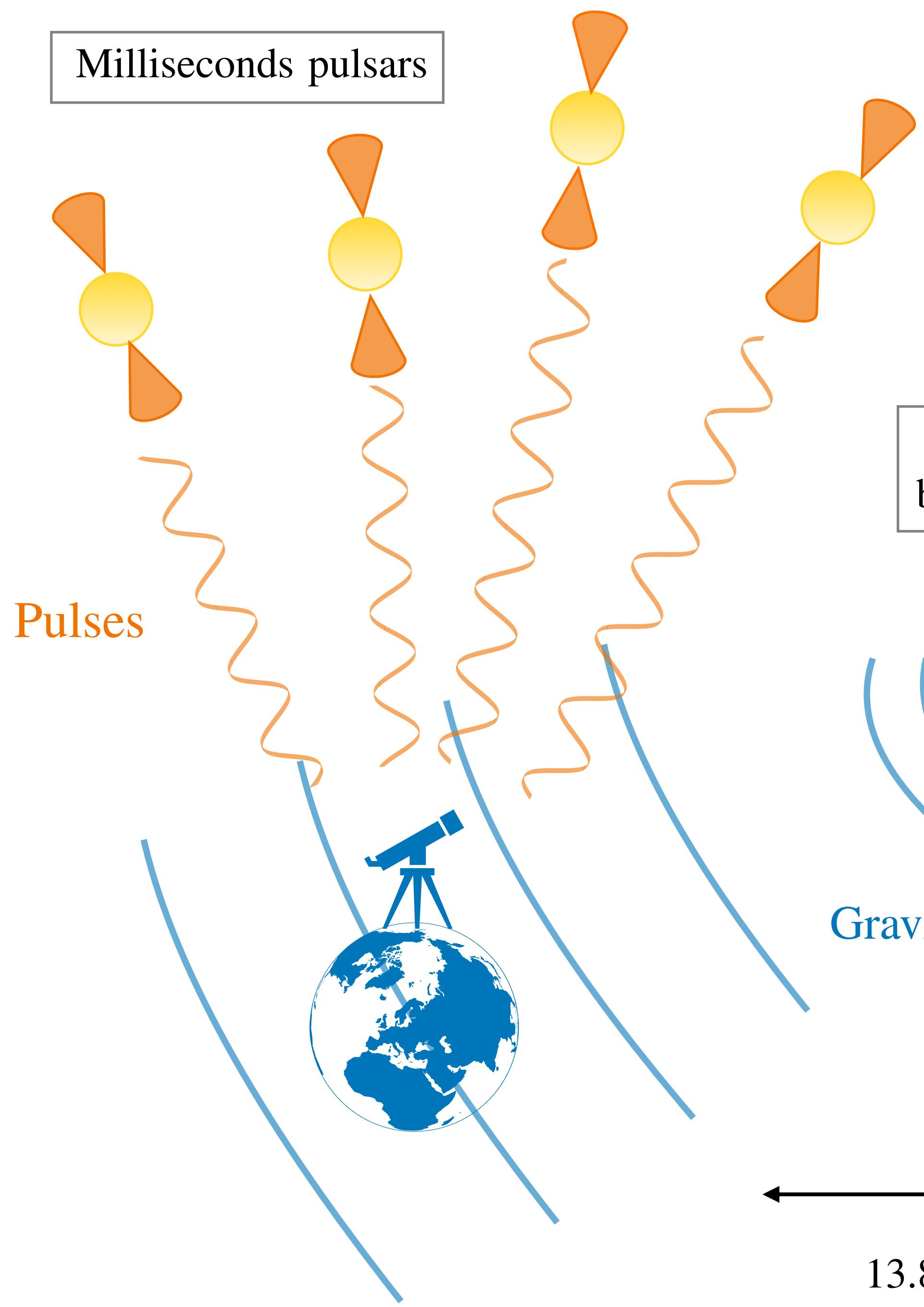








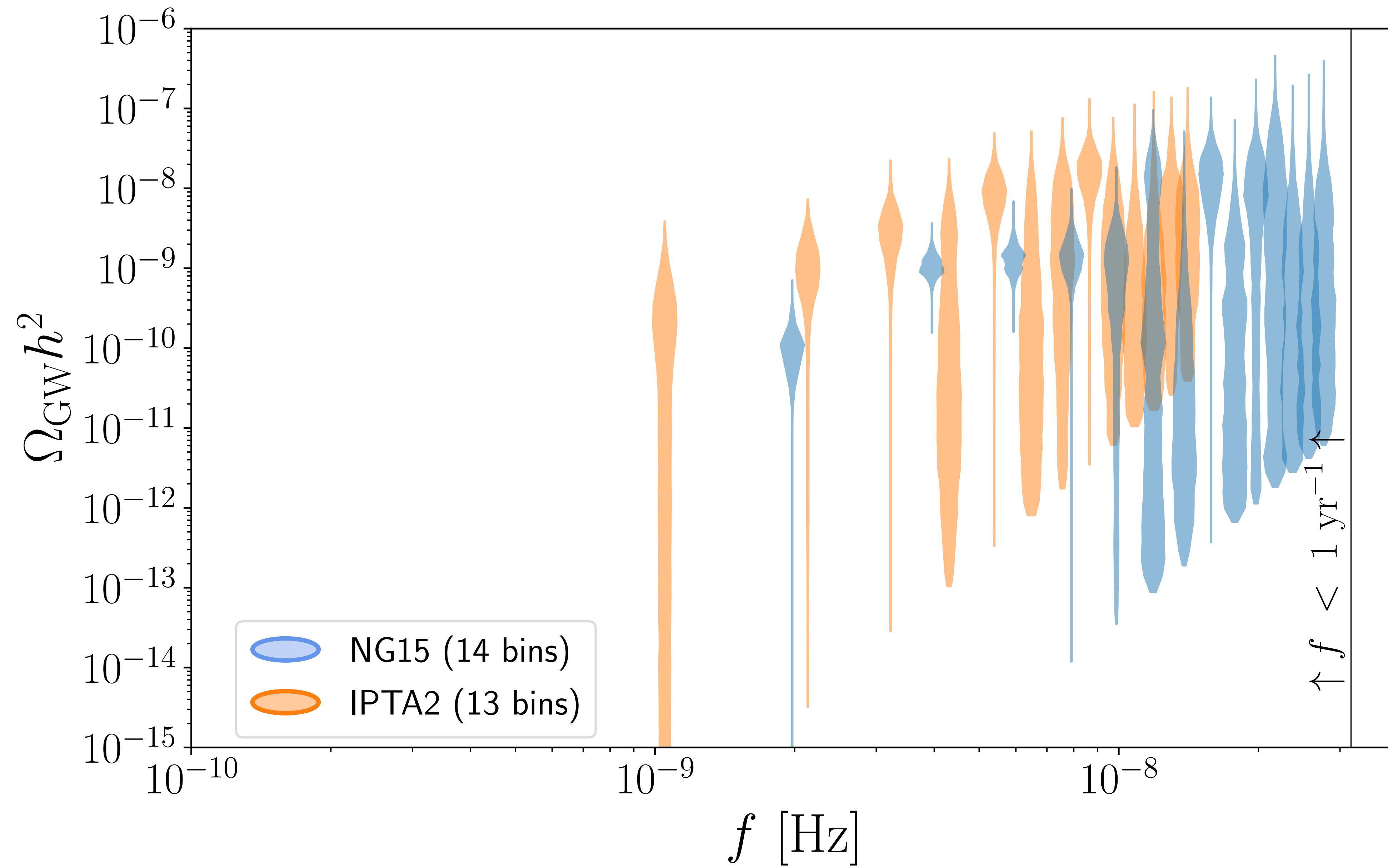
Milliseconds pulsars

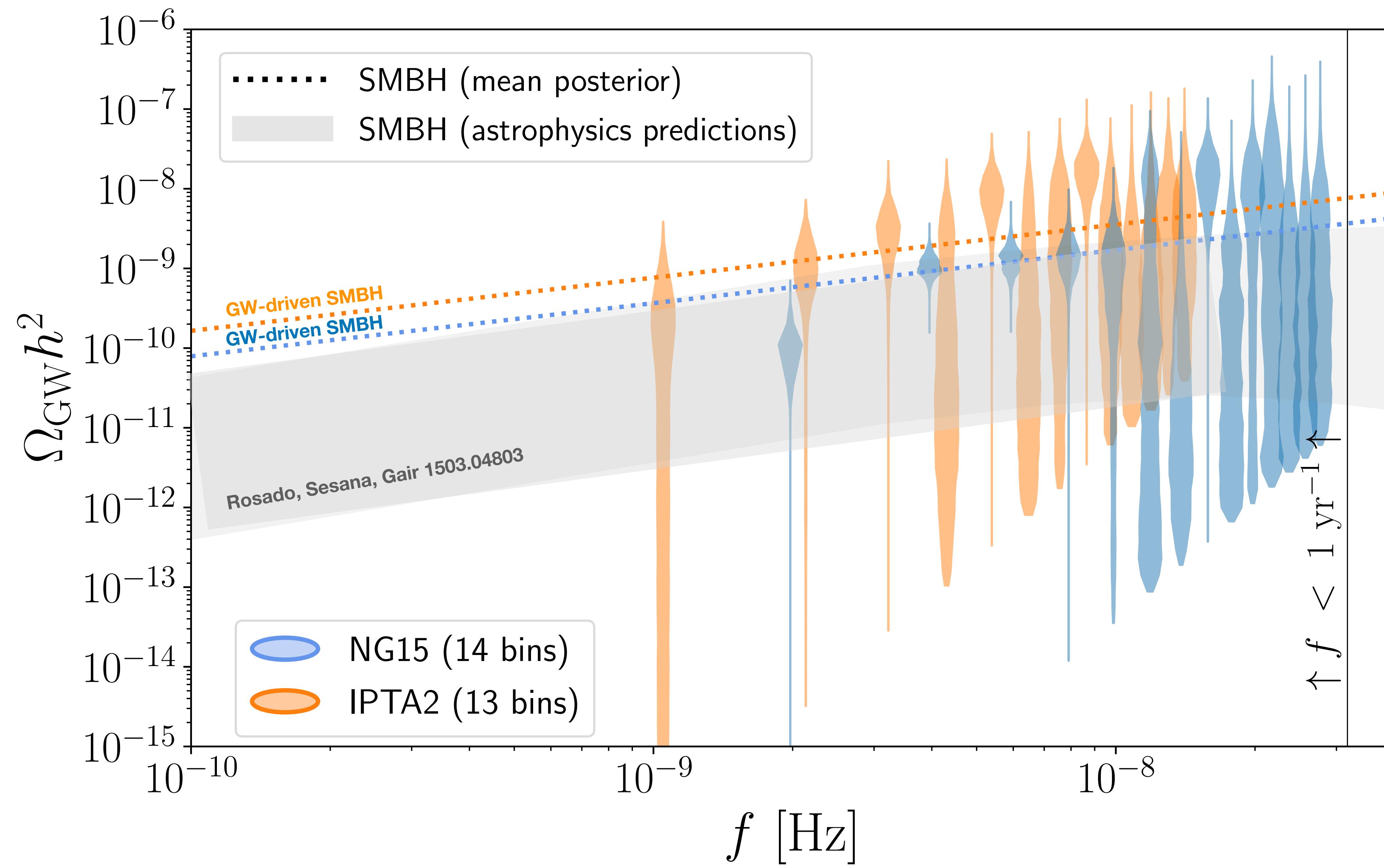


Supermassive
black holes binaries

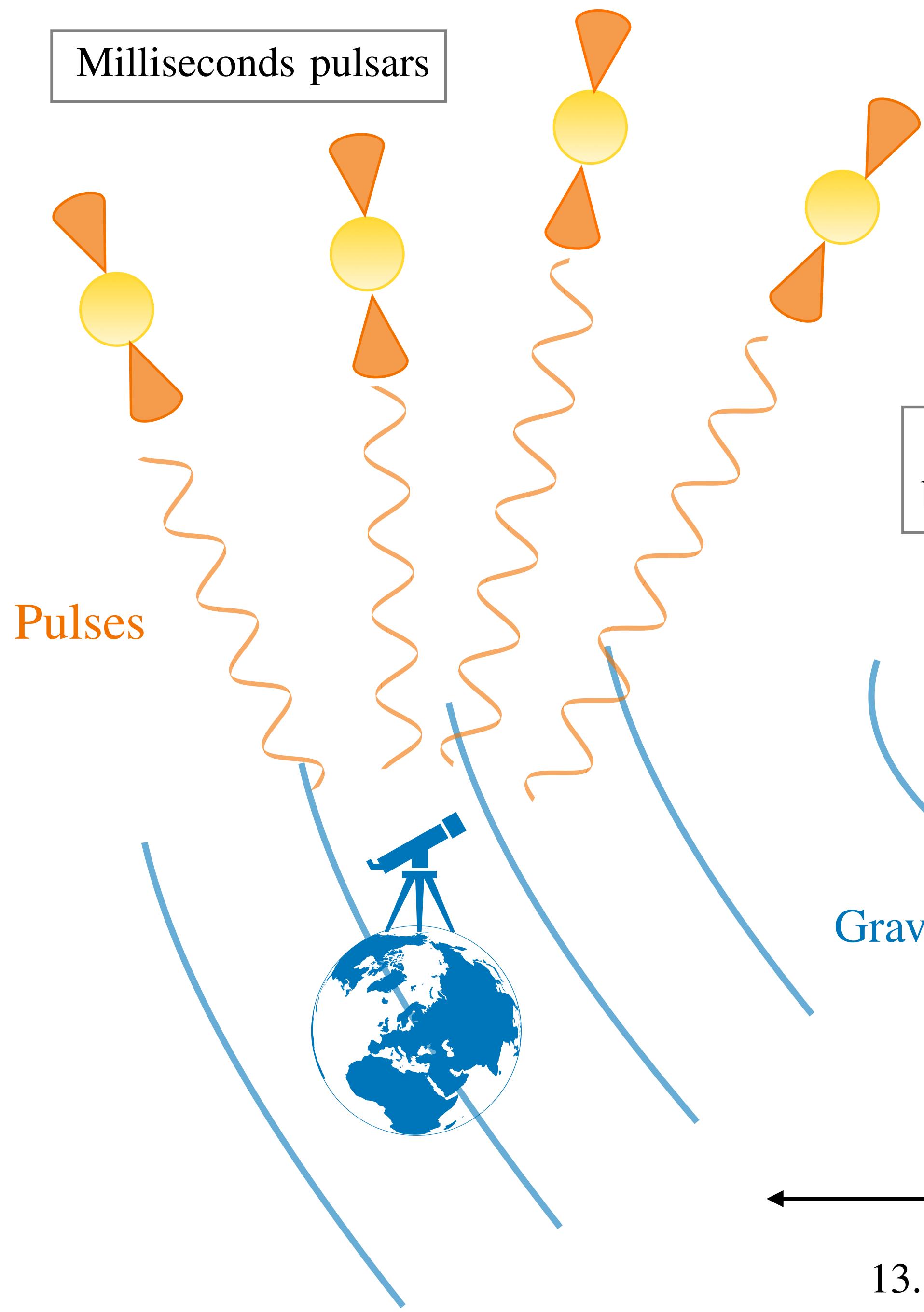
Gravitational Waves

$13.8 \text{ Gyr} \gtrsim t \gtrsim 500 \text{ Myr}$





Milliseconds pulsars

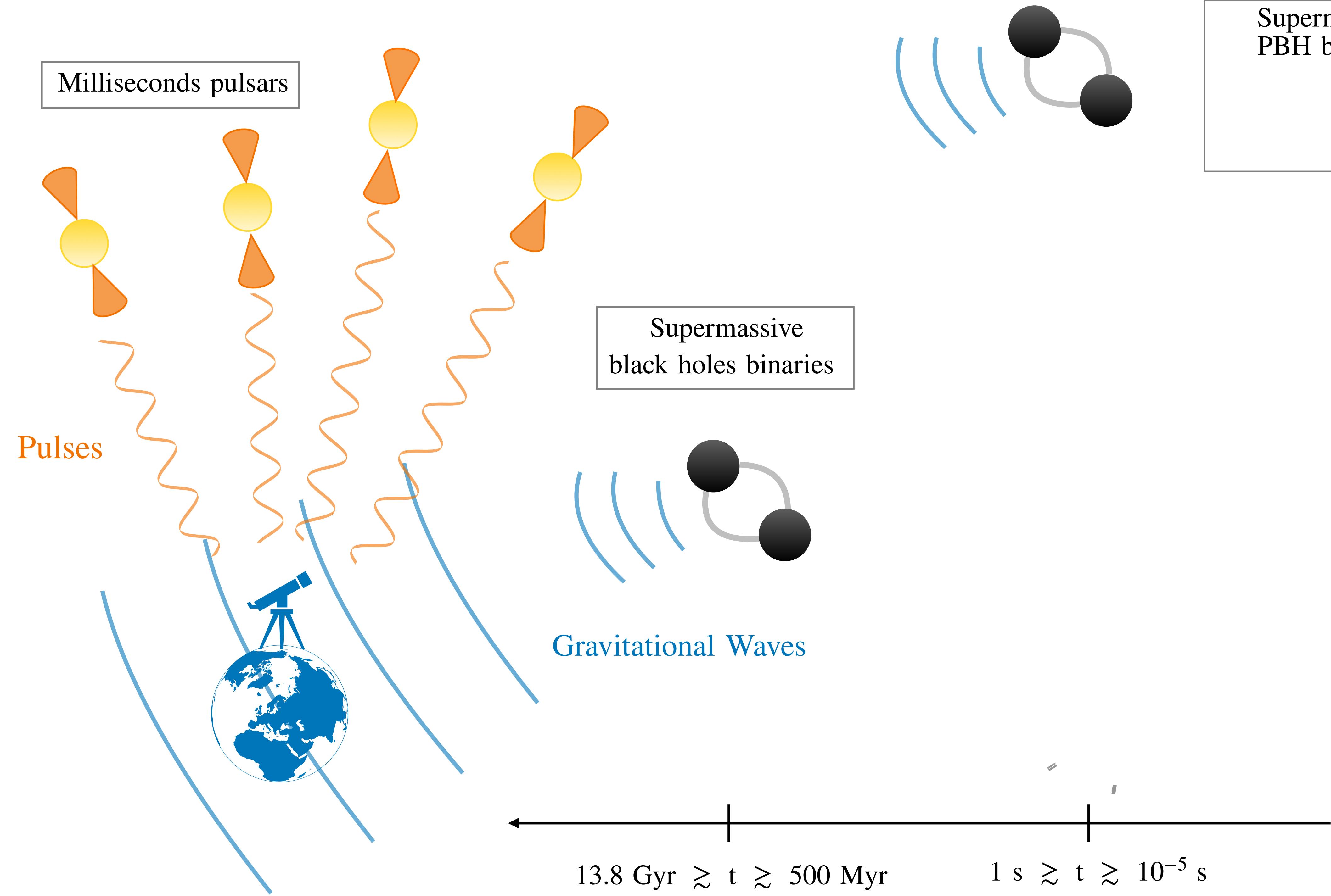


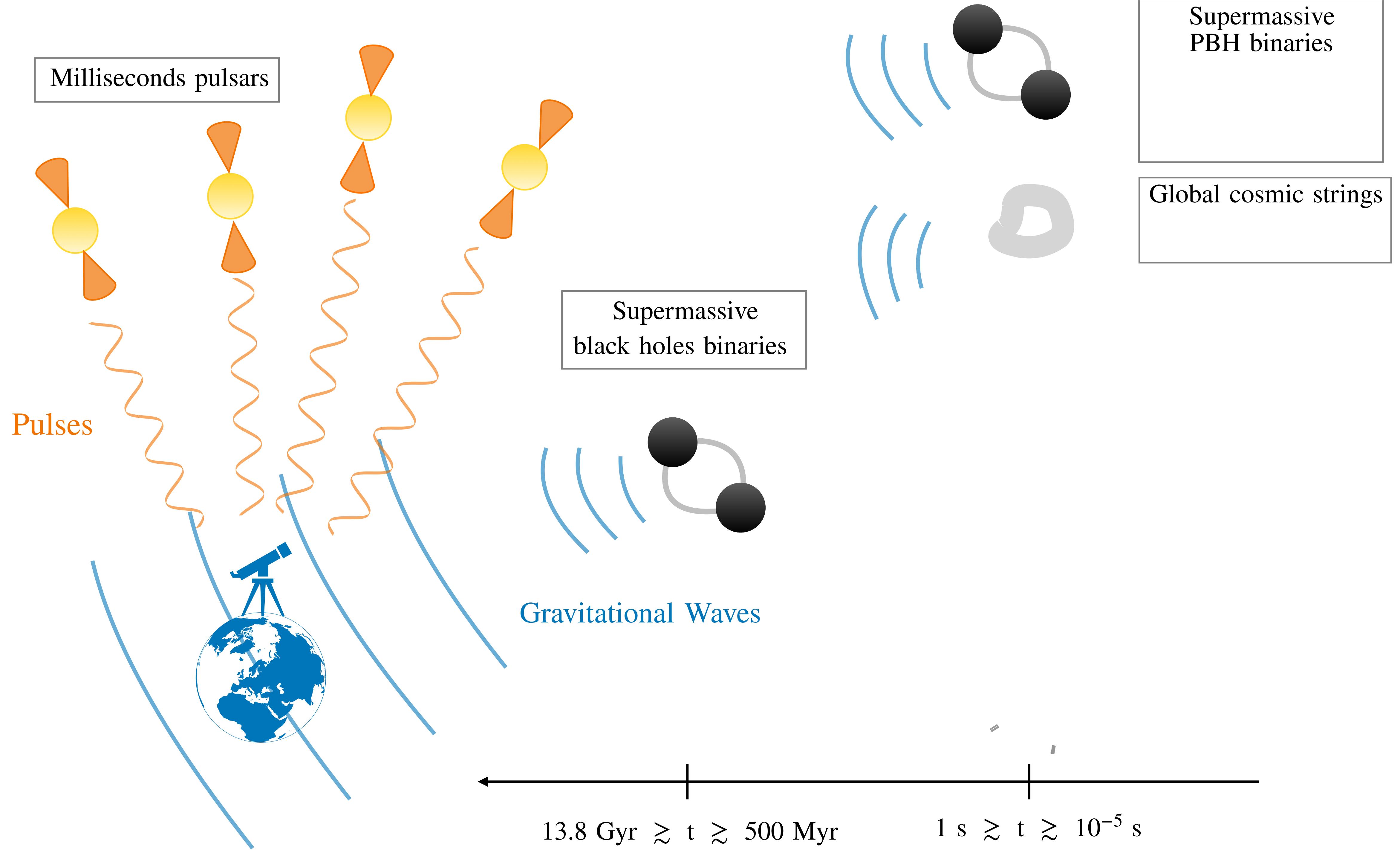
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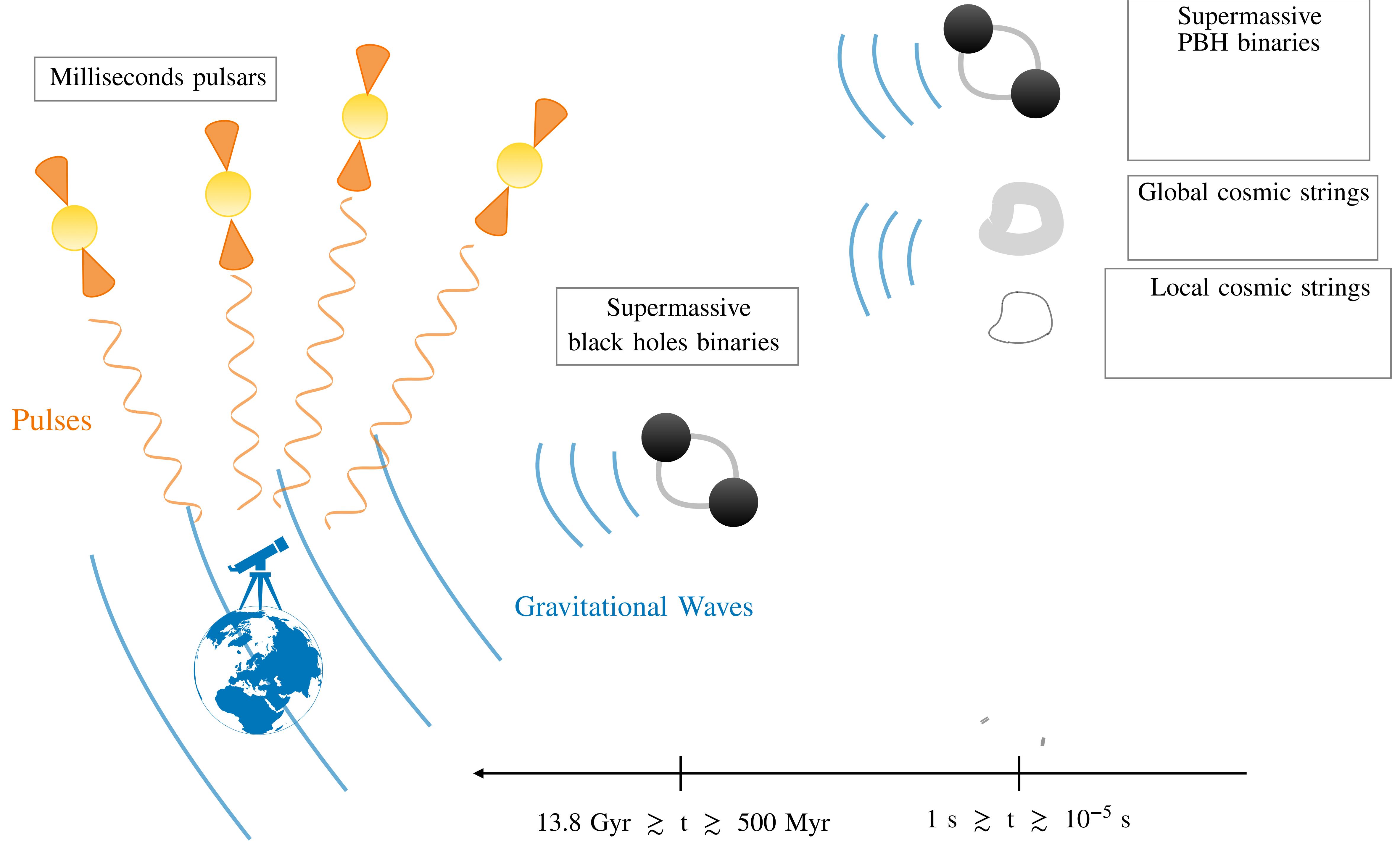
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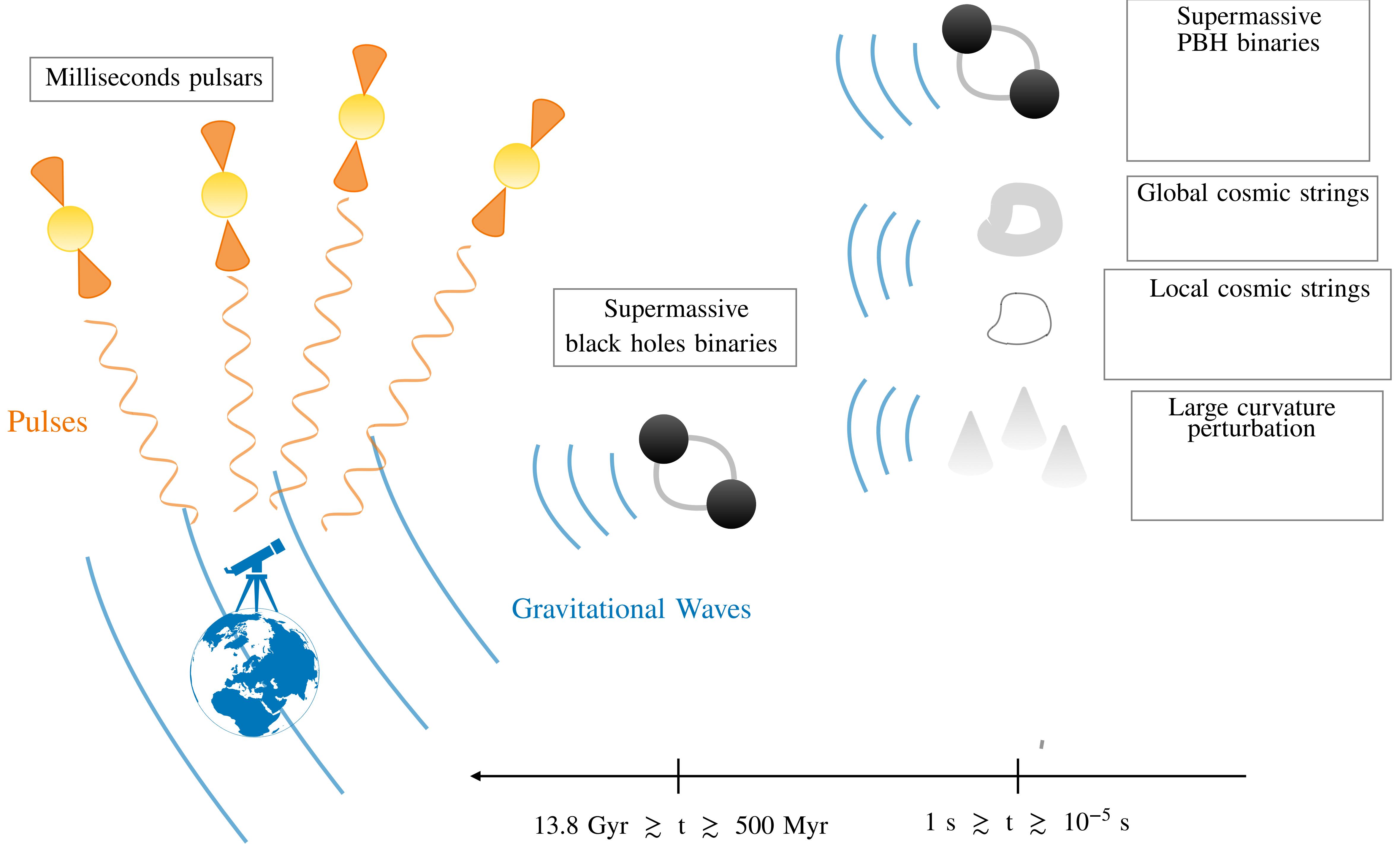
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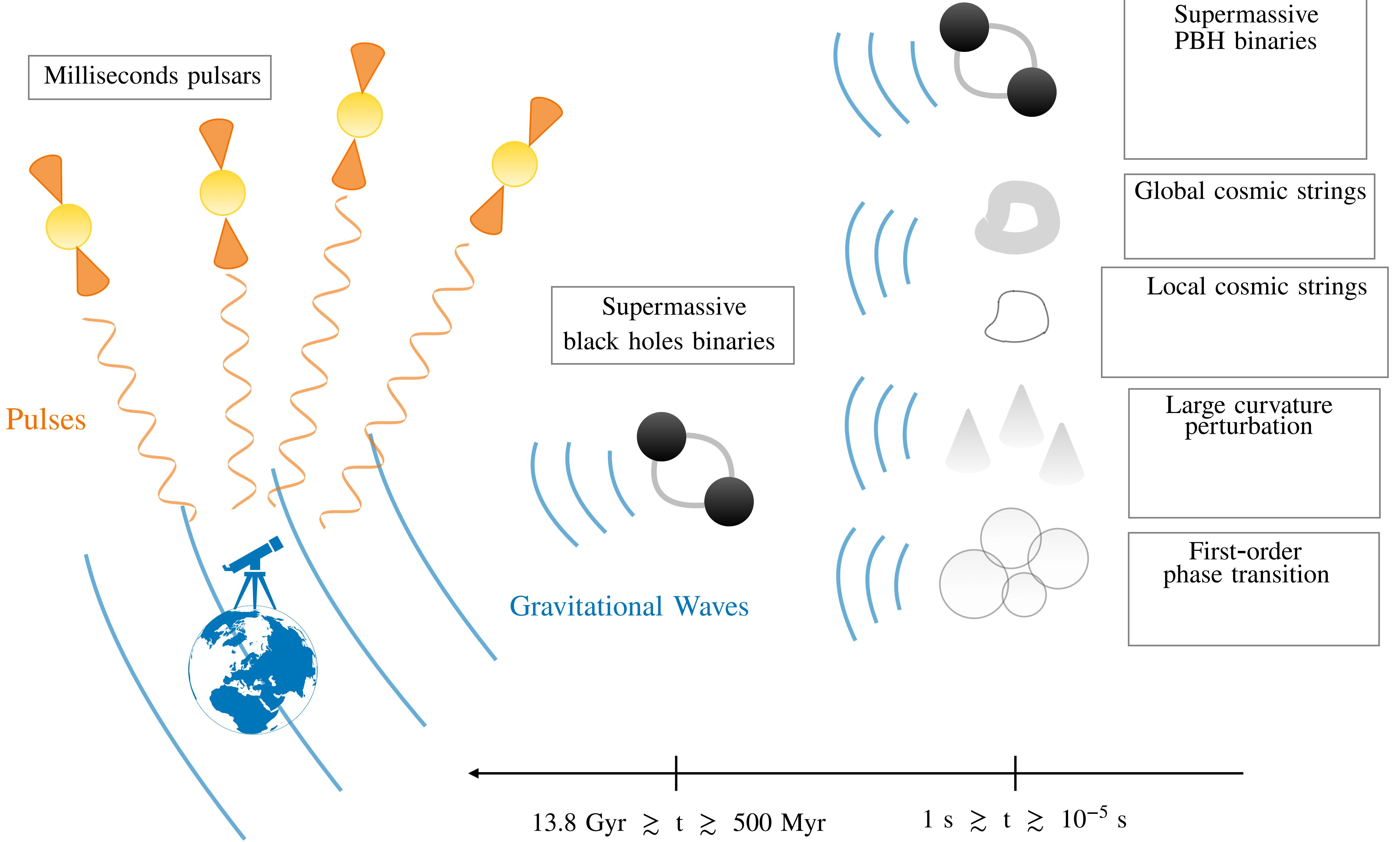
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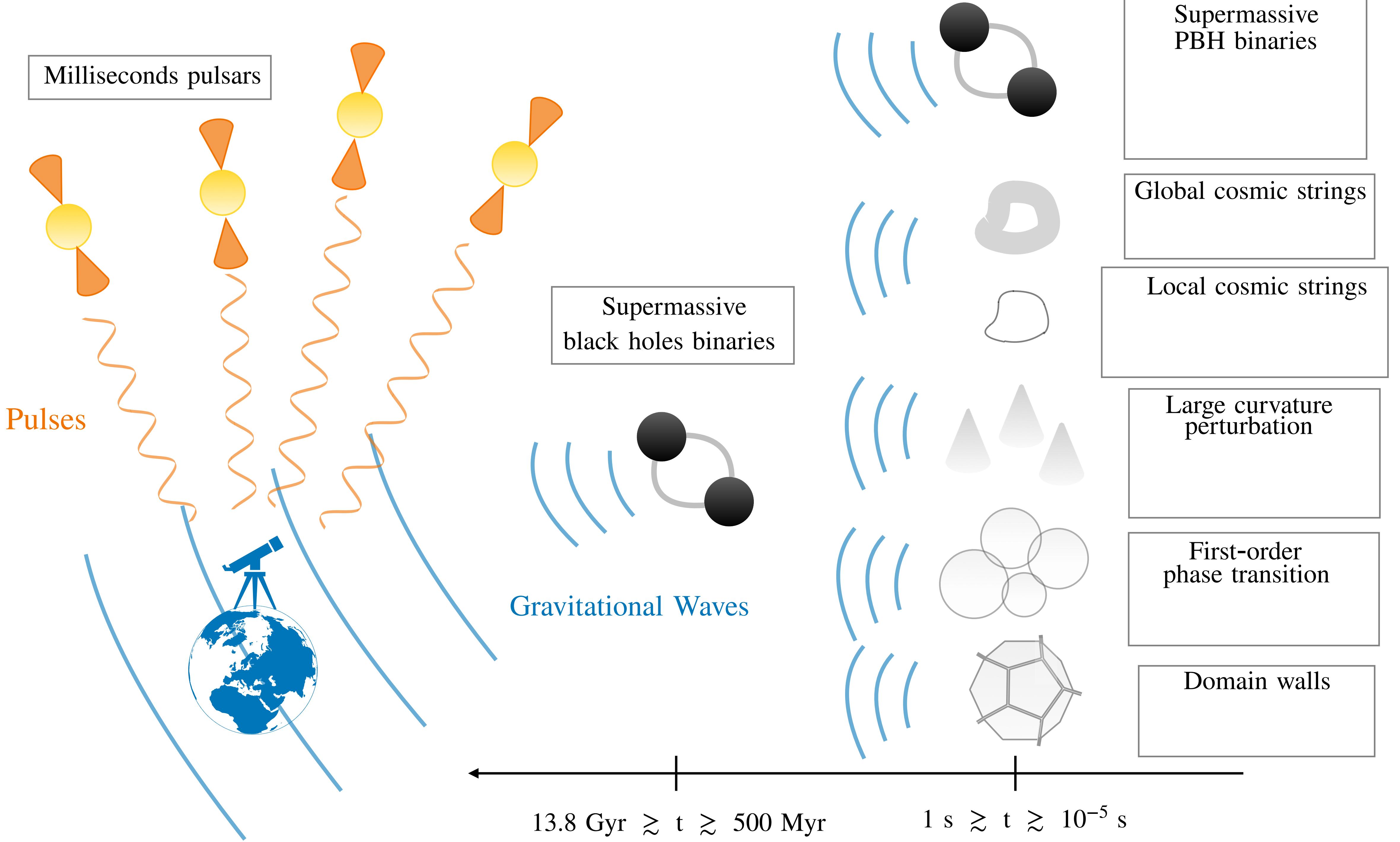


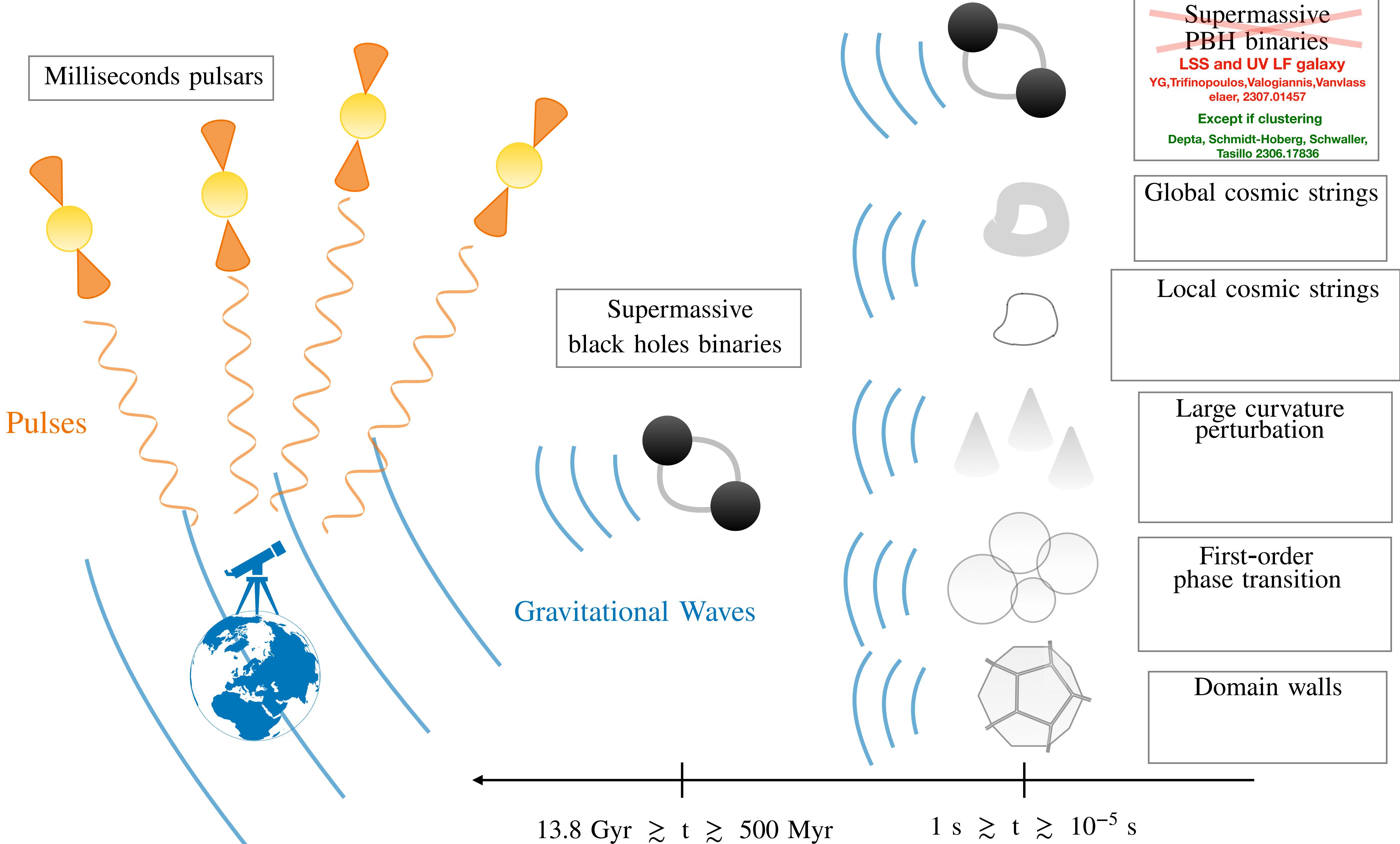


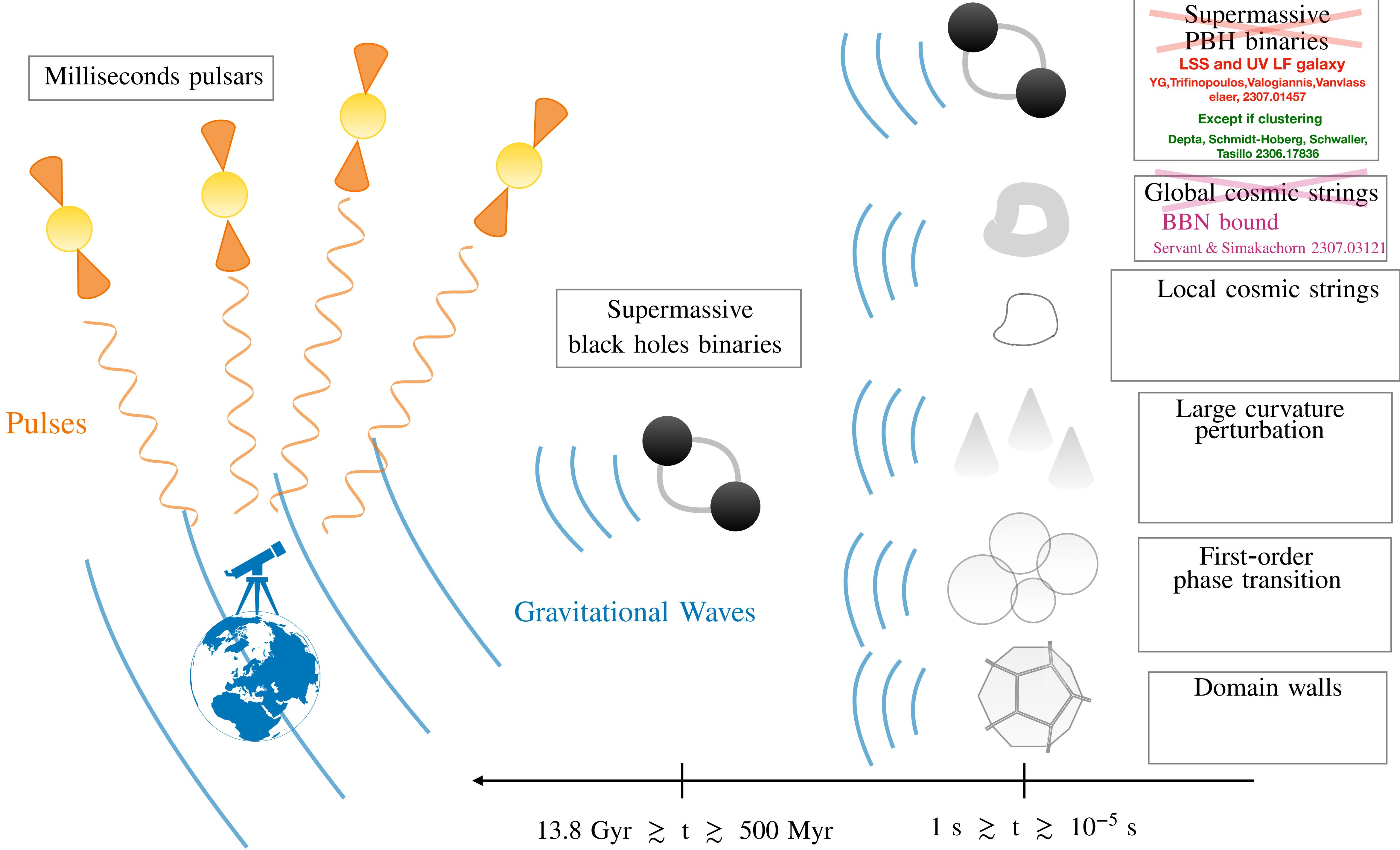


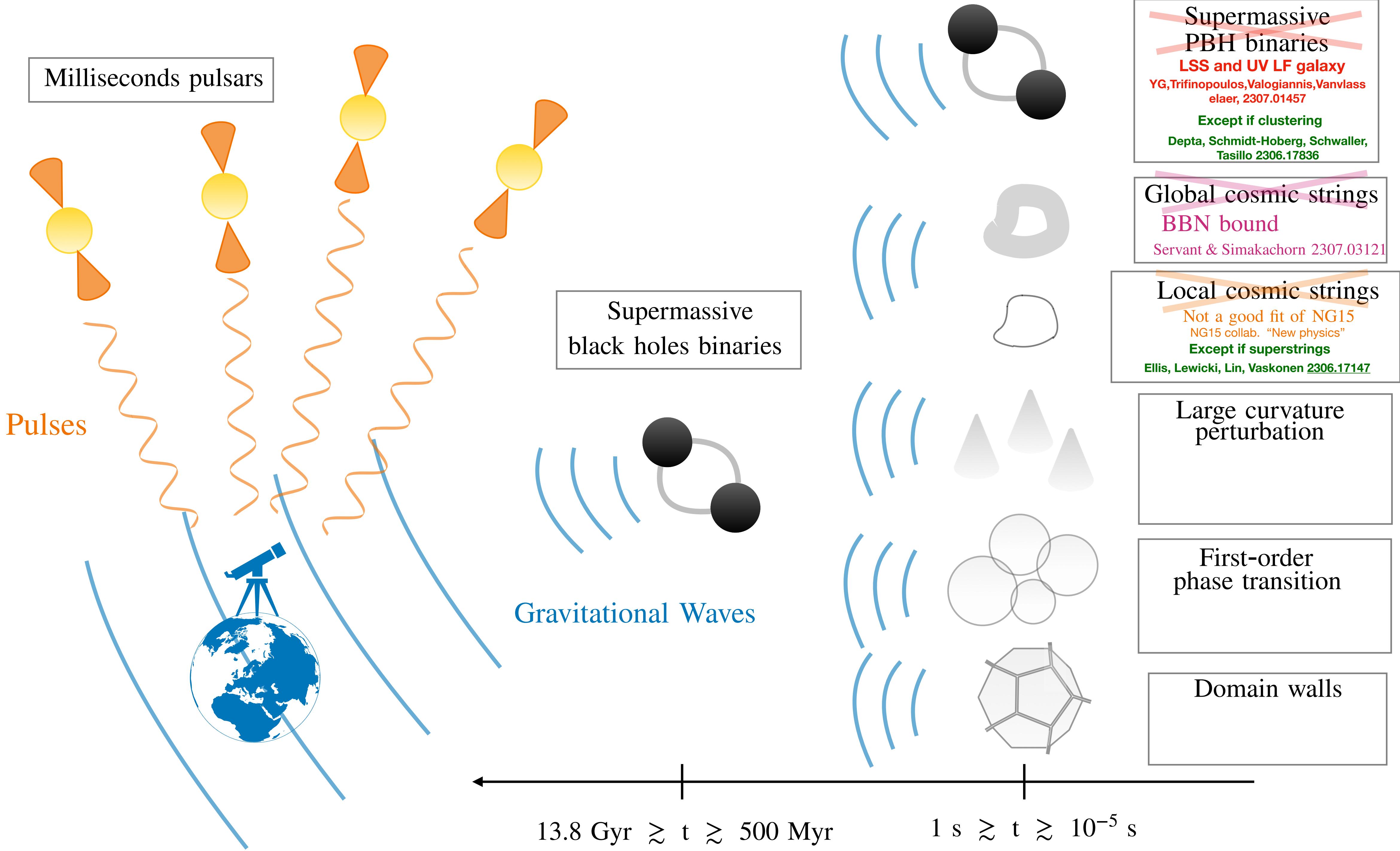


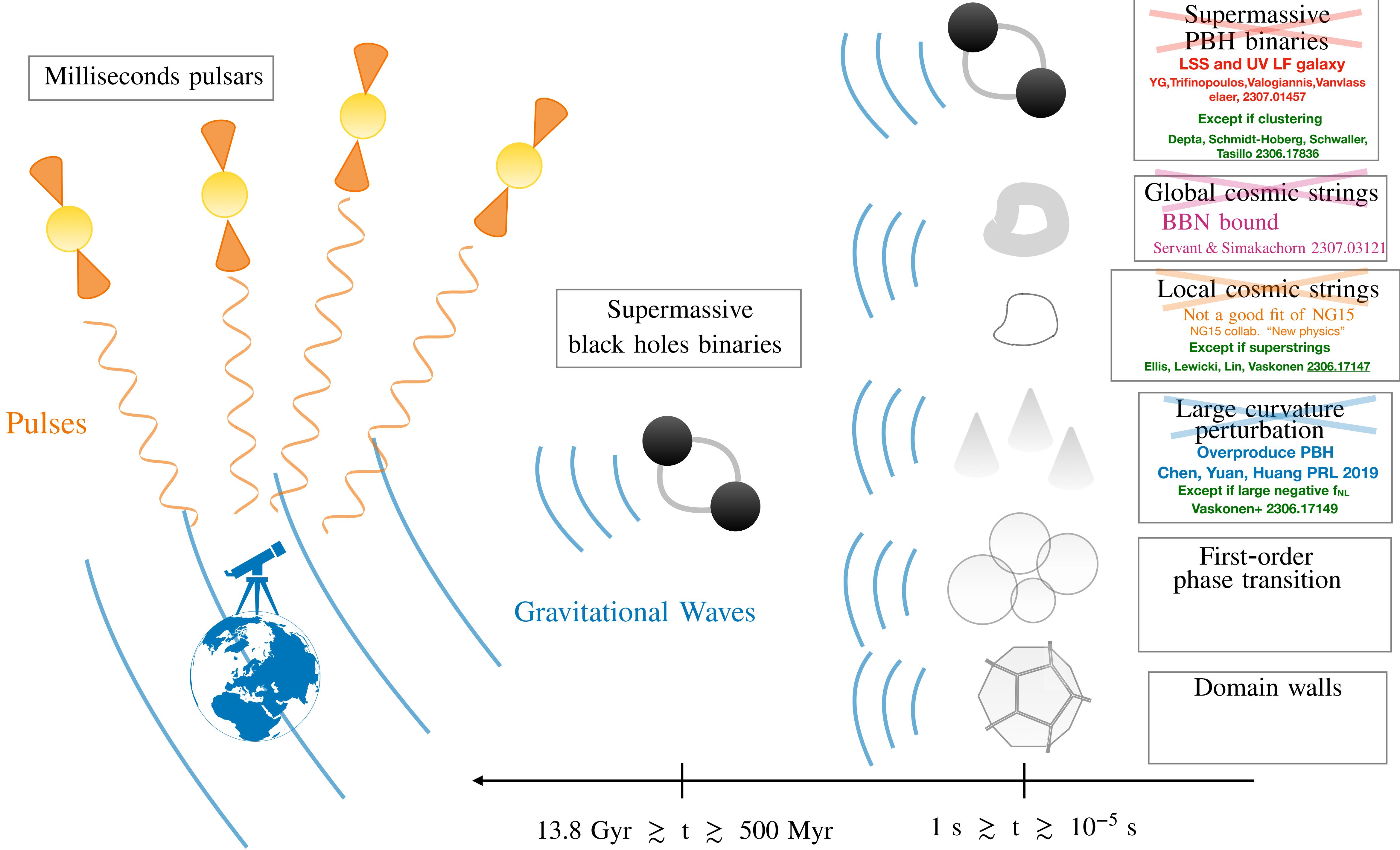


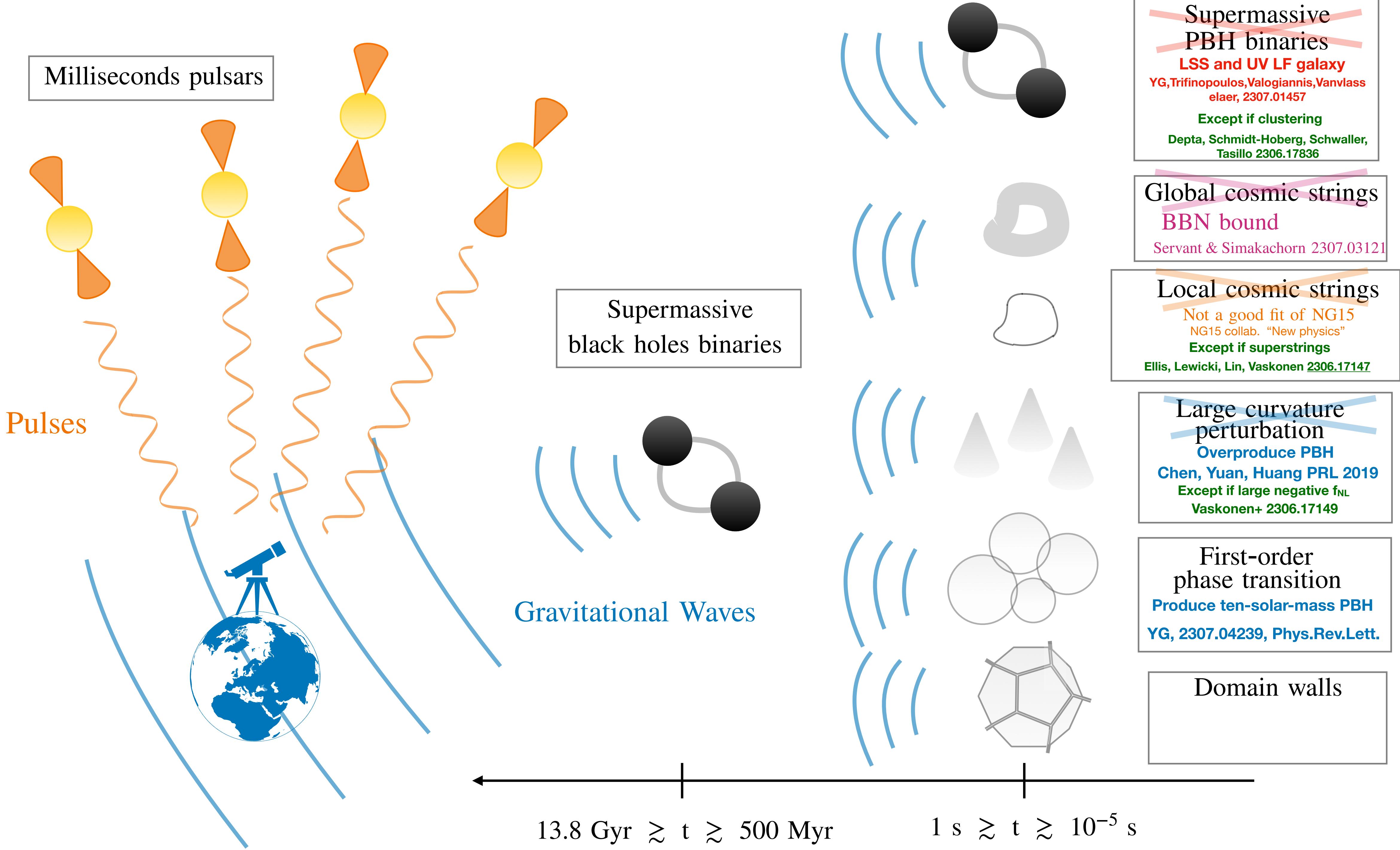


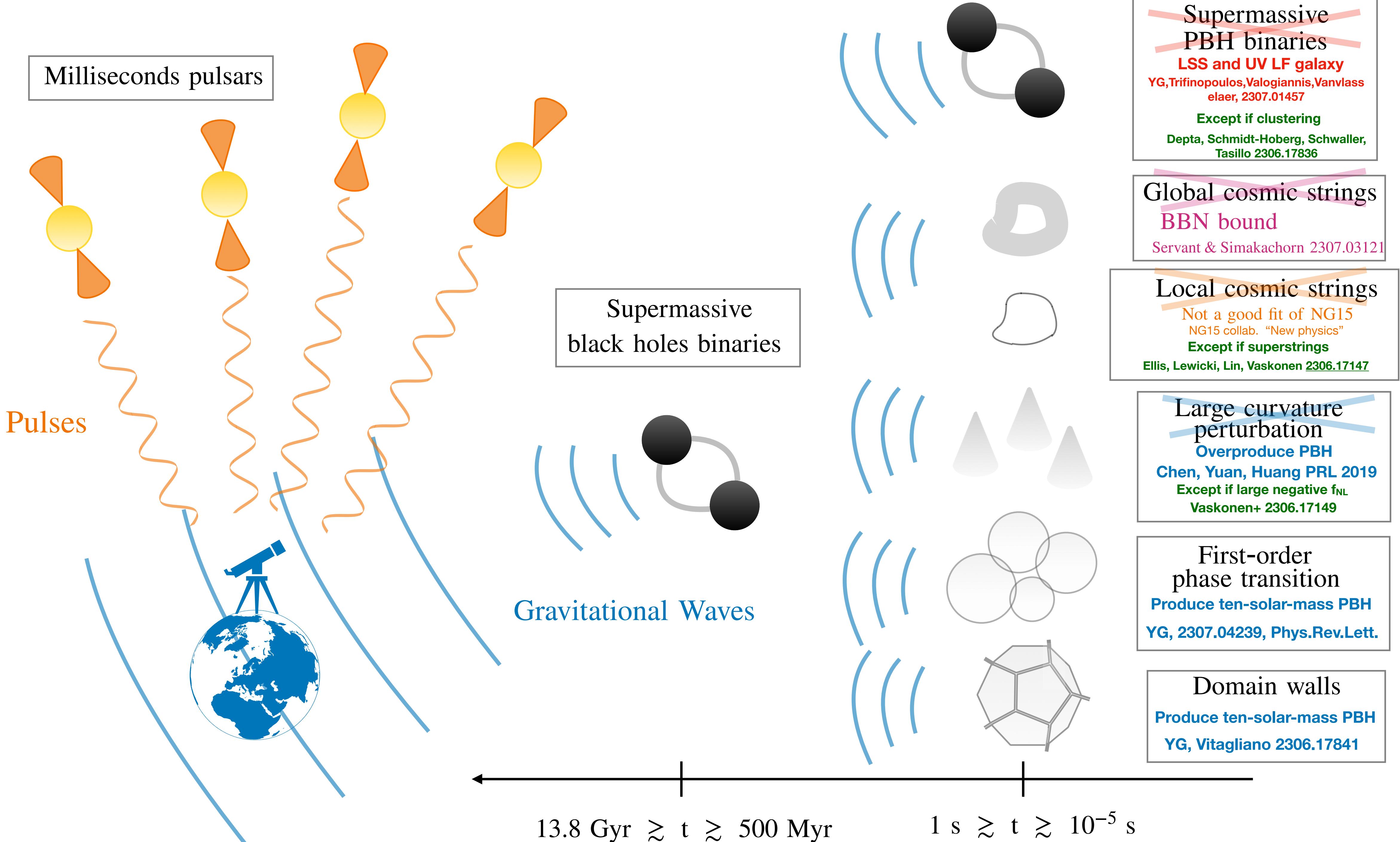












What is Primordial Black Holes ?

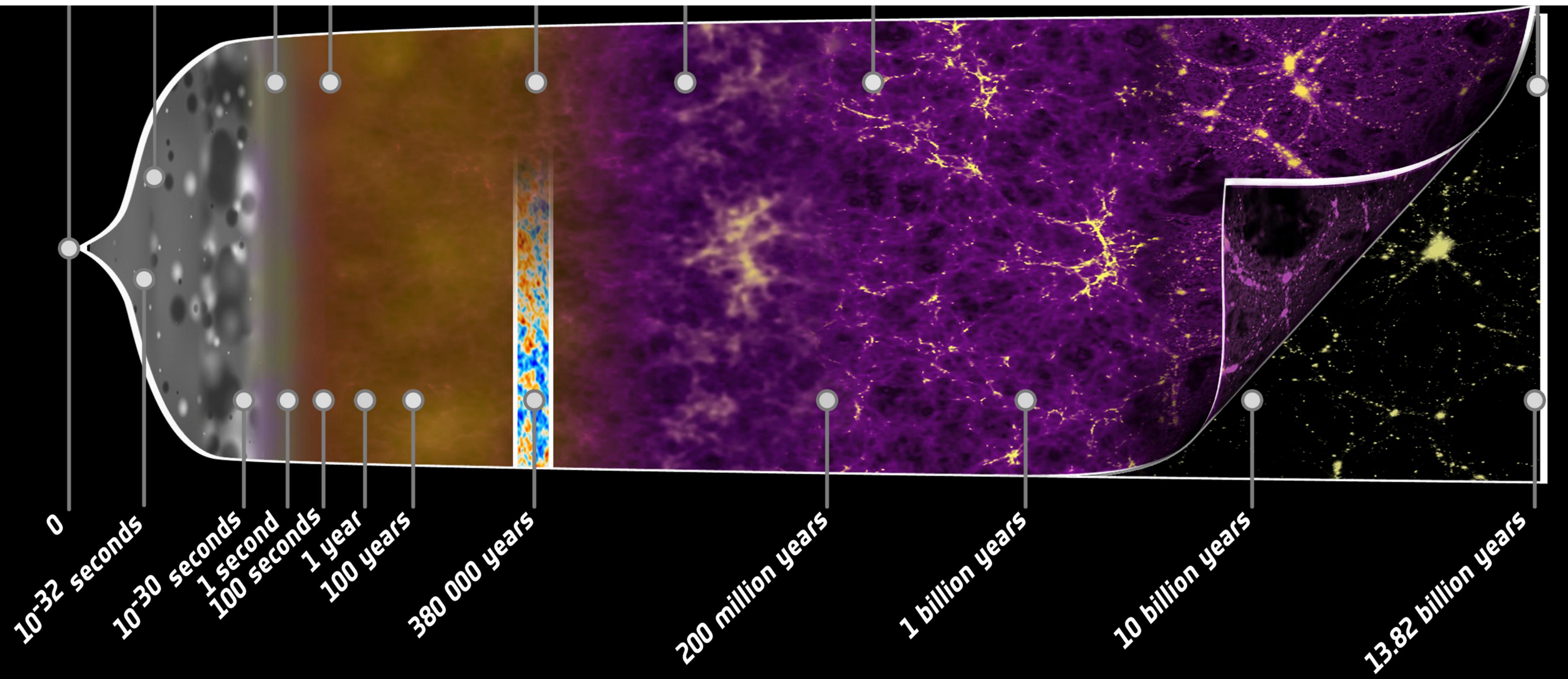
→ BH formed before any astrophysical objects exists

PBH formation

$$z \gg 10^3$$

Star formation

$$z \lesssim 30$$



How do they form ?

Friedmann's equation :

$$H^2 = \frac{8\pi G}{3} \rho$$

How do they form ?

Friedmann's equation :

$$H^{-3} \times H^2 = \frac{8\pi G}{3} \rho \times H^{-3}$$

How do they form ?

Friedmann's equation :

$$H^{-1} = 2G \times \frac{4\pi H^{-3}}{3} \rho$$

How do they form ?

Friedmann's equation :

$$H^{-1} = 2G \times \frac{4\pi H^{-3}}{3} \rho \equiv R_H \quad \equiv M_H$$

How do they form ?

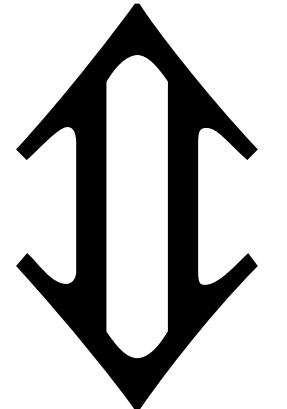
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$$R_H = 2GM_H$$

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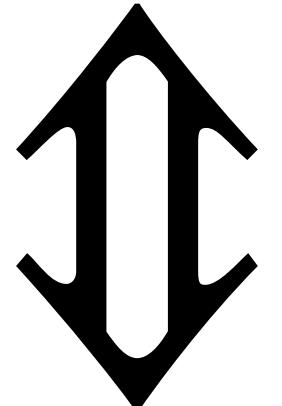


Schwarzschild's equation

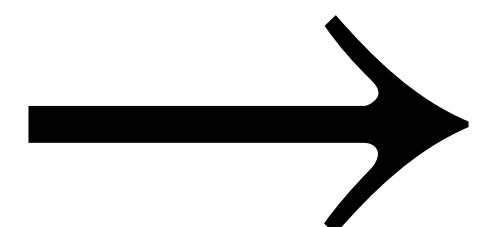
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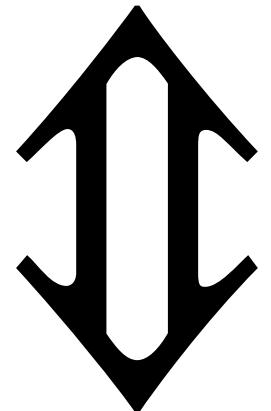
Schwarzschild's equation



Hubble patches are on the edge to collapse into black holes

How do they form ?

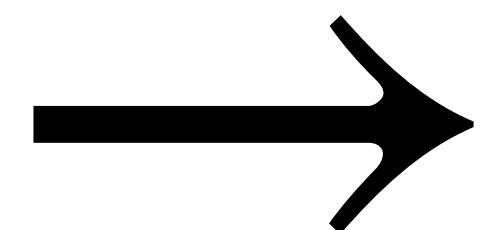
Friedmann's equation :



$$\frac{R_H - 2GM_H}{R_H} \gtrsim 0.45$$

Radiation pressure

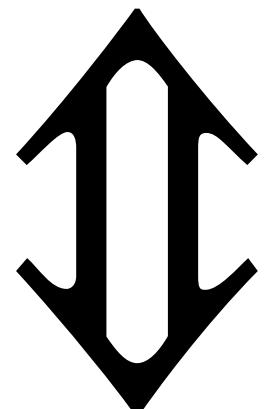
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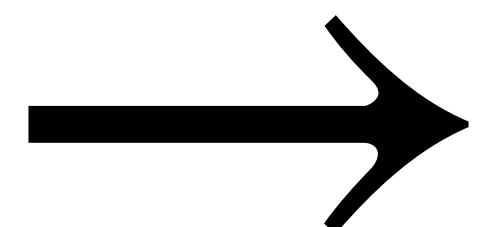
Friedmann's equation :



$$\frac{\langle \delta\rho \rangle_H}{\rho} \gtrsim 0.45$$

Radiation pressure

Schwarzschild's equation



Hubble patches are on the edge to collapse into black holes

What can generate large $\langle \delta\rho \rangle/\rho$?

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1) PBHs from primordial scalar fluctuation

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4) PBHs from Supercooled 1st-order Phase Transition

1982: *Kodama, Sasaki, Sato, (Prog.Theor.Phys. 68 (1982) 1979)*

2021: *Liu, Bian, Can, Guo, Wang, 2106.05637, Phys.Rev.D 105 (2022) 2*

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4) PBHs from Supercooled 1st-order Phase Transition

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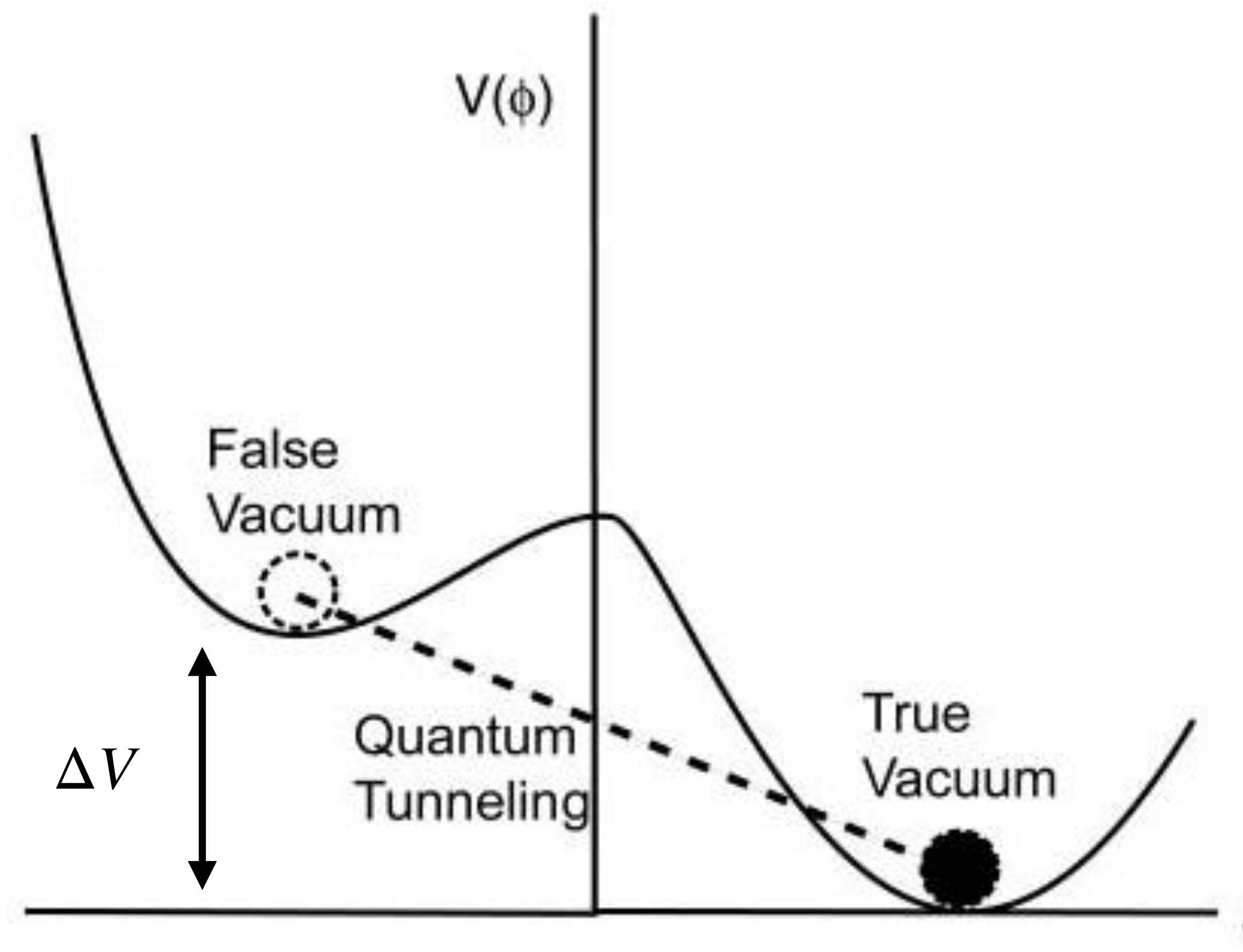
2022: *Kawana, T. Kim, and P. Lu, 2212.14037*

YG, 2311.13640

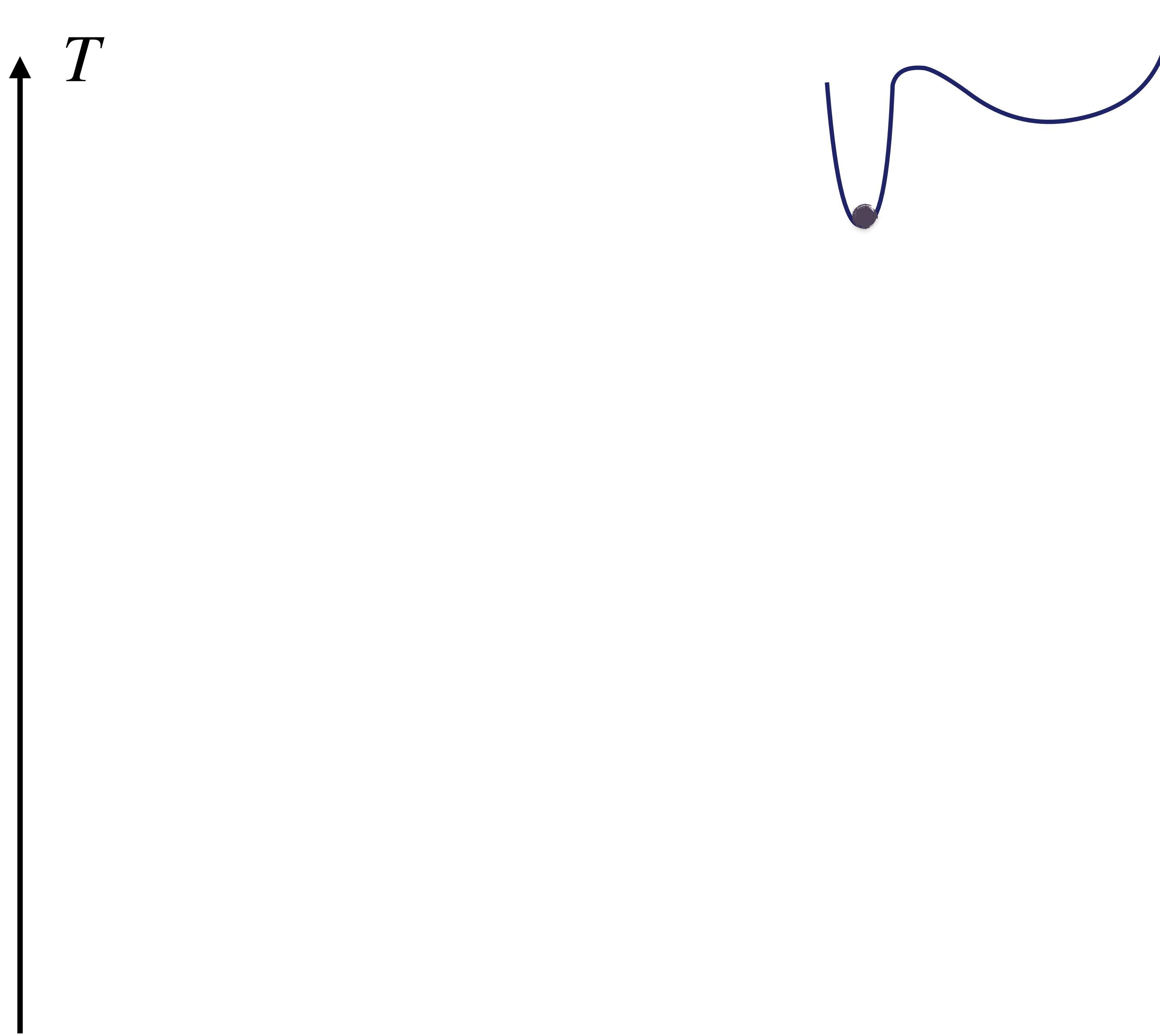
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PBHs formation during supercooled phase transition

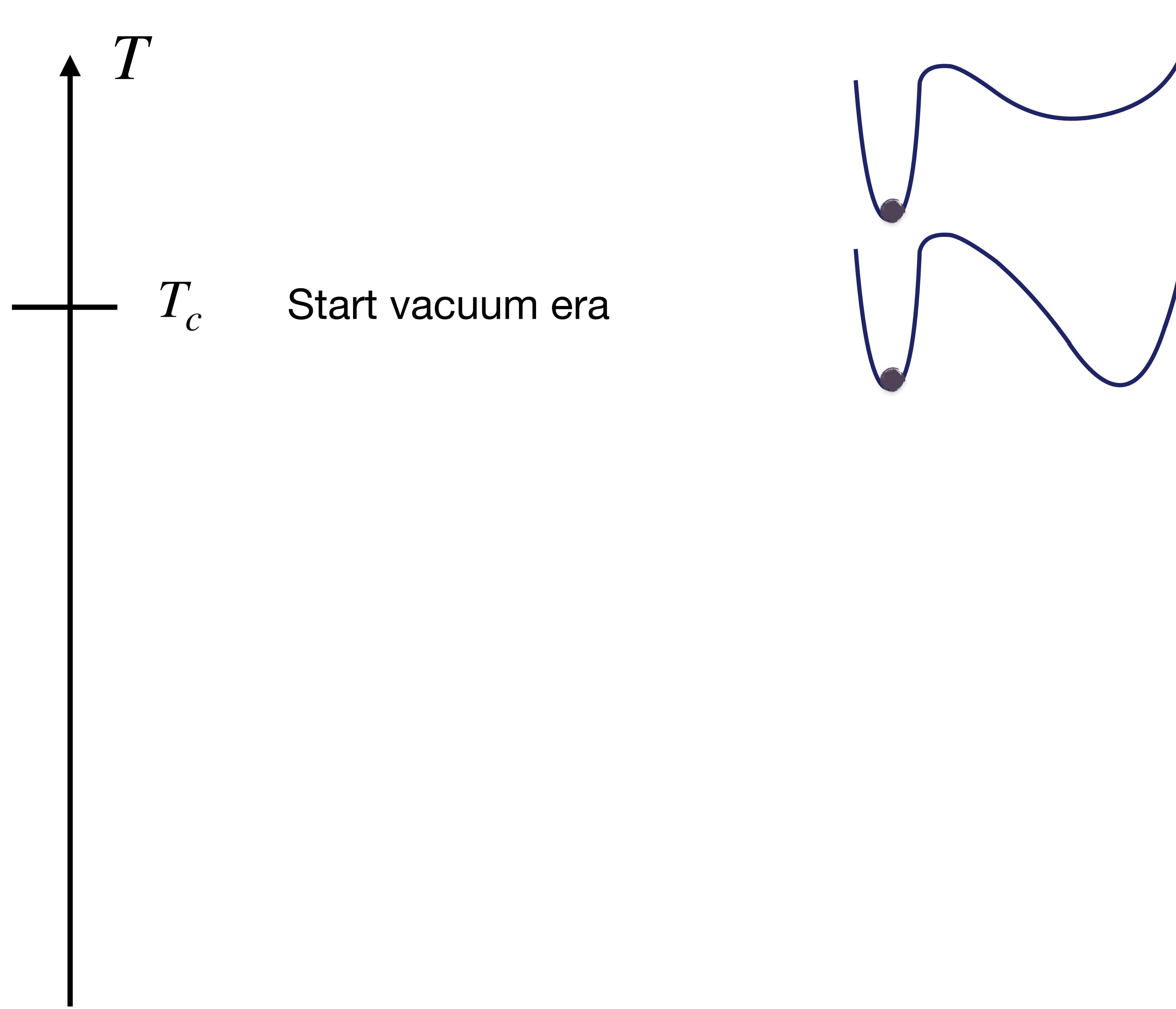
Guth 1980 "Old inflation idea"



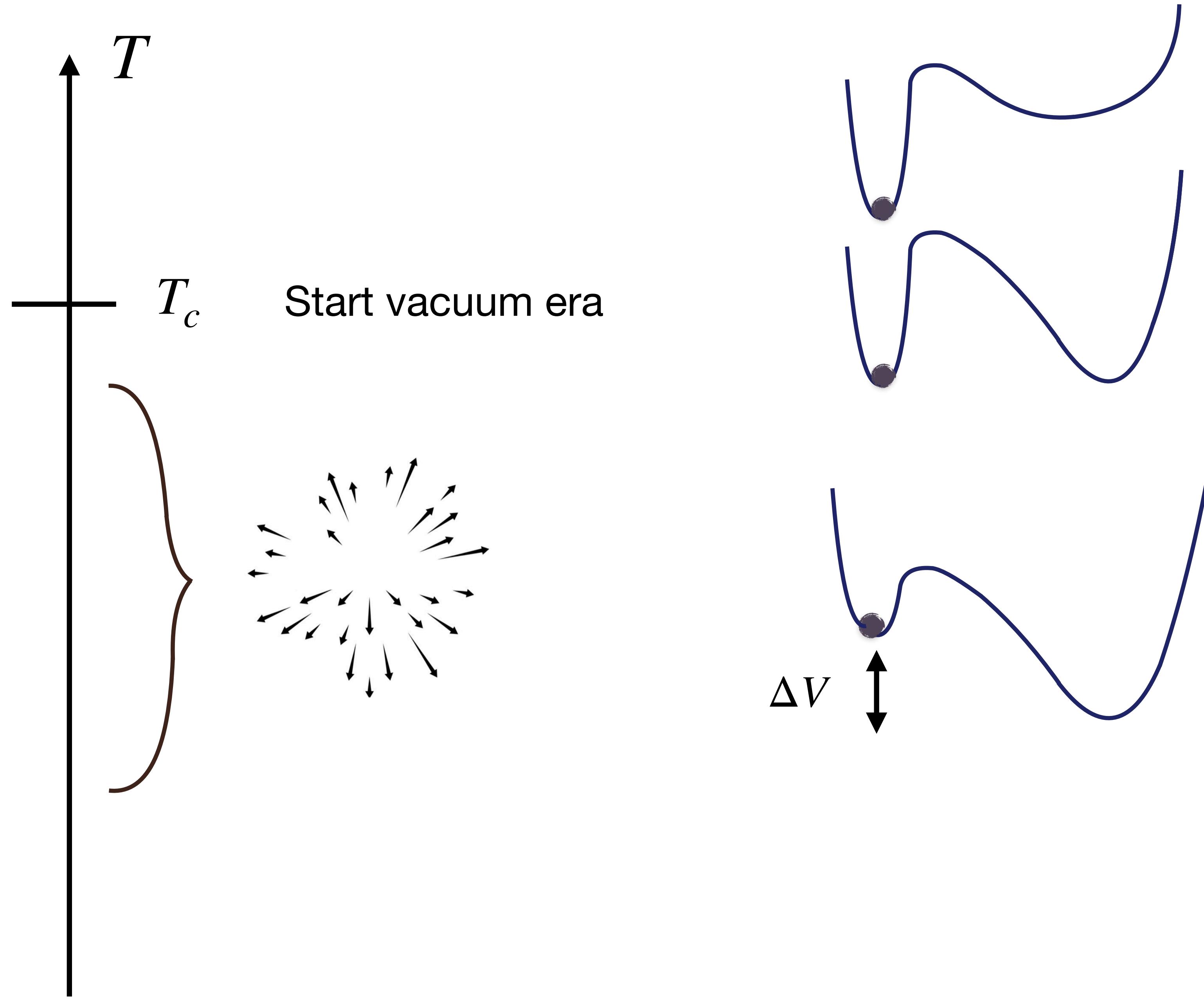
Supercooled 1stOPT = delayed PT



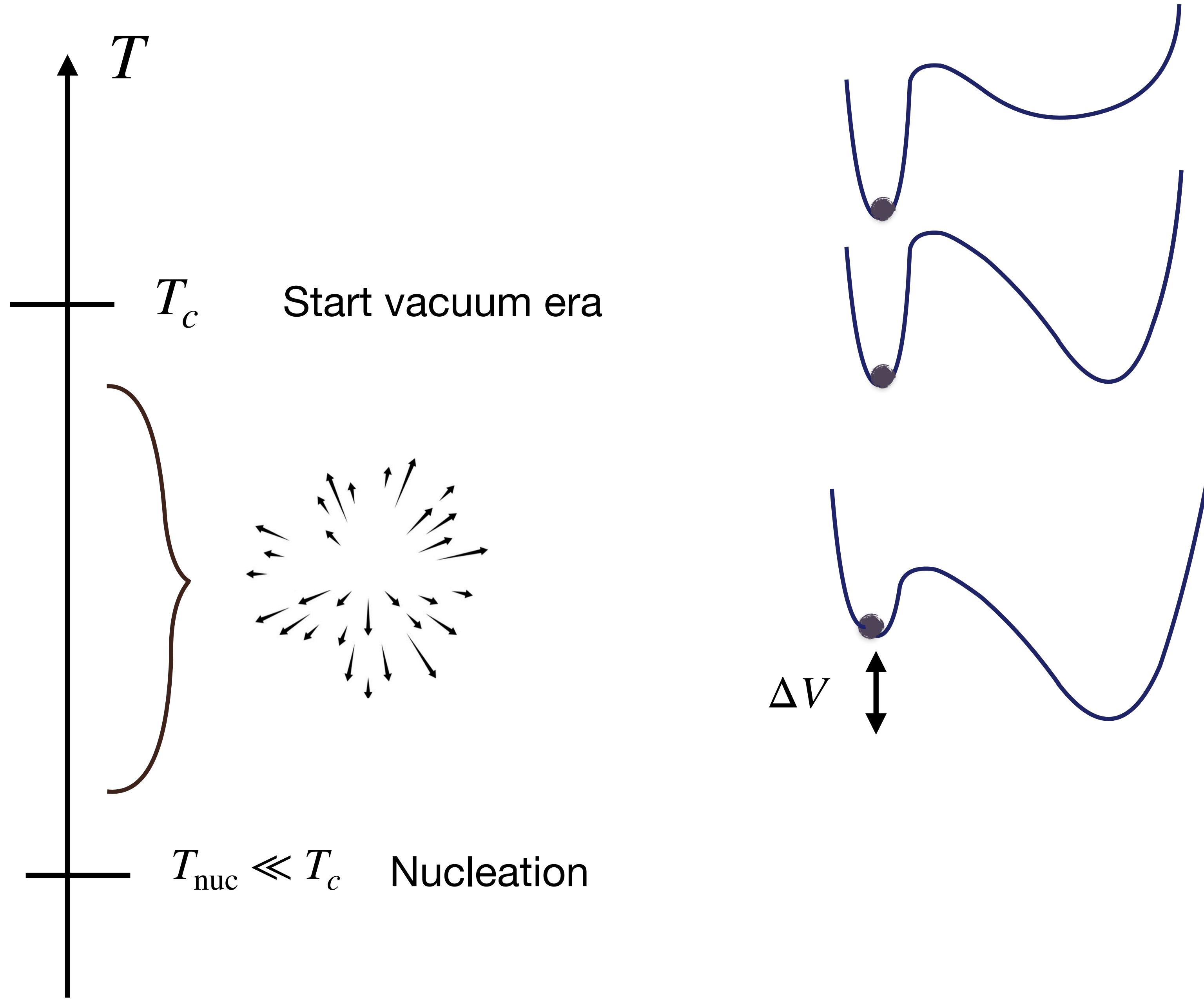
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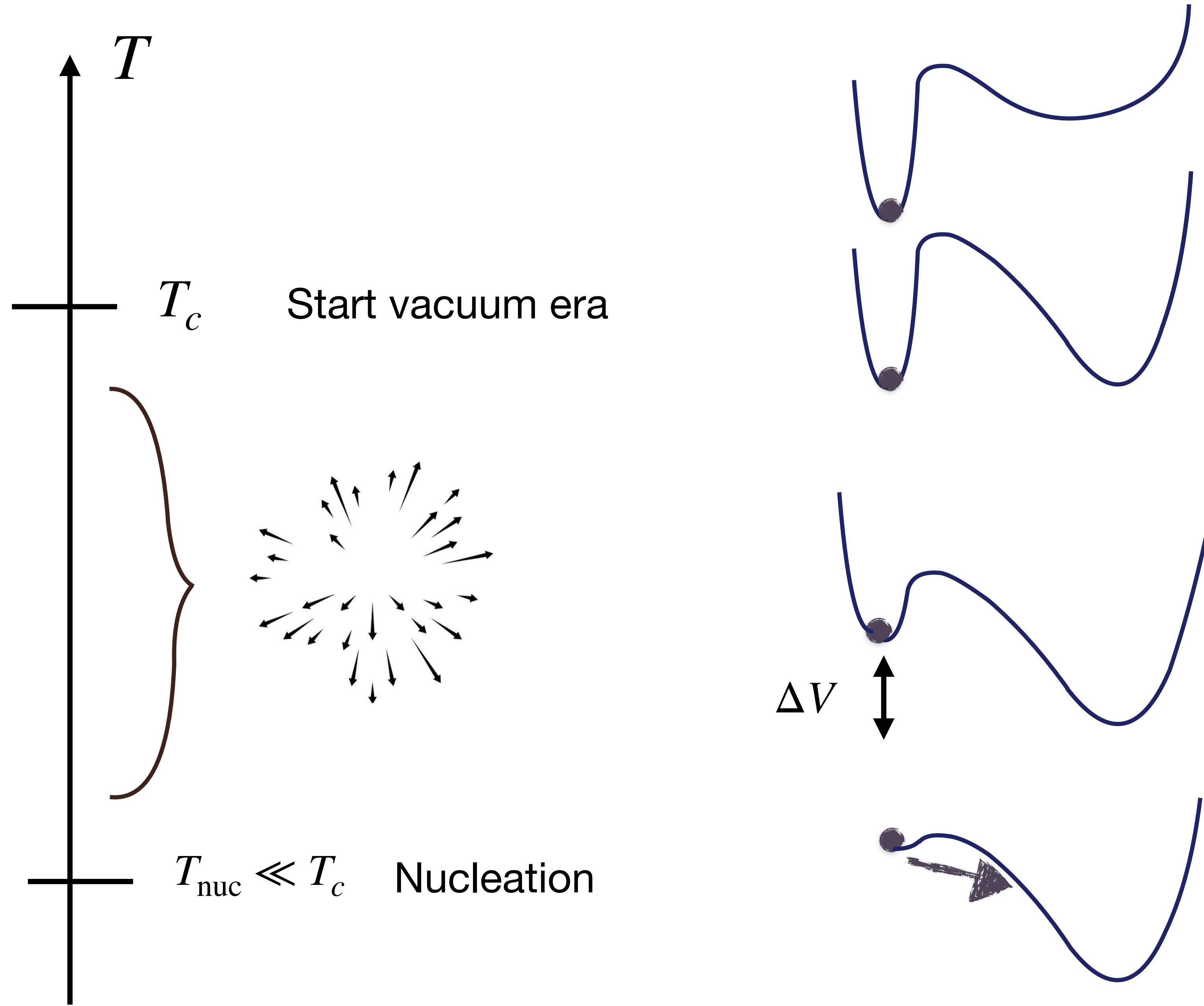
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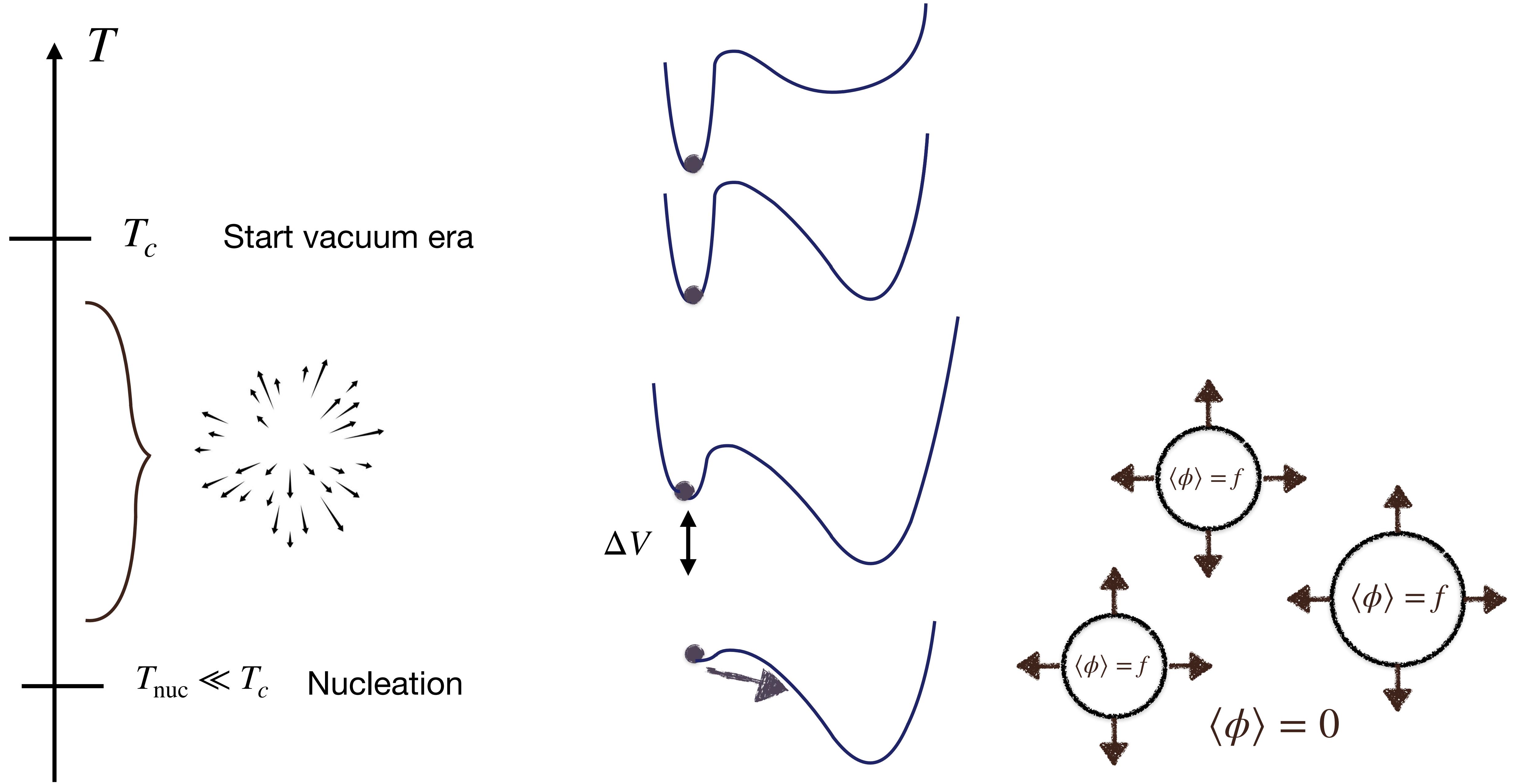
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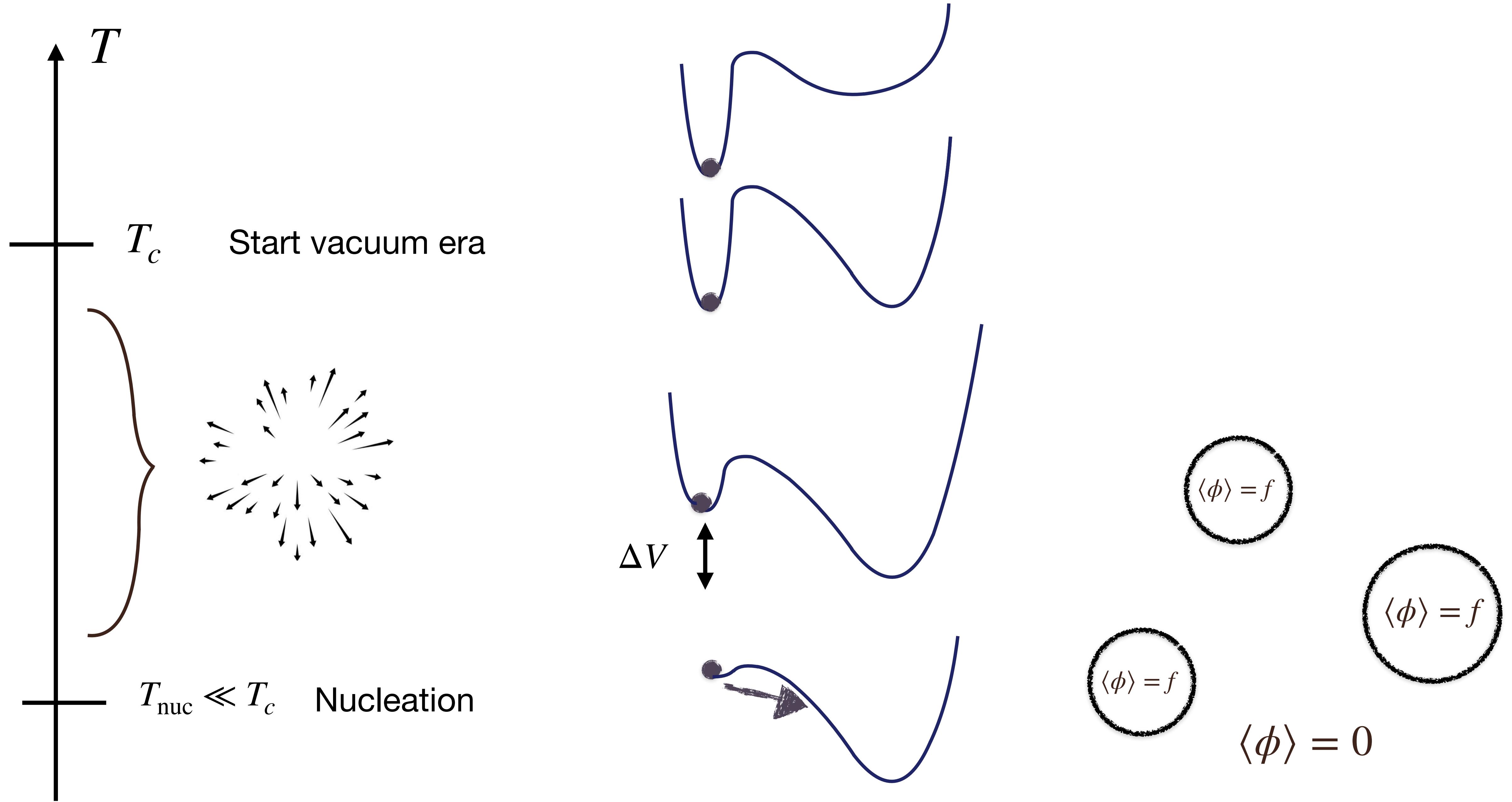
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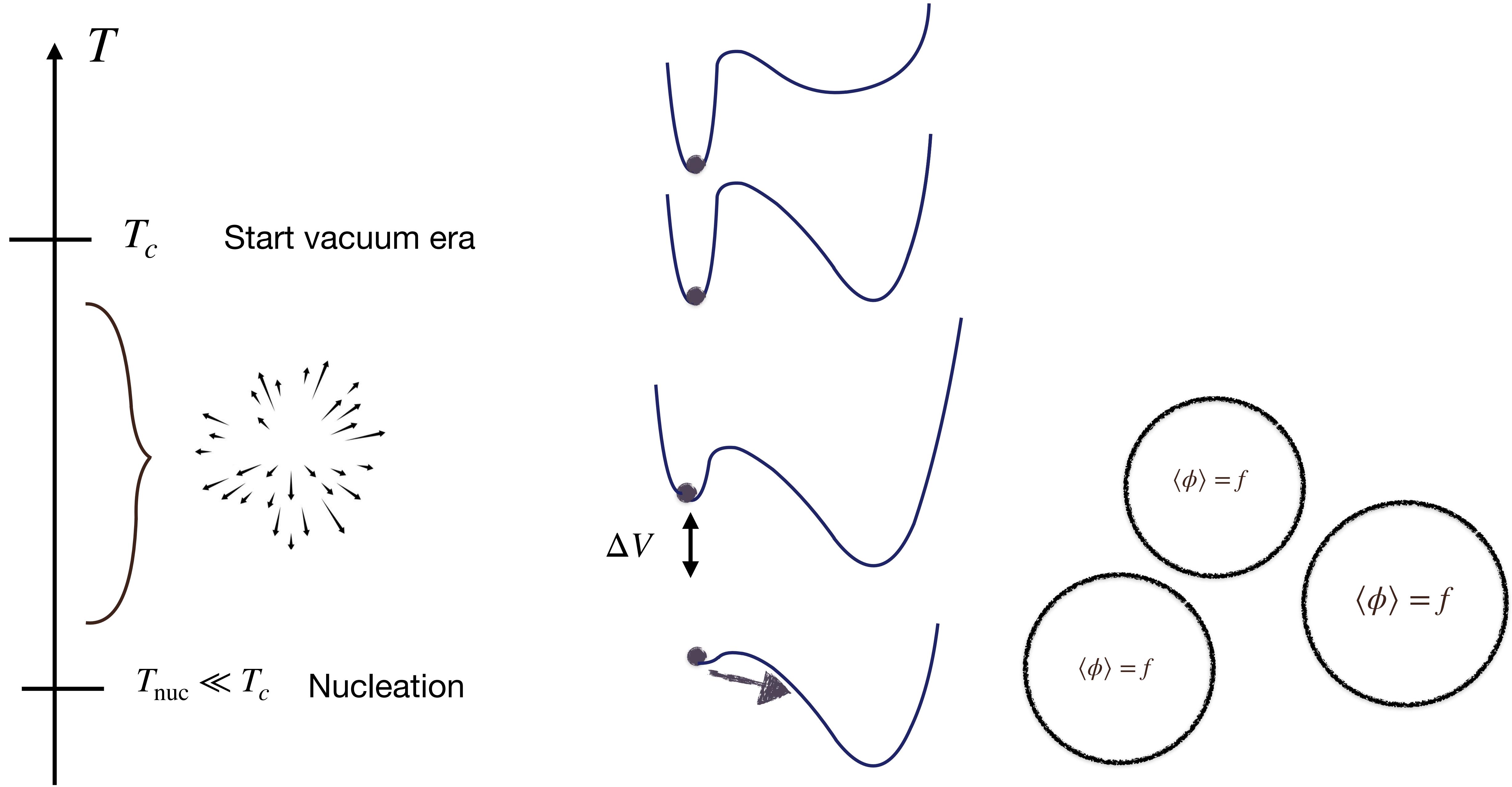
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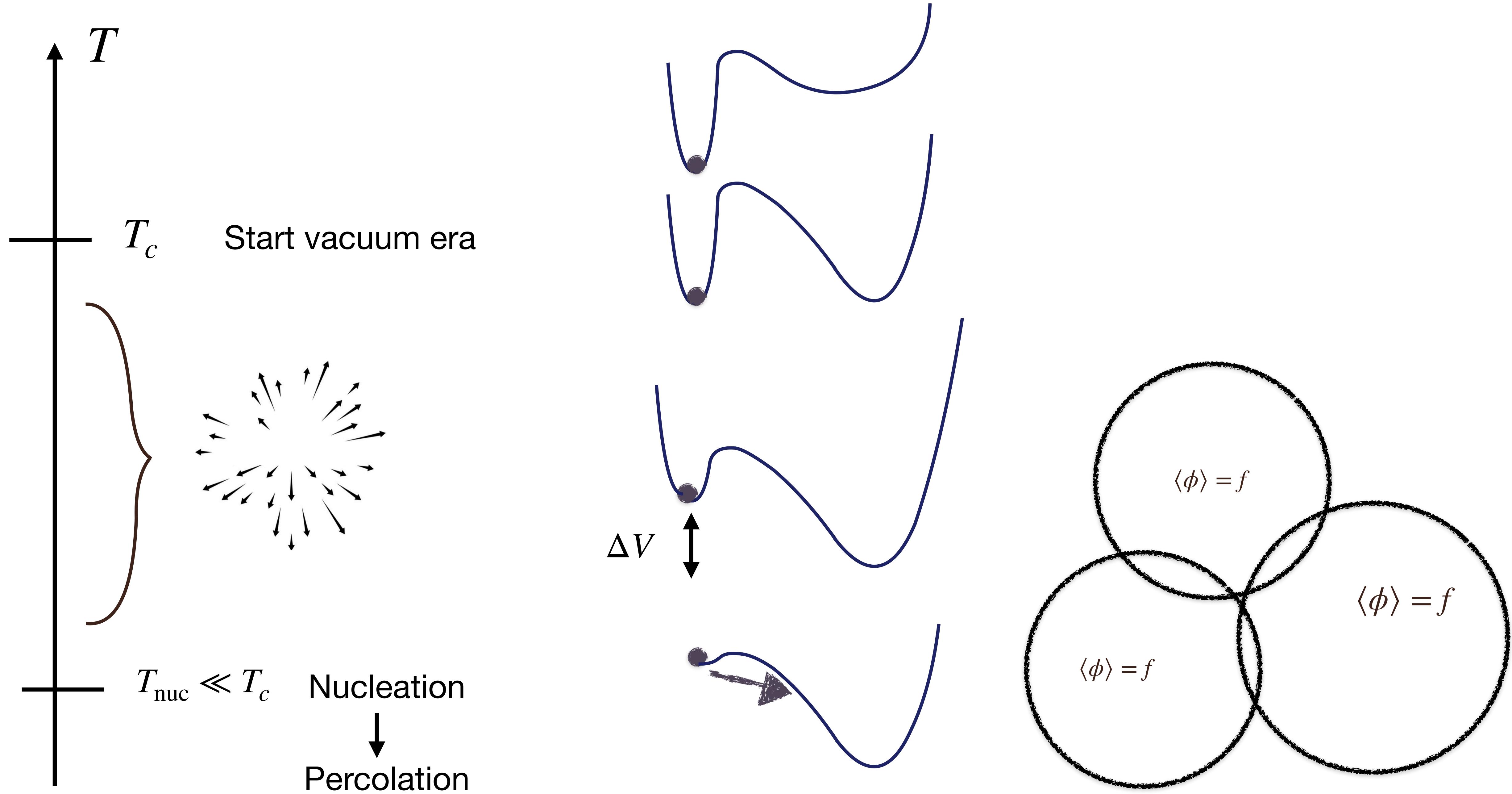
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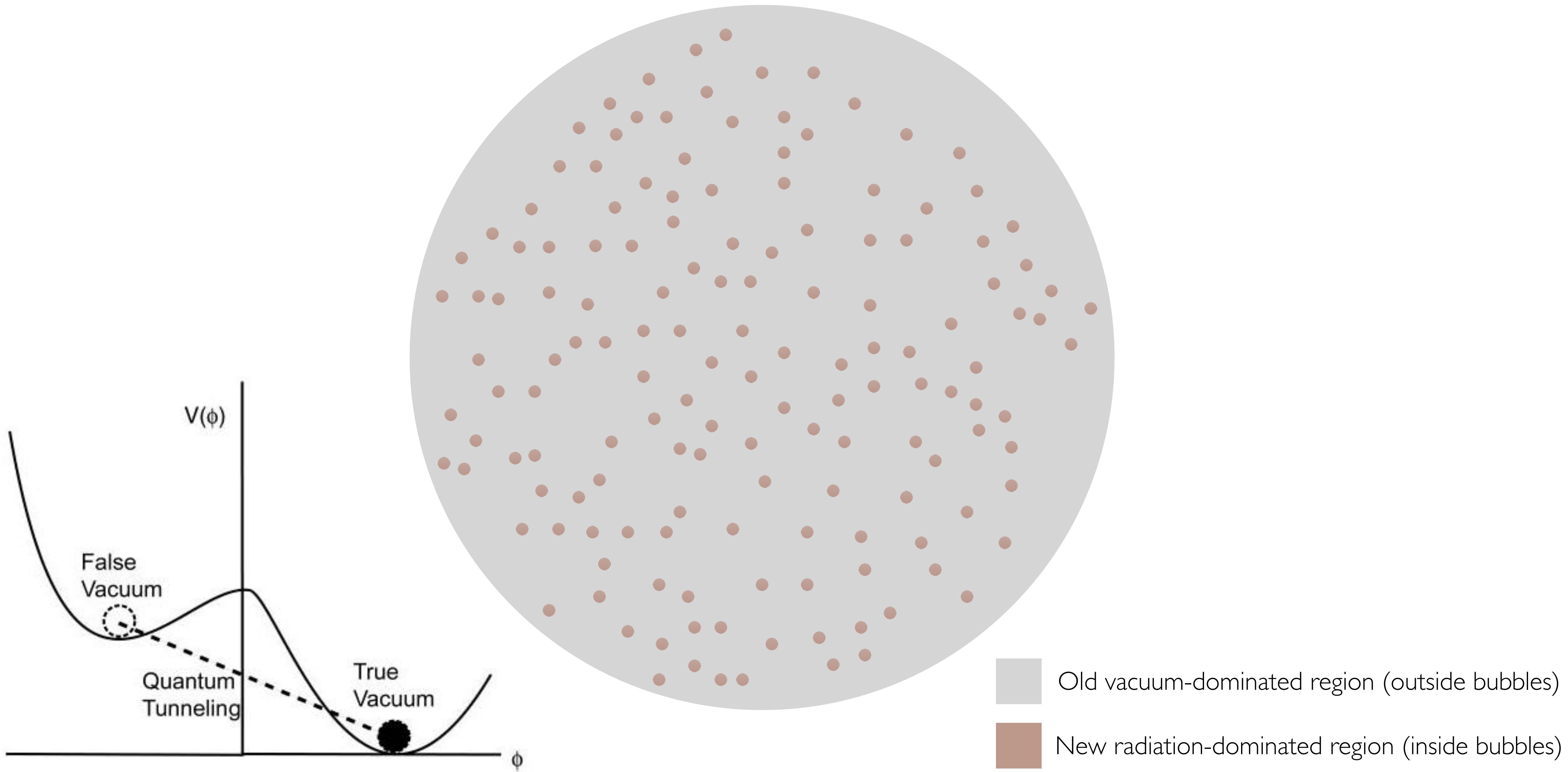


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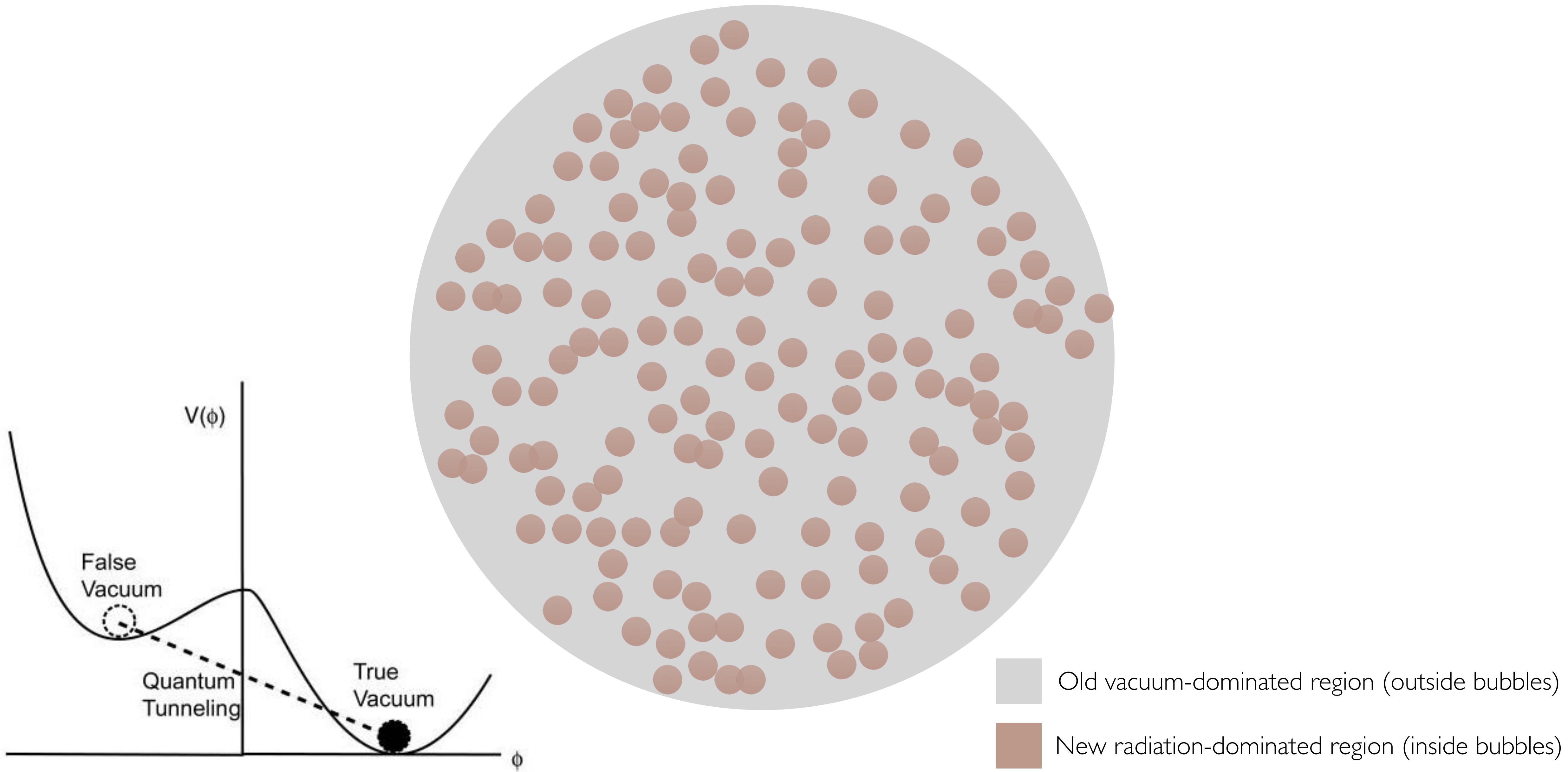
PBHs from 1stOPT

YG, Volansky 2305:04942



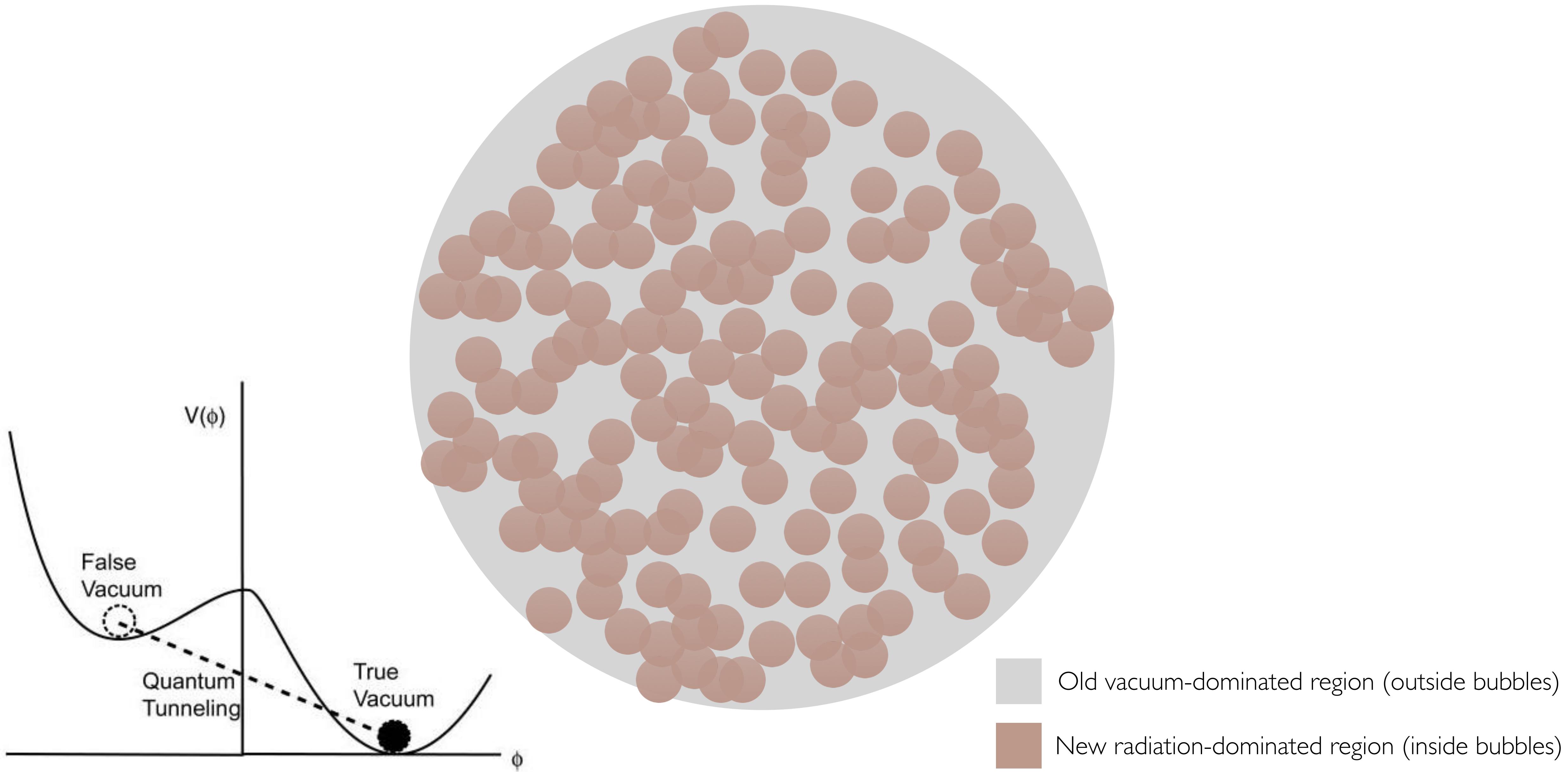
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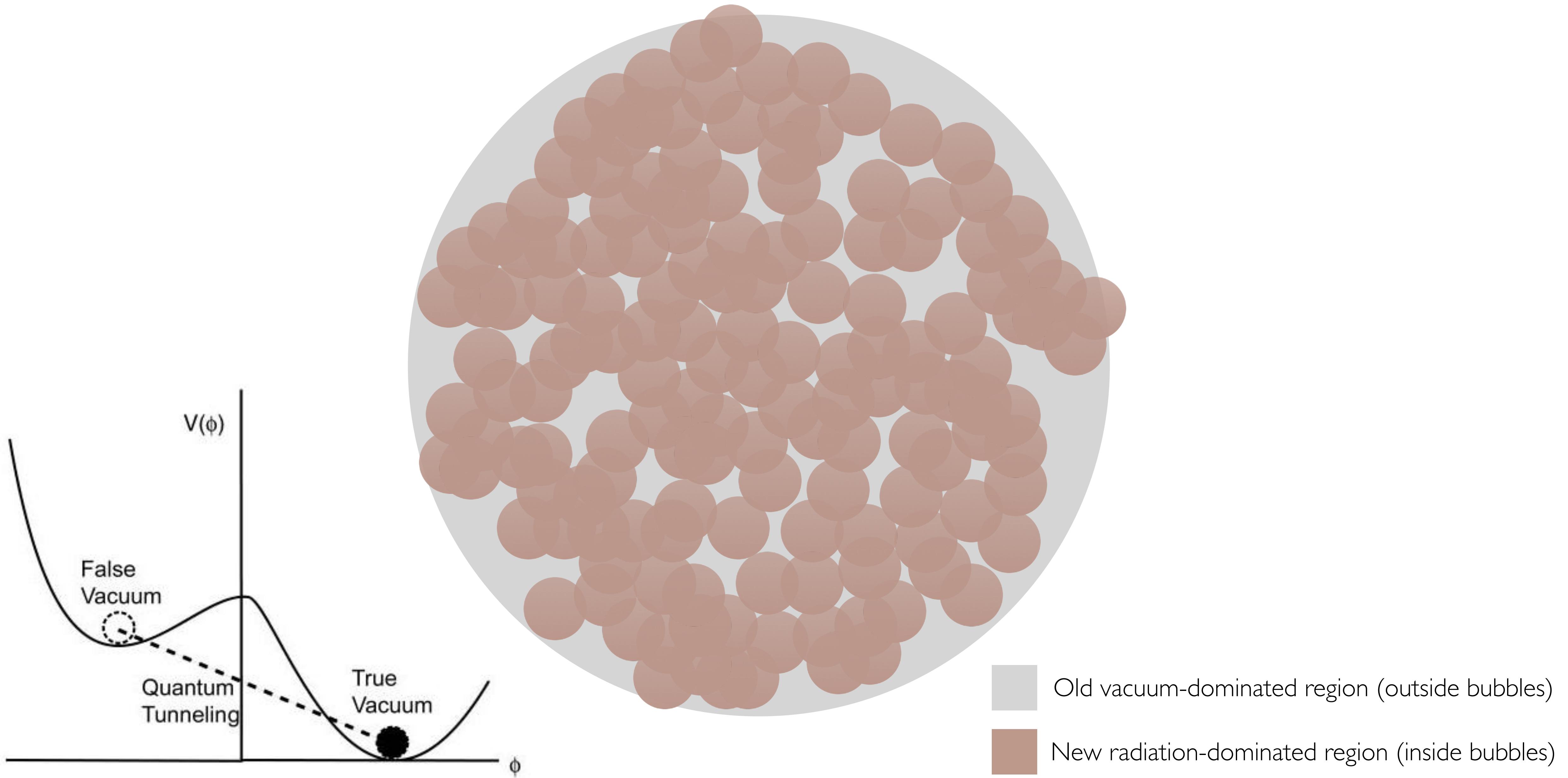
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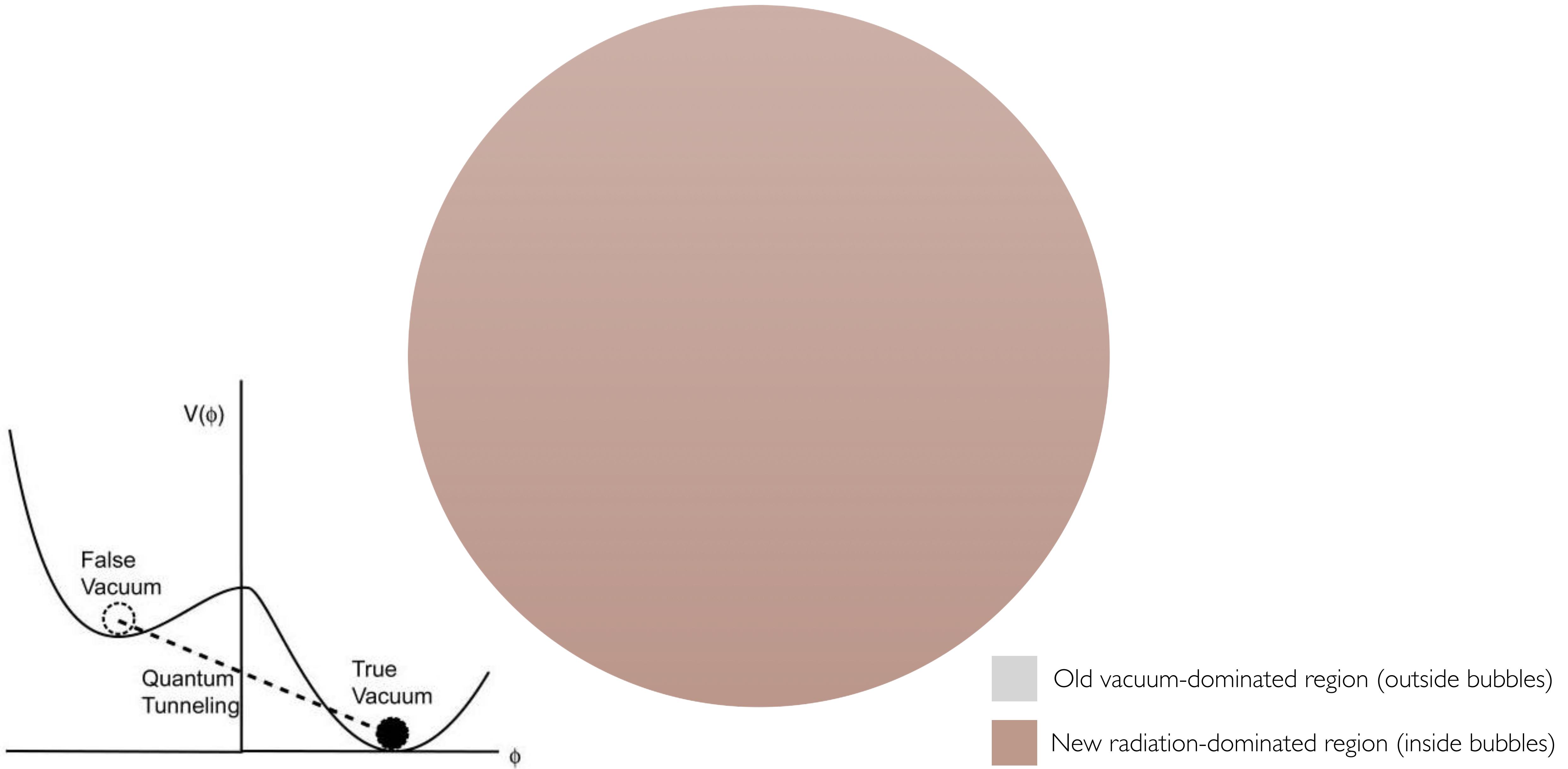
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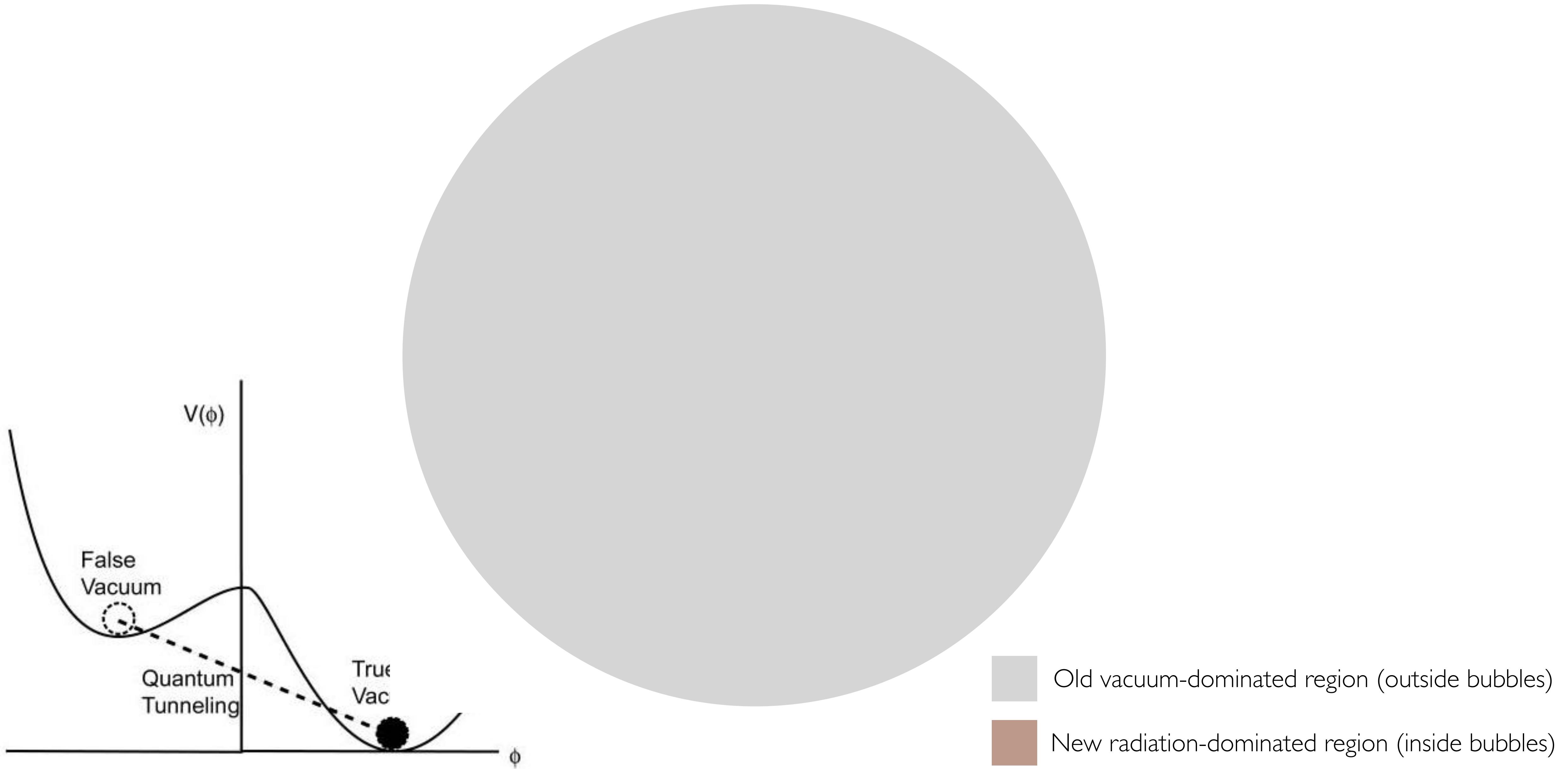
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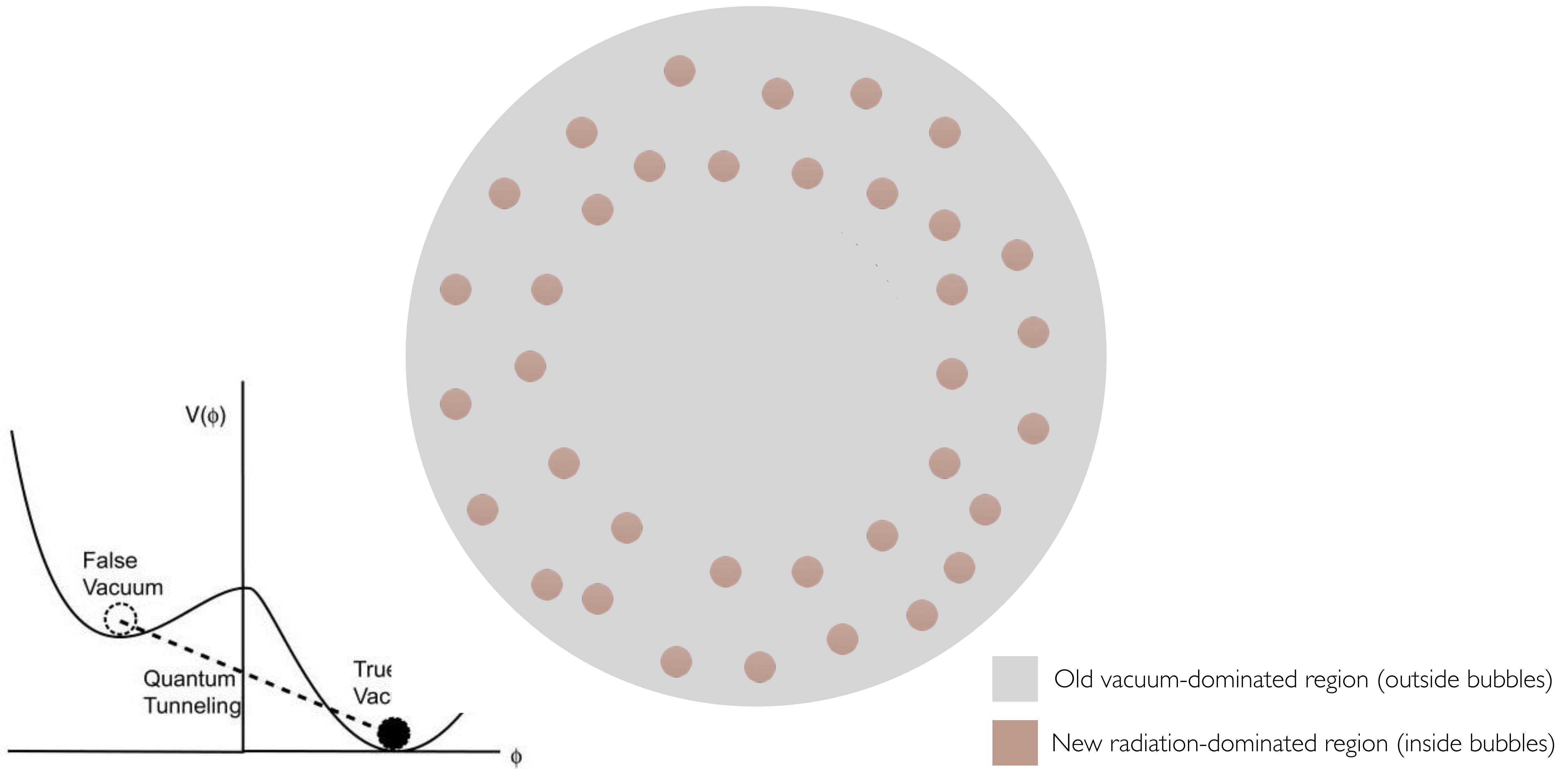
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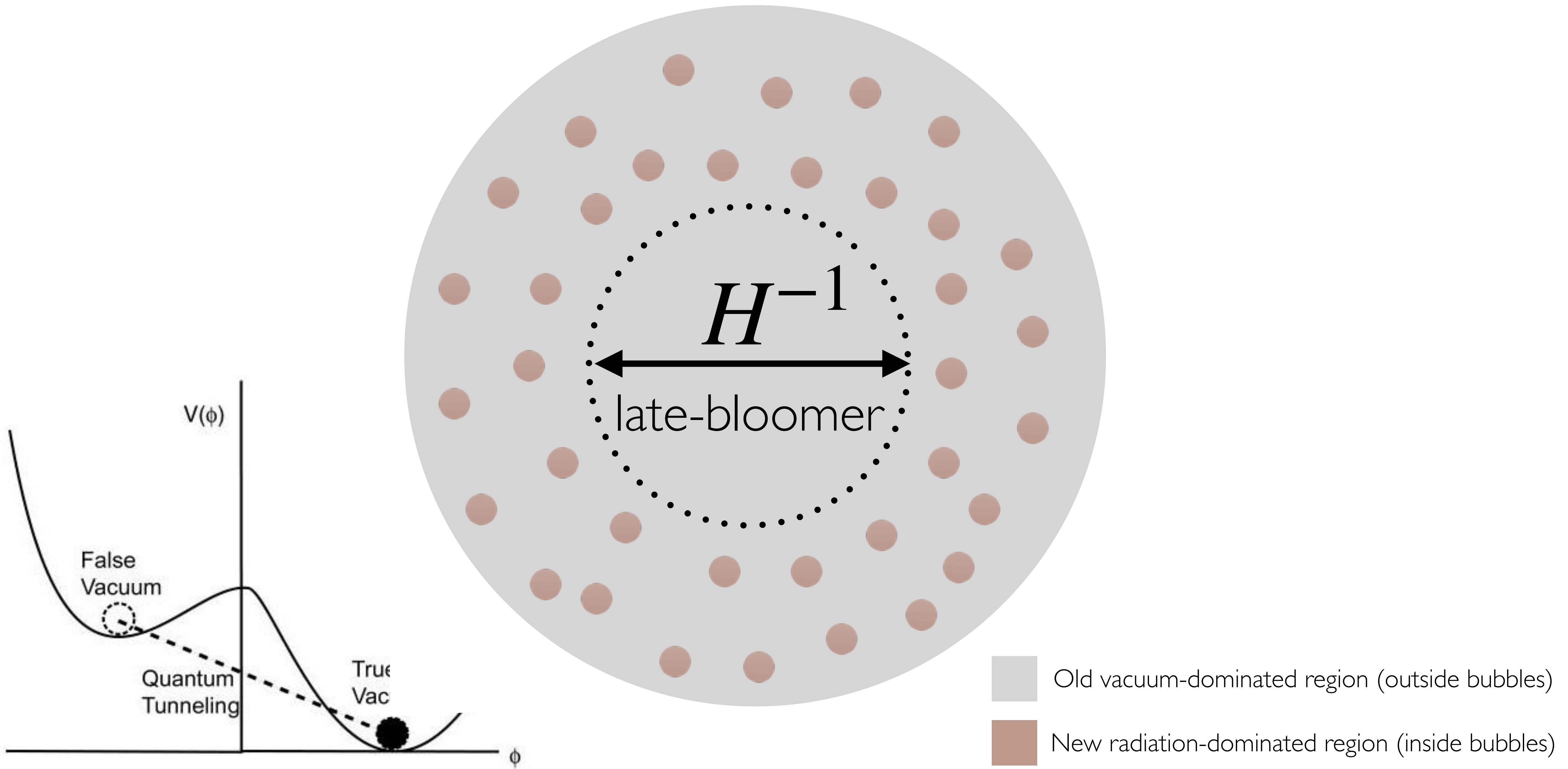
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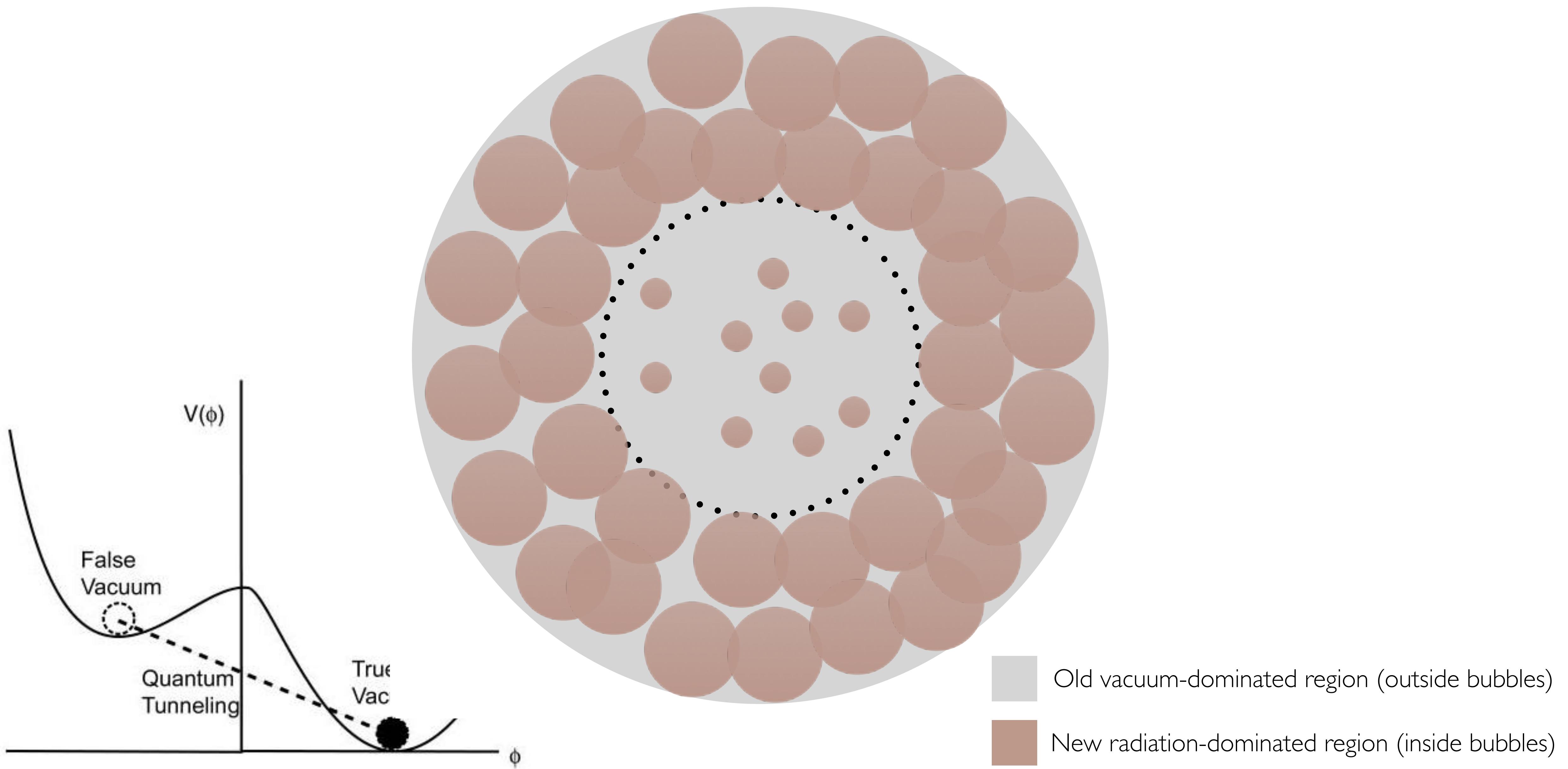
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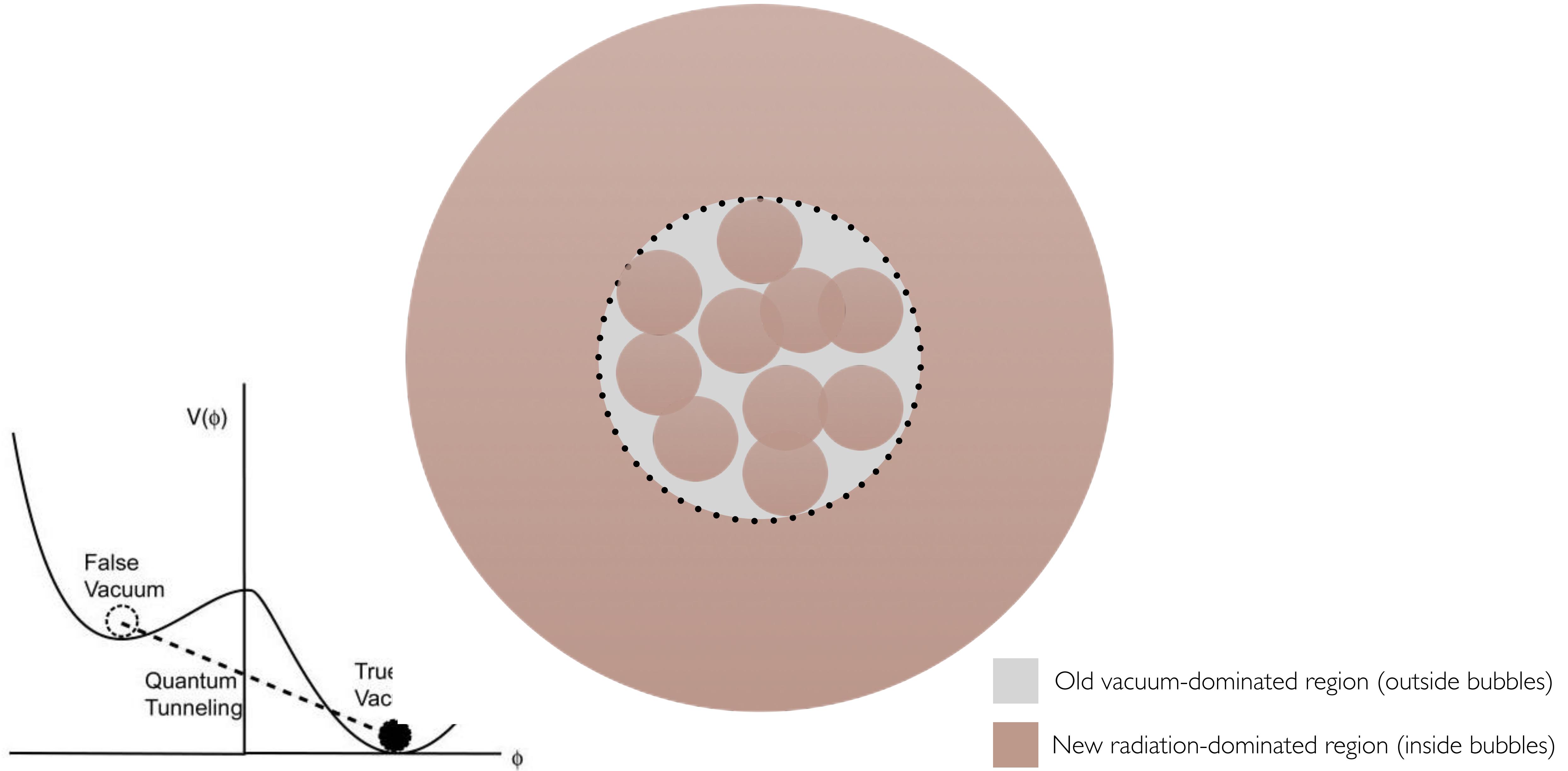
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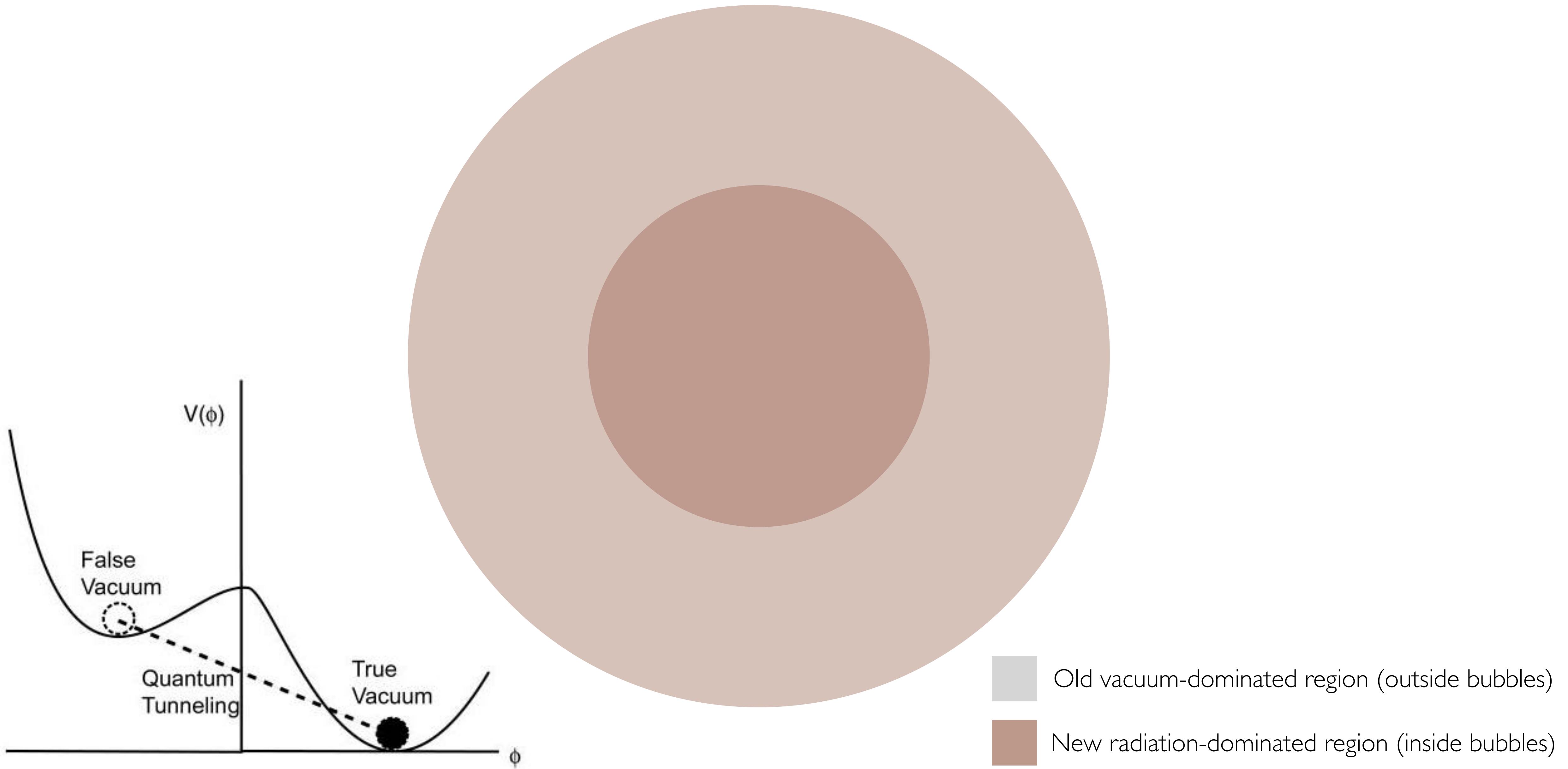
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YG, Volansky 2305:04942

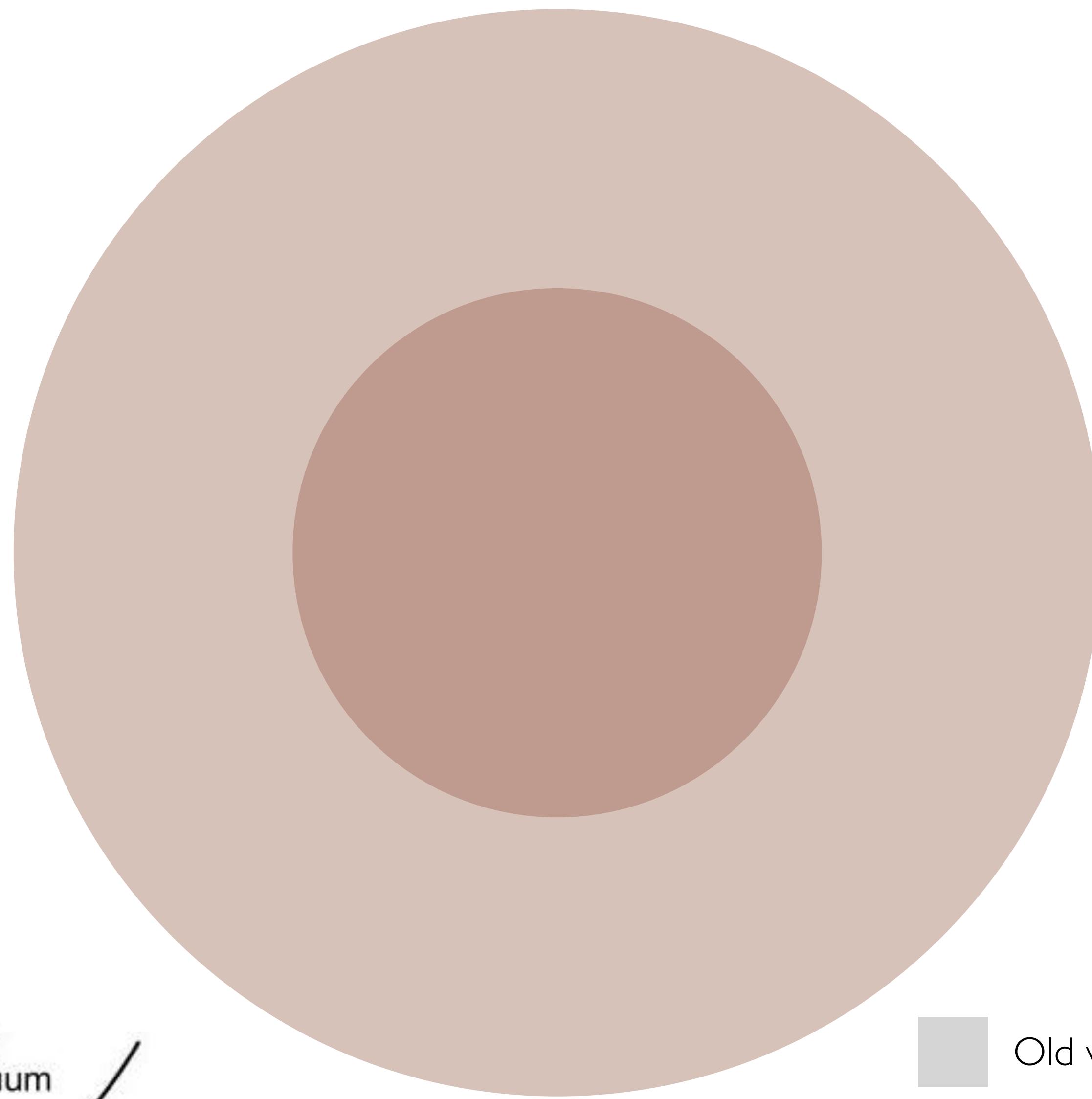
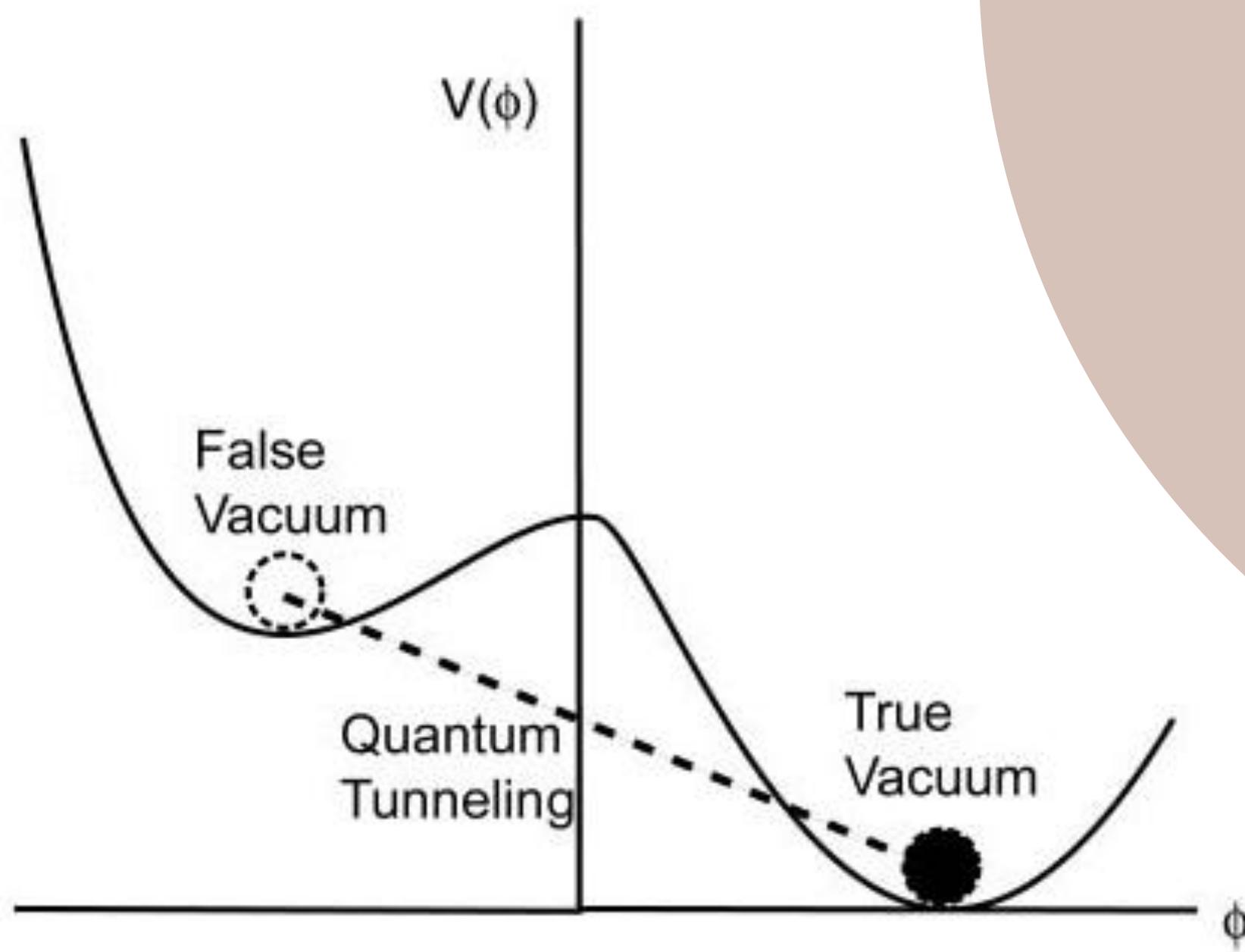


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YG, Volansky 2305:04942

if

$$\delta\rho/\rho \gtrsim 0.45.$$



- Old vacuum-dominated region (outside bubbles)
- New radiation-dominated region (inside bubbles)

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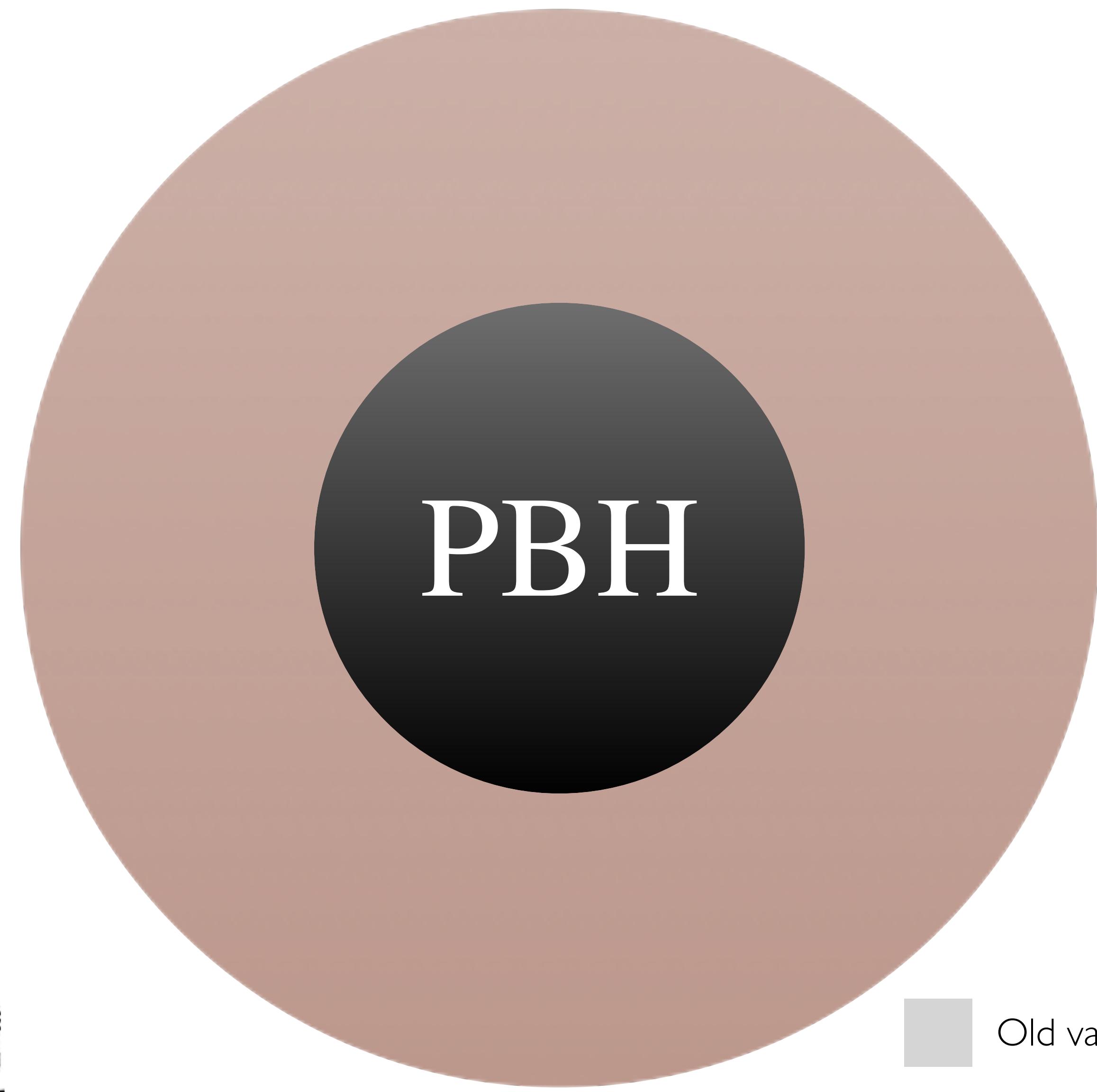
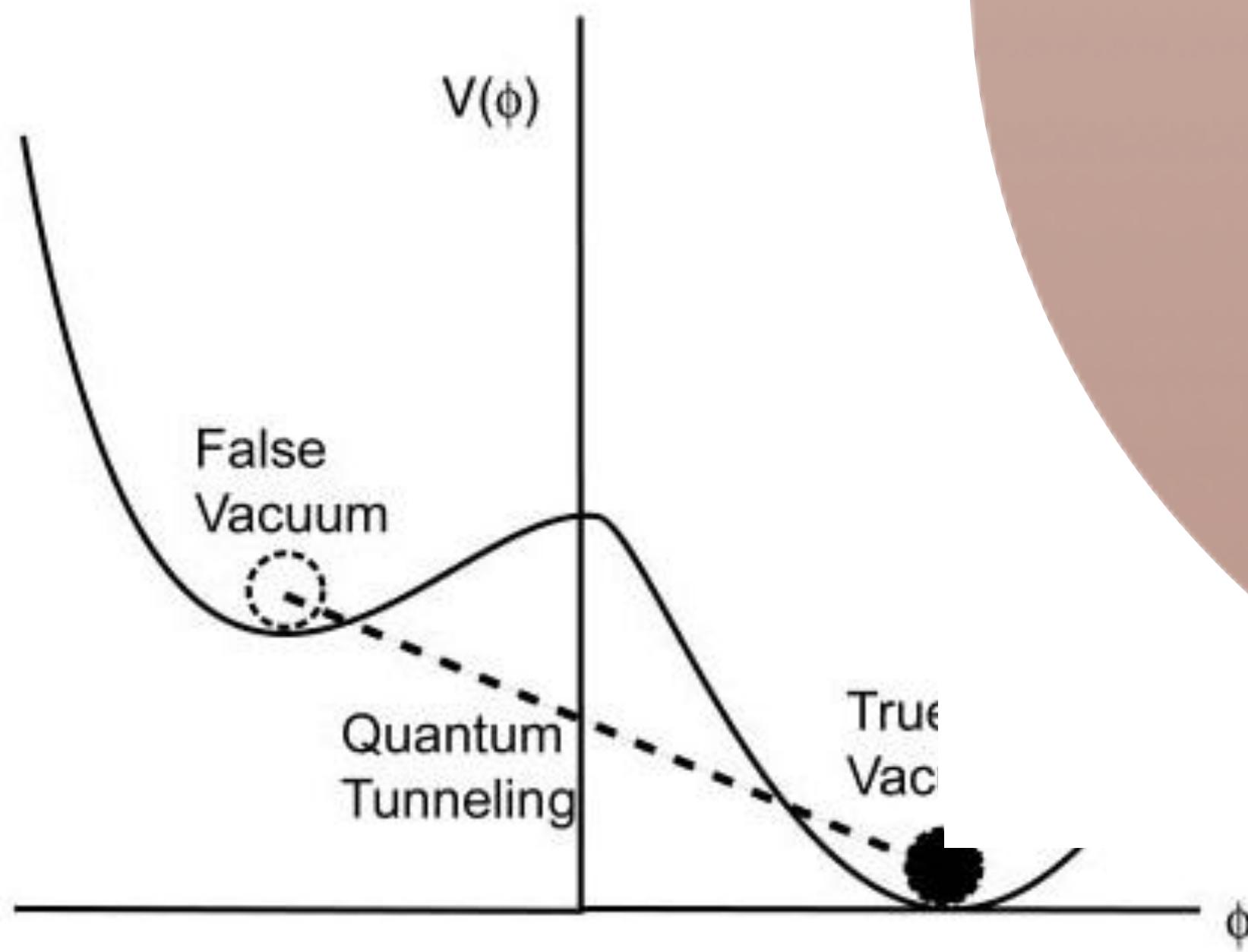
YG, Volansky 2305:04942

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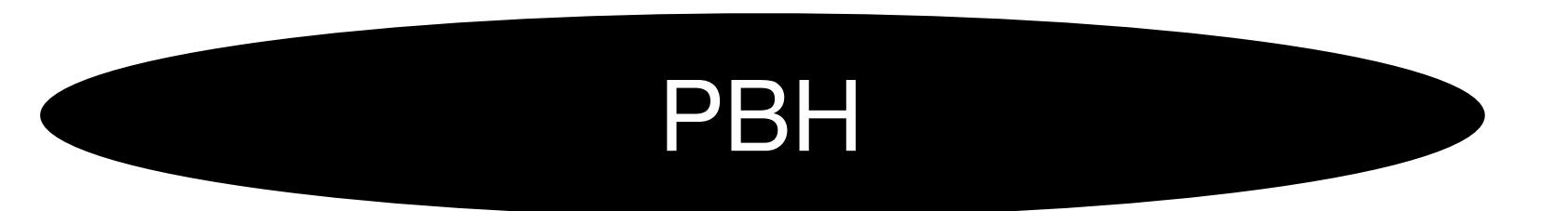
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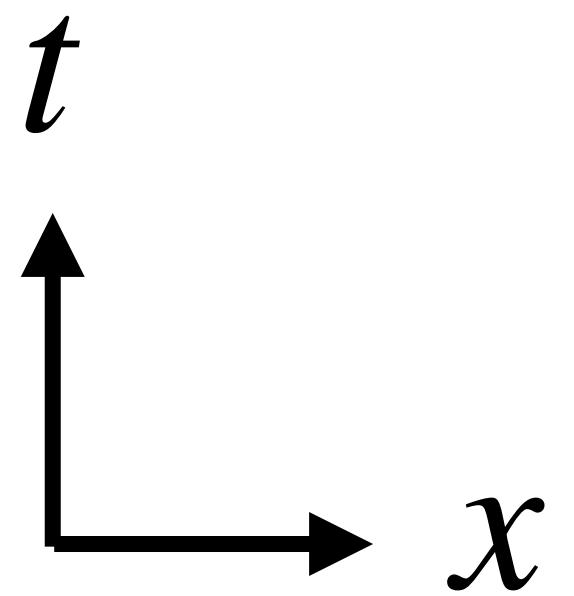
PBH

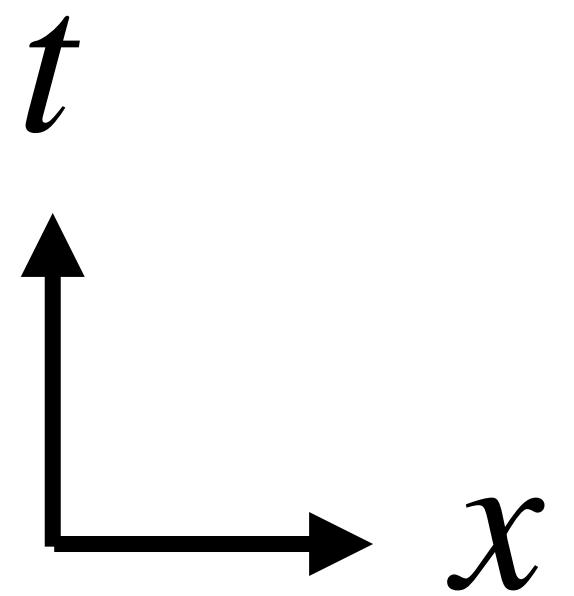


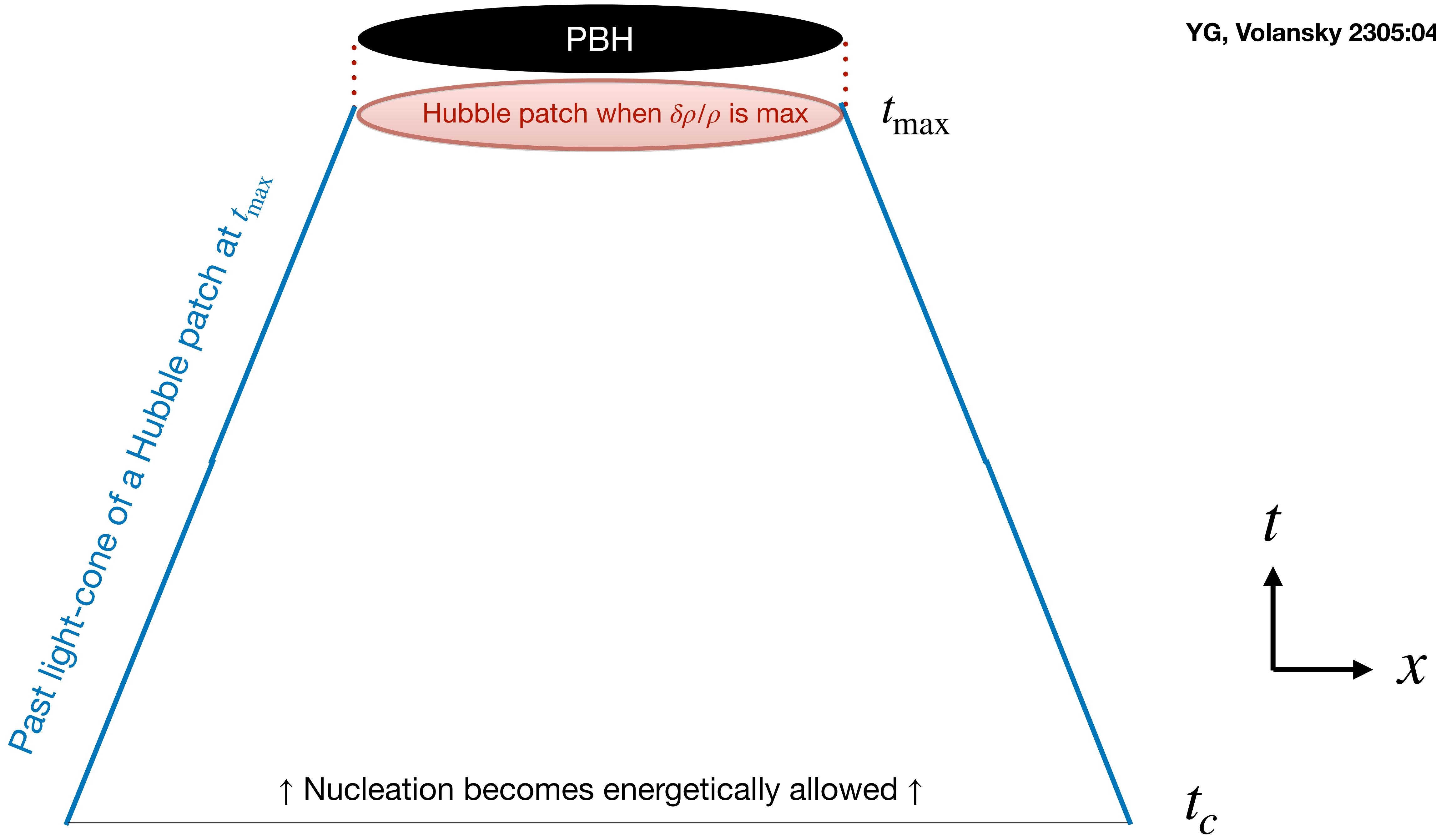
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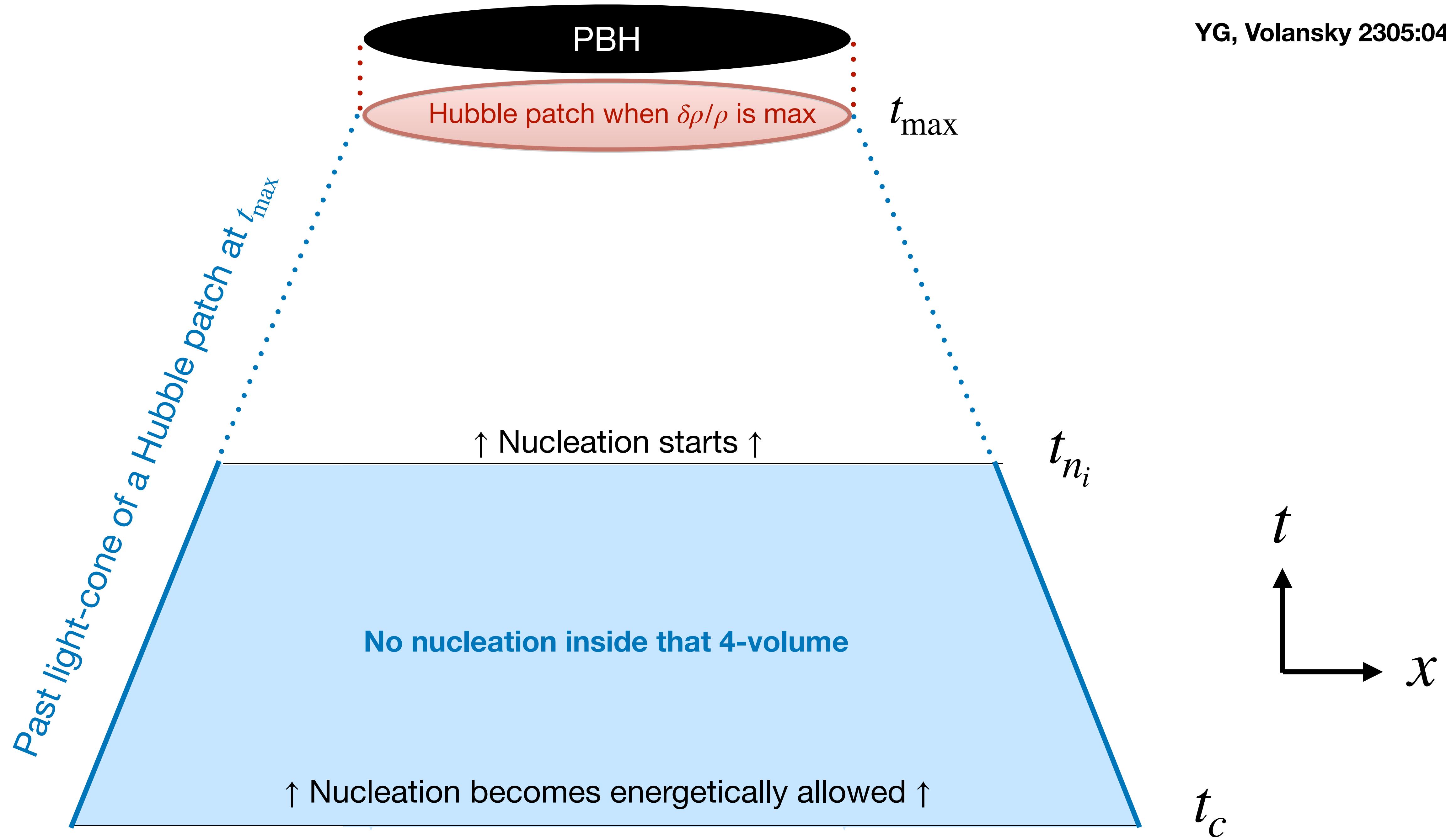


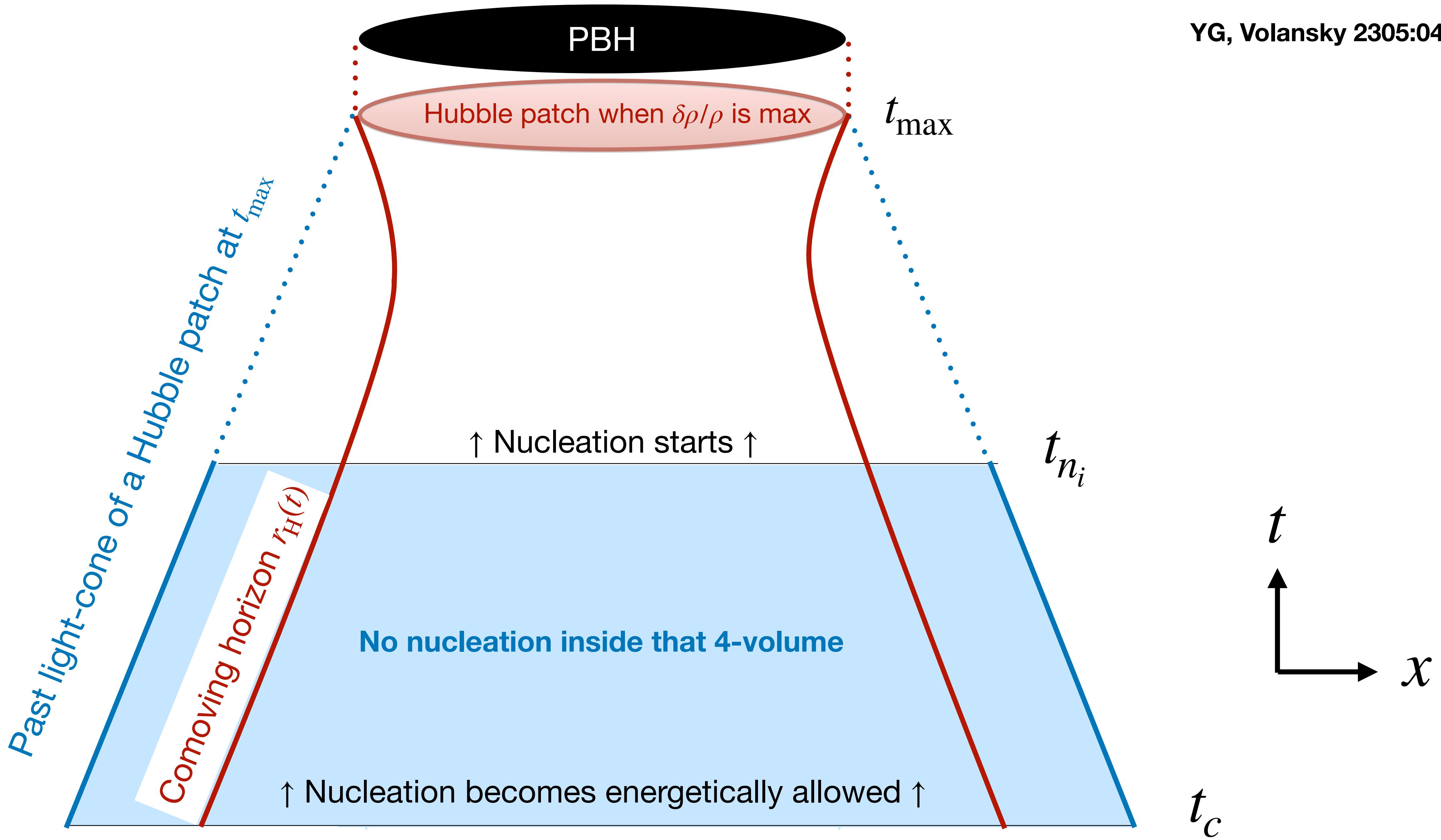
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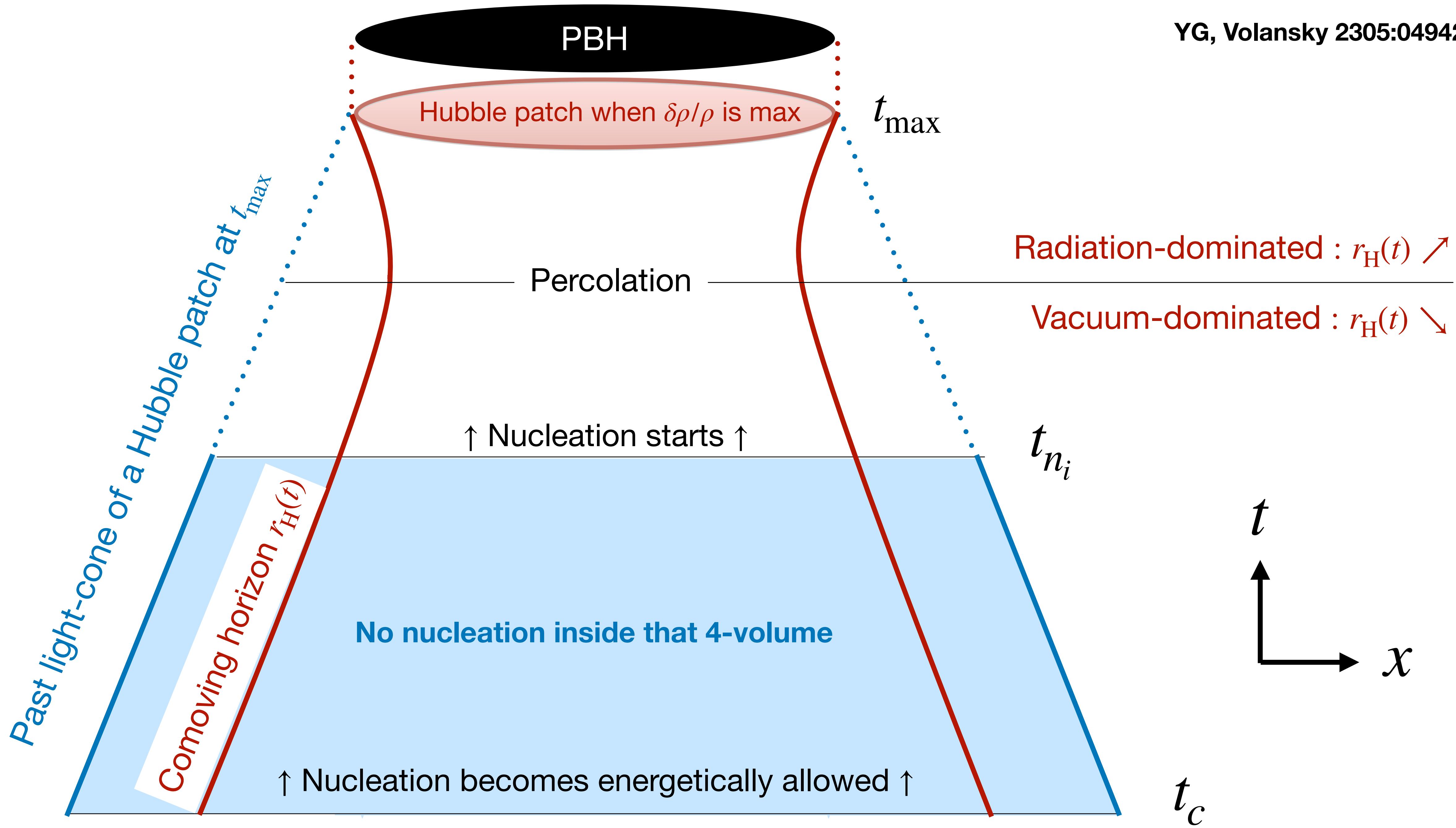












Collapse probability :

$$\mathcal{P}_{\text{coll}} = \exp \left[- \int_{t_c}^{t_{n_i}} dt' \Gamma(t') a(t')^3 \frac{4\pi}{3} \left(\frac{1}{a(t_{\max}) H(t_{\max})} + \int_{t'}^{t_{\max}} \frac{d\tilde{t}}{a(\tilde{t})} \right)^3 \right]$$

Friedmann equation :

$$\frac{\dot{a}(t)}{a(t)} = \sqrt{\frac{\rho_V(t; t_{n_i}) + \rho_R(t; t_{n_i})}{3M_{\text{pl}}^2}}$$

Vacuum energy :

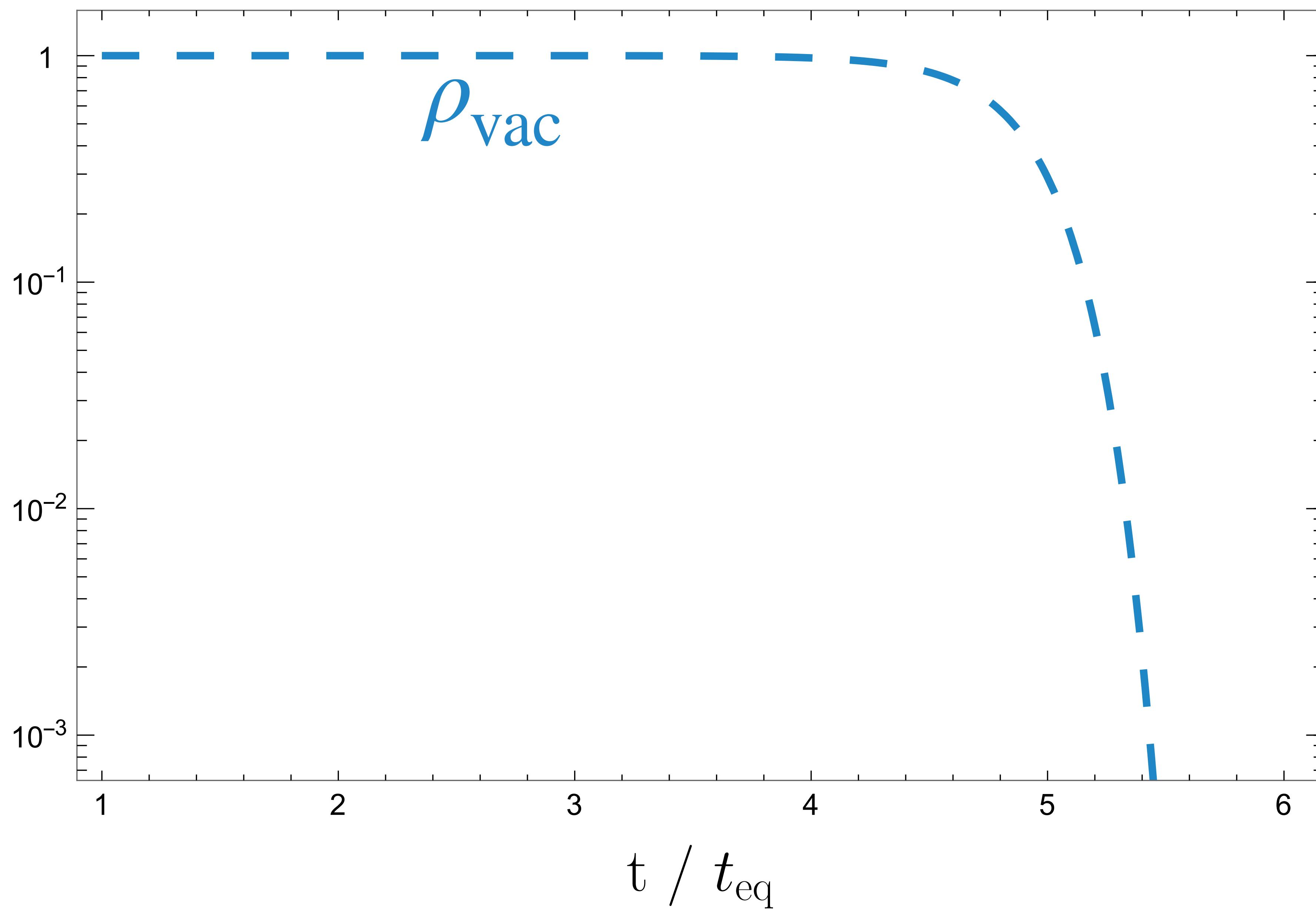
$$\rho_V(t; t_{n_i}) = \Delta V \exp \left[- \int_{t_{n_i}}^t dt' \Gamma(t') a(t')^3 \frac{4}{3} \pi \left(\int_{t'}^t \frac{d\tilde{t}}{a(\tilde{t})} \right)^3 \right]$$

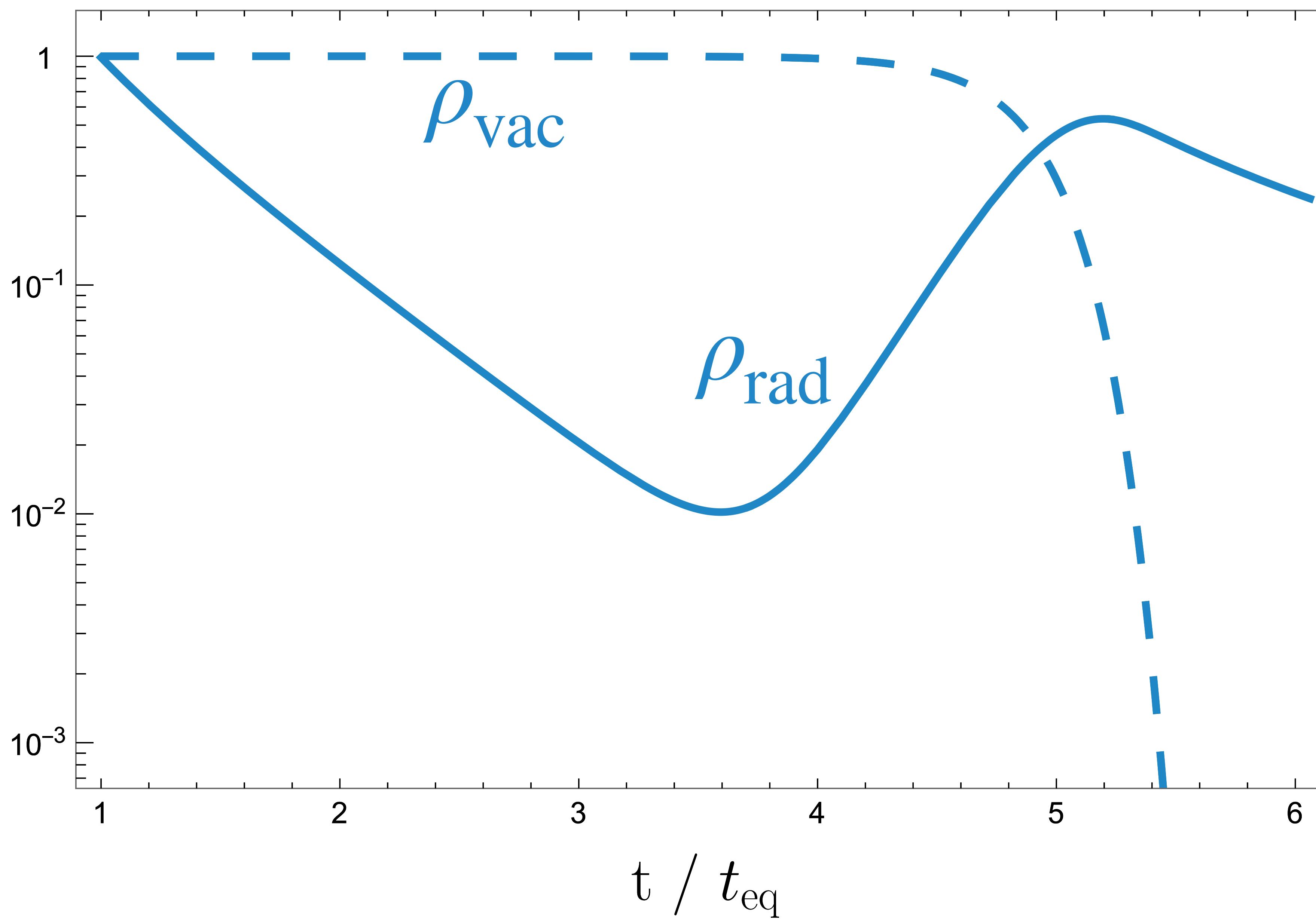
Radiation energy :

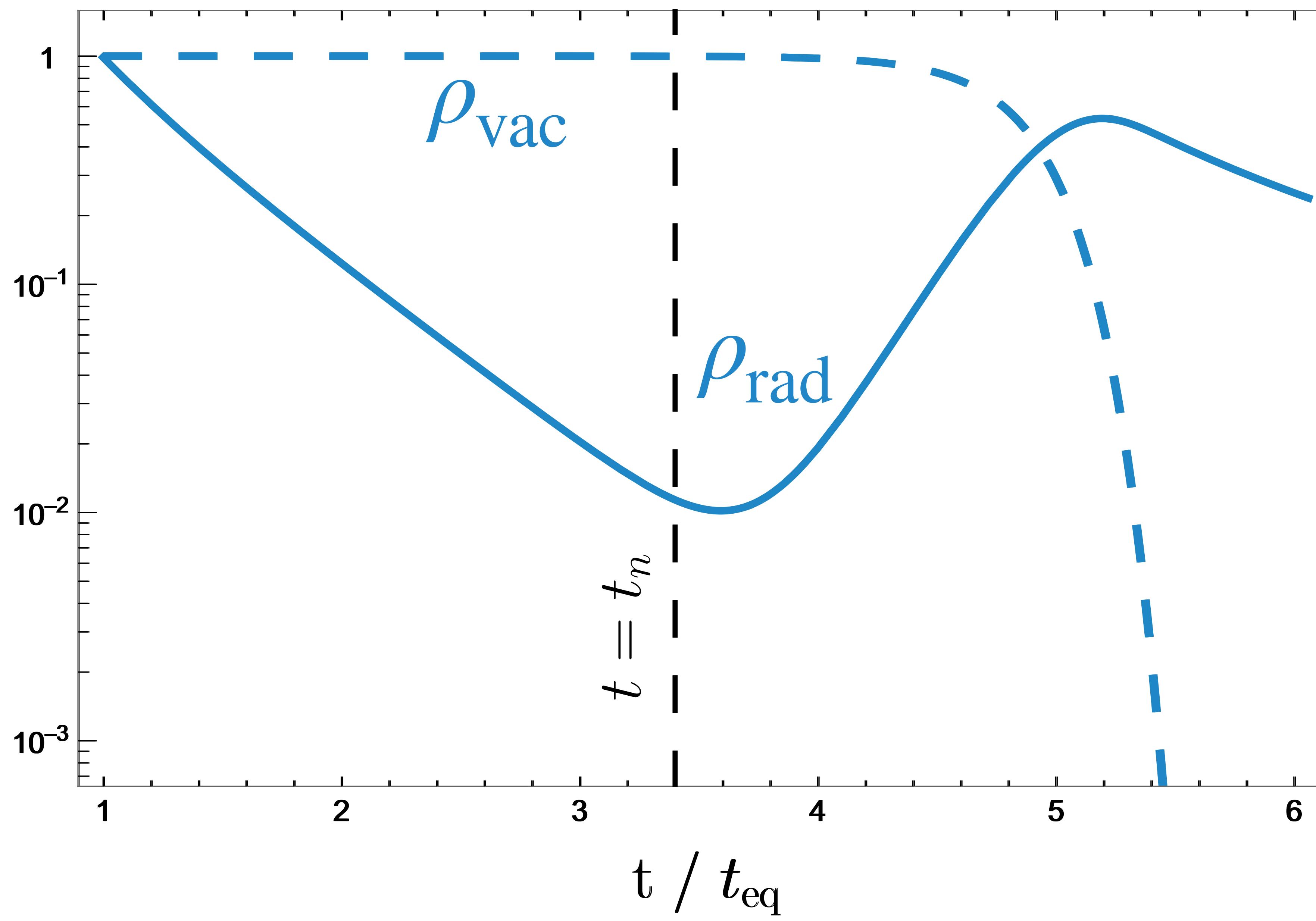
$$\dot{\rho}_R(t; t_{n_i}) + 4H\rho_R(t; t_{n_i}) = -\dot{\rho}_V(t; t_{n_i})$$

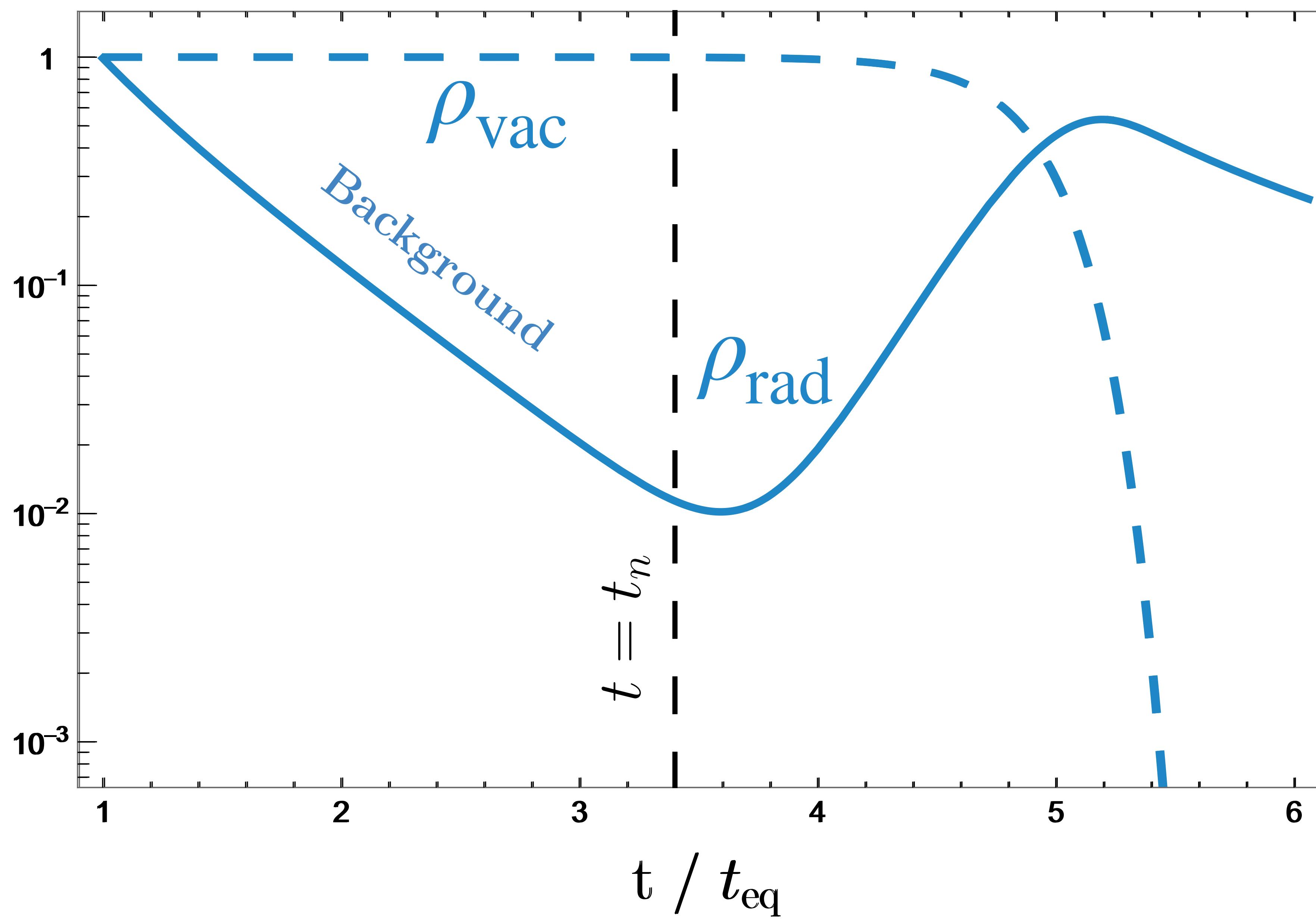
PBH formation threshold :

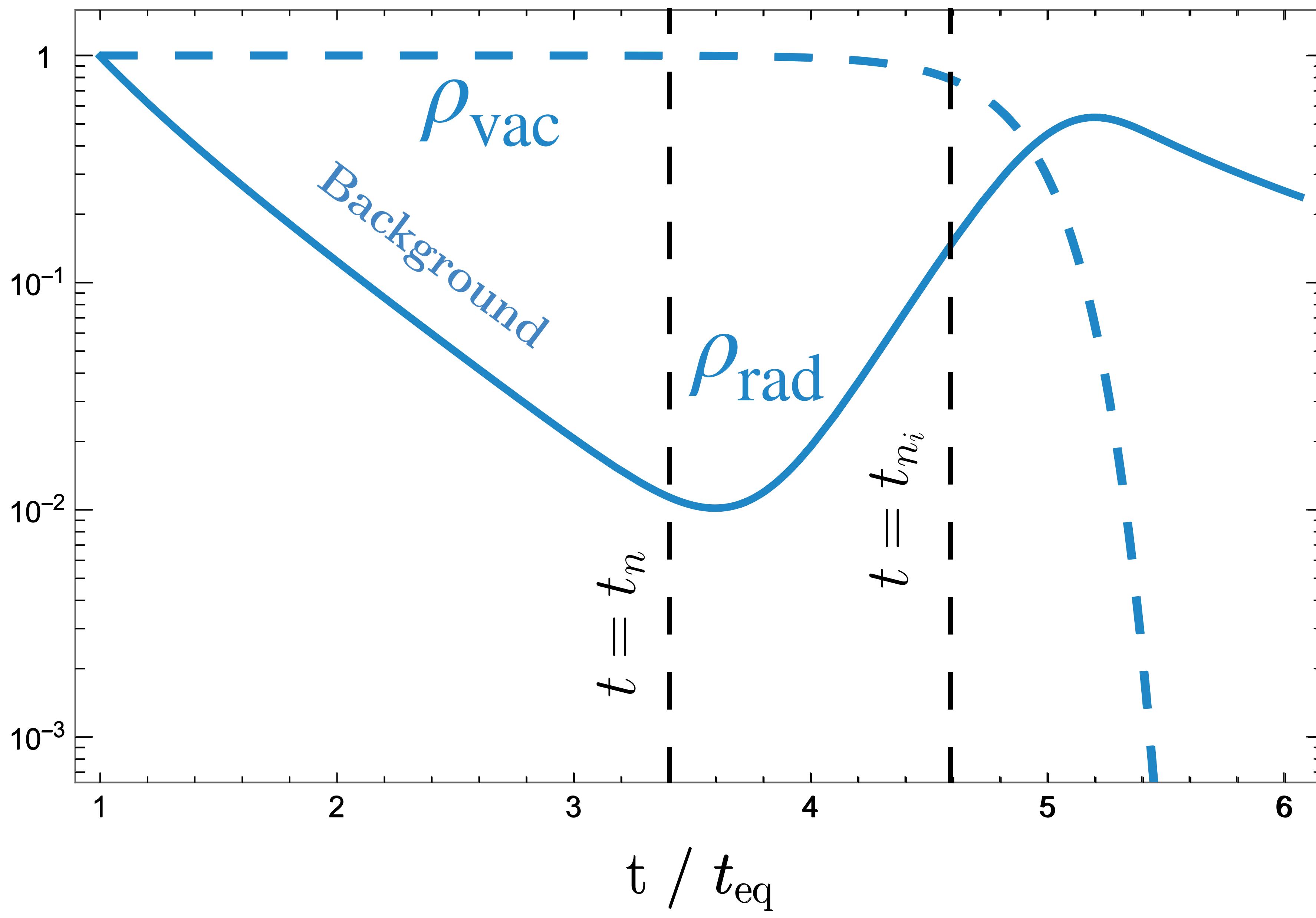
$$\frac{\rho_R(t_{\max}; t_{n_i}) - \rho_R(t_{\max}; t_c)}{\rho_R(t_{\max}; t_c)} \simeq 0.45,$$

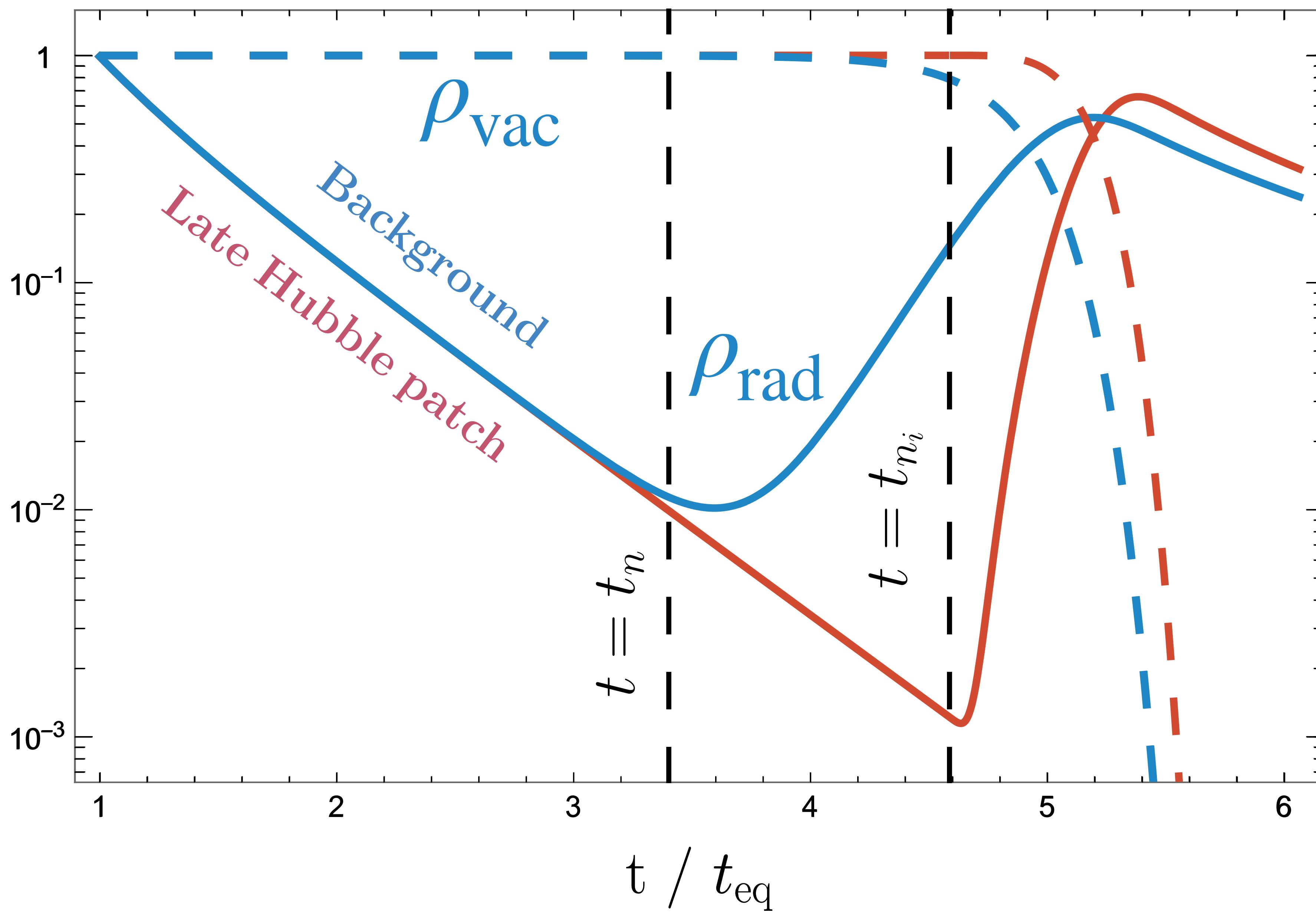


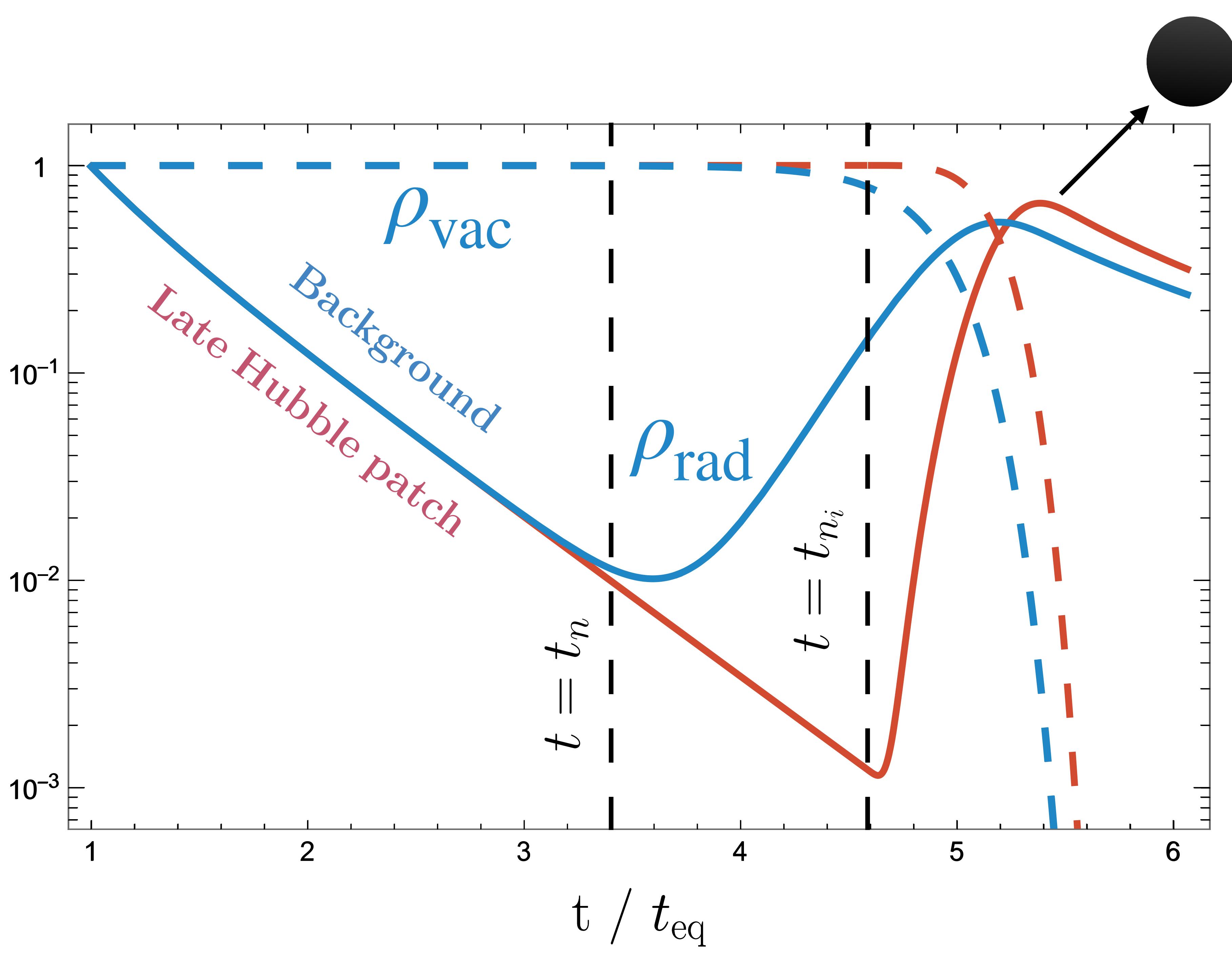












PBH from supercooled phase transitions

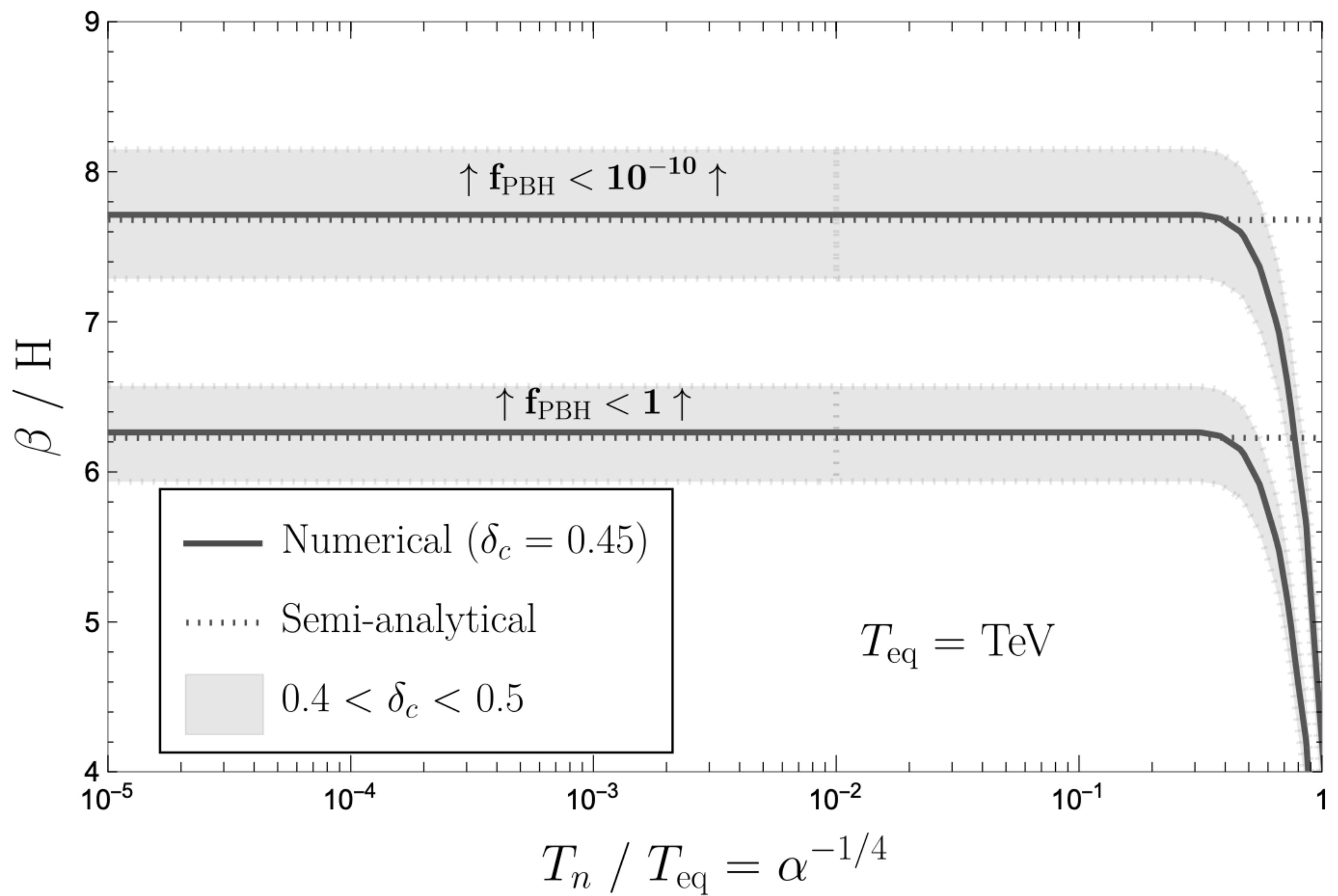
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$$\Gamma = \Gamma_0 e^{\beta t}$$

$$\beta \equiv \frac{d \log \Gamma}{dt}$$

$\beta^{-1} \simeq$ PT duration

\simeq bubble size



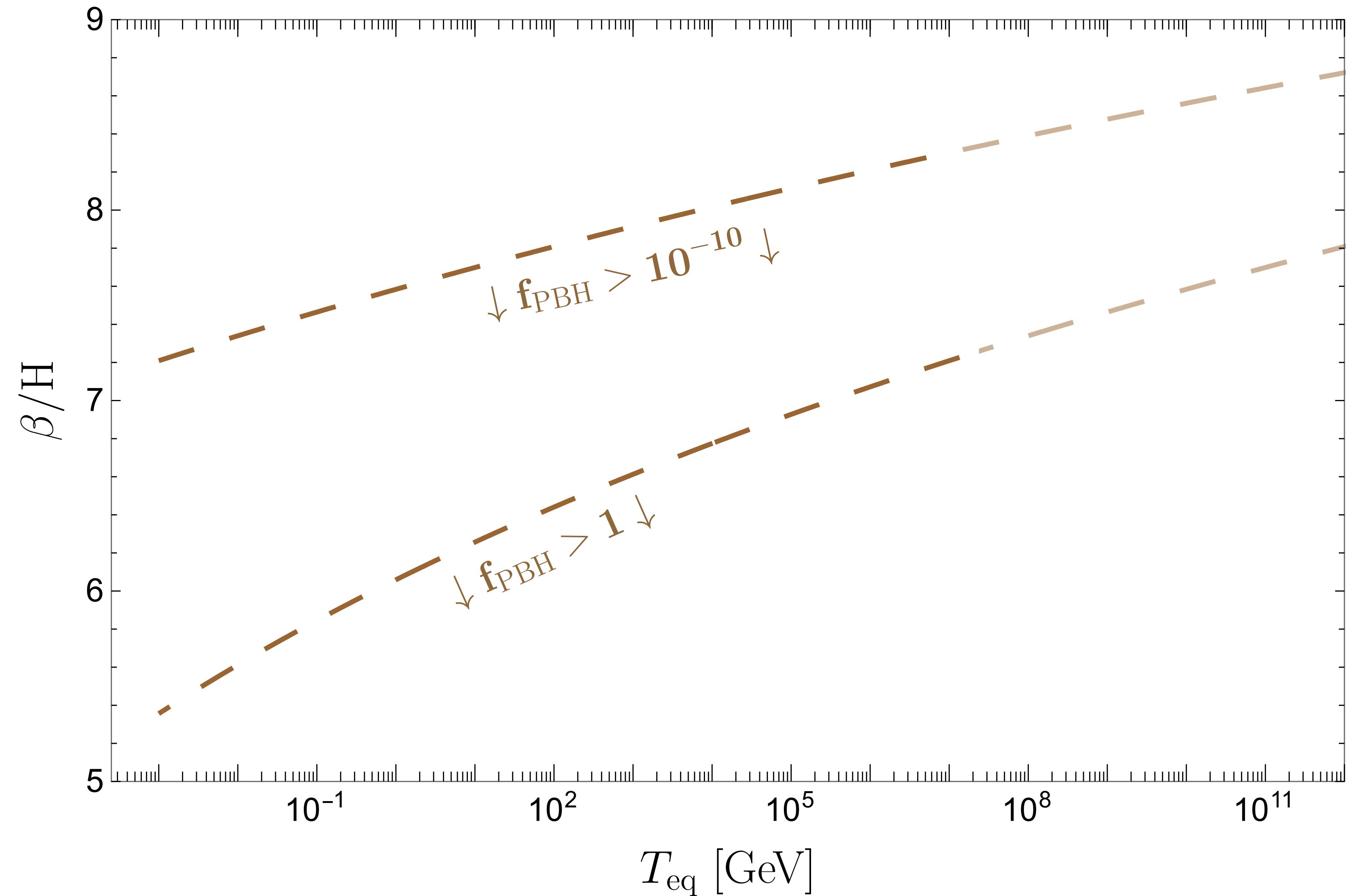
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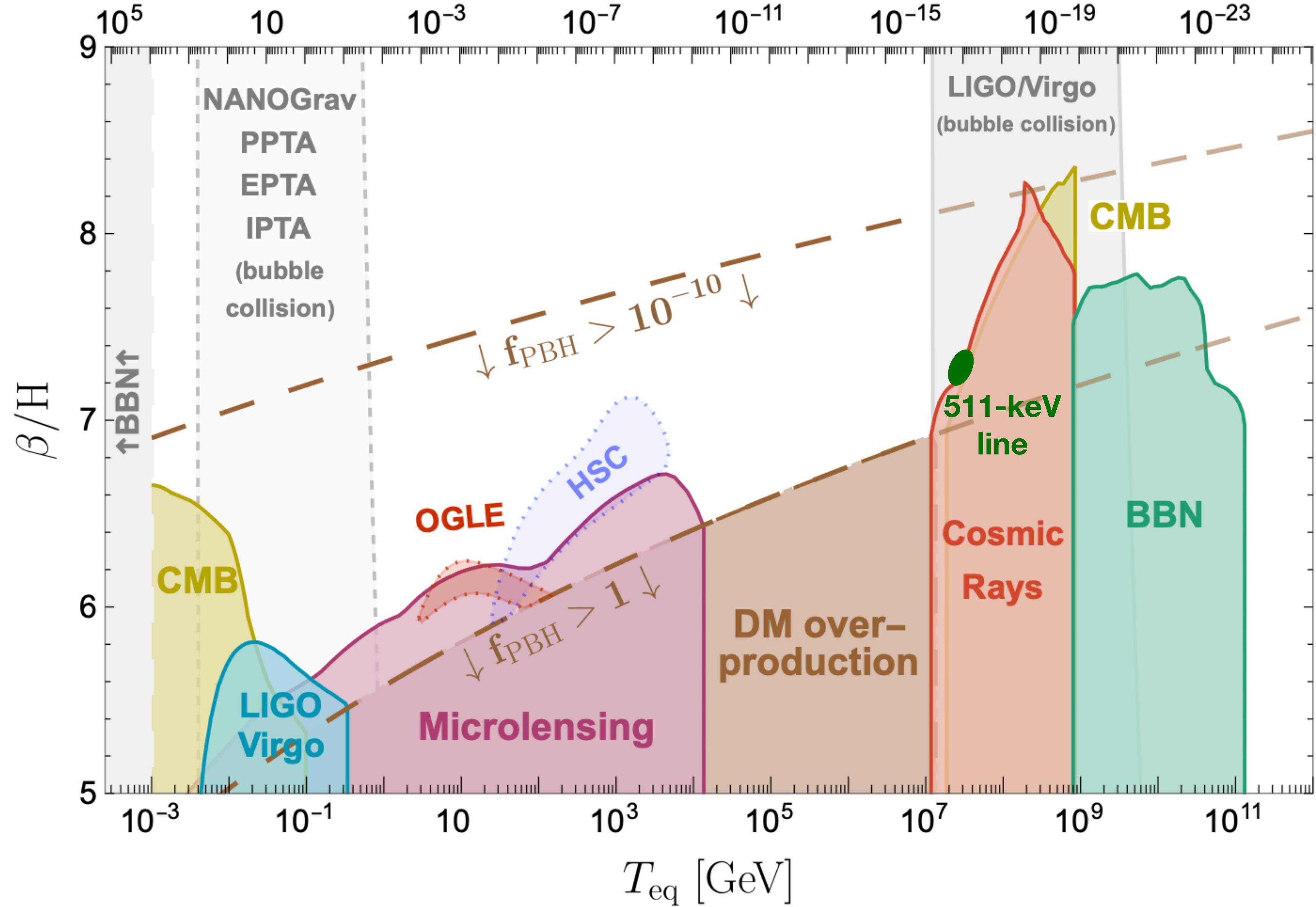


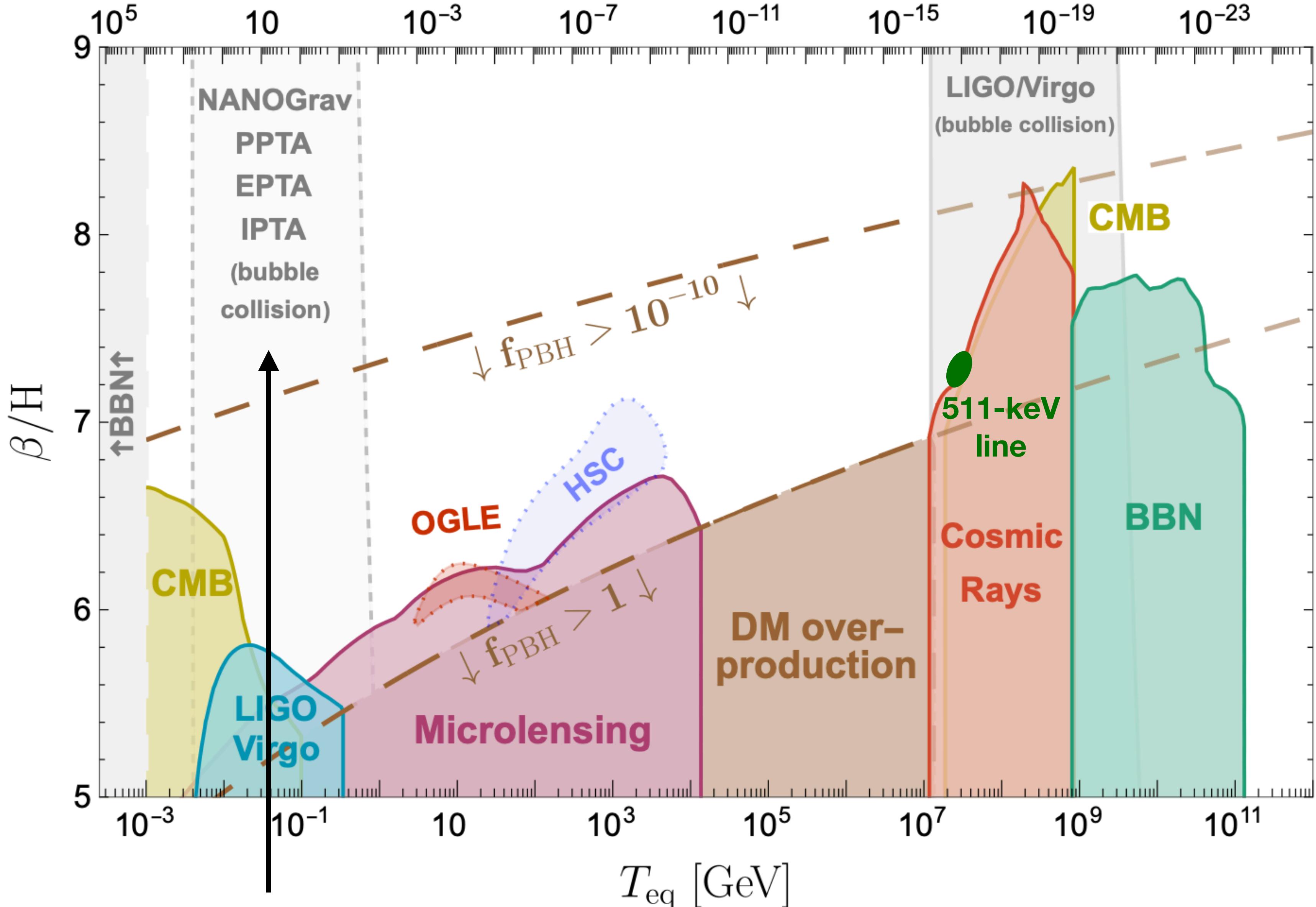
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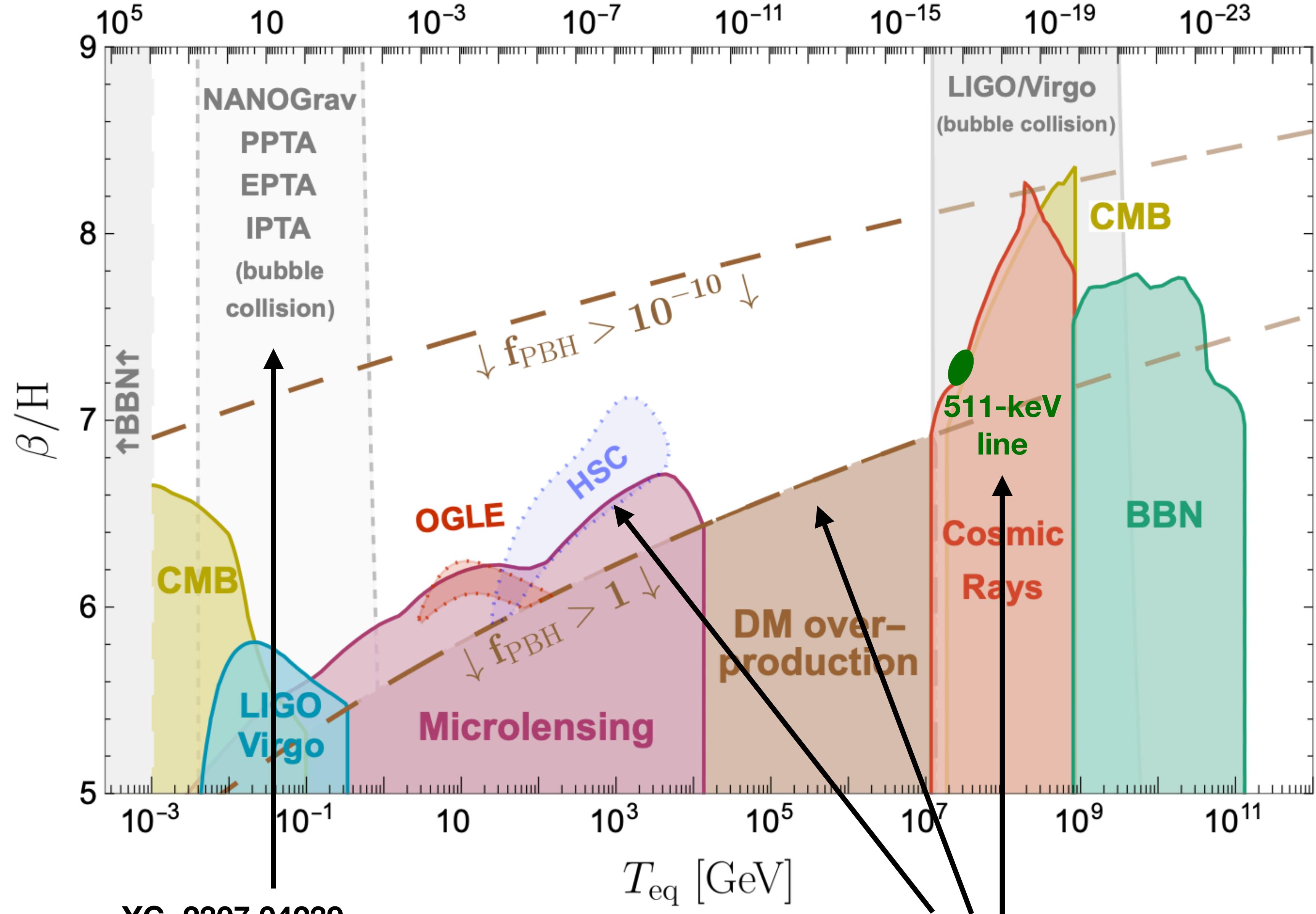
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YG, 2311.13640

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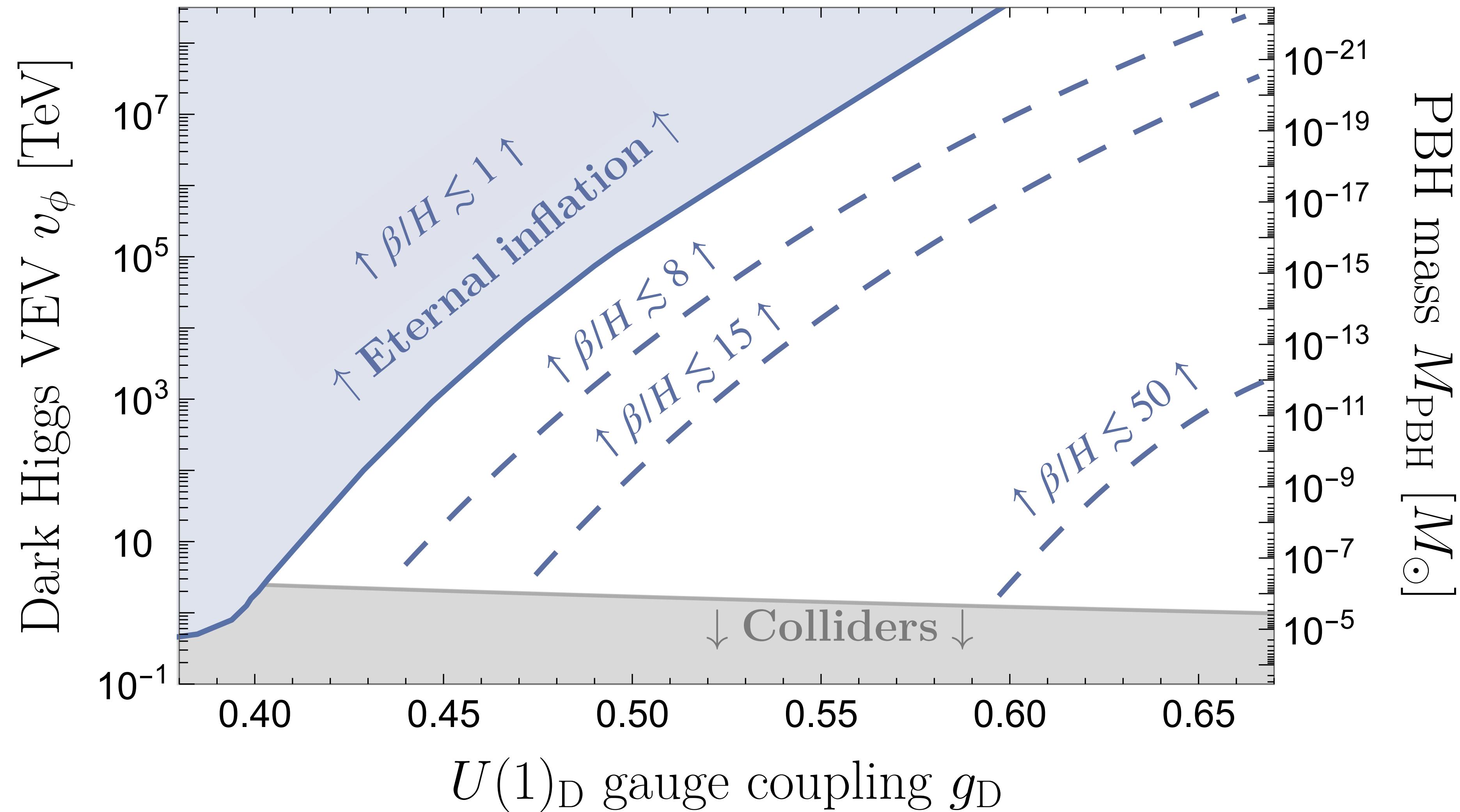
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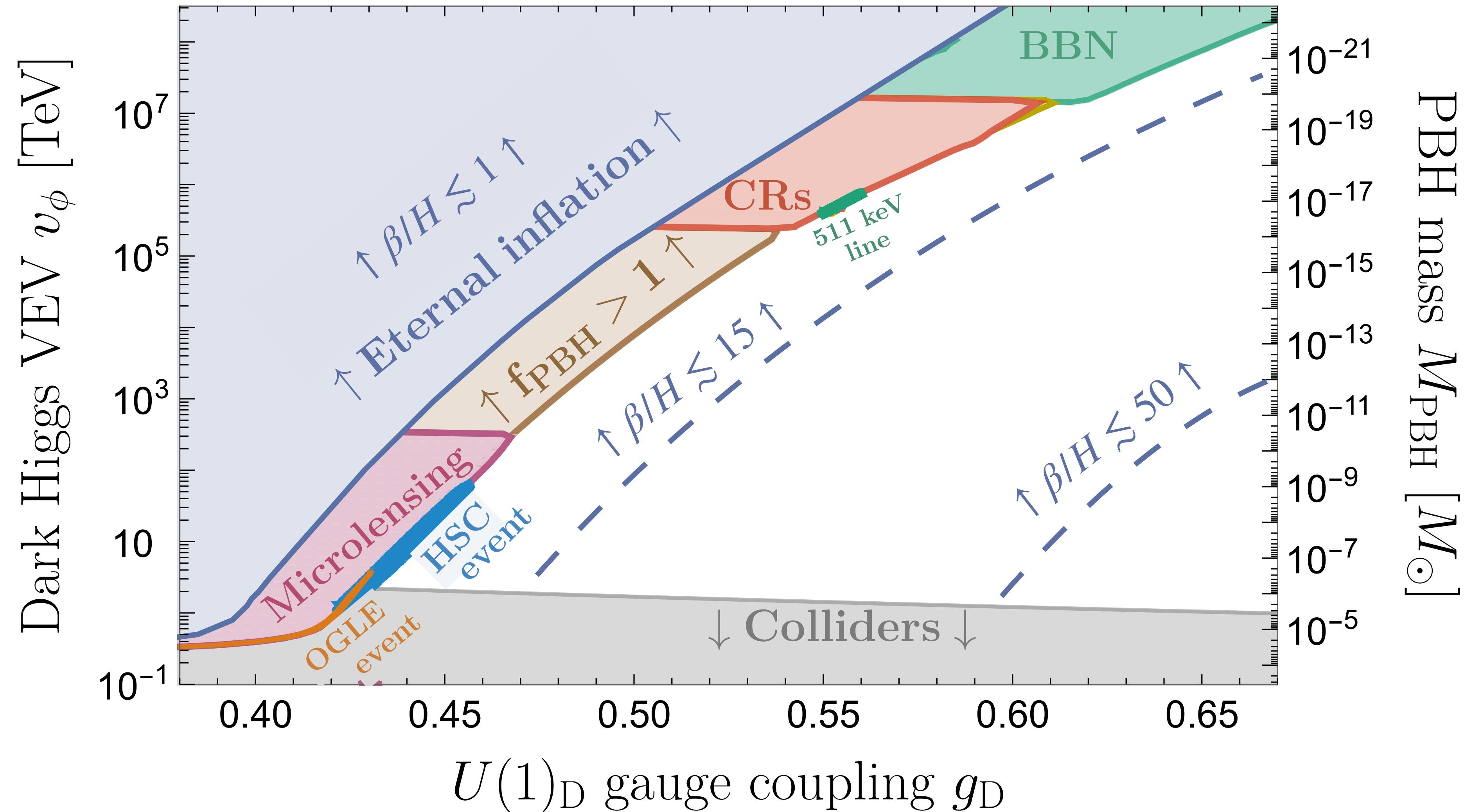
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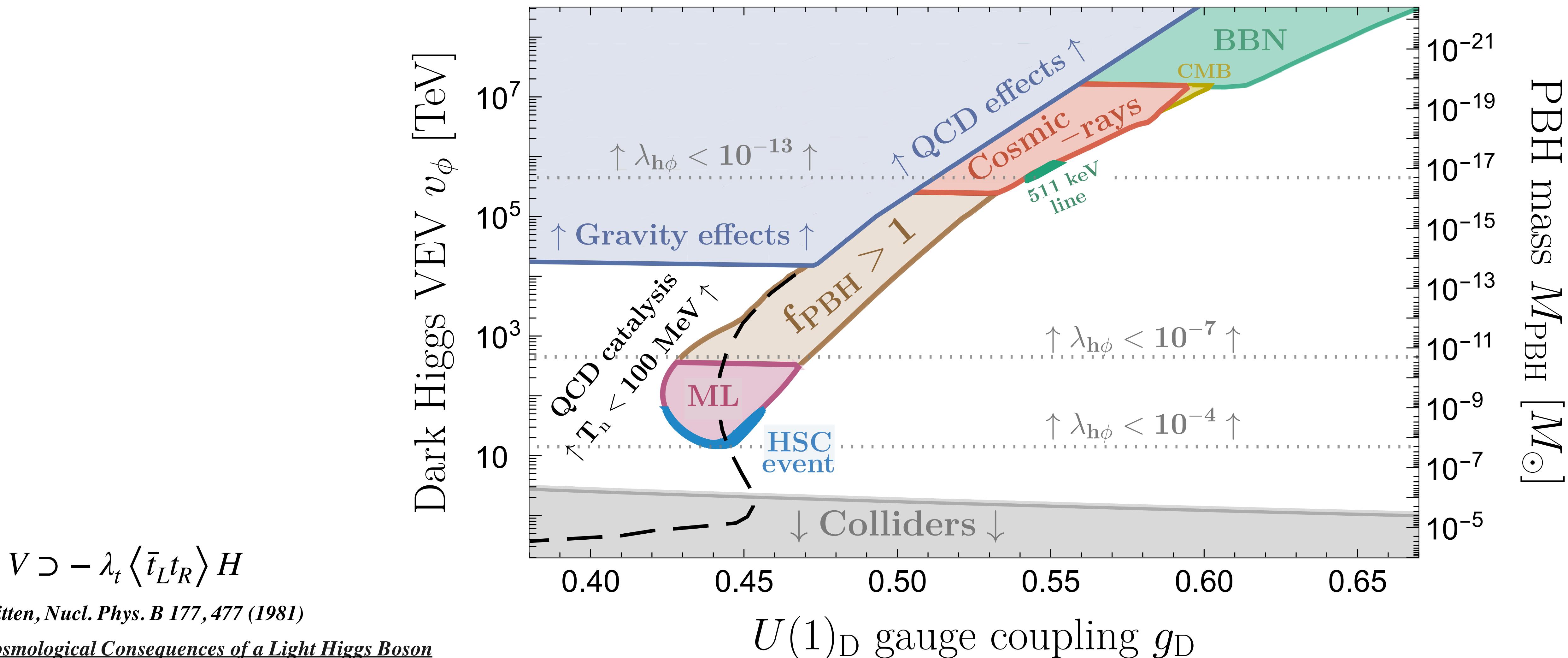
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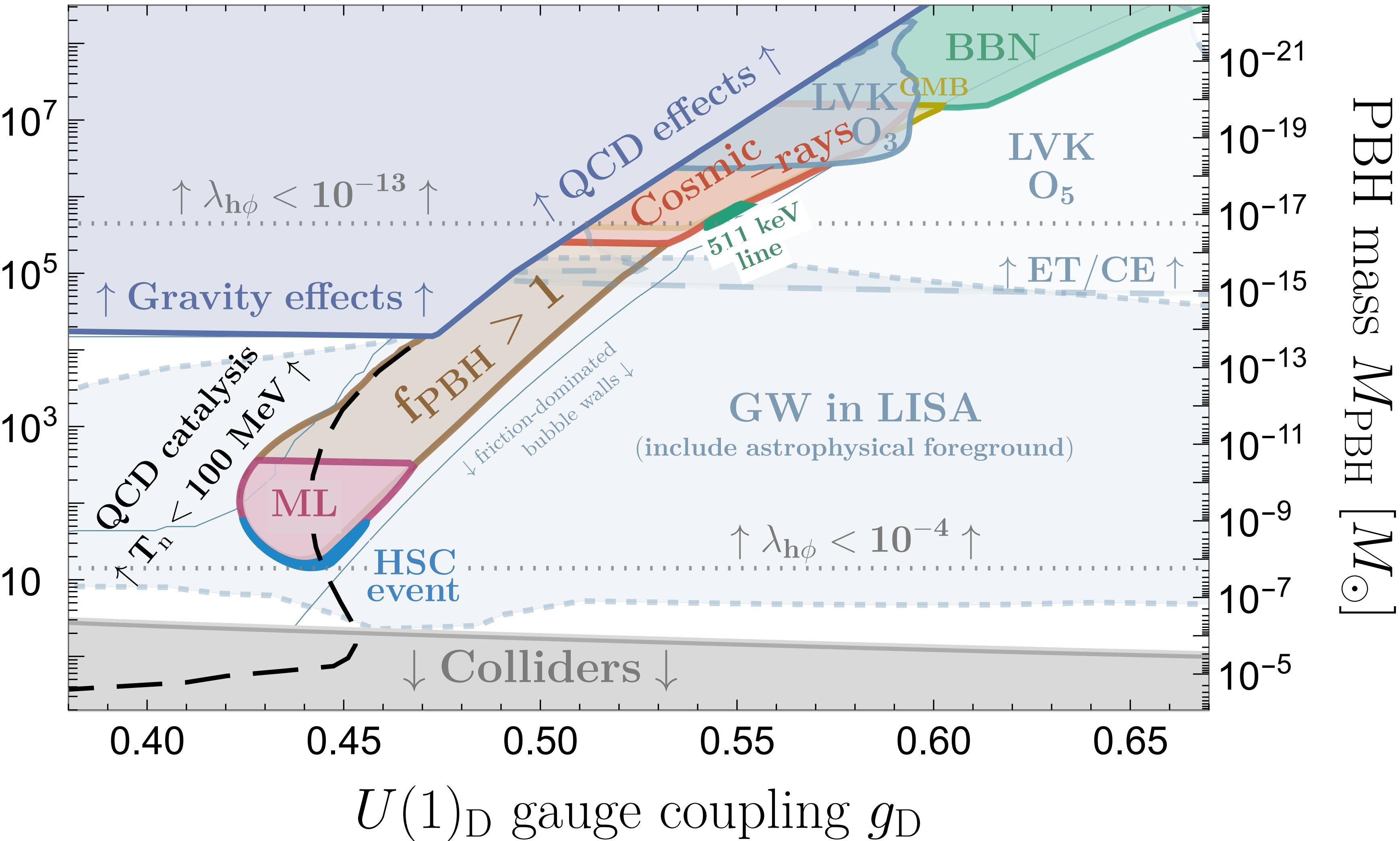
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Witten, Nucl. Phys. B 177, 477 (1981)

Cosmological Consequences of a Light Higgs Boson



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$$\Omega_{\text{GW}} \rightarrow D^{-4/3} \Omega_{\text{GW}}$$

$$D \simeq \frac{T_{\text{dom}}}{\sqrt{M_{\text{pl}} \Gamma_\phi}} \propto \lambda_{h\phi}$$

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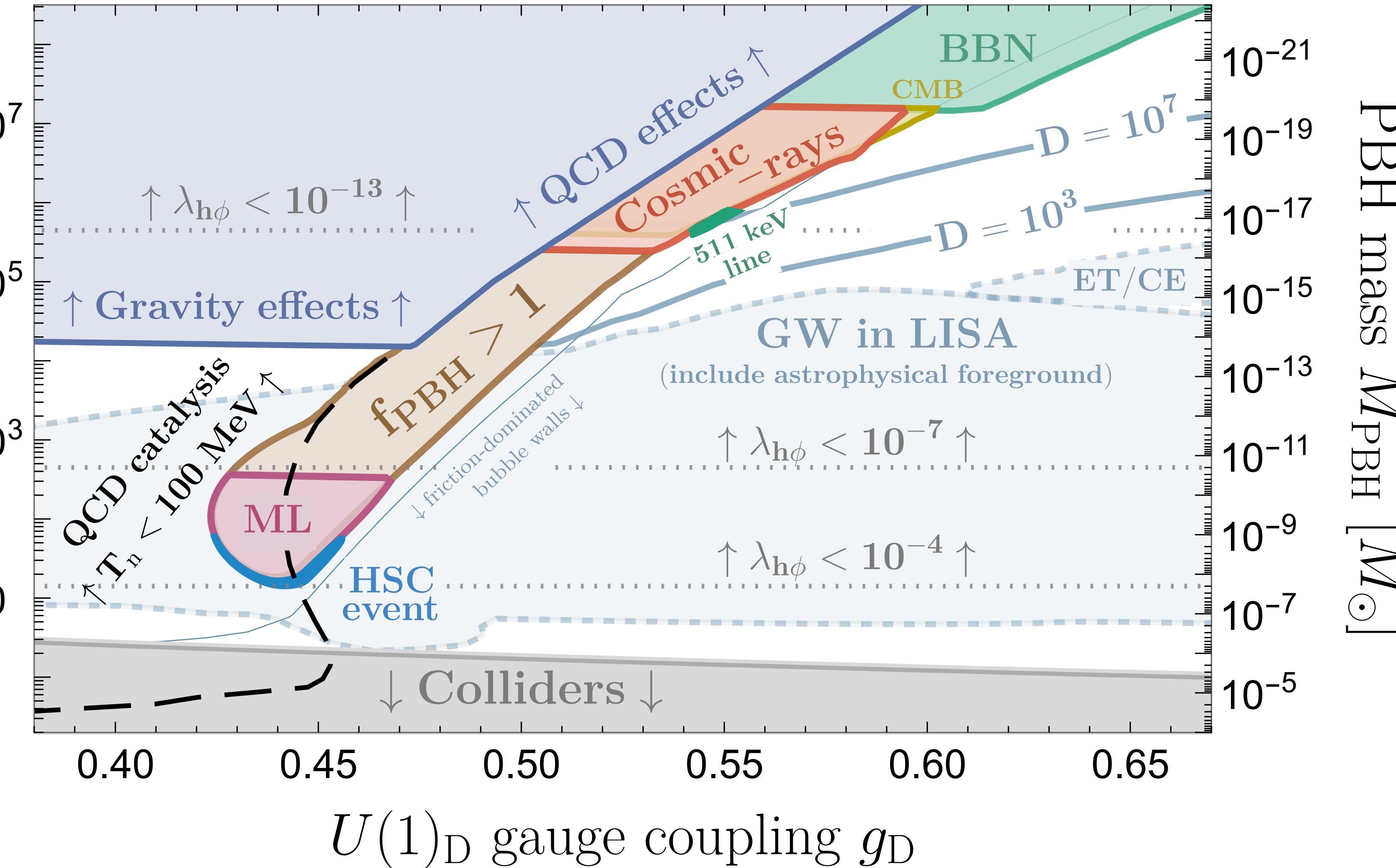
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Dark Higgs VEV v_ϕ [TeV]

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YG, Volansky 2305:04942

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YG, 2307.04239, Phys.Rev.Lett. 131 (2023) 17

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YG, 2307.04239, Phys.Rev.Lett. 131 (2023) 17

4) **Scale-invariant U(1) extension of SM:**

Only two additional parameters g_D and v_ϕ

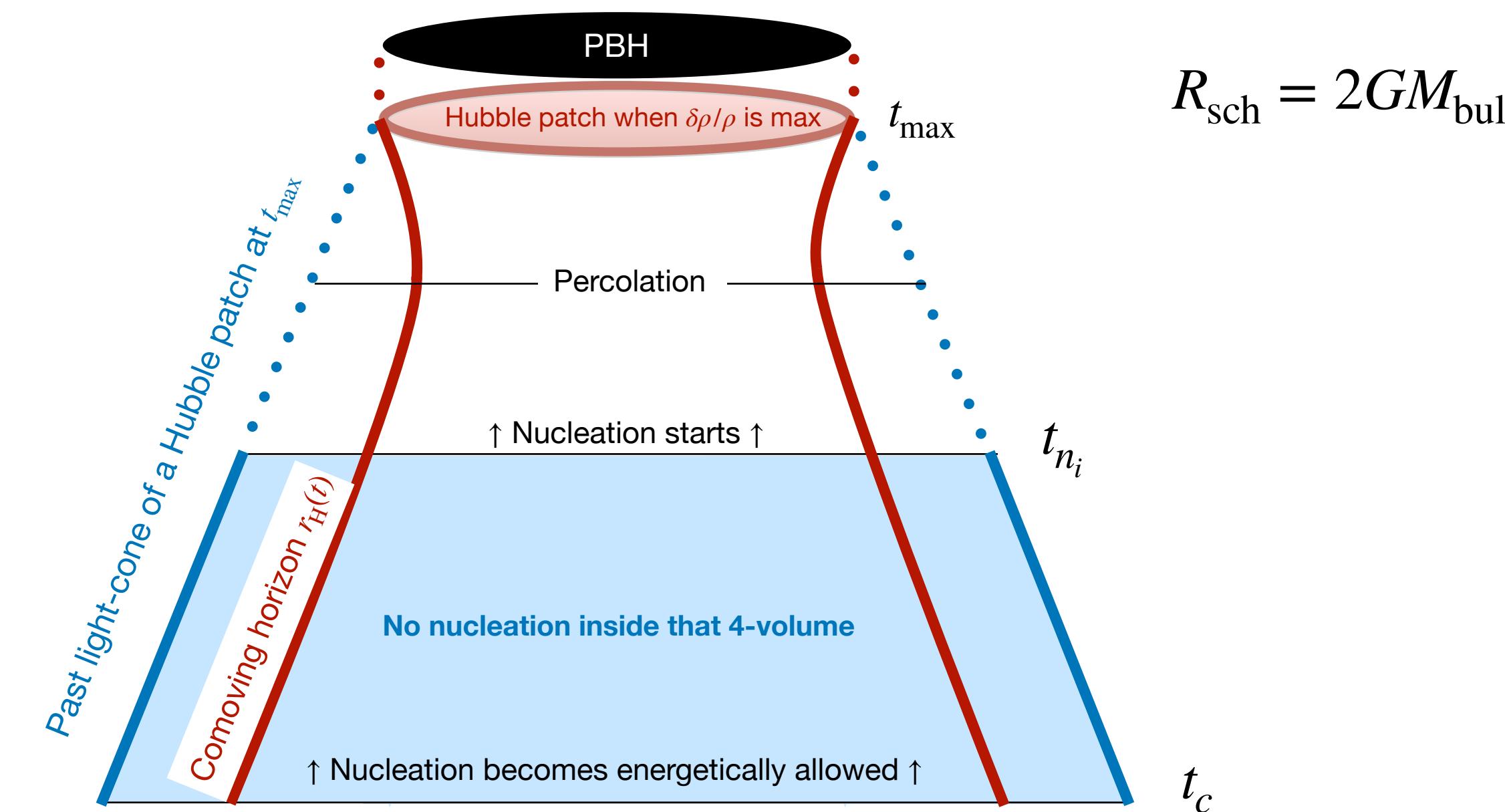
YG, 2311.13640

- Explain HSC lensing anomaly ($v_\phi \sim 20$ TeV)
- Explain 100% of DM ($v_\phi \in [300 \text{ TeV}, 300 \text{ PeV}]$)
- Explain 511-keV line ($v_\phi \sim 5 \times 10^8 \text{ GeV}$)

2023: Primordial Black Holes from Supercooled Phase Transitions,
YG, Volansky, 2305.04942

1982: Kodama, Sasaki, Sato, Abundance of Primordial Holes Produced by Cosmological First Order Phase Transition
(Prog.Theor.Phys. 68 (1982) 1979)

2023: Primordial black holes from strong first-order phase transitions, Lewicki, Toczek, Vaskonen,
JHEP 09 (2023) 092, 2305.04924

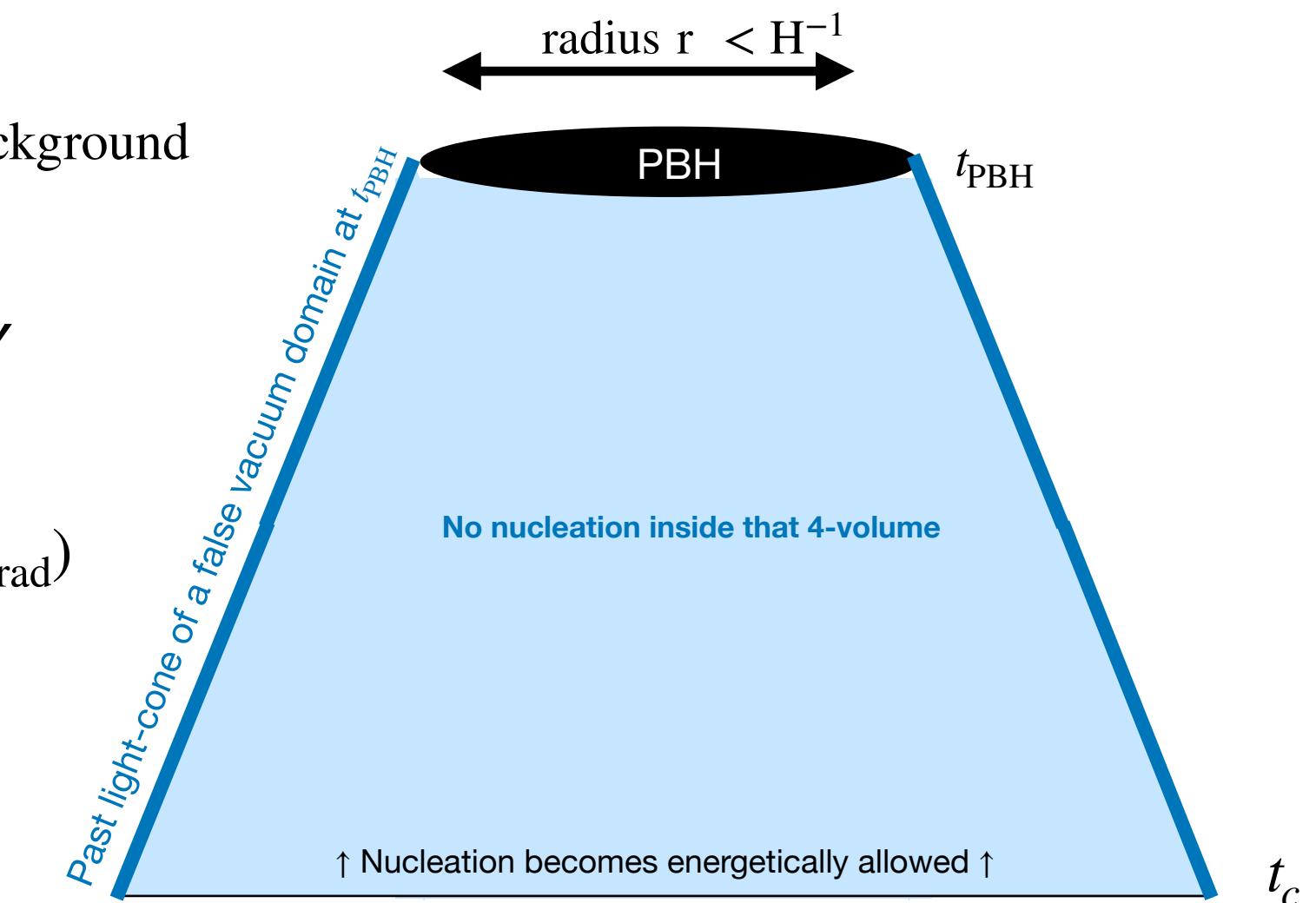


$$R_{sch} = 2G\delta M$$

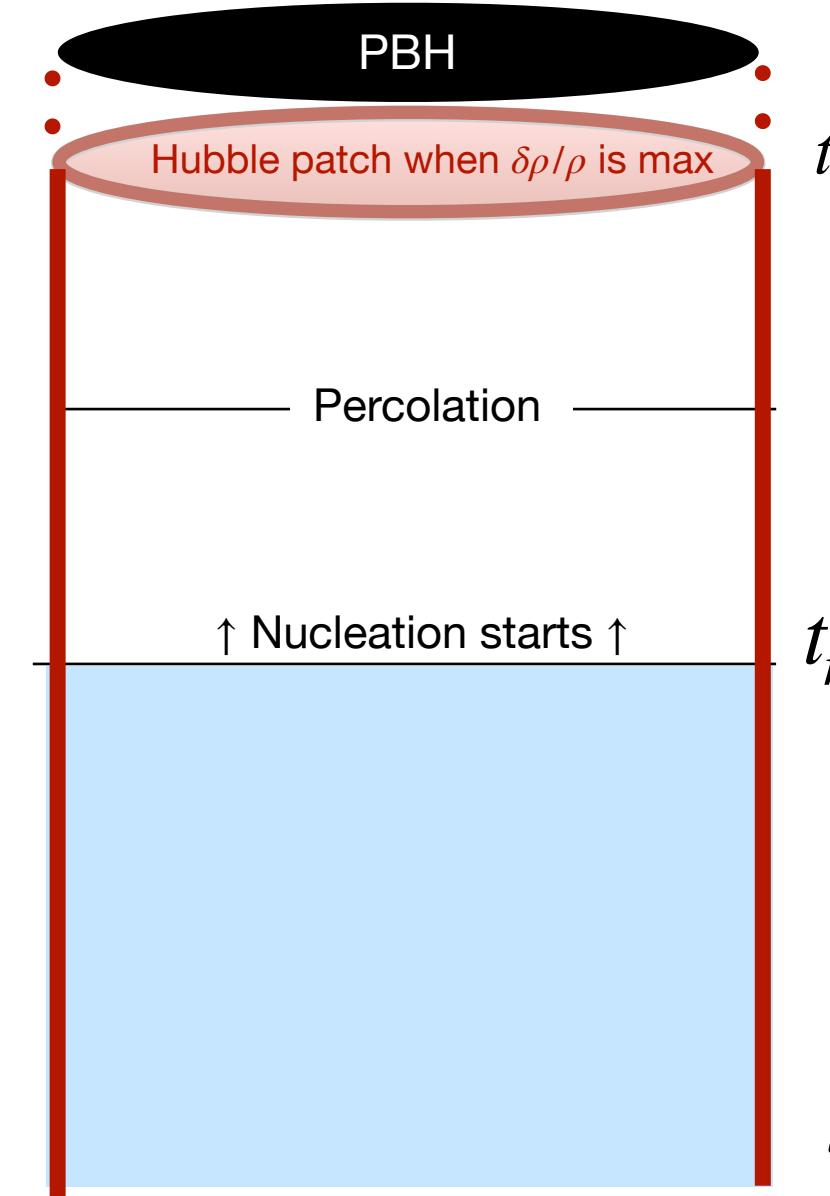
$$\delta M = M_{bulk} + M_{wall} - M_{background}$$

$$M_{bulk} \simeq \frac{4\pi}{3} r^3 \Delta V + 4\pi r^2 \sigma \gamma$$

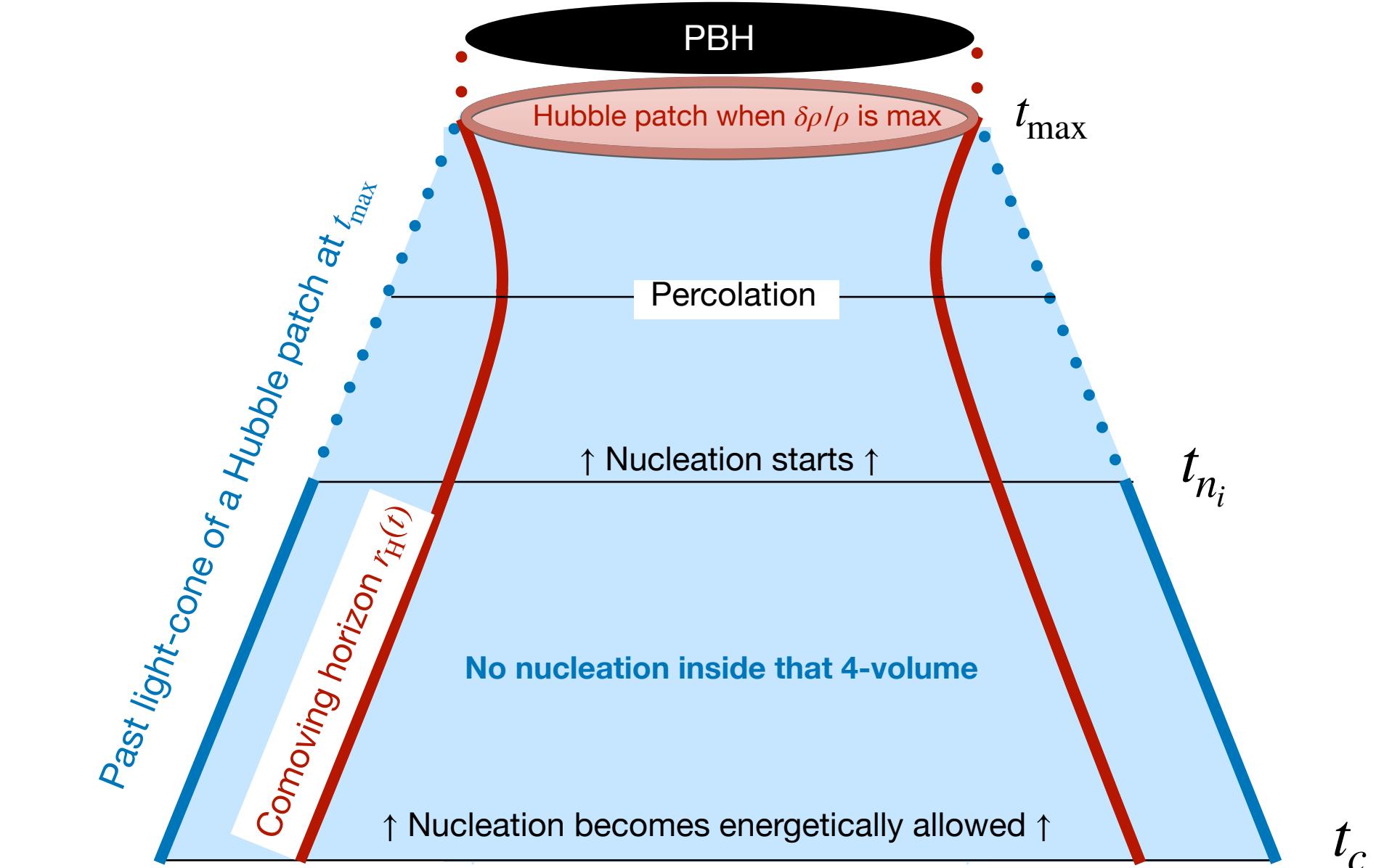
$$M_{background} \simeq \frac{4\pi}{3} r^3 (\rho_{vac} + \rho_{wall} + \rho_{rad})$$



2021: Liu, Bian, Can, Guo, Wang, Primordial black hole production during first-order phase transitions, 2106.05637, Phys.Rev.D 105 (2022) 2



2022: Kawana, T. Kim, and P. Lu, PBH Formation from Overdensities in Delayed Vacuum Transitions, 2212.14037



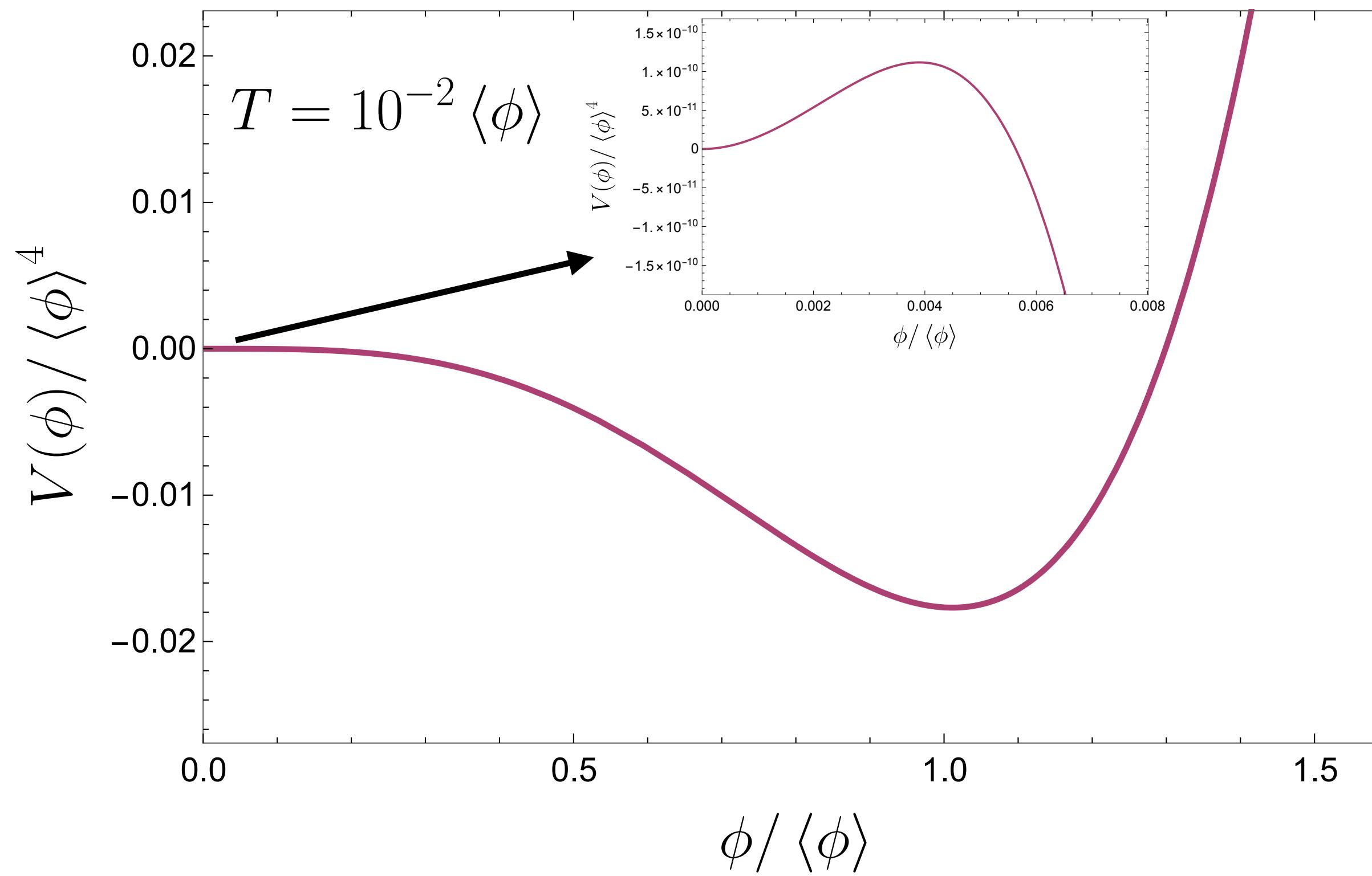
PBH from conformal Higgs

YG, 2311.13640

Scale invariant Higgs + U(1)

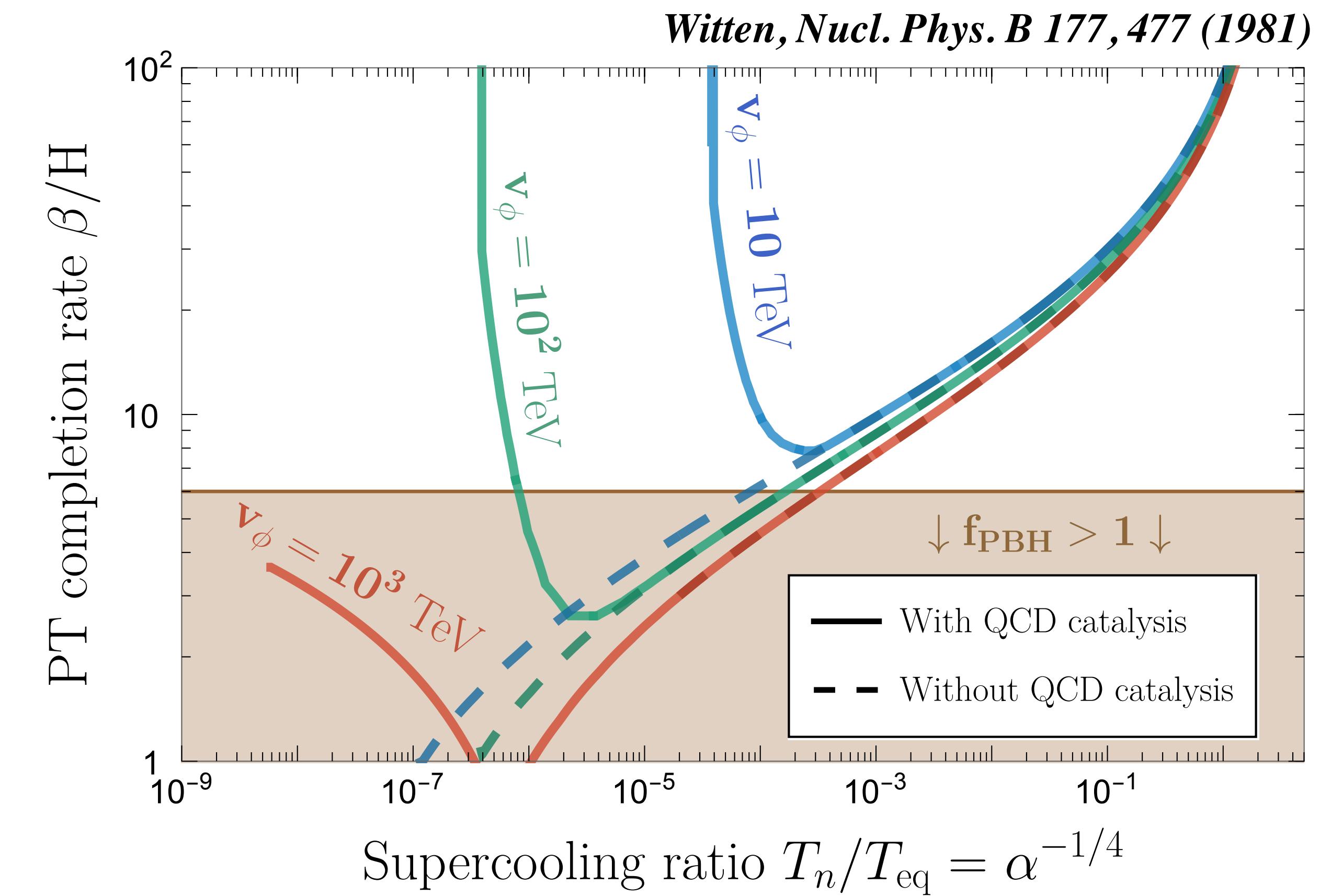
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$$T_n \simeq T_c \exp\left(-\frac{127}{g_D^3 S_c}\right)$$

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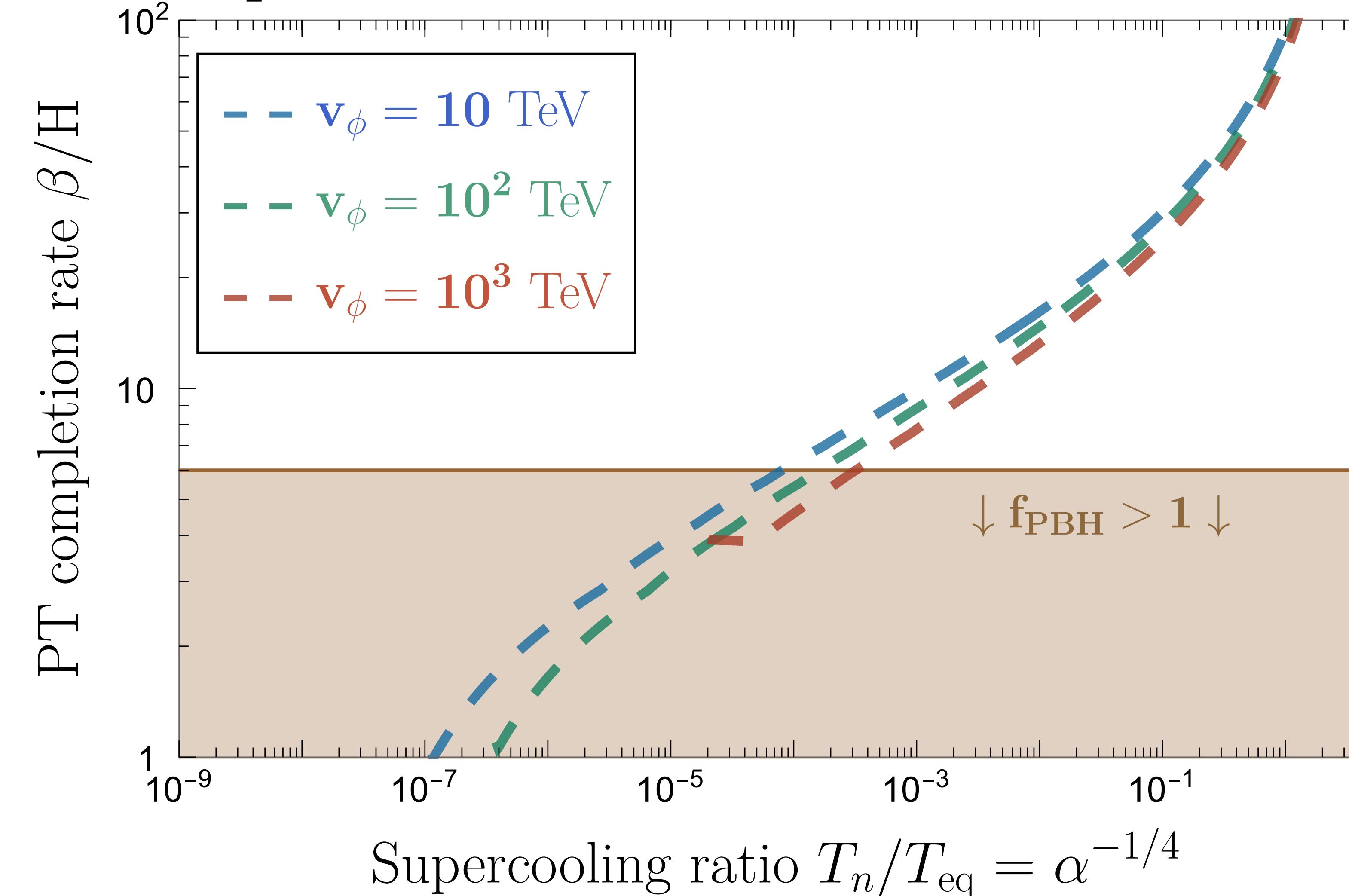
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