Primordial black holes as dark matter: Interferometric tests of phase transition origin

lason Baldes Based on work with María Olalla Olea-Romacho, 2307.11639





IRN Terascale Marseille 27 October 2023

PBHs as DM



Escrivà, Kühnel, Tada, 2211.05767

$$f_{
m pbh}\equiv rac{
ho_{
m pbh}}{
ho_{
m \tiny DM}}=1 \hspace{1cm} 10^{-16}M_\odot \lesssim M_{
m \tiny PBH}\lesssim 10^{-10}M_\odot$$

- Inflationary overdensities (ultra-slow roll, waterfall...)
- Phase transition at the end of inflation
- Early universe dissipative processes Flores, Kusenko 2008.12456
- Phase transition starting from radiation dominated epoch focus here.

• ...





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Possible PBH production

Late patch mechanism - overview

Late patch mechanism for PBH production Liu et al. 2106.05637

- In an average patch the first bubbles nucleate at $\Gamma_{\rm bub} \sim H^4.$
- Some rare patches experience late nucleation.
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The PBH mass is related to the Hubble scale/mass which is in turn set by the vacuum energy \rightarrow reheat temperature.

$$M_{
m PBH} \sim rac{M_{
m Pl}^3}{T_{
m RH}^2} \implies 10 \ {
m TeV} \lesssim T_{
m RH} \lesssim 10^4 \ {
m TeV}$$

From previous estimates from the literature: The GW signal $\propto 1/R_{
m bub}^2$

$$\Omega_{\rm GW} \sim 10^{-6} \left(\frac{H}{\beta}\right)^2$$

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 $\frac{\beta}{H}$

$$\approx 8 \qquad \text{and} \qquad 10 \; \mathrm{TeV} \lesssim \, \mathcal{T}_{\rm \tiny RH} \lesssim 10^4 \; \mathrm{TeV}$$

 \implies detectable GWs. The details we calculated follow.

Classically scale invariant gauged B-L with $Q_{\scriptscriptstyle B-L}(\rho)=-2$

$$\mathcal{L} \supset (D_\mu
ho)^* (D^\mu
ho) - \lambda_
ho |
ho|^4 - \lambda_{
ho h} |
ho|^2 |H|^2 - \lambda_h |H|^4$$

Three right handed neutrinos cancel off anomalies.

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Coleman-Weinberg symmetry breaking

$$V_0(
ho) = eta_{\lambda_
ho} rac{
ho^4}{4} \left(\log\left[rac{
ho}{v_
ho}
ight] - rac{1}{4}
ight) \qquad eta_{\lambda_
ho} pprox rac{1}{(4\pi)^2} \left(96g_{B-L}^4 - y_{Ni}^2
ight)$$

Classically scale invariant gauged B - L with $Q_{B-L}(\rho) = -2$

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Coleman-Weinberg symmetry breaking

$$V_0(\rho) = \beta_{\lambda_\rho} \frac{\rho^4}{4} \left(\log \left[\frac{\rho}{v_\rho} \right] - \frac{1}{4} \right) \qquad \beta_{\lambda_\rho} \approx \frac{1}{(4\pi)^2} \left(96g_{B-L}^4 - y_{Ni}^2 \right)$$

$$\Lambda_{\rm vac} = \frac{\beta_{\lambda_{\rho}} v_{\rho}^4}{16}$$

Details - Finite temperature effective potential



Potential barrier from the gauge boson thermal corrections.

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Potential barrier from the gauge boson thermal corrections.

Bubble nucleation rate calculated numerically

$$\Gamma_{\rm bub} \approx {\rm Max} \left[\frac{1}{R_c^4} \left(\frac{S_4}{2\pi} \right)^2 e^{-S_4}, \quad T^4 \left(\frac{S_3}{2\pi T} \right)^{3/2} e^{-S_3/T} \right]$$



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- Solve for the background and late patches.
- Find what initial late first nucleation temperature, T_i , gives $\delta_{\max} = 0.45$.
- Use this to calculate the PBH formation probability.
- The monochromatic PBH mass approximation is used:

$$M_{
m PBH} = rac{4\pi
ho_{
m radlate}c_{
m s}^2}{3H_{
m late}^3}$$

Details - PBH as DM



- The PBH abundance $f_{\rm pbh}$ and $M_{\rm pbh}$ then depend on the gauge coupling $g_{\rm B-L}$ and v_{ρ} (assuming small y_N).
- We numerically find where $f_{\rm pbh} = 1$.
- $\bullet\,$ The macroscopic phase transition properties are then used to estimate $\Omega_{\rm GW}.$

Details - Bubble size



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- We have checked the standard estimate for the bubble radius

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appears appropriate for close-to-conformal potentials.

• The use of R_{\max} would give a larger signal.





• (3+1)D Lattice simulation of scalar field - Cutting et al. 2005.13537



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These all return similar estimates. Detectable above astro foregrounds.

Details - Expected frequency and SNR



$$\mathrm{SNR}_{\mathrm{FGL}} = \sqrt{t_{\mathrm{obs}} \int \left(\frac{\mathrm{Max}[0, \Omega_{\mathrm{GW}}(\nu) - \Omega_{\mathrm{FG}}(\nu)]^2}{\Omega_{\mathrm{sens}}^2 + 2\Omega_{\mathrm{GW}}\Omega_{\mathrm{sens}} + 2\Omega_{\mathrm{GW}}^2}\right) df}$$

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- Not matched to cosmological perturbation theory to calculate second order $\Omega_{\rm GW}$ from subcritical patches e.g. as in Nakama et al. 1612.06264.
- Not yet clear regarding distinguishing $\Omega_{\rm GW}$ from different PBH formation mechanisms.
- Strong signal does not prove $f_{\rm pbh} = 1$ as the quantity is very sensitive to β/H . However, a large $\Omega_{\rm GW}$ would anyway be welcomed.

Conclusions

- Supercooled phase transition can lead to PBH formation.
- \bullet The required phase transition implies large $\Omega_{\rm GW}$ from bubble collisions.
- The PBH mass is related to the Hubble scale.
- The allowed PBH window maps onto GW frequencies covered by upcoming detectors.
- Very promising way of getting indirect evidence of PBH DM or ruling it out from a late patch mechanism.



• Similarly the use of the approximate nucleation rate common in the literature

$$\Gamma_{\rm bub}(t) = H^4(t_n)e^{\beta(t-t_n)}$$

is shown to be appropriate for close-to-conformal potentials.



If nucleation rate is low, we can form bubbles which never meet.



If nucleation grows enough, sufficient bubbles to meet will nucleate.



In the classically scale invariant potential we have a slow transition but an exponentially growing nucleation rate.

We can explicitly check the volume of false vacuum decreases and the bubbles will percolate.



$$P(T) \equiv e^{-I(T)} \lesssim 1/e \implies I(T) = \frac{4\pi}{3} \int_{t_c}^t dt' \Gamma(t') a(t')^3 r(t,t')^3 \gtrsim 1$$
$$\frac{1}{H \mathcal{V}_{\text{false}}} \frac{d\mathcal{V}_{\text{false}}}{dt} = 3 + T \frac{dI}{dT} \lesssim -1.$$

Also see Ellis, Lewicki, No 1809.08242 Ellis, Lewicki, No, Vaskonen 1903.09642

The Friedmann equations are given by

$$egin{aligned} \mathcal{H}^2_{
m bkg} &= rac{8\pi}{3}rac{
ho_{
m vac}+
ho_{
m rad}}{M_{
m Pl}^2}, \ &rac{d
ho_{
m rad}}{dt} &= -4\mathcal{H}_{
m bkg}
ho_{
m rad} - rac{d
ho_{
m vac}}{dt}, \end{aligned}$$

where $H_{\rm bkg}$ denotes the Hubble rate of the average background patch.

$$I = \frac{4\pi}{3} \int_{t_c}^{t} dt' \Gamma_{\text{bub}}(t') a^3(t') r^3(t, t')$$
$$= \frac{4\pi}{3} \int_{T}^{T_c} dT' \frac{\Gamma_{\text{bub}}(T')}{T'^4 H(T')} \left(\int_{T}^{T'} \frac{d\tilde{T}}{H(\tilde{T})} \right)^3.$$
$$\rho_{\text{vac}} = \Lambda_{\text{vac}} e^{-I}.$$

Percolation when I(T) > 1 and $d \log \mathcal{V}_{\text{false}}/dt < -H$.





Soft gauge boson production does not stop the wall accelerating.

The condensate decays rapidly.



$$\begin{split} V_{\rm eff}(\rho,T) &= V_0(\rho) + V_T(\rho,T) + V_{\rm daisy}(\rho,T) \\ V_T(\rho,T) &= \frac{T^4}{2\pi^2} \left(3J_B \left[\frac{M_{Z'}^2}{T^2} \right] + 2J_F \left[\frac{M_{Ni}^2}{T^2} \right] \right) \\ V_{\rm daisy}(\rho,T) &= \frac{T}{12\pi} \left(M_{Z'}^3 - [M_{Z'}^2 + \Pi_{Z'}]^{3/2} \right) \\ \Lambda_{\rm vac} &= \frac{\beta_{\lambda_\rho} v_\rho^4}{16} \end{split}$$



Small gauge couplings result in supercooling.





$$\begin{split} P_{\rm coll} &= \mathrm{Exp}\left[-\int_{t_c}^{t_i} dt' \Gamma_{\rm bub}(t') a_{\rm late}(t')^3 V_{\rm coll}\right] \\ &= \mathrm{Exp}\left[-\int_{T_i}^{T_c} \frac{dT' \Gamma_{\rm bub}(T')}{T' H(T')} a_{\rm late}(T')^3 V_{\rm coll}\right] \end{split}$$

The volume factor is

$$egin{aligned} V_{\mathrm{coll}} &= rac{4\pi}{3} \left[rac{1}{a_{\mathrm{late}}(t_{\delta\mathrm{max}}) H_{\mathrm{late}}(t_{\delta\mathrm{max}})} + r(t_{\delta\mathrm{max}},t')
ight]^3 \ &= rac{4\pi}{3} \left[rac{1}{a_{\mathrm{late}}(\mathcal{T}_{\delta\mathrm{max}}) H_{\mathrm{late}}(\mathcal{T}_{\delta\mathrm{max}})} + \int_{\mathcal{T}_{\delta\mathrm{max}}}^{\mathcal{T}'} rac{d\, ilde{\mathcal{T}}}{ ilde{\mathcal{T}}H(ilde{\mathcal{T}}) a_{\mathrm{bkg}}(ilde{\mathcal{T}})}
ight]^3. \end{aligned}$$