

Top Mass Measurements, JES, and Systematic at CDF

Un-ki Yang

The University of Manchester



Workshop on Top Physics, LPSC, Oct 18-20, 2007

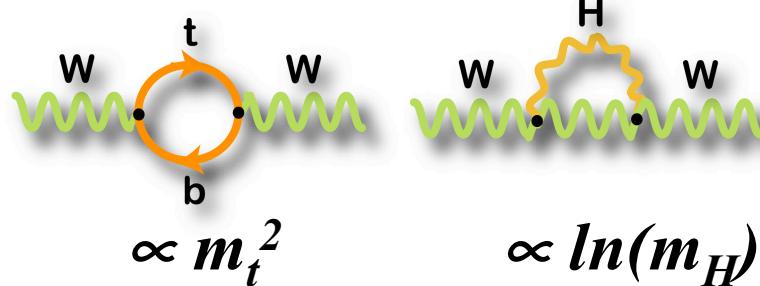
Outline

- Why Precise M_t ?
- Challenges?
- CDF Program (Template in Lepton+Jet)
- Jet Energy Scale and Uncertainty
 - generic jet, light quark jet, and b-jet -
- ISR/FSR and NLO

Why Precise Top Mass?

- Top mass is a fundamental SM parameter

- Important in loop corrections

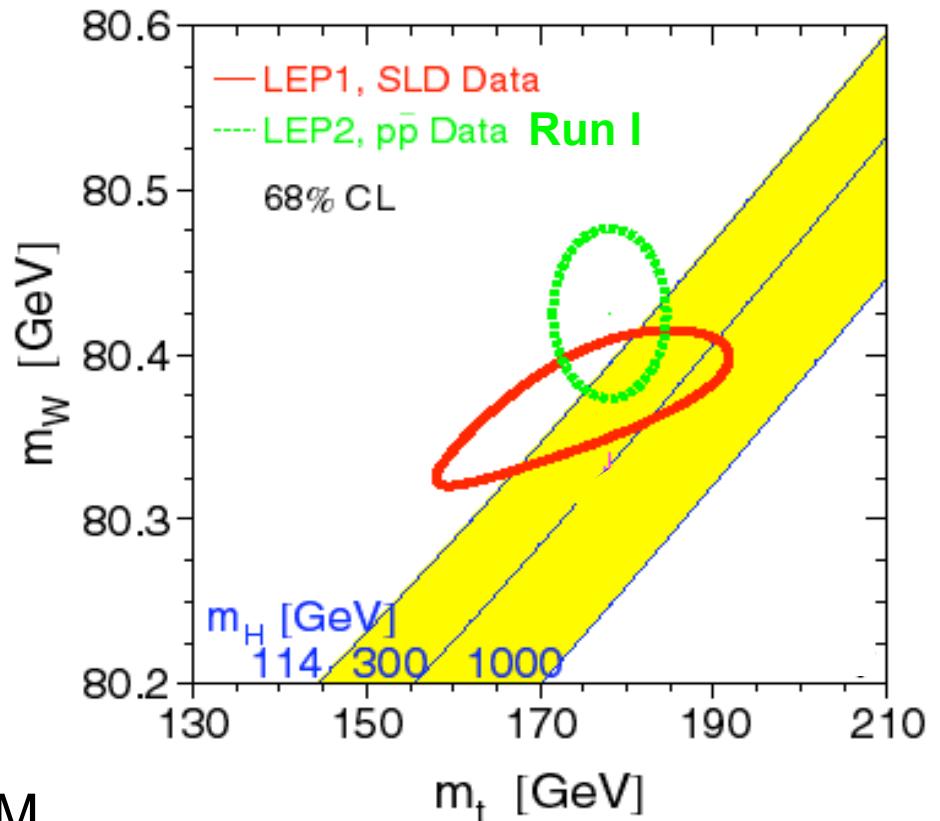


- Precise Top & W masses

- Constraint on SM Higgs
- It can point to physics BSM

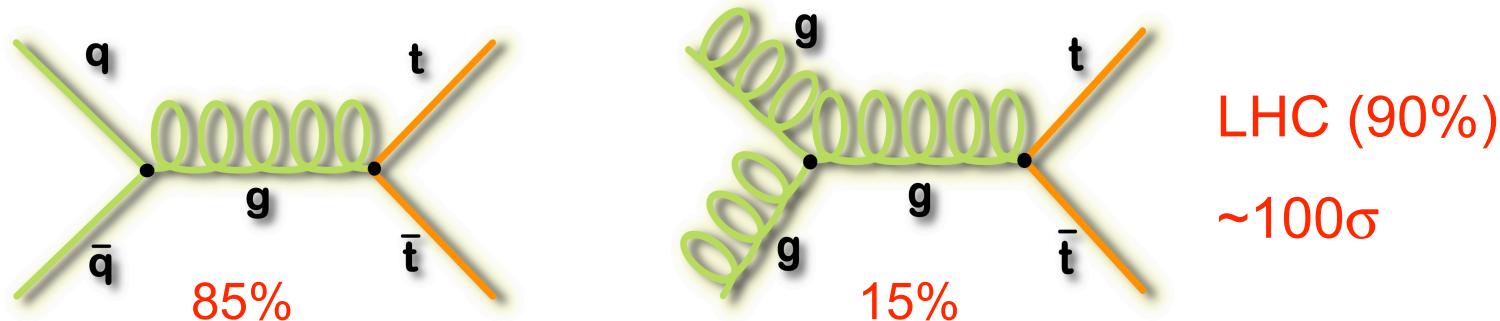
- Constrain new physics (SUSY) with M_{Higgs}

- Is it a SM top?



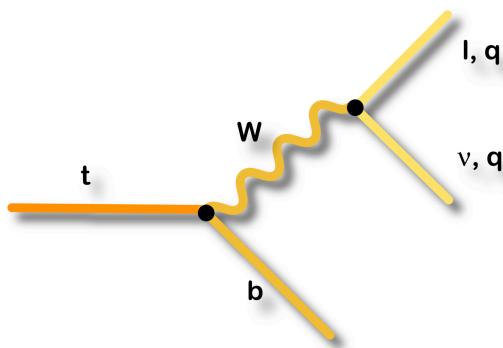
Top Production and Decay

- At the Tevatron, mainly primarily produced in pairs via strong interaction ($\sigma \sim 7\text{ pb}$: 1 for every 10^{10} collisions)

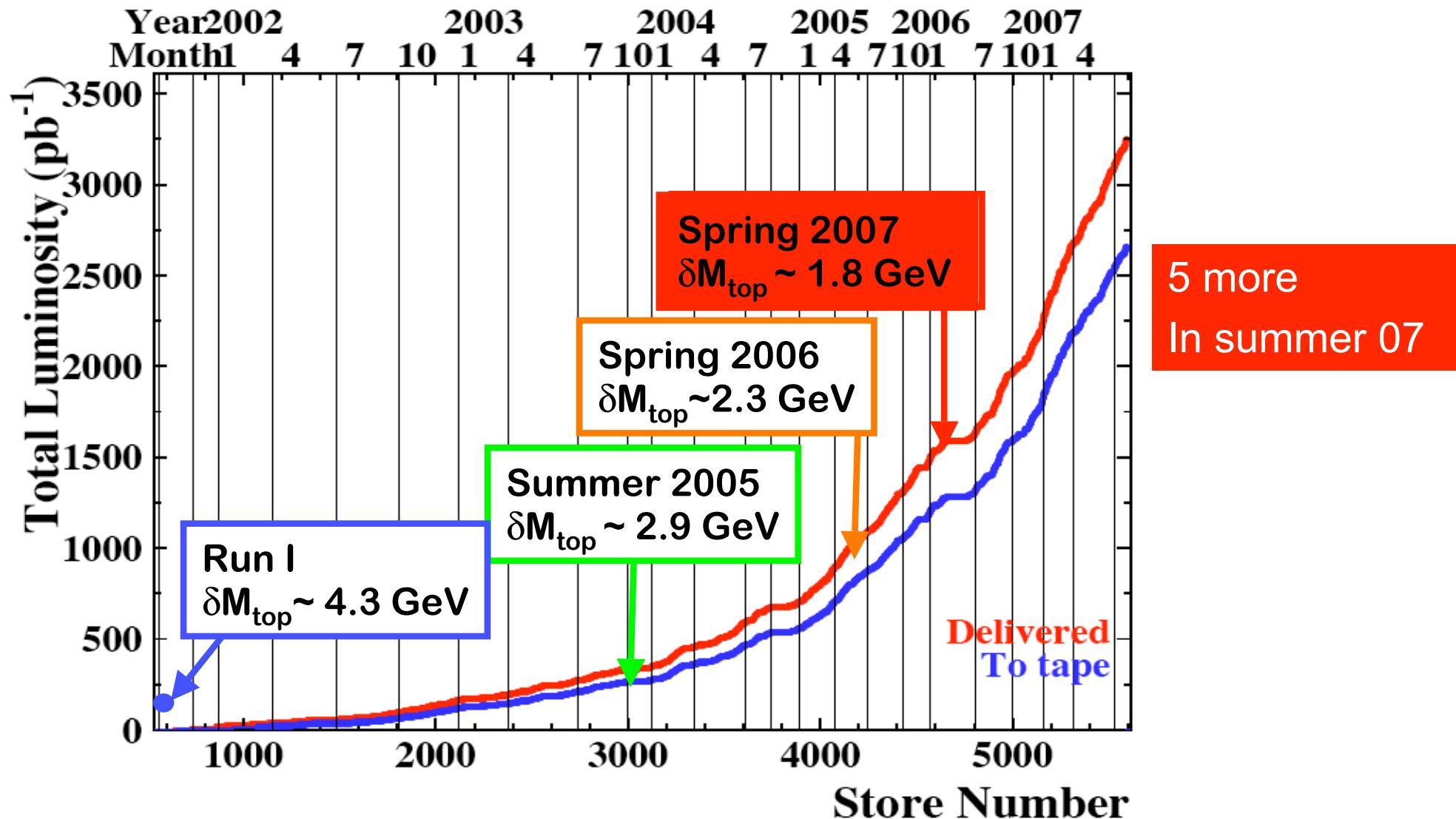


- Top decays as free quark due to large mass ($\tau_{\text{top}} \sim 4 \times 10^{-25} \text{ s}$)

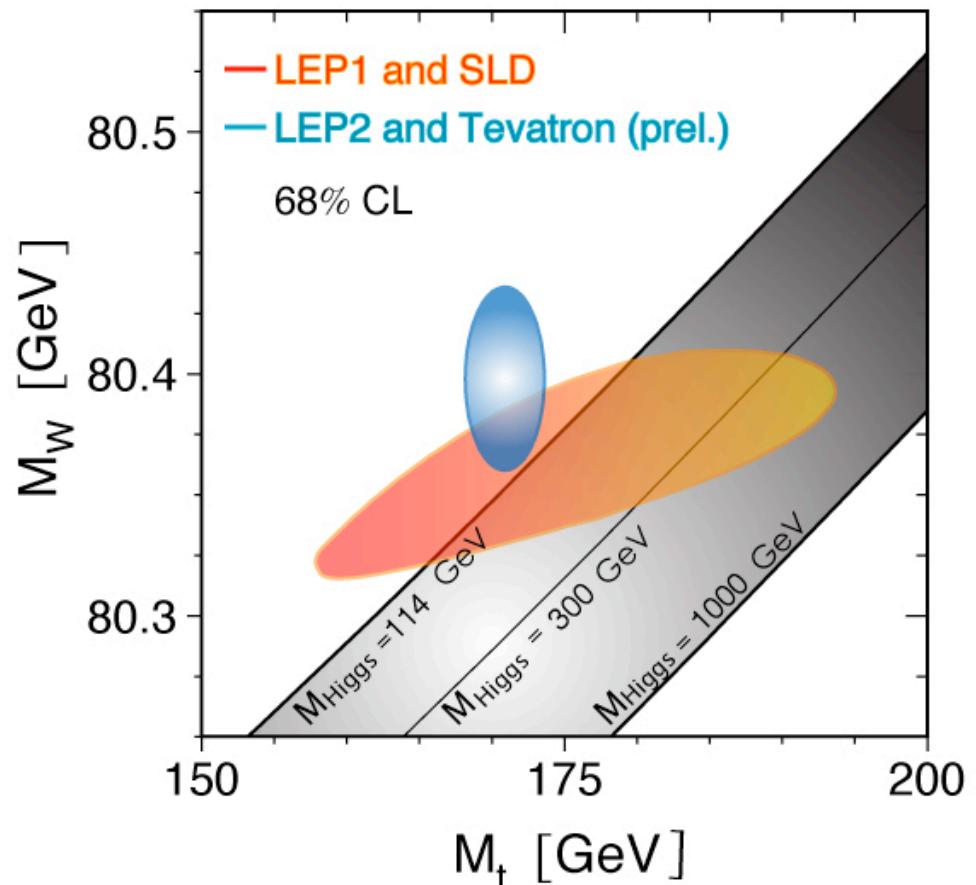
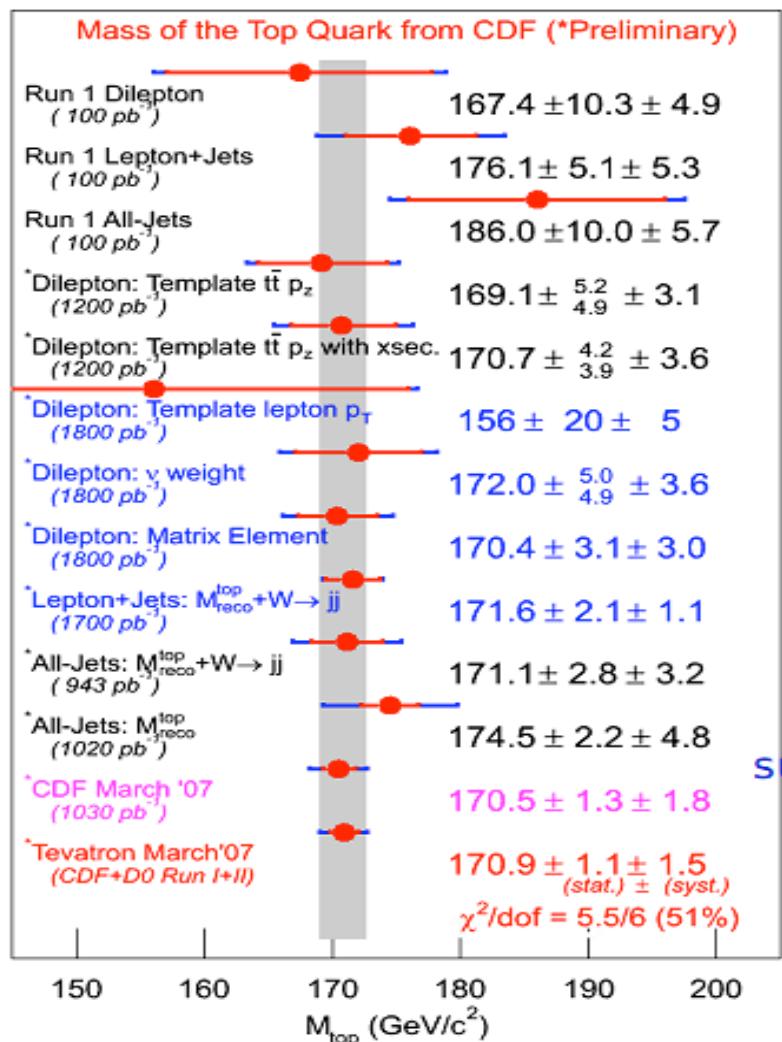
- Dilepton (5%, small bkgds)
2 leptons(e/μ), 2 b jets, missing E_T (2vs)
- Lepton+Jet (30%, manageable bkgds)
1 lepton(e/μ), 4 jets (2 b jets), missing E_T (1v)
- All-hadronic (44%, large bkgds)
6 jets (2 b jets)



Great Performance



Precision Measurements and Impact



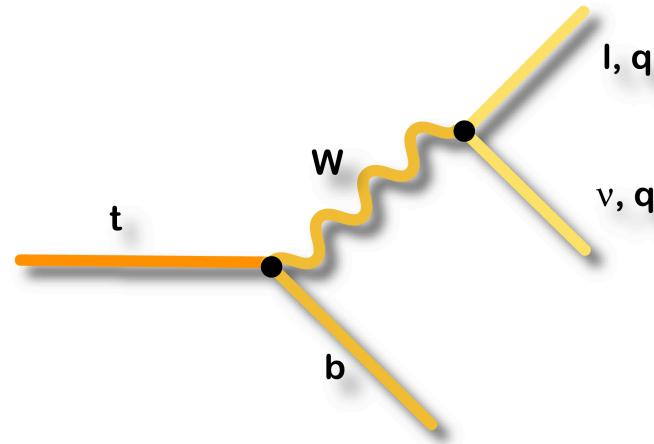
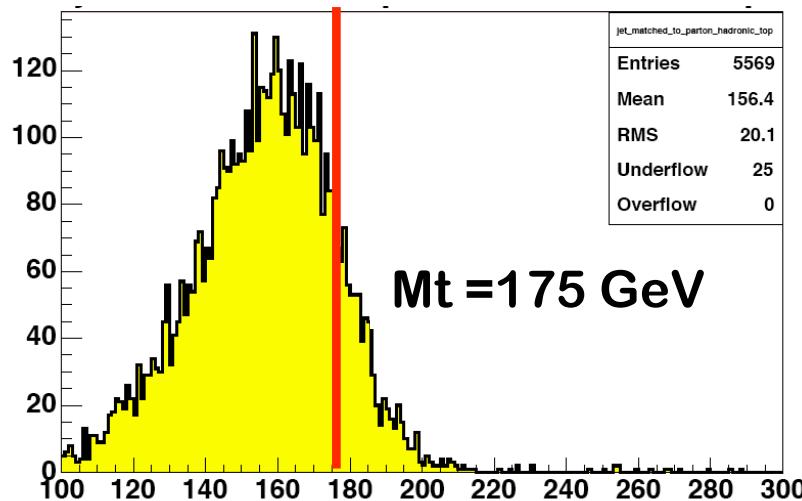
Different channels
with different methods!!!
New best single: 1.25%

$$M_H = 76^{+33}_{-24} \text{ GeV}/c^2$$

$$M_H < 144 \text{ GeV}/c^2 @ 95\% C.L$$

M_{top} Measurement : Challenge 1

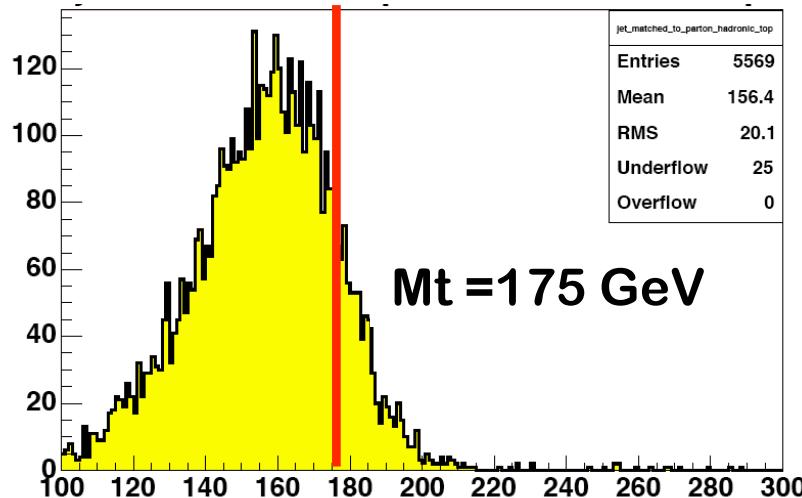
- Not a simple calculation of the invariant mass of $W(jj)$ and b



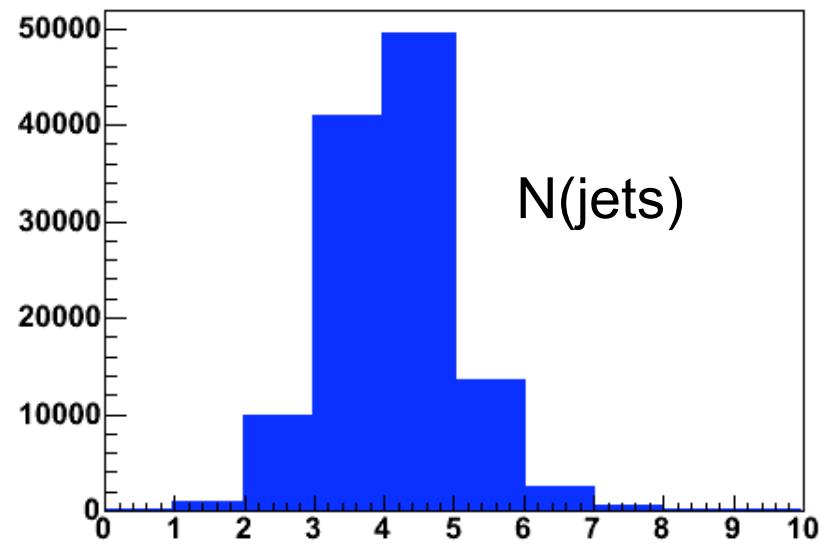
Why $M(bjj) \neq 175 \text{ GeV}$?

M_{top} Measurement : Challenge 1

- Not a simple calculation of the invariant mass of $W(jj)$ and $b!!!$



Why $M(bjj) \neq 175 \text{ GeV?}$

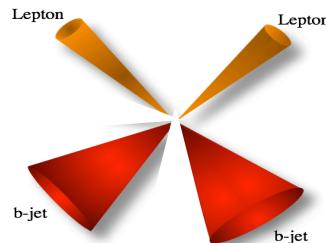


- Measured jet energy
≠ quark energy from top decay
 - Quarks: showering,
hadronization, jet clustering
 - Extra radiated jets

- Require excellent jet energy correction and good modeling of extra gluon radiations (40%)

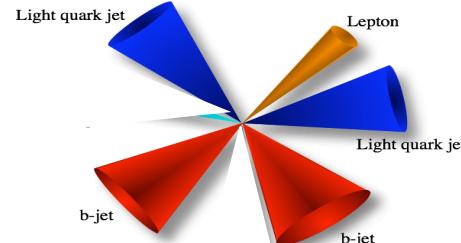
Challenge 2

- Too many combination to reconstruct two top quarks



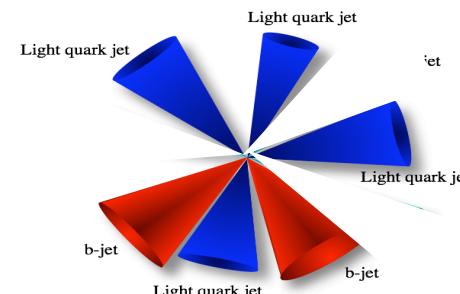
2(2)

2 v:unconstrained



12 (6)

1 v:over-constrained

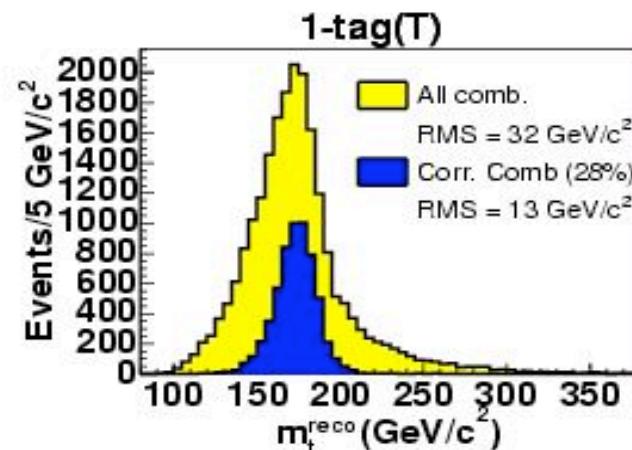
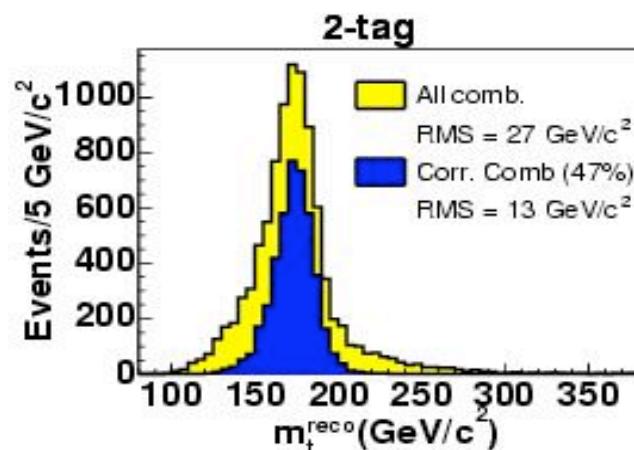


360(90)

No v:over-constrained

3 constraints:
two $M(w)=80.4$
one $M(t)=M(\bar{t})$

- B-tagging helps!: reduces wrong comb. and improves resolution



Top Mass Measurements

Template

- Reconstruct a per-event observable, $M_t(\text{reco})$, L_{xy} etc: sensitive to M_t
- Create “templates” using fully simulated events for different top mass values, and bkgds
- Maximum Likelihood fit using signal+backgrounds templates

Matrix Element

- Calculate probability dist. as M_t for all combinations in each event by Matrix Element calculation
 - maximize dynamic information
- Build Likelihood directly from the probabilities
- Calibrate measured mass and its error using fully simulated events

Strategy

- Precision & consistency
 - Different channels
 - Different methods (using different information)
- New Physics (bias)

Method	Njets		B-tag		JES			Rec. variables
	Exact	+extra	Yes	No	Wjj+std	Wjj	No	
LJ	TMP	4	>4					mt, m_{jj} , Lxy, Pt(e/ μ)
	ME	4						P(Mt,JES)
DIL	TMP	2	>2					mt, Pt(e/ μ)
	ME	2						P(Mt)
All-J	TMP+ME	6	>6					mt, m_{jj}

Completed(~15 analyses groups)

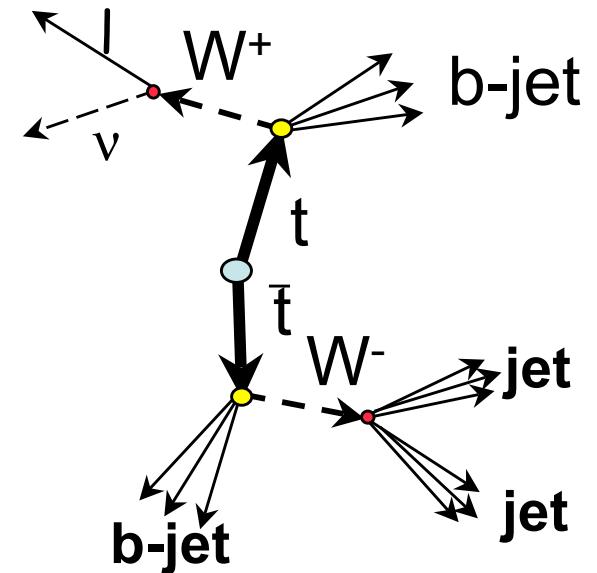
Template Method in Lepton+Jets

➤ Event selection

- High-pt central leptons (e, μ): $P_T > 20$ GeV
- 4 jets: $E_T > 20$ GeV, $|\eta| < 2.0$
- Large missing $E_T > 20$ GeV

➤ χ^2 kinematic fitter: fully reco. ttbar system

$$\begin{aligned}\chi^2 = & \sum_{i=1,4 \text{ jets}} \frac{(\hat{p}_T^i - p_T^i)^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(\hat{p}_T^{UE} - p_T^{UE})^2}{\sigma_j^2} \\ & + \frac{(m_{jj} - m_W)^2}{\Gamma_W^2} + \frac{(m_{lv} - m_W)^2}{\Gamma_W^2} + \frac{(m_{bjj} - m_t)^2}{\Gamma_t^2} + \frac{(m_{blv} - m_t)^2}{\Gamma_t^2}\end{aligned}$$

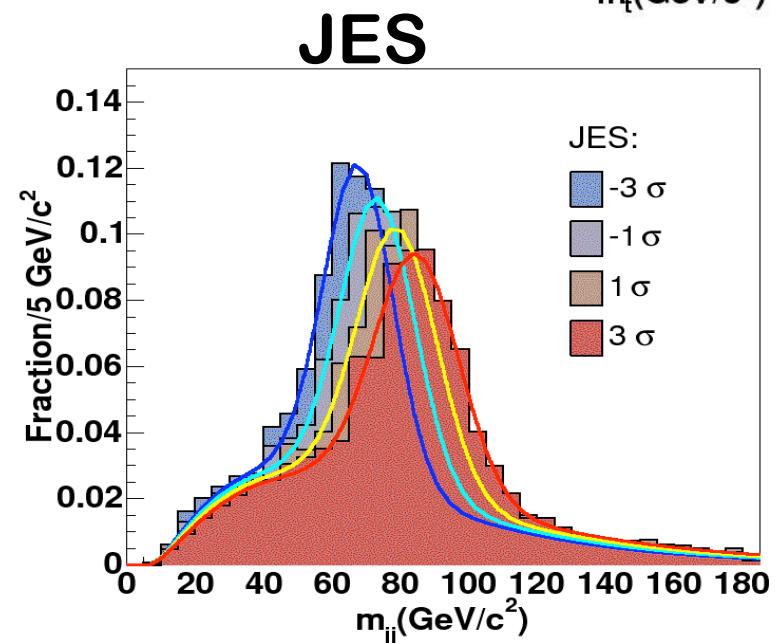
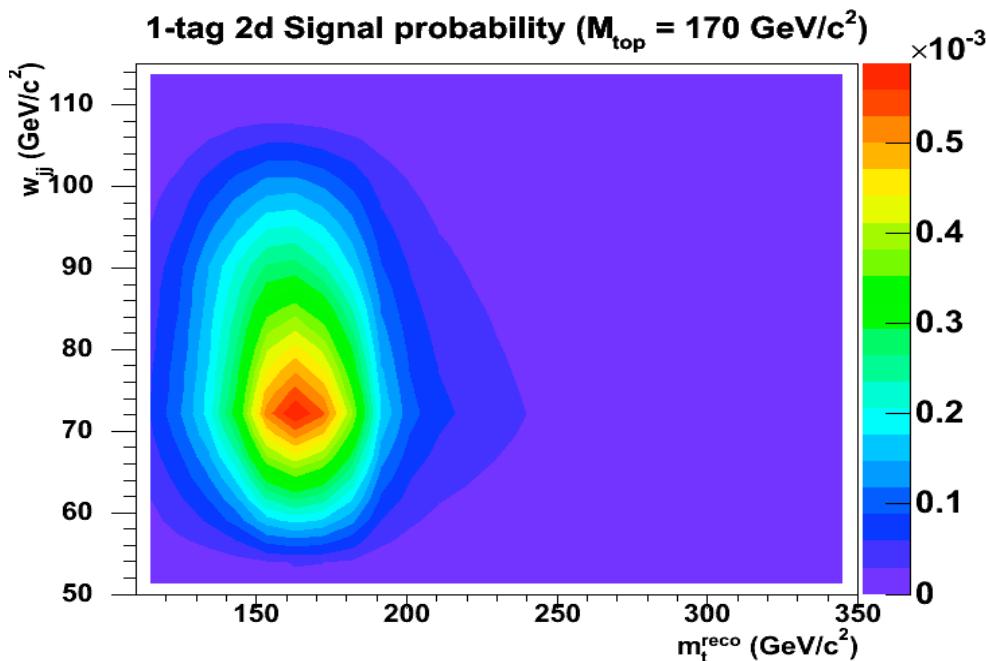
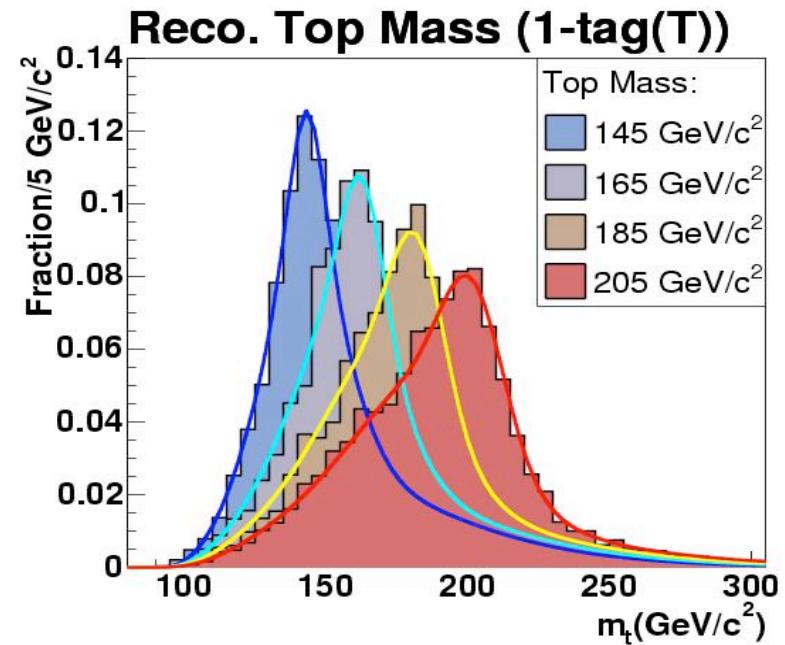
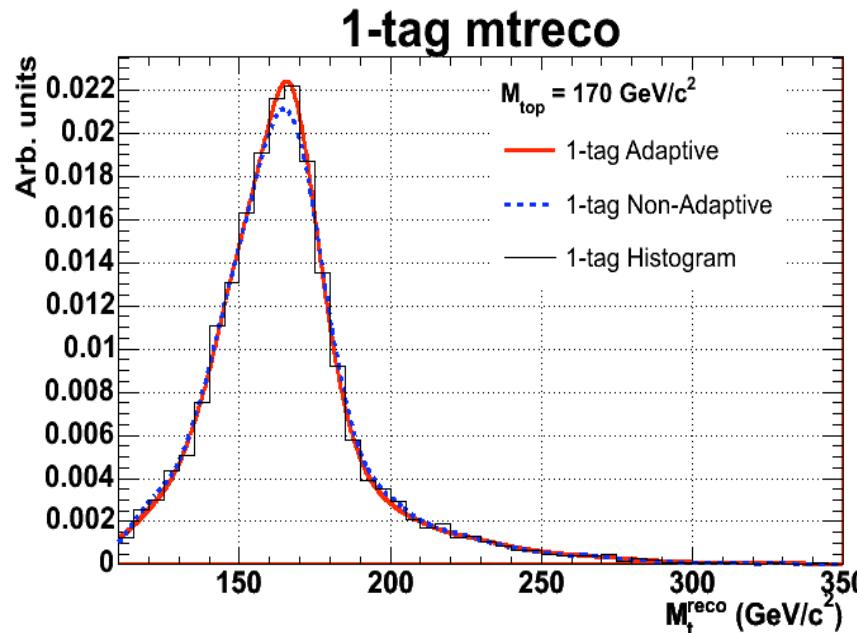


□ Find m_t that fits event best over all combinations

$(m_W = 80.4$ GeV, $m_t = m_{\bar{t}}$)

□ Reject badly reconstructed event

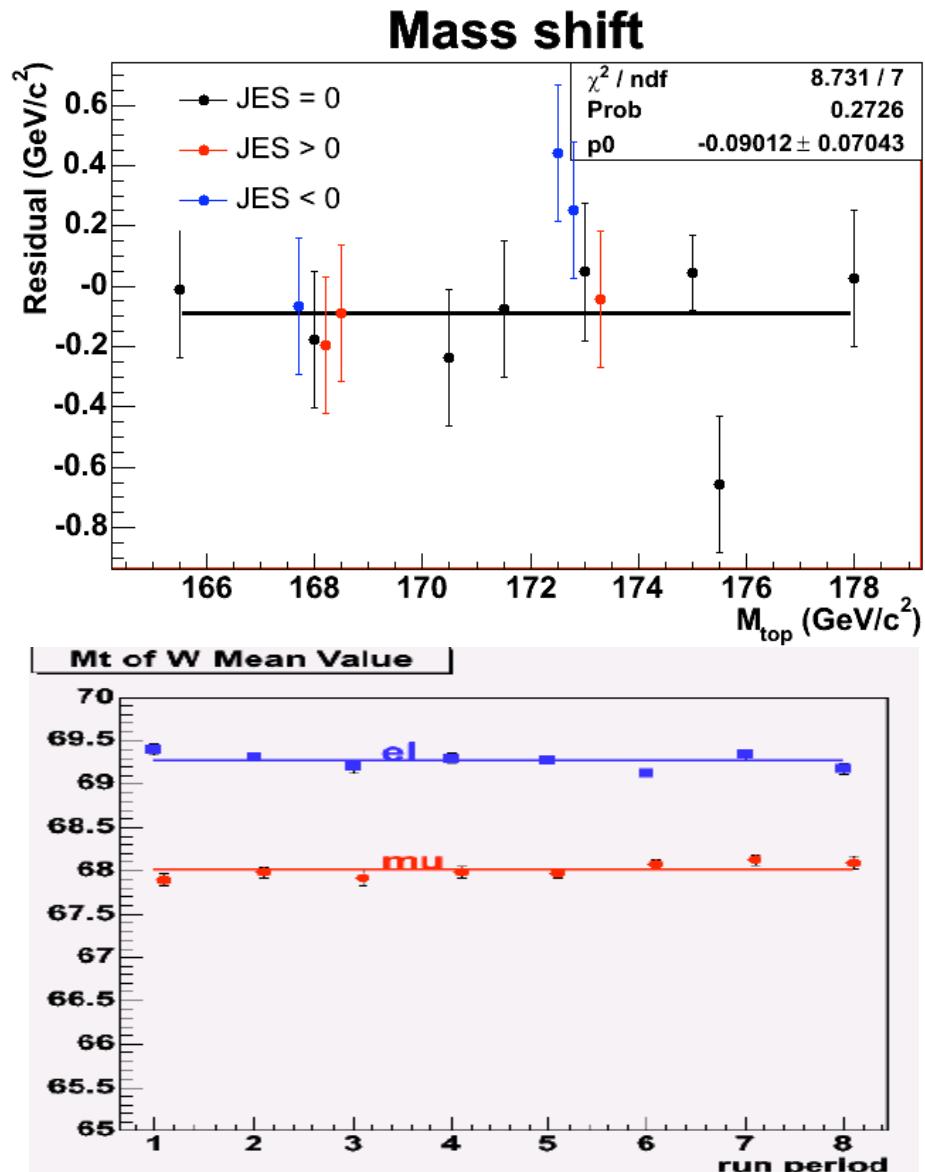
Signal Templates (m_t , JES)



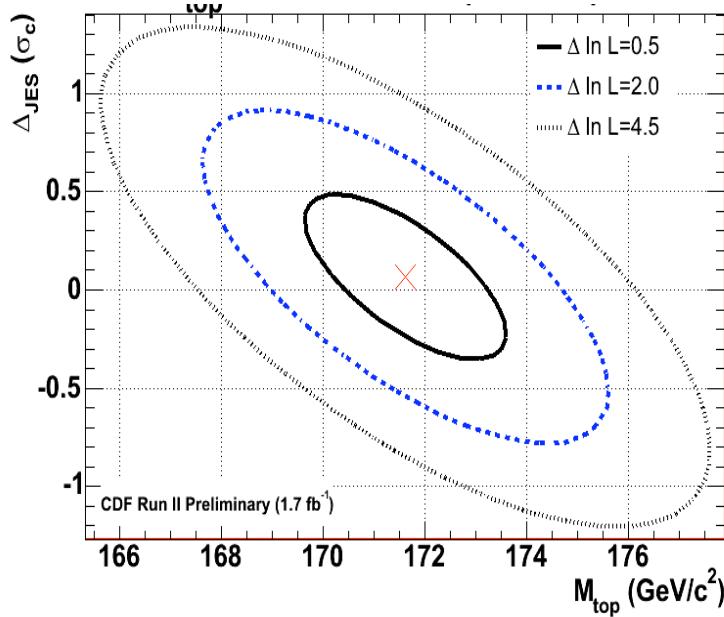
Check Check Check Before the Fit

- Pseudo-experiments
 - Bias in central value
 - Bias in error estimation
 - Test using blind Mt and JES MC sample

- Challenges
 - Acceptance
 - Shapes (mean, RMS for Mt sensitive variables)



Template Results in Lepton+Jets



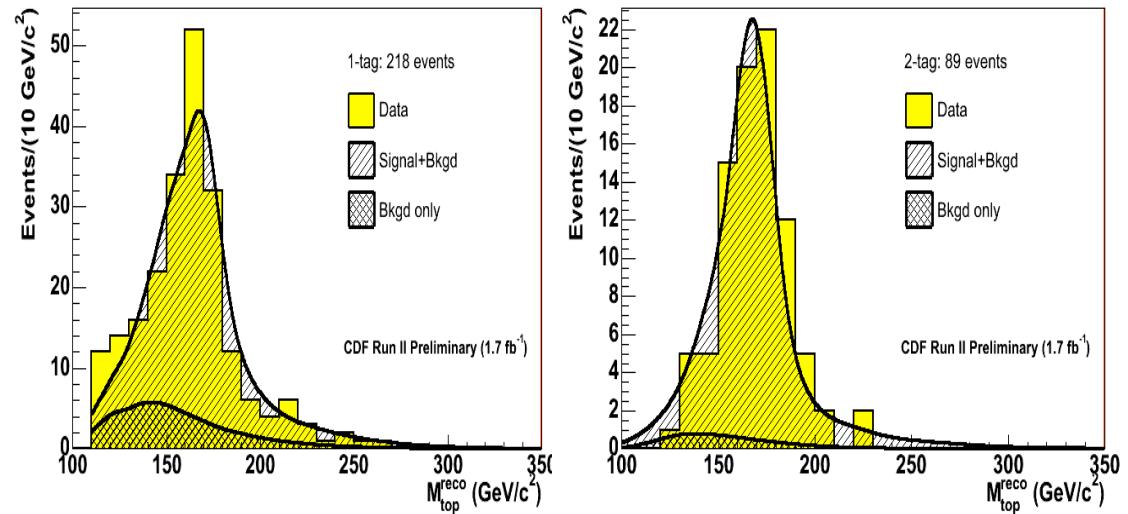
$$M_t = 171.6 \pm 2.1(\text{stat.} + \text{JES})$$

$$\pm 1.1(\text{syst.}) \text{ GeV} / c^2$$

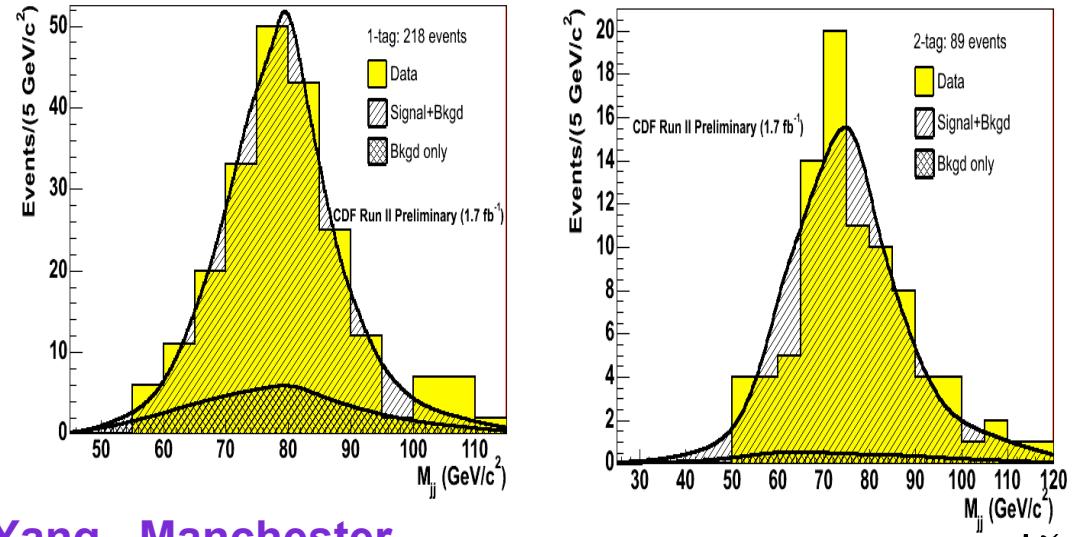
$$\text{JES} = -0.07 \pm 0.42\sigma$$

➤ more than a factor
of two improvement
on JES with 1.7 fb^{-1}

mt (1-tag, 2-tag)



mjj (1-tag, 2-tag)

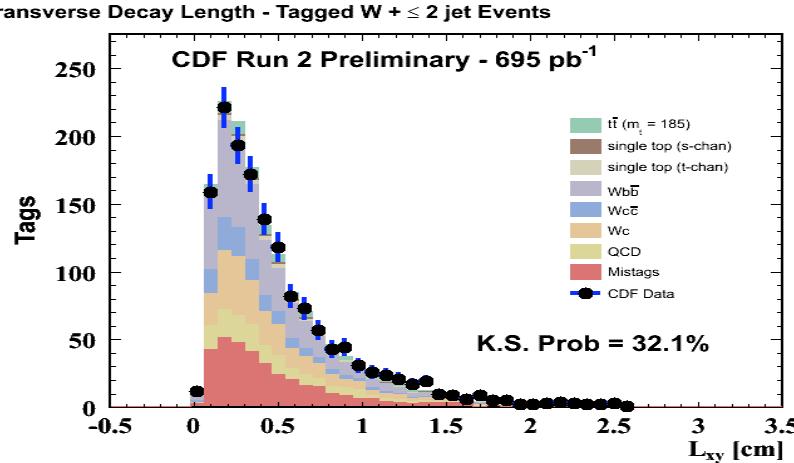
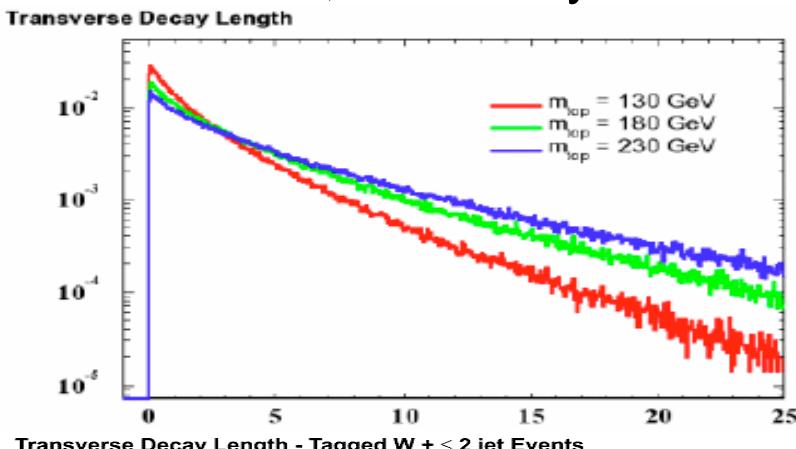


Un-ki Yang, Manchester

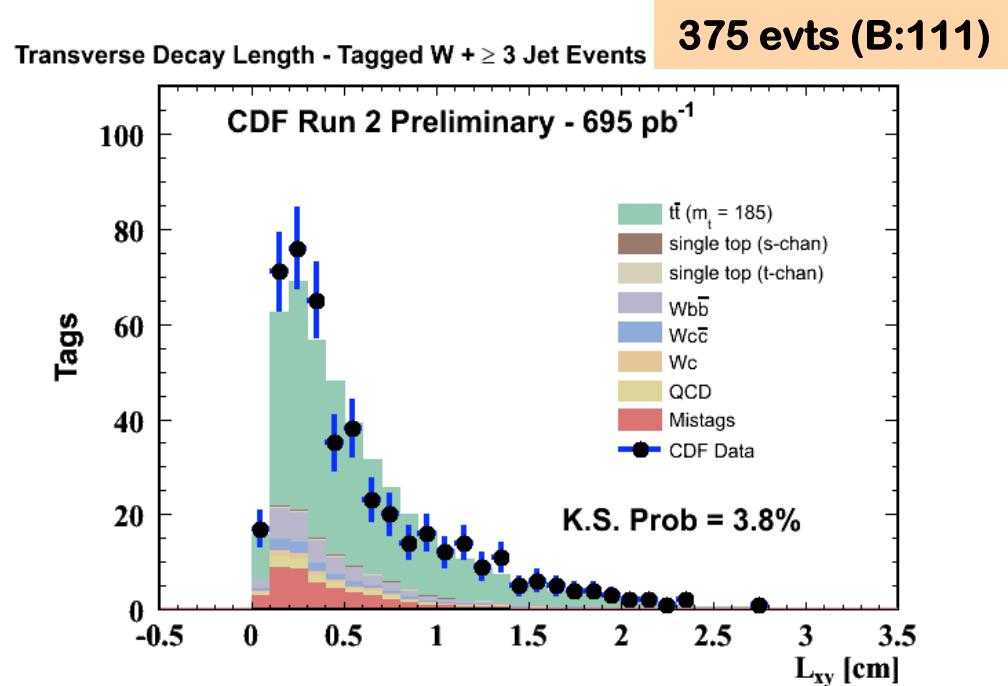
Template using Decay Length (L_{xy})

- Uses the average transverse decay length, L_{xy} of the b-hadrons
- B hadron decay length \propto b-jet boost $\propto M_{top}$ ($>=3$ jets)

PRD 71, 054029 by C. Hill *et al.*



Insensitive to JES,
but need L_{xy} simulation



$$M_{top} = 183.9^{+15.7}_{-13.9} \text{ (stat)} \pm 0.3 \text{ (JES)} \pm 5.6 \text{ (syst)} \text{ GeV}/c^2$$

Statistics limited, but it can make
big contributions at LHC

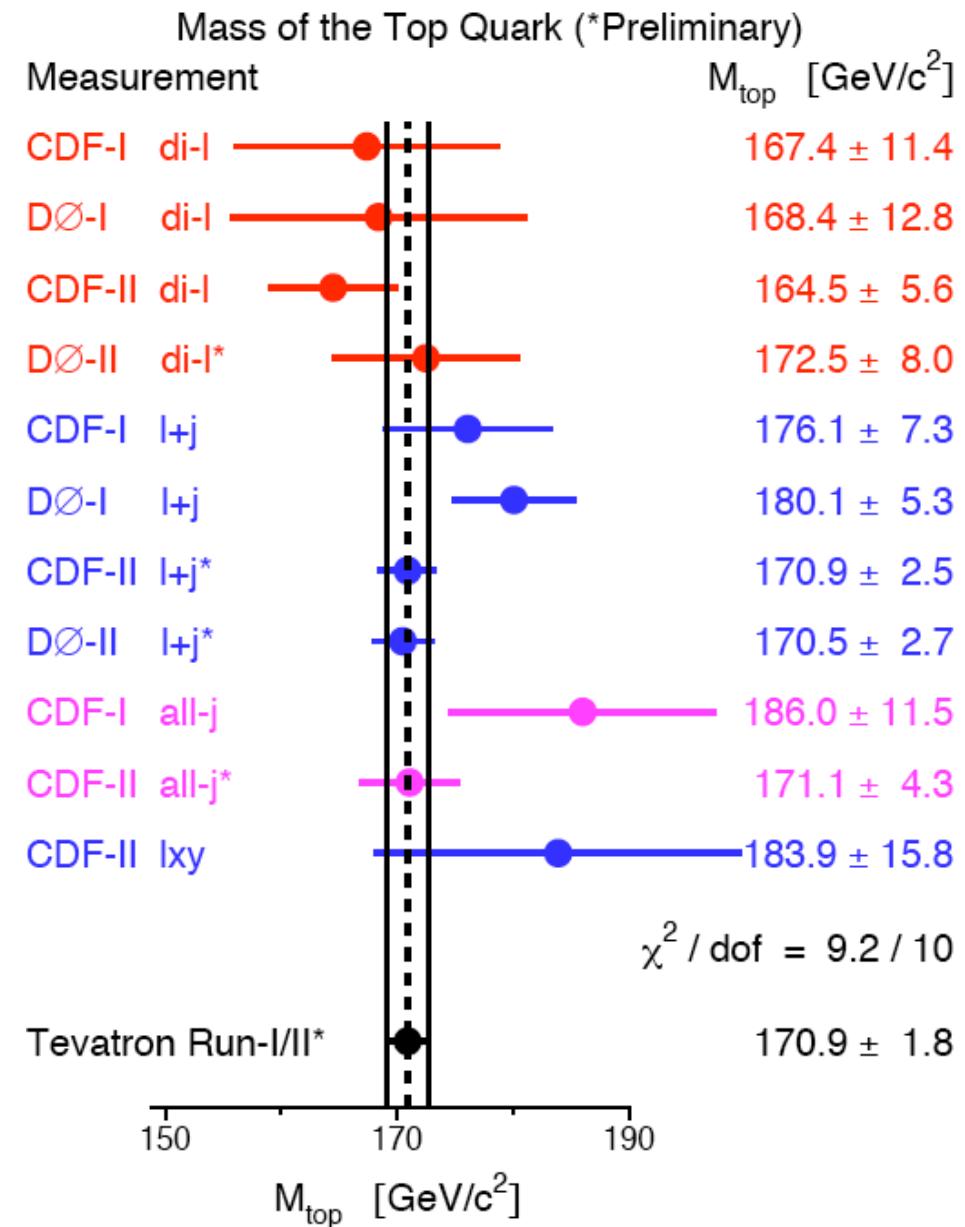
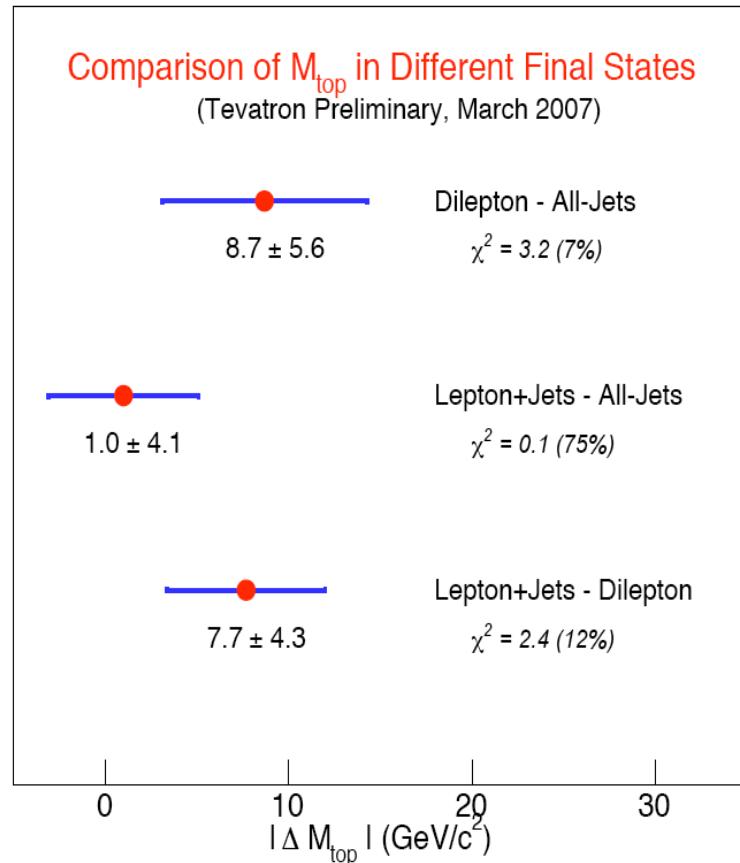
Comparisons in Lepton+Jets (1.7fb^{-1})

Measurement	Template	ME	$\text{L}_{xy} (0.7\text{fb}^{-1})$
JES	(1.5)	(1.2)	0.3
Residual	0.7	0.5	
B-jet JES	0.6	0.4	
ISR/FSR	0.4 0.5	0.5	1.3
Bkgd shapes/ normalization	0.3 0.5	0.6	3.3
Generators	0.3	0.4	0.7
PDFs	0.2 0.3	0.3	Data/MC $\langle \text{L}_{xy} \rangle$ SF 4.2
Methods	0.1 0.3	0.1	
Total	1.1 1.3	1.2	5.6

Red: 0.7fb^{-1} including no b-tag
 Parameterization <- KDE

Combining M_{top} Results

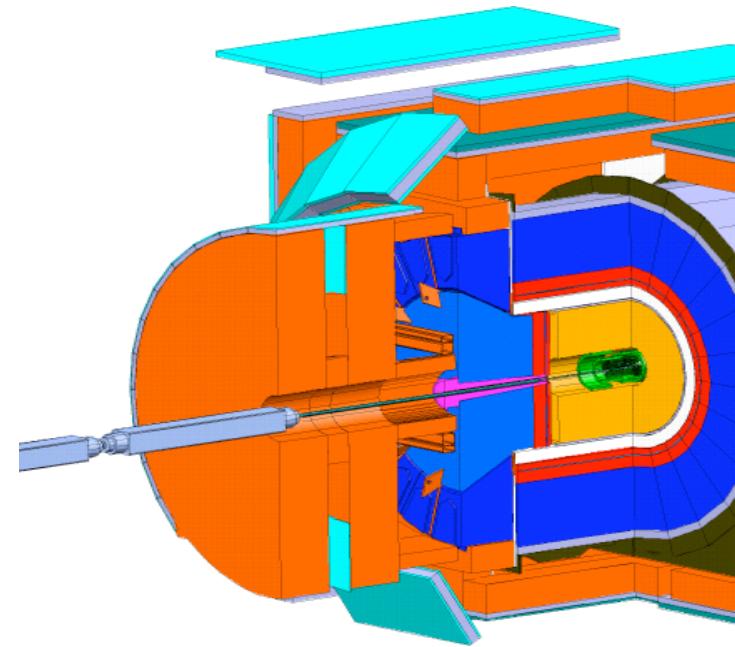
➤ Are all channels consistent ?



$$M_{\text{top}} = 170.9 \pm 1.8 \text{ GeV}/c^2 \quad (1.1\%)$$

Jet Energy Scale at CDF

- Top: cone algorithm (0.4),
QCD: Midpoint and Kt algorithms
- Standard calibration (~3%)
 - Use dijet samples & tuned MC
 - Systematic: difference between MC and data, uncertainty from the method
- Wjj in-situ calibration (~1.3% @ 1.7 fb⁻¹)
 - Light quark JES: consistent with Std calibration
 - Apply to b-JES
 - Rely on MC about JES & b-JES difference
- Z(bbbar) (~2% @ 0.6 fb⁻¹)
 - Special SVT trigger sample
 - Consistent with Std calibration
 - Had not applied to top mass yet.



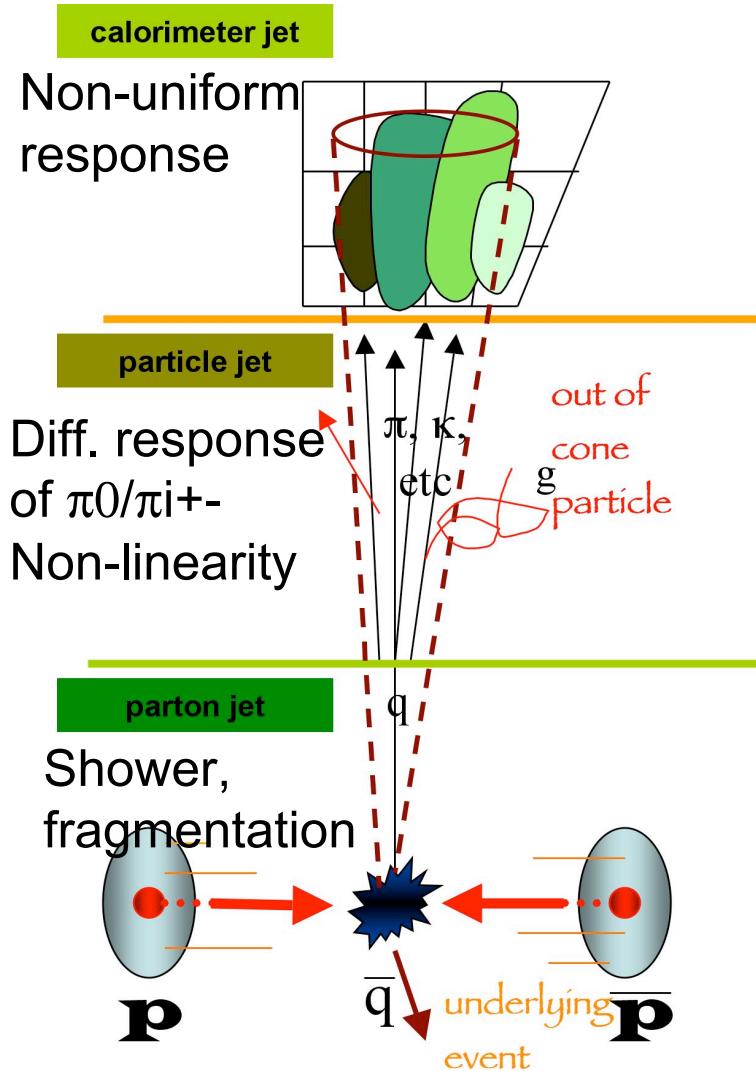
Scintillating tile non-compensating calorimeter with lead/iron absorbers

Electrons: $\sigma_E / E = 13.5\% / \sqrt{E}$ (central)

$\sigma_E / E = 16\% / \sqrt{E}$ (plug)

Jets: $\sigma_E / E \sim 80\% / \sqrt{E}$

Jet Energy Correction



Relative using dijet balance: to make response uniform in η

Multiple ppbar interactions: pileup

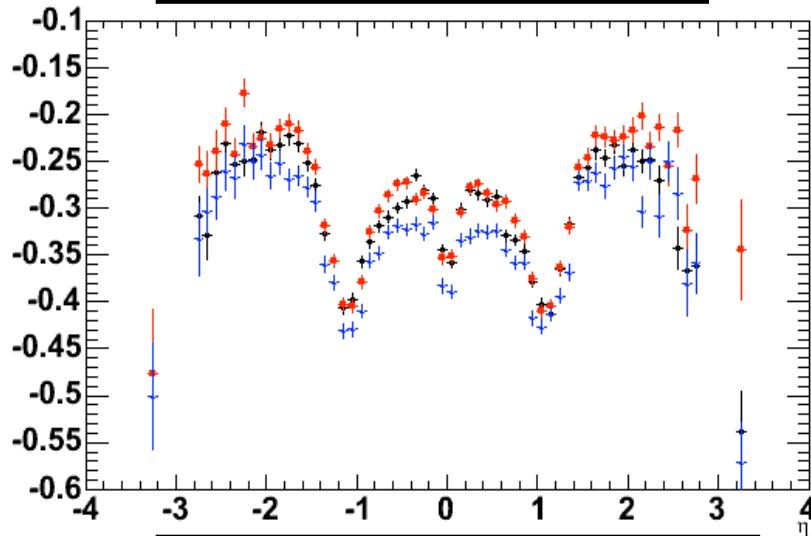
Absolute correction using dijet MC tuned for single particle E/P, material, and fragmentations: due to non-linear and non-compensating calorimeter

Underlying events due to spectators

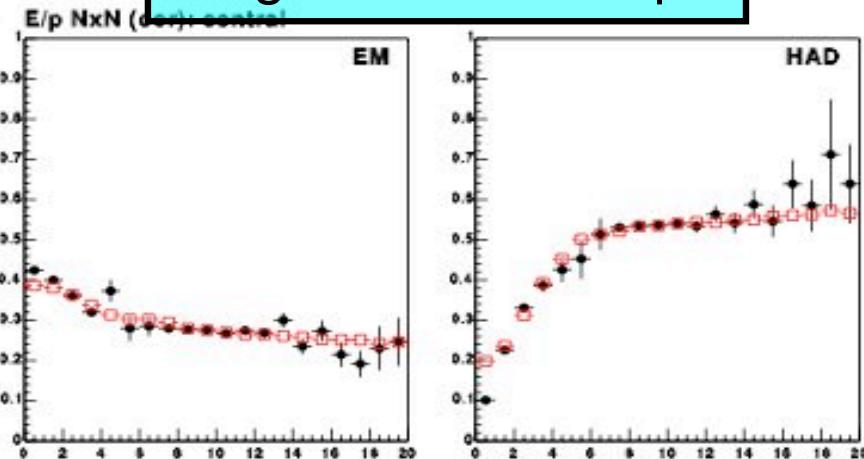
Out-of-Cone : due to energy outside cone

Jet Corrections

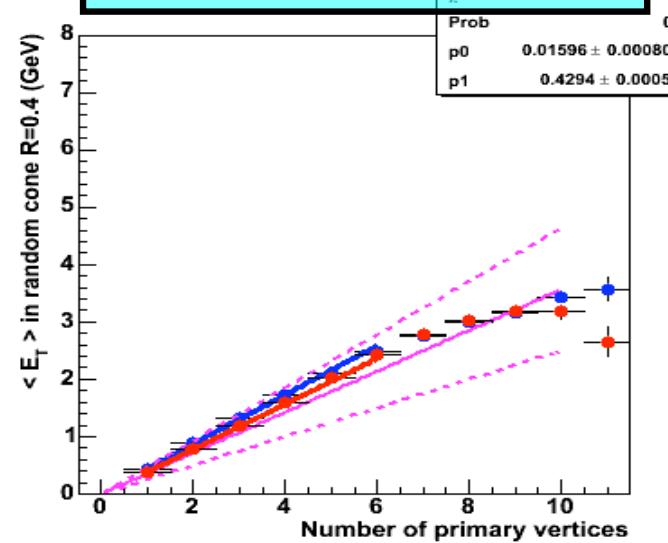
Relative Correction



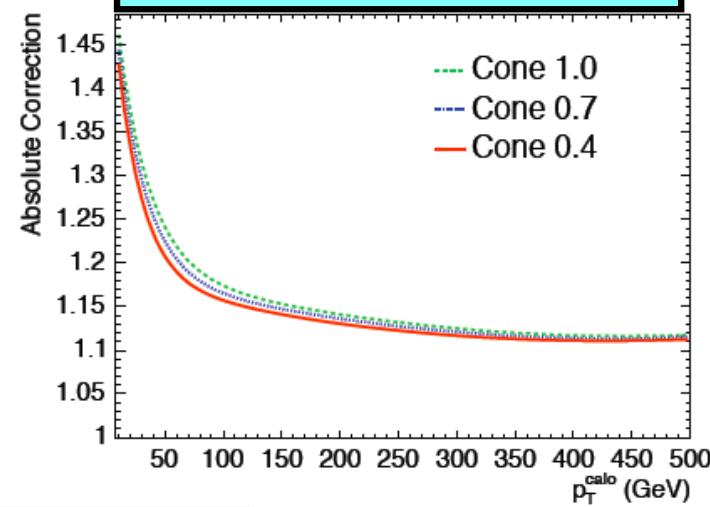
Single Particle Resp.



Multiple Interactions

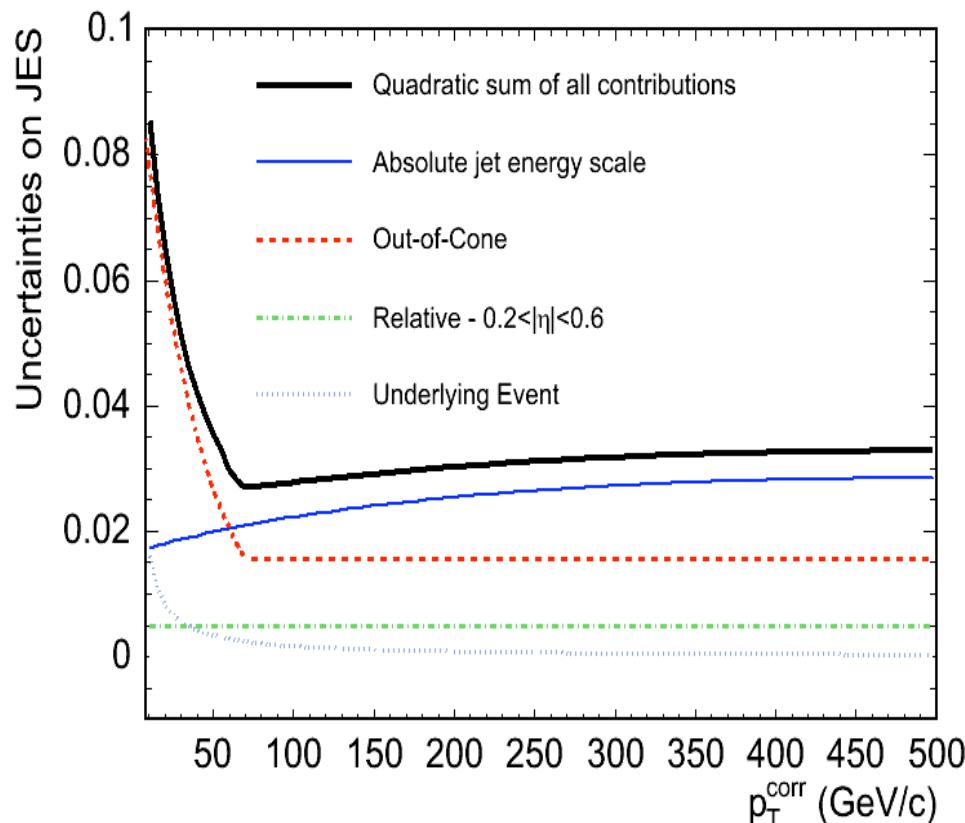


Absolute Correction



JES Uncertainty

Standard calib.



About 3 GeV of M_{top}

Systematic Checks

➤ γ -Jet:

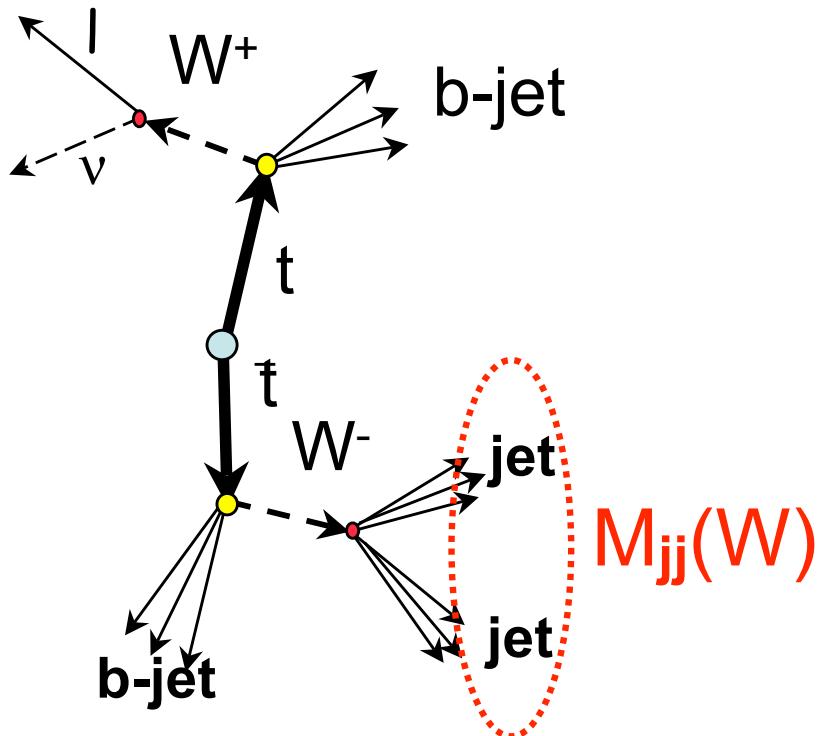
- highest statistics 😊
- systematically limited (kt-kick, BG contributions: π^0) ☹
- Not available for $E_T < 25$ GeV (trigger) ☹

• Z-Jet:

- Usable at lower E_T values than γ -Jet 😊
- lower statistics than γ -Jet at high E_T ☹

In-Situ Wjj JES Calibration

In-situ calibration: $W \rightarrow jj$ resonance



JES uncertainty:
mostly statistical,
scaled with lum

➤ But 70% of δ JES in top mass
comes from b-jet. How can you
apply JES to b-jet?

JES	ΔM_{top}	B-JES	ΔM_{top}
Relative	0.6	B frag.	0.4
Absolute	2.2	Color flow	0.3
OOC	2.1	$Br(b \rightarrow l\nu X)$	0.4
Total	3.1	Total	0.6

Ans) b-jet specific uncertainty
is small

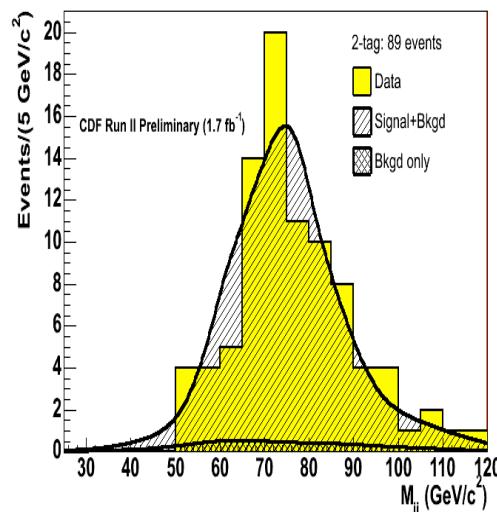
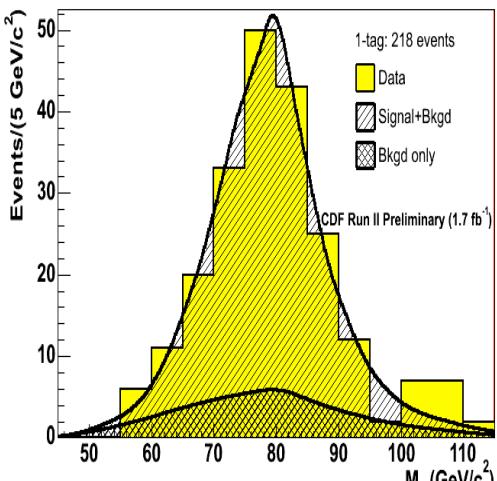
B-JES

- 2-D simultaneous fit to Mt and JES

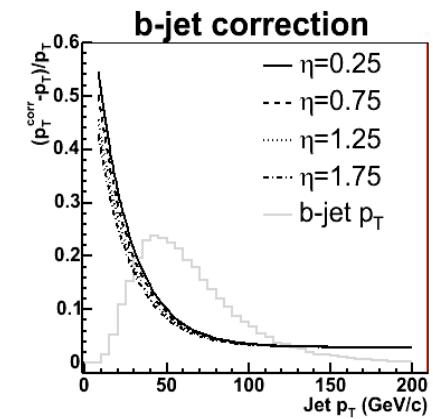
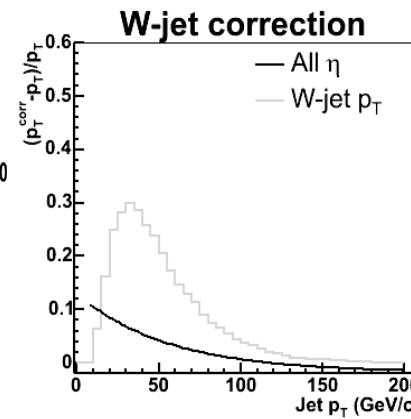
$$\text{JES} = -0.07 \pm 0.42\sigma$$

- Additional correction to correct b-jet back to b-quark level

- Additional B-jet specific uncertainty based on the constraints from other experiments using MC

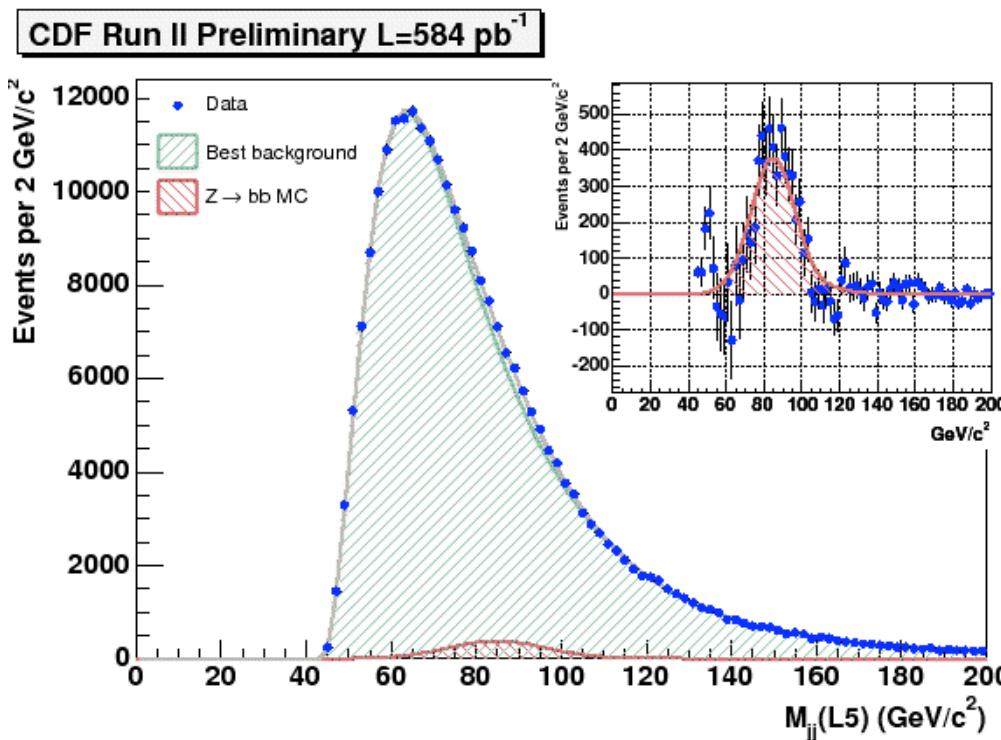


mjj (1-tag, 2-tag): 1.7fb^{-1} ~300 evts
 ~1.3% precision on JES



b-JES using Z(bb)

- Di b-jets with $E_t > 22 \text{ GeV}$, $\Delta\Phi > 3.0$, $E_t^{(3\text{rd})} < 15 \text{ GeV}$
using SVT impact parameter trigger at L2
- To measure data/MC b-JES

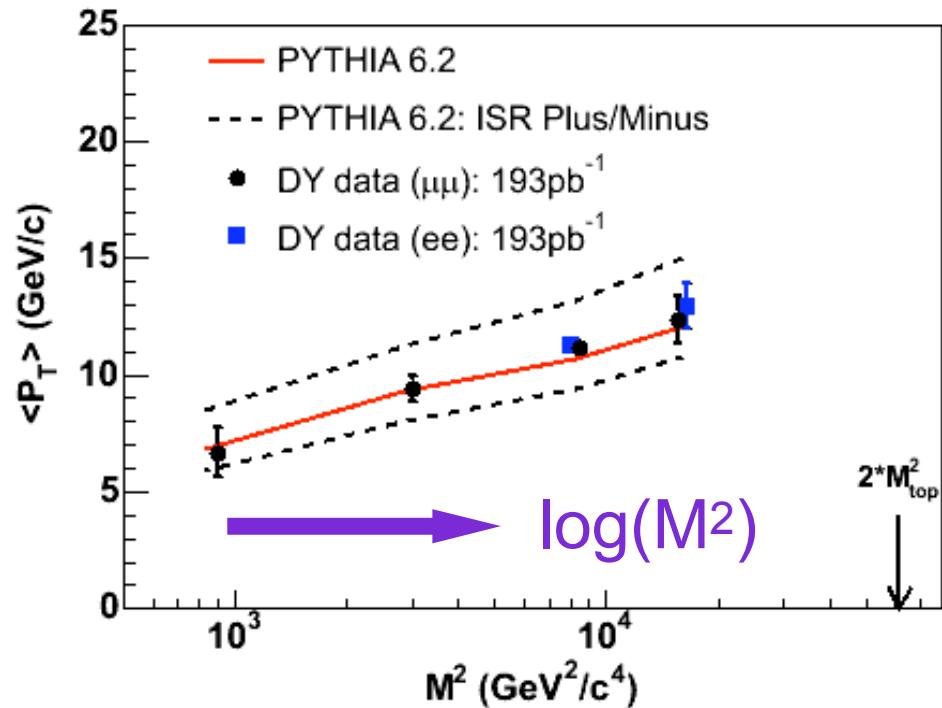
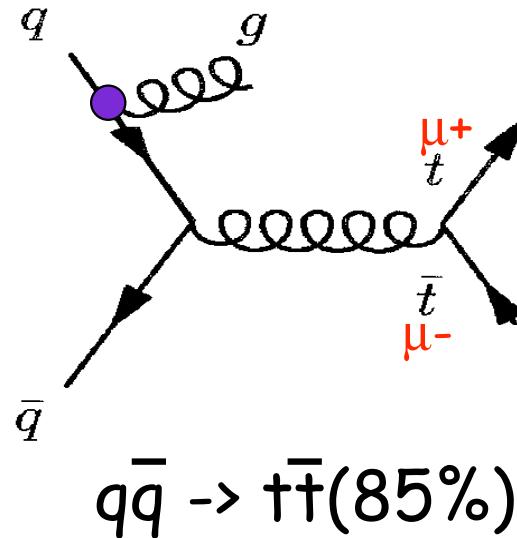


- Has not applied to b-JES in top mass
 - different cone size
 - different pt spectrum

$$\text{b-JES} = 0.974 \pm 0.011(\text{stat}) + ^{+0.017}_{-0.014} (\text{syst})$$

ISR/FSR in $t\bar{t}$ system?

- ISR is governed by DGLAP eq.: Q^2 , Λ_{QCD} , splitting functions, PDFs
- Use DY data for ISR (no FSR): study P_T of the dilepton as $M^2(\text{II})$



A good logarithmic Q^2 ($\sim M^2$) dependence was observed

ISR/FSR Syst.

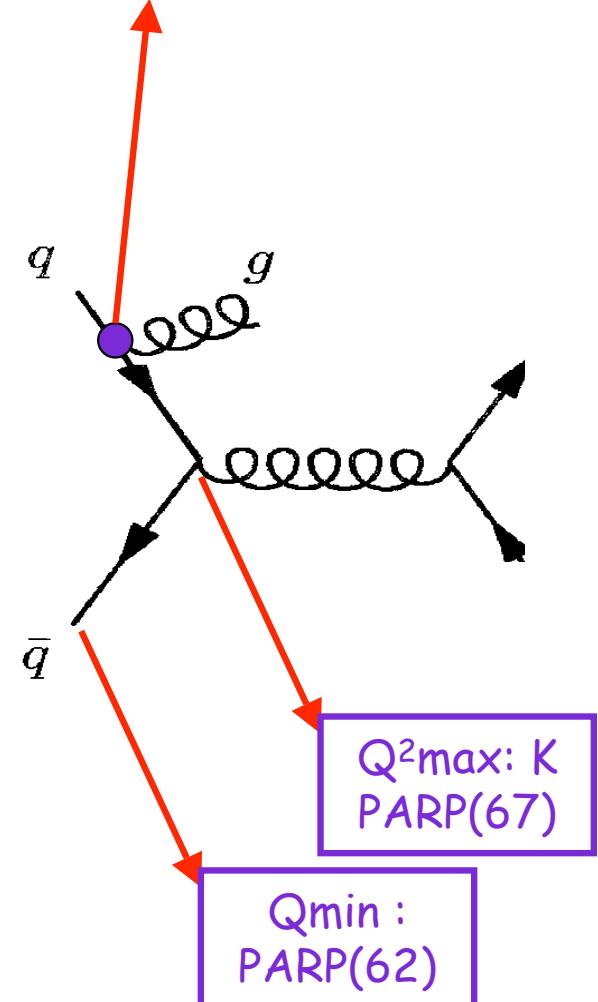
$$Kt^2 = \text{PARP}(64)(1-z)Q^2 : \alpha_s, \text{PDF}$$

$$\Lambda_{\text{QCD}} = \text{PARP} (61) : \alpha_s$$

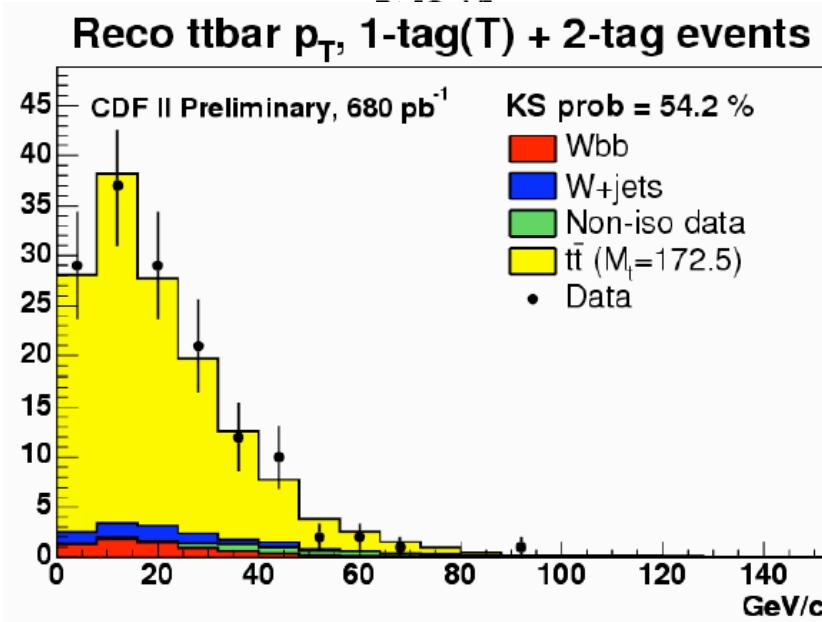
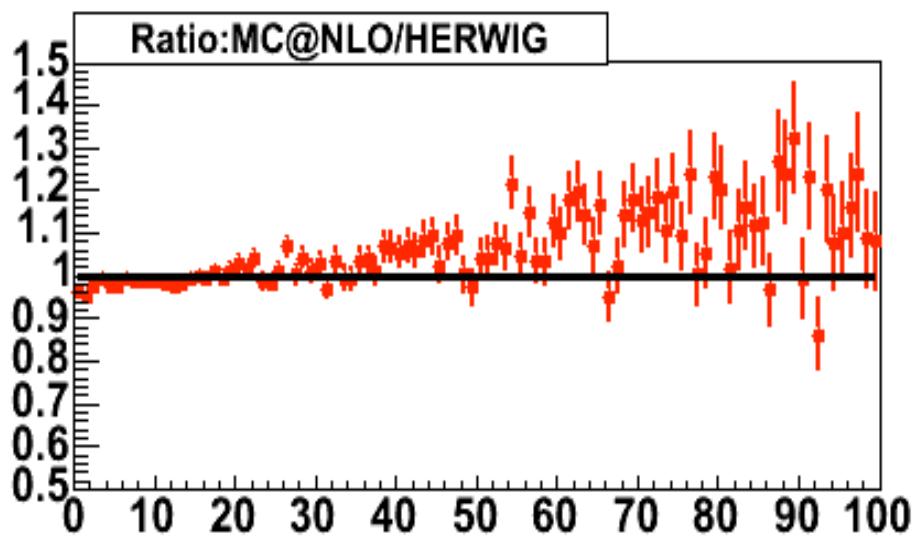
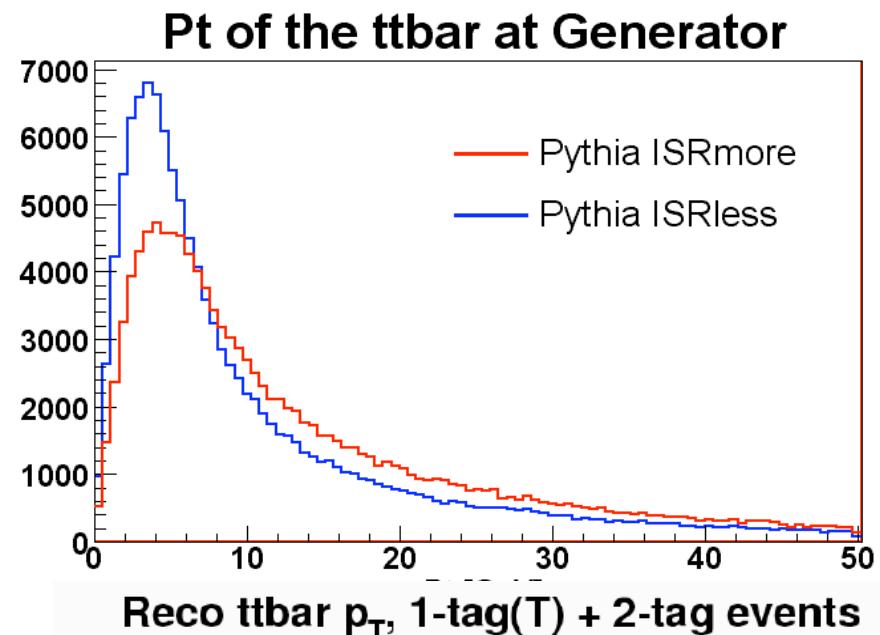
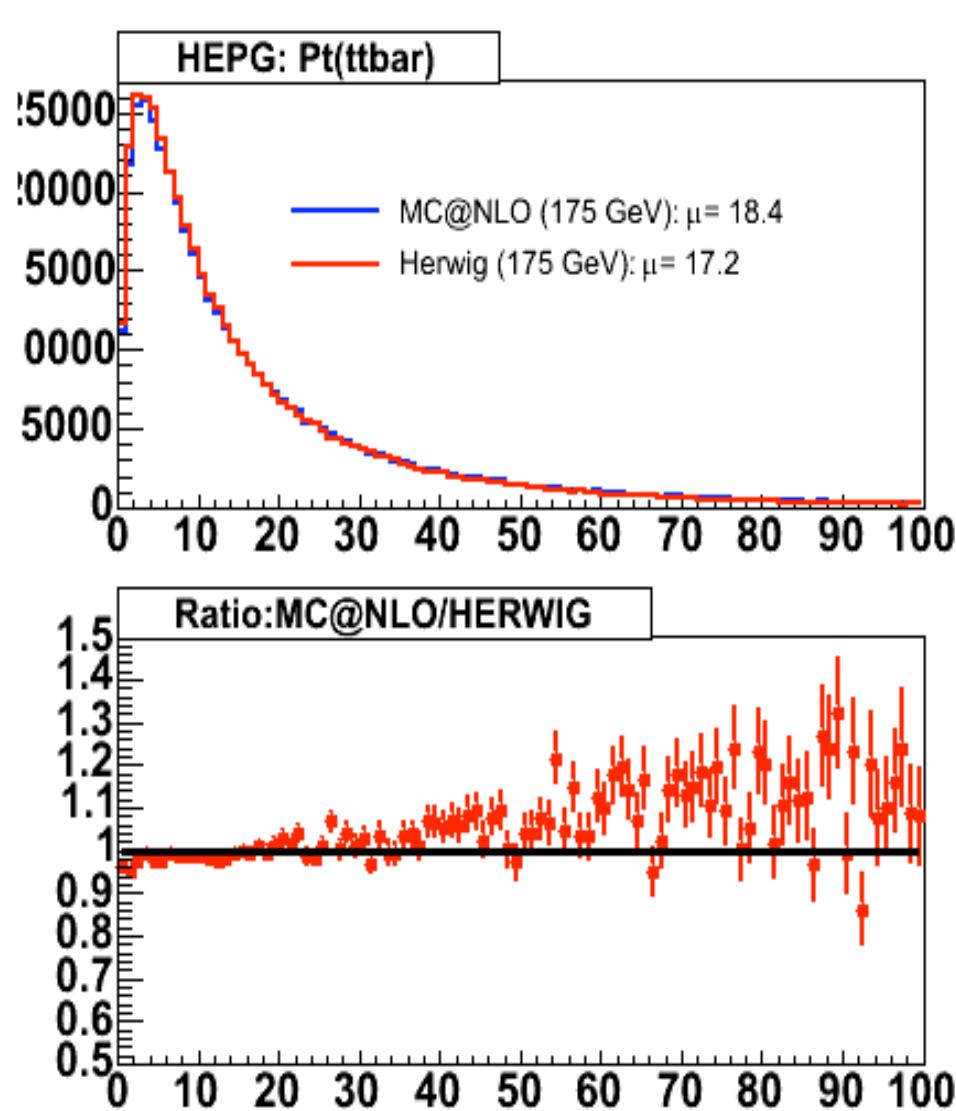
Pythia 6.2	ISR more	ISR less
PARP(61) (D=0.146)	0.292 (5 flavor)	0.073
PARP(64) (D=1.0)	0.25	4.0

Pythia	FSR more	FSR less
PARP(72)	0.292	0.073
PARP(71) (D=4)	8.0	2.0

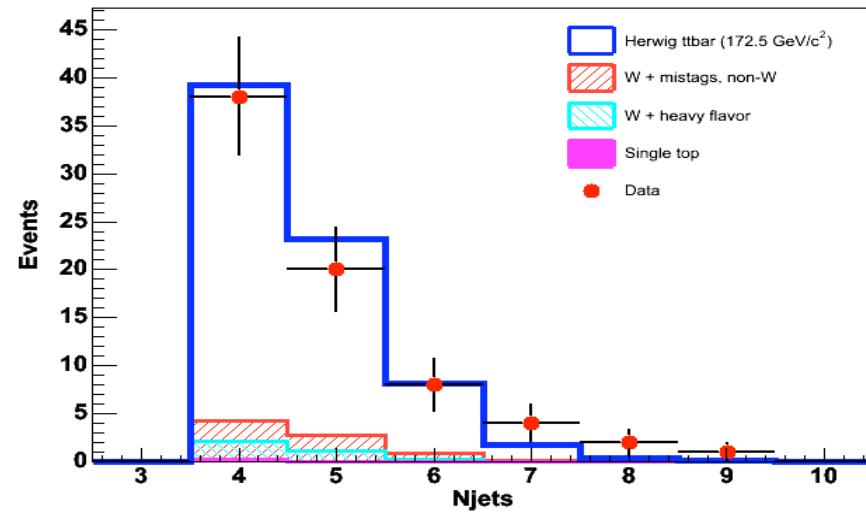
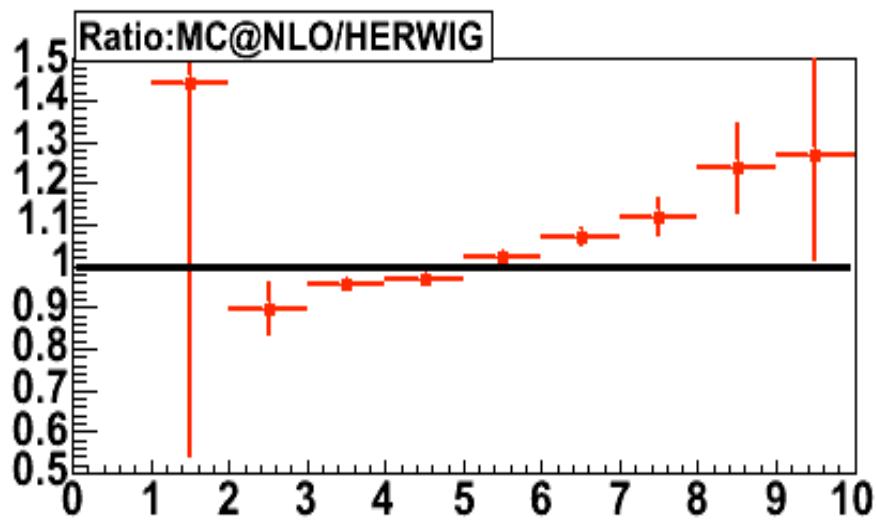
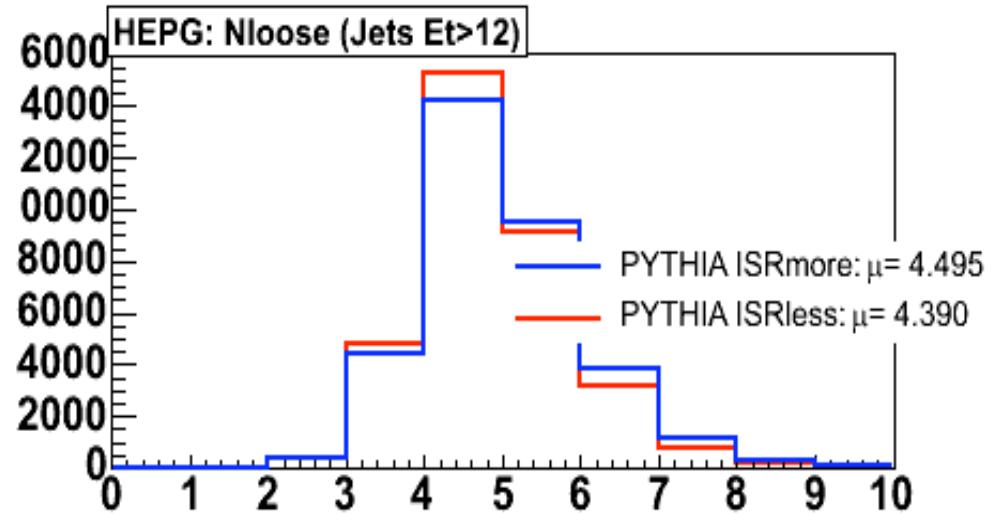
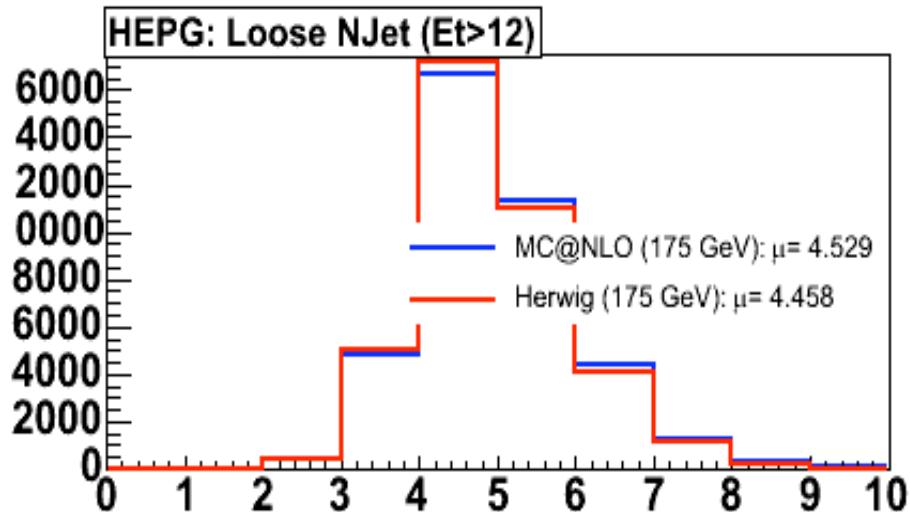
Physics process independent



Pt of $t\bar{t}$: ISR syst. vs NLO



Njets : ISR syst. vs NLO

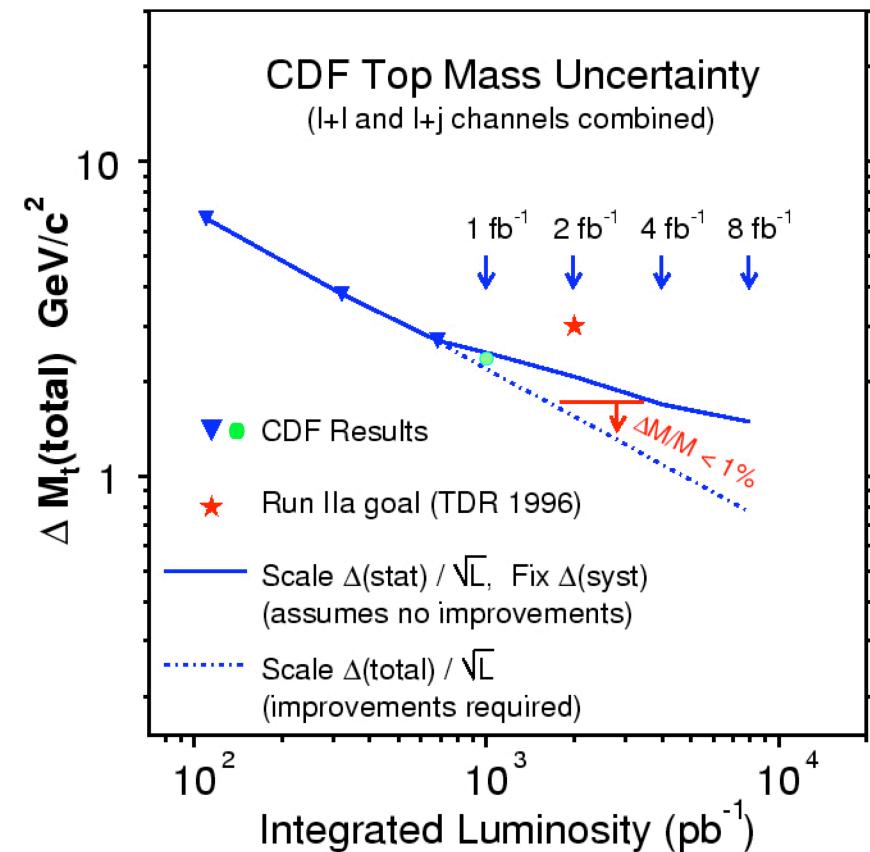


➤ ISR less/more absorbs a NLO effect

Njets for 1-tag+2-tag:
 $E_T > 8$ GeV

Summary and Lessons

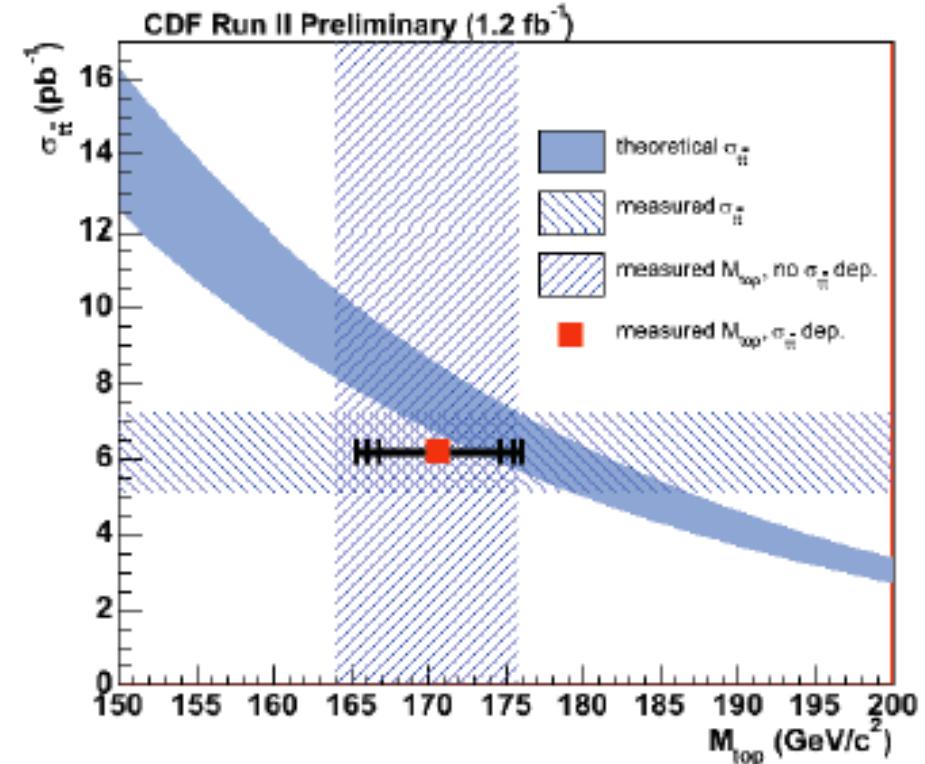
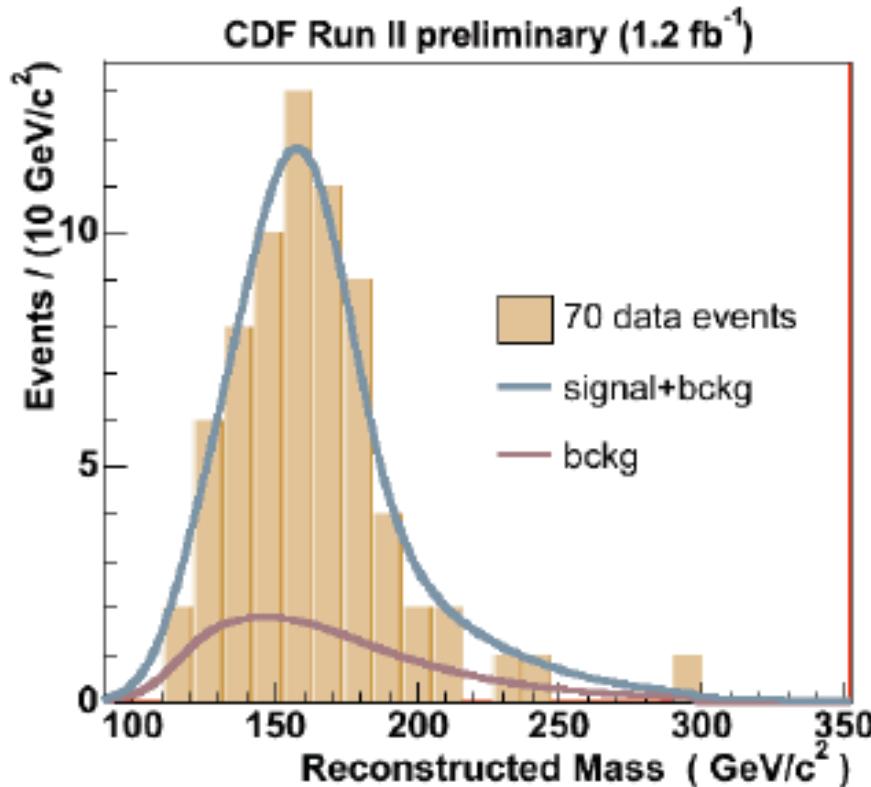
- 1.1% precision and no bias due to new physics appeared yet
- Reasons we surpassed Run-IIa goal:
 - *In-situ* Wjj calibration
 - Dedicated people working coherently
- But *In-situ* calibration will be soon limited by b-jet specific uncertainty
- Small effects at Tevatron (<400 MeV)
 - NLO using MC@NLO
 - qq vs gg events (2 GeV diff.)
 - Spin correlation
 - Multiple interactions(pileup)
 - Color interference?
- What Mt have we measured? Joyful debate @ $\delta M_t < 1 \text{ GeV}/c^2$



Backup: Methods in dilepton

- Unconstrained system;
2 neutrinos, but 1 missing E_T observable
- Template:
 - Assume $\eta(v)$ (or $\phi(v)$, $P_Z(tt)$)
 - Sum over all kinematic solutions, and (l,b) pairs,
select the most probable value as a reco. M_t
- Matrix Element:
 - Integrated over unknown variables using the LO Matrix Element
assuming jet angles, lepton are perfect, and all jets are b's
 - Obtain $P(M_{top})$ for signal and backgrounds
 - Calibrate off-set in pull and pull width using fully simulated MC

Backup: Results in dilepton



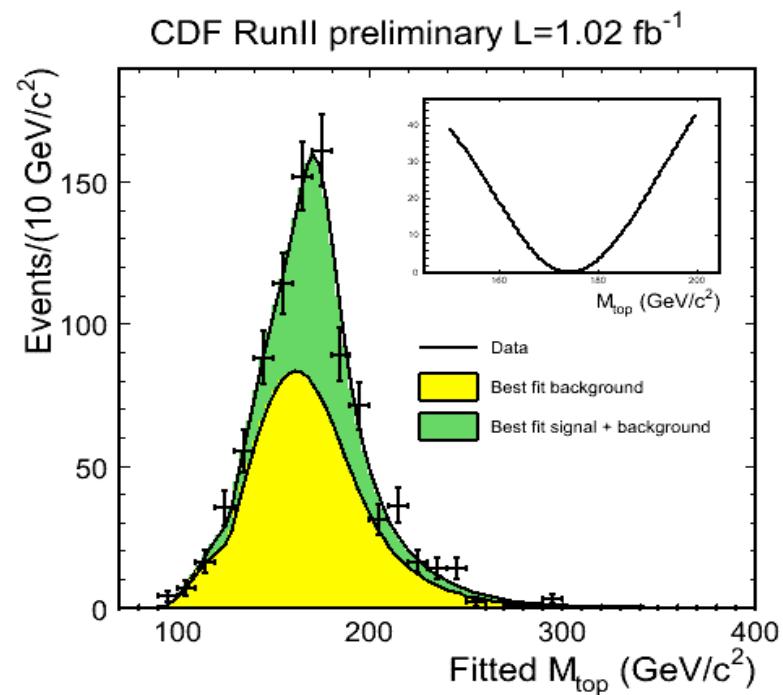
$$M_{top} = 169.7^{+5.2}_{-4.9}(\text{stat.}) \pm 3.1(\text{syst.}) \text{ GeV} / c^2$$

$$M_{top} = 170.7^{+4.2}_{-3.9}(\text{stat.}) \pm 2.6(\text{syst.}) \pm 2.4(\text{the.}) \text{ GeV} / c^2$$

- Event selections: 2 leptons ($\text{Pt} > 20$), 2 jets ($\text{Et} > 15$), $\text{MET} > 25 \text{ GeV}$
- Syst. error is comparable to the stat. error
- Toward 2nd publications with 1fb^{-1}

Backup:Template in all-jets

- Template method with fitted M_{top} as observable
- Choose among all possible combination of 6 jets using a kinematic fitter
- Event selection:
 - $E_T / \sqrt{(\sum E_T)} < 3 \text{ (GeV)}^{1/2}$
 - $\sum E_T \geq 280 \text{ GeV}$
 - $n_{b\text{-tag}} \geq 1$ (b-tag)
 - $6 \leq N_{jet} \leq 8$
 - Neural Network selection to improve S/B = 1/2 (vs 1/8)
- And data-driven background template



$$M_{top} = 174.0 \pm 2.2 (\text{stat.}) \pm 4.5 (\text{JES}) \\ \pm 1.7 (\text{syst.}) \text{ GeV} / c^2$$

New $M_{top} = 171.1 \pm 3.7 (\text{stat. + JES}) \\ \pm 2.1 (\text{syst.}) \text{ GeV} / c^2$