

Top Quark Mass Measurement with the Neutrino Weighting Method at DØ

Workshop on Top Physics: from the TeVatron to the LHC
Grenoble

Content

- ◆ **Ttbar dilepton channel**
- ◆ **Event Selection and yields**
- ◆ **Neutrino Weighting algorithm**
 - ◆ **Modeling of probability density functions**
- ◆ **Calibration with ensemble tests**
- ◆ **Systematic uncertainties**
- ◆ **Results and Summary**



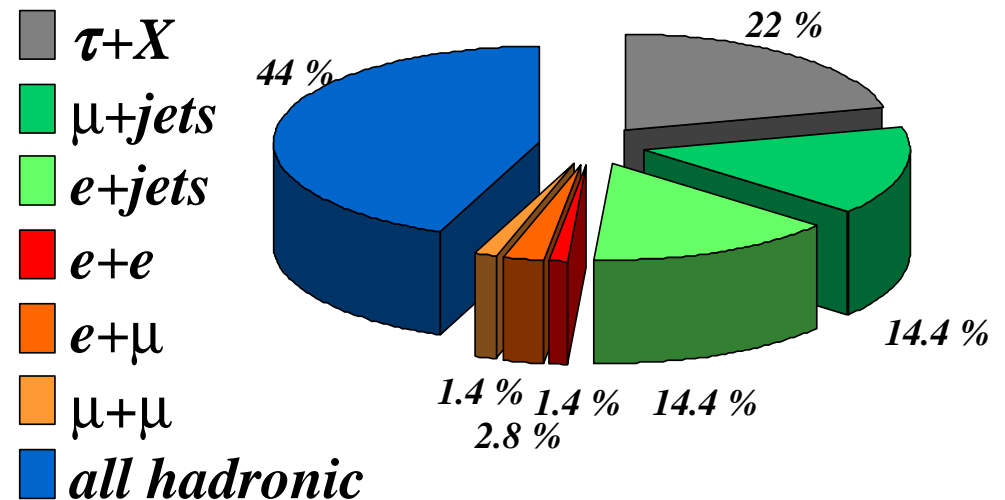
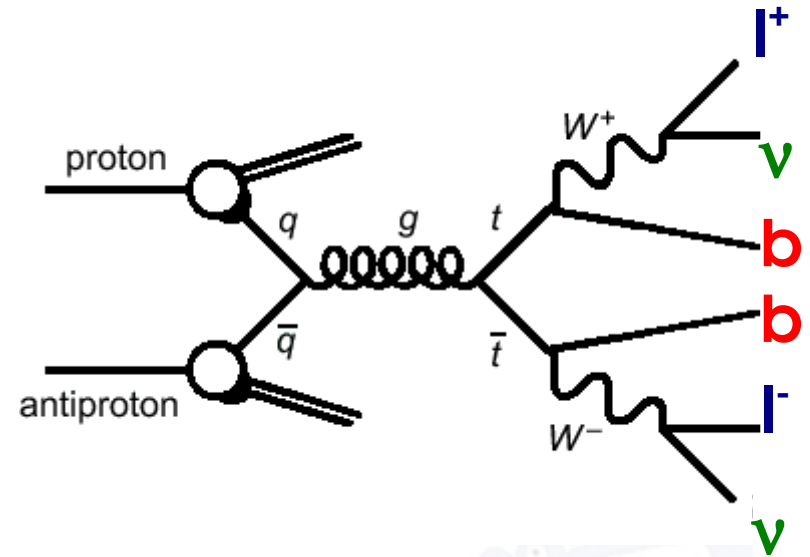
Top Mass in Dilepton Events

Dilepton channel:

- BR($t\bar{t} \rightarrow$ dilepton) $\approx 5\%$
- Statistics is limited at Tevatron
- Clear signature with two high p_T leptons

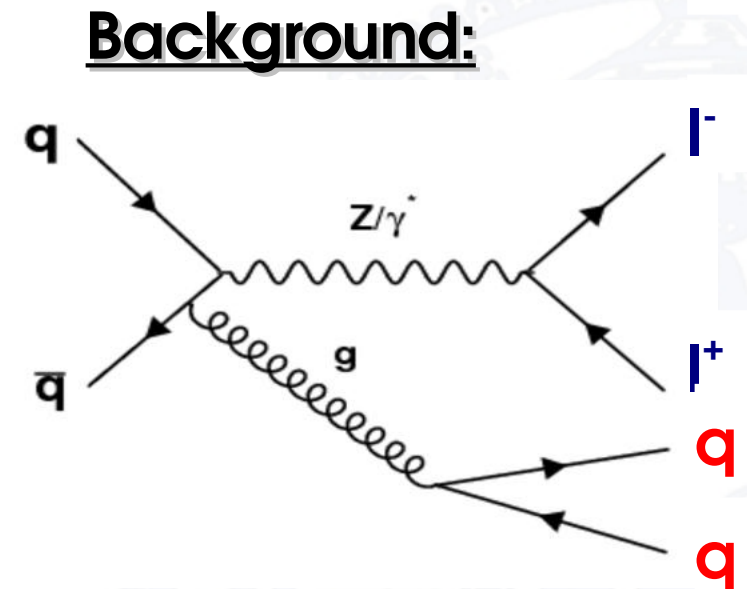
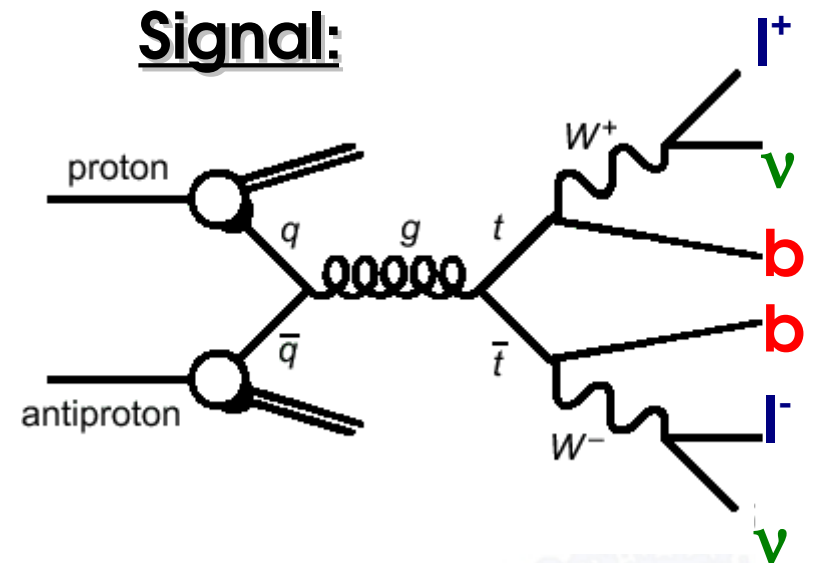
leptons

- Kinematics underconstraint due to two neutrinos
- Top mass measurement in dilepton channel is an important test of the SM!



Event Selection

- ▶ 2 isolated leptons: $p_T > 15 \text{ GeV}$
- ▶ Electrons: $|\eta| < 1.1$ or $1.5 < |\eta| < 2.5$
- ▶ Muons: $|\eta| < 2.0$
- ▶ 2 jets: $p_T > 20 \text{ GeV}$, $|\eta| < 2.5$
- ▶ Topological cuts
 - ▶ $H_T > 115 \text{ GeV}$ ($e\mu$)
 - ▶ Sphericity > 0.15 (ee)
- ▶ Anti-Z-cuts
 - ▶ $M(ee) < 80 \text{ GeV}$ & $MET > 30 \text{ GeV}$ or
 $M(ee) > 100 \text{ GeV}$ & $MET > 40 \text{ GeV}$ (ee)
 - ▶ Z-fitter ($\mu\mu$), $MET > 35 \text{ GeV}$



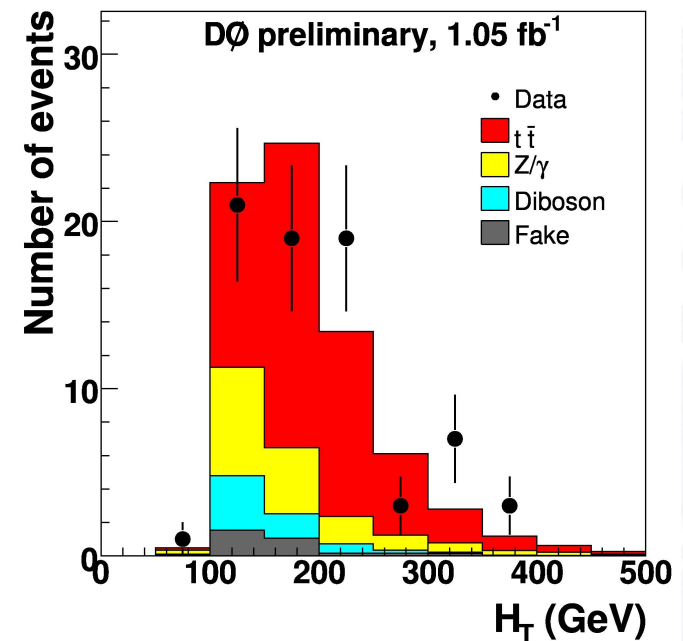
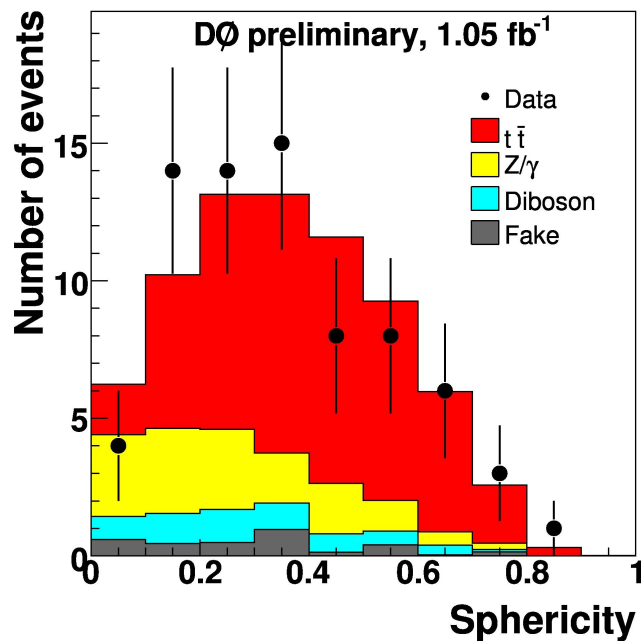
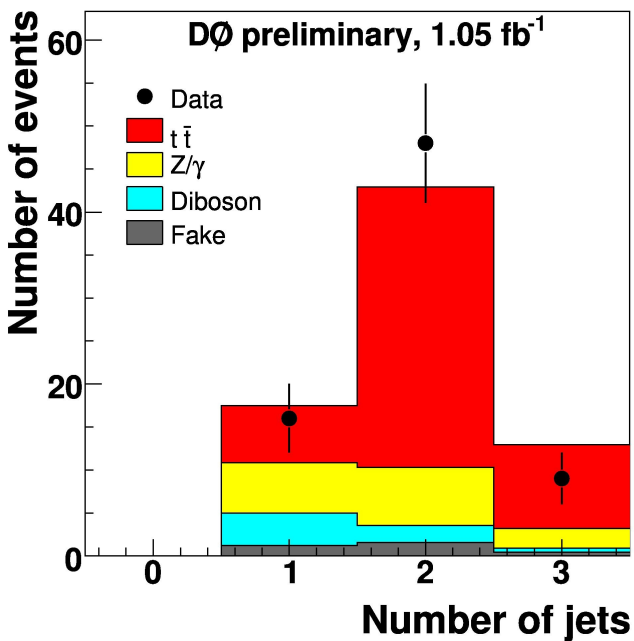
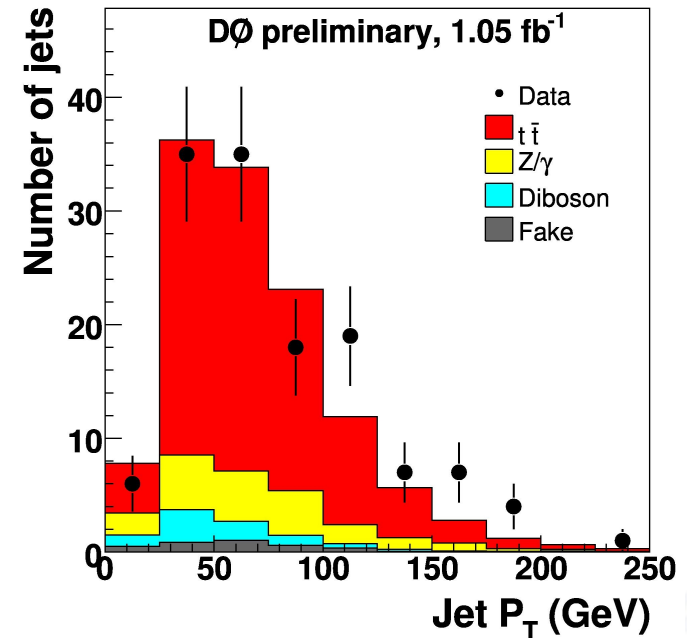
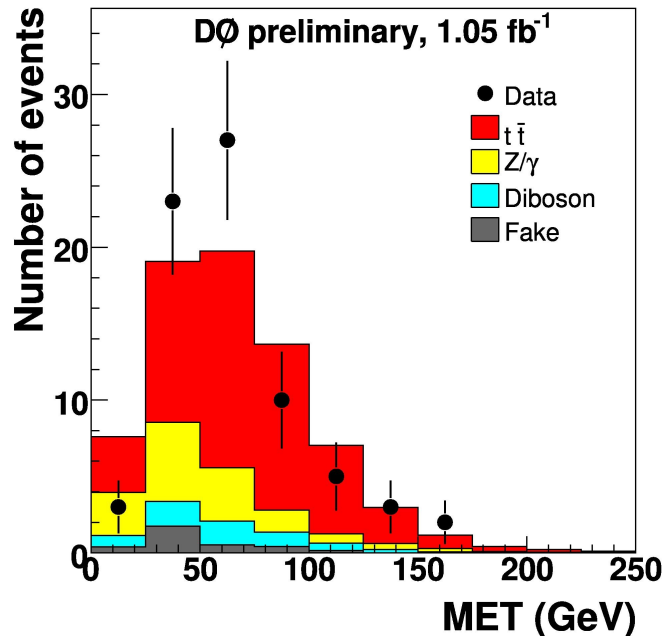
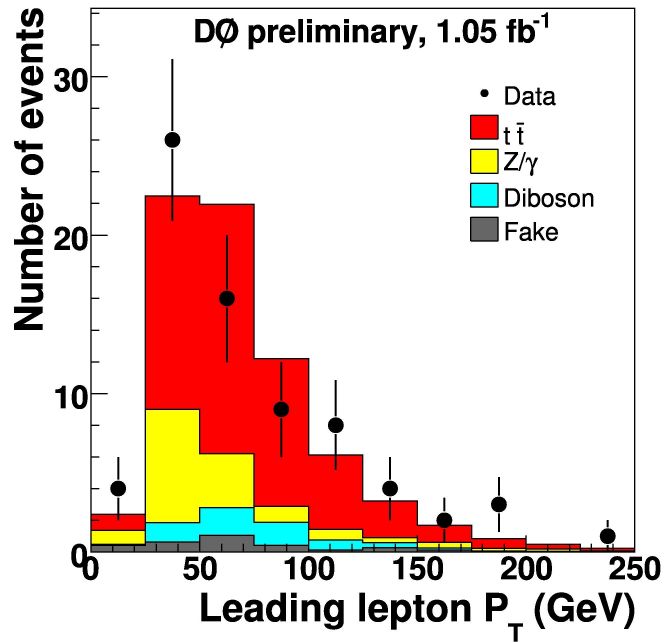
Event Yields

Luminosity: 1.05 fb^{-1}

Category	ee	$\mu\mu$	$e\mu$
integrated luminosity (pb^{-1})	1036	1046	1046
Z/γ^*	$2.4^{+0.4}_{-0.4}$	$2.7^{+0.4}_{-0.4}$	$3.6^{+0.7}_{-0.8}$
WW/WZ and other MC	$0.4^{+0.2}_{-0.2}$	$0.5^{+0.1}_{-0.1}$	$1.4^{+0.6}_{-0.6}$
Instrumental background	$0.2^{+0.2}_{-0.1}$	$0.4^{+0.2}_{-0.2}$	$1.8^{+0.6}_{-0.6}$
Total background	$3.0^{+0.5}_{-0.5}$	$3.6^{+0.5}_{-0.5}$	$6.7^{+1.2}_{-1.2}$
Signal efficiency (%)	$8.3^{+1.2}_{-1.2}$	$5.1^{+0.4}_{-0.4}$	$12.4^{+0.9}_{-1.0}$
Expected signal	$9.5^{+1.4}_{-1.4}$	$5.8^{+0.5}_{-0.5}$	$28.6^{+2.1}_{-2.4}$
Total Sig. + Bkg.	$12.5^{+1.5}_{-1.5}$	$9.4^{+0.7}_{-0.7}$	$35.3^{+2.8}_{-3.2}$
Selected events	16	9	32

56 candidates

Control Distributions



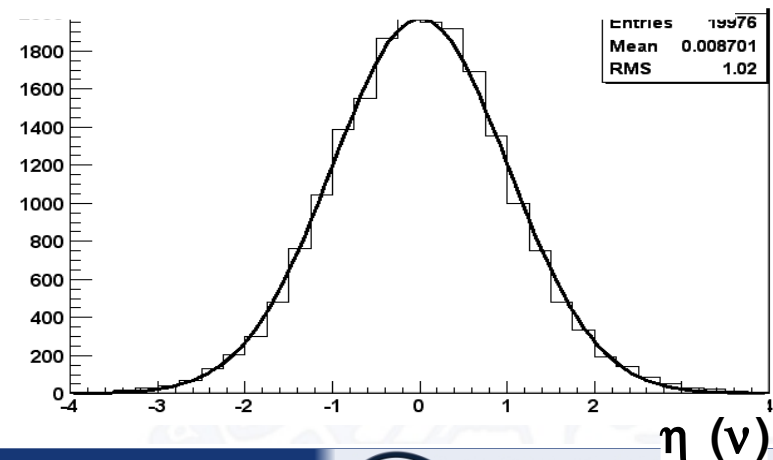
Neutrino Weighting Method

Kinematics underconstraint -> Neutrino Weighting

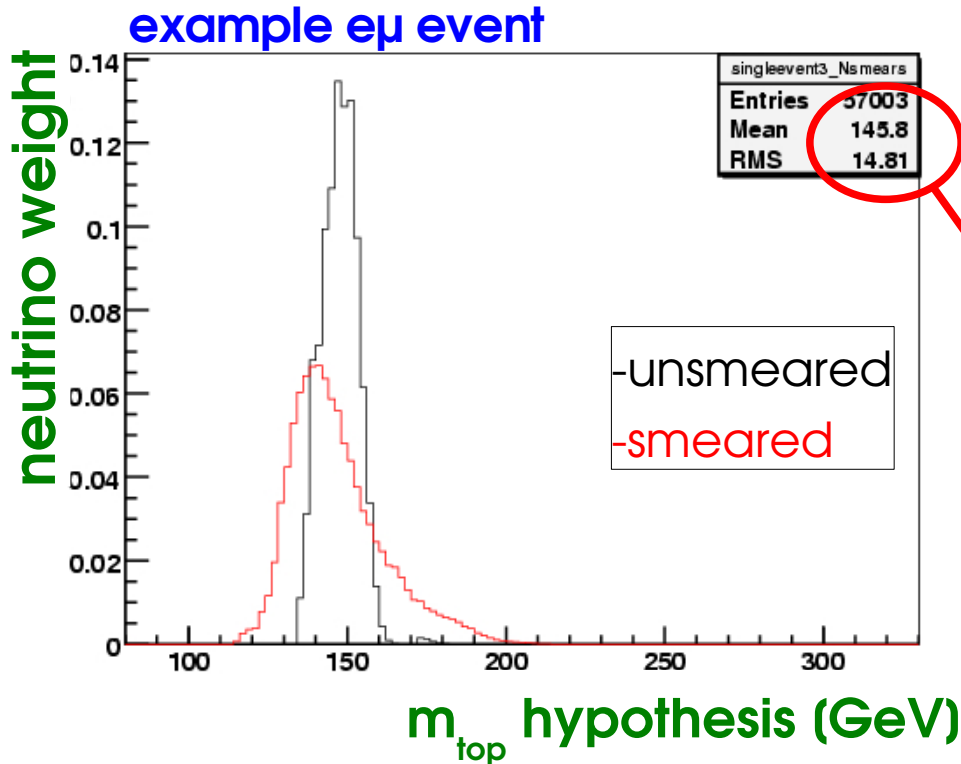
- Assume: $m_{top}, \eta^{\nu}, \eta^{\bar{\nu}}$
- Calculate $p_x^{\nu}, p_y^{\nu}, p_x^{\bar{\nu}}, p_y^{\bar{\nu}}$ using assumptions and kinematical constraints but without using $metx, mety$
- Get weight for each assumption by **comparison with missing transverse energy**:

$$w^{\nu}(m_{top}) = \exp\left(\frac{-\left(metx - p_x^{\nu} - p_x^{\bar{\nu}}\right)^2}{2\sigma^2}\right) \exp\left(\frac{-\left(mety - p_y^{\nu} - p_y^{\bar{\nu}}\right)^2}{2\sigma^2}\right)$$

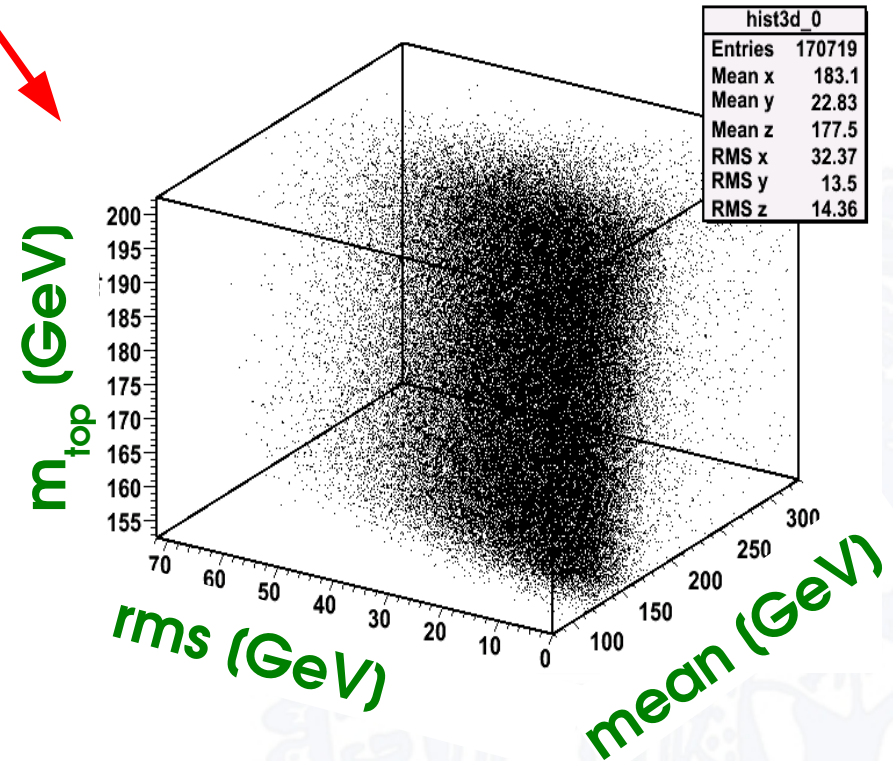
- Sum over all assumptions, all kinematic solutions (2 per neutrino) and both possible jet-lepton-assignments



Neutrino Weighting Method (II)



- Use **MEAN** and **RMS** of neutrino weight distribution
- **3D** signal probability density function

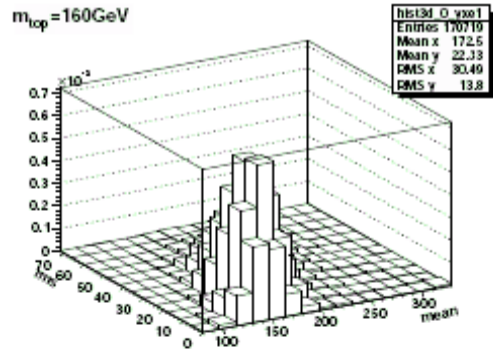


Statistical fluctuations in signal pdf will be smoothed by a 3D fit

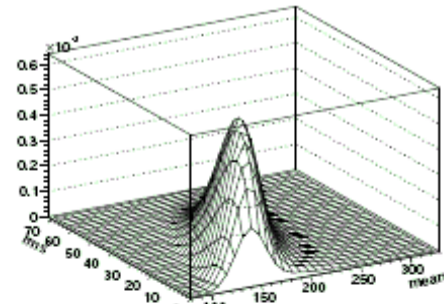
Signal Probability Density Function

$m_{\text{top}} = 160 \text{ GeV}$

histogram

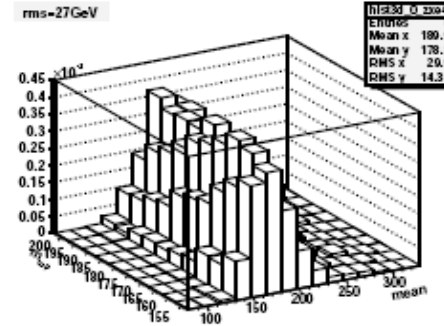


fit

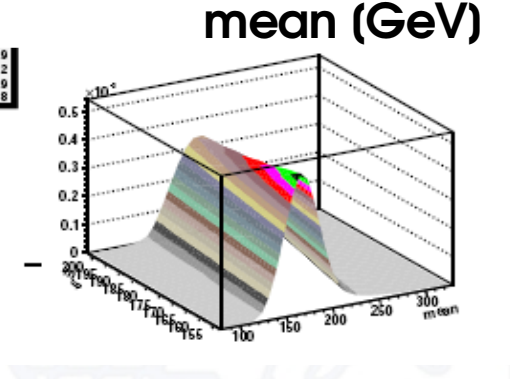
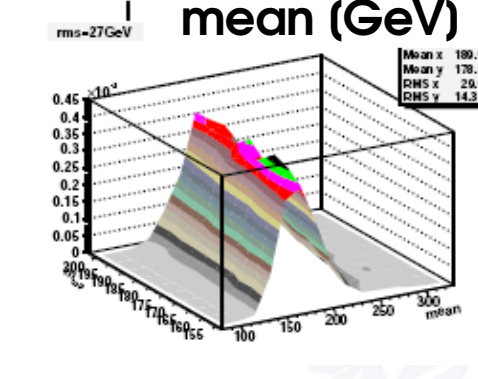
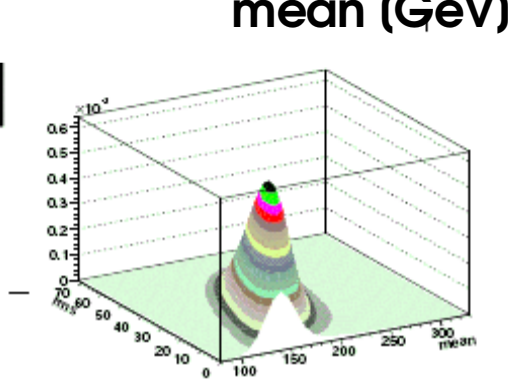
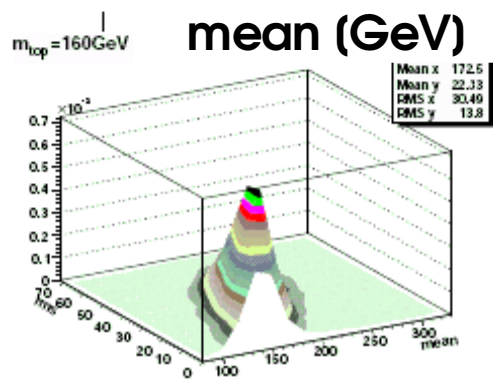
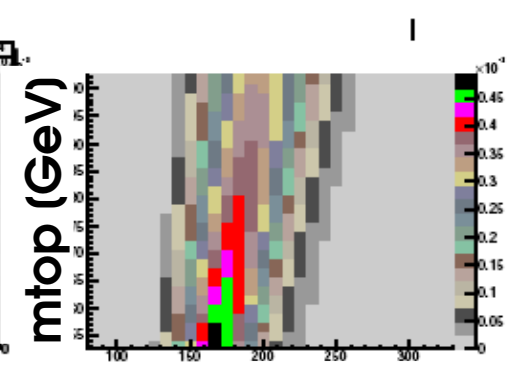
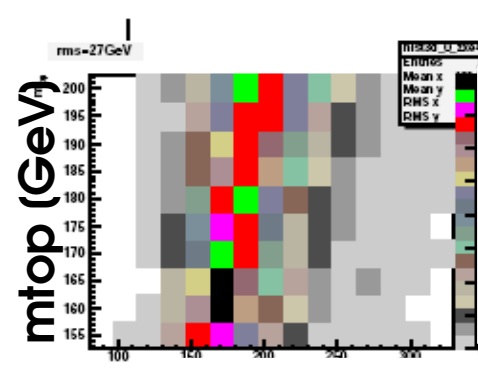
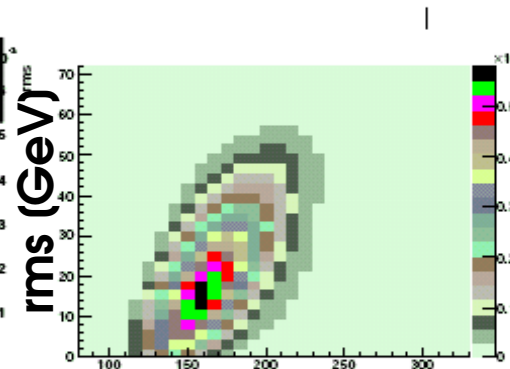
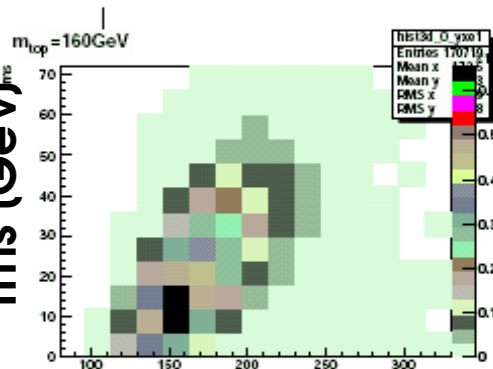
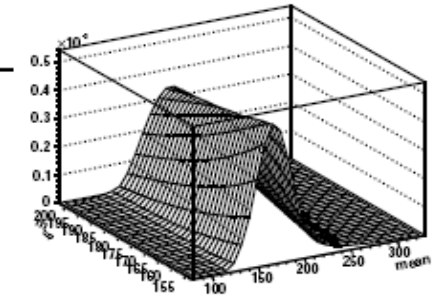


rms = 91 GeV

histogramm



fit

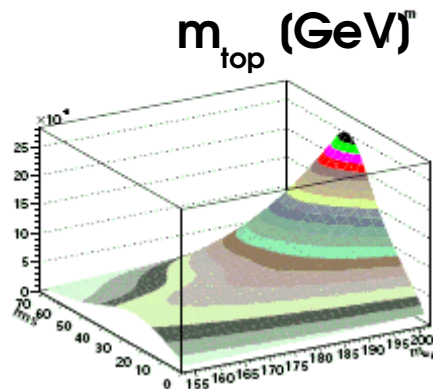
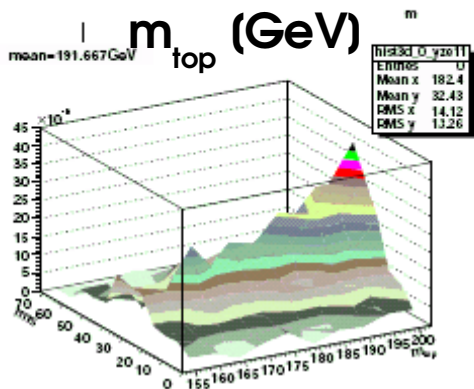
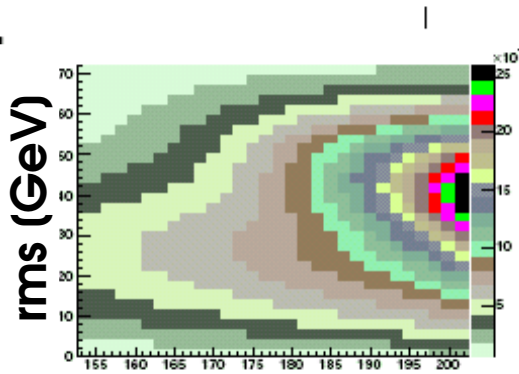
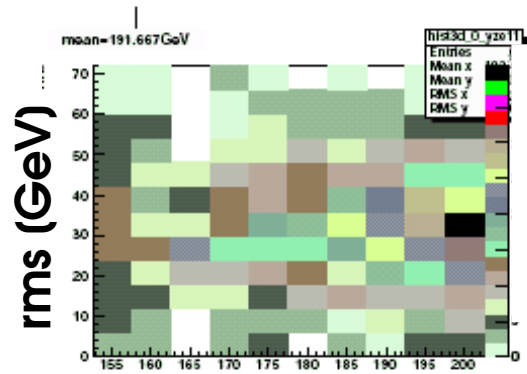
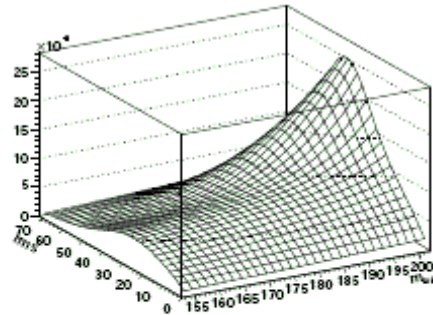
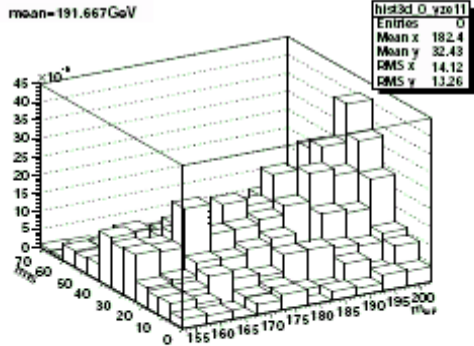


Signal Probability Density Function (II)

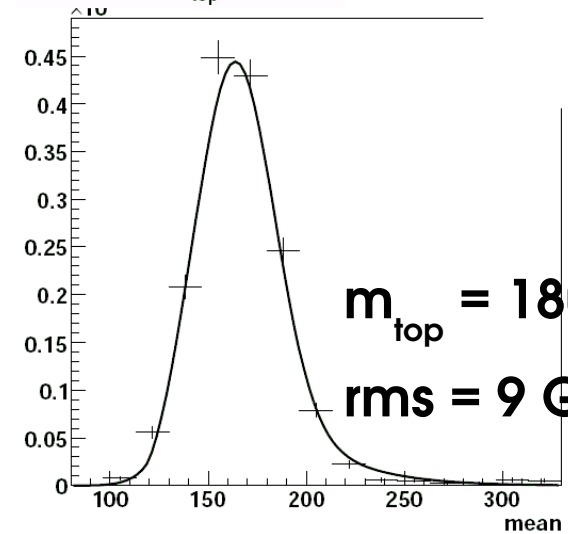
mean = 192 GeV

histogram

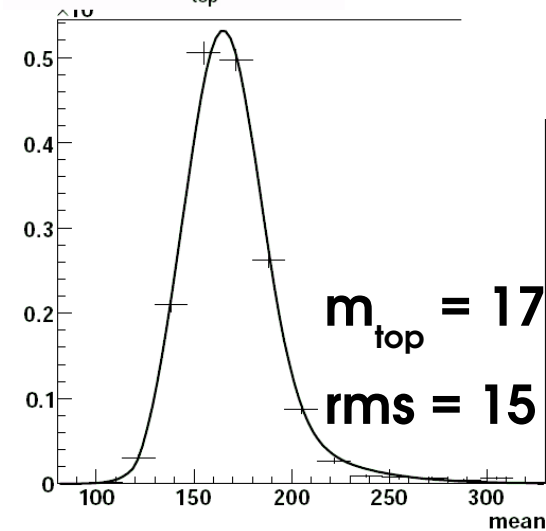
fit



rms=9GeV, $m_{top}=180\text{GeV}$



rms=15GeV, $m_{top}=170\text{GeV}$

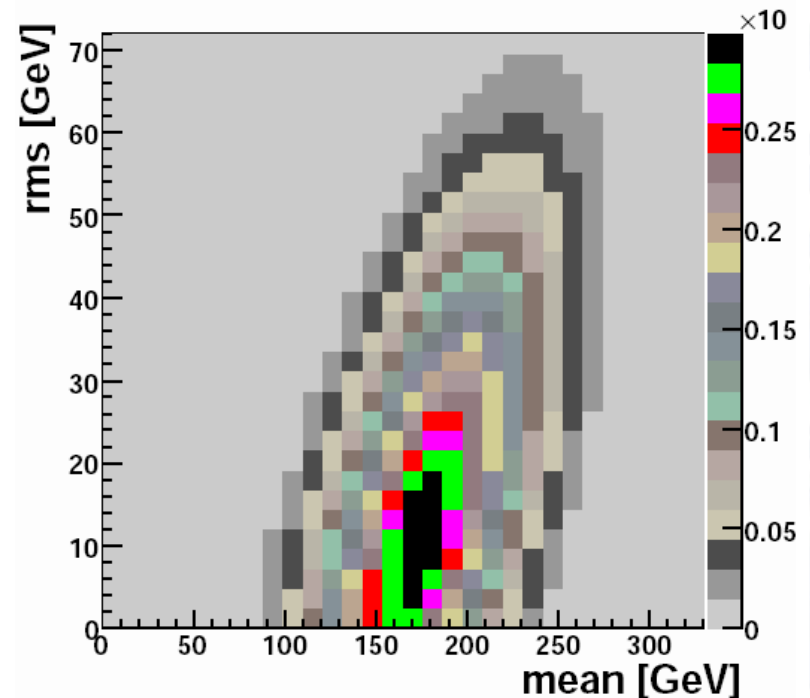


Background Probability Density Function

- Background PDF modeled the same way as signal PDF:
 - apply Neutrino Weighting algorithm to bg events
- No dependence on m_{top}
- Smoothed by 2D-fit

example:

- bg PDF for ee channel
- mainly Z_{jj} ee_{jj} events
- bg fractions correspond to expected yields



Maximum Likelihood Method

Likelihood:

$$L(\text{mean}_i, \text{rms}_i, \bar{n}_b, N | m_{\text{top}}, n_s, n_b) = \frac{1}{\sqrt{2\pi\sigma_b}} \exp\left(\frac{-(n_b - \bar{n}_b)^2}{2\sigma_b^2}\right) \quad \text{Gaussian for } n_b$$
$$\times \frac{\binom{n_s + n_b}{n_s}^N e^{-(n_s + n_b)}}{N!} \quad \text{Poissonian for } n_s + n_b$$

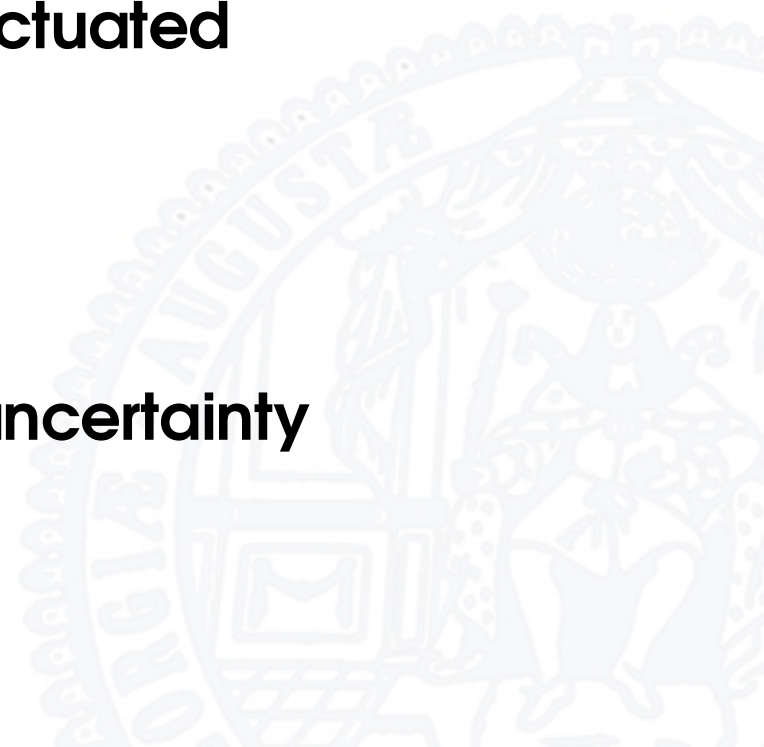
dependence on m_{top}

$$\times \prod_i \frac{n_s f_s(\text{mean}_i, \text{rms}_i | m_{\text{top}}) + n_b f_b(\text{mean}_i, \text{rms}_i)}{n_s + n_b}$$

Extract top quark mass by minimizing $-\ln(\text{likelihood})$
with respect to m_{top} , n_s , and n_b

Ensemble Tests

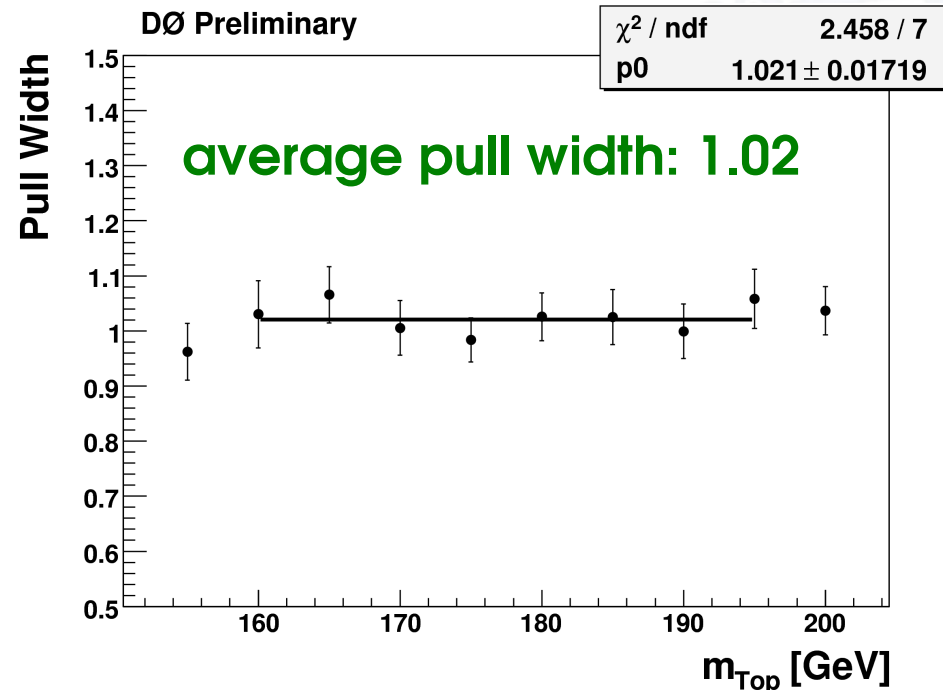
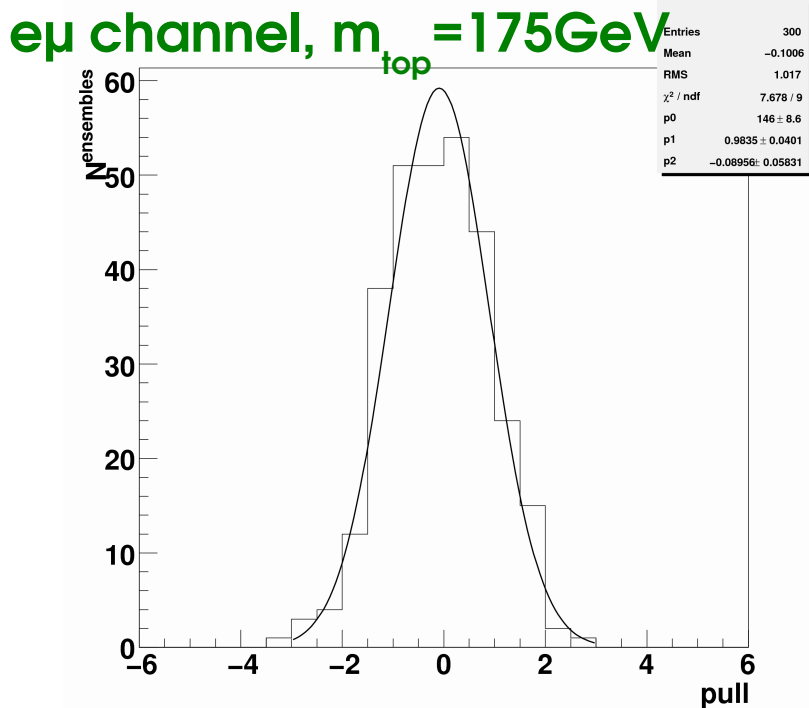
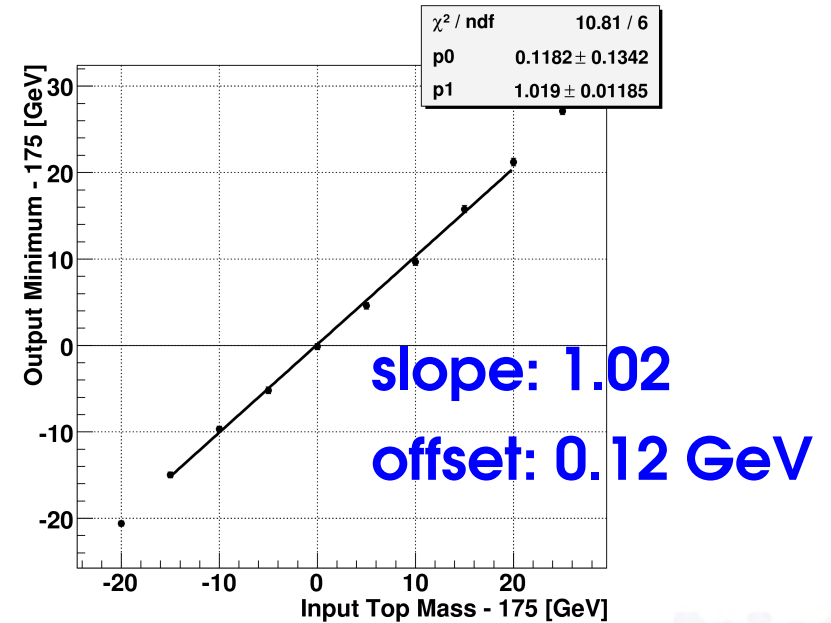
- ▶ 300 ensembles per dilepton channel
 - ▶ Size of ensemble corresponds to the size of data set
 - ▶ Events are randomly chosen from simulated signal and background events
 - ▶ background fraction is Poisson-fluctuated
-
- Test and calibration of method
 - Pull distributions
 - Estimation of expected statistical uncertainty



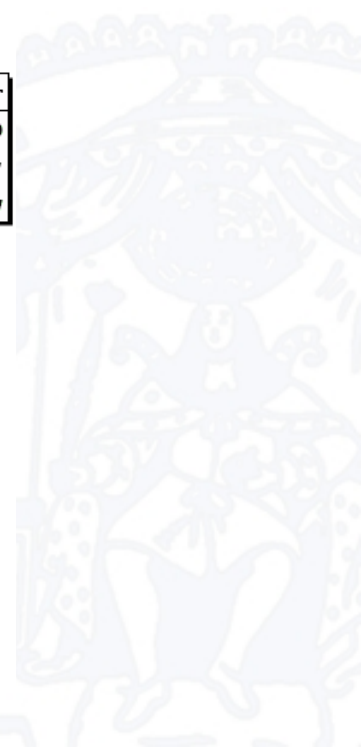
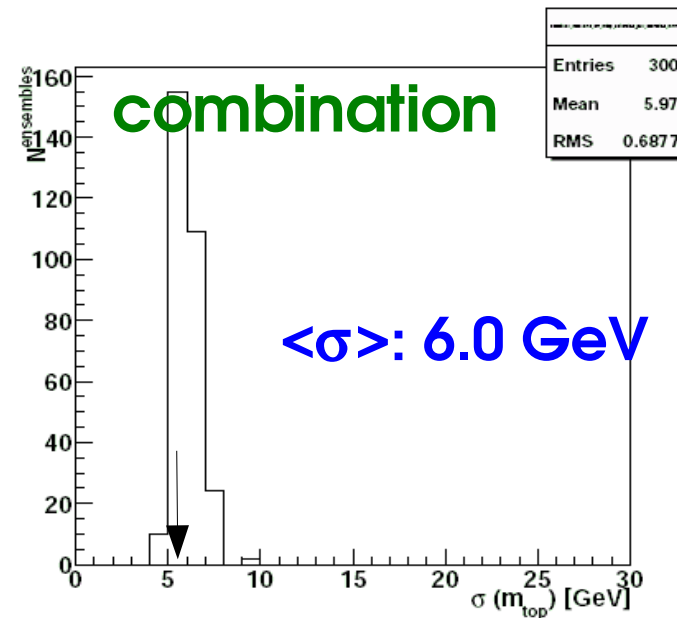
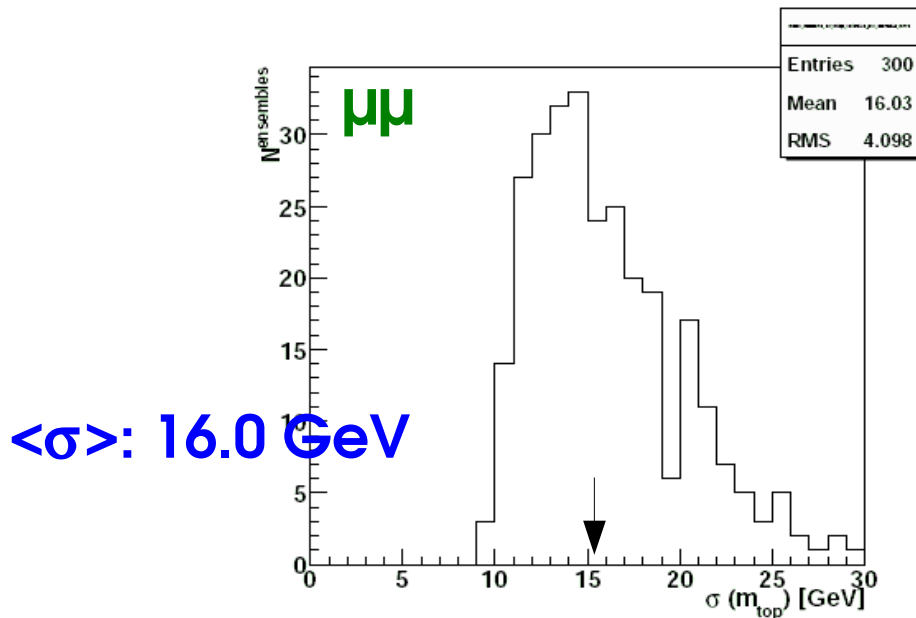
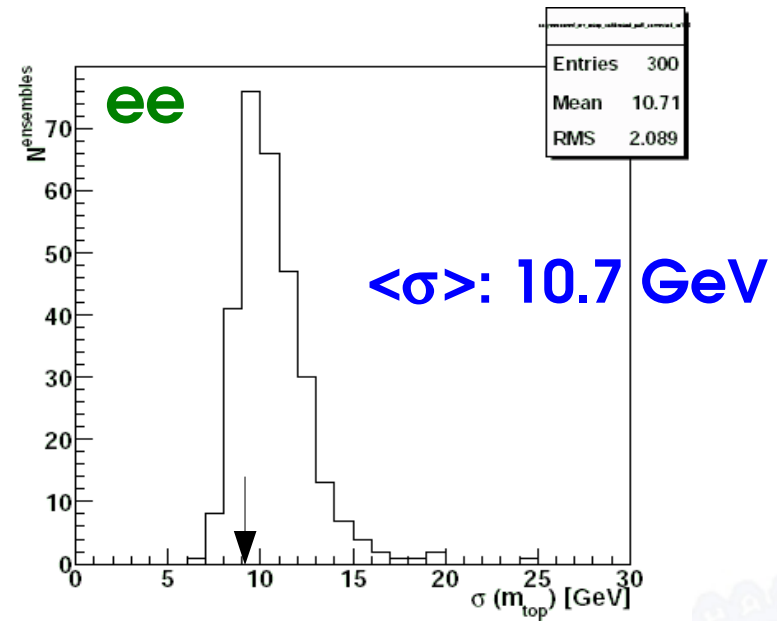
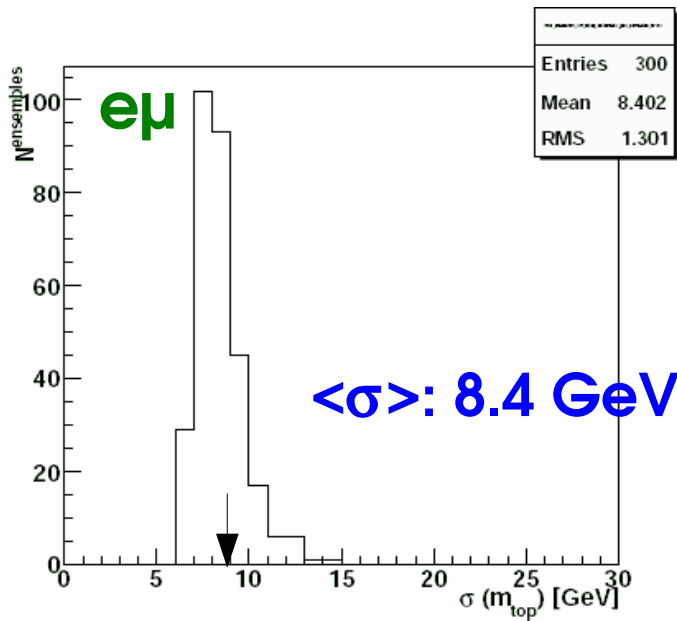
Calibration

Results of ensemble tests:

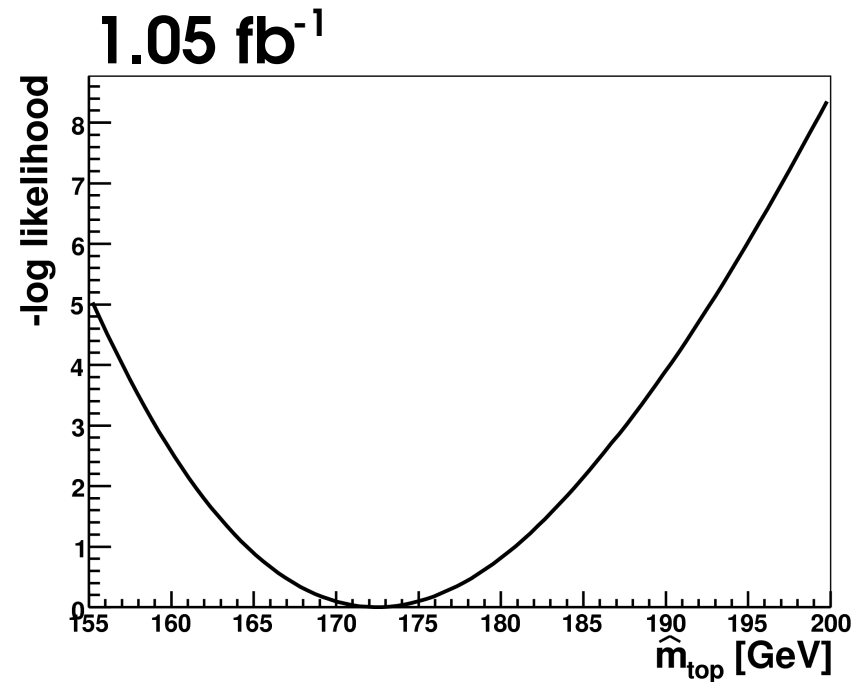
- ◆ Input versus output top quark mass
- ◆ Pull distributions



Expected and Observed Uncertainties



Data Result

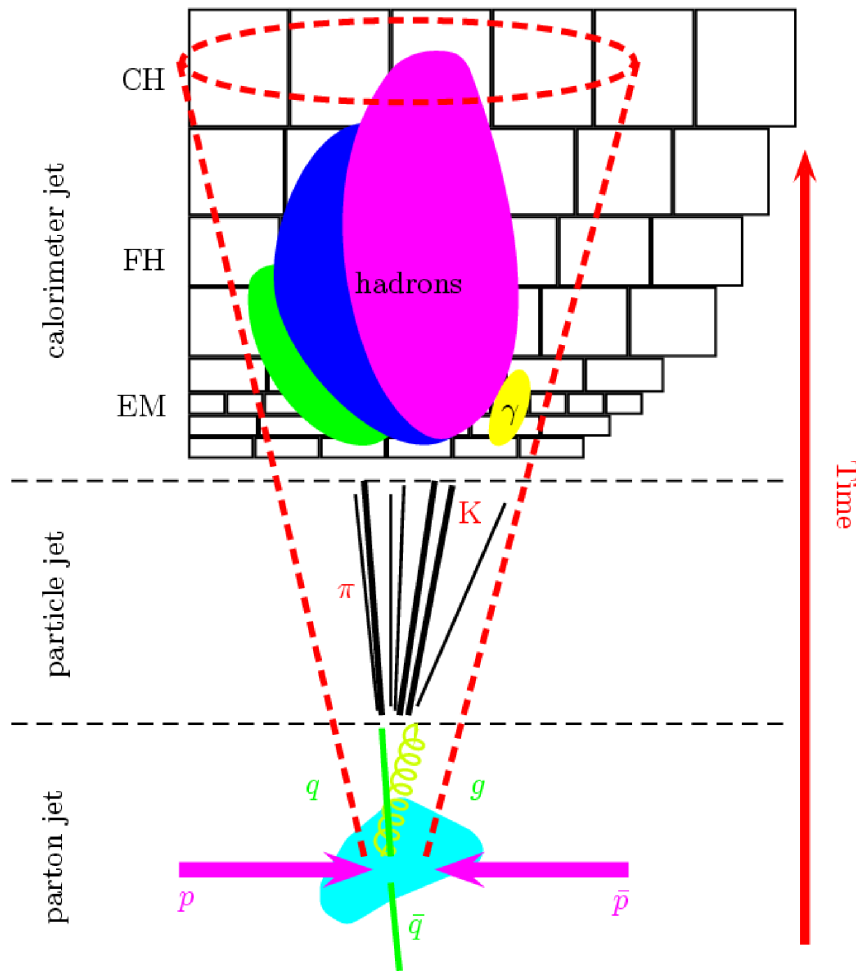


$$m_{\text{top}} = 172.5 \pm 5.8 \text{ (stat)} \pm 3.5 \text{ (syst)} \text{ GeV} \quad (\nu\text{WT})$$

$$m_{\text{top}} = 175.2 \pm 6.1 \text{ (stat)} \pm 3.4 \text{ (syst)} \text{ GeV} \quad (\text{MWT})$$

$$m_{\text{top}} = 173.7 \pm 5.4 \text{ (stat)} \pm 3.4 \text{ (syst)} \text{ GeV}$$

Systematic Uncertainties



Summary of all uncertainties:

Source	Uncertainty (GeV)
Jet Energy Scale	± 2.5
b -Jet Energy Scale	± 2.0
Jet Resolution	± 0.3
Muon Resolution	± 0.4
$t\bar{t}$ + jets	± 0.14
PDF variation	± 0.7
Background Template Shape	± 0.3
Template fit statistics	± 0.9
Underlying event	± 0.13
Total Systematic Uncertainty	± 3.5

**Jet energy scale
uncertainty: ± 2.5 GeV**

Summary

- ♦ Measurement of top quark mass in an unconstrained system with the Neutrino Weighting algorithm
- ♦ Modeling of signal and background pdf by multi-dimensional fit

$$m_{\text{top}} = 172.5 \pm 5.8 \text{ (stat)} \pm 3.5 \text{ (syst)} \text{ GeV} \quad (\text{vWT})$$

backup slides

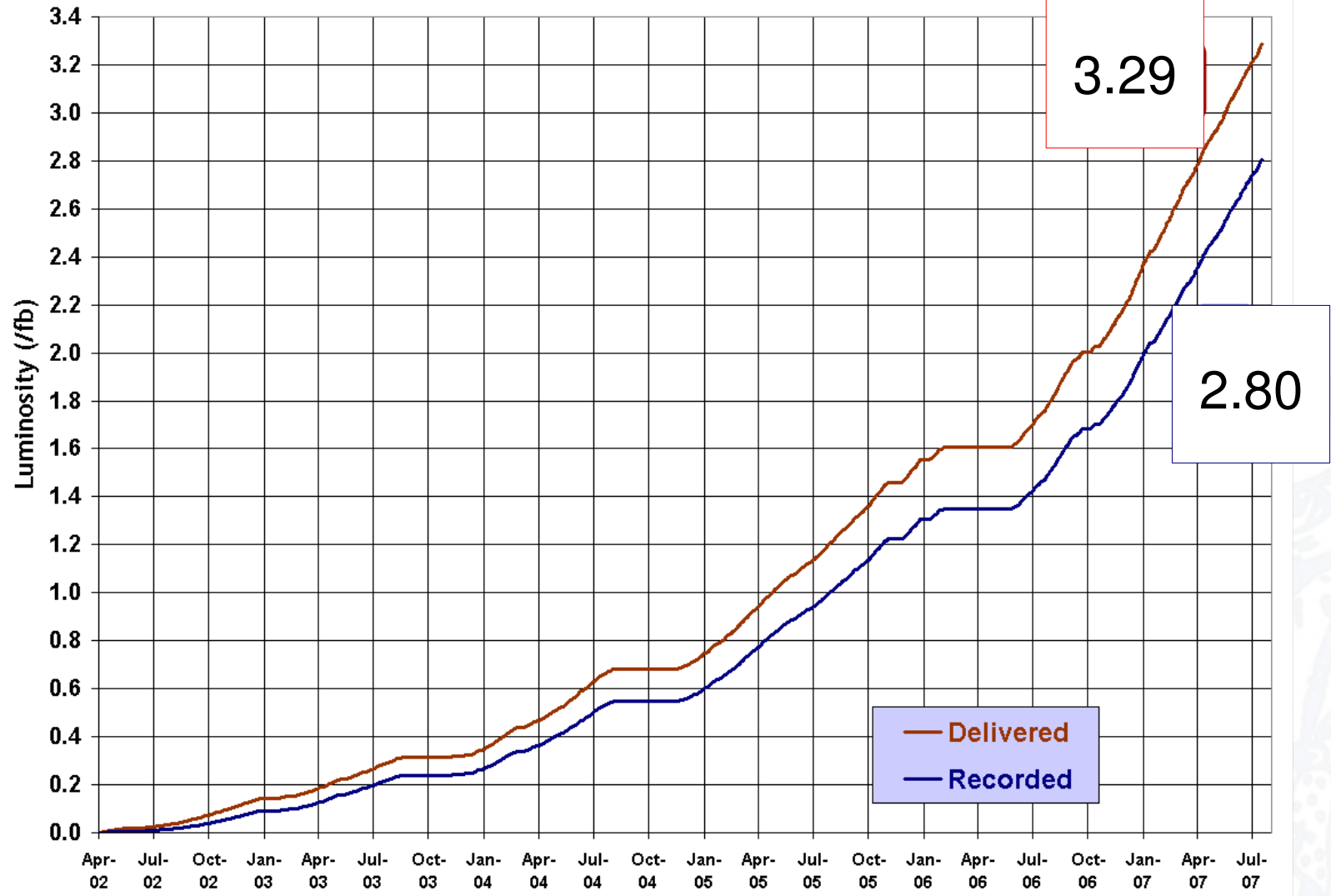


Integrated Luminosity



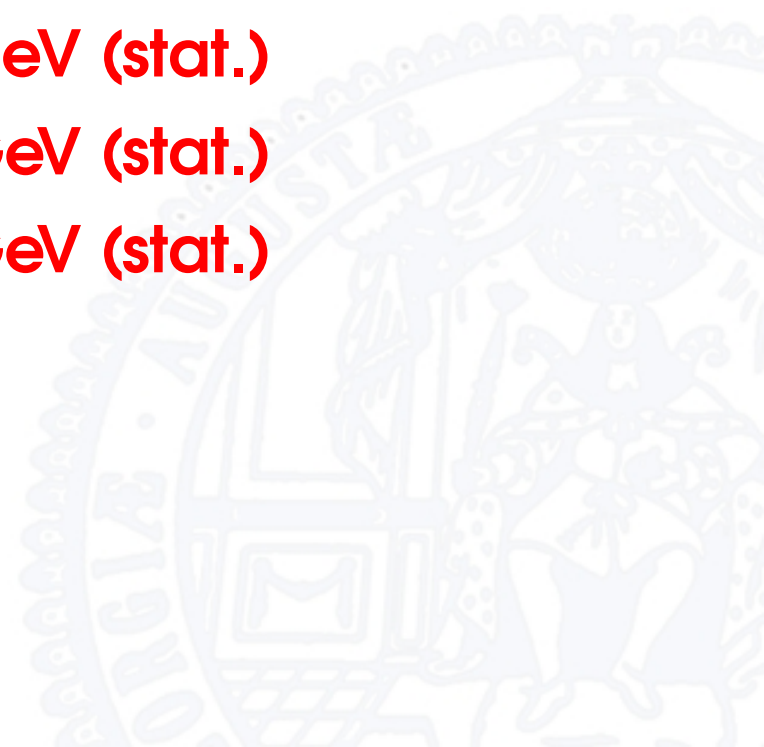
Run II Integrated Luminosity

19 April 2002 - 5 August 2007



Individual channels

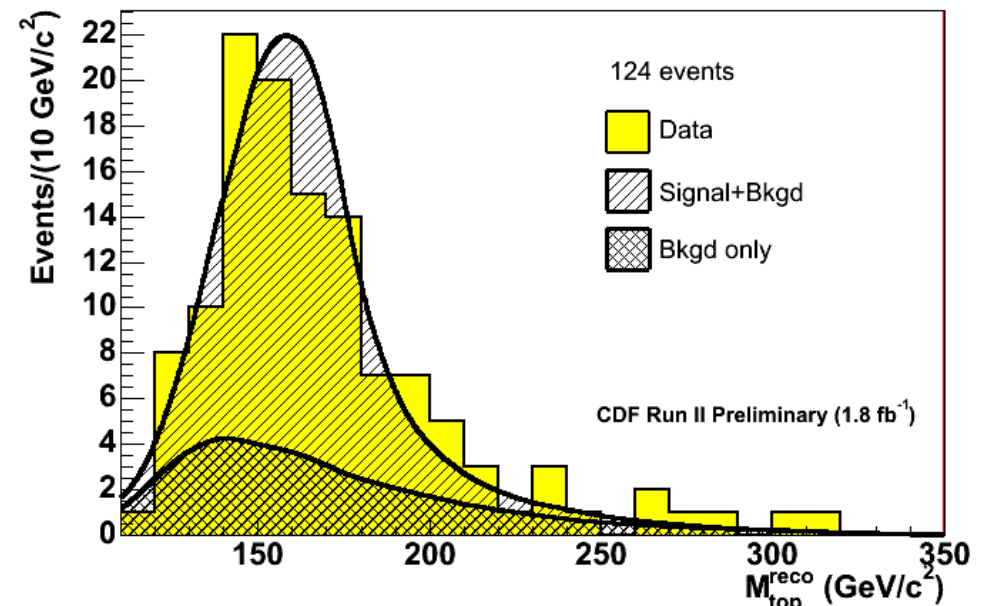
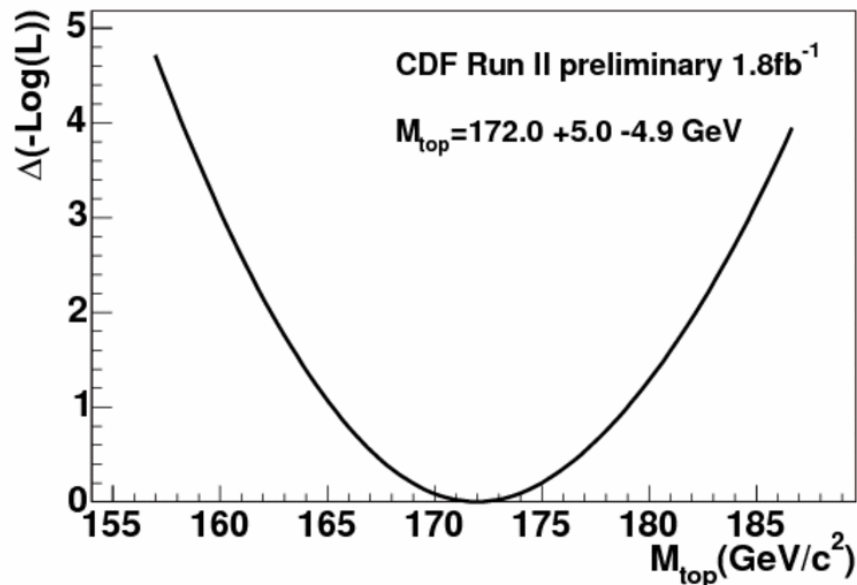
$e\mu$:	170.6 ± 8.6 GeV (stat.)
ee :	173.9 ± 9.3 GeV (stat.)
$\mu\mu$:	179.7 ± 15.5 GeV (stat.)
combination:	172.5 ± 5.8 GeV (stat.)



CDF Result with Neutrino Weighting



- ◆ Same Neutrino Weighting Algorithm
- ◆ 1.8 fb⁻¹, 124 candidates
- ◆ Maximum of weight distribution (instead of mean and rms)
- ◆ Smoothing by Kernel Density Estimation (instead of fit)



$M_{\text{top}} = 172.0 +5.0-4.9 \text{ (stat)} \pm 3.6 \text{ (syst)} \text{ GeV}/c^2$