













Theoretical nuclear reaction analysis for the ISOLDE Superconducting Recoil Separator (ISRS)

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Outline

Introduction

ISRS at ISOLDE and physics cases

Theoretical Framework

Overview of the computational framework and introduction of the codes

Calculations and Results

Residual nuclei and transfer-reaction calculations, cross-sections, and distributions

Summary and Outlook

A summary and future considerations

Overview of the ISRS project

What is ISRS?

- ISRS stands for **ISOLDE Superconducting Recoil Separator**.
- It is an advanced device being developed to be installed at **ISOLDE-CERN** to enable studies of **exotic nuclei**, especially those that are difficult to detect or separate with current instruments.

How will ISRS work?

- Uses superconducting multifunction magnets to bend and focus reaction products.
- Features a compact, lightweight design with very high resolution.
- Includes a compact ring to store and guide ions.

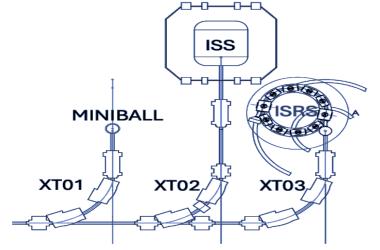
REX-ISOLDE High-beta cryomodules XT01 Miniball SEC XT02 ISRS

What kind of science will it enable?

- Nuclear structure (shells, halos, exotic decays)
- Astrophysics (r-process, nucleosynthesis)
- Reaction mechanisms (breakup, transfer, fusion)

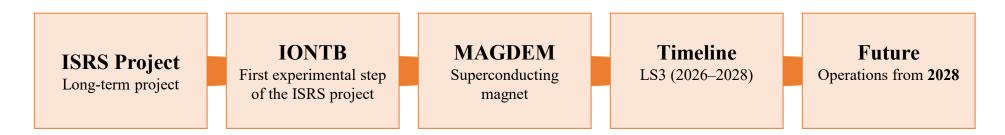
First step: Ion Test Bench (IONTB)

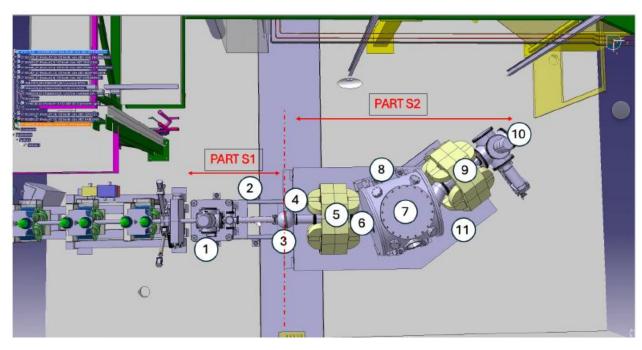
- That **first step** in making the ISRS a reality
- The IONTB is a prototype experimental setup at ISOLDE.



HIE-ISOLDE HALL

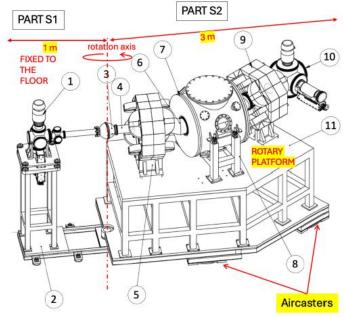
Ion Test Bench (IONTB)





Location of IONTB at HIE-ISOLDE (XT03)

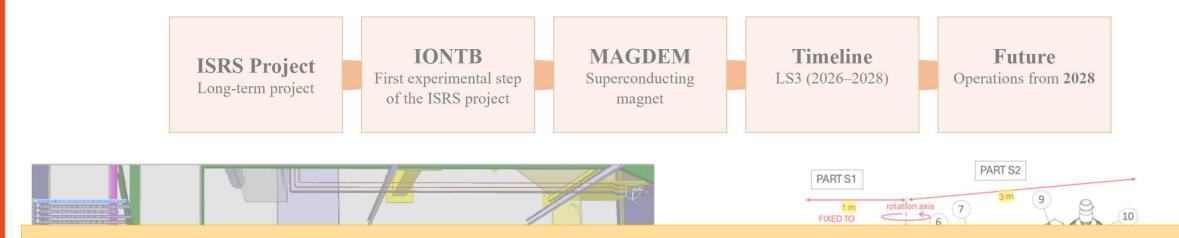
For more detailed information about the ISRS project, please visit: https://www.uhu.es/isrs/



Schematics of the prototype IONTB, composed of parts S1 and S2. Main subsystems: 1-Differential pumping, 2-Fixed platform, 3-Reaction chamber, 4-Beam line, 5-Quadrupole magnet, 6-Beam line, 7-MAGDEM superconducting magnet, 8-Mechanical support, 9-Quadrupole magnet, 10-Focal plane chamber, 11-Rotary platform with air-casters.

ULATIONS AND ANALYSIS

Ion Test Bench (IONTB)



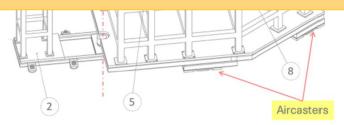
Theoretical focus of the ISRS project:

• Perform reliable nuclear reaction analyses to support beam dynamics simulations, guide the ISRS design, and optimize its performance.



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Selection of physics cases

The main goal of the nuclear reaction studies within the ISRS project is to conduct detailed investigations of reaction mechanisms across a broad range of projectile—target systems. The primary objectives include:

- Residual nuclei production
- Contributions of individual mechanisms

Single and multinucleon transfer reactions

Coulomb excitation

Complete and incomplete fusion

Compound-nucleus decay: fusion-evaporation

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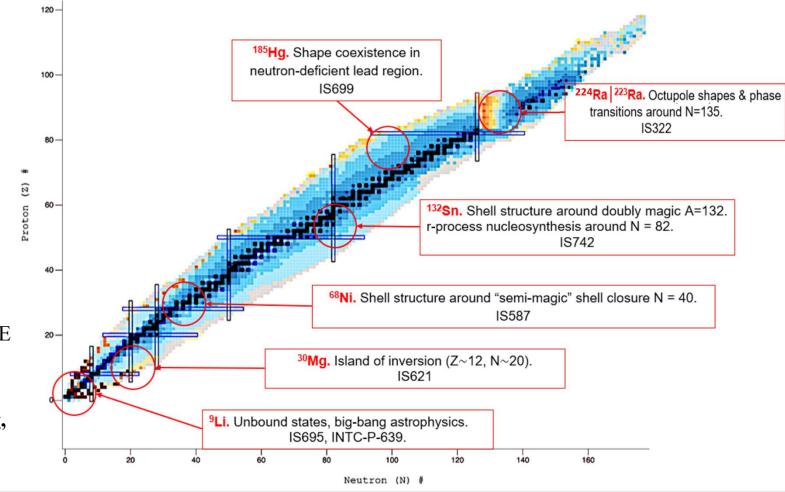
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Initial systems under study

- ☐ Selected based on the approved ISOLDE experimental proposals.
- ☐ Using CD₂ as the target.
- □ Radioactive beams: ⁹Li, ³⁰Mg, ⁶⁸Ni, ¹³²Sn, ¹⁸⁵Hg, and ²²⁴Ra.
- ☐ Beam energies: 5 and 10 MeV/u.



Computational framework for reaction analysis

A crucial initial step in our nuclear reaction analyses is to develop a comprehensive computational framework that accurately describes cross sections using established nuclear reaction codes.

✓ FRESCO — Elastic & Transfer Reactions

Ian J. Thompson, Comput. Phys. Rep. 7 (1988) 167.

☐ This versatile coupled-channels code is widely used for direct nuclear reaction calculations, supporting elastic scattering, inelastic excitation, transfer reactions, and breakup processes.

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✓ PACE4 — Fusion-Evaporation

A. Gavron, Phys. Rev. C 21, 230 (1980).

☐ Evaporation-focused Monte Carlo code for projectile absorption.

✓ EMPIRE — Detailed Reaction Cross-Sections

M. Herman, et al, Nucl. Data Sheets 108, 2655 (2007).

- ☐ First released in 1980, EMPIRE has been continuously improved over time.
- ☐ It includes key nuclear reaction models: Coupled Channels, DWBA, exciton model, Hauser-Feshbach, etc.
- □ Equipped with an extensive input parameter library covering nuclear masses, optical parameters, deformations, discrete levels, etc.
- ☐ The **modified version** integrated DWBA-IAV to estimate the inclusive breakup cross sections.

Deuteron-induced reactions

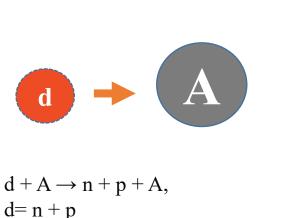
Extensive theoretical and experimental studies have been conducted on the inclusive neutron and proton emission cross sections in deuteron-induced reactions. Yet, the analysis of these reactions continues to be a challenging problem.



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,
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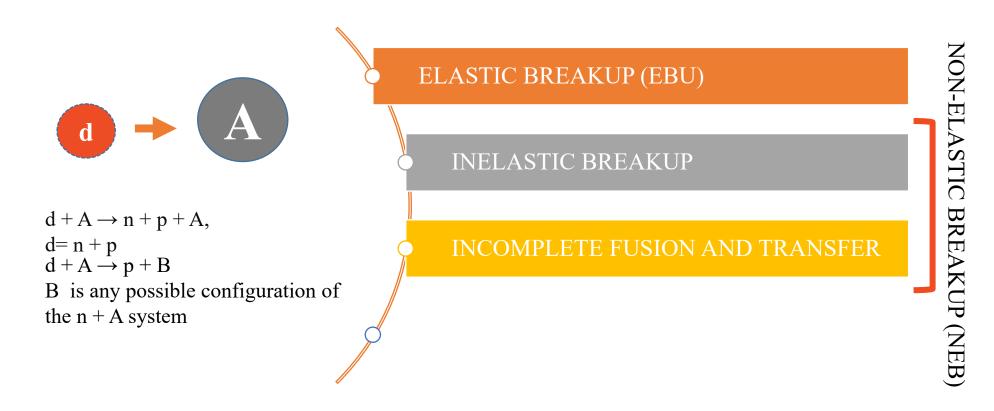
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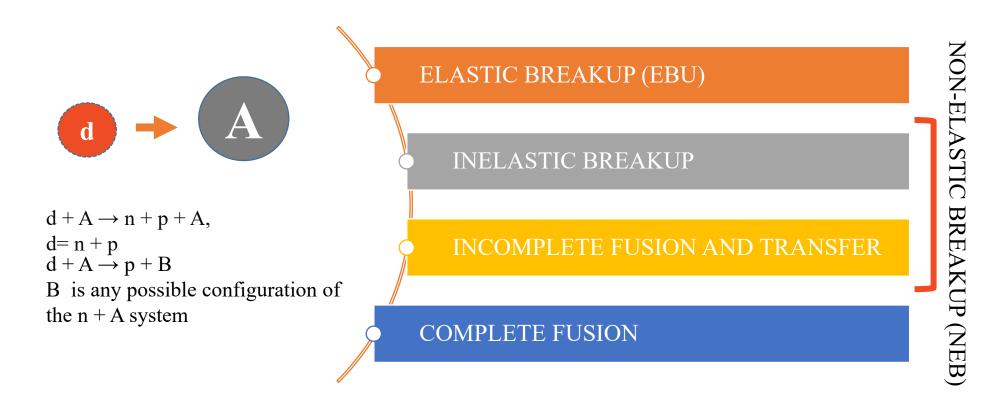
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Use of the post-form distorted wave Born approximation of the Ichimura-Austern-Vincent approach (DWBA-IAV) to describe breakup:

For A(d, p)X (p detected; X = n + A represents a final state of the fragment n together with the target), the inclusive breakup cross sections are obtained as:

$$\frac{d^2\sigma}{d\Omega_p dE_p} = \frac{d^2\sigma^{EBU}}{d\Omega_p dE_p} + \frac{d^2\sigma^{NEB}}{d\Omega_p dE_p}$$

The contribution due to elastic breakup (EBU):

$$\frac{d^2 \sigma^{EBU}}{d\Omega_p dE_p} = \frac{2\pi}{\hbar v_d} \rho_p(E_p) \int |T(\vec{k}_p, \vec{k}_n; \vec{k}_d)|^2 \delta(E_d + \varepsilon_d - E_p - E_n) d\vec{k}_n$$

R. Satchler, Direct nuclear reactions (United Kingdom, 1983)

and C. M. Vincent,

Phys. Rev. C 32, 431 (1985).

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The T-matrix element is approximated by the post-form of the DWBA matrix element

$$T(\vec{k}_p, \vec{k}_n; \vec{k}_d) = \left\langle \tilde{\chi}_p^{(-)}(\vec{k}_p, \vec{r}_p) \tilde{\chi}_n^{(-)}(\vec{k}_n, \vec{r}_n) | v_{np}(\vec{r}) | \chi_d^{(+)}(\vec{k}_d, \vec{R}) \phi_d(\vec{r}) \right\rangle$$

Which can be well-approximated within the zero-range DWBA by including a correction for finite-range effect as

$$T(\vec{k}_p, \vec{k}_n; \vec{k}_d) = D_0 \left\langle \tilde{\chi}_p^{(-)}(\vec{k}_p, a\vec{R}) \tilde{\chi}_n^{(-)}(\vec{k}_n, \vec{R}) \Lambda(R) \mid \chi_d^{(+)}(\vec{k}_d, \vec{R}) \right\rangle$$

n and C. M. Vincent, Phys. Rev. C 23,

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$$\frac{d^2\sigma}{d\Omega_p dE_p} = \frac{d^2\sigma^{EBU}}{d\Omega_p dE_p} + \frac{d^2\sigma^{NEB}}{d\Omega_p dE_p}$$

Following IAV work, the nonelastic component is also added as follows:

The nonelastic breakup (NEB) contribution is obtained from the imaginary part of the optical potential between the absorbed fragment and the target as

$$\frac{d^{2}\sigma^{NEB}}{d\Omega_{n}dE_{n}} = -\frac{2}{\hbar v_{d}}\rho_{b}(E_{B})\left\langle \Psi_{n}(\vec{k}_{p},\vec{r}_{n};\vec{k}_{d}) \middle| W_{n}\left(\vec{r}_{n}\right) \middle| \Psi_{n}(\vec{k}_{p},\vec{r}_{n};\vec{k}_{d}) \right\rangle$$

. R. Satchler, Direct nuclear reactions (United Kingdom, 1983)

M. Ichimura, N. Austern, and C. M. Vincent, Phys. Rev. C 32, 431 (1985).

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$$\left| \Psi_n(\vec{k}_p, \vec{r}_n; \vec{k}_d) \right\rangle = \left(\tilde{\chi}_p^{(-)}(\vec{k}_p, \vec{r}_p) G_n^{(+)}(\vec{r}_n, \vec{r}_n') \left| v_{pn}(\vec{r}) \right| \chi_d^{(+)}(\vec{k}_d, \vec{R}) \phi_d(\vec{r}) \right\rangle$$

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EMPIRE

To accurately describe the inclusive cross sections, the role of preequilibrium and equilibrium processes should also be taken into account:

Exciton model: preequilibrium emissions

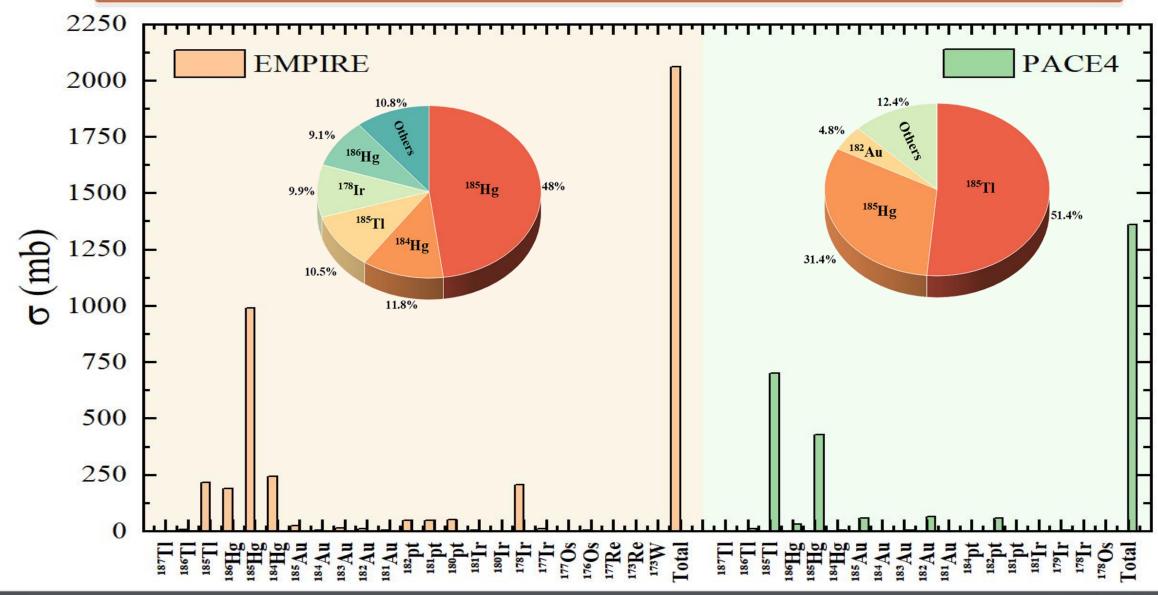
nucleons are emitted before the energy is equally distributed.

The module PCROSS includes the preequilibrium mechanism as defined in the exciton model.

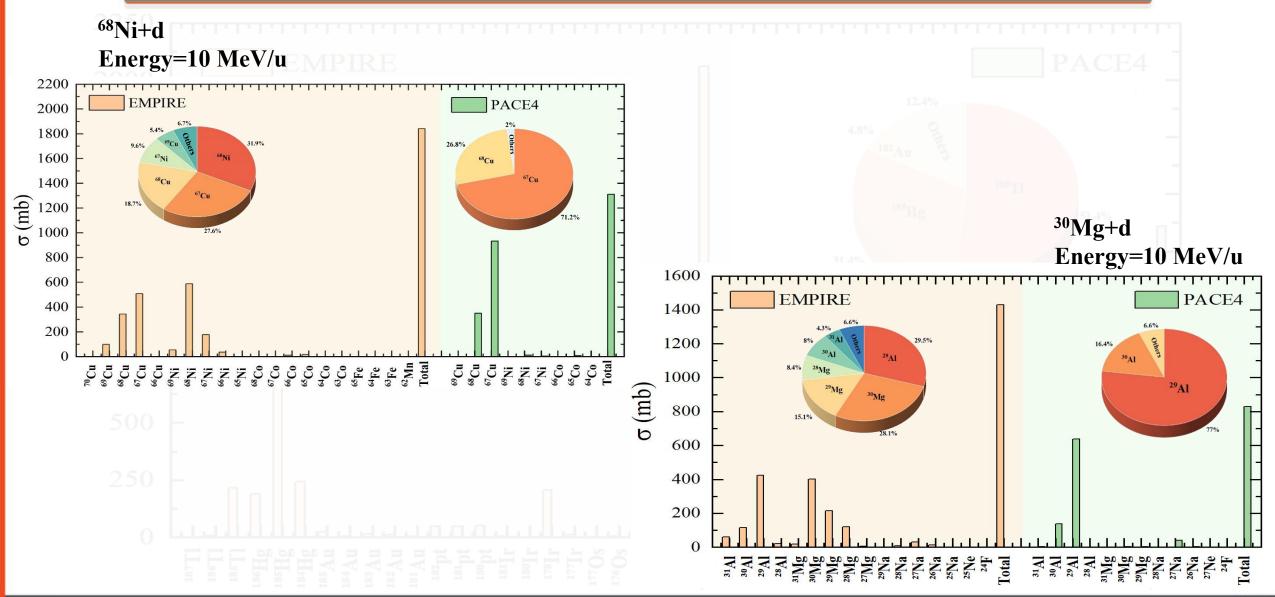
The statistical model: equilibrium emissions

The statistical model used in the EMPIRE is based on the Hauser-Feshbach formalism.

The emission of neutrons, protons, alpha particles, deuterons, tritons, and He-3 is taken into account along with the competing fission channel.



Yields of residual nuclei-EMPIRE, PACE4



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□ EMPIRE:

- Comprehensive nuclear reaction modeling across various projectiles and energy ranges.
- The code accounts for the major nuclear reaction mechanisms, including DWBA-IAV, pre-equilibrium, and compound nucleus, enabling detailed estimation of individual contributions.
- Accounts for the emission of neutrons, protons, deuterons, tritons, He-3, and alpha particles.
- Utilizes an extensive library of input parameters from RIPL-3.
- Requires complex setup and detailed parameter tuning.
- Slower than lightweight codes but highly versatile for diverse reaction types and detailed studies.

☐ PACE4:

- **Evaporation-focused Monte Carlo code** for modelling compound nucleus decay.
- PACE4 is efficient for evaporation-dominated reactions, providing rapid statistical-model calculations with a simplified setup, and is capable of generating approximate angular distributions of evaporation residual nuclei in inverse kinematics.
- Specializes in the emission of neutrons, protons, alpha particles, and gamma rays from the compound nucleus.
- User-friendly, with a straightforward parameter input format.
- Limited in handling complex reaction mechanisms, such as pre-equilibrium processes or direct reactions.

Angular and Energy distributions

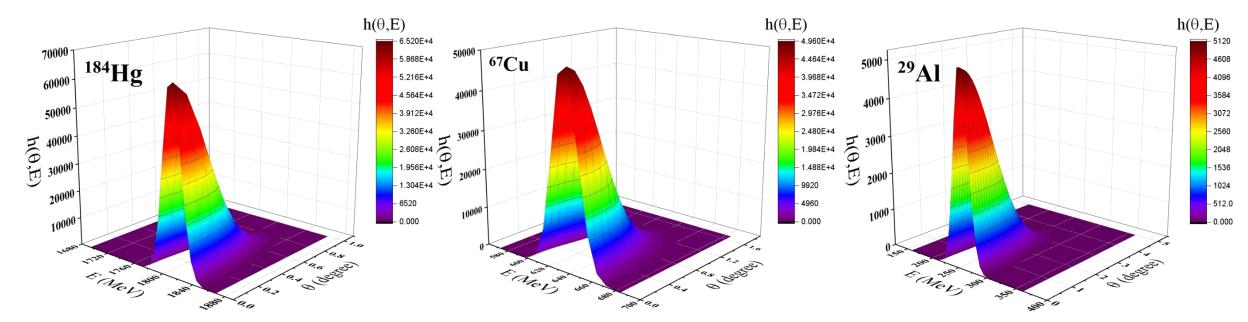
Angular and energy distributions of the residual nuclei were computed for each reaction. These results are used as inputs to beam-dynamics simulations to optimize ISRS performance. To generate these distributions:

- \square *Used PACE4 to simulate angular distributions (strong forward-peaking distributions)* $f(\theta)$.
- □ *Applied Gaussian fits, normalized to EMPIRE cross sections.*
- \square *Fitted energy spectra with normalized Gaussians (as probability distributions) g(E).*
- \square Final distribution: $h(\theta, E) = f(\theta)$. g(E)

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 184 Hg produced in the 185 Hg + d reaction.

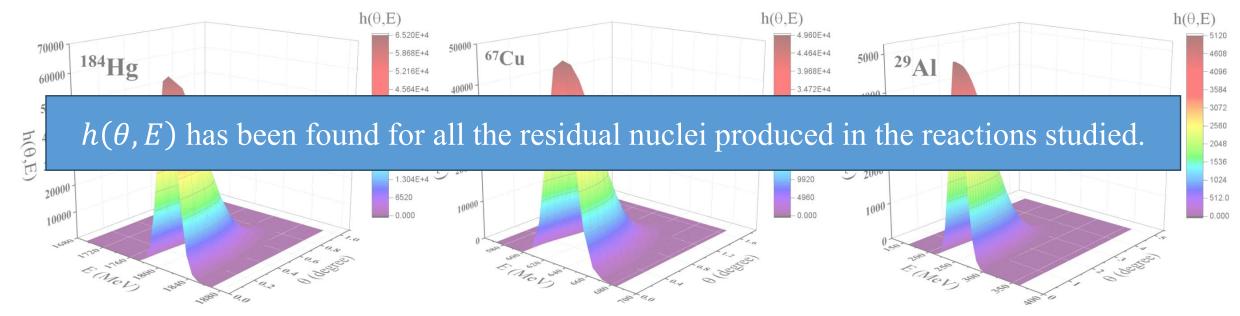
⁶⁷Cu produced in the ⁶⁸Ni + d reaction.

²⁹Al produced in the ³⁰Mg + d reaction.

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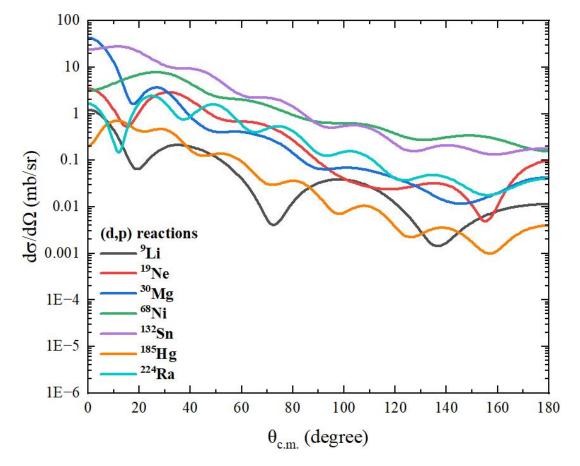


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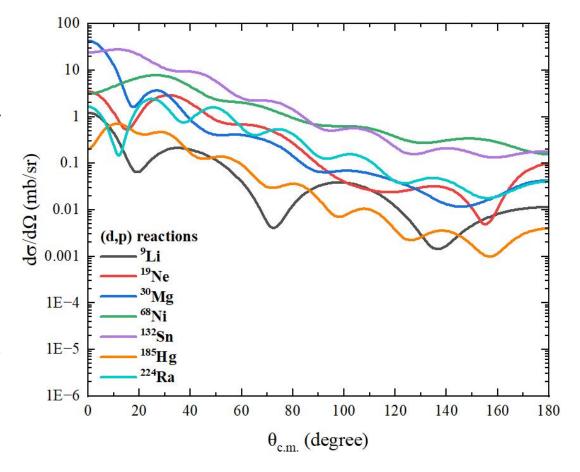
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Studied (d,p) and (d,n) reactions on selected physics cases (⁹Li, ¹⁹Ne, ³⁰Mg, ⁶⁸Ni, ¹³²Sn, ¹⁸⁵Hg, ²²⁴Ra) at 10 MeV/u.



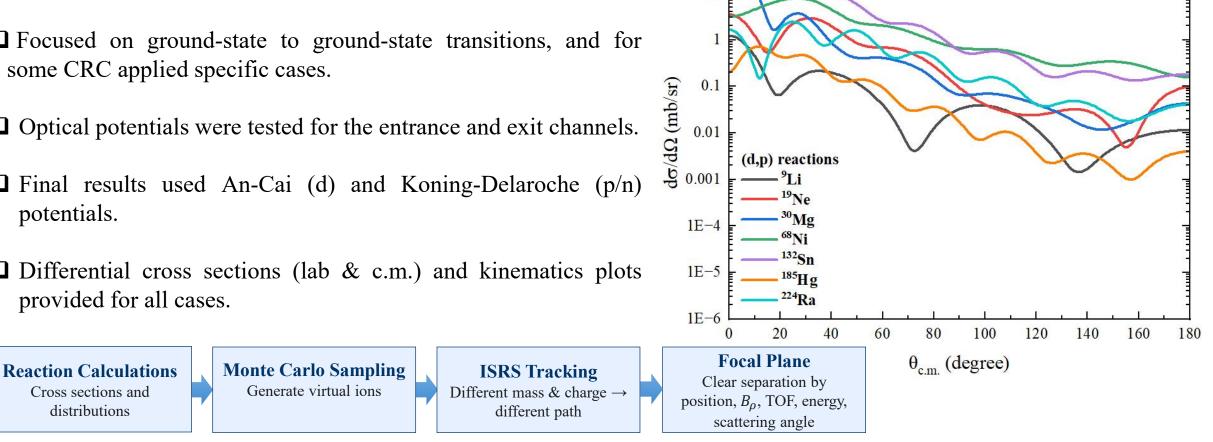
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- ☐ Focused on ground-state to ground-state transitions, and for some CRC applied specific cases.
- ☐ Optical potentials were tested for the entrance and exit channels.
- ☐ Final results used An-Cai (d) and Koning-Delaroche (p/n) potentials.
- ☐ Differential cross sections (lab & c.m.) and kinematics plots provided for all cases.



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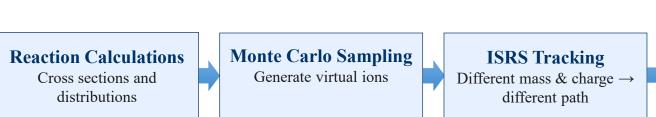


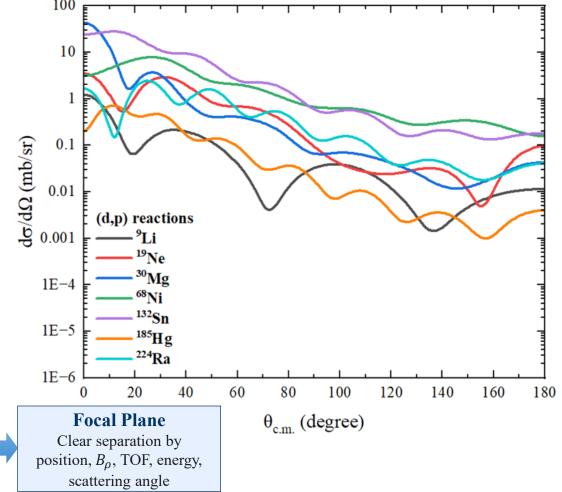
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 19 Ne \implies ion test bench \implies (day 1 experiment).



Summary and outlook

Theoretical Framework

• Integrated workflow using an enhanced version of EMPIRE (DWBA-IAV), PACE4, and FRESCO to produce cross sections and kinematic distributions for selected physics cases.

Residual Nuclei Production

• Residual nuclei were analysed with EMPIRE & PACE4 → Gaussian angular and energy distributions extracted → Exported to beam dynamics simulations → ISRS optimization

Transfer Reaction Studies

• (d,p) and (d,n) reactions investigated with FRESCO \rightarrow Beams: 9 Li, 30 Mg, 68 Ni, 132 Sn, 185 Hg, 224 Ra at 10 MeV/u \rightarrow Results prepared for ISRS beam dynamics simulation

NEXT STEPS: Shape the working physics group

- Our work continues with the expansion of theoretical modelling for reaction analysis, aiming to explore a broader range of physics cases of interest.
- We are establishing the ISRS Physics Working Group to shape the scientific program of the ISOLDE Superconducting Recoil Separator (ISRS) and to incorporate additional physics cases for future analysis. This group will play a central role in developing a focused program of high-precision studies in nuclear structure, astrophysics and reaction dynamics, to be carried out using ISRS.



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https://www.uhu.es/isrs/isrs-physics-working-groups/















Thank you

