

Measurement of the Hoyle State Radius using single and double excitation inelastic scattering

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- **Hoyle state ^{12}C (0_2^+) :**

Resonant state of ^{12}C at 7.65 MeV excitation energy.
Slightly above the 3α threshold ($\sim 0.285\text{keV}$).
Explains the abundance of ^{12}C by considering the 3α process ($\alpha + \alpha \rightarrow {}^8\text{Be}$ & ${}^8\text{Be} + \alpha \rightarrow {}^{12}\text{C} + \gamma$).

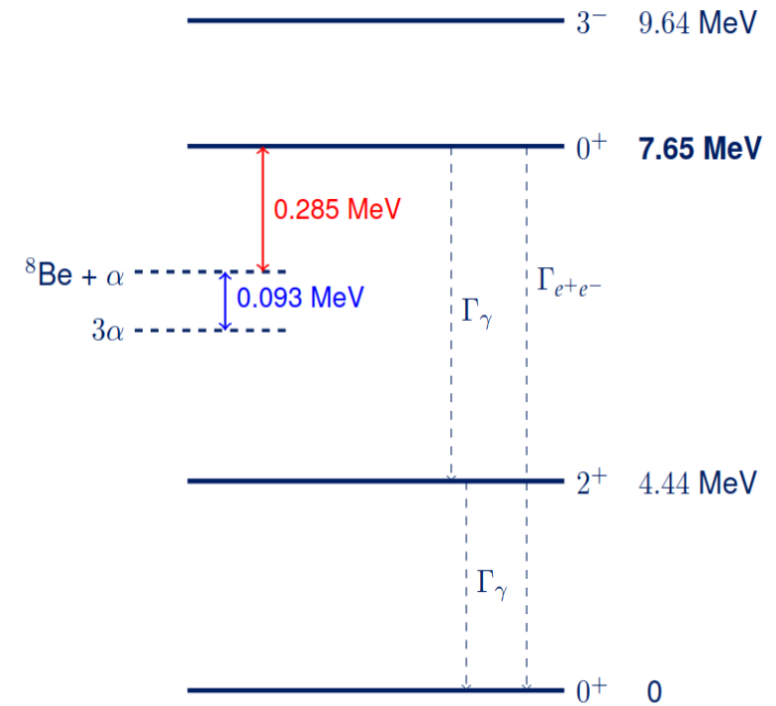
- **Hoyle state Decay :**

→ Sequential Decay : Multi-step decay process
($^{12}\text{C}^* \rightarrow {}^8\text{Be} + \alpha$ & ${}^8\text{Be} \rightarrow \alpha + \alpha$).

→ Direct Decay : Directly to 3α bypassing the ${}^8\text{Be}$ intermediate state ($^{12}\text{C}^* \rightarrow \alpha + \alpha + \alpha$)

→ γ - emission : Transition to 4.44 MeV and then to the ground state.

→ $e^+ - e^-$ production : direct decay to the ground state.



- **Spatial Configuration :**

- Nuclear Lattice EFT [1]:

- Compact structure for the ground state.
 - Obtuse triangle for the Hoyle state.

- Monte Carlo SM [2] :

- Superposition of independent particles and α clusters for the ground state.
 - Compact 3α structure for the Hoyle state.

→ No **consensus** on the Hoyle state **spatial configuration**.

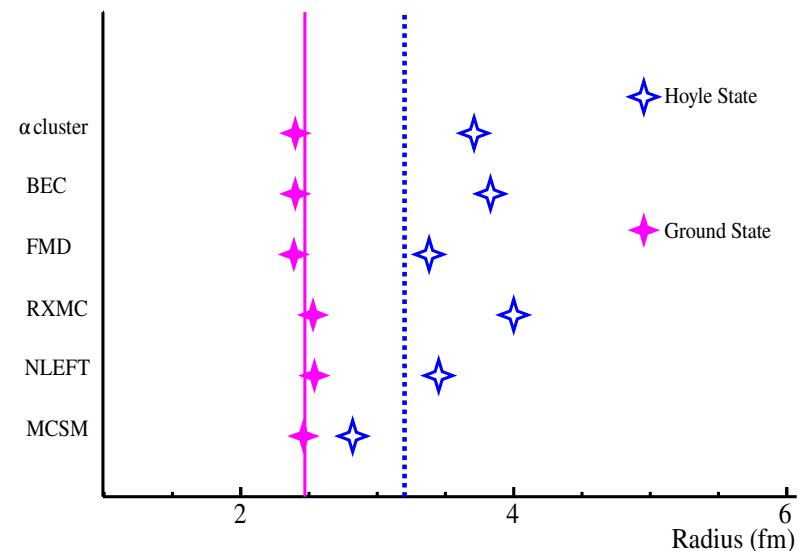
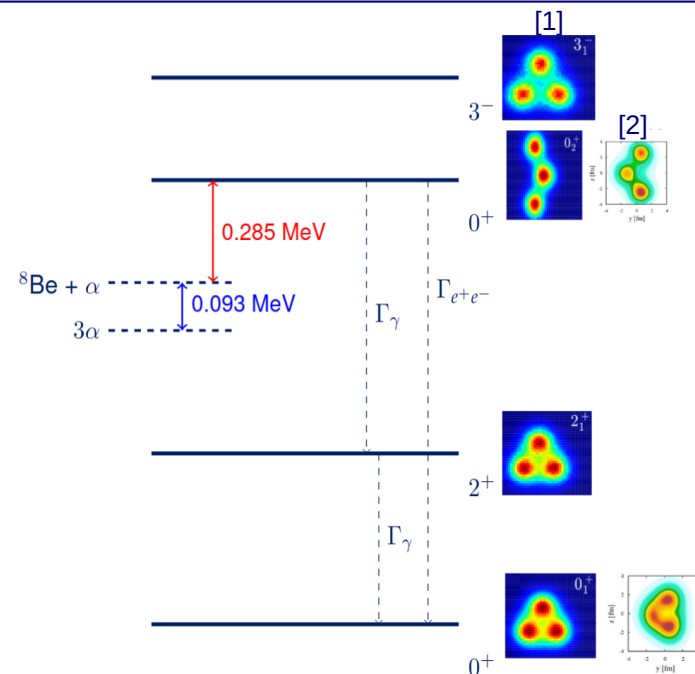
- **Matter Radius :**

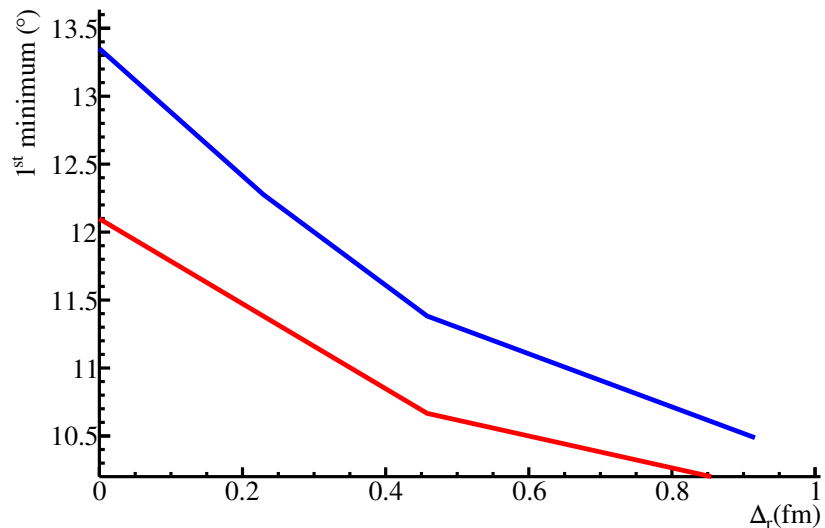
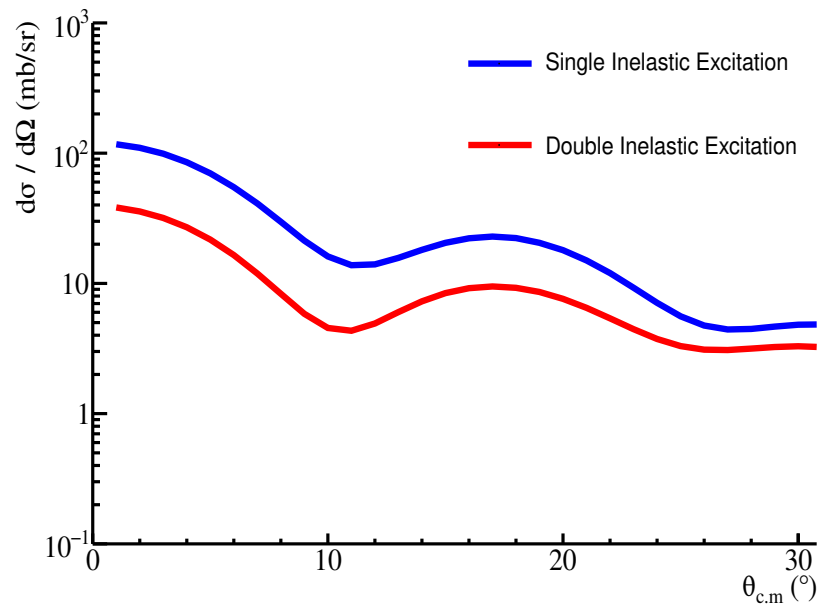
All the theoretical frameworks predict the Hoyle State to be larger than the ground state.
Different models predict different Hoyle state radius values from 2.82 fm to 4 fm.

→ No **consensus** on the Hoyle state **radius** from the theoretical point view

[1] : S. Shen, Nature Com. 14, 2777

[2] : T. Otsuka et al., Nature Com. 13, 2234





➤ How can we measure the Hoyle state radius ?

• **Theoretical Calculations :**

Coupled channel calculations performed for $^{12}\text{C} + ^{12}\text{C}$ at 100 MeV.

Single- and Double-excitation inelastic scattering of the Hoyle state computed with CHUCK3 code by varying the difference between the ground and Hoyle states radii $\Delta_r = 0 - 0.92\text{fm}$.

• **Observable sensitivity to the Hoyle state radius :**

The position of the first and second minima decreases with Δ_r increasing.

➔ **Single- and Double- excitation inelastic cross sections** show a **sensitivity** to the Hoyle state radius.

➤ How can we measure these cross sections ?

• **Experimental Framework :**

A ^{12}C target was irradiated with a ^{12}C beam at an energy of 8.81 MeV/A at GANIL in April 2025.

The diffused ^{12}C or three α particles resulting from the decay of the projectile-like are detected using the FAZIA detector placed at 2° to 13.6° .

- ➔ Process 1 : ^{12}C is diffused without decaying into 3α .
- ➔ Process 2 : ^{12}C decays into 3α .

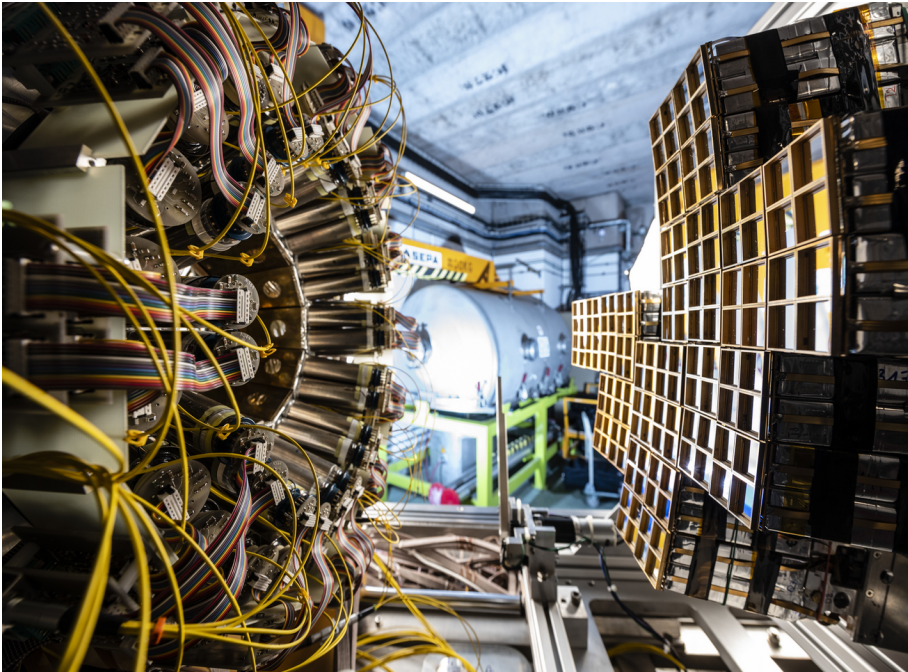
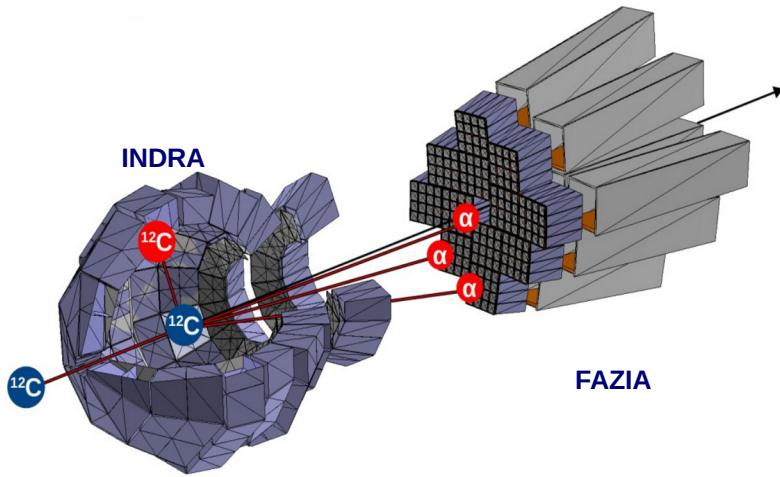
• **FAZIA :**

12 blocks consisting of 16 three stages telescopes ($2 \times 2 \text{ cm}^2$)

- ➔ Si1 (300 μm), Si2 (500 μm) and CsI (10 cm)

Allows for the use of multiple identification methods :

- ➔ PSA (Pulse Shape Analysis)
- ➔ $\Delta E - E$ method



- **Pulse Shape Analysis:**

Ions with different charge or mass exhibit different energy loss profiles.

Use the shape of the signal collected to identify charge Z and mass A .

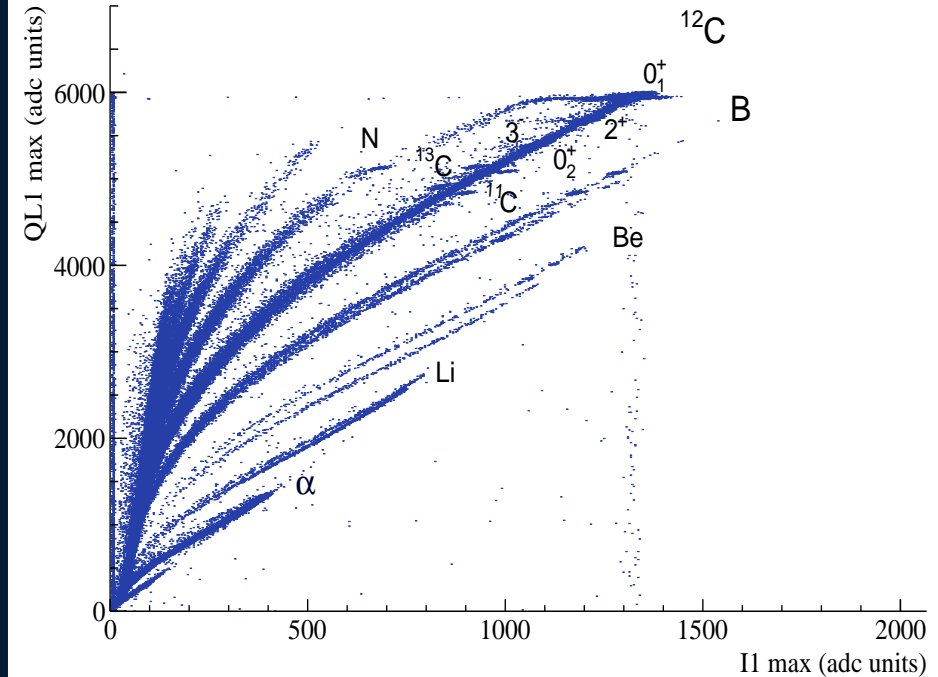
- **Particles stopped in Si1 :**

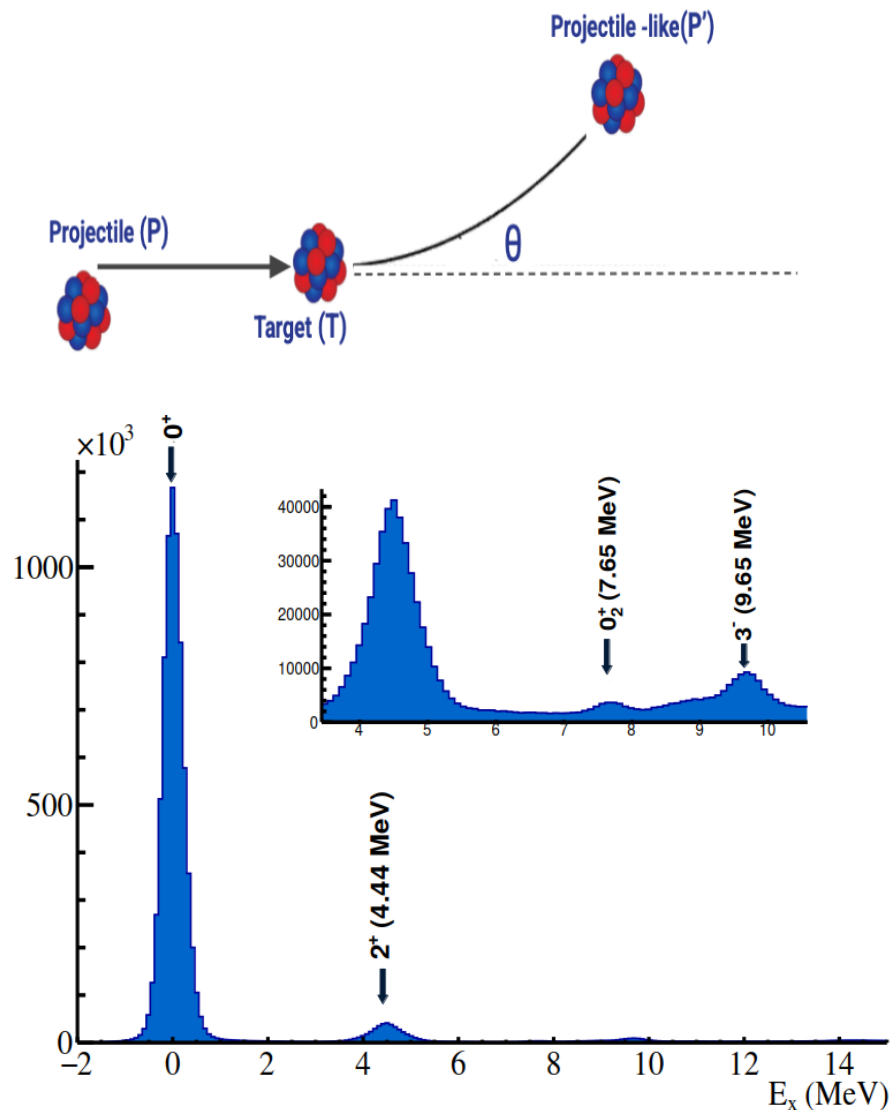
PSA : Correlation of the total collected charge (QL1 max proportional to the deposited energy) to the maximum current (I max).

Each line corresponds to the different particles charge and mass.

- Charge identification up to $Z \sim 9$.
- Isotopic Identification up to $Z \sim 6$.

On the line corresponding to ^{12}C : We can also spot the elastic peak + some excited states (2^+ , 0_2^+ , 3^-).





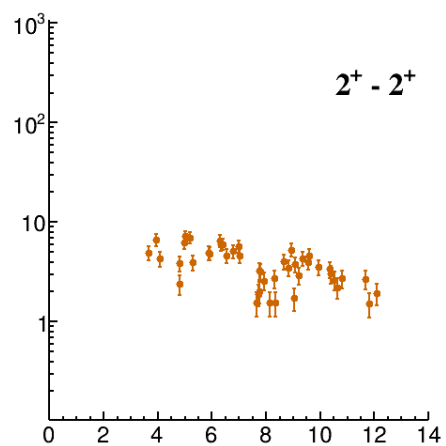
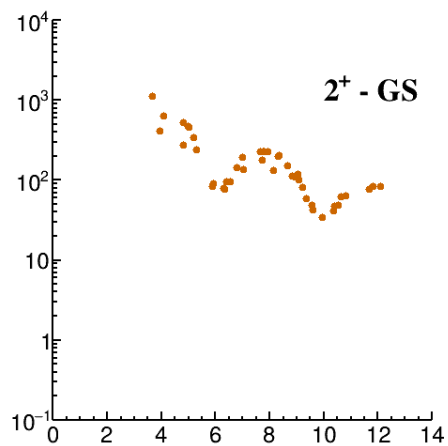
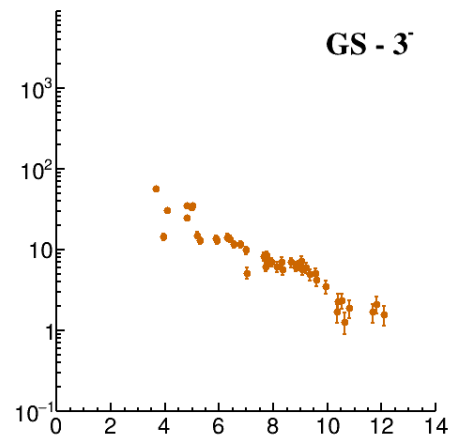
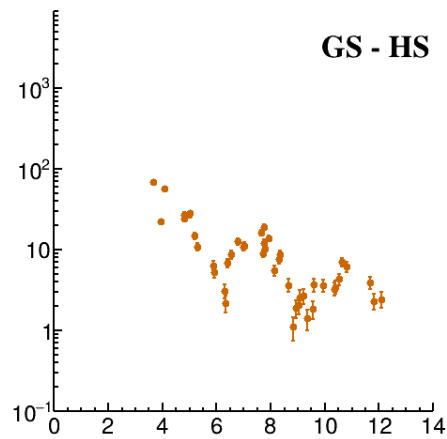
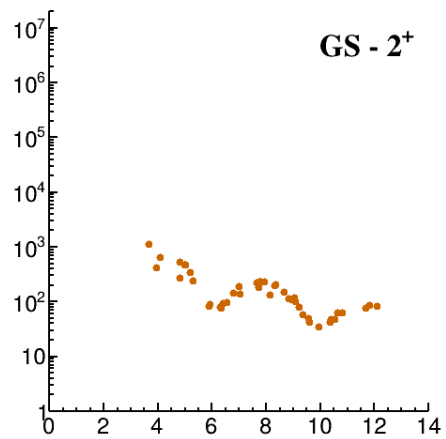
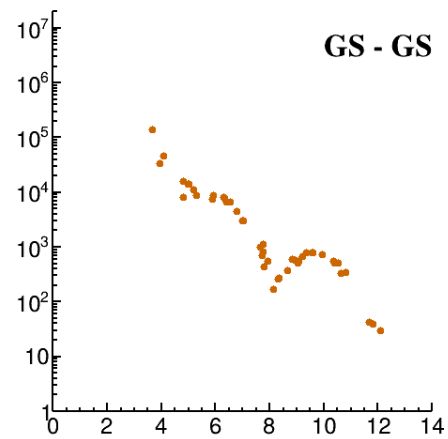
- **Direct missing mass :**

Non decaying projectile-like ^{12}C are directly detected in the first stage Si1.

Using 2-body kinematics, we reconstruct the dissipated energy.

- Probe projectile-like excited states **below** the particle emission threshold.
- Cross sections of multiple inelastic channels are extracted and evaluated to compare with theoretical models.

$d\sigma / d\Omega$ (mb / sr)



$\theta_{lab} (^\circ)$

➤ **What if the projectile-like decays ?**

• **Invariant mass :**

Employ the invariant mass method on the detected 3α to extract the projectile-like properties.

➔ **Projectile-like** excitation energy can be extracted.

• **Indirect missing mass :**

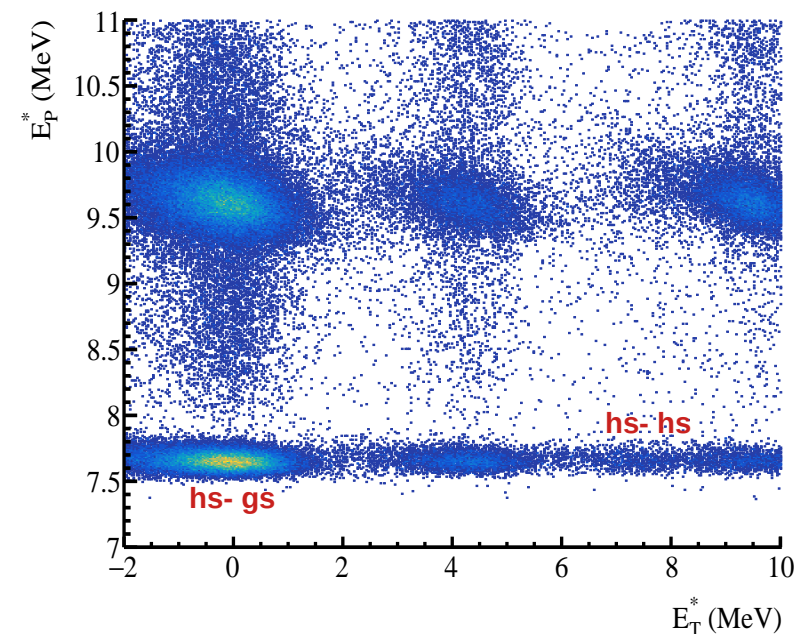
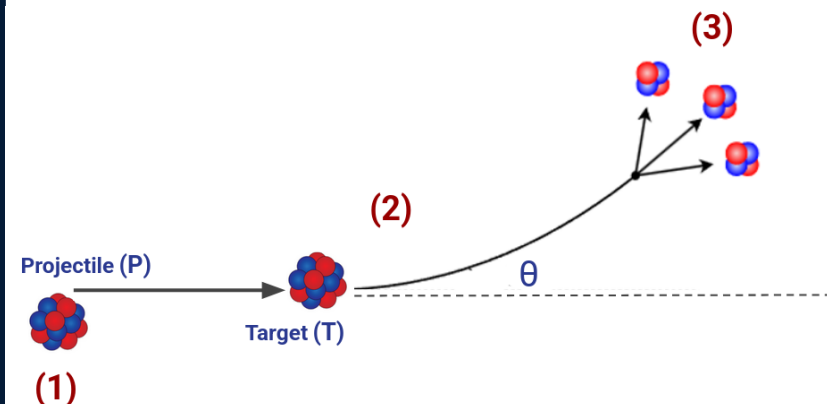
Apply the missing mass technique on the reconstructed $^{12}\text{C}^*$ to determine the excitation energy of the target-like.

➔ **Target-like** excitation energy can be extracted.

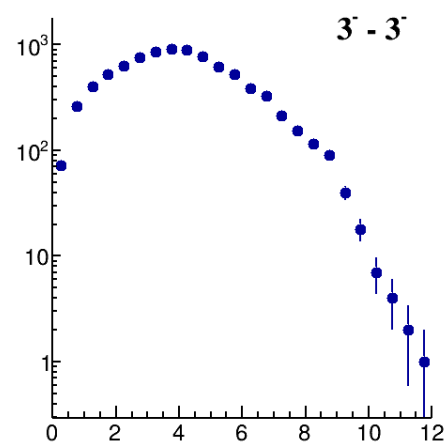
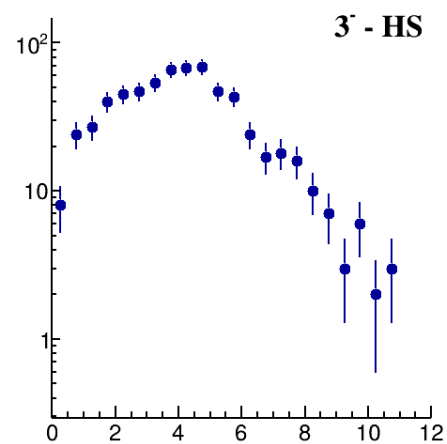
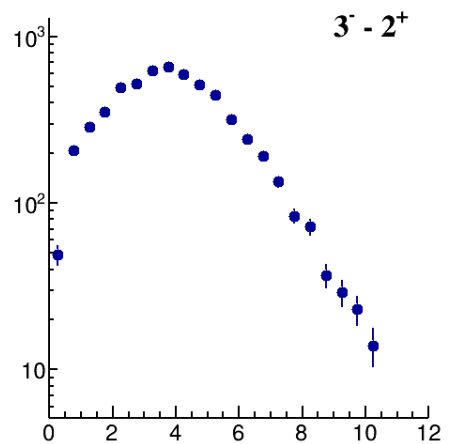
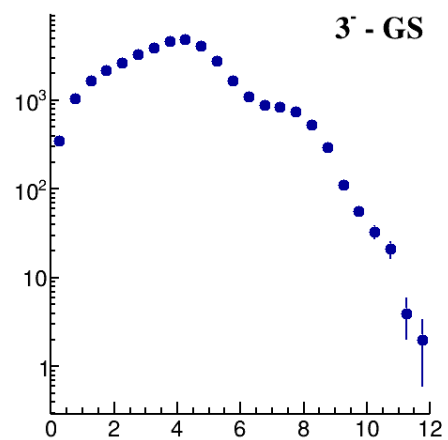
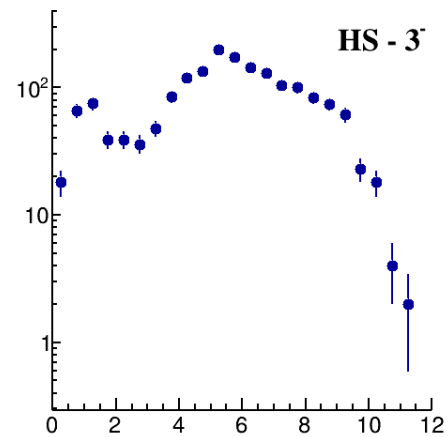
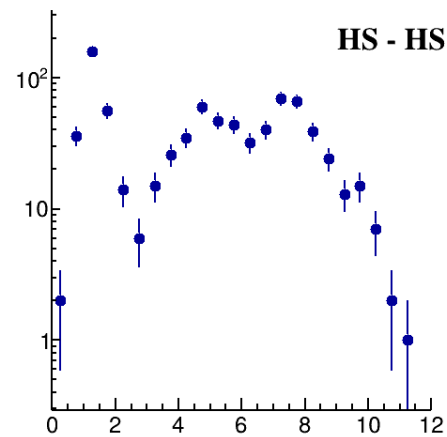
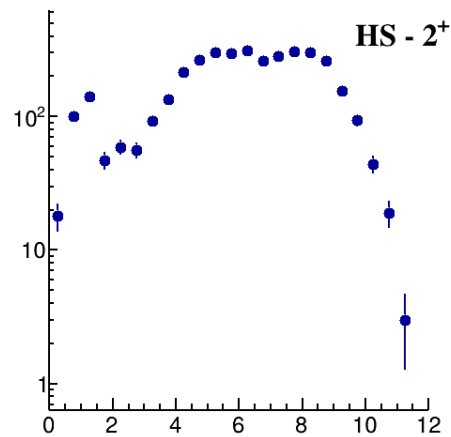
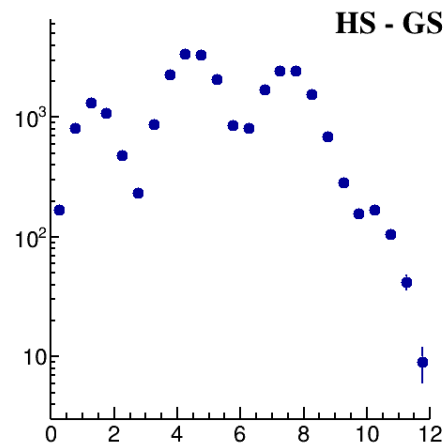
• **Projectile-Target Channels :**

Multiple channels such as the HS - GS ,
HS – HS, 3^- - GS, 3^- - GS ... ,

➔ Extract the angular distribution corresponding to each (Projectile-like – Target-like) reaction channel.



dN (no corr, no norm)



$\theta (^{\circ})$

- **Experimental Output :**

- Angular distribution for (almost) all combination of projectile and target excitation.

- **2⁻ - HS**, and **2⁻ - 3⁻** angular distributions can be obtained soon.

- **Next steps :**

- Efficiency correction and normalization for the indirect missing mass channels (blue).

- Theoretical calculations can be conducted using these angular distributions as an input.

