

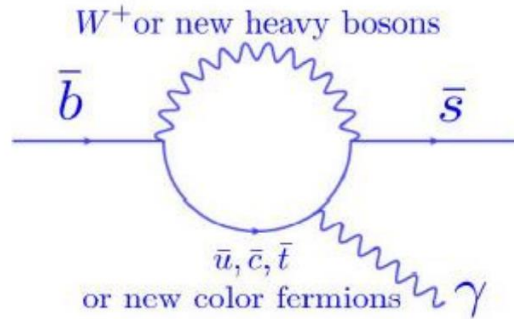


# Measurement of time-dependent CP asymmetry using $B^0 \rightarrow K_S^0 \pi^+ \pi^- \gamma$ decays in Belle II

---

Petros Stavroulakis, on behalf of the IPHC Strasbourg Belle II group  
GDR-InF annual workshop at Mont Sainte-Odile, November 8<sup>th</sup> 2023

# Photon polarization in $b \rightarrow s \gamma$



- In the Standard Model (SM) the polarization of the photon in  $b \rightarrow s \gamma$  transitions is predominantly left-handed but New Physics (NP) may modify this
  - Atwood et al., Phys. Rev. Lett. 79, 185
  - E. Kou et al., JHEP 12 (2013) 102 [1305.3173]
  - N. Haba et al., JHEP 03 (2015) 160 [1501.00668]
- This polarization can be tested through a measurement of the time-dependent CP asymmetry of  $B \rightarrow K_{\text{res}} \gamma$  decays

$$\mathcal{M} \simeq -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} [(C_{7\gamma}^{SM} + C_{7\gamma}^{NP}) \langle \mathcal{O}_{7\gamma} \rangle + C_{7\gamma}'^{NP} \langle \mathcal{O}'_{7\gamma} \rangle]$$

# TDCP asymmetry of $B^0 \rightarrow K_{res}\gamma \rightarrow K_S^0\pi^+\pi^-\gamma$ decays

$$\mathcal{A}_{CP}(\Delta t) = \frac{\Gamma(B_{\text{tag}=\bar{B}^0}(\Delta t) \rightarrow f_{CP}) - \Gamma(B_{\text{tag}=B^0}(\Delta t) \rightarrow f_{CP})}{\Gamma(B_{\text{tag}=\bar{B}^0}(\Delta t) \rightarrow f_{CP}) + \Gamma(B_{\text{tag}=B^0}(\Delta t) \rightarrow f_{CP})} = \mathbf{S} \cdot \sin(\Delta m_d \Delta t) - \mathbf{C} \cdot \cos(\Delta m_d \Delta t)$$

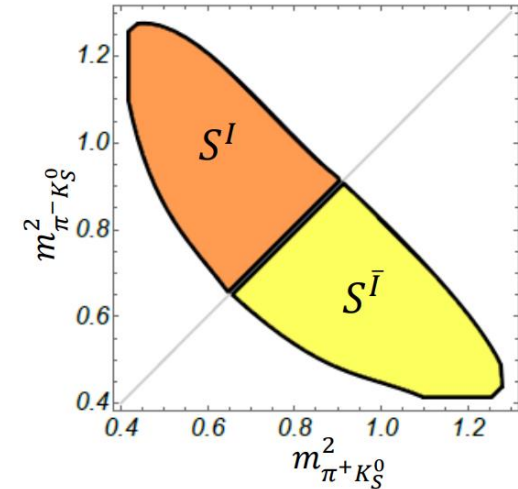
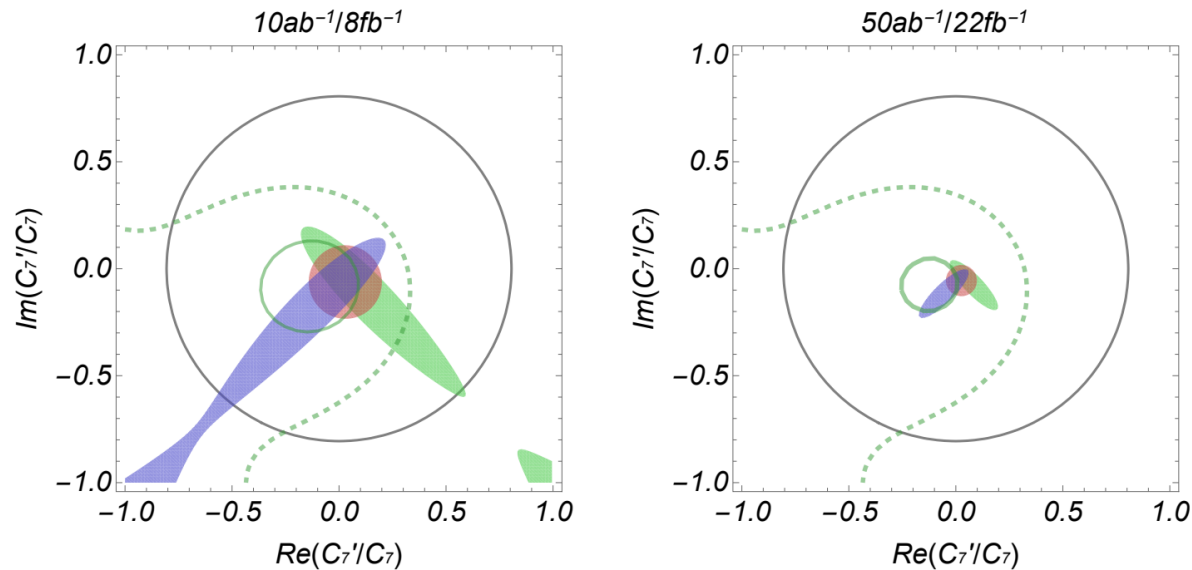
- We are interested in measuring  $\mathbf{S}$  of the CP-eigenstate:  $B^0 \rightarrow K_{res}\gamma \rightarrow K_S^0\rho^0\gamma \rightarrow K_S^0\pi^+\pi^-\gamma$
- A dilution factor is needed to properly account for non-CP-eigenstates resulting from various interfering kaonic resonances:

$$\mathcal{D} = \frac{S_{K_S^0\pi^+\pi^-\gamma}}{S_{K_S^0\rho^0\gamma}}$$

- Previous measurements:
  - [BaBar PRD93 \(2015\)](#):  $S_{K_S^0\pi^+\pi^-\gamma} = 0.14 \pm 0.25 \pm 0.03$  (using  $471 \times 10^6 B\bar{B}$  pairs)
  - [Belle PRL101 \(2008\)](#):  $S_{K_S^0\pi^+\pi^-\gamma} = 0.09 \pm 0.27 \pm 0.07$  (using  $657 \times 10^6 B\bar{B}$  pairs)
- We plan to do a combined measurement using the entire Belle ( $711 \text{ fb}^{-1}$ ) and current Belle II datasets ( $362 \text{ fb}^{-1}$ )

# New constraints on $C_7$

- Work by *S. Akar, et al.*, proposes new observables by dividing the dataset in the Dalitz-plane
- The two new observables will provide orthogonal constraints to the real and imaginary parts of  $C_7'/C_7$  in the complex plane

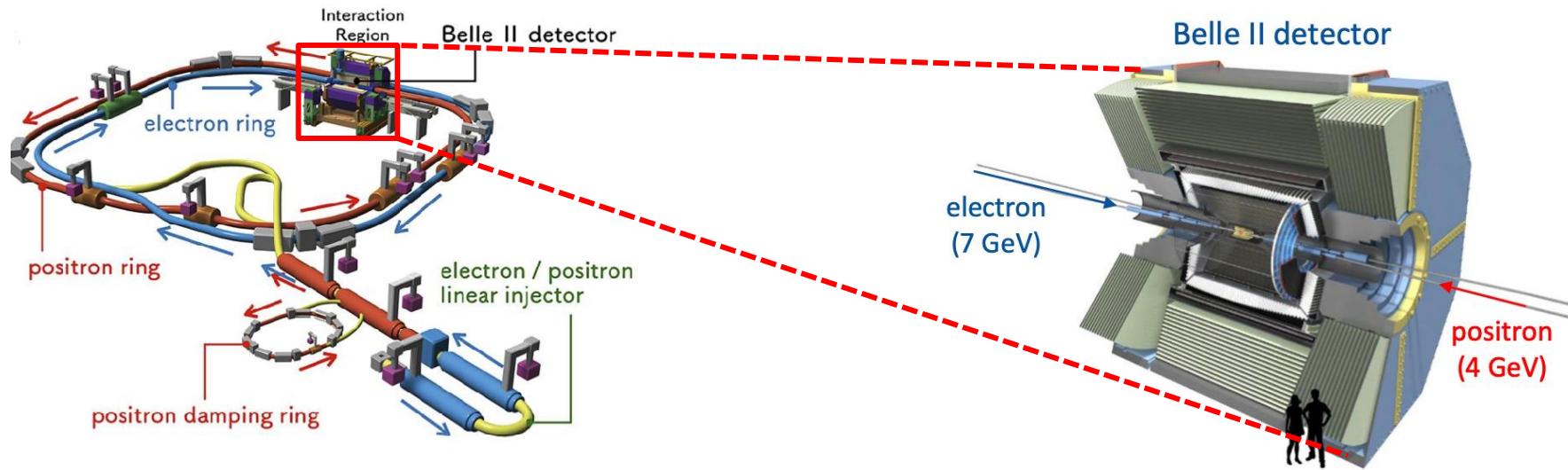


- New observables:

$$S_{K_S^0 \rho^0 \gamma}^+ = S^I + S^{\bar{I}}$$

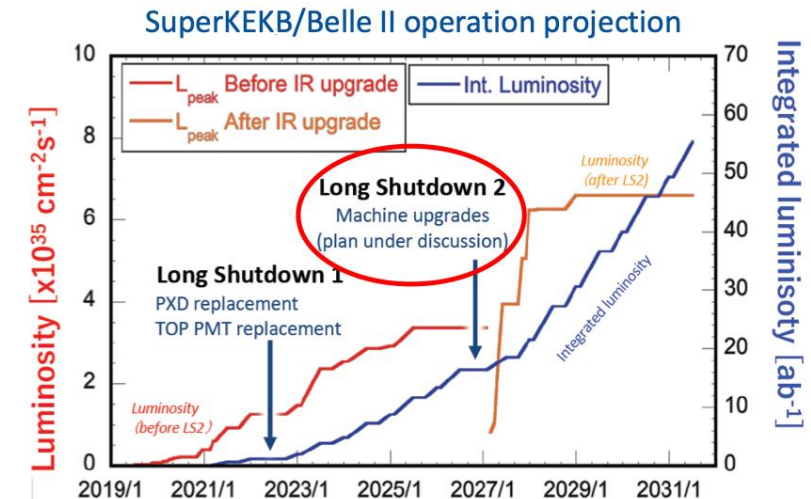
$$S_{K_S^0 \rho^0 \gamma}^- = S^I - S^{\bar{I}}$$

# SuperKEKB & Belle II

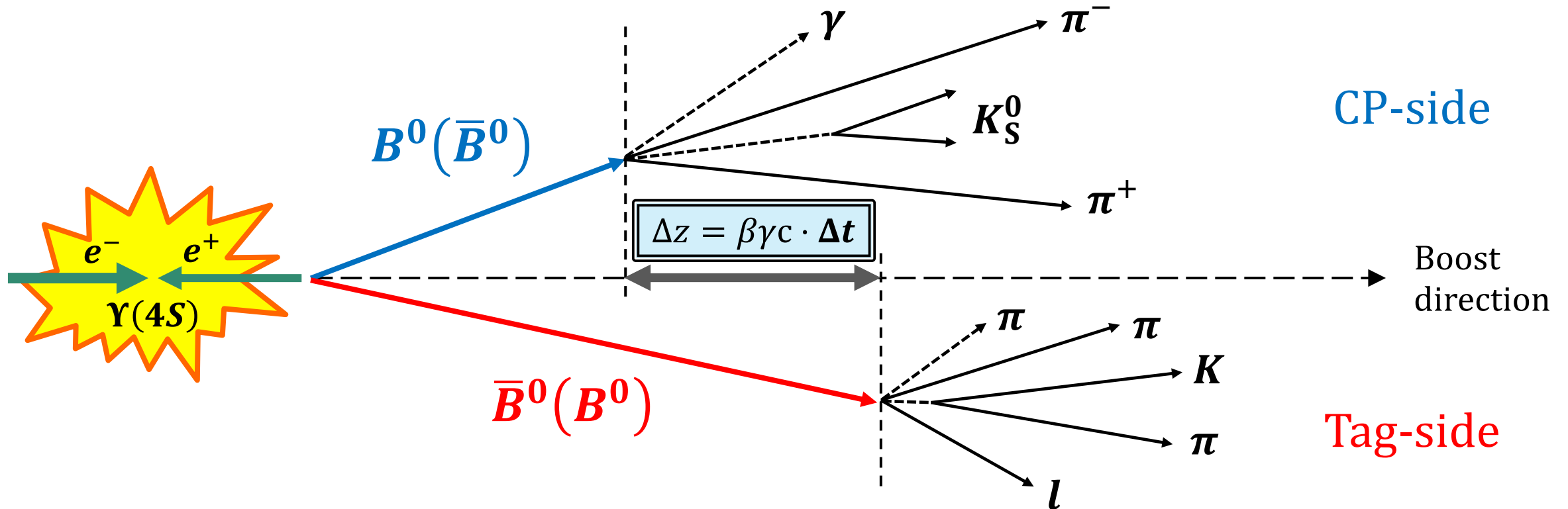


## ➤ SuperKEKB: the “brightest” $e^+e^-$ collider:

- Current peak instantaneous luminosity:  $4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$  (WR)
- Target instantaneous luminosity:  $6 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$  ( $\sim 30$  times larger than at KEKB) achieved by **nano-beam scheme**
- Already at  $427 \text{ fb}^{-1} \approx \text{BaBar dataset}$



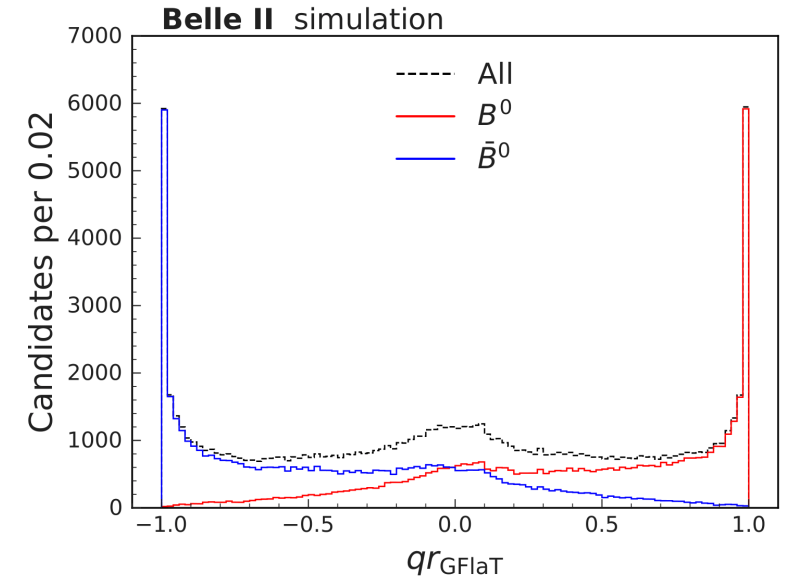
# Event Reconstruction



- After fully reconstructing and vertexing the CP-side B candidate, the tracks from the rest of the event are used to vertex the tag-side  $\Rightarrow \Delta t$  measured indirectly using vertex positions
- Then the **Flavor Tagger** is run on the rest of the event to determine the  $B$  flavor at the time of decay

# Flavor Tagging at Belle II

- $B$  flavor currently estimated with a BDT classifier based on individual flavor estimators (i.e. high- $p_T$  leptons, Kaons, etc.)
- The **Flavor Tagger** provides the tag- $B$  flavor  $q = \pm 1$  and a confidence factor  $r = 1 - 2w$ , where  $w$  is the mistag fraction
- 7 intervals of  $r$ : [0.0, 0.1, 0.25, 0.45, 0.6, 0.725, 0.875, 1.0] with the last bin corresponding to best flavor assignment
- Ongoing development to improve the Flavor Tagger based on deep learning techniques
- Expected improvement on statistical uncertainty of  $S$ :  $\sim 10\%$



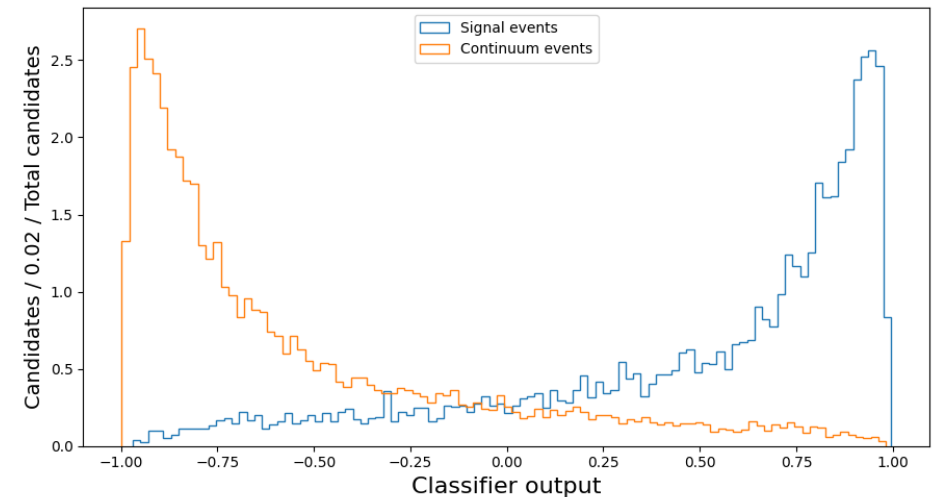
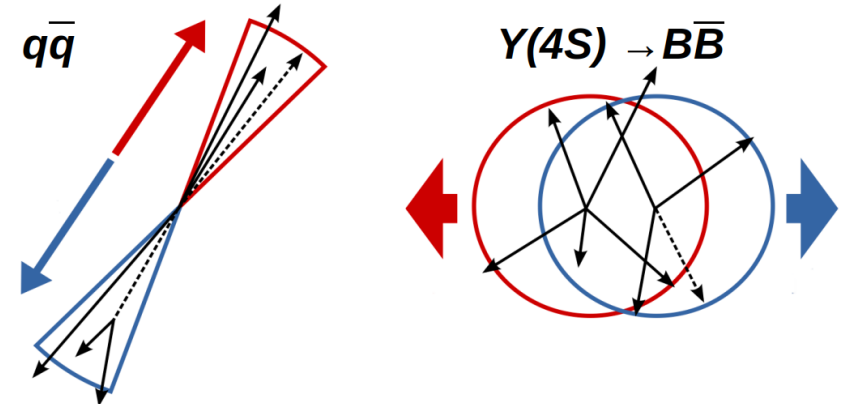
$r$ -bin	$w(\%)$	$\Delta w(\%)$	$\mu(\%)$
0	48.29	0.78	-1.72
1	42.07	-1.41	-0.94
2	34.63	-0.04	-0.28
3	24.17	1.64	3.21
4	16.98	1.36	1.17
5	11.50	-0.26	-1.13
6	2.62	0.75	-0.18

Calibrated Flavor Tagger parameters using  $362 \text{ fb}^{-1}$  data

# Continuum Suppression

- Most dominant source of background is due to non-resonant  $e^+e^- \rightarrow q\bar{q}$  events, with  $q \in \{u, d, c, s\}$
- Has a jet-like topology as opposed to  $\Upsilon(4S) \rightarrow B\bar{B}$  events which have a spherically symmetric topology
- Train a BDT classifier to suppress continuum background using event-shape variables as inputs:
  - Cosine of the angle between the thrust axes of the event
  - Cosine of the  $B$ -momentum polar angle in the CMS
  - Fox-Wolfram moments

$$H_l = \sum_{i,j} \frac{|p_i||p_j|}{E_{\text{event}}^2} P_l(\cos\theta_{i,j})$$





# Selection Criteria

## ➤ Pre-selection:

- $1.4 < E_\gamma < 4$  GeV
- Loose event-level cuts regarding no. of tracks & calorimeter clusters
- Rest-of-Event (RoE) cuts to remove tracks & clusters due to beam background

## ➤ Additional selections:

- $\pi^0$  likeness of photon  $< 0.7$
- Prompt  $\pi^\pm$  pionID  $> 0.1$
- $M_{K_S\pi\pi} < 1.8$  GeV/c<sup>2</sup>
- $0.6 < M_{\pi\pi} < 0.9$  GeV/c<sup>2</sup> ( $\rho$  mass window)
- “ $K_S$  selector” MVA classifier  $> 0.95$  (optimised)
- Continuum Suppression MVA classifier  $> 0.28$  (optimised)
- Single Candidate Selection (random)

Cut	Signal Efficiency (%)
$\pi^\pm$ pionID $> 0.1$	91.6 (91.6)
$\pi^0$ likeness $< 0.7$	80.8 (74.0)
$M_{K_S\pi\pi} < 1.8$	78.9 (58.4)
$0.6 < M_{\pi\pi} < 0.9$	52.6 (30.7)
$K_S$ MVA $> 0.95$	92.0 (28.3)
CSMVA $> 0.28$	73.1 (20.7)
Single Candidate	84.1 (17.4)

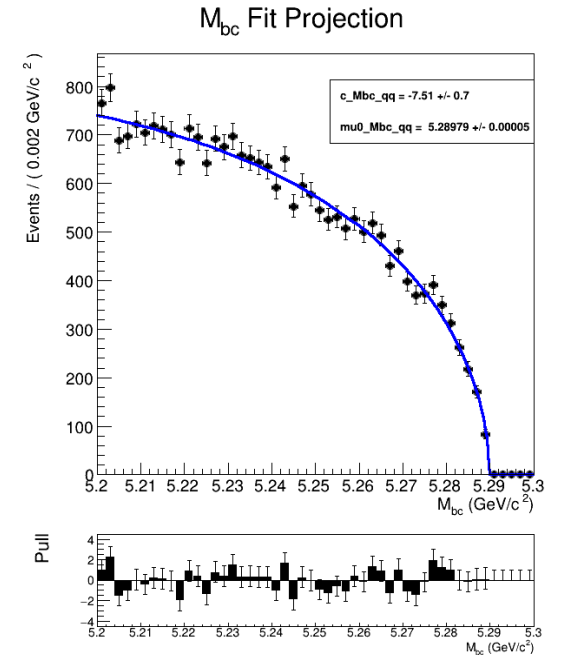
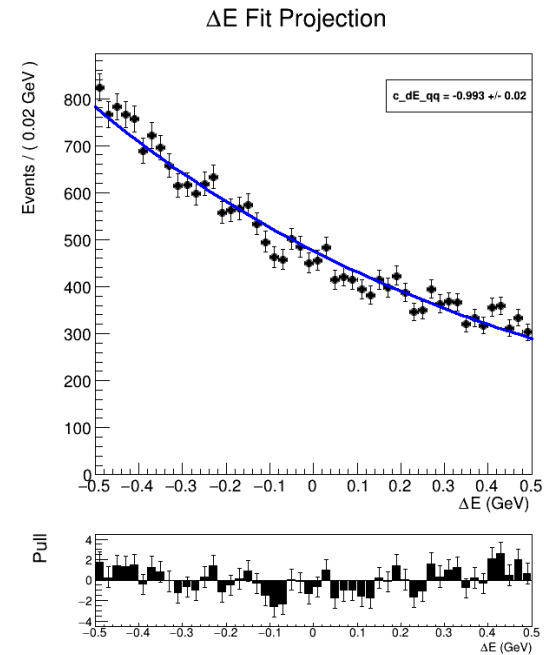
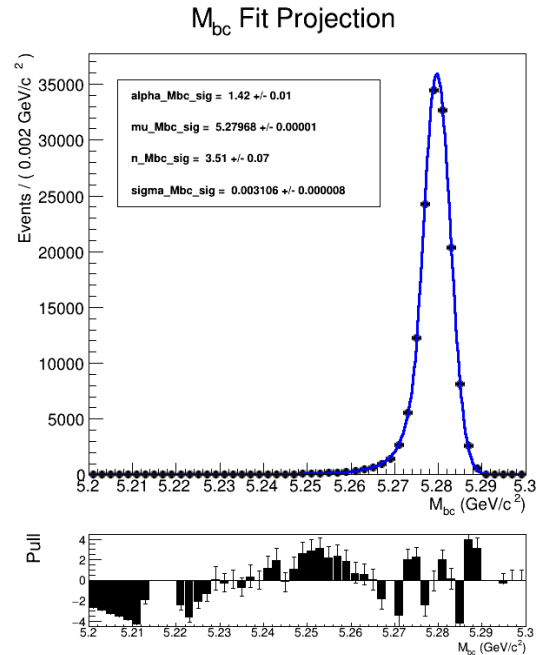
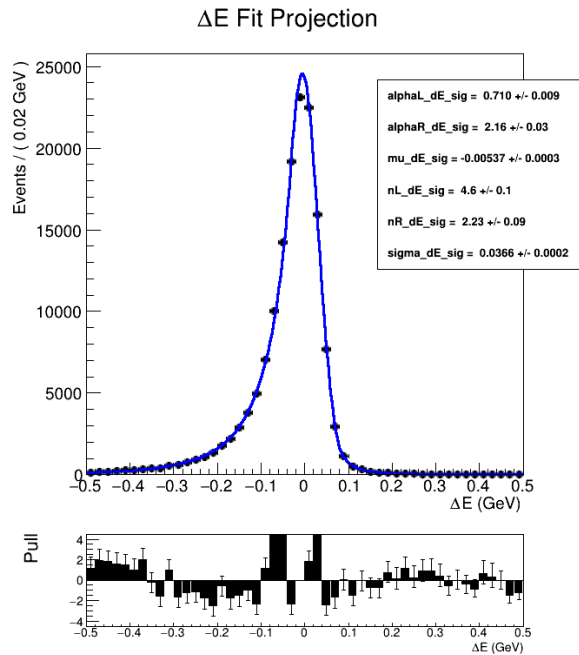
\*cumulative efficiencies in parentheses

# Fit Strategy

- Four separate fit components: signal, self crossfeed (SCF), continuum and  $B\bar{B}$  background → shape parameters of fit components obtained from fit to simulated  $M_{bc}$  and  $\Delta E$  distributions
- $\Delta t$  resolution model parameters determined from fit to  $\Delta t$  residual distribution of pure signal MC sample (more details on this shortly)
- Signal and background yields extracted via a 2D fit to  $M_{bc}$  and  $\Delta E$
- Subtract background in  $\Delta t$  using *sPlot* [[arxiv.org/abs/physics/0402083](https://arxiv.org/abs/physics/0402083)] and then fit resulting  $\Delta t$  distribution for  $S$  and  $C$

$$M_{bc} = \sqrt{E_{\text{beam}}/2^2 - p_B^{*2}}$$
$$\Delta E = E_B^* - \sqrt{s}/2$$

# Shape parameters extraction



## Signal:

- $\Delta E$  : Double-sided Crystal Ball
- $M_{bc}$  : Crystal Ball

## Continuum:

- $\Delta E$  : Exponential
- $M_{bc}$  : Argus

# $\Delta t$ Model

➤ The signal  $\Delta t$  model can be written as:

$$\mathcal{P}(\Delta t, q = \pm 1) = \frac{e^{-|\Delta t|/\tau_{B0}}}{2\tau_{B0}} \{1 - q\Delta w + q\mu(1 - 2w) +$$
$$+ [q(1 - 2w) + \mu(1 - q\Delta w)][\mathbf{S} \sin(\Delta m_d \Delta t) - \mathbf{C} \cos(\Delta m_d \Delta t)]\} \otimes \mathcal{R}_{\text{det}}$$

# $\Delta t$ Model

➤ The signal  $\Delta t$  model can be written as:

$$\mathcal{P}(\Delta t, q = \pm 1) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{2\tau_{B^0}} \{1 - q\Delta w + q\mu(1 - 2w) +$$
$$+ [q(1 - 2w) + \mu(1 - q\Delta w)] [\mathbf{S} \sin(\Delta m_d \Delta t) - \mathbf{C} \cos(\Delta m_d \Delta t)]\} \otimes \mathcal{R}_{\text{det}}$$

CP violation parameters

# $\Delta t$ Model

➤ The signal  $\Delta t$  model can be written as:

$$\mathcal{P}(\Delta t, q = \pm 1) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{2\tau_{B^0}} \left\{ 1 - \boxed{q\Delta w + q\mu(1 - 2w)} + \right. \\ \left. + \boxed{q(1 - 2w) + \mu(1 - q\Delta w)} \left[ \mathcal{S} \sin(\Delta m_d \Delta t) - \mathcal{C} \cos(\Delta m_d \Delta t) \right] \right\} \otimes \mathcal{R}_{\text{det}}$$

Flavor Tagger parameters

# $\Delta t$ Model

➤ The signal  $\Delta t$  model can be written as:

$$\mathcal{P}(\Delta t, q = \pm 1) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{2\tau_{B^0}} \{1 - q\Delta w + q\mu(1 - 2w) +$$
$$+ [q(1 - 2w) + \mu(1 - q\Delta w)][\mathcal{S} \sin(\Delta m_d \Delta t) - \mathcal{C} \cos(\Delta m_d \Delta t)]\} \otimes \mathcal{R}_{\text{det}}$$

where  $\mathcal{R}_{\text{det}}$  is the  $\Delta t$  resolution function, which models smearing effects due to the finite resolution of the detector in measuring the CP-side and tag-side  $B$  vertex positions, which are used to determine  $\Delta t$

# $\Delta t$ Model

➤ The signal  $\Delta t$  model can be written as:

$$\mathcal{P}(\Delta t, q = \pm 1) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{2\tau_{B^0}} \{1 - q\Delta w + q\mu(1 - 2w) + [q(1 - 2w) + \mu(1 - q\Delta w)][\mathcal{S} \sin(\Delta m_d \Delta t) - \mathcal{C} \cos(\Delta m_d \Delta t)]\} \otimes \mathcal{R}_{\text{det}}$$

where  $\mathcal{R}_{\text{det}}$  is the  $\Delta t$  resolution function, which models smearing effects due to the finite resolution of the detector in measuring the CP-side and tag-side  $B$  vertex positions, which are used to determine  $\Delta t$

➤ Similar model for  $\mathcal{R}_{\text{det}}$  to the one used in BaBar to account for detector resolution effects:

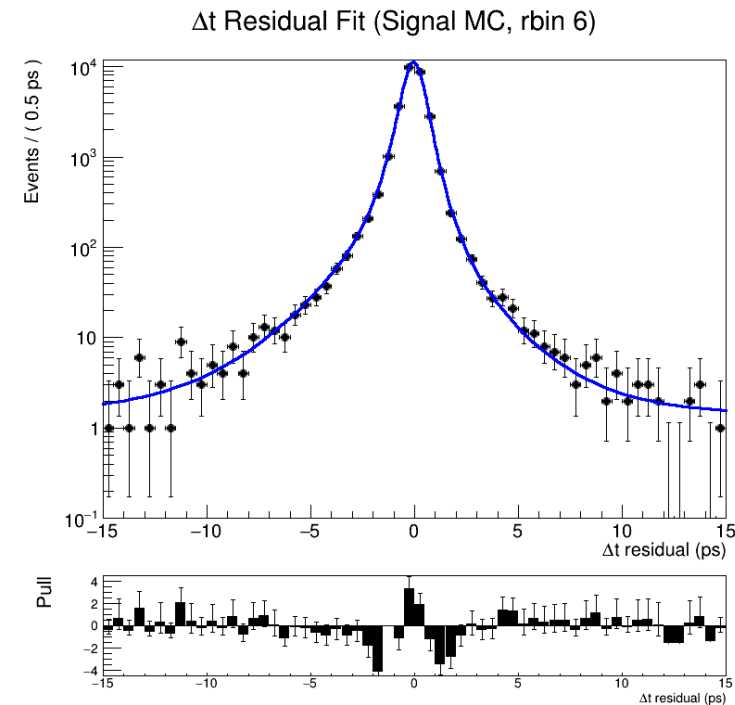
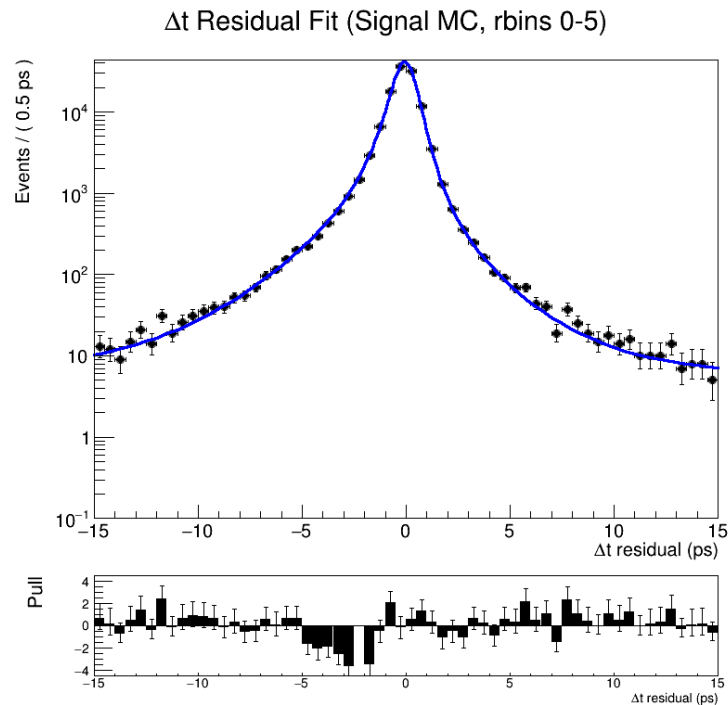
$$\mathcal{R}(\delta\Delta t; \sigma) = (1 - f_{\text{OL}})\mathcal{R}_{\text{core}}(\delta\Delta t; \sigma) + f_{\text{OL}}\mathcal{R}_{\text{OL}}(\delta\Delta t; \sigma)$$

$$\begin{aligned} \mathcal{R}_{\text{core}}(\delta\Delta t; \sigma) = & (1 - f_{\text{tail}}) \cdot G(\delta\Delta t; \mu_{\text{main}} \cdot \sigma, s_{\text{main}} \cdot \sigma) \\ & + (1 - f_{\text{exp}}) \cdot f_{\text{tail}} \cdot G(\delta\Delta t; \mu_{\text{tail}} \cdot \sigma, s_{\text{tail}} \cdot \sigma) \\ & + f_{\text{tail}} \cdot f_{\text{exp}} \cdot G(\delta\Delta t; \mu_{\text{tail}} \cdot \sigma, s_{\text{tail}} \cdot \sigma) \\ & \otimes ((1 - f_{\text{R}}) \exp_{-}(\delta\Delta t/c \cdot \sigma) + f_{\text{R}} \exp_{+}(-\delta\Delta t/c \cdot \sigma)) \end{aligned}$$



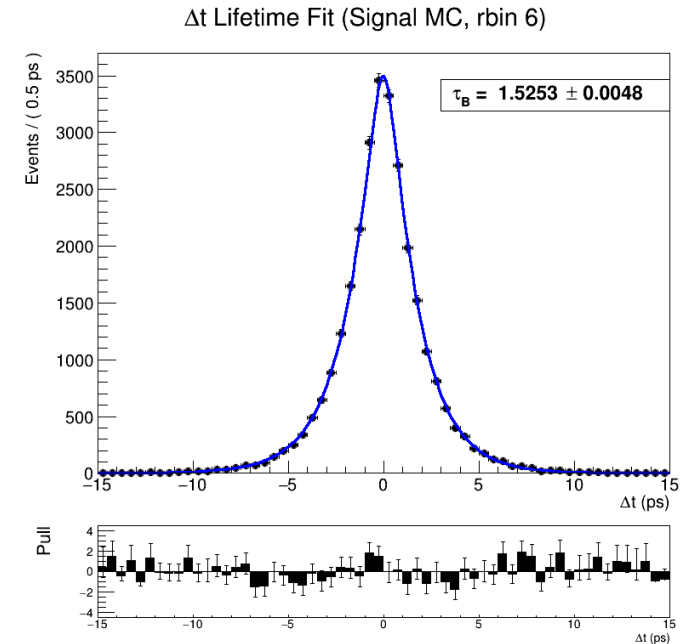
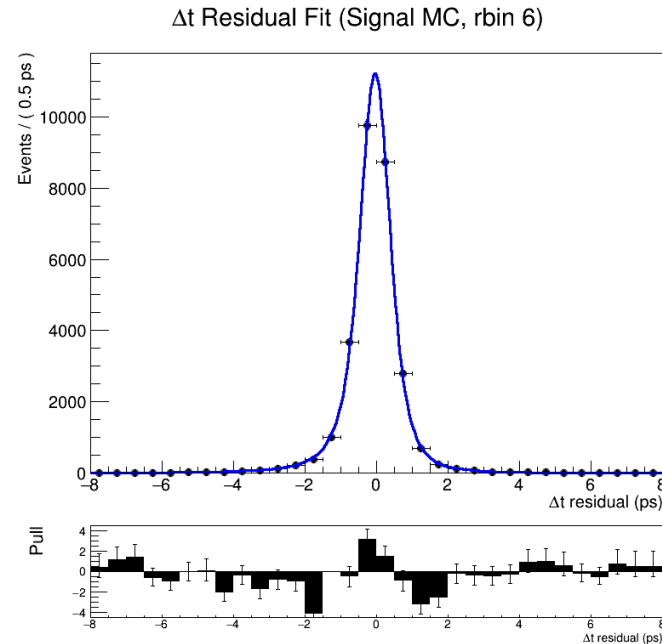
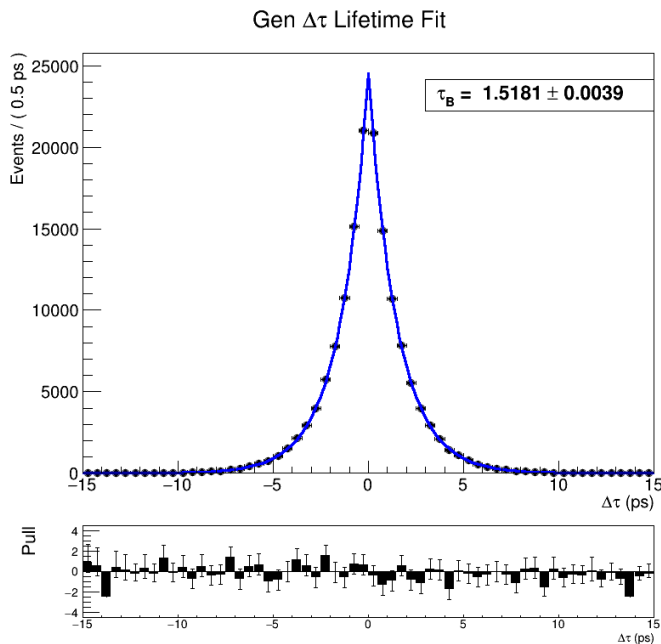
# $\Delta t$ Residual fits

- $\Delta t$  resolution parameter values determined by fitting the distribution of  $\delta\Delta t = \Delta t^{\text{reco}} - \Delta t^{\text{true}}$  in the pure signal MC sample simultaneously in  $r$ -bins 0-5 and 6
- Resolution model parameter values noticeably different in two  $r$ -bin categories



# Lifetime fits

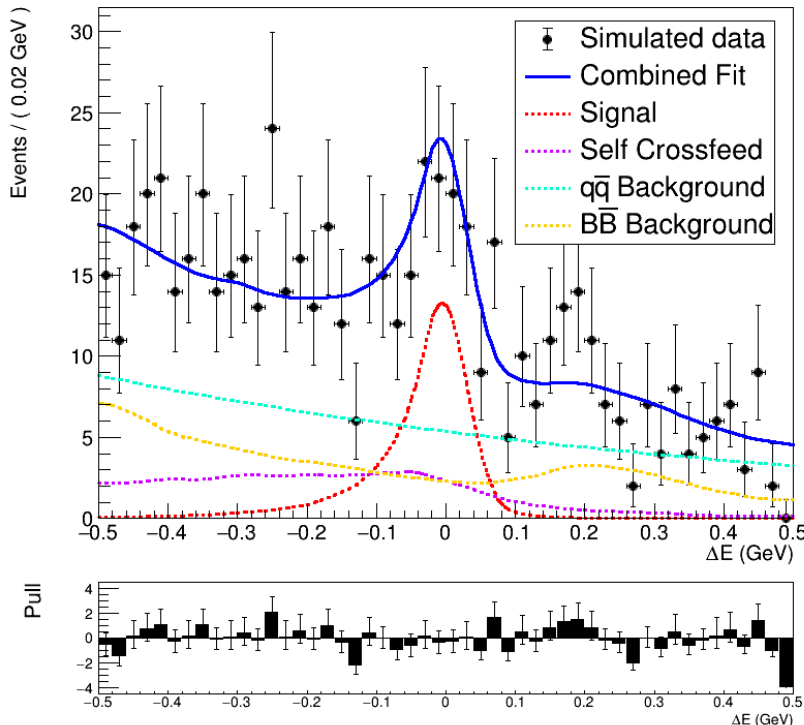
- One important check is to fit for the  $B$  lifetime ( $\tau_{B^0}$ ) without taking into account information on the  $B$  flavor
- The  $\Delta t$  resolution model is convolved with the pure physics  $\Delta t$  model



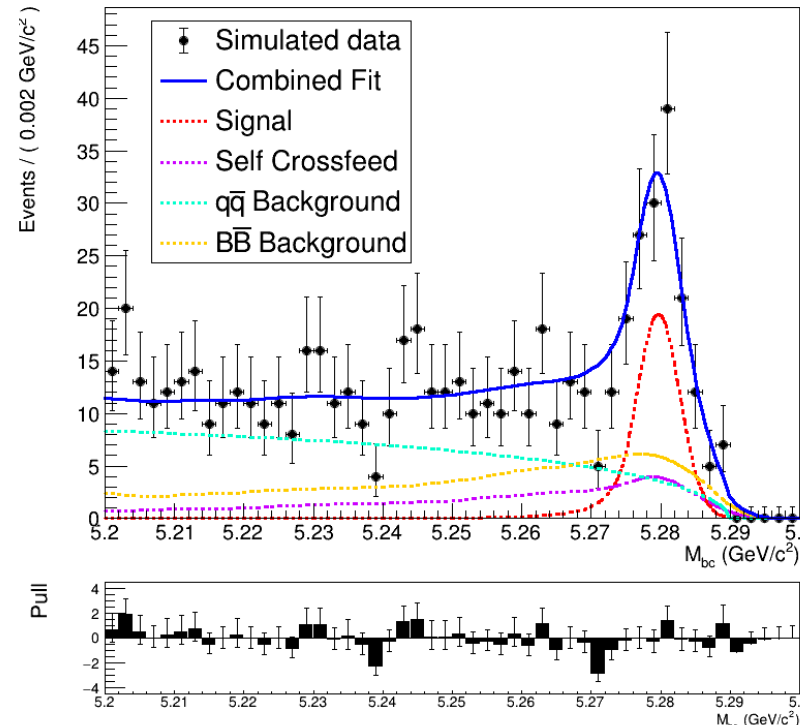
# Yield extraction

➤ We fit the product of  $M_{bc}$  and  $\Delta E$  to extract the signal and background yields

2D Fit:  $\Delta E$  Fit Projection, rbin 6



2D Fit:  $M_{bc}$  Fit Projection, rbin 6



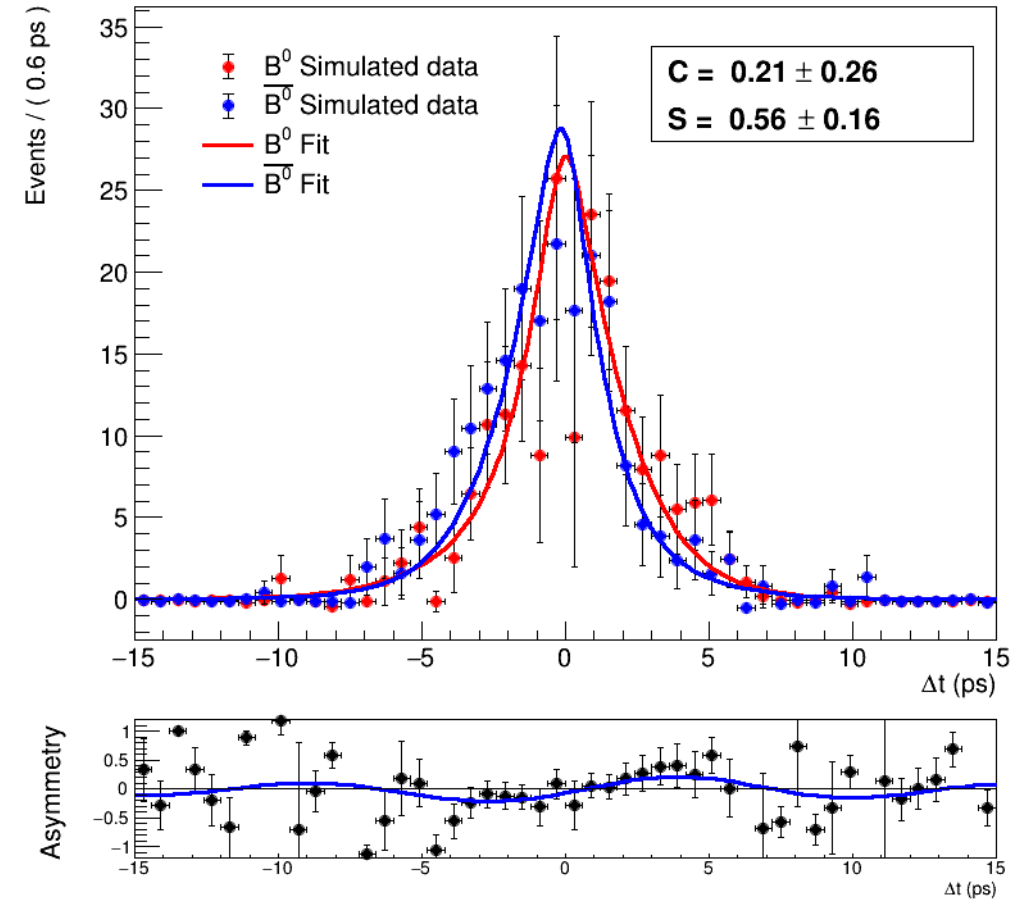
Yields (expected)	$r$ -bins 0-5	$r$ -bin 6
Signal	$390 \pm 30$	$90 \pm 10$
Background	$10800 \pm 110$	$540 \pm 20$

\* MC sample equivalent in size to the  $362 \text{ fb}^{-1}$  real data sample

# $\Delta t$ fit

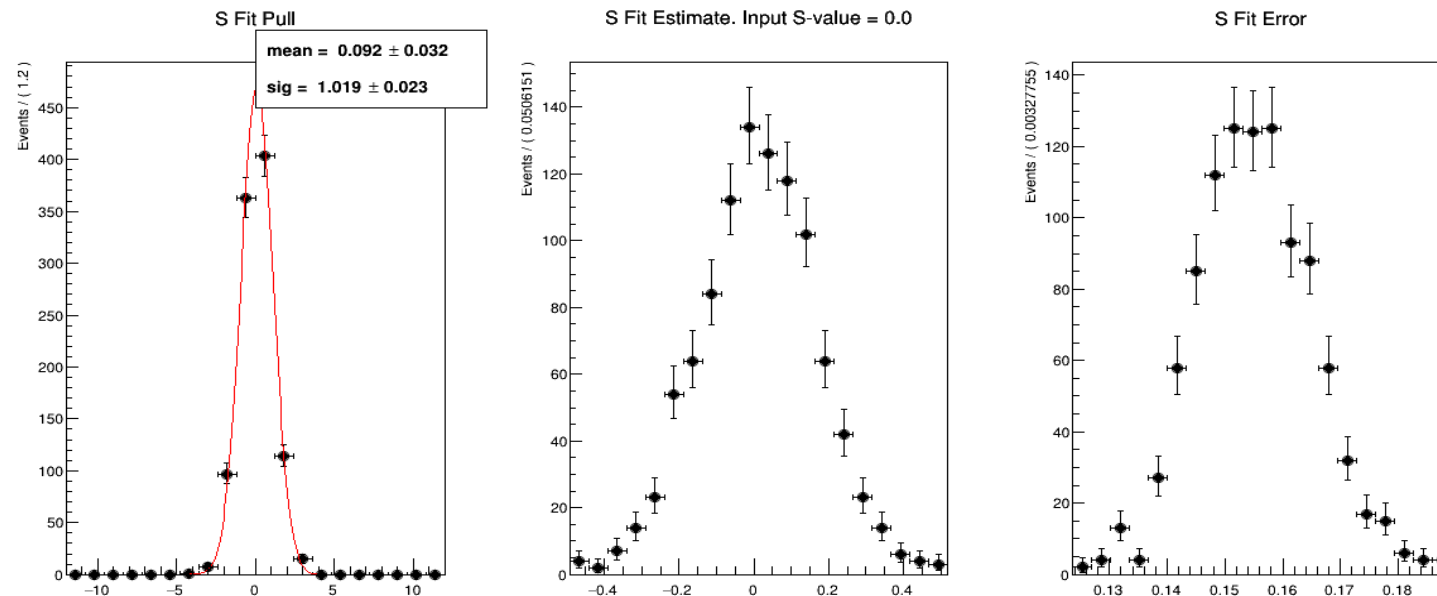
- *sPlot* is used to subtract background in  $\Delta t$
- We fit the *sWeighted*  $\Delta t$  distribution of a sample that contains signal events generated with inputs  $(C, S) = (0, 0.6)$
- Procedure to fit for  $S^\pm$  already in place

*sWeighted*  $\Delta t$  Fit, rbins 0-5

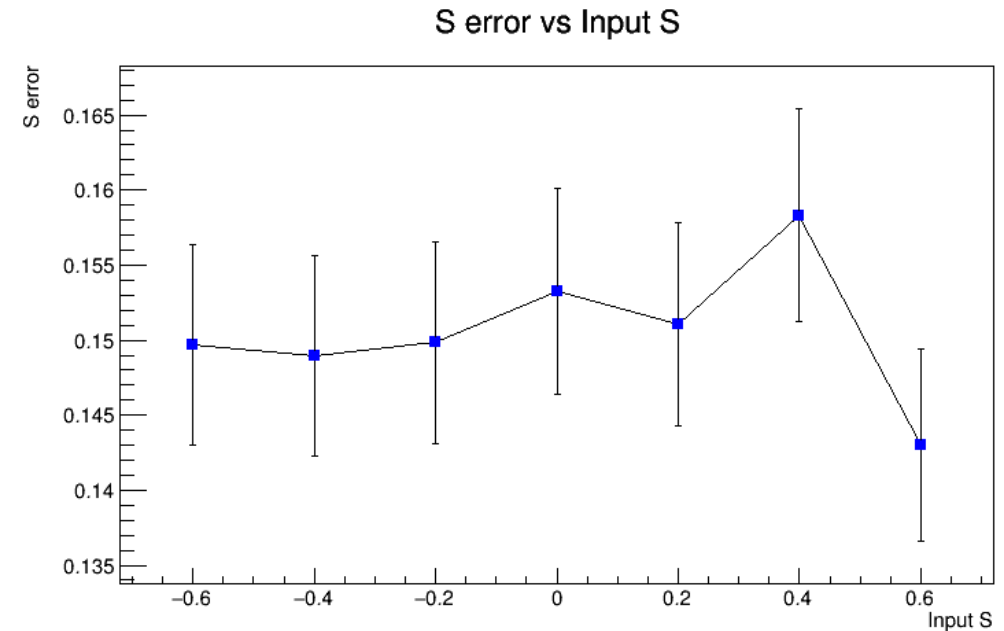
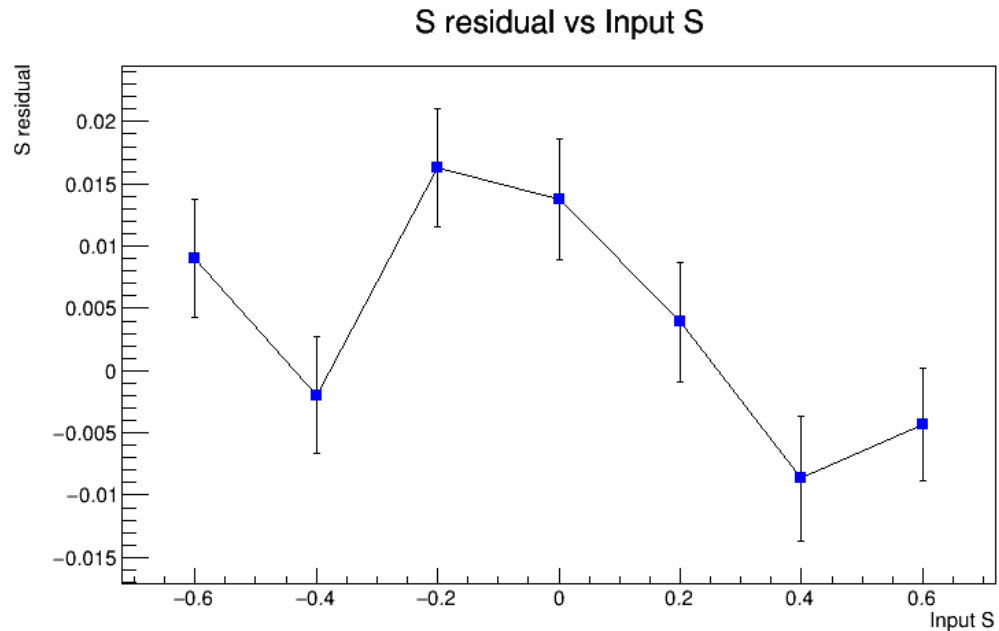


# Linearity studies

- We generate 1 million signal events with  $C = 0$  and  $S = [-0.6, -0.4, -0.2, 0.0, 0.2, 0.4, 0.6]$  using an implementation of SVP\_CP model from EvtGen in the Belle II software
- We make 1000 bootstrapped replicas using our simulated sample and perform the full fit on each of them to try and identify potential biases in the fit procedure



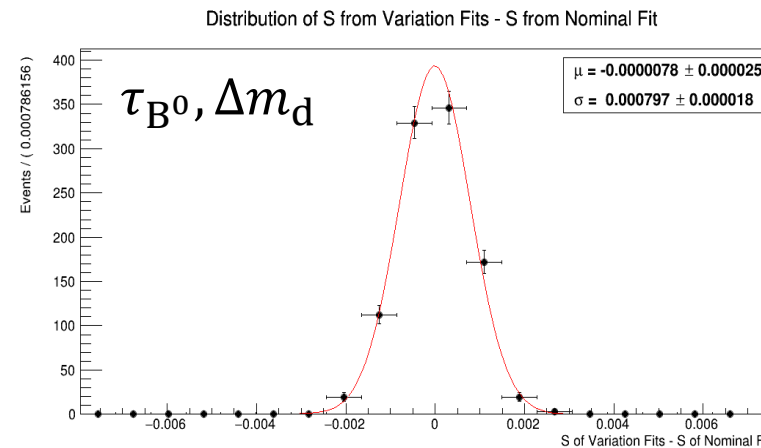
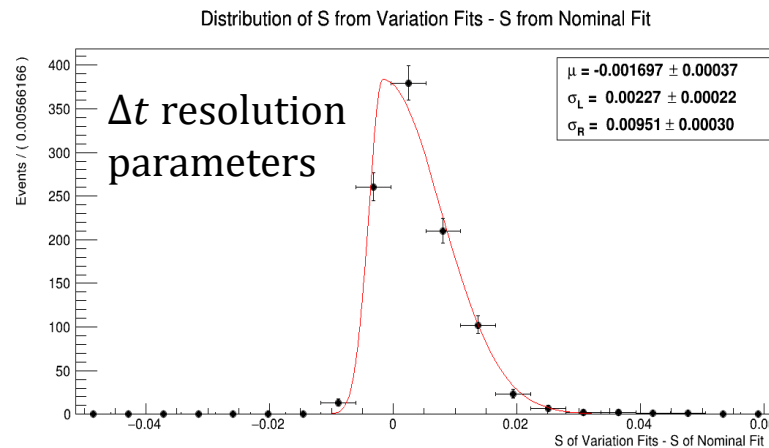
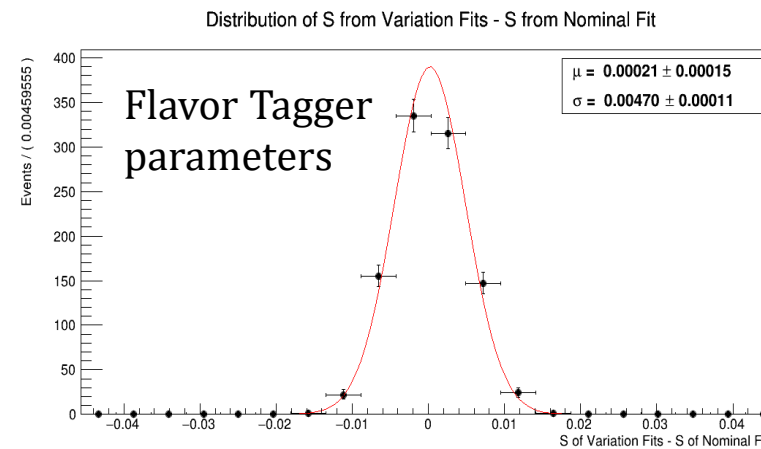
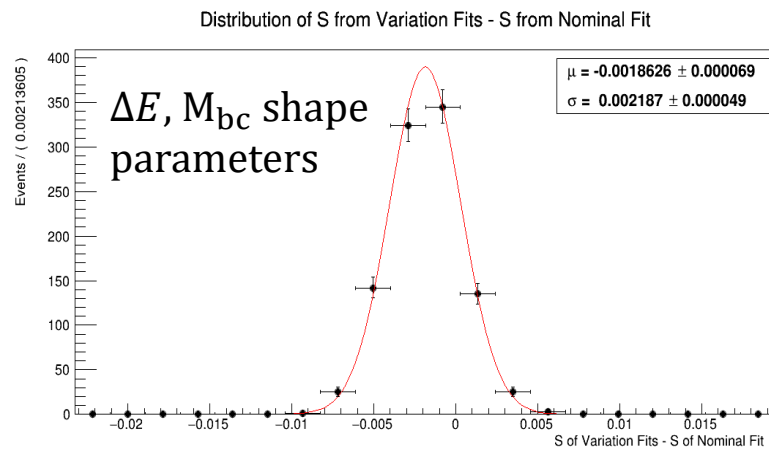
# Linearity studies



- No particular trend observed in the residual of  $S = S^{\text{fit}} - S^{\text{true}}$
- Expected uncertainty on  $S$  is  $\sim 0.15$ , which is  $\sim 36\%$  larger than the one expected from the Belle analysis with half the dataset size

# Systematics

- First few sources of systematic uncertainty already estimated (from MC)



# Conclusion & prospects

- ✓ Current fit strategy used for Belle II analysis seems robust
  - Belle analysis is already in a mature state (not shown here)
- ✓ Already started estimating systematics
- Next steps:
  - Control channel:  $B^0 \rightarrow J/\psi K\pi$  for fit validation and data/MC corrections
  - Finish up systematics estimation (also for  $S^\pm$ )

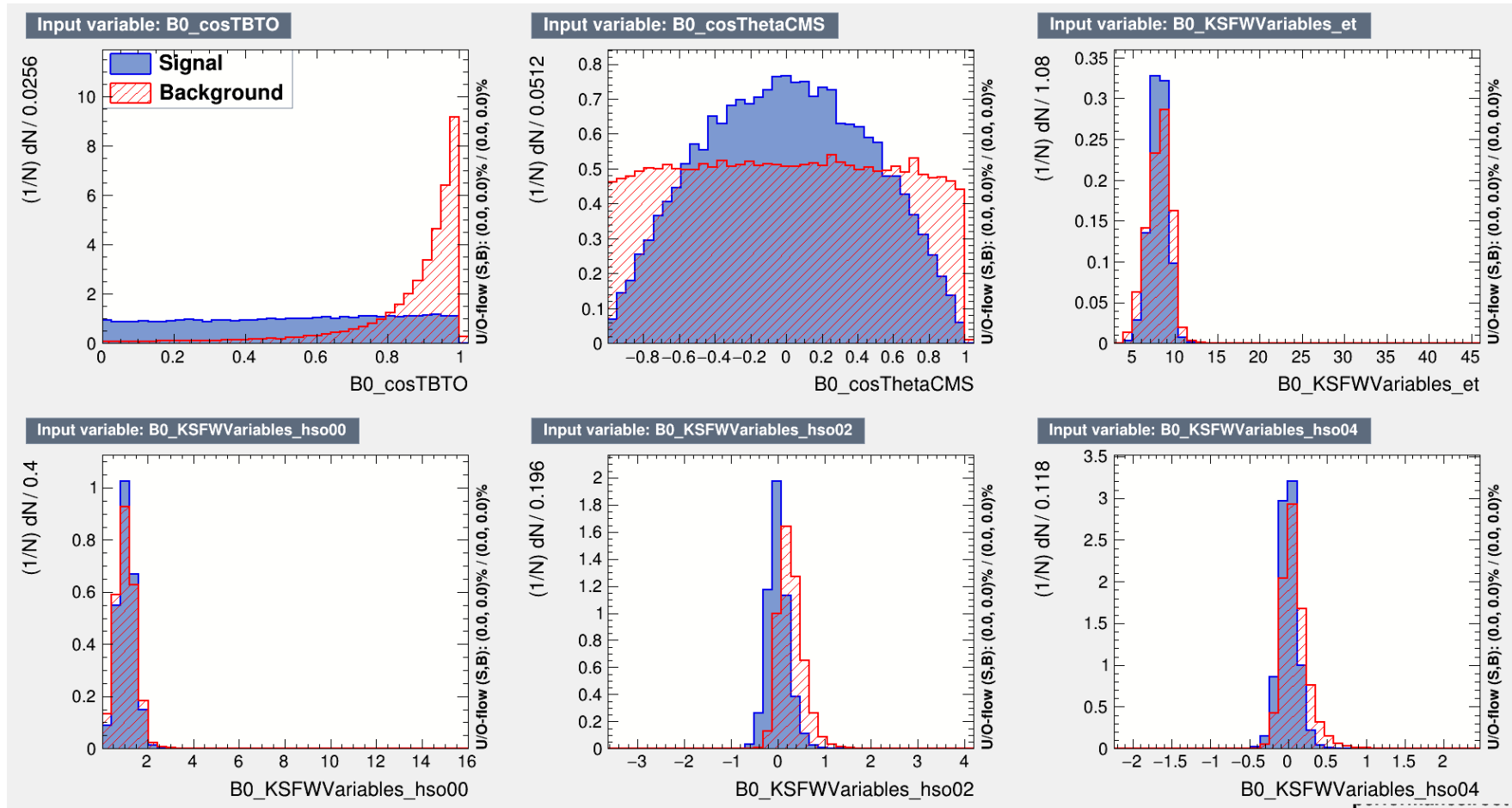


Thank You!

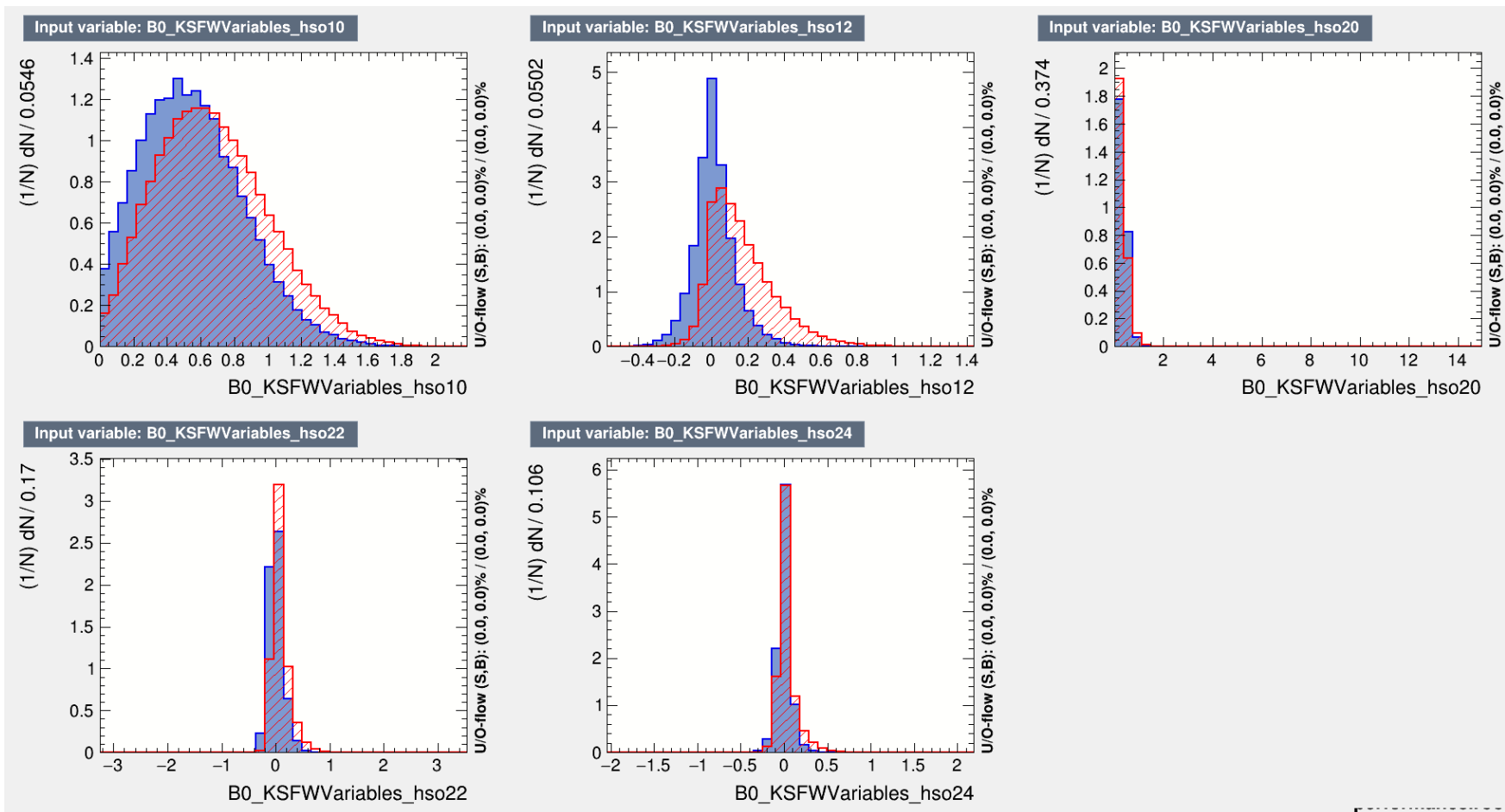
Questions?

Backup

# Continuum Suppression

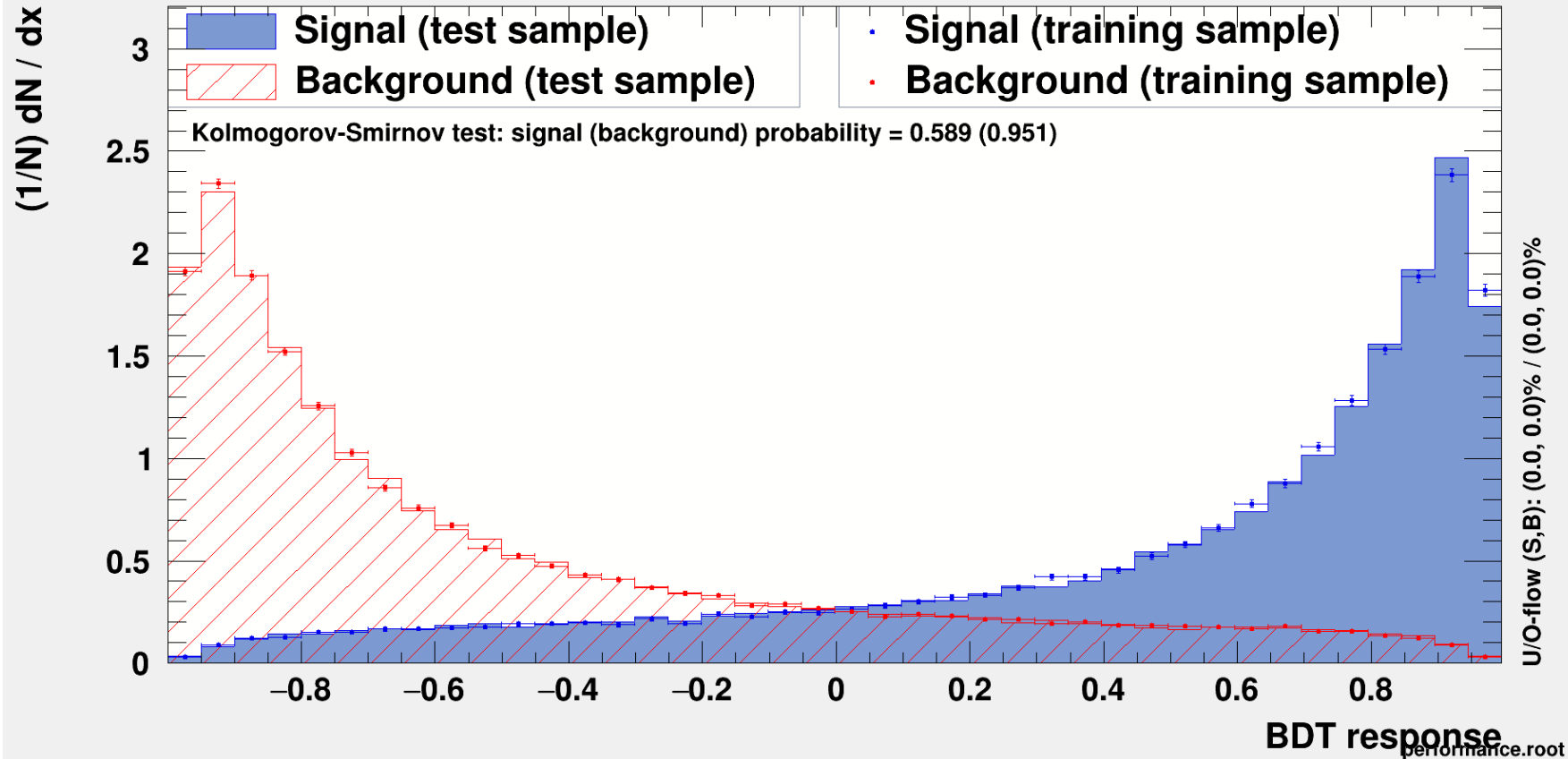


# Continuum Suppression

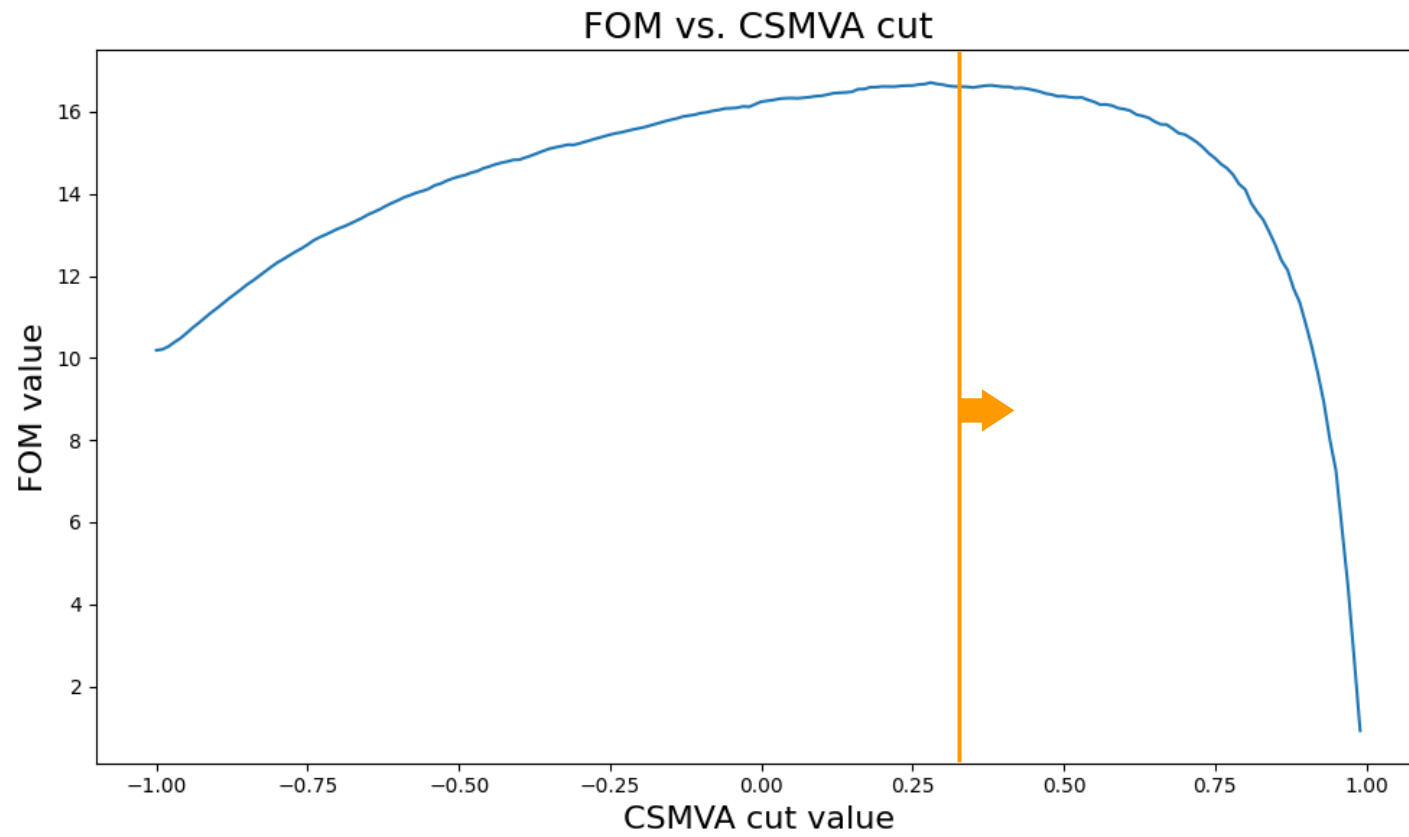


# Continuum Suppression

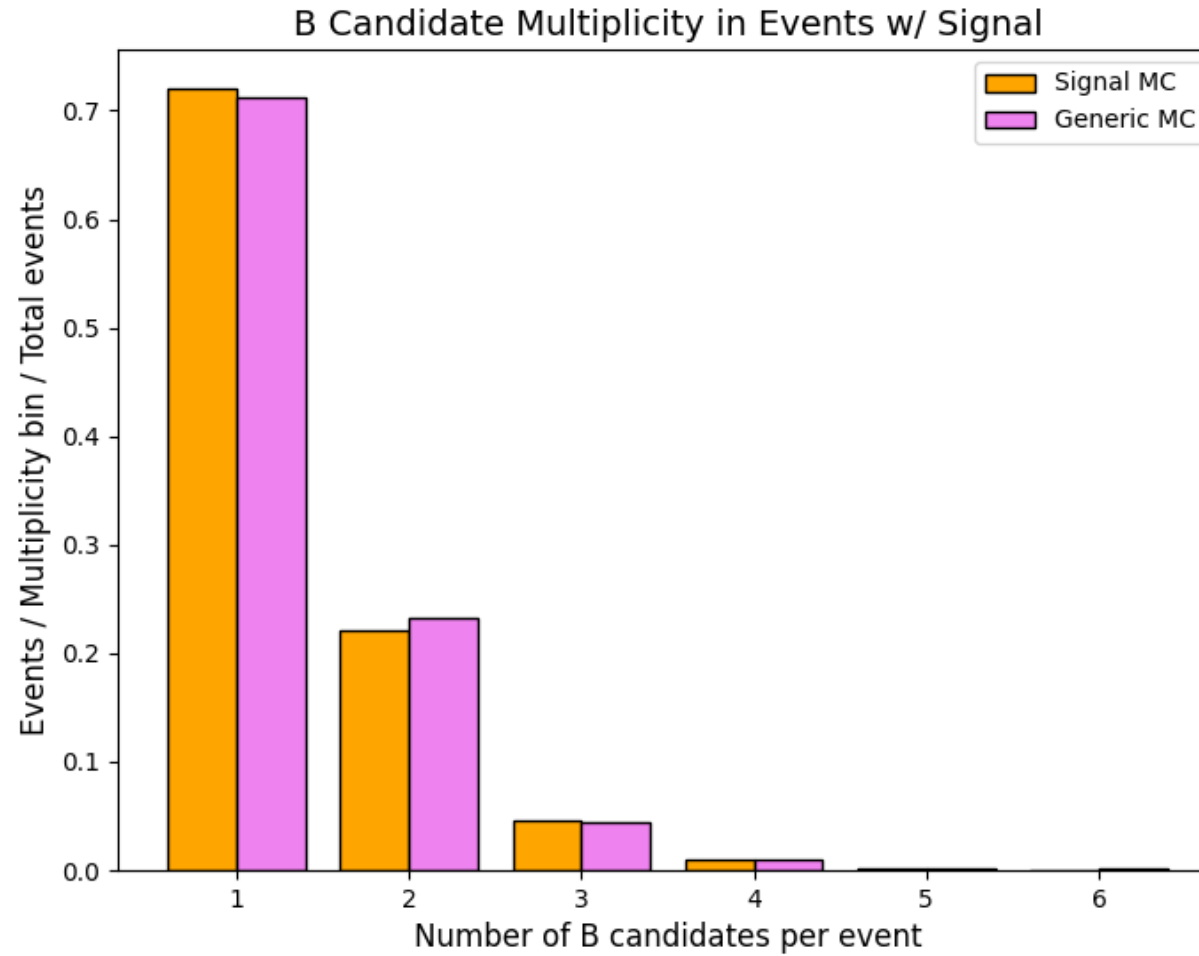
TMVA overtraining check for classifier: BDT



# CSMVA cut optimisation

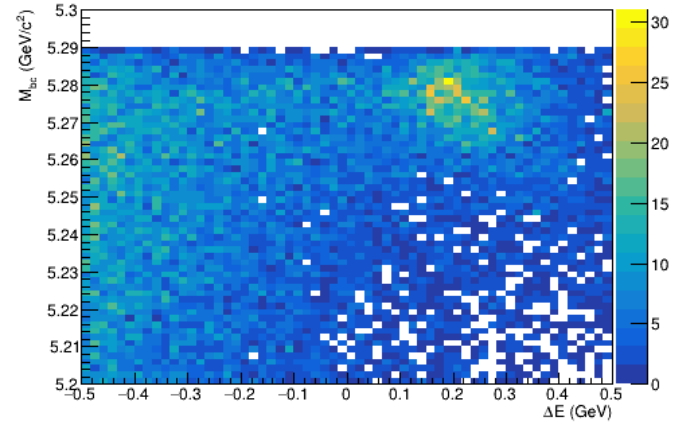


# Candidate Multiplicity

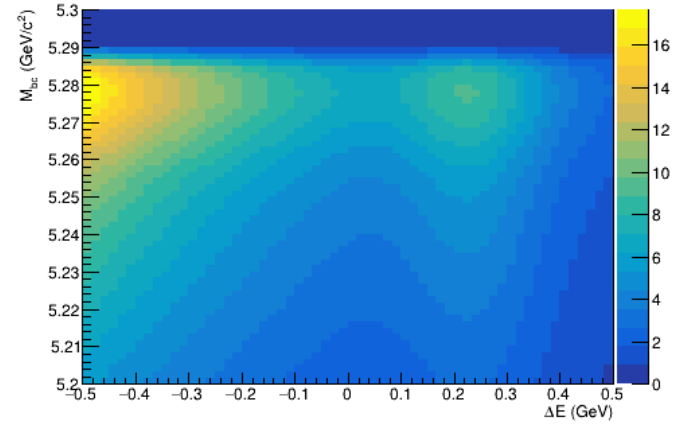


# 2D residual – $B\bar{B}$ bkg

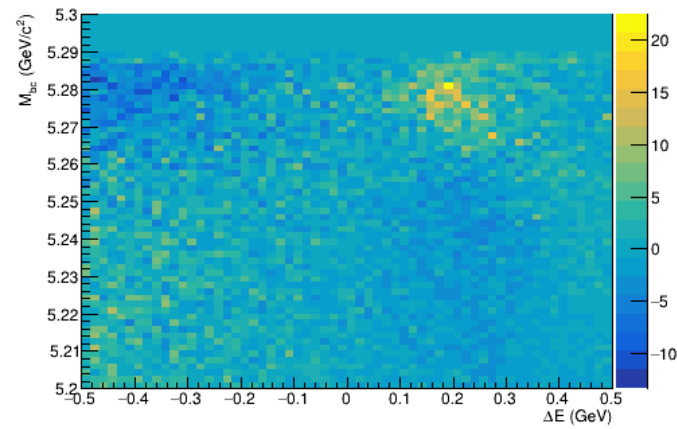
Data Histogram



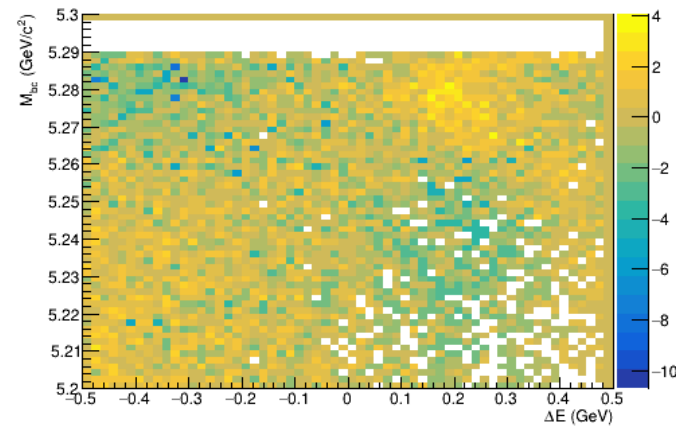
PDF Histogram



Residual



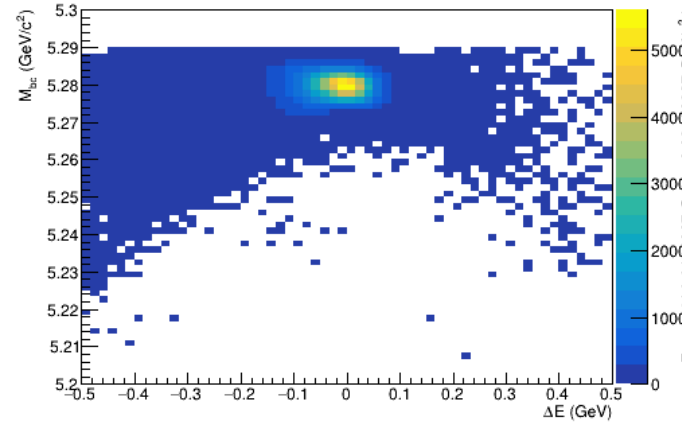
Pull



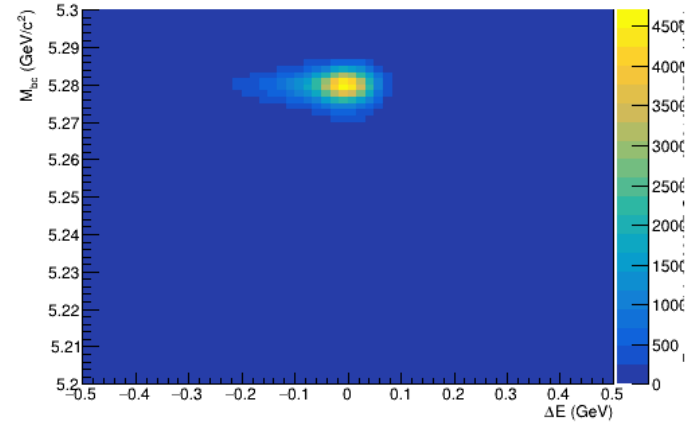


# 2D residual – Signal

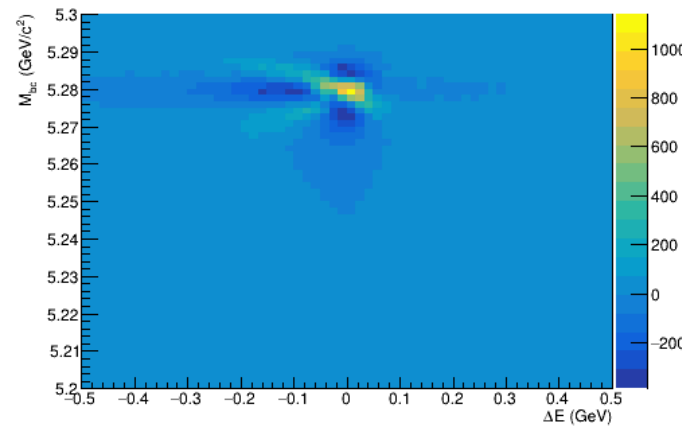
Data Histogram



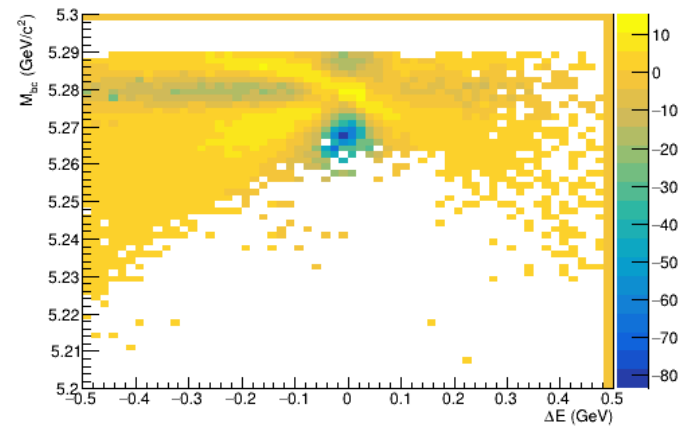
PDF Histogram



Residual

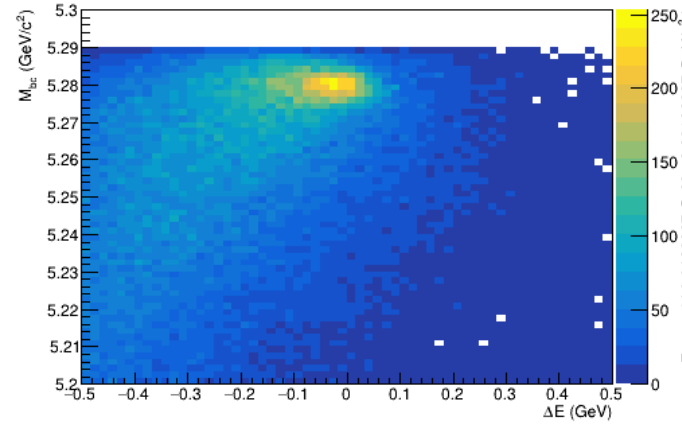


Pull

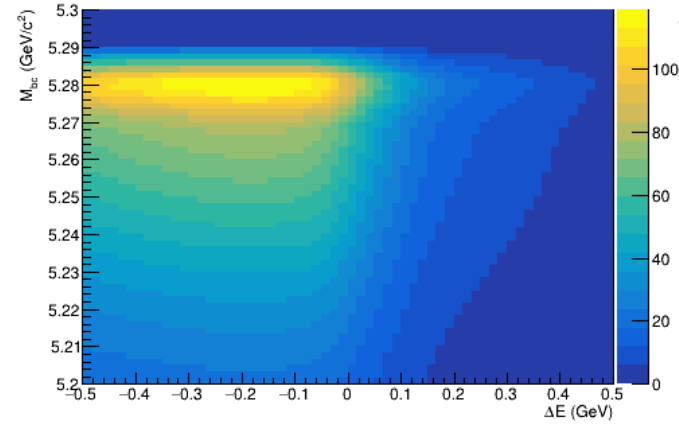


# 2D residual – SCF

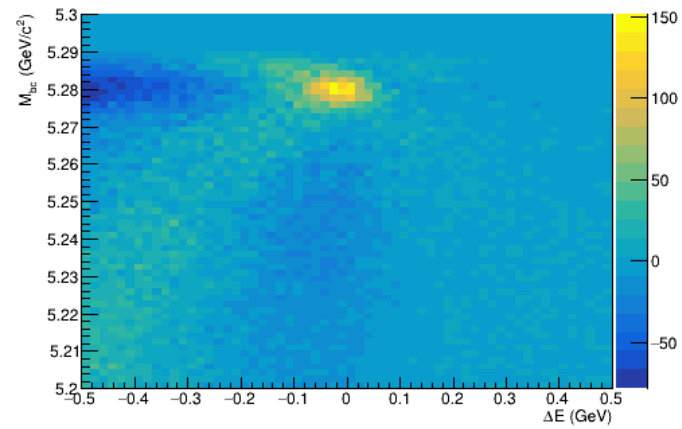
Data Histogram



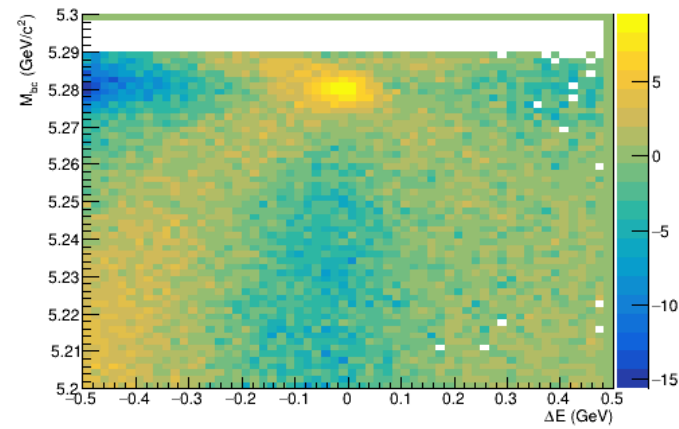
PDF Histogram



Residual

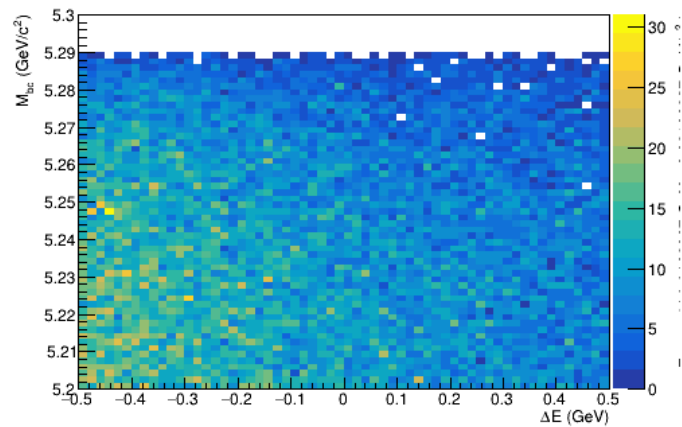


Pull

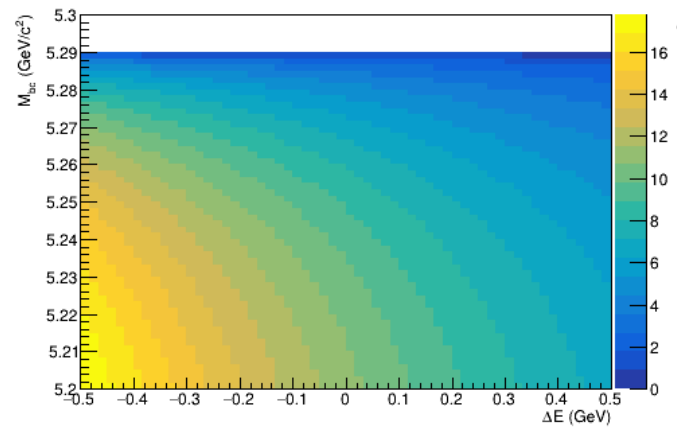


# 2D residual – Continuum

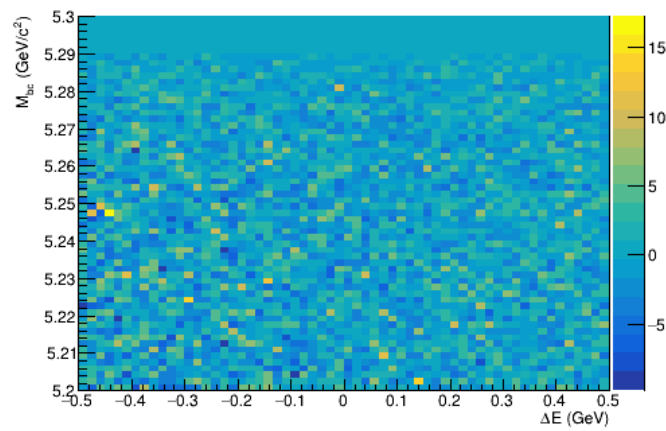
Data Histogram



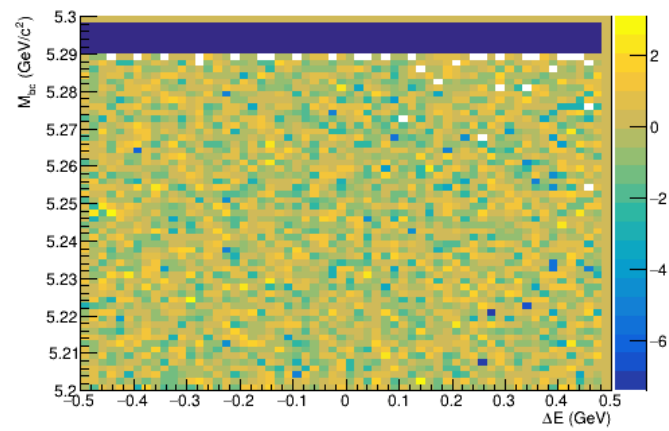
PDF Histogram



Residual

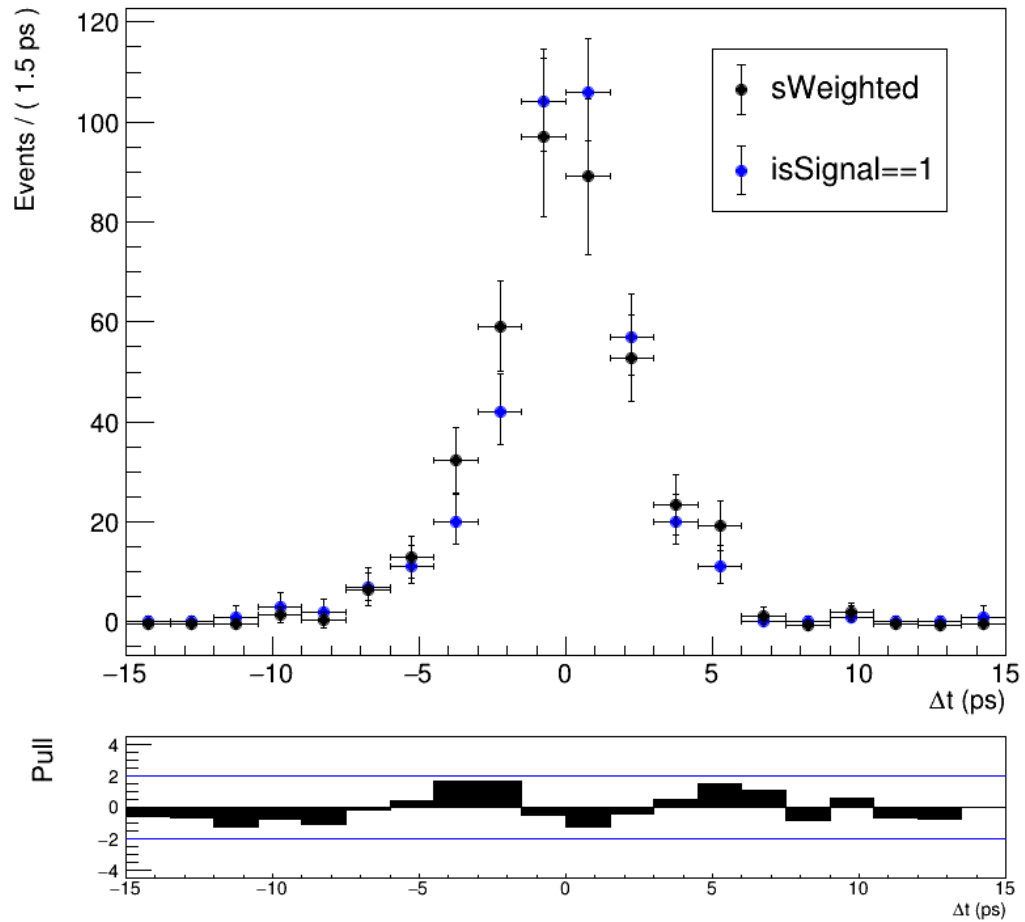


Pull

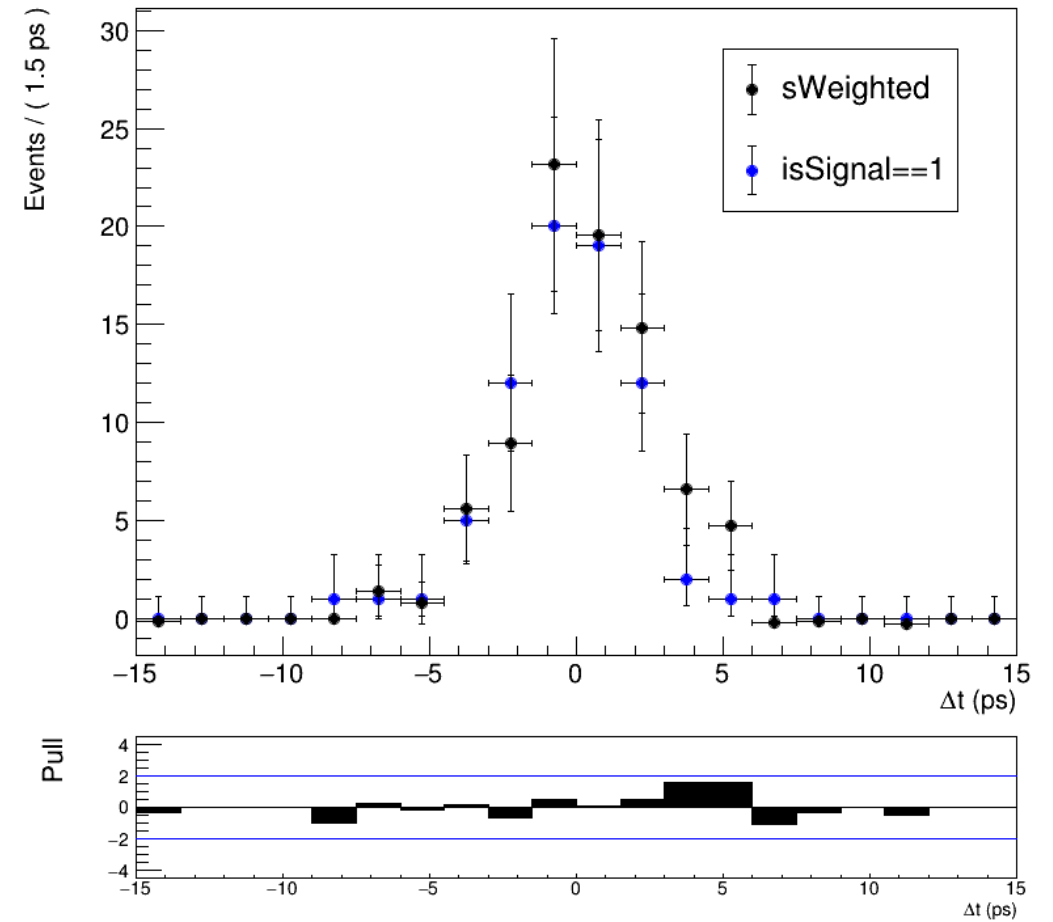


# sWeights validation – $\Delta t$

sWeighted  $\Delta t$  distributions, rbins 0-5

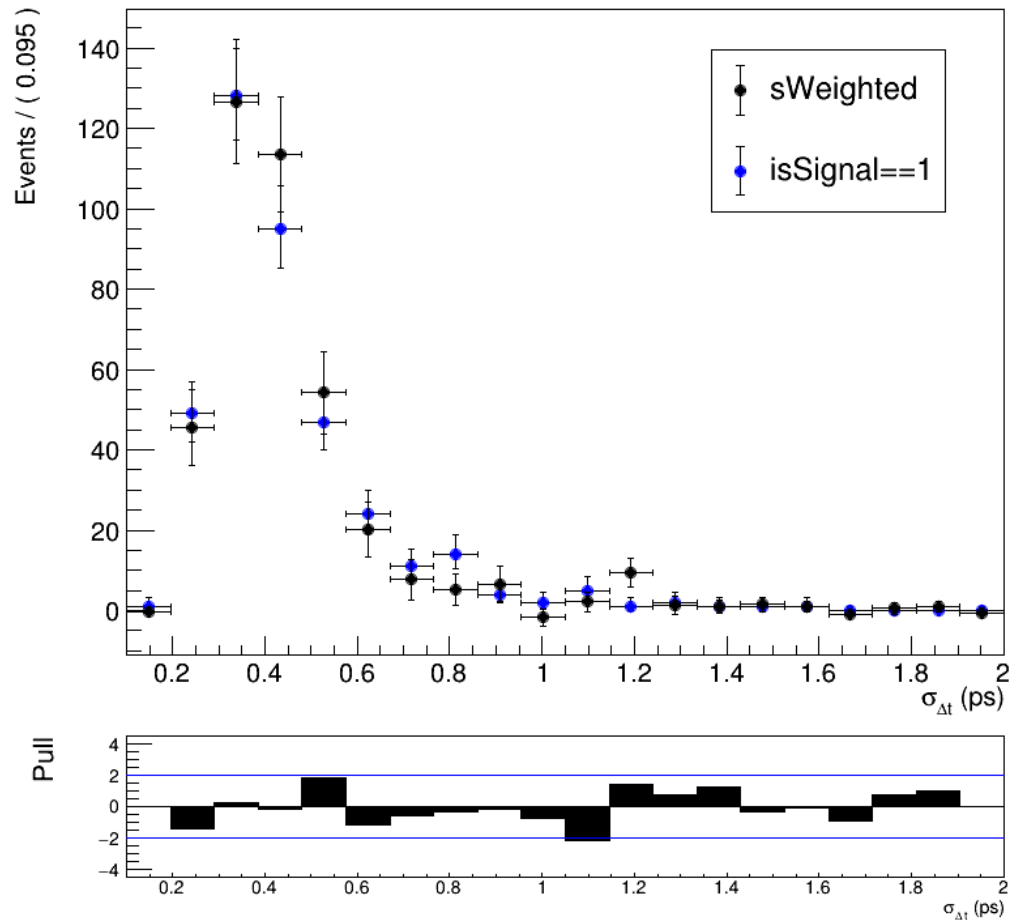


sWeighted  $\Delta t$  distributions, rbin 6

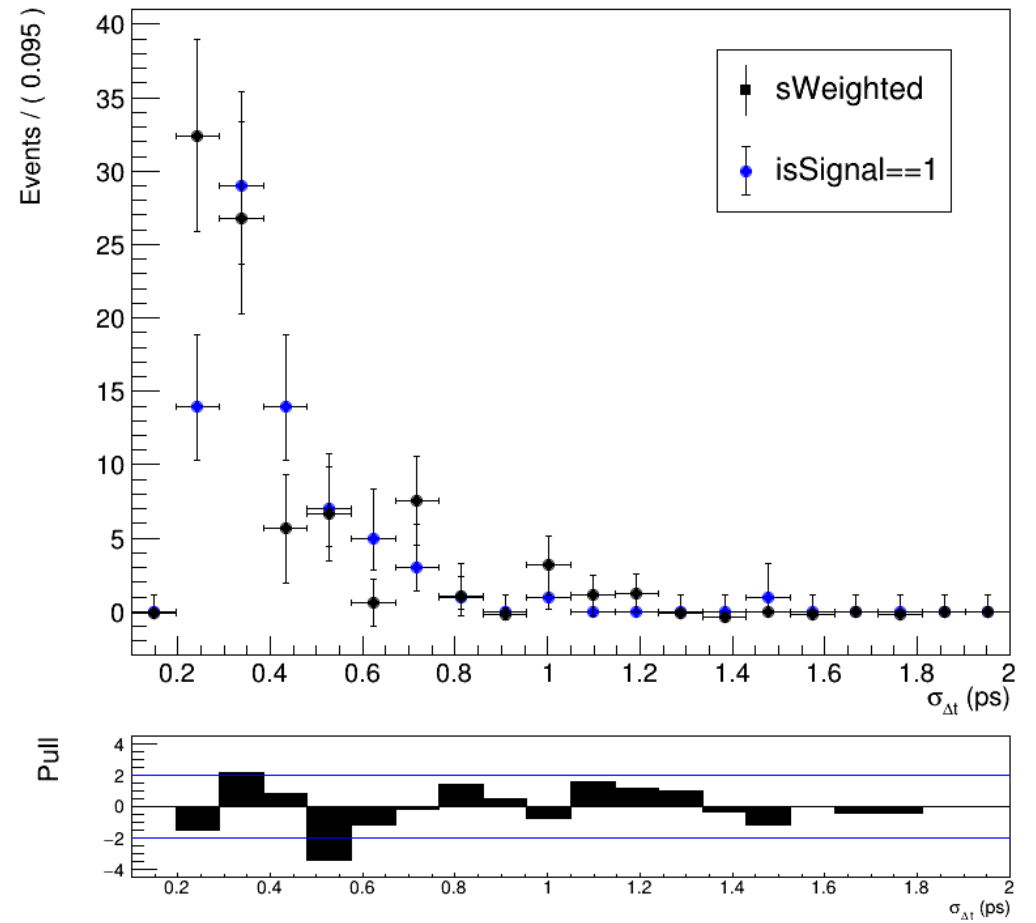


# sWeights validation – $\sigma_{\Delta t}$

sWeighted  $\sigma_{\Delta t}$  distributions, rbins 0-5

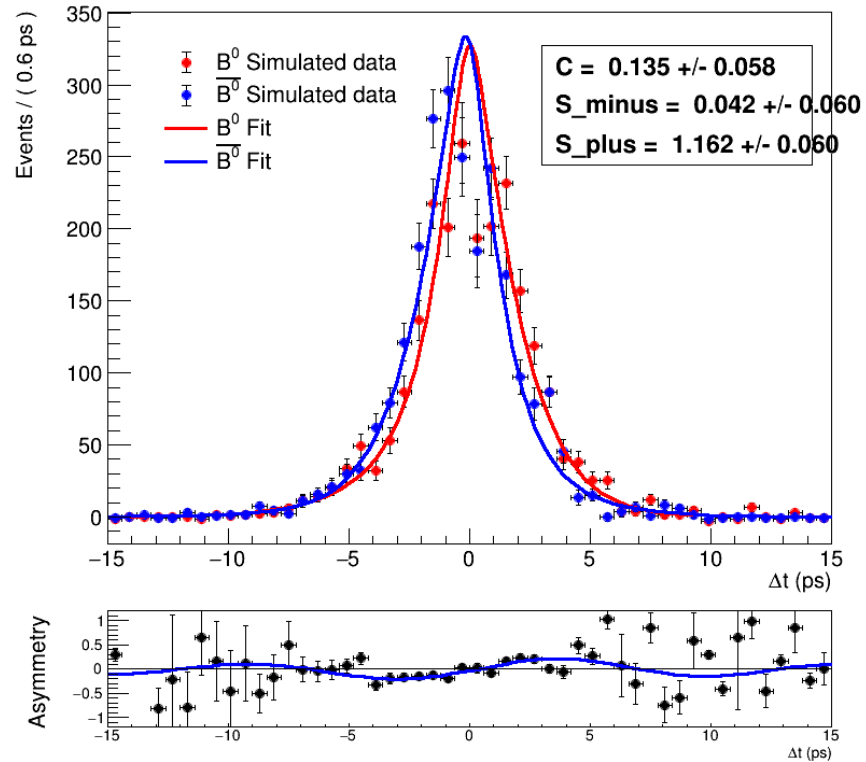


sWeighted  $\sigma_{\Delta t}$  distributions, rbin 6

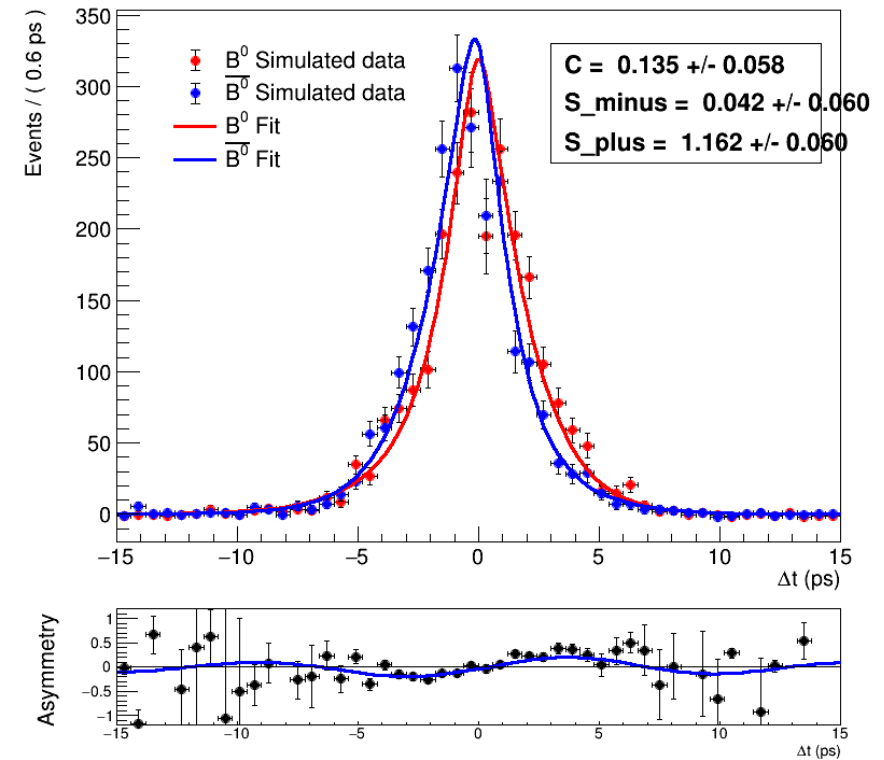


# Dalitz plane halves $\Delta t$ fits

sWeighted  $\Delta t$  Fit, rbins 0-5 - Dalitz "I" region

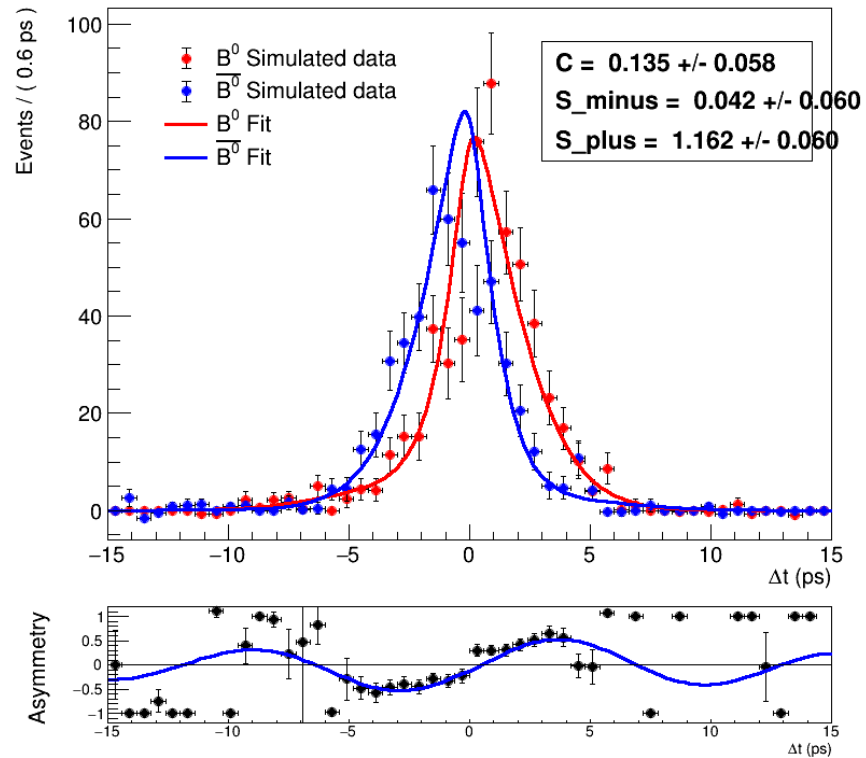


sWeighted  $\Delta t$  Fit, rbins 0-5 - Dalitz " $\bar{I}$ " region



# Dalitz plane halves $\Delta t$ fits

sWeighted  $\Delta t$  Fit, rbin 6 - Dalitz "I" region



sWeighted  $\Delta t$  Fit, rbin 6 - Dalitz " $\bar{I}$ " region

