

New Physics search via CP observables in $B_s^0 \rightarrow \phi\phi$ decay

Tejhas Kapoor and Emi Kou

IJCLab, Orsay, France

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Introduction

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Motivation: $b \rightarrow s\bar{s}s$ pure penguin process

Penguin Quantum Loop -> new heavy particles

No tree-penguin interference -> clean channel

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SM Prediction: $\phi_s^{s\bar{s}s} = 0$ (phases cancel out)

$$\arg\left(\frac{q}{p}\right) = 2\beta_s, \arg\left(\frac{\bar{A}}{A}\right) = -2\beta_s, \beta_s = \arg\left(\frac{-V_{tb}^* V_{ts}}{V_{cb}^* V_{cs}}\right)$$

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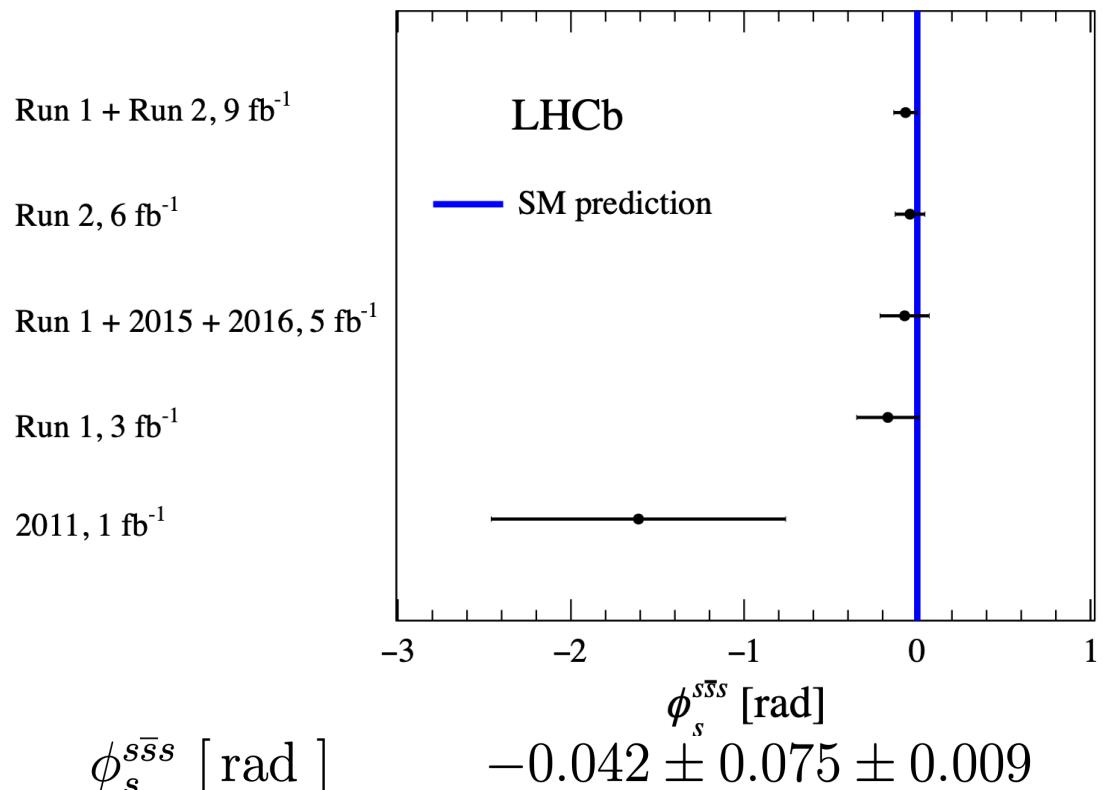
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Plan:

How exactly is this phase measured

(and parameterisation used) ?

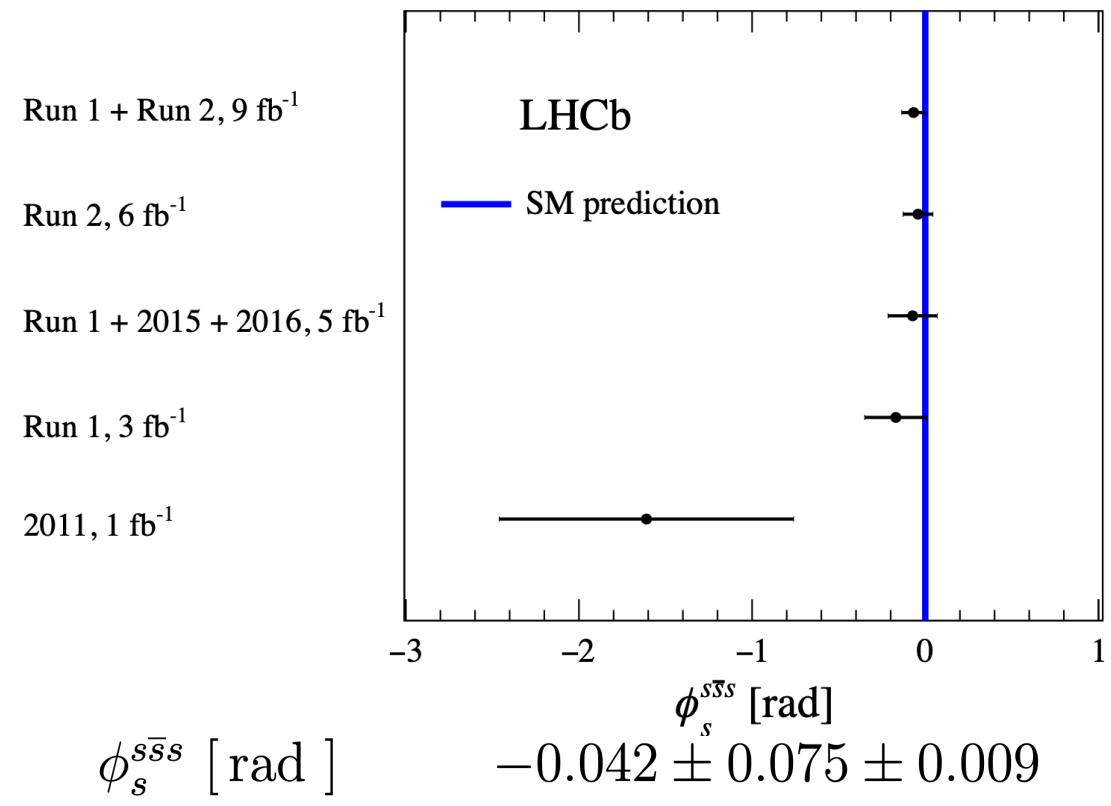
What are the assumptions taken ?

What can we infer from it (especially about NP)?

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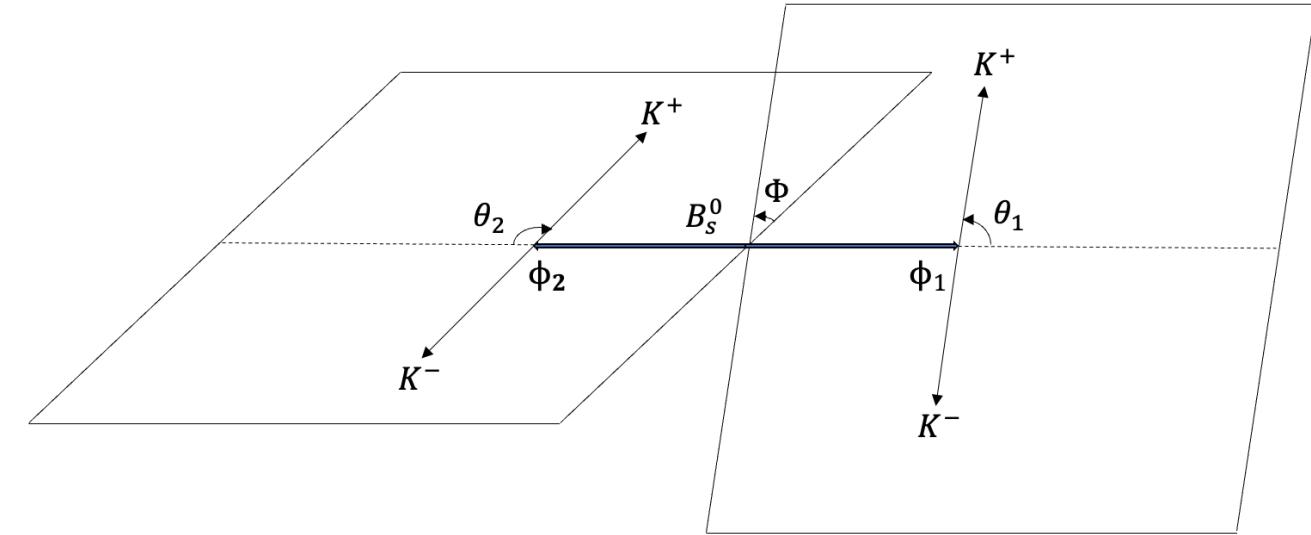
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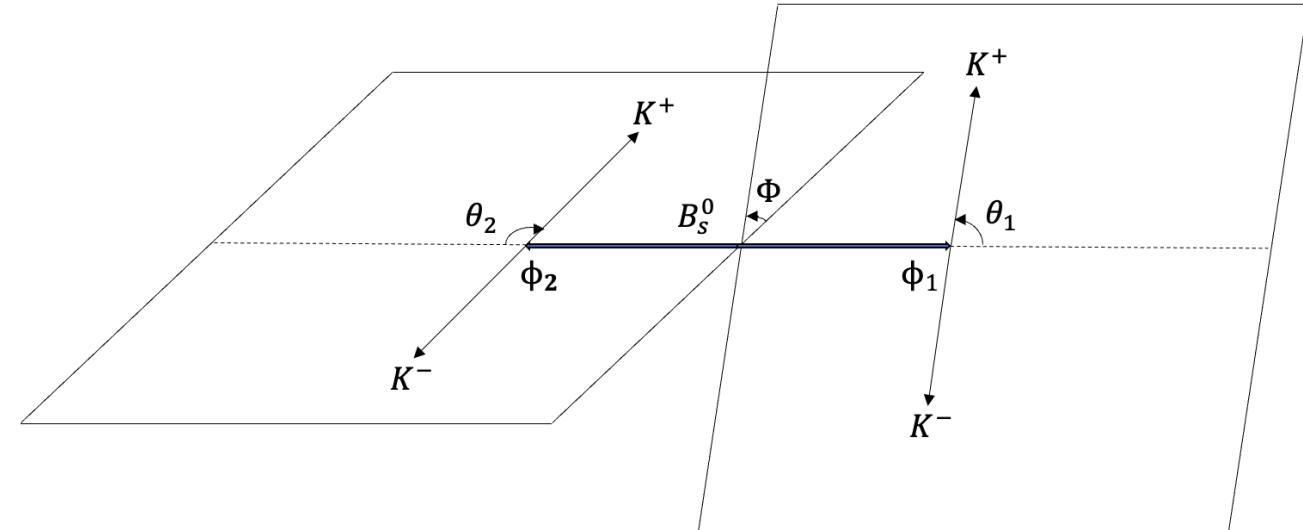


How: Time-dependent Angular Analysis

$A_{0,\parallel,\perp}(t)$: transversity amplitudes of $B_s^0 \rightarrow \phi\phi$ decay

$$A_k(t) = \left\langle (\phi\phi)_k \middle| H \middle| B_s^0(t) \right\rangle$$

(k : 0: longitudinal, \parallel , \perp : transverse)



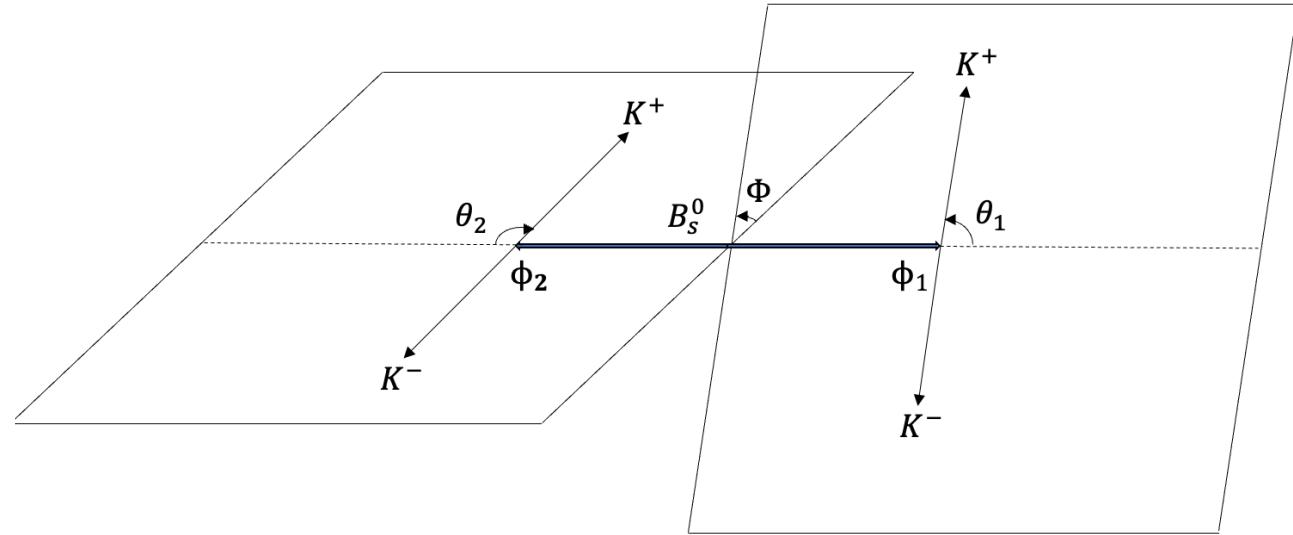
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$$\begin{aligned} \mathcal{A}(t, \theta_1, \theta_2, \Phi) &= A_0(t) \cos \theta_1 \cos \theta_2 + \frac{A_{\parallel}(t)}{\sqrt{2}} \sin \theta_1 \sin \theta_2 \cos \Phi \\ &+ i \frac{A_{\perp}(t)}{\sqrt{2}} \sin \theta_1 \sin \theta_2 \sin \Phi, \end{aligned}$$



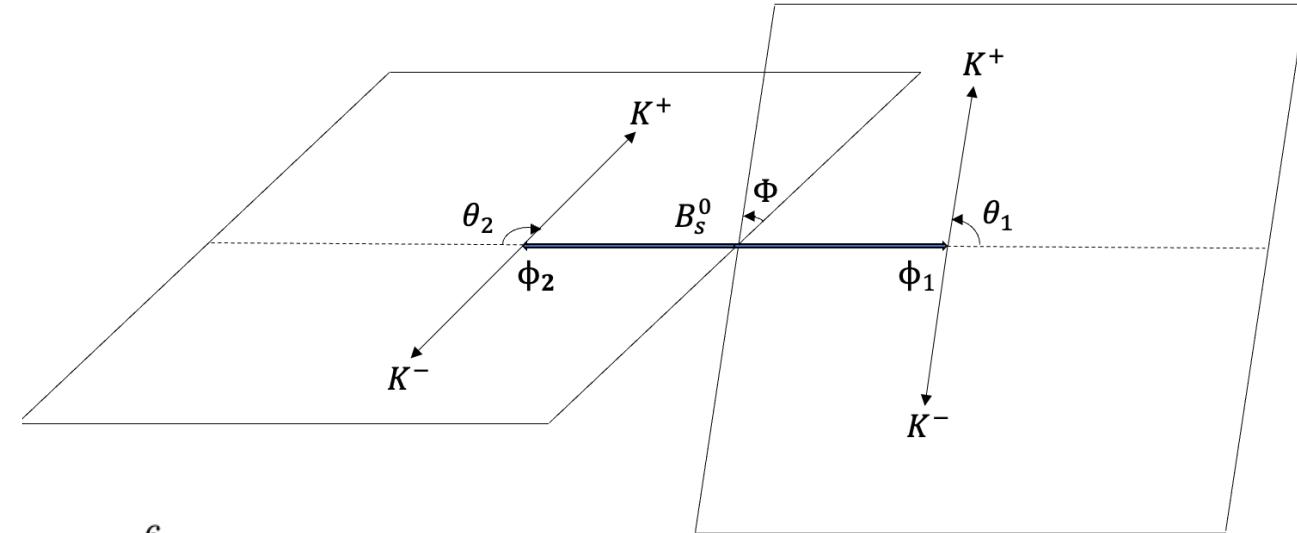
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Angular Decay
Distribution:

$$\frac{d^4\Gamma}{dt d\cos\theta_1 d\cos\theta_2 d\Phi} \propto |\mathcal{A}(t, \theta_1, \theta_2, \Phi)|^2 = \frac{1}{4} \sum_{i=1}^6 K_i(t) f_i(\theta_1, \theta_2, \Phi)$$

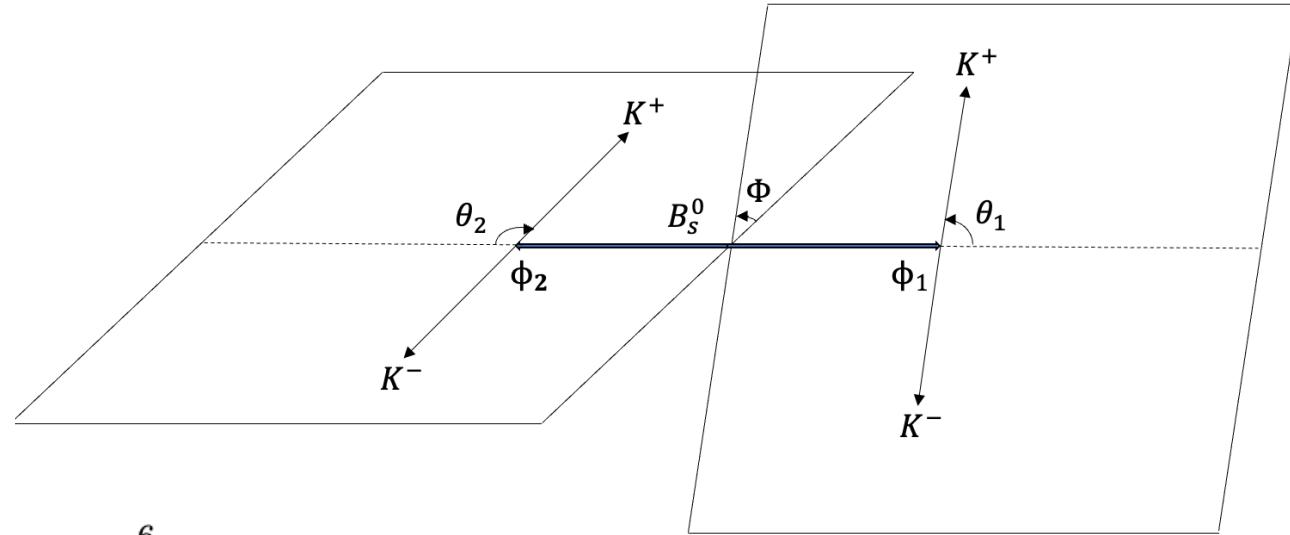
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$$K_i(t) = N_i e^{-\Gamma_s t} \left[a_i \cosh \left(\frac{1}{2} \Delta\Gamma_s t \right) + b_i \sinh \left(\frac{1}{2} \Delta\Gamma_s t \right) + c_i \cos(\Delta m_s t) + d_i \sin(\Delta m_s t) \right]$$

$$\begin{aligned} \Delta m_s &= m_H - m_L \\ \Delta\Gamma_s &= \Gamma_L - \Gamma_H \end{aligned}$$

$$\Gamma_s = (\Gamma_H + \Gamma_L)/2$$

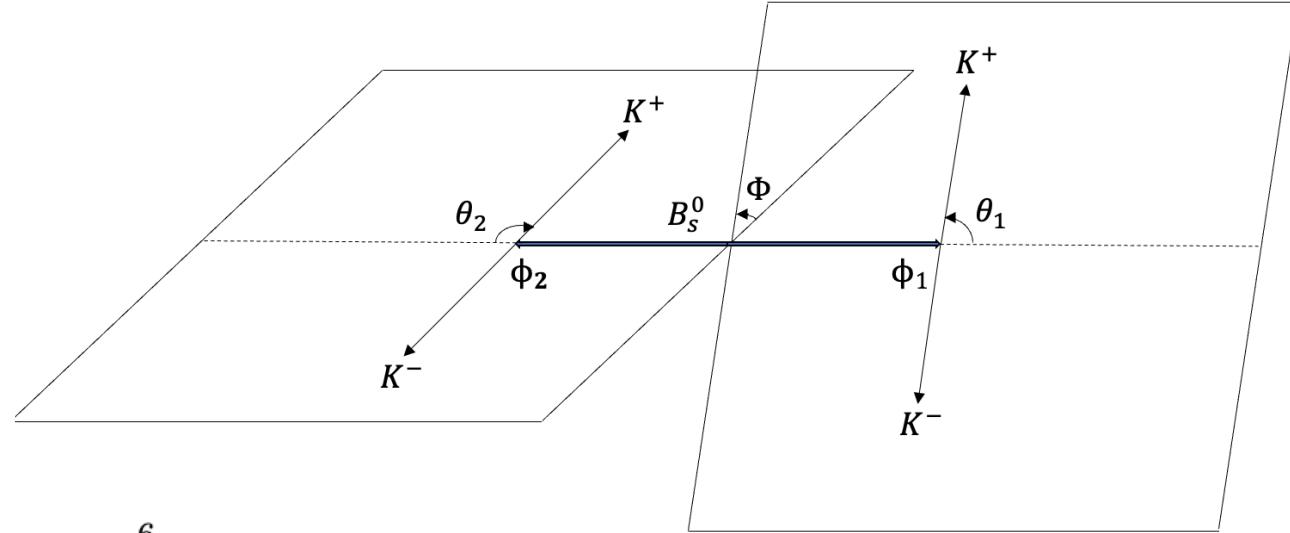
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N_i, a_i, b_i, c_i, d_i are Experimental Observables, their structure depend upon form of A_k

Experimental Observables

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Transversity Decay Amplitude: $A_k = |A_k^{SM}| e^{i\phi_k^{SM}} e^{i\delta_k^{SM}} + |A_k^{NP}| e^{i\phi_k^{NP}} e^{i\delta_k^{NP}}$

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mixture of strong and weak SM and NP phases.

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(SM Amplitude) (NP Amplitude)

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General amplitude to search for NP (SM Amplitude) (NP Amplitude)

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i	N_i	a_i	b_i	c_i	d_i	f_i
1	$ A_0 ^2$	$(1 + \lambda_0^2)/2$	$-\lambda_0 \cos(\theta_0^c - \theta_0)$	$(1 - \lambda_0^2)/2$	$-\lambda_0 \sin(\theta_0^c - \theta_0)$	$4 \cos^2 \theta_1 \cos^2 \theta_2$
2	$ A_{ } ^2$	$(1 + \lambda_{ }^2)/2$	$-\lambda_{ } \cos(\theta_{ }^c - \theta_{ })$	$(1 - \lambda_{ }^2)/2$	$-\lambda_{ } \sin(\theta_{ }^c - \theta_{ })$	$\sin^2 \theta_1 \sin^2 \theta_2 (1 + \cos 2\Phi)$
3	$ A_{\perp} ^2$	$(1 + \lambda_{\perp}^2)/2$	$\lambda_{\perp} \cos(\theta_{\perp}^c - \theta_{\perp})$	$(1 - \lambda_{\perp}^2)/2$	$\lambda_{\perp} \sin(\theta_{\perp}^c - \theta_{\perp})$	$\sin^2 \theta_1 \sin^2 \theta_2 (1 - \cos 2\Phi)$
4	$ A_{ } A_{\perp} /2$	$\begin{aligned} &\sin(\delta_{\perp} - \delta_{ } + \theta_{\perp} - \theta_{ }) \\ &-\lambda_{\perp} \lambda_{ } \sin(\delta_{\perp} - \delta_{ } + \theta_{\perp}^c - \theta_{ }^c) \end{aligned}$	$\begin{aligned} &\lambda_{\perp} \sin(\delta_{\perp} - \delta_{ } + \theta_{\perp}^c - \theta_{ }) \\ &-\lambda_{ } \sin(\delta_{\perp} - \delta_{ } + \theta_{\perp} - \theta_{ }^c) \end{aligned}$	$\begin{aligned} &\sin(\delta_{\perp} - \delta_{ } + \theta_{\perp} - \theta_{ }) \\ &+\lambda_{\perp} \lambda_{ } \sin(\delta_{\perp} - \delta_{ } + \theta_{\perp}^c - \theta_{ }^c) \end{aligned}$	$\begin{aligned} &-\lambda_{\perp} \cos(\delta_{\perp} - \delta_{ } + \theta_{\perp}^c - \theta_{ }) \\ &-\lambda_{ } \cos(\delta_{\perp} - \delta_{ } + \theta_{\perp} - \theta_{ }^c) \end{aligned}$	$-2 \sin^2 \theta_1 \sin^2 \theta_2 \sin 2\Phi$
5	$ A_{ } A_0 /2$	$\begin{aligned} &\cos(\delta_0 - \delta_{ } + \theta_0 - \theta_{ }) \\ &+\lambda_0 \lambda_{ } \cos(\delta_0 - \delta_{ } + \theta_0^c - \theta_{ }^c) \end{aligned}$	$\begin{aligned} &-\lambda_0 \cos(\delta_0 - \delta_{ } + \theta_0^c - \theta_{ }) \\ &-\lambda_{ } \cos(\delta_0 - \delta_{ } + \theta_0 - \theta_{ }^c) \end{aligned}$	$\begin{aligned} &\cos(\delta_0 - \delta_{ } + \theta_0 - \theta_{ }) \\ &-\lambda_0 \lambda_{ } \cos(\delta_0 - \delta_{ } + \theta_0^c - \theta_{ }^c) \end{aligned}$	$\begin{aligned} &-\lambda_0 \sin(\delta_0 - \delta_{ } + \theta_0^c - \theta_{ }) \\ &+\lambda_{ } \sin(\delta_0 - \delta_{ } + \theta_0 - \theta_{ }^c) \end{aligned}$	$\sqrt{2} \sin 2\theta_1 \sin 2\theta_2 \cos \Phi$
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Many experimental observables, but LHCb needed assumptions to reduce the parameters

LHCb Assumptions: Fit Schemes

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LHCb arXiv 1907.10003

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Helicity-Independent (HI) Assumption

- Interference phase ($\phi_{s,k} = \theta_k - \theta_k^c$) same for all transversities

$$\phi_{s,0} = \phi_{s,\parallel} = \phi_{s,\perp} = \phi_s^{s\bar{s}s} \rightarrow 1 \text{ free parameter}$$

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$\phi_{s,\parallel}$ [rad]	0.014 ± 0.055
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New Physics Model: Chromomagnetic Operator

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T.K., E. Kou

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Interference Phase and direct CPV measurement
parameters are “*clean observables*” to search for NP!
(*null-test parameters*)

Sensitivity Study Results

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We generate fake data by generating covariance matrix from the LHCb results.

arXiv: 2303.04494

We have two sets of LHCb results – we generate two pseudo datasets
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Fit Parameter	Data HD		Data HI	
	Central Value	σ	Central Value	σ
λ_0	0.978	0.058	0.984	0.070
$ A_0 ^2$	0.386	0.025	0.385	0.032
$ A_\perp ^2$	0.287	0.018	0.288	0.036
$\theta_0 - \theta_0^c$	-0.002	0.055	0.066	0.053
$\delta_\parallel - \delta_\perp$	-0.259	0.054	-0.261	0.056
$\delta_\parallel - \delta_0 - \theta_0$	2.560	0.071	2.589	0.079

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Parameter	$ A_0 ^2$	0.386	0.025	0.385	0.032
Interference Phase (ϕ_k)	$ A_\perp ^2$	0.287	0.018	0.288	0.036
	$\theta_0 - \theta_0^c$	-0.002	0.055	0.066	0.053
	$\delta_\parallel - \delta_\perp$	-0.259	0.054	-0.261	0.056
	$\delta_\parallel - \delta_0 - \theta_0$	2.560	0.071	2.589	0.079

Sensitivity Study Results

We generate fake data by generating covariance matrix from the LHCb results.

arXiv: 2303.04494

We have two sets of LHCb results – we generate two pseudo datasets

T.K., E. Kou

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Sensitivity on CP violating parameters with the current statistics : $\theta_0 - \theta_0^c \sim 6\%$ and $\lambda_0 \sim 7\%$

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NP signatures are different, one can be bigger/smaller than the other

Role of $B_d^0 \rightarrow \phi K_s$ decay

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Is NP left- or right-handed ?

arXiv: 2303.04494
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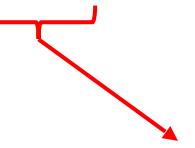
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Chirality of NP can be determined, under the assumption that NP is either only LH or RH

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“Thank you for your
attention ☺ ”

Backup Slides

CP Violation

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CPV Types

$$\text{Decay: } \lambda = \frac{|A|}{|A|} \neq 1$$

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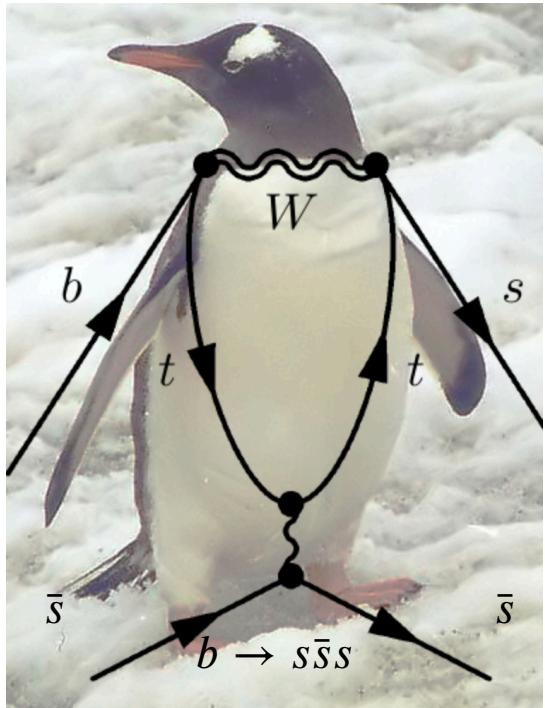
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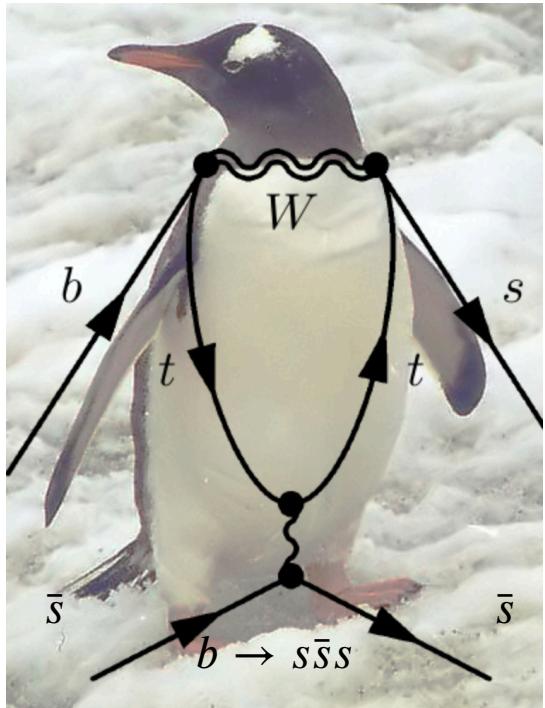
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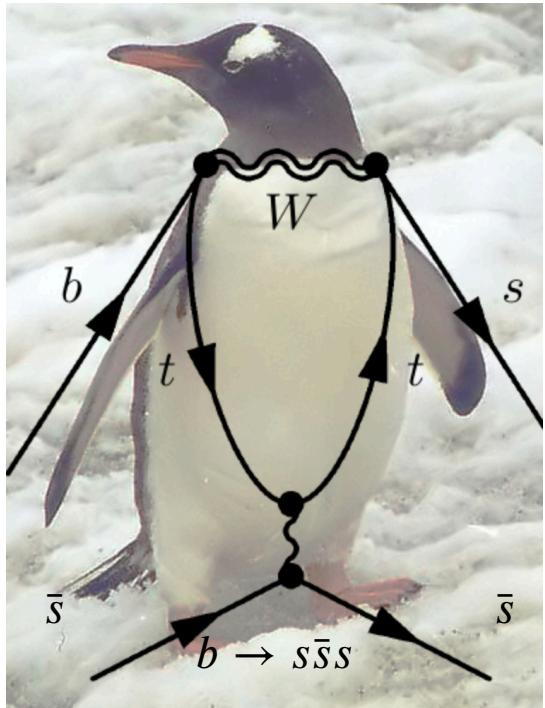
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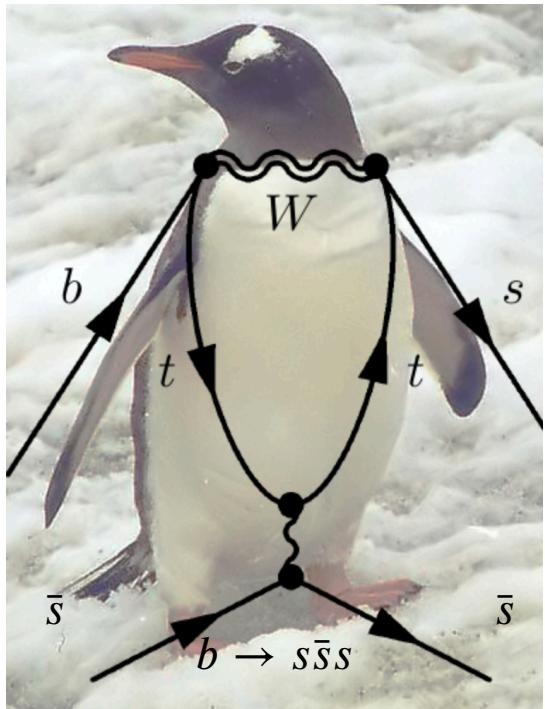
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CP Violating quantities are known precisely in SM
Quantum loop makes it sensitive to NP

Introduction: Chromomagnetic Operator

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New Physics (NP) Model:

Chromomagnetic Operator (O_{8g}) $b \rightarrow sg$ (g is on-shell)

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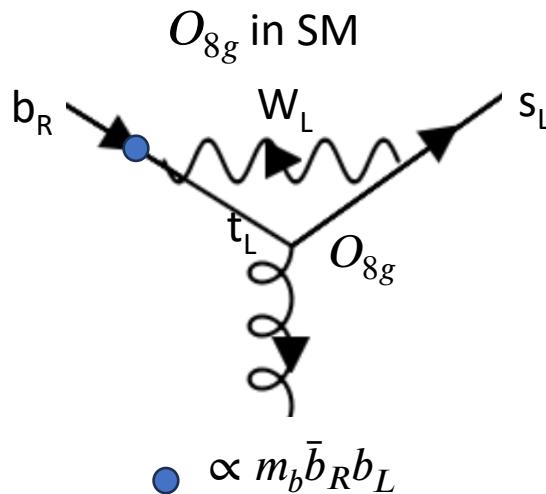
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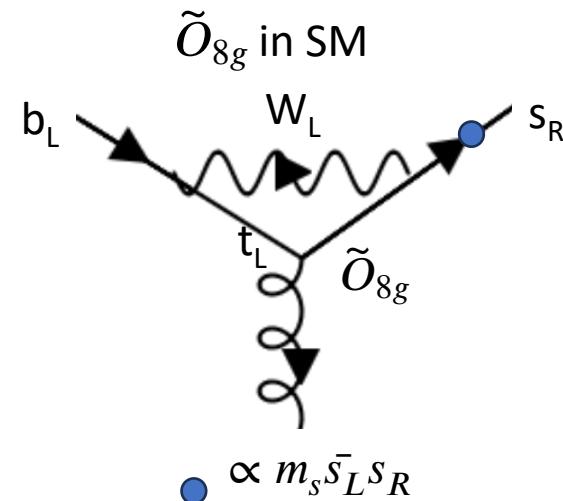
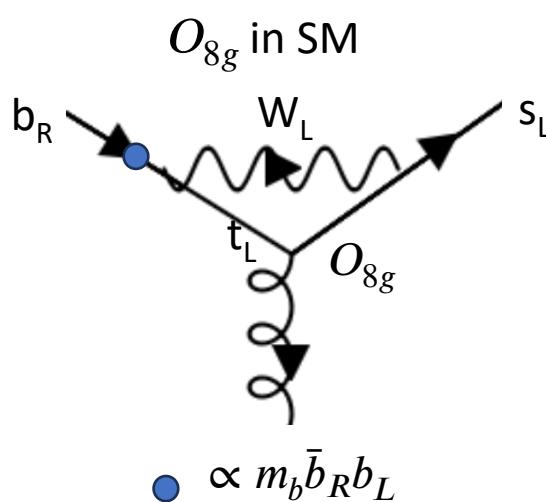
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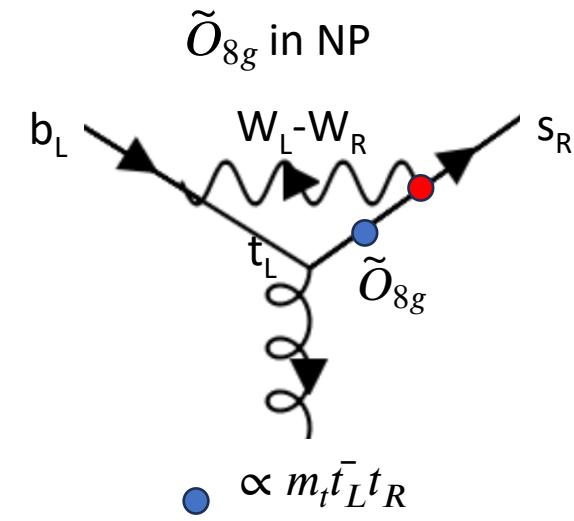
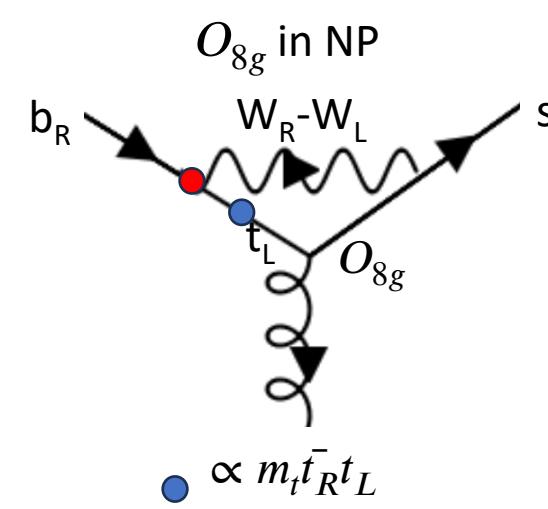
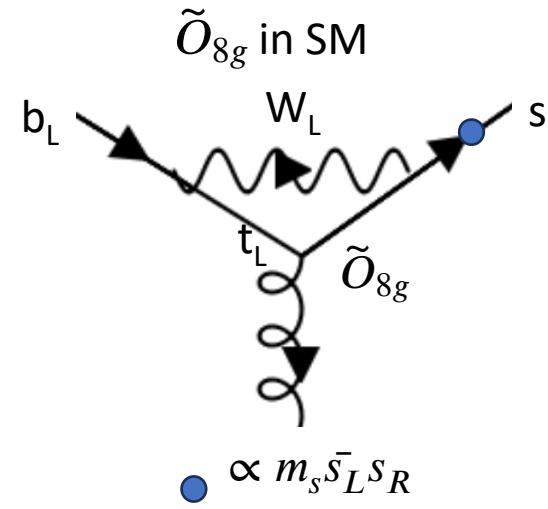
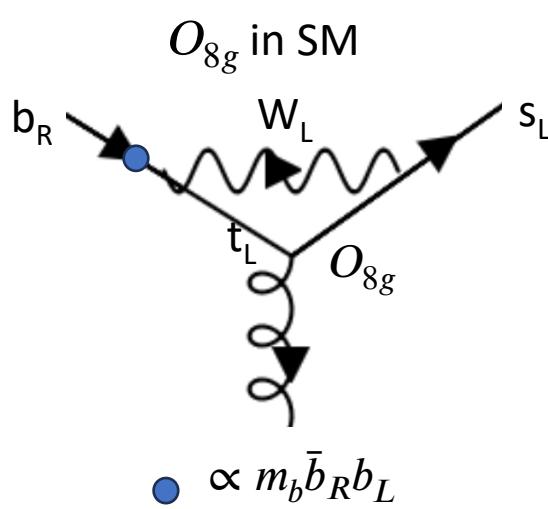
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● Mass Insertion Approximation

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New Physics (NP) Model:

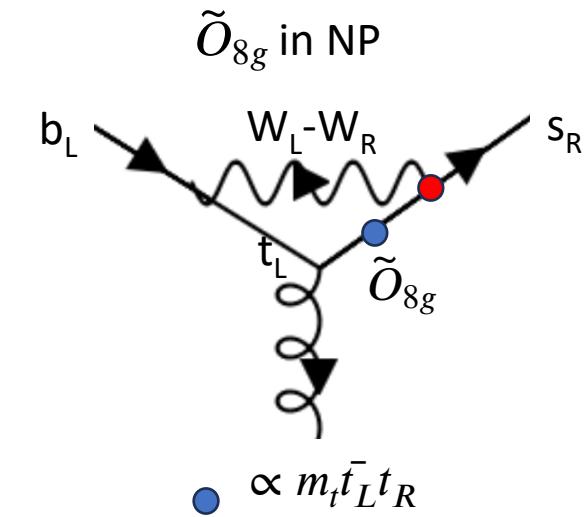
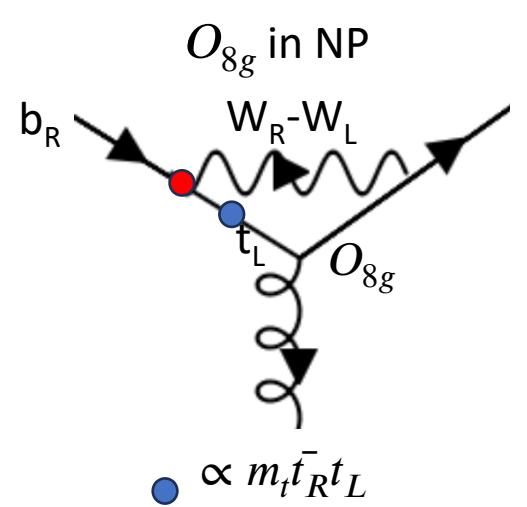
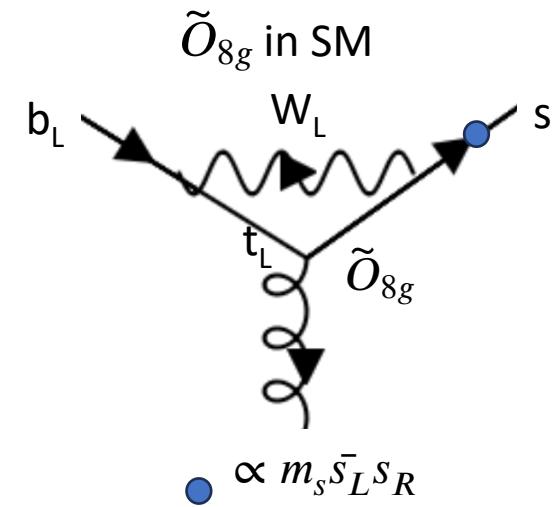
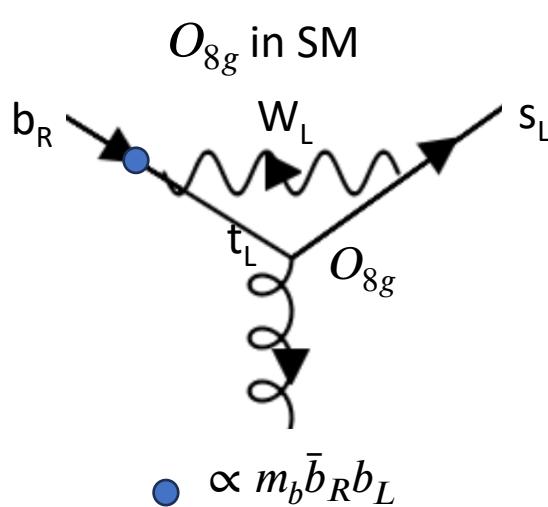
Chromomagnetic Operator (O_{8g}) $b \rightarrow sg$ (g is on-shell)

\tilde{O}_{8g} : O_{8g} with $1 + \gamma^5 \rightarrow 1 - \gamma^5$

$$O_{8g} = \frac{g_s}{8\pi^2} m_b \bar{s}_\alpha \sigma^{\mu\nu} (1 + \gamma^5) \frac{\lambda_{\alpha\beta}^a}{2} b_\beta G_{\mu\nu}^a$$

It's a **suppressed** SM operator

O_{8g} sensitive to NP due to Chiral Enhancement



- Mass Insertion Approximation

- Right-Handed CKM Matrix elements

Chromomagnetic operator sensitive to Right-Handed currents

CP Violating parameters

Total amplitude is sum of SM and NP amplitude (at t=0)

$\delta_k^{SM(NP)}$: Strong phase in SM (NP) ,

$\phi_{(k)}^{SM(NP)}$: Weak phase in SM (NP) ($k = \{ \parallel, \perp, 0 \}$)

$$\begin{aligned} A_k &= A_k^{SM} + A_k^{NP} \\ &= |A_k^{SM}|e^{i\delta_k^{SM}}e^{i\phi^{SM}} + |A_k^{NP}|e^{i\delta_k^{NP}}e^{i\phi_k^{NP}} \\ &= |A_k^{SM}|e^{i\delta_k^{SM}}e^{i\phi^{SM}} \left(1 + r_k^{NP} e^{i(\phi_k^{NP} - \phi^{SM})} e^{i(\delta_k^{NP} - \delta_k^{SM})} \right) \\ &= |A_k^{SM}|e^{i\delta_k^{SM}}e^{i\phi^{SM}} X_k e^{i\theta_k}, \end{aligned}$$

$$\begin{aligned} \bar{A}_k &= \eta_k |A_k^{SM}| e^{i\delta_k^{SM}} e^{-i\phi^{SM}} \left(1 + r_k^{NP} e^{-i(\phi_k^{NP} - \phi^{SM})} e^{i(\delta_k^{NP} - \delta_k^{SM})} \right) \\ &= \eta_k |A_k^{SM}| e^{i\delta_k^{SM}} e^{-i\phi^{SM}} X_k^c e^{i\theta_k^c}. \\ r_k^{NP} &= \frac{|A_k^{NP}|}{|A_k^{SM}|} \end{aligned}$$

$\theta_k^{(c)}$ is a mixture of 'weak' and 'strong' phases!

The interference phase is then given by $\theta_k - \theta_k^c$

$$\frac{q}{p} \frac{\bar{A}_k}{A_k} = \eta_k \lambda_k e^{-i(\theta_k - \theta_k^c)}$$

NP Search - Null-test parameters:

1. Interference Phase

$(\theta_k - \theta_k^c = 0 \text{ in SM})$

2. Direct CP Violation parameter

$(\lambda_k - 1 = 0 \text{ in SM})$



"If these quantities deviate from 0, it indicates the presence of NP!"

New Physics Model: Chromomagnetic Operator

- Effective Hamiltonian of $B_s^0 \rightarrow \phi\phi$ decay:

$$\mathcal{H}_{\text{eff}} = -\frac{G_F}{\sqrt{2}} V_{tb}^* V_{tq} \left[\sum_{i=3}^6 (C_i^{\text{SM}} O_i) + C_{8g} O_{8g} + \tilde{C}_{8g} \tilde{O}_{8g} \right] + \text{h.c.}$$

$$O_{8g} = \frac{g_s}{8\pi^2} m_b \bar{b}_\alpha \sigma^{\mu\nu} (1 + \gamma^5) \frac{\lambda_{\alpha\beta}^a}{2} s_\beta G_{\mu\nu}^a.$$

- Amplitude: $B_s^0 \rightarrow \phi\phi$ final state has three helicity states \Rightarrow three amplitudes

A_k : Transversity Amplitudes	$A_0 = H_0, \quad A_{\parallel} = \frac{1}{\sqrt{2}}(H_+ + H_-), \quad A_{\perp} = \frac{1}{\sqrt{2}}(H_+ - H_-)$	H_k : Helicity Amplitudes
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- Hierarchy of amplitudes (V-A structure of current)

$$H_0 : H_+ : H_- \approx 1 : \left(\frac{\Lambda_{\text{QCD}}}{m_b}\right) : \left(\frac{\Lambda_{\text{QCD}}}{m_b}\right)^2$$

Ann. diagrams contribute to transverse amplitudes
BUT
Followed in O_{8g} (Ann. contribution subsubleading)



“Contribution from O_{8g} is suppressed in Transverse Penguin Operator”

New Fit Configuration

- Total NP Amplitude (longitudinal):

$$\mathcal{M}_{0,\phi\phi}^{\text{Total}} = -\frac{G_F}{\sqrt{2}} V_{tb}^* V_{ts} (\xi_0^{\text{SM}} \mathcal{F}_{0,\phi\phi}^{\text{SM}} + \xi_0^L \mathcal{F}_{0,\phi\phi}^{\text{NP}} - \xi_0^R \mathcal{F}_{0,\phi\phi}^{\text{NP}})$$



Notice Sign Change! Comes from V^\pm

- Our Fit Scheme

$$\frac{q}{p} \frac{\bar{\mathcal{M}}_{0,\phi\phi}^{\text{Total}}}{\mathcal{M}_{0,\phi\phi}^{\text{Total}}} = \lambda_0 e^{-i(\theta_0 - \theta_0^c)}$$

 $\theta_{||} = \theta_{||}^c = \theta_{\perp} = \theta_{||}^c = 0$ and
 $\lambda_{||} = \lambda_{\perp} = 1$ and (SM Values).
 λ_0 and $\theta_0 - \theta_0^c$ are free parameters.

$\mathcal{F}_0^p(p = \{\text{SM}, \text{NP}\})$ contains contribution from matrix elements (can be calculated in any model)

- contains strong (CP -even) phases (σ)

$\xi_0^h(h = \{\text{SM}, \text{L}, \text{R}\})$ are combination of Wilson Coefficients

- *A structure of current contains weak (CP -odd) phases (ω_L, ω_R)*

- LHCb Fit Scheme ($\phi_k = \theta_k - \theta_k^c$)

Helicity-Independent (HI) Scheme:

$$\lambda_k = \lambda, \phi_k = \phi \quad \forall k \in \{0, ||, \perp\}.$$

Free parameters: ϕ and λ .

Helicity-Dependent (HD) Scheme:

$$\phi_0 = 0, \lambda_k = 1 \quad \forall k \in \{0, ||, \perp\}.$$

Free parameters: $\phi_{||}$ and ϕ_{\perp} .

LHCb arXiv: 1907.10003 [hep-ex]

Chromomagnetic dipole operator

The Chromomagnetic operator for $\bar{b} \rightarrow \bar{s}g$ is given by

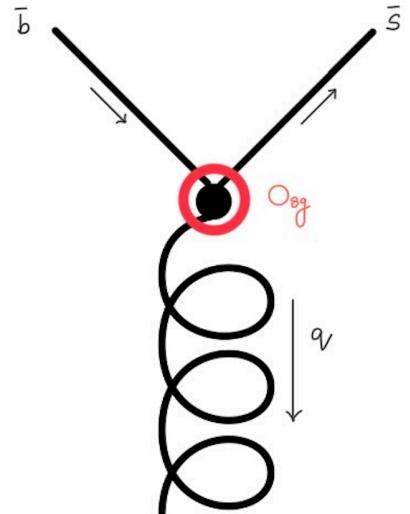
$$O_{8g} = \frac{g_s}{8\pi^2} m_b \bar{b}_\alpha \sigma^{\mu\nu} (1 + \gamma^5) \frac{\lambda_{\alpha\beta}^a}{2} s_\beta G_{\mu\nu}^a.$$

To make it a 4-quark operator (in order to write the matrix elements): attach a quark current

$$O_{8g}^4 = \frac{\alpha_s}{\pi} \frac{m_b}{q^2} \bar{b}_\alpha \gamma^\mu q (1 + \gamma^5) \frac{\lambda_{\alpha\beta}^a}{2} s_\beta \bar{q}'_\rho \gamma_\mu \frac{\lambda_{\rho\sigma}^a}{2} q'_\sigma$$

Simplifying approximation: $q^\mu = \sqrt{\langle q^2 \rangle} \frac{p_b^\mu}{m_b}$

(for two body decays, when the 3-momenta of two quarks coming from gluon has same magnitude but opposite direction in b -quark rest frame)



Using Fierz identity and Dirac equation, we express

$$\frac{\lambda_{\alpha\beta}^a}{2} \frac{\lambda_{\rho\sigma}^a}{2} = \frac{1}{2} (\delta_{\alpha\sigma} \delta_{\beta\rho} - \frac{1}{3} \delta_{\alpha\beta} \delta_{\rho\sigma})$$

Effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = -\frac{G_F}{\sqrt{2}} V_{tb}^* V_{tq} \sum_{i=3}^6 (C_i^{\text{SM}} O_i + C_i^{\text{L}} O_i + C_i^{\text{R}} \tilde{O}_i)$$

$$\langle O_{8g}^4 \rangle = \frac{\alpha_s}{4\pi} \frac{m_b}{\sqrt{\langle q^2 \rangle}} \left[\langle O_4 \rangle + \langle O_6 \rangle - \frac{1}{3} (\langle O_3 \rangle + \langle O_5 \rangle) \right]$$

Effective Wilson Coefficients

$$C_{3,5}^{\text{L(R)}} = -\frac{1}{3} \frac{\alpha_s}{4\pi} \frac{m_b}{\sqrt{\langle q^2 \rangle}} \tilde{C}_{8g}$$

$$C_{4,6}^{\text{L(R)}} = \frac{\alpha_s}{4\pi} \frac{m_b}{\sqrt{\langle q^2 \rangle}} \tilde{C}_{8g}$$

Effect of Rescattering

With dominant t -quark contribution, we can have c - and u - quark contribution too which can arise due to $c\bar{c} \rightarrow q\bar{q}$ and $u\bar{u} \rightarrow q\bar{q}$ rescattering from $\bar{b} \rightarrow \bar{c}c\bar{s}$ and $\bar{b} \rightarrow \bar{u}u\bar{s}$ tree diagrams.

$$A_k^{\text{SM}} = \lambda_t P_{t,k} + \lambda_c R_{c,k} + \lambda_u R_{u,k} \quad \lambda_q = V_{qb}^* V_{qs}$$

Using Unitarity to eliminate c-quark term

$$\begin{aligned} A_k^{\text{SM}} &= |V_{tb}^* V_{ts}| e^{-i\beta_s} |PR_{tc,k}| e^{i\delta_{tc,k}} + |V_{ub}^* V_{us}| e^{i\gamma} |RR_{uc,k}| e^{i\delta_{uc,k}} \\ &= |V_{tb}^* V_{ts}| e^{-i\beta_s} |PR_{tc,k}| e^{i\delta_{tc,k}} \left[1 + r_k^{\text{SM}} e^{i(\gamma+\beta_s)} e^{i(\delta_{uc,k} - \delta_{tc,k})} \right] \\ &= |A_k^{\text{SM}}| e^{i\phi^{\text{SM}}} e^{i\delta_k^{\text{SM}}}, \end{aligned}$$

$$r_k^{\text{SM}} = \frac{|V_{ub}^* V_{us}| |RR_{uc,k}|}{|V_{tb}^* V_{ts}| |PR_{tc,k}|}$$

Depending upon rescattering contribution (say, 20-40% of dominant penguin amplitude) $\Rightarrow r_k^{\text{SM}} = O(\lambda^3)$

If CP violating observables are $O(\lambda^3)$ away from their SM value, it indicates NP!

New LHCb Results

Helicity-Independent Fit

LHCb arXiv: 2304.06198 [hep-ex]

Parameter	Result
ϕ_s^{sss} [rad]	$-0.042 \pm 0.075 \pm 0.009$
$ \lambda $	$1.004 \pm 0.030 \pm 0.009$
$ A_0 ^2$	$0.384 \pm 0.007 \pm 0.003$
$ A_\perp ^2$	$0.310 \pm 0.006 \pm 0.003$
$\delta_{\parallel} - \delta_0$ [rad]	$2.463 \pm 0.029 \pm 0.009$
$\delta_{\perp} - \delta_0$ [rad]	$2.769 \pm 0.105 \pm 0.011$

Issues:

Large Errors

No information given as to how the Helicity-Dependent fit done

No details of approximations

When doing HD fit, nuisance parameters (strong phases and amplitudes not given)

Helicity-Dependent Fit

$$\phi_{s,0} = -0.18 \pm 0.09 \text{ rad ,}$$

$$|\lambda_0| = 1.02 \pm 0.17$$

$$\phi_{s,\parallel} - \phi_{s,0} = 0.12 \pm 0.09 \text{ rad ,}$$

$$|\lambda_\perp/\lambda_0| = 0.97 \pm 0.22$$

$$\phi_{s,\perp} - \phi_{s,0} = 0.17 \pm 0.09 \text{ rad ,}$$

$$|\lambda_\parallel/\lambda_0| = 0.78 \pm 0.21$$

Sensitivity Study: Toy Monte-Carlo Method

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*arXiv: 2303.04494
T.K., E. Kou*

Generate pseudo data from “truth values”

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Generate pseudo data from “truth values”

When we have large (infinite) statistics ($N \rightarrow \infty$):

- MLE gives truth values
- Sensitivity (σ) $\rightarrow 0$

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$$\text{Covariance Matrix} \longrightarrow V_{ij}^{-1} = N \int \left(\frac{\partial \hat{f}(x)_{\vec{v}}}{\partial v_i} \frac{\partial \hat{f}(x)_{\vec{v}}}{\partial v_j} \frac{1}{\hat{f}(x)_{\vec{v}}} \right) \Big|_{\vec{v}=\vec{v}^*} dx$$

Number of events

Parameters of Interest ($\delta_k, \theta_k \dots$)

Truth Values (Experimental Results)

Normalised PDF (Angular Decay Distribution)

Phase Space (angles, time)

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Parameters of Interest ($\delta_k, \theta_k\dots$) Truth Values (Experimental Results)

Number of events Normalised PDF (Angular Decay Distribution)

Phase Space (angles, time)

The diagram illustrates the components of the covariance matrix formula. It shows the formula $V_{ij}^{-1} = N \int \left(\frac{\partial \hat{f}(x)_{\vec{v}}}{\partial v_i} \frac{\partial \hat{f}(x)_{\vec{v}}}{\partial v_j} \frac{1}{\hat{f}(x)_{\vec{v}}} \right) \Big|_{\vec{v}=\vec{v}^*} dx$. Above the formula, 'Parameters of Interest ($\delta_k, \theta_k\dots$)' and 'Truth Values (Experimental Results)' are listed. Below the formula, 'Number of events' and 'Normalised PDF (Angular Decay Distribution)' are listed. To the right, 'Phase Space (angles, time)' is mentioned. Blue arrows indicate the flow of information: one arrow points from 'Number of events' to the integral sign; another points from 'Normalised PDF (Angular Decay Distribution)' to the denominator; and a third points from 'Phase Space (angles, time)' to the differential dx .

Advantages: **Fast** and **Easy** to program

Experimental Observables: LHCb Version

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Transversity Amplitude:

$$A_k = |A_k| e^{i\delta_k} \xrightarrow{\text{Strong Phase}}$$

Approximate Parameterisation
(no weak phase, single amp. (SM))

LHCb arXiv 1907.10003

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η_k : CP eigenvalue of
the transversity state
($\eta_{0,\parallel} = 1$, $\eta_\perp = -1$)

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$$\frac{q \bar{A}_k}{p A_k} = \eta_k |\lambda_k| e^{-i\phi_{s,k}} \longrightarrow \begin{array}{l} \text{Interference Phase (Hel. Dep.)} \\ \text{Direct CP Measurement} \\ \text{Parameter} \end{array}$$

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LHCb arXiv 1907.10003

i	N_i	a_i	b_i	c_i	d_i	f_i
1	$ A_0 ^2$	$1 + \lambda_0 ^2$	$-2 \lambda_0 \cos(\phi)$	$1 - \lambda_0 ^2$	$2 \lambda_0 \sin(\phi)$	$4 \cos^2 \theta_1 \cos^2 \theta_2$
2	$ A_{\parallel} ^2$	$1 + \lambda_{\parallel} ^2$	$-2 \lambda_{\parallel} \cos(\phi_{s,\parallel})$	$1 - \lambda_{\parallel} ^2$	$2 \lambda_{\parallel} \sin(\phi_{s,\parallel})$	$\sin^2 \theta_1 \sin^2 \theta_2 (1 + \cos 2\Phi)$
3	$ A_{\perp} ^2$	$1 + \lambda_{\perp} ^2$	$2 \lambda_{\perp} \cos(\phi_{s,\perp})$	$1 - \lambda_{\perp} ^2$	$-2 \lambda_{\perp} \sin(\phi_{s,\perp})$	$\sin^2 \theta_1 \sin^2 \theta_2 (1 - \cos 2\Phi)$
4	$\frac{ A_{\parallel} A_{\perp} }{2}$	$\begin{aligned} &\sin(\delta_{\parallel} - \delta_{\perp}) - \lambda_{\parallel} \lambda_{\perp} \cdot \\ &\sin(\delta_{\parallel} - \delta_{\perp} - \phi_{s,\parallel} + \phi_{s,\perp}) \end{aligned}$	$\begin{aligned} &- \lambda_{\parallel} \sin(\delta_{\parallel} - \delta_{\perp} - \phi_{s,\parallel}) \\ &+ \lambda_{\perp} \sin(\delta_{\parallel} - \delta_{\perp} + \phi_{s,\perp}) \end{aligned}$	$\begin{aligned} &\sin(\delta_{\parallel} - \delta_{\perp}) + \lambda_{\parallel} \lambda_{\perp} \cdot \\ &\sin(\delta_{\parallel} - \delta_{\perp} - \phi_{s,\parallel} + \phi_{s,\perp}) \end{aligned}$	$\begin{aligned} & \lambda_{\parallel} \cos(\delta_{\parallel} - \delta_{\perp} - \phi_{s,\parallel}) \\ &+ \lambda_{\perp} \cos(\delta_{\parallel} - \delta_{\perp} + \phi_{s,\perp}) \end{aligned}$	$-2 \sin^2 \theta_1 \sin^2 \theta_2 \sin 2\Phi$
5	$\frac{ A_{\parallel} A_0 }{2}$	$\begin{aligned} &\cos(\delta_{\parallel} - \delta_0) + \lambda_{\parallel} \lambda_0 \cdot \\ &\cos(\delta_{\parallel} - \delta_0 - \phi_{s,\parallel} + \phi) \end{aligned}$	$\begin{aligned} &- \lambda_{\parallel} \cos(\delta_{\parallel} - \delta_0 - \phi_{s,\parallel}) \\ &+ \lambda_0 \cos(\delta_{\parallel} - \delta_0 + \phi) \end{aligned}$	$\begin{aligned} &\cos(\delta_{\parallel} - \delta_0) - \lambda_{\parallel} \lambda_0 \cdot \\ &\sin(\delta_{\parallel} - \delta_0 - \phi_{s,\parallel} + \phi) \end{aligned}$	$\begin{aligned} &- \lambda_{\parallel} \sin(\delta_{\parallel} - \delta_0 - \phi_{s,\parallel}) \\ &+ \lambda_0 \sin(\delta_{\parallel} - \delta_0 + \phi) \end{aligned}$	$\sqrt{2} \sin 2\theta_1 \sin 2\theta_2 \cos \Phi$
6	$\frac{ A_0 A_{\perp} }{2}$	$\begin{aligned} &\sin(\delta_0 - \delta_{\perp}) - \lambda_0 \lambda_{\perp} \cdot \\ &\sin(\delta_0 - \delta_{\perp} - \phi + \phi_{s,\perp}) \end{aligned}$	$\begin{aligned} &- \lambda_0 \sin(\delta_0 - \delta_{\perp} - \phi) \\ &+ \lambda_{\perp} \sin(\delta_0 - \delta_{\perp} + \phi_{s,\perp}) \end{aligned}$	$\begin{aligned} &\sin(\delta_0 - \delta_{\perp}) + \lambda_0 \lambda_{\perp} \cdot \\ &\sin(\delta_0 - \delta_{\perp} - \phi + \phi_{s,\perp}) \end{aligned}$	$\begin{aligned} & \lambda_0 \cos(\delta_0 - \delta_{\perp} - \phi) \\ &+ \lambda_{\perp} \cos(\delta_0 - \delta_{\perp} + \phi_{s,\perp}) \end{aligned}$	$-\sqrt{2} \sin 2\theta_1 \sin 2\theta_2 \sin \Phi$

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6	$\frac{ A_0 A_{\perp} }{2}$	$\begin{aligned} &\sin(\delta_0 - \delta_{\perp}) - \lambda_0 \lambda_{\perp} \cdot \\ &\sin(\delta_0 - \delta_{\perp} - \phi + \phi_{s,\perp}) \end{aligned}$	$\begin{aligned} &- \lambda_0 \sin(\delta_0 - \delta_{\perp} - \phi) \\ &+ \lambda_{\perp} \sin(\delta_0 - \delta_{\perp} + \phi_{s,\perp}) \end{aligned}$	$\begin{aligned} &\sin(\delta_0 - \delta_{\perp}) + \lambda_0 \lambda_{\perp} \cdot \\ &\sin(\delta_0 - \delta_{\perp} - \phi + \phi_{s,\perp}) \end{aligned}$	$\begin{aligned} & \lambda_0 \cos(\delta_0 - \delta_{\perp} - \phi) \\ &+ \lambda_{\perp} \cos(\delta_0 - \delta_{\perp} + \phi_{s,\perp}) \end{aligned}$	$-\sqrt{2} \sin 2\theta_1 \sin 2\theta_2 \sin \Phi$

CP Violating parameters are inside the experimental observables

Experimental Observables: LHCb Version

Transversity Amplitude:

$$A_k = |A_k| e^{i\delta_k} \xrightarrow{\text{Strong Phase}}$$

Approximate Parameterisation
(no weak phase, single amp. (SM))

$$\frac{q \bar{A}_k}{p A_k} = \eta_k |\lambda_k| e^{-i\phi_{s,k}} \xrightarrow{\text{Interference Phase (Hel. Dep.)}}$$

$$\xrightarrow{\text{Direct CP Measurement Parameter}}$$

η_k : CP eigenvalue of
the transversity state
($\eta_{0,\parallel} = 1, \eta_{\perp} = -1$)

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i	N_i	a_i	b_i	c_i	d_i	f_i
1	$ A_0 ^2$	$1 + \lambda_0 ^2$	$-2 \lambda_0 \cos(\phi)$	$1 - \lambda_0 ^2$	$2 \lambda_0 \sin(\phi)$	$4 \cos^2 \theta_1 \cos^2 \theta_2$
2	$ A_{\parallel} ^2$	$1 + \lambda_{\parallel} ^2$	$-2 \lambda_{\parallel} \cos(\phi_{s,\parallel})$	$1 - \lambda_{\parallel} ^2$	$2 \lambda_{\parallel} \sin(\phi_{s,\parallel})$	$\sin^2 \theta_1 \sin^2 \theta_2 (1 + \cos 2\Phi)$
3	$ A_{\perp} ^2$	$1 + \lambda_{\perp} ^2$	$2 \lambda_{\perp} \cos(\phi_{s,\perp})$	$1 - \lambda_{\perp} ^2$	$-2 \lambda_{\perp} \sin(\phi_{s,\perp})$	$\sin^2 \theta_1 \sin^2 \theta_2 (1 - \cos 2\Phi)$
4	$\frac{ A_{\parallel} A_{\perp} }{2}$	$\sin(\delta_{\parallel} - \delta_{\perp}) - \lambda_{\parallel} \lambda_{\perp} \cdot$ $\sin(\delta_{\parallel} - \delta_{\perp} - \phi_{s,\parallel} + \phi_{s,\perp})$	$- \lambda_{\parallel} \sin(\delta_{\parallel} - \delta_{\perp} - \phi_{s,\parallel})$ $+ \lambda_{\perp} \sin(\delta_{\parallel} - \delta_{\perp} + \phi_{s,\perp})$	$\sin(\delta_{\parallel} - \delta_{\perp}) + \lambda_{\parallel} \lambda_{\perp} \cdot$ $\sin(\delta_{\parallel} - \delta_{\perp} - \phi_{s,\parallel} + \phi_{s,\perp})$	$ \lambda_{\parallel} \cos(\delta_{\parallel} - \delta_{\perp} - \phi_{s,\parallel})$ $+ \lambda_{\perp} \cos(\delta_{\parallel} - \delta_{\perp} + \phi_{s,\perp})$	$-2 \sin^2 \theta_1 \sin^2 \theta_2 \sin 2\Phi$
5	$\frac{ A_{\parallel} A_0 }{2}$	$\cos(\delta_{\parallel} - \delta_0) + \lambda_{\parallel} \lambda_0 \cdot$ $\cos(\delta_{\parallel} - \delta_0 - \phi_{s,\parallel} + \phi)$	$- \lambda_{\parallel} \cos(\delta_{\parallel} - \delta_0 - \phi_{s,\parallel})$ $+ \lambda_0 \cos(\delta_{\parallel} - \delta_0 + \phi)$	$\cos(\delta_{\parallel} - \delta_0) - \lambda_{\parallel} \lambda_0 \cdot$ $\sin(\delta_{\parallel} - \delta_0 - \phi_{s,\parallel} + \phi)$	$- \lambda_{\parallel} \sin(\delta_{\parallel} - \delta_0 - \phi_{s,\parallel})$ $+ \lambda_0 \sin(\delta_{\parallel} - \delta_0 + \phi)$	$\sqrt{2} \sin 2\theta_1 \sin 2\theta_2 \cos \Phi$
6	$\frac{ A_0 A_{\perp} }{2}$	$\sin(\delta_0 - \delta_{\perp}) - \lambda_0 \lambda_{\perp} \cdot$ $\sin(\delta_0 - \delta_{\perp} - \phi + \phi_{s,\perp})$	$- \lambda_0 \sin(\delta_0 - \delta_{\perp} - \phi)$ $+ \lambda_{\perp} \sin(\delta_0 - \delta_{\perp} + \phi_{s,\perp})$	$\sin(\delta_0 - \delta_{\perp}) + \lambda_0 \lambda_{\perp} \cdot$ $\sin(\delta_0 - \delta_{\perp} - \phi + \phi_{s,\perp})$	$ \lambda_0 \cos(\delta_0 - \delta_{\perp} - \phi)$ $+ \lambda_{\perp} \cos(\delta_0 - \delta_{\perp} + \phi_{s,\perp})$	$-\sqrt{2} \sin 2\theta_1 \sin 2\theta_2 \sin \Phi$

CP Violating parameters are inside the experimental observables

Many experimental observables, only few parameters that can be fit!

η_k factor origin

Here, we take a moment to explain the η_k factors used. When we write the CP conjugate decay, we replace the particles by their antiparticles. The effect of this replacement on the helicity angle is $\phi \rightarrow 2\pi - \phi$, which gives rise to a negative sign in those terms which contain amplitudes having a negative CP parity (A_\perp in our case). Therefore, using η_k in the definition of amplitude allows us to use the same angular functions for B_s^0 and \bar{B}_s^0 decays, which facilitates calculations in untagged samples [23].