



# Testing cosmological models with massive black hole binaries

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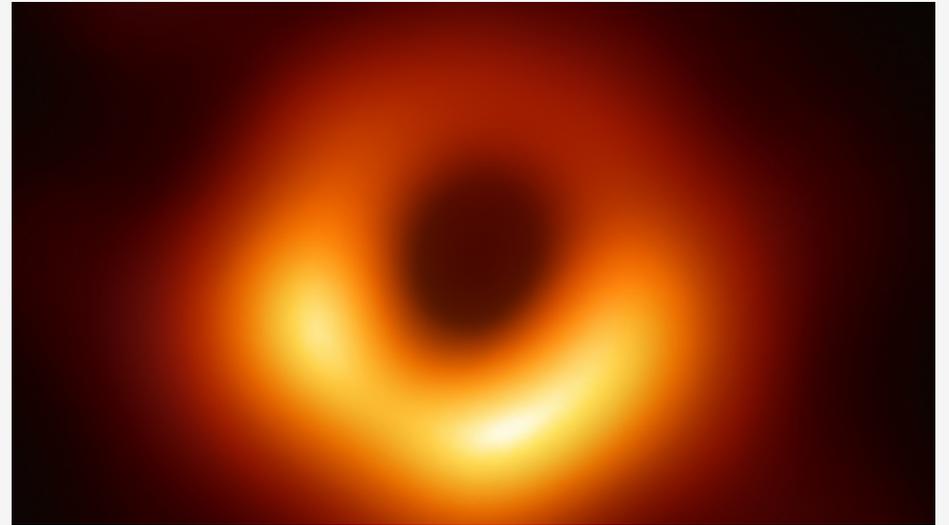
Astroparticule et Cosmologie (APC), Paris

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# What are massive black holes (MBHs)?

We currently believe that MBHs are hosted at the center of galaxies with masses up to  $\sim 10^9 - 10^{10} M_{\odot}$

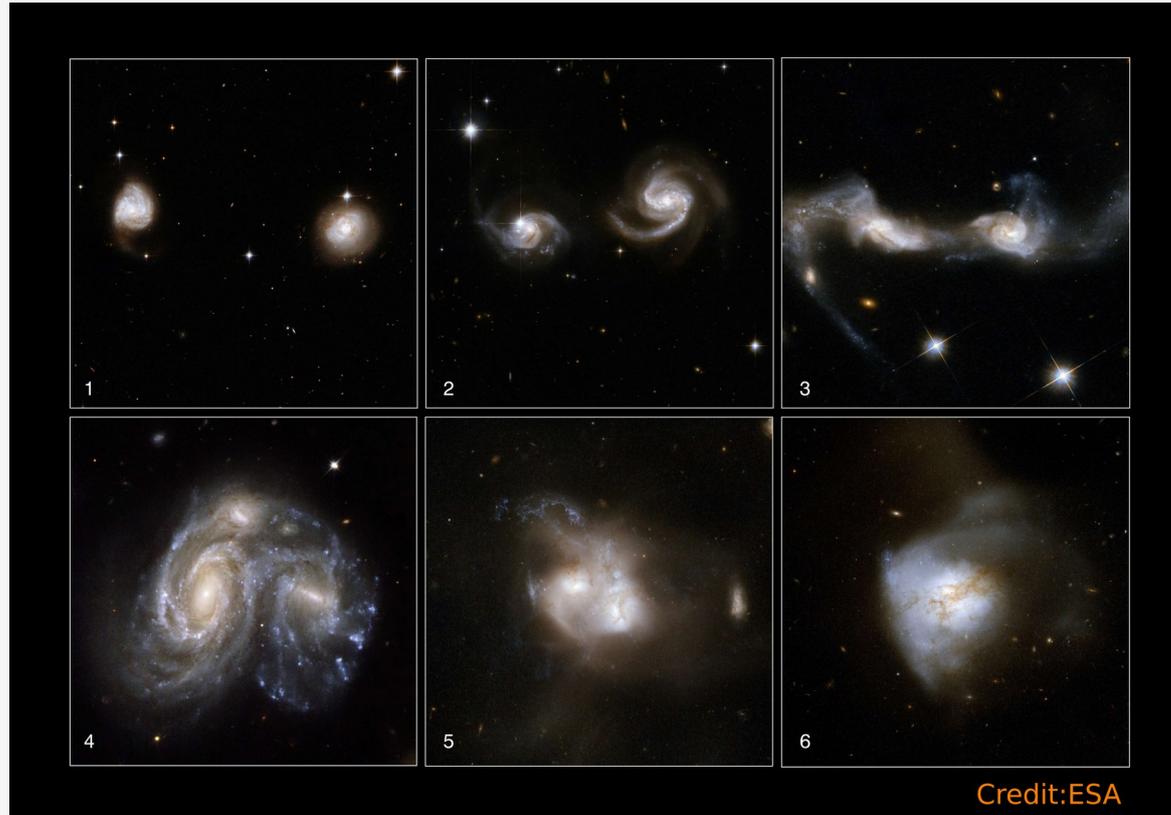


For today talk, let's focus on the interval

$$M_{\text{BH}} \sim 10^{4-7} M_{\odot}$$

# From single MBH to binaries

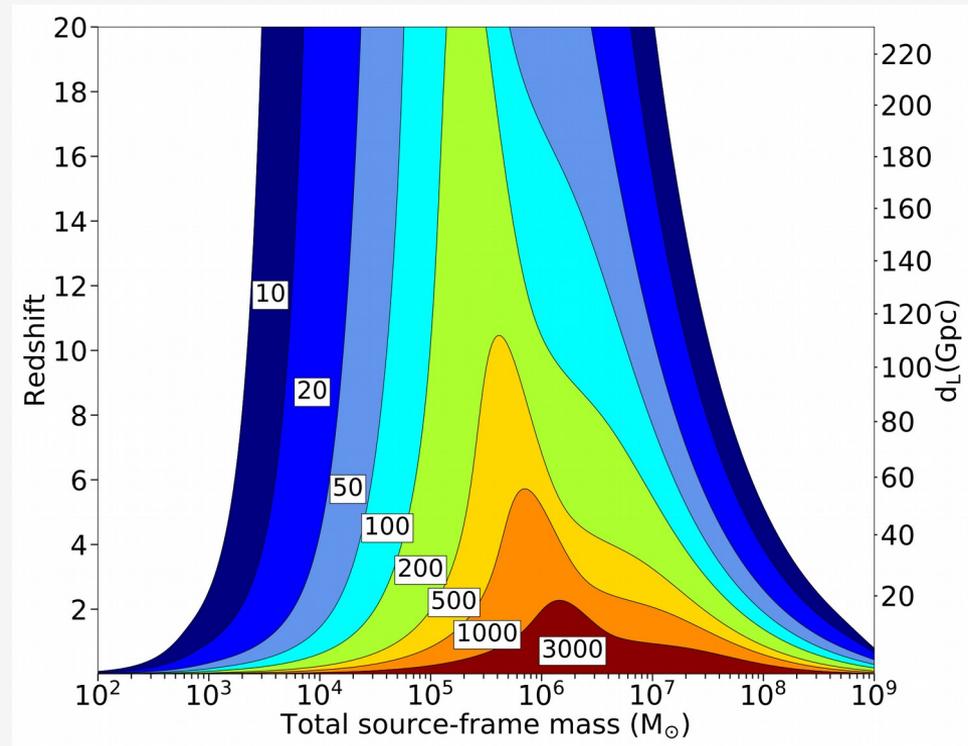
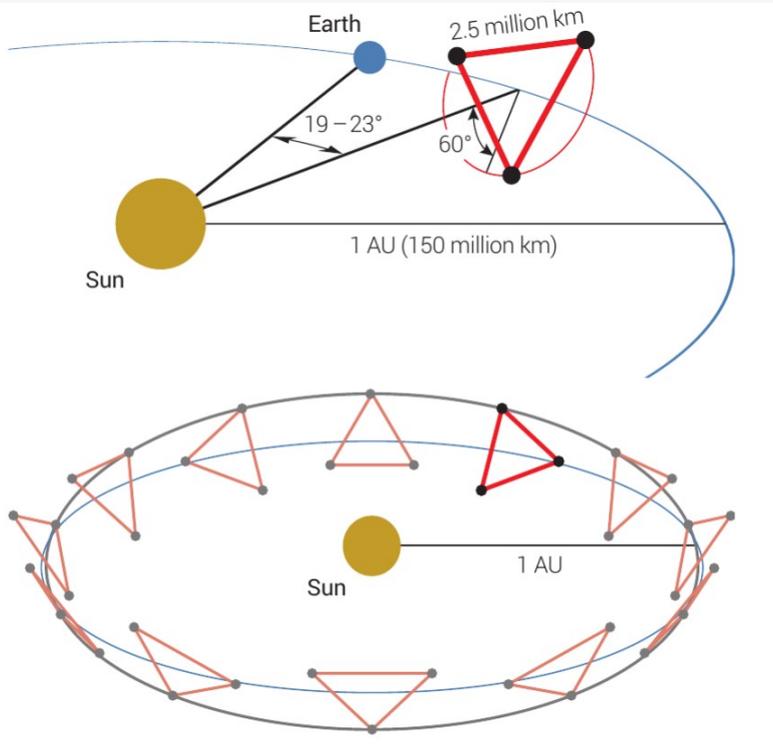
When two galaxies merge, the MBHs in their center form a binary and merge emitting gravitational waves (GWs) and electromagnetic (EM)/particles radiation



# Observing the entire Universe with GWs

In mid-2030s LISA (Laser Interferometer Space Antenna) will observe the GWs from the coalescence of MBHBs in the entire Universe (ArXiv:1702.00786)

- 3rd Large class mission selected by European Space Agency (ESA)
- Now in Phase B1 - Mission adoption in January 2024



# MBHBs : new cosmological probes

The  $\Lambda$ -Cold Dark Matter ( $\Lambda$ CDM) is the most common cosmological parametrization:

- ✓ Simple model with good fit to the bulk of data
- ✗ Current tensions :
  - Early Universe: Cosmic Microwave Background (CMB) observations at  $z > 1000$
  - Late Universe: SNIa, lensed images at  $z \sim 2.5$

We need new models and new probes!

Standard sirens are new cosmological probes

- Direct information on  $d_L \rightarrow$  No calibration errors and no intrinsic scatter
- Independent from CMB or SNIa  $\rightarrow$  Independent estimates

Bright sirens, i.e. Redshift information from the EM counterpart

What constraints can we put on the expansion of the Universe at high redshift with bright MBHBs?

## Key improvements respect to previous works (Tamanini+16)

- Improve the modeling of the EM counterpart
- Bayesian analysis for GW signal (Marsat+20) → expensive but realistic
- Bayesian cosmological inference

## Starting point

- Semi-analytical models: tools to construct MBHBs catalogs (Barausse+12)

### Three astrophysical models

Light

From PopIII stars

BHs  $\sim 10^3 M_{\odot}$

Heavy

From the collapse of  
hydrogen cloud

BHs  $\sim 10^{4-6} M_{\odot}$

Heavy-no-delays

Same as Q3d but  
without delay times

# Constructing the population of MBHBs with EM counterpart

In AM+2207.10678 we estimate the rate of MBHBs with a detectable EM counterpart

## Observing strategies

### Optical

*LSST, Rubin Obs.*

- FOV  $\sim 10 \text{ deg}^2$
- Identification+redshift

### Radio

*SKA*

- FOV  $\sim 10 \text{ deg}^2$
- Redshift with ELT

### X-Ray

*Athena*

- FOV  $\sim 0.4 \text{ deg}^2$
- Redshift with ELT

We also explored the possibility of AGN obscuration and collimated radio emission

## Number of EMcp in 4 yr

- Strong decrease with obscuration and radio jet
- Parameter estimation selects preferentially heavy models

(In 4 yr)	Standard	w Obsc./Colli. radio
Light	6.4	1.6
Heavy	14.8	3.3
Heavy-no-delays	20.7	3.5

Here we focus on the ‘Standard’ case

# Overview of cosmological models in our study (AM+23, in prep.)

## $\Lambda$ CDM Universe

- $\Lambda$ CDM parametrization  
2-parameters model:  $(H_0, \Omega_m)$

## Dark energy/modified gravity

- CPL parametrization for  $\omega(z)$   
4-parameters model:  $(H_0, \Omega_m, \omega_0, \omega_a)$
- Phenomenological Tracker model (Bull+20)  
6-parameters model:  $(H_0, \Omega_m, \omega_0, \omega_\infty, z_c, \Delta z)$   
(work in progress)
- Sign-switching  $\Lambda$  (Akarsu+23)  
3-parameters model:  $(H_0, \Omega_m, z_\dagger)$   
(work in progress)
- Phenomen. modified gravity (Belgacem+19)  
2-parameters model:  $(\Xi_0, n)$

## At high redshift

- Redshift bins approach  
Model-independent  
2-parameter models:  $d_C(z_p), H(z_p)$
- Matter-only approximation  
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- Splines interpolation  
Model-independent  
Constrain at any redshift  $< 6$

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# Matter-only approximation

Fit:  $d_C(z) = d_C(z_p) + 2(1+z_p)H^{-1}(z_p) \left( 1 - \frac{\sqrt{1+z_p}}{\sqrt{1+z}} \right)$

with 10yr of LISA observations

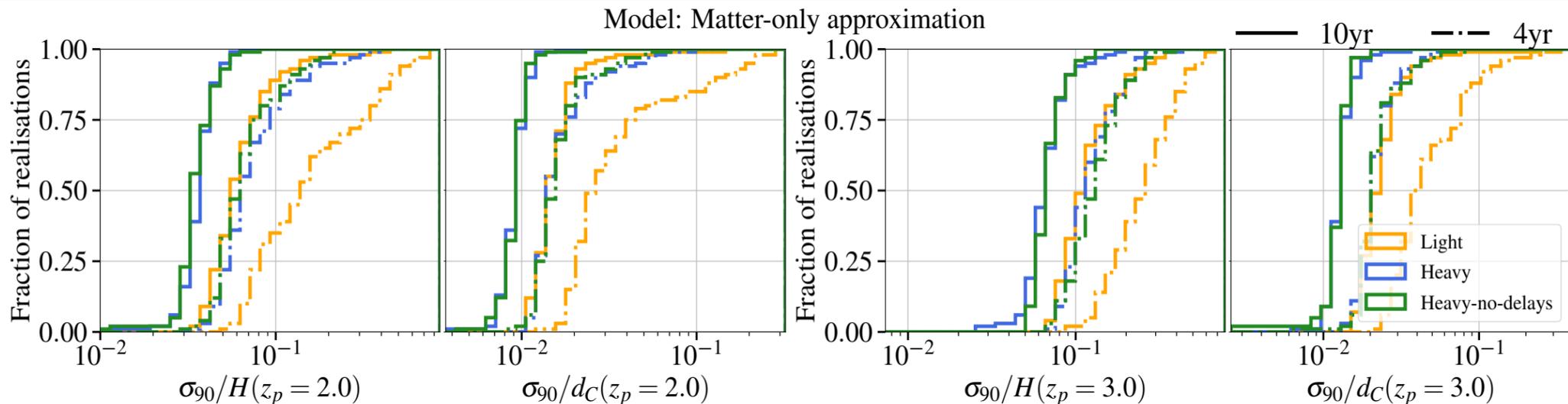
(in 4yr)	$z_p = 2, z > 1$	$z_p = 3, z > 1.5$
Light	5.3	4.4
Heavy	12.5	10.9
Heavy-no-delays	17.3	14.5

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$H(z=2)$  constrained to few percent  
and  $H(z=3) \sim 10\%$

# Splines interpolation

Fit: Luminosity distance at 6 fixed knots  
redshifts at [0, 0.2, 0.7, 2, 4, 6]  
with 10yr of LISA observations

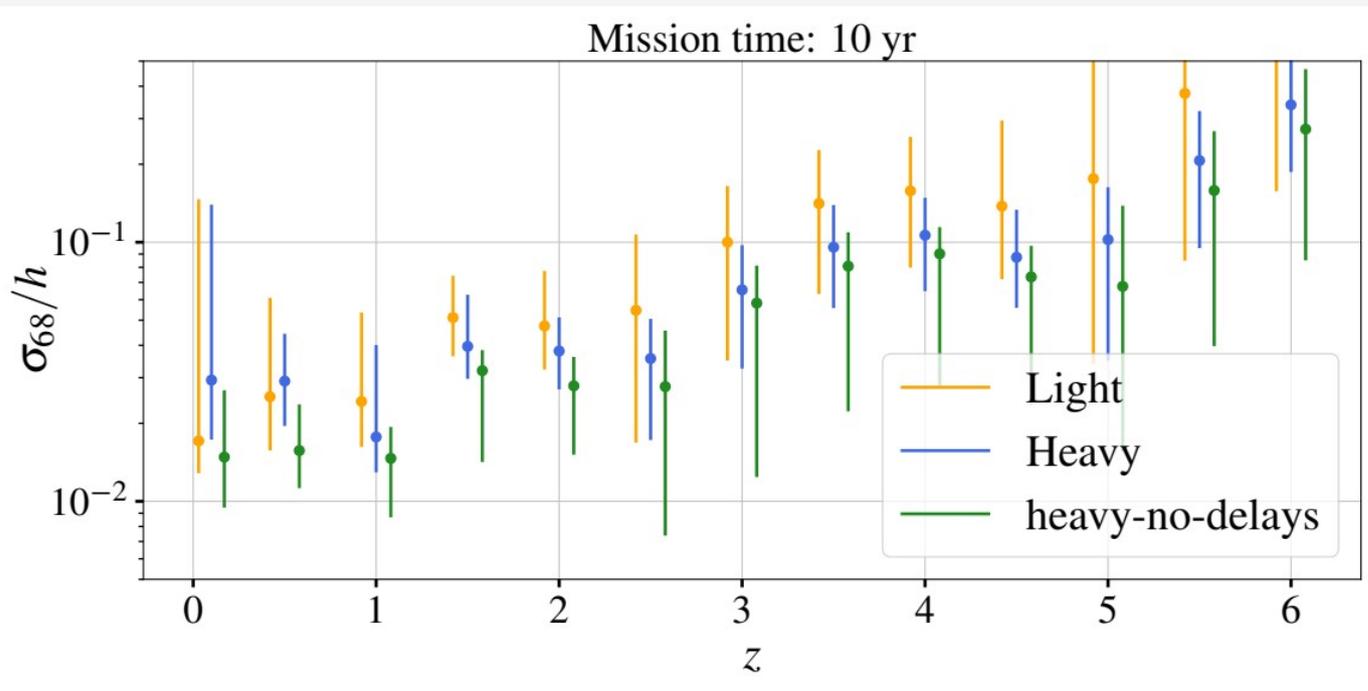
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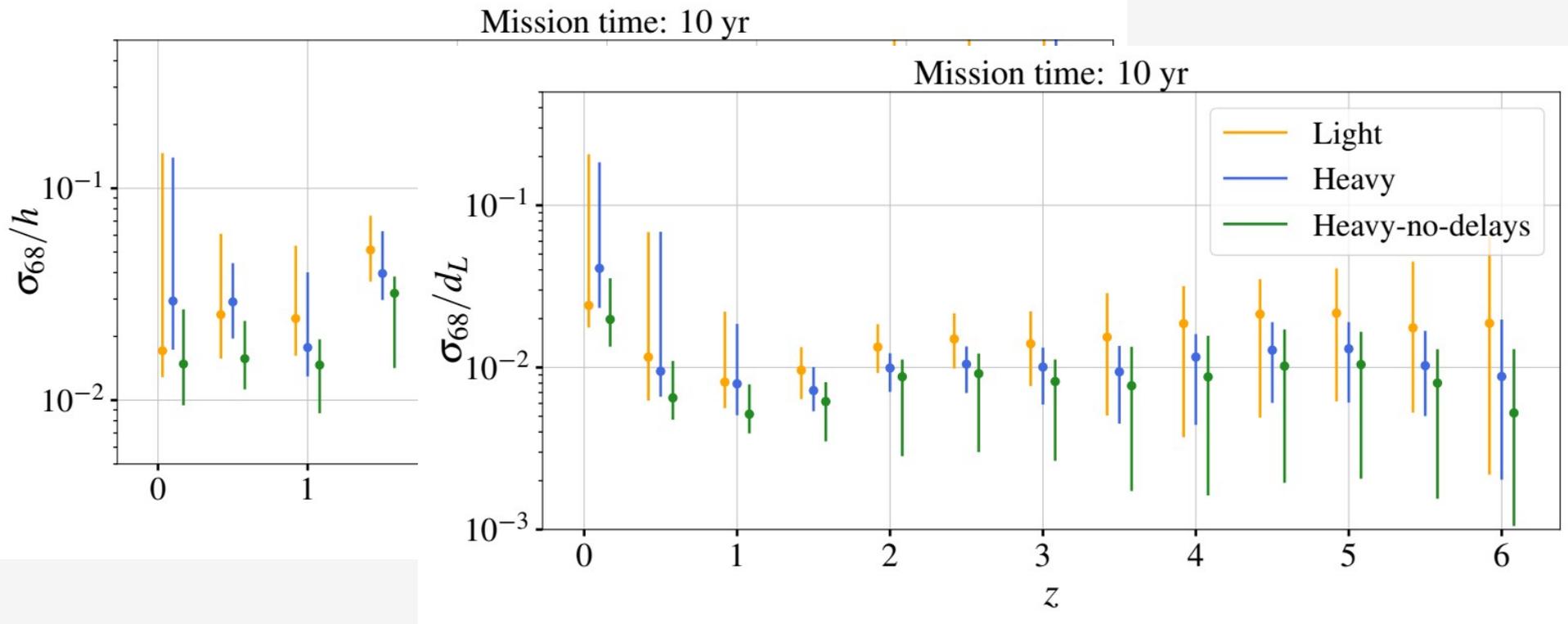


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# Conclusion

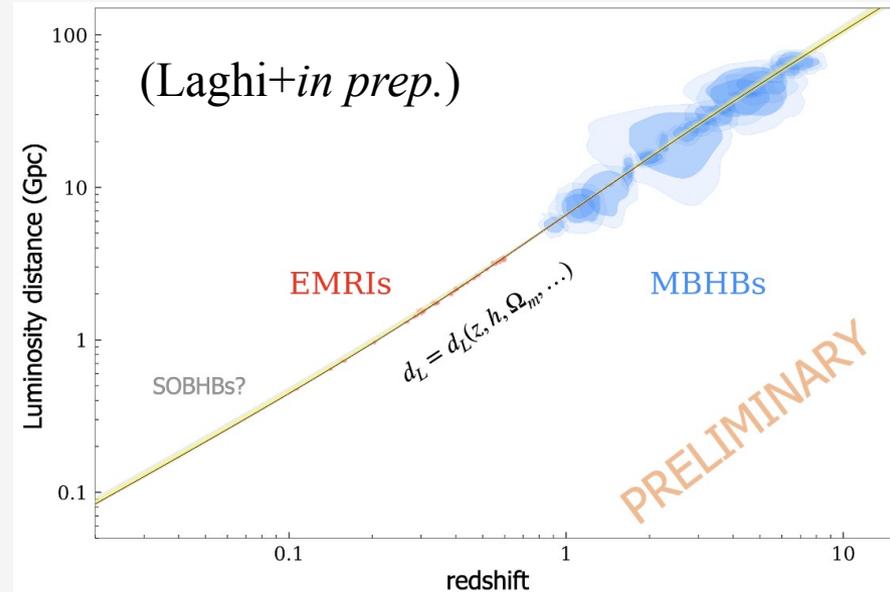
Cosmology with bright sirens will be challenging

## From the current results

- Potential to constrain  $H(z)$  at high redshifts
- Information also on the comoving distance
- Strong dependence from the EM counterpart

## Prospects for the future

- Need better modeling for the EM counterpart
- Combine MBHBs with other LISA sources as SOBHBs and EMRIs



# Conclusion

Cosmology with bright sirens will be challenging

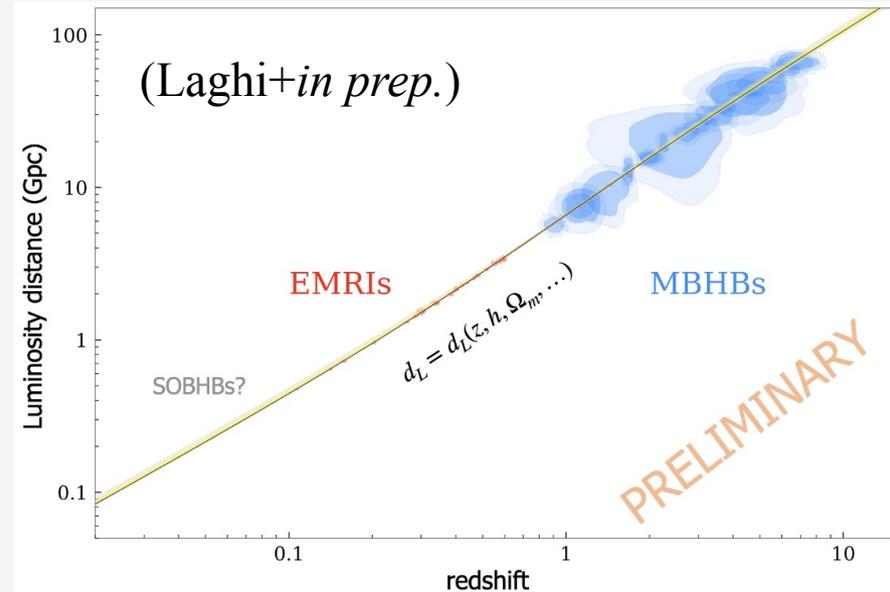
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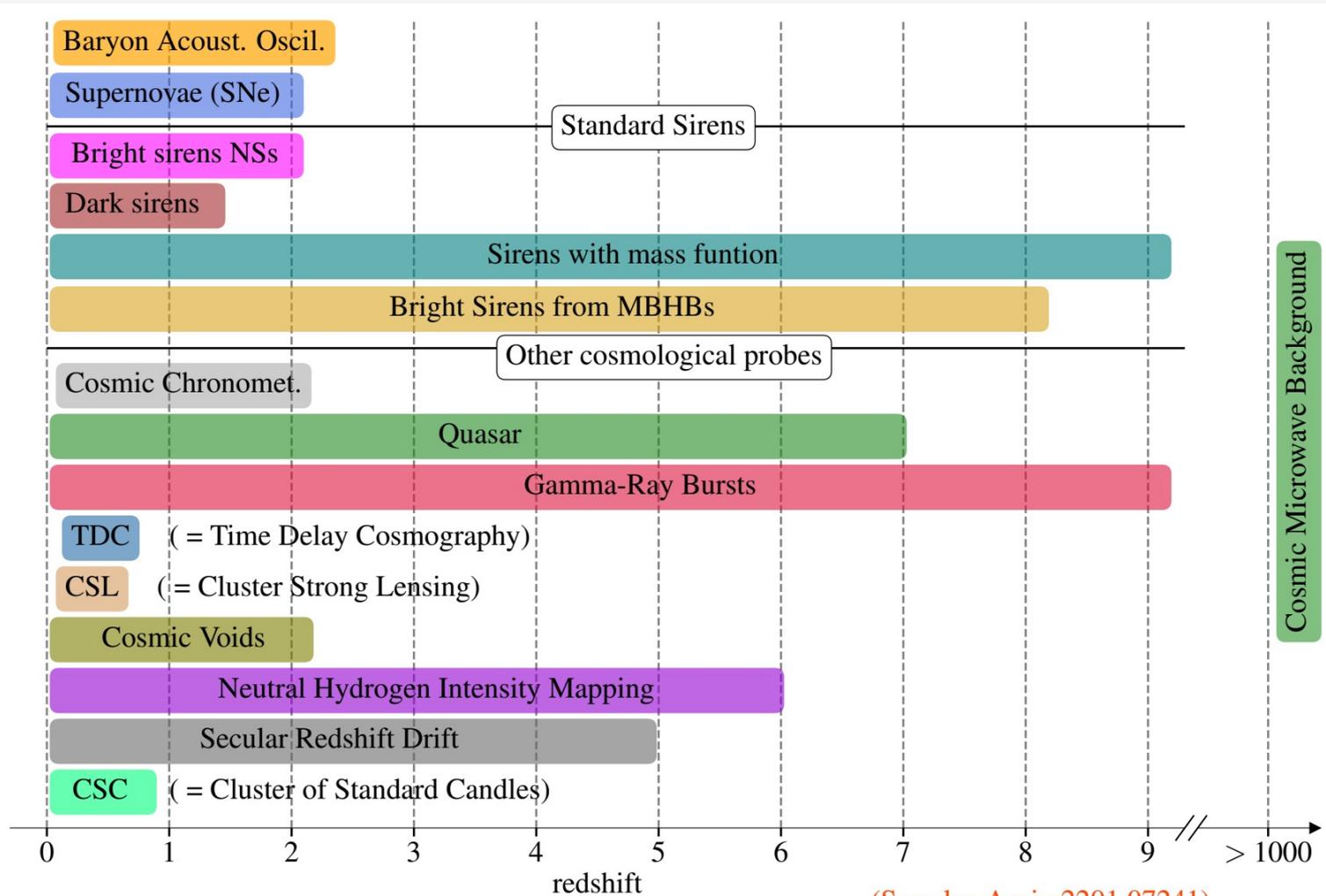
- Need better modeling for the EM counterpart
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Any questions ?



Backup slides

# MBHBs can go up to high redshift



(See also Arxiv:2201.07241)

# Matter-only approximation and redshift bins

## ➤ Matter-only approximation

$$d_C(z) = d_C(z_p) + 2(1+z_p)H^{-1}(z_p) \left(1 - \frac{\sqrt{1+z_p}}{\sqrt{1+z}}\right)$$

with  $z_p = 2-3$

We also remove EMcps at  $z \leq 1-1.5$

## ➤ Redshift bins

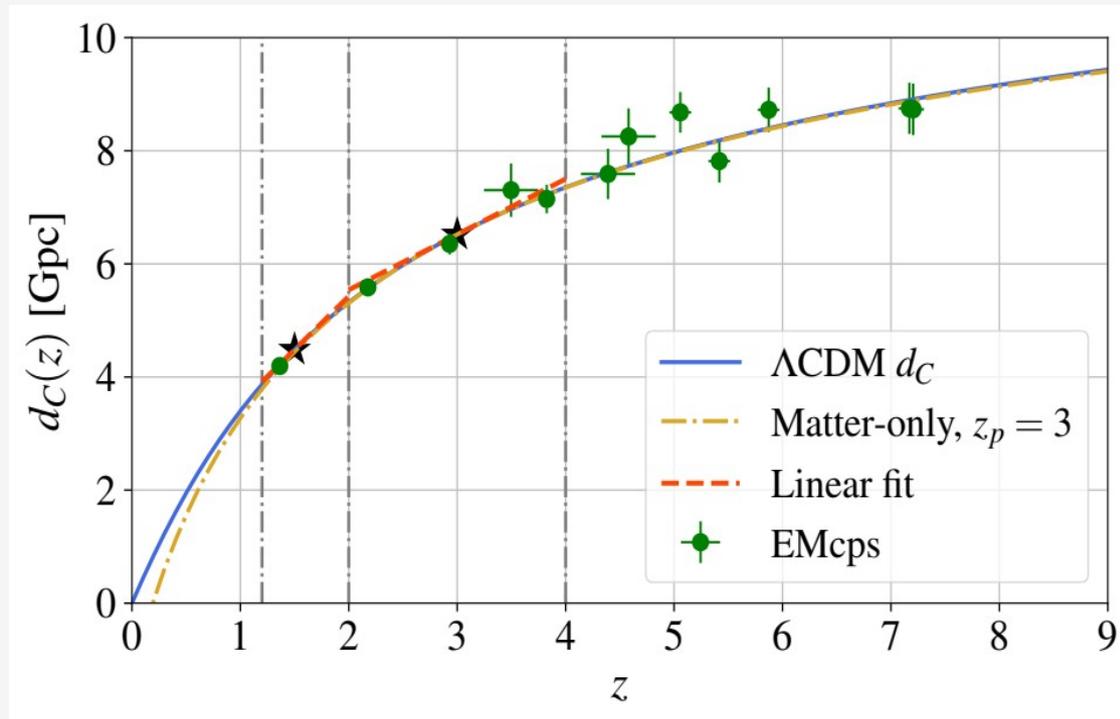
$$d_C(z) = c \int_0^z \frac{dz'}{H(z')} \quad H(z) = \left(\frac{dd_C}{dz}\right)^{-1}$$

Trade-off between:

- Bin size
- Number of EMcps in each bin

Requirement:  $D(z)$  accuracy  $\leq 5\%$

Not all the redshift bins are informative

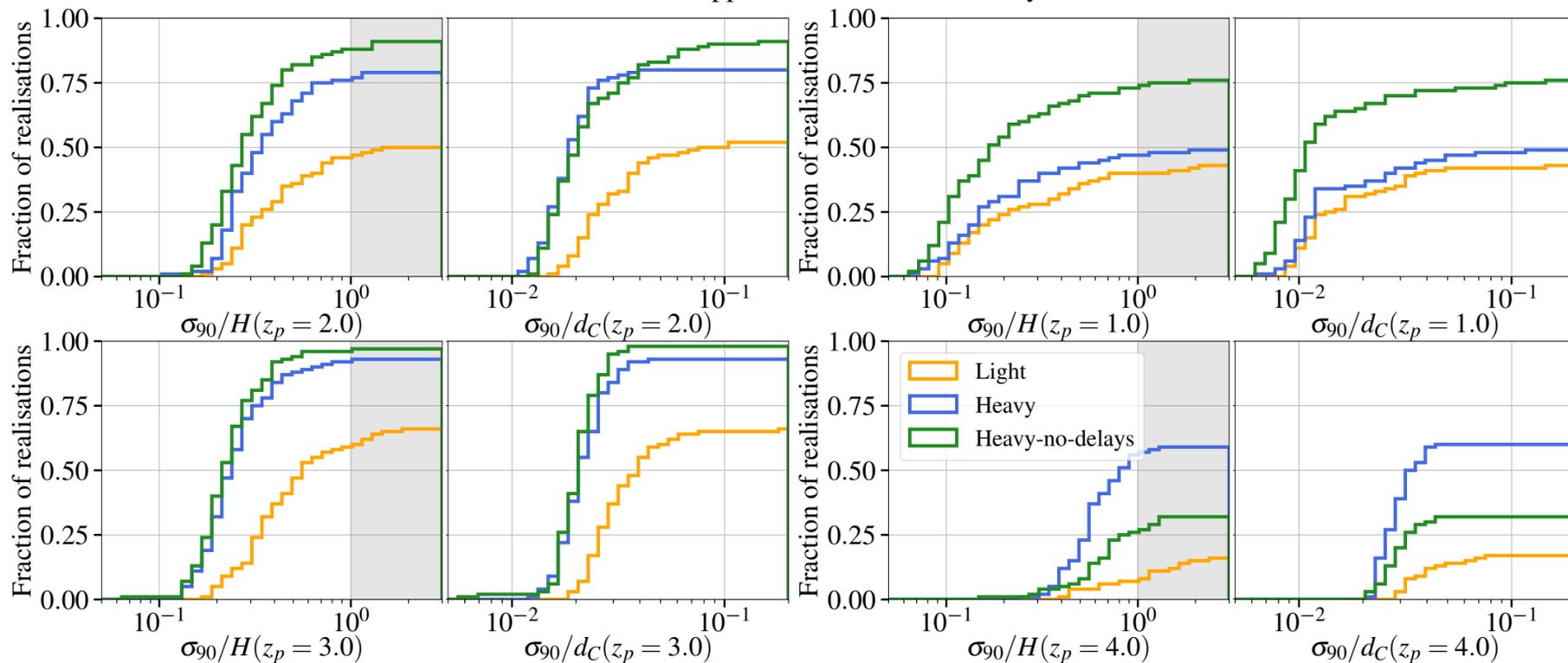


# Redshift bins

Fit:  $D(z) = D(z_p) + H(z_p)^{-1}(z - z_p)$   
with 10yr of LISA observations

$z_p = 3$	Light	Heavy	Heavy-no-delays
$2 < z < 4$	6.1	14.6	20.7

Model: Bins approach; Time mission: 10yr



# Luminosity distance and redshift estimates

## Luminosity distance

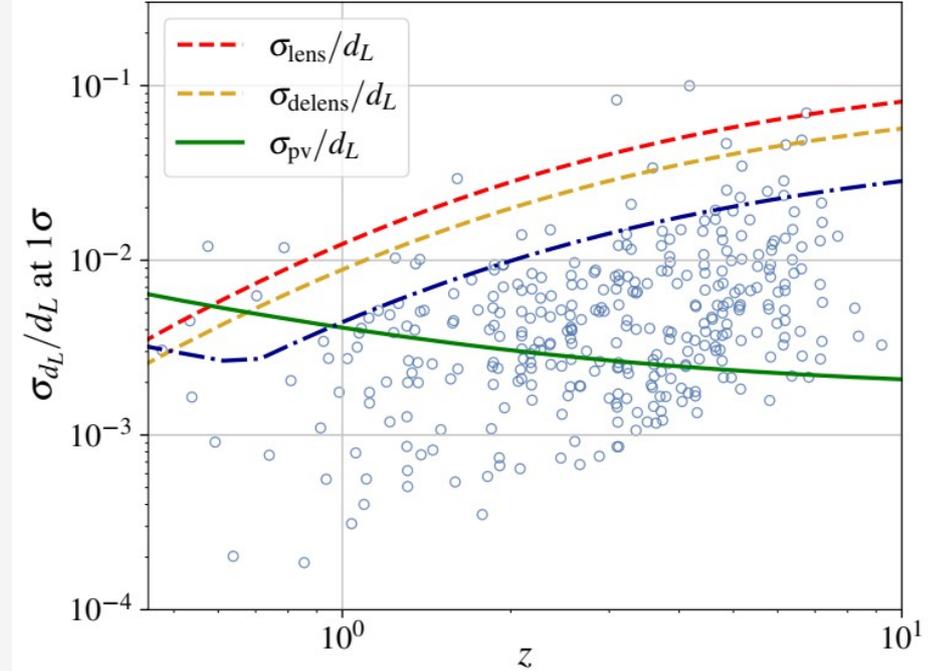
- Accurate estimate of luminosity distance  $\rightarrow \Delta d/d_L < 10\%$
- Lensing relevant for  $z > 2-3$
- Peculiar velocities are negligible

## Redshift measurements

LSST/Rubin Obs.

- Photometric measurements with  $\Delta z = 0.03(1 + z)$  (Laigle + 19)

ELT

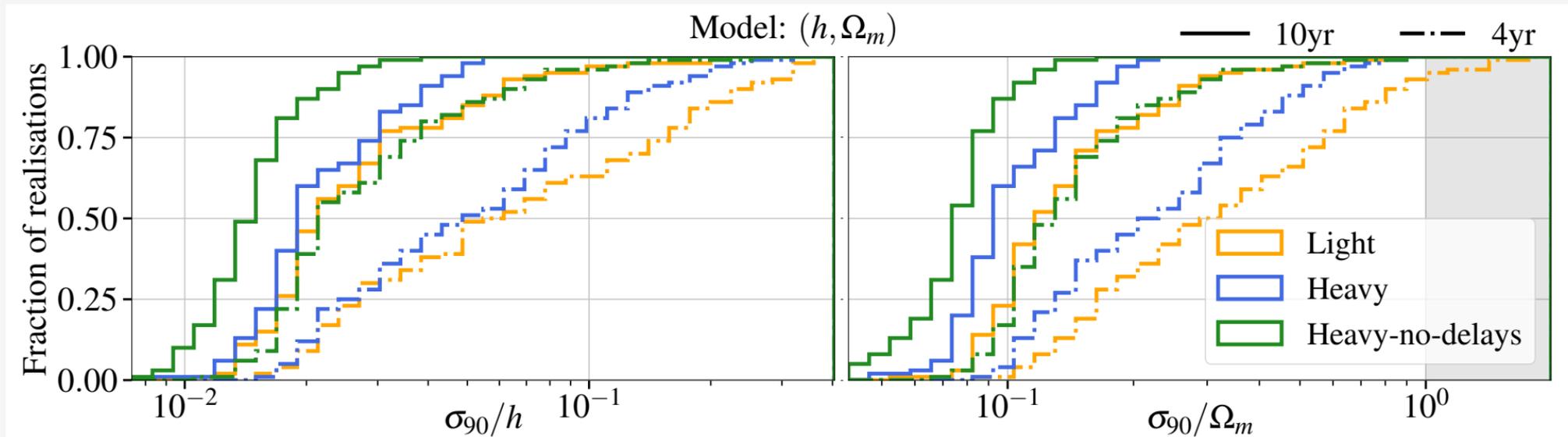


	$m_{\text{gal,ELT}} < 27.2$	$27.2 < m_{\text{gal,ELT}} < 31.3$
$z \leq 0.5$	$\Delta z = 10^{-3}$	No redshift information
$0.5 < z \leq 5$		$\Delta z = 0.5$
$z > 5$		$\Delta z = 0.2$

# Prospects for $H_0$ and $\Omega_m$

Fit:  $H(z) = H_0 \sqrt{\Omega_m(1+z)^3 + (1-\Omega_m)}$  (in 4 yr)

Light	Heavy	Heavy-no-delays
6.4	14.8	20.7



$H_0$  can be constrained to few percent  
Larger uncertainties on  $\Omega_m$

For CPL parametrization  $\rightarrow$  Poor constrains on  $\omega_0$  and no constrain on  $\omega_a$  22

# What to do with uninformative realisations?

No or few events in a redshift bin



The realisation is not informative



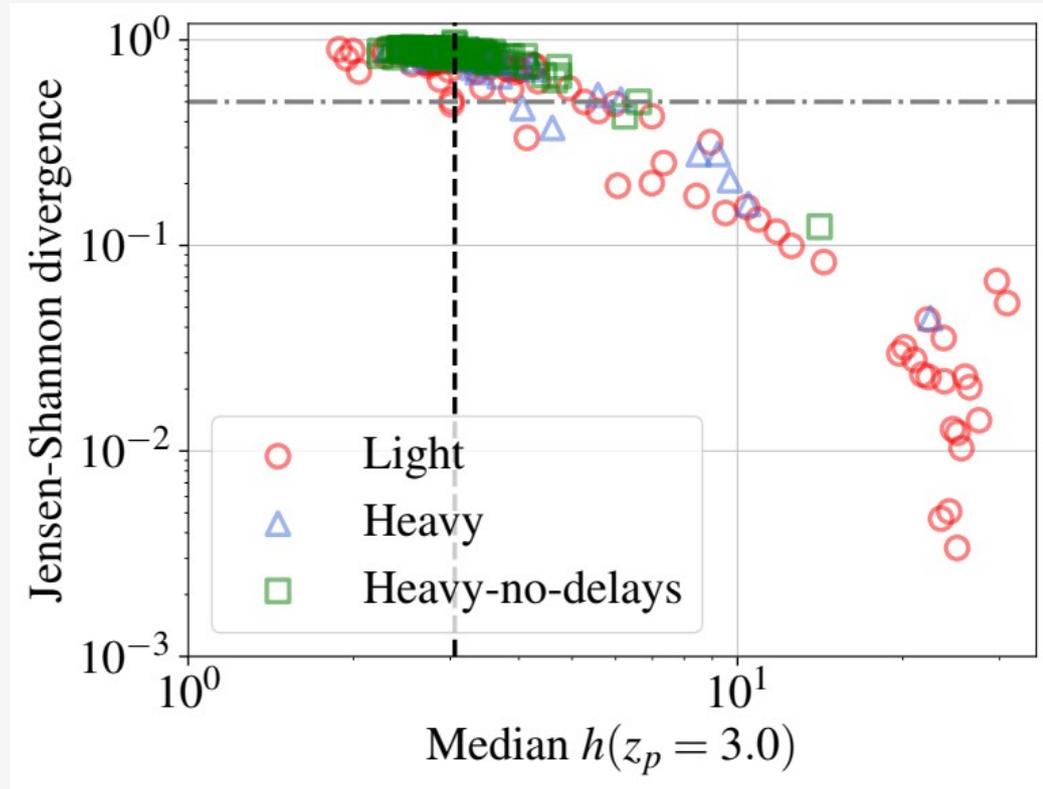
The posterior distribution coincides with the prior

## Jensen-Shannon (JS) test

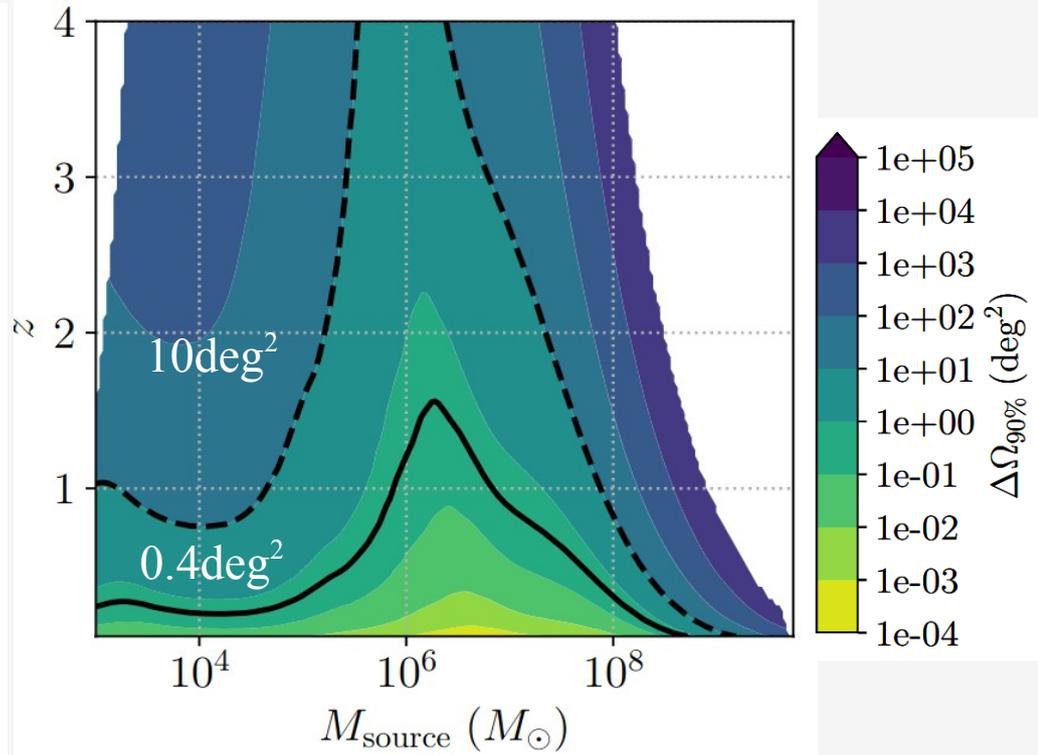
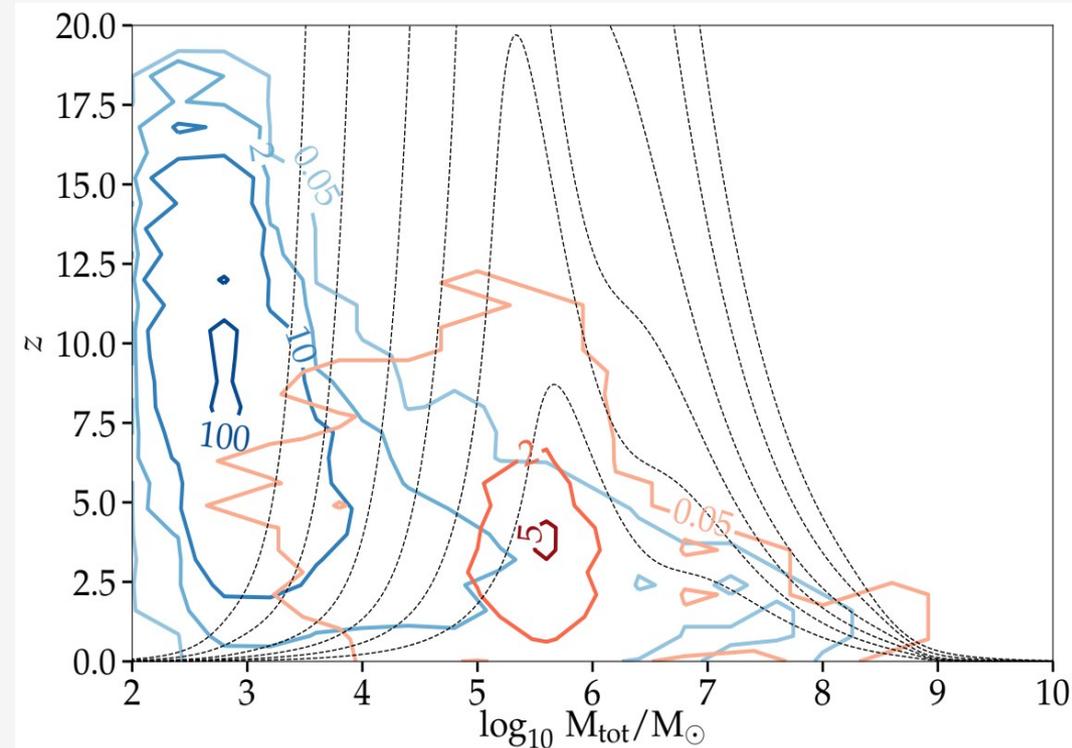
We compare the posterior and the prior distributions

- JS=0 if posterior == prior
- JS=1 if posterior != prior

In this case, uniform prior for  $h(z=3)$  in  $[0.1, 50]$



# Mass-redshift distributions and sky localization



Blue : Light seeds

Red : Heavy seeds

Contour lines:  $\frac{dN}{d \log_{10} M_{\text{tot}} dz dt} \times 4\text{yr}$

(Marsat,..., AM+ *in prep.*)