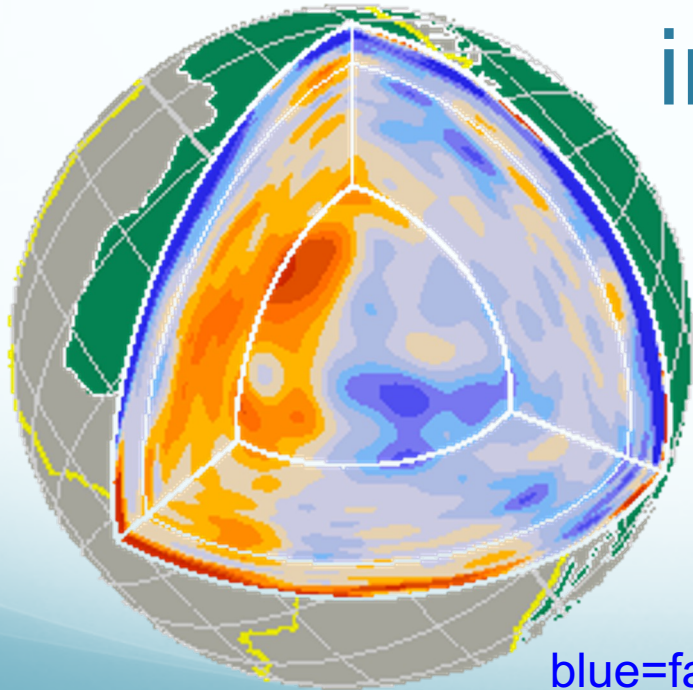




Whole Earth oscillations: The key to imaging density in Earth's deep interior using seismic data



blue=fast
red=slow

Arwen Deuss

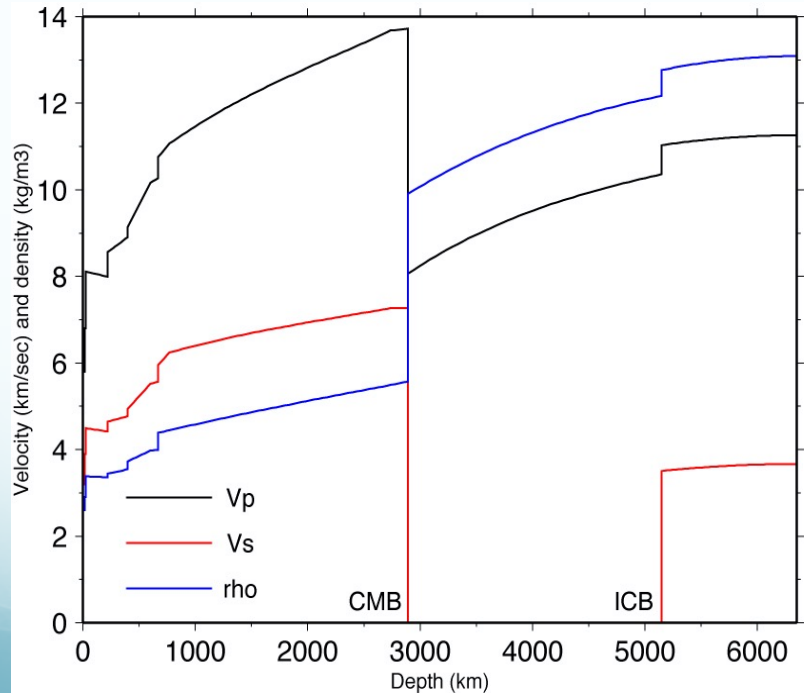
Runa van Tent, Ashim Rijal, Laura Cobden

Universiteit Utrecht



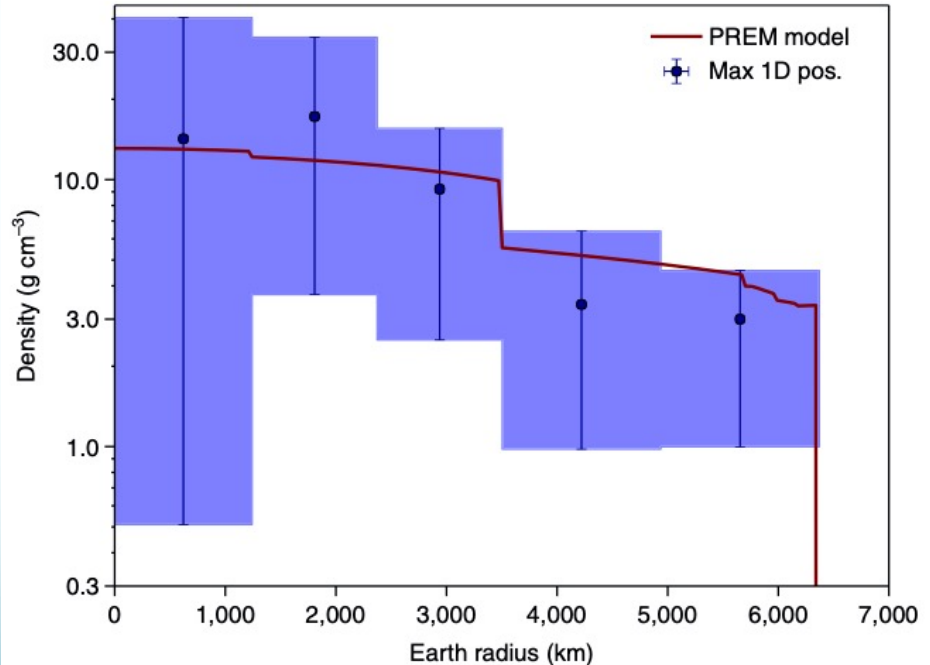
1D density profile

Seismic tomography



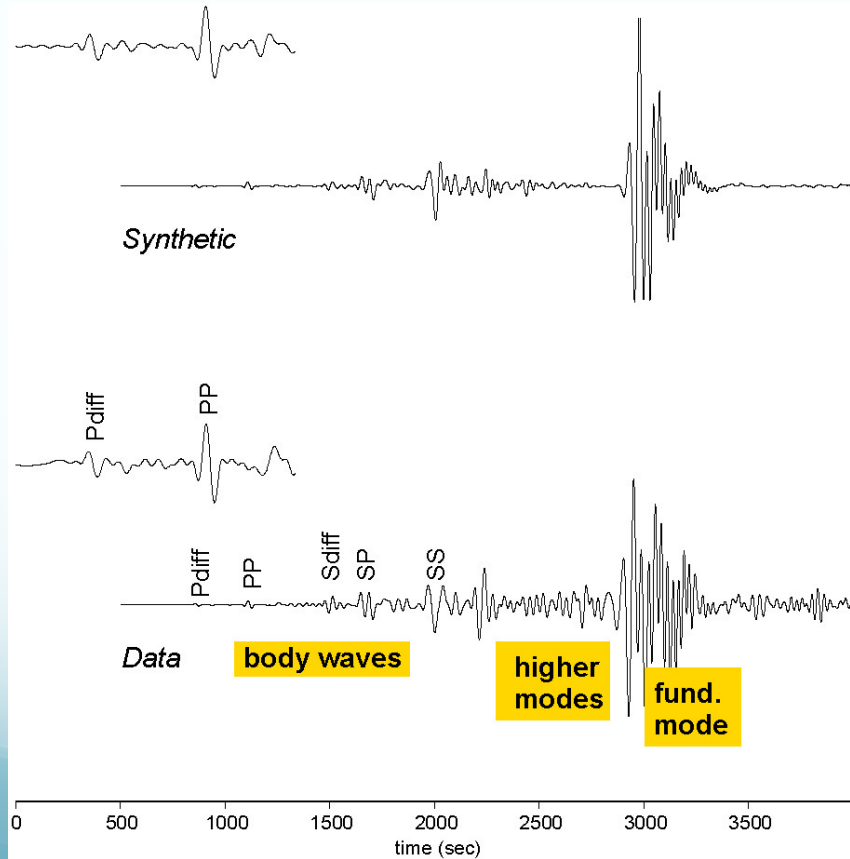
PREM, Dziewonski & Anderson (1981)

Neutrino tomography



Donini *et al* (2019)

Seismological Data



Synthetics computed using normal mode summation up to 6 seconds for PREM

Event 21 May 1998 (Indonesia)
at TSUM (Tsumeb, Namibia)

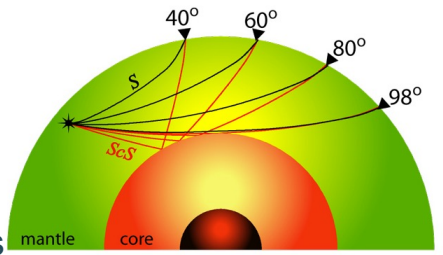
Depth = 28km,
Mw= 6.6, Mb=6.3,
 $\Delta = 101.5$

(1) Body waves

Imaging small scale structure and discontinuities

Only velocity information

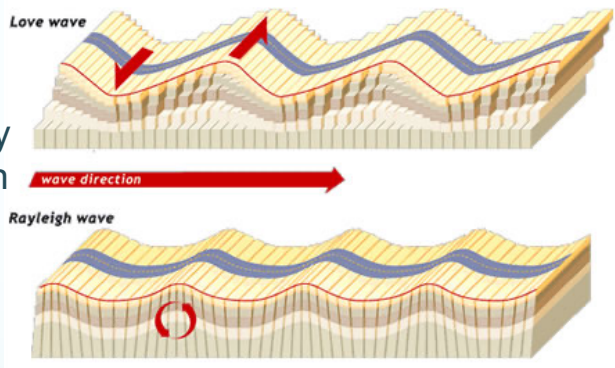
Ray theoretical approximations



Short period
(~ 0.05-1Hz)

(2) Surface waves

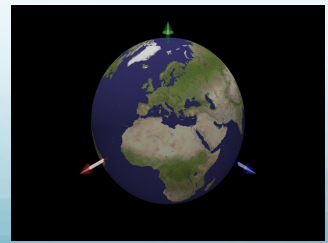
Imaging upper mantle only
Mainly velocity information
(limited density)



(0.3-40 mHz)

(3) Whole Earth oscillations

Density and velocity information
Only large scale structure
Complete theory



Long period
(0.2-10 mHz)

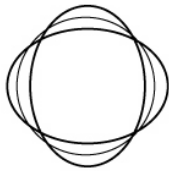


Whole Earth oscillations

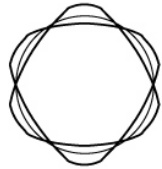
Spheroidal modes ${}_nS_l$

n = radial order, l = angular order

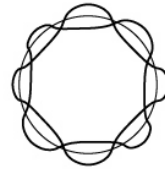
Surface patterns



${}_0S_2$

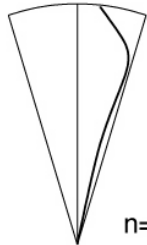


${}_0S_3$



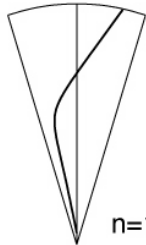
${}_0S_4$

Radial patterns



$n=0$

Fundamental



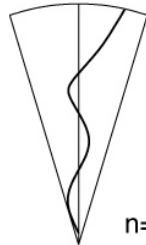
$n=1$

First Overtone



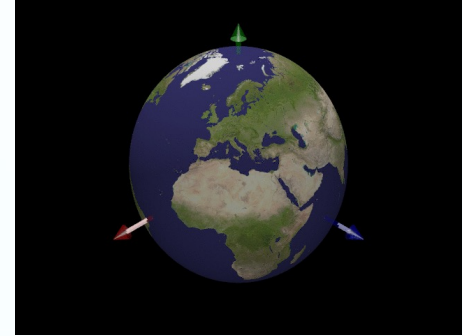
$n=2$

Second Overtone

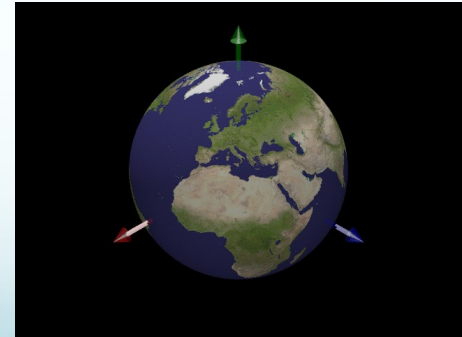


$n=3$

Third Overtone

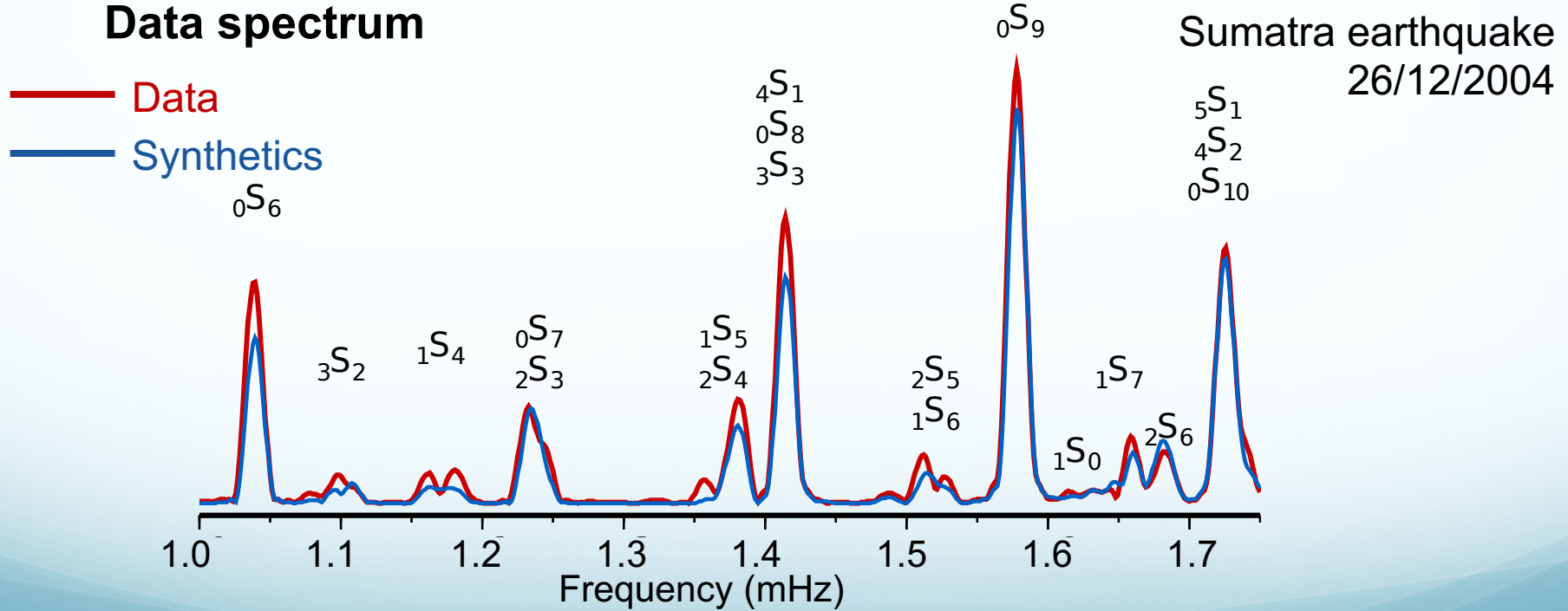


${}_0S_2$: 54 minutes
“football mode”



${}_0S_0$: 20 minutes
“breathing mode”

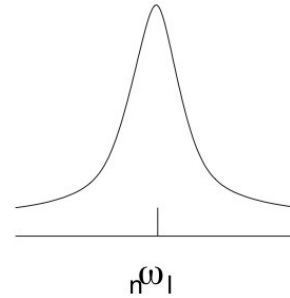
Normal mode data



SNREI

- * spherical symmetric,
- * non-rotating,
- * isotropic Earth

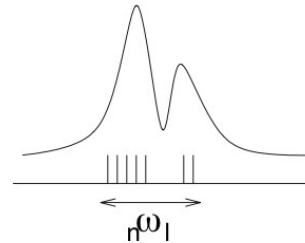
degeneracy:
2l+1 singlets have same frequency



Real Earth

- * Rotation
- * Ellipticity
- * Heterogeneity
- * Anisotropy

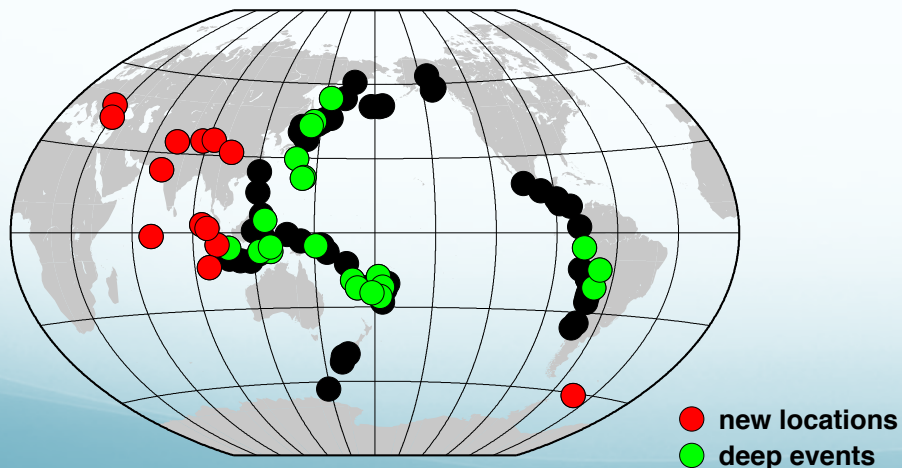
degeneracy removed:
2l+1 singlets have different frequency



↓
splitting and coupling

Normal mode observations

- Data set of 93 events with $M_w > 7.4$ since 1978
- Select frequency window for specific normal mode
- Combine all spectra for one splitting function
- Start from PREM predictions
- Iterative least squares spectral fitting



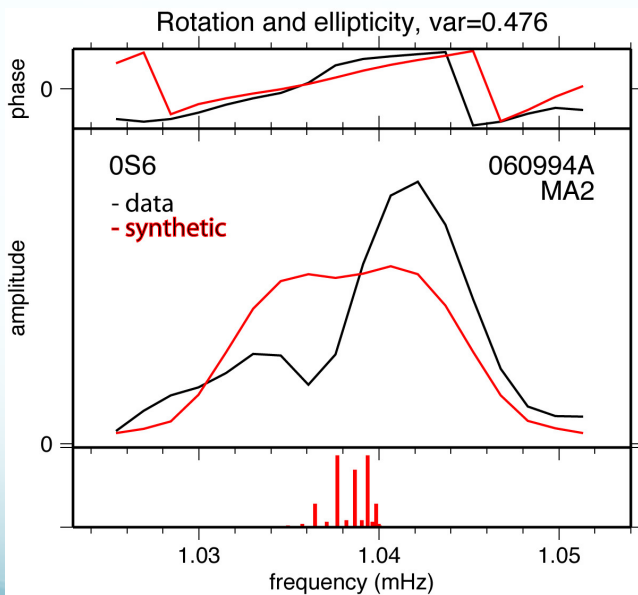
Including:

- 2004 Sumatra ($M_w=9.0$)
- 2010 Chile ($M_w=8.8$)
- 2011 Japan ($M_w=9.0$)

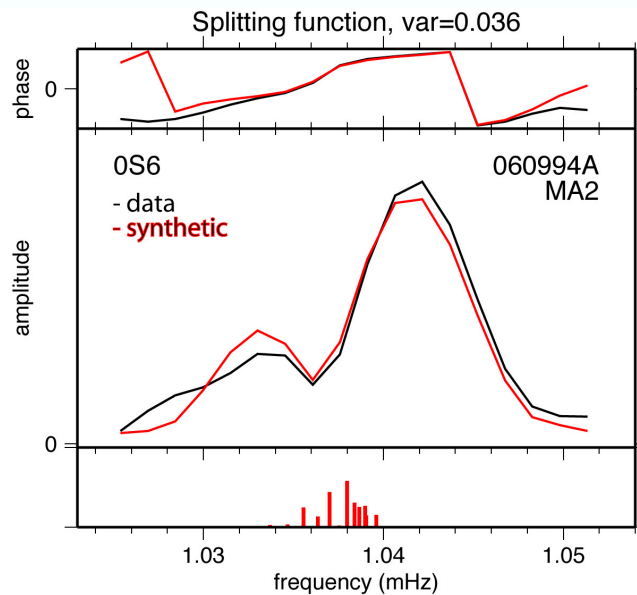
(Deuss et al., *GJI*, 2013)

Normal mode spectra

Before splitting function measurement:



After splitting function measurement:



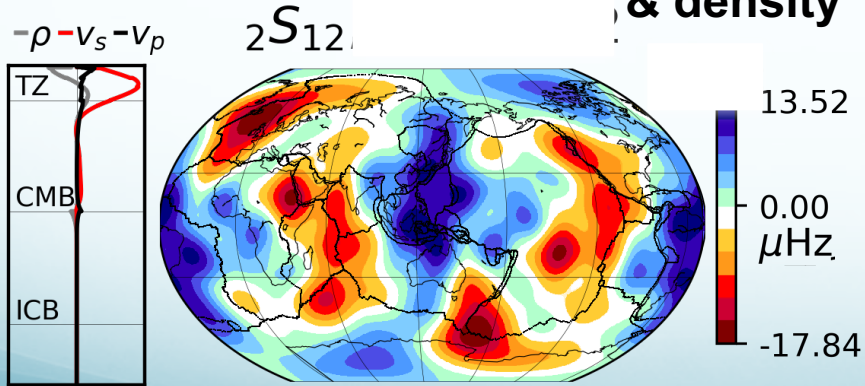
Splitting functions

$$F(\theta, \phi) = \sum C_{st} Y_s^t(\theta, \phi)$$

s=angular order
t=azimuthal order

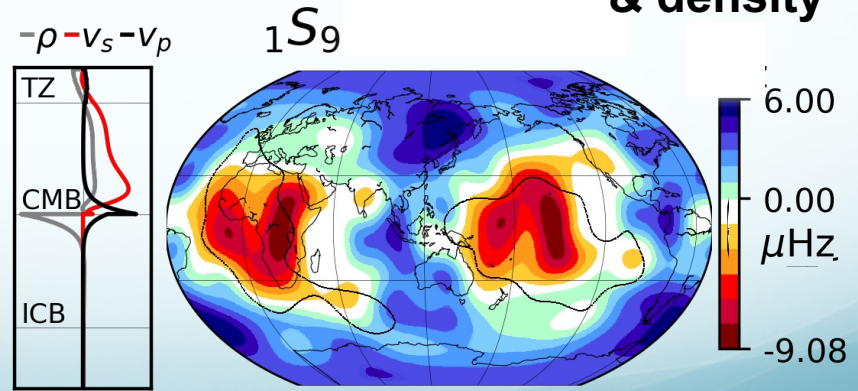
Upper mantle

Elastic splitting function – **3D velocity & density**



Lower mantle

Elastic splitting function – **3D velocity & density**



Splitting functions

$$F(\theta, \phi) = \sum C_{st} Y_s^t(\theta, \phi)$$

s=angular order
t=azimuthal order

Coefficients C_{st} depend on Earth structure

$$C_{st} = \int_0^a \delta m_{st}(r) K_s(r) dr$$

$\delta m_{st}(r)$ are model parameters (v_s , v_p , ρ)

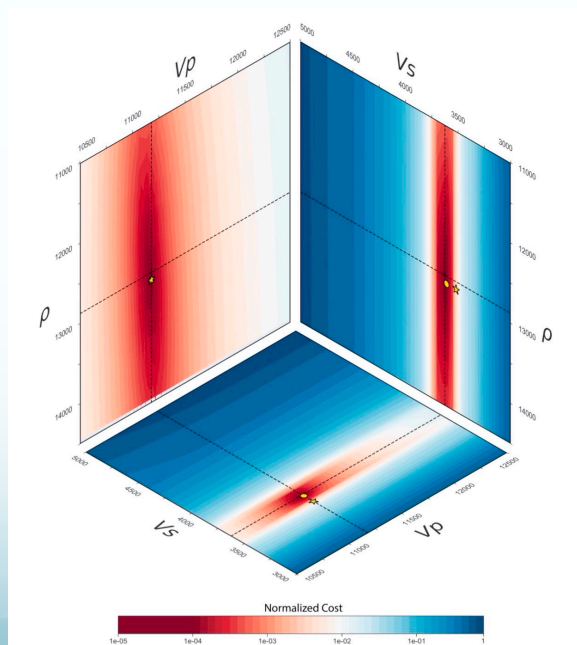
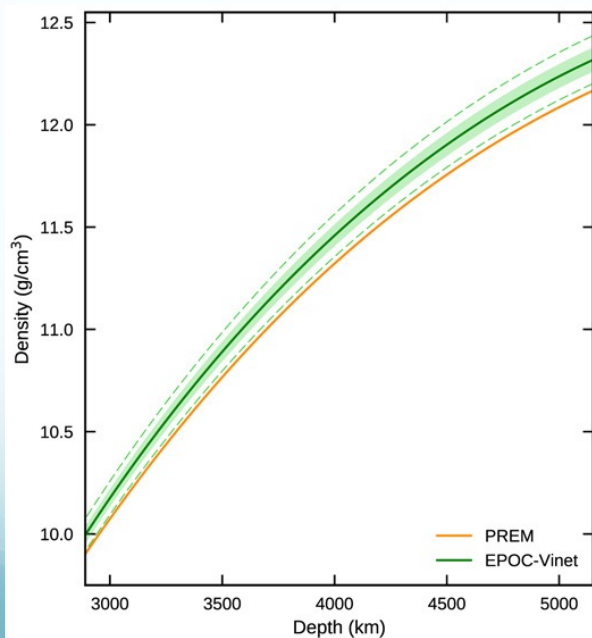
$K_s(r)$ are the kernels

$s=0$ 'center frequencies' \longrightarrow 1D structure

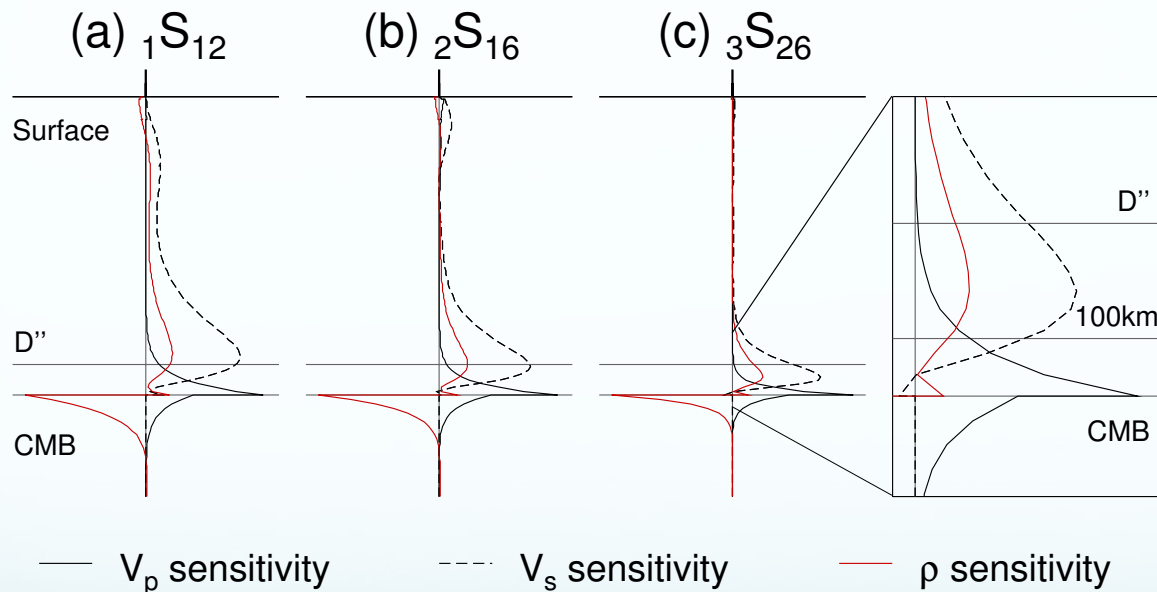
$s > 0$ 'splitting function' \longrightarrow 3D structure

1D structure

- Outer core is denser than PREM (Irving et al, 2018)
- Inner core is lighter than PREM (Robson & Romanowicz, 2019)



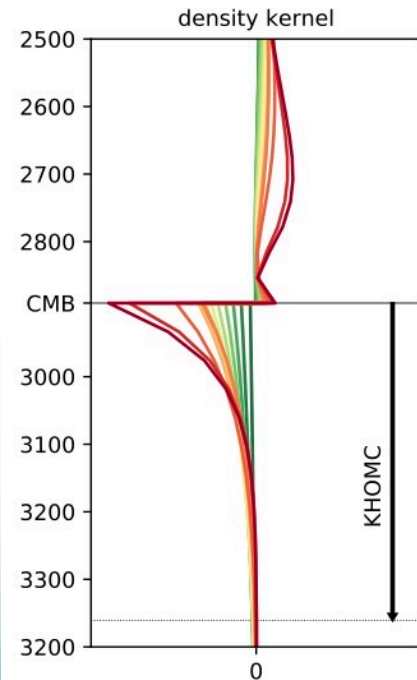
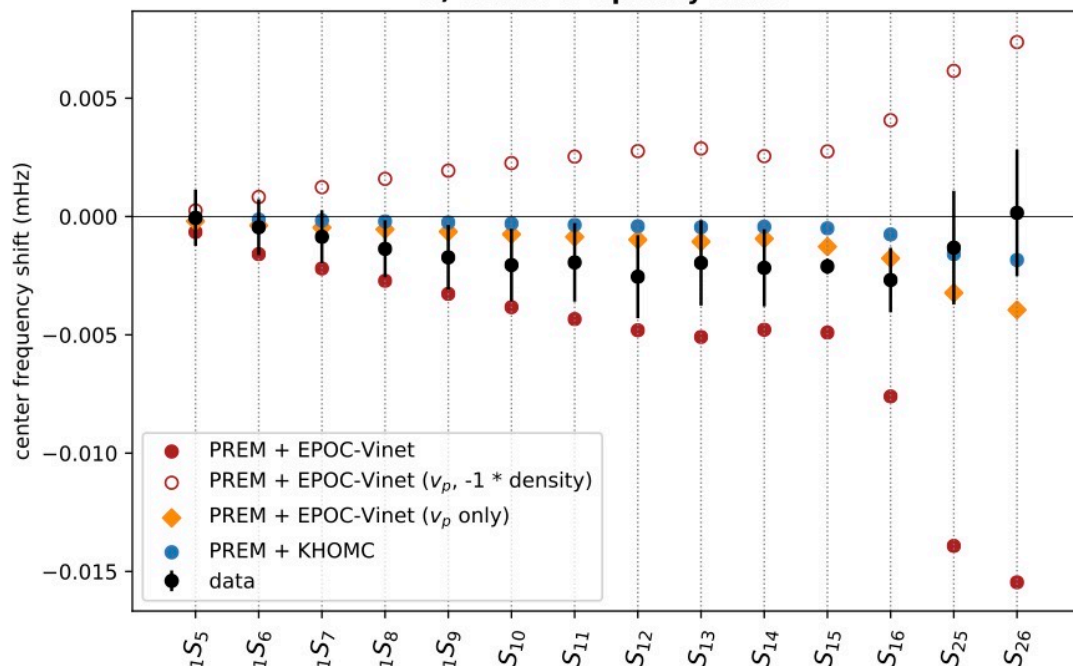
Core Mantle Boundary Stoneley modes



- Strong sensitivity to the Core Mantle Boundary
- Difficult to observe, as almost no surface expression!

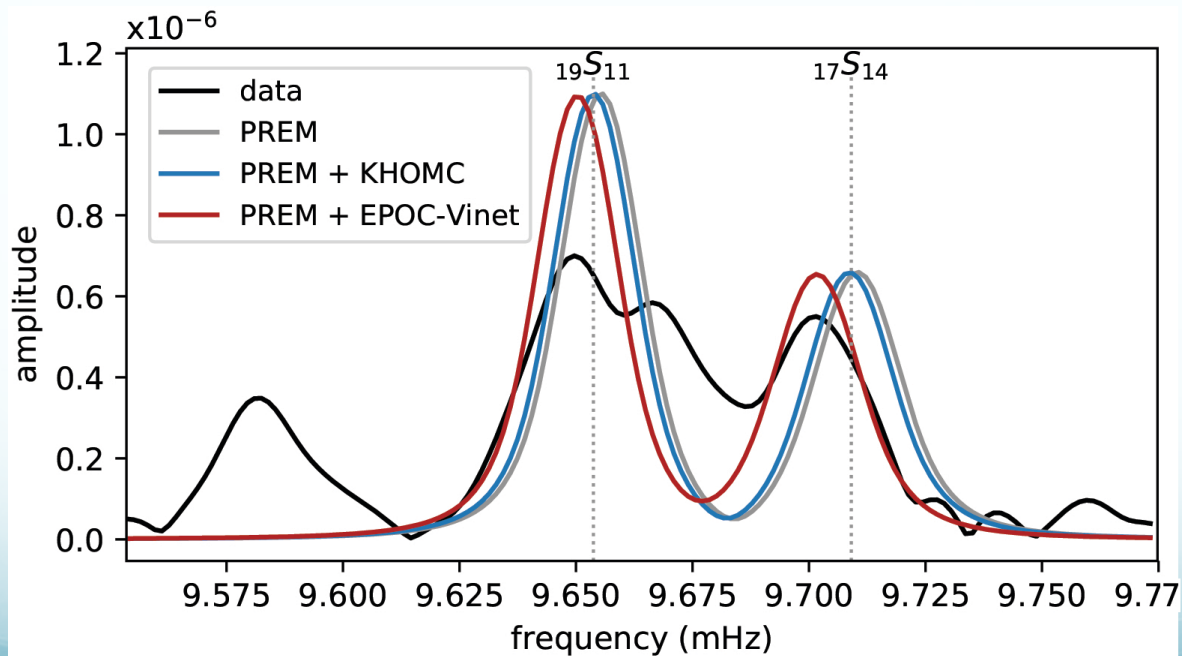
1D structure

Outer core density – center frequency shifts



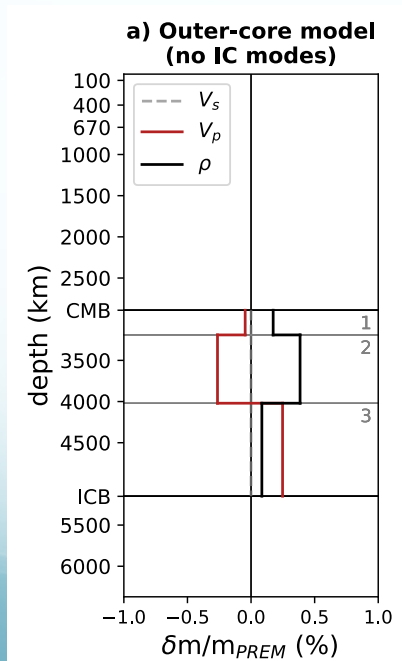
1D structure

Normal mode spectra– outer core density



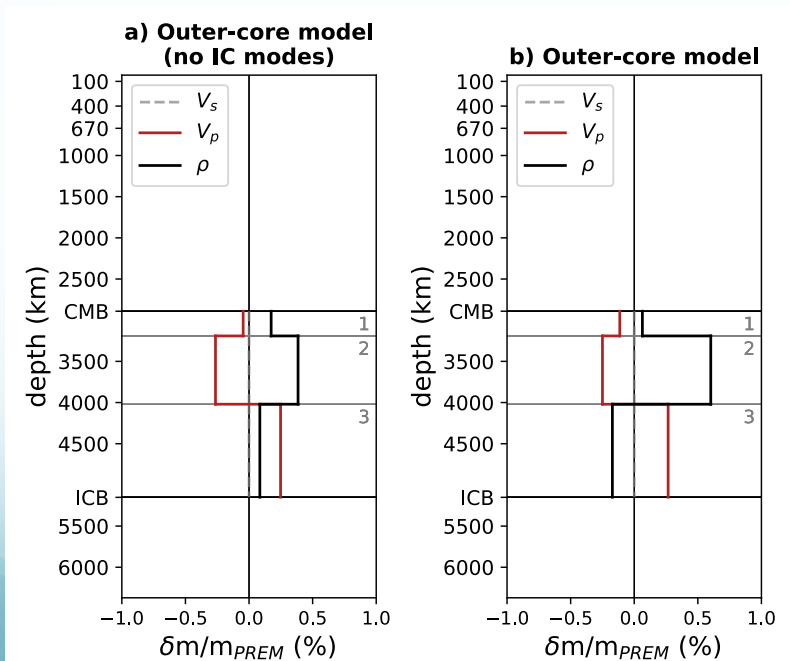
1D structure

- Outer core is denser than PREM?
- Inner core is lighter than PREM?



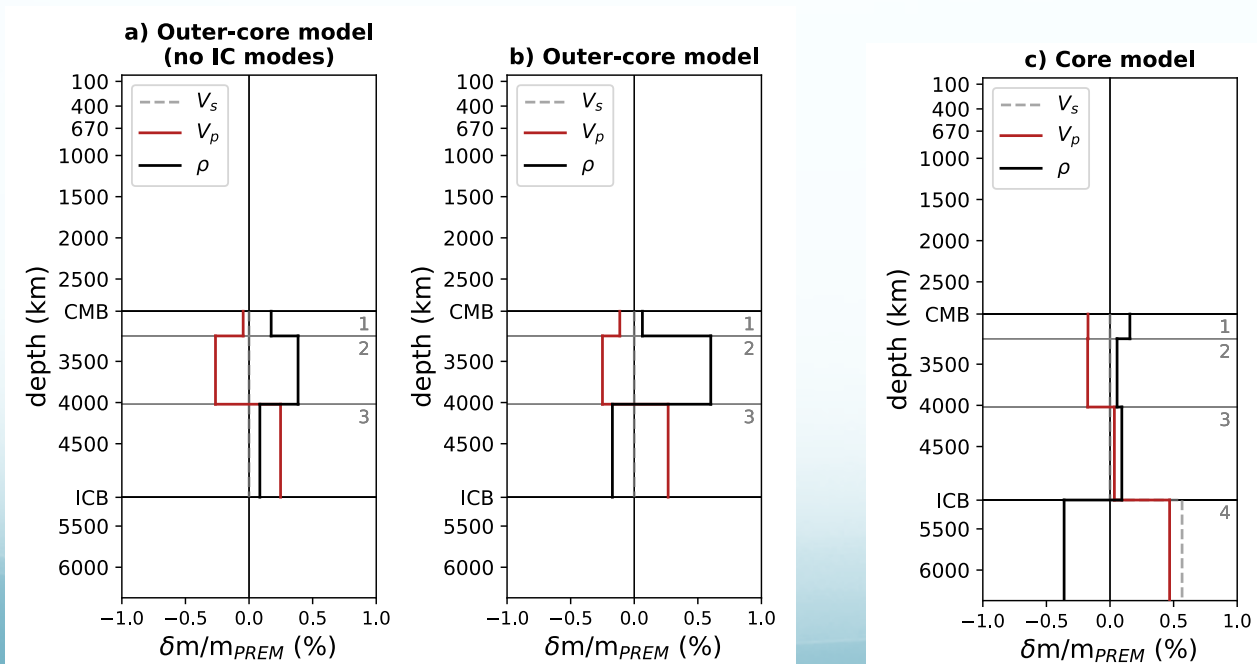
1D structure

- Outer core is denser than PREM?
- Inner core is lighter than PREM?



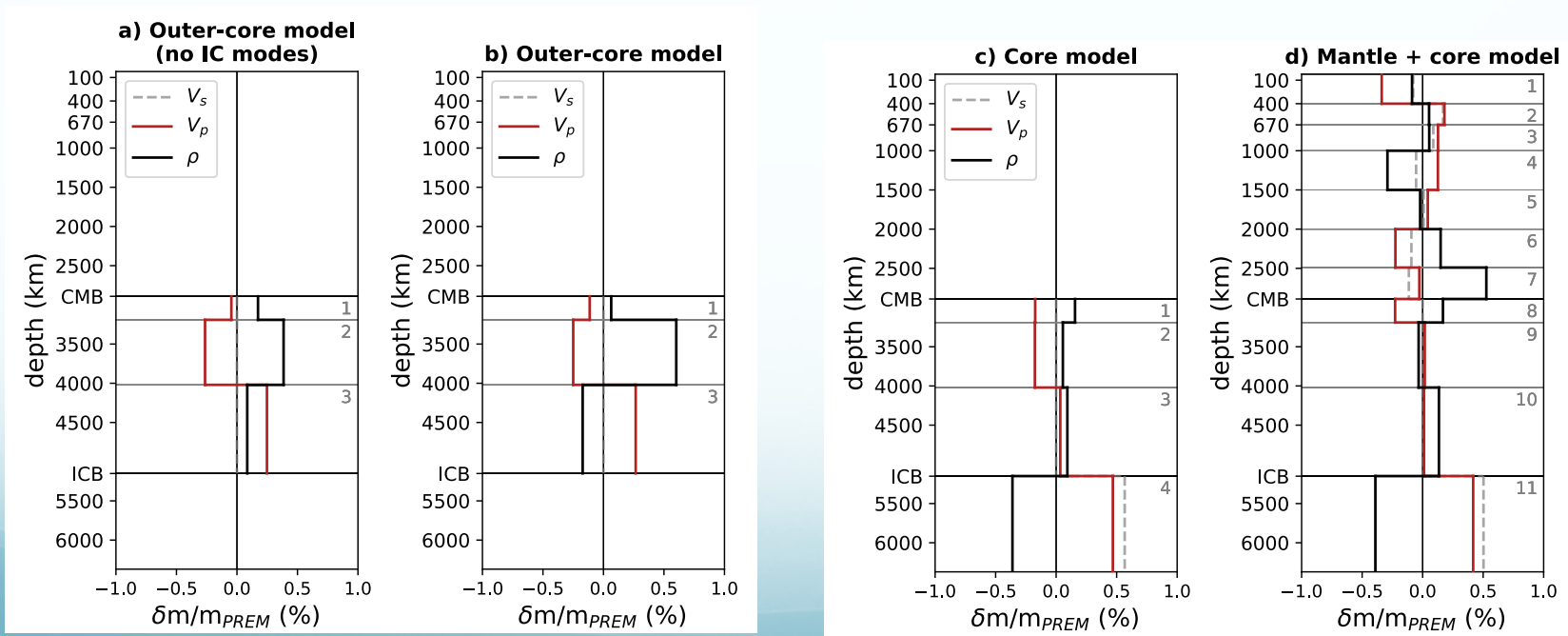
1D structure

- Outer core is denser than PREM?
- Inner core is lighter than PREM?



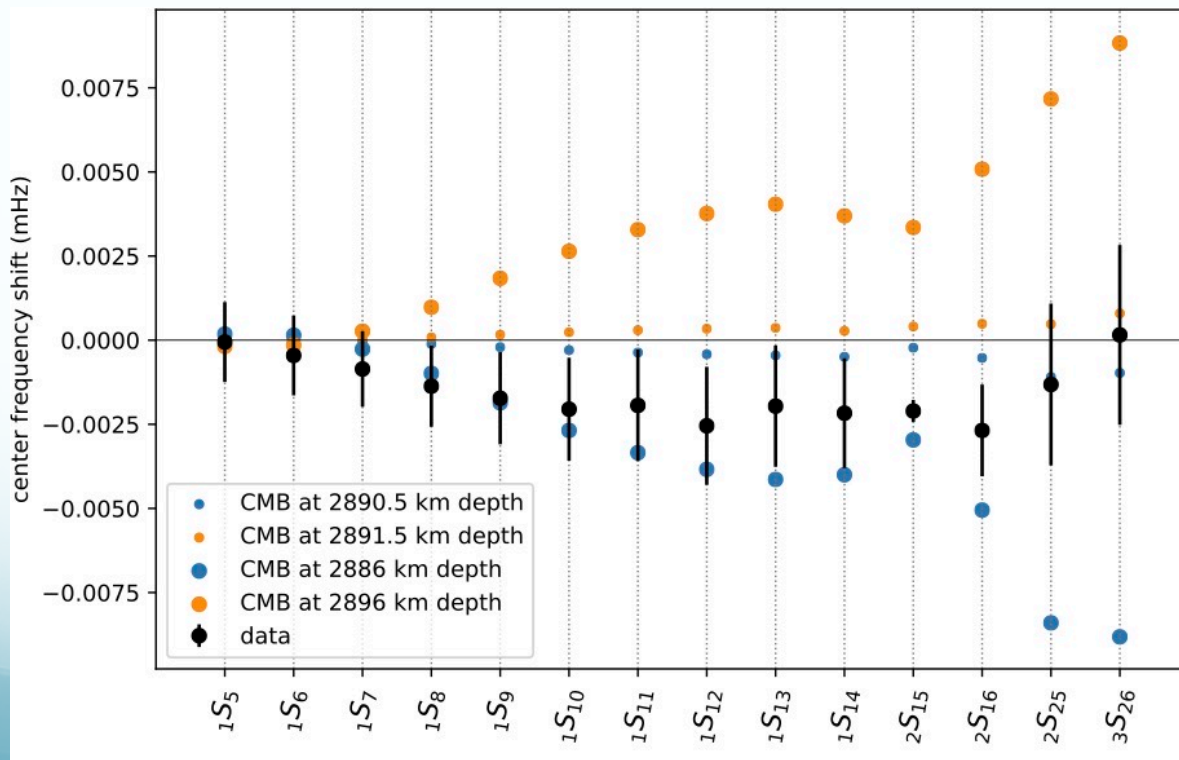
1D structure

- Outer core is denser than PREM? **0.2% denser near the top**
- Inner core is lighter than PREM? **0.4% lighter**



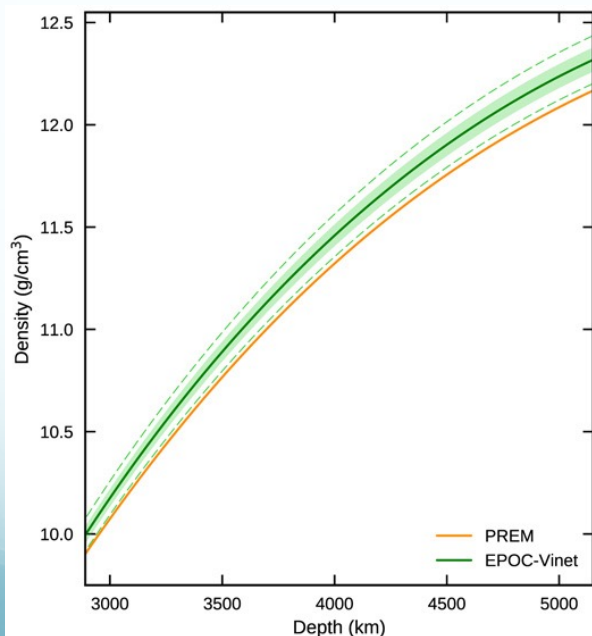
1D structure

CMB depth – 5km shift is already too much!

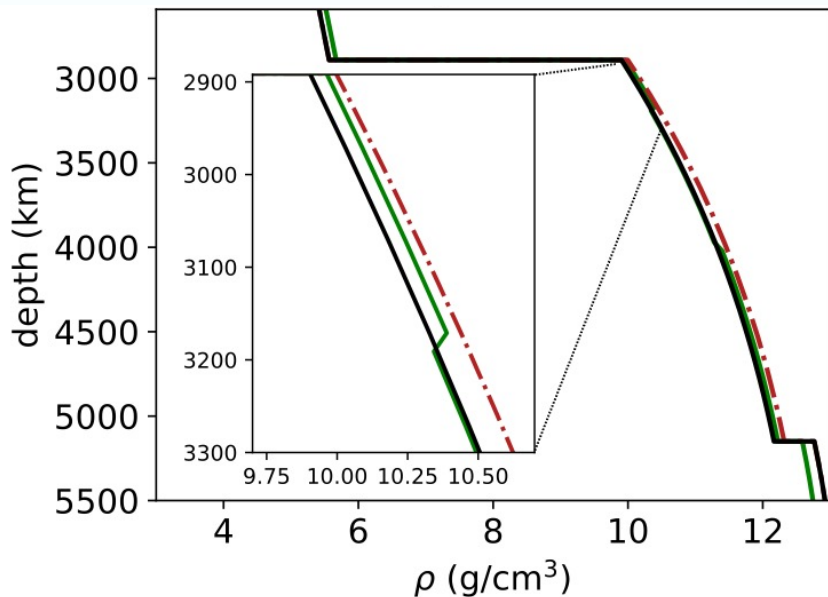
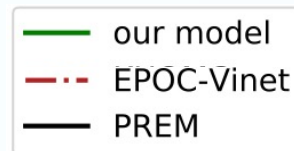


1D structure

- Outer core is denser than PREM (Irving et al, 2018)

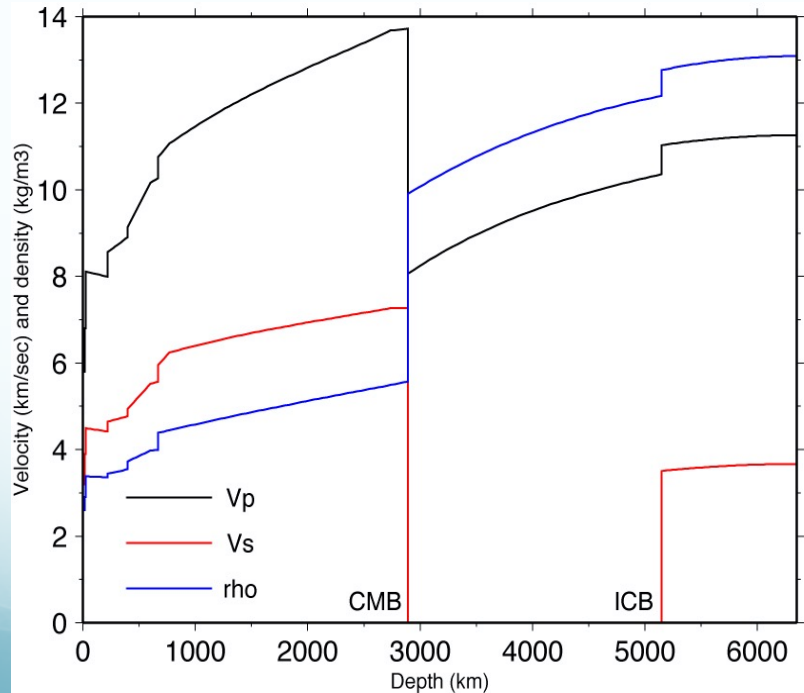


- Outer core is only denser at the top



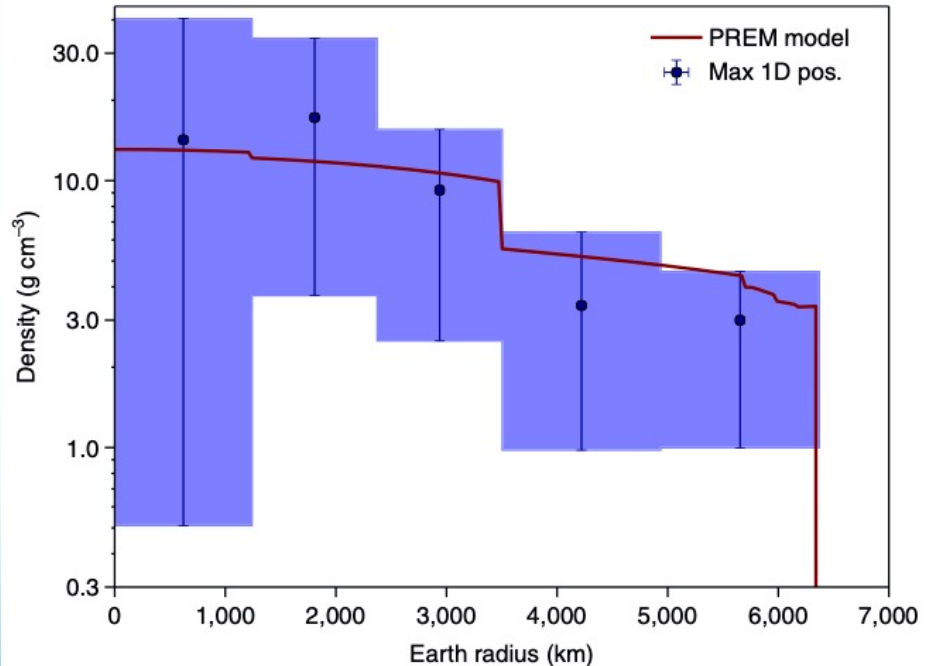
1D density profile

Seismic tomography



PREM, Dziewonski & Anderson (1981)

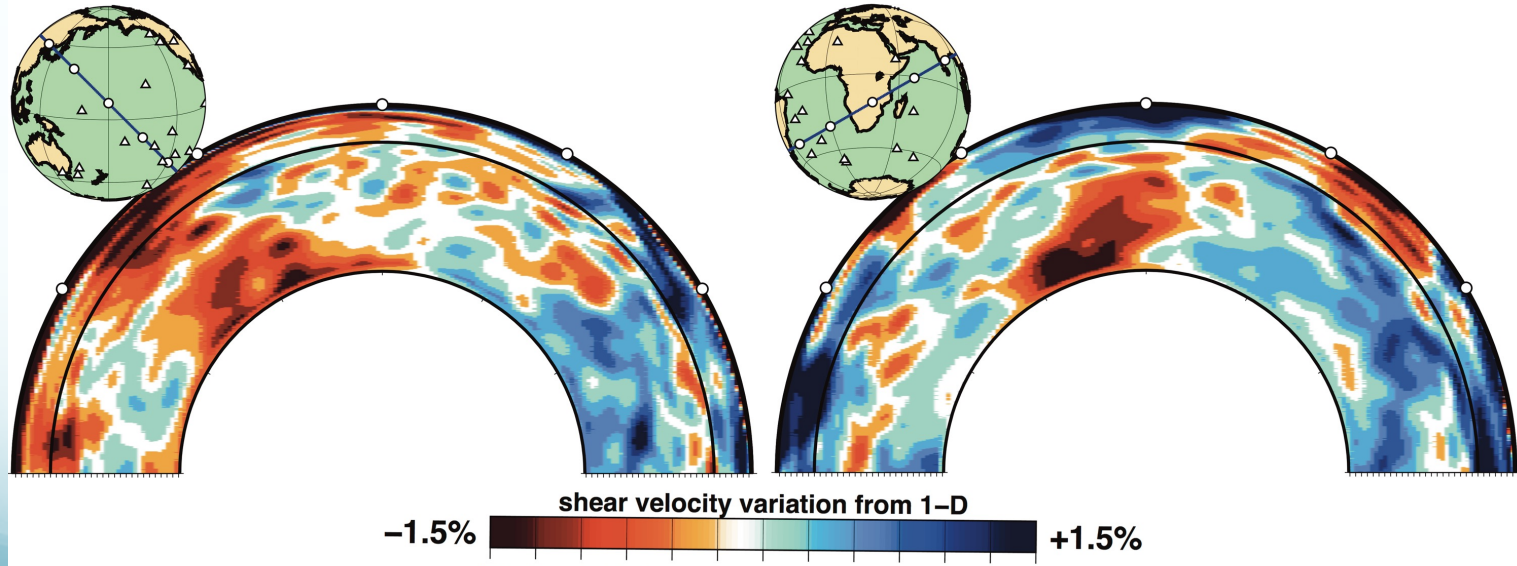
Neutrino tomography



Donini *et al* (2019)

3D structure

Large Low Shear Velocity Provinces (LLSVPs):
Hot superplume or **stable mantle anchor**?



LLSVP density – previous studies

Seismic normal modes

Tomographic models	- LLSVPs are dense	Ishii & Tromp (1999) Trampert et al. (2004) Mosca et al. (2012)
Stoneley modes	- LLSVPs are light	Koelemeijer et al.(2017)
Geoid	- LLSVPs are light	Hager et al. (1985)
Tidal data	- LLSVPs are dense	Lau et al. (2017)

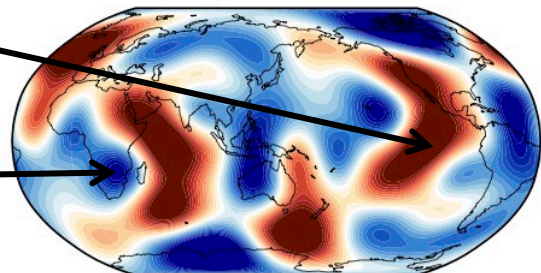
Density tomography

(Using Hamiltonian Monte Carlo sampling)

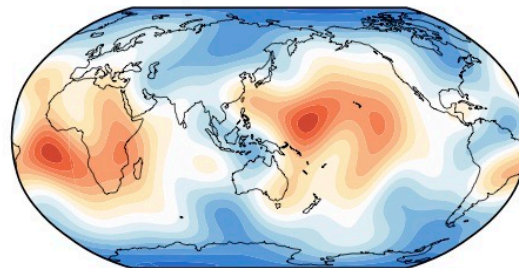
Spreading ridges

Shields

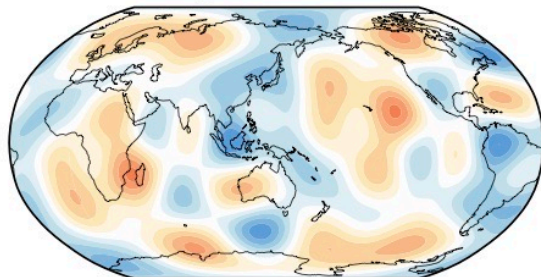
Velocity
 V_s , 100 km



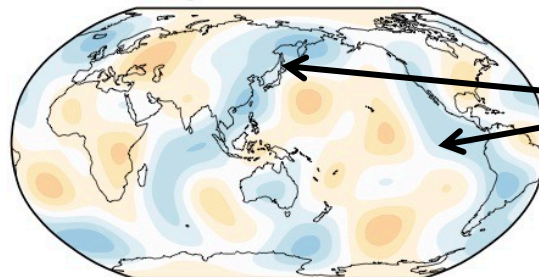
Density
 ρ , 100 km



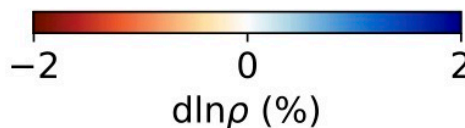
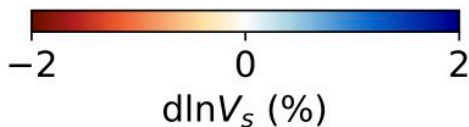
V_s , 670 km



ρ , 670 km



Subducting slabs

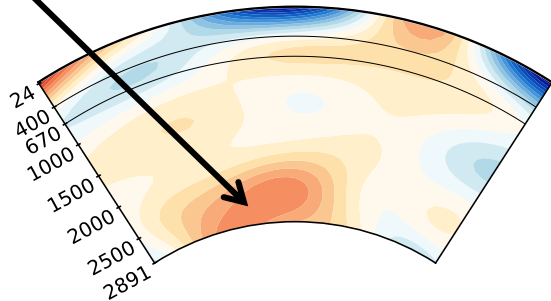
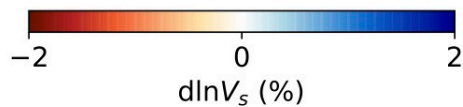
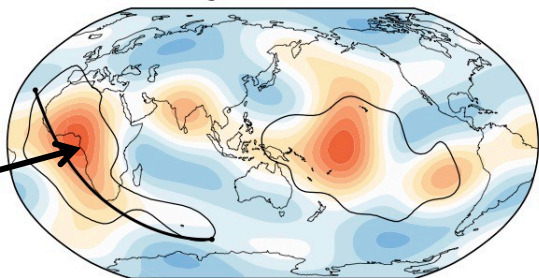


Density tomography

(Using Hamiltonian Monte Carlo sampling)

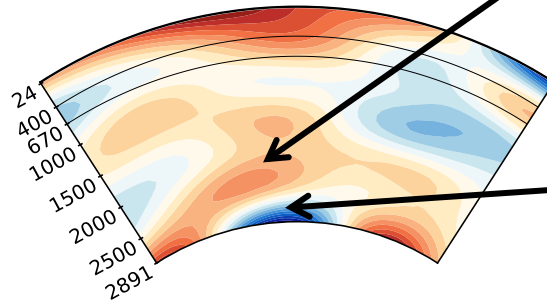
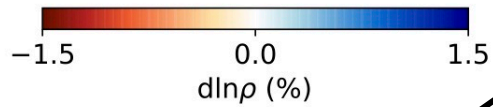
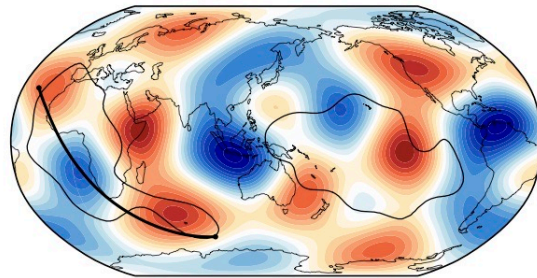
Velocity

V_s , 2850 km



Density

ρ , 2850 km

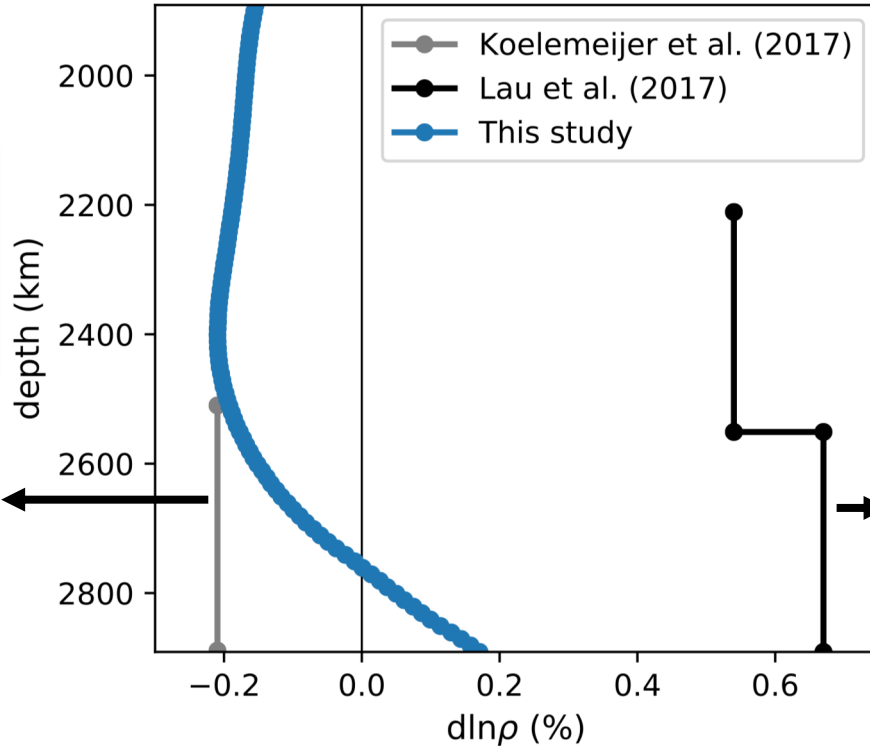


Light top

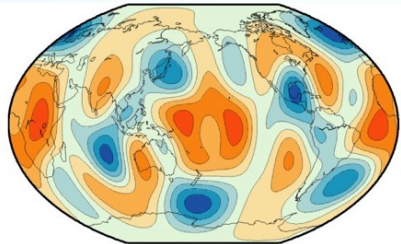
Dense base

Comparing density models

Average LLSVP density

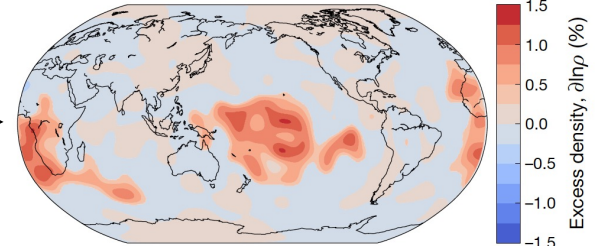


Koелеmeijer et al. (2017)



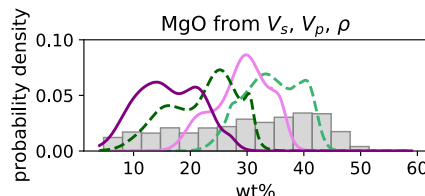
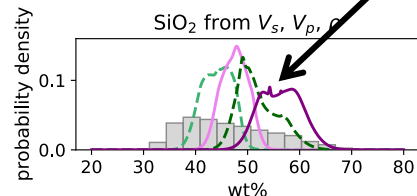
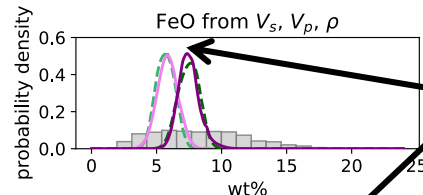
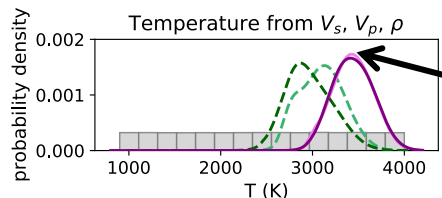
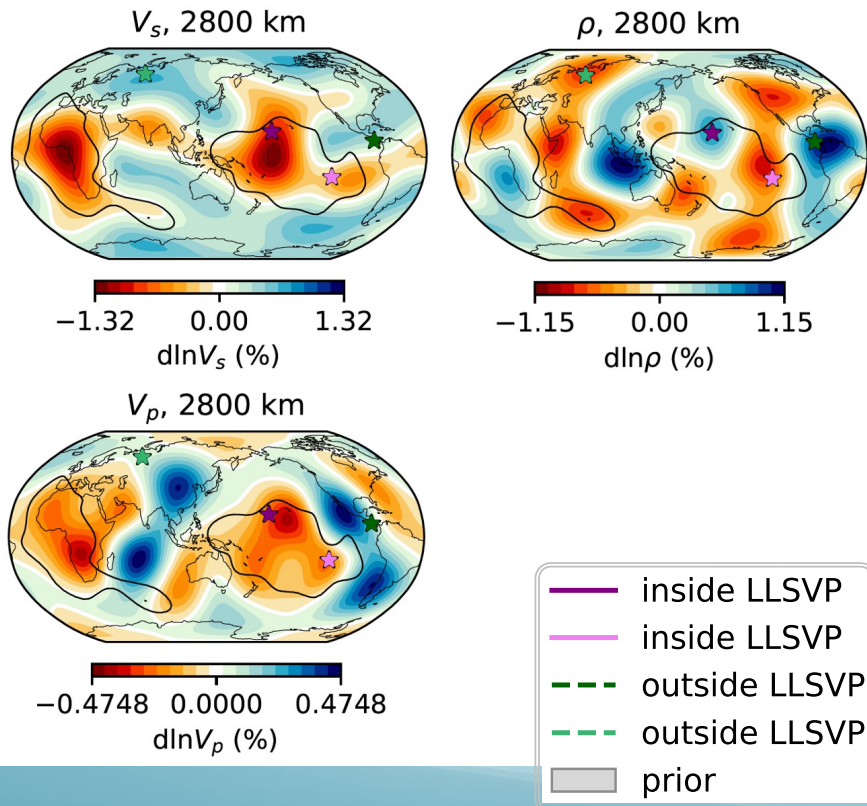
-1.5 -1.0 -0.5 0.0 0.5 1.0 1.5
Density variations from 1D (%)

Lau et al. (2017)

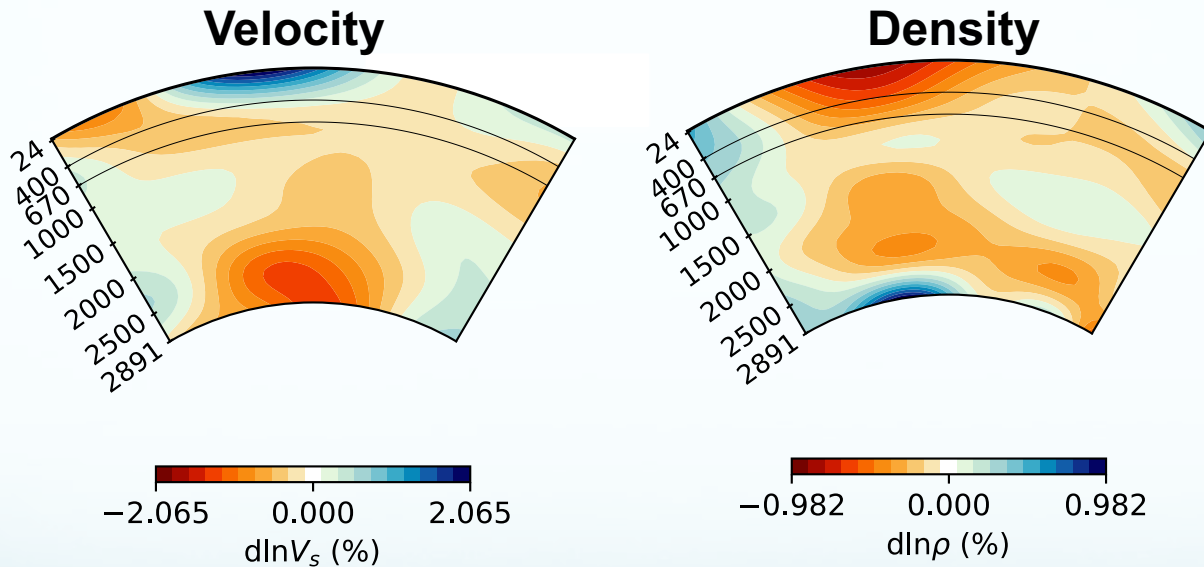


Excess density, $d \ln \rho$ (%)

Thermochemical inversion



Synthesis - LLSVPs



The continental sized **LLSVPs** are divided into a **dense** base and a **light** top. They have a **high temperature**; their higher density is due to increased **iron content**, which makes them rather stable.

Conclusions

- The outer core is 0.2% denser than PREM
- The inner core is 0.4% lighter than PREM.
- We find 1% denser regions at the base of otherwise light LLSVPs, reconciling apparently contradicting earlier constraints
- The dense base of the LLSVP regions correspond to a change in composition with an increase in **FeO and SiO₂**, within overall **high temperature** LLSVPs

