



Simultaneous Jet Calibration with ML including in situ JER Measurement

Journées de Rencontre des Jeunes Chercheurs

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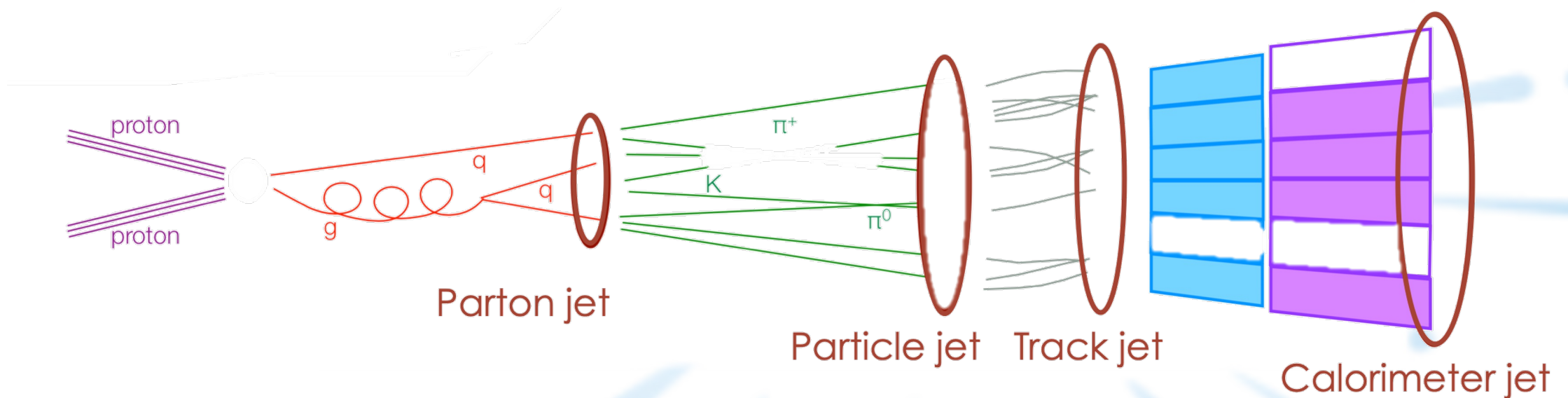


Overview

- Quick summary of jet calibration
- Introduction to machine learning (ML)
- Initial machine learning model
- Modifications of machine learning model
- Intermediate results
- Outlook

Jets Physics

- Jets represent the shower produced by the hadronisation of a quark or gluon and is usually characterised by 4-vector: (\vec{p}, E)
- Its exact definition depends on the jet algorithm (often anti-kT algorithm¹)

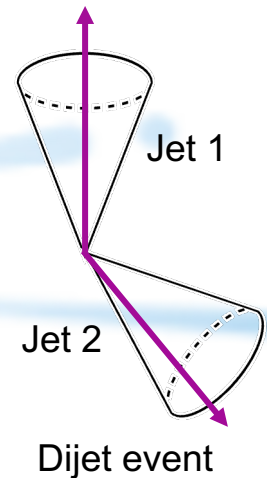
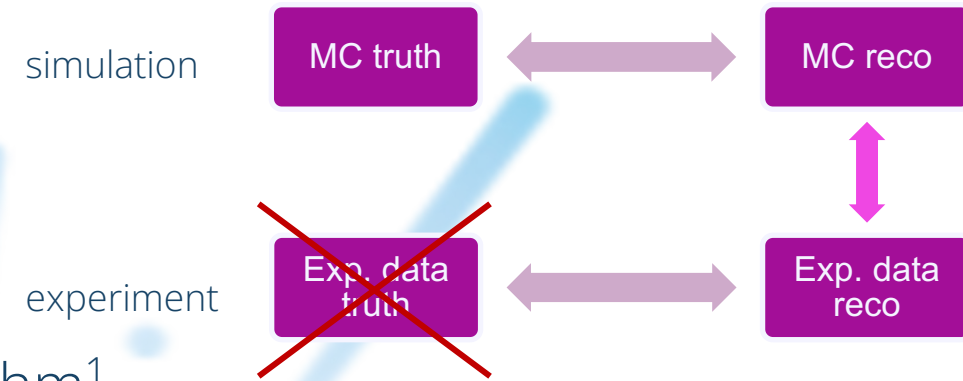


(figure from [“Jet Inputs and MC Calibration”](#), Dilia María Portillo, ATLAS collaboration, 2023)

¹ ([“The anti-kt jet clustering algorithm”](#), Cacciari et al., 2008)

Jet Calibration

- Jet is an exp. observable defined by anti-kT algorithm¹
 - Consist of shower of fundamental particles
 - Characterised by 4-vector: (\vec{p}, E)
- Calibration is essential because detector reacts differently to different kinds of particles (EM vs hadronic) → energy deposits differ depending on particle
- Truth jets:
 - “Hadron-level (‘truth’) jets are formed from detector-stable simulated particles...”²
 - Clustered using anti-kt jet algorithm
- Reco jets:
 - “Detector-level (‘reco’) jets are formed from topologically connected, noise-suppressed calorimeter cellclusters at the electromagnetic scale using [...] the anti-kt jet algorithm...”²



¹ (“The anti-kt jet clustering algorithm”, Cacciari et al., 2008)

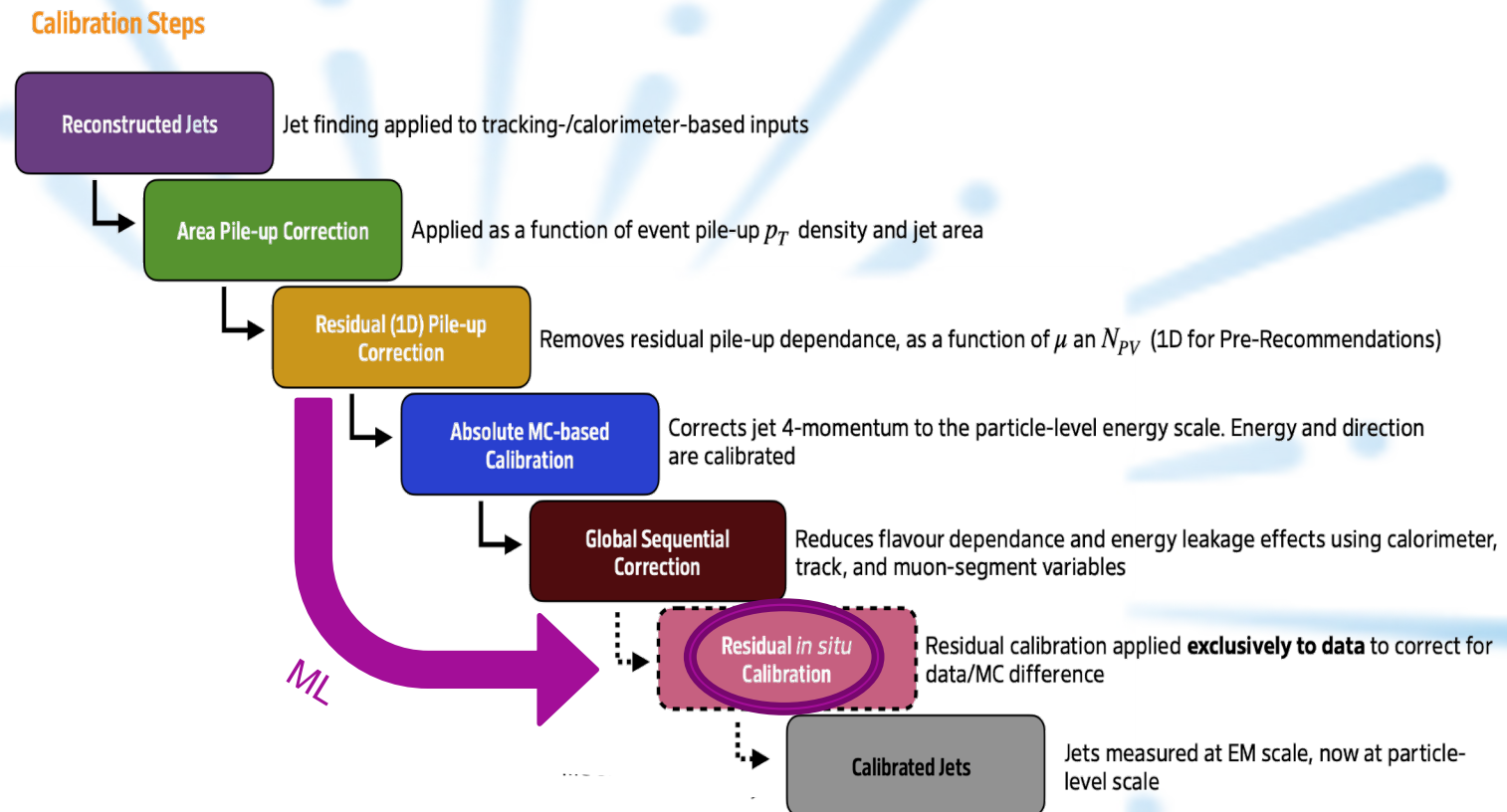
² (“Generalized Numerical Inversion: A Neural Network Approach to Jet Calibration”, ATLAS, 2018)

Jet Calibration in ATLAS

- On-going studies to replace current multi-step calibration scheme by ML model¹

- Current research: try to merge Absolute MC-based Calibration (MCJES) and GSC for faster testing of new algorithms
- Currently done in MonteCarlo (MC) simulations only

- My task: optimise jet energy resolution (JER) including information from exp. data (in addition to MC)



[HCW slides](#), Gediminas Glemža, 2022

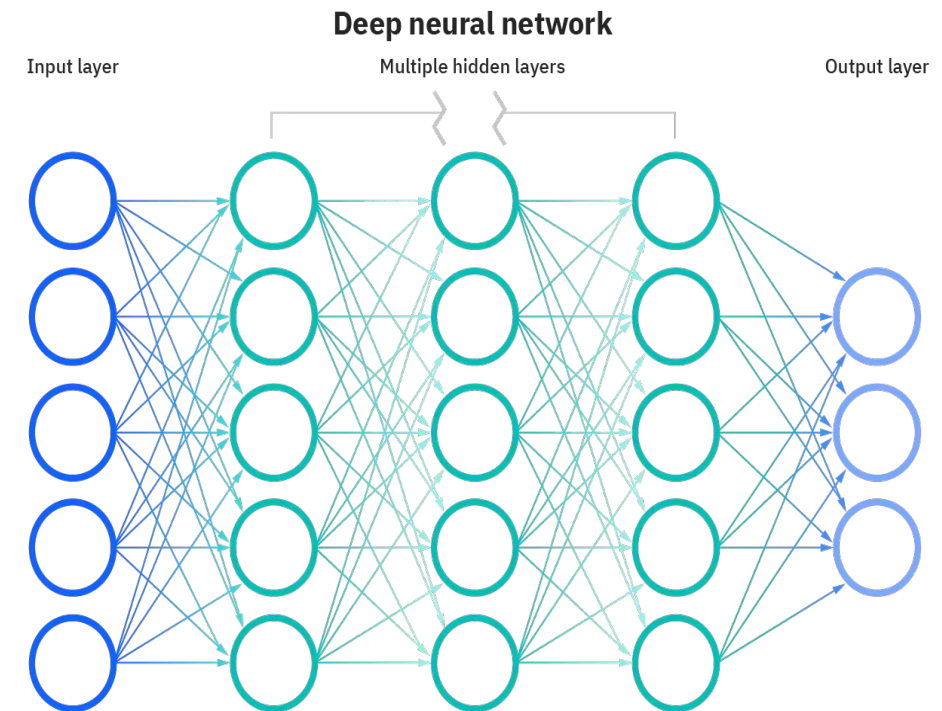
¹ (["New techniques for jet calibration with the ATLAS detector"](#), ATLAS collaboration, 2023)

Machine Learning

“Machine learning is the science of getting computers to act without being explicitly programmed.”

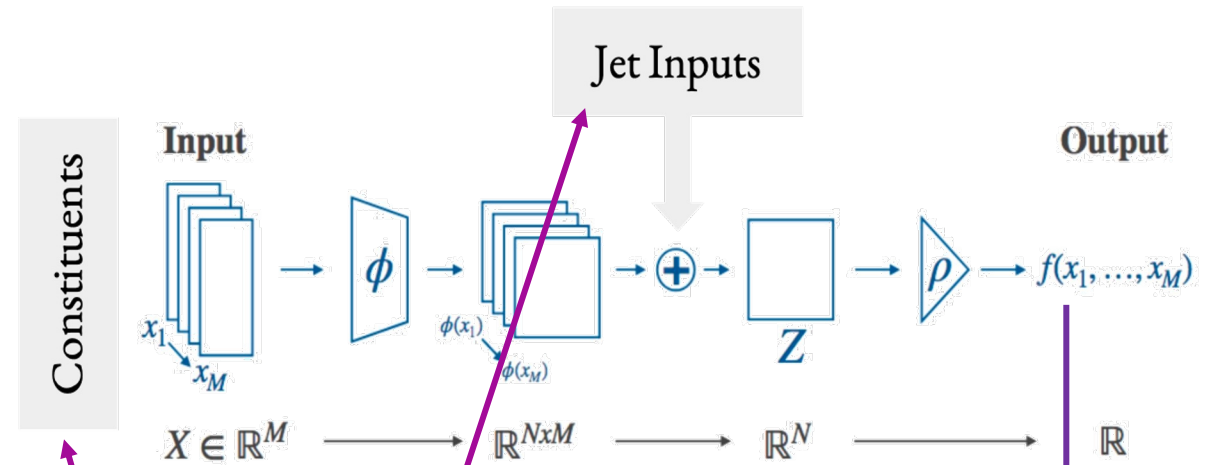
([Andrew Ng](#), Stanford University)

- Deep learning describes part of ML focusing on (deep) Neural Networks (NN)
- Can be used for learning more elaborate functions
- In general, learning model tries to optimise a loss function by repeatedly adjusting its own parameters
- We distinguish between supervised and unsupervised learning:
 - Supervised: we train the model by comparing the model's predictions to a known ground truth (e.g. mean-squared error)
 - Unsupervised: we don't have any ground truth to base our training on



ML Model for Jet Calibration

- Regression problem
 - Output is a probability distribution: $(\mu_{p_T}, \sigma_{p_T})$
 - Mean corresponds to calibration factor
- Deep sets¹
 - Constructed using 2 NN, 1 for jet constituents, 1 for jet 4-vector
 - Model contains permutation invariant layer (e.g. sum layer) because order of events doesn't matter



"Machine Learning the MC JES", K. Greif, C. Pollard, J. Roloff

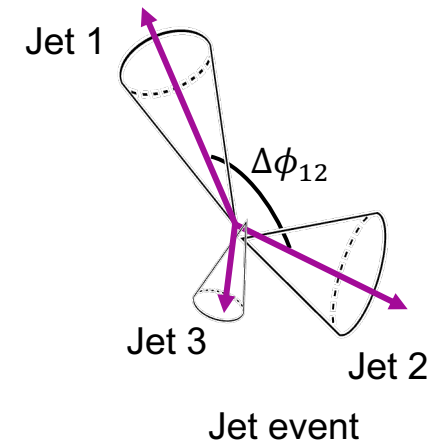
- Supervised learning problem:
 - Compare truth μ to reco level $\mu(\theta), \sigma(\theta)$
 - Likelihood $\mathcal{L}(\theta) = \frac{1}{\sqrt{2\pi\sigma^2(\theta)}} \exp\left(-\frac{(\mu(\theta)-\mu)^2}{2\sigma^2(\theta)}\right)$
 - $\text{loss}(\theta) = \min_{\theta} (-\log \mathcal{L}(\theta))$
 $= \min_{\theta} \left[\frac{1}{2} \frac{(\mu(\theta) - \mu)^2}{\sigma^2(\theta)} + \log \sigma(\theta) + \text{const.} \right]$

Jet Constituents	Jet Inputs (reco)	True Jets	Outputs: calibration factor
(p_x, p_y, p_z, p_T)	(p_x, p_y, p_T, η, E)	$(p_x^{\text{true}}, p_y^{\text{true}}, p_T^{\text{true}}, \eta^{\text{true}}, E^{\text{true}})$	$(\mu_{p_T}, \log(\sigma_{p_T}))$
(80, 4)	(5,)	(5,)	(2,)

¹ ("Deep sets", Zaheer et al., 2018), ("Energy Flow Networks: Deep Sets for Particle Jets", Komiske et al., 2019)

Dijet Events

Jet Constituents	Jet Inputs (reco)	True Jets
(p_x, p_y, p_z, p_T)	(p_x, p_y, p_T, η, E)	$(p_x^{true}, p_y^{true}, p_T^{true}, \eta^{true}, E^{true})$
(80, 4)	(5,)	(5,)

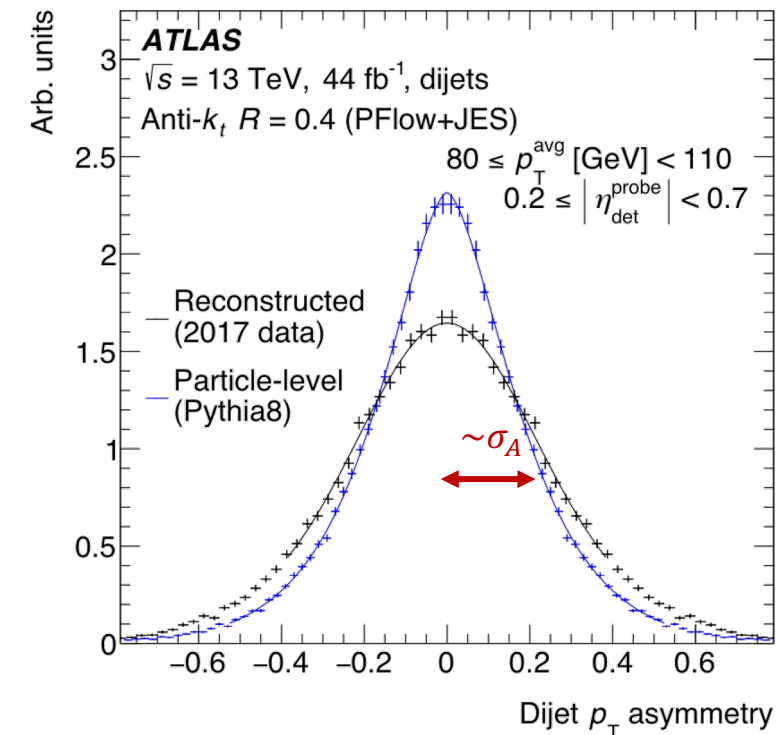


- Each collision event can register several jets
- Focus on events with two jets, i.e. dijet events
- Define dijet asymmetry¹:

$$\mathcal{A} = \frac{p_T^{ref} - p_T^{prob}}{p_T^{avg}}, \quad \text{with } p_T^{avg} = \frac{p_T^{ref} + p_T^{prob}}{2},$$

where ref and probe are randomly assigned to the two leading jets of every dijet event

- Because of momentum conservation, this should be 0 in perfect case (i.e. no noise, reconstruction error)
- For experimental data, we observe distribution around 0 where standard deviation (std) depends on our reconstructed jet resolution



¹ (["Jet energy scale and resolution measured in proton-proton collisions at \$\sqrt{s} = 13 \text{ TeV}\$ with the ATLAS detector"](#), ATLAS collaboration, 2021)

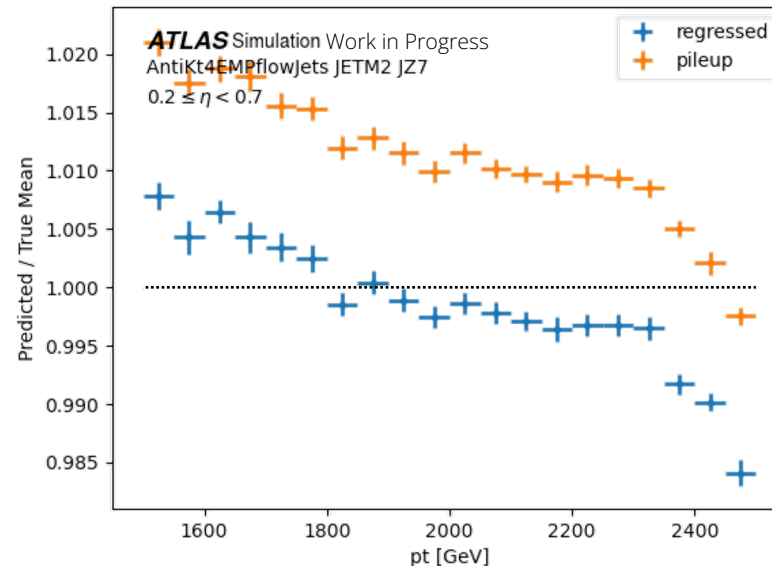
Jet Energy Resolution (JER)

- Jet energy resolution (JER) is related to std of dijet asymmetry (after subtracting the smearing from physics effects, present at hadron level):¹
 - $(\sigma_{\mathcal{A}}^{det})^2 = (\sigma_{\mathcal{A}}^{reco})^2 - (\sigma_{\mathcal{A}}^{truth})^2$, in central part of detector
- Relative JER can be estimated from $\sigma_{\mathcal{A}}^{det}$:
 - Relative JER: $\frac{\sigma_{pT}}{pT} = \frac{\sigma_{\mathcal{A}}^{det}}{\sqrt{2}} \cong \frac{\sigma_{\mathcal{A}}^{reco}}{\sqrt{2}} \sim \sigma_{\mathcal{A}}^{reco}$
 - NN-based correction shouldn't impact truth, so it's sufficient to directly use $\sigma_{\mathcal{A}}^{reco}$
 - Completely independent of true labels → useful for exp. Data
- Update loss function:
 - $loss(\theta) \rightarrow loss(\theta) + f * \sigma_{\mathcal{A}}'(\theta)$
 - ML model simultaneously minimises the JER measured in-situ and the original loss
 - No longer fully dependent on truth level, ML model is only partially supervised

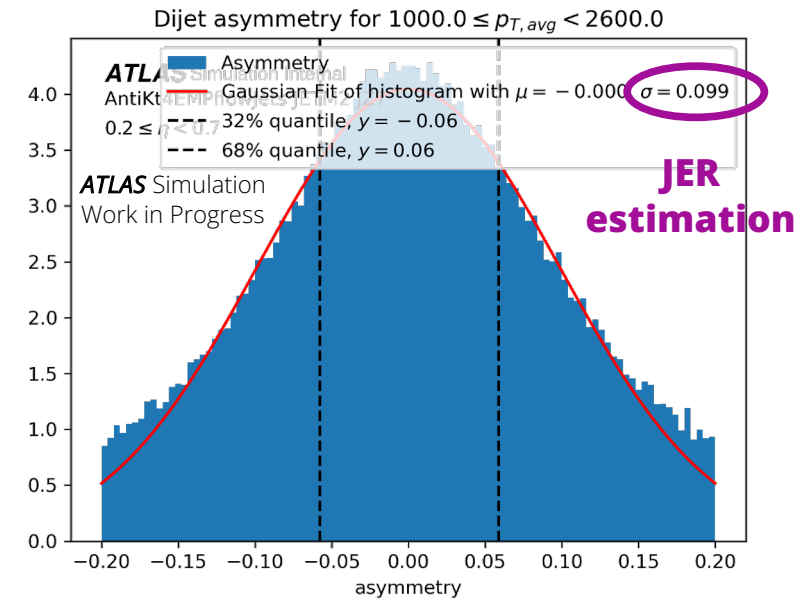
¹(["Jet energy scale and resolution measured in proton-proton collisions at \$\sqrt{s} = 13\$ TeV with the ATLAS detector"](#), ATLAS collaboration, 2021)

Results with $f = 0$

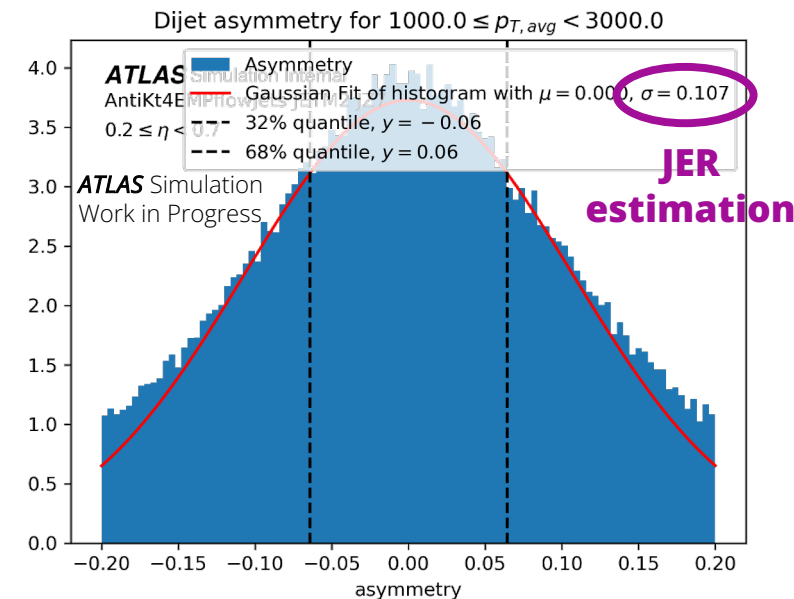
- Asymmetry factor f is fixed to 0
- ML model doesn't improve/has little effect on JER
 - JER of reco jets (at pileup level): $\sim 9.9\%$
 - JER of regressed jets (i.e. after applying calibration factors predicted by ML model): $\sim 10.7\%$
- Can JER be improved by adding asymmetry term in loss function, i.e. $f \neq 0$?



Testing set: reco jets



Testing set: regressed jets



First results: $f = 0$ vs $f \neq 0$

$f = 0$

- Asymmetry factor f is fixed to 0
- Predicted pT values:
 - $p_T^{true} \in [1100, 2600]$ GeV
 - $p_T \in [1000, 3000]$ GeV
- JER estimation:
 - JER of jets before training: $\sim 9.9\%$
 - JER of regressed jets (i.e. after applying calibration factors predicted by ML model): $\sim 10.7\%$

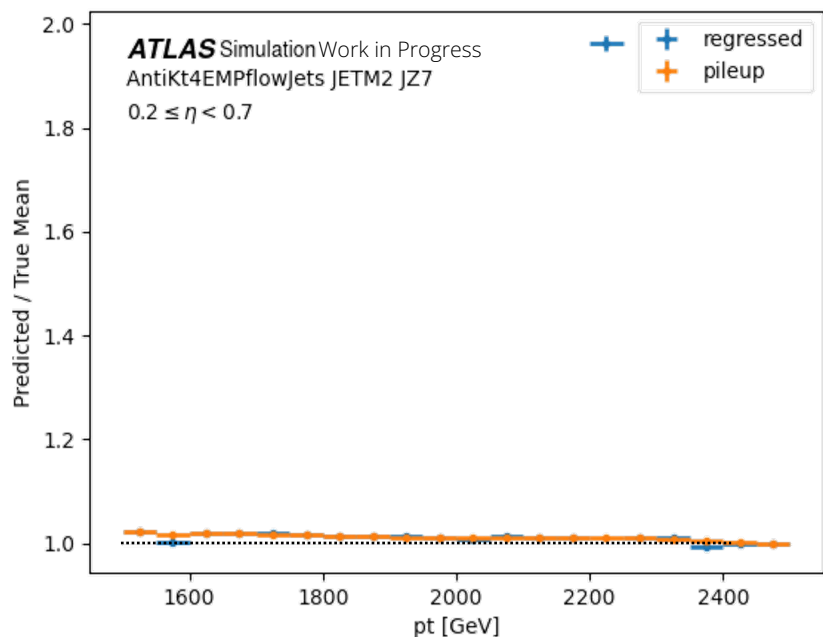
$f \neq 0$

- Asymmetry factor f is varied between 0 and 10
- Predicted pT values:
 - $p_T^{true} \in [1100, 2600]$ GeV
 - $p_T \in [-1'792'700, 394'000]$ GeV
- JER estimation:
 - JER of jets before training: $\sim 9.9\%$
 - JER of regressed jets (i.e. after applying calibration factors predicted by ML model): $\sim 10.2\%$

→ First naive implementation failed!

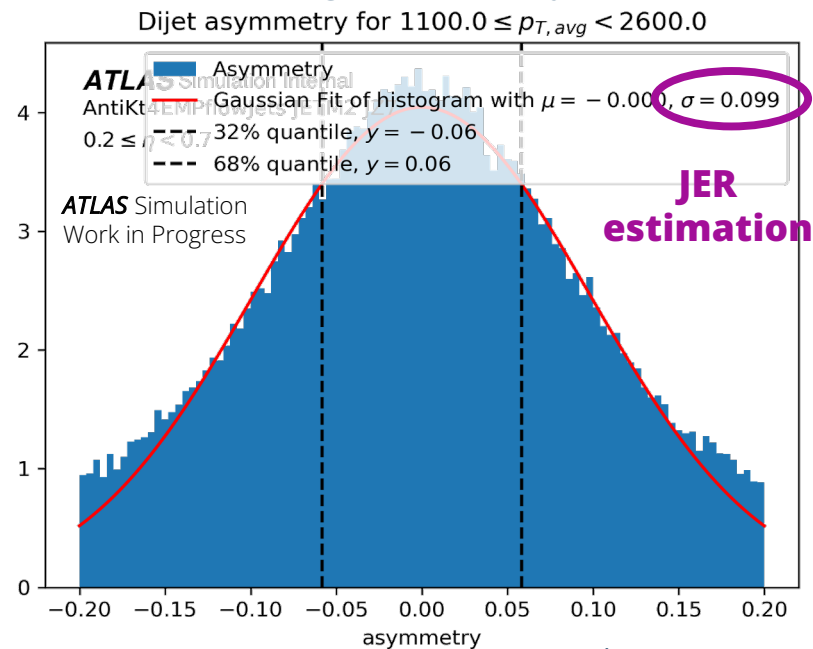
First Results with $f \neq 0$

- Predicted pT much worse
- Predicted JER slightly better:
 - JER of jets before training: $\sim 9.9\%$
 - JER of regressed jets (i.e. after applying calibration factors predicted by ML model): $\sim 10.2\%$

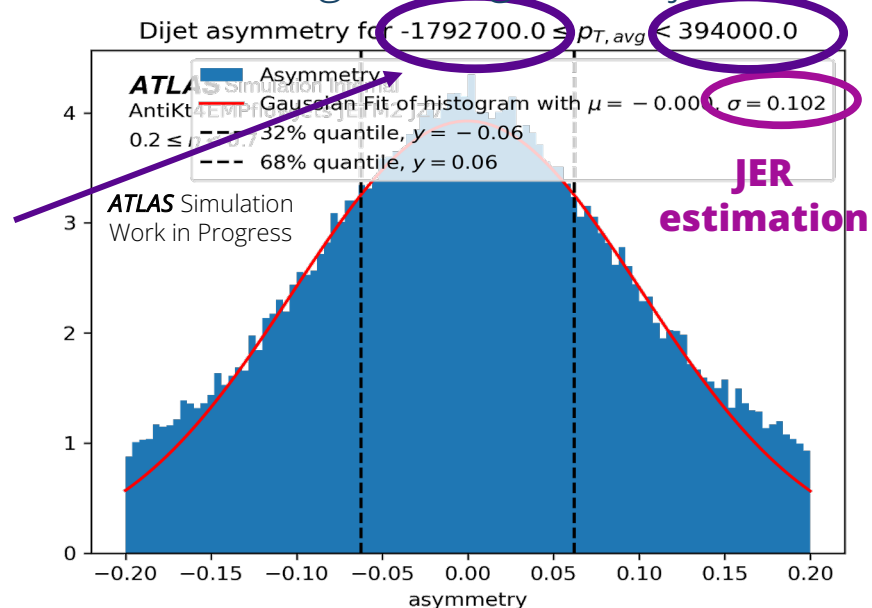


Problem: Why do we have negative calibration factors?

Testing set: reco jets



Testing set: regressed jets



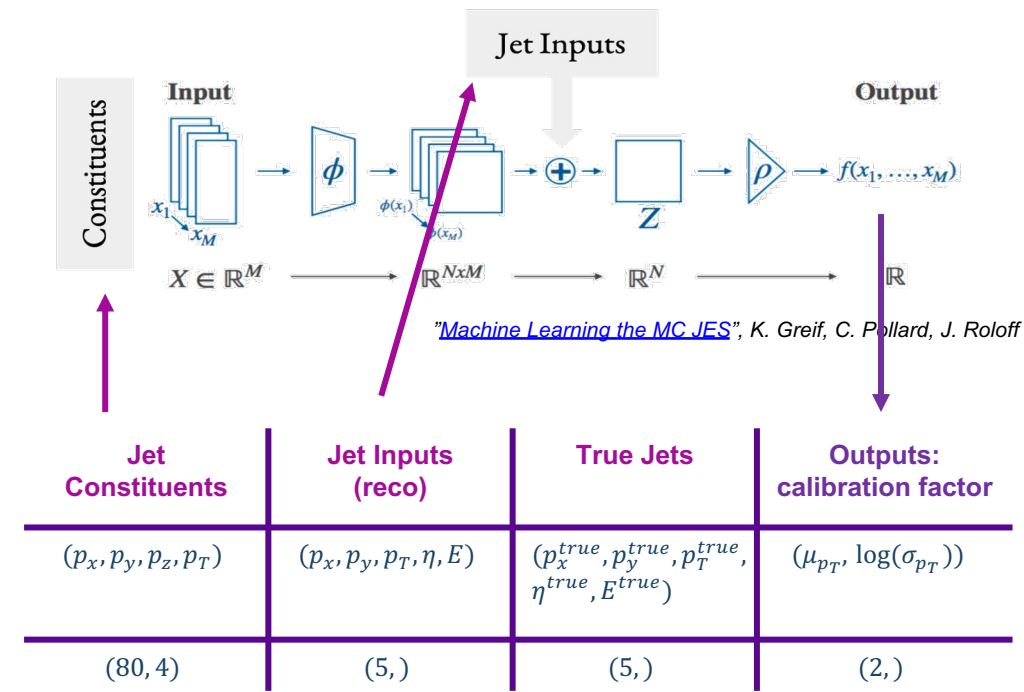
What's next

- Naive approach doesn't work immediately
- It seems the two loss terms contradict/work against each other
 - Add softplus layer to restrict outputs of NN to positive values¹
 - Introduce penalty term that forbids unphysical solution
 - Standardise truth targets
- Use **GSC variables**² (which are known to improve JER) in addition to jet 4-vector as jet inputs

NEW! **GSC variables**

Energy fractions, tracking, detector eta, muon segments, pileup etc.

(20,)

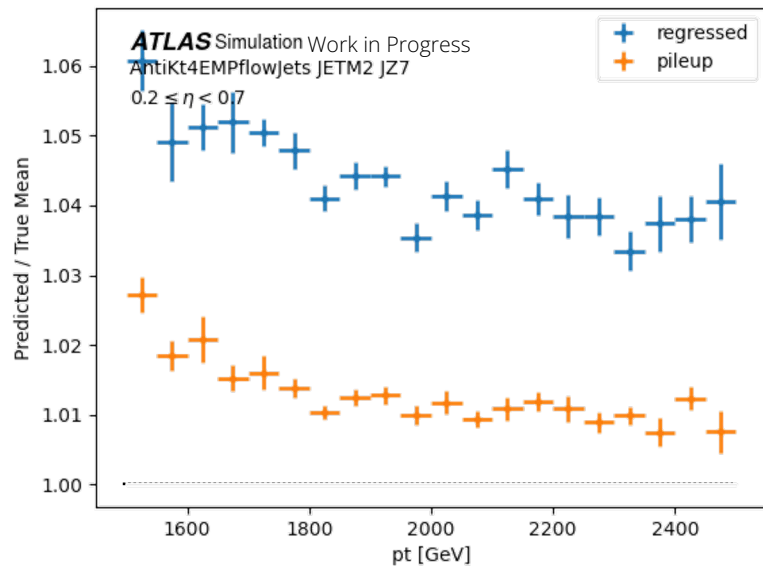


¹ ("tf.math.softplus", TensorFlow, September 2022),

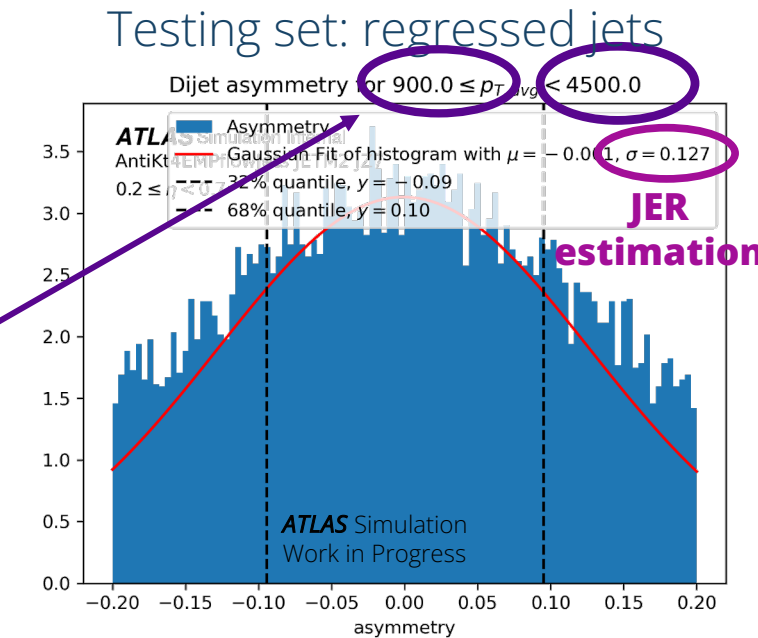
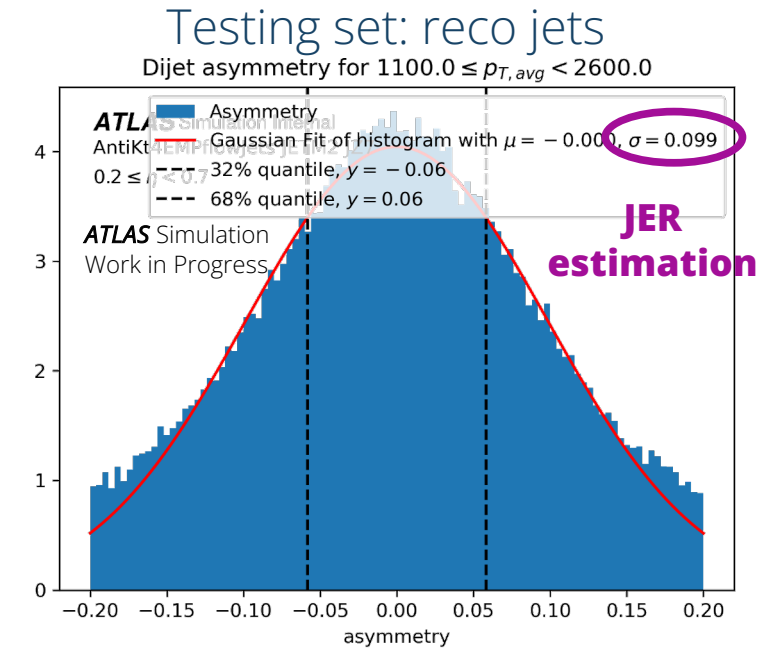
² ("New techniques for jet calibration with the ATLAS detector", ATLAS collaboration, 2023)

More results with $f \neq 0$

- New variables added
- Softplus layer applied
- Predicted / True ratio pf pT is getting closer to 1 but JER is worse
 - JER of reco jets: $\sim 9.9\%$
 - JER of regressed jets (i.e. after applying calibration factors predicted by ML model): $\sim 12.7\%$



Problem: pT predictions are still off





Thank you for your attention!

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Backup



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Deep Sets Model

- Model contains permutation invariant layer (e.g. sum layer)
- Why do we want permutation invariance for jet physics?
 - Order of events doesn't matter, each collision event happens independently
 - Can guarantee infrared and collinear (IRC) safety which is important for comparing QCD theory predictions to experimental results

IRC-Safe Observable Decomposition. *An IRC-safe observable \mathcal{O} can be approximated arbitrarily well as:*

$$\mathcal{O}(\{p_1, \dots, p_M\}) = F \left(\sum_{i=1}^M z_i \Phi(\hat{p}_i) \right), \quad (1.2)$$

where z_i is the energy (or p_T) and \hat{p}_i the angular information of particle i .

Approximate functions F, Φ
with neural networks

¹(["Deep sets"](#), Zaheer et al., 2018),
(["Energy Flow Networks: Deep Sets for Particle Jets"](#), Komiske et al., 2019)

ML Model for Jet Calibration

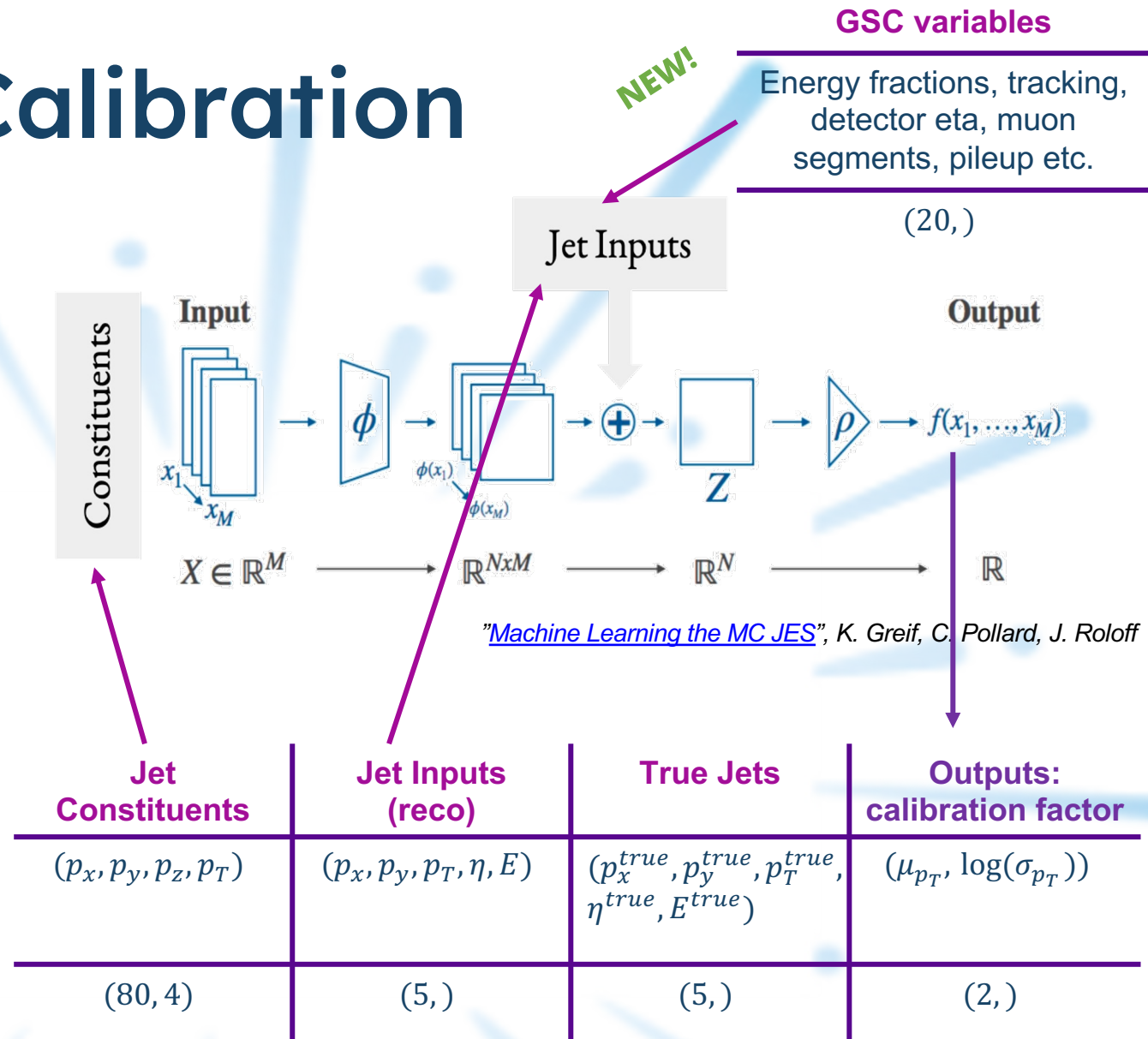
- Regression problem
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 - Constructed using 2 NN, 1 for jet constituents, 1 for jet 4-vector
 - Model contains permutation invariant layer (e.g. sum layer) because order of events doesn't matter
- Supervised learning problem:

Compare truth μ to reco level $\mu(\theta)$, $\sigma(\theta)$

$$\text{Likelihood } \mathcal{L}(\theta) = \frac{1}{\sqrt{2\pi\sigma^2(\theta)}} \exp\left(-\frac{(\mu(\theta)-\mu)^2}{2\sigma^2(\theta)}\right)$$

$$\text{loss}(\theta) = \min_{\theta} (-\log \mathcal{L}(\theta))$$

$$= \min_{\theta} \left[\frac{1}{2} \frac{(\mu(\theta) - \mu)^2}{\sigma^2(\theta)} + \log \sigma(\theta) + \text{const.} \right]$$



¹ (*"Deep sets"*, Zaheer et al., 2018), (*"Energy Flow Networks: Deep Sets for Particle Jets"*, Komiske et al., 2019)

Add GSC variables

Calorimeter	$f_{\text{LAr}0-3}^*$	The E_{frac} measured in the 0th-3rd layer of the EM LAr calorimeter
	$f_{\text{Tile}0*-2}$	The E_{frac} measured in the 0th-2nd layer of the hadronic tile calorimeter
	$f_{\text{HEC},0-3}$	The E_{frac} measured in the 0th-3rd layer of the hadronic end cap calorimeter
	$f_{\text{FCAL},0-2}$	The E_{frac} measured in the 0th-2nd layer of the forward calorimeter
Jet kinematics	$N_{90\%}$	The minimum number of clusters containing 90% of the jet energy
	$p_{\text{T}}^{\text{JES}*}$	The jet p_{T} after the MCJES calibration
Tracking	η^{det}	The detector η
	w_{track}^*	The average p_{T} -weighted transverse distance in the η - ϕ plane between the jet axis and all tracks of $p_{\text{T}} > 1$ GeV ghost-associated with the jet
	N_{track}^*	The number of tracks with $p_{\text{T}} > 1$ GeV ghost-associated with the jet
Muon segments	f_{charged}^*	The fraction of the jet p_{T} measured from ghost-associated tracks
	N_{segments}^*	The number of muon track segments ghost-associated with the jet
Pile-up	μ	The average number of interactions per bunch crossing
	N_{PV}	The number of reconstructed primary vertices

Table 1: List of variables used as input to the GNNC. Variables with a * correspond to those that are also used by the GSC.

¹ (see table 1 in [“New techniques for jet calibration with the ATLAS detector”](#), ATLAS collaboration, 2023)

Bayesian Optimisation of Hyperparameters

- Training set:
 - JETM2 JZ7
 - Initially 3Mio events but after selection cuts (dijet & η) only ca. 677k
 - Unflattened (because current resampling seems bad for training)
- Bayesian optimisation of hyperparameters
 - 10 trials with 10 different validation folds

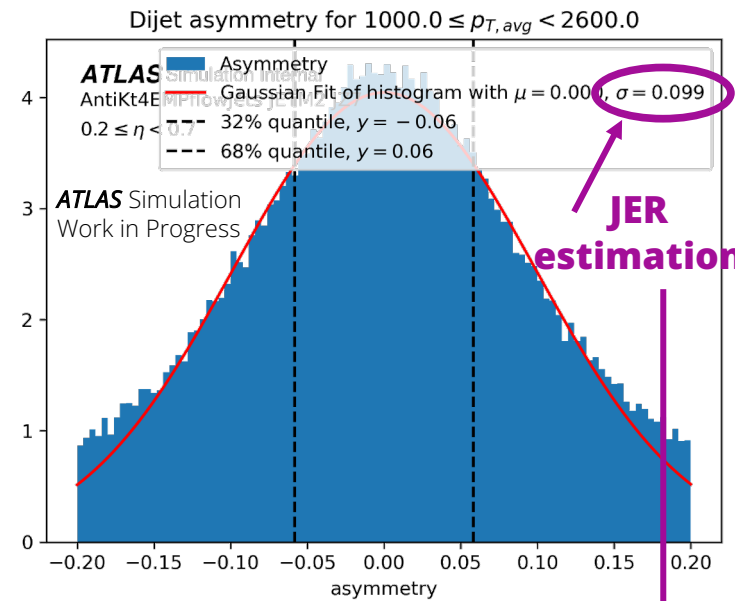
Hyperparameter Search Space

Use $\log(p_T)$	Dropout cluster	Dropout jet	Learning rate	Factor asymmetry term
[False, True]	[0.0, 0.1, 0.2, 0.3, 0.4, 0.5]	[0.0, 0.1, 0.2, 0.3, 0.4, 0.5]	[0.0001, 0.01]	$f \in [0, 10]$

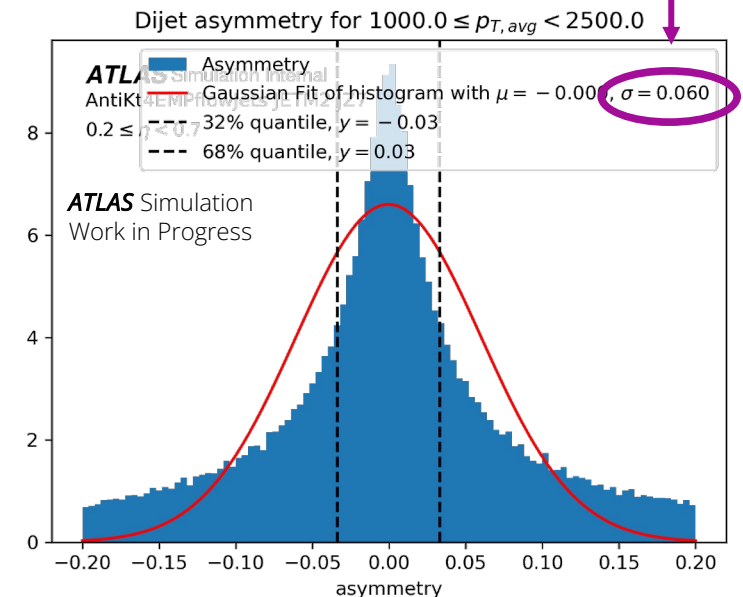
Dijet Asymmetry of JETM2 JZ7 (before Training)

- Truth dijet asymmetry has non-Gaussian tails
 - Use Gaussian as a first approximation
 - Can be improved by fitting convolution of exponential and Gaussian function¹
- Goal is to minimise JER
 - Cannot get better than truth level
 - True asymmetry is limited by smearing from physics effect
- After training:
 - Apply predicted calibration factors to uncalibrated test samples
 - Check their p_T distribution, dijet asymmetry & estimate the JER from it
 - Call them 'regressed jets'

Testing set: reco jets



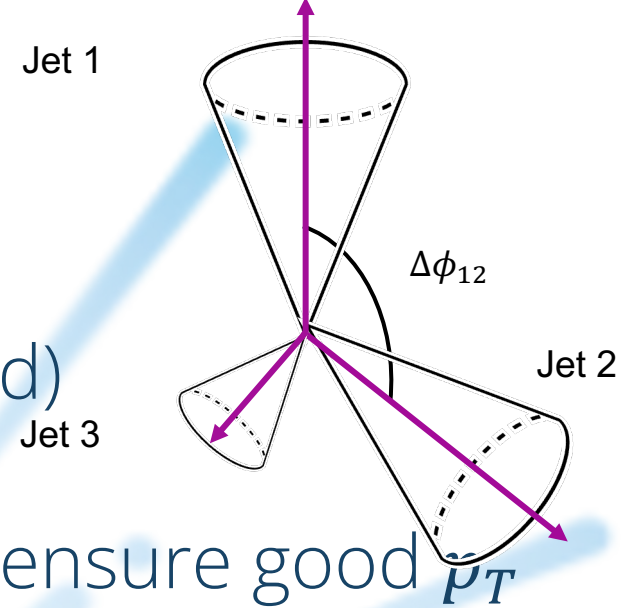
Testing set: true jets



¹ ("[Jet energy scale and resolution measured in proton-proton collisions at \$\sqrt{s} = 13\$ TeV with the ATLAS detector](#)", ATLAS collaboration, 2021)

Input: Selection Criteria

- Central jets (to simplify problem, will be extended)
 $|\eta| \in [0.2, 0.7]$
- Apply dijet topology cuts¹ on jet components to ensure good balance between leading jets
 $\Delta\phi_{12} > 2.7 \text{ rad}$
 $p_{T3} < \max(25 \text{ GeV}, 0.25 \cdot p_{T,avg})$
- pT between 800 and 2800 GeV because using JZ7
 - Later add more JZ slices

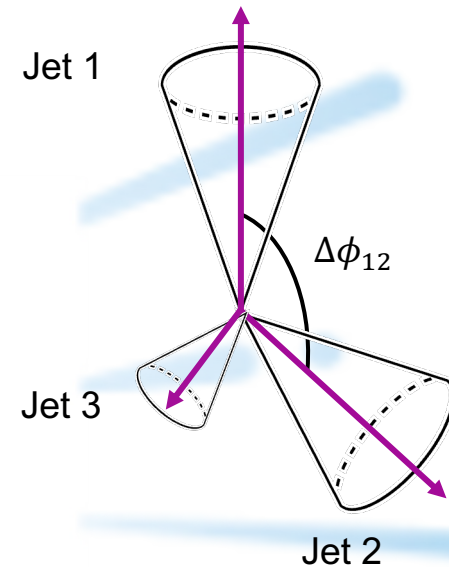


¹(["Jet energy scale and resolution measured in proton-proton collisions at \$\sqrt{s} = 13 \text{ TeV}\$ with the ATLAS detector"](#), ATLAS collaboration, 2021)

Input: MC Samples

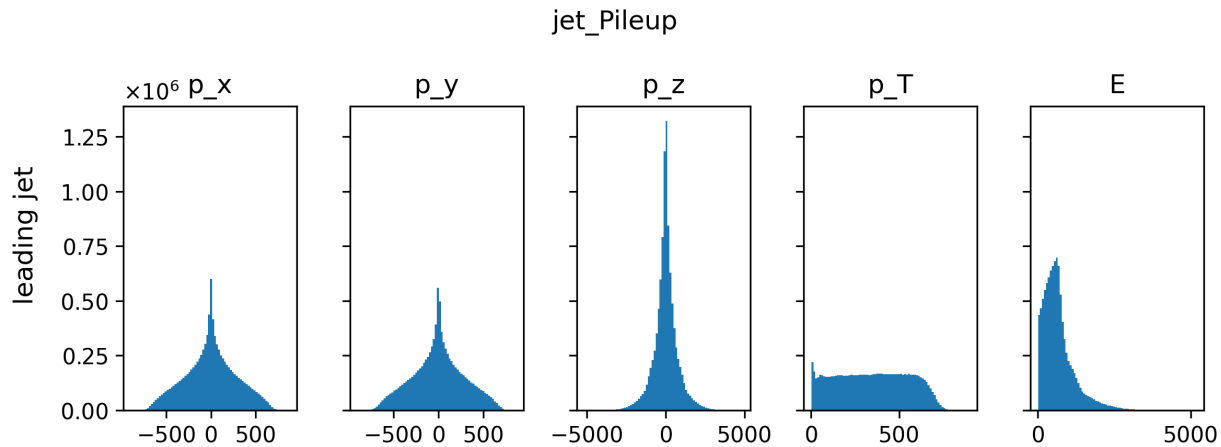
- Old input samples:
 - Per event: 1-2 leading jets, no event info
 - All jets are treated independently
 - Isolated jets, lots of monojet events
 - Empty entries are filled with mask value: 0
 - Info about masking will be passed on to NN
- Modify format of input samples:
 - Keep event info of 3 leading jets
 - Empty entries are filled with new mask value: -10k
- Motivation: apply dijet topology cuts on jet components to ensure good p_T balance between leading jets

Input data	Jet Constituents	Jet Inputs
old	(p_x, p_y, p_z, p_T)	(p_x, p_y, p_z, p_T, E)
new	$(p_{x_i}, p_{y_i}, p_{T_i}, \eta_i),$ $i \in \{1, 2, 3\}$	$(p_{T_i}),$ $i \in \{1, 2, 3\}$

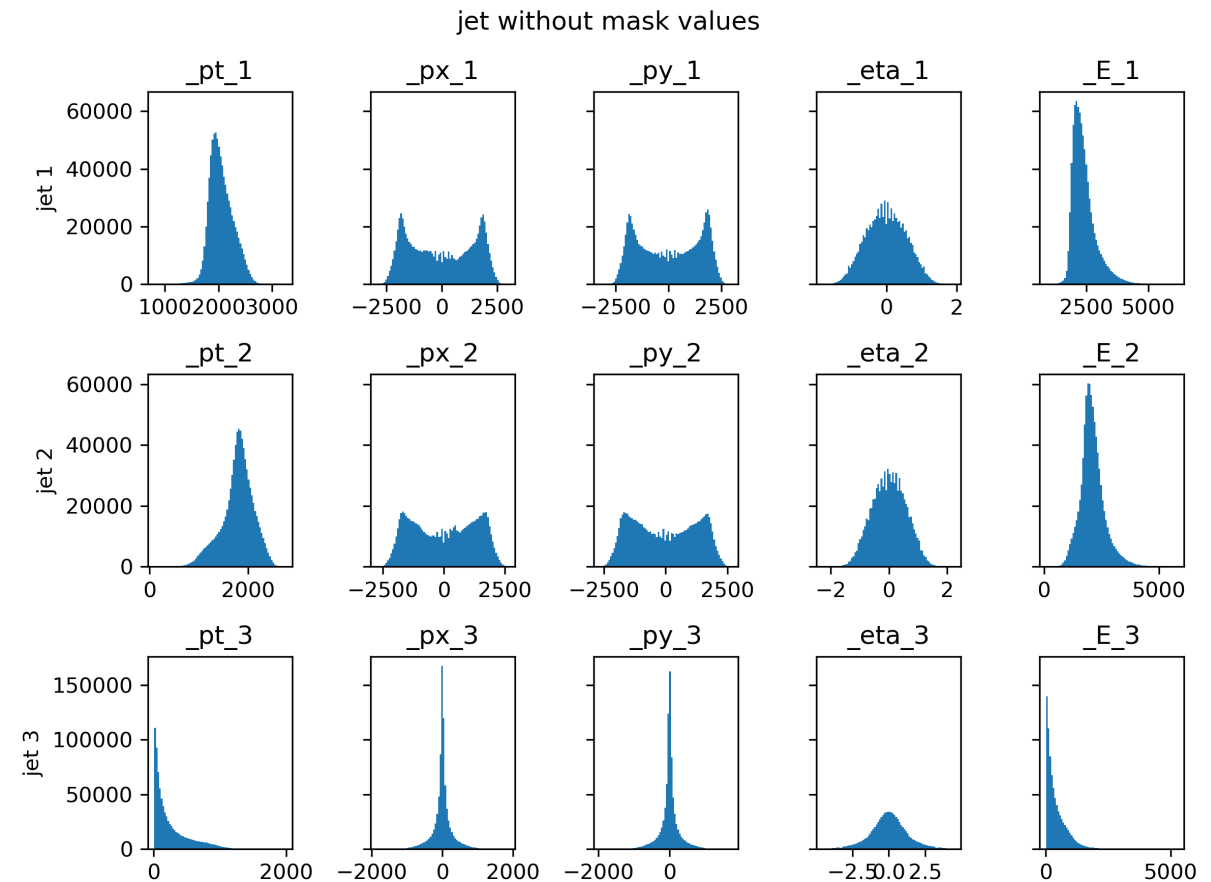


Input: Jet Components

Old MC samples



New MC samples



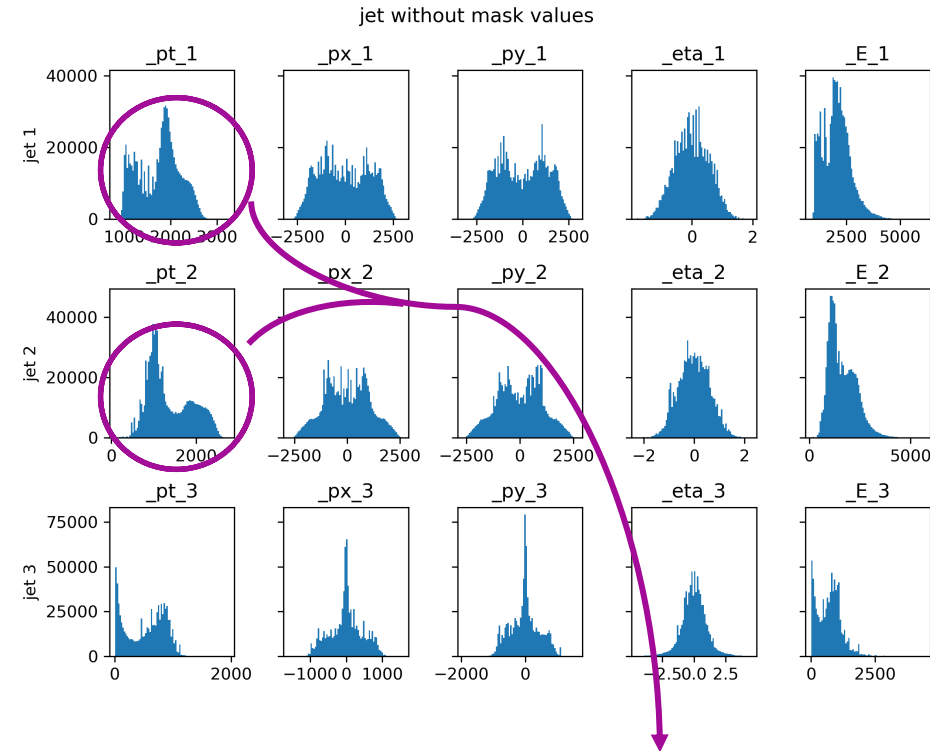
- Note that p_T distribution on LHS has been flattened by resampling
- On RHS no resampling/flattening

Produced from mc20a, JETM2, JZ7

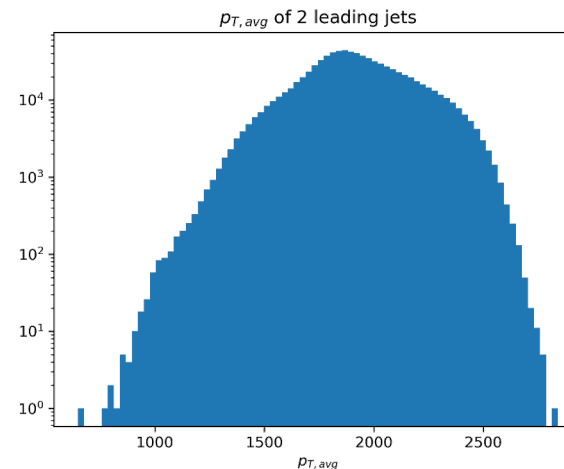
Input: Jet Components

- Events have been resampled to flatten distribution of $\log p_T^{avg}$ where $p_T^{avg} = (p_{T_1} + p_{T_2})/2$
 - This approach was chosen because $\log p_T^{avg}$ is physically significant
- **PROBLEM:**
 - Resampling assigns some very large weights to certain events
 - Weights differ by several orders of magnitude

New MC samples: resampled



Before resampling



With resampling

