



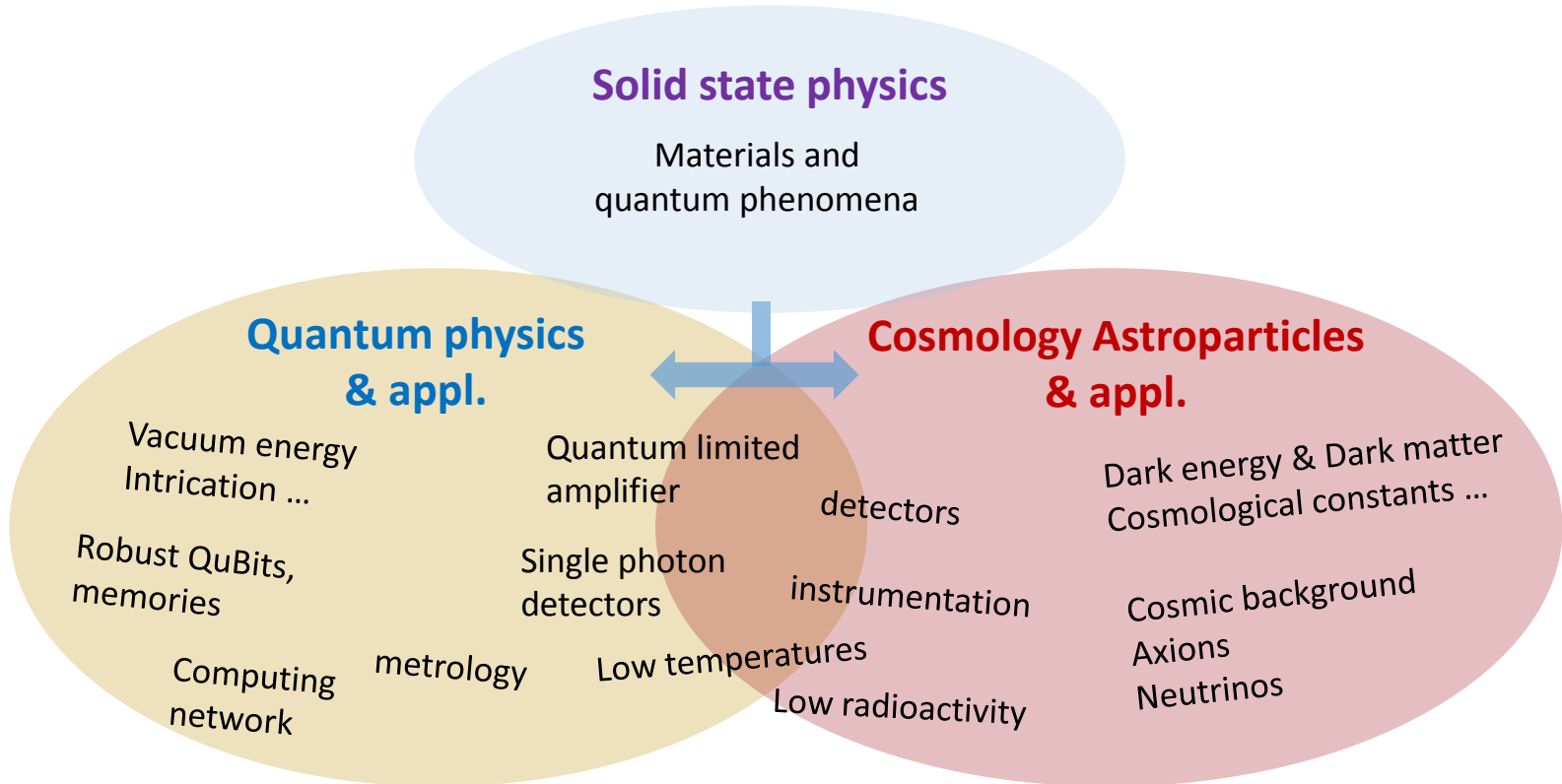
# Quantum Technologies applied to $2\infty$ physics

Hélène le Sueur



# QT / 2 $\infty$

What do they have in common?



**Qu-tech**



**reaching the « quantum limit »**

**Advanced electronics  
Shields from radioactivity**



**Cosmology – astroparticles**

# “Quantum Detectors”

What are we talking about?

**Quantum Sensing, C.L. Degen et al.**

“ Use of a *quantum system*, *quantum properties* or *quantum phenomena* to perform a measurement of a physical quantity”

Rev. Mod. Phys. **89**, 035002 (2017)

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Device based on quantum physics (eg solid state...)?

→ ~ all of them

Device that operates in the quantum regime ?

i.e.  $kT \ll$  characteristic energies

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i.e.  $kT \ll$  characteristic energies

**More specifically:** detectors that exploit

- Quantum coherence
- Superposition
- Entanglement
- Squeezing
- backaction evasion

# “Quantum Detectors”

## Synopsis

**General scope:** single ‘X’ (atom, electron, ...) devices

**Key feature:** quantum coherence

**Figure of merit:** strong sensitivity to external disturbances

**Famous examples:**

Atom clocks, squids, cold atom gravimeters, gravitational wave detectors

**Already exploited to measure:**

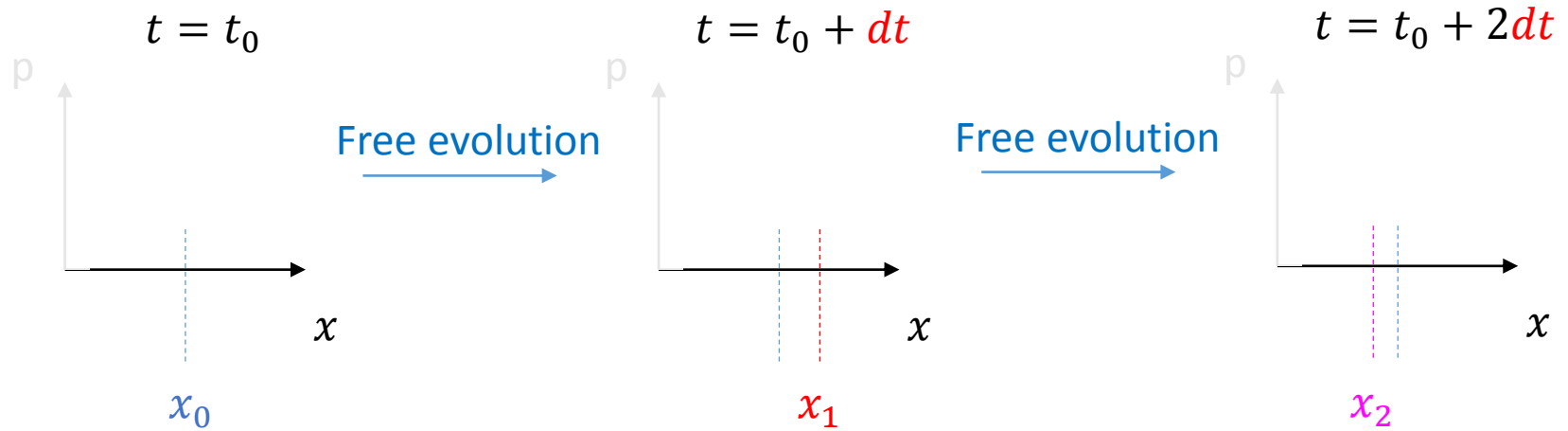
magnetic and electric fields, time and frequency, gravity field (eg rotations...), temperature, pressure...

# Today's menu

- What does a « quantum measurement » mean ?  
A bit of definitions
- Two strategies for em field measurements:  
click or flux
- How to build a superconducting quantum circuit  
low losses and some nonlinearity
- 2 nice examples of QT detectors applied to  $2\infty$   
The parametric amplifier and the single microwave photon counter

# Measurement in quantum mechanics

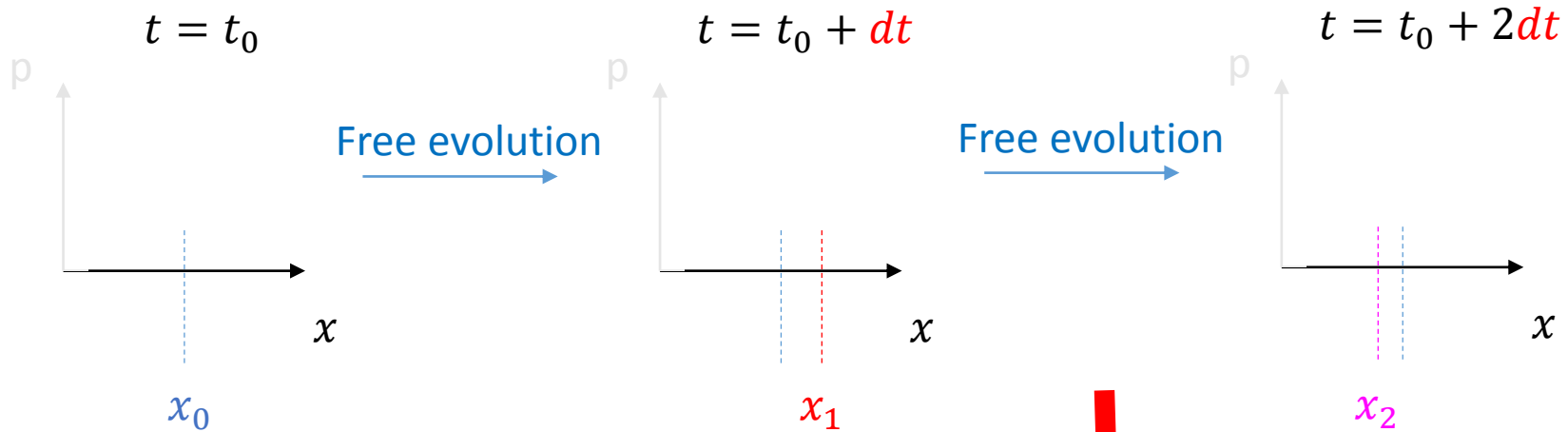
Measure the position  $x$  of a free particle with super high precision





# Measurement in quantum mechanics

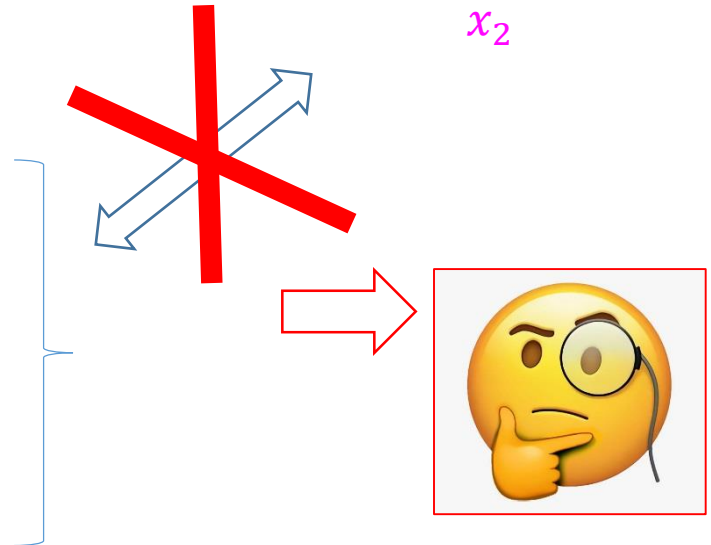
Measure the position  $x$  of a free particle with super high precision



$$x_1 = x_0 + \frac{p}{m} dt$$

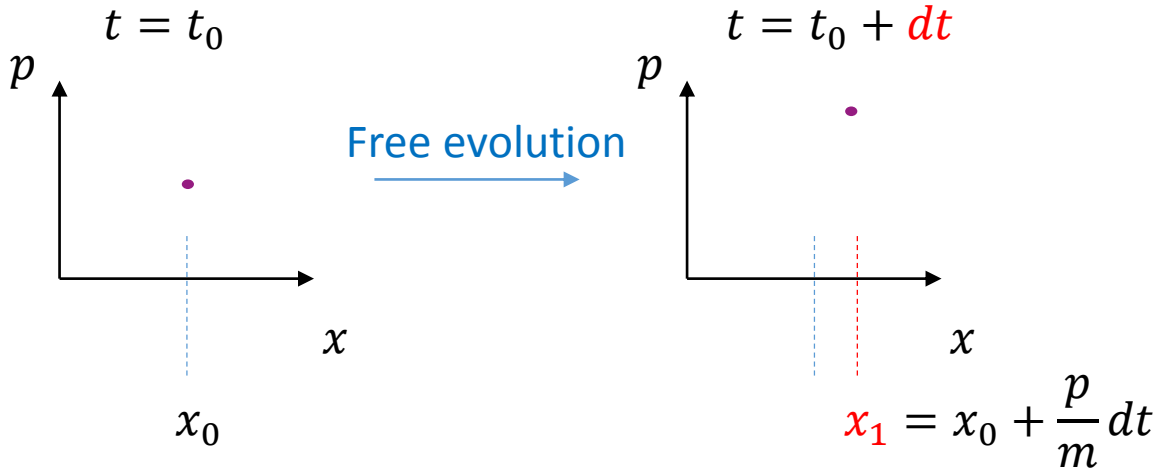
$$x_2 = x_1 + \frac{p}{m} dt$$

Free evolution :  $p$  conserved



# Measurement in quantum mechanics

Measure the position  $x$  of a free particle with super high precision

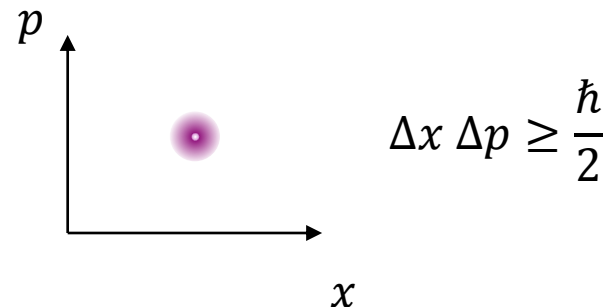


$x$  measurement has given an unpredictable (and non reproducible) kick on  $p$

Conversely, measuring  $p$  would push  $x$  in an unpredictable (and non reproducible) way

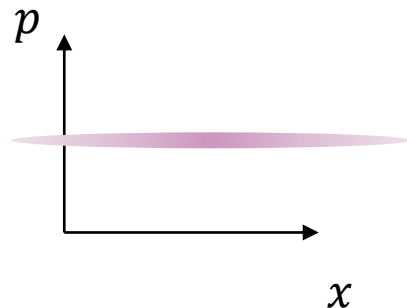
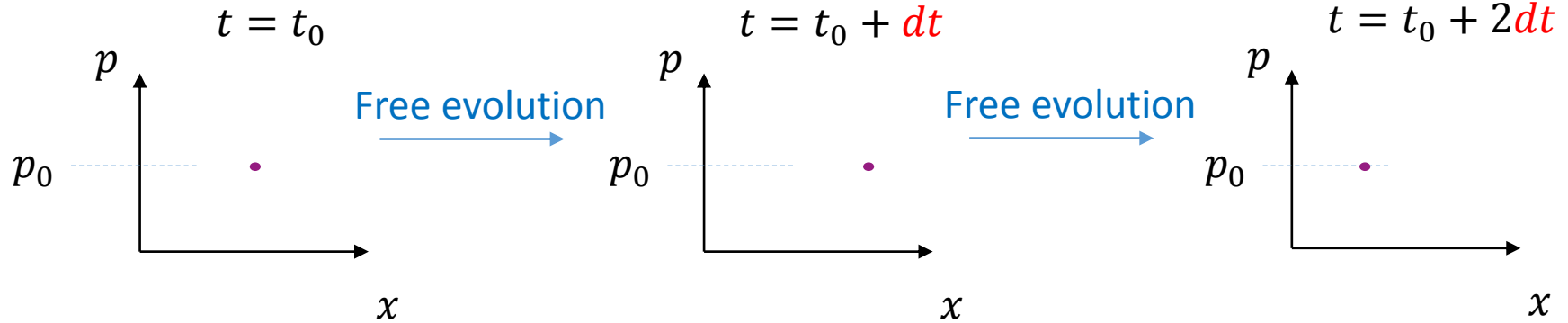
« measurement back-action »

$$[\hat{x}, \hat{p}] \neq 0$$



# Measurement in quantum mechanics

Measure the momentum  $p$  of a free particle with super high precision



$$x_1 = x_0 + \frac{p}{m} dt$$

$$x_2 = x_1 + \frac{p}{m} dt$$

Free evolution :  $p$  conserved



« Quantum Non Demolition measurement of  $p$  »

# Measurement in quantum mechanics

## Quantum non demolition

$$[\hat{a}(t), \hat{a}(t + dt)] = 0$$

V. Braginsky, Y. I. Vorontsov, and K. P. Thorne, Science 209, 547 (1980),  
see also Caves, Unruh

## Free particle

$$[\hat{x}(t), \hat{x}(t + dt)] = i \hbar dt/m$$

$$[\hat{p}(t), \hat{p}(t + dt)] = 0$$

$$\hat{H} |n\rangle = E_n |n\rangle$$

$p$  and  $E$  are continuous QND observables

## Oscillator

$$[\hat{x}(t), \hat{x}(t + dt)] = \frac{i \hbar}{m\omega} \sin(\omega dt)$$

$$[\hat{p}(t), \hat{p}(t + dt)] = i \hbar m\omega \sin(\omega dt)$$

$x$  and  $p$  are stroboscopic QND observables !

$$E \text{ and } x \pm i \frac{p}{m\omega}$$

are continuous QND observables !



Quadratures do not commute

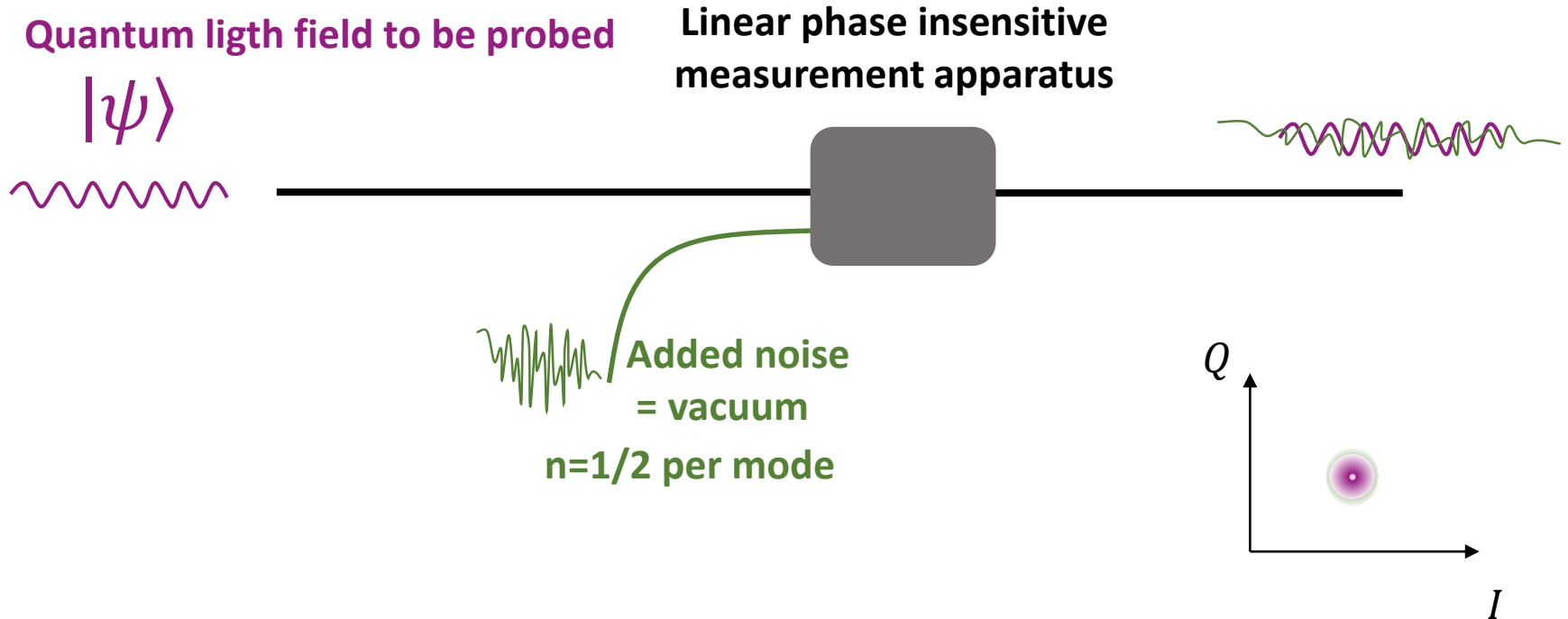
← amplitude

**Measure one quadrature of the amplitude : « Backaction evading measurements »**

# Measuring small (coherent) fields

Noise added by vacuum fluctuations

Caves, Phys. Rev. D **1981**, 23, 1693–1708



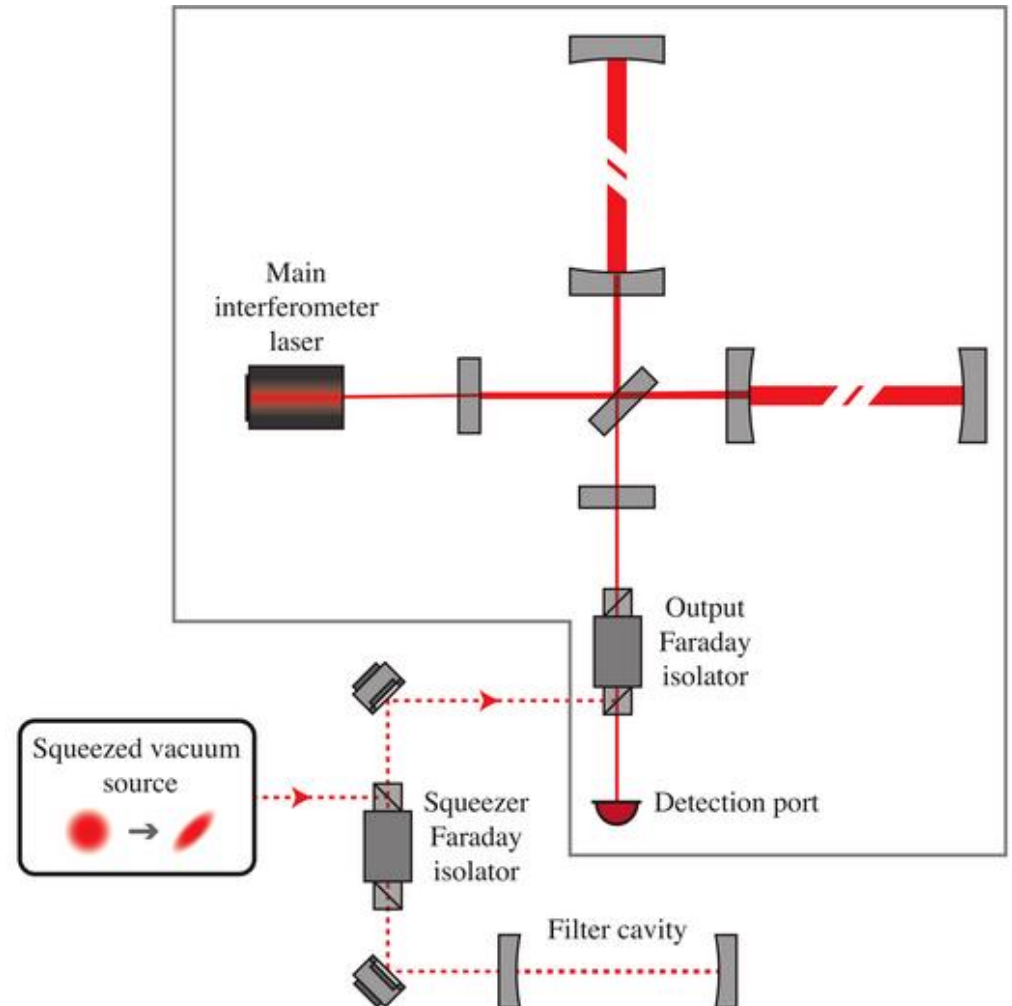
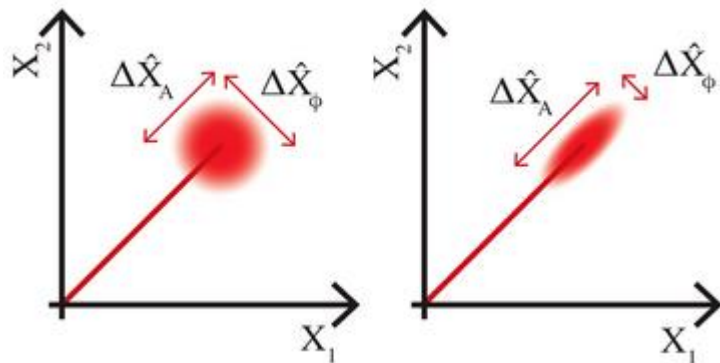
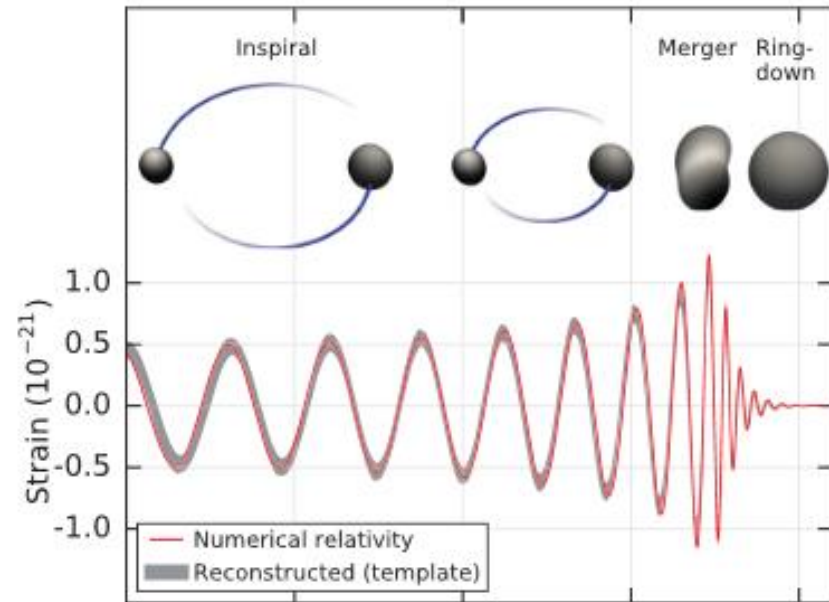
« Standard quantum limit »

Strategy: Prepare vacuum in a « squeezed state » to reduce measurement noise

# GW detectors use squeezing in order to beat standard quantum limit

PRL **116**, 061102 (2016)

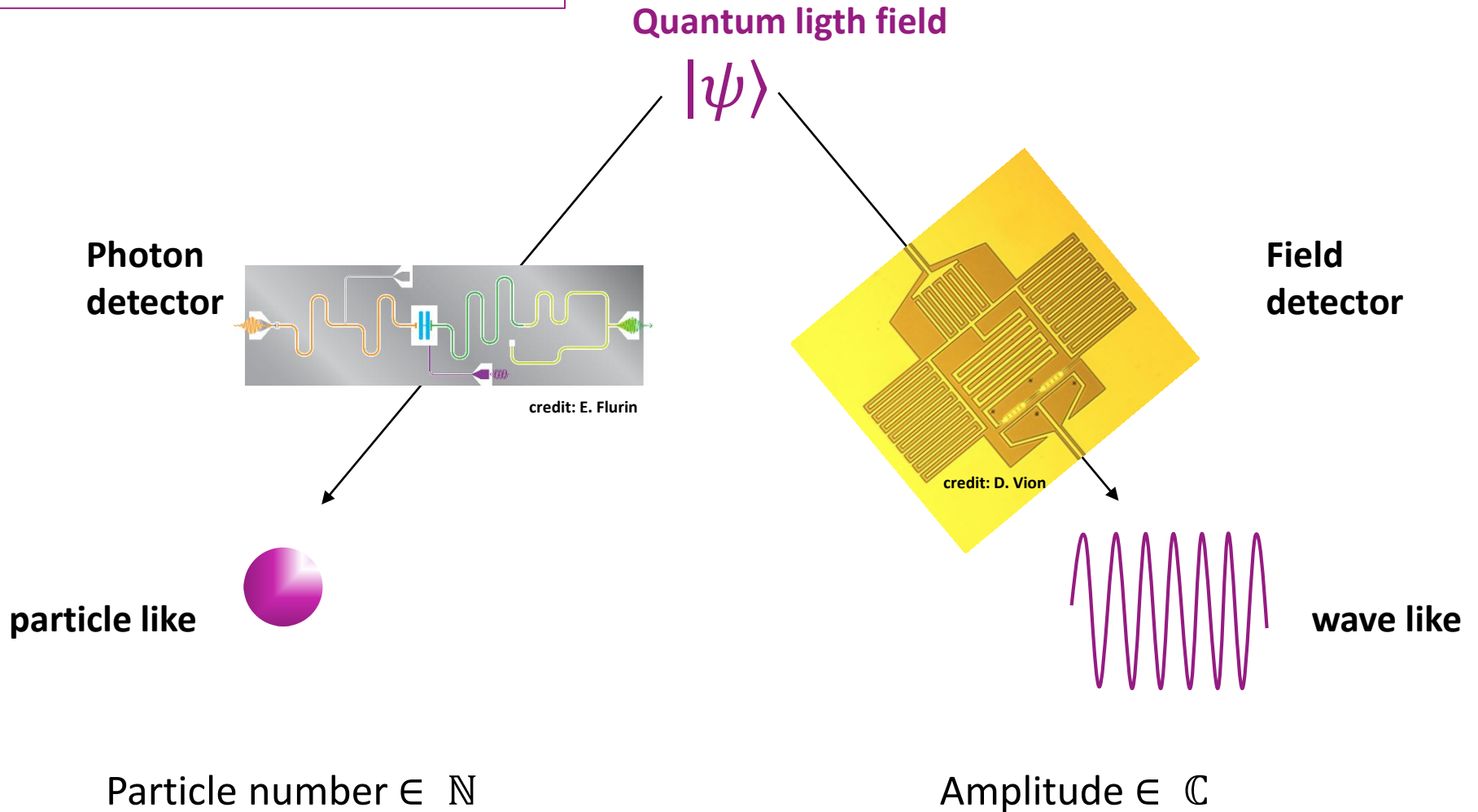
Galaxies 2022, 10(2), 46



quantum

# Click detector versus flux detector

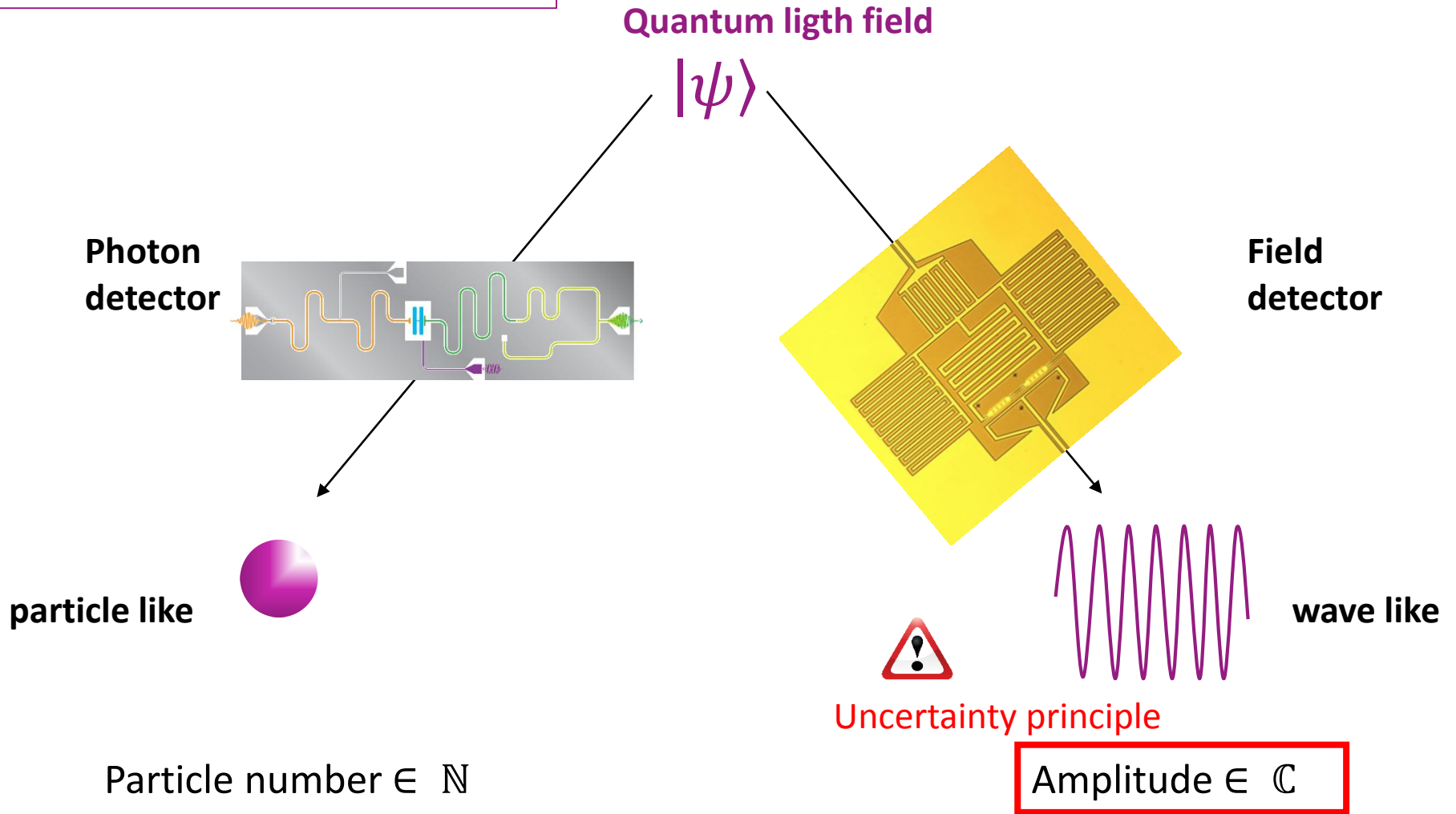
Example of photon - em detection



quantum

# Click detector versus flux detector

Example of photon - em detection



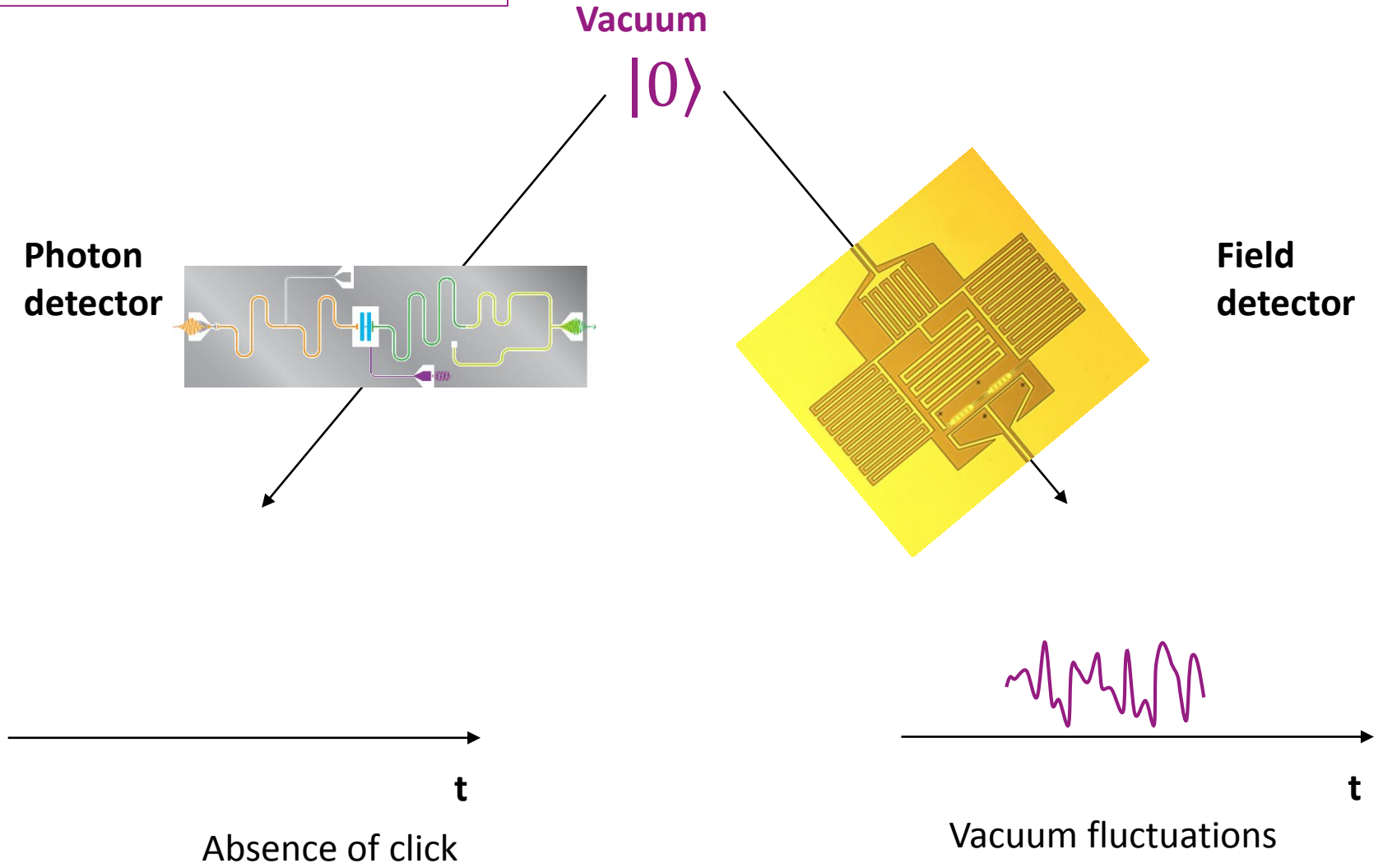
$2^\infty$ : Rare events, incoherent  $\rightarrow$  needs mostly **click detectors**



quantum

# Click detector versus flux detector

Example of photon - em detection



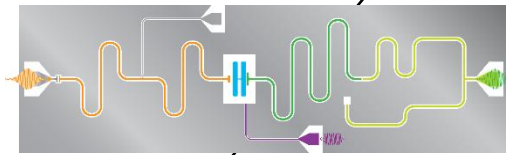
# Click detector versus flux detector

Example of photon - em detection

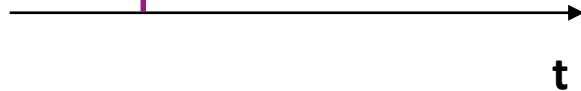
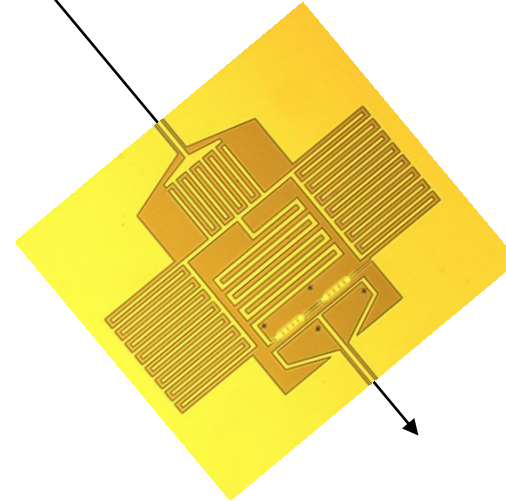
Single photon

$|1\rangle$

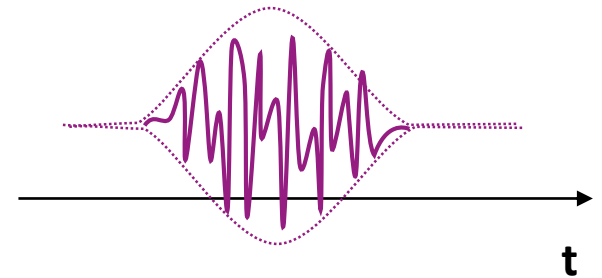
Photon detector



Field detector



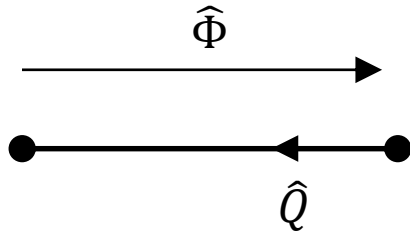
single click



Excess fluctuations

# (superconducting) circuit description

for Quantum Technologies



$$\hat{\Phi}(t) = \int_{-\infty}^t \hat{V}(t') dt'$$

flux - « position »

$$\hat{Q}(t) = \int_{-\infty}^t \hat{I}(t') dt'$$

charge - « momentum »

$$[\hat{\Phi}, \hat{Q}] = i\hbar$$

conjugate variables

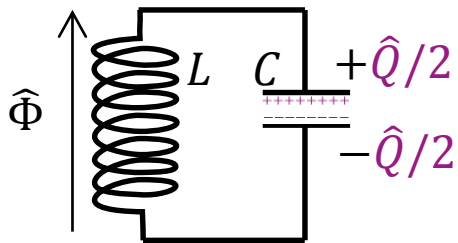
dimensionless variables :

$$\hat{\varphi} = 2\pi \frac{\hat{\Phi}}{h/2e} \quad \text{“phase”}$$

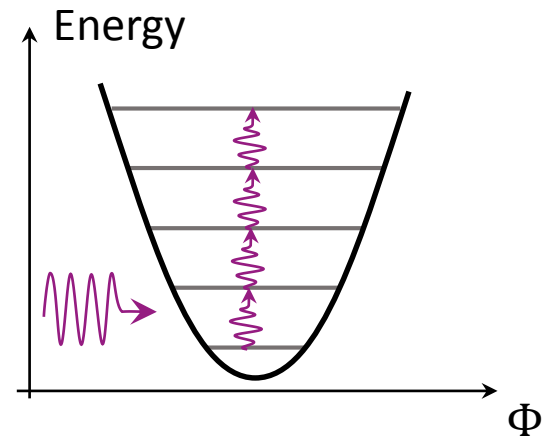
$$\hat{N} = \hat{Q}/2e \quad \text{# Cooper pairs}$$

$$[\hat{\varphi}, \hat{N}] = i$$

simplest quantum object : **harmonic oscillator**



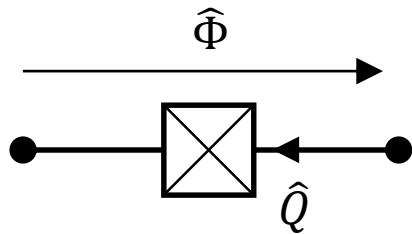
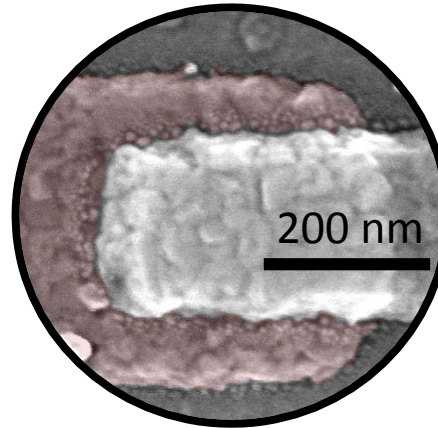
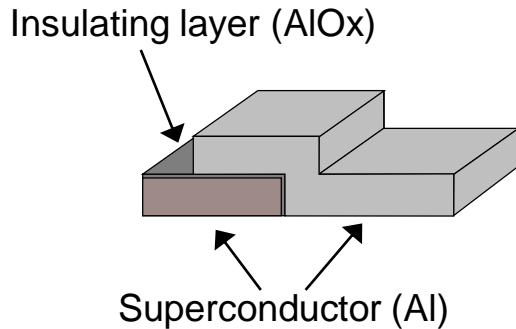
$$H = \frac{\hat{\Phi}^2}{2L} + \frac{\hat{Q}^2}{2C}$$



need to add non-linearity !

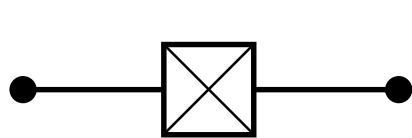
# Josephson Junction

THE non-linear element at the root of most superconducting quantum devices

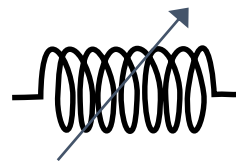


potential term  ~~$\frac{\hat{\Phi}^2}{2L}$~~  becomes  $E_J \cos(\hat{\Phi}) \equiv \frac{\hat{\Phi}^2}{2L(\Phi)}$

(analogous to a pendulum)



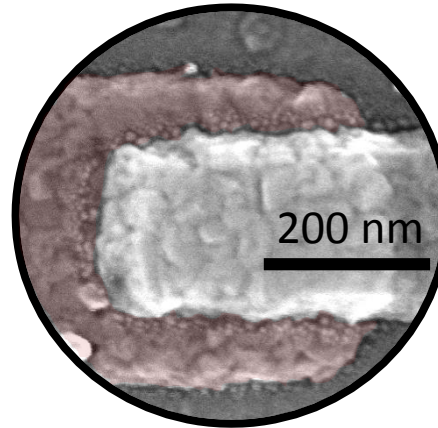
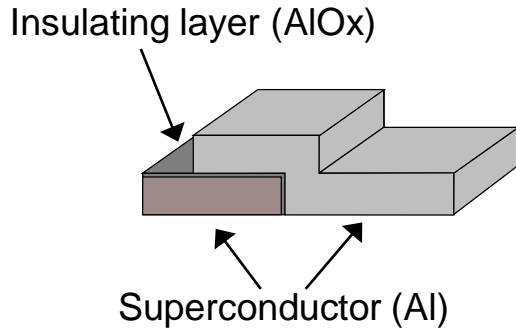
$\Leftrightarrow$



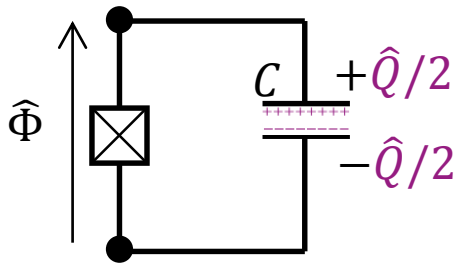
non linear inductor

# Josephson Junction

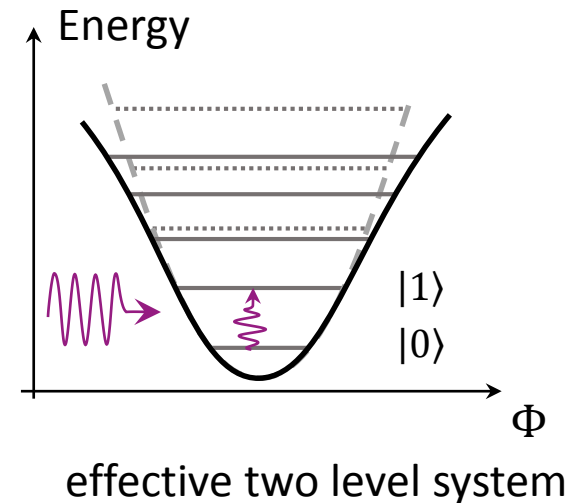
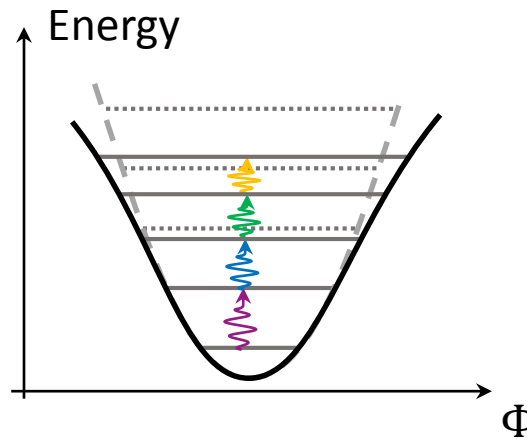
dissipationless nonlinear inductor



QuBit: non-linear **oscillator**



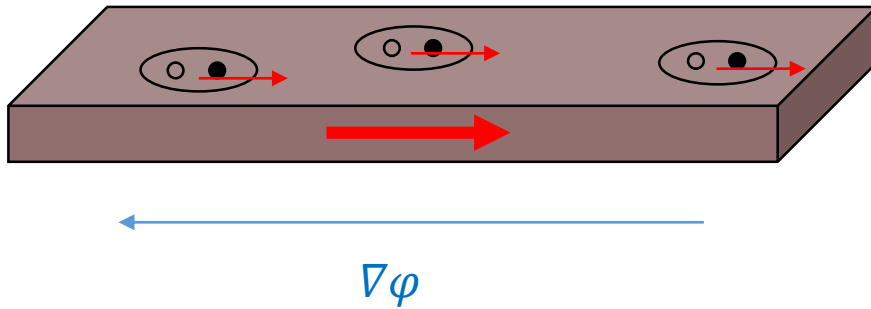
$$H = E_J \cos(\hat{\Phi}) + \frac{\hat{Q}^2}{2C}$$



# Josephson / kinetic Inductance

property of the superfluid condensate

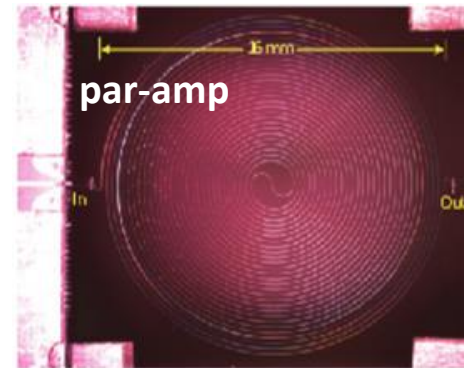
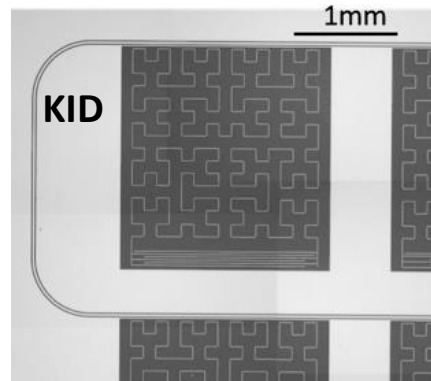
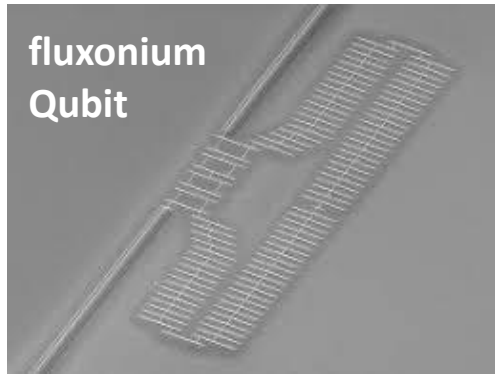
$$|\Psi\rangle = \Delta e^{i\phi}$$



kinetic inductance

$$\left. \frac{\partial I}{\partial \phi} \right|_{I=\chi} \equiv L_K^{-1}$$

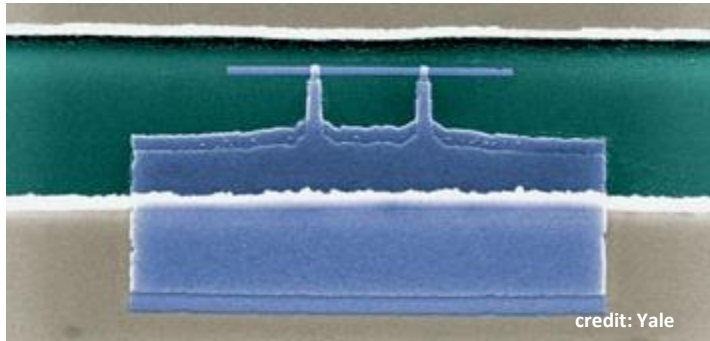
Used in many fields: **quantum technologies and cosmology / astroparticles**



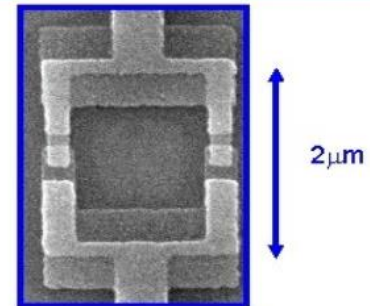
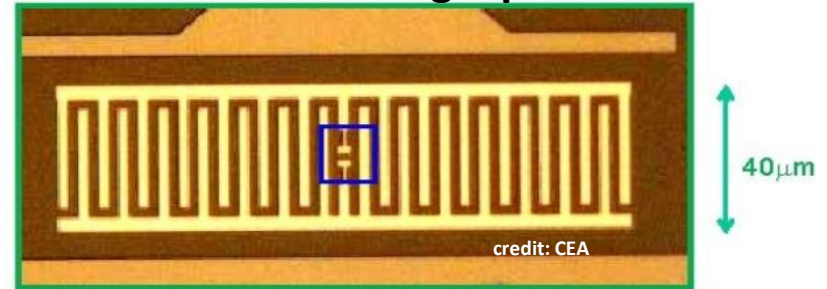
# Famous examples

Superconducting quantum devices used for Dark Matter Search

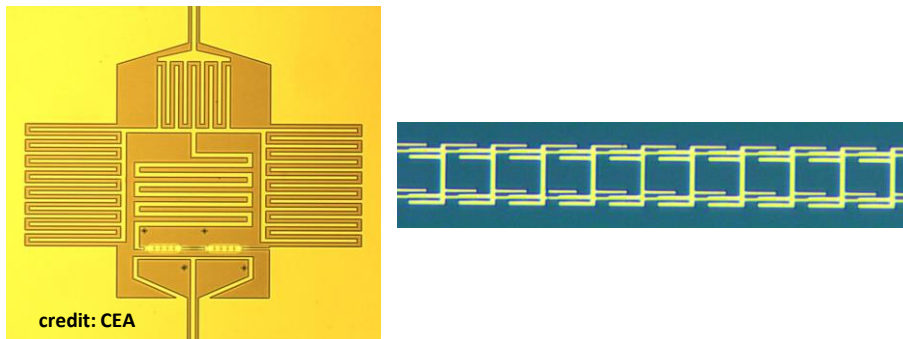
## Cooper pair box Electrometer



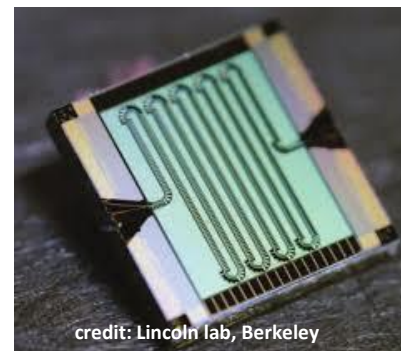
## Transmon Qubit → Single $\mu\text{W}$ Photon Det



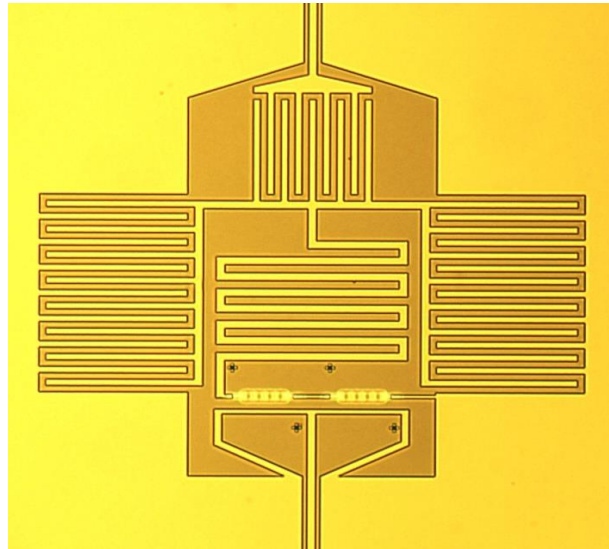
## Josephson Parametric Amplifier



## TWPA



# Parametric Amplifier



**Example of 3 wave mixing**

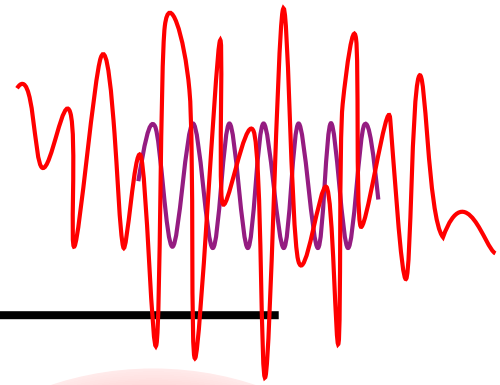
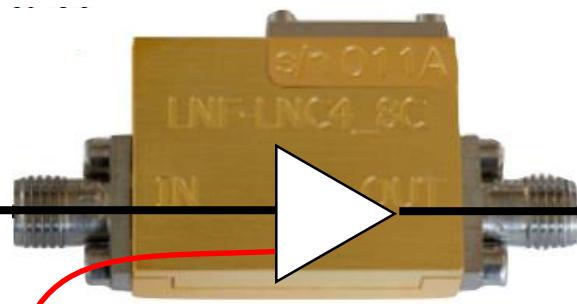
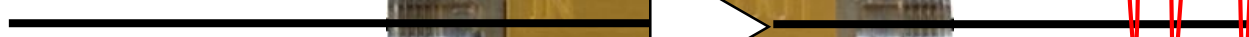


# Measuring small microwave (coherent) fields

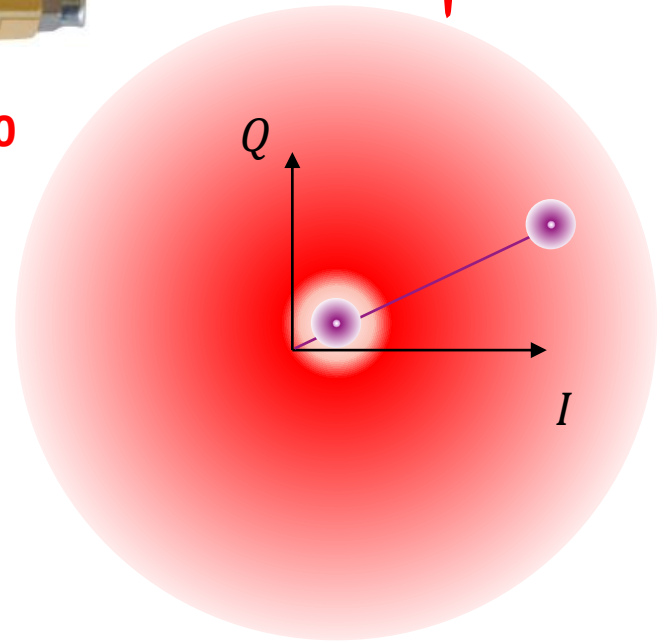
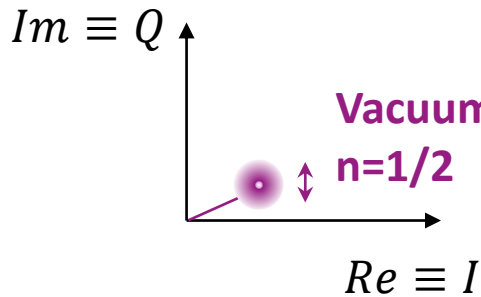
(~best) Commercial HEMT

Quantum lighth field

$|\psi\rangle$



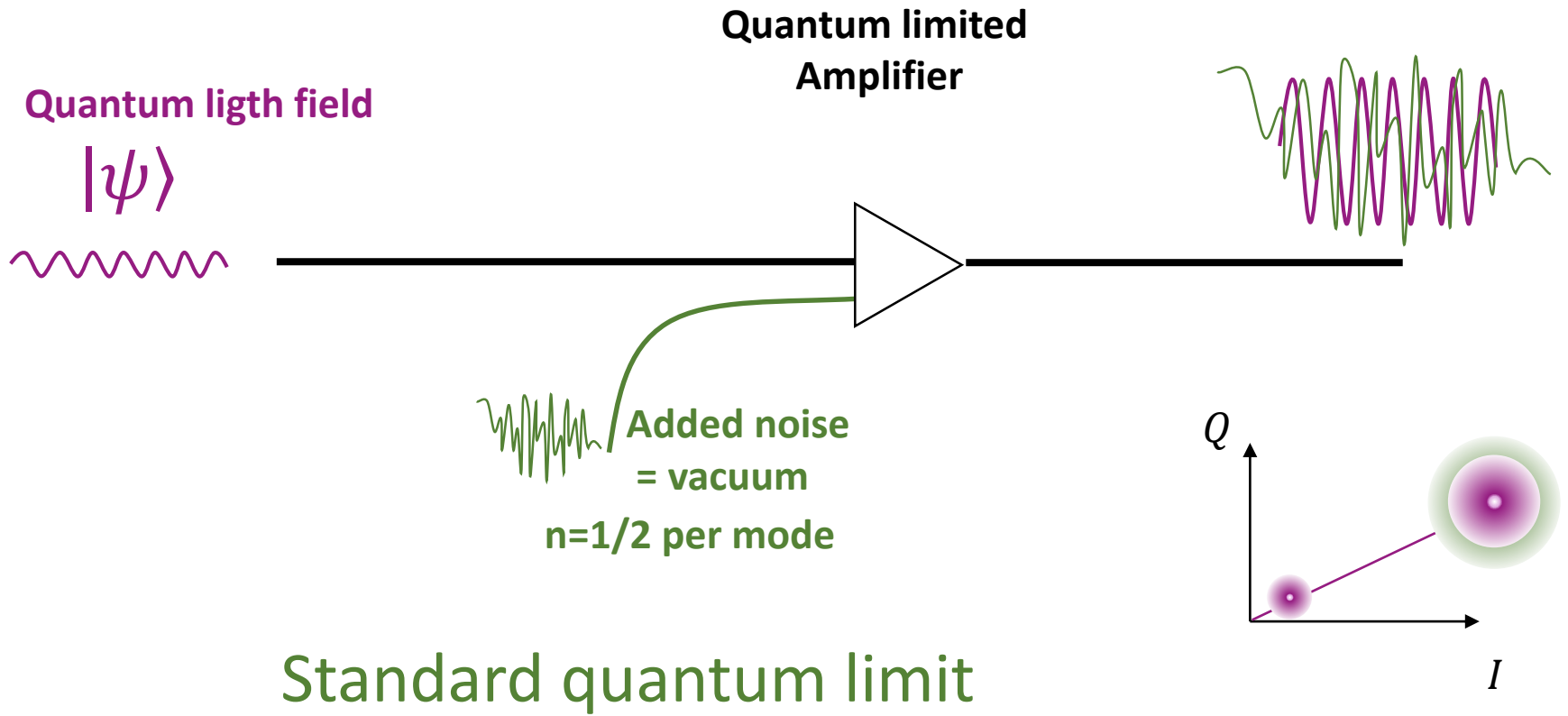
Added noise:  $n \geq 10$



Amplifier figure of merit:  $T_N$

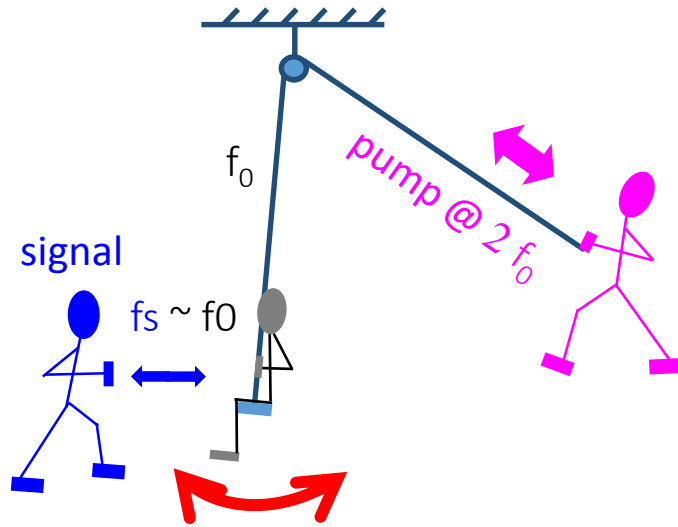
noise power per unit bandwidth [W/Hz] =  $k_B T_N = n h \nu$

# Measuring small microwave (coherent) fields



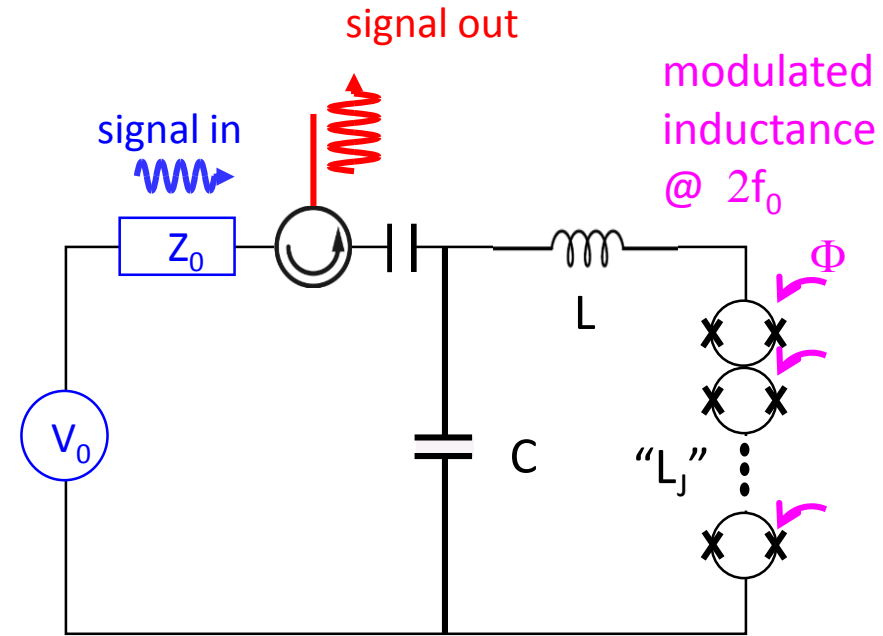
# Josephson quantum limited amplifiers

## Principle of parametric amplifiers



### 3 wave mixing

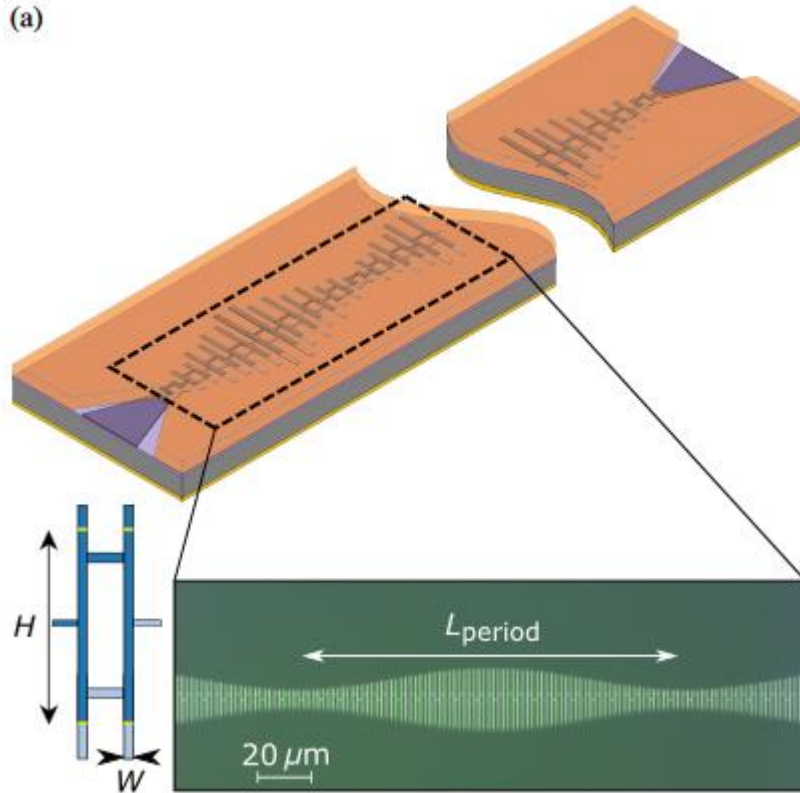
$$\omega_p = \omega_s + \omega_i$$



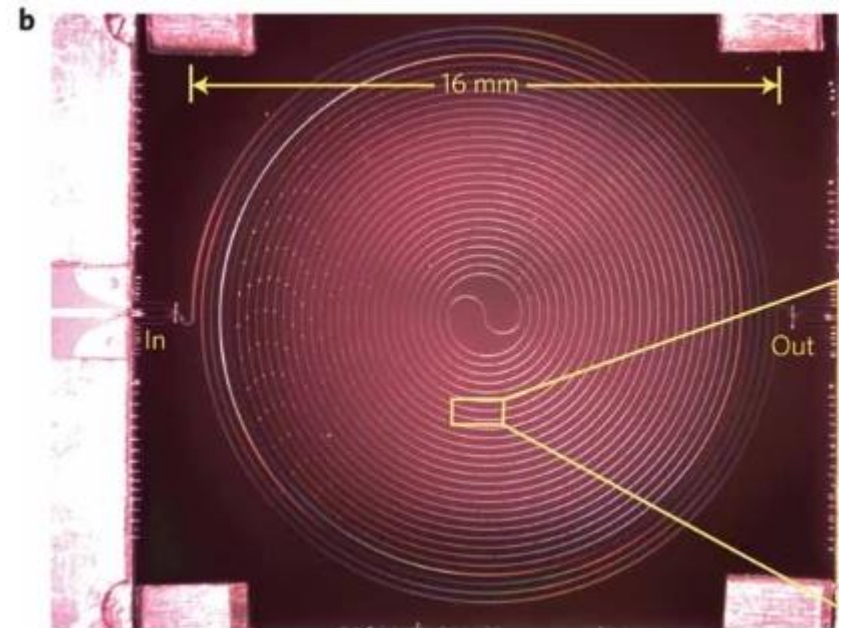
implemented with SQUIDS

# Nice example : travelling wave parametric amplifier

PHYS. REV. X 10, 021021 (2020)

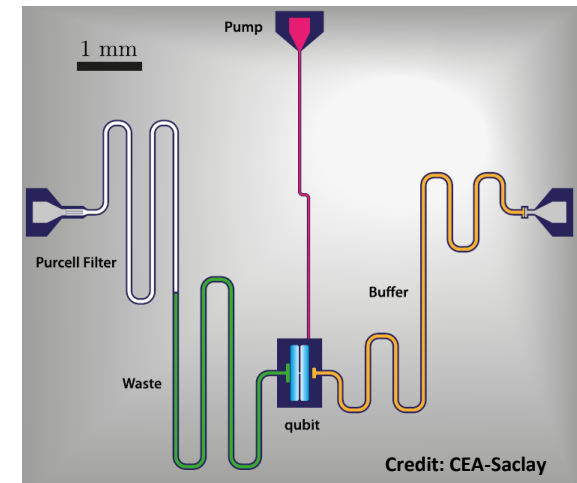
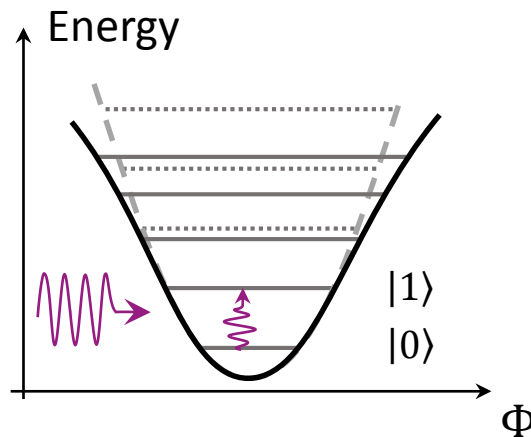
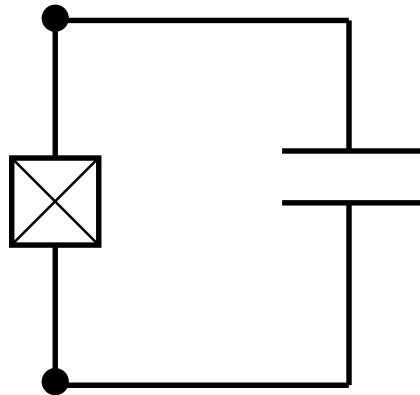


Nature Physics volume 8, pages 623–627 (2012)



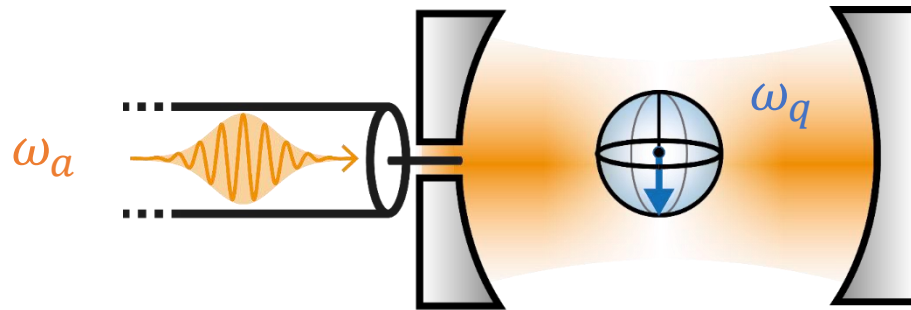
# Single Microwave Photon Detector SMPD

Transmon QuBit

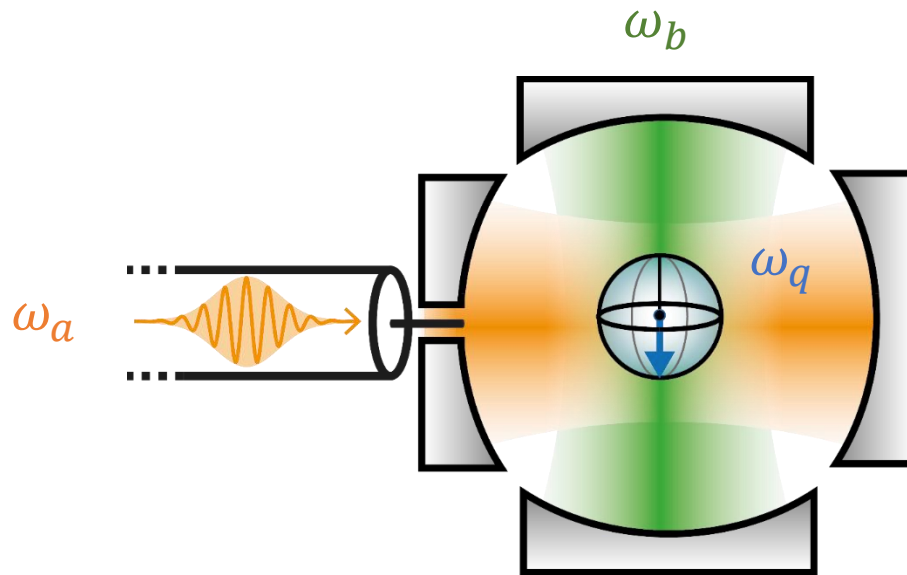


E. Flurin, P. Bertet, (SPEC, Université Paris-Saclay, CEA)  
QUAX collaboration

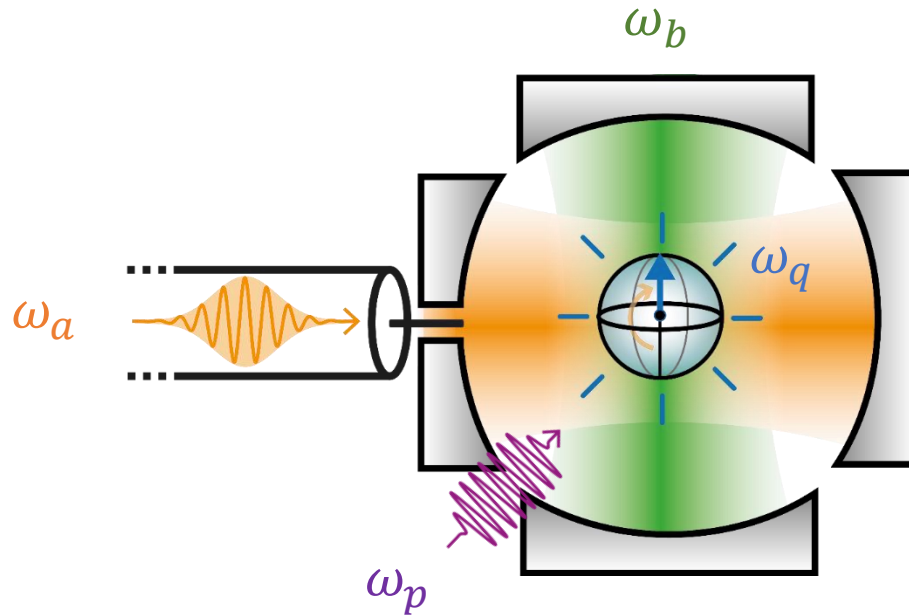
# Single microwave photon counter : principle



# Single microwave photon counter : principle



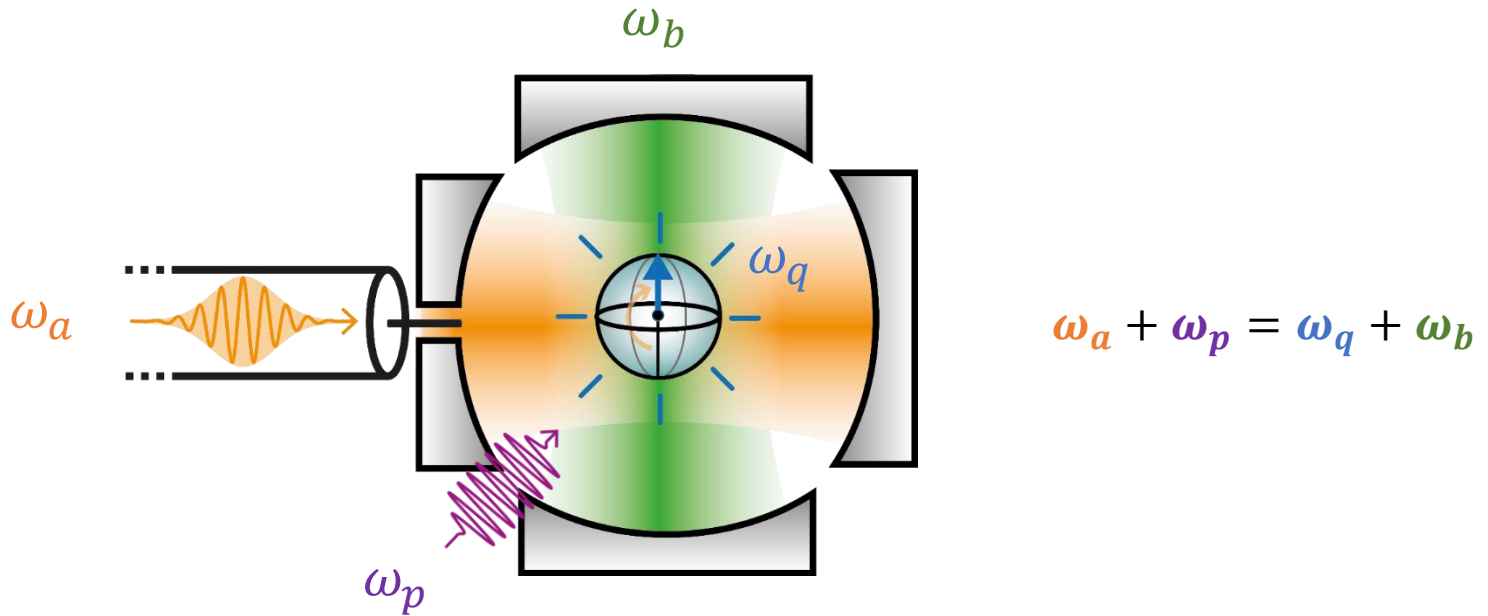
# Single microwave photon counter : principle



$$\omega_a + \omega_p = \omega_q + \omega_b$$



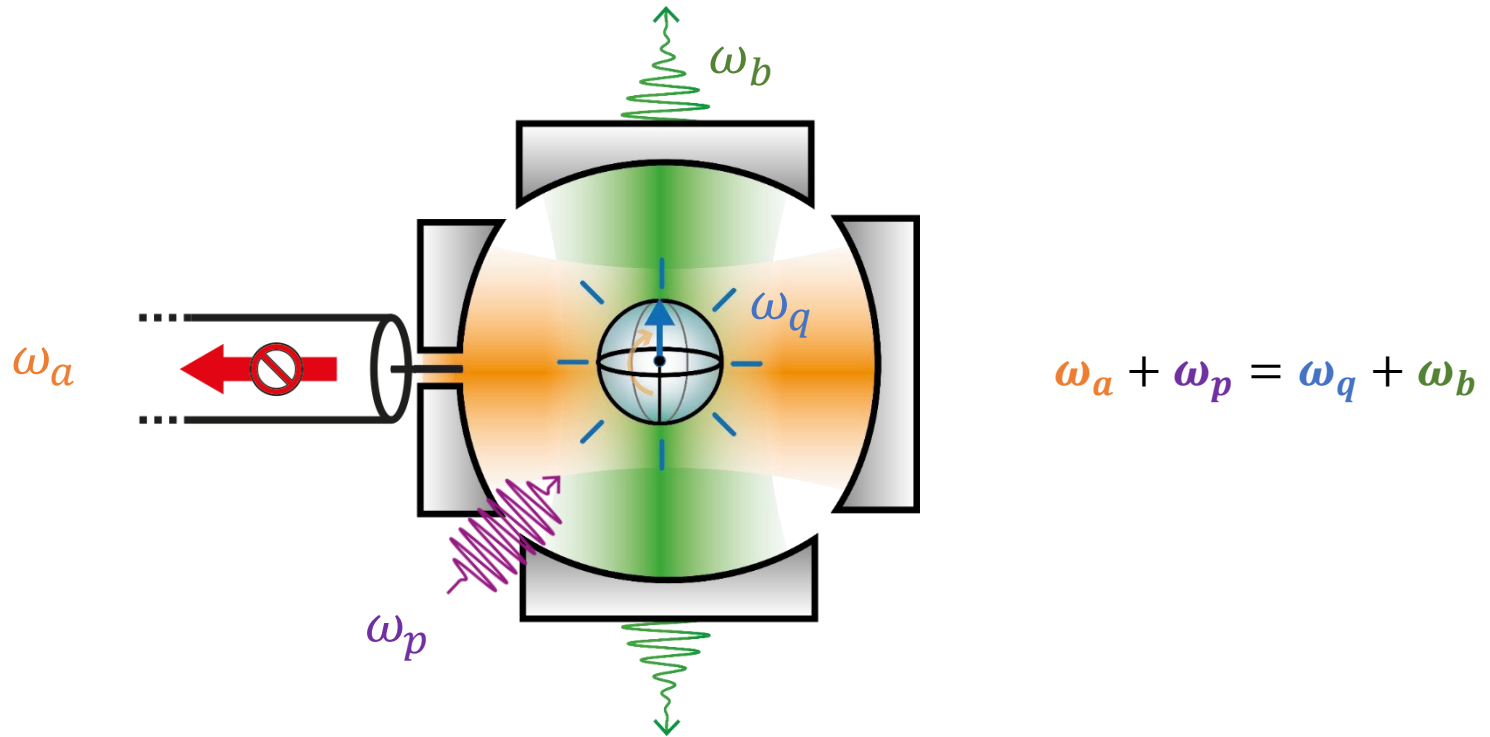
# Single microwave photon counter : principle



Four-Wave mixing-based Photodetection

$$\hat{H} = g_4 \cdot (\xi \hat{a} \hat{\sigma}^+ \hat{b}^+ + \xi^* \hat{a}^+ \hat{\sigma} \hat{b})$$

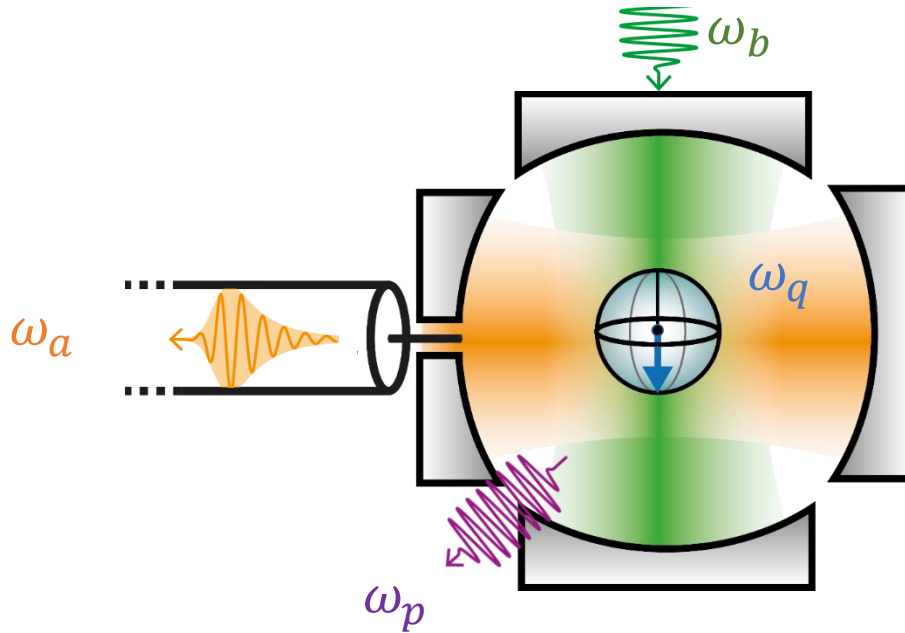
# Single microwave photon counter : principle



$$\hat{H} = g_4 \cdot (\xi \hat{a} \hat{\sigma}^+ \hat{b}^+ + \xi^* \hat{a}^+ \hat{\sigma} \hat{b})$$

$$\hat{L} = \hat{a} \hat{\sigma}^+$$

# Built-in detector reset



$$\omega_q + \omega_b = \omega_a + \omega_p$$

$$\hat{H} = g_4 \cdot (\xi \hat{\sigma} \hat{\sigma}^+ \hat{b}^+ + \xi^* \hat{a}^+ \hat{\sigma} \hat{b})$$

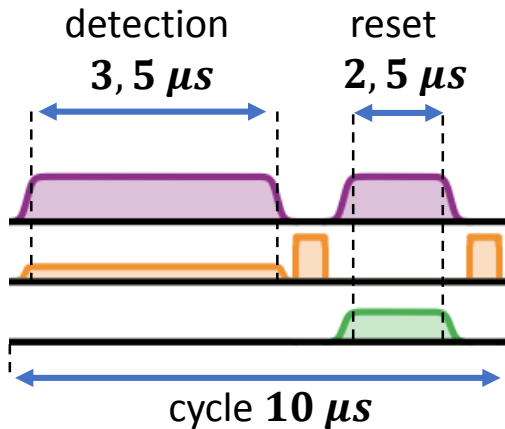
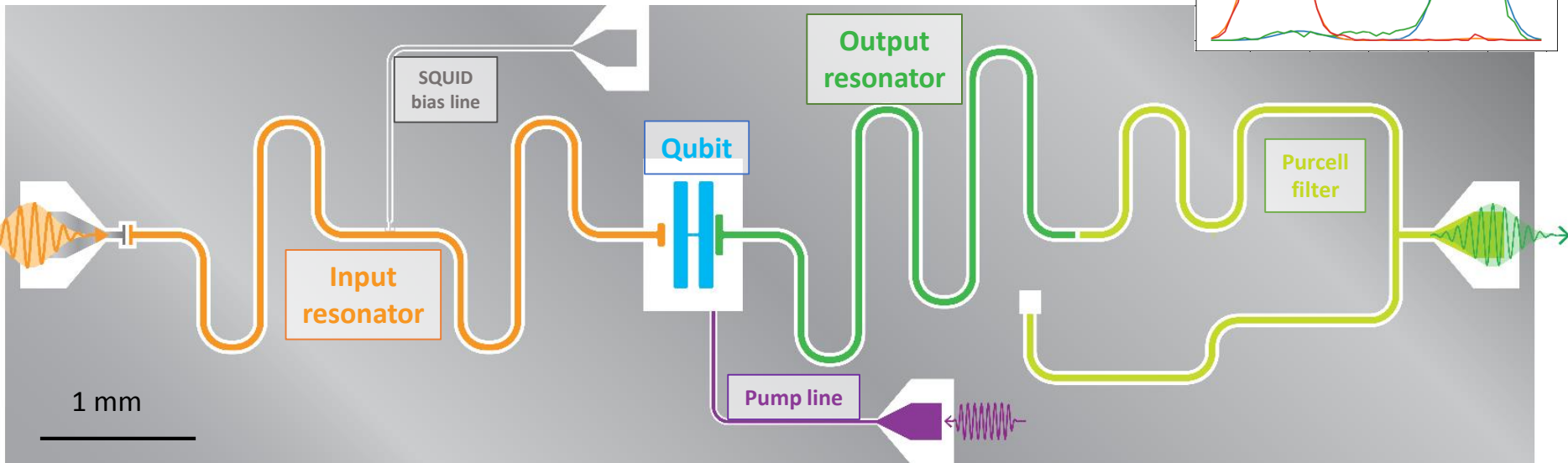
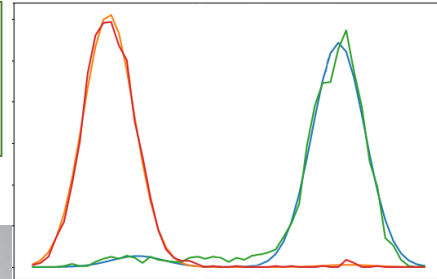
# Implementation

$f_{in} = 7,1 \text{ GHz}$   
 $Q_{in} = 7,5 \text{ k}$   
 $\chi_{in q}/2\pi = 3,5 \text{ MHz}$

$f_q = 6,1 \text{ GHz}$   
 $T_1 = 8 - 9 \mu\text{s}$   
 $T_2^* = 13 \mu\text{s}$

$f_{out} = 7,6 \text{ GHz}$   
 $Q_{out} = 16 \text{ k}$   
 $\chi_{out q}/2\pi = 8,1 \text{ MHz}$

single shot measurement



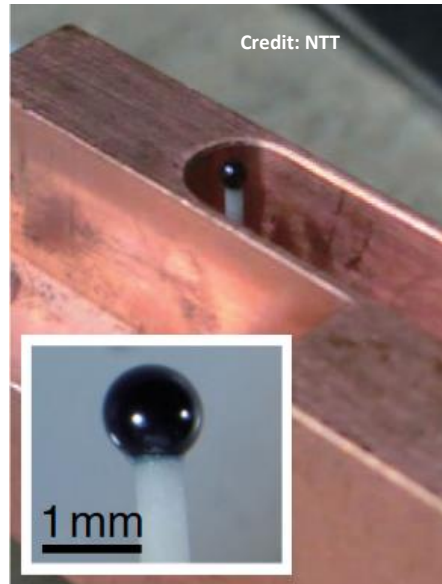
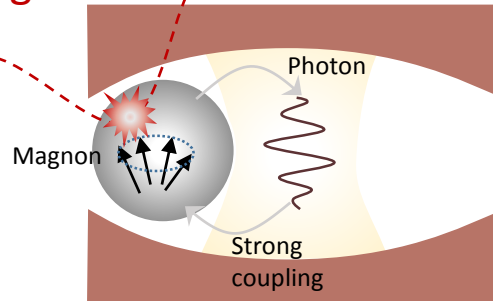
35% duty cycle

Dark count rate:  $\alpha = 0.4 \text{ ms}^{-1}$

Total efficiency: 20%

# Axion detectors (“haloscopes”)

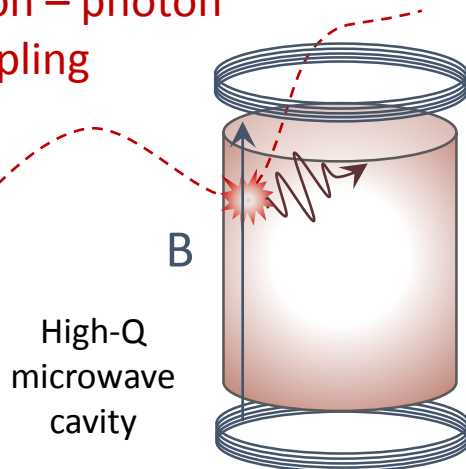
Axion – electron spin coupling



« Ferromagnetic haloscope »

Crescini, COMMUNICATIONS PHYSICS (2020)

Axion – photon coupling



How to detect the photon ?

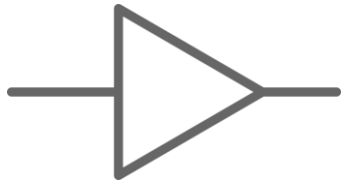
- Squid amplifier (ADMX)  
(J. Clarke) Rev. Mod. Phys., Vol. 75, No. 3, July 2003
- Josephson Parametric amplifier (HAYSTAC)  
(K. Lehnert) Phys. Rev. Lett. 118, 061302 (2017)
- Single microwave photon detector (QUAX)  
Lescanne et al., PRX 2020  
(D. Schuster) Dixit et al. PRL 2021

# Dark matter Axion detection

Advantage of SMPD over linear detectors operated at the quantum limit

$$SNR = P_S/P_N$$

Signal-to-noise with linear amplifier at the quantum limit



$$SNR_{\text{lin}} = \frac{P_{\text{axion}}}{\hbar\omega/2} \sqrt{\frac{t_{\text{lin}}}{\kappa_{\text{axion}}}}$$

← axion linewidth  $\sim 10$  kHz

Signal-to-noise with SMPD



$$SNR_{\text{SMPD}} = \frac{P_{\text{axion}}}{\hbar\omega} \sqrt{\frac{t_{\text{SMPD}}}{\alpha_{\text{DC}}}}$$

← axion power  $\sim 1$  photon.s<sup>-1</sup>

← darkcount  $\sim 5 - 50$  click.s<sup>-1</sup>

$$\frac{t_{\text{lin}}}{t_{\text{SMPD}}} = \frac{1}{4} \frac{\kappa_{\text{axion}}}{\alpha_{\text{DC}}} \sim 50 - 500$$

# Thank you!



Quantronics Group, Service de Physique de l'Etat  
Condensé, **CEA Saclay**