



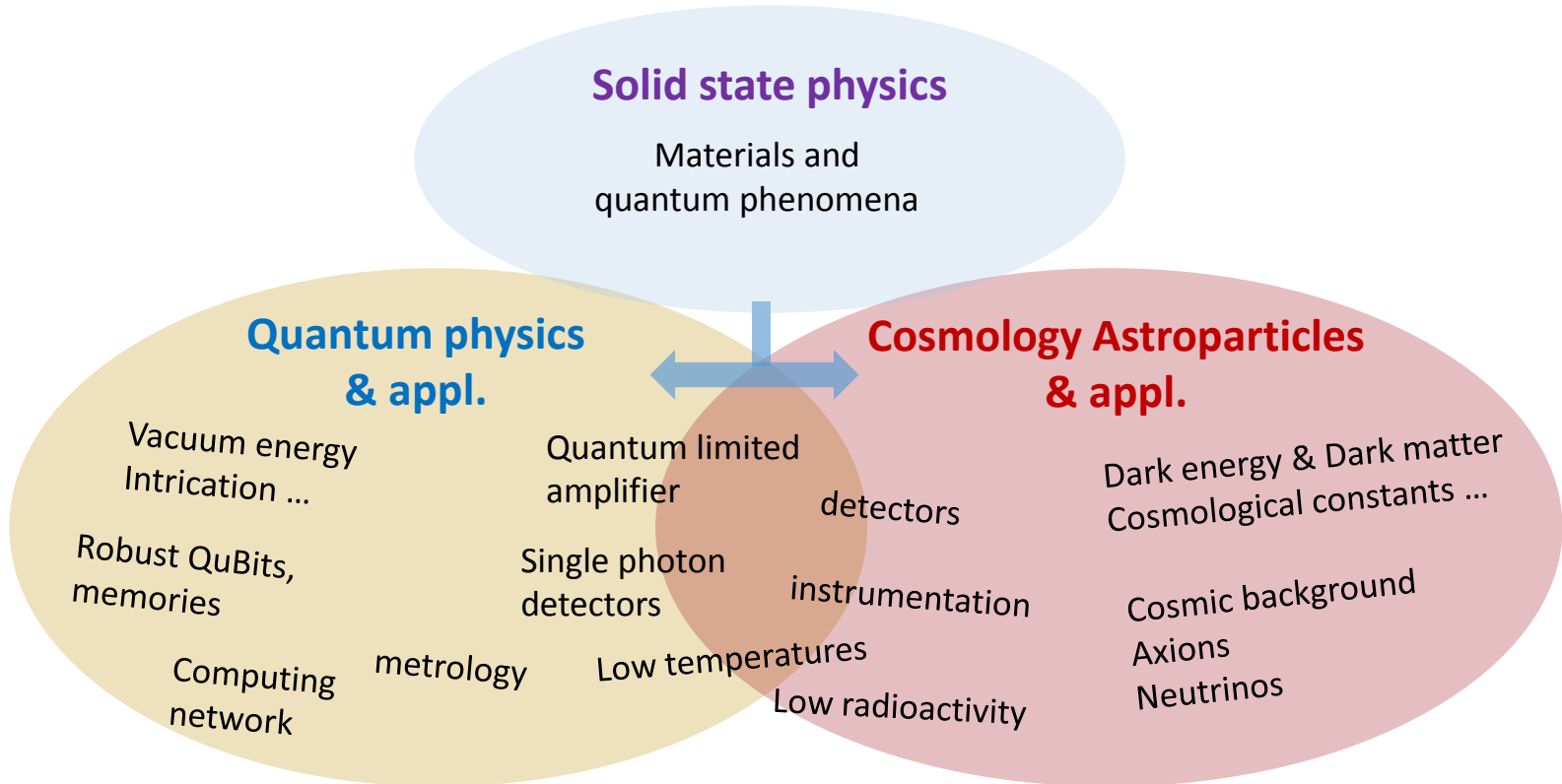
Quantum Technologies applied to 2∞ physics

Hélène le Sueur



QT / 2 ∞

What do they have in common?



Qu-tech



reaching the « quantum limit »

**Advanced electronics
Shields from radioactivity**



Cosmology – astroparticles

“Quantum Detectors”

What are we talking about?

Quantum Sensing, C.L. Degen et al.

“ Use of a *quantum system*, *quantum properties* or *quantum phenomena* to perform a measurement of a physical quantity”

Rev. Mod. Phys. **89**, 035002 (2017)

“Quantum Detectors”

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Rev. Mod. Phys. **89**, 035002 (2017)

Device based on quantum physics (eg solid state...)?

→ ~ all of them

Device that operates in the quantum regime ?

i.e. $kT \ll$ characteristic energies

More specifically: detectors that exploit

- Quantum coherence
- Superposition
- Entanglement
- Squeezing
- backaction evasion

“Quantum Detectors”

Synopsis

General scope: single ‘X’ (atom, electron, ...) devices

Key feature: quantum coherence

Figure of merit: strong sensitivity to external disturbances

Famous examples:

Atom clocks, squids, cold atom gravimeters, gravitational wave detectors

Already exploited to measure:

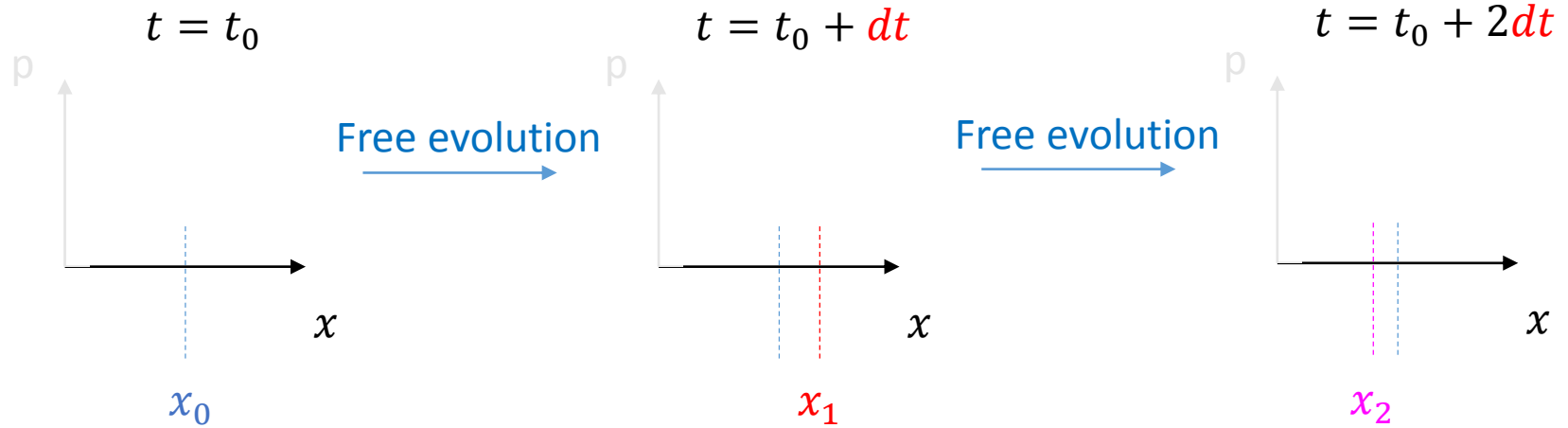
magnetic and electric fields, time and frequency, gravity field (eg rotations...), temperature, pressure...

Today's menu

- What does a « quantum measurement » mean ?
A bit of definitions
- Two strategies for em field measurements:
click or flux
- How to build a superconducting quantum circuit
low losses and some nonlinearity
- 2 nice examples of QT detectors applied to 2∞
The parametric amplifier and the single microwave photon counter

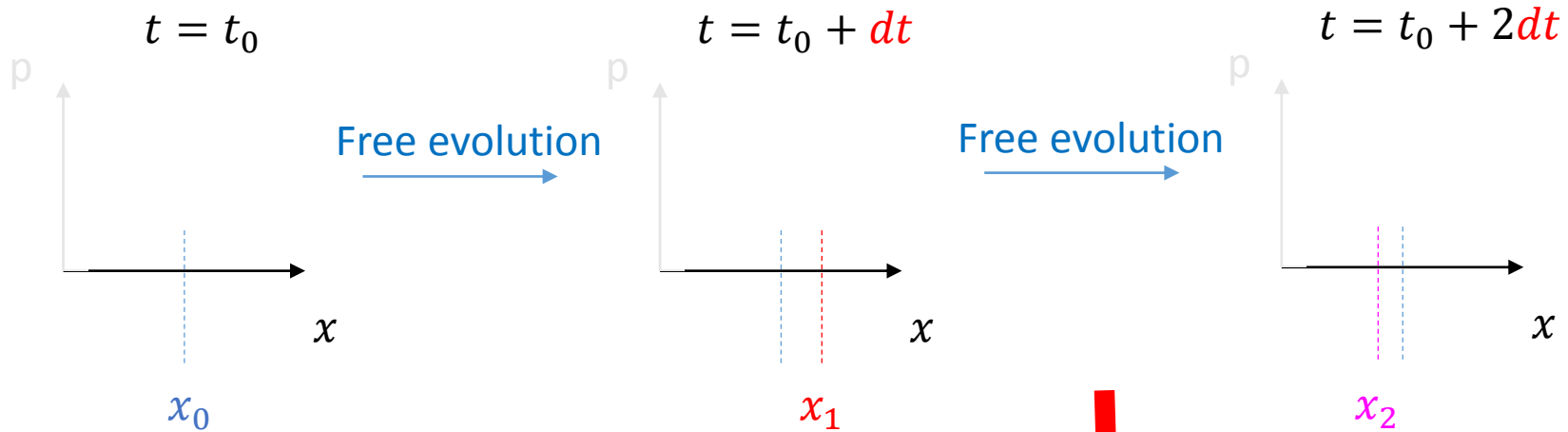
Measurement in quantum mechanics

Measure the position x of a free particle with super high precision



Measurement in quantum mechanics

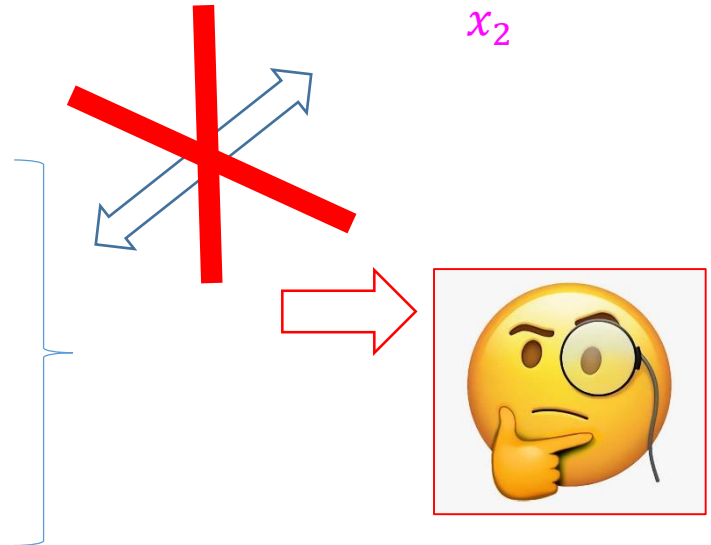
Measure the position x of a free particle with super high precision



$$x_1 = x_0 + \frac{p}{m} dt$$

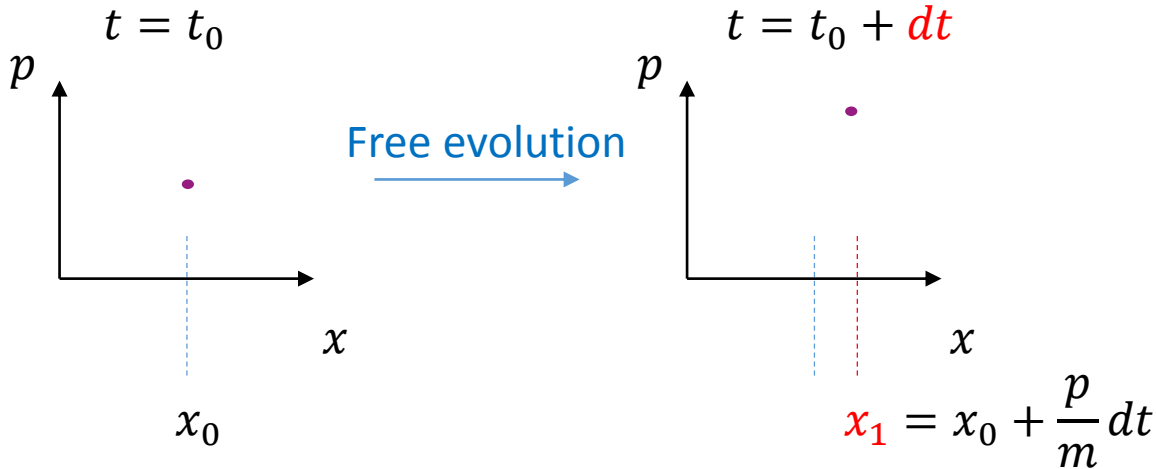
$$x_2 = x_1 + \frac{p}{m} dt$$

Free evolution : p conserved



Measurement in quantum mechanics

Measure the position x of a free particle with super high precision

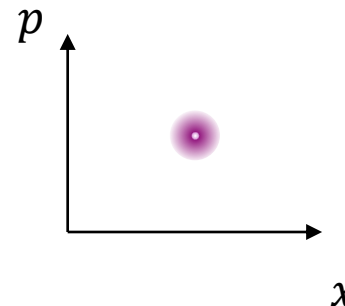


x measurement has given an unpredictable (and non reproducible) kick on p

Conversely, measuring p would push x in an unpredictable (and non reproducible) way

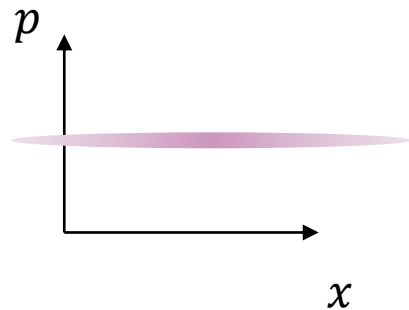
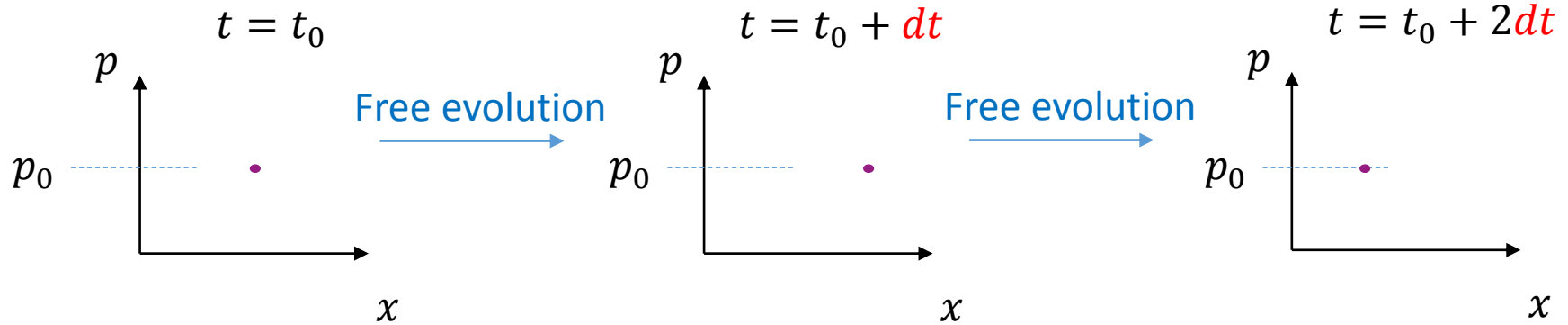
« measurement back-action »

$$[\hat{x}, \hat{p}] \neq 0$$



Measurement in quantum mechanics

Measure the momentum p of a free particle with super high precision



$$x_1 = x_0 + \frac{p}{m} dt$$

$$x_2 = x_1 + \frac{p}{m} dt$$

Free evolution : p conserved



« Quantum Non Demolition measurement of p »

Measurement in quantum mechanics

Quantum non demolition

$$[\hat{a}(t), \hat{a}(t + dt)] = 0$$

V. Braginsky, Y. I. Vorontsov, and K. P. Thorne, Science 209, 547 (1980),
see also Caves, Unruh

Free particle

$$[\hat{x}(t), \hat{x}(t + dt)] = i \hbar dt/m$$

$$[\hat{p}(t), \hat{p}(t + dt)] = 0$$

$$\hat{H} |n\rangle = E_n |n\rangle$$

p and E are continuous QND observables

Oscillator

$$[\hat{x}(t), \hat{x}(t + dt)] = \frac{i \hbar}{m\omega} \sin(\omega dt)$$

$$[\hat{p}(t), \hat{p}(t + dt)] = i \hbar m\omega \sin(\omega dt)$$

x and p are stroboscopic QND observables !

$$E \text{ and } x \pm i \frac{p}{m\omega}$$

are continuous QND observables !



Quadratures do not commute

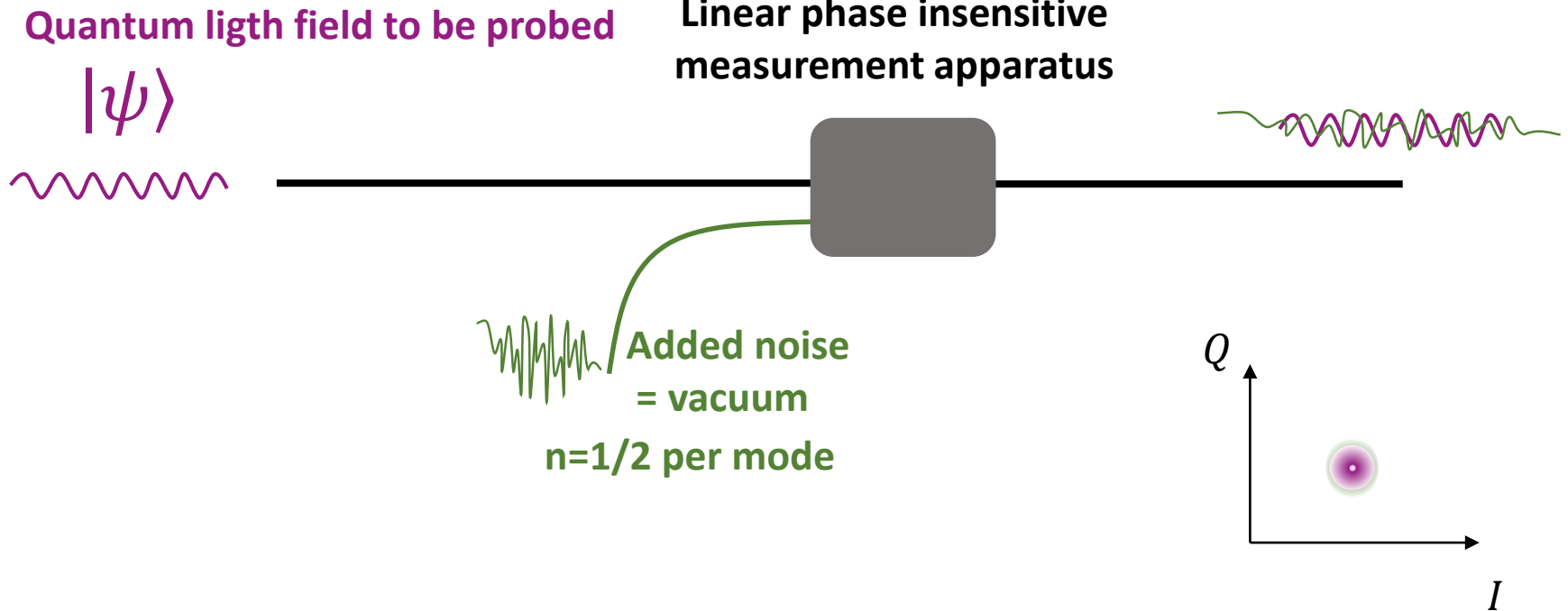
← amplitude

Measure one quadrature of the amplitude : « Backaction evading measurements »

Measuring small (coherent) fields

Noise added by vacuum fluctuations

Caves, Phys. Rev. D **1981**, 23, 1693–1708



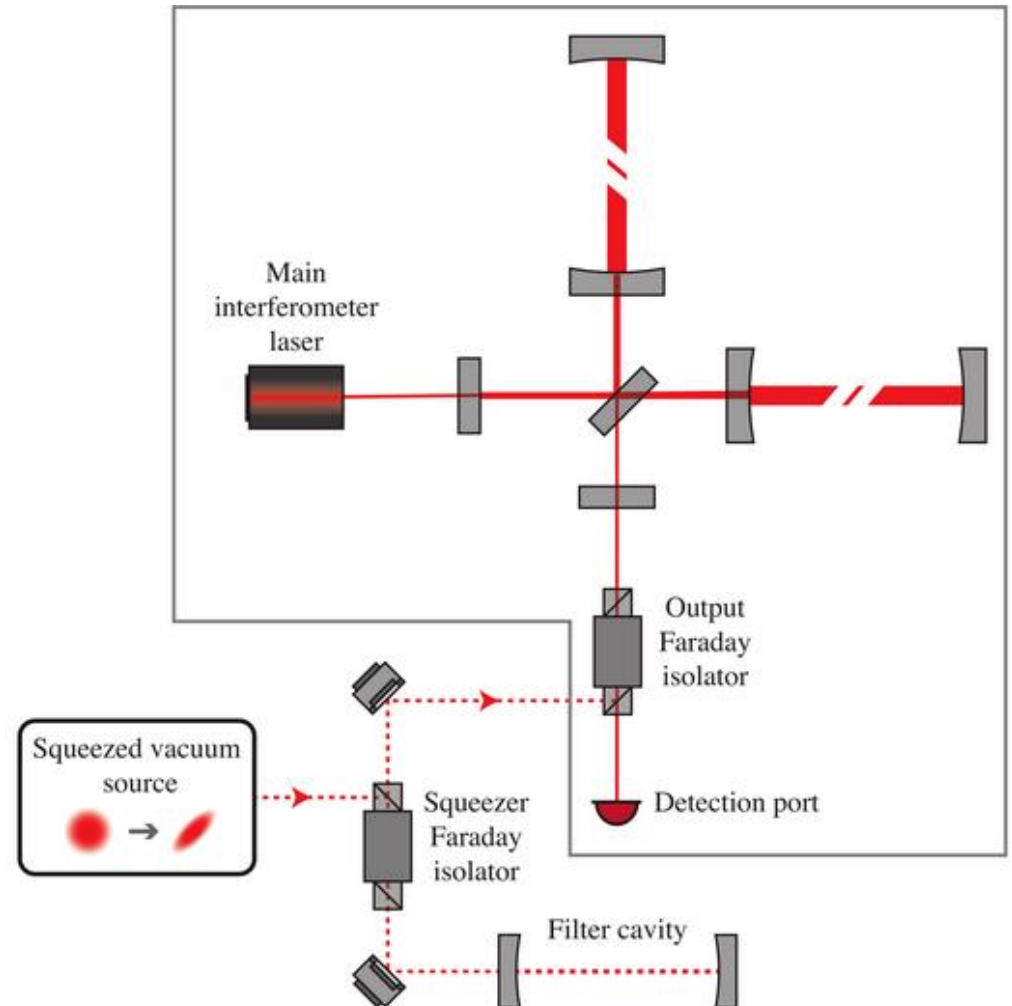
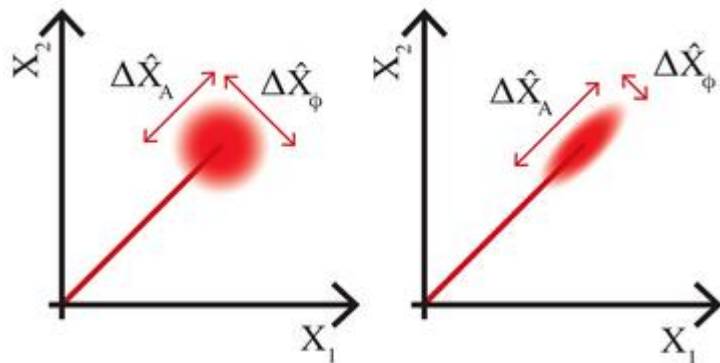
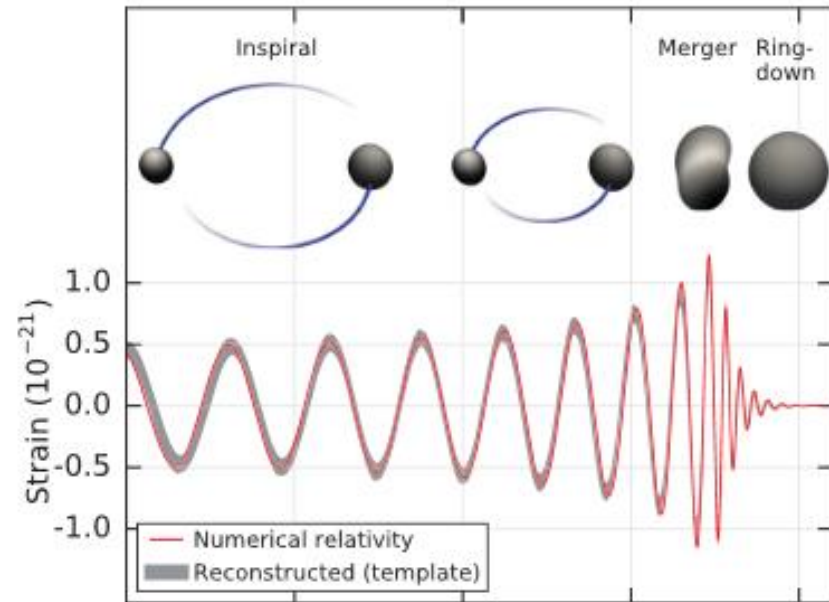
« Standard quantum limit »

Strategy: Prepare vacuum in a « squeezed state » to reduce measurement noise

GW detectors use squeezing in order to beat standard quantum limit

PRL **116**, 061102 (2016)

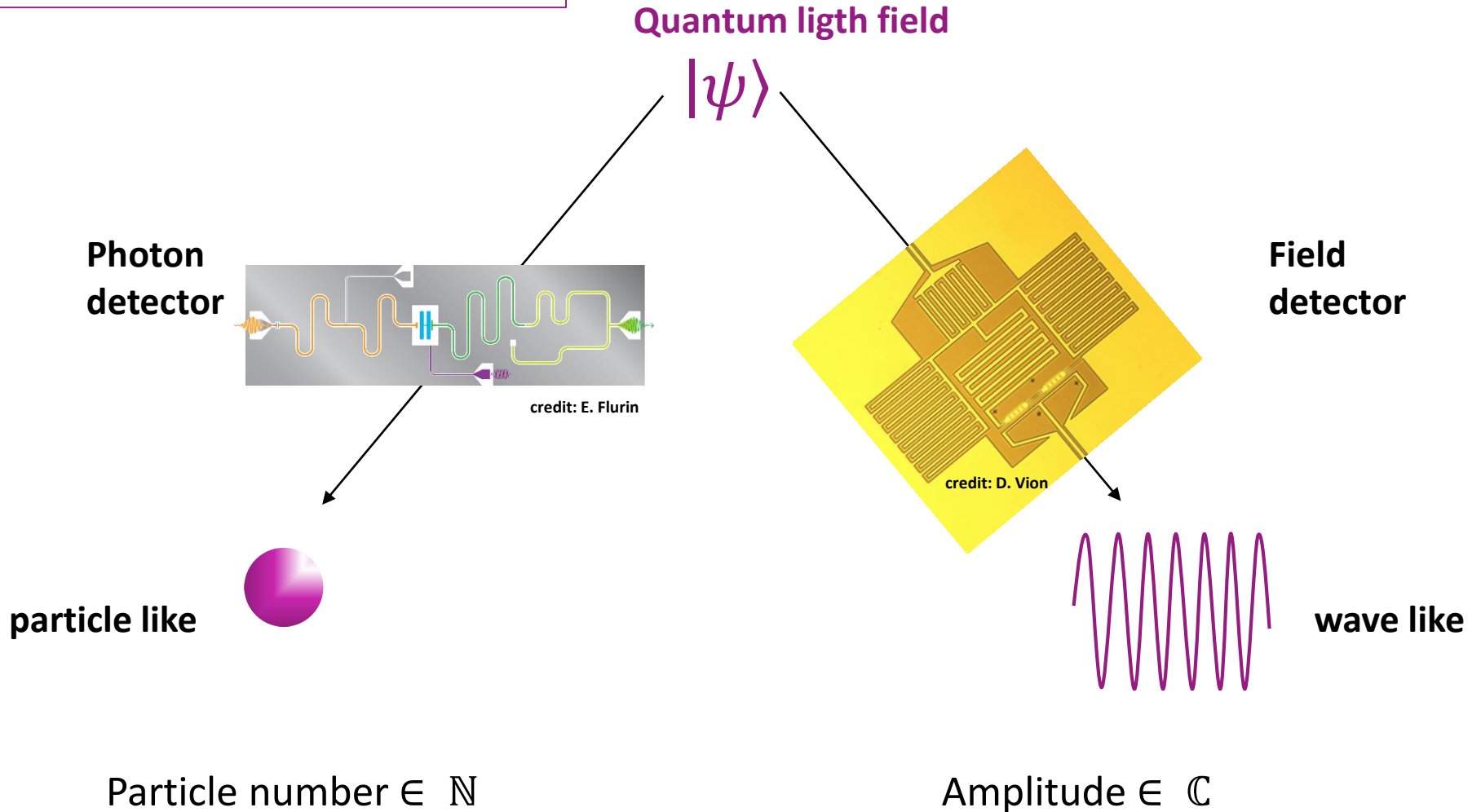
Galaxies 2022, 10(2), 46



quantum

Click detector versus flux detector

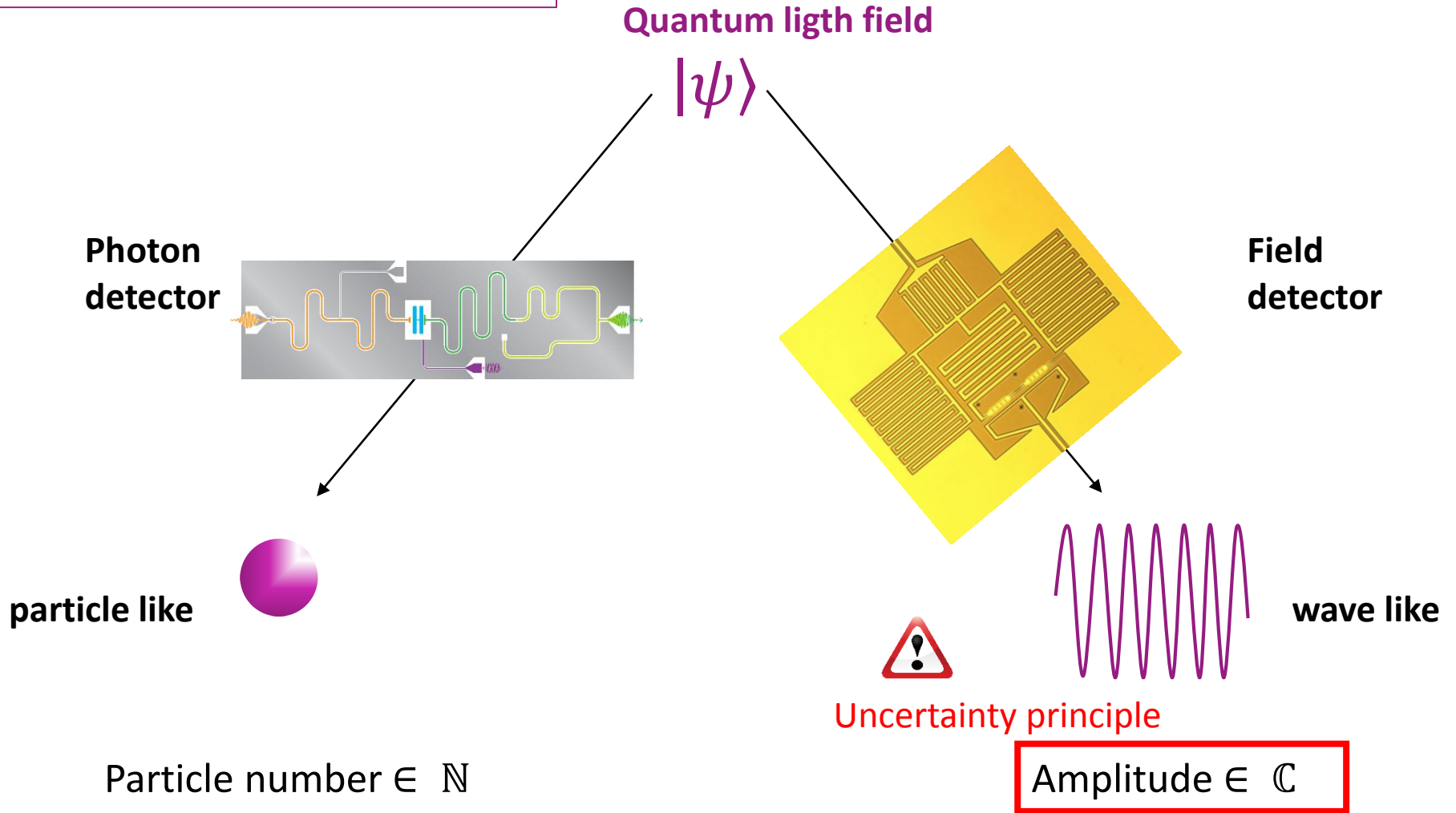
Example of photon - em detection



quantum

Click detector versus flux detector

Example of photon - em detection

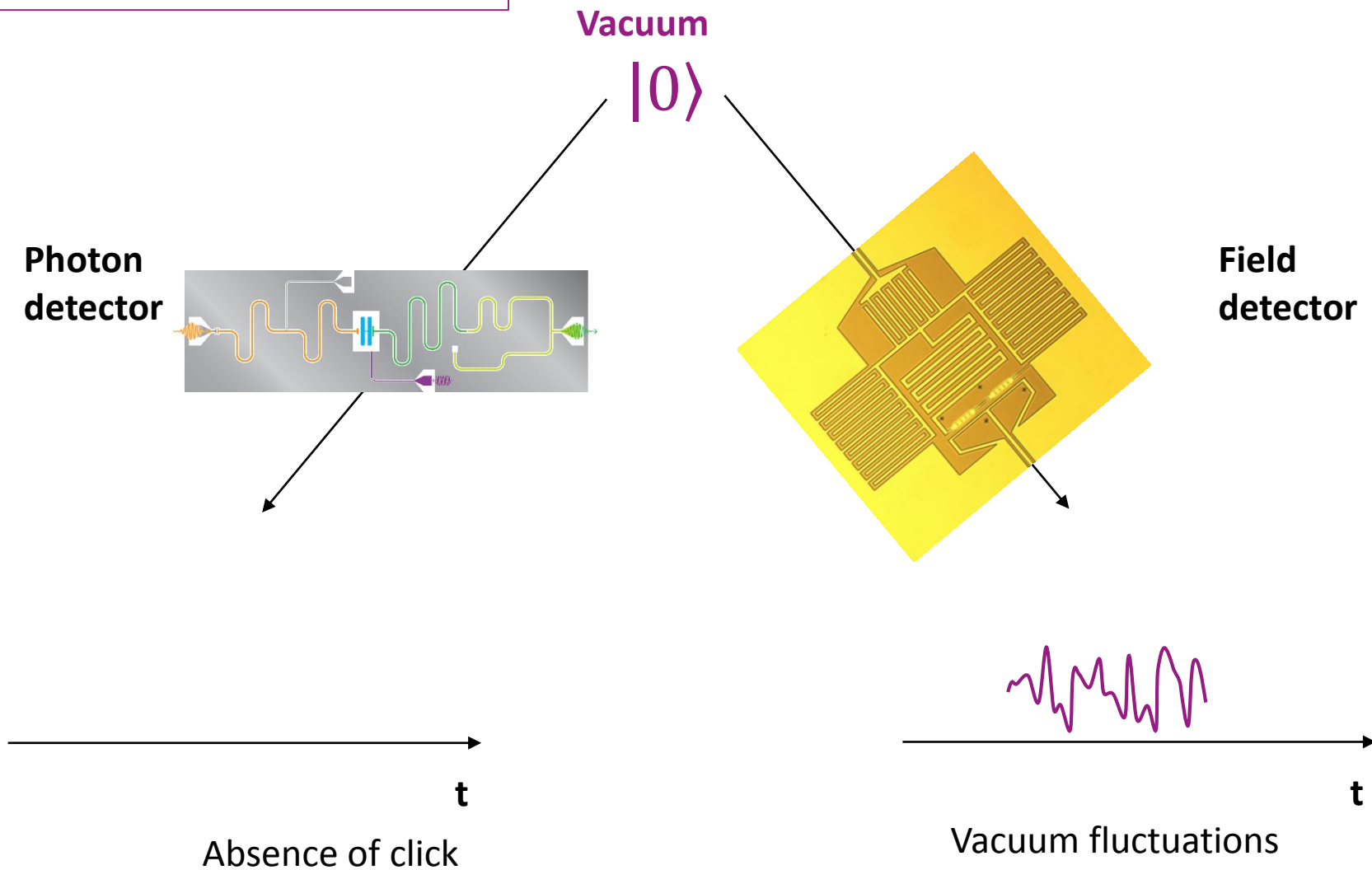


2^∞ : Rare events, incoherent \rightarrow needs mostly **click detectors**

quantum

Click detector versus flux detector

Example of photon - em detection



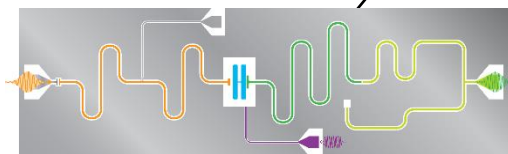
Click detector versus flux detector

Example of photon - em detection

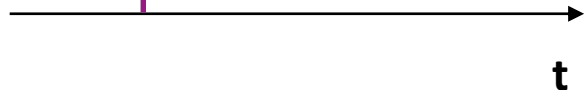
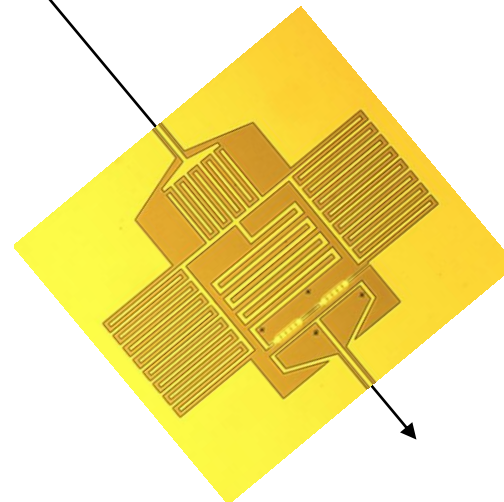
Single photon

$|1\rangle$

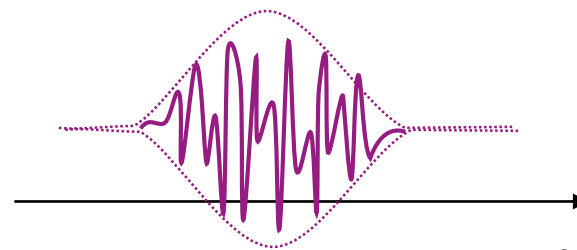
Photon detector



Field detector



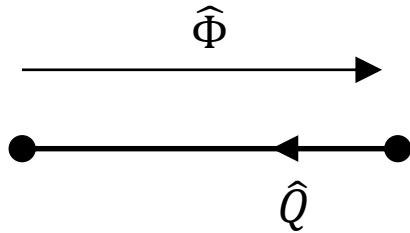
single click



Excess fluctuations

(superconducting) circuit description

for Quantum Technologies



$$\hat{\Phi}(t) = \int_{-\infty}^t \hat{V}(t') dt'$$

flux - « position »

$$\hat{Q}(t) = \int_{-\infty}^t \hat{I}(t') dt'$$

charge - « momentum »

$$[\hat{\Phi}, \hat{Q}] = i\hbar$$

conjugate variables

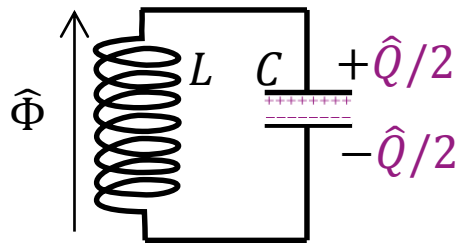
dimensionless variables :

$$\hat{\varphi} = 2\pi \frac{\hat{\Phi}}{h/2e} \quad \text{“phase”}$$

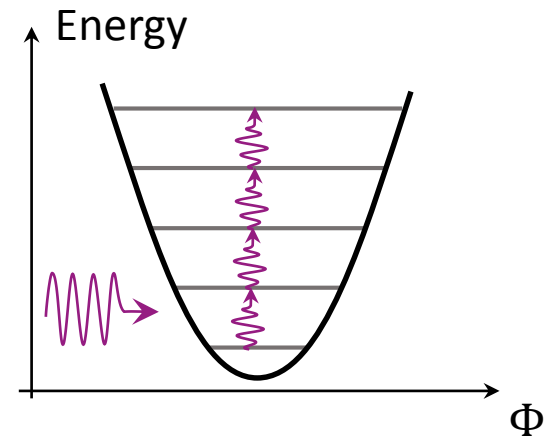
$$\hat{N} = \hat{Q}/2e \quad \text{# Cooper pairs}$$

$$[\hat{\varphi}, \hat{N}] = i$$

simplest quantum object : **harmonic oscillator**



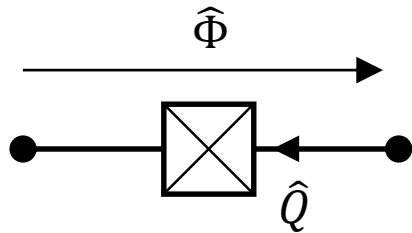
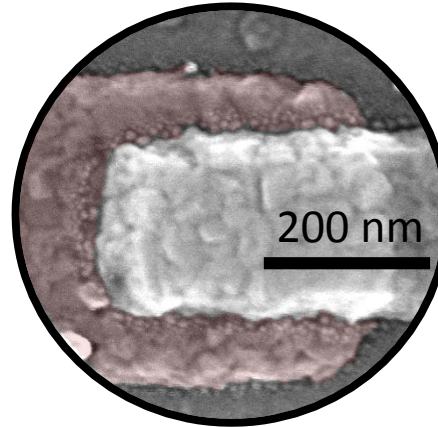
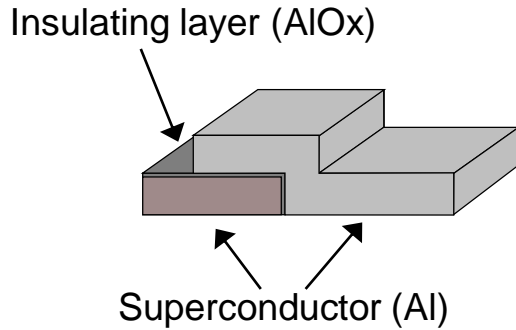
$$H = \frac{\hat{\Phi}^2}{2L} + \frac{\hat{Q}^2}{2C}$$



need to add non-linearity !

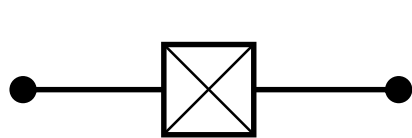
Josephson Junction

THE non-linear element at the root of most superconducting quantum devices

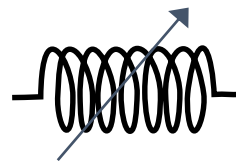


potential term ~~$\frac{\hat{\Phi}^2}{2L}$~~ becomes $E_J \cos(\hat{\Phi}) \equiv \frac{\hat{\Phi}^2}{2L(\Phi)}$

(analogous to a pendulum)



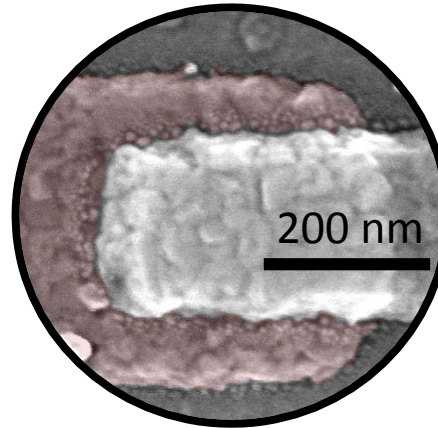
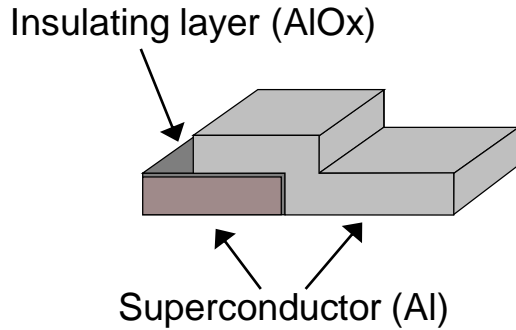
\Leftrightarrow



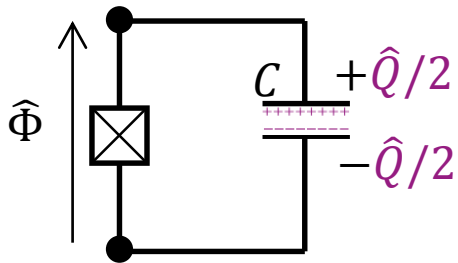
non linear inductor

Josephson Junction

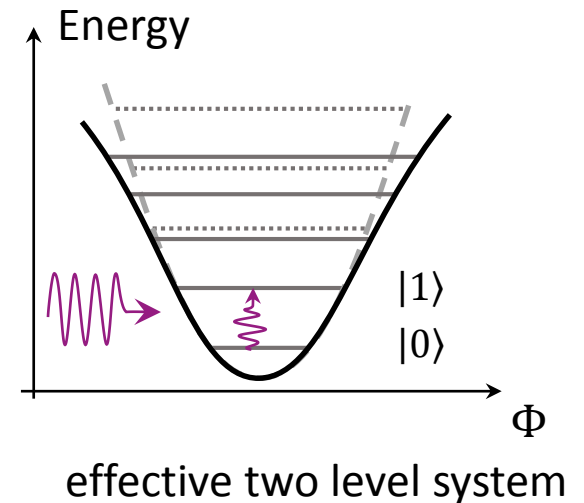
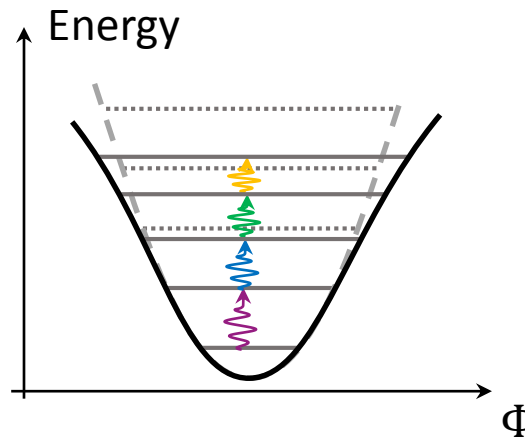
dissipationless nonlinear inductor



QuBit: non-linear **oscillator**



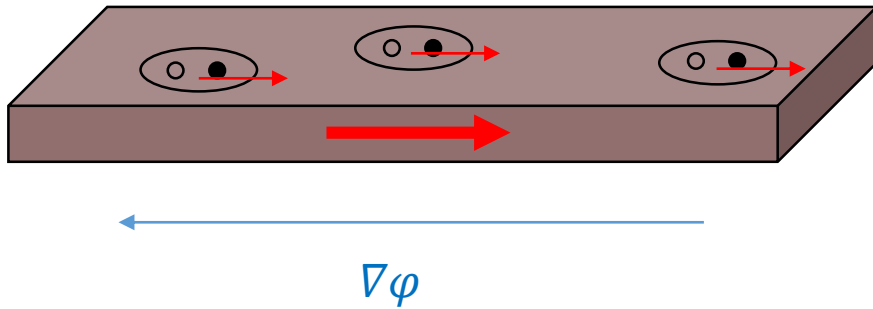
$$H = E_J \cos(\hat{\Phi}) + \frac{\hat{Q}^2}{2C}$$



Josephson / kinetic Inductance

property of the superfluid condensate

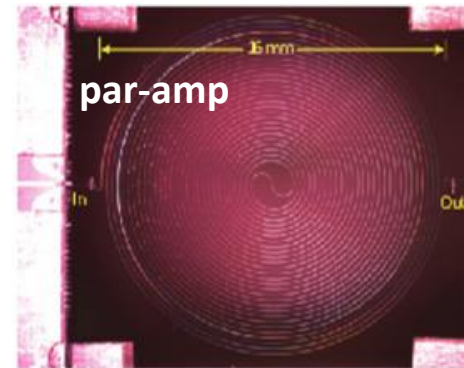
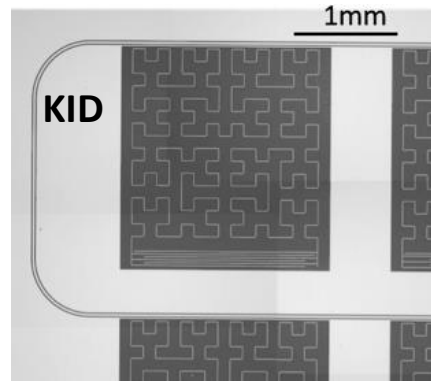
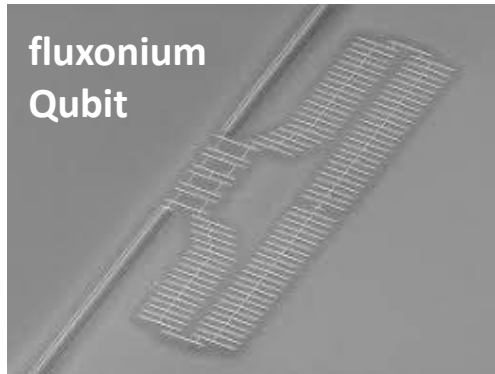
$$|\Psi\rangle = \Delta e^{i\phi}$$



kinetic inductance

$$\left. \frac{\partial I}{\partial \phi} \right|_{I=\chi} \equiv L_K^{-1}$$

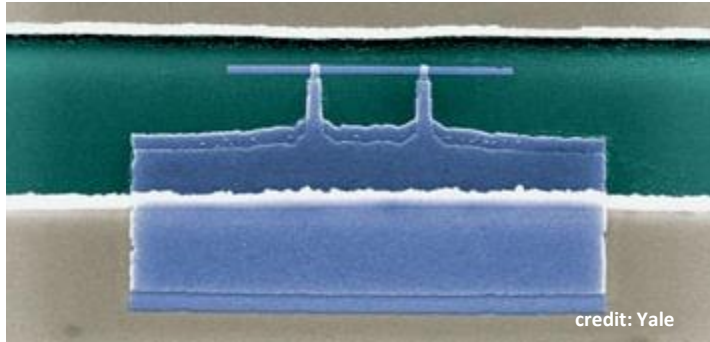
Used in many fields: **quantum technologies and cosmologie / astroparticles**



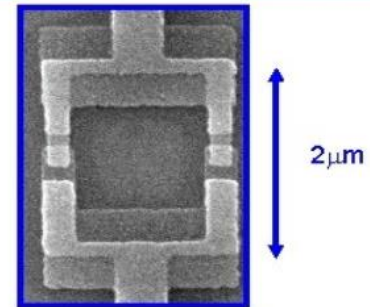
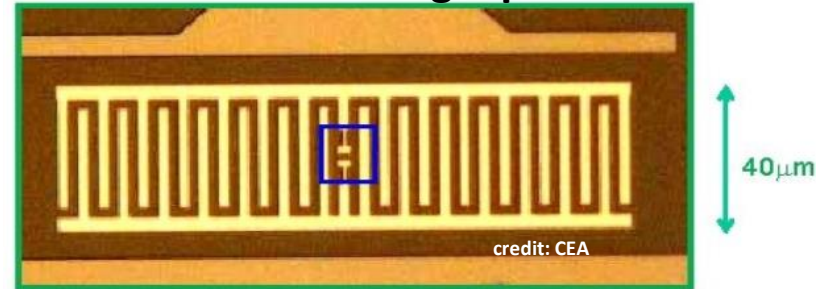
Famous examples

Superconducting quantum devices used for Dark Matter Search

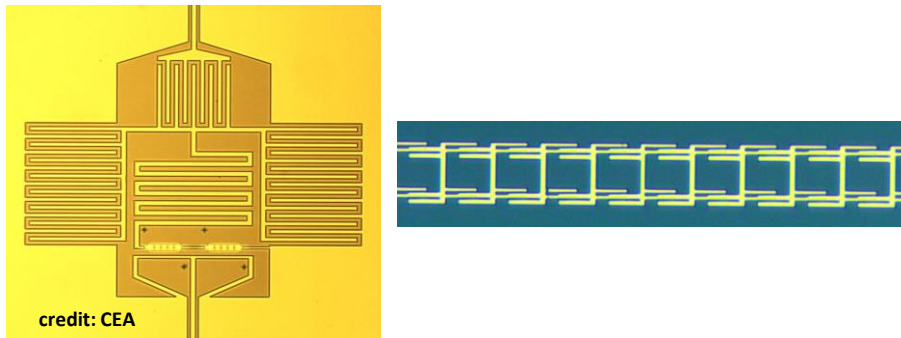
Cooper pair box Electrometer



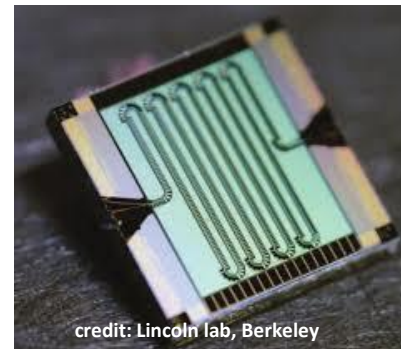
Transmon Qubit → Single μW Photon Det



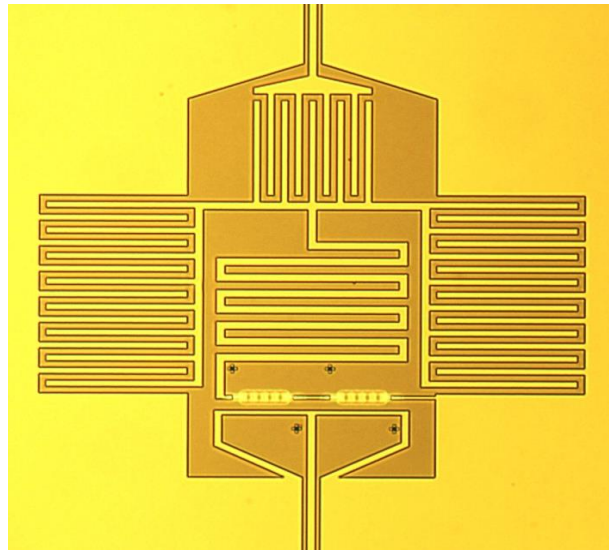
Josephson Parametric Amplifier



TWPA



Parametric Amplifier



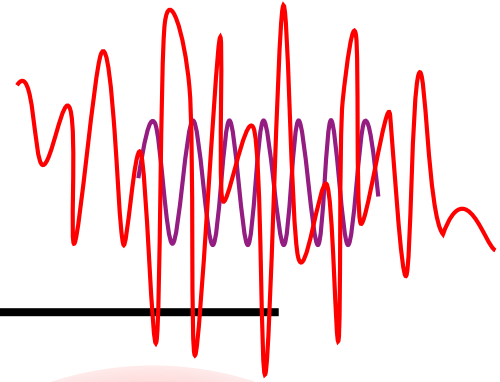
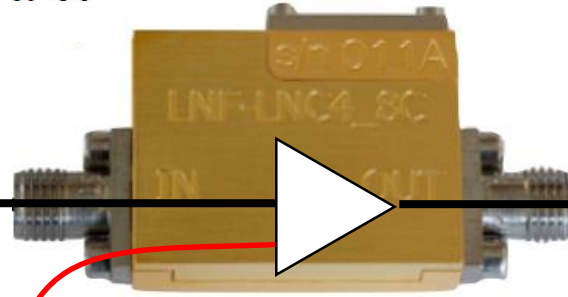
Example of 3 wave mixing

Measuring small microwave (coherent) fields

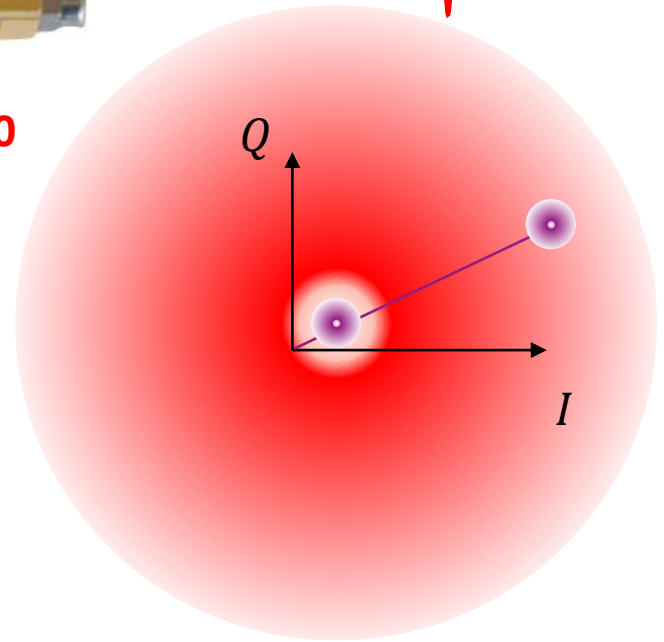
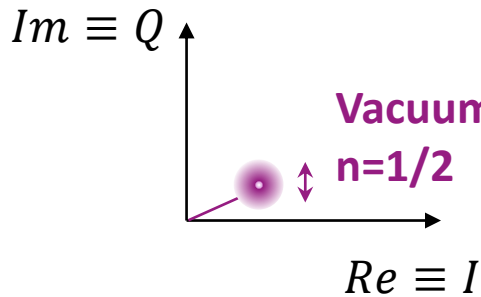
(~best) Commercial HEMT

Quantum lighth field

$|\psi\rangle$



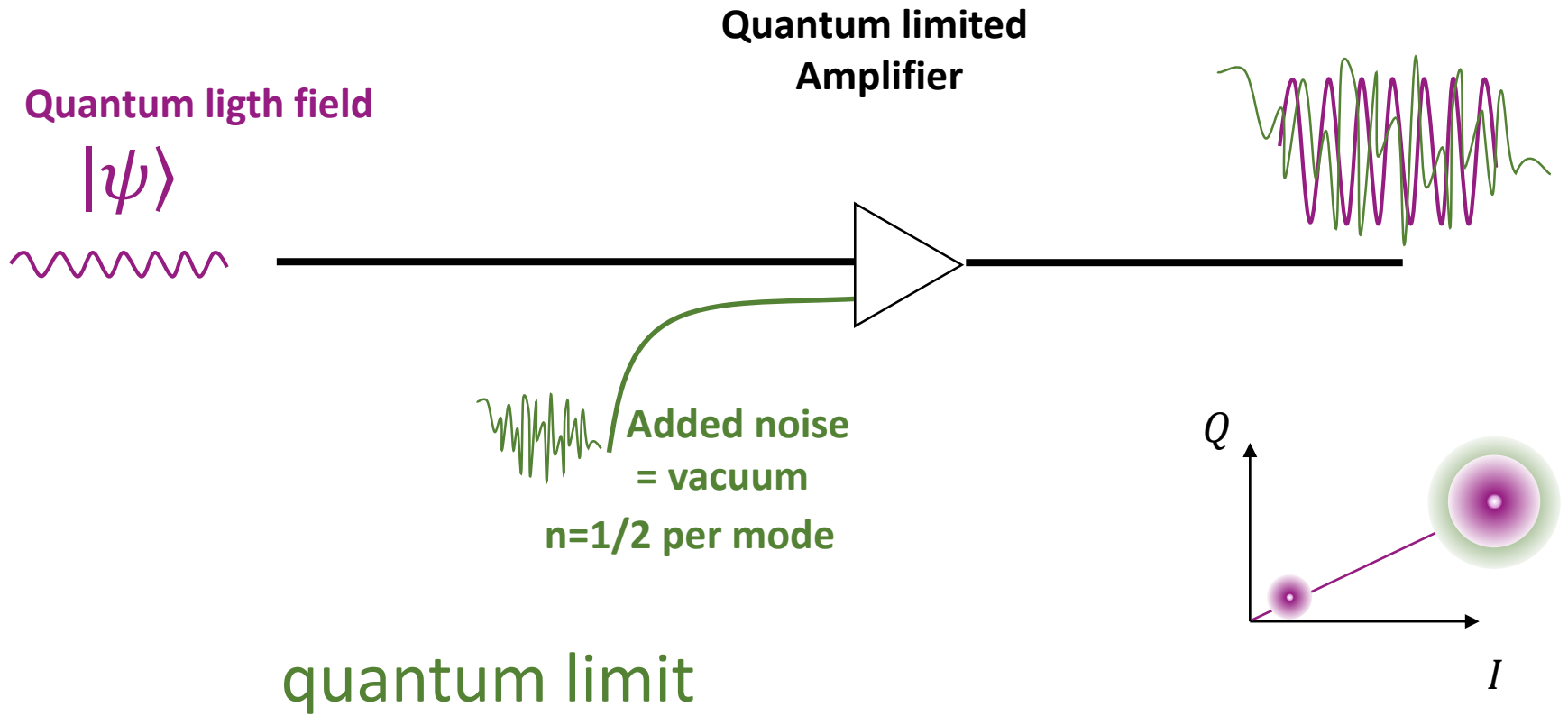
Added noise: $n \geq 10$



Amplifier figure of merit: T_N

noise power per unit bandwidth [W/Hz] = $k_B T_N = n h \nu$

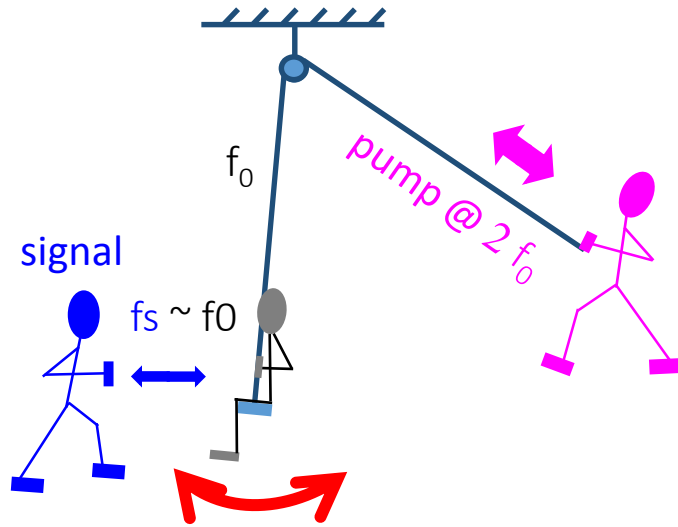
Measuring small microwave (coherent) fields



quantum limit

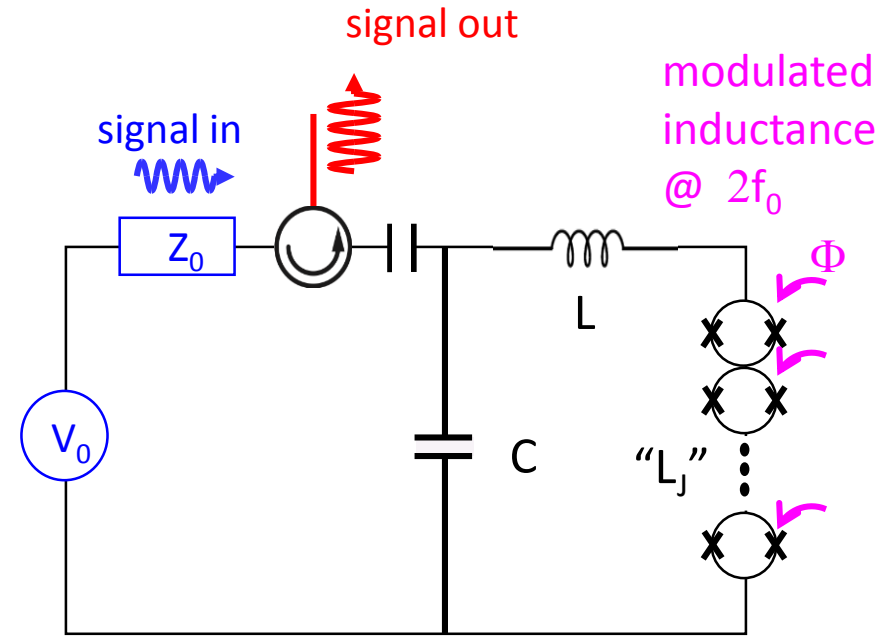
Josephson quantum limited amplifiers

Principle of parametric amplifiers



3 wave mixing

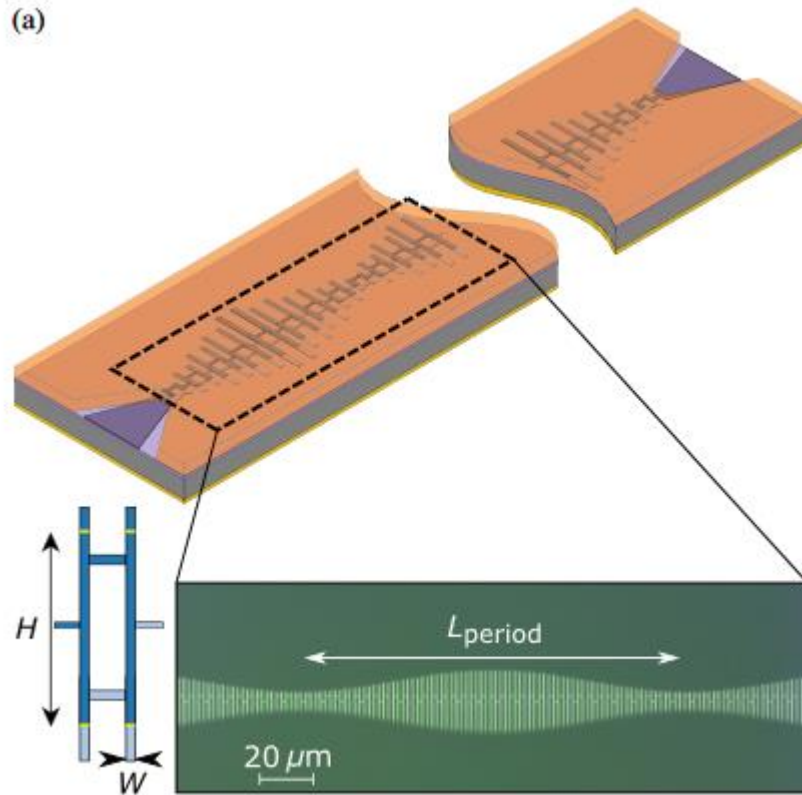
$$\omega_p = \omega_s + \omega_i$$



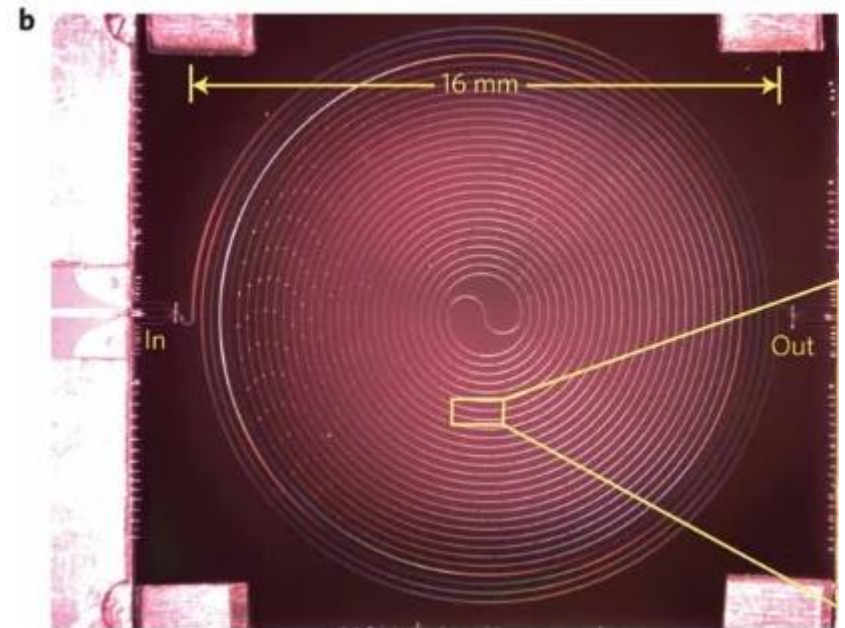
implemented with SQUIDS

Nice example : travelling wave parametric amplifier

PHYS. REV. X 10, 021021 (2020)

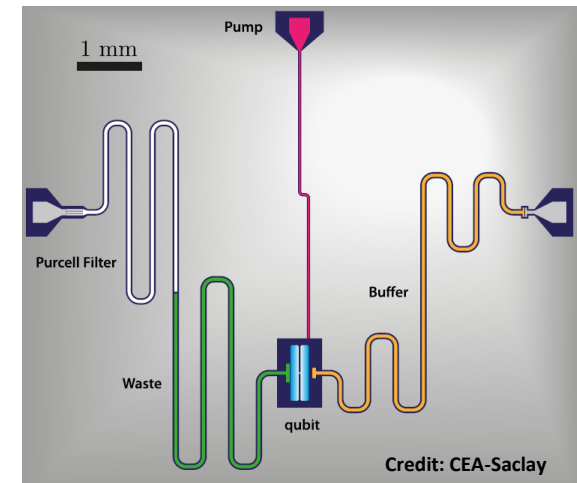
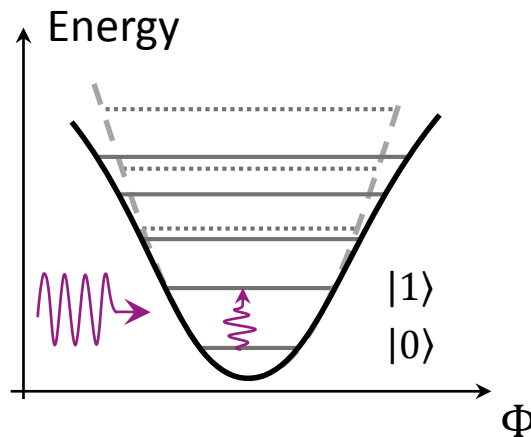
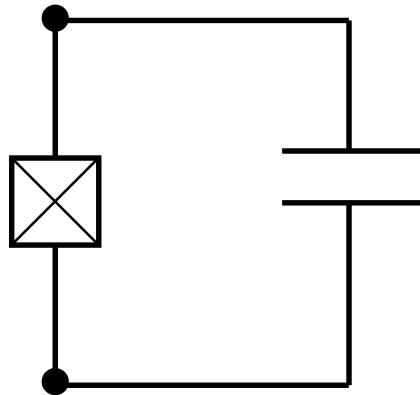


Nature Physics volume 8, pages 623–627 (2012)



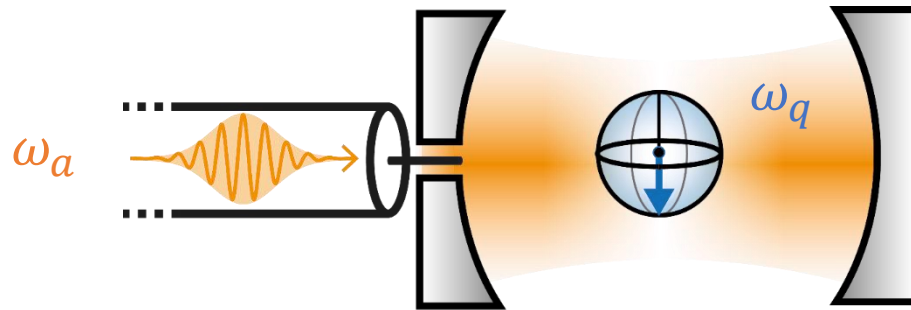
Single Microwave Photon Detector SMPD

Transmon QuBit

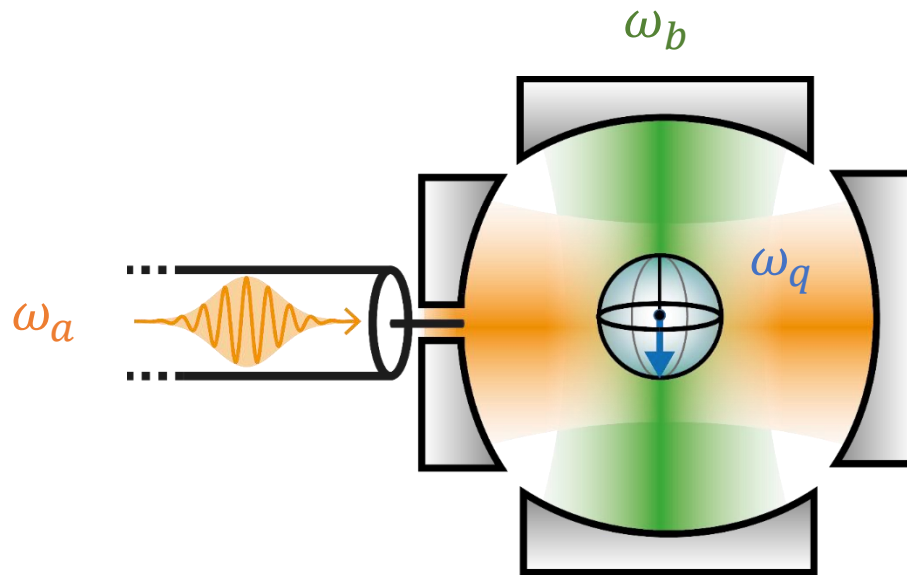


E. Flurin, P. Bertet, (SPEC, Université Paris-Saclay, CEA)
QUAX collaboration

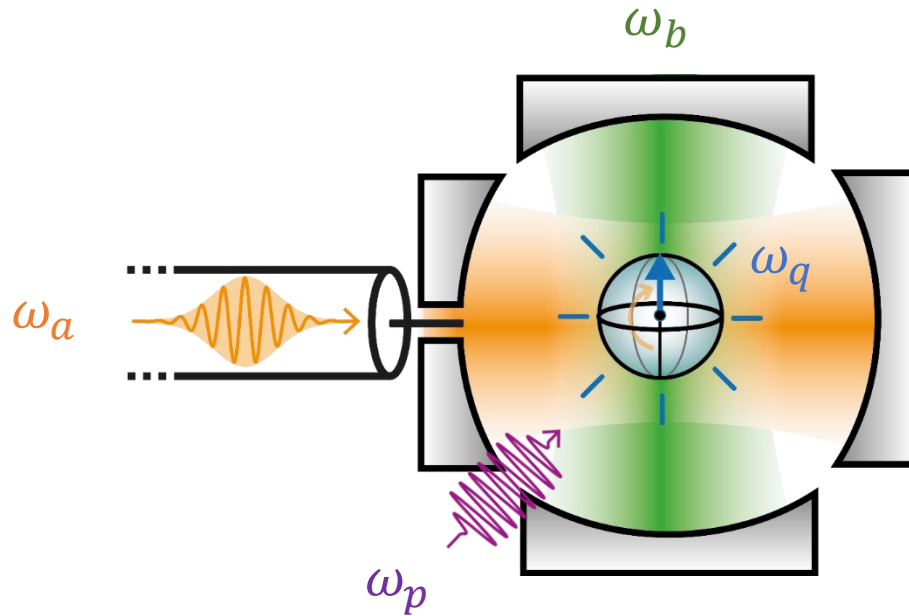
Single microwave photon counter : principle



Single microwave photon counter : principle

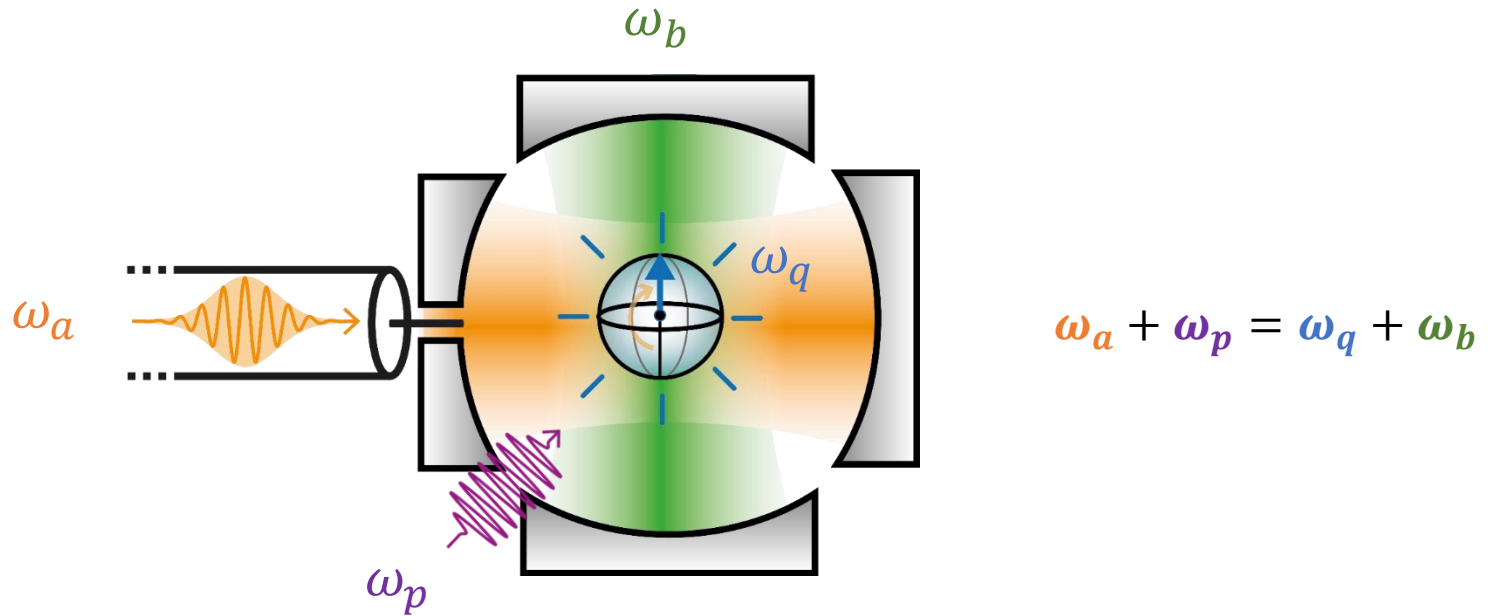


Single microwave photon counter : principle



$$\omega_a + \omega_p = \omega_q + \omega_b$$

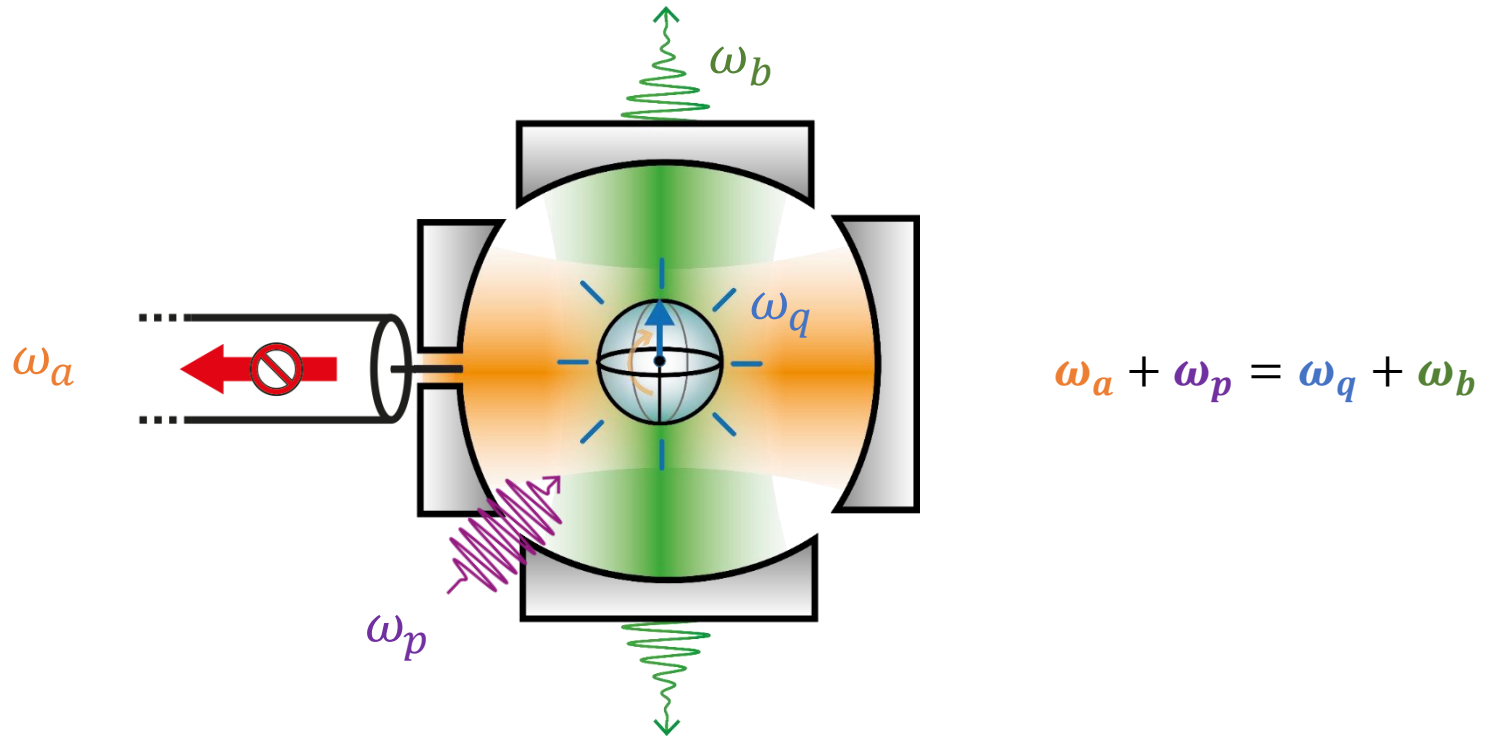
Single microwave photon counter : principle



Four-Wave mixing-based Photodetection

$$\hat{H} = g_4 \cdot (\xi \hat{a} \hat{\sigma}^+ \hat{b}^+ + \xi^* \hat{a}^+ \hat{\sigma} \hat{b})$$

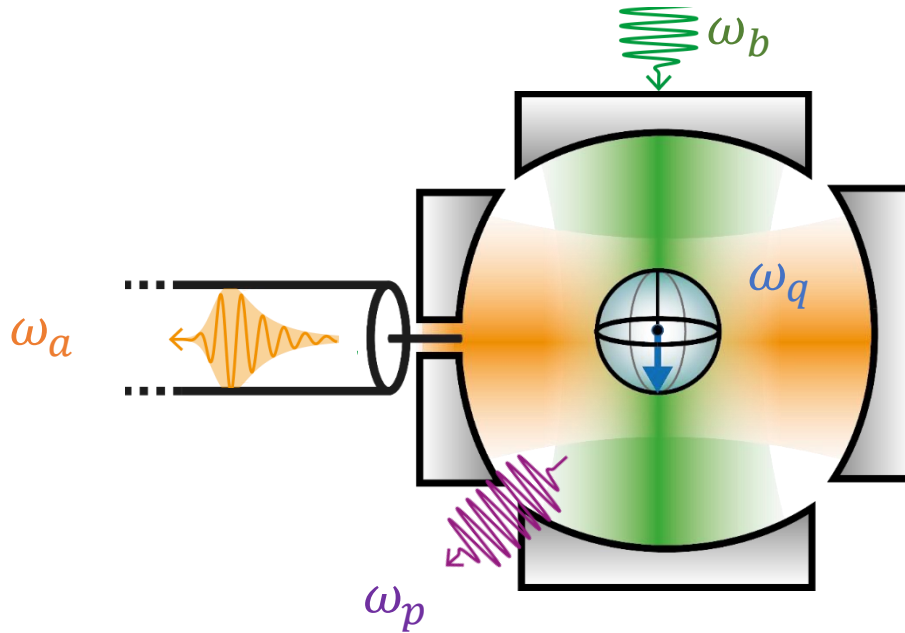
Single microwave photon counter : principle



$$\hat{H} = g_4 \cdot (\xi \hat{a} \hat{\sigma}^+ \hat{b}^+ + \xi^* \hat{a}^+ \hat{\sigma} \hat{b})$$

$$\hat{L} = \hat{a} \hat{\sigma}^+$$

Built-in detector reset



$$\omega_q + \omega_b = \omega_a + \omega_p$$

$$\hat{H} = g_4 \cdot (\xi \hat{\sigma} \hat{\sigma}^+ \hat{b}^+ + \xi^* \hat{a}^+ \hat{\sigma} \hat{b})$$

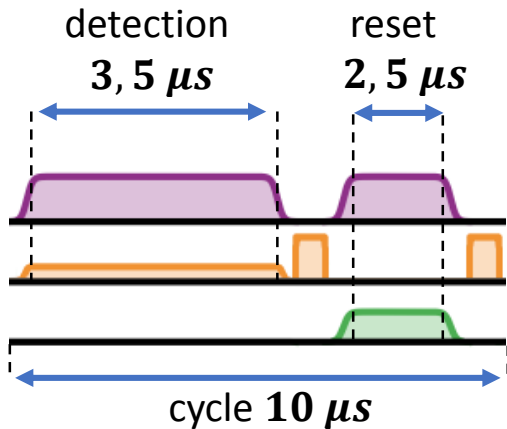
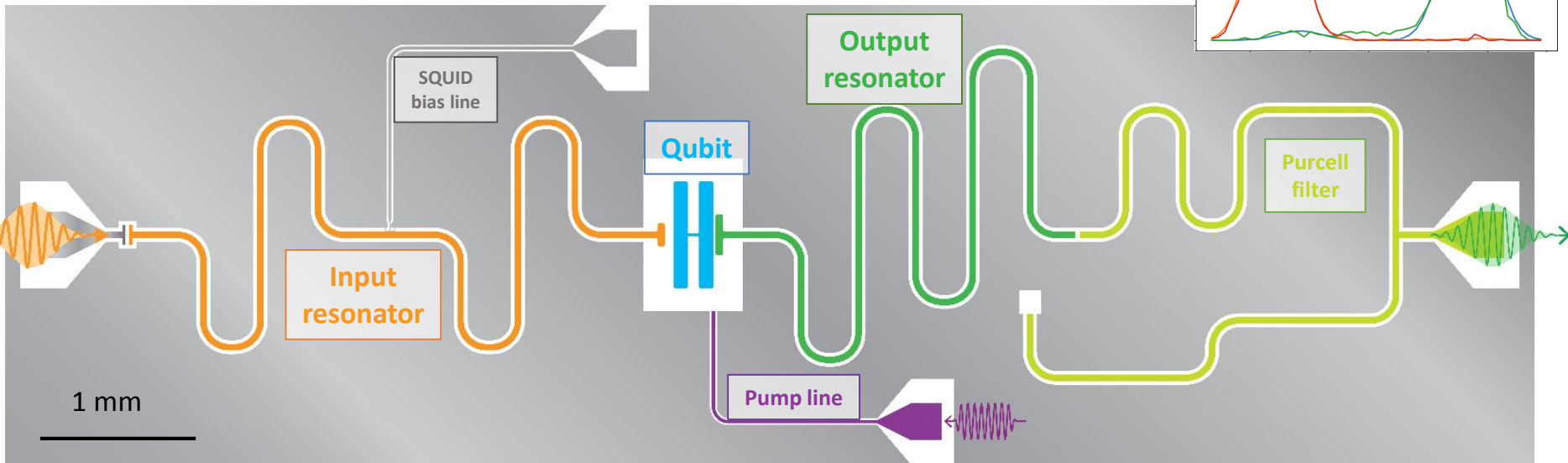
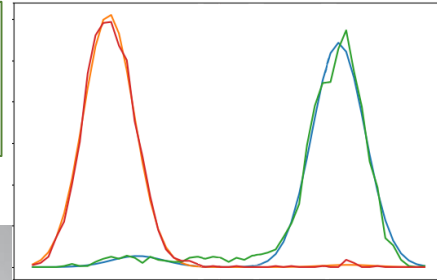
Implementation

$f_{in} = 7,1 \text{ GHz}$
 $Q_{in} = 7,5 \text{ k}$
 $\chi_{in q}/2\pi = 3,5 \text{ MHz}$

$f_q = 6,1 \text{ GHz}$
 $T_1 = 8 - 9 \mu\text{s}$
 $T_2^* = 13 \mu\text{s}$

$f_{out} = 7,6 \text{ GHz}$
 $Q_{out} = 16 \text{ k}$
 $\chi_{out q}/2\pi = 8,1 \text{ MHz}$

single shot measurement



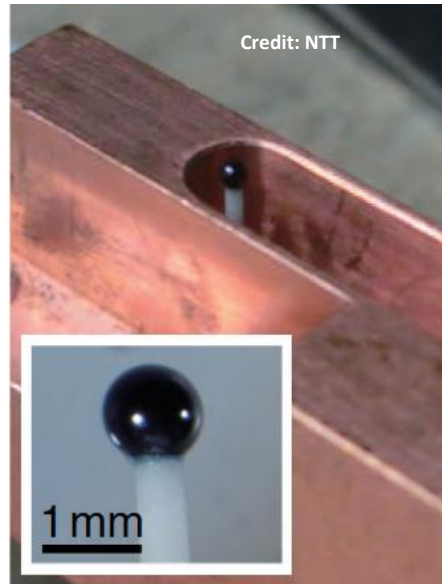
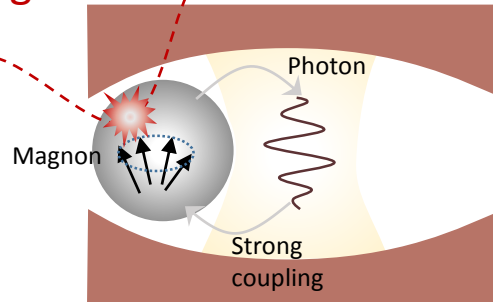
35% duty cycle

Dark count rate: $\alpha = 0.4 \text{ ms}^{-1}$

Total efficiency: 20%

Axion detectors (“haloscopes”)

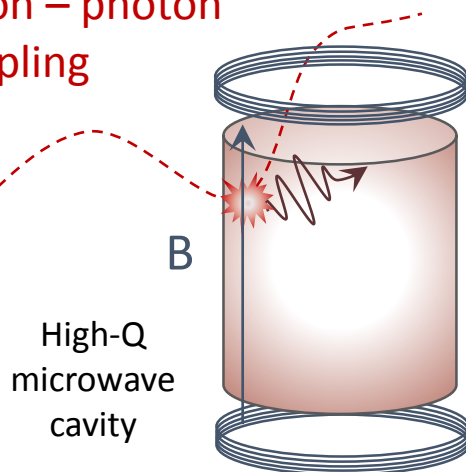
Axion – electron spin coupling



« Ferromagnetic haloscope »

Crescini, COMMUNICATIONS PHYSICS (2020)

Axion – photon coupling



How to detect the photon ?

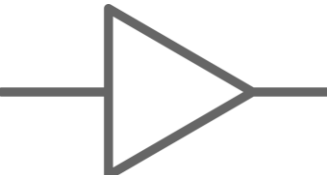
- Squid amplifier (ADMX)
(J. Clarke) Rev. Mod. Phys., Vol. 75, No. 3, July 2003
- Josephson Parametric amplifier (HAYSTAC)
(K. Lehnert) Phys. Rev. Lett. 118, 061302 (2017)
- Single microwave photon detector (QUAX)
Lescanne et al., PRX 2020
(D. Schuster) Dixit et al. PRL 2021

Dark matter Axion detection

Advantage of SMPD over linear detectors operated at the quantum limit

$$SNR = P_S/P_N$$


Signal-to-noise with linear amplifier at the quantum limit



$$SNR_{\text{lin}} = \frac{P_{\text{axion}}}{\hbar\omega/2} \sqrt{\frac{t_{\text{lin}}}{\kappa_{\text{axion}}}}$$

← axion linewidth ~ 10 kHz

Signal-to-noise with SMPD



$$SNR_{\text{SMPD}} = \frac{P_{\text{axion}}}{\hbar\omega} \sqrt{\frac{t_{\text{SMPD}}}{\alpha_{\text{DC}}}}$$

← axion power ~ 1 photon.s⁻¹

← darkcount $\sim 5 - 50$ click.s⁻¹

$$\frac{t_{\text{lin}}}{t_{\text{SMPD}}} = \frac{1}{4} \frac{\kappa_{\text{axion}}}{\alpha_{\text{DC}}} \sim 50 - 500$$

Thank you!



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