

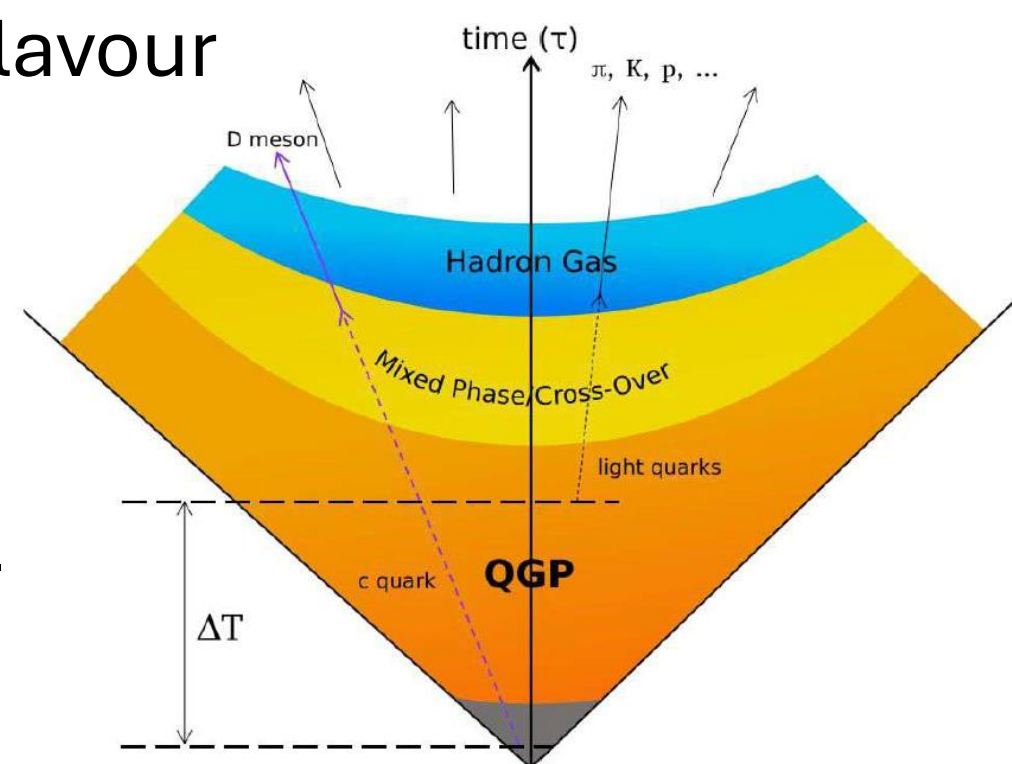
How far can we see back in time in high-energy collisions using charm quarks?

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Motivation

- In high-energy collisions light-flavour and strange hadrons mostly carry information about the final state
- Heavy-flavour c and b quarks are produced in the initial stages of a collision and experience the whole evolution of the system
- Measurement of heavy-flavour hadron production allows for studying the earlier stages of a collision
- The non-extensive Tsallis – Pareto statistical framework[1] has been shown to describe well the spectra of light-flavour hadrons[2]
- In this work we evaluate applicability of non-extensive thermodynamical principles on heavy-flavour production
- We use D mesons to investigate the thermodynamical properties of earlier stages of the system



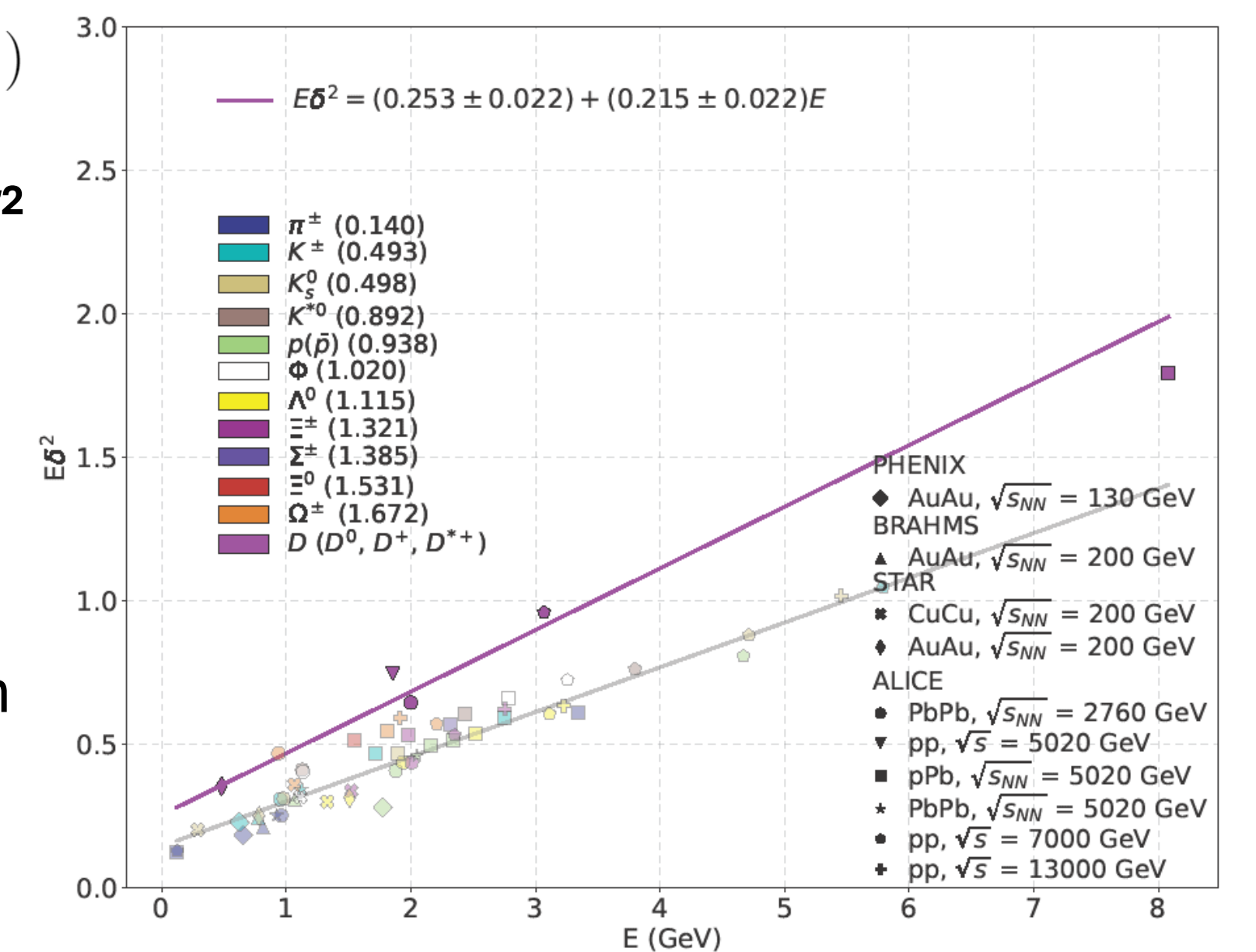
Common Tsallis parameters

Tsallis parameters can be defined from the fluctuations of the number of the produced particles: $T = \frac{E}{\langle n \rangle}$, $q = 1 - \frac{1}{\langle n \rangle} + \frac{\Delta n^2}{\langle n \rangle^2}$, $\delta^2 := \frac{\Delta n^2}{\langle n \rangle^2}$

This leads to an energy-dependent linear correlation between the Tsallis parameters: $T = E(\delta^2 - (q - 1))$

Observations from the $E - E\delta^2$ diagram:

- relative size of multiplicity fluctuations is larger for D mesons compared to the light-flavour hadrons
- fitted E values increase with decreasing system size



The common Tsallis parameters were determined by fitting D-meson points with the inverted equation $E\delta^2 = T - (q - 1)E$

Obtained values:

$$T_D = 0.253 \pm 0.022 \text{ GeV} \quad T_{LF} = 0.144 \pm 0.010 \text{ GeV}$$

$$q_D = 1.215 \pm 0.022 \quad q_{LF} = 1.156 \pm 0.007$$

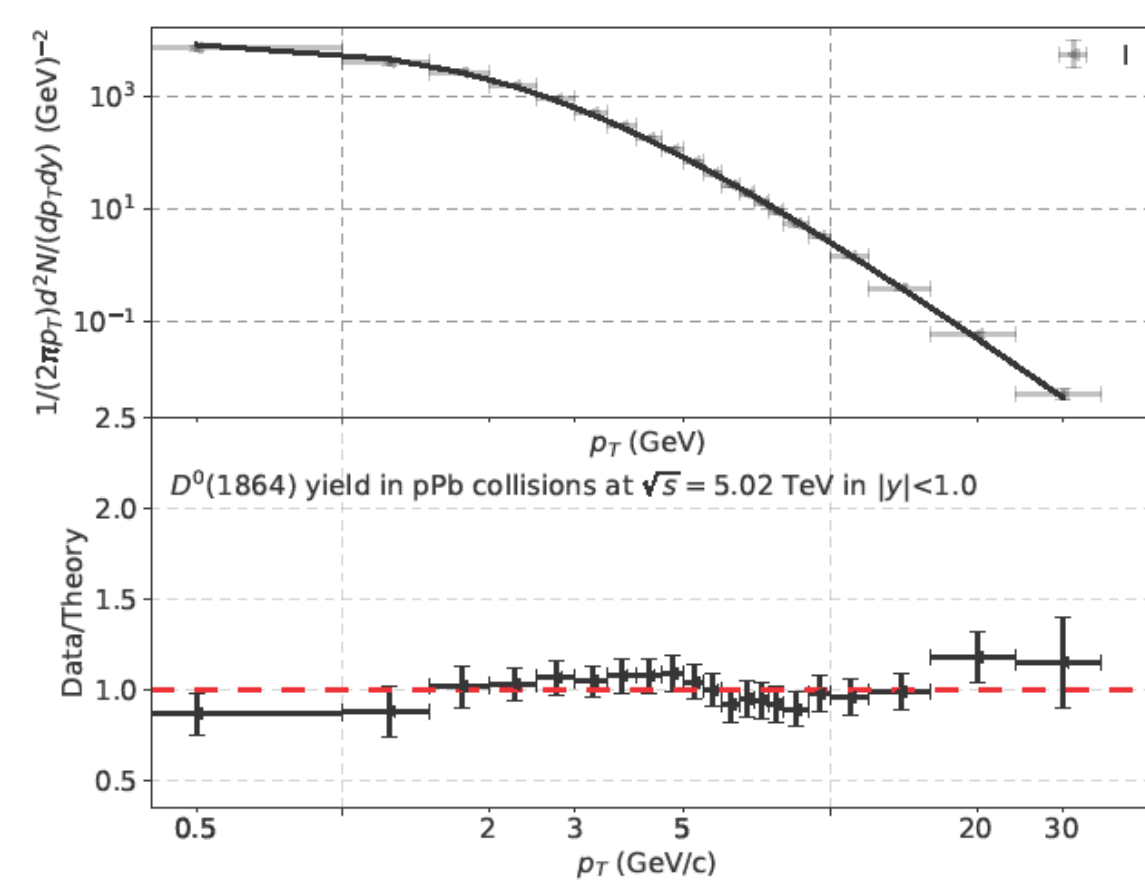
Method

Low- p_T part of spectrum:

- Boltzmann – Gibbs distribution
- characterized by the kinetic freeze-out temperature

High- p_T part of spectrum:

- power-law distribution
- perturbative QCD hadron production



The Tsallis – Pareto distribution, motivated by non-extensive thermodynamics, provides a unified description of the full spectrum:

$$\frac{d^2N}{2\pi p_T dp_T dy} \Big|_{y \approx 0} \equiv Am_T f^q = Am_T \left[1 + \frac{q-1}{T} (m_T - \mu) \right]^{-\frac{q}{q-1}}$$

Spectra used in this analysis

STAR experiment:

- D^0 in Au–Au collisions at $\sqrt{s_{NN}} = 200$ GeV

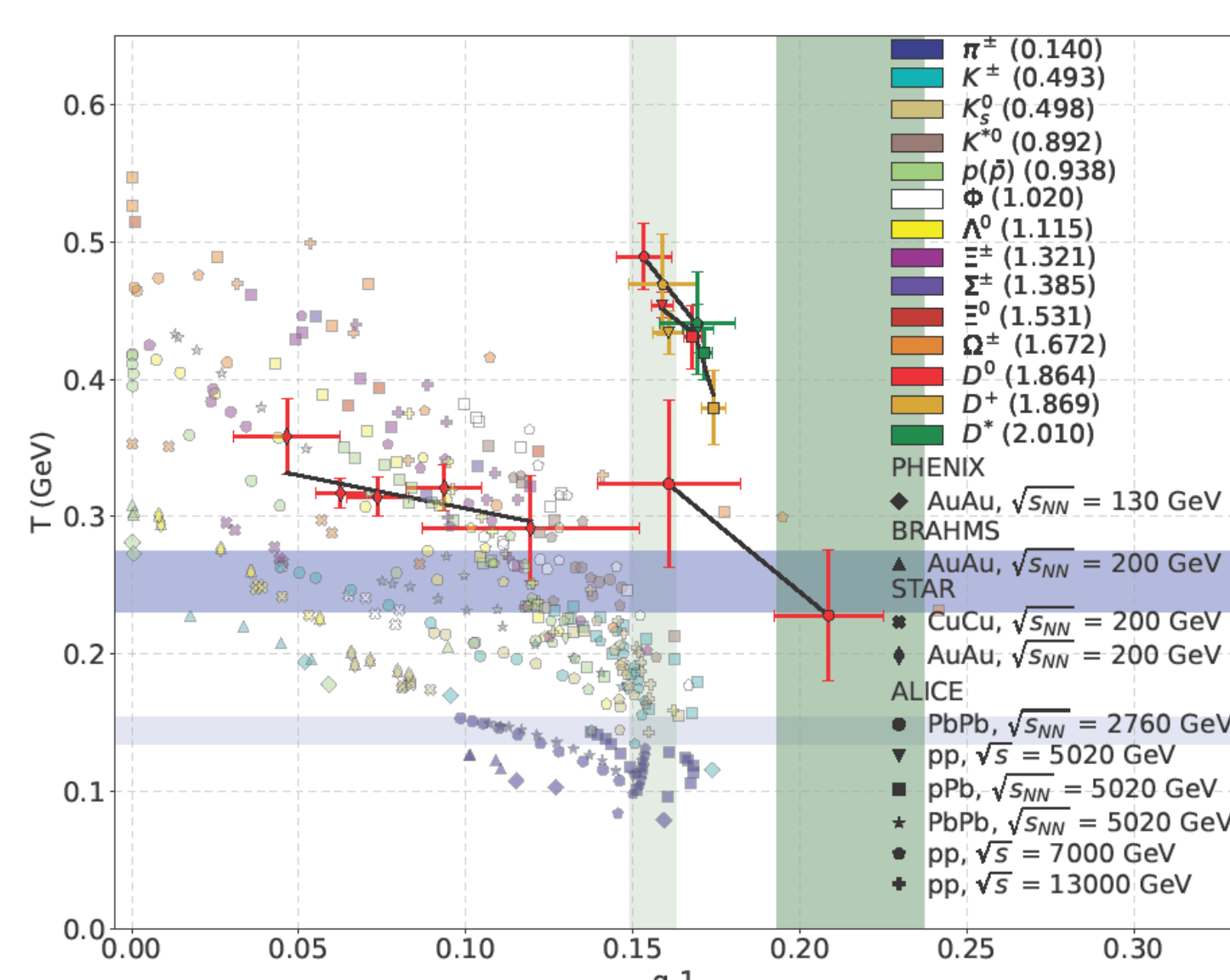
ALICE experiment:

- D^0 in Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV
- D^0 , D^+ and D^{*+} in p–Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV
- D^0 , D^+ and D^{*+} in pp collisions at $\sqrt{s} = 5.02$ TeV
- D^0 , D^+ and D^{*+} in pp collisions at $\sqrt{s} = 7$ TeV

Light-flavour and strange hadron spectra are from references in [1]

Tsallis-thermometer

The T and q parameters, extracted from the D-meson fits, are presented in the „Tsallis-thermometer”, $T - (q-1)$ diagram



Observations:

- mass hierarchy (T increases with particle mass and multiplicity)
- grouping based on the center-of-mass energy and collision system
- in small systems c quarks come directly from the early stages of the collisions, corresponding to high T values
- grouping of all the hadrons at small multiplicities around specific common T_{eq} and q_{eq} values

How far can we see back in time?

A simple Bjorken model can be utilized as the expansion mechanism of the ideal, ultra-relativistic matter. It yields the relation between

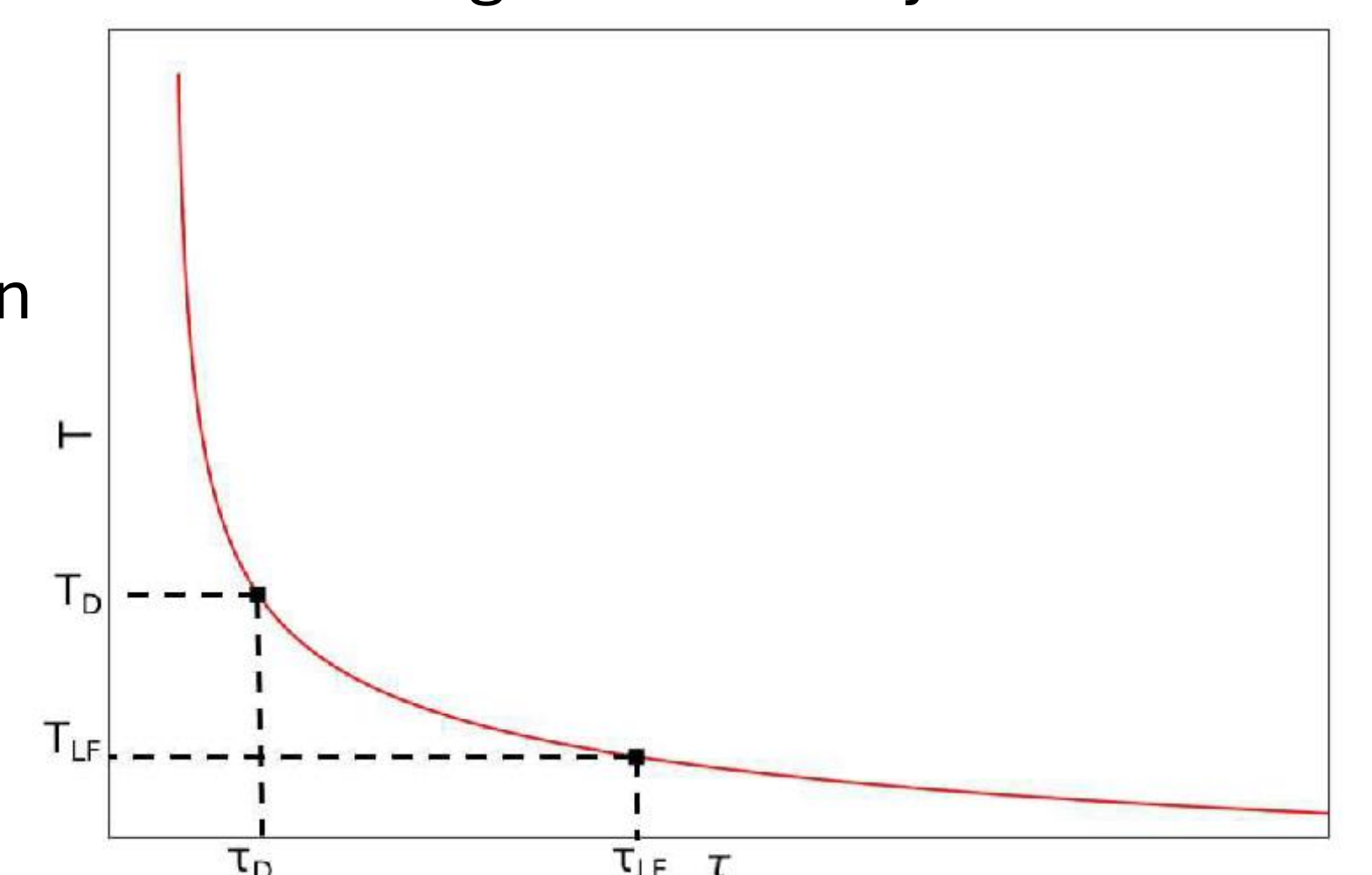
temperature and proper time (cooling curve) [2]: $\tau = \tau_0 \left(\frac{T_0}{T} \right)^3$

Assuming the same initial conditions for light- and heavy-flavour

hadrons: $\tau_D = \tau_{LF} \left(\frac{T_{LF}}{T_D} \right)^3$

By substituting the common Tsallis-temperatures we obtain:

$$\tau_D = (0.18 \pm 0.06) \tau_{LF}$$



Summary

- Transverse momentum distributions of heavy-flavour D mesons are well described by the Tsallis – Pareto distribution motivated by non-extensive thermodynamics
- The Tsallis parameters of the fits to D-meson data exhibit a scaling behaviour with charged particle multiplicity and with the collision energy
- The T_{eq} parameter for D mesons is higher compared to the light flavours. Coming from a much hotter state of the system, D mesons preserve this information, unlike the light-flavour hadrons
- Production of D mesons corresponds to a significantly earlier proper time than light-flavour hadrons. Based on the Bjorken expansion, we estimated it as $\tau_D = (0.18 \pm 0.06) \tau_{LF}$

References

- [1] Eur.Phys.J.A 40 (2009) 257-266
- [2] J. Phys. G, 47(10):105002, 2020
- [3] Phys. Rev. C, 97(6):064903, 2018

Acknowledgements

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Full paper

