

A Realistic Coalescence Model for Deuteron Production

Maximilian Mahlein, Laura Fabbietti,
Bhawani Singh, Chiara Pinto

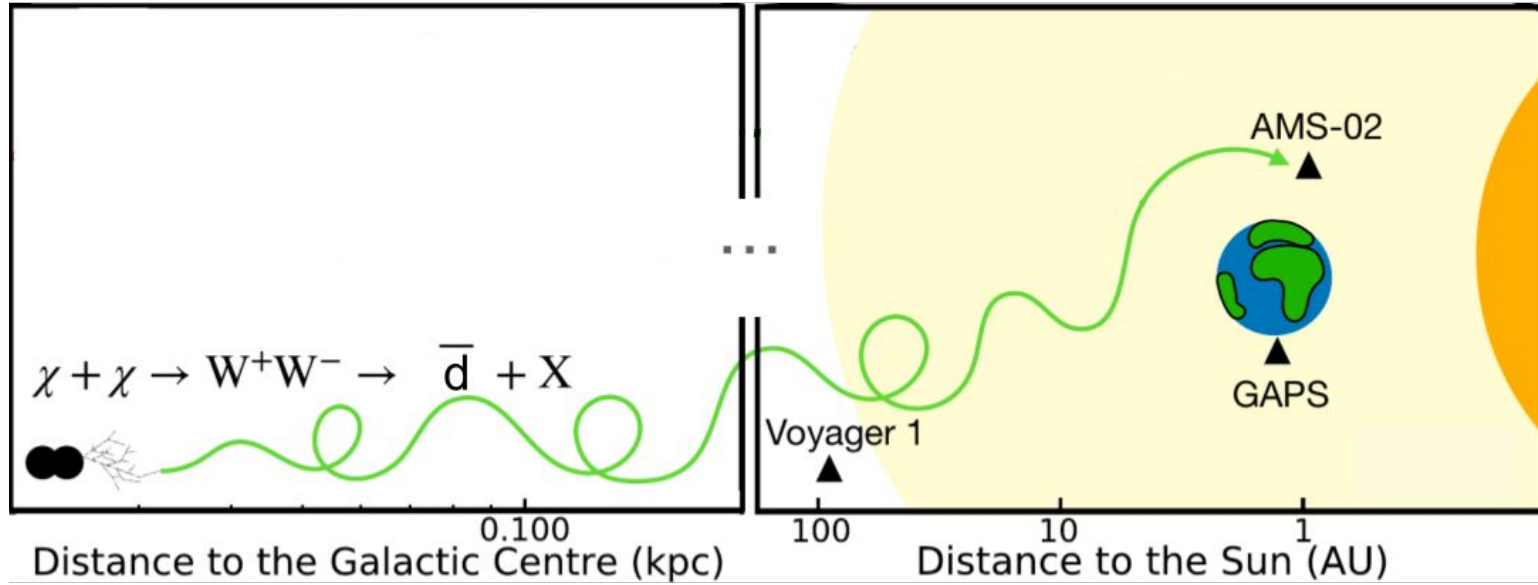
Based on: arXiv:2404.03352

Technical University Munich



Cosmic Rays

Antinuclei in Cosmic Rays

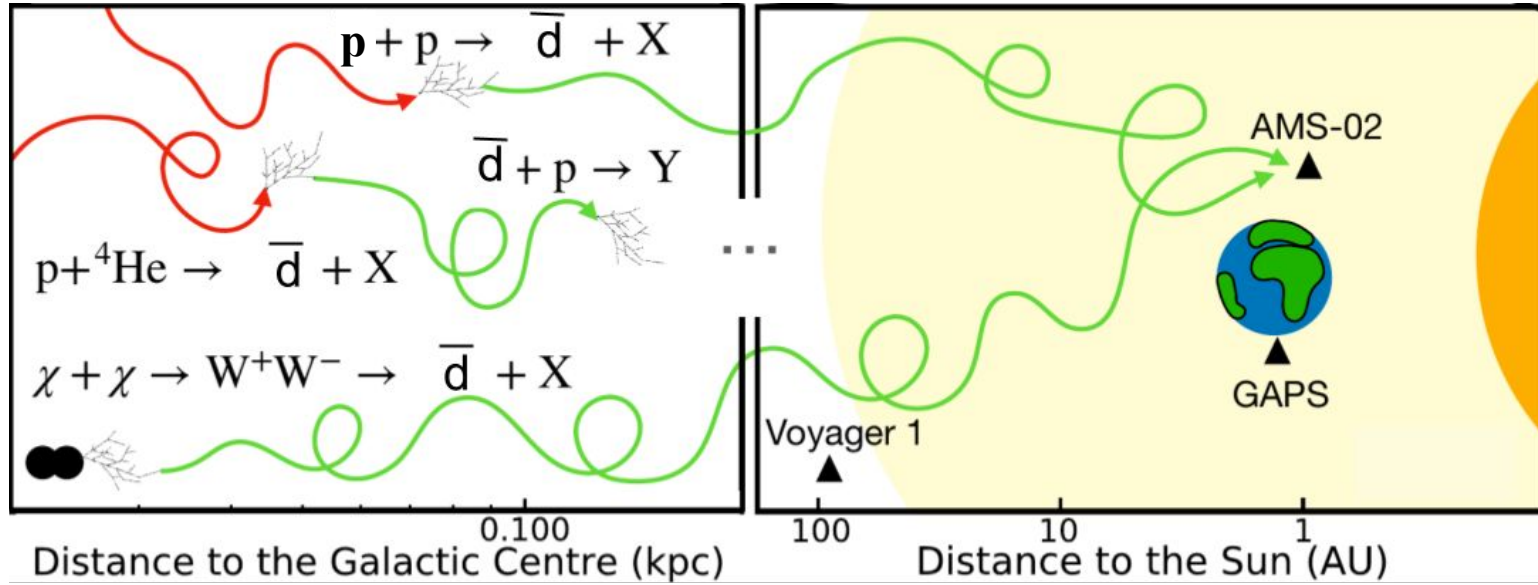


ALICE Collaboration, Nat. Phys. 19, 61–71 (2023)

- Antinuclei could be a probe for indirect Dark Matter searches

Cosmic Rays

Antinuclei in Cosmic Rays

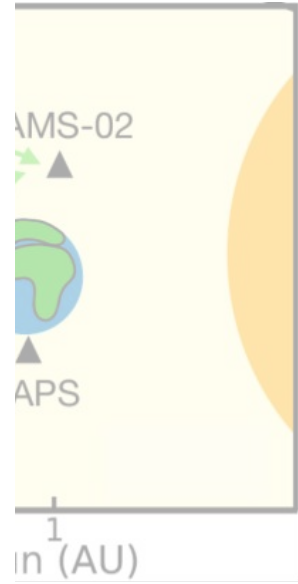
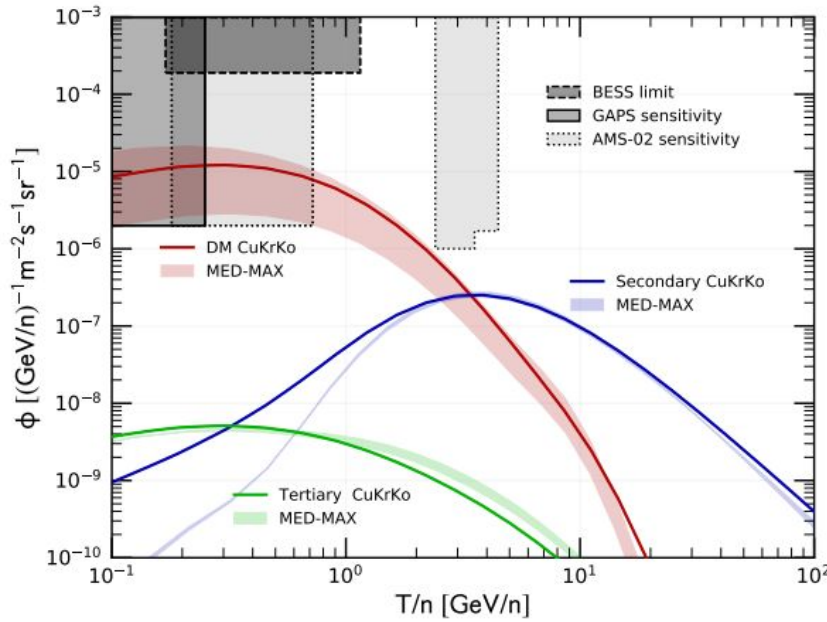
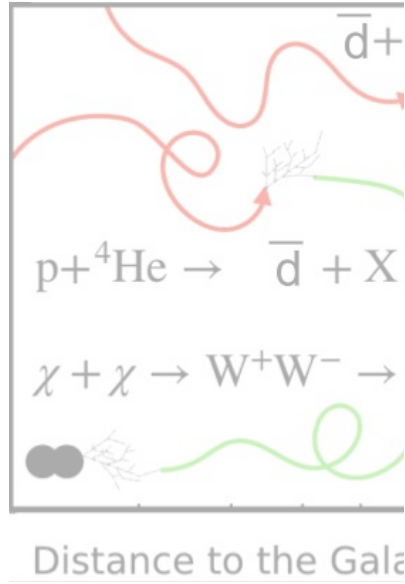


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- However: Astrophysical background from cosmic rays expected

Cosmic Rays

Antinuclei in Cosmic Rays



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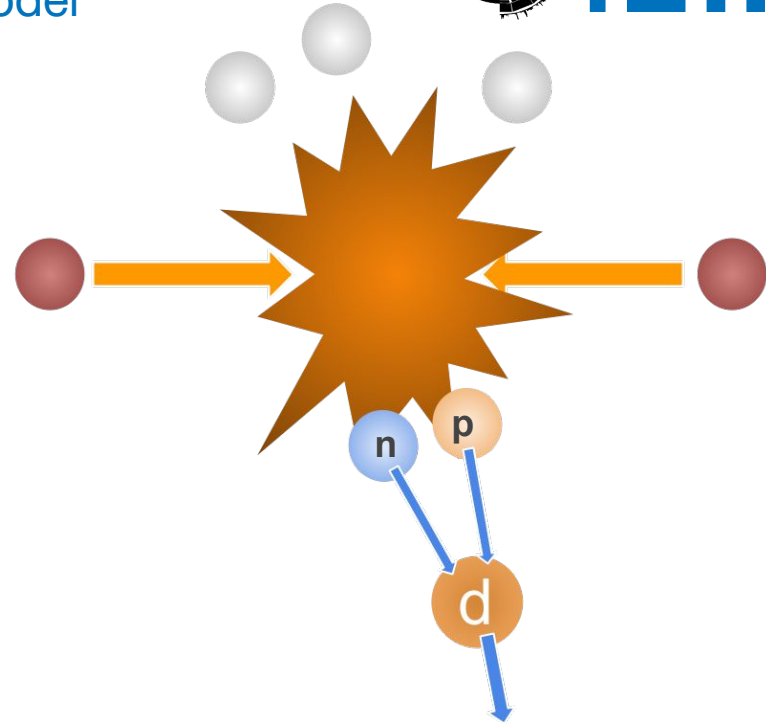
- Antinuclei could be a probe for indirect Dark Matter searches
- However: Astrophysical background from cosmic rays expected
- High Signal/Noise ratio ($\sim 10^2$ - 10^4) at low E_{kin} expected by many models!

Modelling (Anti)nuclei Production

The Coalescence Model



- Nucleons bind after freeze-out if they are close in phase-space



Modelling (Anti)nuclei Production

The Coalescence Model



- Nucleons bind after freeze-out if they are close in phase-space
- Wigner function formalism:

$$\frac{dN_d}{d^3P} = S_d \int d^3x_1 \int d^3x_2 \int d^3x'_1 \int d^3x'_2 \Psi_d^*(\vec{x}'_1, \vec{x}'_2) \times \Psi_d(\vec{x}_1, \vec{x}_2) \langle \Psi_2^\dagger(\vec{x}'_2) \Psi_1^\dagger(\vec{x}'_1) \Psi_1(\vec{x}_1) \Psi_2(\vec{x}_2) \rangle$$

$$p(\sigma, q) = \int d^3r_p d^3r_n h(r_n) h(r_p) W(q, r)$$

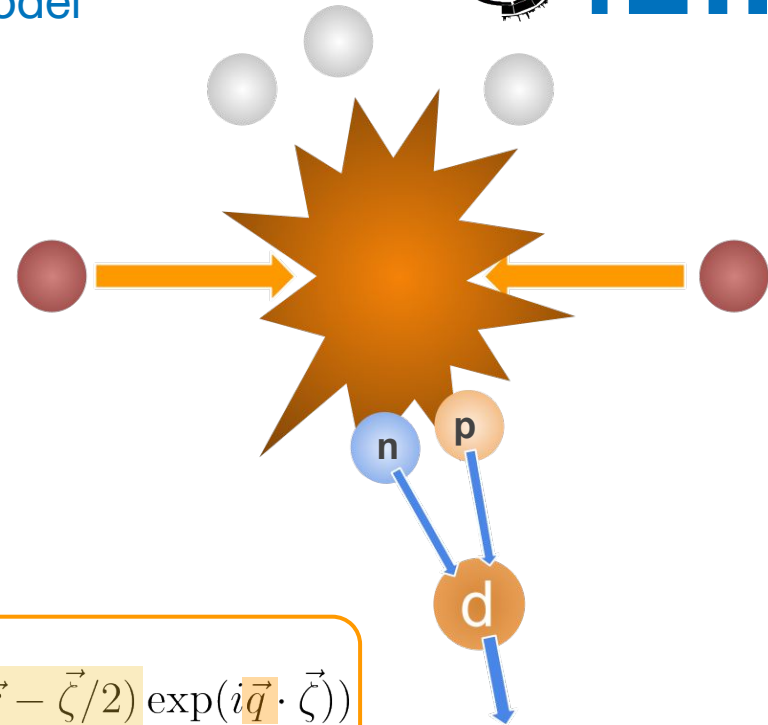
$$= \frac{1}{(2\pi\sigma^2)^3} \exp\left(-\frac{\vec{r}_n^2 + \vec{r}_p^2}{2\sigma^2}\right)$$

Source size

$$= \int d^3\zeta \Psi(\vec{r} + \vec{\zeta}/2) \Psi^*(\vec{r} - \vec{\zeta}/2) \exp(i\vec{q} \cdot \vec{\zeta})$$

Nucleus wave function

Relative momenta of nucleons



Modelling (Anti)nuclei Production

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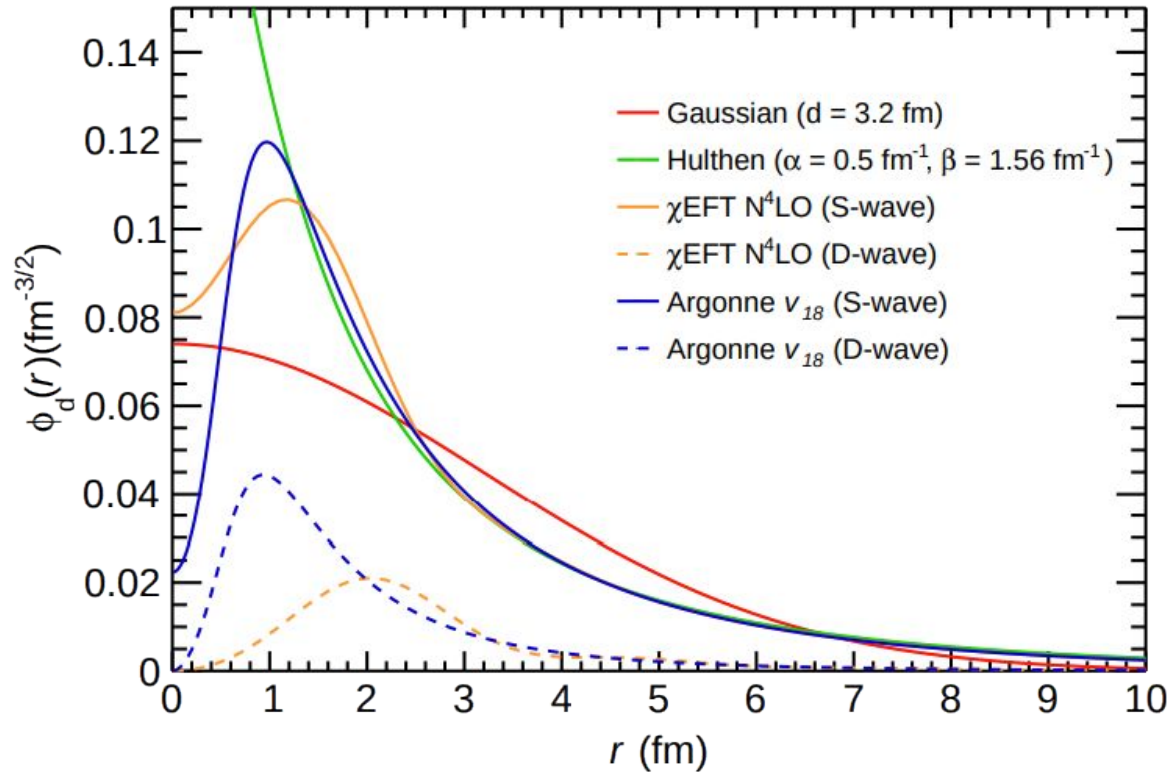


- Nucleons bind are close in phase space
- Wigner function

$$p(\sigma, q) = \int d^3r$$

$$= \frac{1}{(2\pi\sigma^2)^3} \exp\left(-\frac{\vec{r}^2}{2\sigma^2}\right)$$

So



MM et al .Eur.Phys.J.C 83 (2023) 9, 804

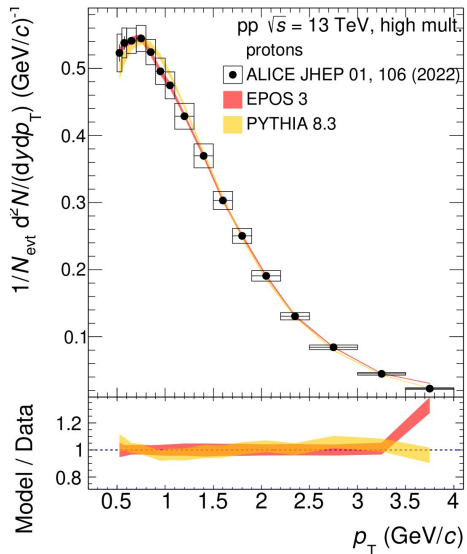
Coalescence Results EPOS

Deuteron spectra



MM et al .Eur.Phys.J.C 83 (2023) 9, 804

- Corrections to Protons, Source, Multiplicity
- Wavefunctions: Gaussian, Hulthén and Argonne v_{18}
- v_{18} reproduces data to $\sim 10\%$



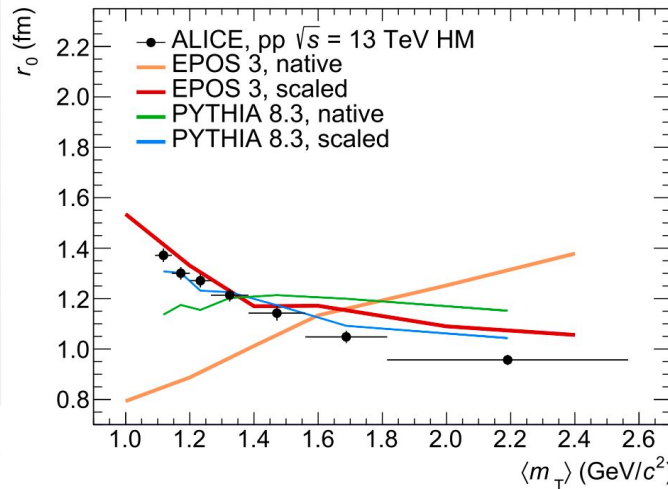
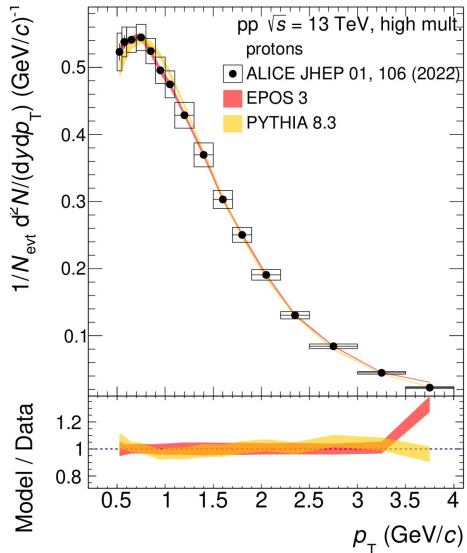
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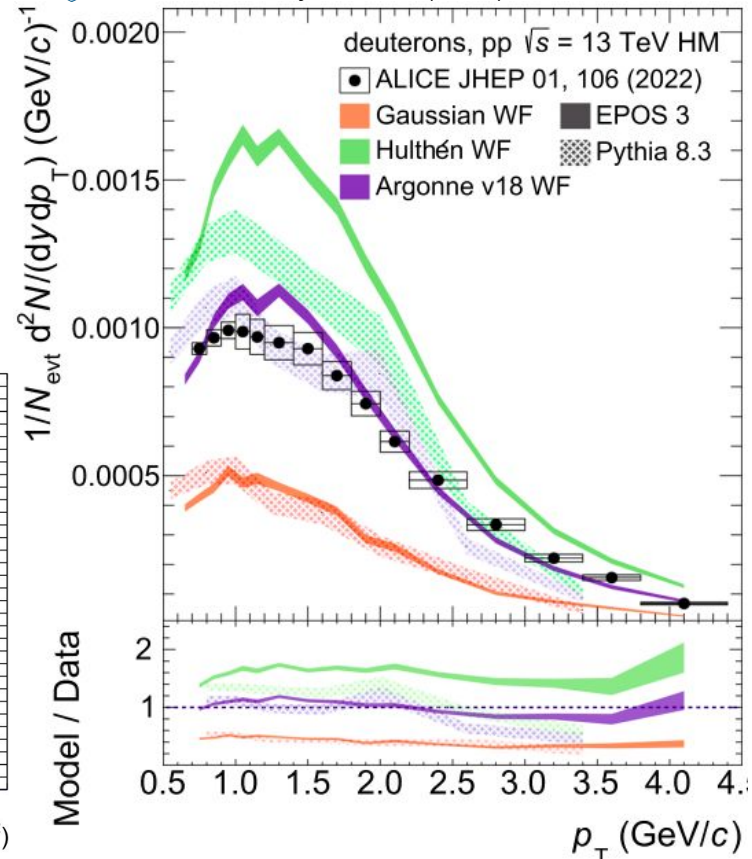
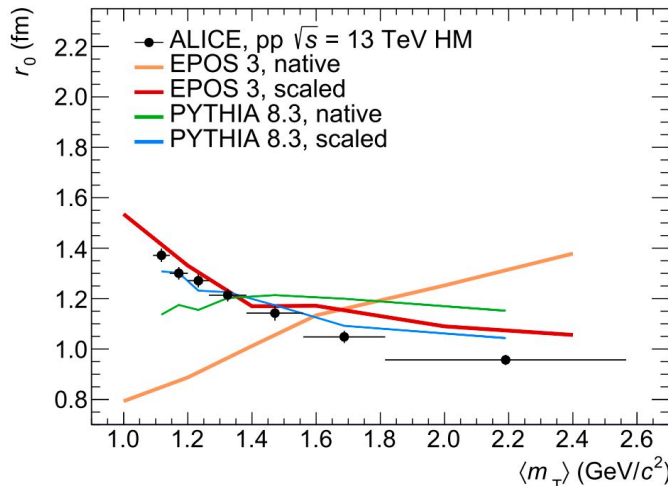
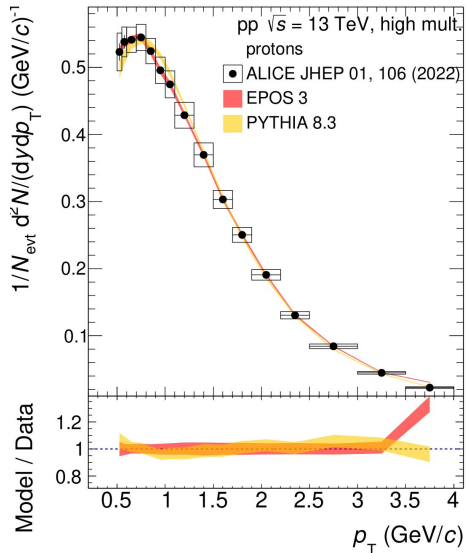
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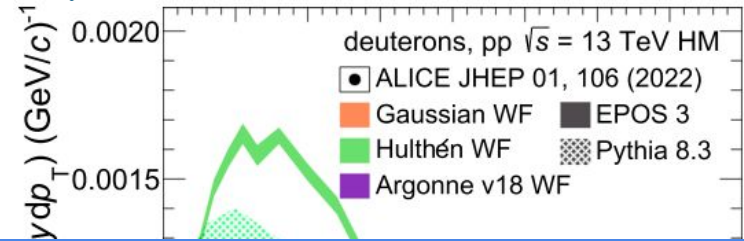
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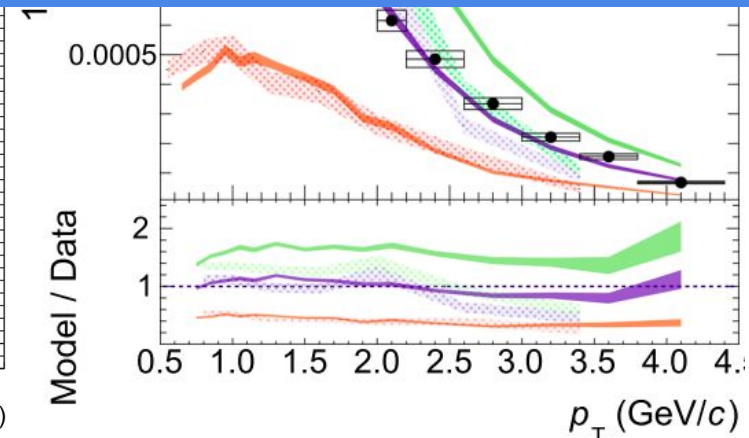
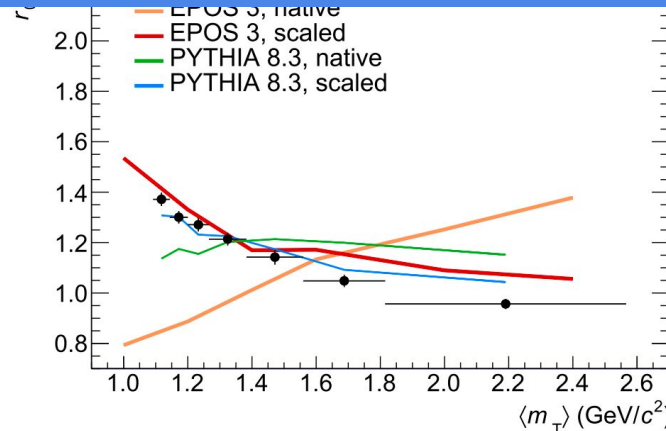
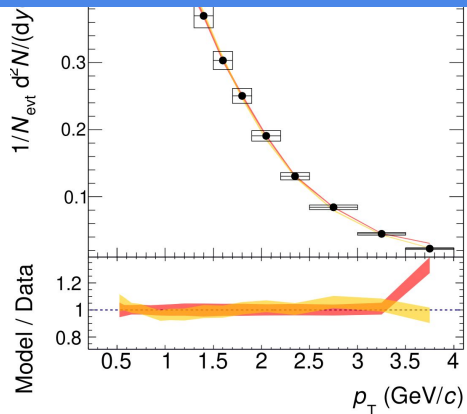
Deuteron spectra

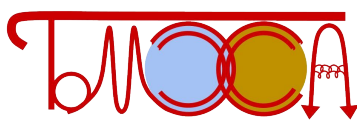
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Most advanced coalescence model with realistic wave function!





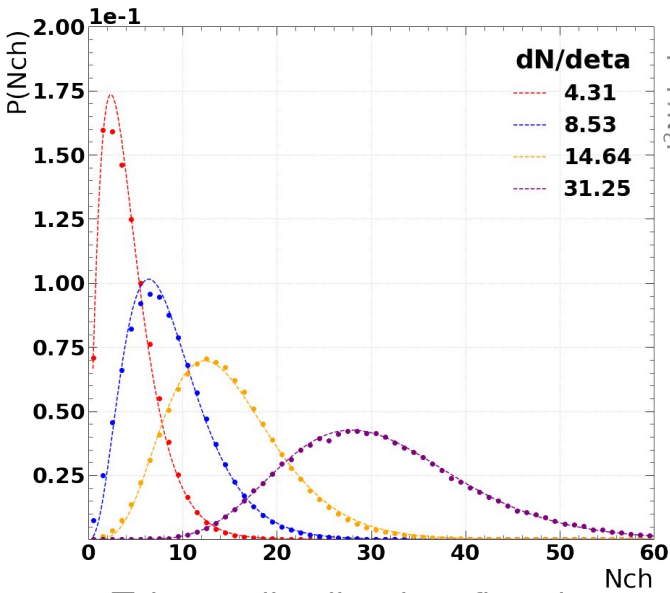
The ToMCCA Model

A Toy Monte Carlo Coalescence Afterburner



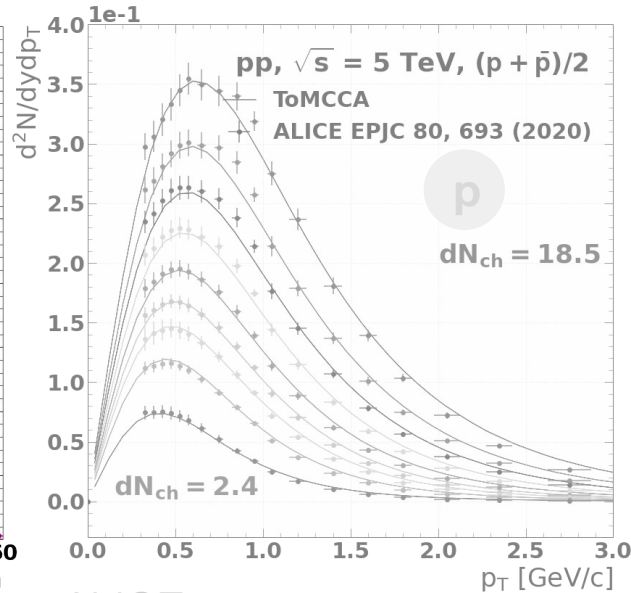
Main Inputs: Multiplicity, momentum distributions, source size

Multiplicity



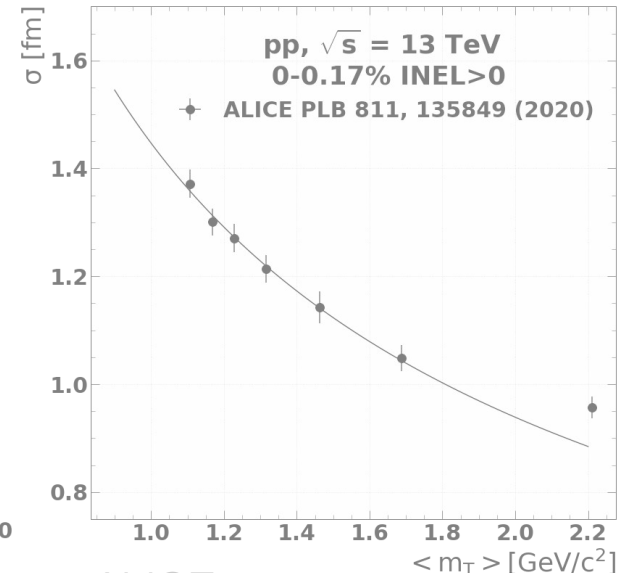
Erlang distribution fitted to EPOS3 simulations

Momentum distribution

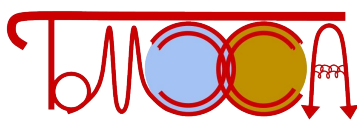


ALICE measurements over a large multiplicity range

Source size



ALICE measurement in high-multiplicity collisions



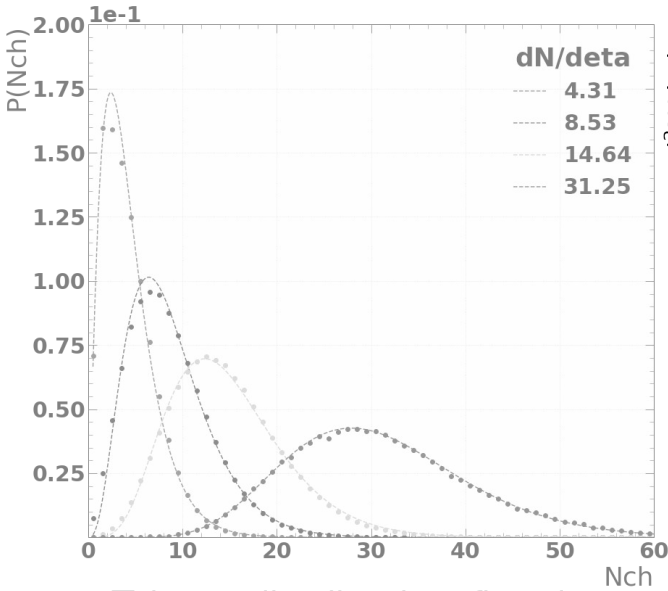
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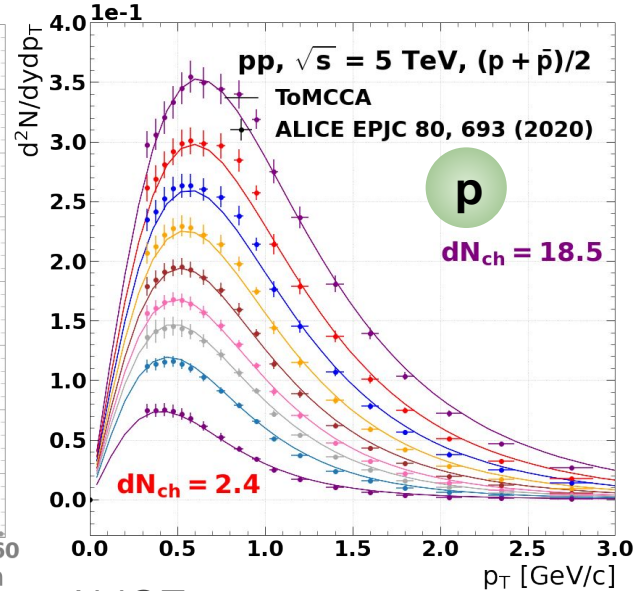
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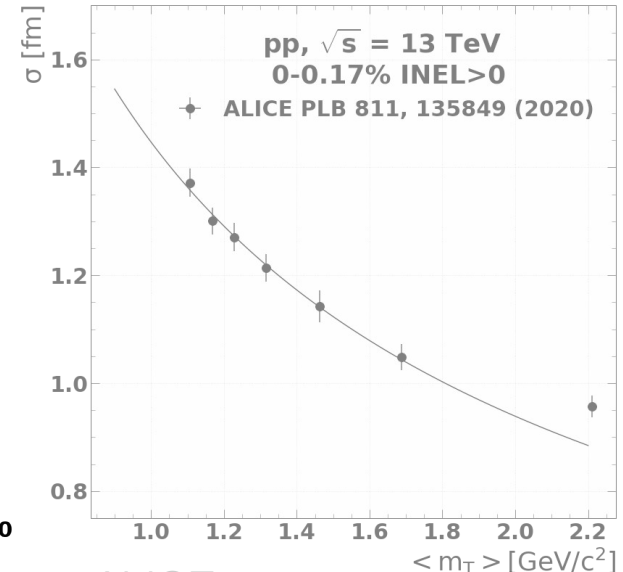
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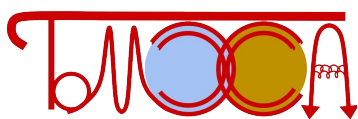


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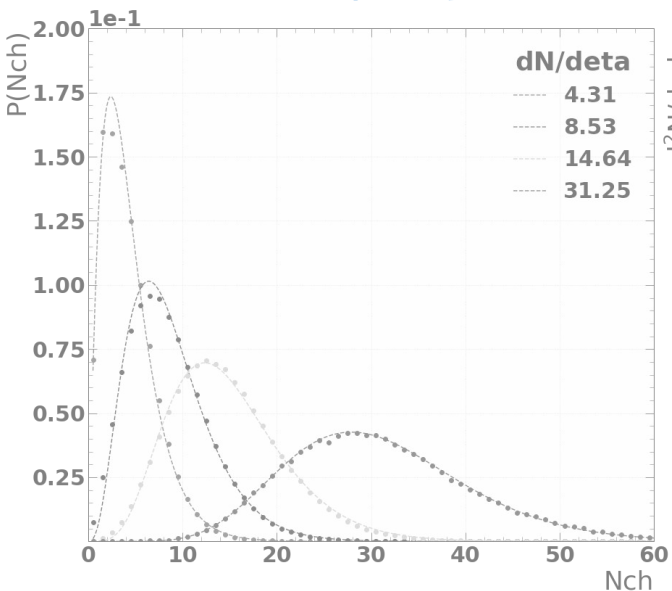
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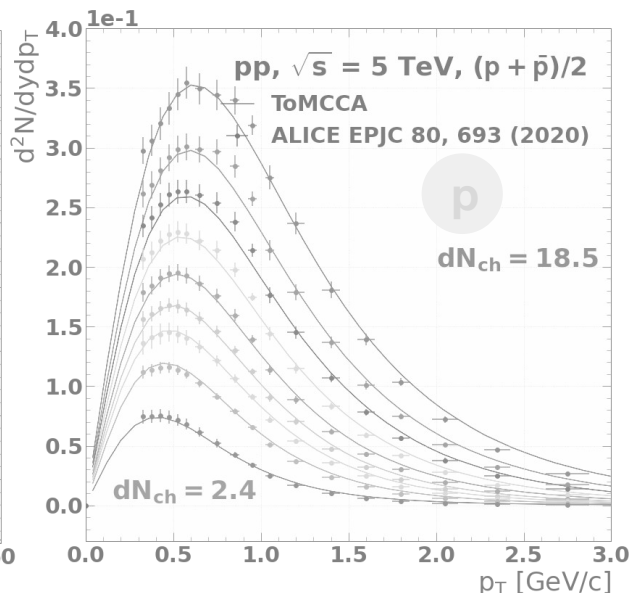
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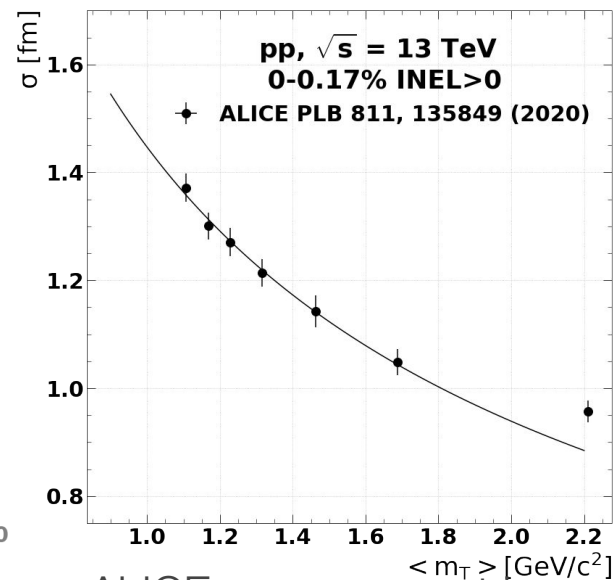
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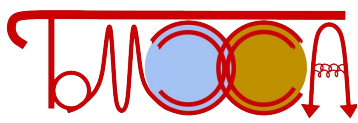


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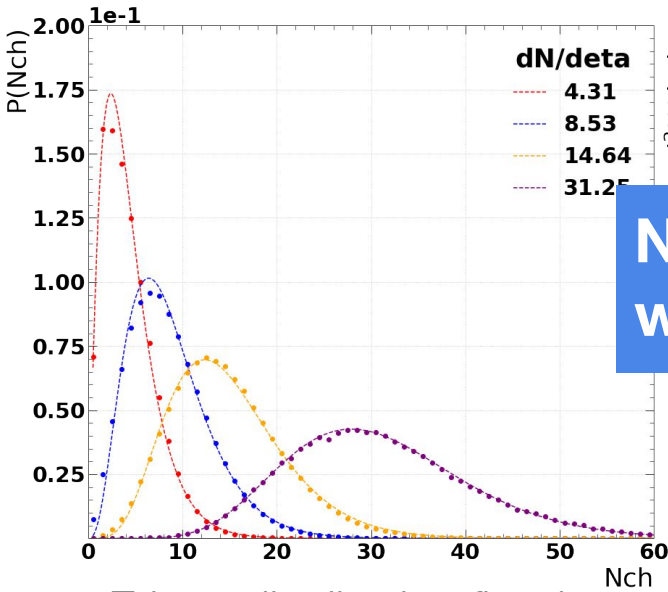
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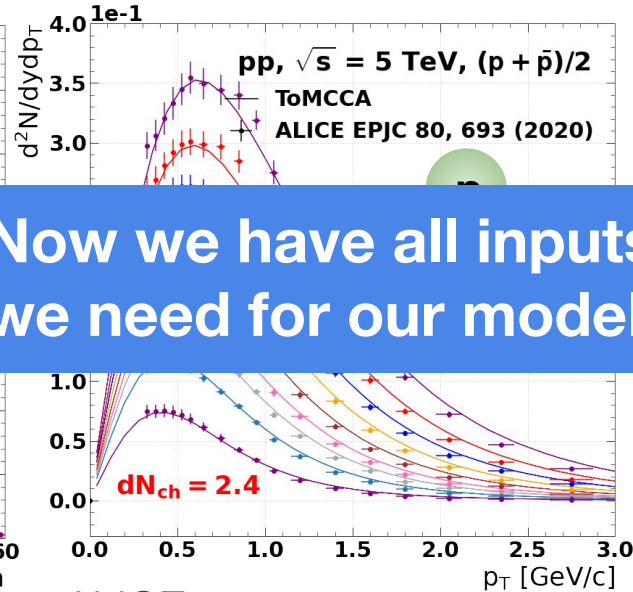
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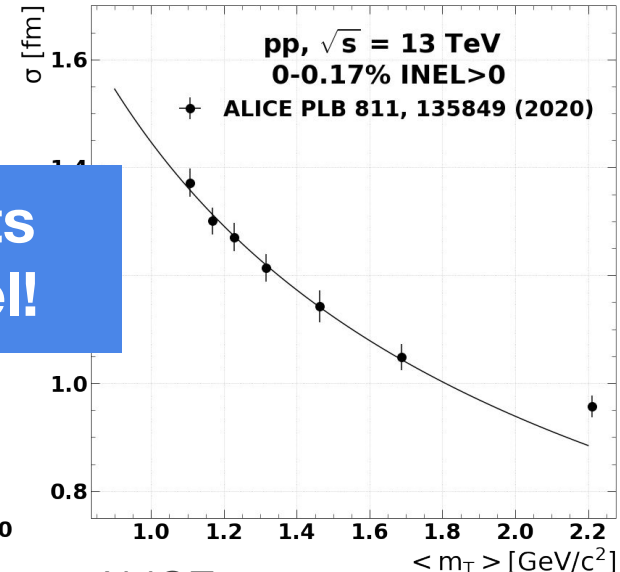
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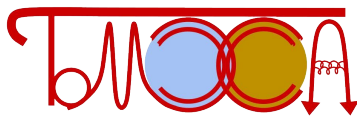
ALICE measurements over a large multiplicity range

Source size



ALICE measurement in high-multiplicity collisions

Now we have all inputs we need for our model!

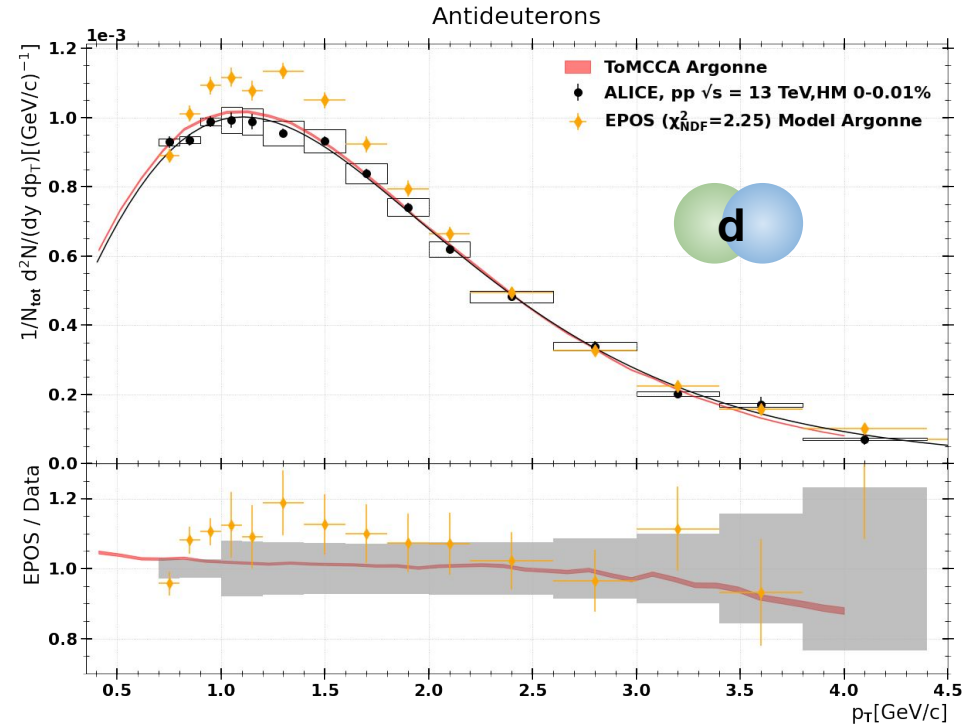


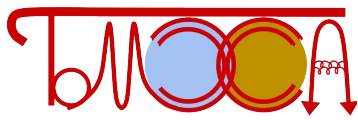
Deuteron Spectra

ToMCCA Model in HM pp Collisions



- Using ToMCCA for 13 TeV HM collisions ($(dN_{ch}/dn)_{|\eta|<0.8} \sim 31$) we can reproduce measured spectra
- No free parameters!





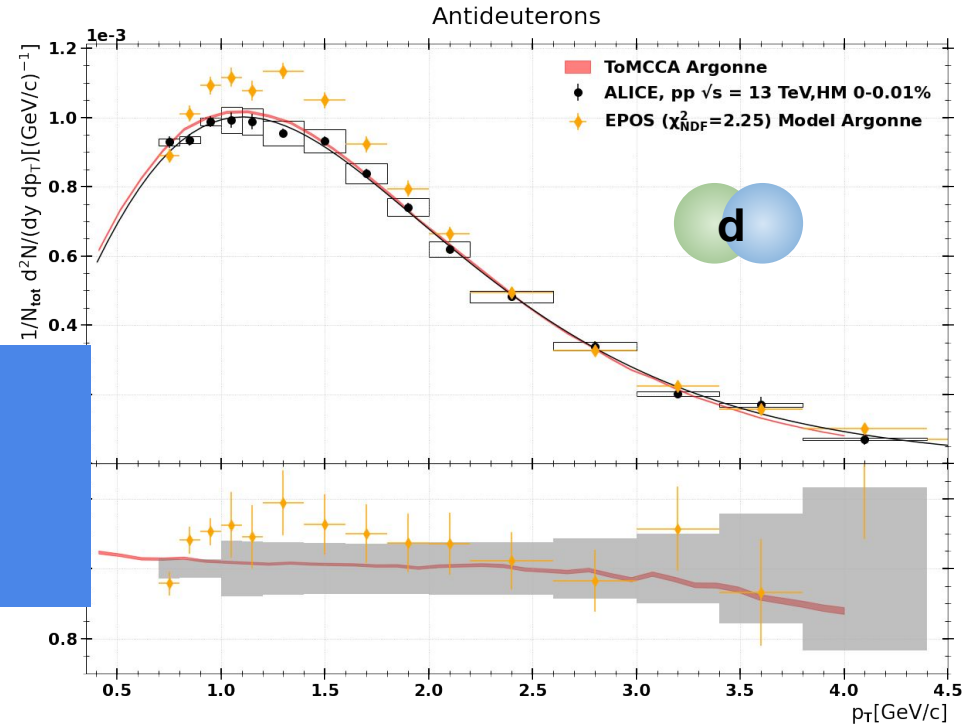
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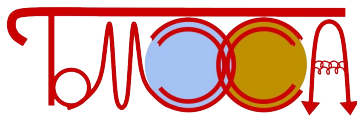
ToMCCA Model in HM pp Collisions



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Does this help us in predicting Cosmic Ray fluxes?



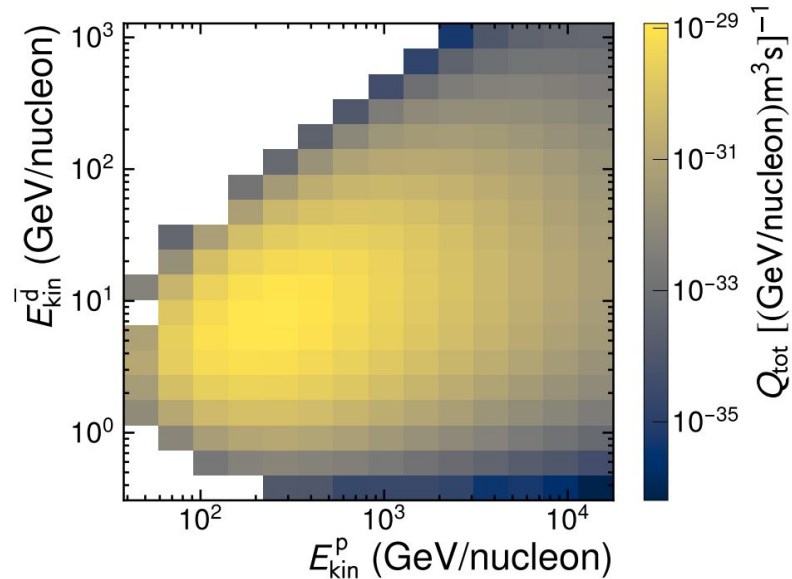


Cosmic Rays

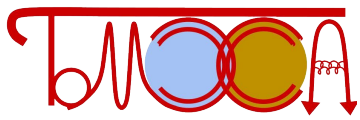
Production energy of antinuclei



- Antideuteron production predominantly for protons of $E_{\text{kin}} \sim 200\text{-}500$ GeV ($\sqrt{s} \sim \mathbf{19\text{-}30}$ GeV for p-H)



 Šerkšnytė, et al. PRD 105, 083021 (2022)



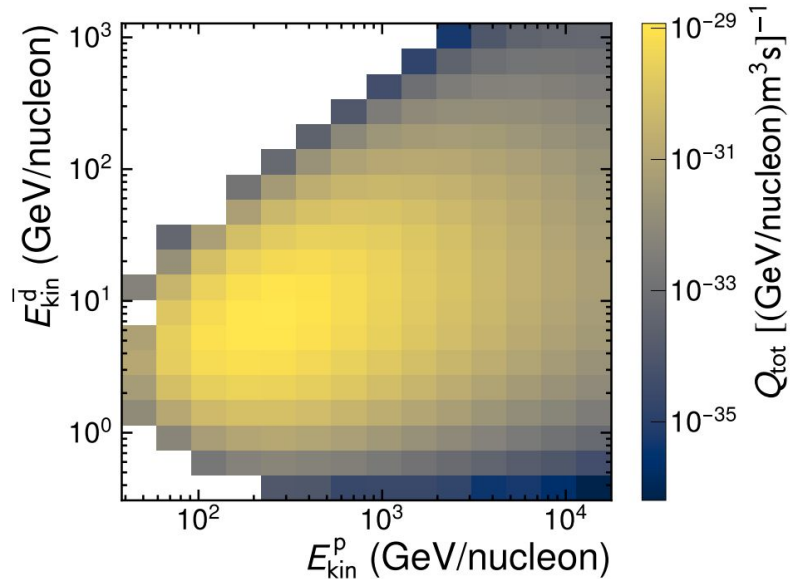
Cosmic Rays

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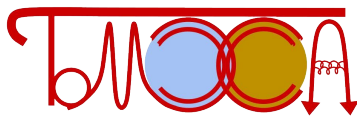


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- Extrapolation to lower energies via event multiplicity



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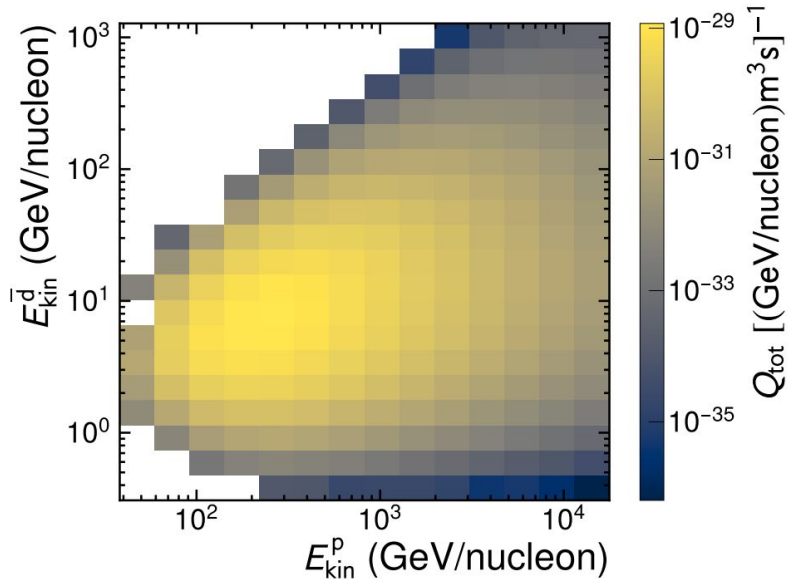
Cosmic Rays

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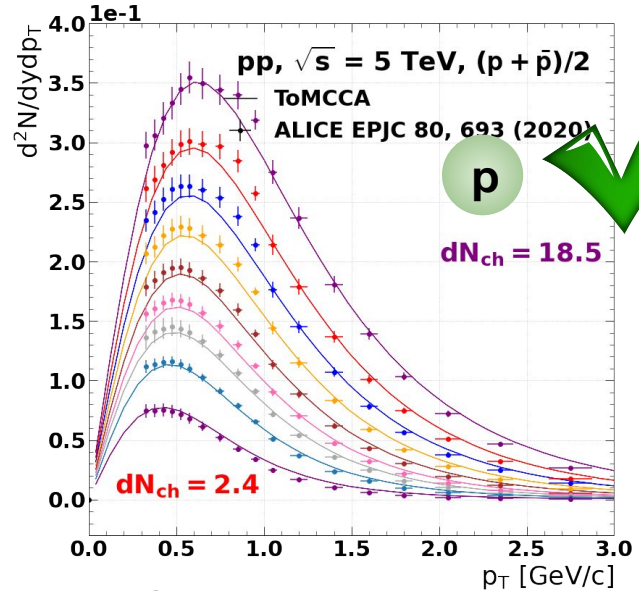
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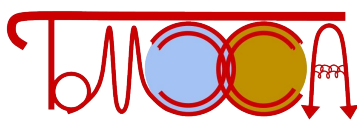


Šerkšnytė, et al. PRD 105, 083021 (2022)

Momentum distribution



ALICE measurements over a large range in multiplicity



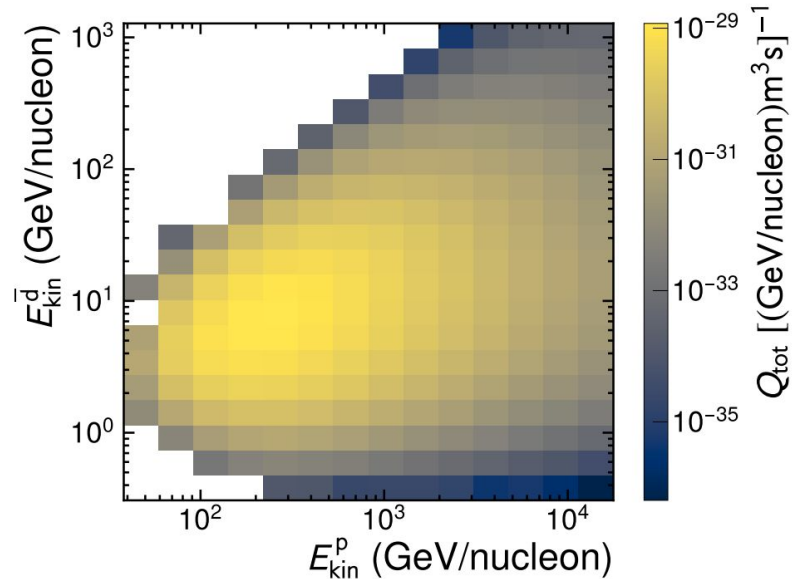
Cosmic Rays

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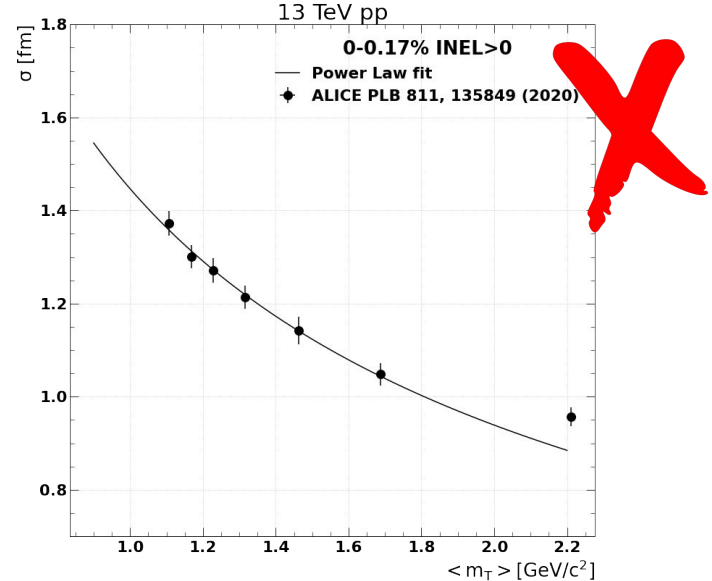
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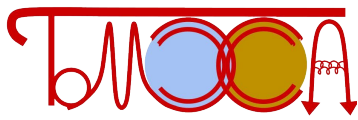


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Source size



ALICE measurement in high-multiplicity collisions

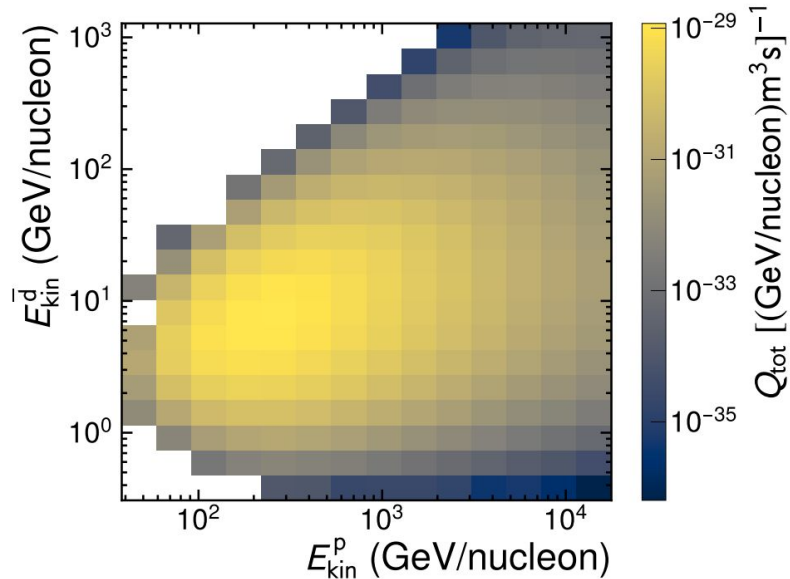


Cosmic Rays

Production energy of antinuclei



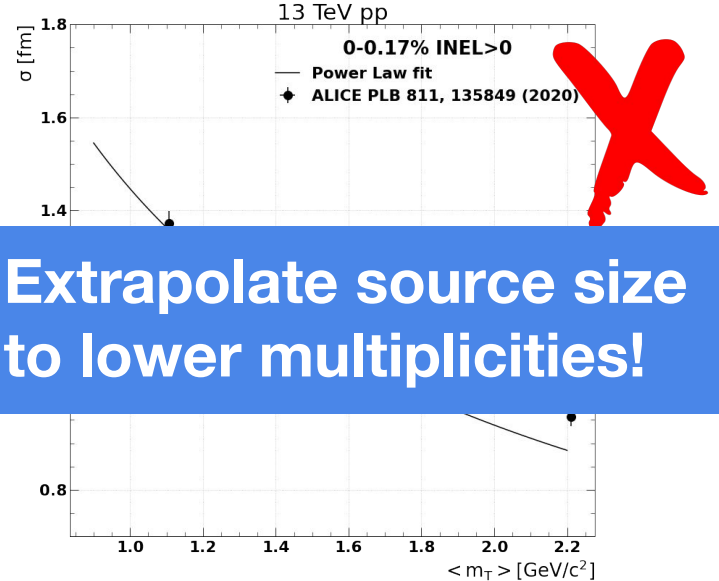
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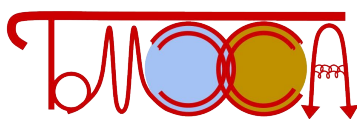
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Source size



Extrapolate source size to lower multiplicities!

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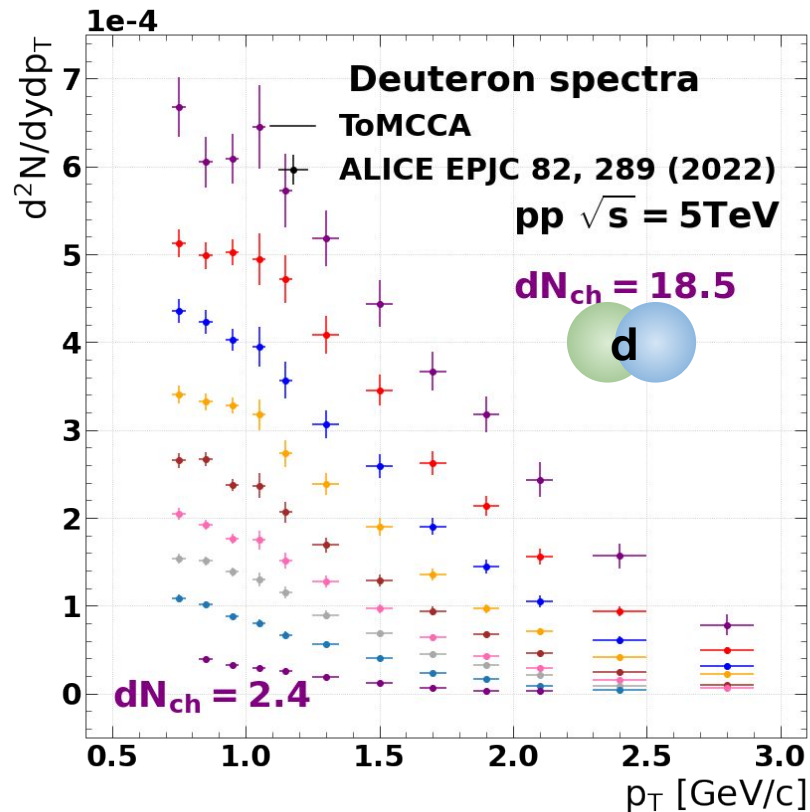


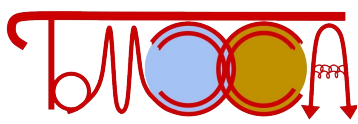
Extrapolating the Source

Using ToMCCA as a fitting tool



- Deuterons were also measured by ALICE Collab. for different multiplicities
- Fit source size and scaling with m_T to measured data
- Cross check at different energies



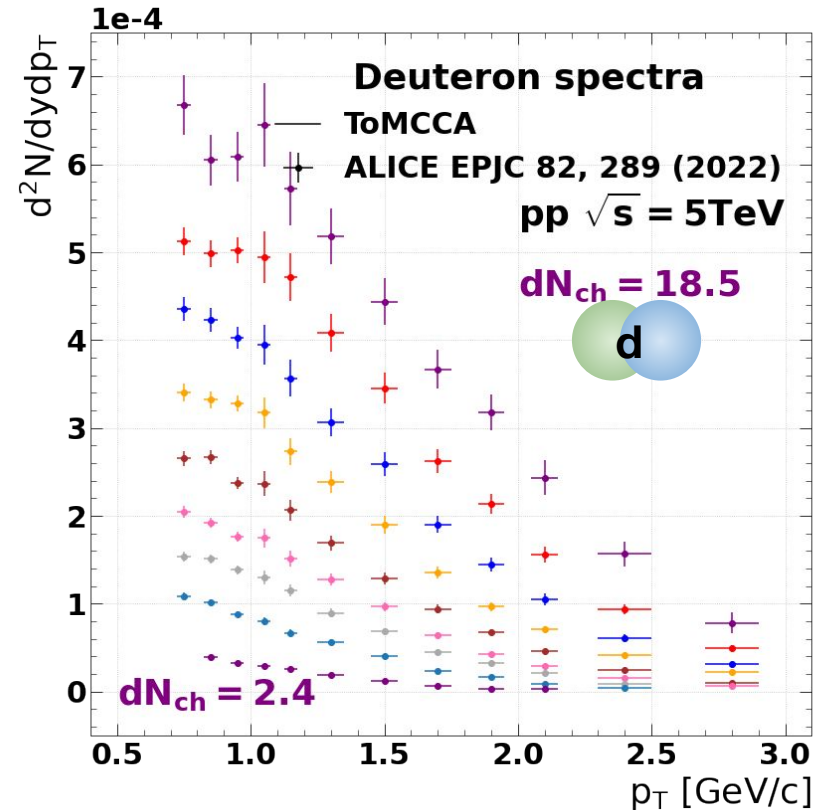
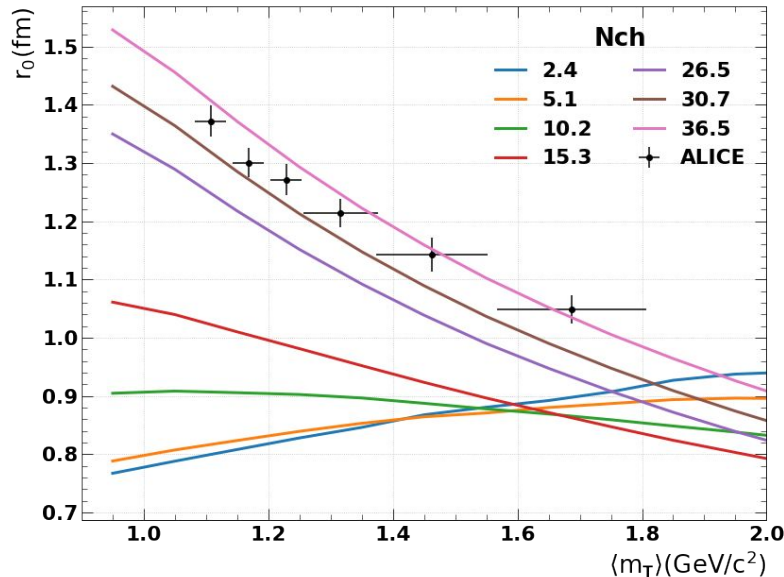


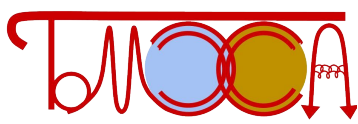
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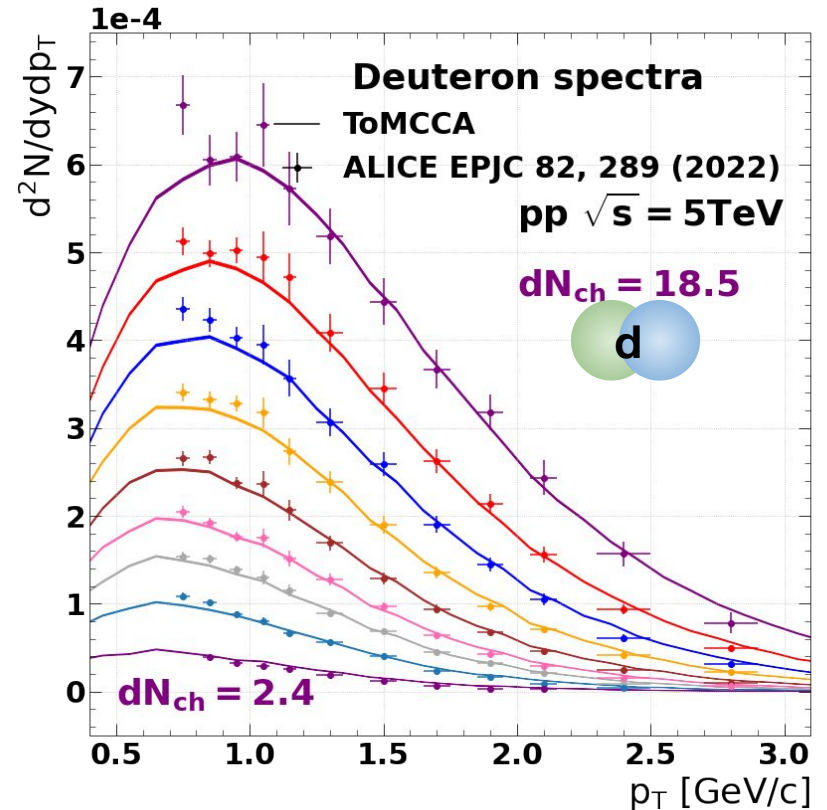
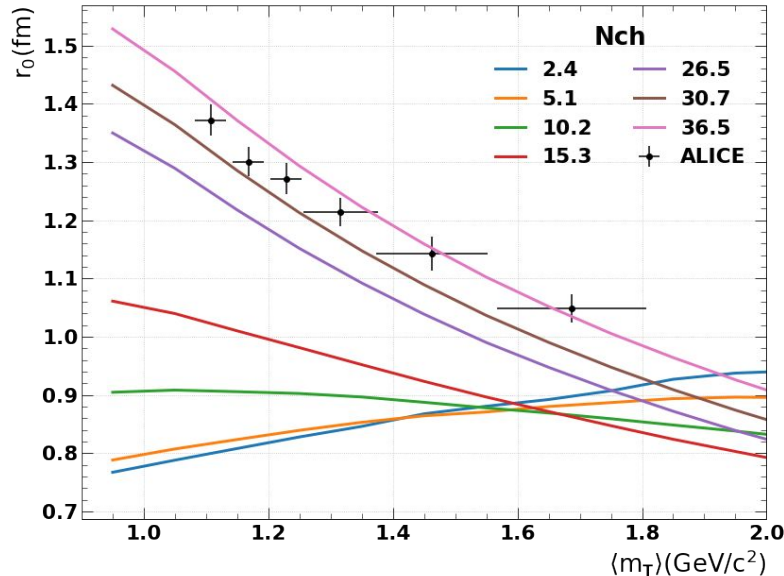


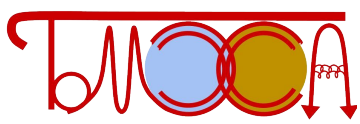
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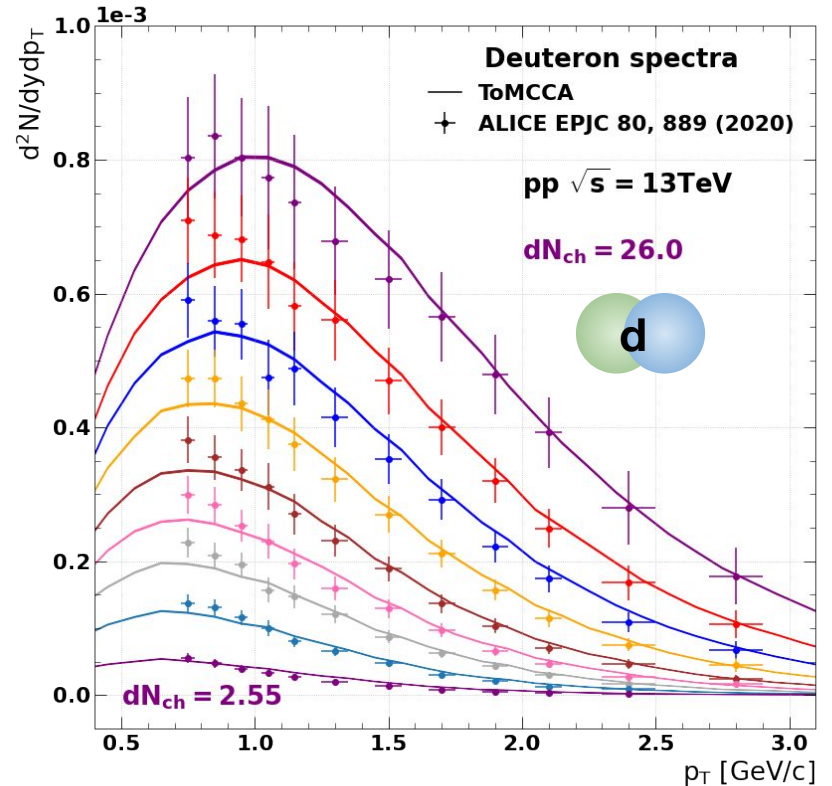
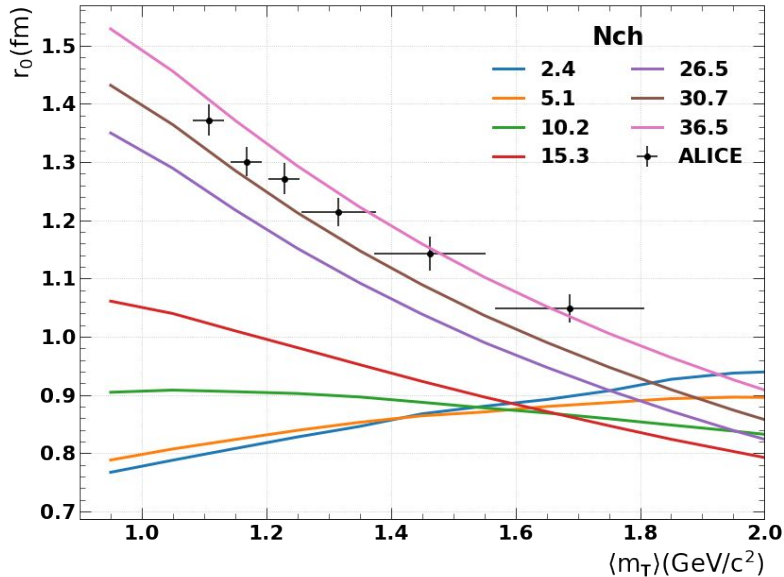


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Using ToMCCA as a fitting tool



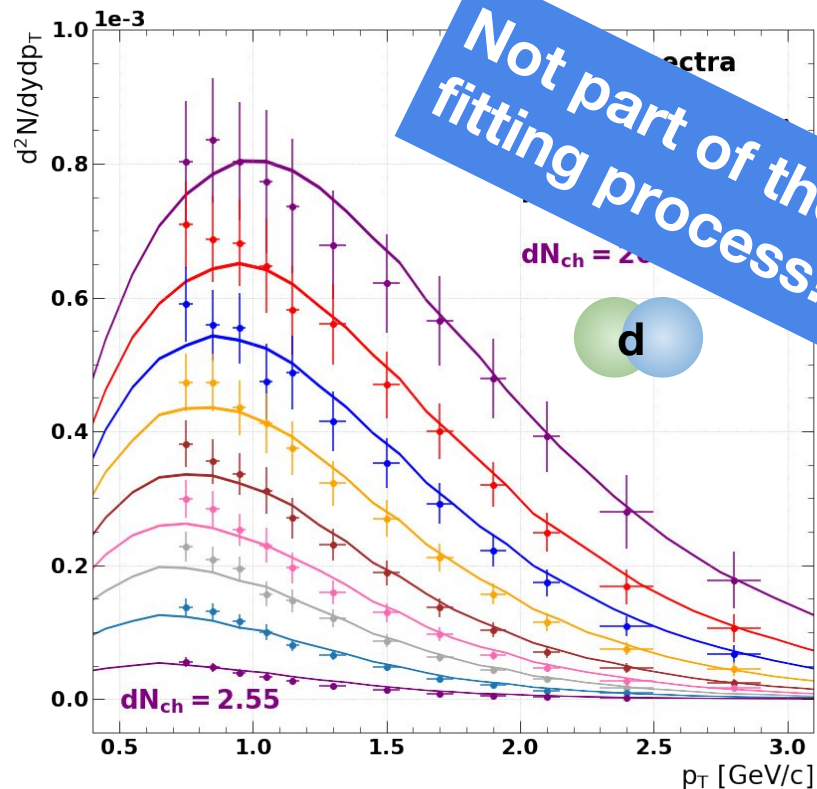
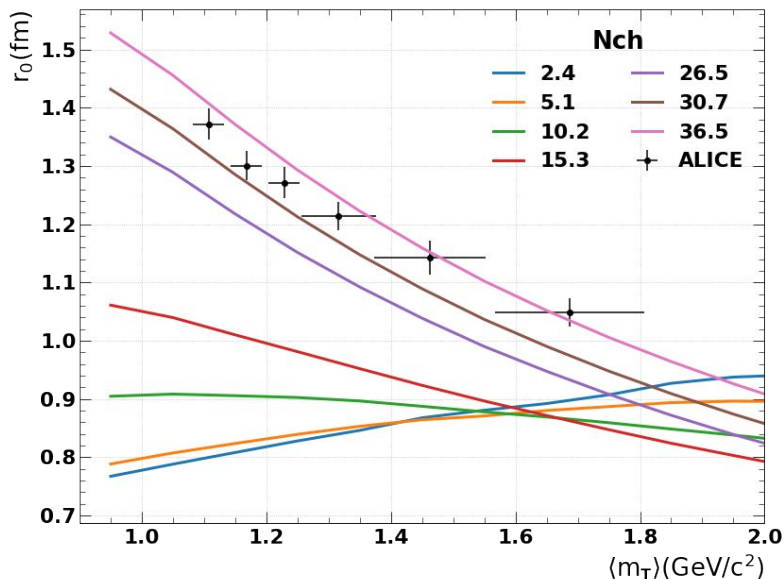
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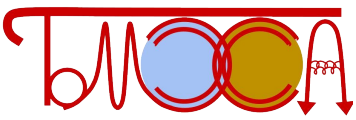


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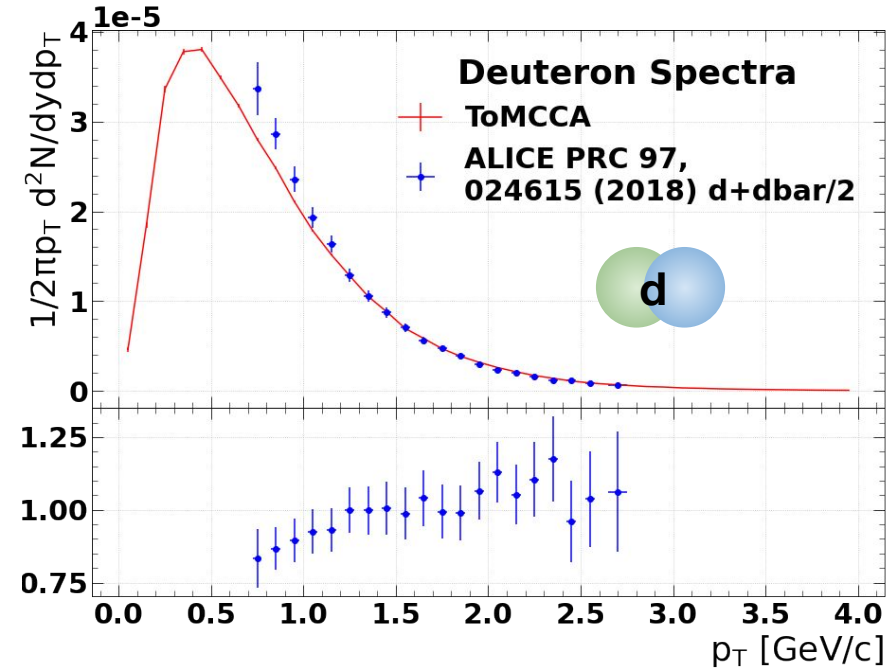


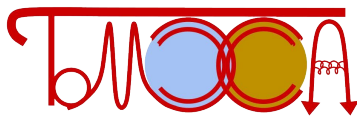
Deuteron results

Minimum bias 7 TeV



- Deuterons were also measured by ALICE Collab. for different multiplicities
- Fit source size and scaling with m_T to measured data
- Cross check at different energies
- Minimum Bias works well



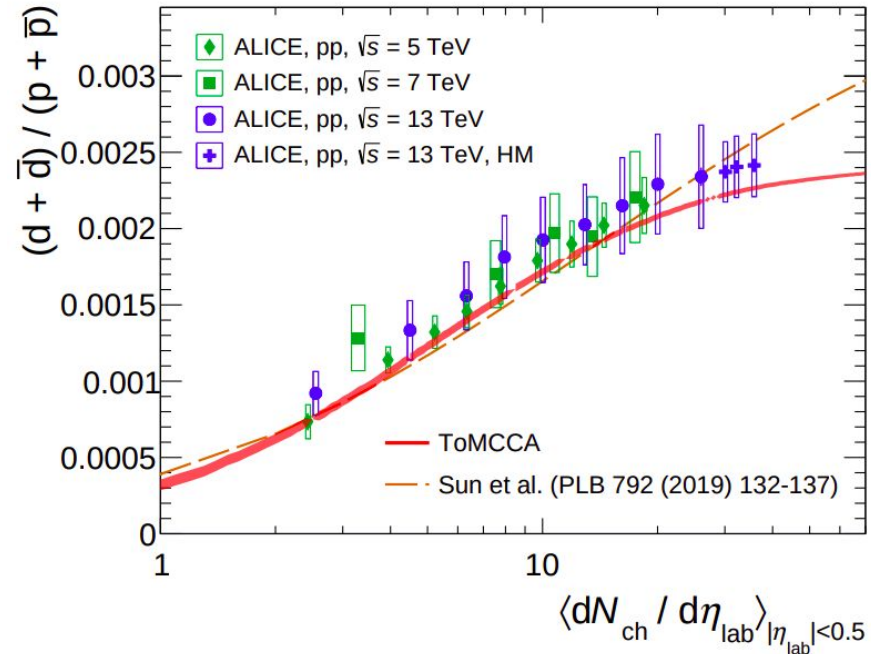


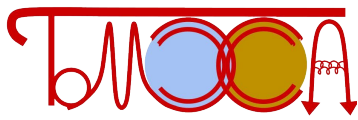
Deuteron results

d/p ratio



- Deuterons were also measured by ALICE Collab. for different multiplicities
- Fit source size and scaling with m_T to measured data
- Cross check at different energies
- Minimum Bias works well
- d/p ratio reproduces data well, tension to previous predictions at high multiplicity





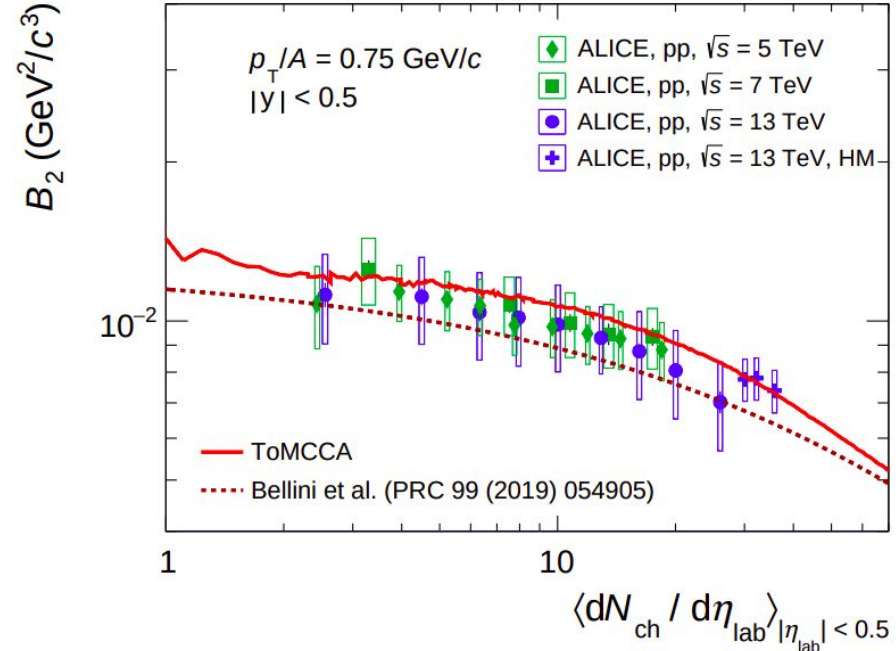
Deuteron results

B_2 parameter



- Deuterons were also measured by ALICE Collab. for different multiplicities
- Fit source size and scaling with m_T to measured data
- Cross check at different energies
- Minimum Bias works well
- d/p ratio reproduces data well, tension to previous predictions at high multiplicity
- B_2 also reproduced well

$$B_A(p_T^p) = E_A \frac{d^3 N_A}{dp_A^3} \Big/ \left(E_p \frac{d^3 N_p}{dp_p^3} \right)^A$$



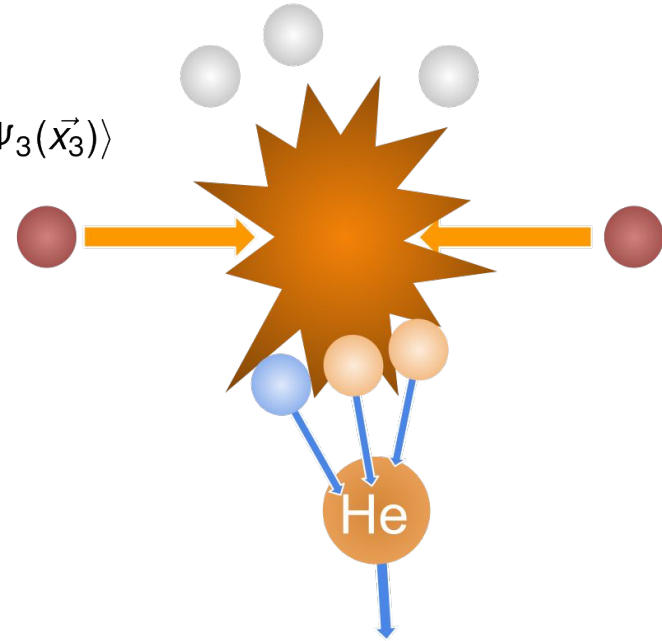
Add 3rd particle to basic formalism

$$\frac{dN_{He}}{d^3P} = S_{He} \int d^3x_1 \int d^3x_2 \int d^3x_3 \int d^3x'_1 \int d^3x'_2 \int d^3x'_3$$

$$\times \Psi_{He}^* (\vec{x}'_1, \vec{x}'_2, \vec{x}'_3) \Psi_{He} (\vec{x}_1, \vec{x}_2, \vec{x}_3) \langle \Psi_3^\dagger(\vec{x}'_3) \Psi_2^\dagger(\vec{x}'_2) \Psi_1^\dagger(\vec{x}'_1) \Psi_1(\vec{x}_1) \Psi_2(\vec{x}_2) \Psi_3(\vec{x}_3) \rangle$$

Similarly the probability can be expressed as

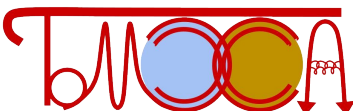
$$\mathcal{P}(k_1, q_1, \sigma, b) = \frac{S_{He}}{(2\pi)^3 2^9 \sigma^6} \int d^3r_1 d^3r_2 \mathcal{D}(\vec{q}_1, \vec{k}_1, \vec{r}_1, \vec{r}_2) e^{-\frac{r_1^2 + r_2^2}{4\sigma^2}}$$



Extension to A=3

Helium-3

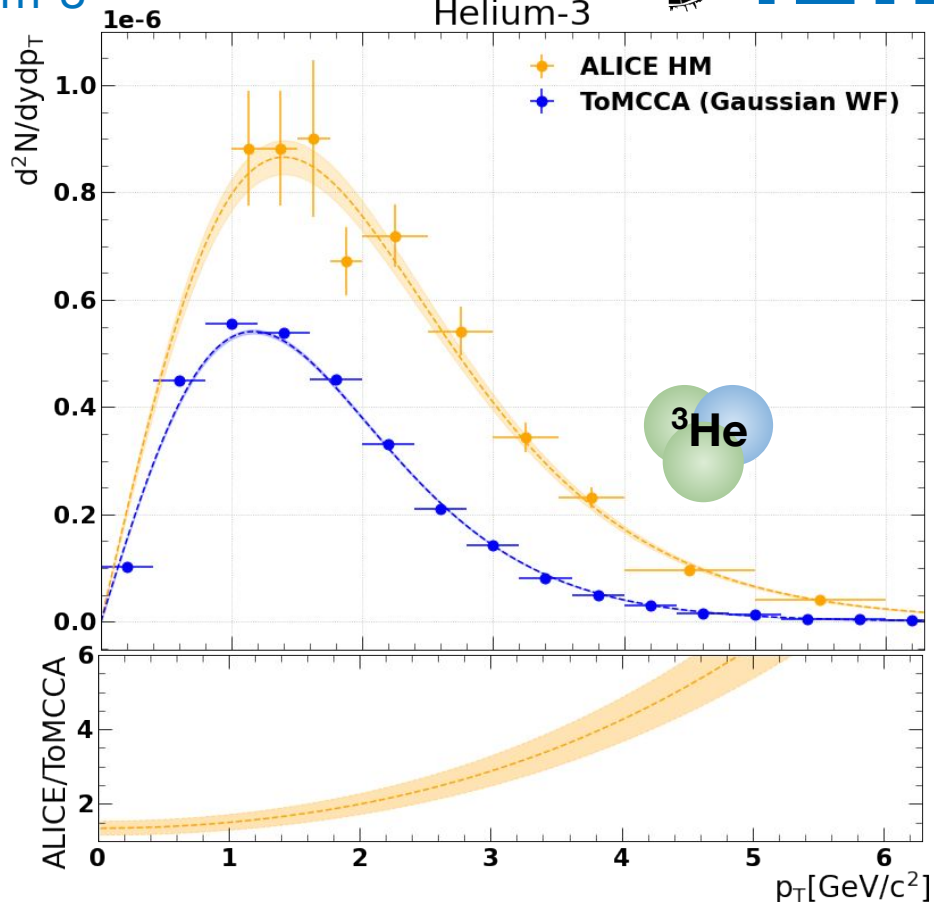
Helium-3



Extension to A=3 coalescence

- Use 2-body source size
 - Assign every pair a distance
 - Geometric mean of distance for coalescence probability
- For now only Gaussian wave function:
 - Yield *~50% lower* than data
 - Shape at large p_T deviates

$$\mathcal{P}(k, q, \sigma) = \frac{S 64 b^6}{(b^2 + 2\sigma^2)^3} \exp[-b^2(k^2 + q^2)]$$



Extension to $A=3$

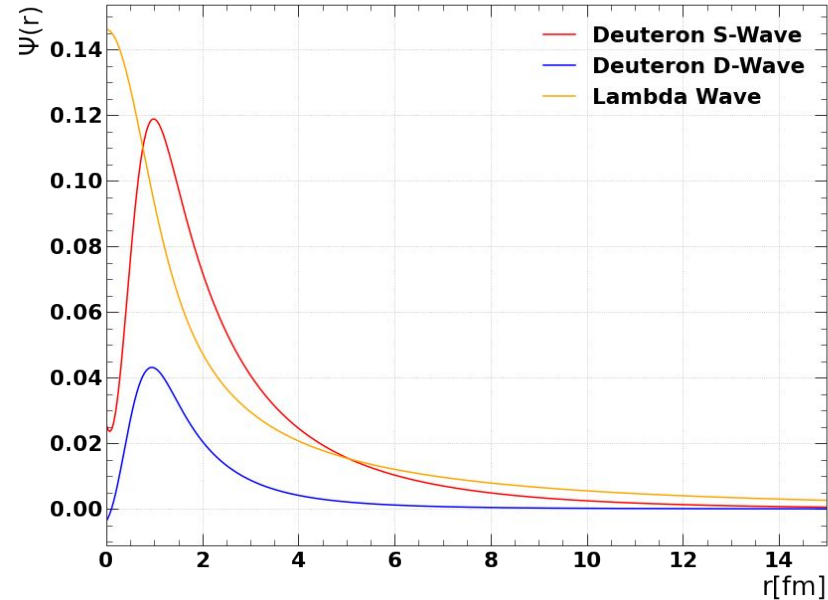
Hypertriton



- Congleton¹ wavefunction

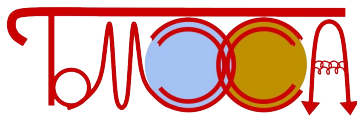
$$\psi_{\Lambda}(q) = N \frac{\exp[-(q/\Lambda)^2]}{q^2 + \alpha^2}$$

- Assumes factorization of Hypertriton wavefunction into deuteron+ Λ
- Scattering parameters retuned to latest Hypertriton formfactor calculations²



¹ J G Congleton 1992 J. Phys. G: Nucl. Part. Phys. 18 339

² F. Bellini et al.: Phys.Rev.C 103, 1 (2021)



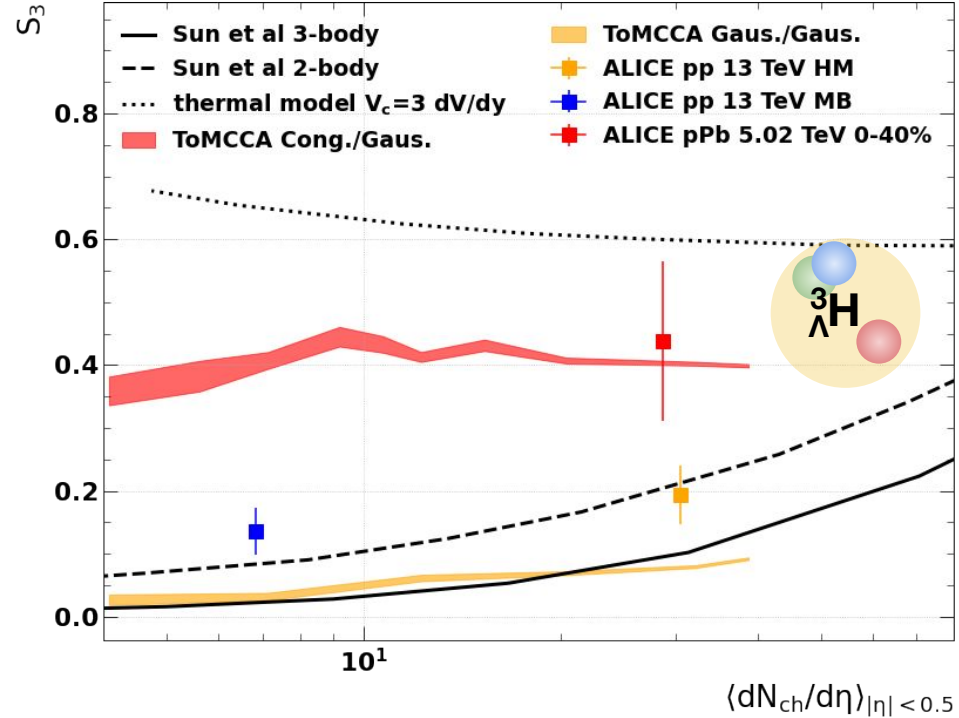
Extension to $A=3$

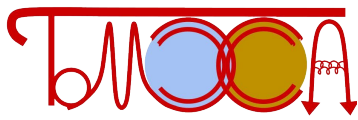
Hypertriton



- S_3 observable is expected to be very sensitive to production mechanism
- Using Gaussian for LH3 and He-3 gives comparable results to Sun et al.
- Using Congleton for LH3 overestimates S_3

$$S_3 = (\Lambda^3\text{H}/^3\text{He}) / (\Lambda/p)$$





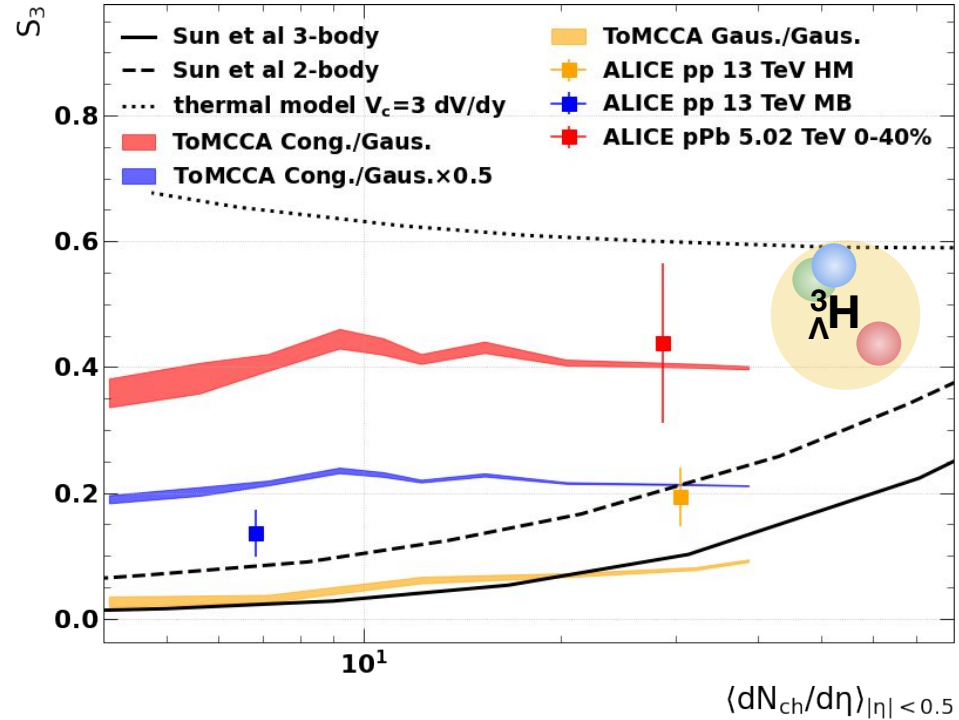
Extension to $A=3$

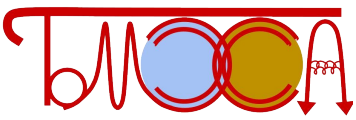
Hypertriton



- S_3 observable is expected to be very sensitive to production mechanism
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- Using Congleton for LH3 overestimates S_3
- He-3 yield is underestimated \rightarrow Scale by 0.5

$$S_3 = (\Lambda^3\text{H}/\Lambda^3\text{He}) / (\Lambda/p)$$



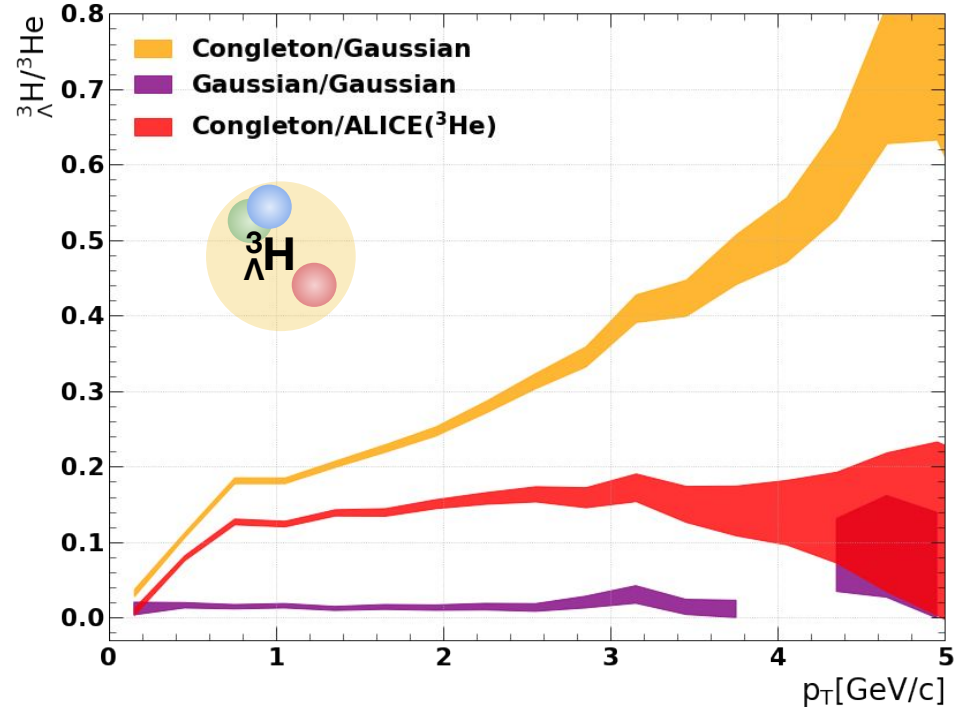


Extension to $A=3$

Hypertriton



- S_3 observable is expected to be very sensitive to production mechanism
- Using Gaussian for LH3 and He-3 gives comparable results to Sun et al.
- Using Congleton for LH3 overestimates S_3
- He-3 yield is underestimated \rightarrow Scale by 0.5
- ${}^3\text{H}/{}^3\text{He}$ Ratio shows increasing behaviour
- However: ${}^3\text{He}$ does not reproduce shape of measured spectra
- Flat behaviour when using measured ${}^3\text{He}$ spectra



Conclusion



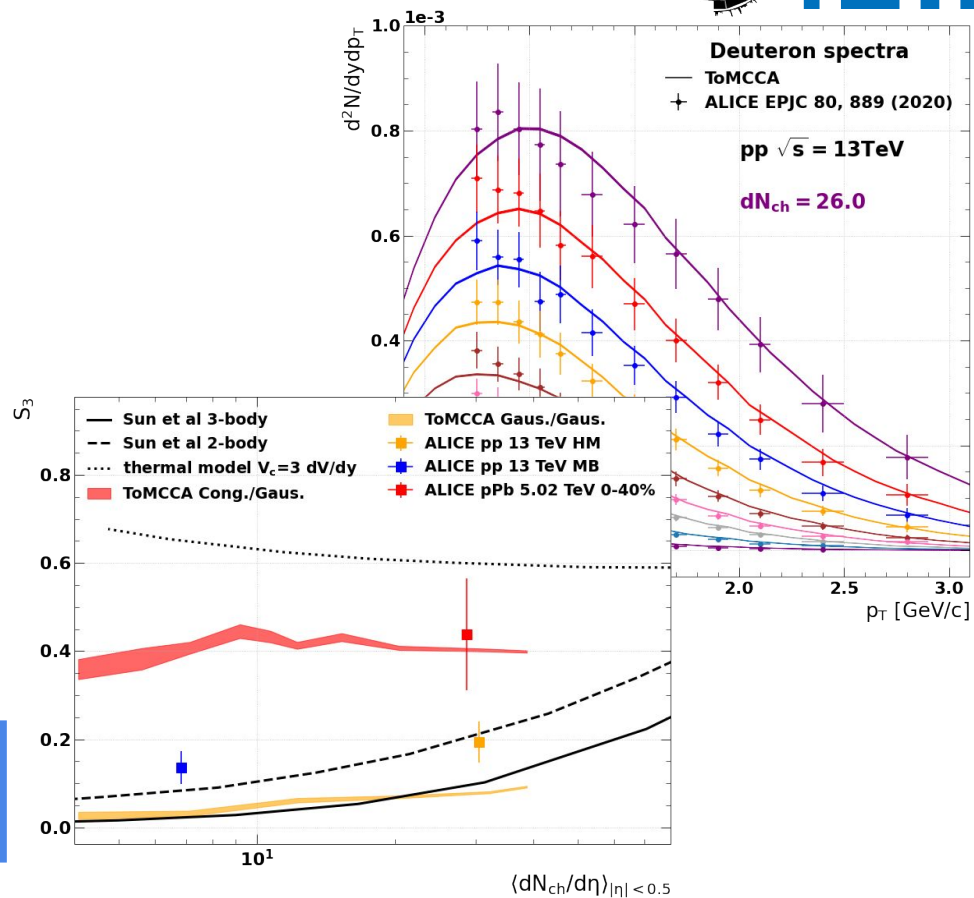
Deuterons:

- Coalescence model reproduces data with no free parameters
- Realistic wavefunction required
- ToMCCA allows for an extension to arbitrary multiplicities

A=3 Coalescence

- Successful extension of the model to A=3
- Nuclei and *Hyper*nuclei
- Realistic wavefunctions required

ToMCCA is available under:
<https://github.com/horstma/tomcca-public>



Conclusion

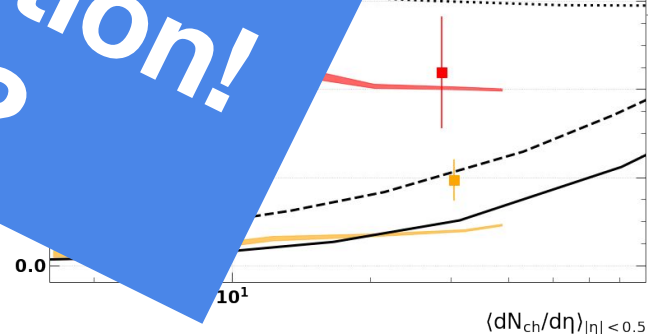
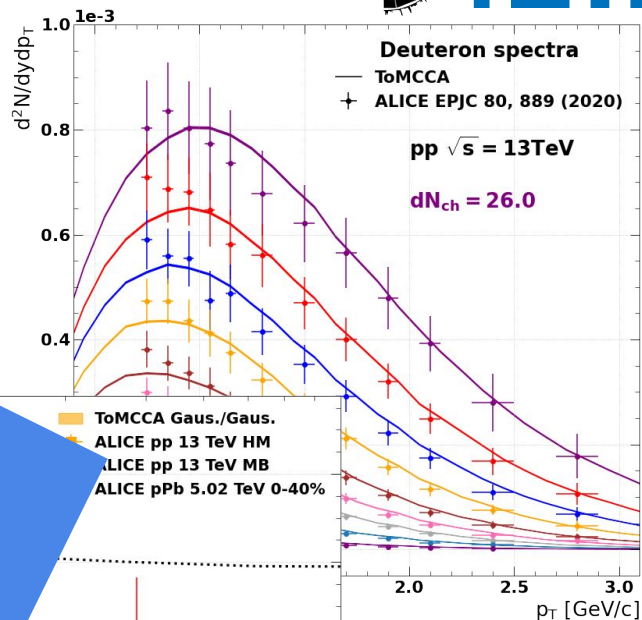


Deuterons:

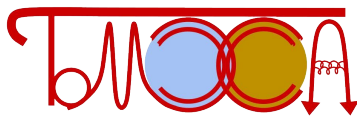
- Coalescence model describes data with no free parameters
 - Realistic wavefunctions
 - ToMCCA allows arbitrary multiplicity
- A=3 Coalescence
- Successful description of A=3
 - Nuclei and Hypernuclei
 - Realistic wavefunctions

Thanks for your attention!
Questions?

ToMCCA is available under:
<https://github.com/horstma/tomcca-public>



BACKUP

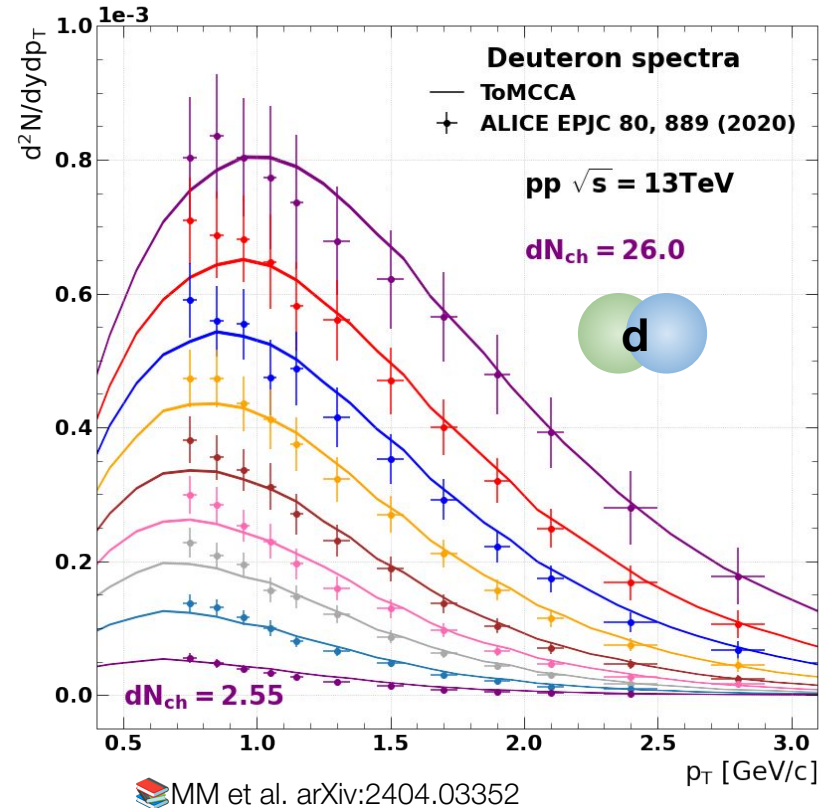


Conclusion

Deuteron production



- Understanding nuclei formation on earth can open a window to **indirect dark matter** searches
- **Wigner function formalism** can predict nuclei yields with no free parameters
- ToMCCA allows us to extrapolate to arbitrary multiplicities



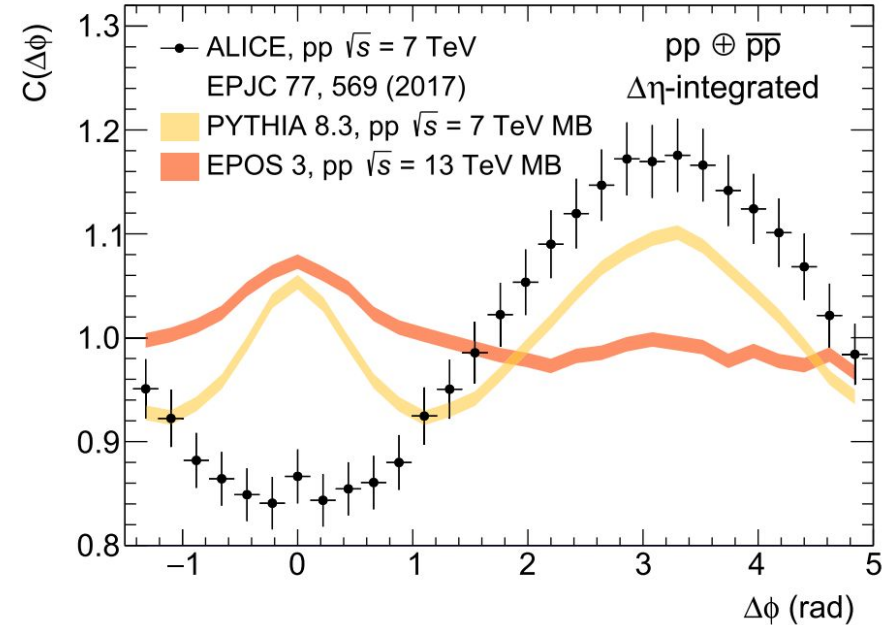
Coalescence Results EPOS

Angular correlations



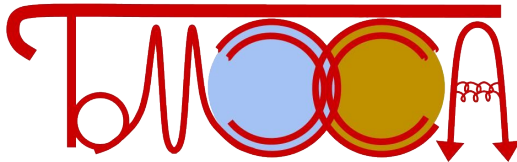
- $\Delta\phi$ of pp (pn) pairs
- Not reproduced by EPOS or Pythia
- No real control over these behaviours in general purpose event generators

MM et al .Eur.Phys.J.C 83 (2023) 9, 804



- $\Delta\phi$ of pp (pn) pairs
- Not reproduced by EPOS or Pythia
- No real control over these behaviours in general purpose event generators

Introducing:

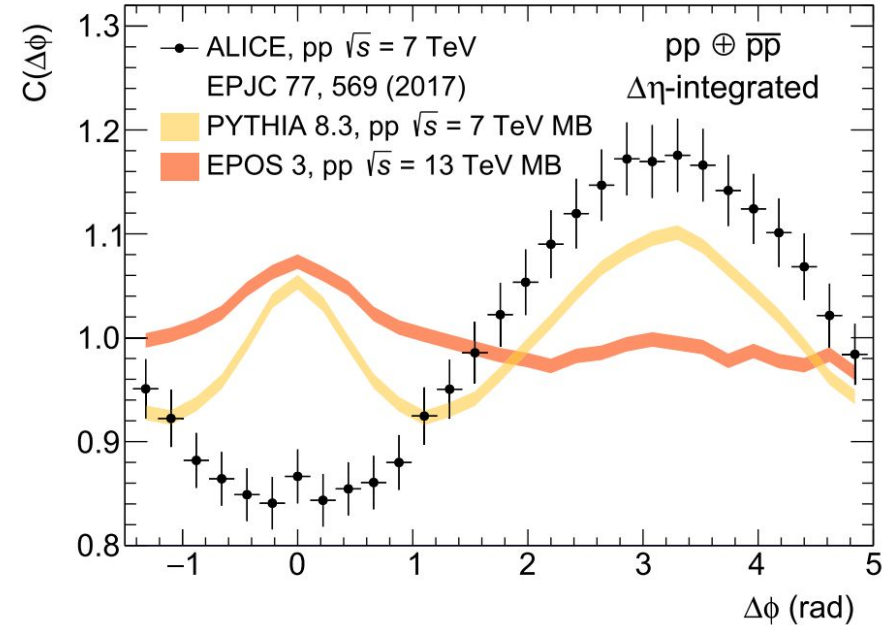


Toy Monte Carlo Coalescence

Afterburner

arXiv:2404.03352

MM et al .Eur.Phys.J.C 83 (2023) 9, 804



Comparison to previous predictions



- Important observable in accelerator measurements: \mathbf{B}_A

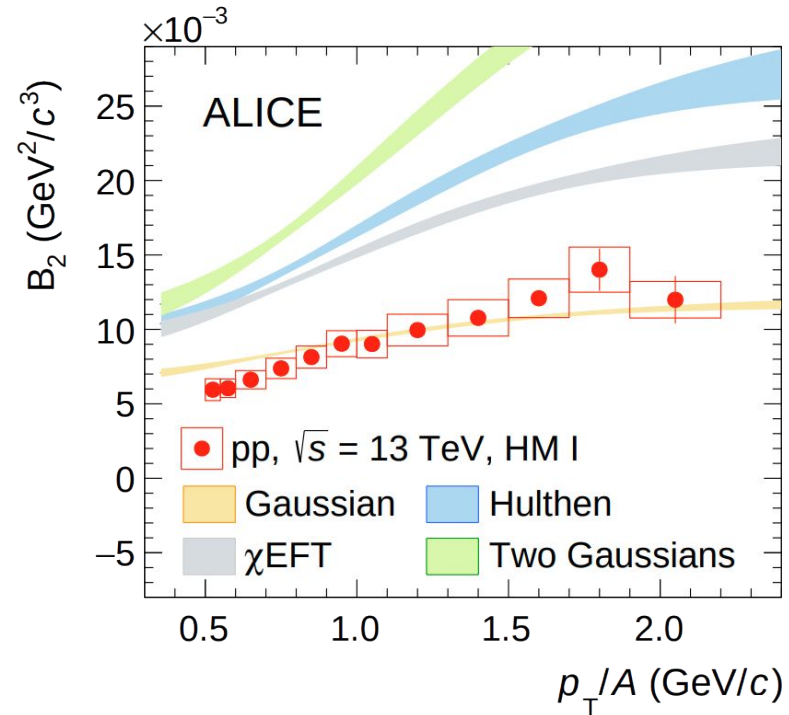
$$B_A(p_T^p) = E_A \frac{d^3 N_A}{dp_A^3} \bigg/ \left(E_p \frac{d^3 N_p}{dp_p^3} \right)^A$$

- Theoretical prediction [1]

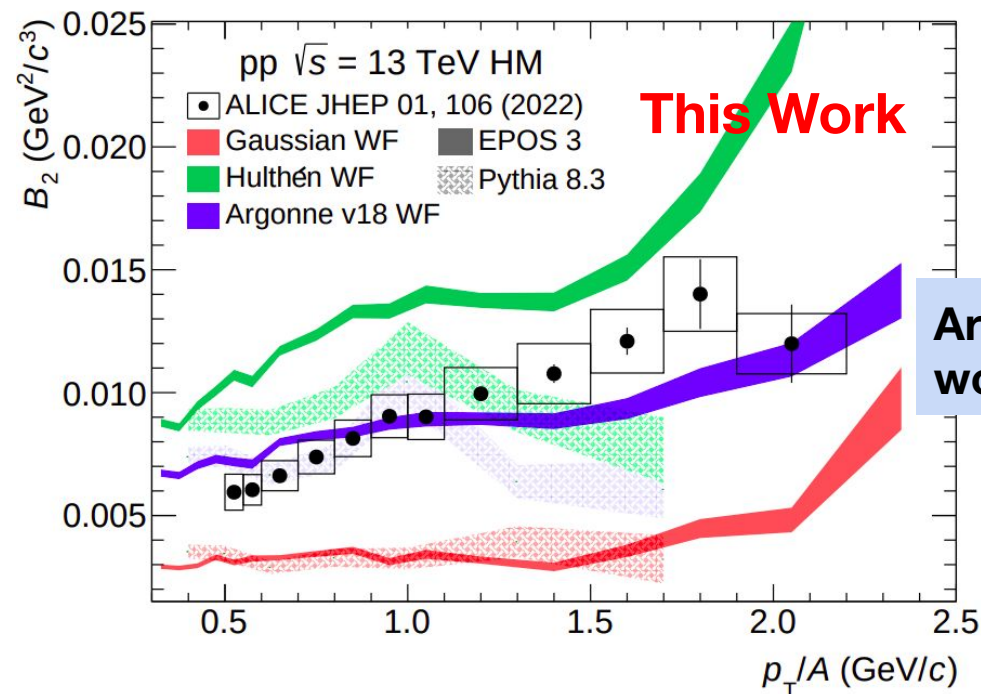
$$B_2(\vec{p}) \approx \frac{3}{2m} \int d^3 q D(\vec{q}) e^{-R^2(p_T) q^2}$$

$$D(\vec{q}) = \int d^3 r |\phi_d(\vec{r})|^2 e^{-i\vec{q}\cdot\vec{r}}$$

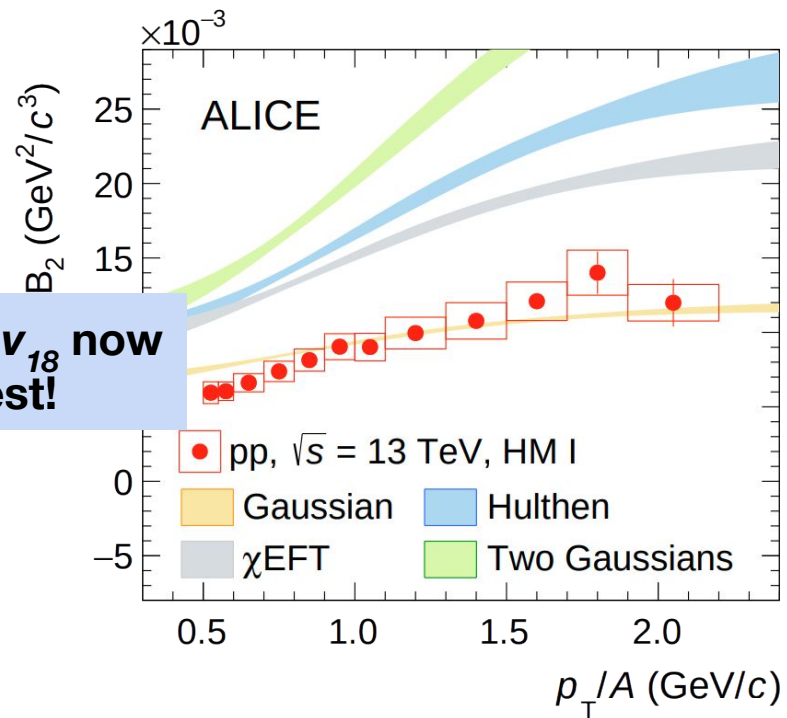
- This neglects momentum difference between Nucleons
- approximate to 10% in Pb–Pb, factor 2 in pp



[1] Blum, Takimoto, PRC 99 (2019) 044913



Argonne v_{18} now works best!

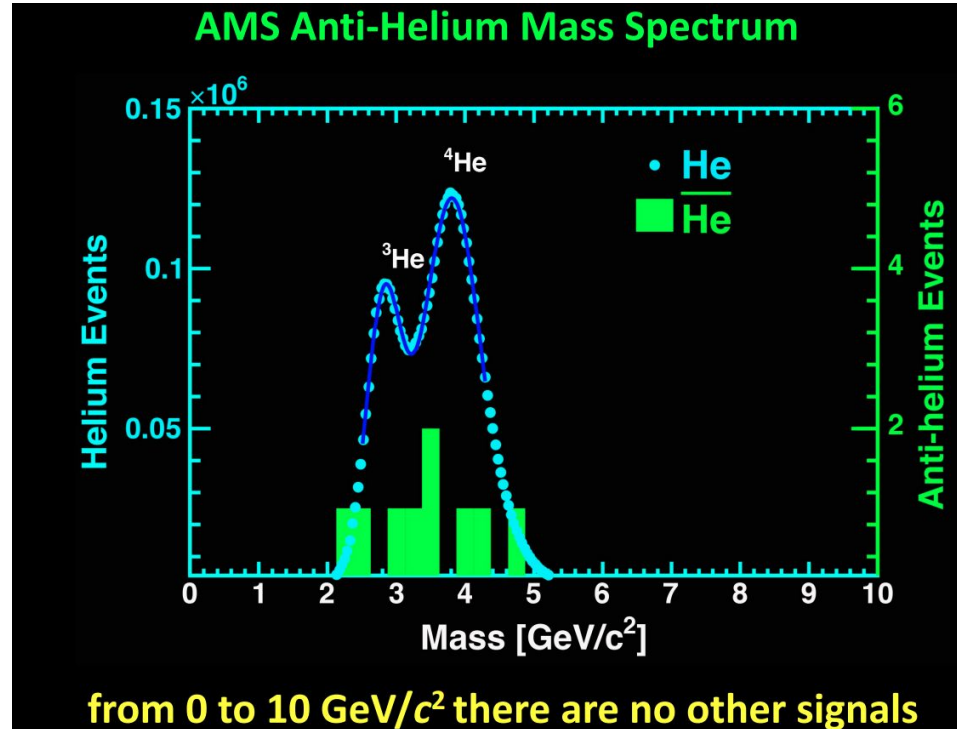


Cosmic Rays

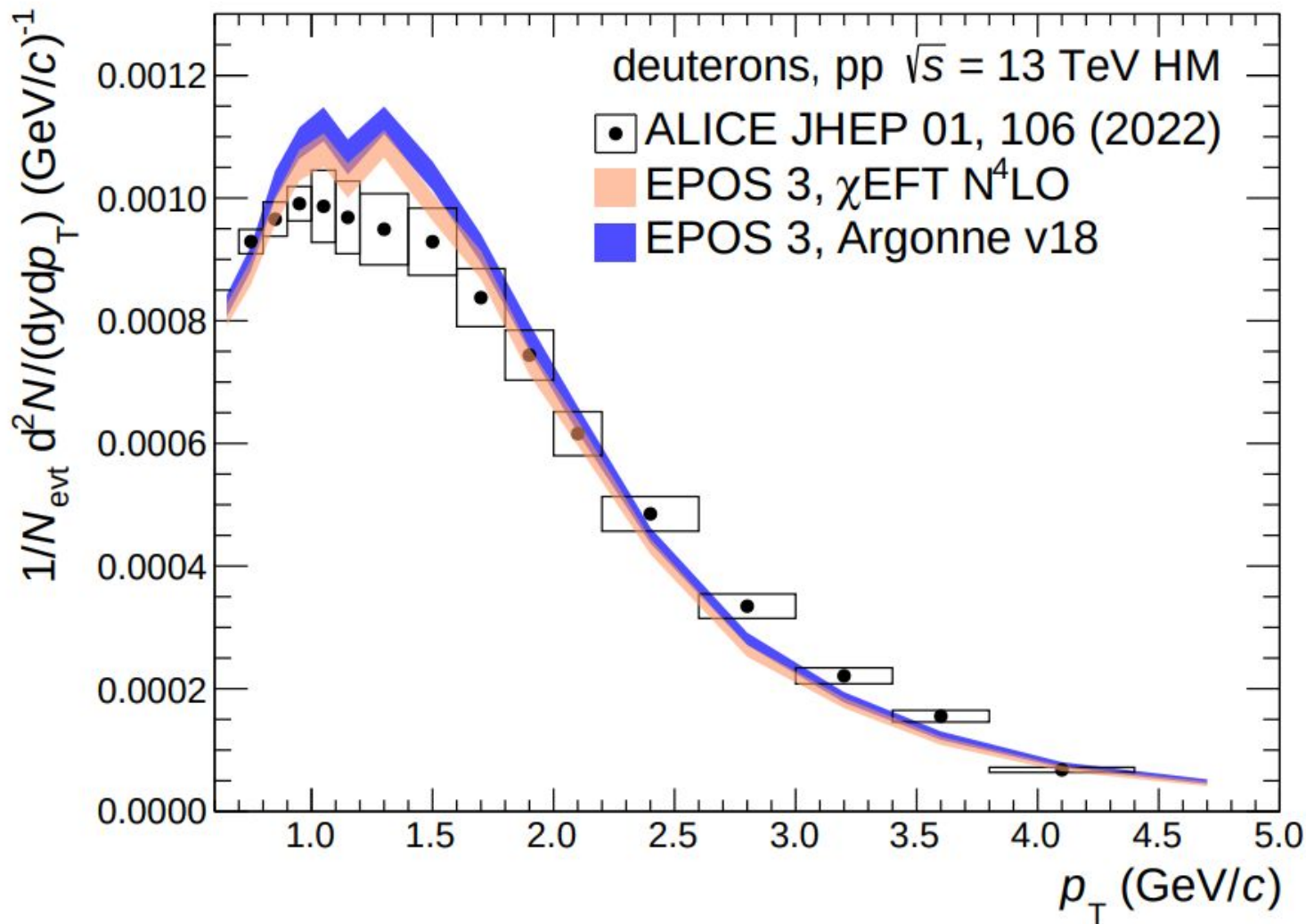
Antinuclei in Cosmic Rays?



- AMS-02 @ ISS has measured 9 antihelium candidates
- Not yet published
- What could be the origin of these antinuclei?



Pauolo Zuccon for AMS-02 Collaboration at MIAPP workshop 2022



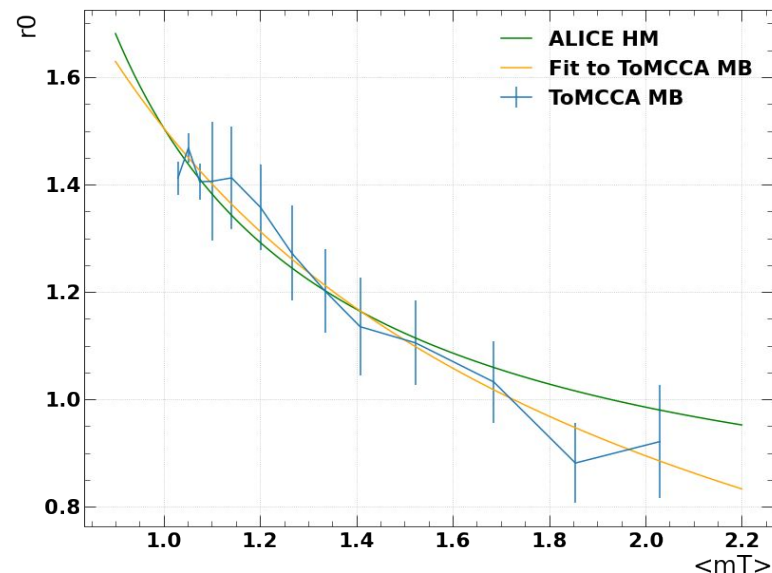
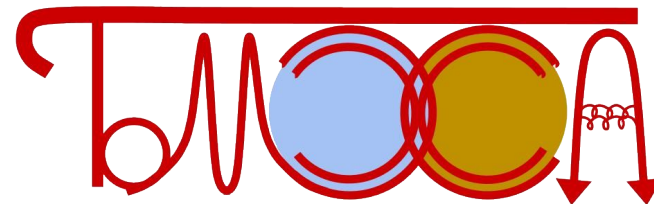
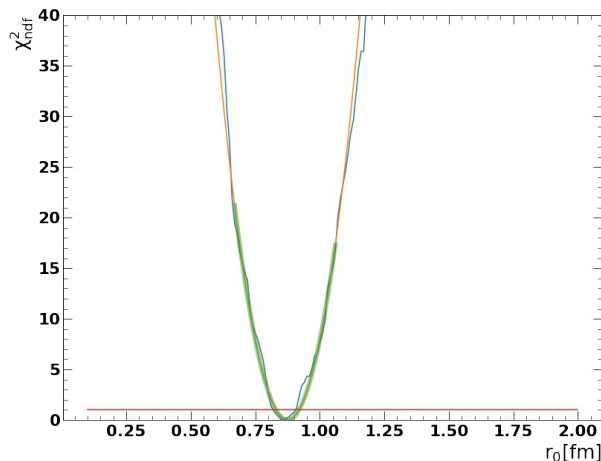
Next generation coalescence Model



Fitting the Source

Fitting Procedure:

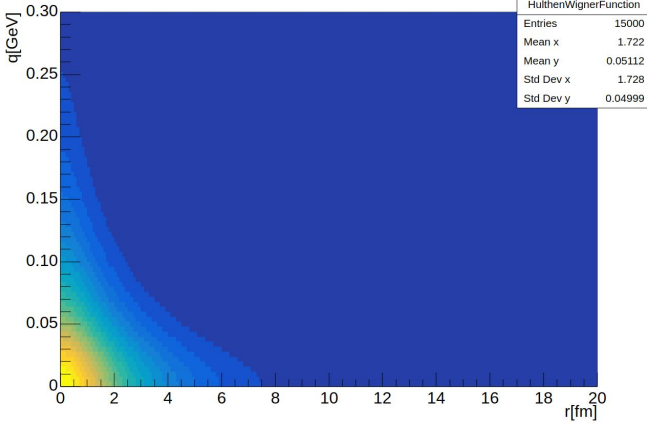
- Run ToMCCA with a fixed source size (e.g. 1.8 fm, flat in m_T)
- For the resulting deuteron spectra calculate the χ^2 for each bin and save it
- Reduce source size
- Repeat until source size is 0



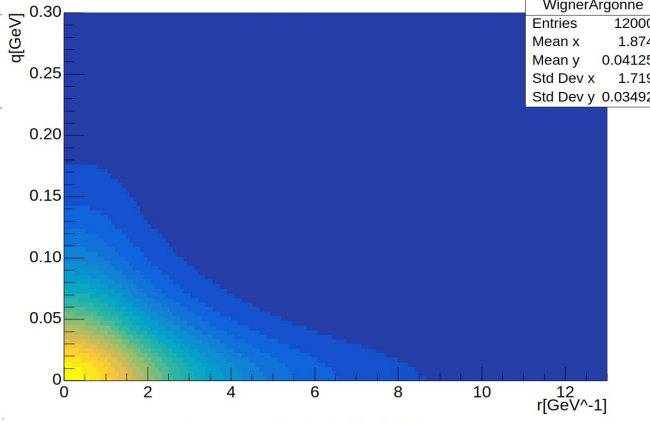
New Wigner functions/Probabilities



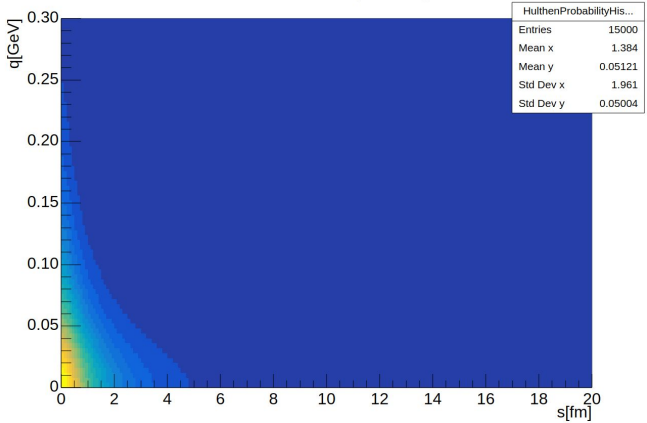
HulthenWignerFunction



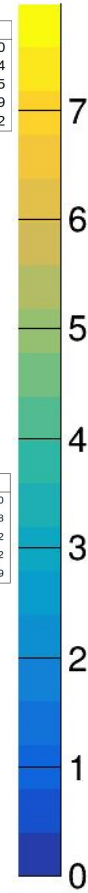
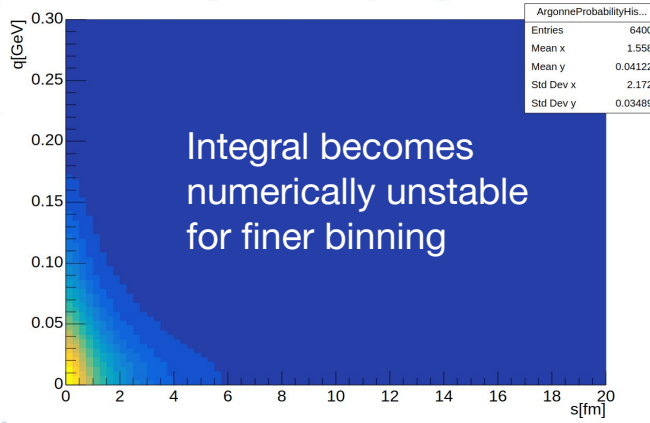
WignerArgonne



HulthenProbabilityHistogram



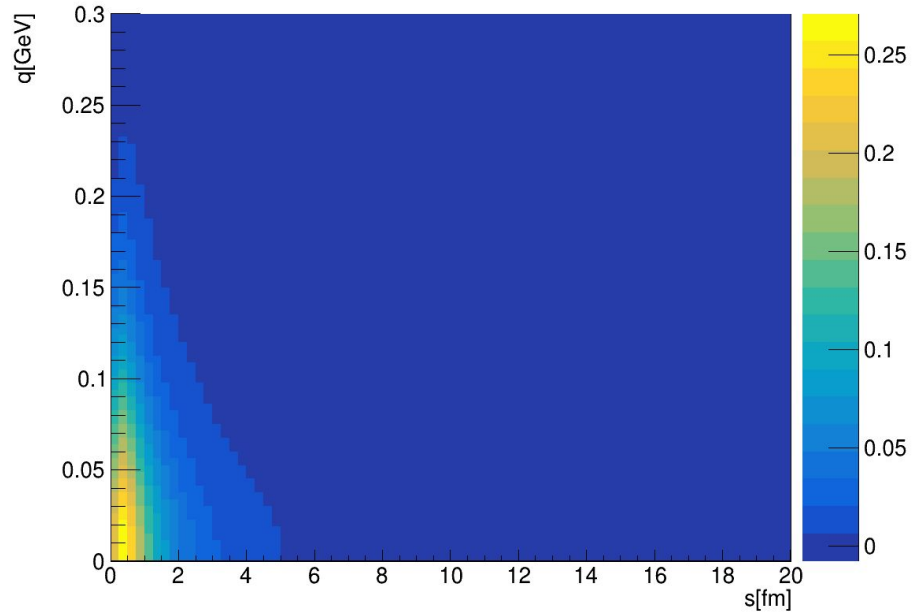
ArgonneProbabilityHistogram



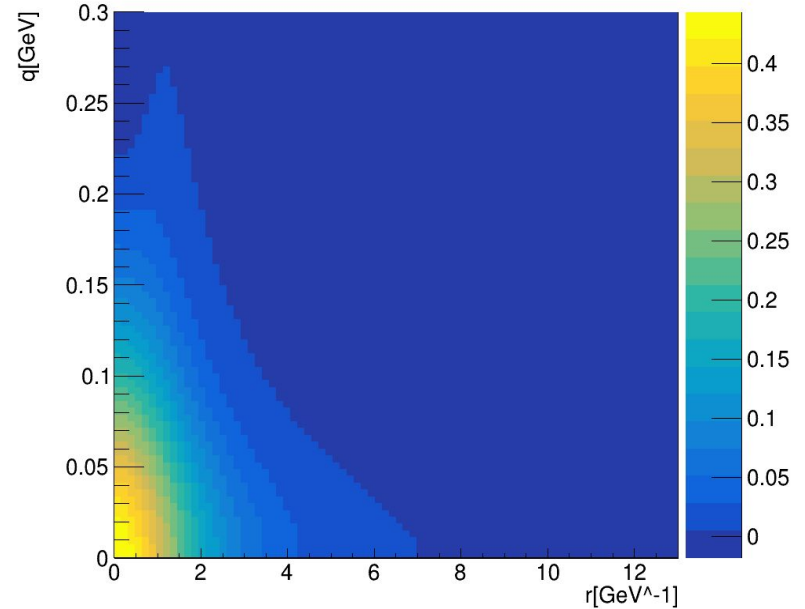
Argonne D-State probability



ArgonneProbabilityHistogramDWave



WignerArgonne_D_Wave



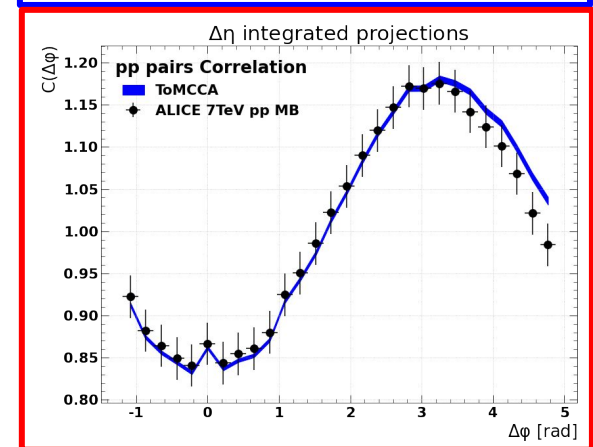
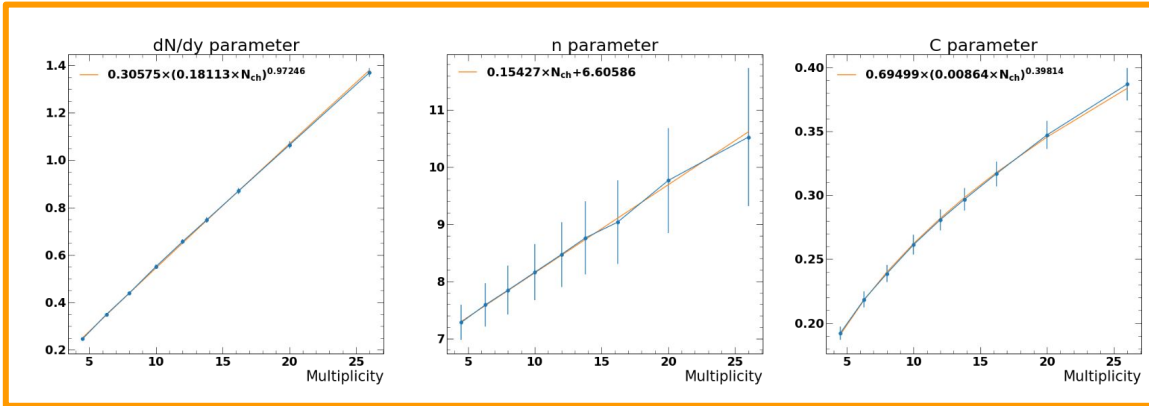
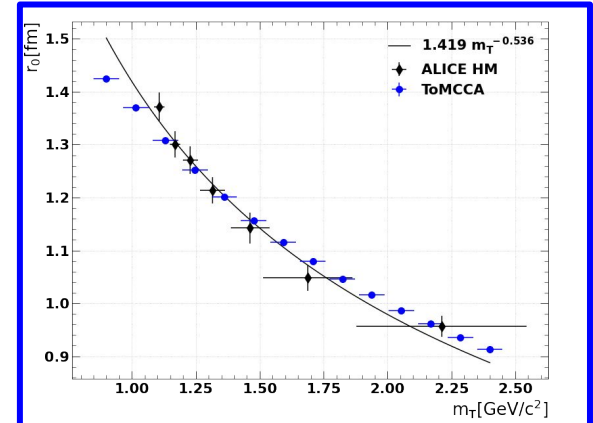
D-State probability is 6% → Maximum ~11% effect

Recap: ToMCCA

Inputs



- ToMCCA is a Toy Monte Carlo → it requires everything as an **input**:
 - **Momentum distribution** → Fully parameterized
 - **Multiplicity** → Poissonian/Event Generator
 - **Angular distribution** → From Measurement
 - **Source Size** → ALICE Measurement



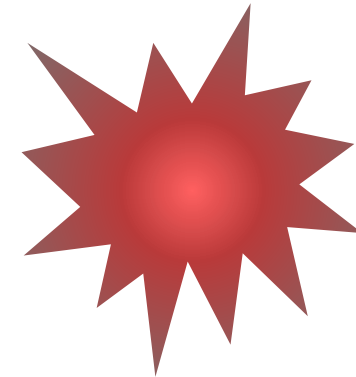
$$\frac{d^2N}{dy dp_T} = \frac{dN}{dy} \frac{p_T(n-1)(n-2)}{nC[nC+m_p(n-2)]} \left(1 + \frac{m_T - m_p}{nC}\right)^{-n}$$

Using a toy MC for Coalescence

Basics of ToMCCA



Event Loop:



Using a toy MC for Coalescence

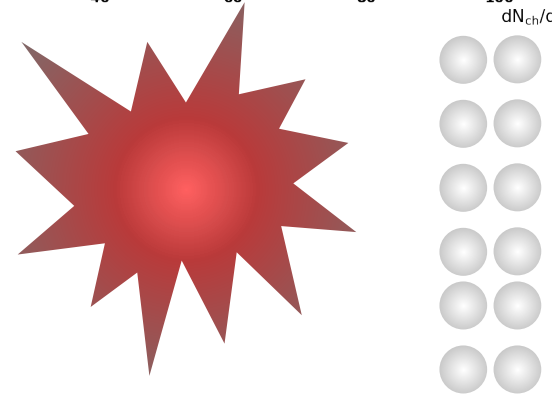
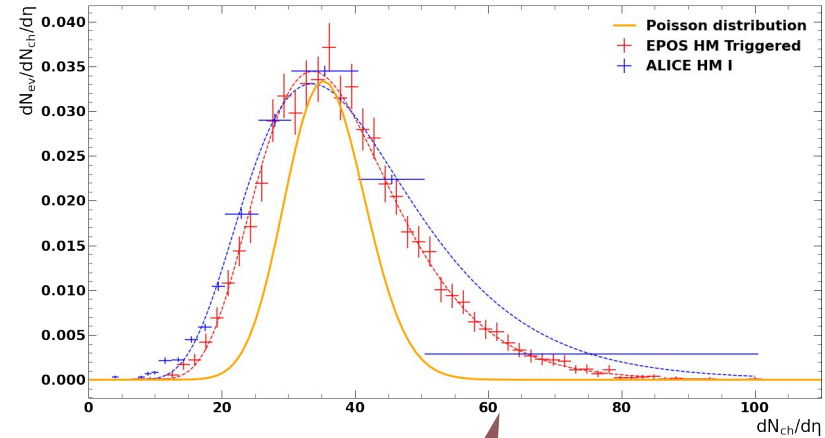
Basics of ToMCCA



Event Loop:

Get number of charged particles

1. Poissonian distribution with given mean
2. $dN/d\eta$ measurements by ALICE
3. Event generator output



Using a toy MC for Coalescence

Basics of ToMCCA



Event Loop:

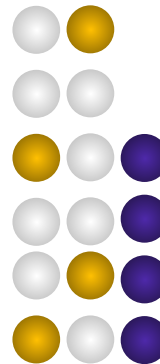
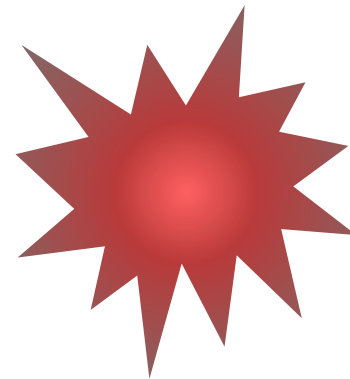
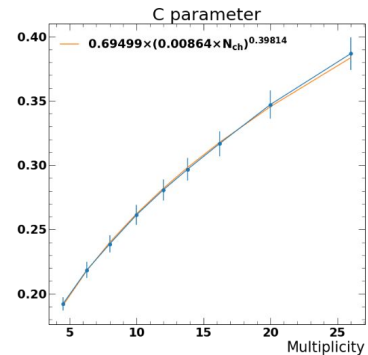
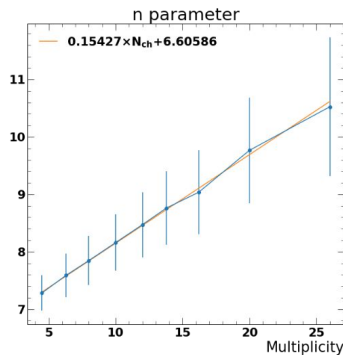
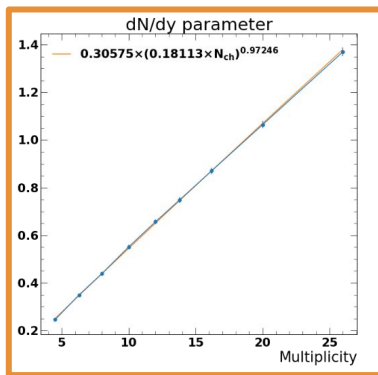
- Get number of charged particles
- Get proton yield
- Get neutron yield

Fit all proton spectra for 13TeV using a Lévy Tsallis:

$$\frac{d^2N}{dydp_T} = \frac{dN}{dy} \frac{p_T(n-1)(n-2)}{nC[nC+m_p(n-2)]} \left(1 + \frac{m_T-m_p}{nC}\right)^{-n}$$

Yield parameter!

Full parameterization as a function of multiplicity



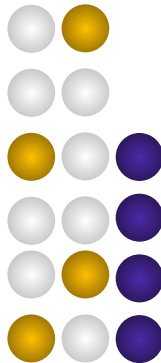
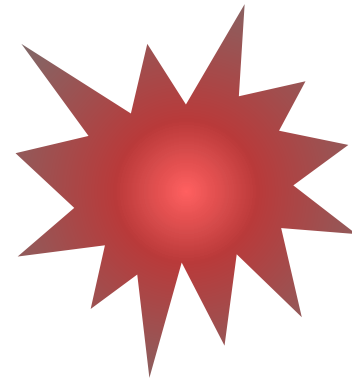
Using a toy MC for Coalescence

Basics of ToMCCA



Event Loop:

- Get number of charged particles
- Get proton yield
- Get neutron yield
- ↻ Loop over all protons





Event Loop:

Get number of charged particles

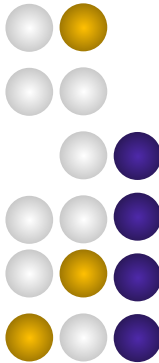
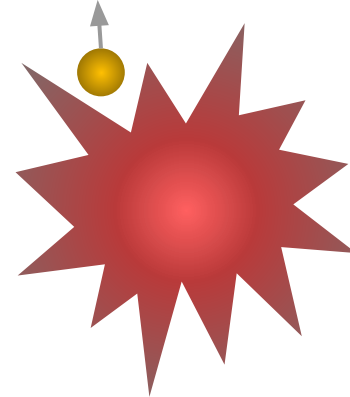
Get proton yield

Get neutron yield

↻ Loop over all protons

Get 3D momentum of proton

- Draw p_T from parameterization
- Draw flat rapidity $y=[-0.5,0.5]$
- Draw random $\phi=[0,2\pi)$



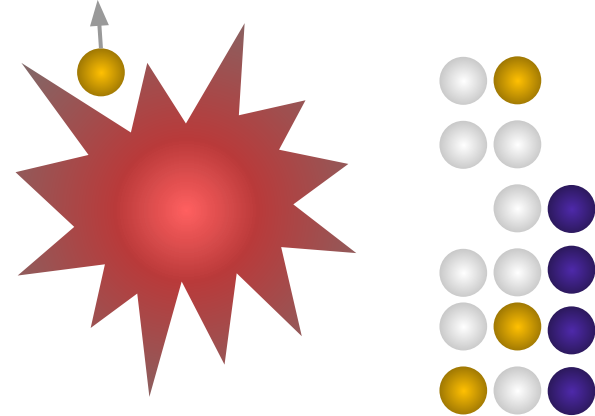
Using a toy MC for Coalescence

Basics of ToMCCA



Event Loop:

- Get number of charged particles
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- Get neutron yield
- ↻ Loop over all protons
 - Get 3D momentum of proton
- ↻ Loop over all neutrons



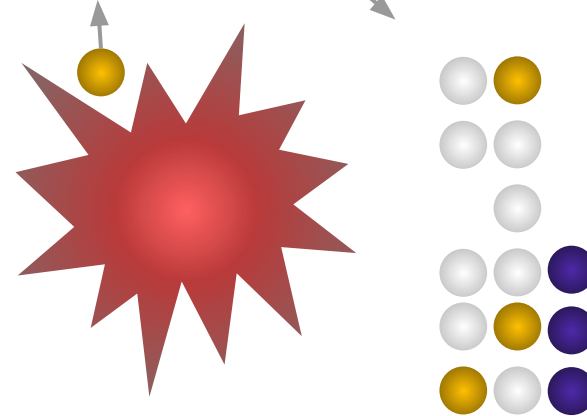
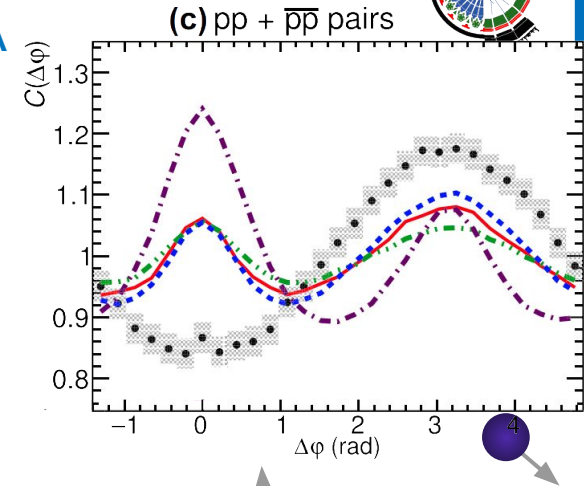
Using a toy MC for Coalescence

Basics of ToMCCA



Event Loop:

- Get number of charged particles
- Get proton yield
- Get neutron yield
- ↻ Loop over all protons
 - Get 3D momentum of proton
- ↻ Loop over all neutrons
 - Get 3D momentum of neutron
 - Draw p_T from parameterization
 - Draw flat rapidity $y=[-0.5,0.5]$
 - Draw random $\Delta\phi$ from ALICE measurement



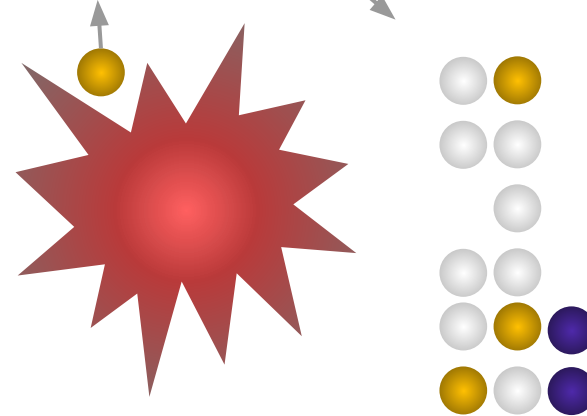
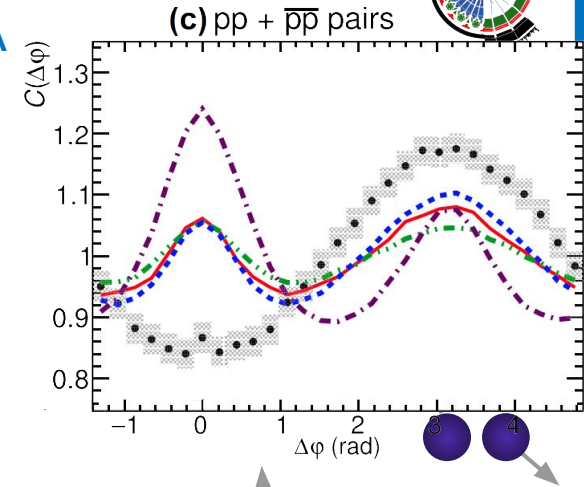
Using a toy MC for Coalescence

Basics of ToMCCA



Event Loop:

- Get number of charged particles
- Get proton yield
- Get neutron yield
- ↻ Loop over all protons
 - Get 3D momentum of proton
- ↻ Loop over all neutrons
 - Get 3D momentum of neutron
 - Draw p_T from parameterization
 - Draw flat rapidity $y=[-0.5,0.5]$
 - Draw random $\Delta\phi$ from ALICE measurement



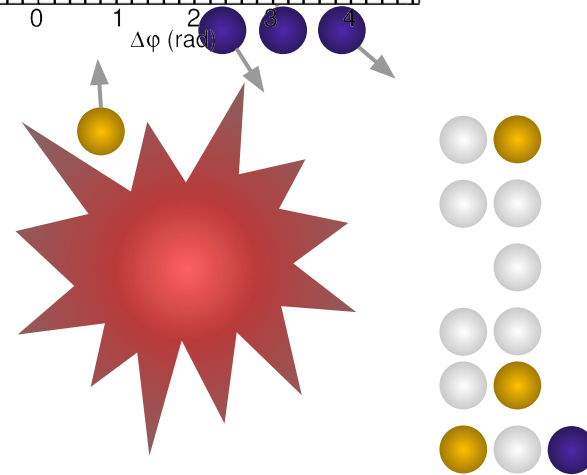
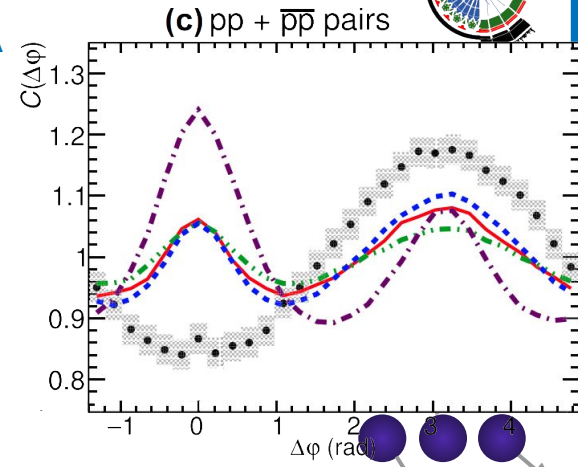
Using a toy MC for Coalescence

Basics of ToMCCA



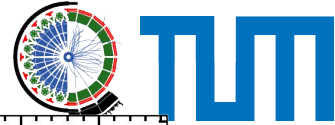
Event Loop:

- Get number of charged particles
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- Get neutron yield
- ↻ Loop over all protons
 - Get 3D momentum of proton
- ↻ Loop over all neutrons
 - Get 3D momentum of neutron
 - Draw p_T from parameterization
 - Draw flat rapidity $y=[-0.5,0.5]$
 - Draw random $\Delta\phi$ from ALICE measurement



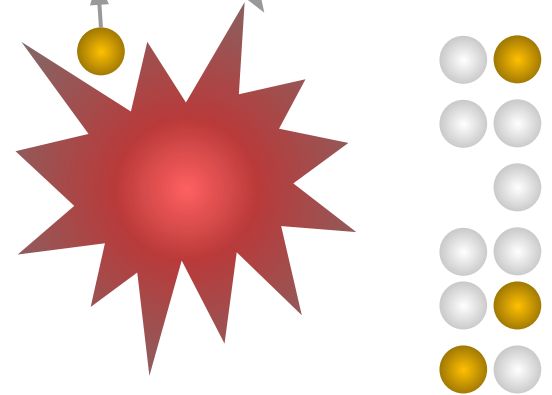
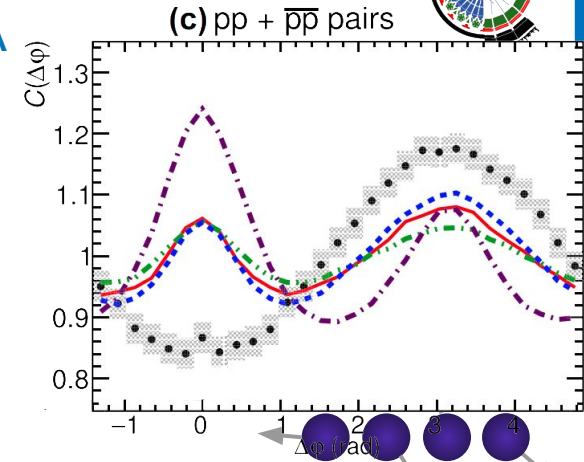
Using a toy MC for Coalescence

Basics of ToMCCA



Event Loop:

- Get number of charged particles
- Get proton yield
- Get neutron yield
- ↻ Loop over all protons
 - Get 3D momentum of proton
- ↻ Loop over all neutrons
 - Get 3D momentum of neutron
 - Draw p_T from parameterization
 - Draw flat rapidity $y=[-0.5,0.5]$
 - Draw random $\Delta\phi$ from ALICE measurement



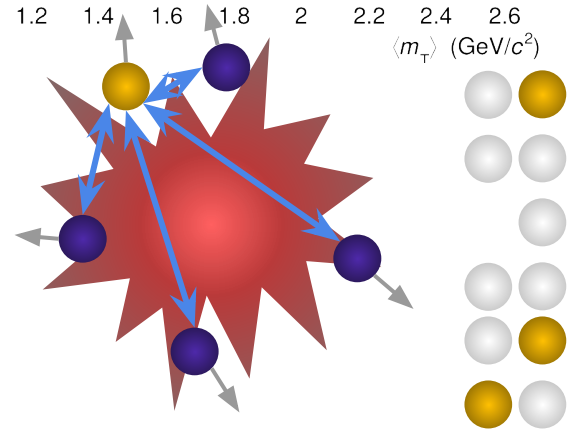
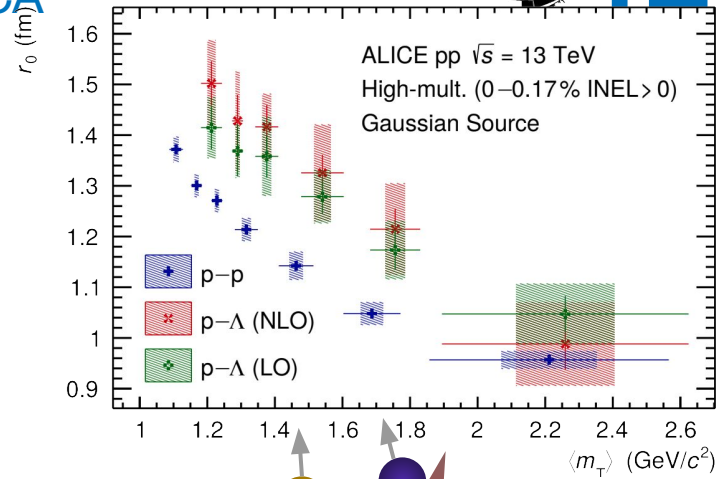
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 - Get source size



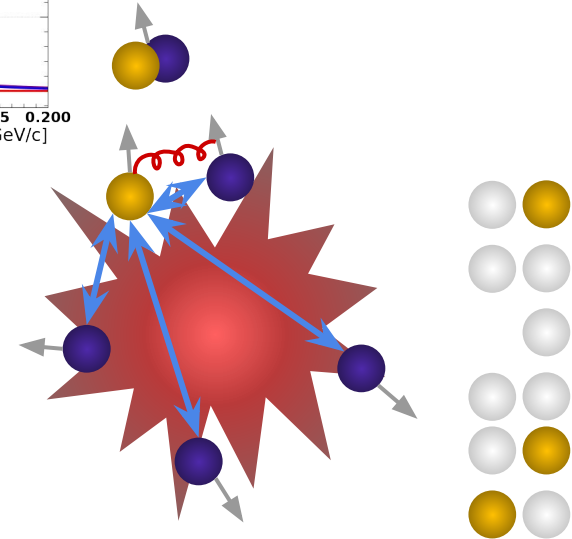
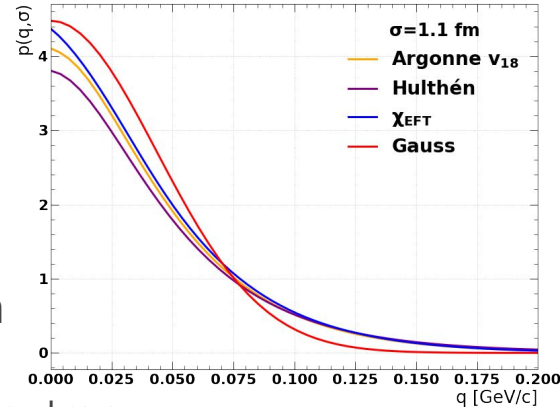
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 - Apply coalescence condition



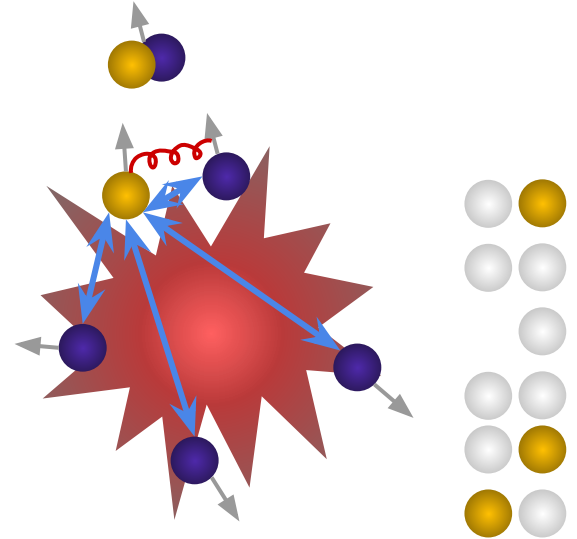
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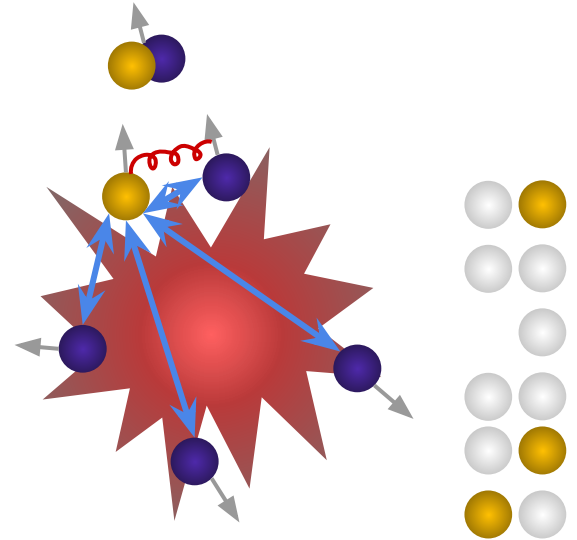
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 - Apply coalescence condition
 - ✓ make deuteron, number of neutrons -1
 - ✗ try next neutron



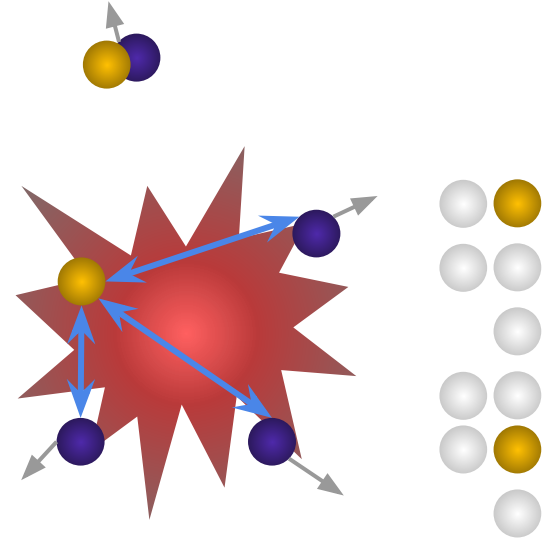
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Using a toy MC for Coalescence

Basics of ToMCCA



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Get proton yield

Get neutron yield

↻ Loop over all protons

 Get 3D momentum of proton

 ↻ Loop over all neutrons

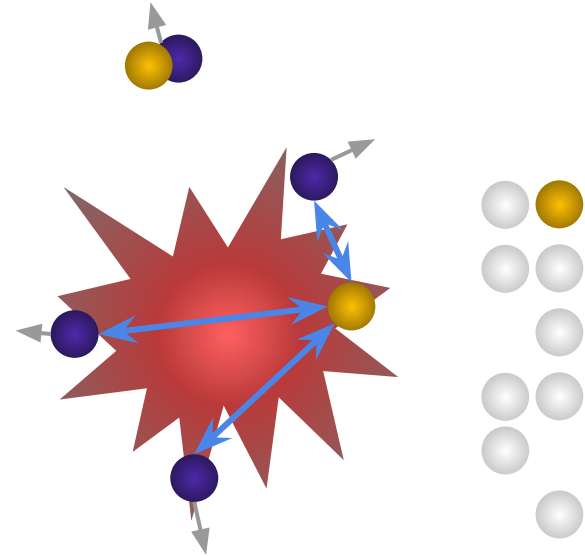
 Get 3D momentum of neutron

 Get source size

 Apply coalescence condition

make deuteron, number of neutrons -1

try next neutron



Using a toy MC for Coalescence

Basics of ToMCCA



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Get neutron yield

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 Get 3D momentum of proton

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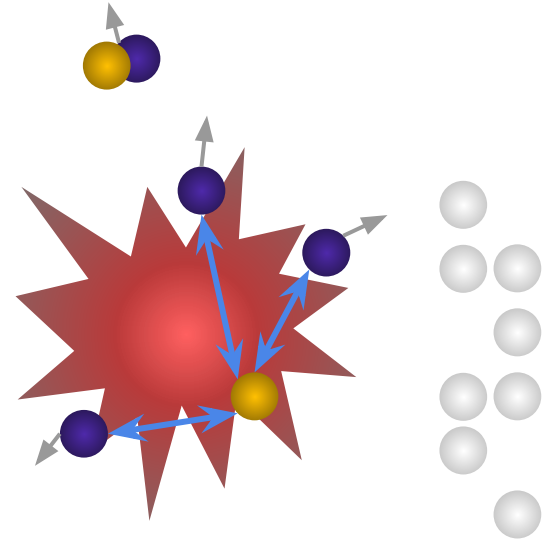
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try next neutron



Using a toy MC for Coalescence

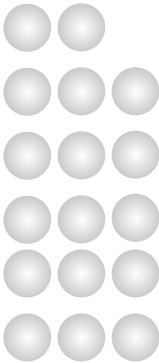
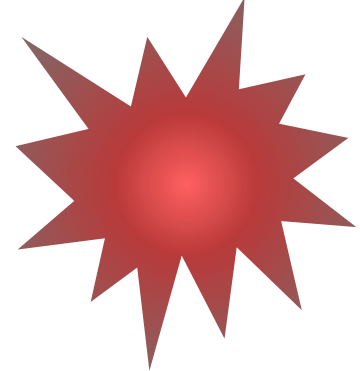
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Next Event..



Verifying the Model

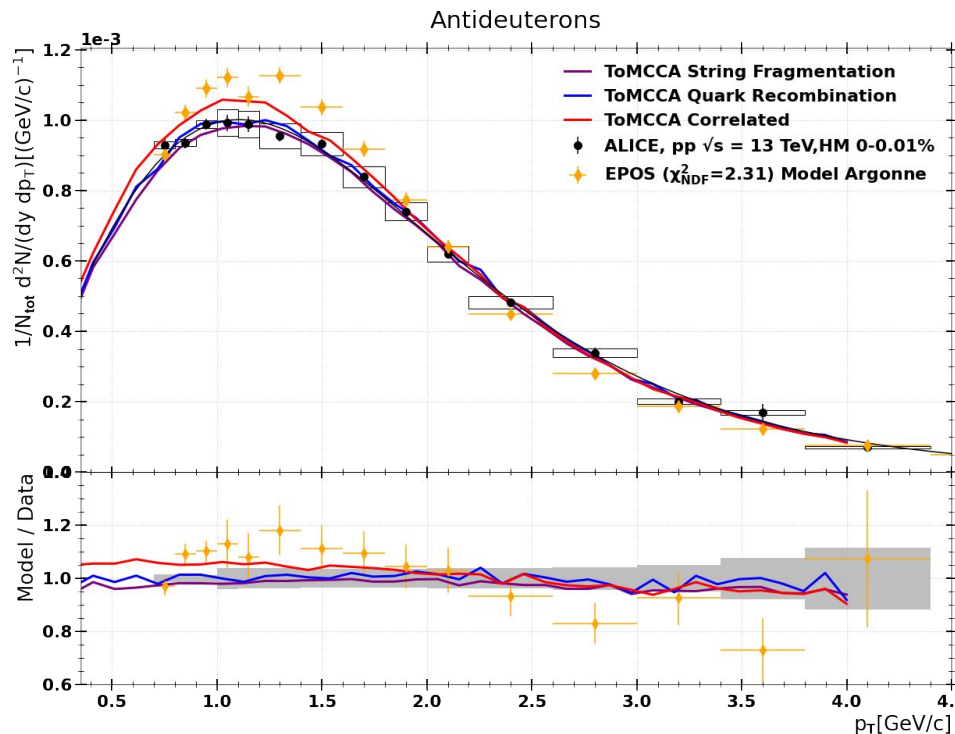
Comparison to ALICE deuteron Spectra



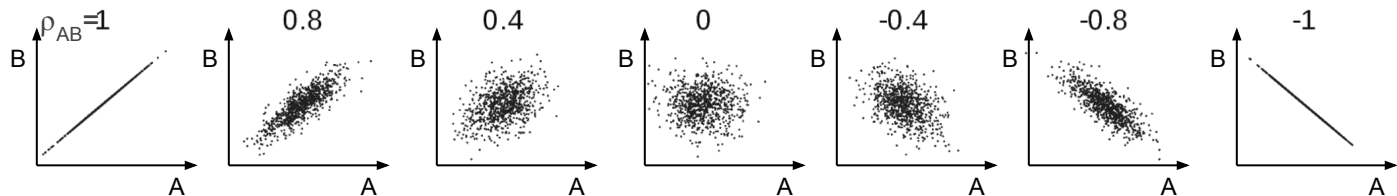
Comparison of ToMCCA and EPOS to ALICE deuteron spectra 13 TeV pp with a HM trigger

- EPOS reproduces spectra within $\sim 20\%$
- EPOS does not reproduce the $\Delta\phi$ measurement by ALICE
- ToMCCA with string fragmentation and quark recombination mode reproduces the measurement perfectly
- ToMCCA with correlated emission overshoots data at lower p_T

➔ Model reproduces the data, with no free parameters!



- To shed a light on the nuclei production mechanism measure more differential observables and test them against the common models (CSM, coalescence)
- Rationale:
 - a. In the CSM deuterons and protons are produced independently (“poissonian”)
 - b. In the coalescence model a deuteron is formed from two independent nucleons → combination of two poissonian distributions does not yield a poissonian distribution
- The observables:
 - a. $\kappa_1 = \langle n \rangle$ the mean number of particles per event
 - b. $\kappa_2 = \langle (n - \langle n \rangle)^2 \rangle$ the variance of the number distribution
 - c. $\rho_{pd} = \frac{\langle (n_p - \langle n_p \rangle)(n_d - \langle n_d \rangle) \rangle}{\sqrt{\kappa_{2p}\kappa_{2d}}}$ The pearson correlation coefficient



Deuteron number fluctuations



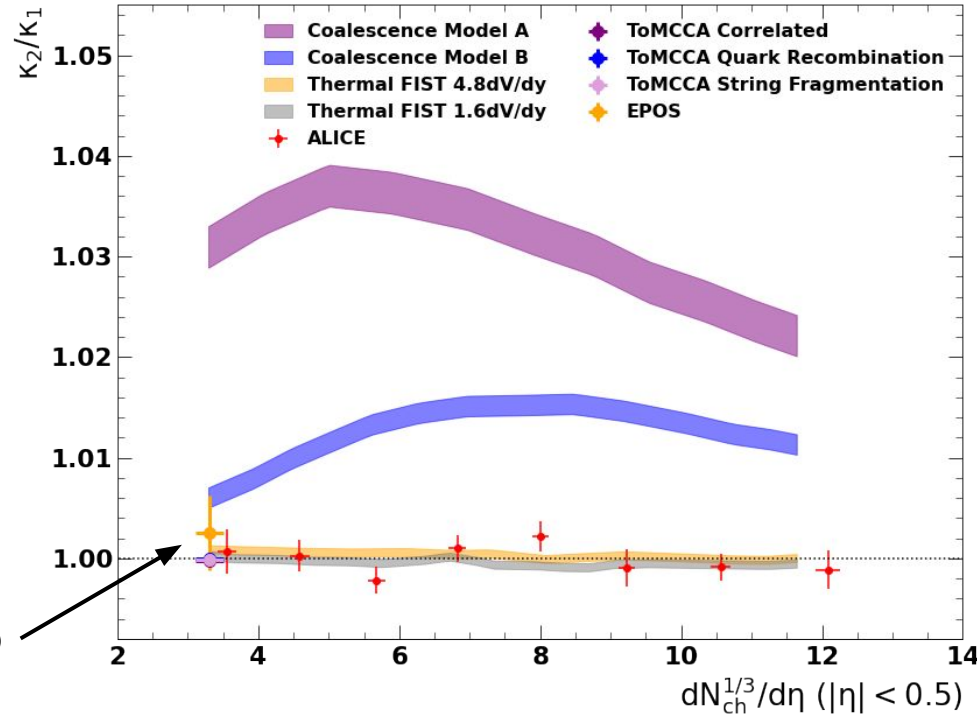
Results κ_2/κ_1

κ_2/κ_1 : Data is consistent with 1

- This implies a poissonian fluctuation of the deuteron number
- This is expected in the *CSM* since protons and deuterons are emitted independently (barring canonical suppression)
- *Coalescence* model shows a (positive) deviation of $O(1\%)$ indicating a deviation from the poissonian baseline
- All 3 versions of ToMCCA reproduce the $\kappa_2/\kappa_1=1$
- EPOS reproduces data with in large uncertainty

We can only work with pp
13 TeV HM 1 (Mult ~36)

Data translated from Centrality to mean multiplicity (using <https://twiki.cern.ch/twiki/bin/viewauth/ALICE/ReferenceMult>)



Deuteron number fluctuations



Results ρ_{pd}

ρ_{pd} : Data shows a negative pearson coefficient $O(0.1\%)$

- This implies that deuteron and proton numbers are negatively correlated
- In the *CSM* this can be achieved by including canonical suppression (Baryon number conservation)
- In the *coalescence* model there are two effects at play:
 - a. Deuterons “take away” protons in the formation process ($d\uparrow \rightarrow p\downarrow$)
 - b. Non-linear formation relation between protons and deuterons ($p\uparrow \rightarrow d\uparrow\uparrow$)
- String fragmentation and Quark recombination come close to data
- Correlated emission and EPOS too high

Data translated from Centrality to mean multiplicity (using <https://twiki.cern.ch/twiki/bin/viewauth/ALICE/ReferenceMult>)

