



Quarkonium dynamics in the quantum Brownian regime with non-abelian quantum master equations

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Open quantum systems



Quantum Master Equation (Quantum Brownian Regime)



1D Potential



- Based on a 3D potential inspired from Lattice results D. Lafferty, A. Rothkopf (2020)
- Real part: parametrization to reproduce 3D mass spectra
- Imaginary part: separated in a coulombic and string part, aims at reproducing 3D decay widths R. Katz, S.D, P-B. Gossiaux (2022)

cc evolution at fixed temperature



- Initial singlet in-medium 1S state at T = 300 MeV
- Octet populated via dipolar transitions
- Repulsive octet potential
 ⇒ delocalization
- Delocalization in singlet channel via transitions
- Surviving central peak in singlet channel
- ► Non-diagonal elements (width equal to $\lambda_{th} = \frac{1}{\sqrt{MT}}$)

$c\overline{c}$ evolution at fixed temperature



- Instantaneous projections on vacuum eigenstates
- In-medium 1S state very close to vacuum (p_{1S,v}(0) ≈ 0.95)
- Complex evolution of p_{2S} (coupling to other states + decay to continuum)
- Delayed appearence of 1P states (chain of transitions at 3rd order in perturbation theory)
- Global evolution towards asymptotic values (dashed horizontal lines)

Temperature dependence



- $\triangleright \ \rho_{s}(r,t) = \mathcal{D}_{s}(r,r,t)$
- Density reaching box boundaries between 5 and 10 fm/c
 - \Rightarrow Level off to asymptotic value
- At 20 fm/c: stationnary pedestal at large distances with trace of bound state at small distances
- ► T = 600 MeV: harder and more frequent collisions ⇒ faster increase of relative distance
- Central peak disappears faster than at 300 MeV, no peak after 5 fm/c (potential not binding at 600 MeV)

Temperature dependence



- Initial singlet vacuum 1S state
- ▶ Exponential decay of *p*_{1S}
- Growth of p_{1P}/p_{2S} followed by global decay
- Faster evolution with increasing T
- Close asymptotic values as T increases (D_s nearly diagonal)
- Oscillations of p_{2S} disappear for T ≥ 300 MeV (overdamped regime)

Hierarchy of operators in different regimes



$$\begin{split} \langle \mathcal{L}_{k} \rangle &= \\ \sum_{i,i'} \left| \mathcal{L}_{k}^{\text{ss}}[\mathcal{D}_{\text{s}}] + \mathcal{L}_{k}^{\text{so}}[\mathcal{D}_{\text{o}}] \right|_{i,i'} + \left(N_{c}^{2} - 1 \right) \left| \mathcal{L}_{k}^{\text{os}}[\mathcal{D}_{\text{s}}] + \mathcal{L}_{k}^{\text{oo}}[\mathcal{D}_{\text{o}}] \right|_{i,i'} \\ \sum_{i,i'} \left| \mathcal{D}_{\text{s}} \right|_{i,i'} + \left(N_{c}^{2} - 1 \right) \left| \mathcal{D}_{\text{o}} \right|_{i,i'} \end{split}$$

- \blacktriangleright Clear hierarchy at T = 200 MeV
- Effect of \mathcal{L}_1 less and less impactful
- $\blacktriangleright \ \langle \mathcal{L}_2 \rangle \sim \langle \mathcal{L}_3 \rangle \Rightarrow \text{Equilibrium}$
- Marginal \mathcal{L}_4 contribution

Comparison of states populations early time evolution



- ► Dashed lines: $\dot{p}_{nS}(\sigma, 0) = -\Gamma_{nS}p_{nS}(\sigma, 0)$
- Full lines: analytical solution with \mathcal{L}_2 only
- Points: Full QME results
- Good agreement between QME and "L₂-only" evolution around σ = σ_{1S}
- Very different results between dashed and full curves: quantum effects
- Positive derivative for 2S completely absent from dashed curves

Bottomonium system

- ► 3 different initial states:

 - Mixture of S and P states:



4 different medium settings

Fixed temperature T = 400 MeV

Average temperature profiles obtained from EPOS4 for three different centrality classes:

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Bottomonium dynamics at fixed temperature



- by a factor 100
- Factor 2 between 1S and 2S

▶ Similar 2S/1S ratio

 1S (2S) evolution similar to the evolution with the 1S (2S) initial state

Bottomonium dynamics in a dynamical medium



- Reduction of suppression for more peripheral profiles
- S not much more suppressed than 2S for more central collisions

Semi-classical approach

Semi-classical approaches can treat multiple pairs

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J.-P. Blaizot and M.-A Escobedo, JHEP 06 (2018) 034
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▶ Focus on *cc* (more affected by recombination)

A. Daddi Hammou, J.-P. Blaizot, S. D, P.-B. Gossiaux and T. Gousset (in preparation)

- Case of abelian dynamics ("scalar QCD") as first step towards QCD case as QCD requires semi-classical treatment of color
- Full QME as reference for comparison $\frac{d\mathcal{D}_{sQCD}}{dt} = \frac{d\mathcal{D}_s}{dt}\Big|_{\mathcal{D}_s = \mathcal{D}_o}$
- Semi-classical treatment not including \mathcal{L}_4 \Rightarrow "Uncertainty band" for QME results by turning on and off \mathcal{L}_4 contribution
- Real potential regularized for SC approach as the original potential is sharp at the origin

Comparison with semi-classical results



$$W(r,p) = rac{1}{2\pi\hbar}\int\mathrm{d}y\; e^{-rac{ipy}{\hbar}}\left\langle r+rac{y}{2}\left|\hat{\mathcal{D}}
ight|r-rac{y}{2}
ight
angle$$

- Initial vacuum 1S state, T = 300 MeV
- Differences at early times, due to the presence of quantum effects absent in semi-classical approach
- Very good agreement later on

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Comparison with semi-classical results



- Overall good agreement
- Differences at high temperatures due to overheating from QME



- Good agreement at high temperatures
- \blacktriangleright Differences at 200 MeV due to quantum effects. Agreement from \approx 12 fm/c

Starting temperature from a realistic AA scenario would be high anyways Small systems (lower T) \Rightarrow Fewer pairs \Rightarrow Full quantum treatment possible

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Conclusions and perspectives

- Resolution of a quantum master equation in the quantum brownian regime
- Study of various temperature regimes, highlighting distinctive features of the QQ evolution
- Direct application to $b\overline{b}$: Quantum evolution captures the general trends
- Benchmark of semi-classical approach in "scalar QCD" case: overall very good agreement
- Improvements of the QME (treatment of energy gaps)
- Study related to the potential (screening for example)
- Revisit the phenomenological study of $b\overline{b}$ with more statistics
- Extension of the semi-classical approach to QCD

Back-up

Quantum Master Equation

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$$n_x^a$$
: color charge density
 $n_x^a = \delta(x - r) t^a \otimes \mathbb{I} - \mathbb{I} \otimes \delta(x - r) \tilde{t}^a$

▶ Can recover \mathcal{L}_3 from \mathcal{L}_2 by performing:

$$\left(\left\{n_{x}^{a}n_{x'}^{a},\mathcal{D}\right\}-2n_{x}^{a}\mathcal{D}n_{x'}^{a}\right) \longrightarrow \left\{\left(n_{x}^{a}-\frac{i}{4T}\dot{n}_{x}^{a}\right)\left(n_{x'}^{a}+\frac{i}{4T}\dot{n}_{x'}^{a}\right),\mathcal{D}\right\}-2\left(n_{x}^{a}+\frac{i}{4T}\dot{n}_{x}^{a}\right)\mathcal{D}\left(n_{x'}^{a}-\frac{i}{4T}\dot{n}_{x'}^{a}\right)$$

▶ Additionnal terms
$$\Rightarrow \mathcal{L}_4$$

Asymptotic Wigner distribution



- $\sqrt{<p^2>}$ does not scale as $\sqrt{\frac{MT}{2}}$ (dotted lines)
- \blacktriangleright Equilibrium limit modified by \mathcal{L}_4
- ► At large distances, scaling as $\sqrt{\frac{1}{1+\frac{\gamma}{2}}\frac{MT}{2}}$ with $\gamma = \frac{\tilde{W}^{(4)}(0)}{16MT\tilde{W}''(0)}$ (dashed lines)