

Measurements of Kaon Femtoscopy in Au+Au Collisions at $\sqrt{s_{NN}} = 3.0 - 4.5$ GeV by the STAR Experiment

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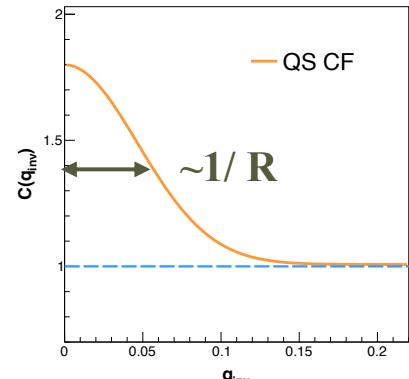
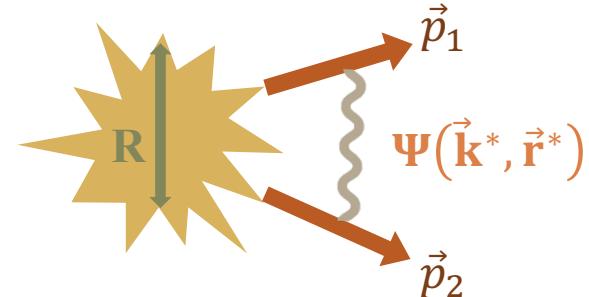
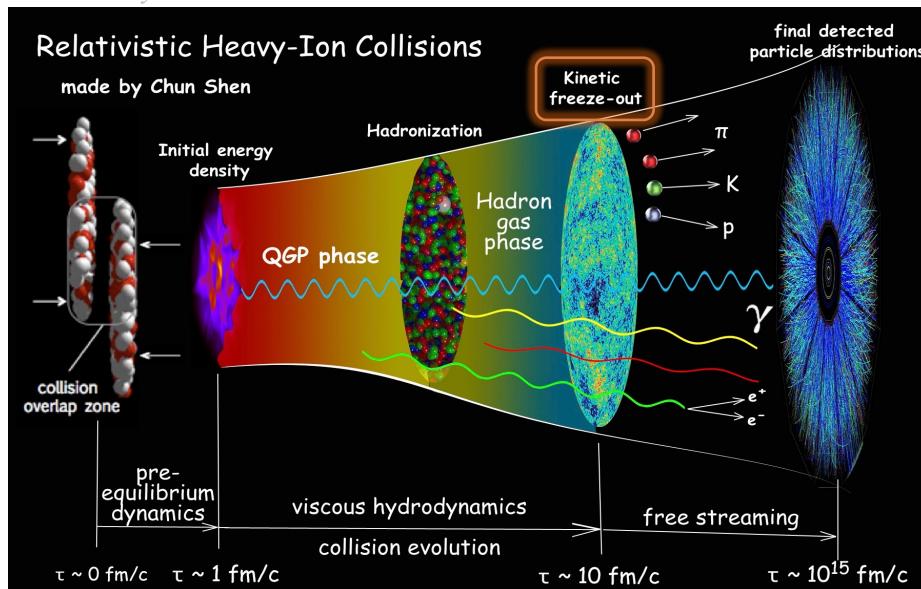


Outline

- ❖ **Introduction**
- ❖ **STAR Experimental Setup**
- ❖ **Analysis Details**
- ❖ **Results and Discussions**
 - 1) Correlation functions**
 - 2) Extracted parameters and m_T - scaling**
- ❖ **Summary**

Introduction - femtoscopy

<https://u.osu.edu/vishnu/2014/08/06/sketch-of-relativistic-heavy-ion-collisions/>



$$C(q_{\text{inv}}) = \int S(\vec{r}^*) |\Psi(q_{\text{inv}}, \vec{r}^*)|^2 d^3 \vec{r}^* = \mathcal{N} \frac{N_{\text{same}}(q_{\text{inv}})}{N_{\text{mixed}}(q_{\text{inv}})}$$

Assumed Determined Measured

❖ Decode space and time evolution of source at kinetic freeze-out.

❖ Why study kaons?

- 1) less contribution from resonances decay
- 2) smaller rescattering cross-section

❖ Two-particle correlations are sensitive to:

- 1) Quantum Statistics (QS);
- 2) Final State Interactions (FSI)

❖ If we assume that we know the **emission function**, the **measured correlation function** can be used to determine **parameters of final state interactions**.

\vec{r}^* : relative distance of the emitters in the Pair Rest Frame (PRF: in which frame the total momentum of the pair is zero)

$S(\vec{r}^*)$: emission function

q_{inv} : relative invariant momentum in PRF

$$q_{\text{inv}} = \sqrt{|\mathbf{q}|^2 - q_0^2}, \text{ where } \mathbf{q} = \mathbf{p}_1 - \mathbf{p}_2, q_0 = E_1 - E_2$$

For identical particles, $q_{\text{inv}} = 2k^*$

$\Psi(q_{\text{inv}}, \vec{r}^*)$: two-particle wave function

$\mathcal{N} \frac{N_{\text{same}}(q_{\text{inv}})}{N_{\text{mixed}}(q_{\text{inv}})}$: measured correlation function

Introduction - Parametrization

- ❖ CF including only Quantum Statistical(QS) effect:

$$CF(q_{inv}) = 1 + \lambda e^{-[R_G^2 q_{inv}^2]}$$

- ❖ For $K^+ - K^+$ and $\pi^+ - \pi^+$, Bowler-Sinyukov^[1] method to include FSI(Coulomb effect):

Coulomb effect QS effect

$$CF(q_{inv}) = N[(1 - \lambda) + K_{coul}(q_{inv}, R_G)\lambda(e^{-[R_G^2 q_{inv}^2]} + 1)]$$

R_G: source radii parameter;
λ: correlation strength;
N: normalization factor;

- ❖ For $K_S^0 - \bar{K}_S^0$, Lednický-Lyuboshitz (L-L)^[2] approach to include FSI(Strong interaction):

QS effect

Strong interaction through $f_0(980)$ / $a_0(980)$ resonances

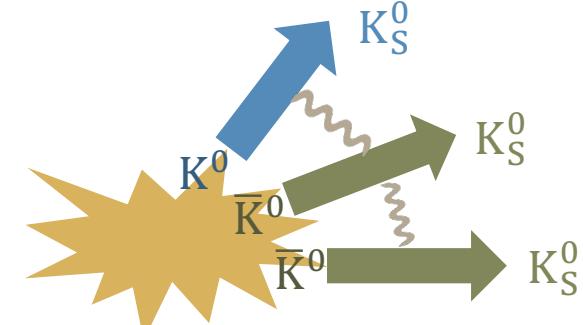
$$CF(q_{inv}) = 1 + \lambda(e^{-[R_G^2 q_{inv}^2]} + \frac{1 - \epsilon^2}{2} [\left| \frac{f(k^*)}{R_G} \right|^2 + \frac{4\text{Re}[f(k^*)]}{\sqrt{\pi}R_G} F_1(q_{inv}R_G) - \frac{2\text{Im}[f(k^*)]}{R_G} F_2(q_{inv}R_G)])$$

abundance asymmetry ϵ

$$\epsilon = \frac{K - \bar{K}}{K + \bar{K}}$$

Resonance parameters:

	m_{f_0}	$\gamma_{f_0 KK}$	$\gamma_{f_0 \pi\pi}$	m_{a_0}	$\gamma_{a_0 KK}$	$\gamma_{a_0 \pi\eta}$
Antonelli ^[3]	0.973	2.763	0.5283	0.985	0.4038	0.3711



- $K_S^0 - \bar{K}_S^0$ consist of $K^0 - K^0$ ($\bar{K}^0 - \bar{K}^0$) and $K^0 - \bar{K}^0$ states
- Kaon abundance asymmetry can be extracted by $K_S^0 - \bar{K}_S^0$ CF

$$F_1(z) = \int_0^z dx \frac{e^{x^2 - z^2}}{z}; F_2(z) = \frac{1 - e^{-z^2}}{z}.$$

$$\text{scattering amplitude: } f(k^*) = \frac{f_0(k^*) + f_1(k^*)}{2}$$

$$f_I(k^*) = \frac{\gamma_I}{m_I - s - i\gamma_I k^* - i\gamma'_I k'_I}, s = 4(m_K^2 + k^{*2})$$

$I = 0$ or 1 for the f_0 or a_0 ;

m_I : mass of the resonance;

γ_I and γ'_I : couplings of the resonances to their decay channels;

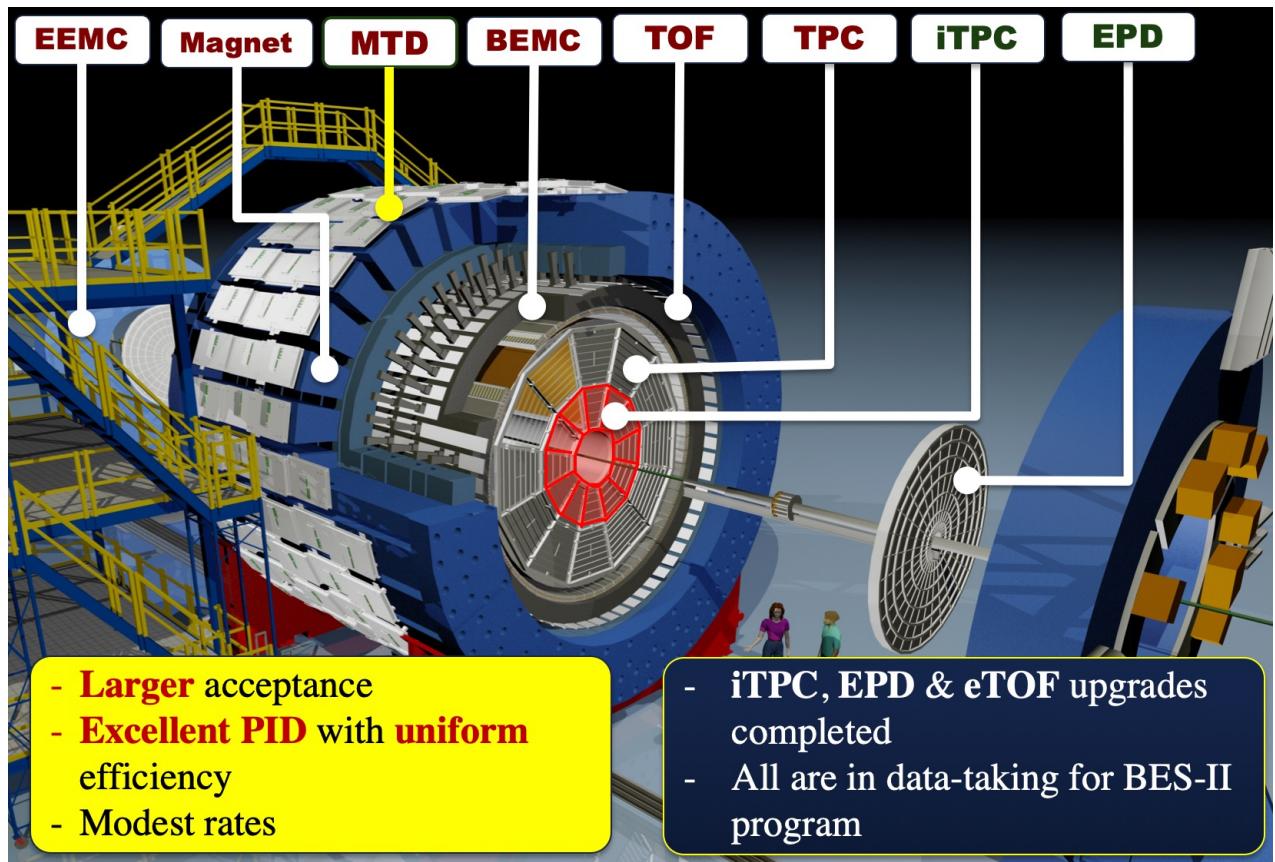
k'_I : momentum in the second decay channel.

[1] Phys. Lett. B, 432(3-4), 248-257 (1998)

[2] J.Nucl.Phys. 35, 770 (1982)

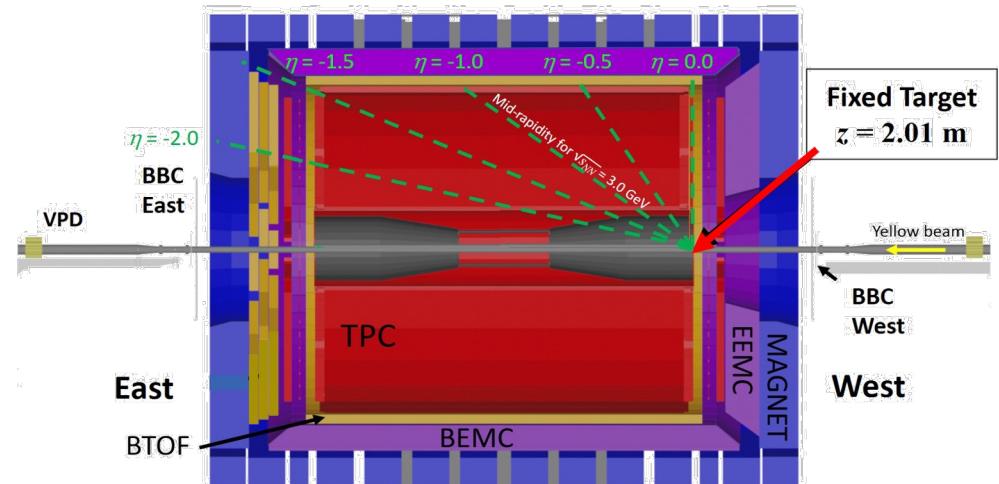
[3] eConfC020620, THAT06 (2002)

STAR Experimental Setup



Main sub-detectors for PID

- ❖ Time Projection Chamber (TPC): Ionization energy loss (dE/dx)
- ❖ Time of Flight (TOF): m^2



BES-II Upgrades

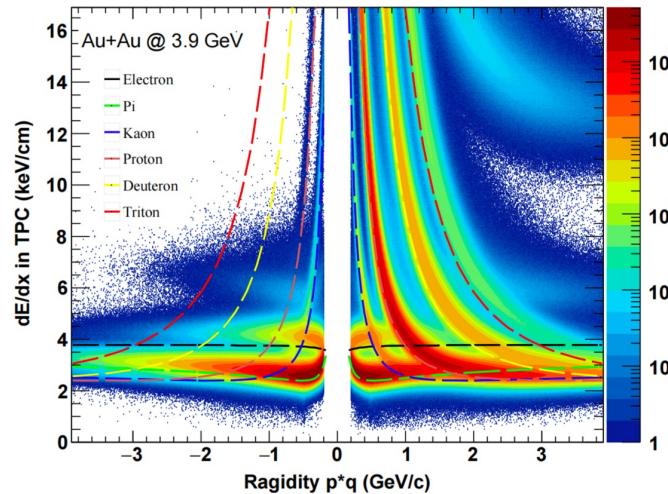
- ❖ Inner-Time Projection Chamber (iTPC)
 - Extended eta acceptance and improved tracking and dE/dx resolution
- ❖ Endcap Time of Flight (eTOF)
 - Extended PID coverage
- ❖ Event Plane Detector (EPD)
 - Improved Event plane resolution

Fixed-Target Experiment

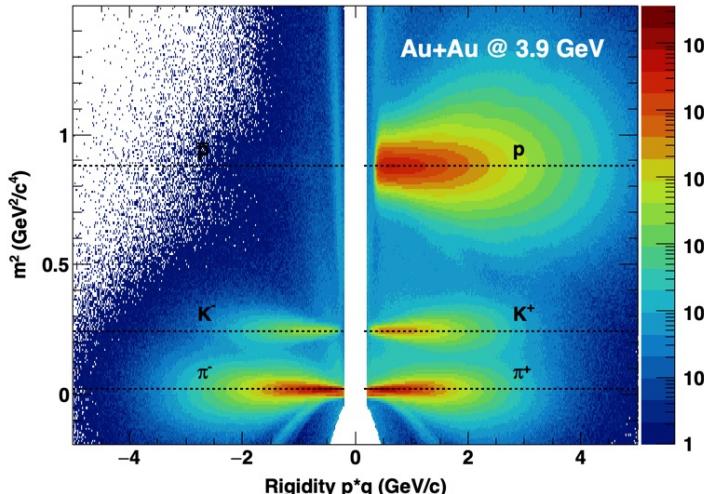
- ❖ FXT extends energy reach down to 3 GeV ($\mu_B = 750$ MeV)

Analysis details – PID, reconstruction

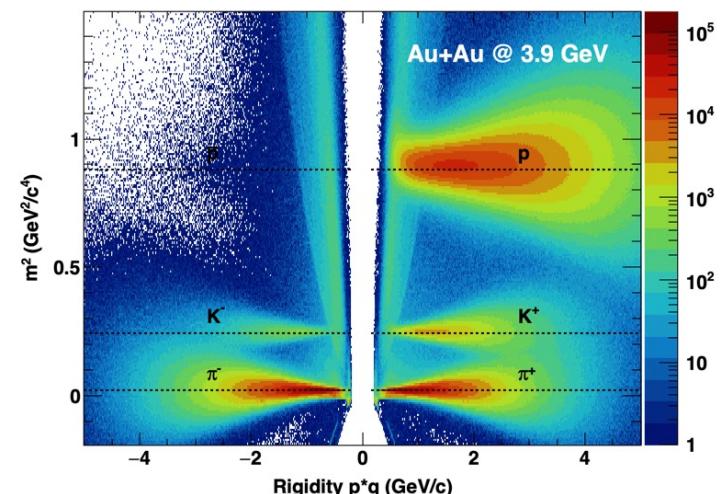
TPC



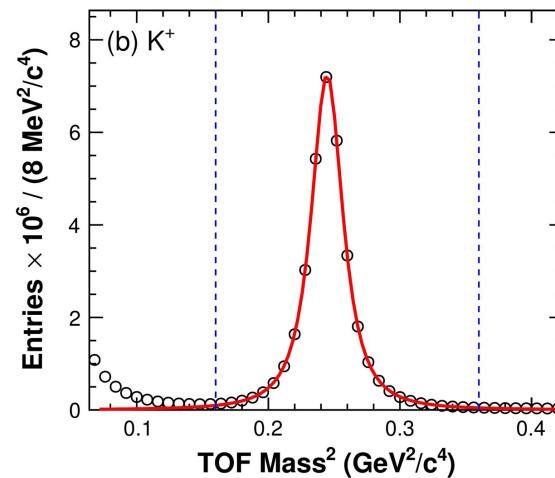
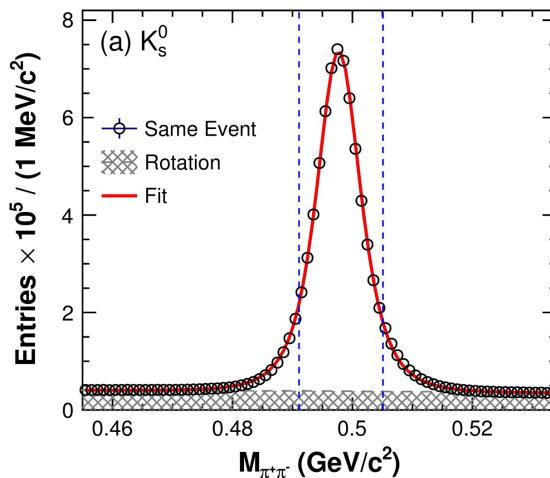
bTOF



eTOF



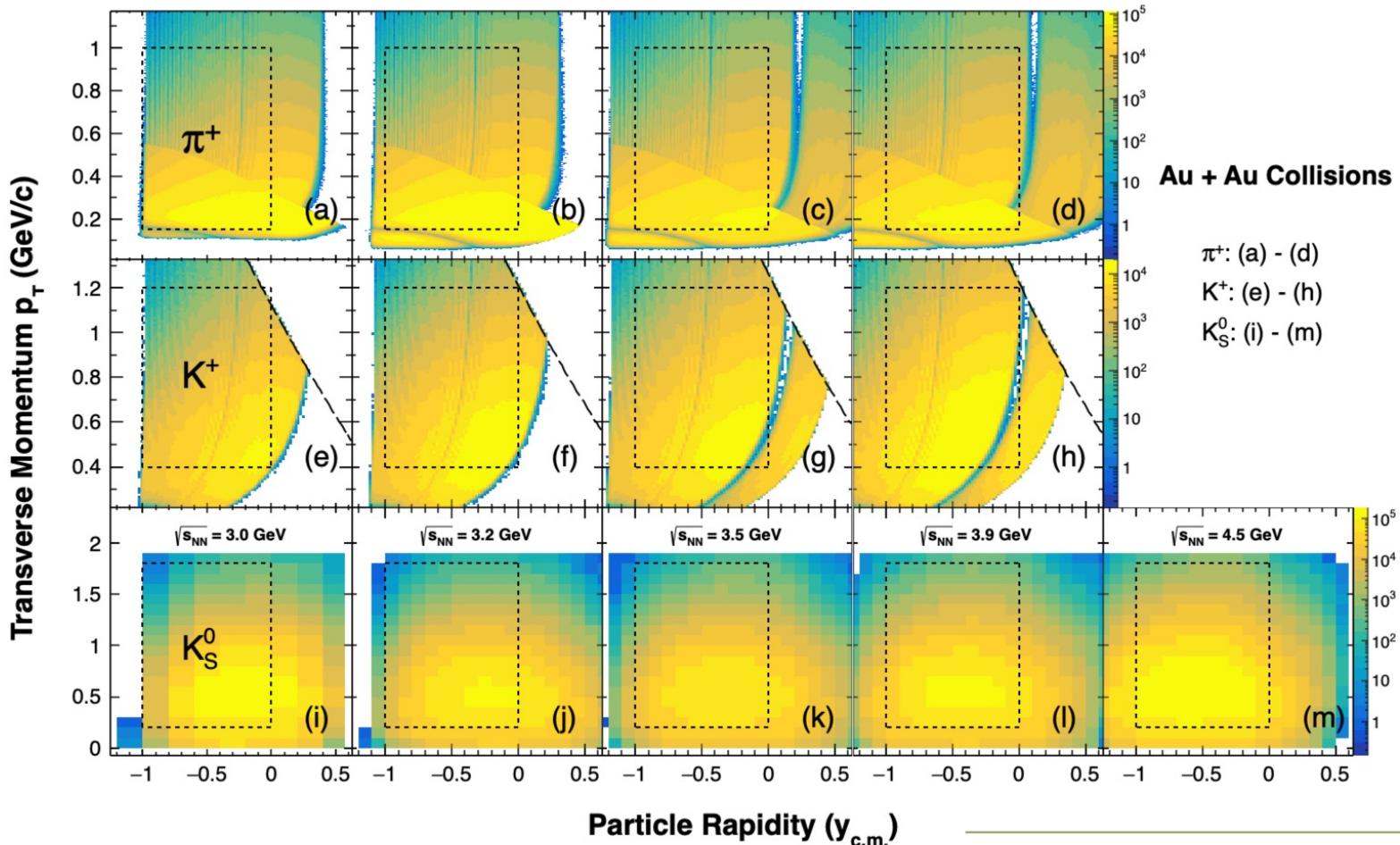
3.9 GeV Au + Au Collisions at RHIC



- ❖ π^+ and K^+ particles identified by TPC and TOF
- ❖ K_S^0 hadrons reconstructed using invariant mass method:

$$K_S^0 \rightarrow \pi^+ \pi^-$$

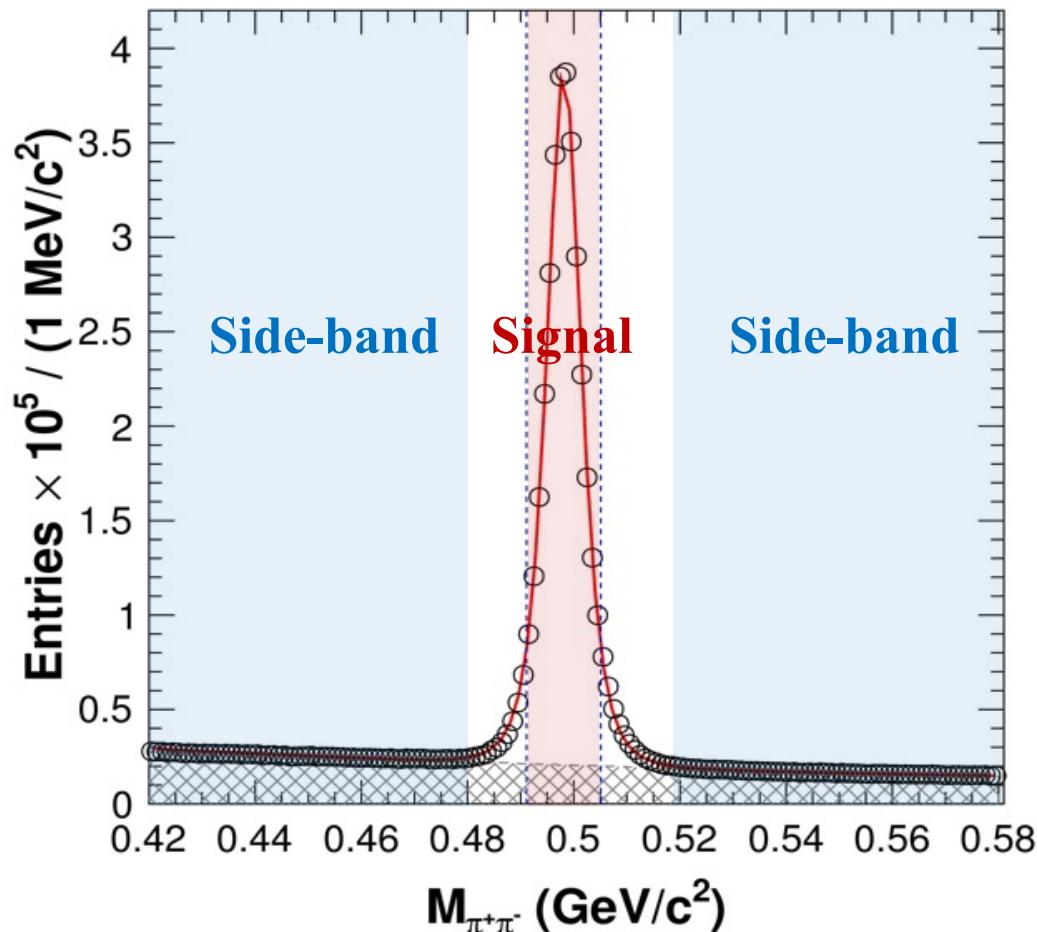
Analysis details – acceptance



- ❖ K_S^0 reconstruction: KF Particle package
- ❖ Good coverage from beam-rapidity to mid-rapidity

Particle	Analysis window
π^+	$-1.0 < y < 0, 0.15 < p_T < 1.0 \text{ (GeV/c)}$
K^+	$-1.0 < y < 0, 0.4 < p_T < 1.2 \text{ (GeV/c)}$
K_S^0	$-1.0 < y < 0, 0.2 < p_T < 1.8 \text{ (GeV/c)}$

Analysis details – Purity correction



$$C(q_{\text{inv}}) - 1 =$$

measured

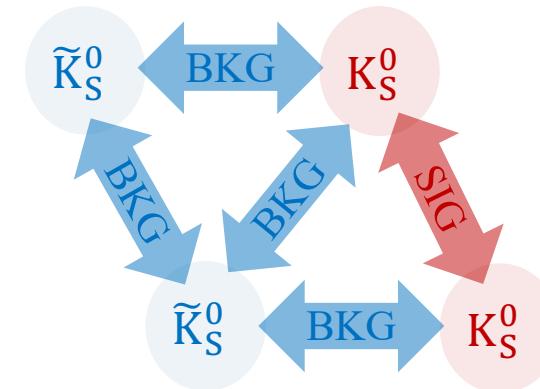
$$\omega_{\text{Pair Purity}}[C_{\text{pure}}(q_{\text{inv}}) - 1] +$$

we want this

$$(1 - \omega_{\text{Pair Purity}})[C_{\text{BKG}}(q_{\text{inv}}) - 1]$$

background

Combinatorial background



K_S^0 : Signal

\tilde{K}_S^0 : Background

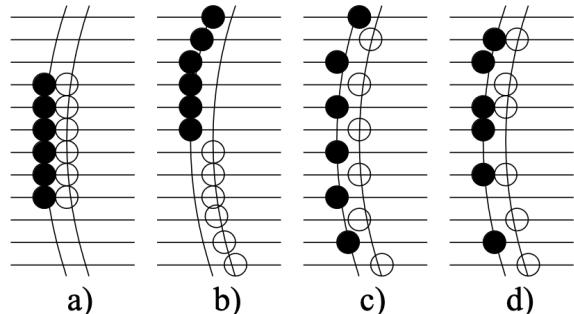
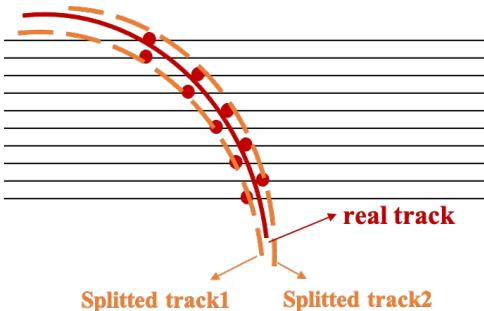
Signal pair: $K_S^0 - K_S^0$

Background pair: $K_S^0 - \tilde{K}_S^0$, $\tilde{K}_S^0 - \tilde{K}_S^0$



Analysis details – Pair track correction

Track-splitting effect



$$\text{Splitting Level (SL)} \equiv \frac{\sum_i S_i}{\text{Nhits}_1 + \text{Nhits}_2}$$

$S_i = +1$: one hit
 $S_i = -1$: two hits^[1]
 $S_i = 0$: no hit

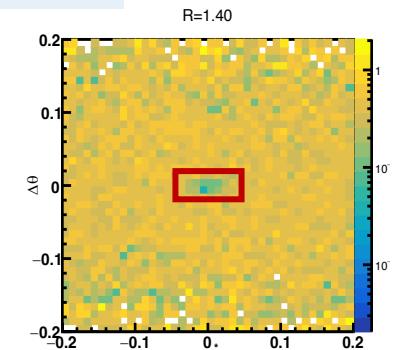
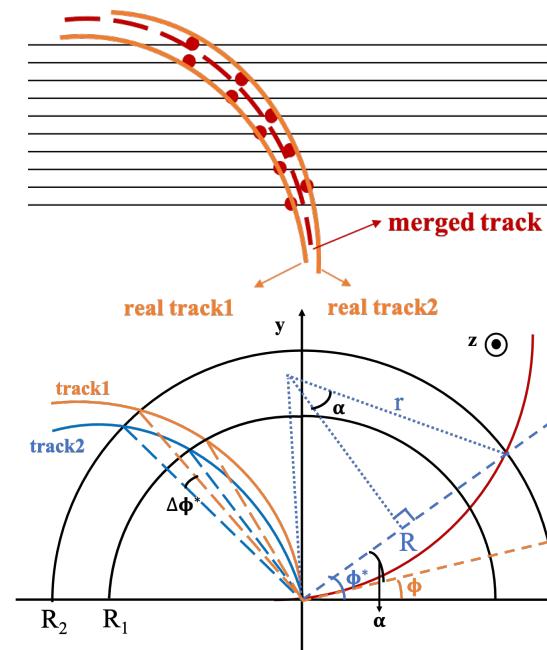
- ❖ Results in an increase of pairs, amplifying signal of CF
- ❖ Remove: $-0.5 < \text{SL} < 0.6$ used both for Kaon and pion

i - the pad-row number

Nhits₁ & Nhits₂ - the total number of hits associated to each track in the pair

[1] arXiv:nul-ex/0411036

Track-merging effect

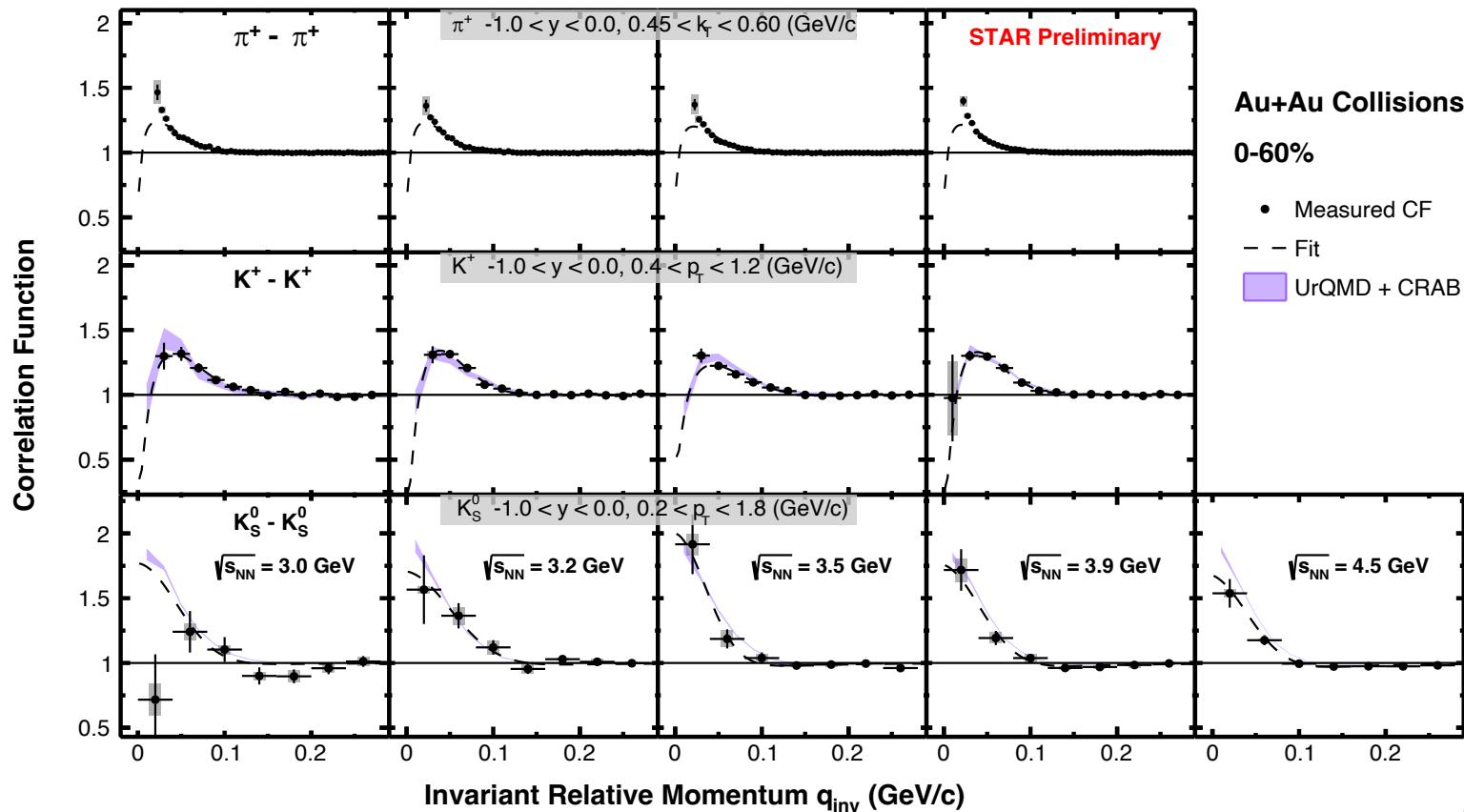


R - The radius of TPC we choose;
r - The radius of the rotation of particle;
B - Magnetic field intensity;
q - The charge of particle;
p_T - The transverse momentum of particle;

$$\Delta\phi^* = \Phi_1^* - \Phi_2^* = \Delta\phi + \sin^{-1}\left(\frac{0.15q_1BR}{p_{T1}}\right) - \sin^{-1}\left(\frac{0.15q_2BR}{p_{T2}}\right)$$

- ❖ Results in a reduction of pairs, reducing signal of CF
- ❖ Remove: for Kaon, $|\Delta\theta| > 0.02 \quad \text{||} \quad |\Delta\phi^*(R = 1.4m)| > 0.05$
for pion, $|\Delta\eta| > 0.04 \quad \text{||} \quad |\Delta\phi^*(R = 1.4m)| > 0.06$

Results - Correlation functions



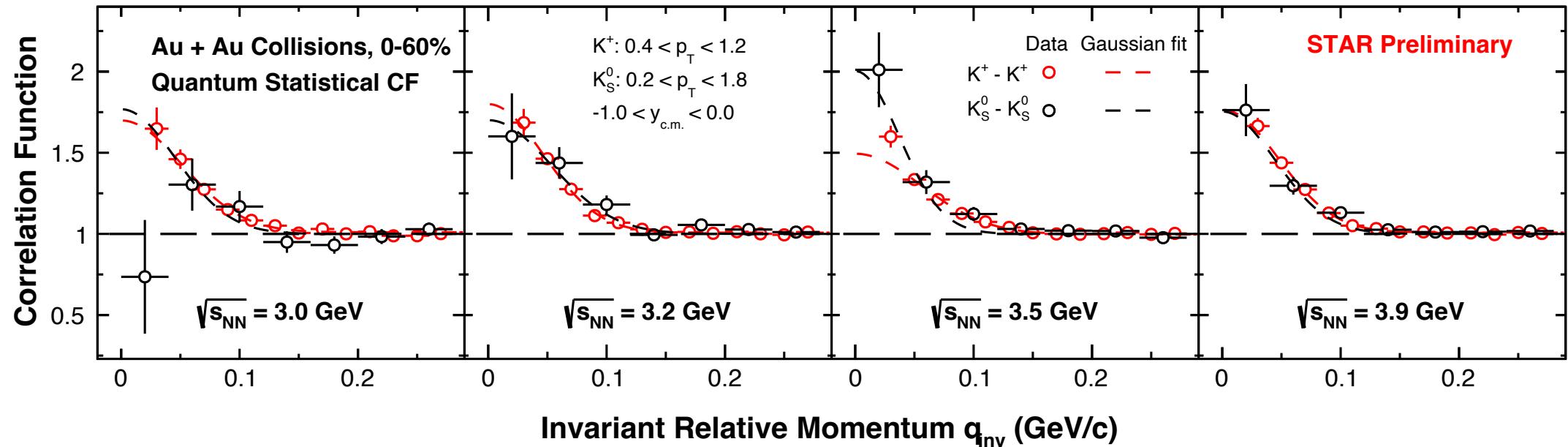
- ❖ UrQMD (provide phase space)^[5,6]
Version: 3.4
- Cascade mode
- ❖ CRAB (generate correlation: QS, FSI)
Version: 3.0b

<https://web.pa.msu.edu/people/pratts/freecodes/crab/home.html>

- ❖ CF of π^+ , K^+ , and K_S^0 with same rapidity range are shown
- ❖ Calculations of UrQMD+CRAB consistent with experimental data
- ❖ Four different scattering amplitude parameters^[1,2,3,4] for K_S^0 compared, and consistent with each other

- [1] *eConfC020620, THAT06 (2002)*
- [2] *Phys. Rev. D 63, 094007 (2001)*
- [3] *Phys. Rev. D 68, 014006 (2003)*
- [4] *Nucl. Phys. B 121, 514–530 (1977)*
- [5] *S.A.Bass et al., Prog.Part.Nucl.Phys. 41 (1998) 225*
- [6] *M.Bleicher et al., J.Phys. G25 (1999) 1859*

Results - Correlation functions

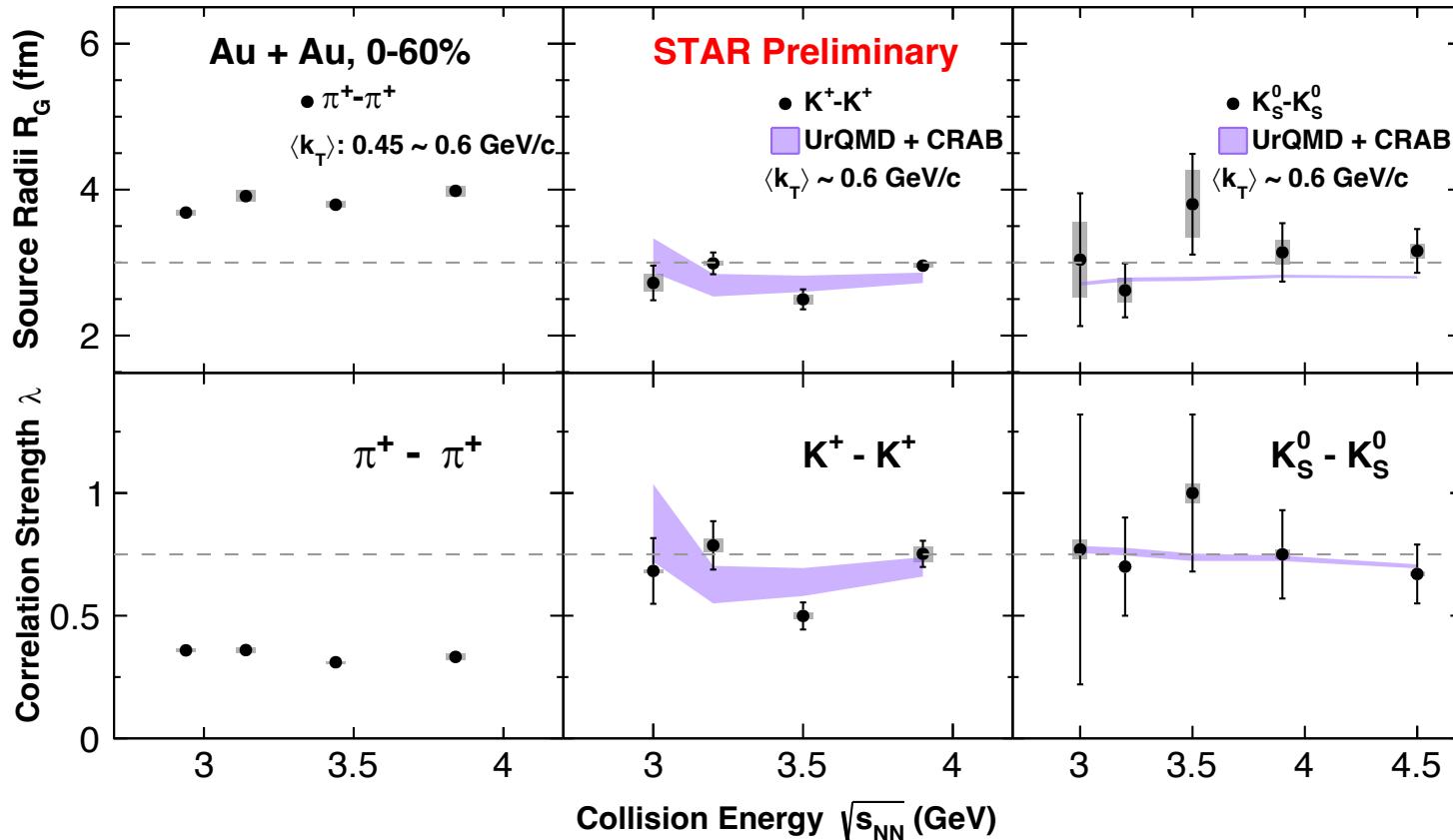


- ❖ CF of $K^+ - K^+$ after subtracting Coulomb effect consistent with $K_S^0 - K_S^0$ without strong interaction

Extraction of QS correlation function:

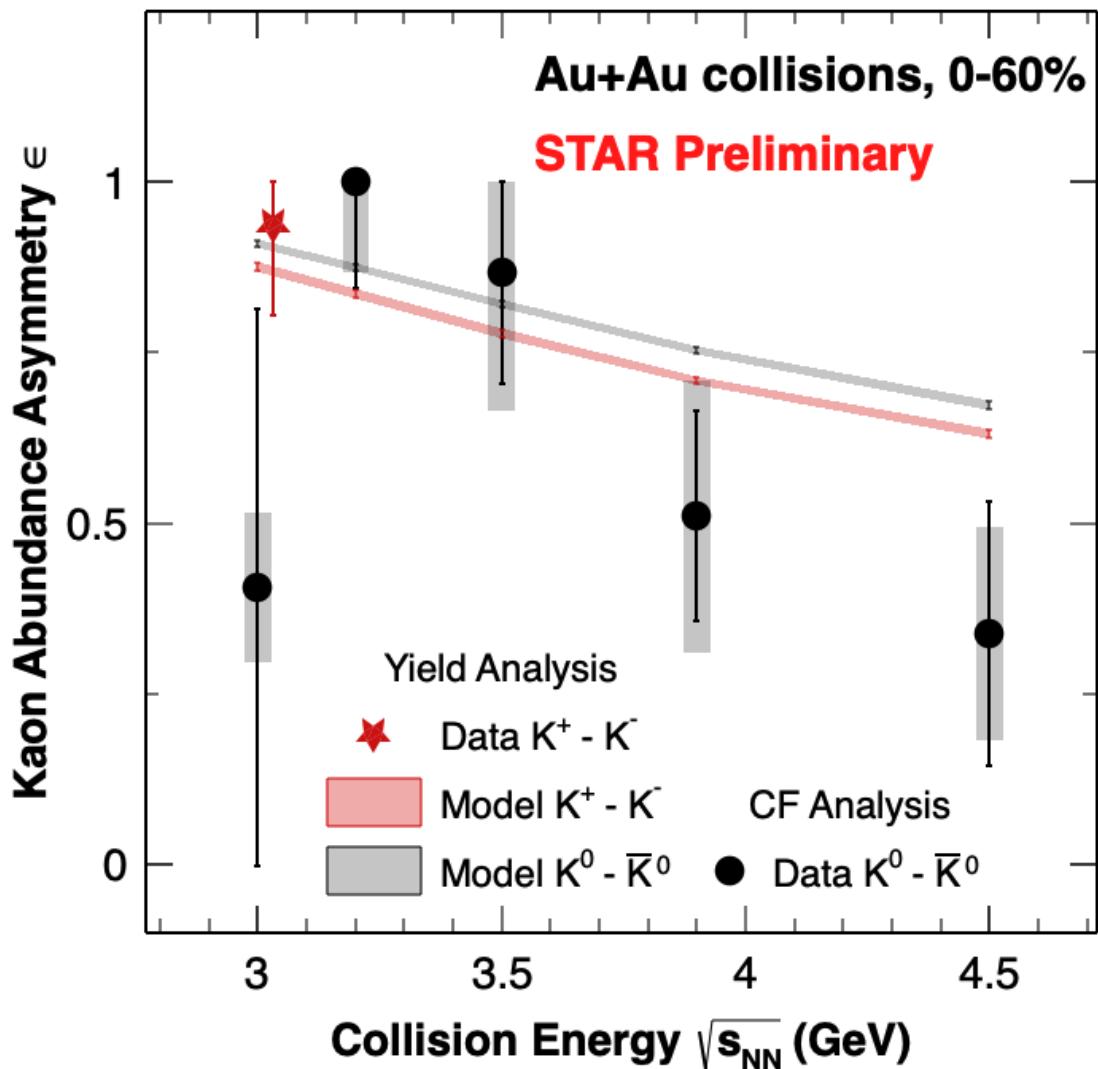
1. Fit the measured correlation function
2. Extract the parameters and get the FSI function
3. Subtract FSI from data points to get the Quantum statistics part contribution

Results - extracted parameters

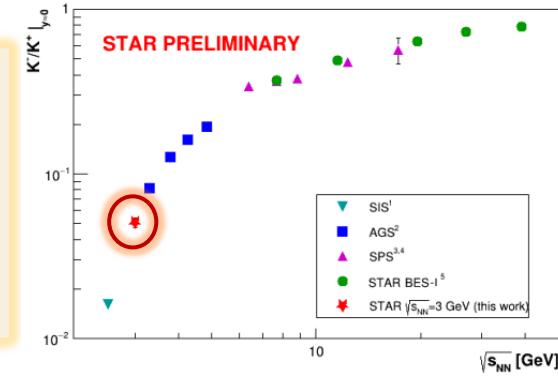


- ❖ No clear energy dependence for R_G and λ , model consistent with data
- ❖ λ of kaons larger than pions', implying less impact from resonances decay
- ❖ Within uncertainties, R_G and λ of charged kaon correlation data consistent with that from neutral kaon

Results – Kaon abundance asymmetry

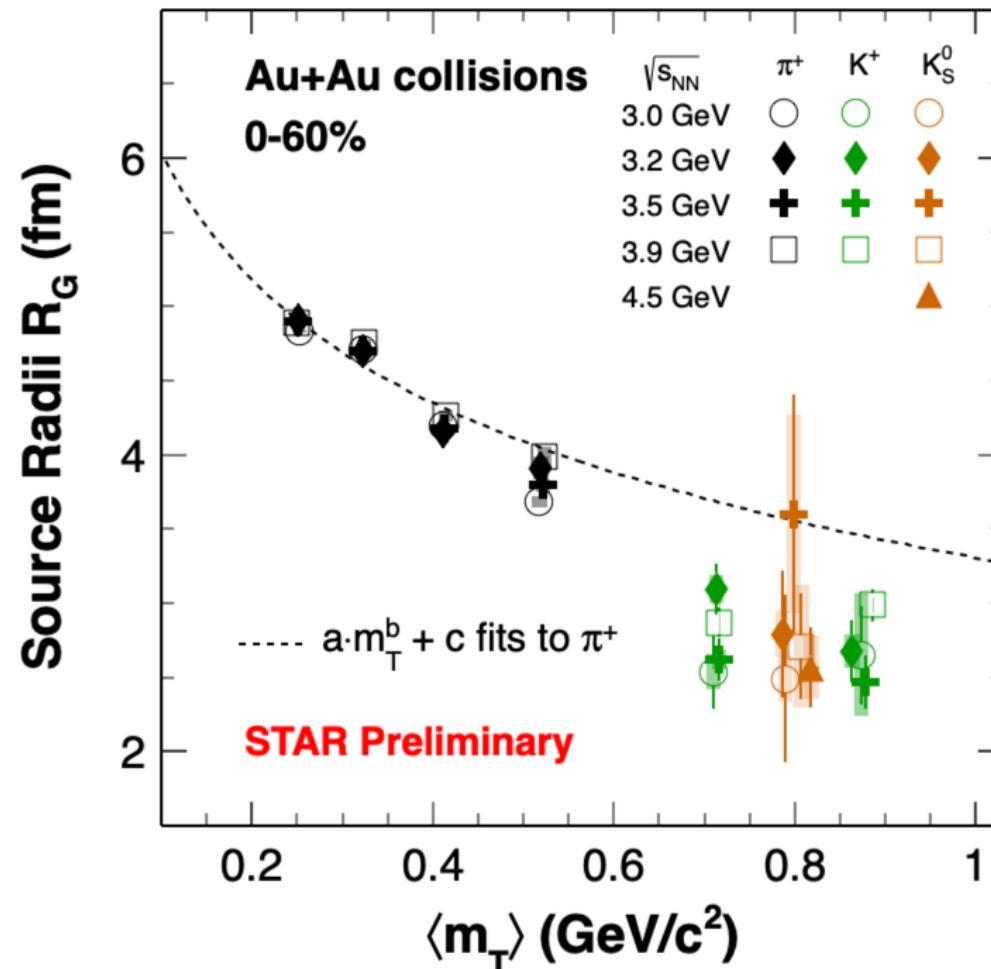


- ❖ Yield Analysis: $\epsilon = \frac{K - \bar{K}}{K + \bar{K}}$
- ❖ CF Analysis: L-L fitting from $K_S^0 - \bar{K}_S^0$ CF



- ❖ K_S^0 is a mixture of s, \bar{s} quarks, thus can extract ϵ by correlation function
- ❖ First measurement of neutral kaon ϵ in heavy ion collisions
- ❖ ϵ of kaon decreases with energy, model reproduce trend of data
 - 1) Associate production dominates at high baryon density
 - 2) Pair production more important at higher energies

Results - m_T - scaling



- ❖ R_G of kaons smaller than that of pions
- ❖ R_G of kaons do not follow m_T - scaling of pions', implying no equilibrium amongst pions and kaons at high baryon density

Summary

- ❖ First measurement of kaon and pion femtoscopy at high baryon density
- ❖ Within uncertainties, extracted parameters of charged kaon correlation data are consistent with that from neutral kaon
- ❖ λ of kaons larger than pions', implying less impact from resonances decay
- ❖ For $\sqrt{s_{NN}} = 3.0 - 4.5$ GeV:
 - 1) No clear energy dependence of R_G and λ while ϵ of kaon decreases with energy
 - 2) R_G of kaons do not follow m_T - scaling of pion's, implying no equilibrium amongst pions and kaons

Thanks for your attention!