



The Ohio State University



# Investigating the nature of the $K_0^*(700)$ state with $\pi^\pm K_S^0$ correlations with ALICE at the LHC

**ALICE Collaboration**

Thomas Humanic (Ohio State University)

## Outline of talk

- Introduction
- Previous ALICE study of  $a_0(980)$
- **New** results from ALICE study of  $K_0^*(700)$
- Summary



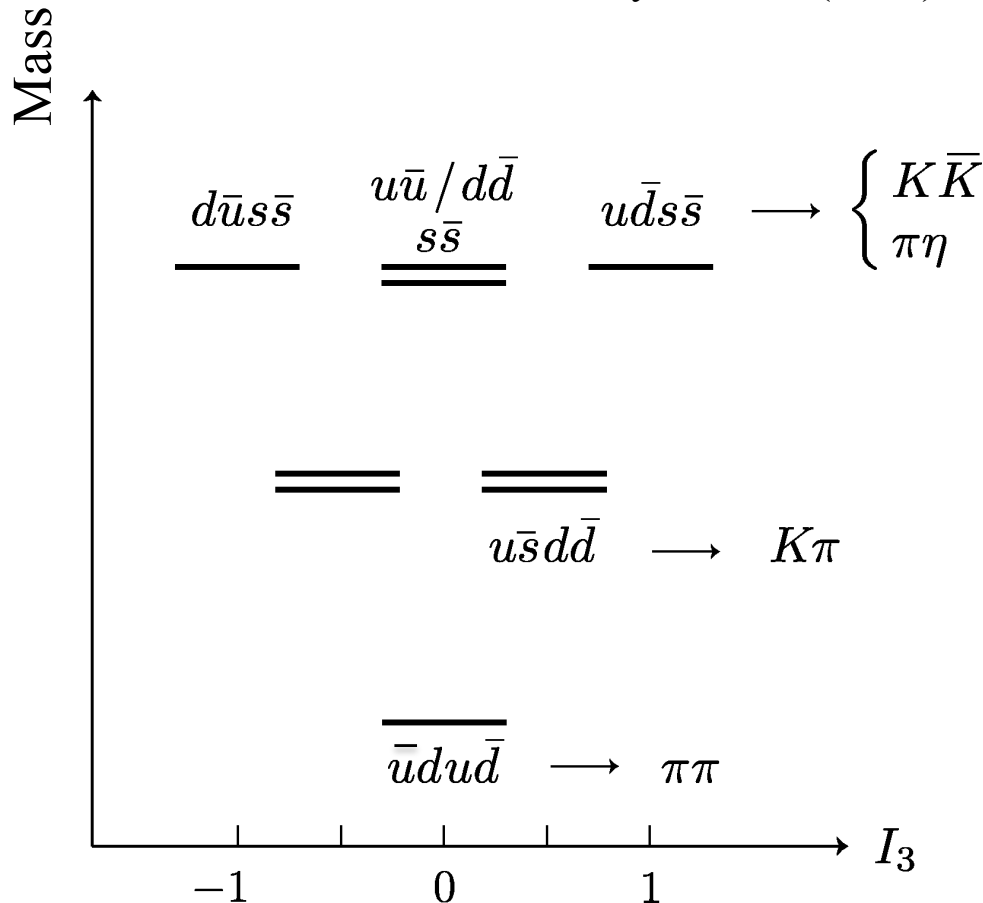
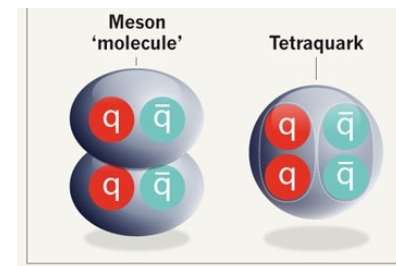
The 21<sup>st</sup> International Conference on Strangeness in Quark Matter  
3-7 June 2024, Strasbourg, France



# Predicted low-lying tetraquark nonet

## Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



Low-lying tetraquark states have been predicted for > 40 years.

Candidate mesons with the expected masses, isospins and decay channels have been found:

e.g.  $a_0(980)$ ,  $f_0(980)$ ,  $K_0^*(700)$ ,  $f_0(500)$ ..

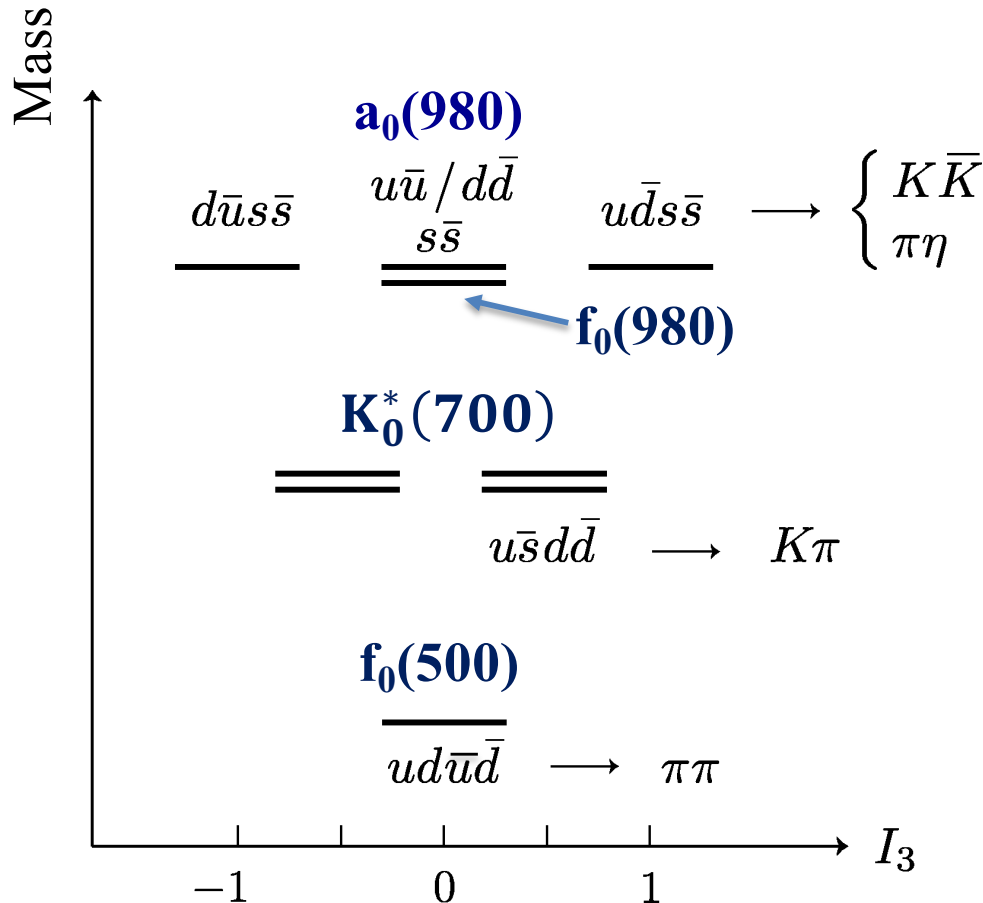
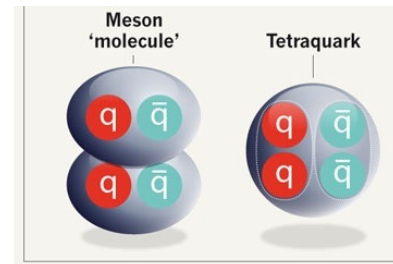
→ But, it is still controversial whether or not these mesons are four-quark states (e.g. see “Non-qq-bar Mesons” in 2021 Review of Particle Physics).

# Predicted low-lying tetraquark nonet with candidate mesons



## Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



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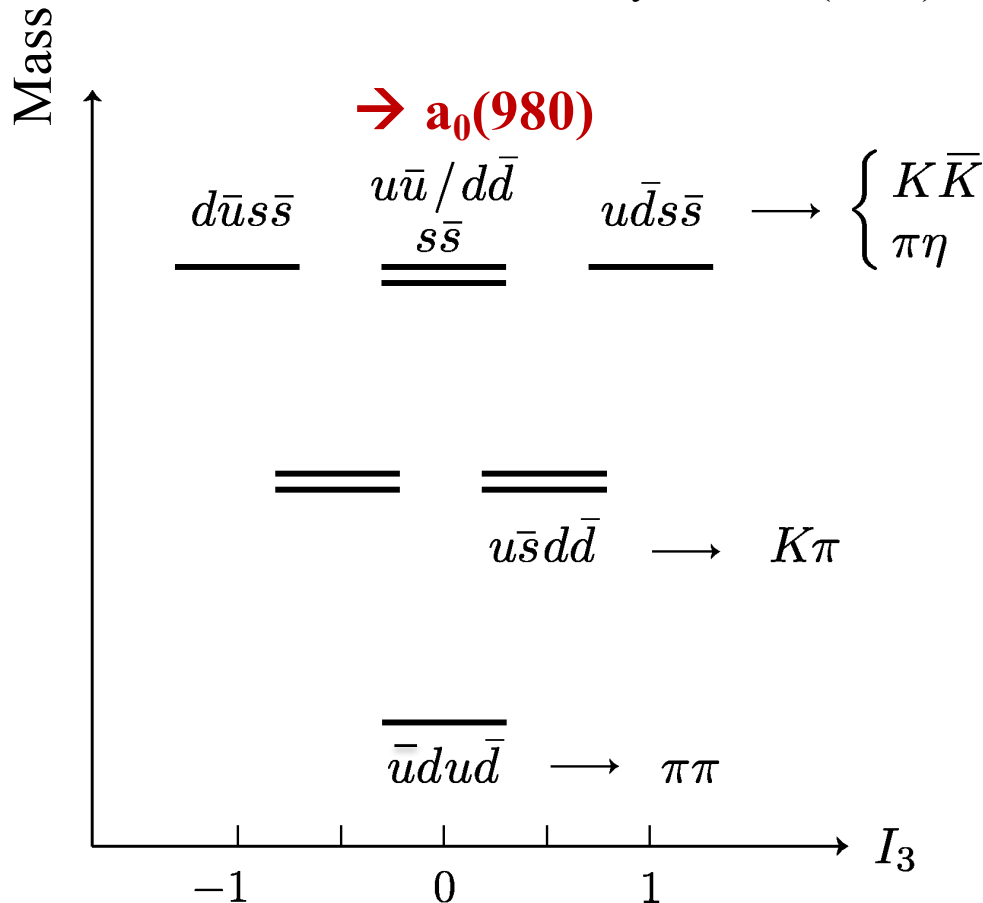
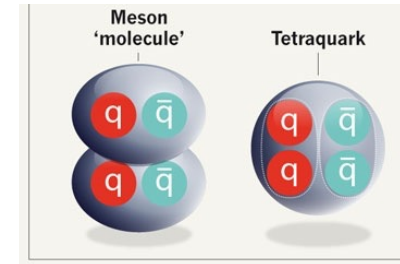
e.g.  $a_0(980)$ ,  $f_0(980)$ ,  $K_0^*(700)$ ,  $f_0(500)$ ..

→ But, it is still controversial whether or not these mesons are four-quark states (e.g. see “Non-qq-bar Mesons” in 2021 Review of Particle Physics).

# Predicted low-lying tetraquark nonet with $a_0(980)$ candidate meson

## Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



$f_0(980)$  [1]

$$I^G(J^{PC}) = 0^+(0^{++})$$

Mass  $m = 990 \pm 20$  MeV  
Full width  $\Gamma = 10$  to 100 MeV

$f_0(980)$  DECAY MODES

DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$\pi\pi$	dominant	476
$K\bar{K}$	seen	36
$\gamma\gamma$	seen	495

$a_0(980)$  [1]

$$I^G(J^{PC}) = 1^-(0^{++})$$

Mass  $m = 980 \pm 20$  MeV  
Full width  $\Gamma = 50$  to 100 MeV

$a_0(980)$  DECAY MODES

DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$\eta\pi$	dominant	319
$K\bar{K}$	seen	†
$\gamma\gamma$	seen	490

From Review of Particle Physics for light quark-antiquark mesons

The  $a_0(980)$  has been studied with  $K_S^0 K^\pm$  femtoscopy in pp and Pb–Pb collisions by ALICE → PLB 774 (2017), PLB 790 (2019), PLB 833 (2022).

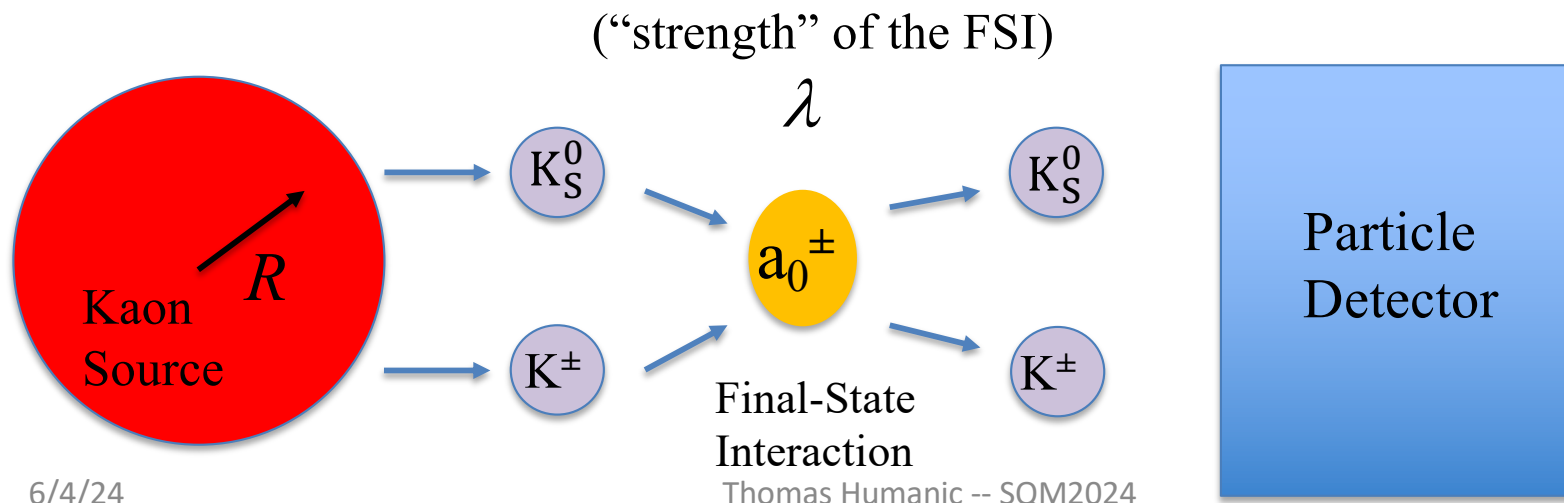
# $K_S^0 K^\pm$ femtoscopy

**(ALICE first to study this!)**

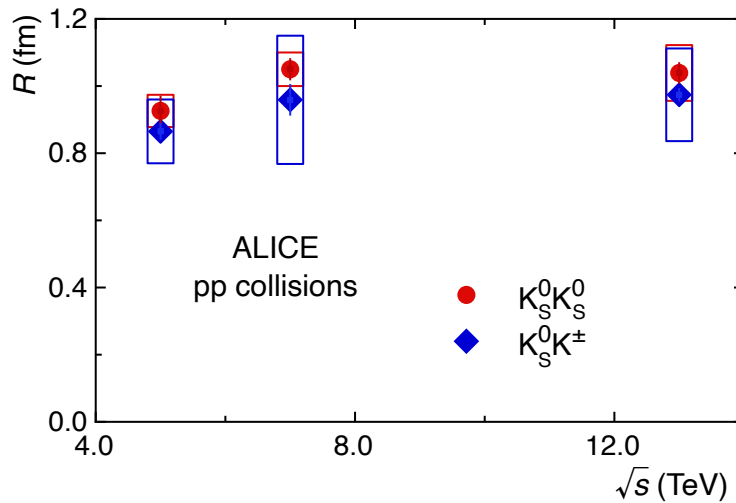
## Pair-wise interactions present (or absent) for $K_S^0 K^\pm$ pairs

- Non-identical pairs  $\rightarrow$  no quantum statistics.
  - $K_S^0$  is uncharged  $\rightarrow$  no Coulomb interaction.
  - $f_0(980)$  resonance is isospin = 0  $\rightarrow$  no  $f_0(980)$  strong interaction.
  - $a_0(980)$  resonance is isospin = 1  $\rightarrow$   $a_0(980)$  strong interaction.
- should be present for both  $K_S^0 K^+$  and  $K_S^0 K^-$  pairs.

**$\rightarrow K_S^0 K^\pm$  femtoscopy selects for the  $a_0(980)^\pm$  as the Final-state Interaction (FSI).**



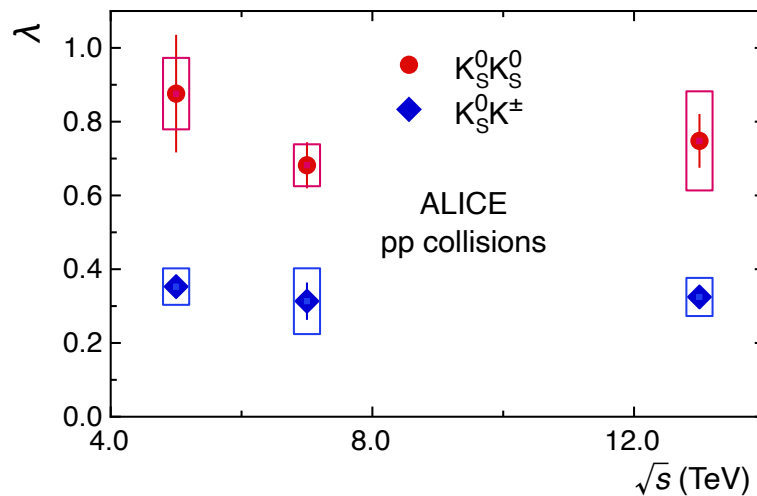
# ALICE results for $K_S^0 K_S^0$ and $K_S^0 K_S^\pm$ femtoscopy in 5.02, 7 and 13 TeV pp collisions (*Phys. Lett. B833 (2022)*)



➤  $a_0(980)$  is the FSI for the  $K_S^0 K_S^\pm$  pair. The  $K_S^0 K_S^0$  correlation function is dominated by quantum statistics due to identical-boson pairs.

➤  $\lambda$  from  $K_S^0 K_S^\pm$  is significantly smaller than  $\lambda$  from  $K_S^0 K_S^0$ .

➔ **tetraquark signature for the  $a_0(980)$ ?**



$$\Rightarrow \left\langle \frac{\lambda_{K_S^0 K_S^\pm}}{\lambda_{K_S^0 K_S^0}} \right\rangle \approx 0.44 \pm 0.07$$

# A simple geometric picture in pp collisions

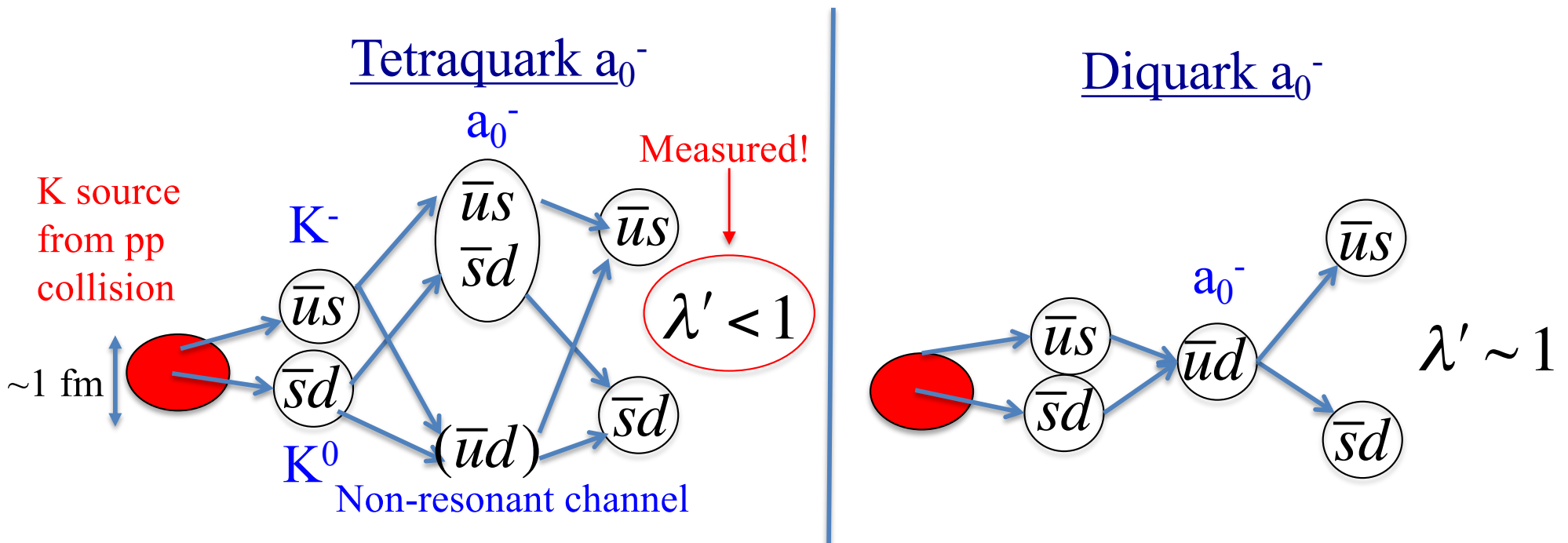


**Tetraquark  $a_0^-$  FSI** -- suppressed due to strange quark annihilation opening up a non-resonant channel.

**Diquark  $a_0^-$  FSI** -- favored from the annihilation process.

Identical kaon  $\lambda$  - parameter

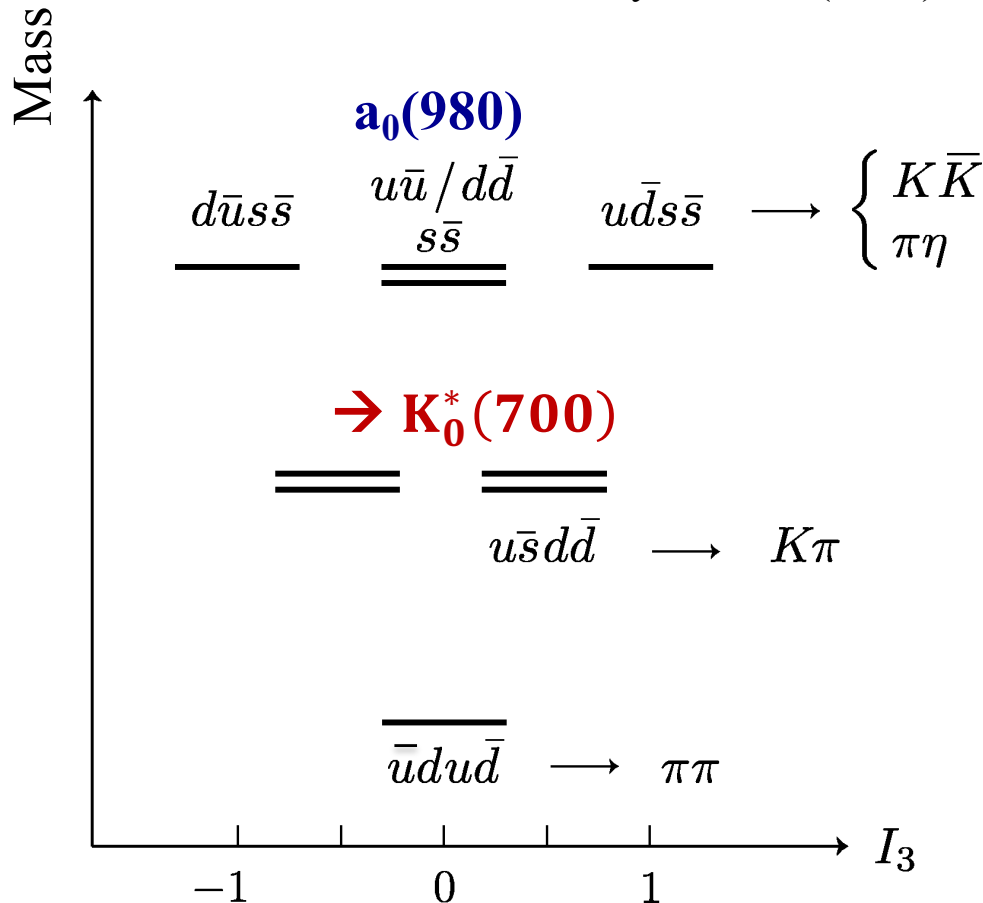
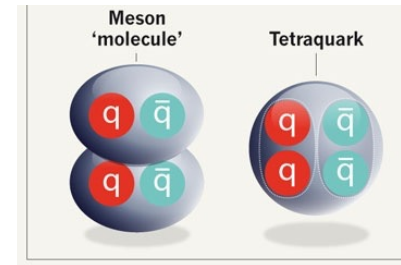
$$\lambda' \equiv \lambda_{K^0 K^-} / \lambda_{KK} \text{ for } \bar{u}s\bar{s}d \text{ vs. } \bar{u}d \text{ } a_0^- \text{ expected from geometry}$$



# Predicted low-lying tetraquark nonet with $K_0^*(700)$ candidate meson

## Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



$K_0^*(700)$

$$I(J^P) = \frac{1}{2}(0^+)$$

Mass (T-Matrix Pole  $\sqrt{s}$ ) =  $(630-730) - i(260-340)$  MeV  
 Mass (Breit-Wigner) =  $824 \pm 30$  MeV  
 Full width (Breit-Wigner) =  $478 \pm 50$  MeV

$K^*(892)$

$$I(J^P) = \frac{1}{2}(1^-)$$

$K^*(892)^\pm$  hadroproduced mass  $m = 891.76 \pm 0.25$  MeV  
 $K^*(892)^\pm$  in  $\tau$  decays mass  $m = 895.5 \pm 0.8$  MeV  
 $K^*(892)^0$  mass  $m = 895.55 \pm 0.20$  MeV ( $S = 1.7$ )  
 $K^*(892)^\pm$  hadroproduced full width  $\Gamma = 50.3 \pm 0.8$  MeV  
 $K^*(892)^\pm$  in  $\tau$  decays full width  $\Gamma = 46.2 \pm 1.3$  MeV  
 $K^*(892)^0$  full width  $\Gamma = 47.3 \pm 0.5$  MeV ( $S = 1.9$ )

$K^*(892)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$P$ (MeV/c)
$K\pi$	$\sim 100$	%	290
$K^0\gamma$	$(2.46 \pm 0.21) \times 10^{-3}$		307
$K^\pm\gamma$	$(1.00 \pm 0.09) \times 10^{-3}$		309
$K\pi\pi$	$< 7$	$\times 10^{-4}$	95% 223

$K_0^*(700)$  decay channel listed in RPP as 100%  $\pi K$  ..... same as for  $K^*(892)$

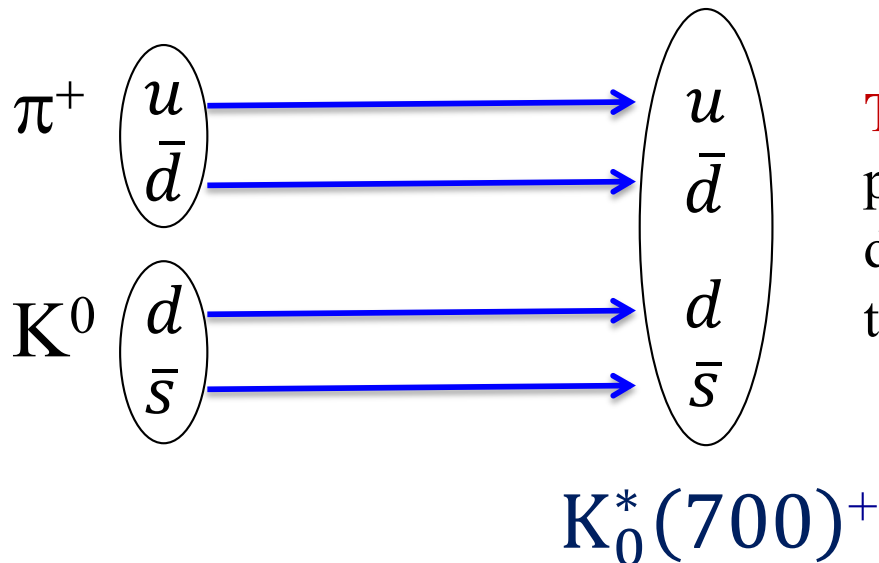
The  $K_0^*(700)$  has been studied with  $\pi^\pm K_S^0$  femtoscopy in 13 TeV pp collisions by the ALICE Collaboration  $\rightarrow$  Paper is submitted to PLB (arXiv:2312.12830v2).



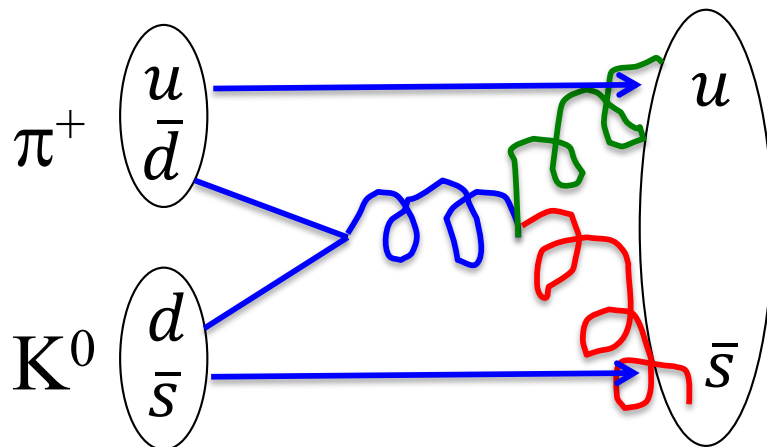
# Two scenarios for FSI of $\pi^+K^0 \rightarrow K_0^*(700)^+ \rightarrow \pi^+K^0$



## Tetraquark vs. Diquark



**Tetraquark** formation is a 1<sup>st</sup>-order process that proceeds through the direct transfer of existing quarks to the  $K_0^*(700)$  from the collision of  $\pi^+K^0$ .



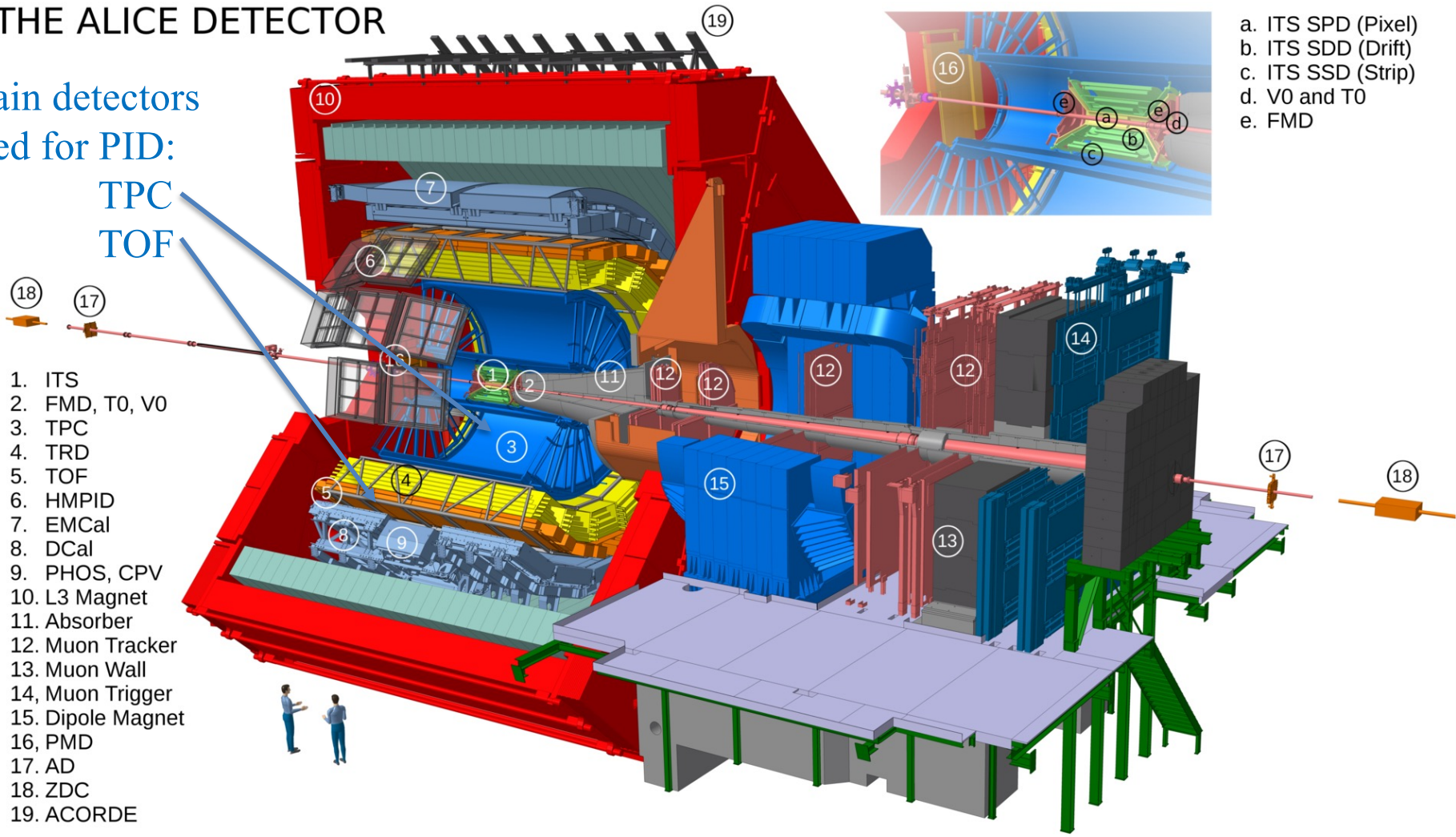
**Diquark** formation is a higher-order process requiring the annihilation of the  $d$  quarks in the  $\pi^+K^0$  collision and transfer of energy via gluons to  $K_0^*(700)$ .

**Can we see a signature of tetraquark vs. diquark in femtoscopy?**

# THE ALICE DETECTOR

Main detectors used for PID:

TPC  
TOF



1. ITS
2. FMD, T0, V0
3. TPC
4. TRD
5. TOF
6. HMPID
7. EMCal
8. DCal
9. PHOS, CPV
10. L3 Magnet
11. Absorber
12. Muon Tracker
13. Muon Wall
14. Muon Trigger
15. Dipole Magnet
16. PMD
17. AD
18. ZDC
19. ACORDE

- a. ITS SPD (Pixel)
- b. ITS SDD (Drift)
- c. ITS SSD (Strip)
- d. V0 and T0
- e. FMD

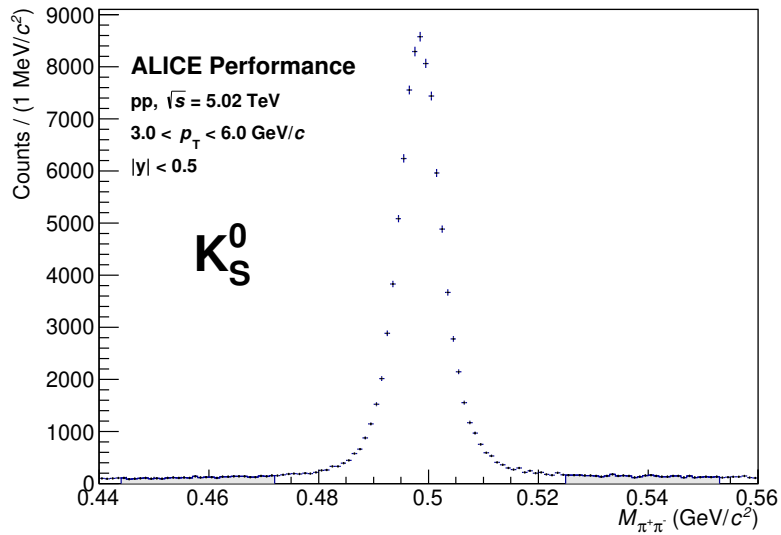
**Run 2 data set used in this analysis**



$\sqrt{s} = 13$  TeV pp collisions, minimum bias trigger

# Excellent PID purity for $K_S^0$ and $\pi^\pm$

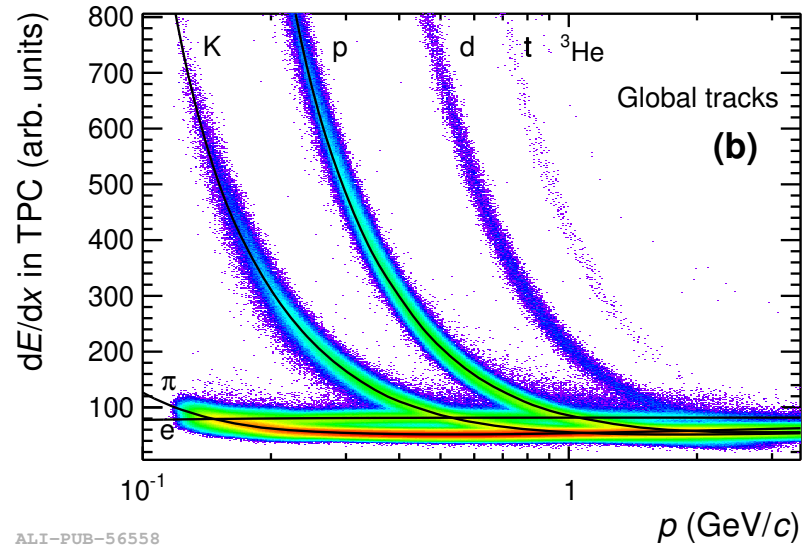
Particle ID using  $K_S^0 \rightarrow \pi^+\pi^-$



ALI-PERF-145079

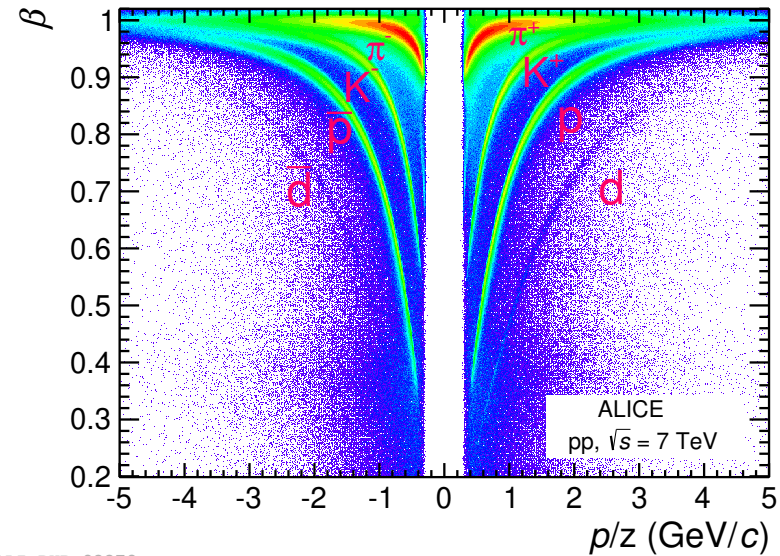
$K_S^0$  purity  $\sim 98\%$

$dE/dx$



ALI-PUB-56558

TOF



ALI-PUB-92279

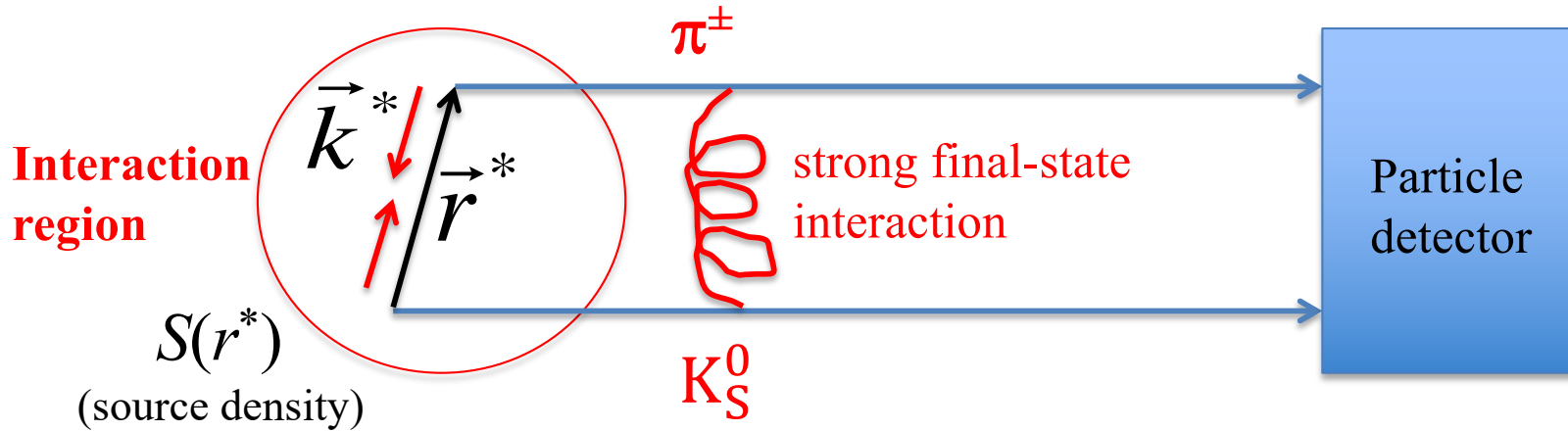
$\pi^\pm$  purity  $\sim 98\%$

# Femtoscscopy using strong final-state interactions

R. Lednický and V.L. Lyuboshits, (Sov. J. Nucl. Phys. 35 (1982) 770)



Consider the correlations of two **non-identical particles**, e.g.  $\pi^\pm K_S^0$ , emitted from the interaction region



$\vec{r}^*$  → relative distance between the particle emission points in the pair reference frame.  
 $\vec{k}^*$  → momentum of the particles in the pair reference frame.

The wave function describing the elastic interaction between the particles is:

$$\Psi_{-\vec{k}^*} = e^{-\vec{k}^* \cdot \vec{r}^*} + f(\vec{k}^*) \frac{e^{ik^* r^*}}{r^*}$$

plane wave      S-wave final-state interaction (FSI) term

S-wave scattering amplitude



ALICE

Correction to spherical outgoing wave assumption

## Two-particle correlation function:

$$C(k^*) = \int d^3\vec{r}^* S(r^*) |\Psi_{-\vec{k}^*}(\vec{r}^*)|^2, \text{ where } S(r^*) \sim e^{-\frac{r^{*2}}{4R^2}}$$

Radius parameter

Lambda parameter

$$\rightarrow C(k^*) = 1 + \lambda\alpha \left[ \frac{1}{2} \left| \frac{f(k^*)}{R} \right|^2 + \frac{2\Re f(k^*)}{\sqrt{\pi}R} F_1(2k^*R) - \frac{\Im f(k^*)}{R} F_2(2k^*R) + \overline{\Delta C} \right]$$

Integral functions

Assume the FSI of the  $\pi^\pm K_S^0$  is due to a **Resonance**  $\rightarrow f(k^*) = \frac{\gamma}{M_R^2 - s - i\gamma k^*}$

$\gamma$  is the coupling parameter for the decay of the resonance into  $\pi^\pm K_S^0$   $\rightarrow \Gamma_R = \frac{\langle k^* \rangle}{M_R} \gamma$

where  $M_R$  and  $\Gamma_R$  are the mass and width of the FSI resonance, and  $\langle k^* \rangle$  is the average  $k^*$  over the fit range.

**$C(k^*)$  is measured experimentally as**  $\rightarrow C(k^*) = \frac{A(k^*)}{B(k^*)}$

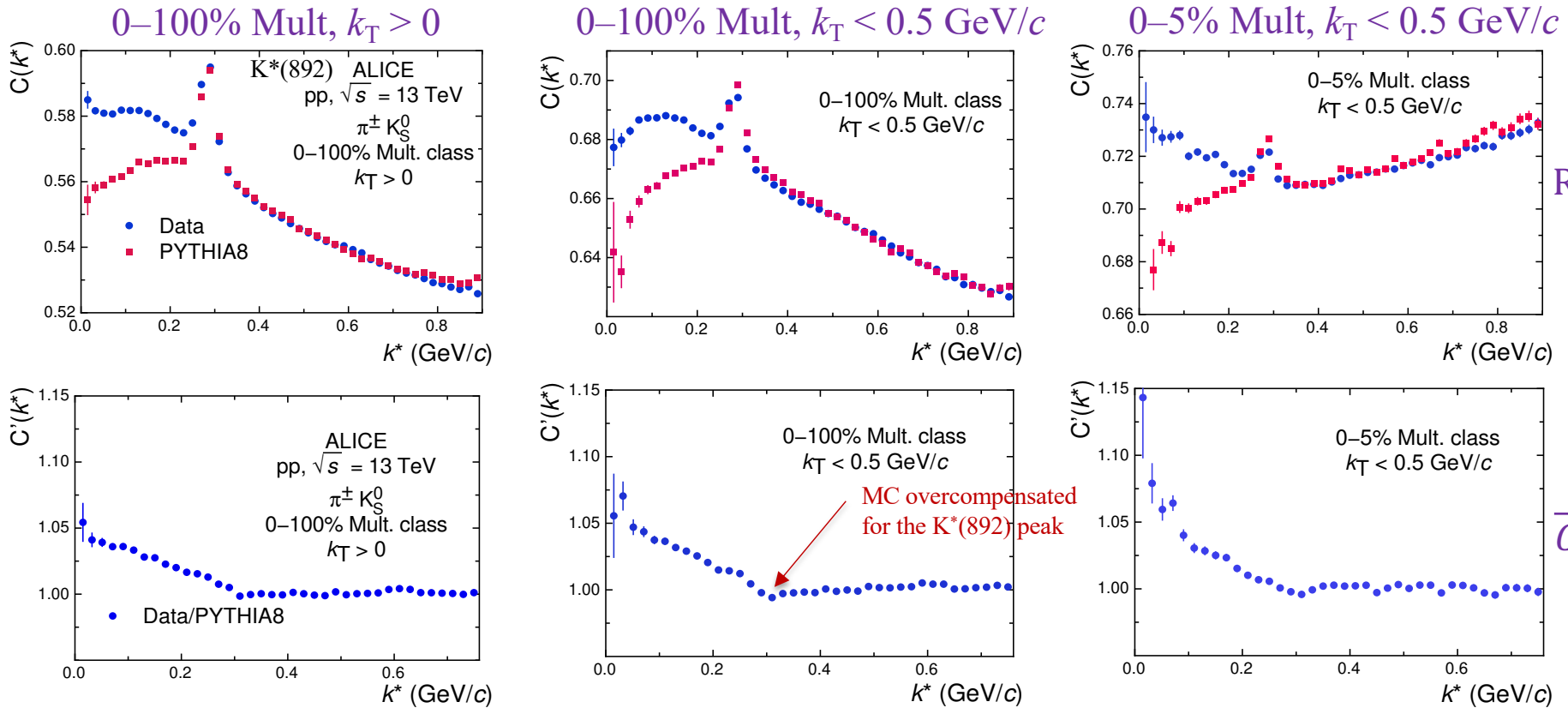
where  $A(k^*)$  is the measured distribution of particle pairs from the same event in a  $k^*$  bin, and  $B(k^*)$  is the reference distribution of particle pairs from mixed events in a  $k^*$  bin.

# Raw $C(k^*)$ from 13 TeV pp $\rightarrow \pi^\pm K_S^0$ data compared with PYTHIA8

(PYTHIA8 run through GEANT to simulate ALICE data)



NEW



arXiv:2312.12830v2

Analyze these three sets of  $C(k^*)$  with different kinematic cuts in order to extract the multiplicity and  $k_T$  dependences of  $\lambda$  and  $R$ .

PYTHIA8 does a good job describing the baseline of the data.

Data show large enhancement at  $k^* \sim 0$  compared with PYTHIA8.

$\rightarrow$  Is the extra enhancement in the data due to  $K_0^*(700)$  FSI ??

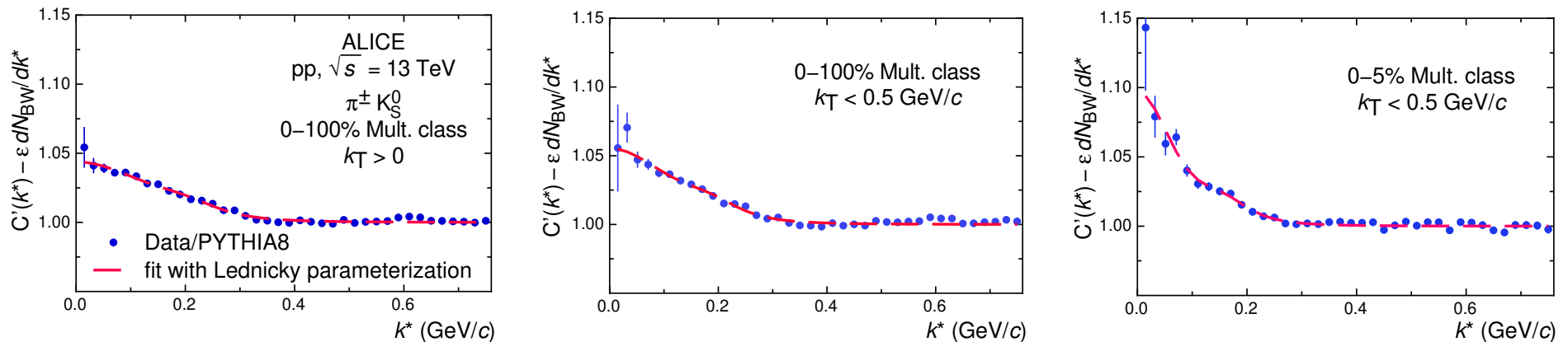
Add a Breit-Wigner resonance term to the Lednicky equation to fit out the small  $K^*(892)$  overcompensation in the MC:

$$C'(k^*) = C(k^*) + \varepsilon \frac{dN_{BW}}{dm} \frac{dm}{dk^*} \quad \text{where,} \quad \frac{dN_{BW}}{dm} \propto \frac{\Gamma_{892}}{(m - m_{892})^2 + \Gamma_{892}^2/4}$$

→ Fit  $C'(k^*)$  to  $C_{\text{data}}(k^*)/C_{\text{MC}}(k^*)$ , with fit parameters  $R, \lambda, M_R, \gamma$  and  $\varepsilon$

NEW

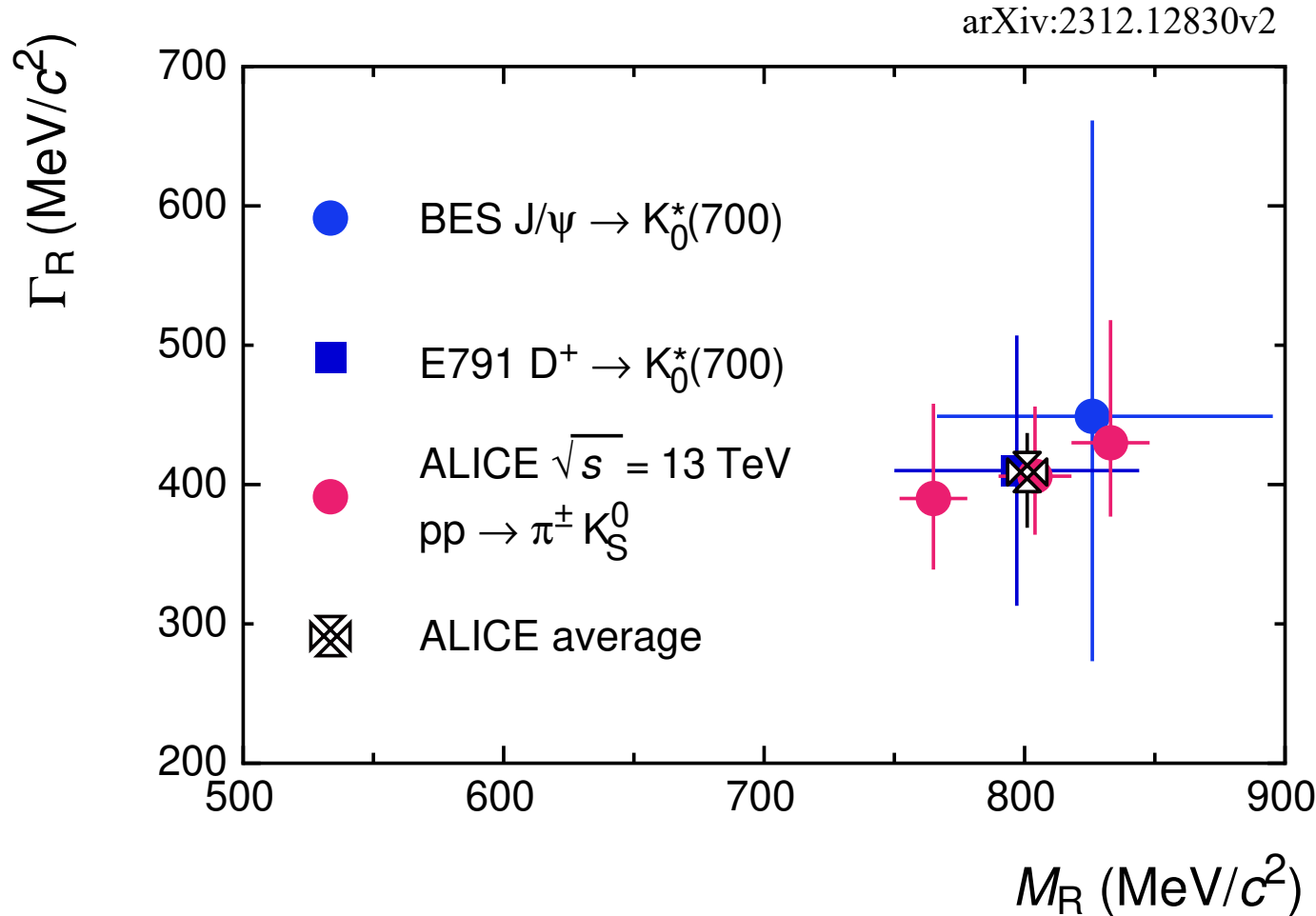
Lednicky + BW fits to data/PYTHIA8 for 13 TeV pp →  $\pi^\pm K_S^0$



arXiv:2312.12830v2

The Lednicky equation, assuming a resonance FSI, does a good job fitting the correlation function for each case.

# Results of Lednický fits to 13 TeV $pp \rightarrow \pi^\pm K_S^0$ for $(M_R, \Gamma_R)$ and comparisons with other measurements



NEW

BES Collab.  
PLB 698 (2011)

E791 Collab.  
PRL 89 (2002)

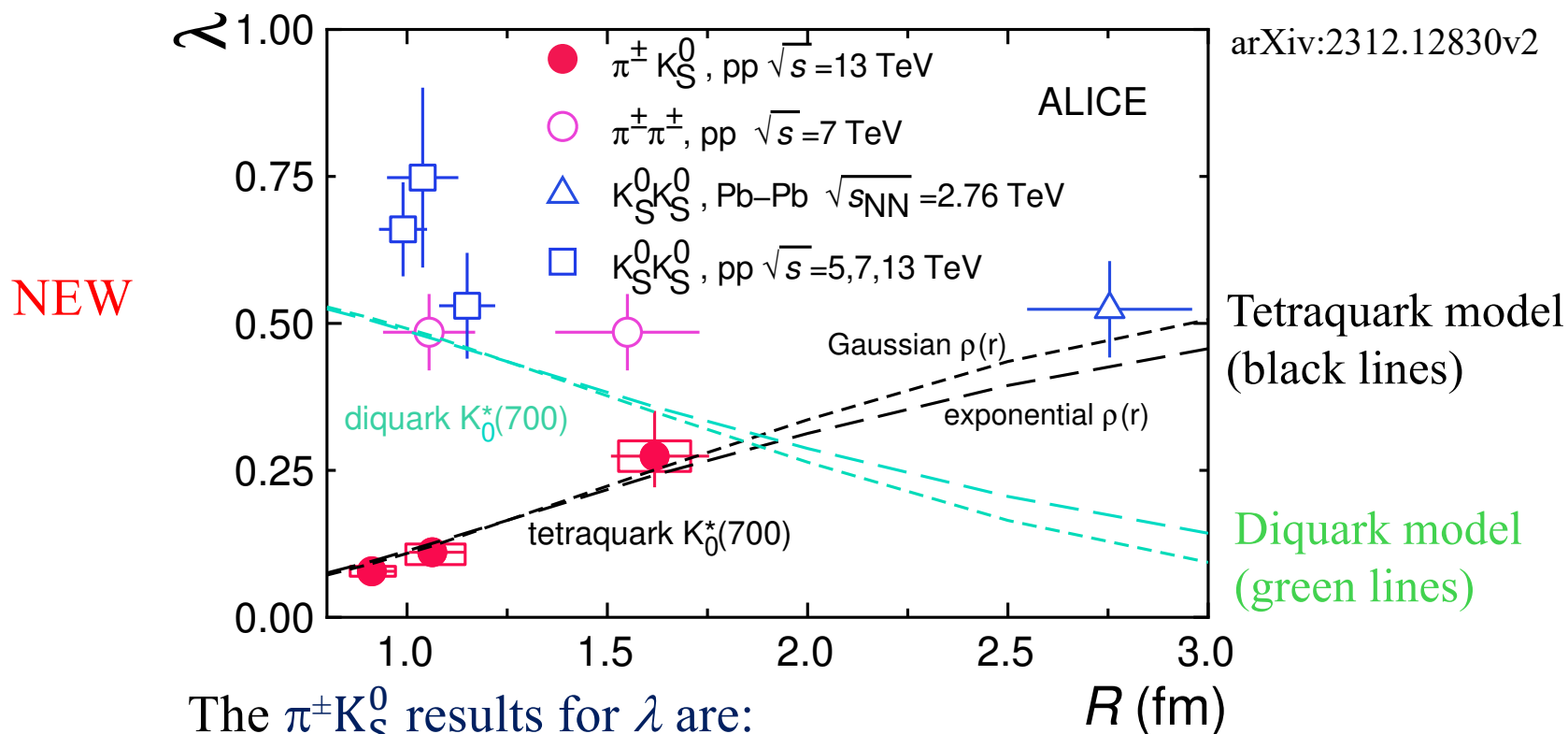
The  $\pi^\pm K_S^0$   $\Gamma_R$  and  $M_R$  agree with BES and E791 measurements of  $K_0^*(700)$ .  
**→ Shows that the  $\pi^\pm K_S^0$  FSI is due to the  $K_0^*(700)$ .**



# Results of Lednický fits to 13 TeV $pp \rightarrow \pi^\pm K_S^0$ for $(R, \lambda)$ and comparisons with other measurements and a toy model



$\lambda$  vs  $R$  from published ALICE  $pp$ ,  $Pb-Pb \rightarrow K_S^0 K_S^0$ ,  $\pi\pi$  (PLB 833 (2022), PRC92 (2015), PRD84 (2011)) and the new 13 TeV  $pp \rightarrow \pi^\pm K_S^0$  results.



The  $\pi^\pm K_S^0$  results for  $\lambda$  are:

- smaller than for  $K_S^0 K_S^0$  and  $\pi\pi$ .
  - increase with  $R$ , unlike  $K_S^0 K_S^0$ ,  $\pi\pi$ .
  - consistent with the Tetraquark toy model  $R$  dependence.
- ➔ **Behavior expected for a tetraquark  $K_0^*(700)$ .**

# Summary

- $K_S^0 K^\pm$  femtoscopic analyses in  $\sqrt{s_{NN}} = 2.76$  TeV Pb–Pb, and  $K_S^0 K^\pm$  and  $K_S^0 K_S^0$  analyses in  $\sqrt{s} = 5.02, 7$  and 13 TeV pp collisions from ALICE are published in PLB

## Main physics take-away:

**A simple geometric model used to explain these results is suggestive of the  $a_0(980)$  being a tetraquark state.**

- $\pi^\pm K_S^0$  femtoscopic analysis in  $\sqrt{s} = 13$  TeV pp collisions from ALICE was shown.

## Main physics take-aways:

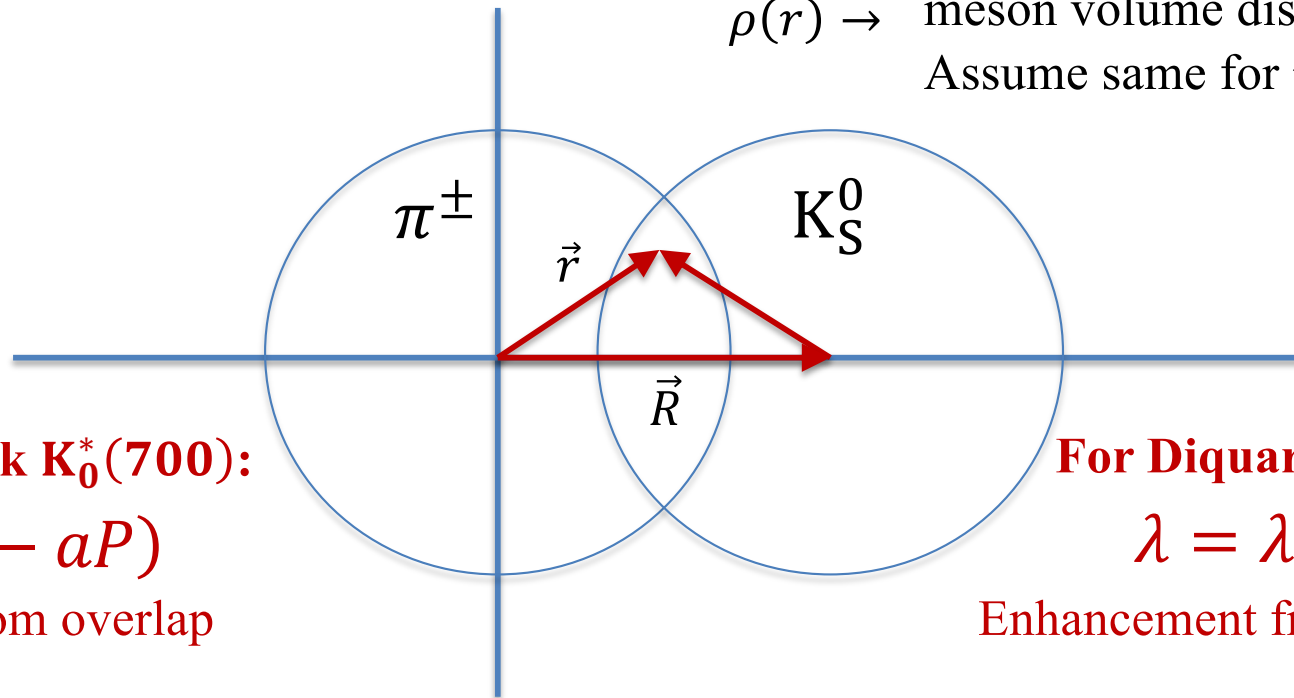
- 1) The FSI is shown to be due to the formation of the  $K_0^*(700)$ .
- 2) The extracted  $R$  parameters are comparable to those from published  $\pi\pi$  and  $K_S^0 K_S^0$  measurements in pp collisions.
- 3) The  $\lambda$  parameter is much smaller than in the identical boson measurements.
- 4) The dependence of  $\lambda$  on  $R$  is as expected by a geometric toy model assuming a tetraquark  $K_0^*(700)$ .**

# Backup slides

# Toy model based on geometry to describe R dependence of $\lambda$ for 13 TeV pp $\rightarrow \pi^\pm K_S^0$



$\rho(r) \rightarrow$  meson volume distribution  
Assume same for  $\pi^\pm$  and  $K_S^0$



**For Tetraquark  $K_0^*(700)$ :**

$$\lambda = \lambda_0(1 - aP)$$

Suppression from overlap

**For Diquark  $K_0^*(700)$ :**

$$\lambda = \lambda_0(aP)$$

Enhancement from overlap

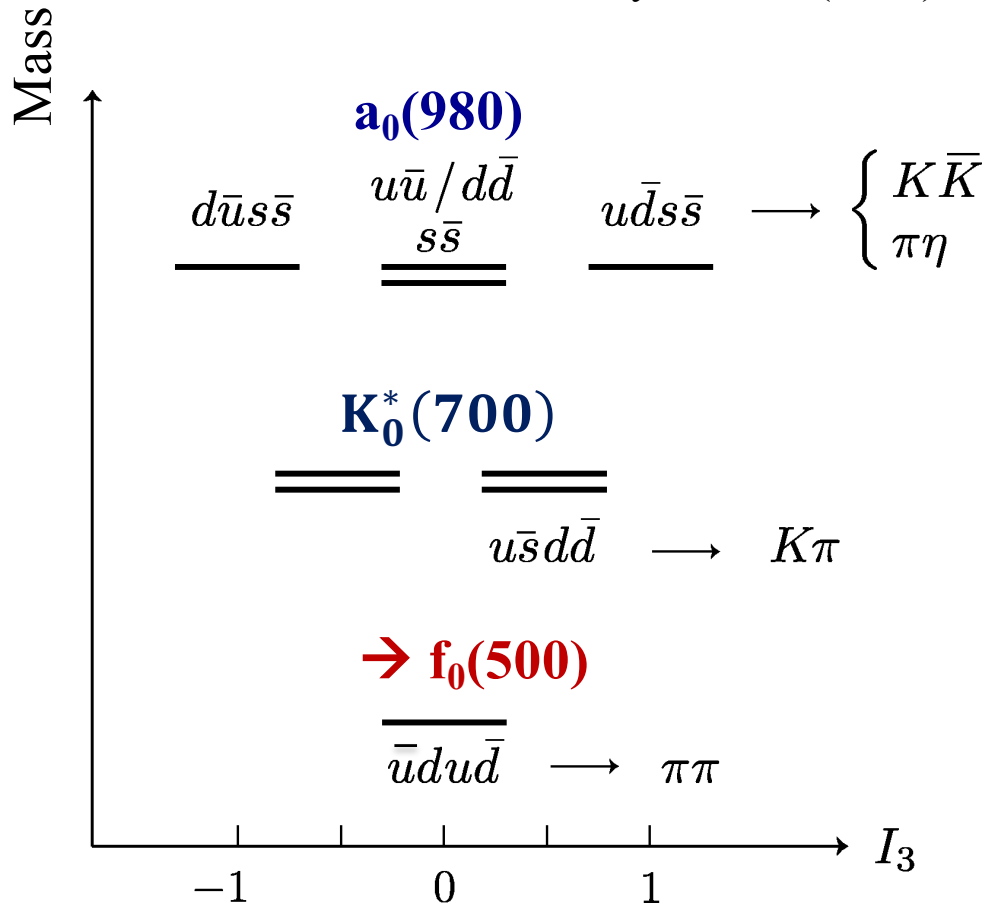
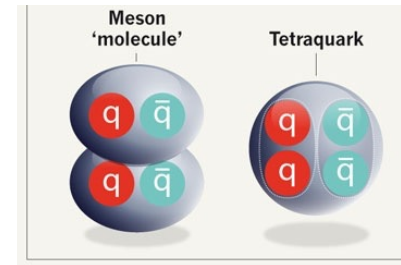
$$P \equiv \frac{\int \rho(r)\rho(|\vec{r} - \vec{R}|)dV}{\int [\rho(r)]^2 dV} \longrightarrow \text{“Overlap Probability”} \quad a \rightarrow \text{“}d - \bar{d}\text{ annihilation efficiency”}$$

Try two cases:  $\left\{ \begin{array}{l} \rho(r) \propto e^{-r^2/2\sigma^2} \quad \lambda_0 = 0.6, \quad \sigma = 1.1 \text{ fm}, \quad a = 1 \\ \rho(r) \propto e^{-r/r_0} \quad \lambda_0 = 0.6, \quad r_0 = 0.85 \text{ fm}, \quad a = 1 \end{array} \right.$

# Predicted low-lying tetraquark nonet with $f_0(500)$ candidate meson

## Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



**$f_0(500)$**   $I^G(J^{PC}) = 0^+(0^{++})$

also known as  $\sigma$ ; was  $f_0(600)$

See the review on "Scalar Mesons below 1 GeV."

Mass (T-Matrix Pole  $\sqrt{s}$ ) =  $(400-550) - i(200-350)$  MeV

Mass (Breit-Wigner) = 400 to 800 MeV

Full width (Breit-Wigner) = 100 to 800 MeV

$f_0(500)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$\pi\pi$	seen	-
$\gamma\gamma$	seen	-

**$\rho(770)$**   $I^G(J^{PC}) = 1^+(1^{--})$

See the review on "Spectroscopy of Light Meson Resonances."

Mass  $m = 775.26 \pm 0.23$  MeV

Full width  $\Gamma = 149.1 \pm 0.8$  MeV

$\rho(770)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	$p$ (MeV/c)
$\pi\pi$	$\sim 100$	%	363

**→ Recently initiated the study of the  $f_0(500)$  with  $\pi^+\pi^-$  femtoscopy in 13 TeV pp collisions by ALICE → Work in progress!**