



# SOM 2024

The 21<sup>st</sup> International Conference on Strangeness in Quark Matter  
3-7 June 2024, Strasbourg, France



## Study of baryon-strangeness and charge-strangeness correlations in Pb–Pb collisions at 5.02 TeV with ALICE

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(for the ALICE Collaboration)

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# Motivation

Correlations between net-conserved quantities such as net-baryon ( $B$ ), net-charge ( $Q$ ), and net-strangeness ( $S$ ) number can **provide valuable insights into the QCD phase structure**:

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- sensitive probes for the equation of state and are directly related to the QCD thermodynamic susceptibilities
- can be studied in the thermal model (HRG) and measurements can constrain the thermal properties of the QCD medium formed at LHC

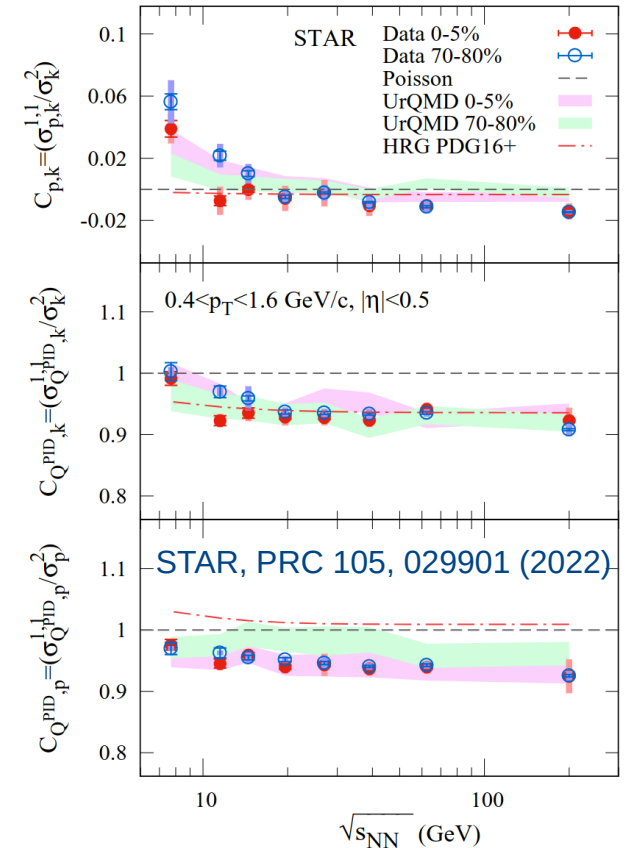
$$\chi_{B,S,Q}^{lmn} = \left[ \frac{\partial^{(l+m+n)} (P(\hat{\mu}_B, \hat{\mu}_S, \hat{\mu}_Q)/T^4)}{\partial \hat{\mu}_B^l \partial \hat{\mu}_S^m \partial \hat{\mu}_Q^n} \right]_{\vec{\mu}=0}$$

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- Compared to similar measurements at lower energy, STAR experiment at RHIC

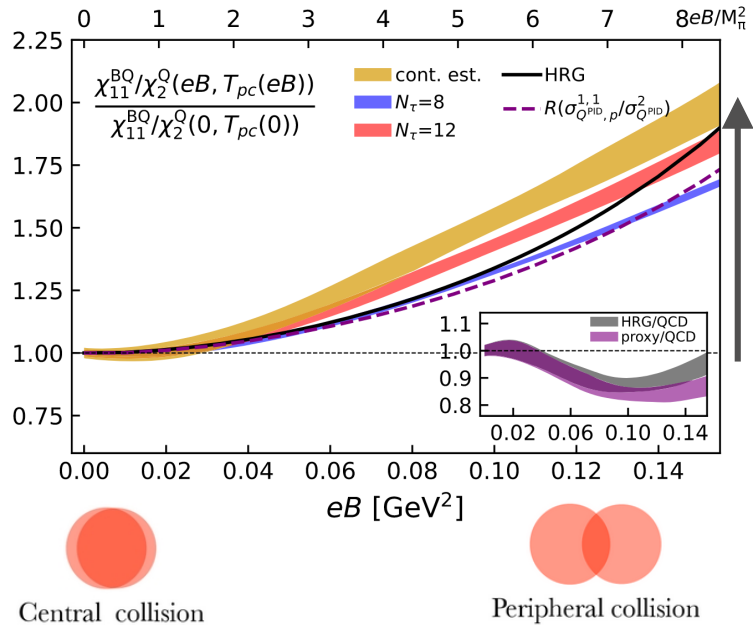


# Motivation



LQCD suggests that correlations of  $B$  and  $Q$  can be a useful probe to detect the imprints of magnetic fields in the final stages of heavy-ion collisions.

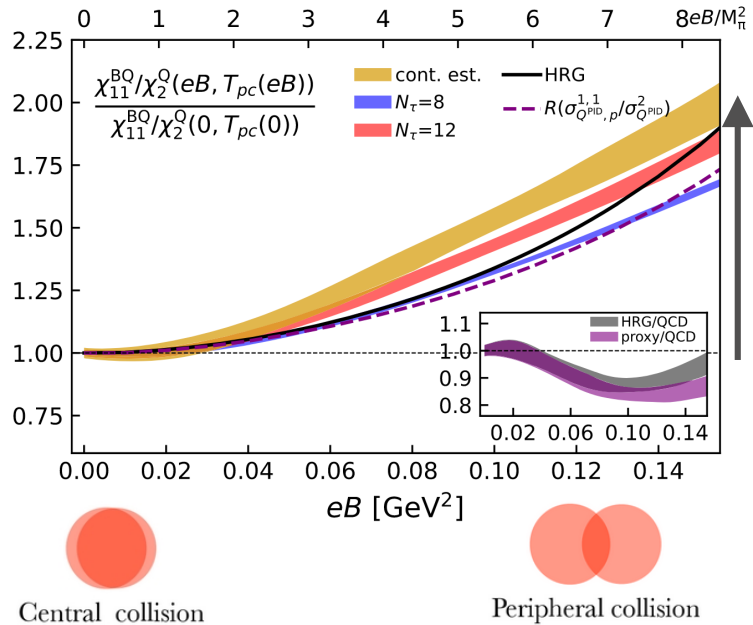
H.-T. Ding et al., *Phy.Rev.Lett* 132 (2024) 201903



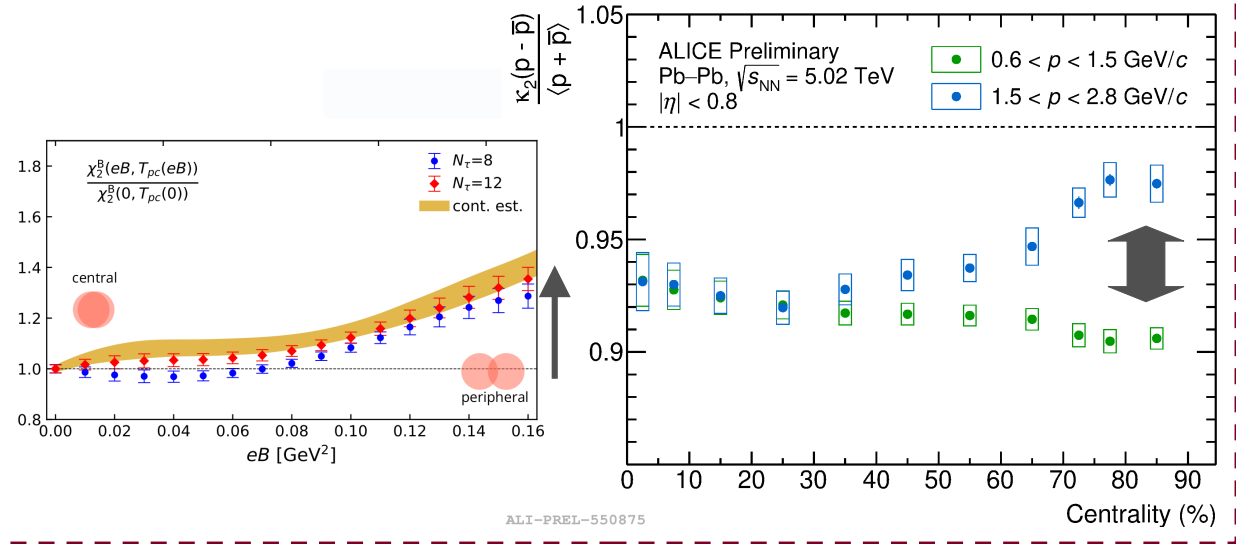
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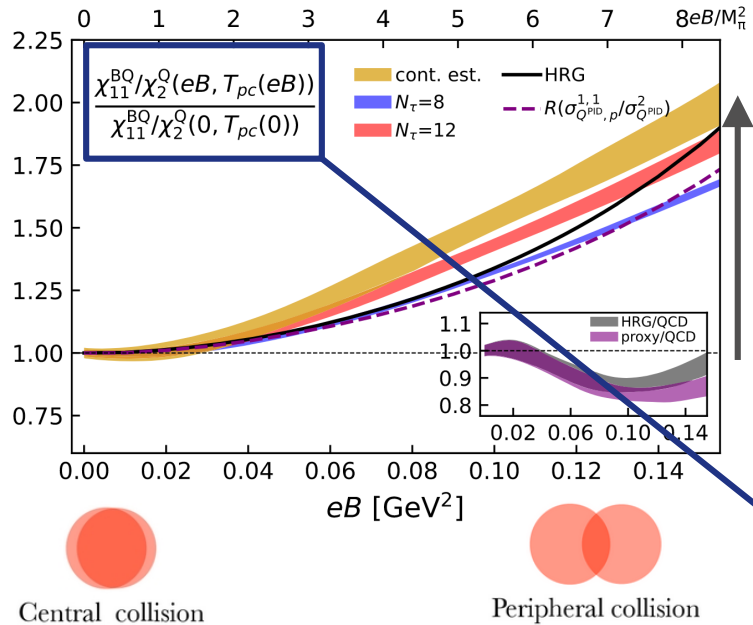
## Quark Matter 2023: 2<sup>nd</sup> order net-proton cumulant



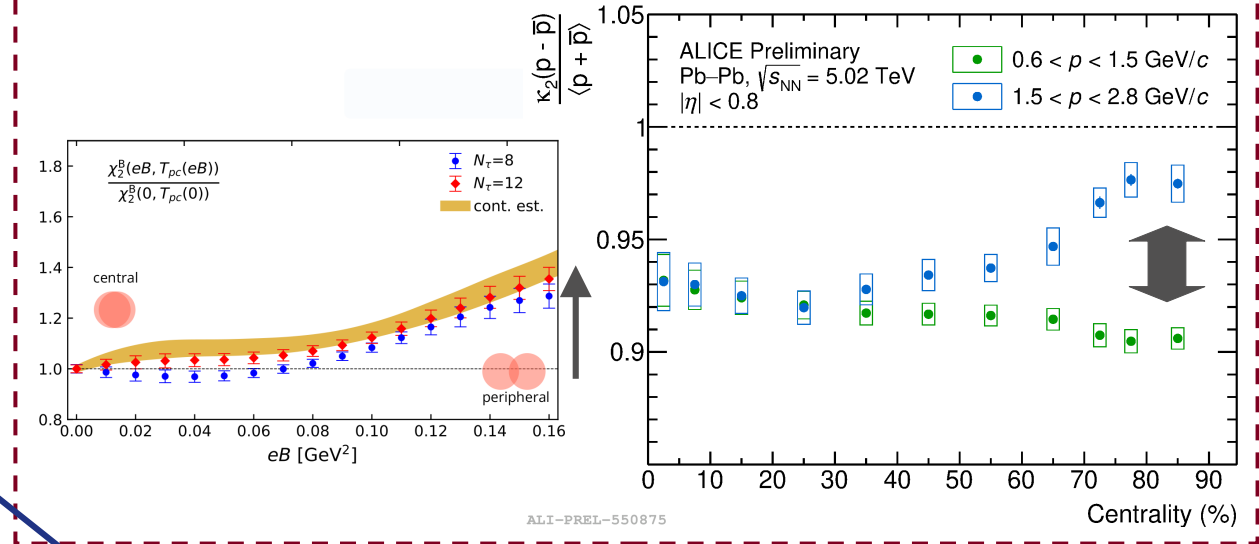
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## Quark Matter 2023: 2<sup>nd</sup> order net-proton cumulant



Can centrality dependence of this quantity reveal a magnetic field in late-stage heavy-ion collisions?

# Observables

The susceptibilities of  $B$ ,  $S$ ,  $Q$  are related to the cumulants ( $\sigma$ ) of the event-by-event distribution of the associated conserved charges:

$$\chi_{B,S,Q}^{lmn} = \frac{1}{VT^3} \sigma_{B,S,Q}^{lmn}$$

**Definitions:**  $Q \rightarrow$  net-charge |  $B \rightarrow$  net-baryon |  $S \rightarrow$  net-strangeness



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Off-diagonal  
cumulants

$$\begin{aligned} \sigma_{B,S}^{11} &= \langle BS \rangle - \langle B \rangle \langle S \rangle \\ \sigma_{Q,S}^{11} &= \langle QS \rangle - \langle Q \rangle \langle S \rangle \\ \sigma_{Q,B}^{11} &= \langle QB \rangle - \langle Q \rangle \langle B \rangle \end{aligned}$$

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$$\begin{aligned} \sigma_Q^2 &= \langle Q^2 \rangle - \langle Q \rangle^2 \\ \sigma_B^2 &= \langle B^2 \rangle - \langle B \rangle^2 \\ \sigma_S^2 &= \langle S^2 \rangle - \langle S \rangle^2 \end{aligned}$$



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$$\delta N_\alpha = (N_{\alpha+} - N_{\alpha-}) - \langle (N_{\alpha+} - N_{\alpha-}) \rangle$$

$\alpha, \beta \rightarrow \mathbf{Q, B, or S}$

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Experiments:

**Proxies:**

- $Q \rightarrow$  net-pion+net-kaon+net-proton
- $B \rightarrow$  net-proton (p)
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$\rightarrow$  this is what we measure

# ALICE Detector



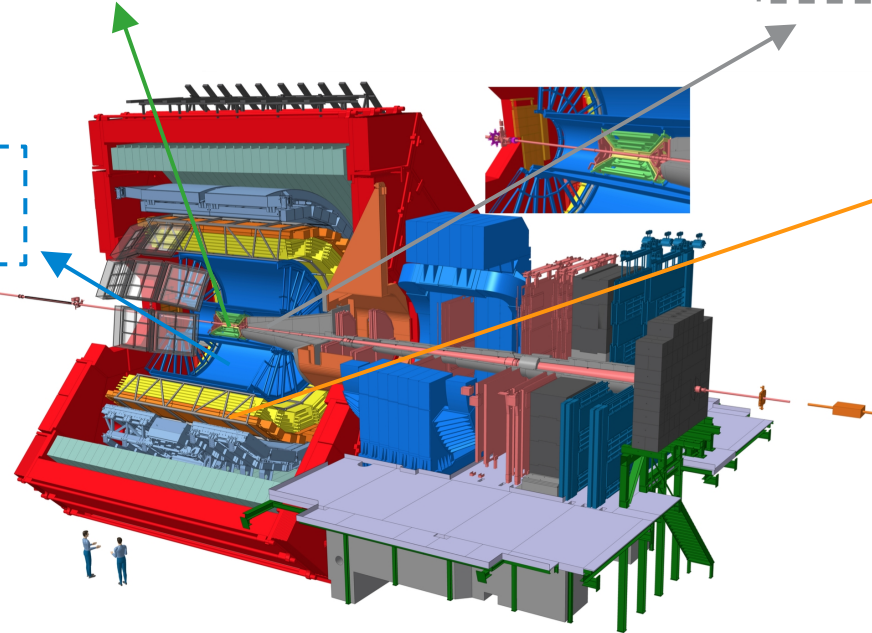
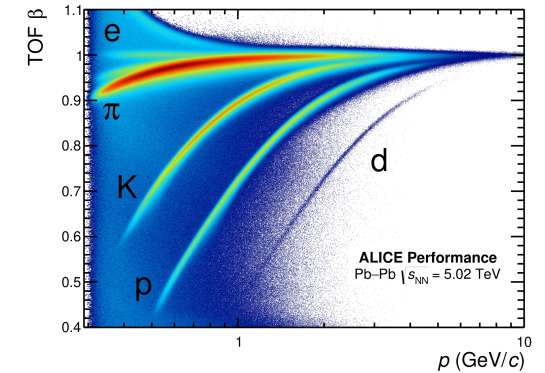
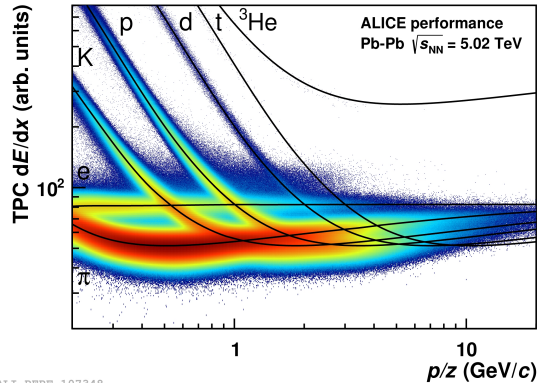
ALICE

**Inner Tracking System (ITS):** tracking, vertexing, trigger

**V0:** trigger, centrality estimation

**Time Projection Chamber (TPC):** tracking, PID via  $dE/dx$

**Time-Of-Flight (TOF):** PID via time of flight



Run 2 data: Pb-Pb  $\sqrt{s_{NN}} = 5.02$  TeV

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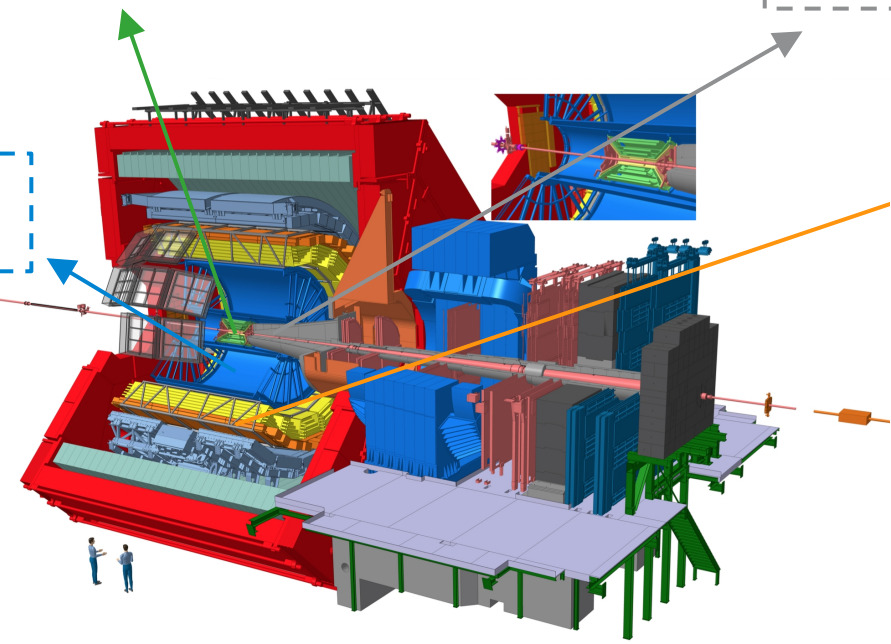
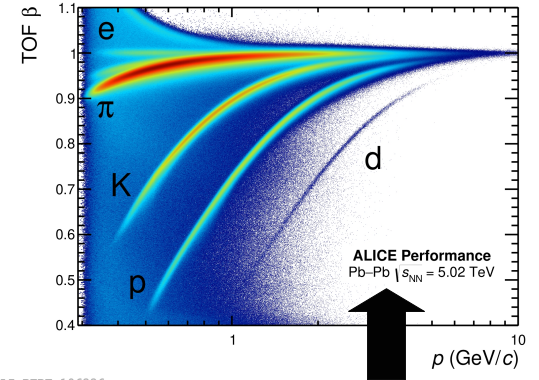
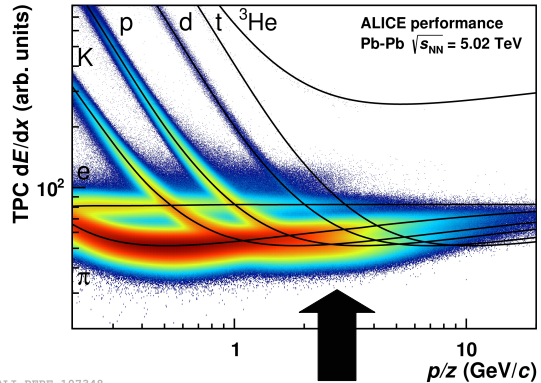
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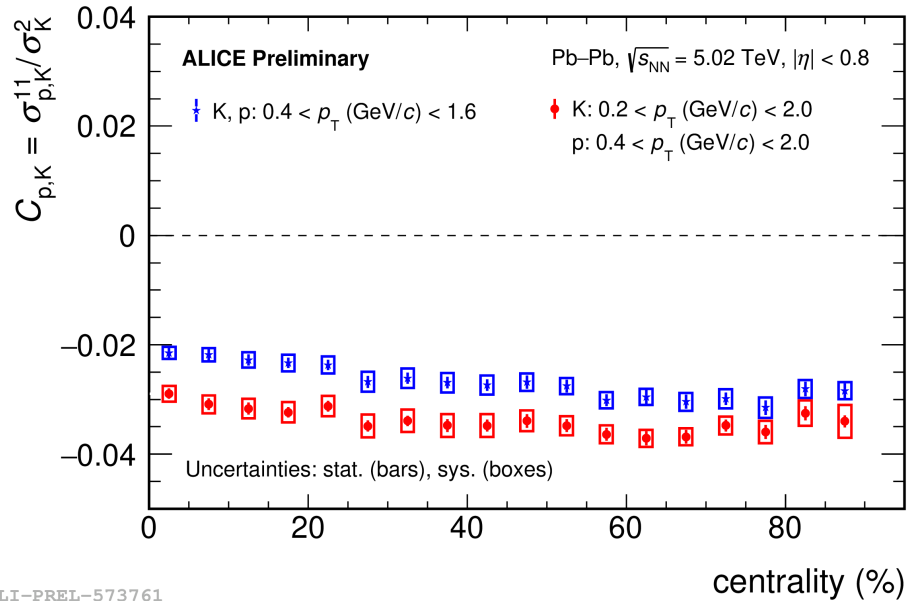


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✓ PID using information from TPC and TOF

# Correlation of net-proton and net-kaon

→ a proxy of  $B - S$  correlation

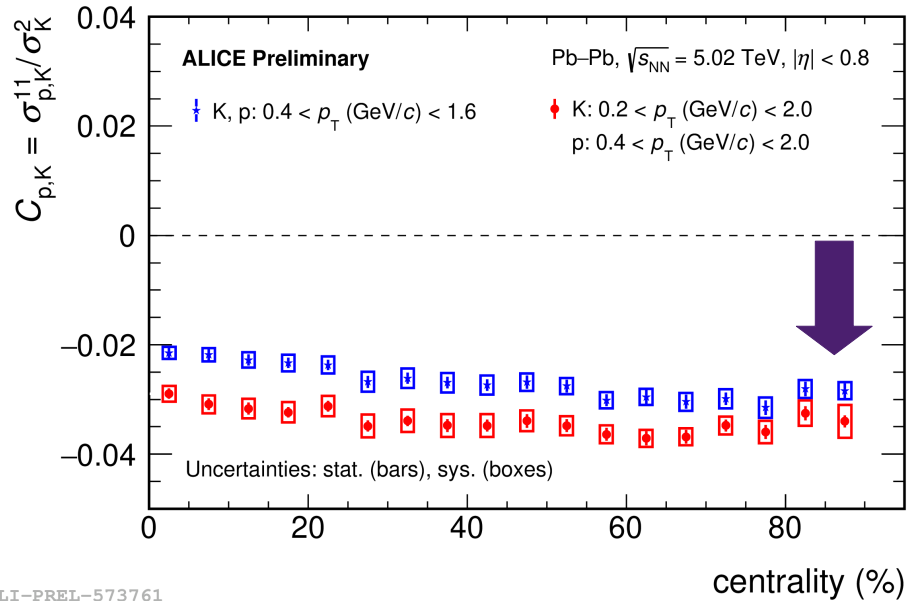


ALI-PREL-573761

- **Anti-correlation** between fluctuations in  $B$  and  $S$
- Momentum range dependence

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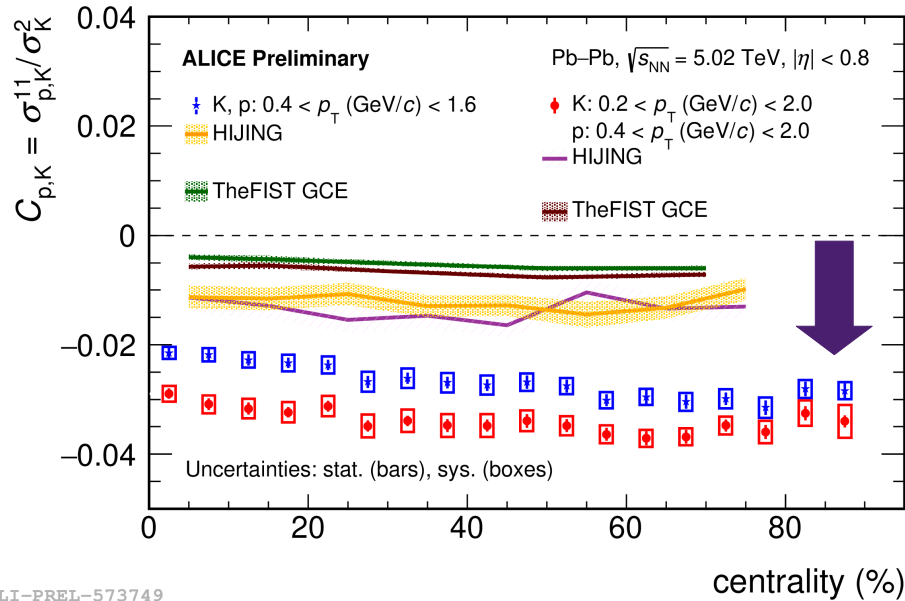
ALI-PREL-573761

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- **Larger correlations** compared to the Poisson baseline



# Correlation of net-proton and net-kaon

→ a proxy of  $B - S$  correlation



ALI-PREL-573749

- **Anti-correlation** between fluctuations in  $B$  and  $S$
- Momentum range dependence
- **Larger correlations** compared to the Poisson baseline, **HIJING** model, and **GCE** limit in thermal model

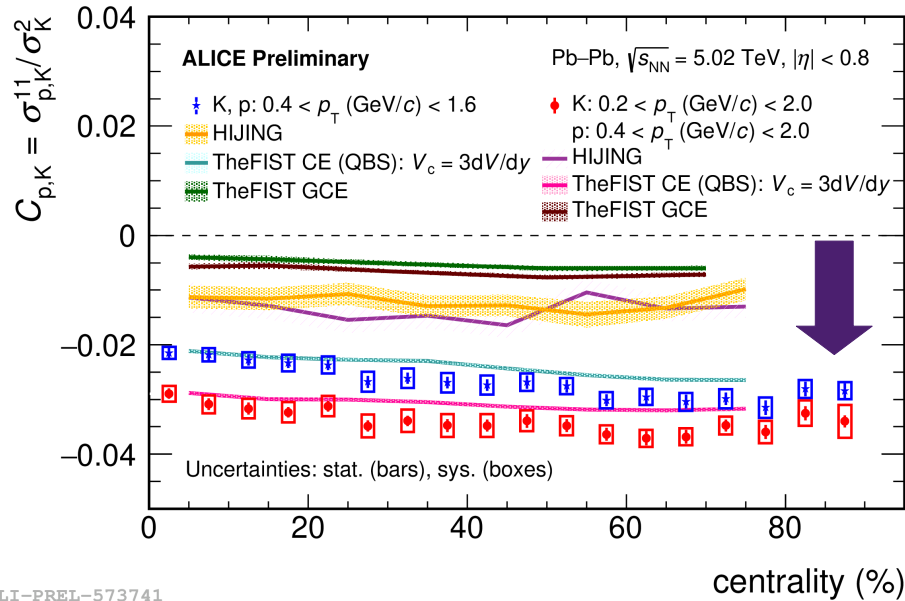
ThermalFIST (Statistical Hadronization Model) - Parameters from published fit

- Grand Canonical Ensemble (**GCE**) → quantum numbers conserved on average

V. Vovchenko et al., Phys.Rev.C 100 (2019) 5, 054906

# Correlation of net-proton and net-kaon

→ a proxy of  $B - S$  correlation



ALI-PREL-573741

- **Anti-correlation** between fluctuations in  $B$  and  $S$
- Momentum range dependence
- **Larger correlations** compared to the Poisson baseline, **HIJING** model, and **GCE** limit in thermal model
- Correlation volume of  $V_c = 3dV/dy$  with  $Q, B, S$  conservation in **CE favours data**

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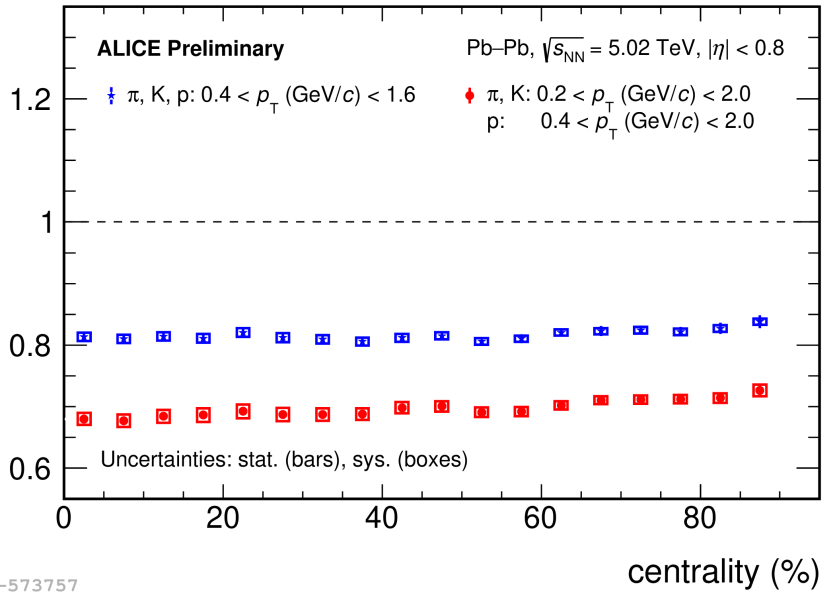
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# Correlation of net-charge and net-kaon

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$$C_{Q,K} = \sigma_{Q,K}^{11} / \sigma_K^2$$

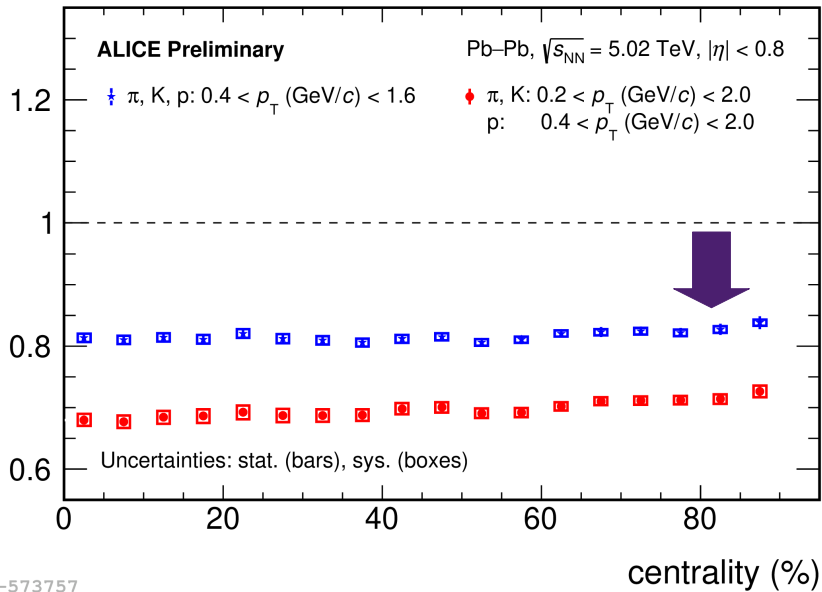


ALI-PREL-573757

- Momentum range dependence

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$$C_{Q,K} = \sigma_{Q,K}^{11} / \sigma_K^2$$



ALI-PREL-573757

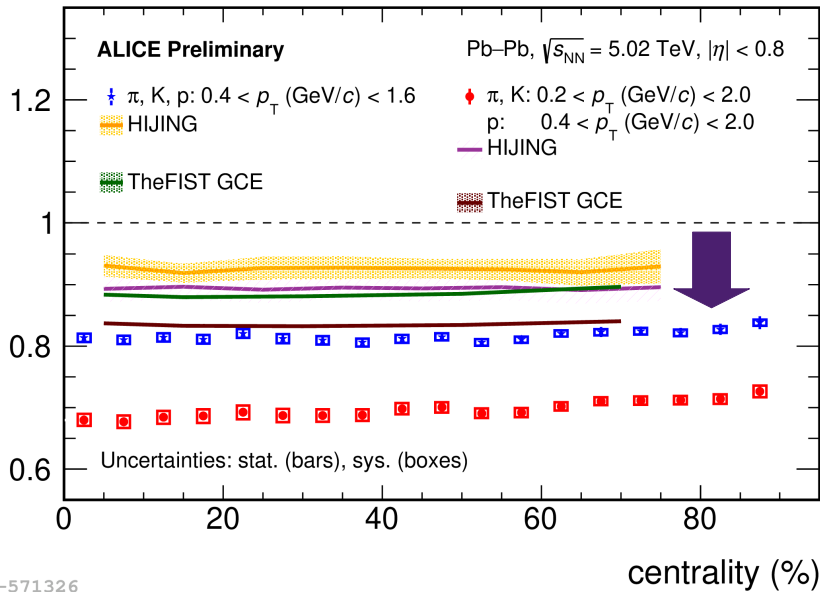
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- **Suppressed correlations** compared to the Poisson baseline

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ALI-PREL-571326

- Momentum range dependence
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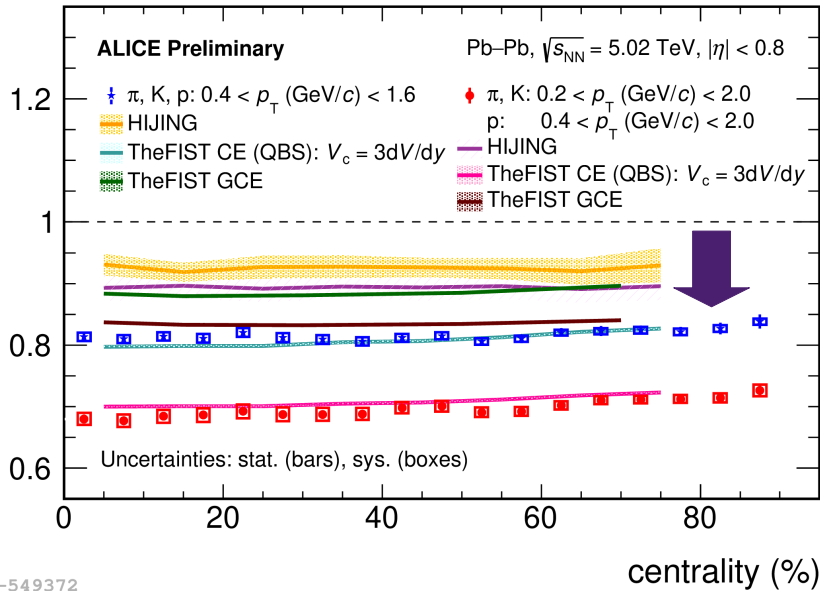
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V. Vovchenko et al., Phys.Rev.C 100 (2019) 5, 054906

# Correlation of net-charge and net-kaon

$$C_{Q,K} = \sigma_{Q,K}^{11} / \sigma_K^2$$



ALI-PREL-549372

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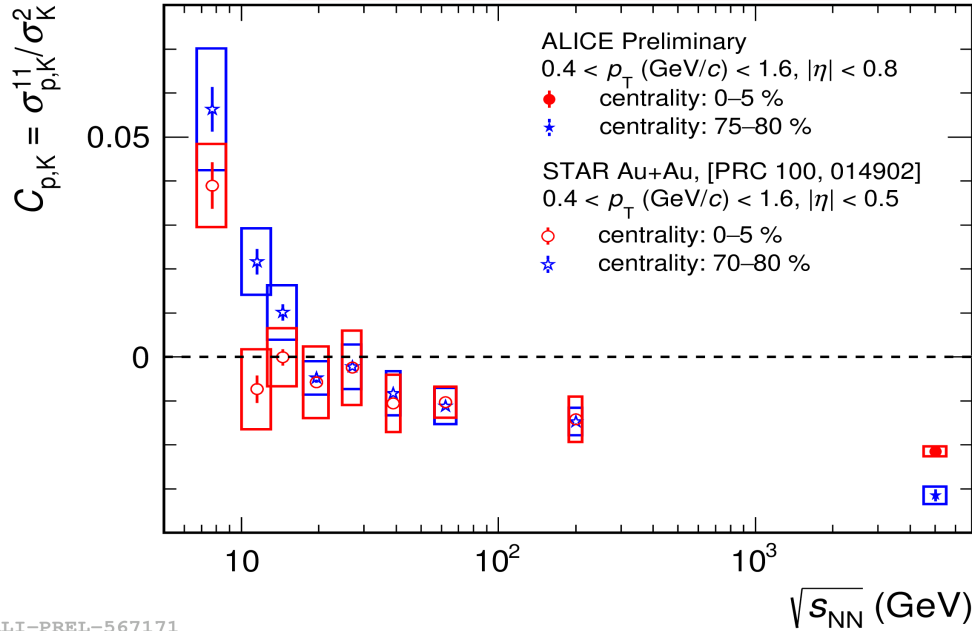
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V. Vovchenko et al., Phys.Rev.C 100 (2019) 5, 054906

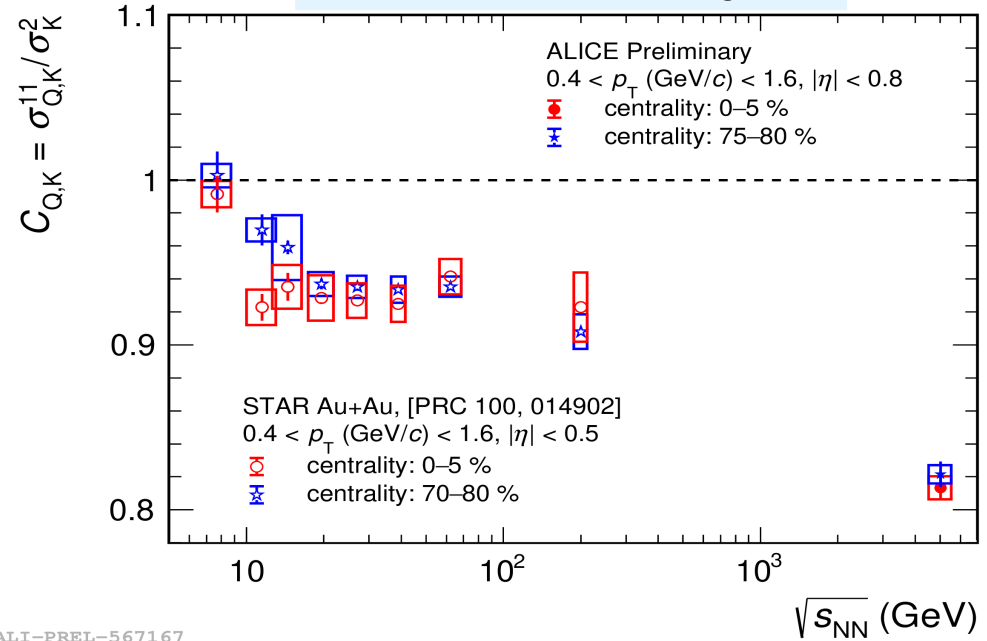
# Energy dependence

## Correlation between p - K



ALI-PREL-567171

## Correlation between Q - K



ALI-PREL-567167

- Decreasing trend of the correlations with increasing energy from RHIC to LHC

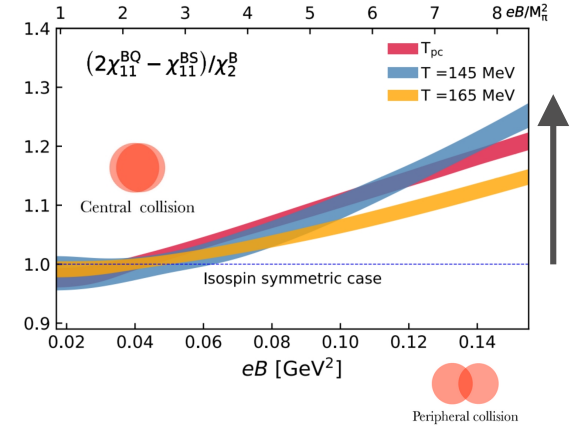
# Magnetic field effect?



Magnetic field: **Absent**  
Isospin symmetry of u and d quarks



Magnetic field: **Present**  
Isospin symmetry breaks

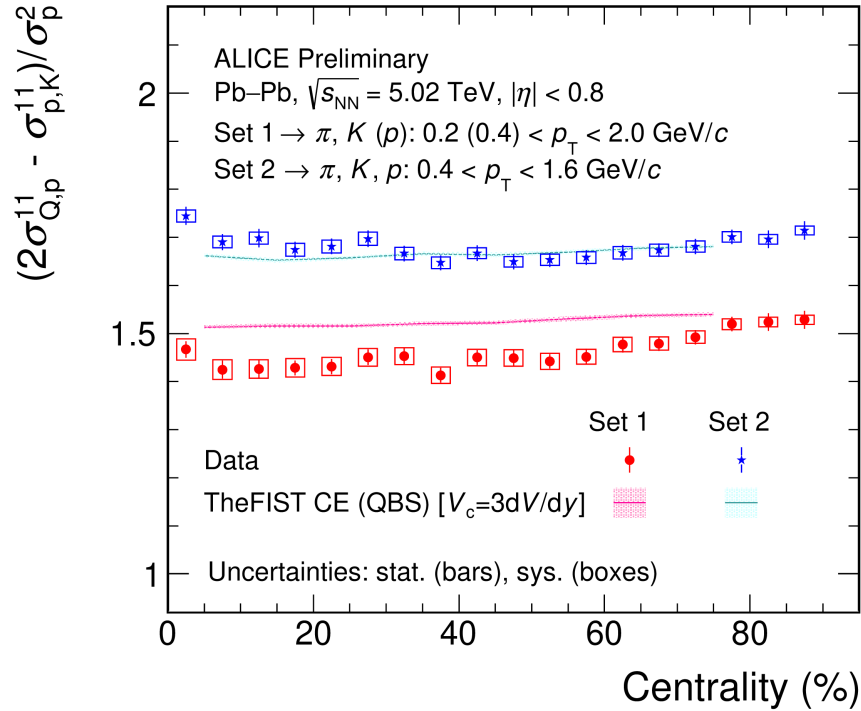


H.-T. Ding et al., EPJ. A (2021) 57:202, CPOD-2024



# Magnetic field effect?

proxy of  $(2\chi_{11}^{BQ} - \chi_{11}^{BS})/\chi_2^B$

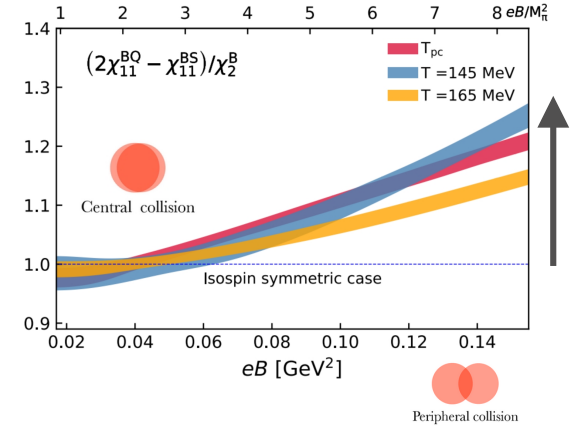


Poisson baseline → 2

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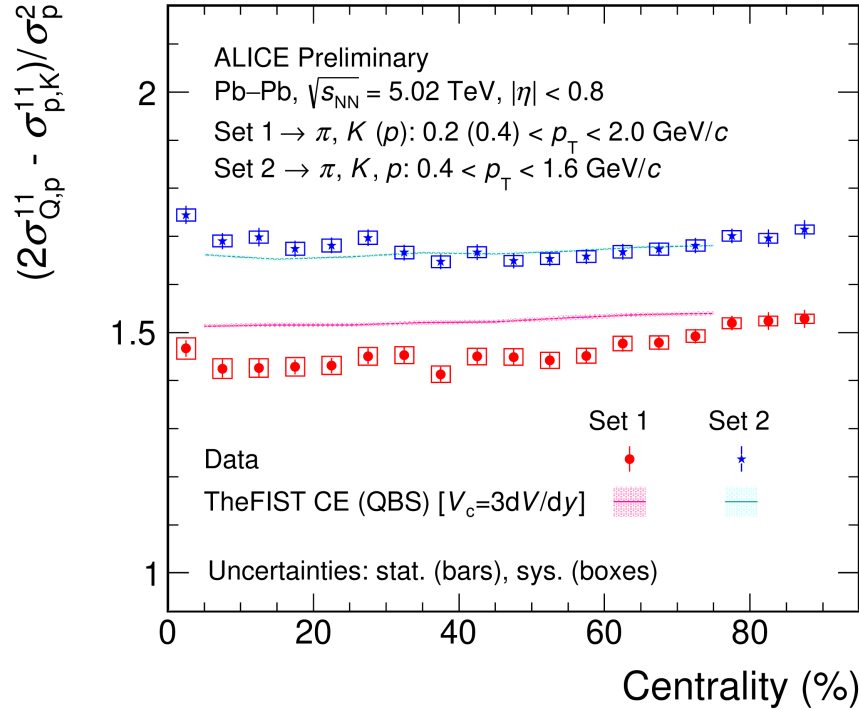
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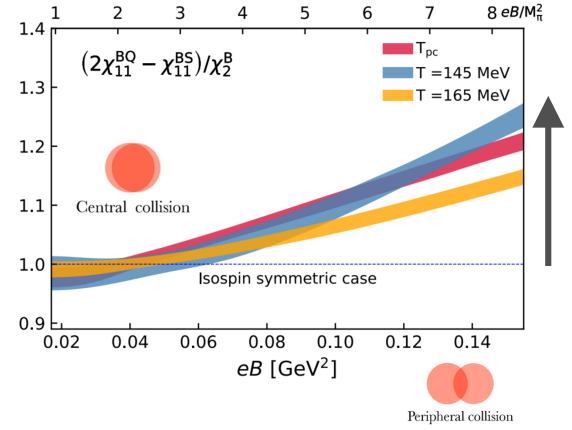


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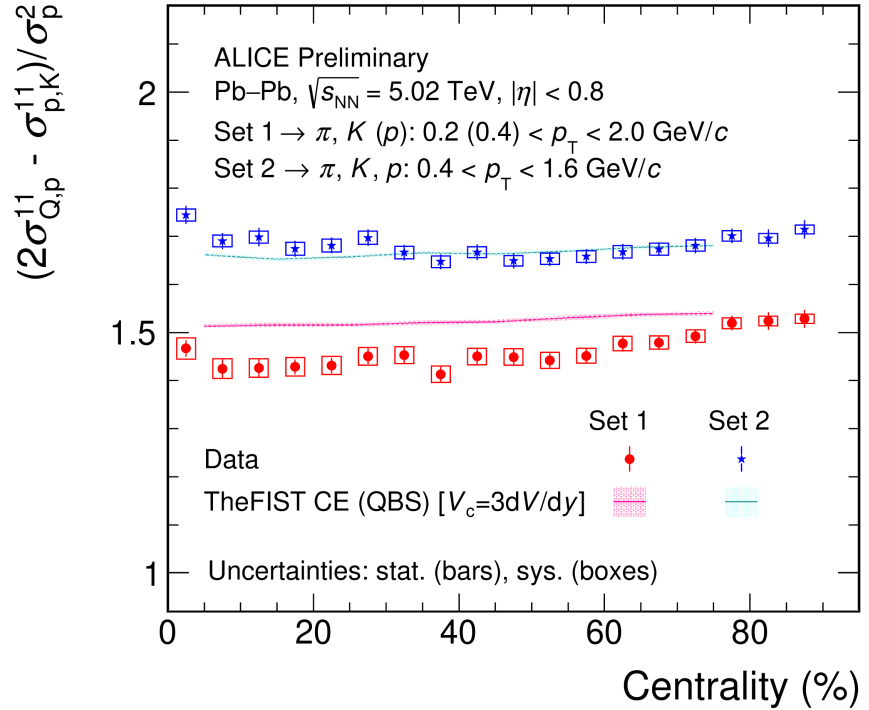
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H.-T. Ding et al., EPJ. A (2021) 57:202, CPOD-2024

- Momentum range dependence
- Deviation from Poisson baseline
- Subtle increasing trend from semicentral to peripheral collisions:  $\sim 4-5\%$ 
  - $\rightarrow$  Resonance decays!
  - $\rightarrow$  Correlation volume effect!
  - $\rightarrow$  Effect of magnetic field??

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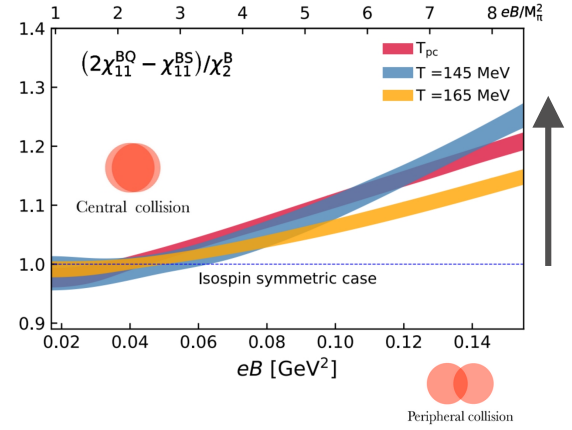


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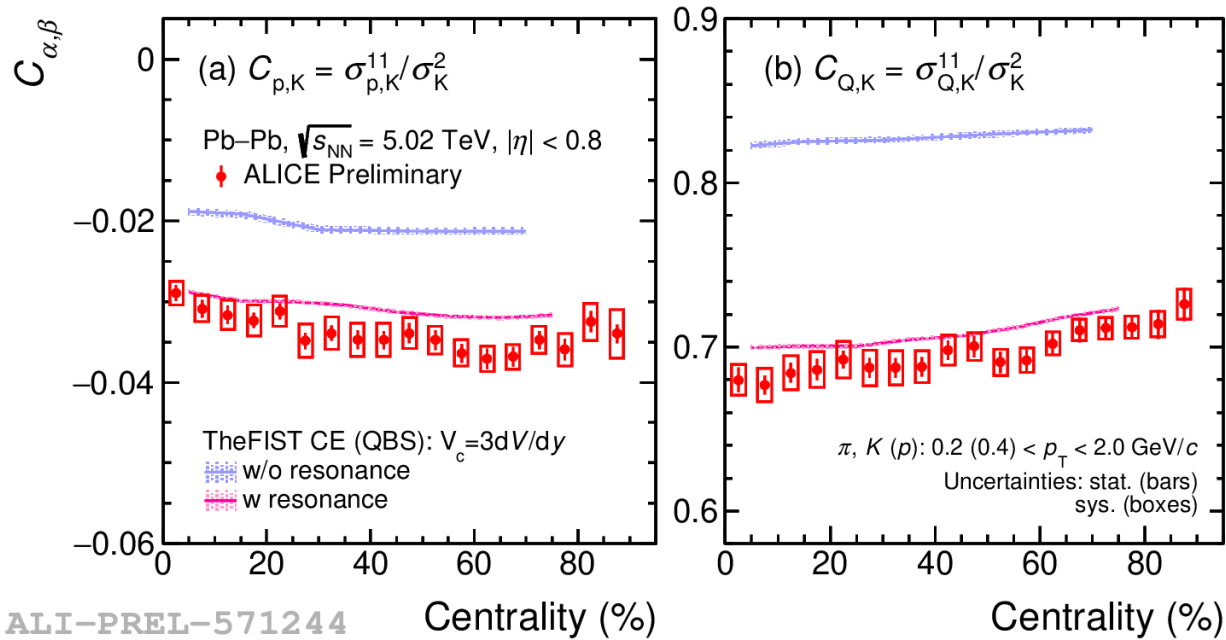
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ALI-PREL-574188

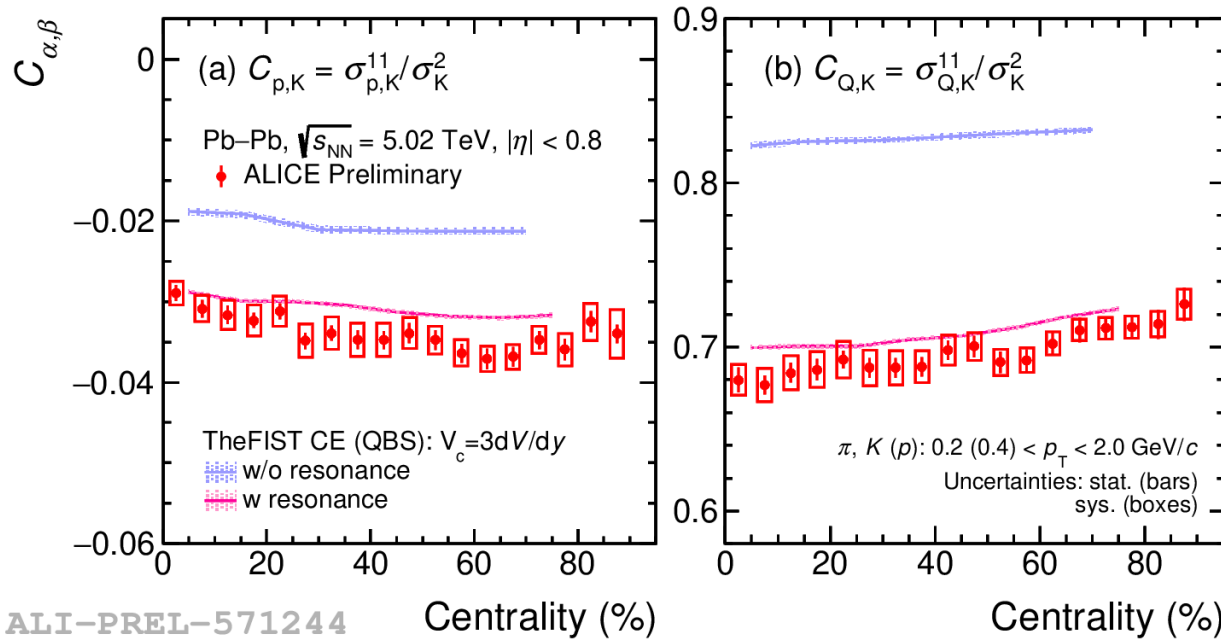
ThermalFIST Model: Parameters from published fit V. Vovchenko et al., Phys.Rev.C 100 (2019) 5, 054906



Canonical ensemble (CE) → exact conservation of  $Q, B, S$  in  $V_c = 3 dV/dy$

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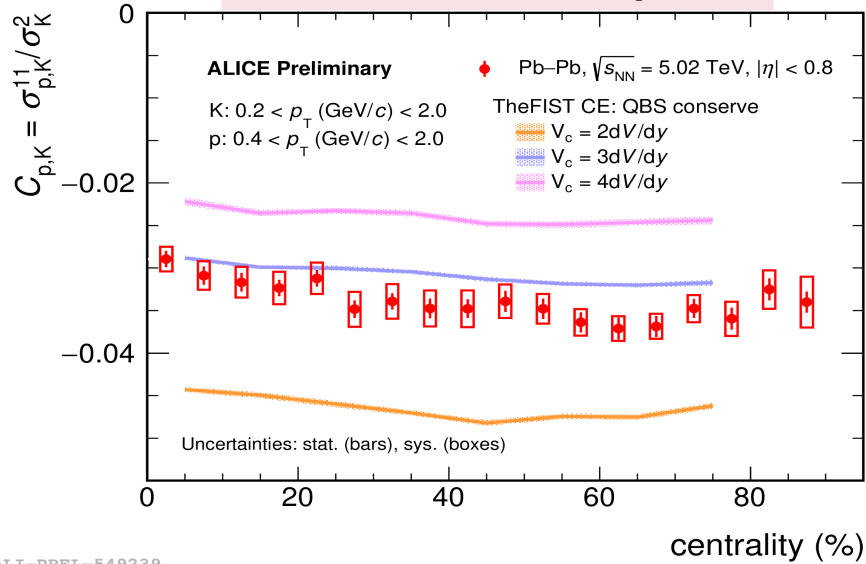


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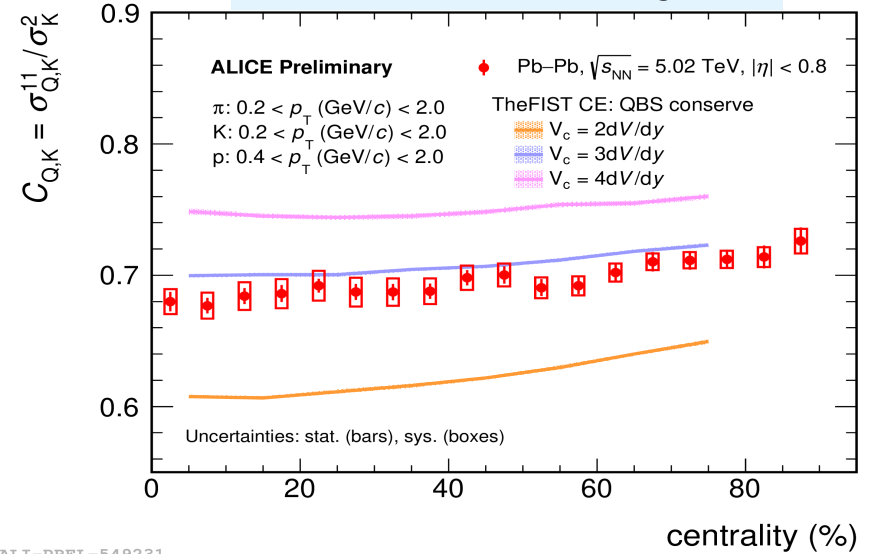
- **Significant impact of resonances**
- **ThermalFIST is comparatively better** in capturing the resonance contributions

# Effect of correlation volume

## Correlation between p – K



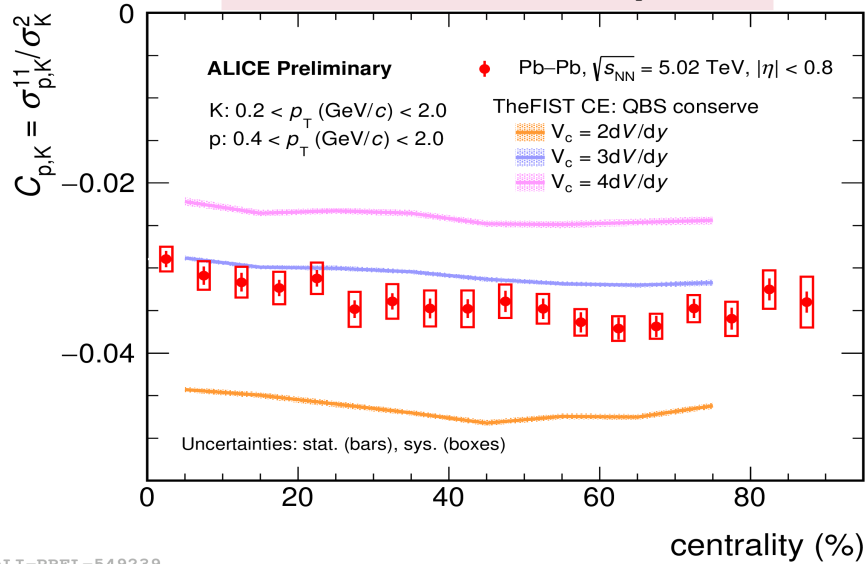
## Correlation between Q – K



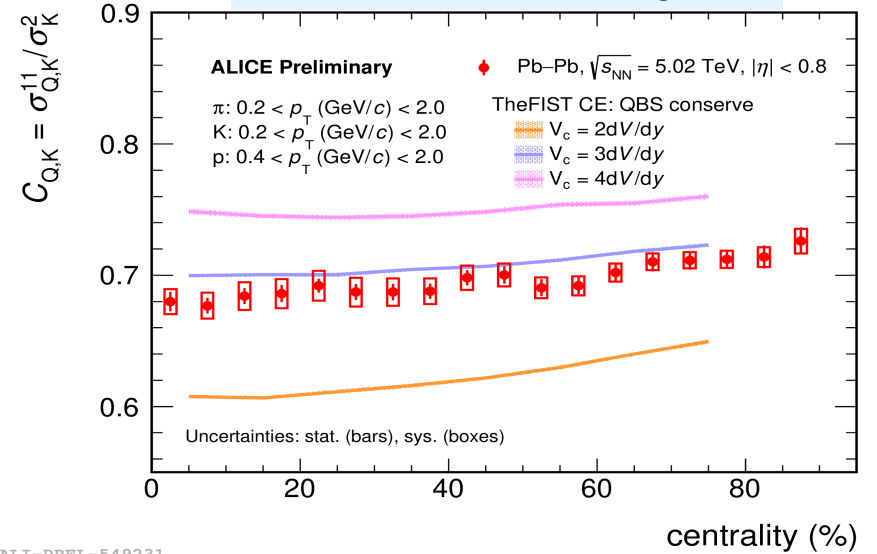
- Sensitive to the correlation volume ( $V_c$ ) in thermal model

# Effect of correlation volume

## Correlation between p – K



## Correlation between Q – K

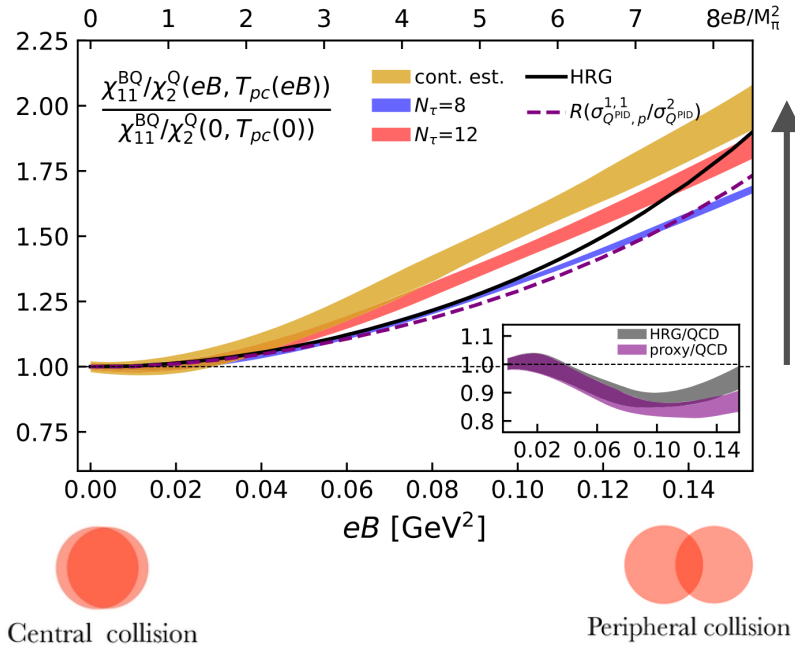


- Sensitive to the correlation volume ( $V_c$ ) in thermal model
- A combined  $\chi^2$ -minimization of three correlations (p – K, Q – K and Q – p) gives  $V_c \sim 2.6dV/dy$  for Q, B, and S conservation
  - slightly lower than that of net-proton fluctuations, net- $\Lambda$  fluctuations, and net- $\Xi$ –net-K correlations ( $V_c \sim 3dV/dy$ )

→ 4 June, Mario Ciacco 4

# Magnetic field effect?

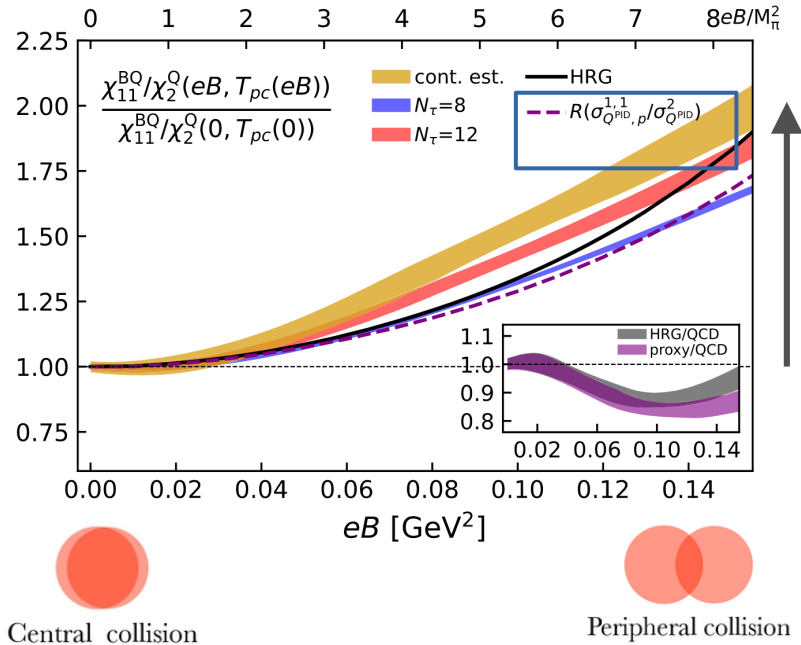
H.-T. Ding et al., *Phys.Rev.Lett* 132 (2024) 201903





# Magnetic field effect?

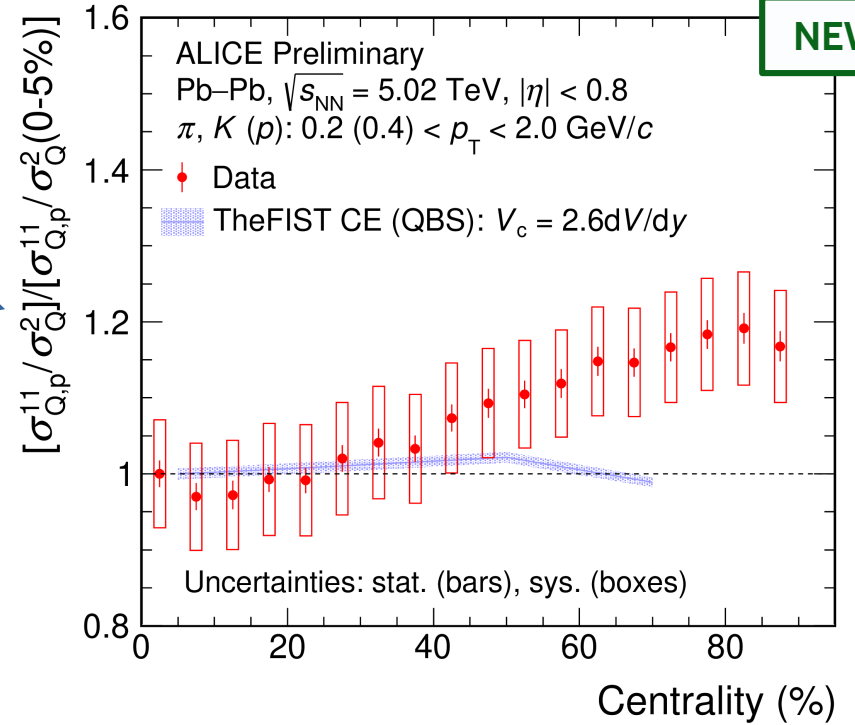
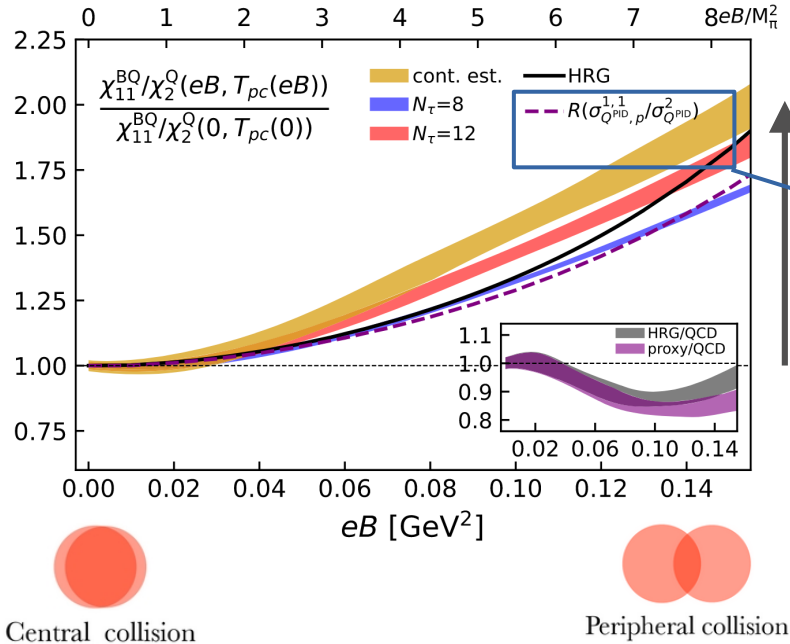
H.-T. Ding et al., *Phys.Rev.Lett* 132 (2024) 201903



# Magnetic field effect?



H.-T. Ding et al., *Phy.Rev.Lett* 132 (2024) 201903

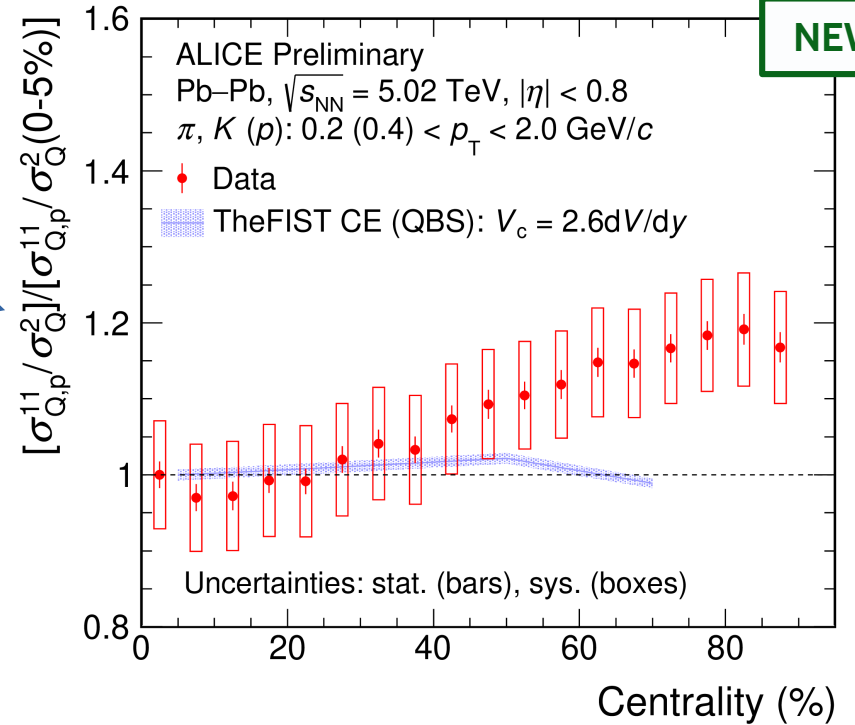
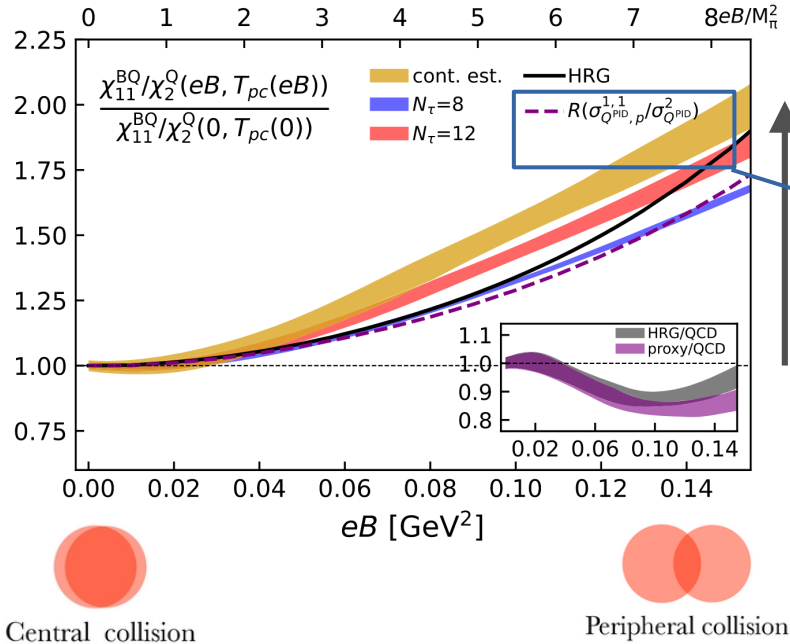


ALI-PREL-573205

# Magnetic field effect?



H.-T. Ding et al., *Phy.Rev.Lett* 132 (2024) 201903



ALI-PREL-573205

- Observed **an increase of ~20% from central to peripheral collisions**  
 – Hint of magnetic field effect?

# Summary

- Correlations among net-charge, net-baryon, net-strangeness are essential probes of QCD phases
  - The measurements provide a crucial input for the understanding of **resonance decays**,  **$Q$ ,  $B$  and  $S$  conservation and building a reliable proxy** while comparing to the LQCD results
- Thermal-FIST model within CE framework and  $Q$ ,  $B$  and  $S$  conservation suggests **long-range correlations** with correlation volume,  $V_c \sim 2.6dV/dy$
- **Hint of magnetic field** effect in correlation of net-charge and net-proton

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Stay tuned for more results on event-by-event fluctuations with Run 3 data.

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Stay tuned for more results on event-by-event fluctuations with Run 3 data.

Thank you



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# Additional slides

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# Theory predictions

Magnetic field **✗**  
Isospin symmetry of u and d quarks

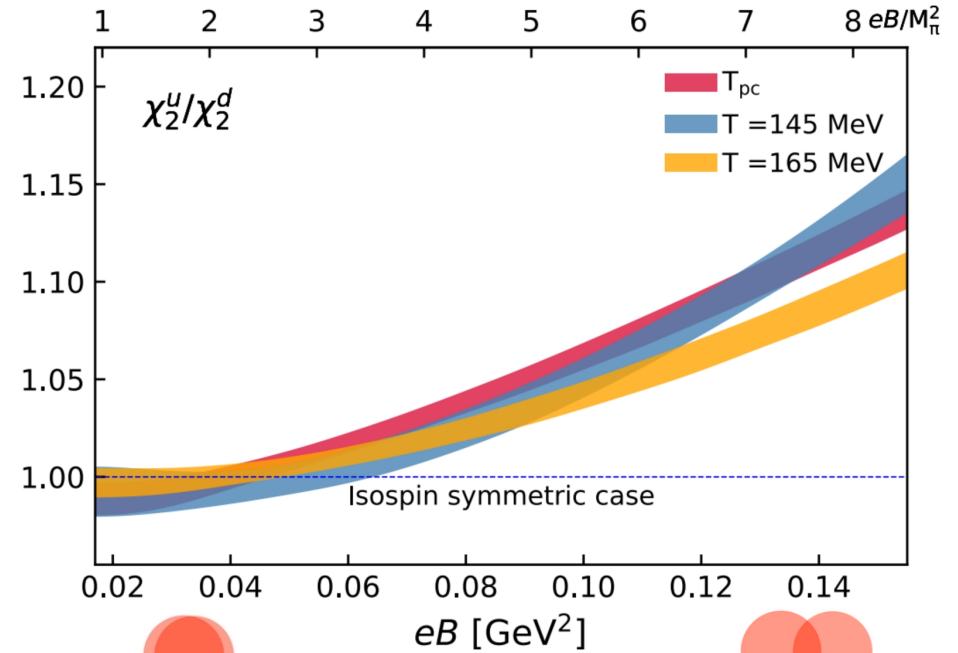


Magnetic field **✓**  
Isospin symmetry breaks

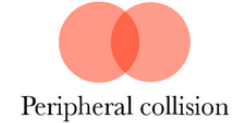
$$\text{At } eB = 0, \chi_u = \chi_d$$

$$2\chi_{11}^{QS} - \chi_{11}^{BS} = \chi_2^S$$

$$2\chi_{11}^{BQ} - \chi_{11}^{BS} = \chi_2^B$$



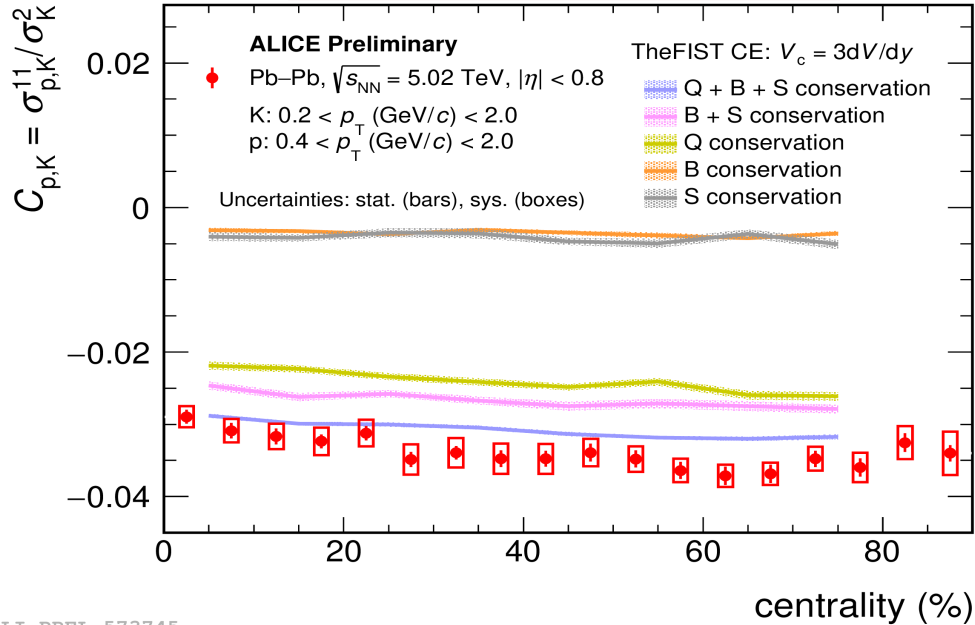
H.-T. Ding et al., EPJ. A (2021) 57:202, CPOD-2024



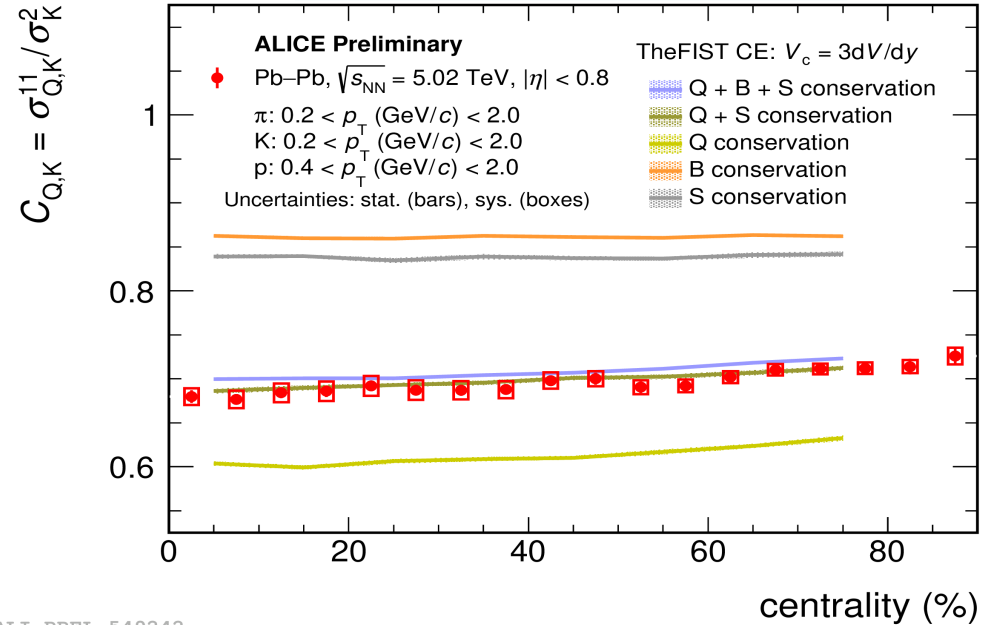


# Effect of charge conservations

## Correlation between p - K



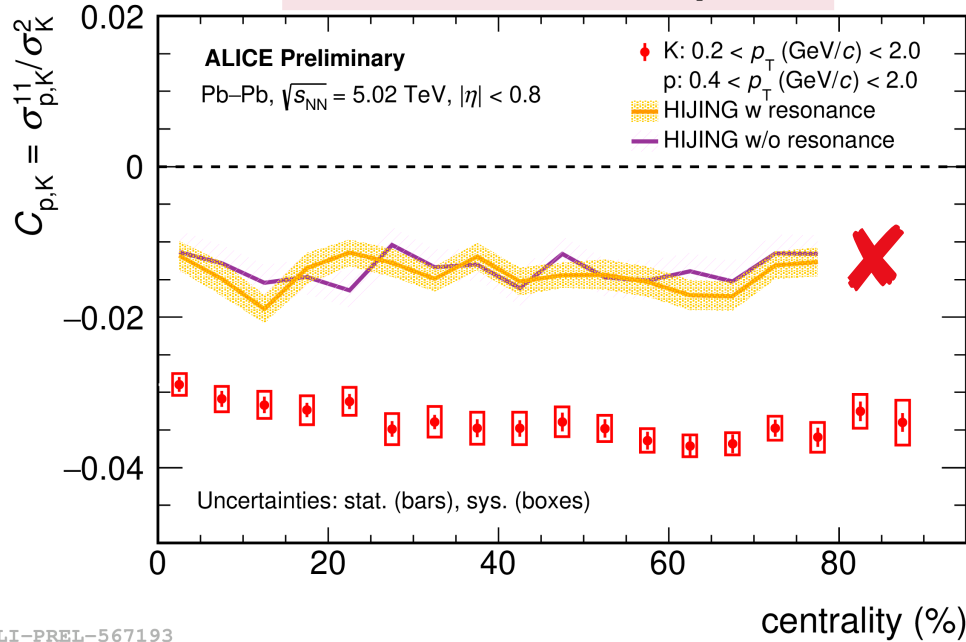
## Correlation between Q - K



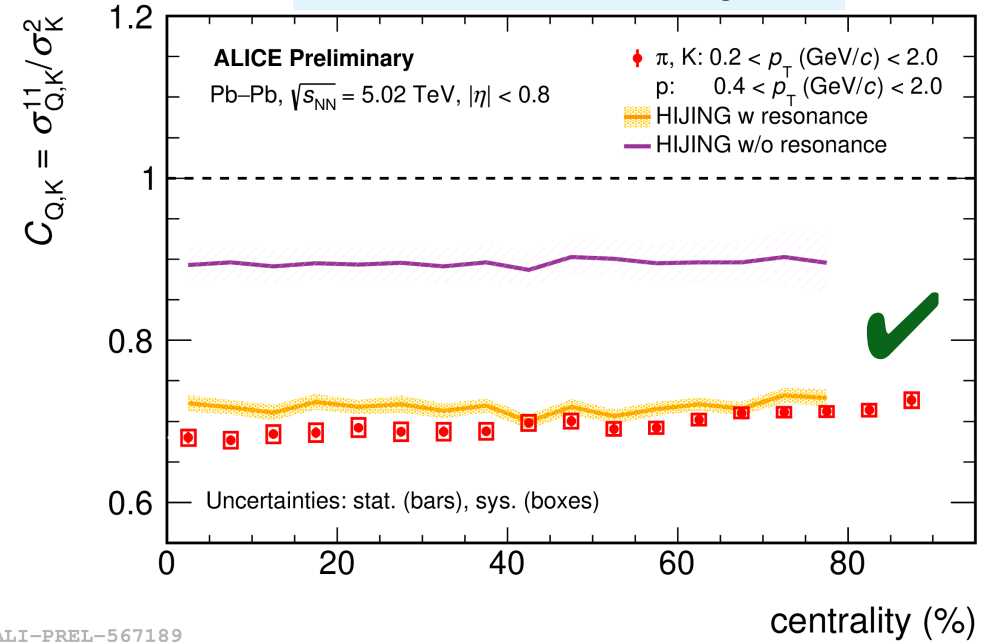
- Contribution to the net-particle correlations from Q, B, and S conservation are shown

# Effect of resonances

## Correlation between p - K

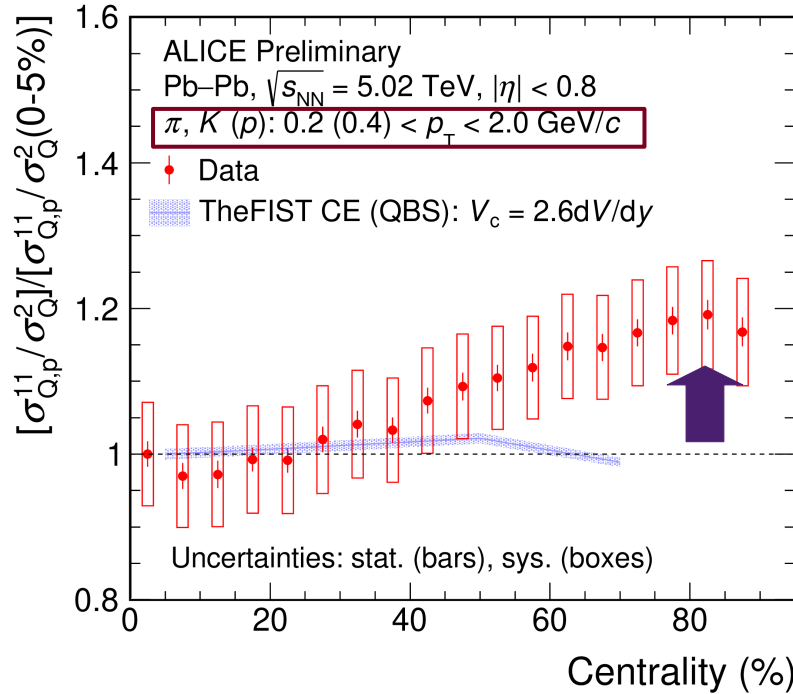


## Correlation between Q - K

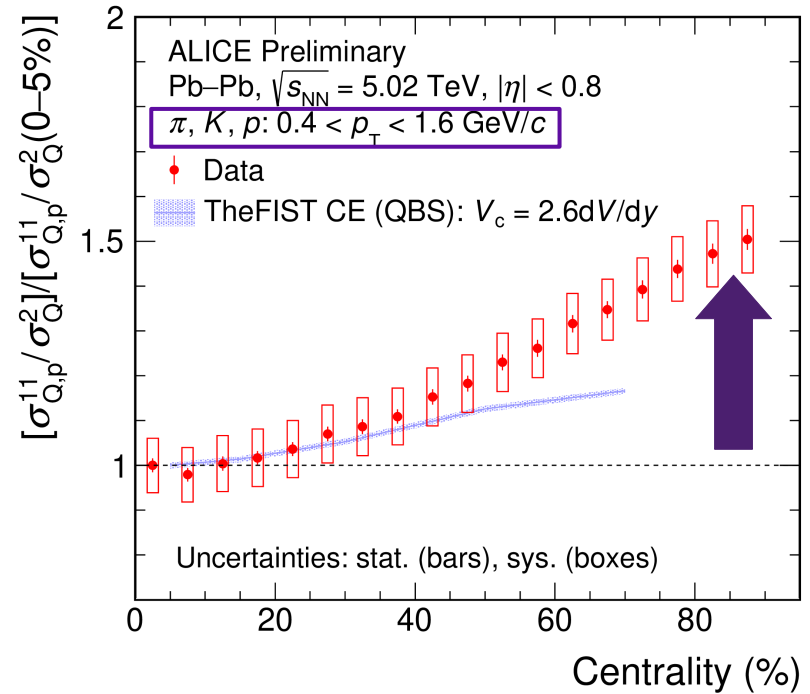


- HIJING is not good in capturing the resonances for  $C_{p,K}$ , but good for  $C_{Q,K}$

# Magnetic Field?



ALI-PREL-573205



ALI-PREL-573623

- Larger deviation with change in momentum range  
→ low  $p_T$  pions diminishing the effect of magnetic field on Q – K correlations?