



U.S. DEPARTMENT OF
ENERGY

Office of
Science



Brookhaven[™]
National Laboratory

PROGRESS TOWARDS UNDERSTANDING FLOW IN SMALL SYSTEMS

BJÖRN SCHENKE, BROOKHAVEN NATIONAL LABORATORY

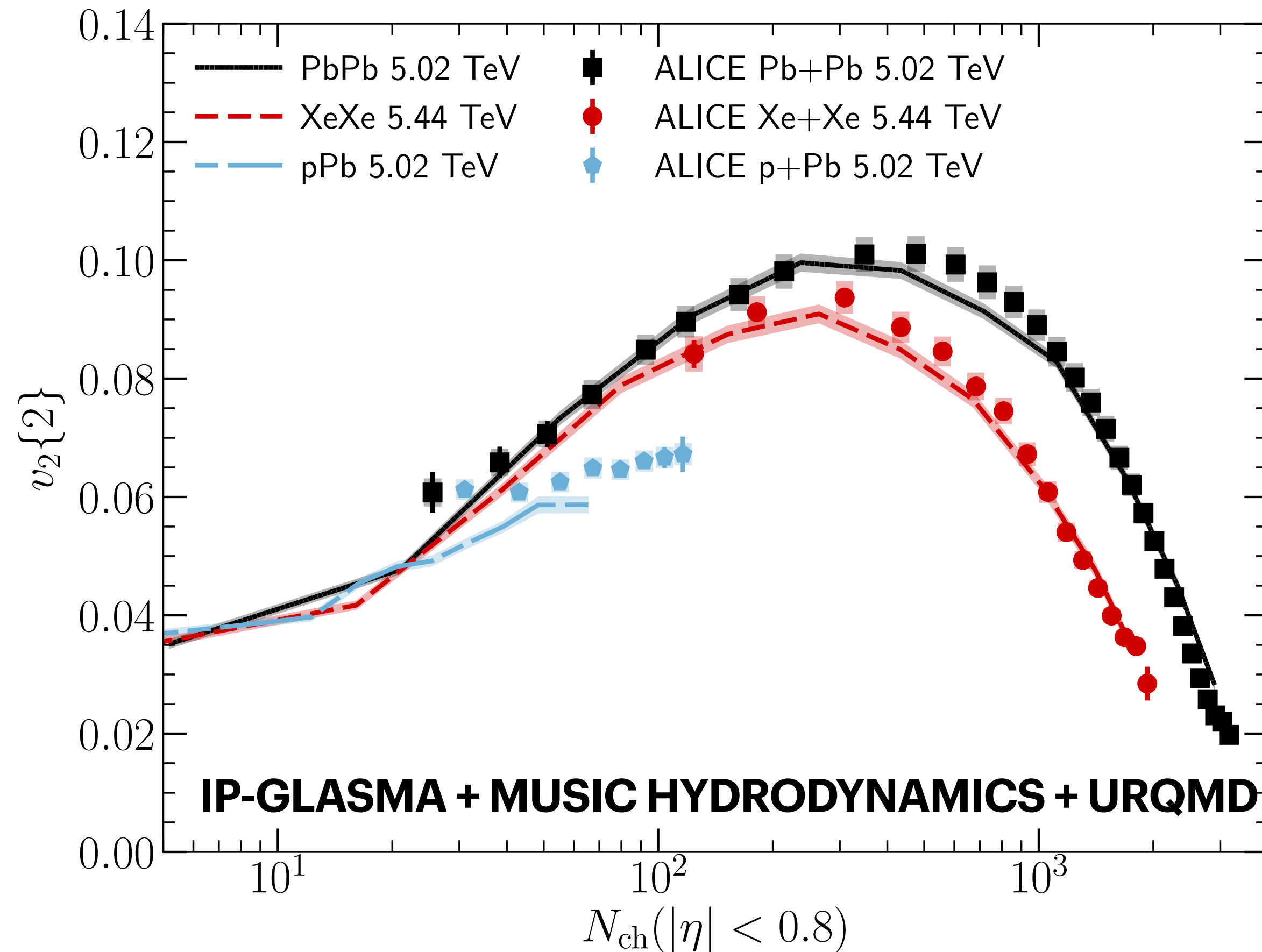
JUNE 7 2024

**STRANGE QUARK MATTER 2024
STRASBOURG, FRANCE**

SOM 2024

The logo for SOM 2024, featuring a circular diagram with a central blue dot, surrounded by concentric rings of green and red, and a black outer ring with small white dots.

FLOW IN SMALL SYSTEMS



Anisotropic flow in heavy ion collisions is driven by **final state response to the initial geometry**

There is evidence that the same is true in high multiplicity small systems

B. Schenke, C. Shen, P. Tribedy, *Phys.Rev.C* 102 (2020) 044905
ALICE Collaboration, *Phys.Rev.Lett.* 123 (2019) 142301

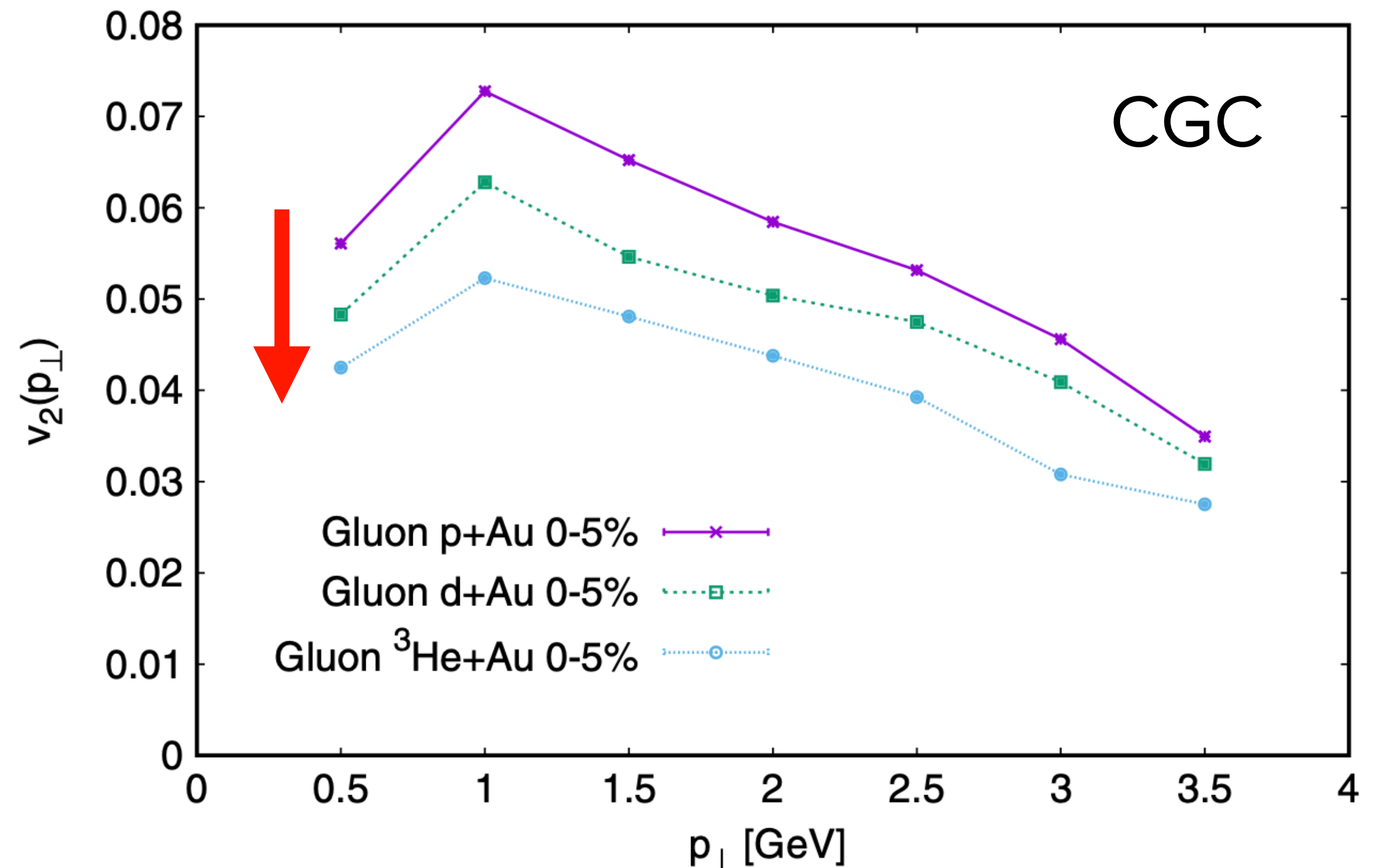
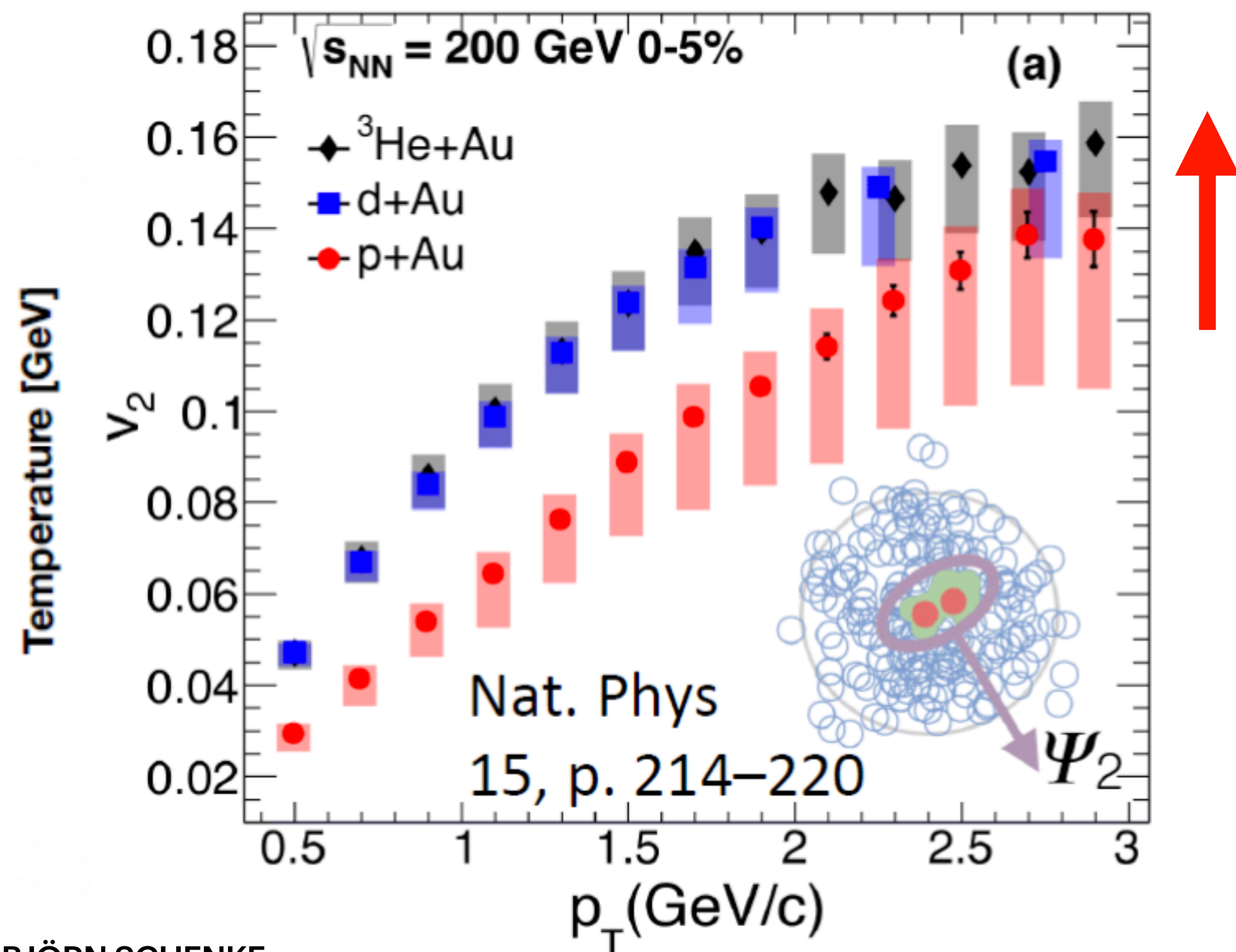
INITIAL STATE EFFECTS?

PHENIX Collaboration, Nature Phys. 15, no.3, 214-220 (2019)

B. Schenke, S. Schlichting, R. Venugopalan, Phys.Lett.B 747 (2015) 76-82, 1502.01331

M. Mace, V. V. Skokov, P. Tribedy, R. Venugopalan, Phys. Rev. Lett. 121, 052301 (2018), PRL123, 039901(E) (2019)

Initial state momentum anisotropy, for example from the Color Glass Condensate:
Cannot get all systematics right:



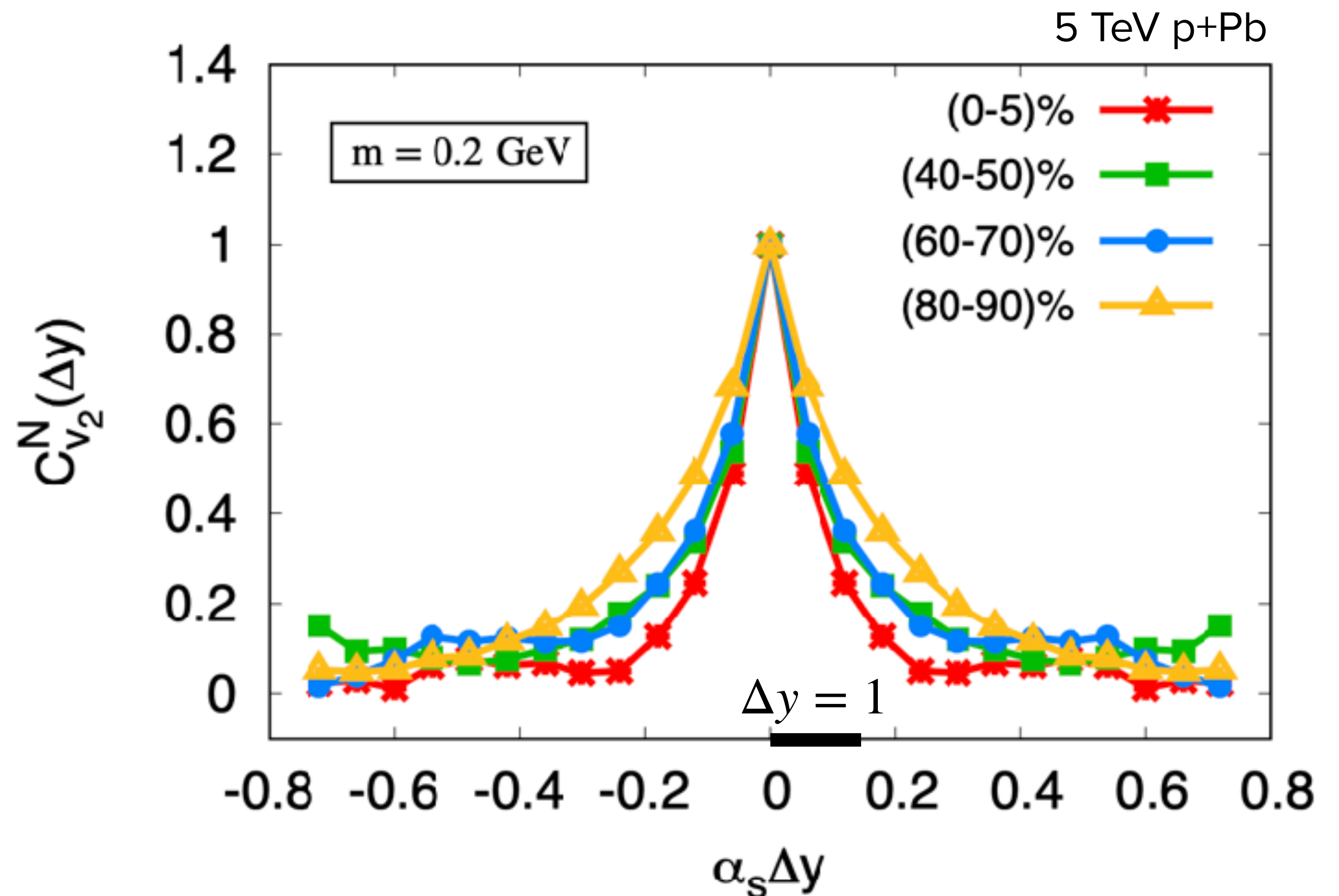
RAPIDITY DEPENDENCE OF INITIAL ANISOTROPHY

B.Schenke, S. Schlichting, and Pragma Singh, Phys.Rev.D 105 (2022) 9, 094023

CGC based IP-Glasma
+ rapidity evolution (JIMWLK)

$$C_{\mathcal{O}}^N(\eta_1, \eta_2) = \frac{\langle \text{Re}(\mathcal{O}(\eta_1)\mathcal{O}^*(\eta_2)) \rangle}{\sqrt{\langle |\mathcal{O}(\eta_1)|^2 \rangle \langle |\mathcal{O}(\eta_2)|^2 \rangle}}$$

Initial momentum anisotropy
decorrelates quickly
with rapidity difference



further evidence: Observed Baryon/meson v_2 grouping and splitting (see You Zhou's talk)

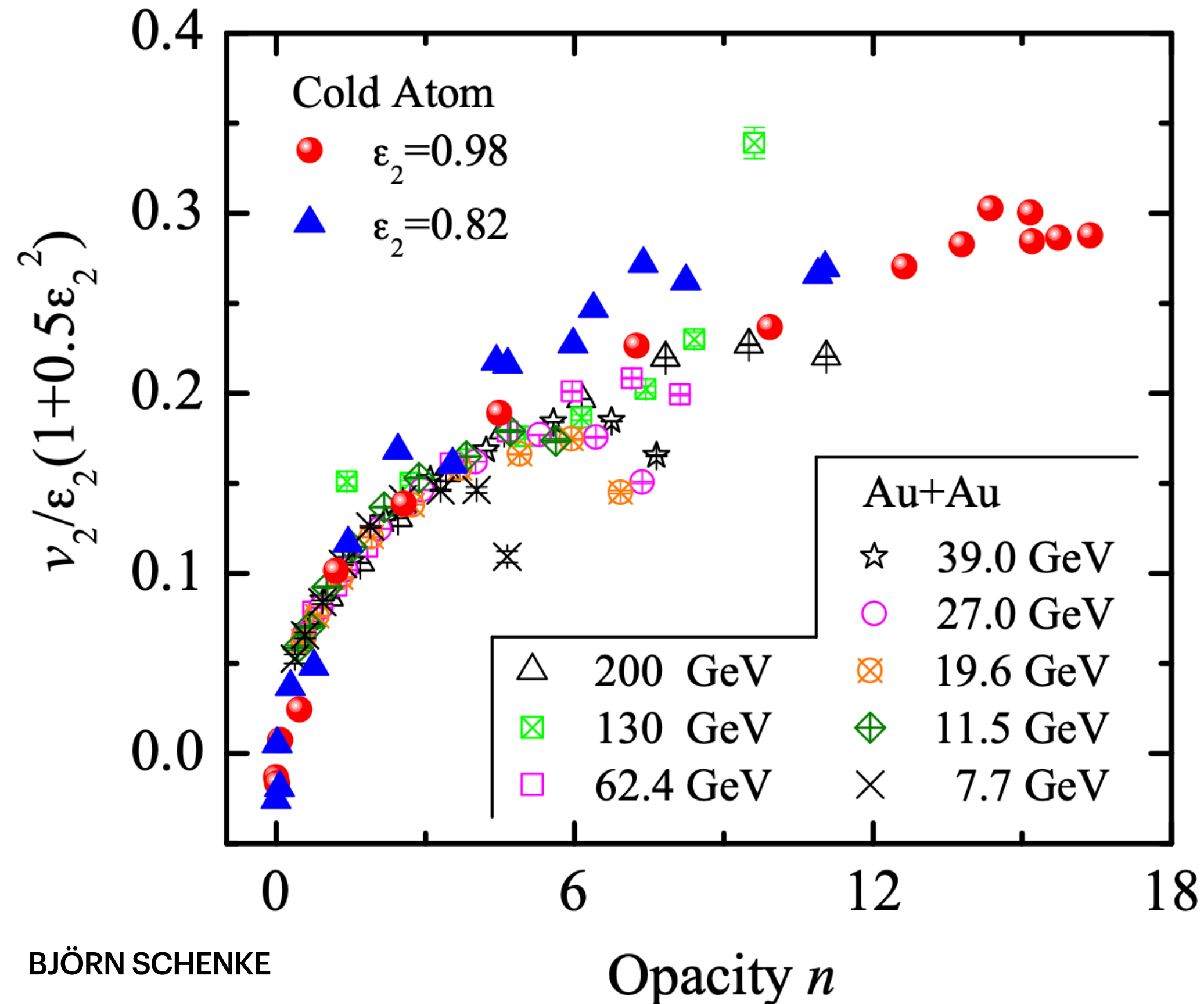
→ **Strong final state interactions needed to describe data**

INSIGHTS FROM COLD ATOMS

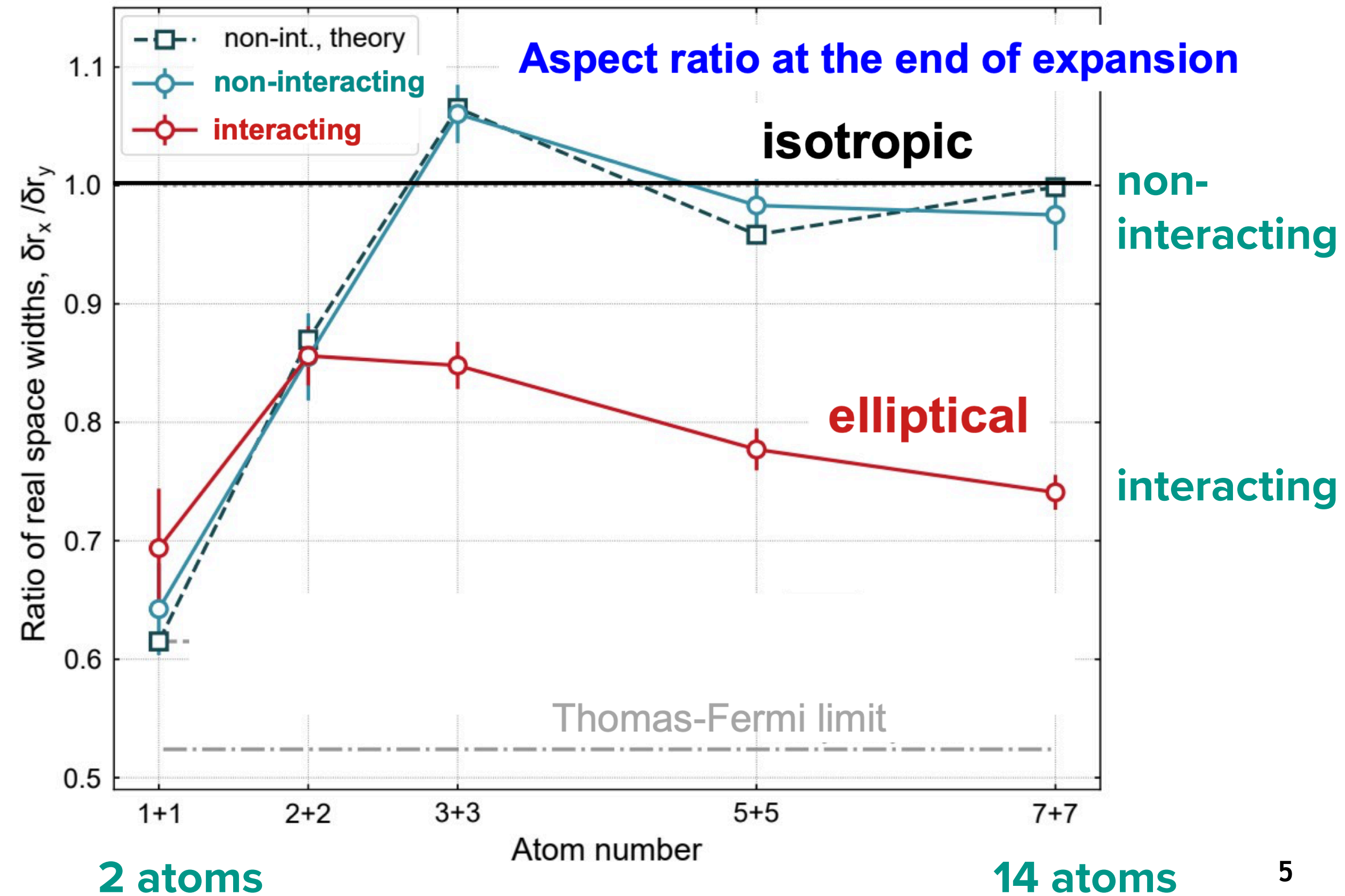
K. Li, H.-F. Song, Y.-L. Sun, H.-J. Xu, F. Wang, arXiv:2405.02847

Bandstetter, Lunt, Heintze, Giacalone, Heyen, Gałka, Subramanian, Holten, Preiss, Floerchinger, Jochim arXiv:2308.09699

Heavy ions vs. cold ${}^6\text{Li}$ ions with varying interaction strength: v_2/ε_2 agree



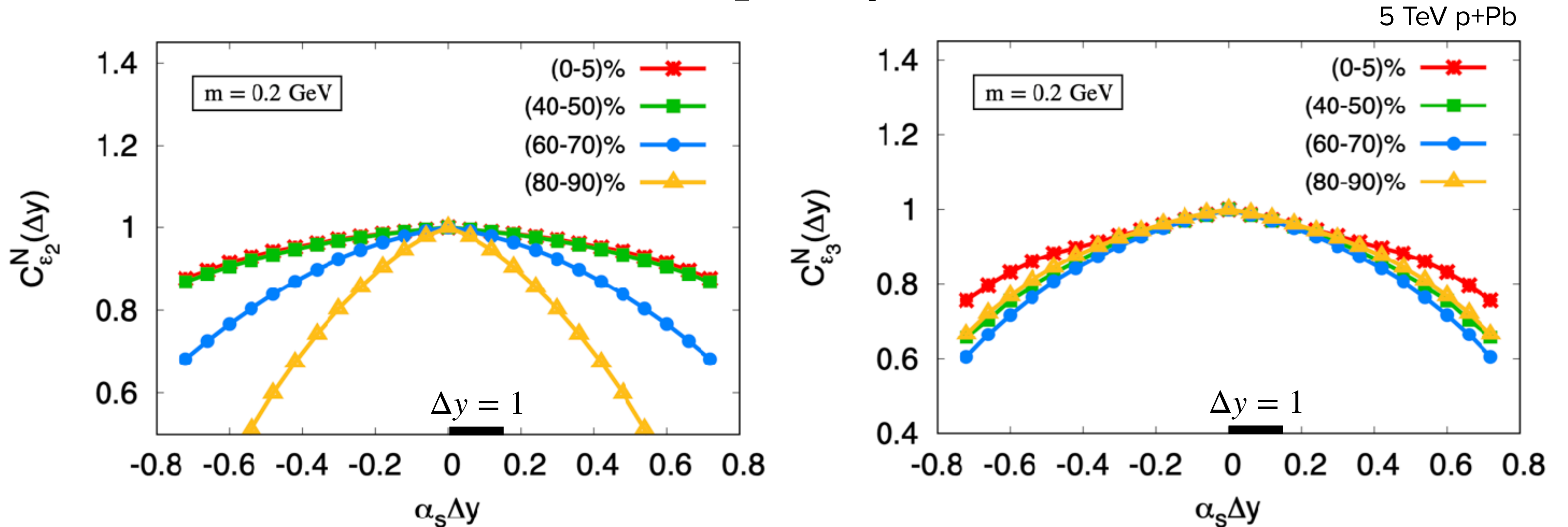
Very few particles: interaction drives elliptic flow for $N_{\text{atoms}} \geq 6$ see talk by Lars Heyen



RAPIDITY DEPENDENCE OF GEOMETRY

B.Schenke, S. Schlichting, and Pragma Singh, Phys.Rev.D 105 (2022) 9, 094023

The geometry, quantified here with ε_2 and ε_3 , decorrelates slowly

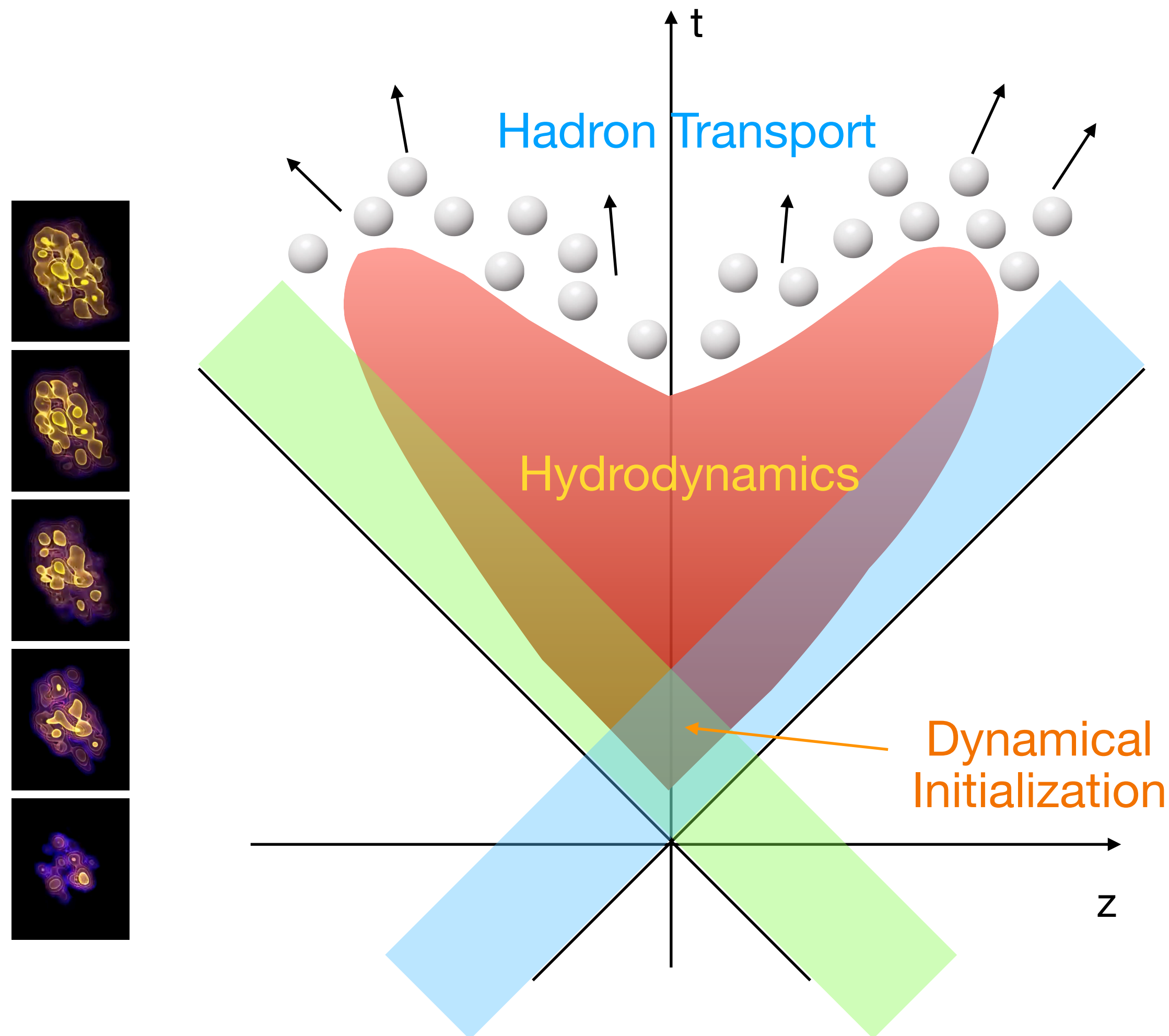


but rapidity dependence is not insignificant

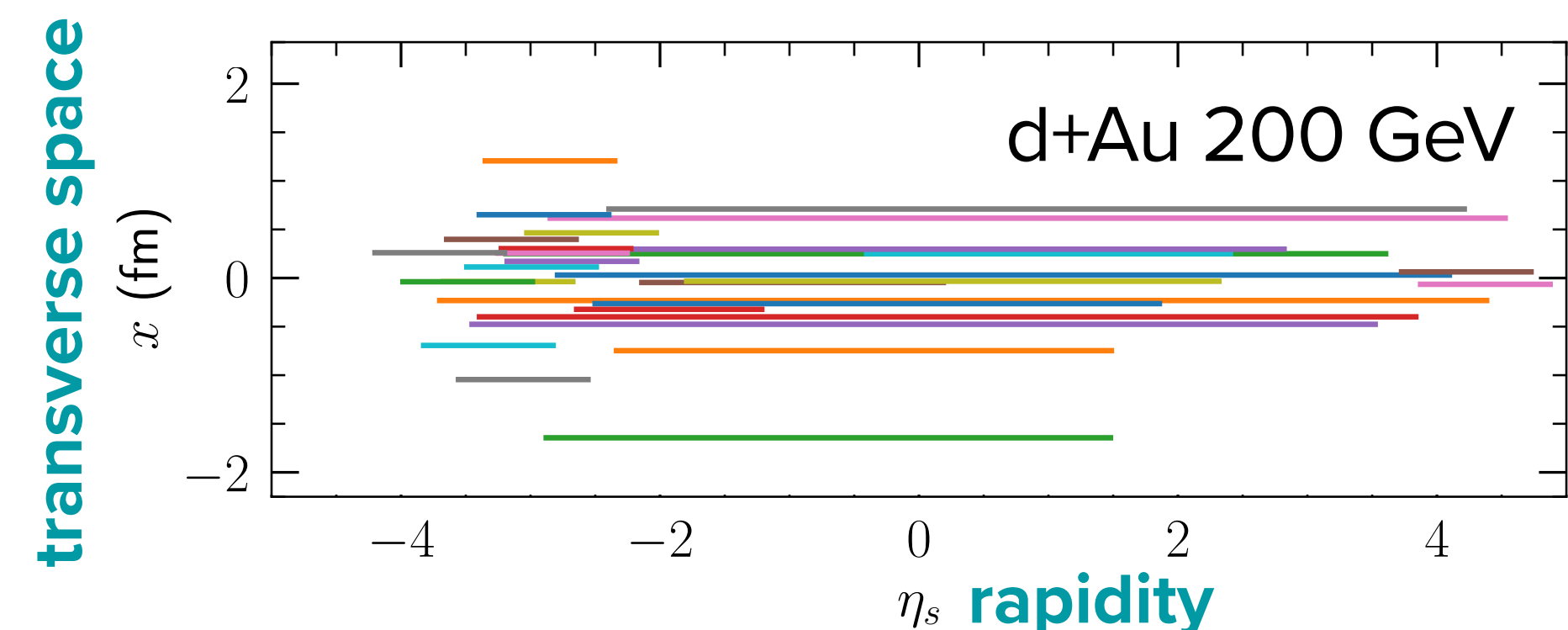
$$C_{\mathcal{O}}^N(n_1, n_2) = \frac{\langle \text{Re}(\mathcal{O}(n_1)\mathcal{O}^*(n_2)) \rangle}{\sqrt{\langle |\mathcal{O}(n_1)|^2 \rangle \langle |\mathcal{O}(n_2)|^2 \rangle}}$$

DYNAMIC 3+1D SIMULATION

C. Shen and B. Schenke, Phys.Rev. C97 (2018) 024907; Phys. Rev. C 105, 064905 (2022)

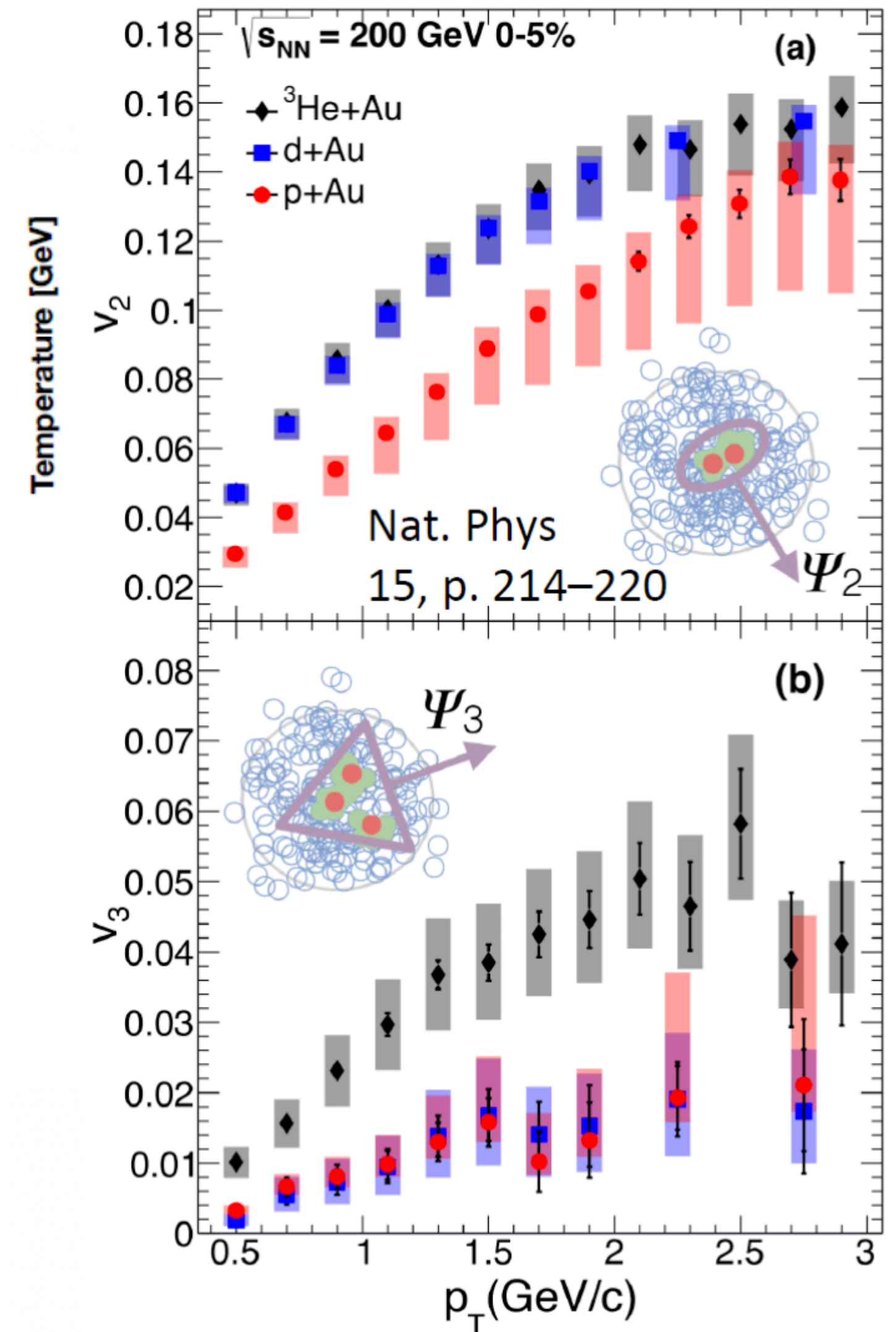
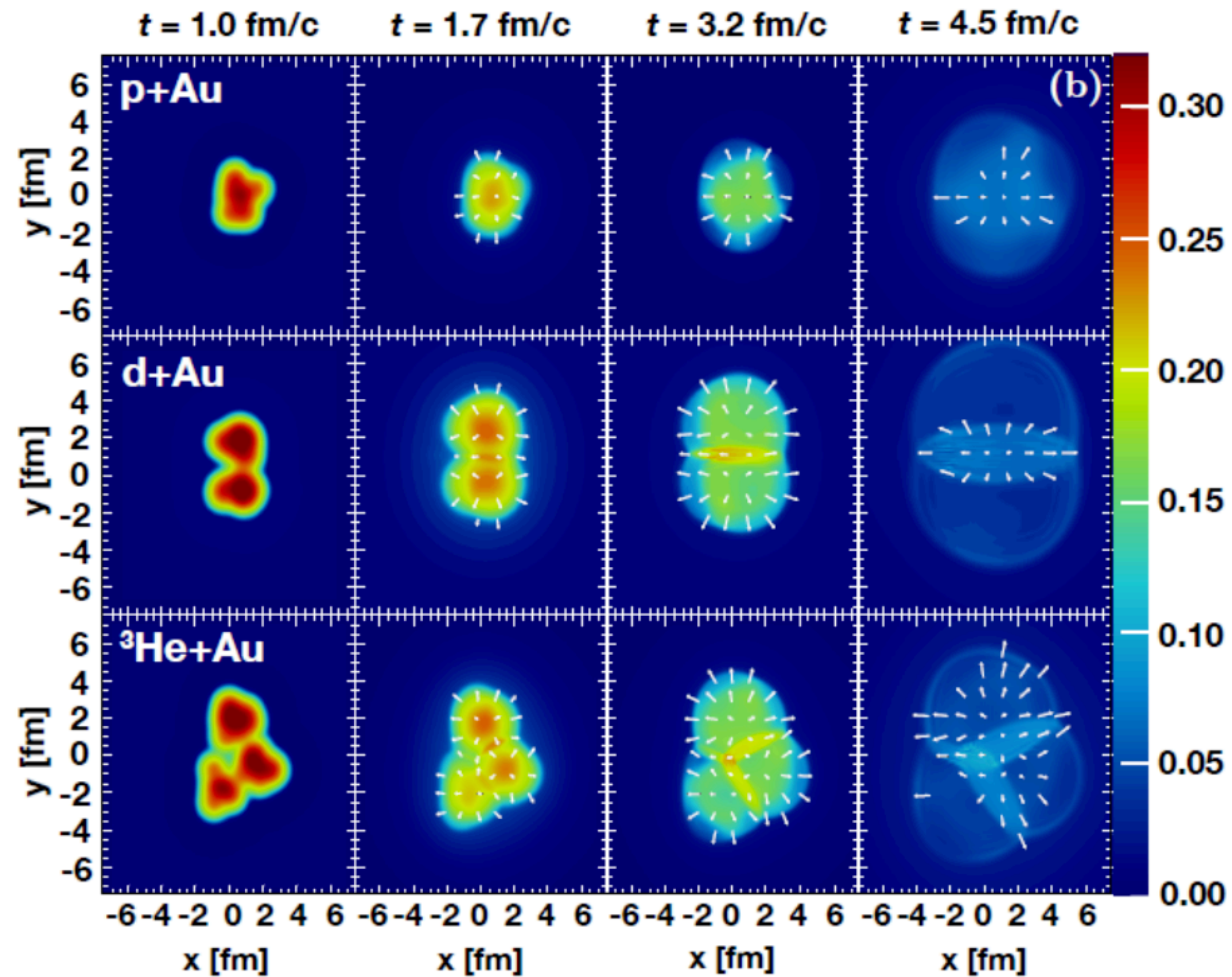


- Simulate small systems dynamically in 3+1D
- Initialize using MC-Glauber + string deceleration model with source terms in hydro
- Provides fluctuating transverse+longitudinal geometry



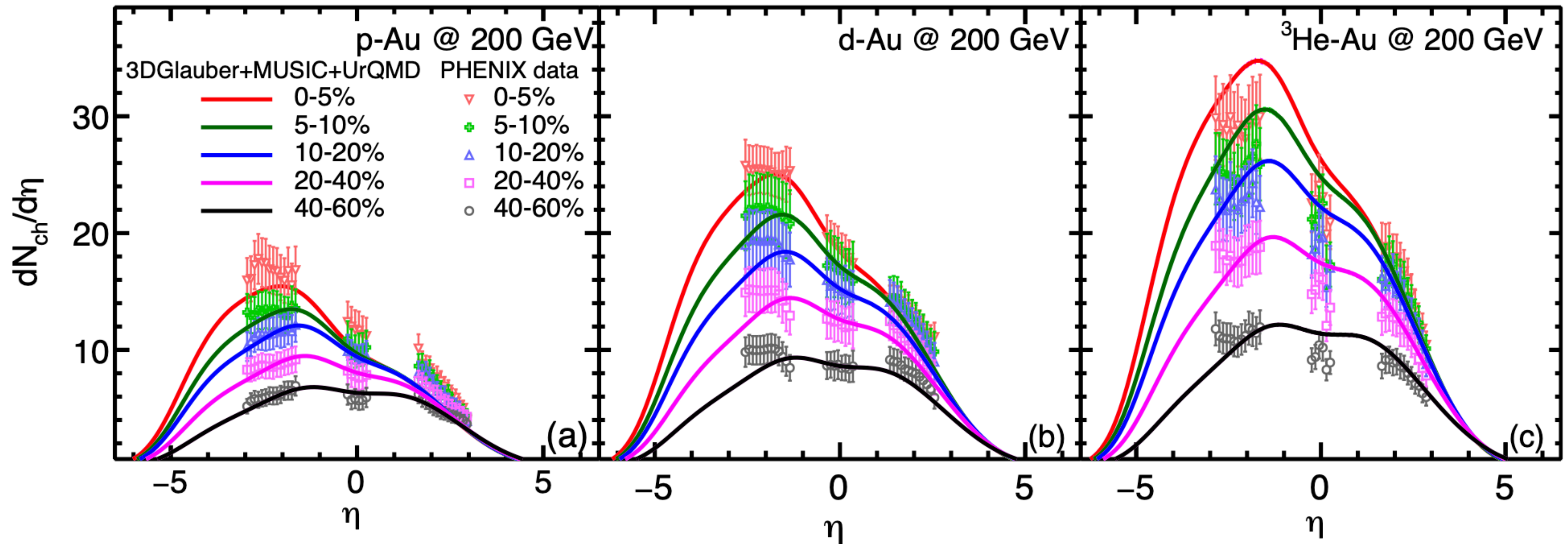
SMALL SYSTEM SCAN AT RHIC

PHENIX Collaboration, Nature Phys. 15, no.3, 214-220 (2019)



MULTIPLICITY VS. RAPIDITY

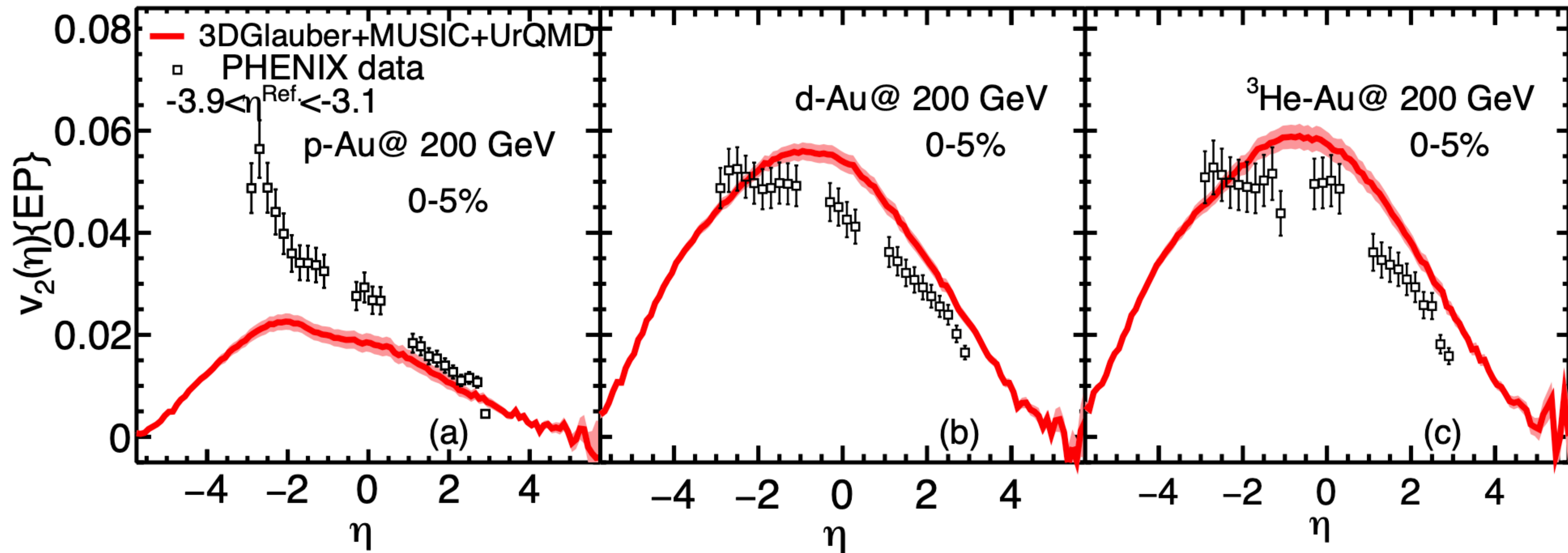
W. Zhao, S. Ryu, C. Shen and B. Schenke, Phys.Rev.C 107 (2023) 1, 014904



The (3+1)D hybrid model captures the rapidity and centrality dependence of $dN^{ch}/d\eta$ for all asymmetric systems

ANISOTROPIC FLOW VS RAPIDITY

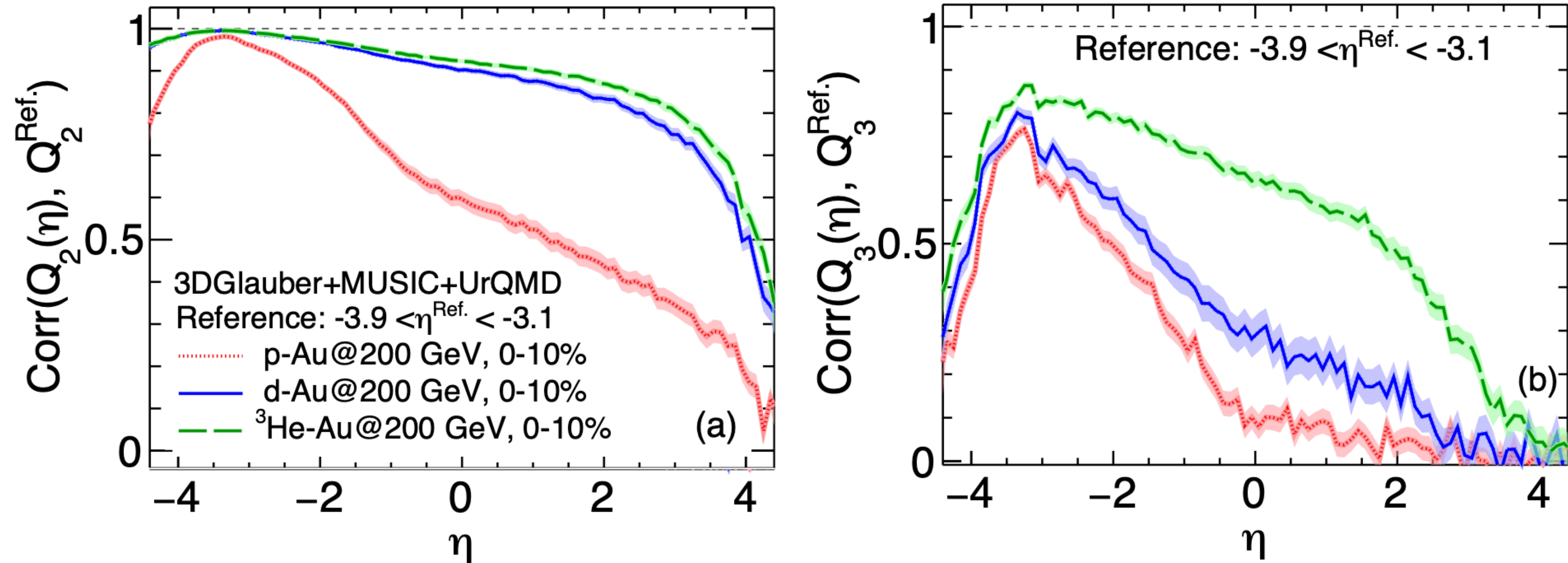
W. Zhao, S. Ryu, C. Shen and B. Schenke, Phys.Rev.C 107 (2023) 1, 014904



- Pseudo-rapidity dependence of $v_2\{EP\}$ reproduced for d+Au and $^3\text{He+Au}$
- The elliptic flow in $\eta < 1$ in p+Au collisions is underestimated because of the strong longitudinal flow decorrelation in our model + potential non-flow

FLOW VECTOR DECORRELATION

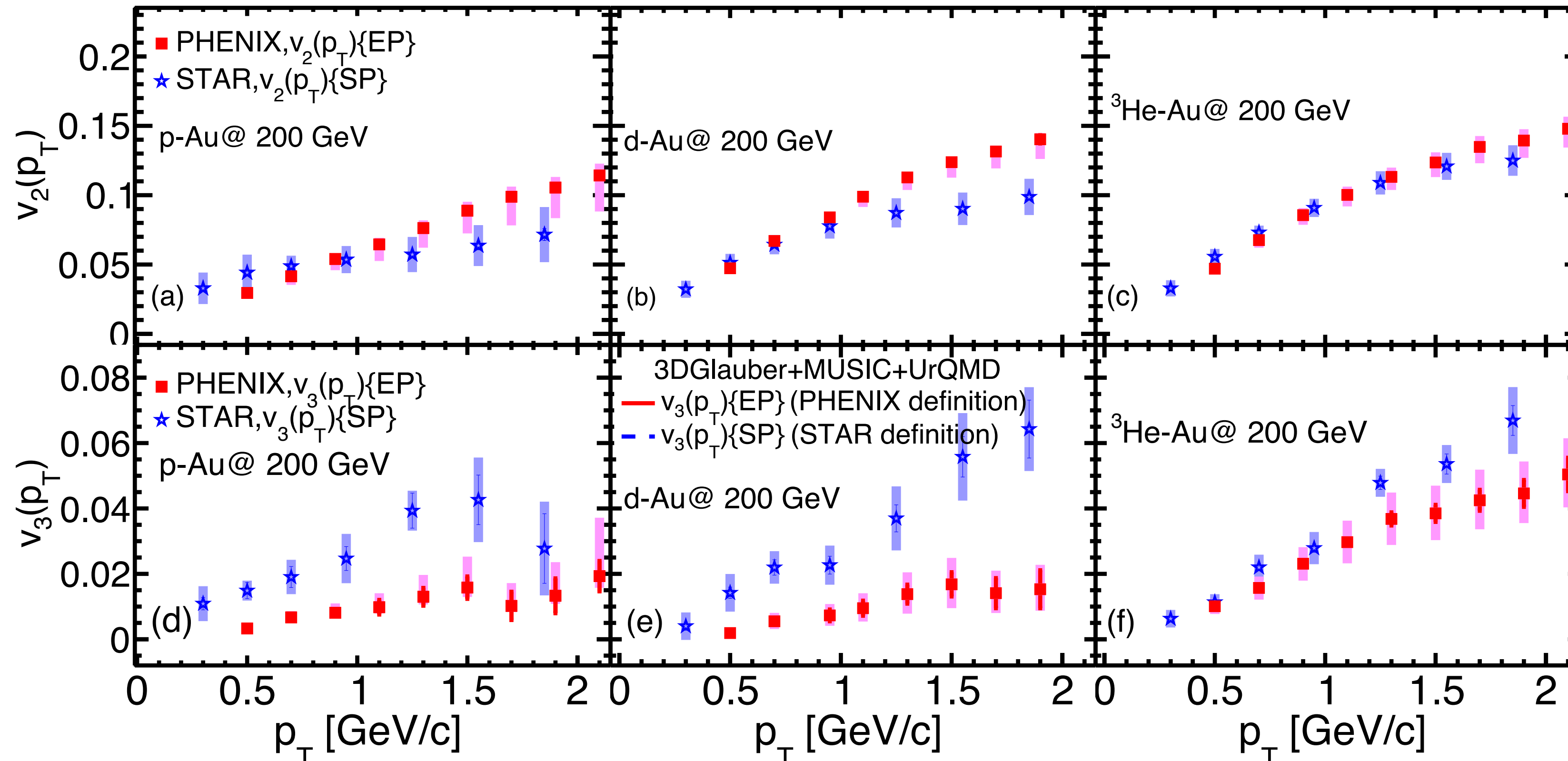
W. Zhao, S. Ryu, C. Shen and B. Schenke, Phys.Rev.C 107 (2023) 1, 014904



- Decorrelation is much stronger in the smaller p+Au system
- Decorrelations of v_3 flow vectors are much stronger than v_2
- **Hierarchy between v_n and systems driven by decorrelation in this model**

COMPARING PHENIX WITH STAR DATA

PHENIX Collaboration, Nature Phys. 15, no.3, 214-220 (2019) STAR Collaboration, Phys.Rev.Lett. 130 (2023) 24, 242301



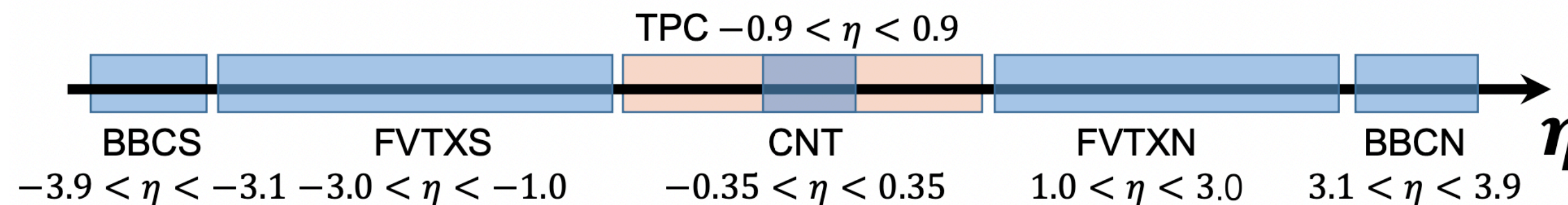
PHENIX:

(p, d)+Au: $\eta_1 \in [-3.9, -3.1]$,
 $\eta_2 \in [-0.35, 0.35]$

$^3\text{He}+\text{Au}$: $\eta_1 \in [-3, -1]$,
 $\eta_2 \in [-0.35, 0.35]$

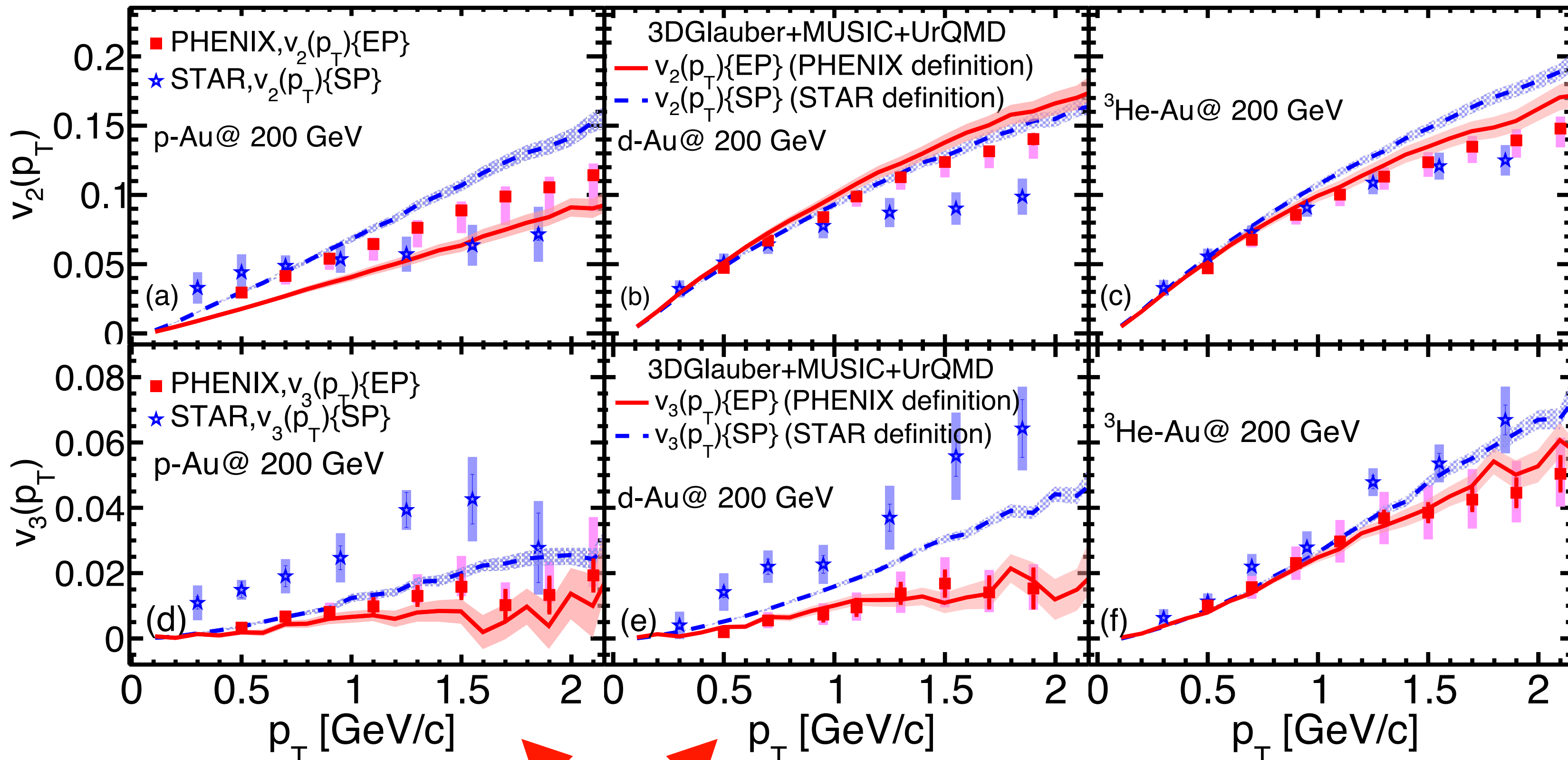
STAR:

$\eta \in [-0.9, 0.9]$ with $|\Delta\eta| > 1$



DIFFERENT RAPIDITY BINS, DIFFERENT RESULTS

W. Zhao, S. Ryu, C. Shen and B. Schenke, Phys.Rev.C 107 (2023) 1, 014904



PHENIX:

(p, d)+Au: $\eta_1 \in [-3.9, -3.1]$,
 $\eta_2 \in [-0.35, 0.35]$

$^3\text{He}+\text{Au}$: $\eta_1 \in [-3, -1]$,
 $\eta_2 \in [-0.35, 0.35]$

STAR:

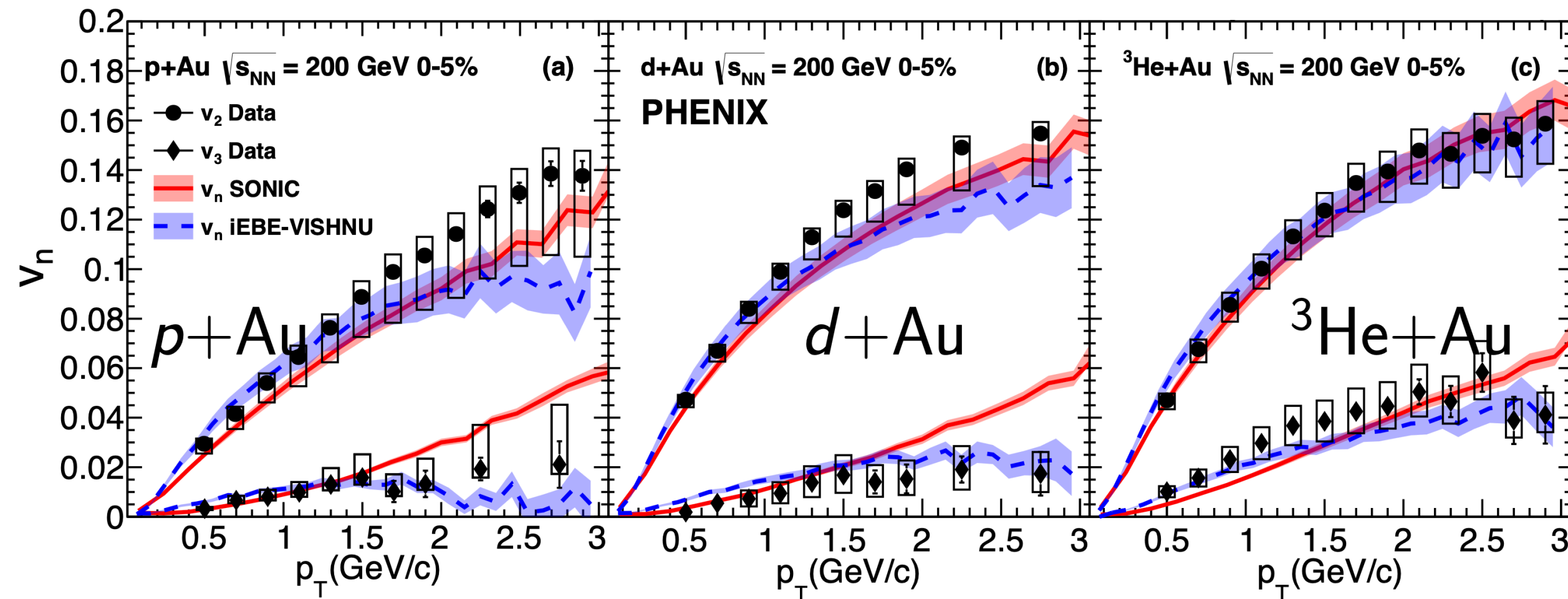
$\eta \in [-0.9, 0.9]$ with $|\Delta\eta| > 1$

Tune to $^3\text{He}+\text{Au}$
 PHENIX $v_n(p_T)$ in
 (d, ^3He)+Au collisions
 well described

Longitudinal flow decorrelations lead to smaller $v_3(p_T)$ for PHENIX, explaining $\sim 50\%$ of the difference between the two measurements

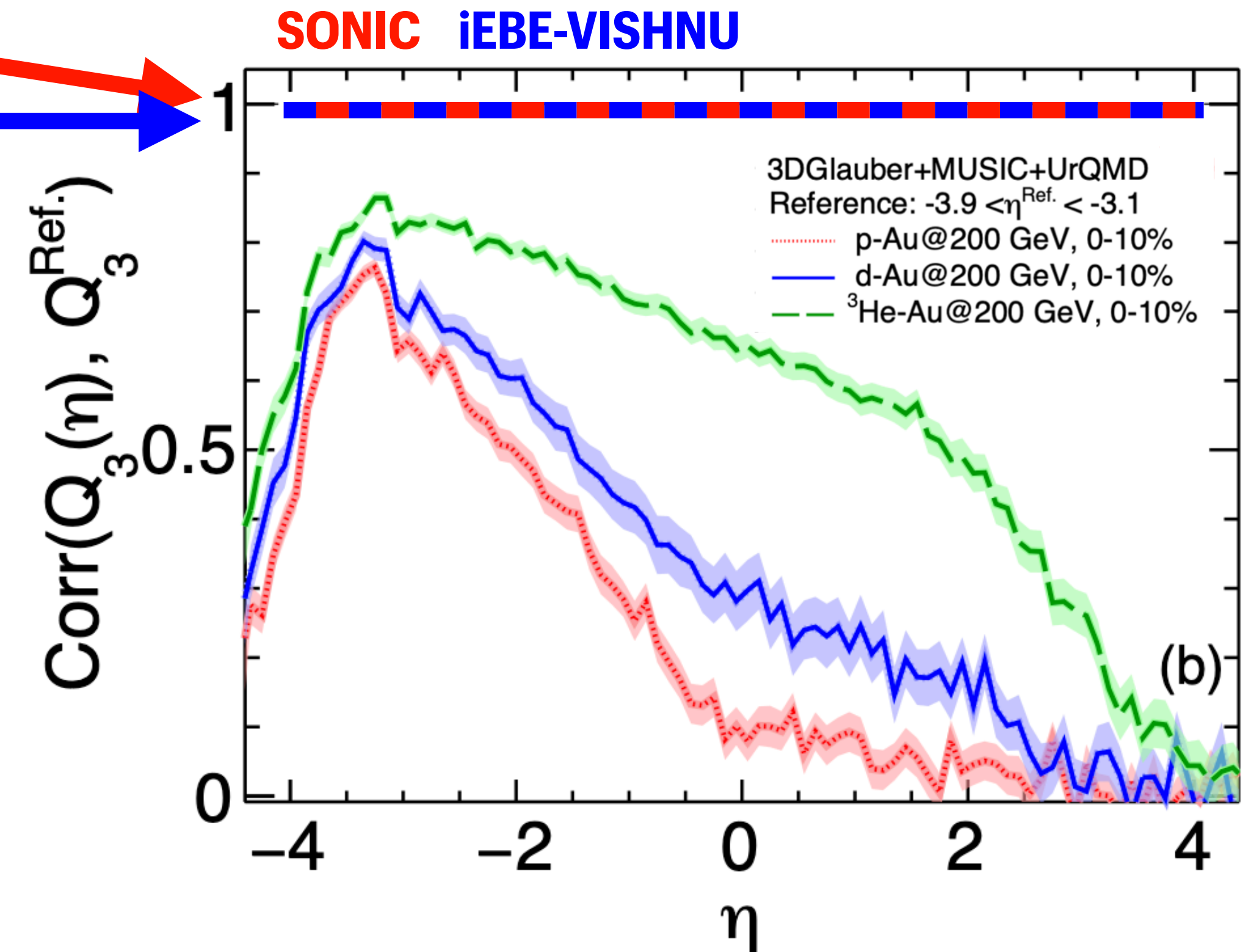
COMPARISON WITH BOOST INVARIANT MODELS

W. Zhao, S. Ryu, C. Shen and B. Schenke, *Phys.Rev.C* 107 (2023) 1, 014904



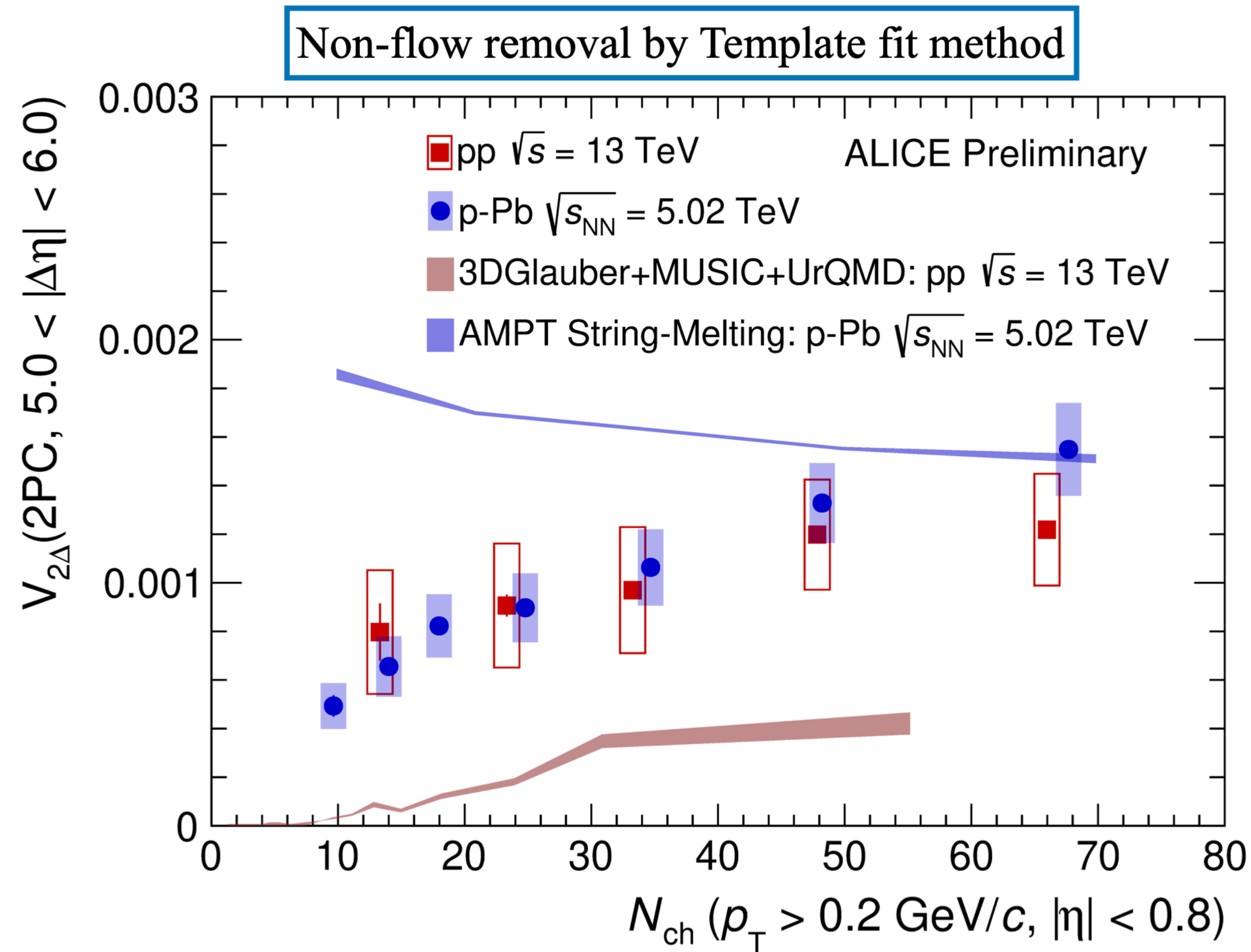
PHENIX Collaboration, *Nature Phys.* 15, no.3, 214-220 (2019)

- Meaningful comparison?
- Assuming boost invariance and ignoring decorrelation can cause large errors
- Same problem for all boost invariant models



VERY LONG RANGE CORRELATIONS

ALICE Collaboration, ALI-PREL-573662, talk by Debojit Sarkar



- p+p collisions at 13 TeV
- $5 < |\Delta\eta| < 6$
- Models do not describe the data
- Need better description of 3D geometry
- Applicability of hydrodynamics?

APPLICABILITY OF HYDRODYNAMICS

- Initial transverse volume in small systems 50 × smaller than in central Pb+Pb
- Locally large Knudsen (macroscopic scale / microscopic scale) and inverse Reynolds numbers (ratio of viscous forces to inertial forces)
- Could lead to inaccurate results
- Use non-equilibrium component: Early time free streaming, effective kinetic theory, or core-corona models
- Far from equilibrium, causality could be violated
- Alternative to Israel-Stewart like theories, BDNK, can be shown to be causal

G. Inghirami, H. Elfner, *Eur.Phys.J.C* 82 (2022) 9, 796

A. Kurkela, A. Mazeliauskas, J.-F. Paquet, S. Schlichting, and D. Teaney
Phys. Rev. Lett. 122(12), 122302

BDNK:

F. S. Bemfica, M. M. Disconzi, and J. Noronha, *Phys. Rev. X.* 12(2), 021044 (2022)

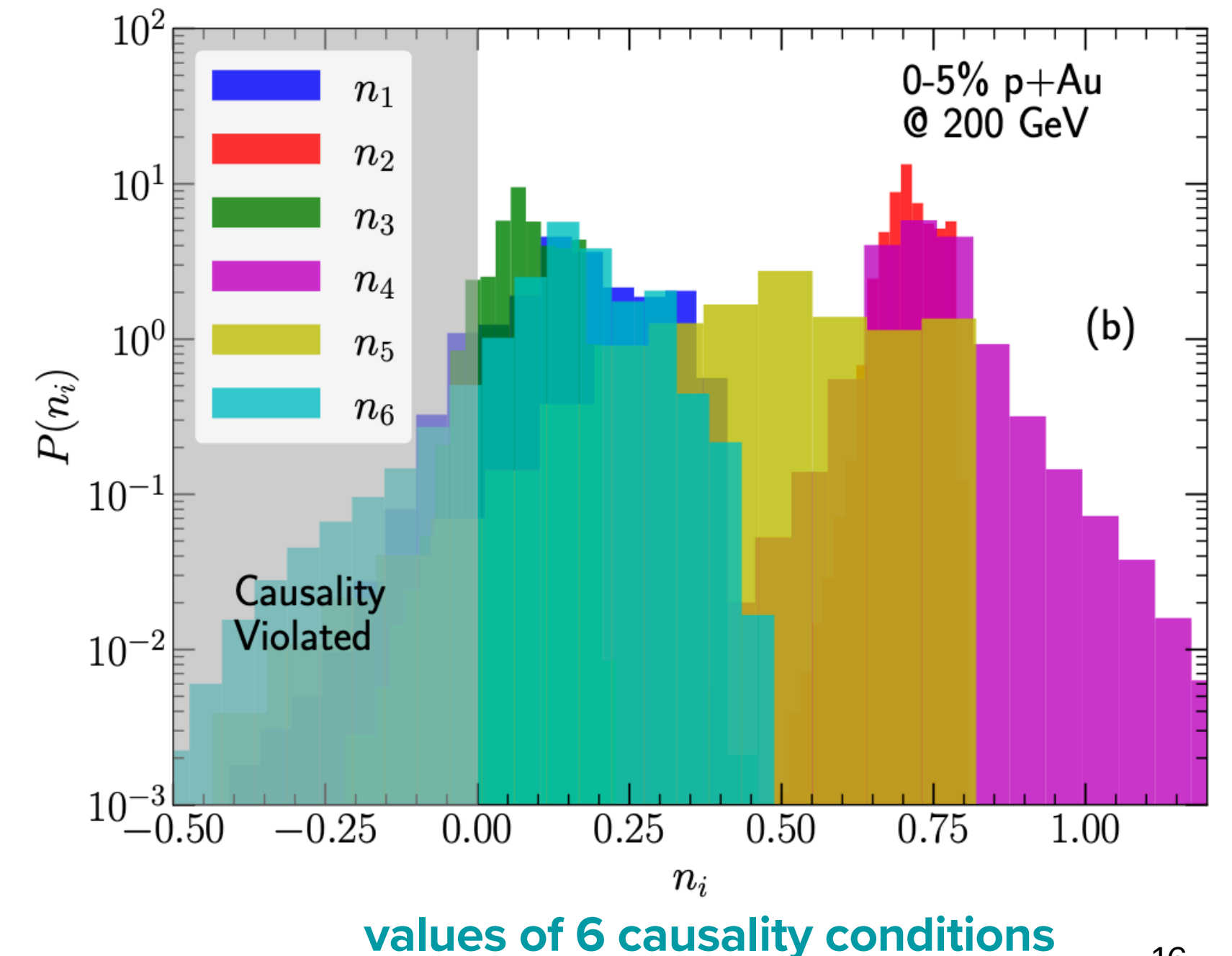
P. Kovtun, *JHEP* 10 (2019) 034

Causality:

C. Plumberg, D. Almaalol, T. Dore, J. Noronha, J. Noronha-Hostler, *Phys. Rev. C.* 105(6), L061901 (2022)

C. Chiu and C. Shen, *Phys. Rev. C.* 103(6), 064901 (2021)

ExTrEMe Collaboration, R. Krupczak et al., *Phys.Rev.C* 109 (2024) 3, 034908



APPLICABILITY OF HYDRODYNAMICS

- Initial transverse expansion
- Locally large Reynolds number
- Could lead to hydrodynamic flow
- Use non-equilibrium hydrodynamic theory, or kinetic theory
- Far from equilibrium
- Alternative: BDNK, causality



See contribution to Quark-Gluon Plasma 6 (World Scientific):

Progress and Challenges in Small Systems

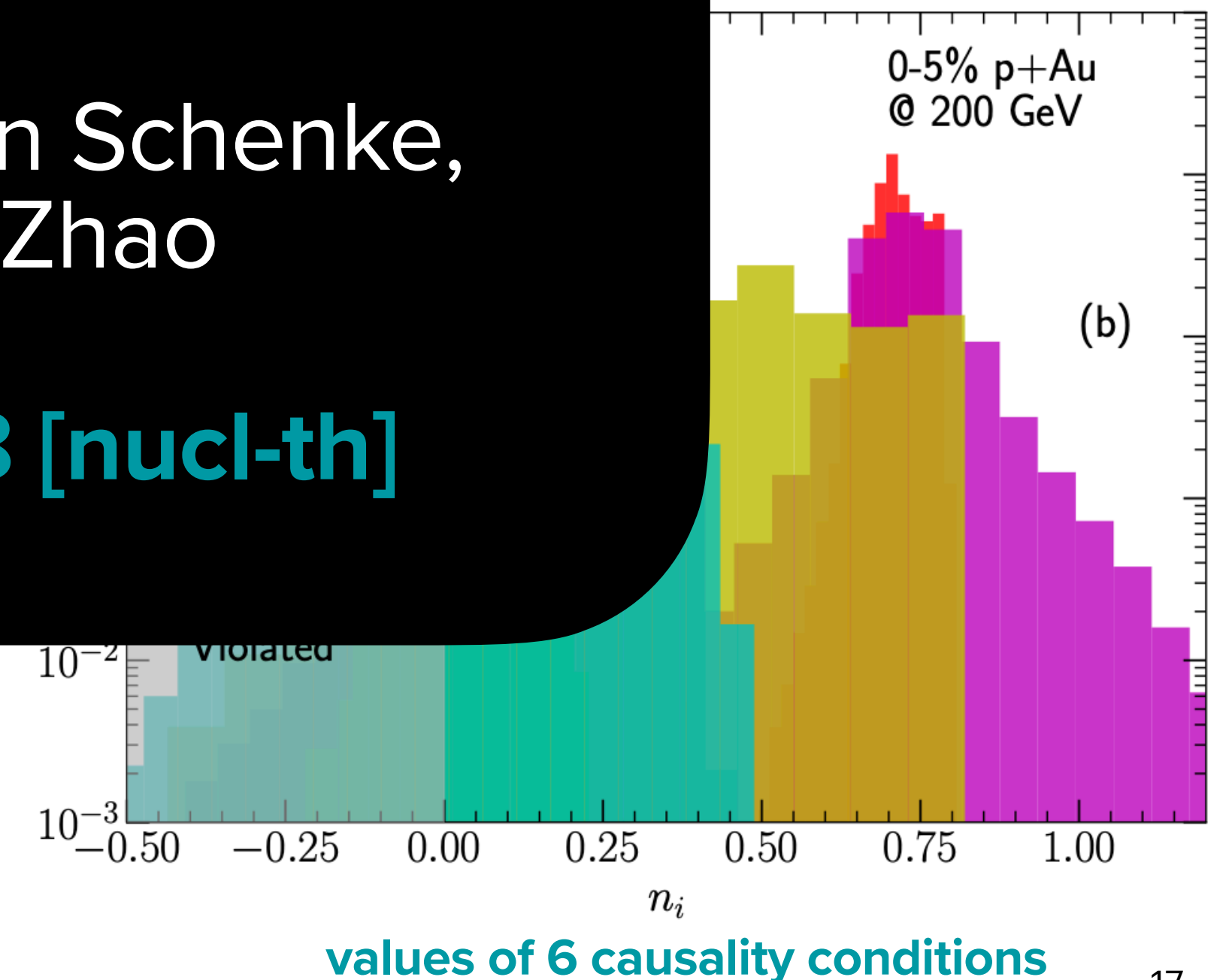
Jorge Noronha, Björn Schenke, Chun Shen, Wenbin Zhao

e-Print: [2401.09208 \[nucl-th\]](https://arxiv.org/abs/2401.09208)

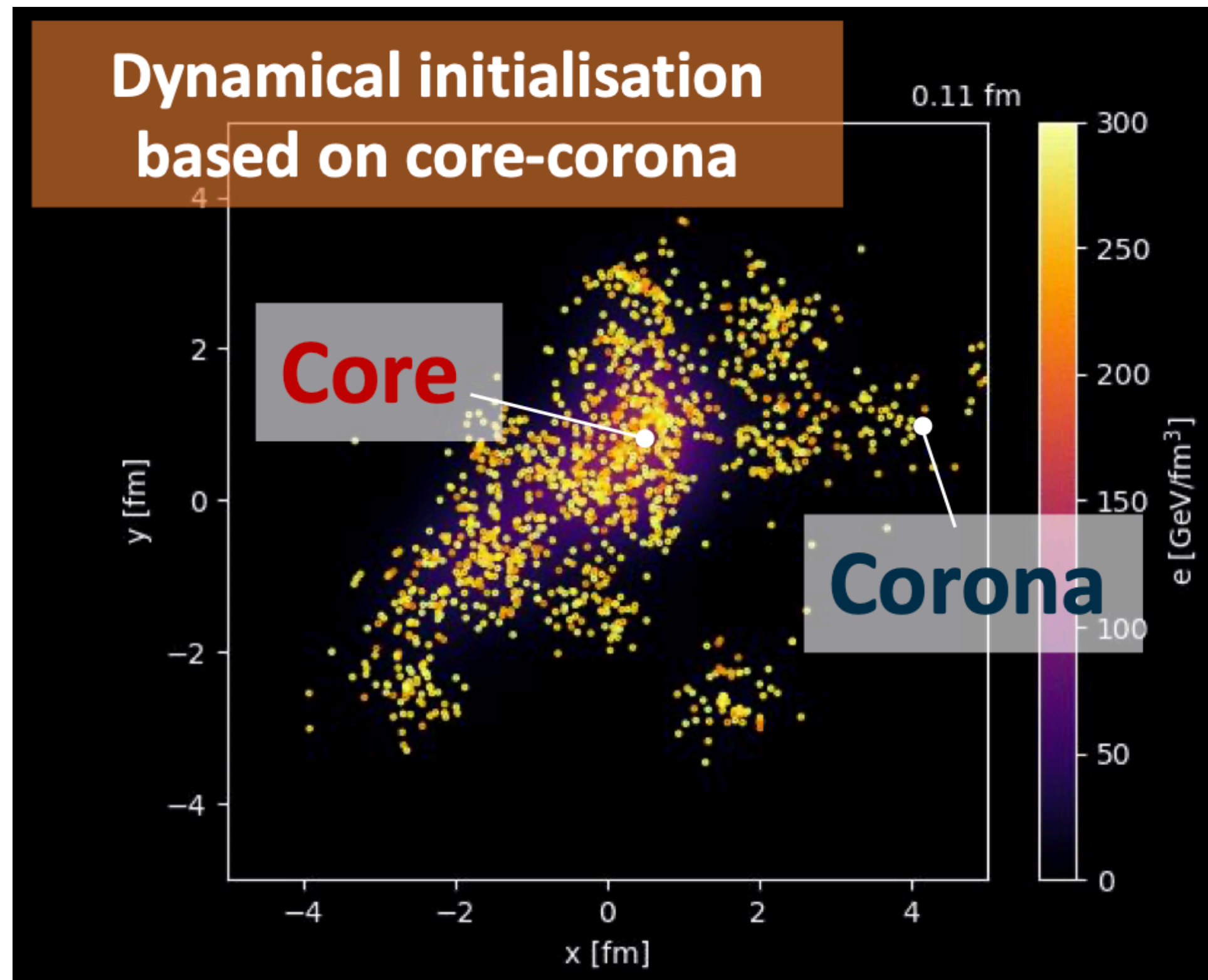
G. Inghirami, H. Elfner, A. Kurkela, A. Mazelia, Phys. Rev. Lett. 122(12)

BDNK: F. S. Bemfica, M. M. Disler, P. Kovtun, JHEP 10 (2019)

Causality: C. Plumberg, D. Almaalol, T. Dore, J. Noronha, J. Noronha-Hostler, Phys. Rev. C. 105(6), L061901 (2022)
C. Chiu and C. Shen, Phys. Rev. C. 103(6), 064901 (2021)
ExTrEMe Collaboration, R. Krupczak et al., Phys.Rev.C 109 (2024) 3, 034908

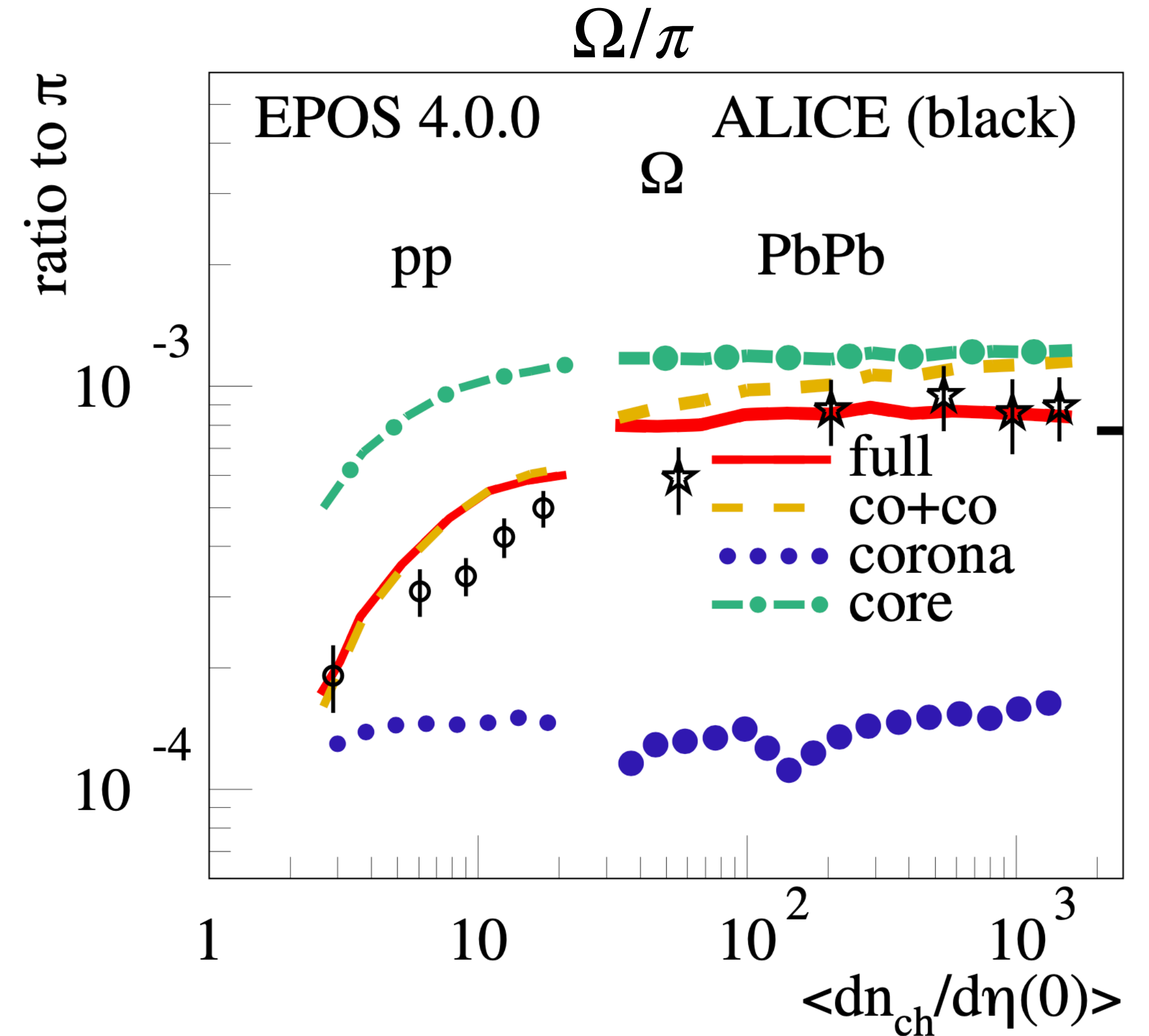


CORE+CORONA PICTURE



Y. Kanakubo, Quark Matter 2023

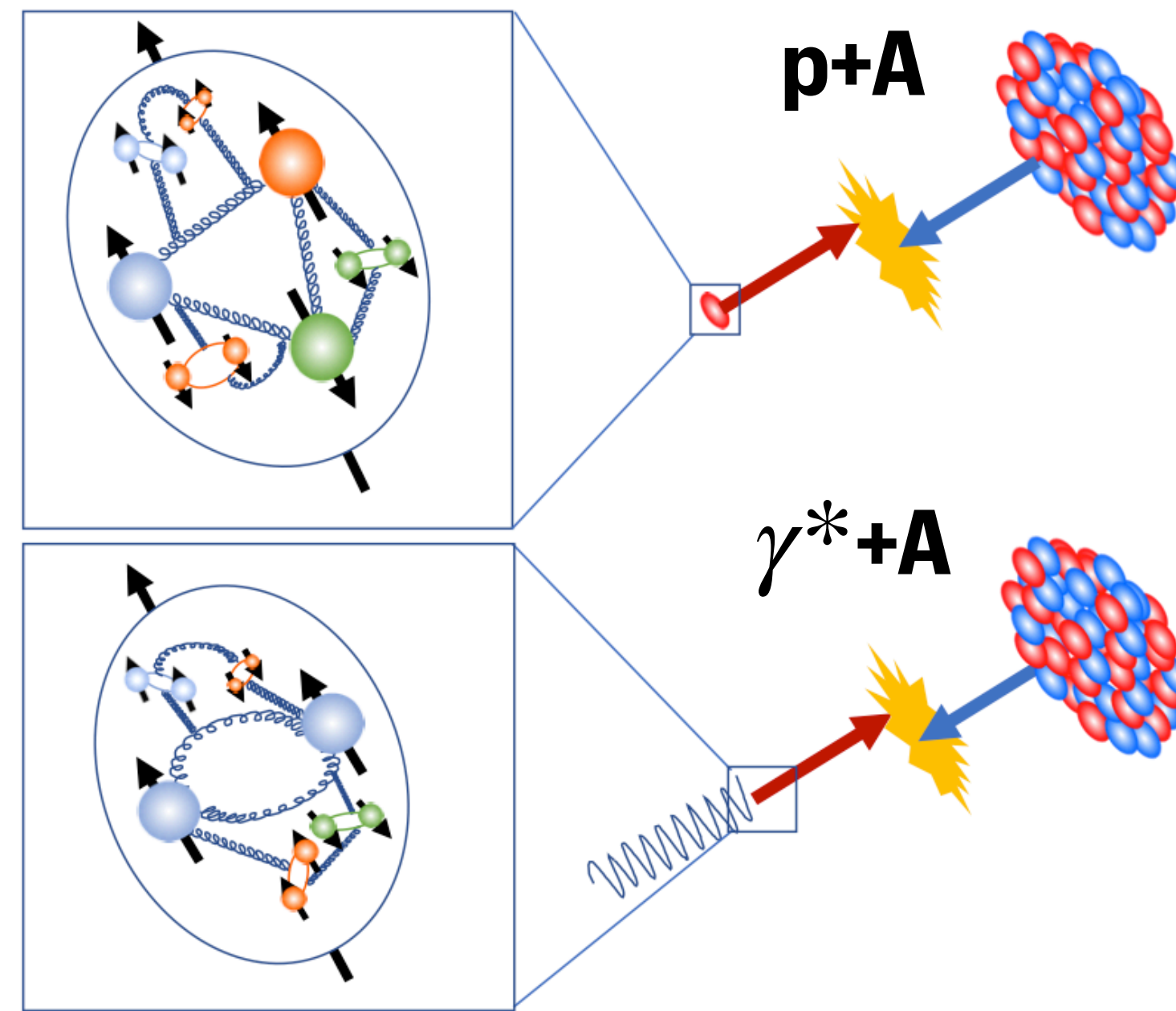
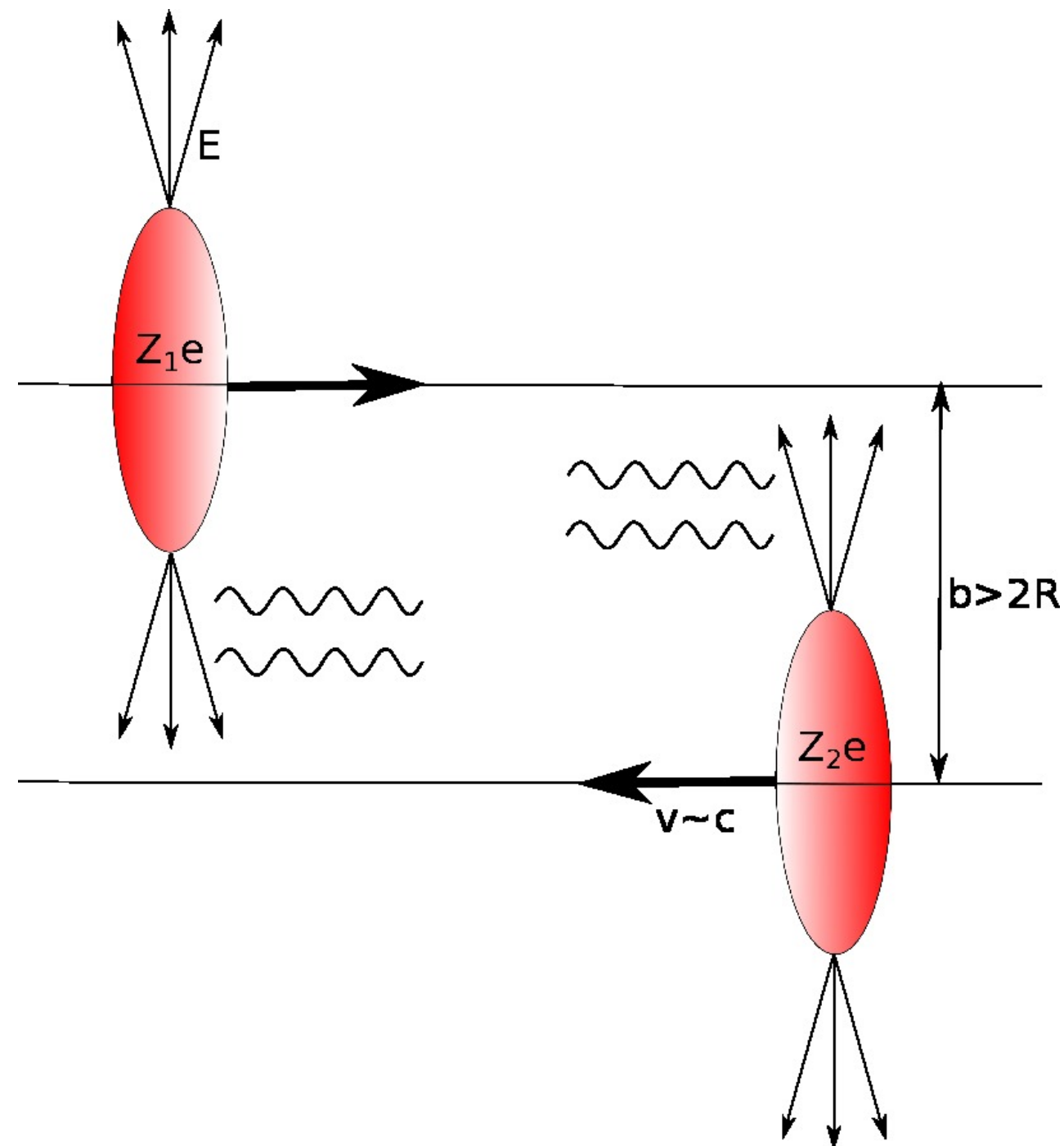
Hydro-like core begins to dominate for $dN_{ch}/d\eta \approx 10 - 20$



K. Werner, Phys.Rev.C 108 (2023) 6, 064903
see talk by P.B. Gossiaux

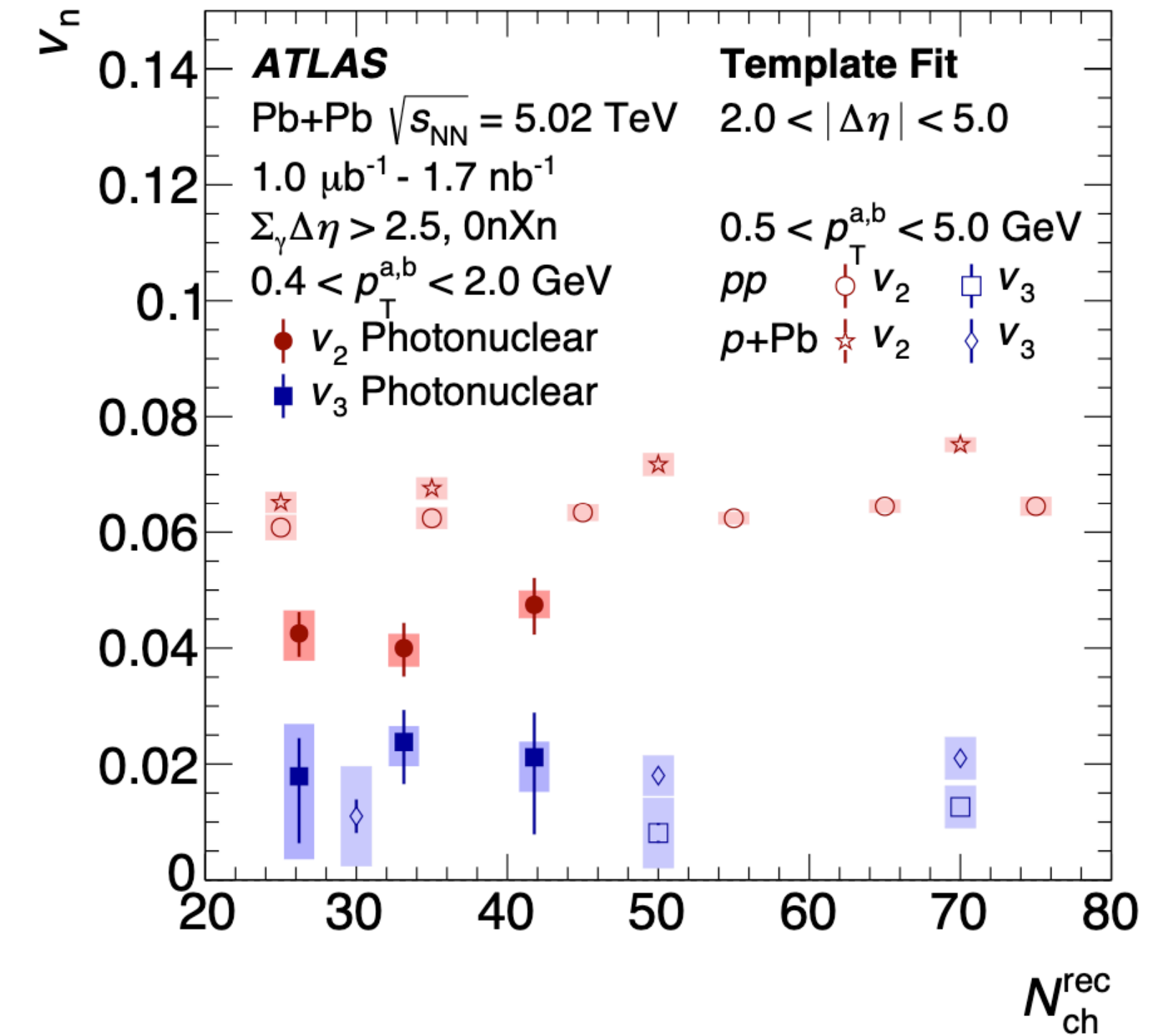
SMALLER: ULTRAPERIPHERAL COLLISIONS

W. Zhao, C. Shen and B. Schenke, Phys.Rev.Lett. 129 (2022) 25, 252302



Phys. Rev. D 103, 054017 (2021)

ATLAS Phys. Rev. C 104, 014903 (2021)

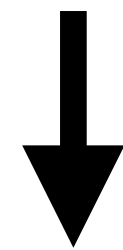


- Long range two-particle correlations were observed in photo-nuclear processes in ultra-peripheral Pb+Pb collisions (UPC) at the LHC
- The magnitudes of v_n in UPCs are comparable with those in p+Pb collisions

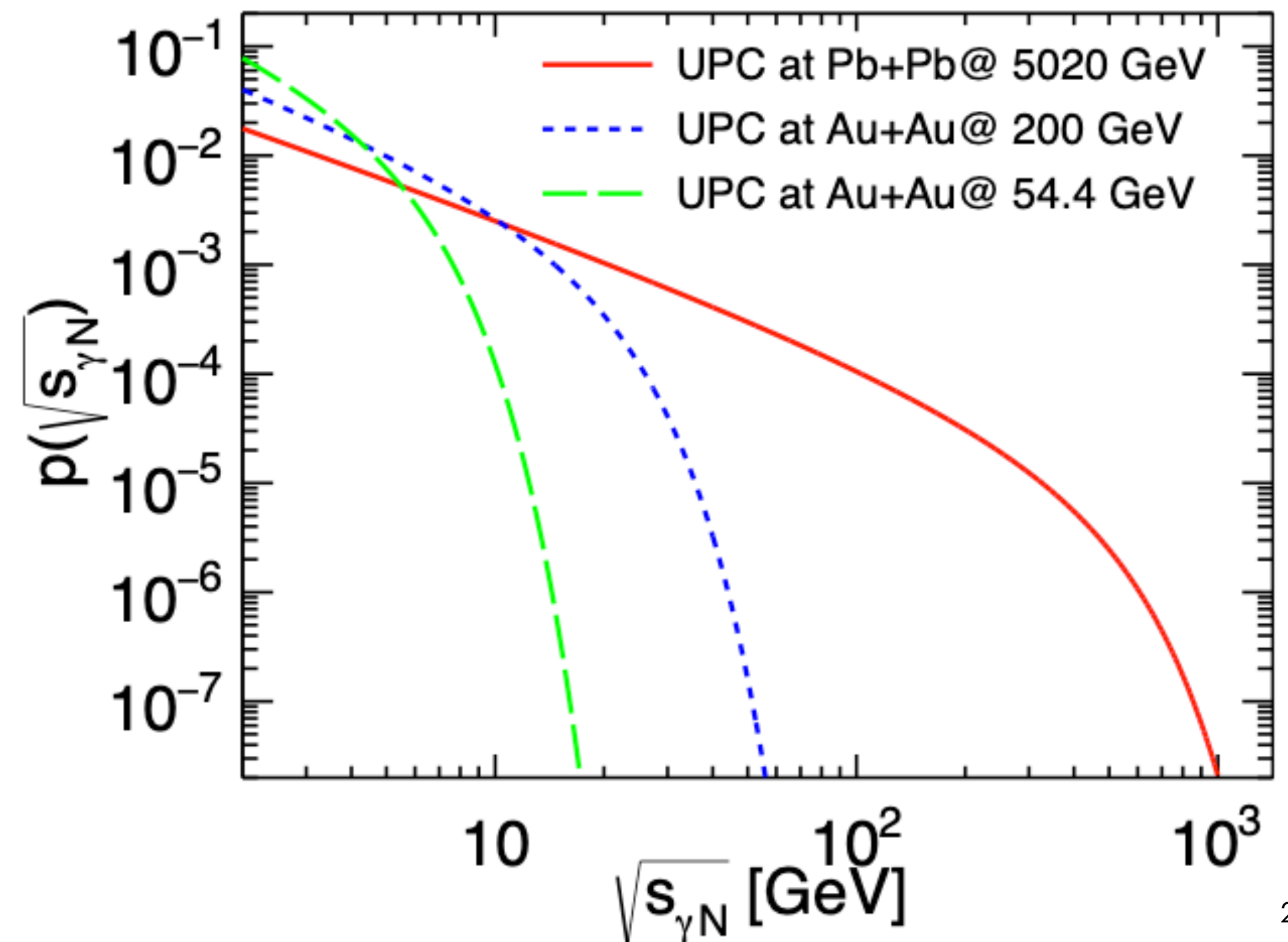
MODELING $\gamma^* + \text{Pb}$

A. J. Baltz *et al.* Phys. Rept. 458, 1-171 (2008); W. Zhao, C. Shen and B. Schenke, Phys.Rev.Lett. 129 (2022) 25, 252302

- Same 3+1D hydrodynamic model
- Virtual photon described as vector meson: quark-antiquark pair plus soft cloud
- Energy of the incoming photon fluctuates event by event

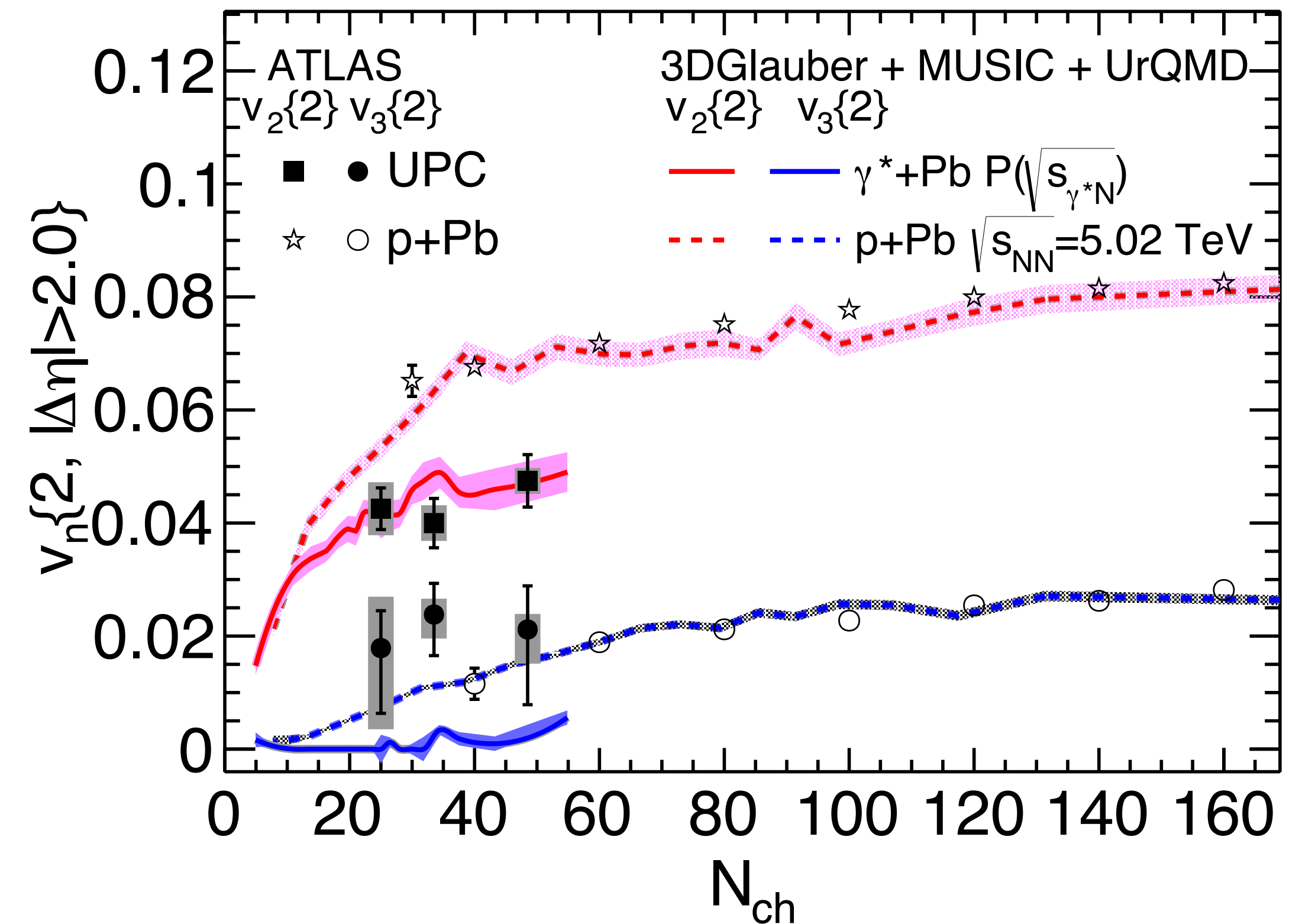
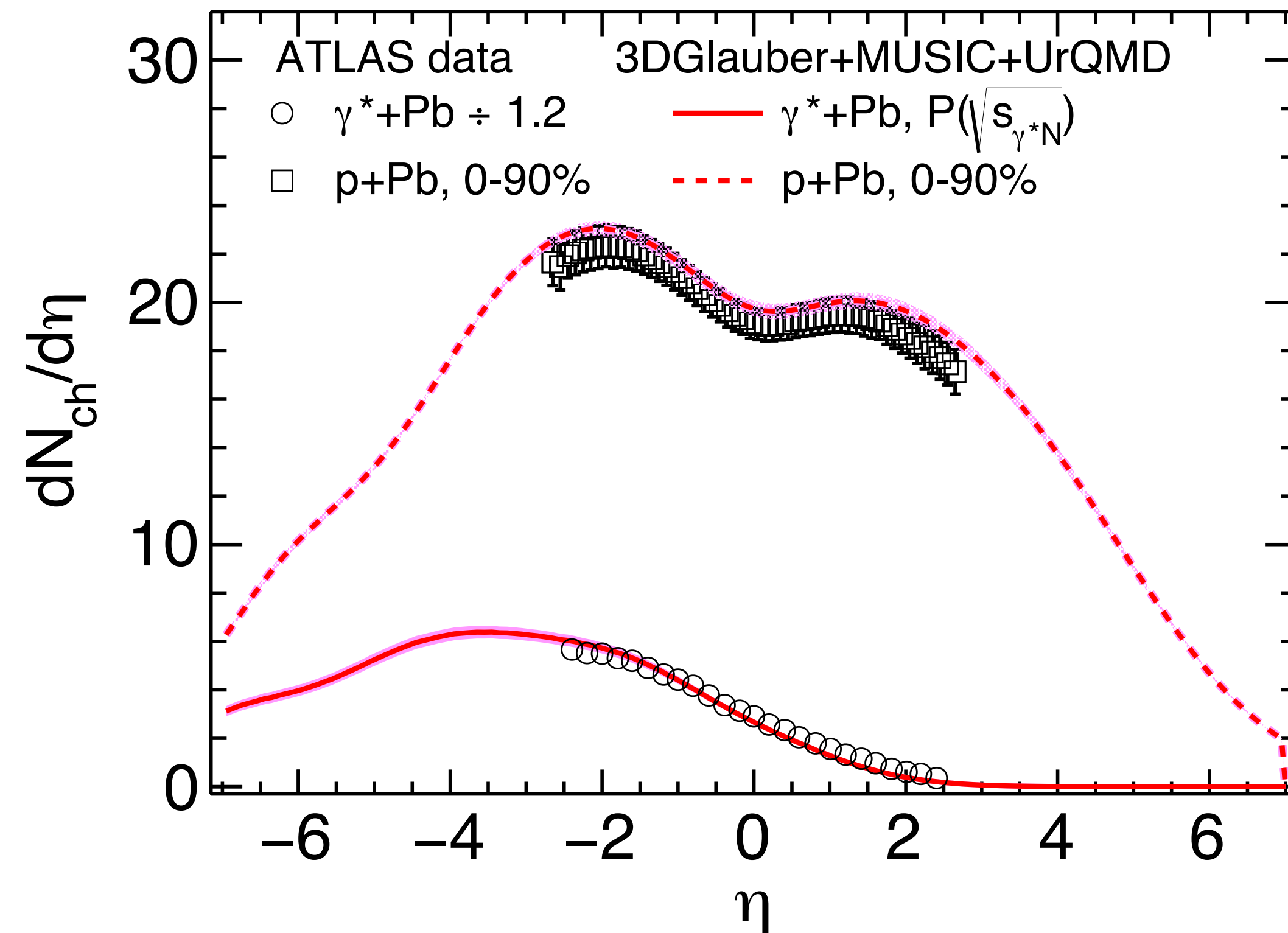


- Center of mass collision energy for the $\gamma^* + A$ system fluctuates
- Center of mass rapidity of $\gamma^* + A$ collision fluctuates in the lab frame



PARTICLE PRODUCTION AND FLOW IN p+A AND γ^*+A

W. Zhao, C. Shen and B. Schenke, Phys.Rev.Lett. 129 (2022) 25, 252302

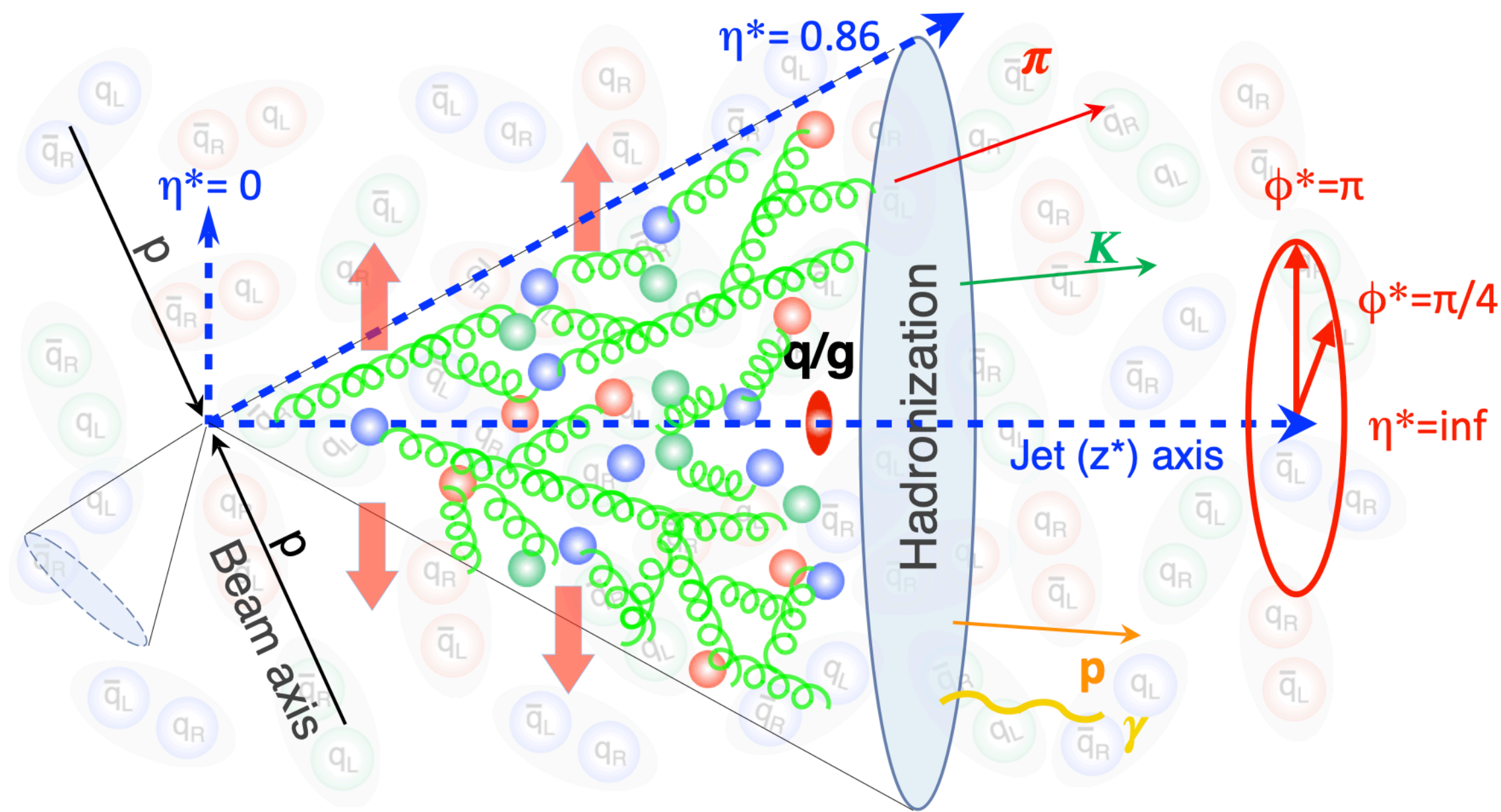


- Shapes of $dN_{ch}/d\eta$ reproduced for p+Pb and γ^*+Pb collisions
- Elliptic flow difference between p+Pb and γ^*+Pb collisions reproduced
 Driven by different amount of longitudinal flow decorrelation

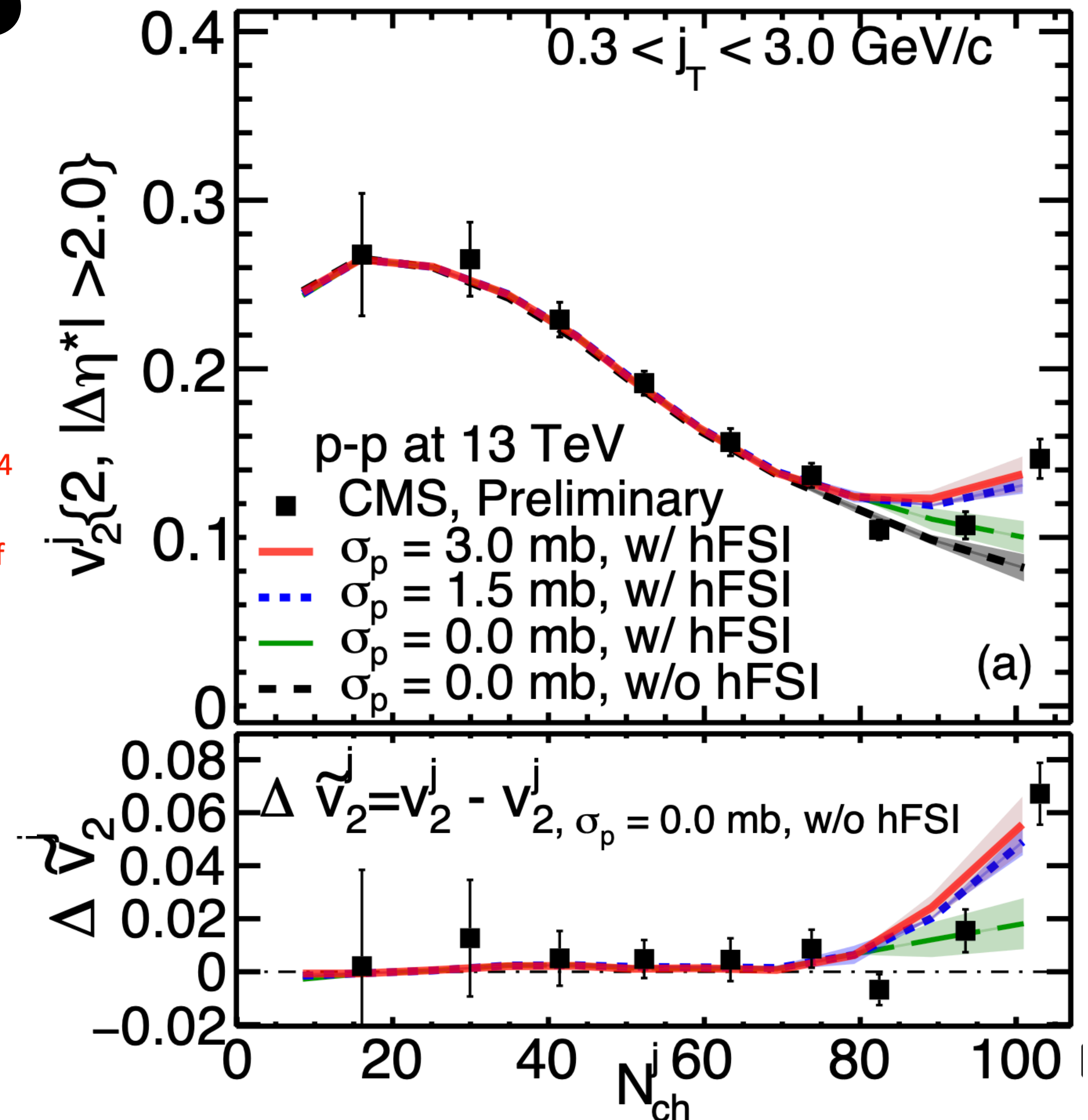
FLOW INSIDE JETS

CMS Collaboration, arXiv:2312.17103

W. Zhao, Z.-W. Lin, X.-N. Wang, arXiv:2401.13137

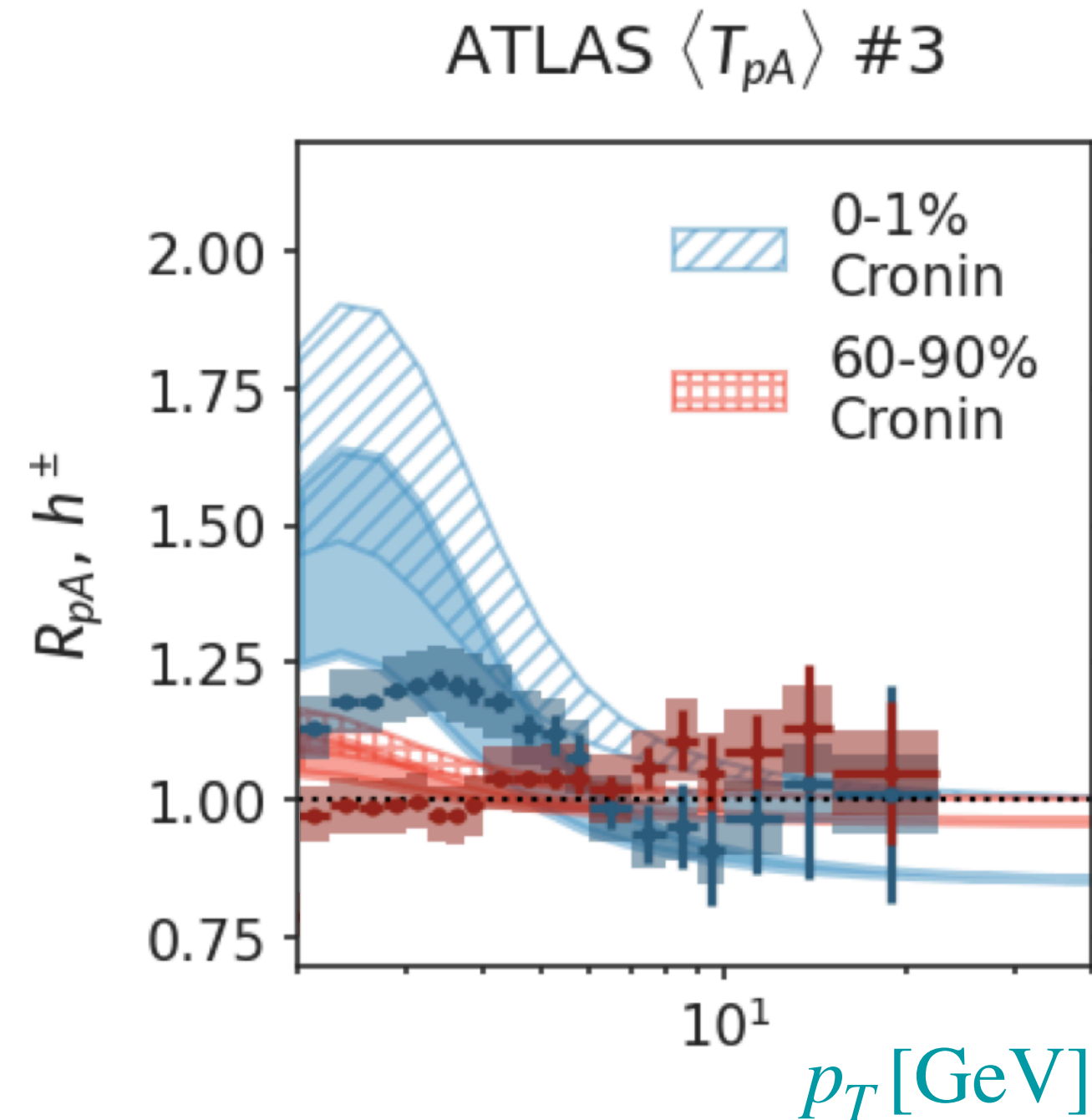


Final state effects can explain increase of v_2 at high multiplicity

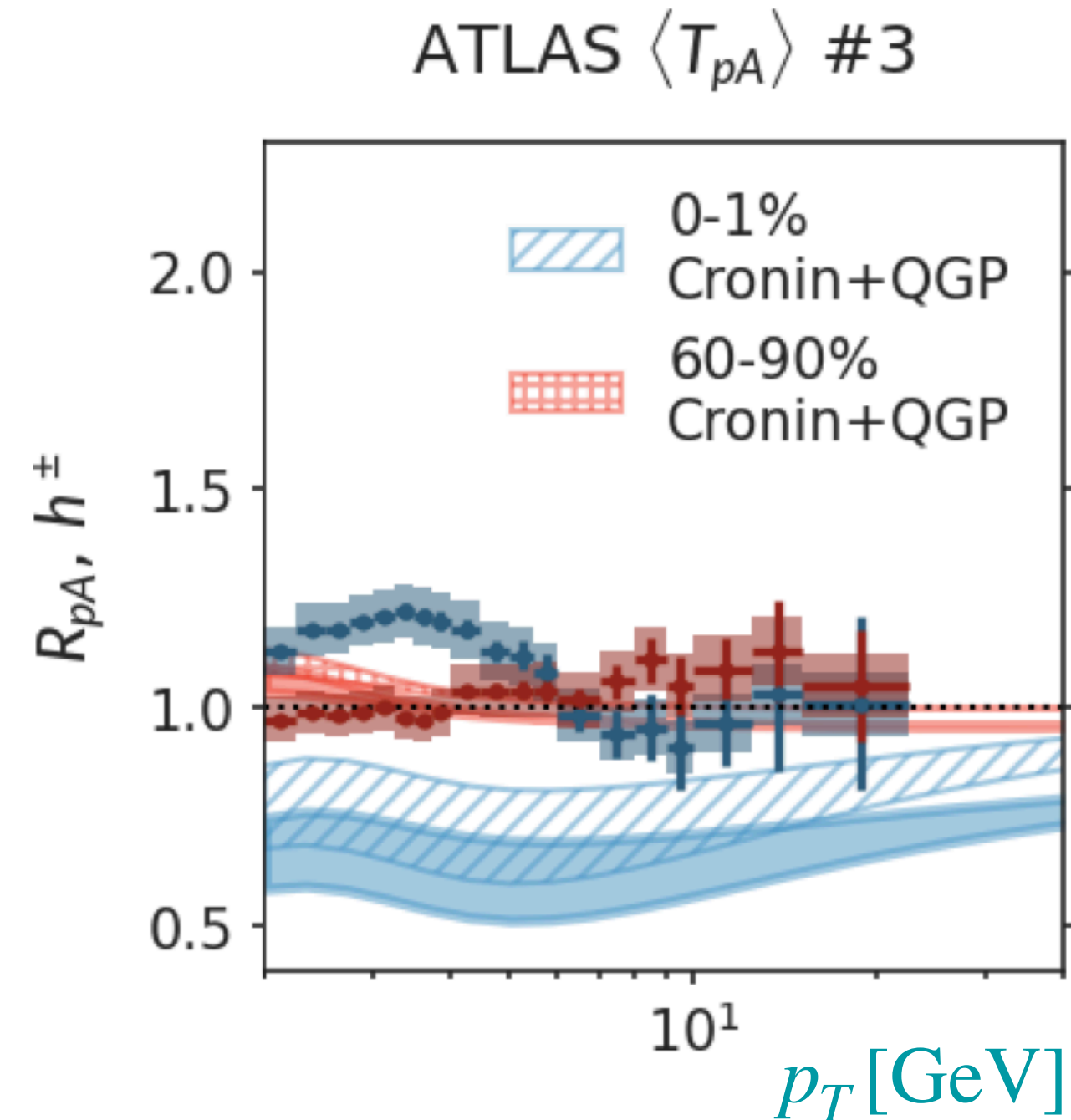


HARD PROBES

W. Ke, I. Vitev, *Phys.Rev.C* 107 (2023) 6, 064903



Calculation including cold nuclear matter effects



Same + QGP energy loss using SCET

Model of QGP formation in p+A as described by hydrodynamics leads to quenching of hadron spectra that is inconsistent with the p+Pb data

Agreement in d+Au collisions is better! (data has opposite high p_T behavior with centrality) \rightarrow

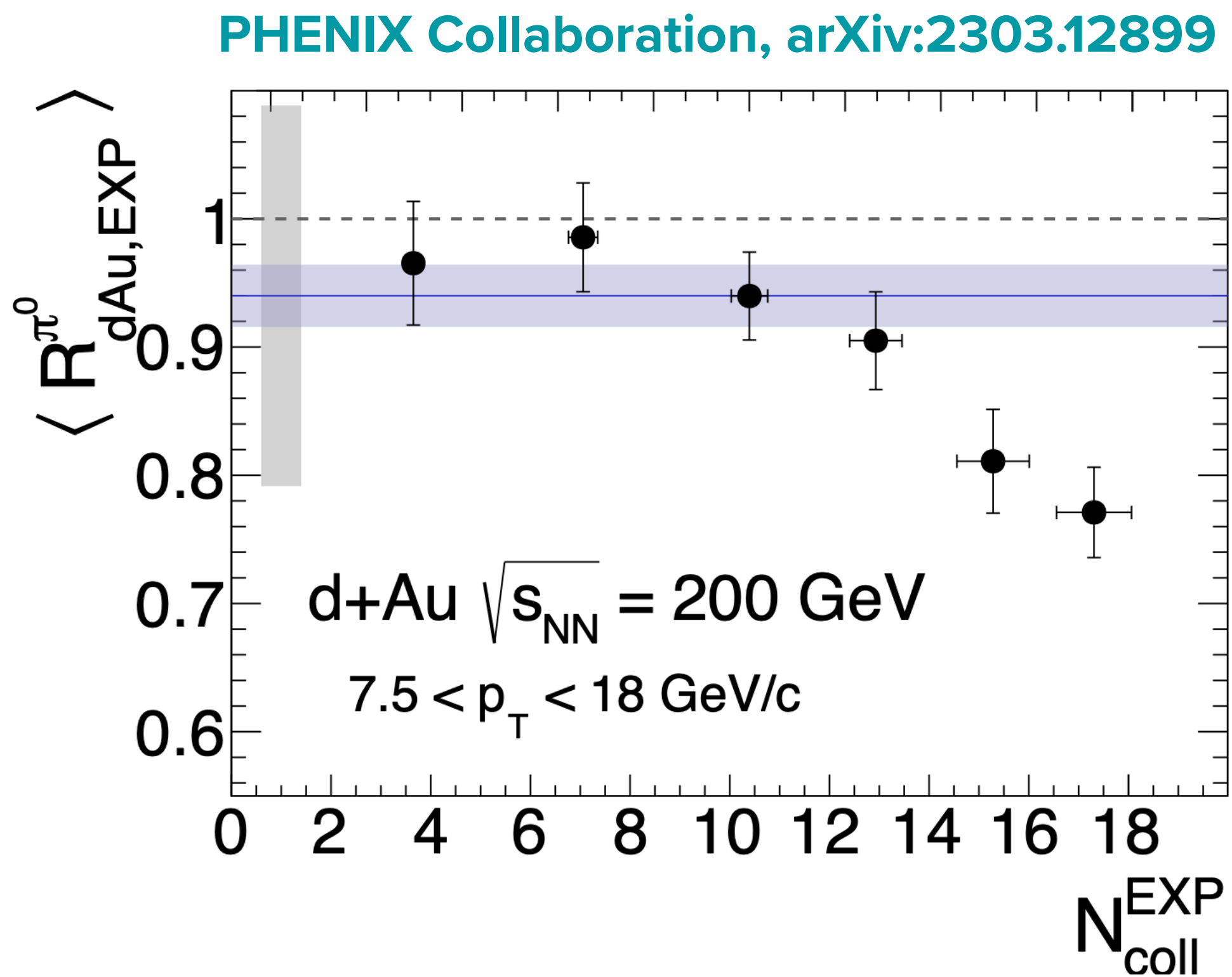
Centrality determination is critical

Correlation between hard and soft degrees of freedom important

A. Majumder for JETSCAPE, [arXiv:2308.02650](https://arxiv.org/abs/2308.02650)

HARD PROBES - EXPERIMENTAL N_{coll}

Removing centrality selection bias in π^0 suppression in d+Au collisions:



event activity from
direct photons



- Direct photons as benchmark for particle production from hard-scattering processes

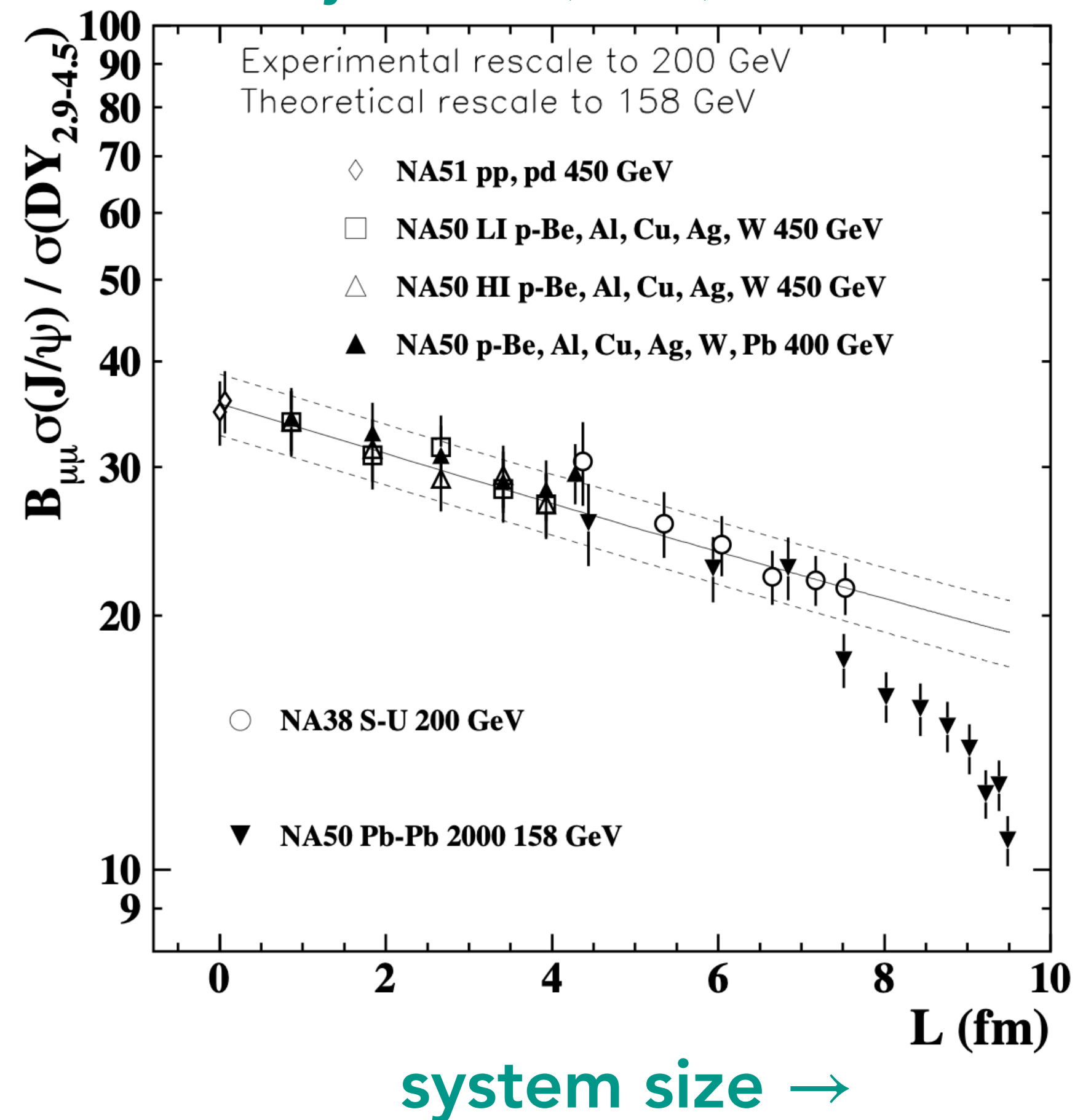
$$N_{\text{coll}}^{\text{EXP}} = Y_{dAu}^{\gamma^{\text{dir}}} / Y_{pp}^{\gamma^{\text{dir}}}$$

- Using a Glauber model N_{coll} led to enhancement at low N_{coll} \rightarrow now removed
- Suppression at large N_{coll} remains

J/PSI SUPPRESSION IN SMALL SYSTEMS

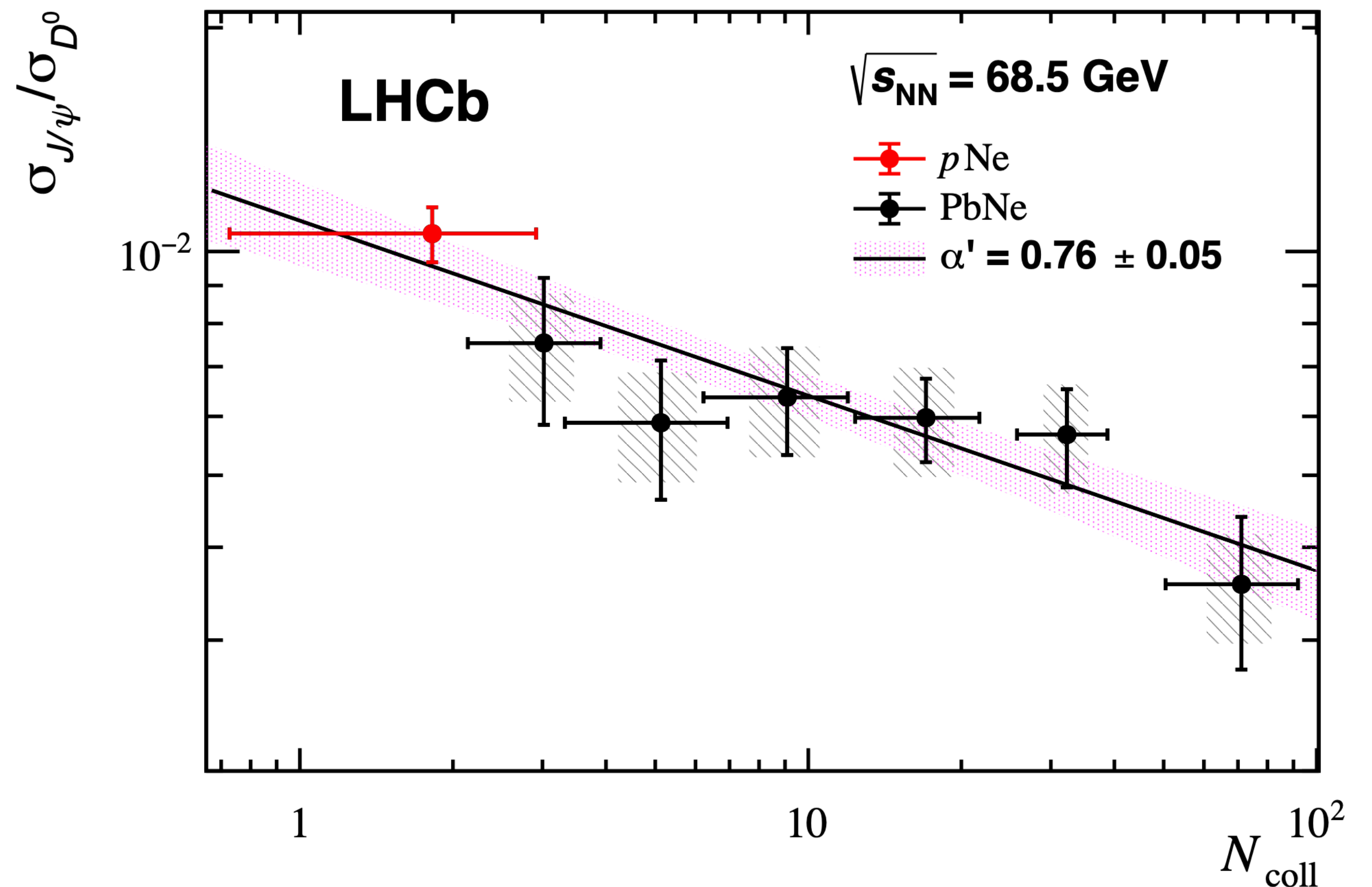
NA50 Collaboration

Eur.Phys.J.C 39 (2005) 335-345



No QGP-like J/ψ suppression in Pb+Ne

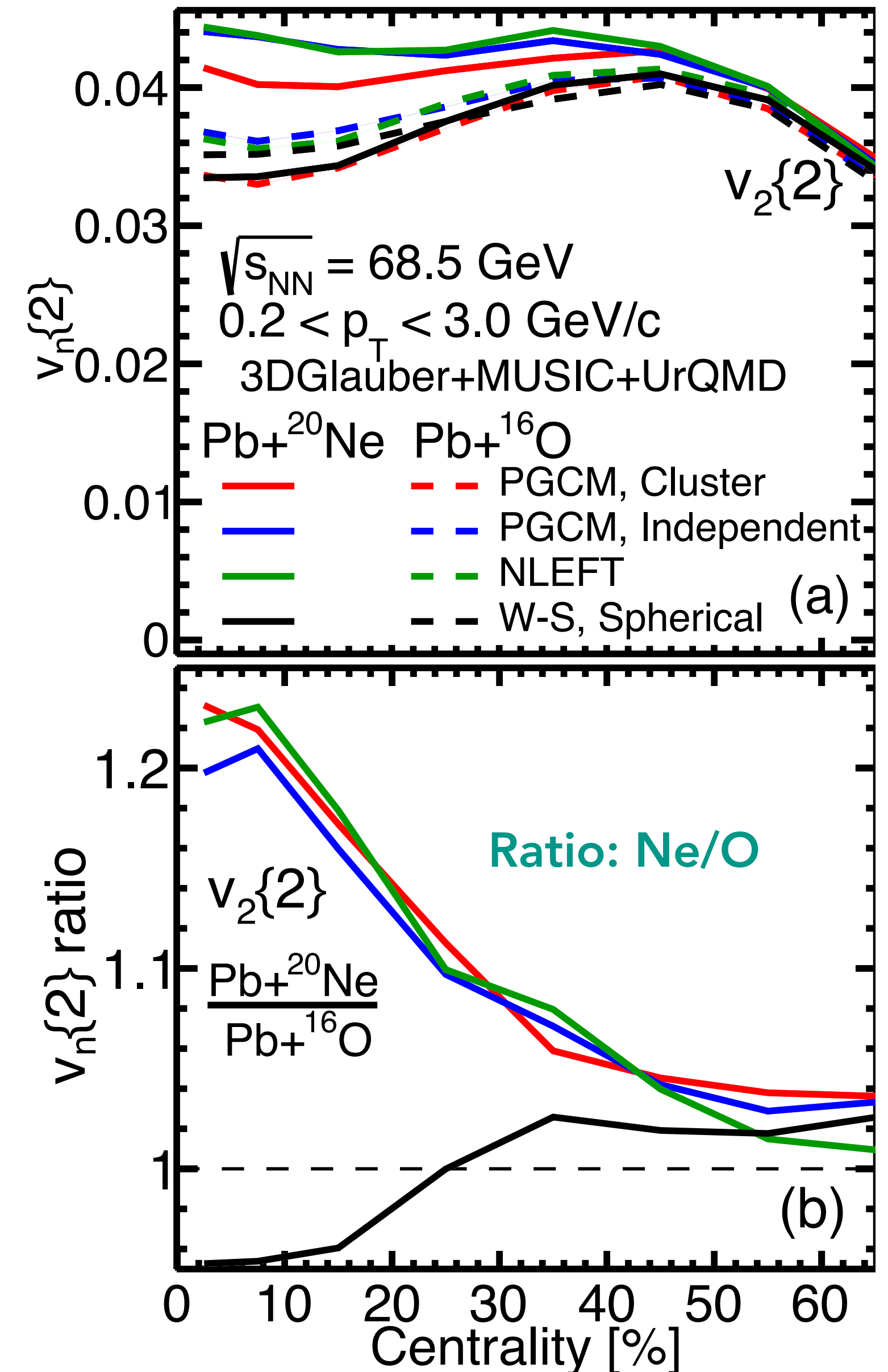
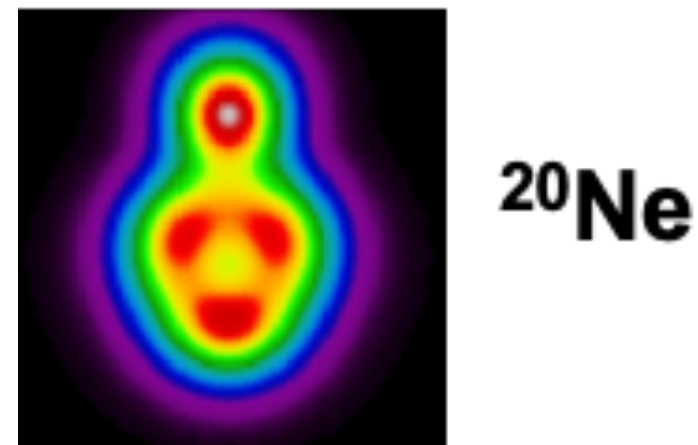
LHCb Collaboration, Eur.Phys.J.C 83 (2023) 7, 658



Pb+Ne and Pb+O

G. Giacalone et al, arXiv:2405.20210

- Flow sensitive to shapes of Ne and O
- Clear predictions from fluid dynamics with input from ab initio calculations of the structure of ^{16}O and ^{20}Ne
- Further test hydrodynamic picture at LHC
see talk by G. Giacalone



SUMMARY

- Strong final state effects provide most consistent description of small systems
- Differences between v_n from STAR and PHENIX from different rapidity ranges
- Elliptic flow in photo-nuclear events well described by same framework used in p+A
- Applicability of hydrodynamics:
Issues of accuracy, causality, stability
- Frameworks with non-equilibrium transport component possible way to go
- Studies of hard probes in small systems plagued by biases from centrality selection

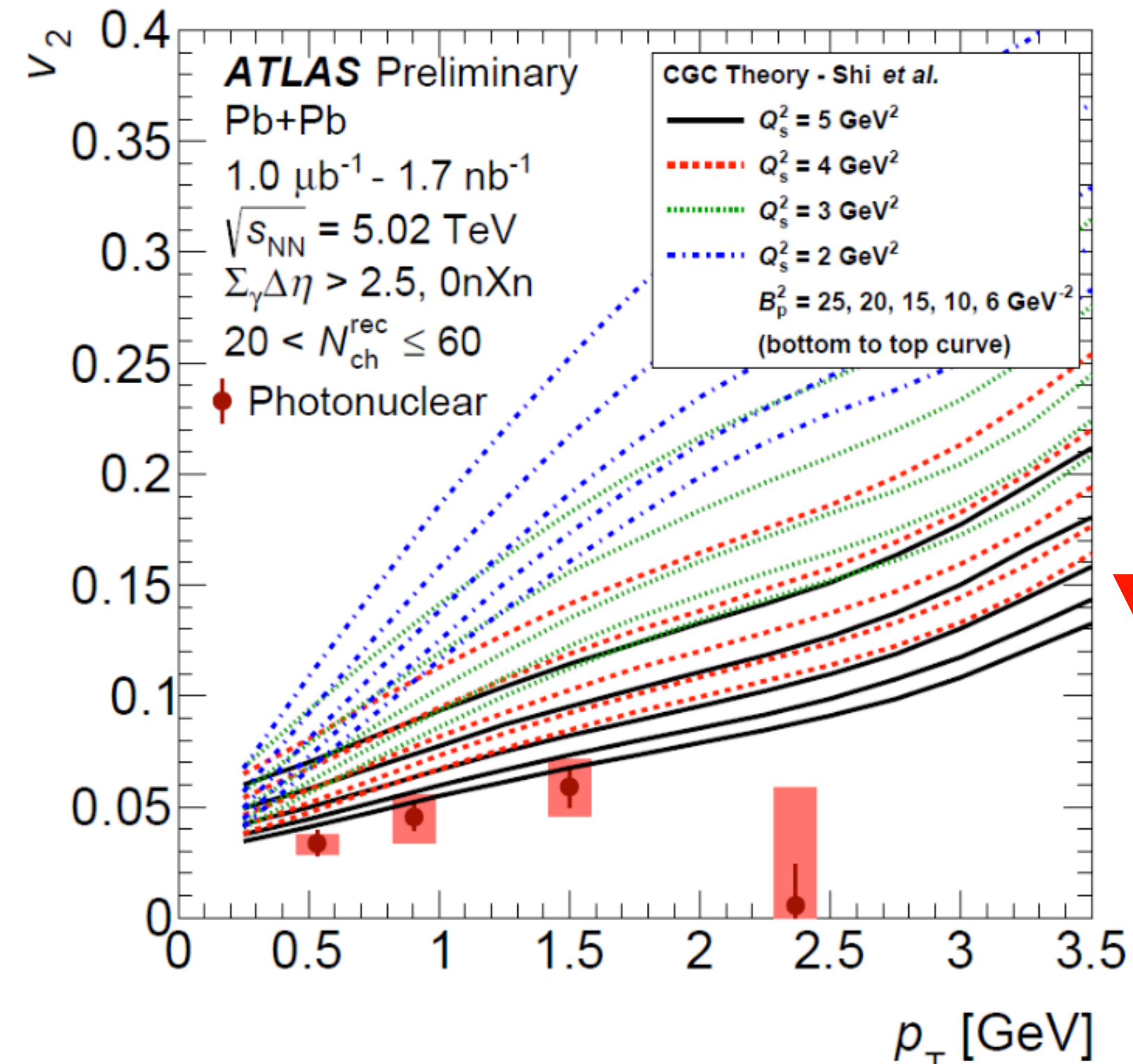
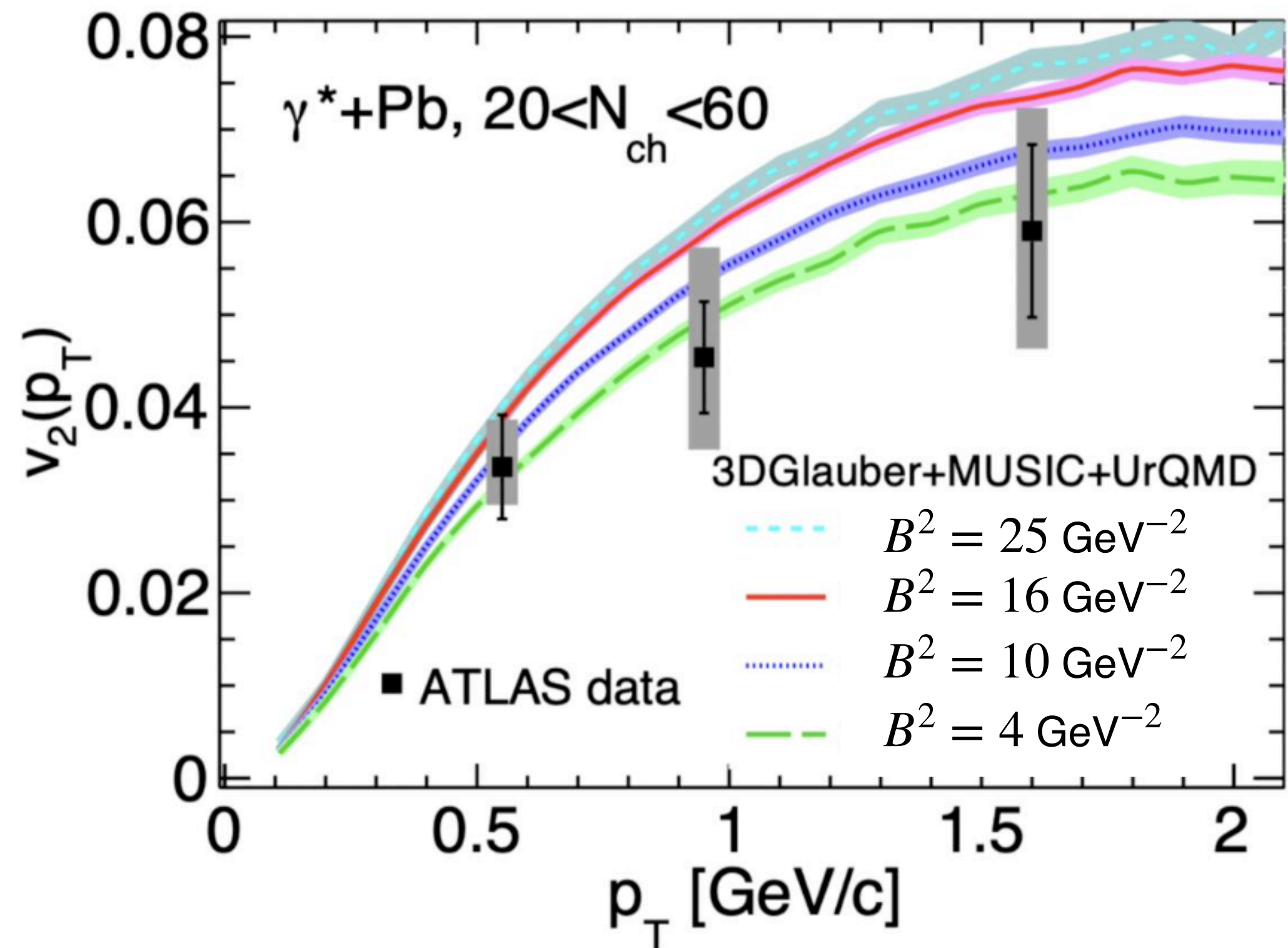


BACKUP

DISTINGUISH MODELS IN $e+A$ COLLISIONS AT EIC

W. Zhao, C. Shen and B. Schenke, *Phys.Rev.Lett.* 129 (2022) 25, 252302

Y. Shi, L. Wang, S. Y. Wei, B. W. Xiao and L. Zheng, *Phys. Rev. D* 103, 054017 (2021)



increasing
transverse size
 $\propto B^2$

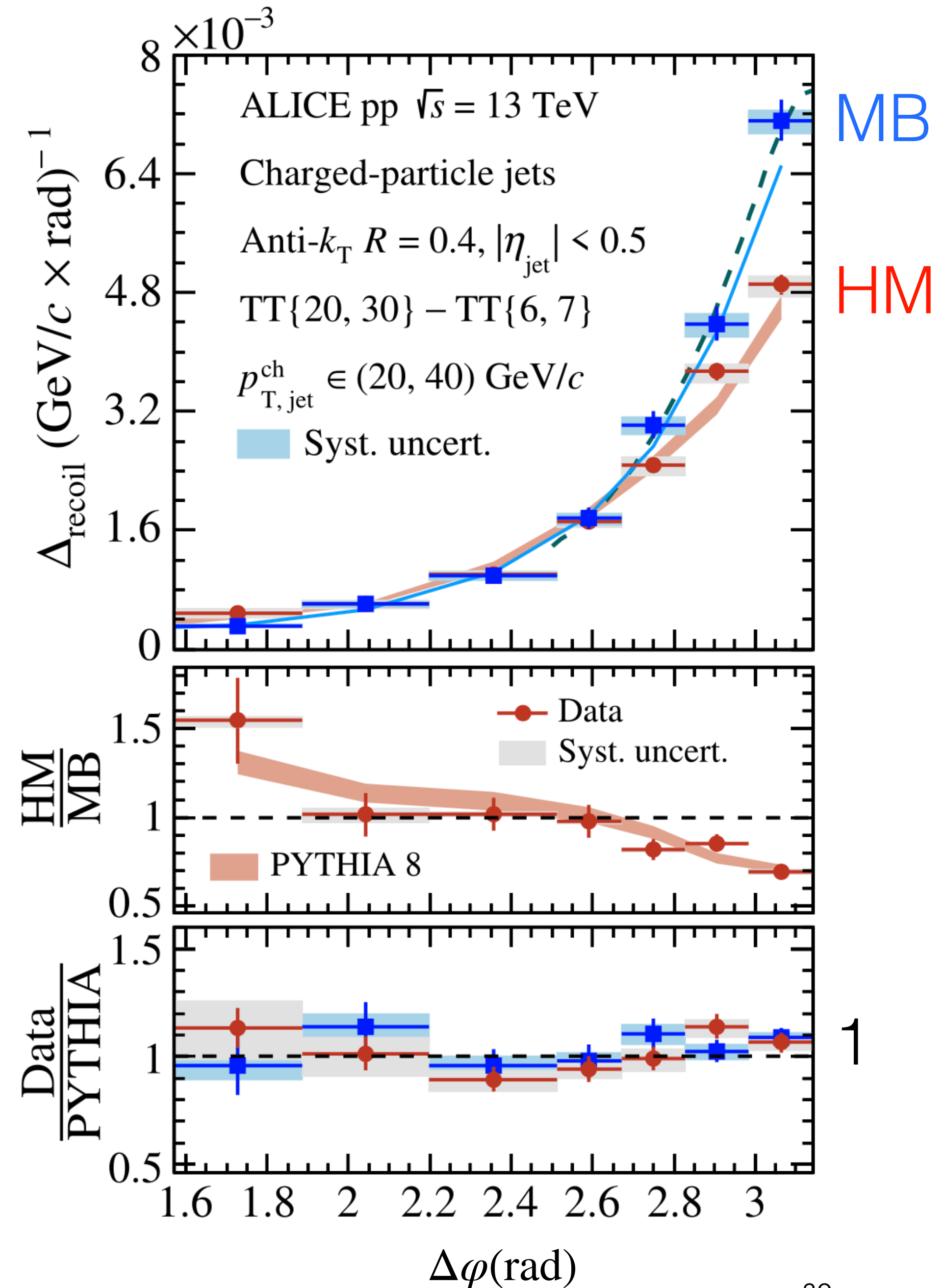
- Hydro: Larger B^2 means larger transverse area for geometry to fluctuate $v_2 \propto B^2$
- CGC: Larger B^2 leads to a larger number of independent domains $v_2 \propto 1/B^2$
- Study Q^2 dependence at the Electron Ion Collider (EIC) to test this

JET QUENCHING

ALICE Collaboration, arXiv:2309.03788

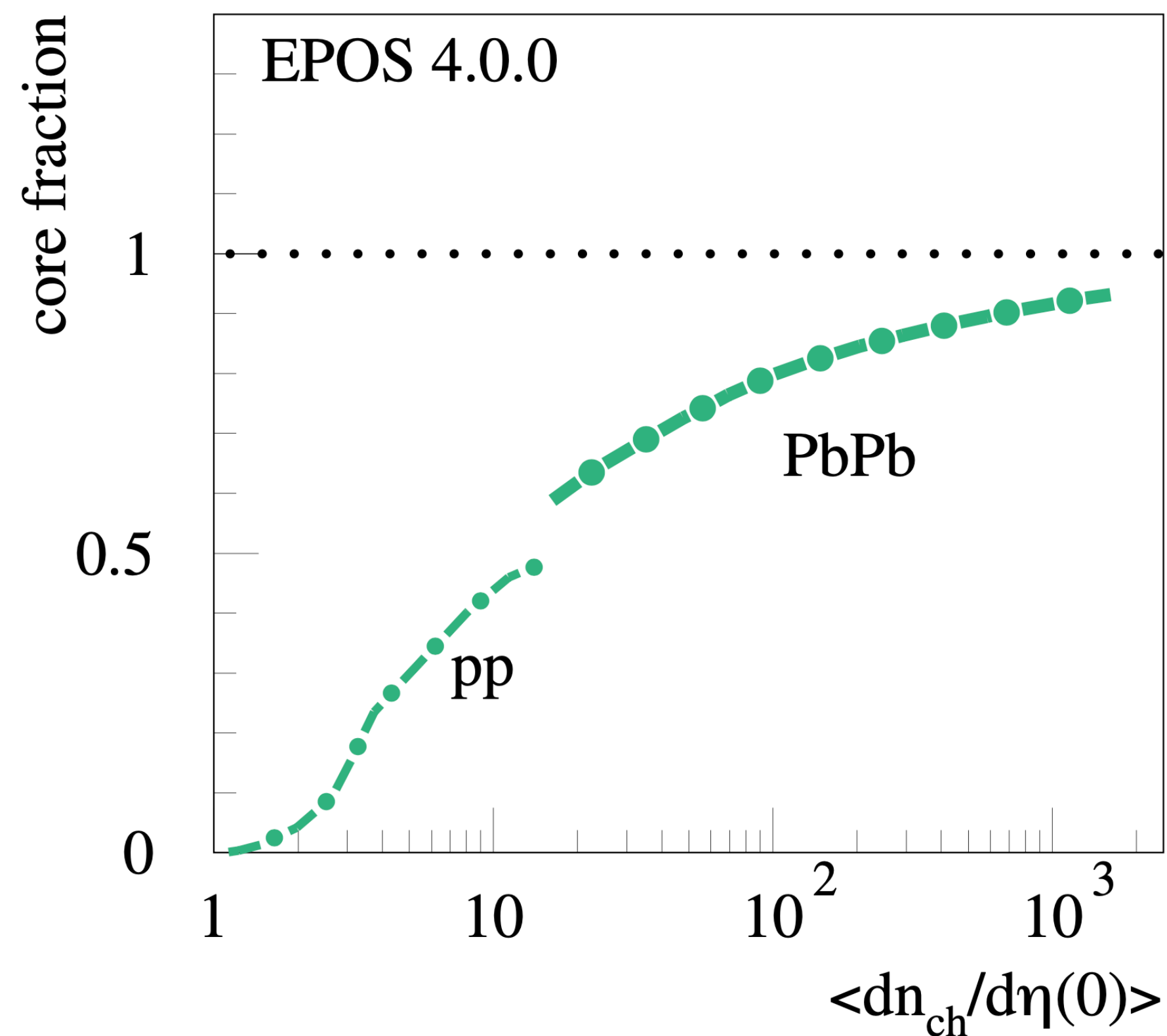
- Recoil jet distribution widens in High Multiplicity (HM) events
- PYTHIA8 (no jet quenching) reproduces effect
- Effect is bias from HM event selection
- Preference for events with recoil jet at forward rapidity where multiplicity is determined, depletes recoil jets at mid rapidity, bias towards multi-jet states

-- pQCD@LO + Sudakov (MB)
 Data: MB (blue squares), HM (red circles)
 PYTHIA 8: MB (blue line), HM (red line)

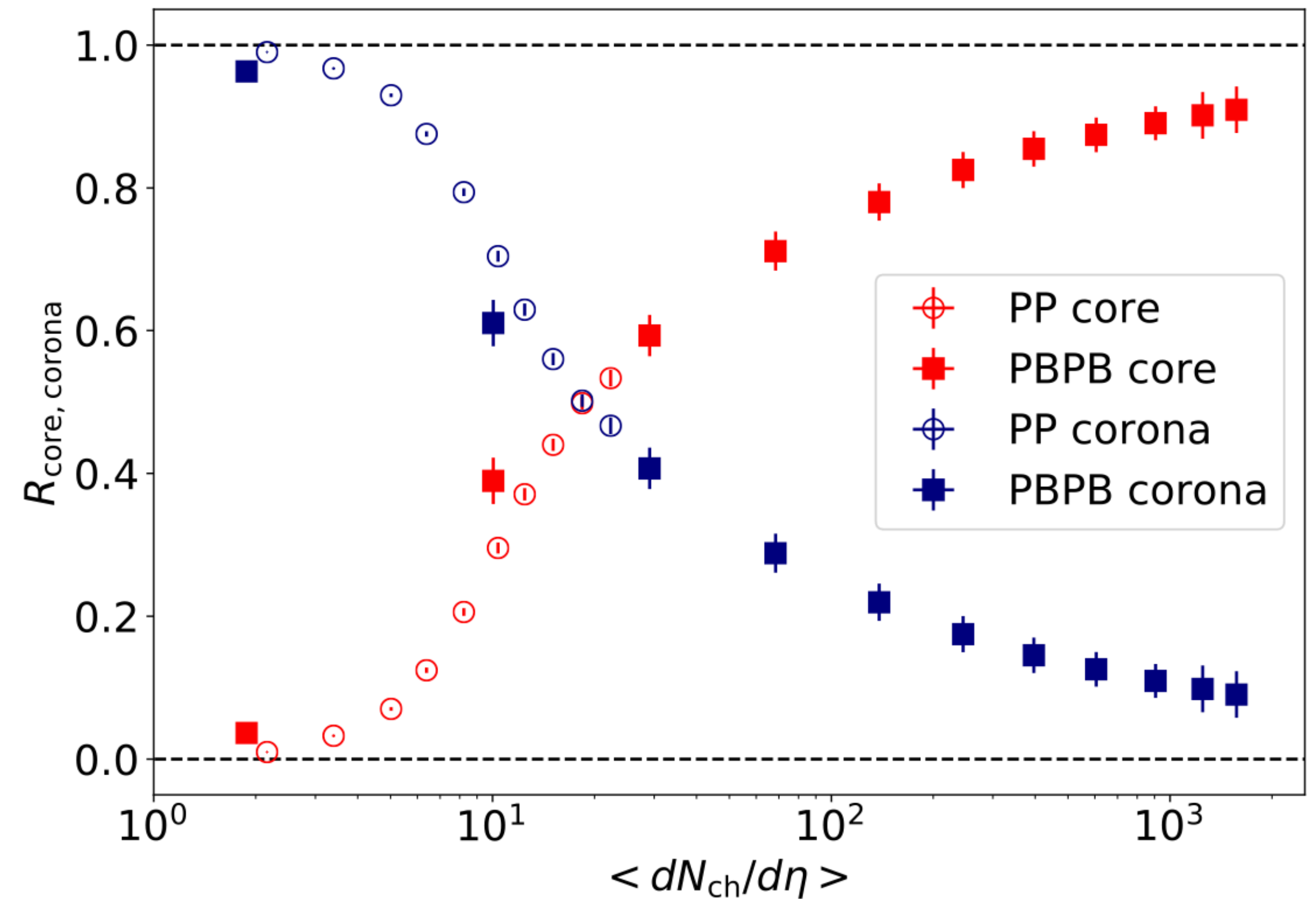


CORE+CORONA PICTURE

Hydro-like core begins to dominate for $dN_{\text{ch}}/d\eta \approx 10 - 20$

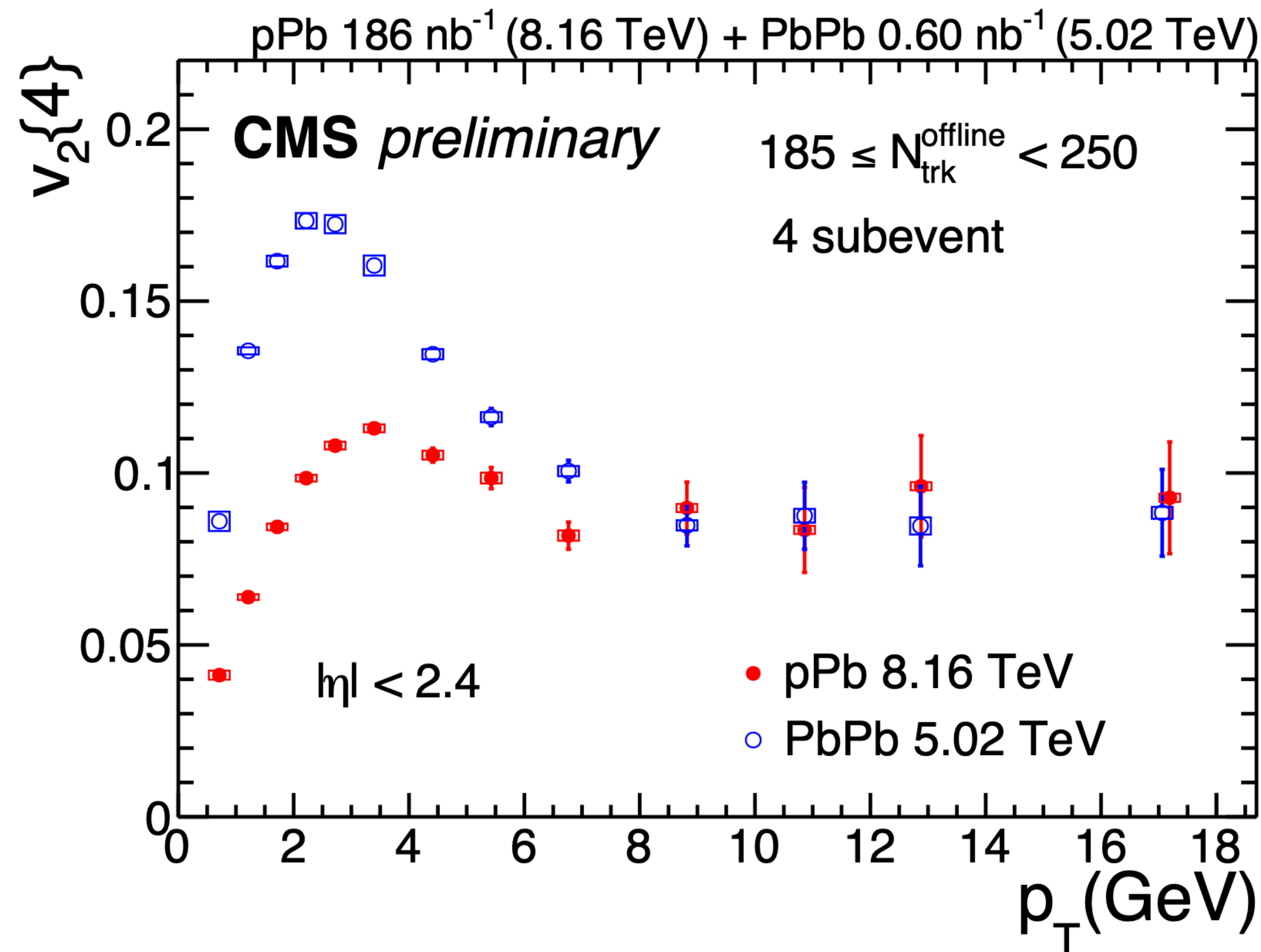


K. Werner, Phys.Rev.C 108 (2023) 6, 064903



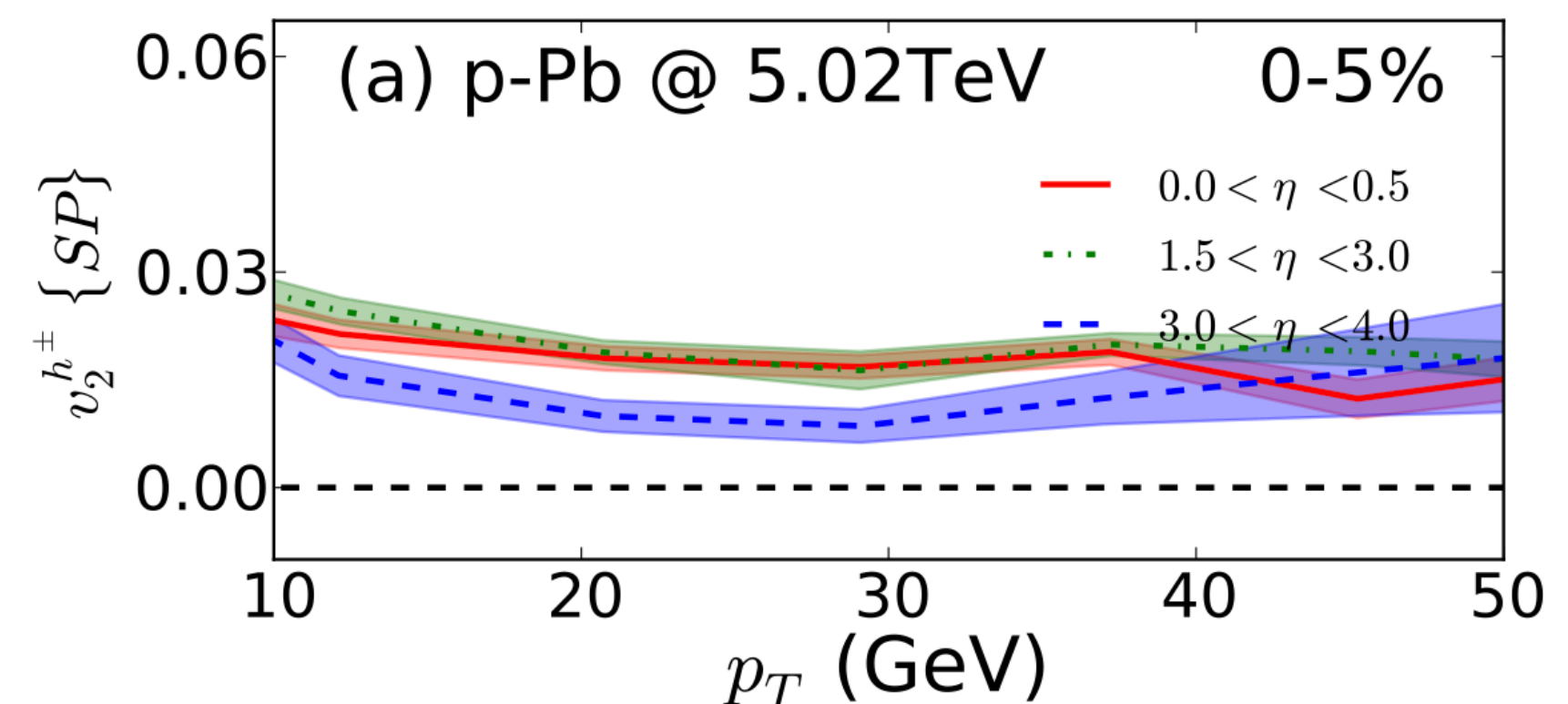
Y. Kanakubo et al., Phys. Rev. C 105 (2022) 2, 024905

HIGH p_T AZIMUTHAL ANISOTROPY



CMS Collaboration, PAS HIN-23-002,
 Rohit Kumar Singh's poster; also see
 ATLAS Collaboration, Eur.Phys.J.C 80 (2020) 1, 73

Path-length dependent energy loss
 in p+Pb? [C. Park, S. Jeon, C. Gale](#)
[Nucl.Part.Phys.Proc. 289-290 \(2017\)](#)



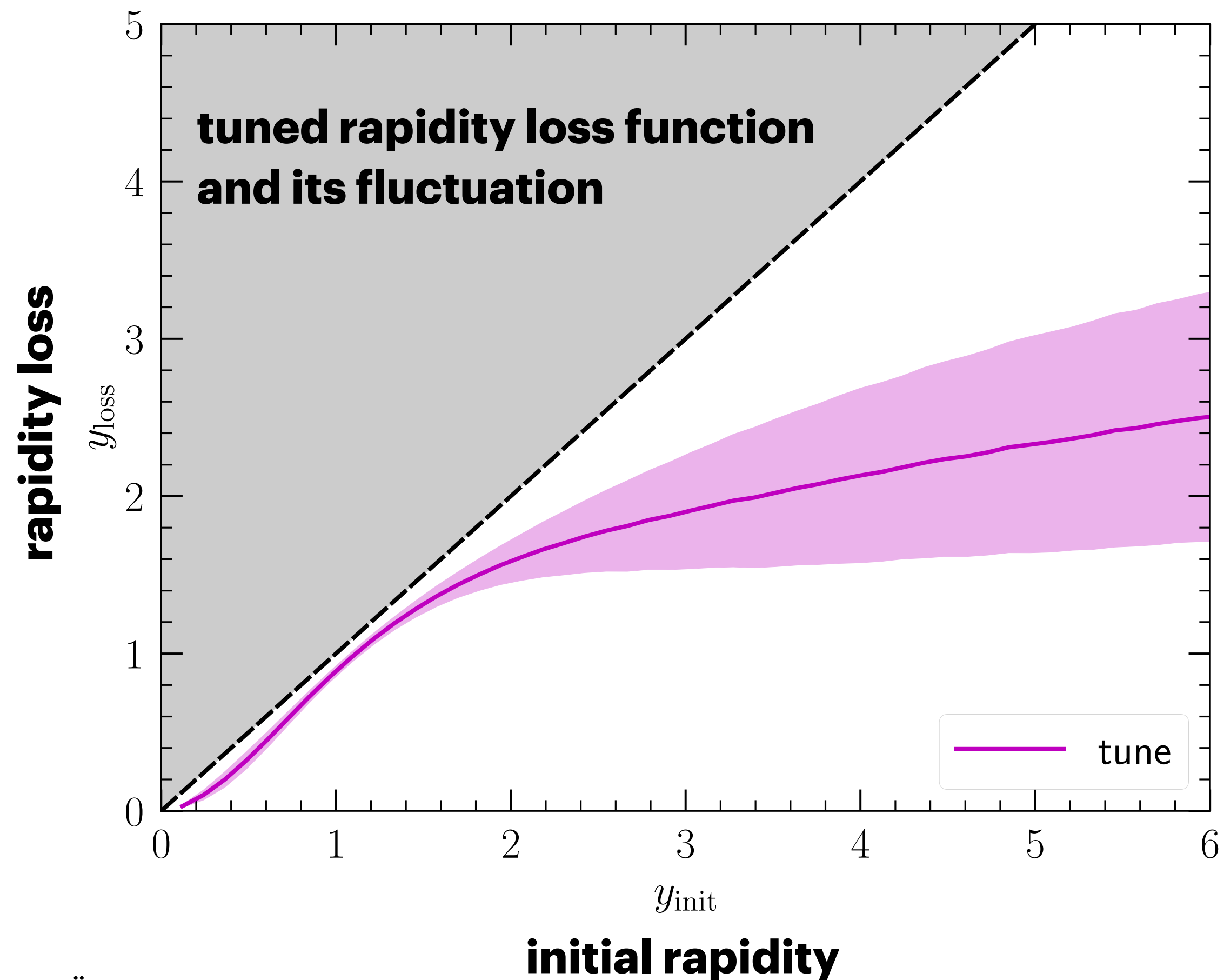
Alternative: Anisotropy from
 transverse momentum of incoming
 partons; Contribution from $gg \rightarrow gg$
 with one gluon linearly polarized
 gives largest contribution to v_2

[I. Soudi, A. Majumder, arXiv:2308.14702, 2404.05287](#)

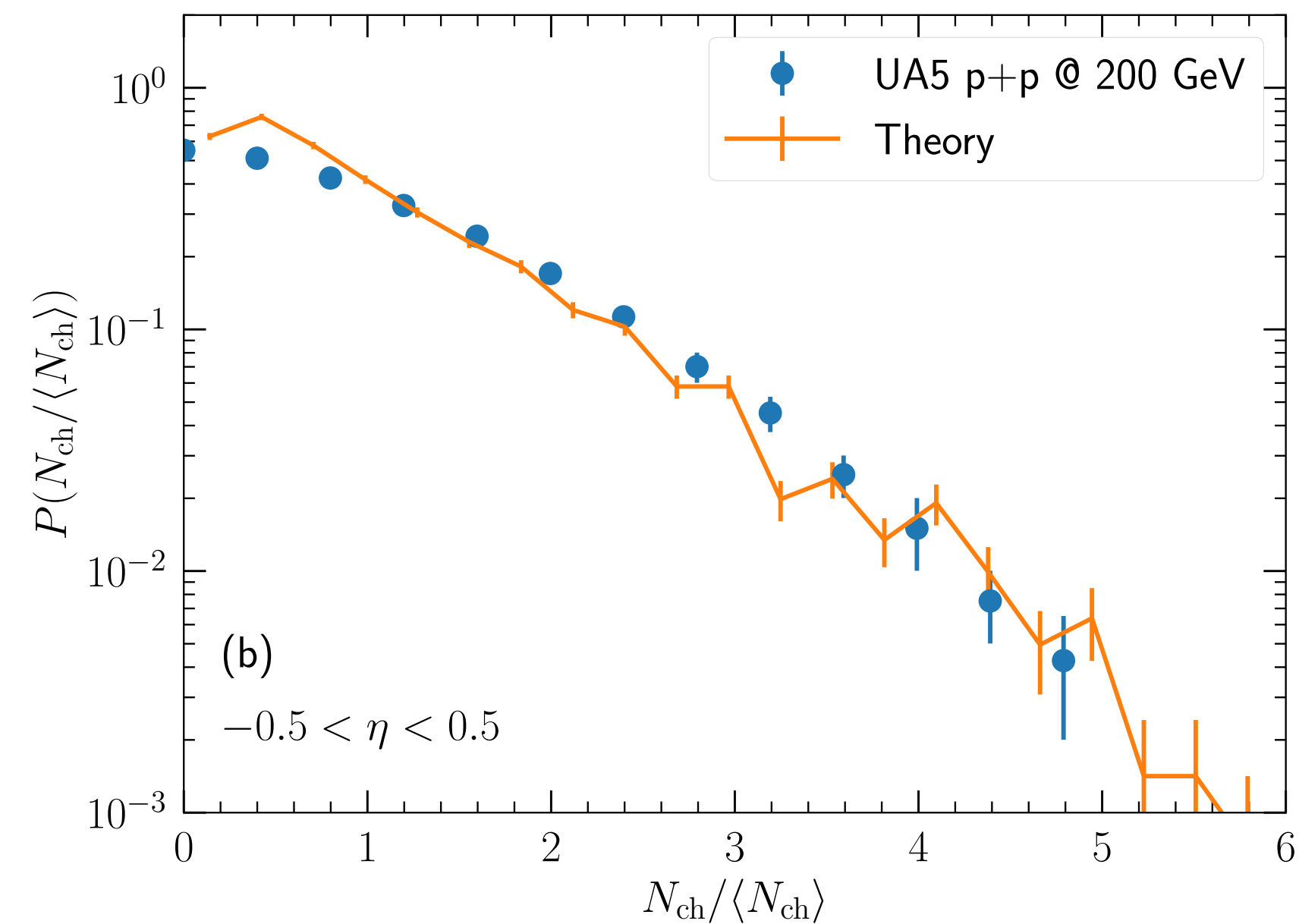
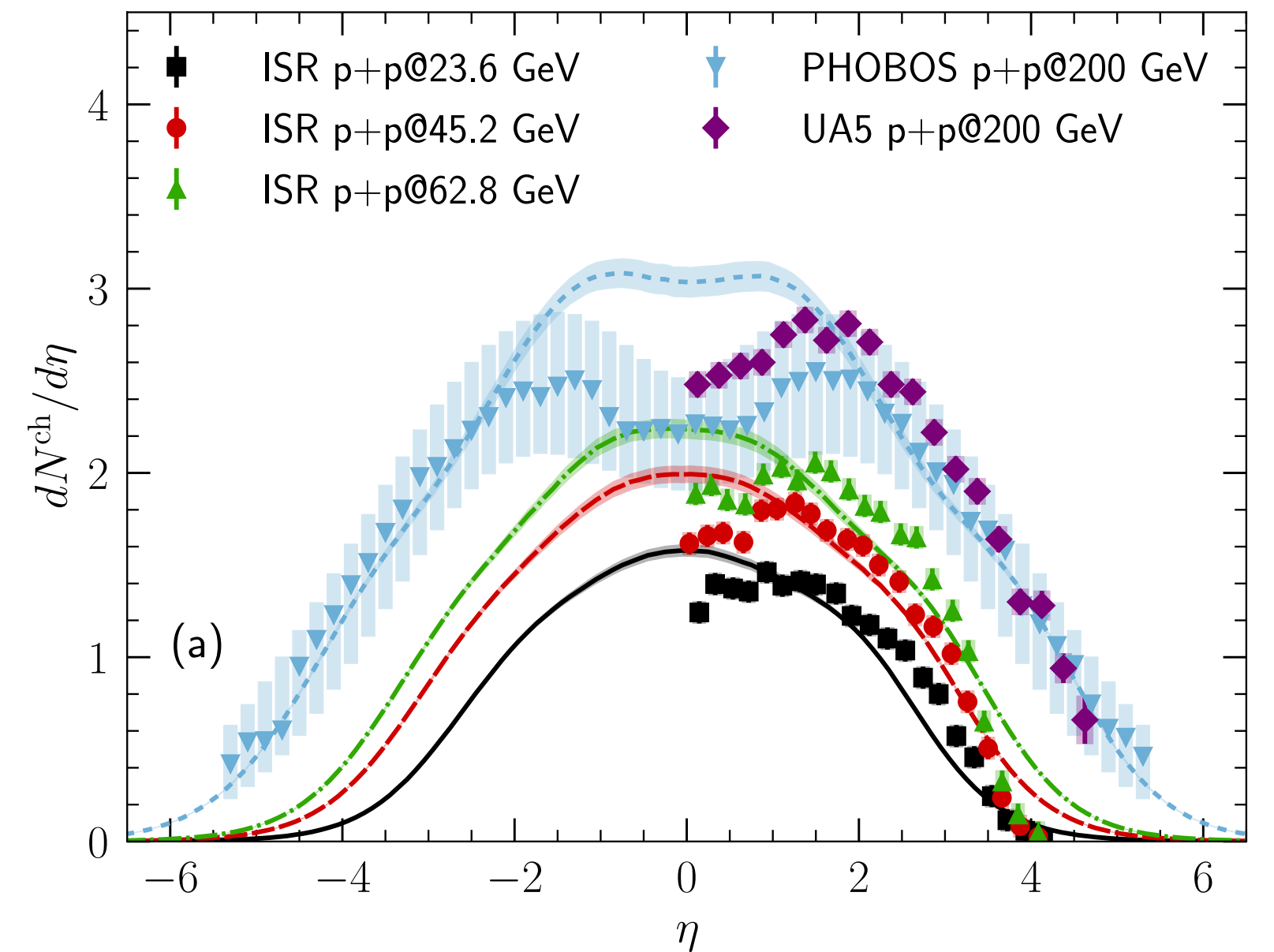
CALIBRATION IN p+p COLLISIONS

C. Shen and B. Schenke, Phys. Rev. C 105, 064905 (2022)

How much rapidity does a valence quark lose in a collision?



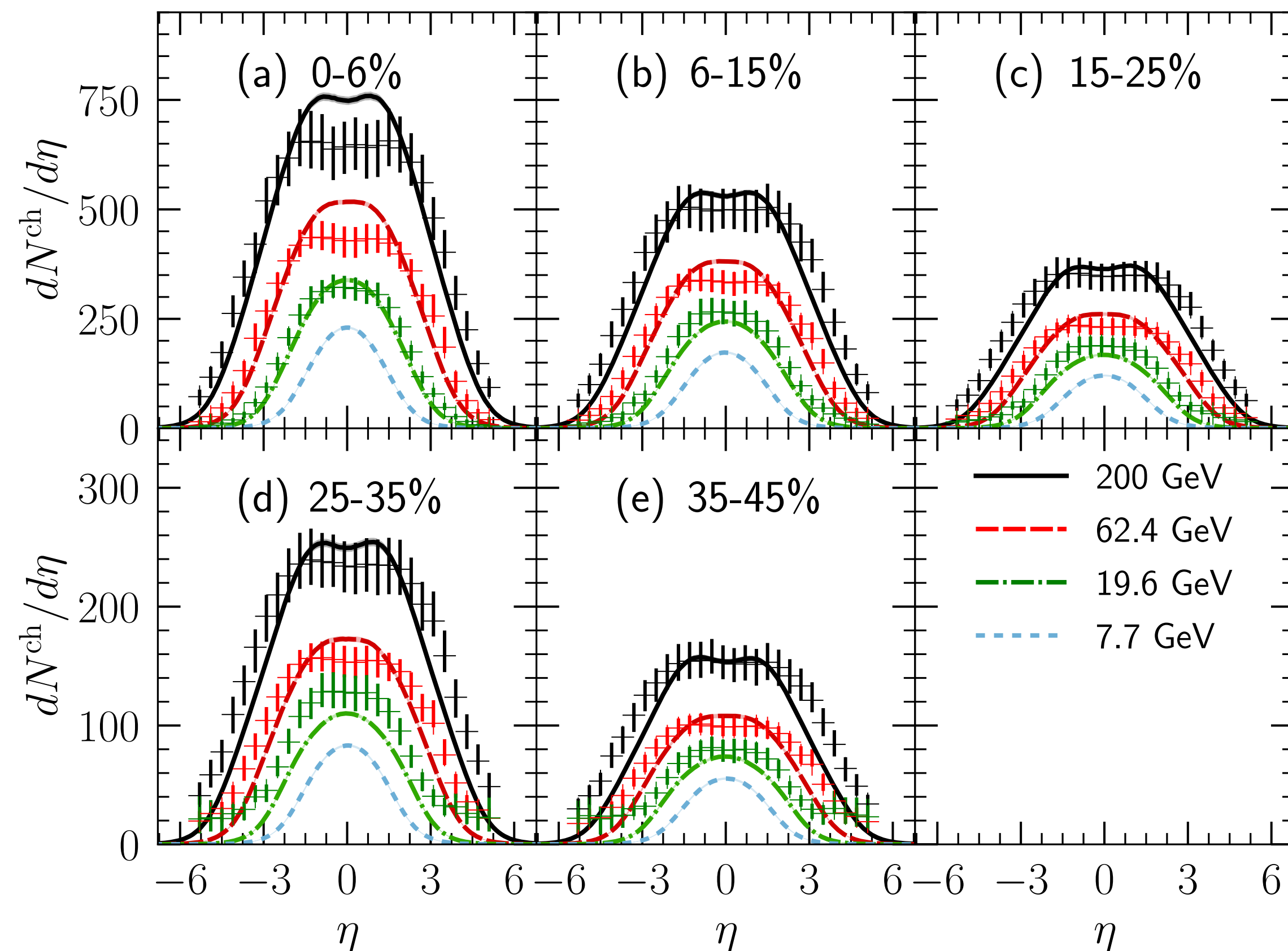
BJÖRN SCHENKE



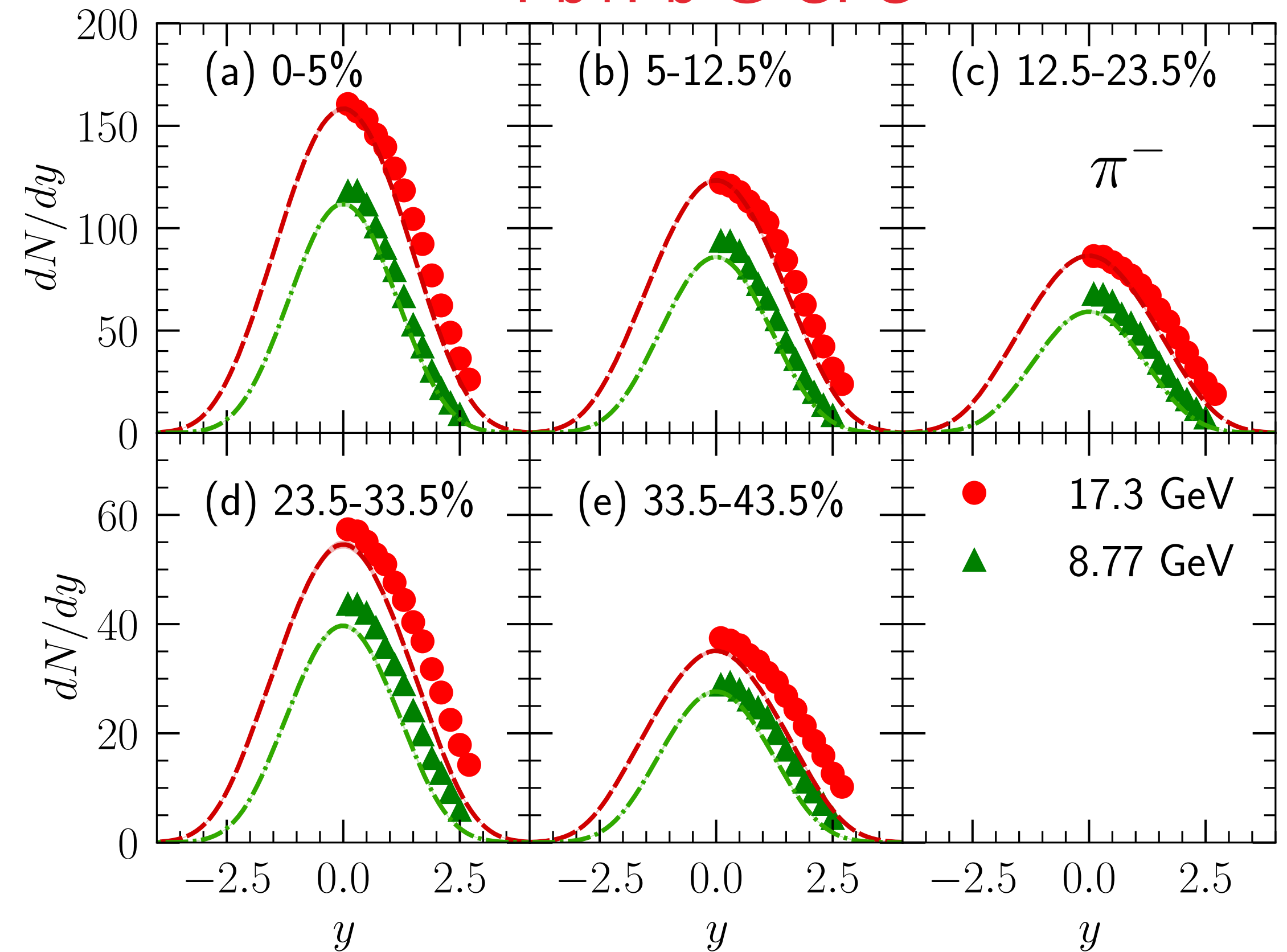
COMPARISON TO A+A DATA

C. Shen and B. Schenke, Phys. Rev. C 105, 064905 (2022)

Au+Au @ RHIC BES



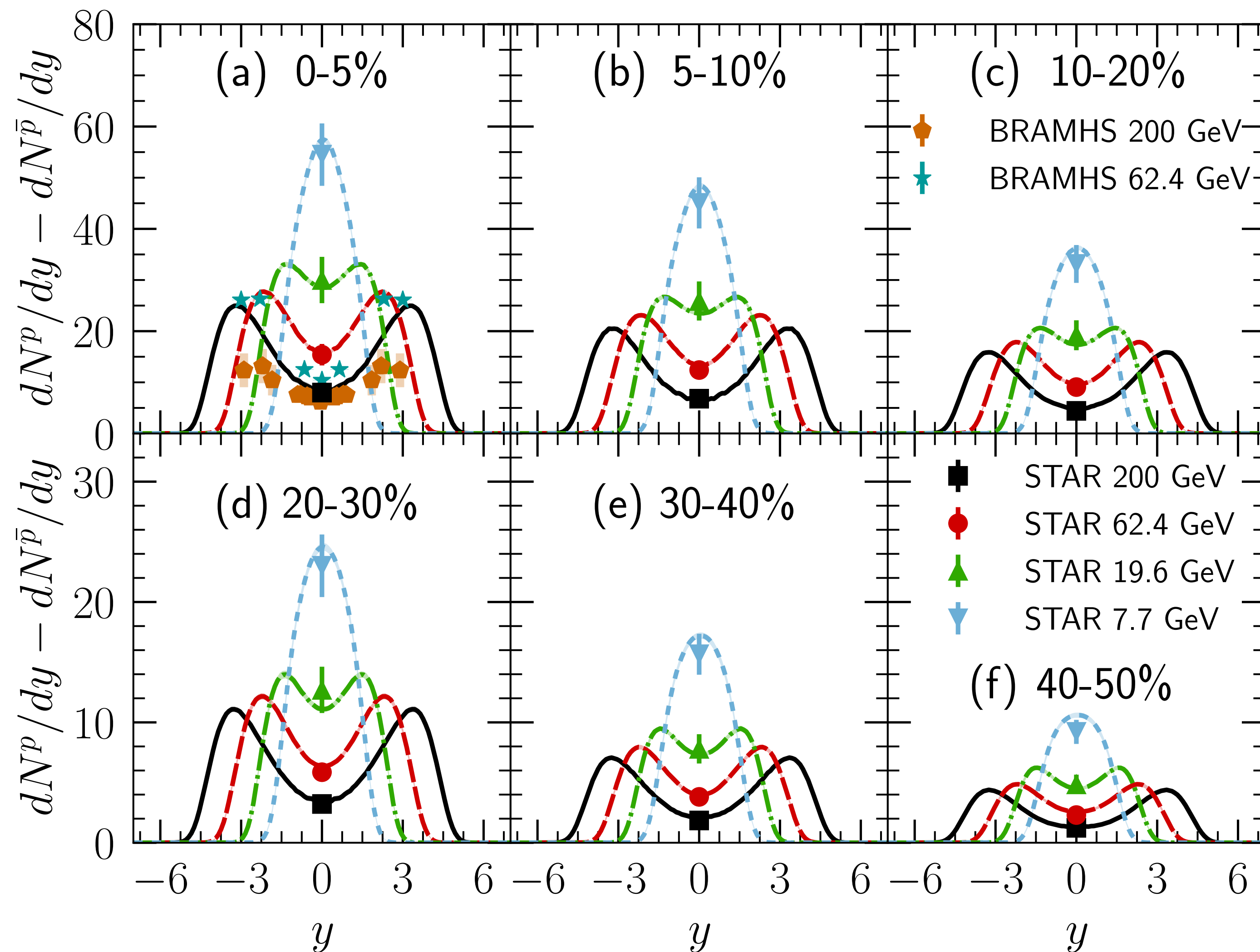
Pb+Pb @ SPS



- Reasonable description of A+A experimental data

NET-PROTON PRODUCTION

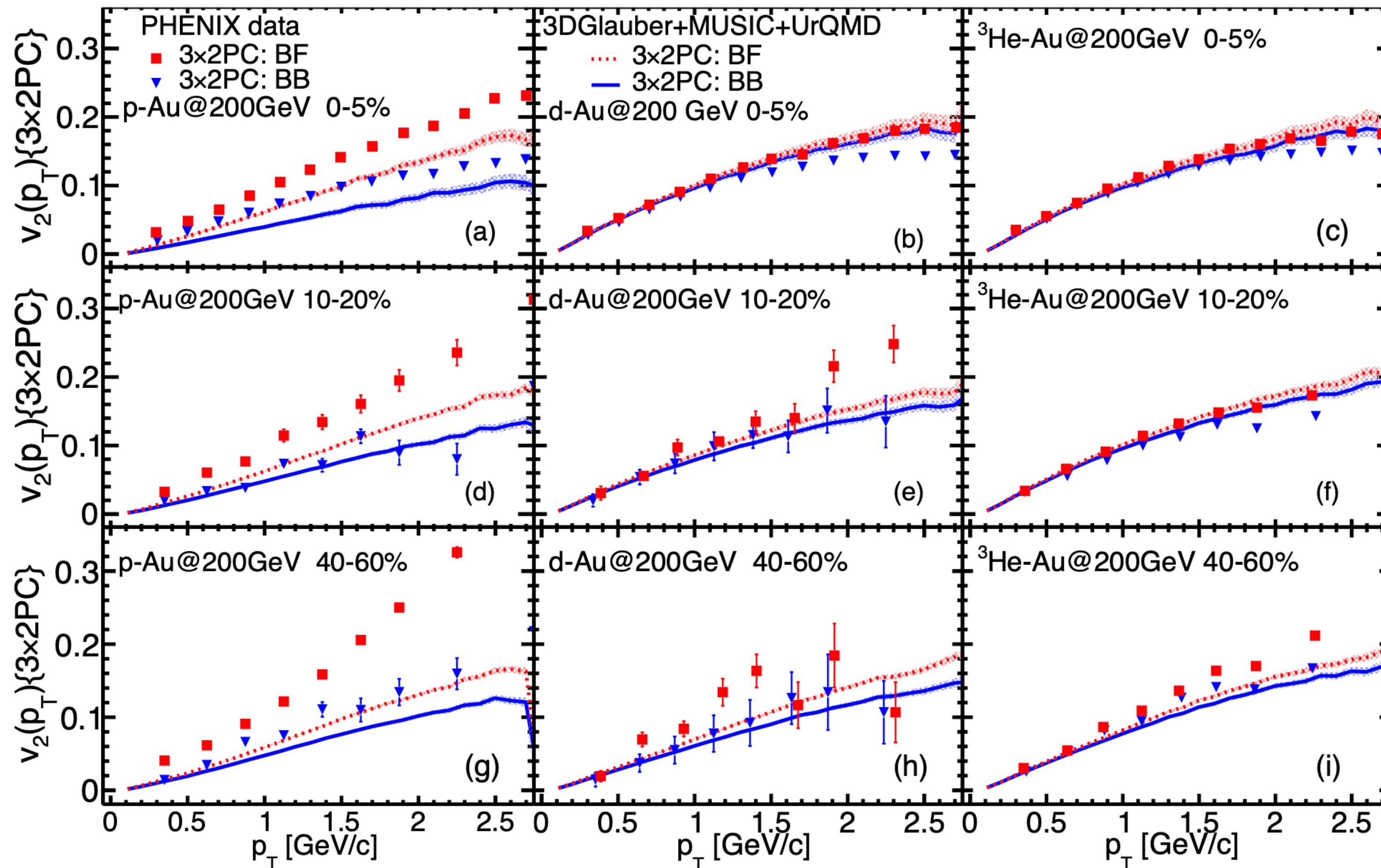
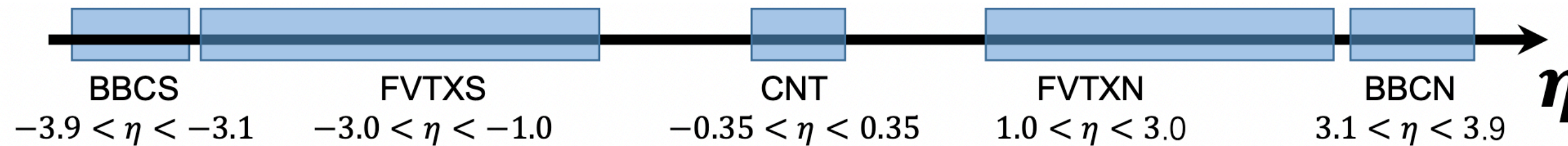
C. Shen and B. Schenke, Phys. Rev. C 105, 064905 (2022)



- Predictions for the net proton rapidity and centrality dependence at RHIC BES energies
- Our results at mid-rapidity are consistent with the STAR measurements
- Measurements of the rapidity dependence can further constrain the distributions of initial baryon charges

PHENIX 3X2PC STUDY

W. Zhao, S. Ryu, C. Shen and B. Schenke, *Phys.Rev.C* 107 (2023) 1, 014904



3 × 2PC

$$C_n^{AB} = \langle Q_{nA} Q_{nB}^* \rangle,$$

$$c_n^{AC}(p_T) = \langle Q_{nA} q_{nC}^*(p_T) \rangle,$$

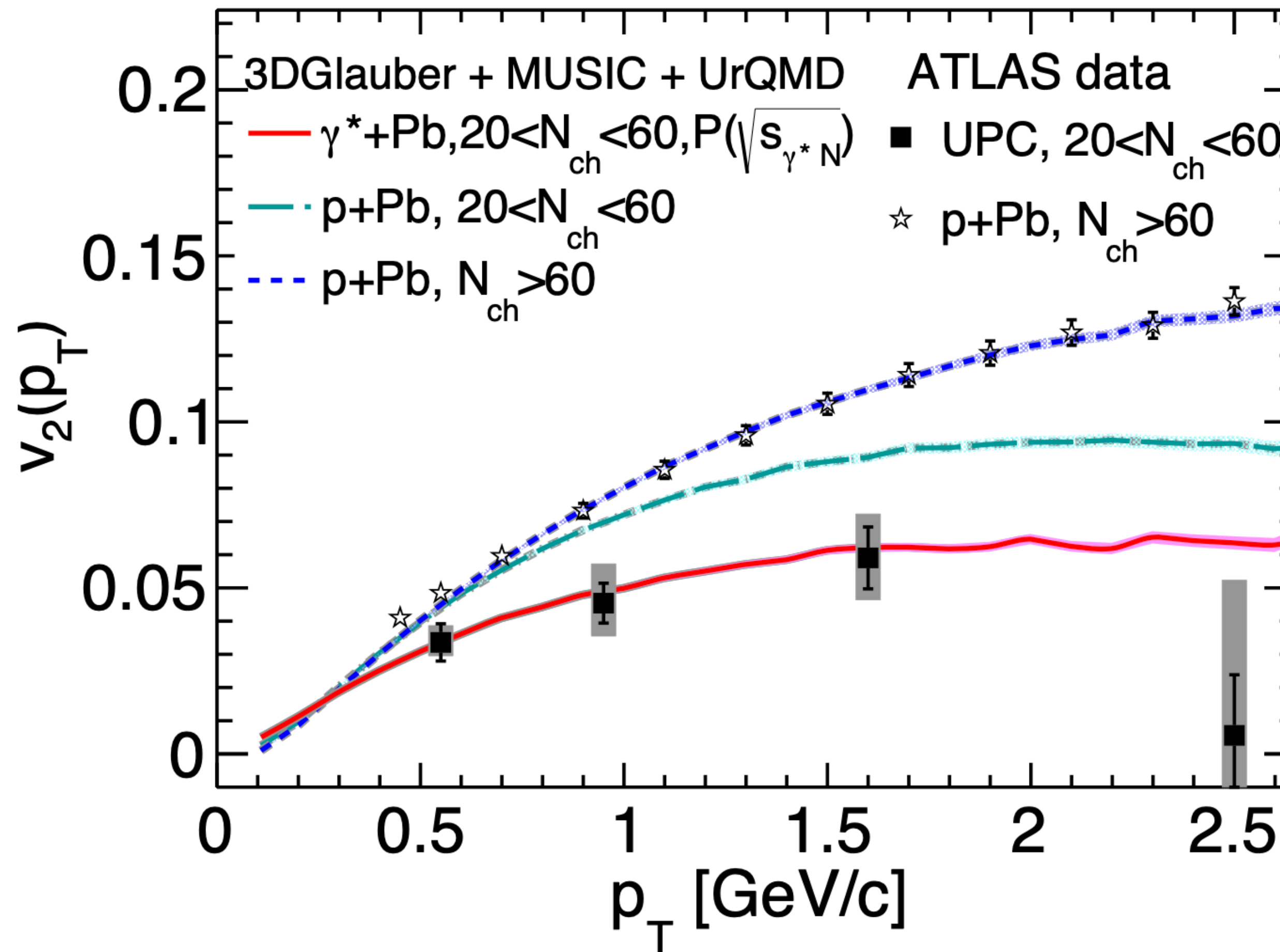
$$c_n^{BC}(p_T) = \langle Q_{nB} q_{nC}^*(p_T) \rangle.$$

$$v_n^C(p_T) = \sqrt{\frac{c_n^{AC}(p_T) c_n^{BC}(p_T)}{C_n^{AB}}}.$$

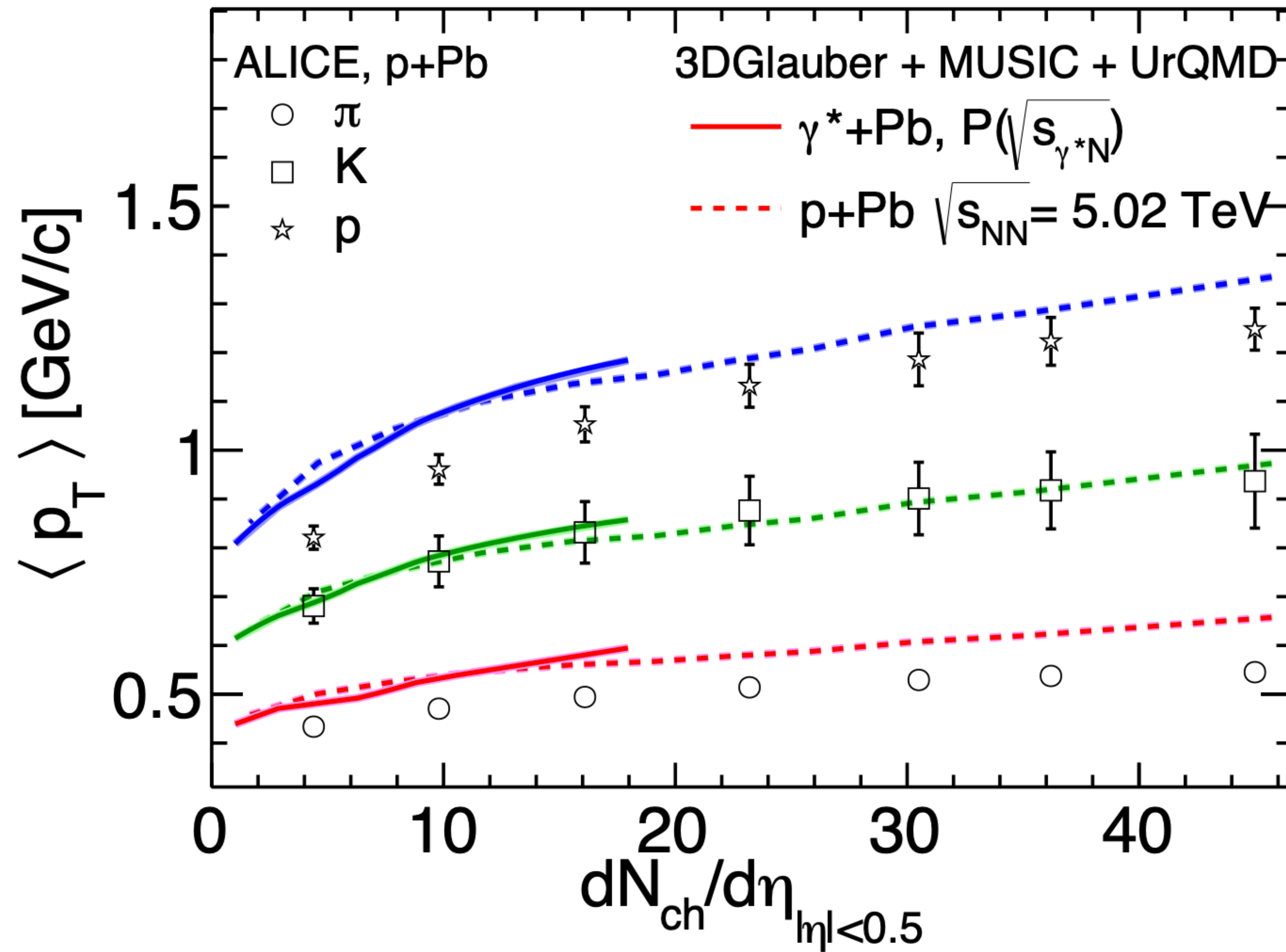
BB: BBCS-FVTXS-CNT
BF: FVTXS-CNT-FVTXT

Longitudinal flow decorrelation reproduces some differences between BB and BF measurements

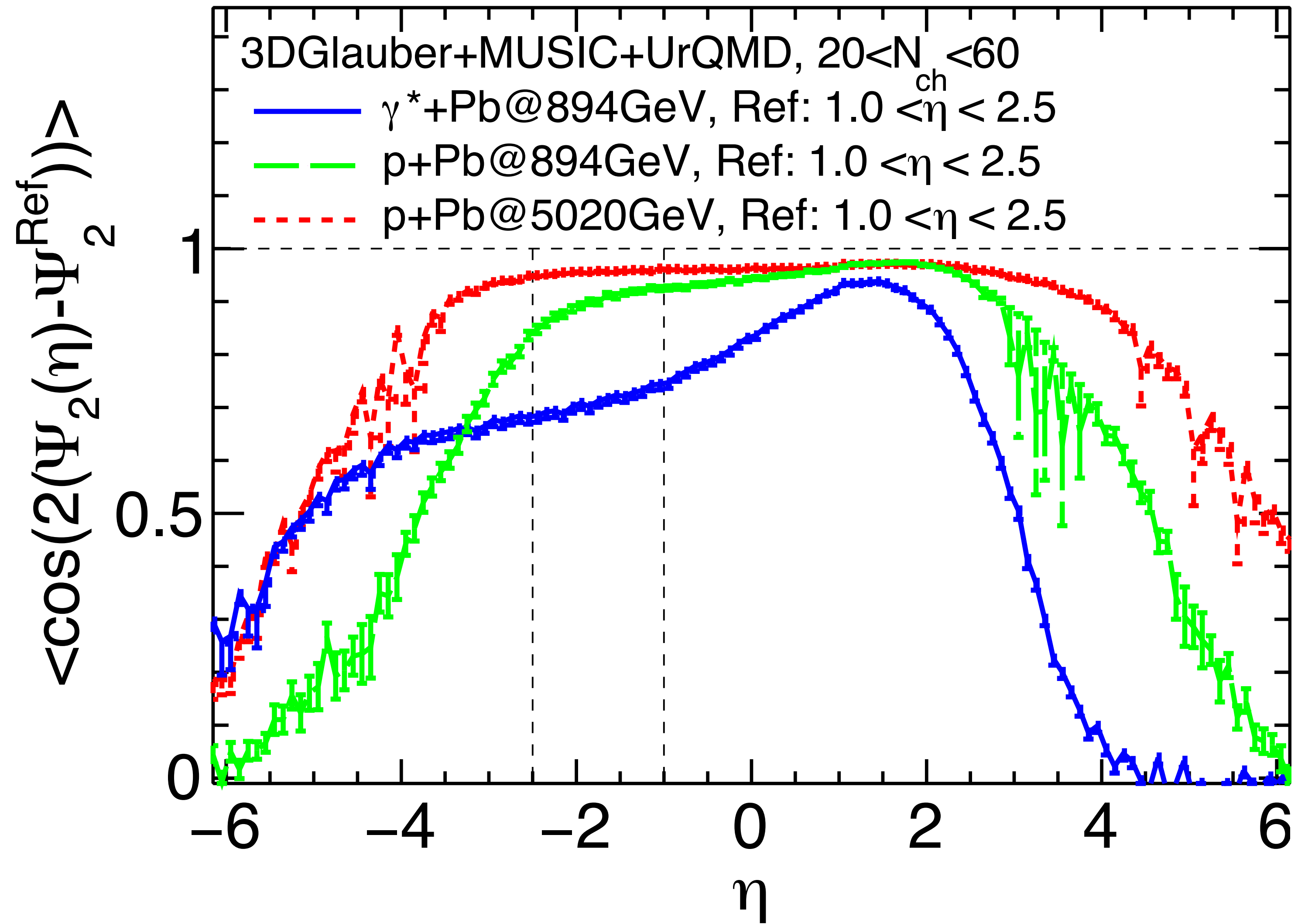
DIFFERENTIAL v_2 IN UPC Pb+Pb



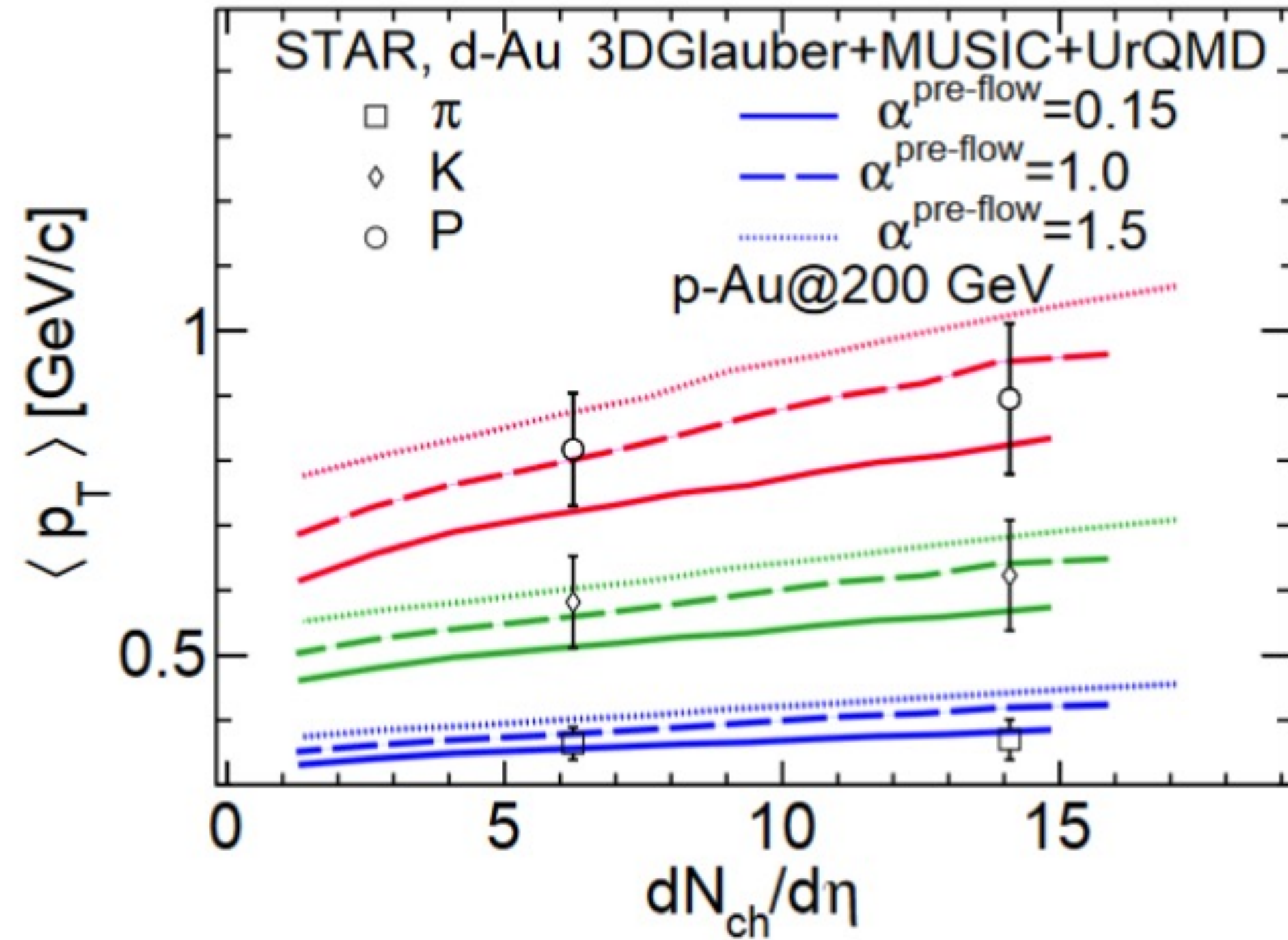
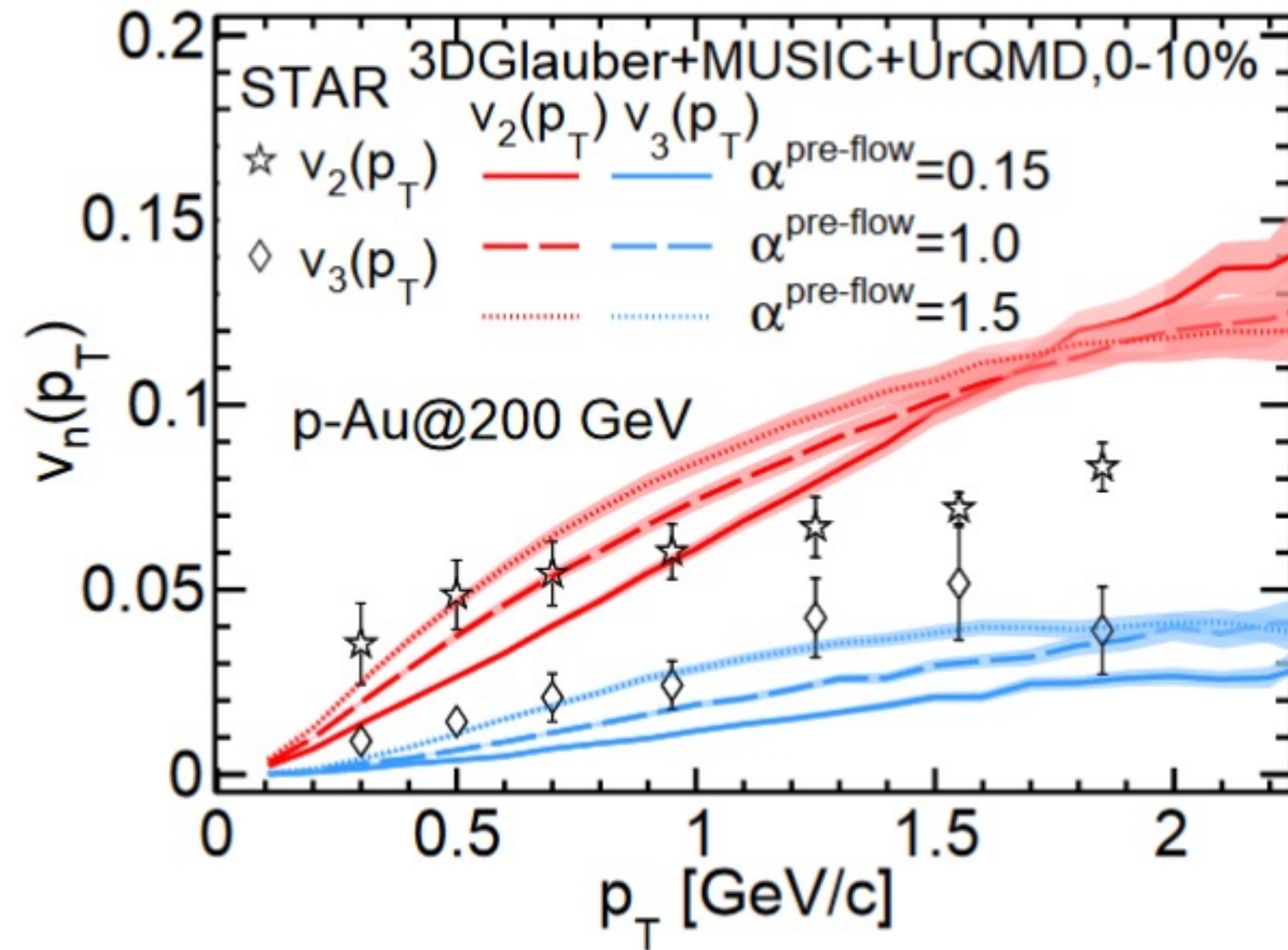
MEAN p_T IN UPC Pb+Pb



DECORRELATION IN UPC



Importance of Pre-Hydrodynamic Evolution



W. Zhao, S. Ryu, C. Shen and B. Schenke Phys. Rev. C 107, 014904 (2023).

A blast-wave like pre-hydrodynamic flow:
 $\eta_{\perp} = \alpha^{\text{pre-flow}} r,$

η_{\perp} is transverse flow rapidity, r is the distance from the point to the string center. The $\alpha^{\text{pre-flow}}$ controls the strength of the pre-hydrodynamic flow.

- Stronger pre-hydrodynamic flow leads to larger mean p_T and anisotropic coefficients.
- A systematic calibration including pre-hydrodynamic flow is important.

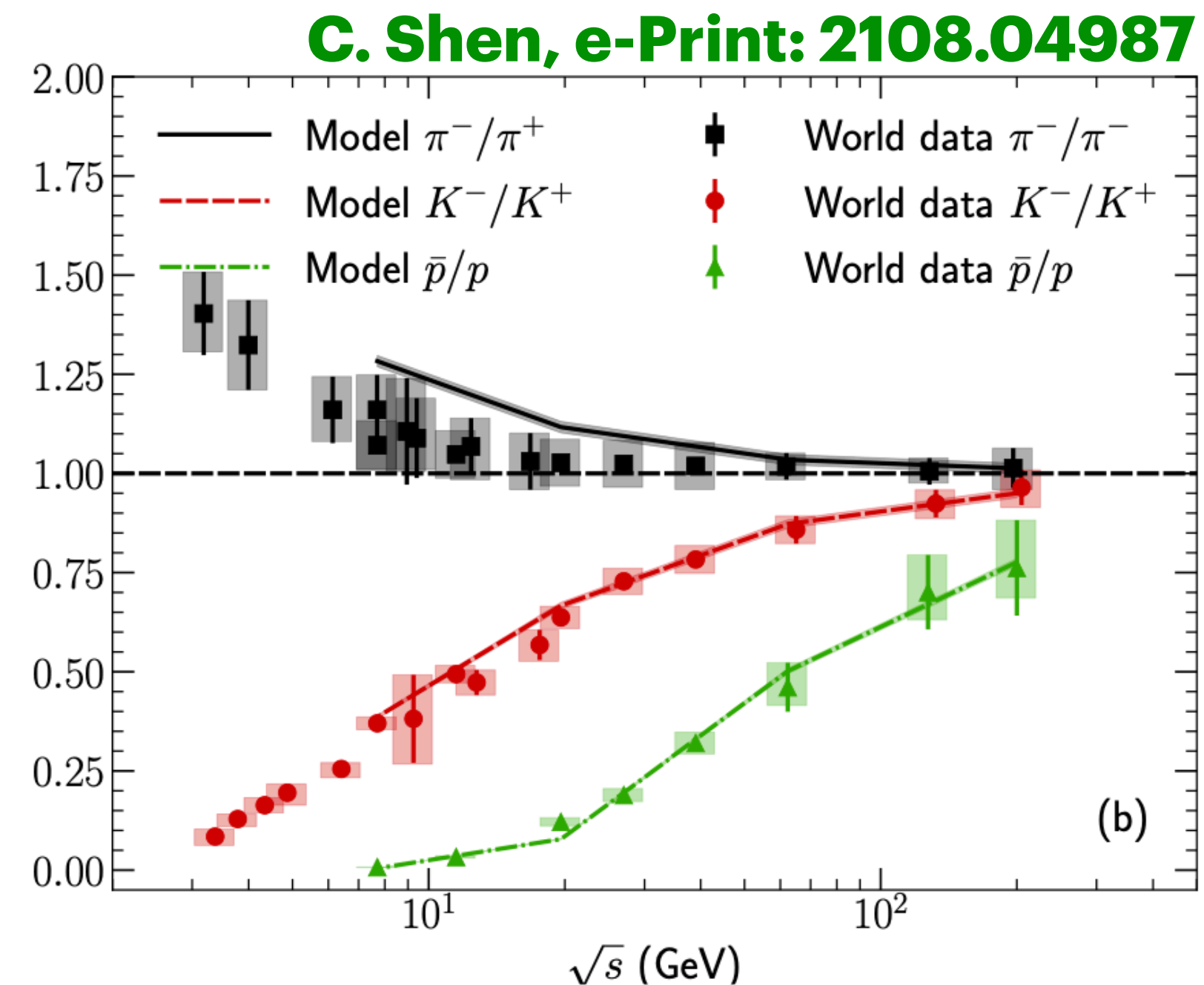
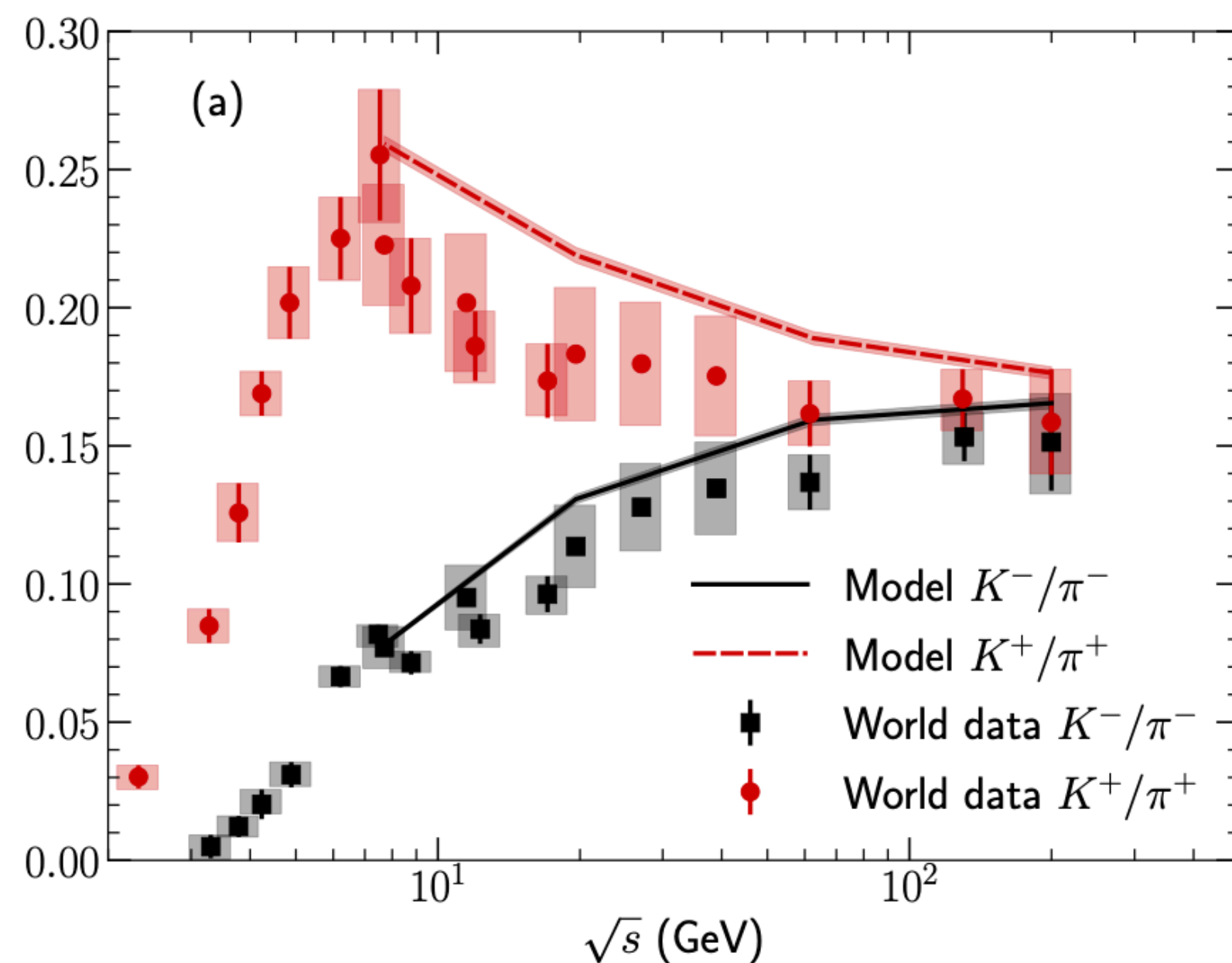
HYDRODYNAMICS AND EOS

- For the equation of state we use NEOS with finite μ_B, μ_S, μ_Q

A. Monnai, B. Schenke, C. Shen, Phys. Rev. C 100, 024907 (2019)

A. Monnai, B. Schenke, C. Shen, Int.J.Mod.Phys.A 36 (2021) 07, 2130007

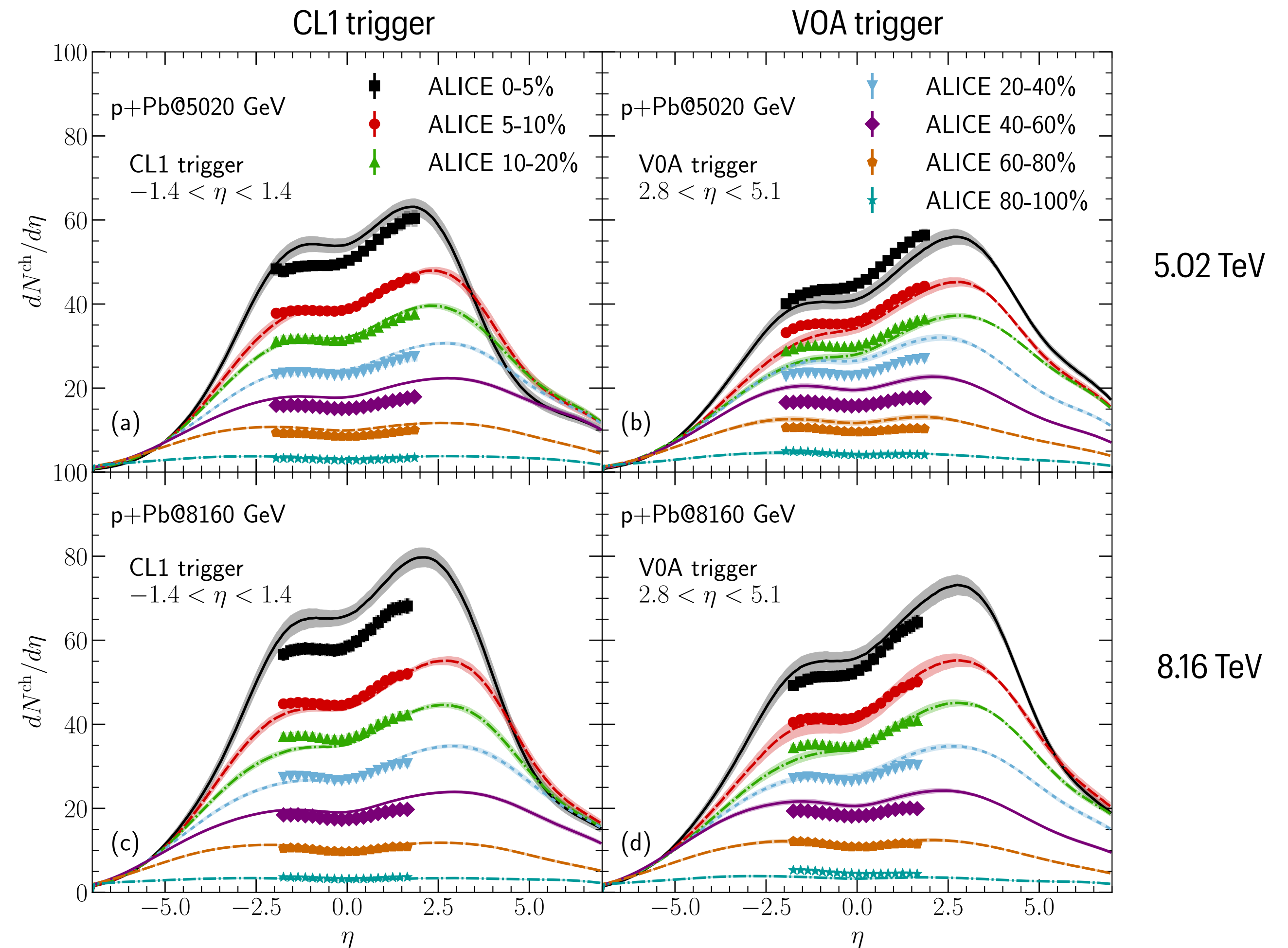
And choose $n_S = 0$ and $n_Q = 0.4n_B$ for Au+Au collisions:



CENTRALITY DEFINITION

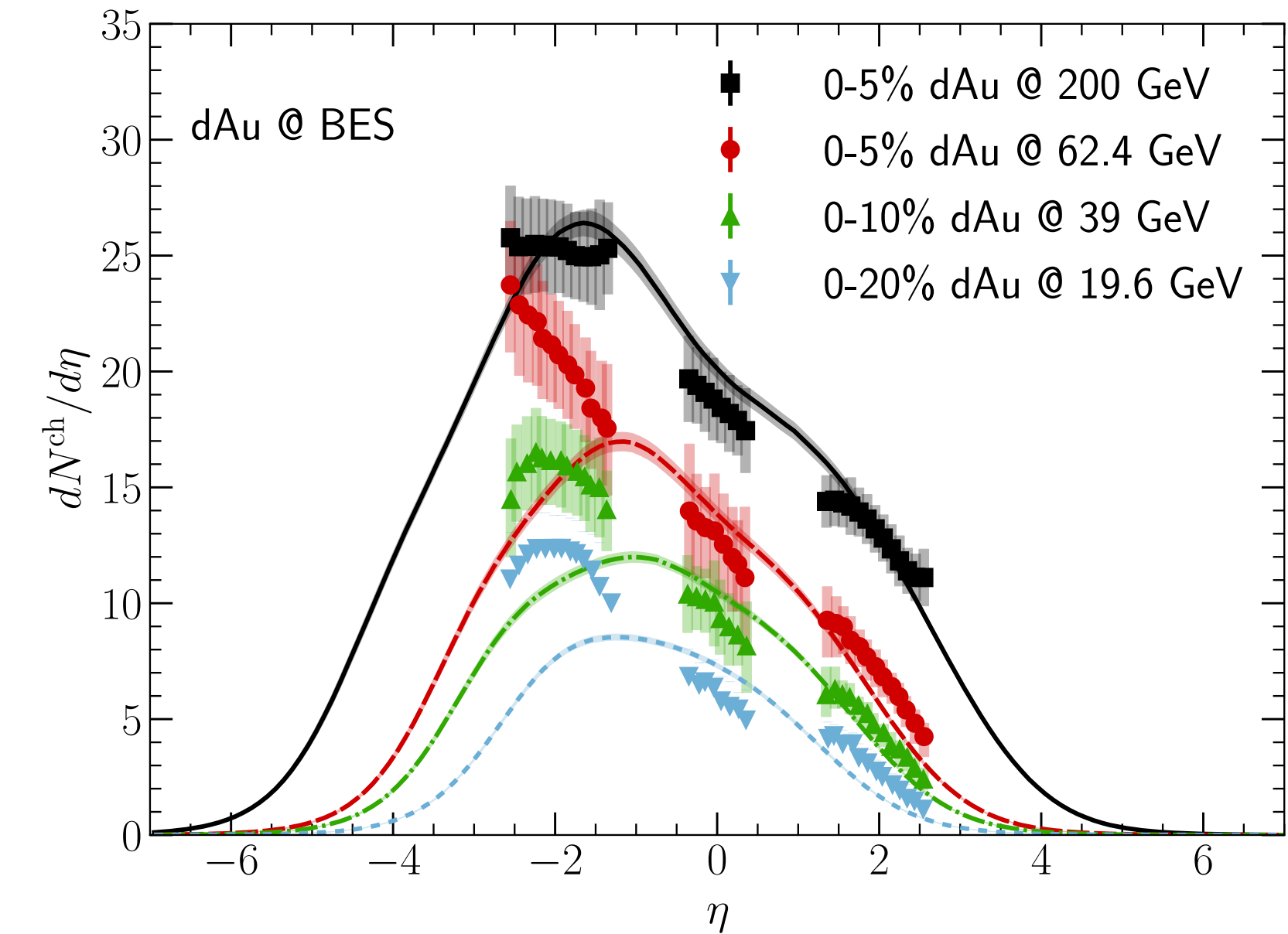
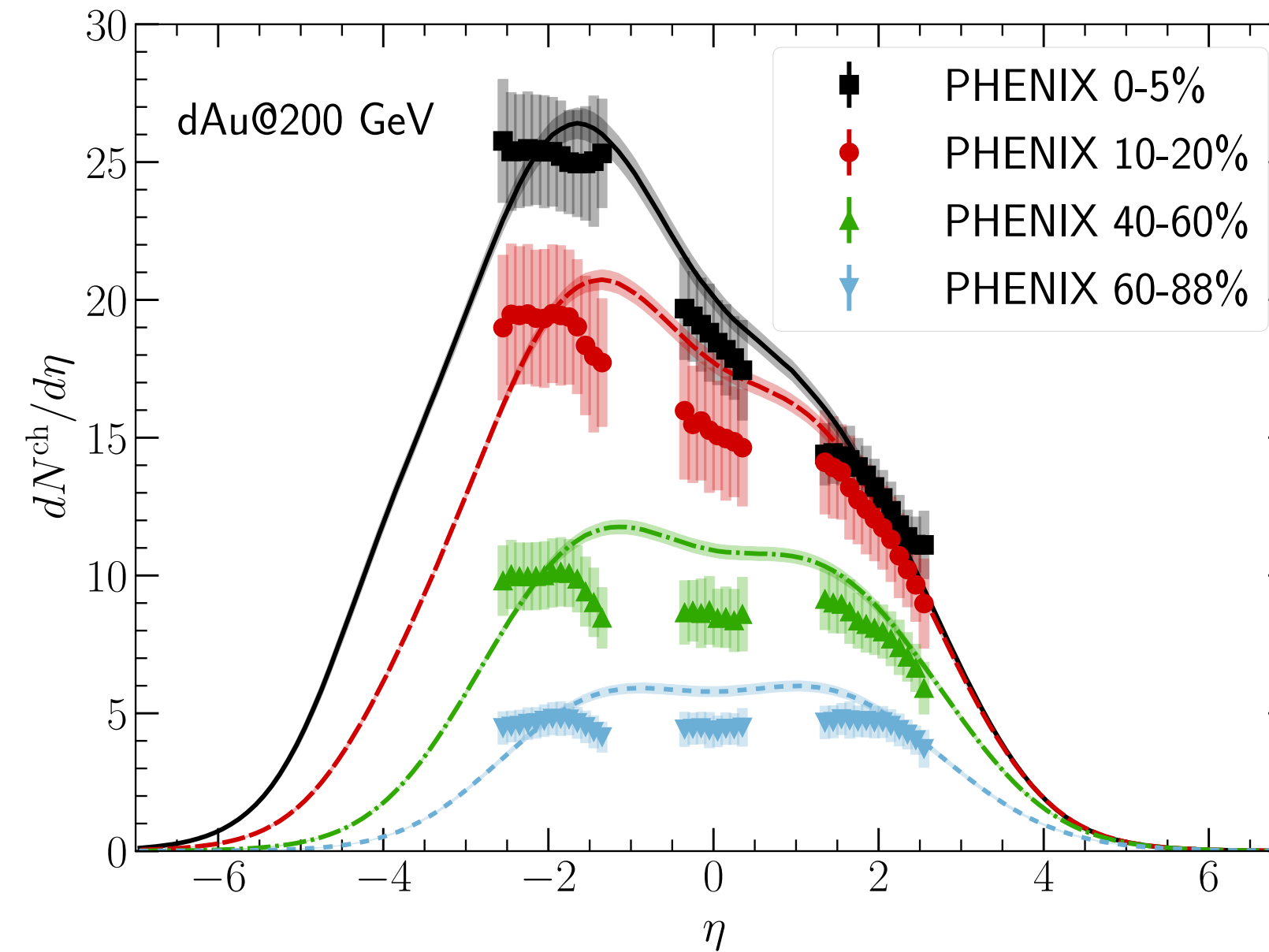
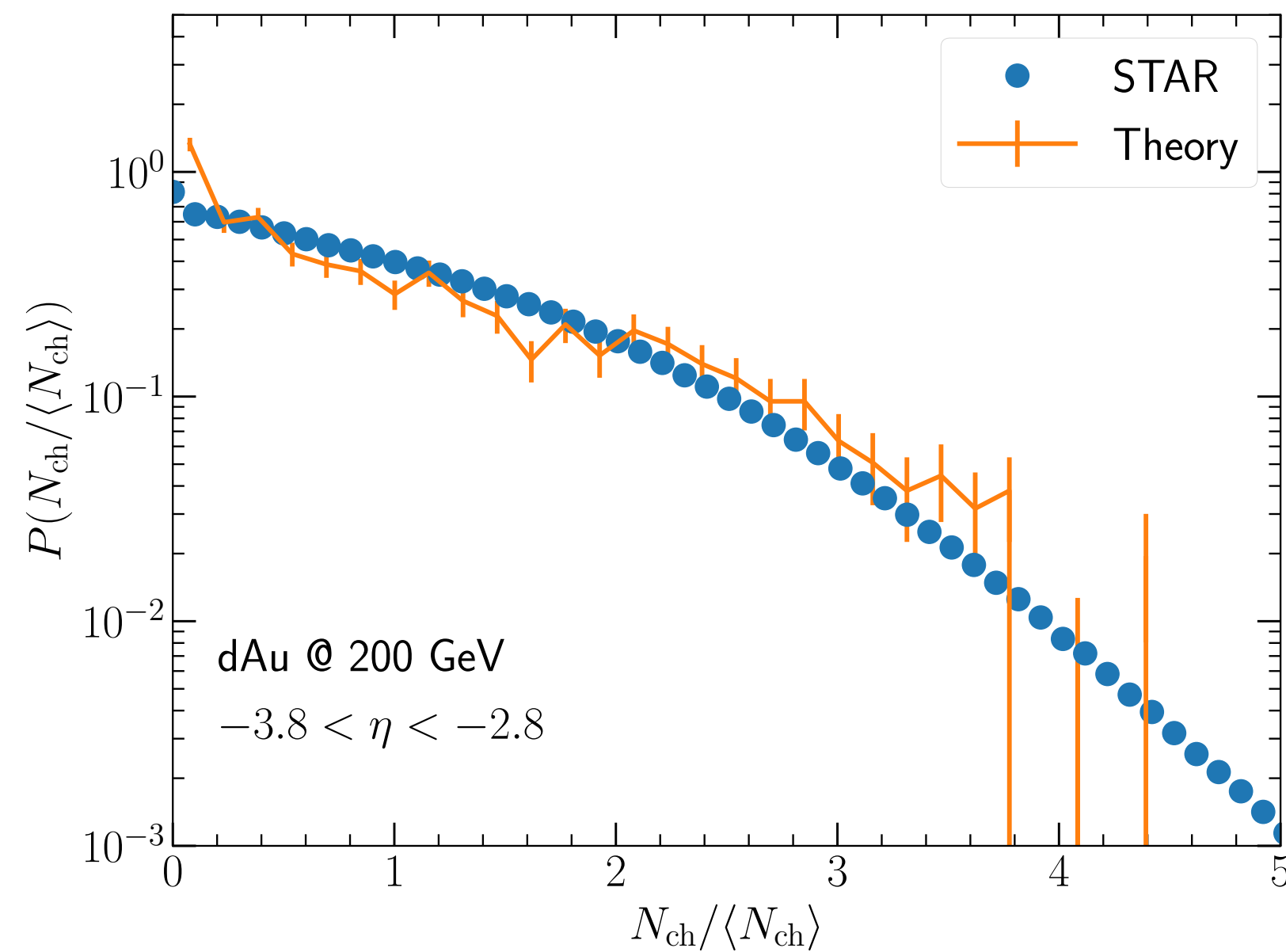
C. Shen and B. Schenke, in preparation

- **We can now determine centrality in the same rapidity bins as the experiments**
- **It does make a difference for the shape of the rapidity distribution**



MULTIPLICITY DISTRIBUTIONS

C. Shen and B. Schenke, in preparation

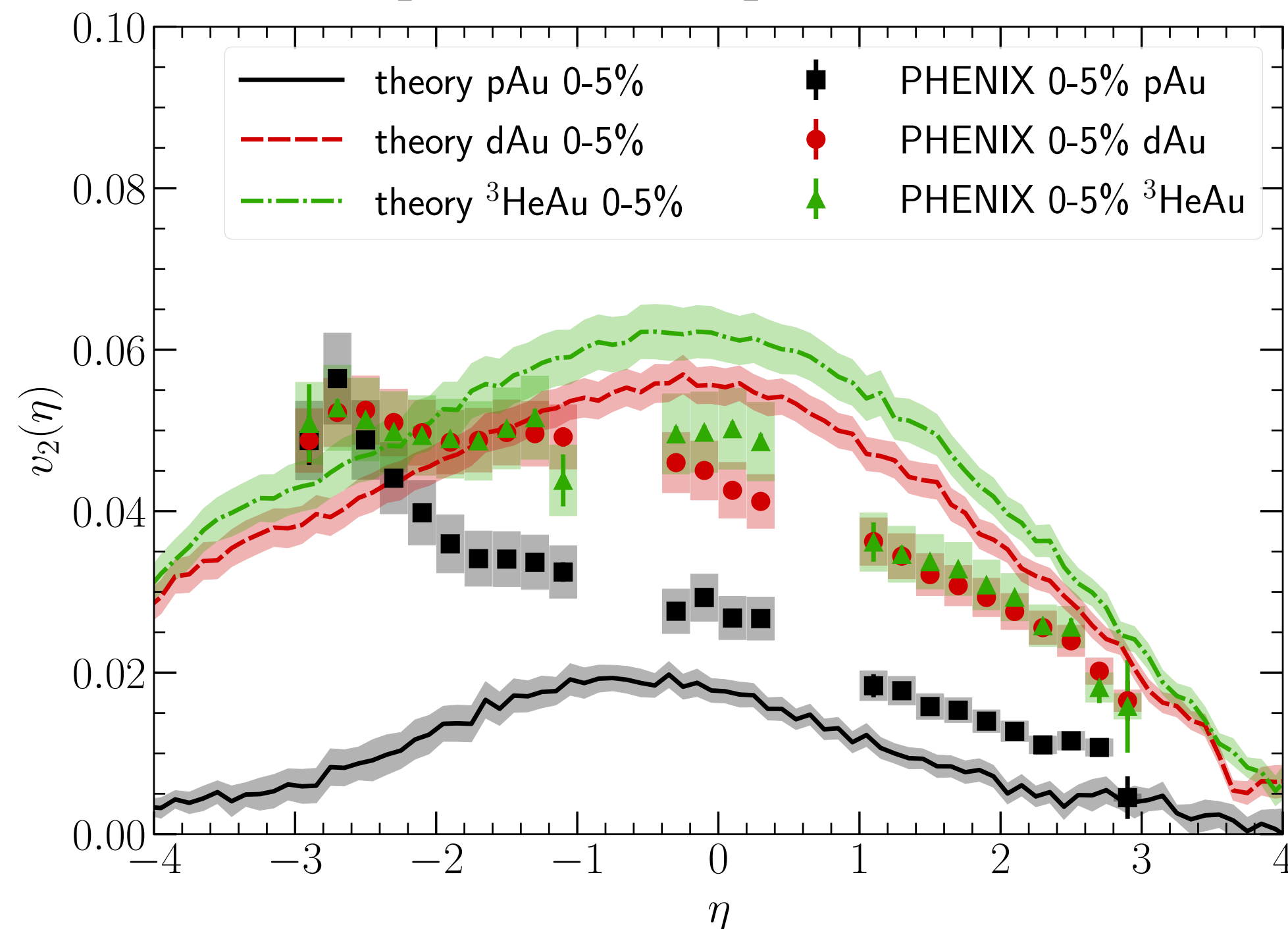


- **Model reproduces the STAR multiplicity distribution in d+Au collisions at 200 GeV**
- **The predicted charged hadron rapidity distribution agrees well with the PHENIX measurements from central to peripheral collisions**
- **The role of spectators at forward rapidity needs further investigation**

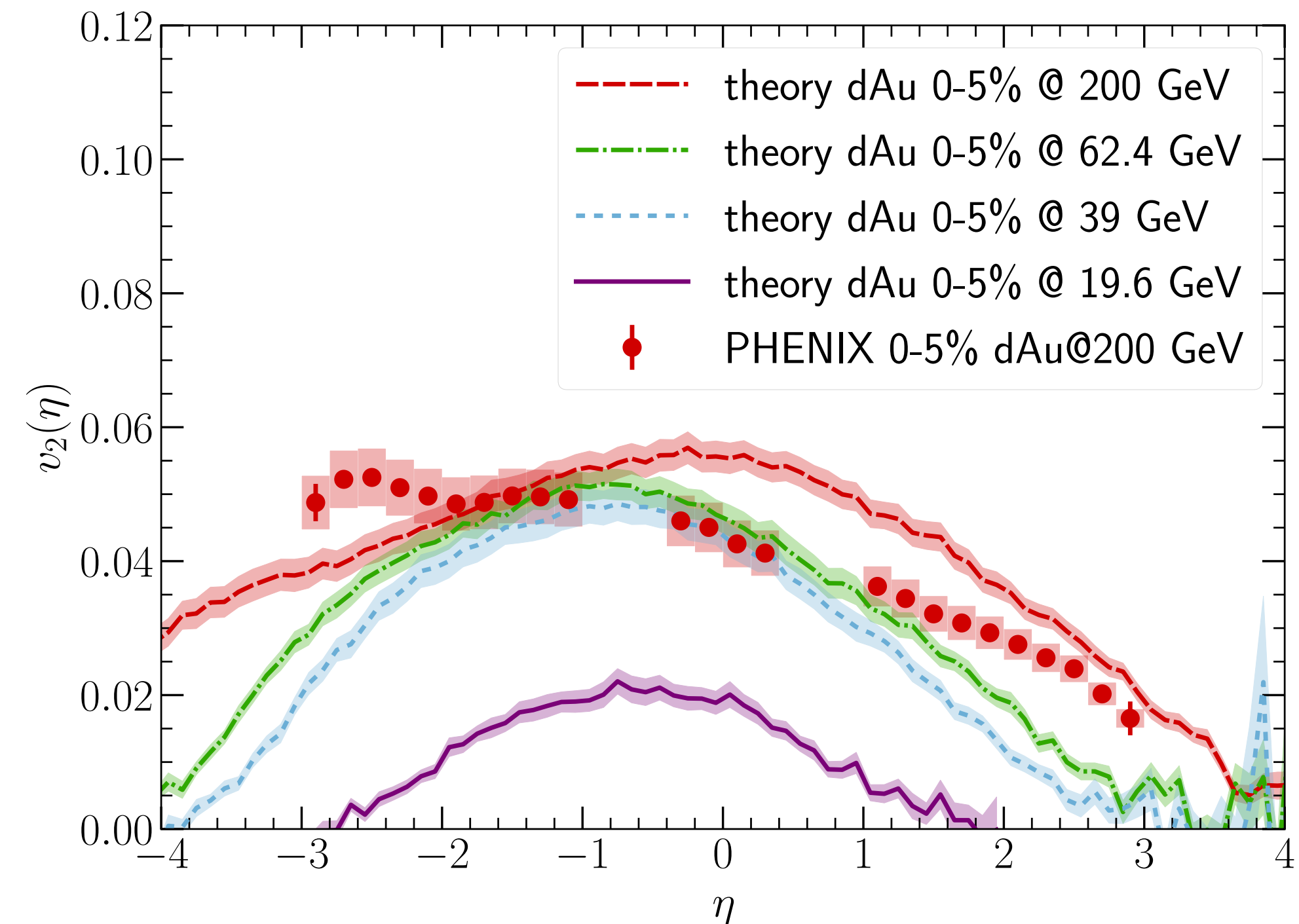
ANISOTROPIC FLOW

C. Shen and B. Schenke, in preparation

System dependence



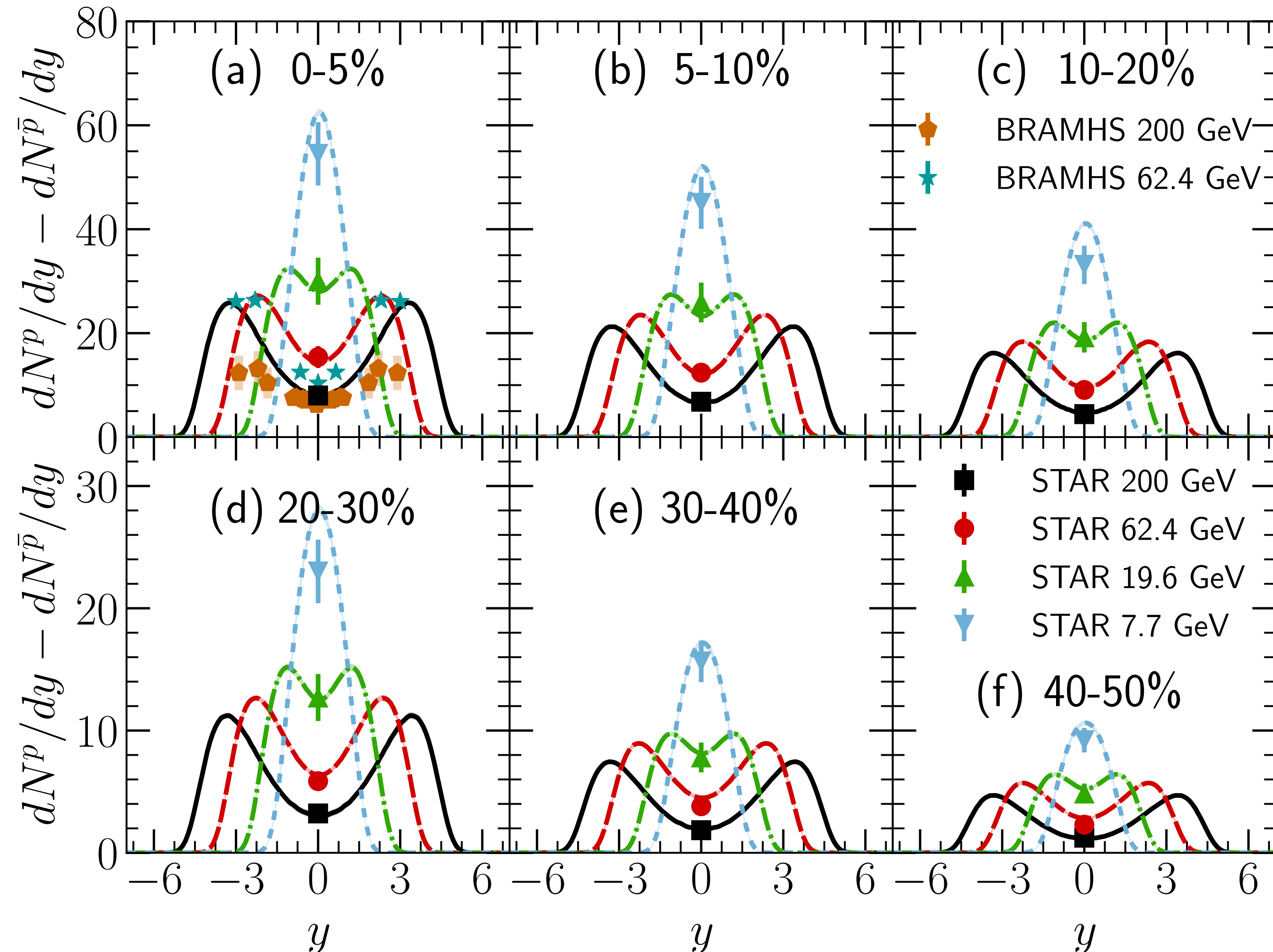
Energy dependence



- **Discrepancies could come from different method being used in the experiment**
- **Biggest deviation from the data in p+Au in the Au going direction (non-flow?)**
- **PHENIX event plane method with event plane at y in $[-3.9, -3.1]$**

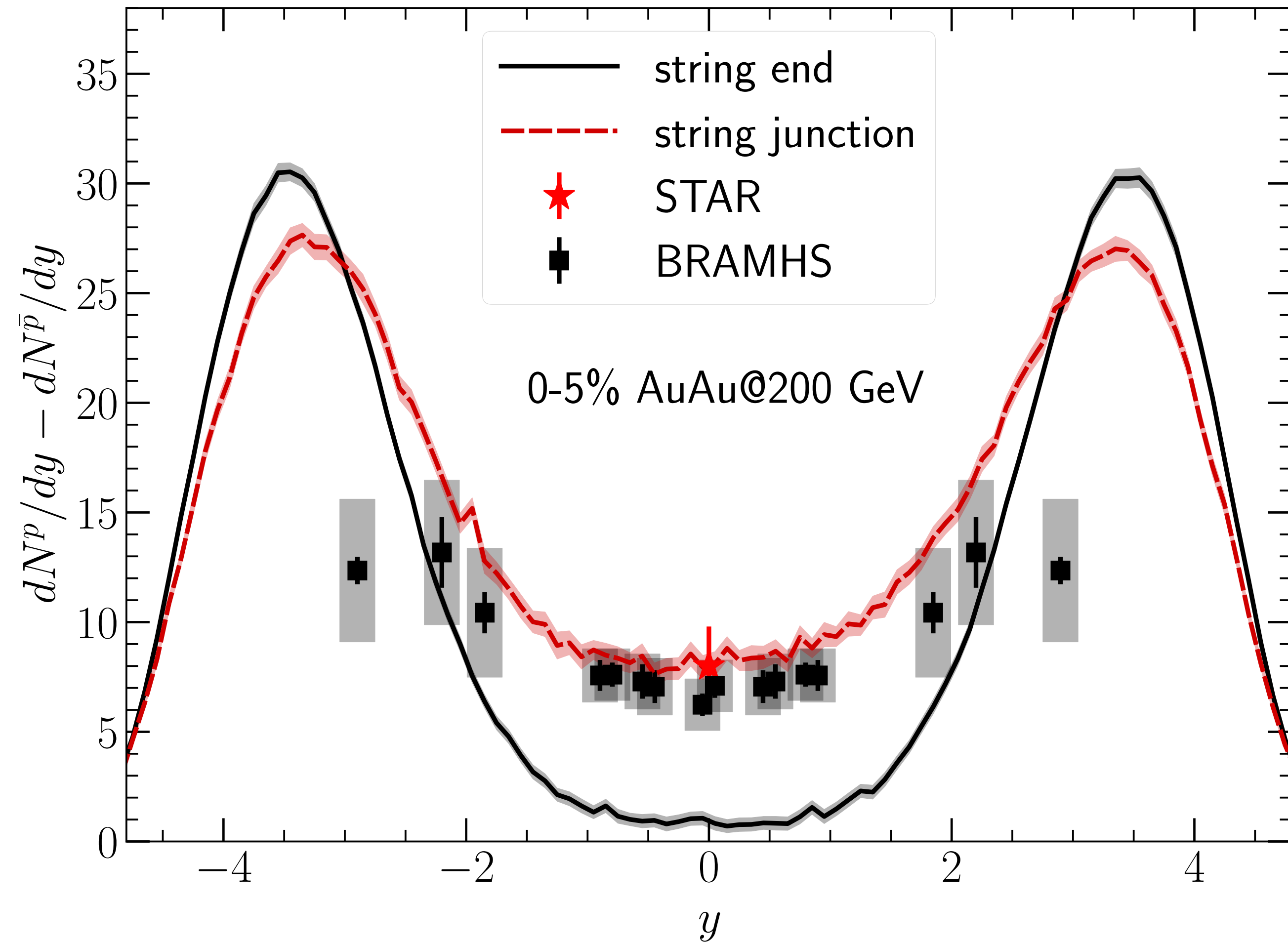
NET-BARYON DISTRIBUTIONS

C. Shen and B. Schenke, in preparation



NET-BARYON DISTRIBUTIONS

C. Shen and B. Schenke, in preparation



Effect of baryon junctions

