

# MOLECULAR STATES WITH CHARM: INSIGHTS FROM VACUUM & FINITE- TEMPERATURE ANALYSES

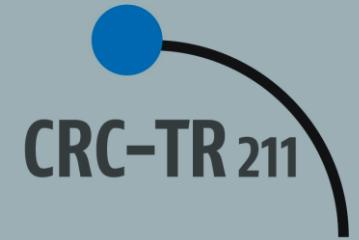


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Deutsche  
Forschungsgemeinschaft

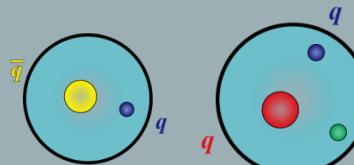


SQM 2024  
The 21<sup>st</sup> International Conference on Strangeness in Quark Matter  
3-7 June 2024, Strasbourg, France

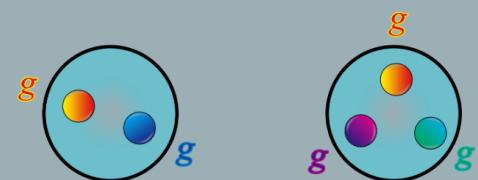
# Introduction

Hadrons as aggregates of more fundamental structures

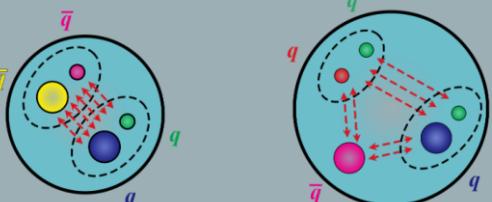
- **Conventional hadrons:** mesons and baryons



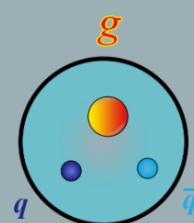
- **Glueballs:** gg, ggg ...



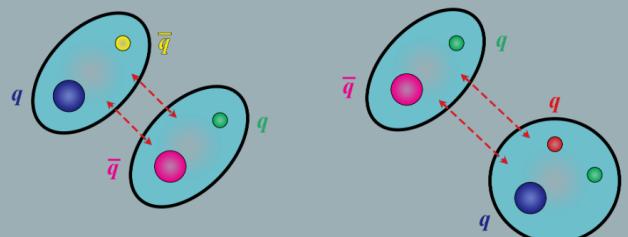
- **Multiquark states:** tetraquarks, pentaquarks...



- **Hybrid:** qqqg, q $\bar{q}$ g ...



- **Hadronic molecules:** colorless states bound by the residual strong force



## Reviews:

- Chen et al., RPP80 (2017) 7, 076201
- Guo et al., RMP90 (2018) 1, 015004
- Brambilla et al., PR873 (2020) 154
- Chen et al., RPP86 (2023) 2, 026201
- Liu et al., arXiv:2404.06399

Pictures credit:

Chen et al. RPP86 (2023) 2, 026201

# Heavy-light molecular states

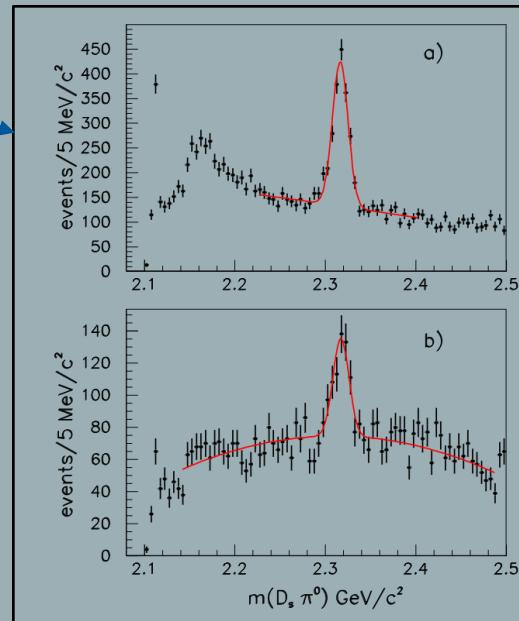
$D_{s0}^*(2317)$   $0(0^+)$   
 $D_{s1}(2460)$   $0(1^+)$

**Exotics:** lower masses than  $q\bar{q}$  prediction and very narrow (below  $DK, DK^*$  thresholds)

BaBar coll. PRL90 (2003) 242001

**Broad states**

$D_0^*(2300)$   $\frac{1}{2}(0^+)$   
 $D_1^*(2430)$   $\frac{1}{2}(1^+)$



**Heavy-quark spin partners**

$D_0^*(2300)$  originally generated as a low-mass pole until “double-pole structure” is proposed  
Albaladejo et al. PLB 767 (2017) 465 ; Guo et al. EPJC79 (2019) 13;  
Meißner, Sym. 12 (2020) 6, 981; JMT-R, Sym. (2022) 13 (2021), 8, 1400

EFT approaches with 2-body dynamics

**Chiral SU(3) EFT with heavy mesons**

Kolomeitsev, Lutz, PLB582 (2004) 39  
Hofmann, Lutz, NPA733 (2004) 142  
Guo et al. PLB641:278-285 (2006)  
Guo, Hanhart, Krewald, Meißner, PLB666 (2008) 251  
Tolos, Torres-Rincon, PRD88, 074019 (2013)  
Altenbuchinger, Geng, Weise, PRD89, 014026 (2014)

**Broken SU(4) EFT**

Gamerman et al. PRD76: 074016 (2007)

**Dominance of hadronic components:**  
Albaladejo et al. EPJC 78 (2018) 9, 722

**Other states**

$D_{sJ}(2860)$  Guo, Meißner, PRD 84, 014013  
 $X_0(2866)$  [ $D^*\bar{K}^*$ ] Liu et al. PRD102 (2020) 091502  
...

# Heavy-meson effective theory

$$\begin{aligned}\mathcal{L}_{\text{LO}} = & \mathcal{L}_{\text{LO}}^{\text{ChPT}} + \langle \nabla^\mu H \nabla_\mu H^\dagger \rangle - m_H^2 \langle HH^\dagger \rangle - \langle \nabla^\mu H^{*\nu} \nabla_\mu H_\nu^{*\dagger} \rangle + m_H^2 \langle H^{*\nu} H_\nu^{*\dagger} \rangle \\ & + ig \langle H^{*\mu} u_\mu H^\dagger - Hu^\mu H_\mu^{*\dagger} \rangle + \frac{g}{2m_D} \langle V_\mu^* u_\alpha \nabla_\beta H_\nu^{*\dagger} - \nabla_\beta V_\mu^* u_\alpha H_\nu^{*\dagger} \rangle \epsilon^{\mu\nu\alpha\beta},\end{aligned}$$

$$\begin{aligned}\mathcal{L}_{\text{NLO}} = & \mathcal{L}_{\text{NLO}}^{\text{ChPT}} - h_0 \langle HH^\dagger \rangle \langle \chi_+ \rangle + h_1 \langle H \chi_+ H^\dagger \rangle + h_2 \langle HH^\dagger \rangle \langle u^\mu u_\mu \rangle + h_3 \langle Hu^\mu u_\mu H^\dagger \rangle \\ & + h_4 \langle \nabla_\mu H \nabla_\nu H^\dagger \rangle \langle u^\mu u^\nu \rangle + h_5 \langle \nabla_\mu H \{u^\mu, u^\nu\} \nabla_\nu H^\dagger \rangle \\ & + \tilde{h}_0 \langle H^{*\mu} H_\mu^{*\dagger} \rangle \langle \chi_+ \rangle - \tilde{h}_1 \langle H^{*\mu} \chi_+ H_\mu^{*\dagger} \rangle - \tilde{h}_2 \langle H^{*\mu} H_\mu^{*\dagger} \rangle \langle u^\nu u_\nu \rangle - \tilde{h}_3 \langle H^{*\mu} u^\nu u_\nu H_\mu^{*\dagger} \rangle \\ & - \tilde{h}_4 \langle \nabla_\mu H^{*\alpha} \nabla_\nu H_\alpha^{*\dagger} \rangle \langle u^\mu u^\nu \rangle - \tilde{h}_5 \langle \nabla_\mu H^{*\alpha} \{u^\mu, u^\nu\} \nabla_\nu H_\alpha^{*\dagger} \rangle,\end{aligned}$$

$h_i, \tilde{h}_i$  : NLO low-energy constants

Guo et al. EPJC79, 1, 13 (2019)

Kolomeitsev, Lutz, PLB582 (2004) 39

Hofmann, Lutz, NPA733 (2004) 142

Guo et al., PLB641 (2006) 278

Guo, Shen, Chiang, PLB647 (2007) 133

Guo et al., PLB666 (2008) 251

Geng et al., PRD82,05422 (2010)

Abreu et al. (JMT-R), AP 326 (2011) 2737

Altenbuchinger, Geng, Weise, PRD89, 014026 (2014)

$$H = (D^0 \ D^+ \ D_s^+)$$

$$H_\mu^* = (D_\mu^{*0} \ D_\mu^{*+} \ D_{s,\mu}^{*+})$$

$$u_\mu = i(u^\dagger \partial_\mu u - u \partial_\mu u^\dagger)$$

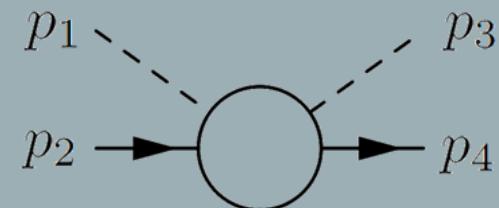
$$u = \exp \left[ \frac{i}{\sqrt{2} f_\pi} \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -\frac{2\eta}{\sqrt{6}} \end{pmatrix} \right]$$

# Heavy-meson effective theory

$$V_{ij}(p_1, p_2, p_3, p_4) = \frac{1}{f_\pi^2} \left[ \frac{C_{\text{LO}}^{ij}}{4} [(p_1 + p_2)^2 - (p_2 - p_3)^2] - 4C_0^{ij} h_0 + 2C_1^{ij} h_1 \right. \\ - 2C_{24}^{ij} \left( 2h_2(p_2 \cdot p_4) + h_4((p_1 \cdot p_2)(p_3 \cdot p_4) + (p_1 \cdot p_4)(p_2 \cdot p_3)) \right) \\ \left. + 2C_{35}^{ij} \left( h_3(p_2 \cdot p_4) + h_5((p_1 \cdot p_2)(p_3 \cdot p_4) + (p_1 \cdot p_4)(p_2 \cdot p_3)) \right) \right]$$

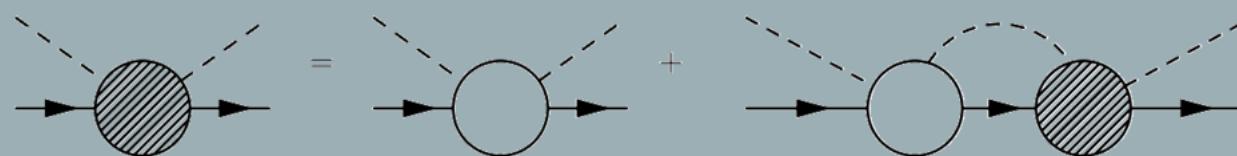
L=0 partial wave

$$V_{ij}^{\text{s-wave}}(p, p'; \sqrt{s}) = \frac{1}{2} \int_{-1}^1 d \cos \theta_{pp'} V_{ij}(p_1, p_2, p_3, p_4)$$



Lippmann-Schwinger equation for the T-matrix elements

$$T_{if}(q', q; z) = V_{if}(q', q; z) + \sum_l \int_0^\infty \frac{4\pi k^2 dk}{(2\pi)^3} \frac{V_{il}(q', k; z) T_{lf}(k, q; z)}{2\omega_{H,l} 2\omega_{\phi,l} (z - \omega_{H,l} - \omega_{\phi,l})}$$

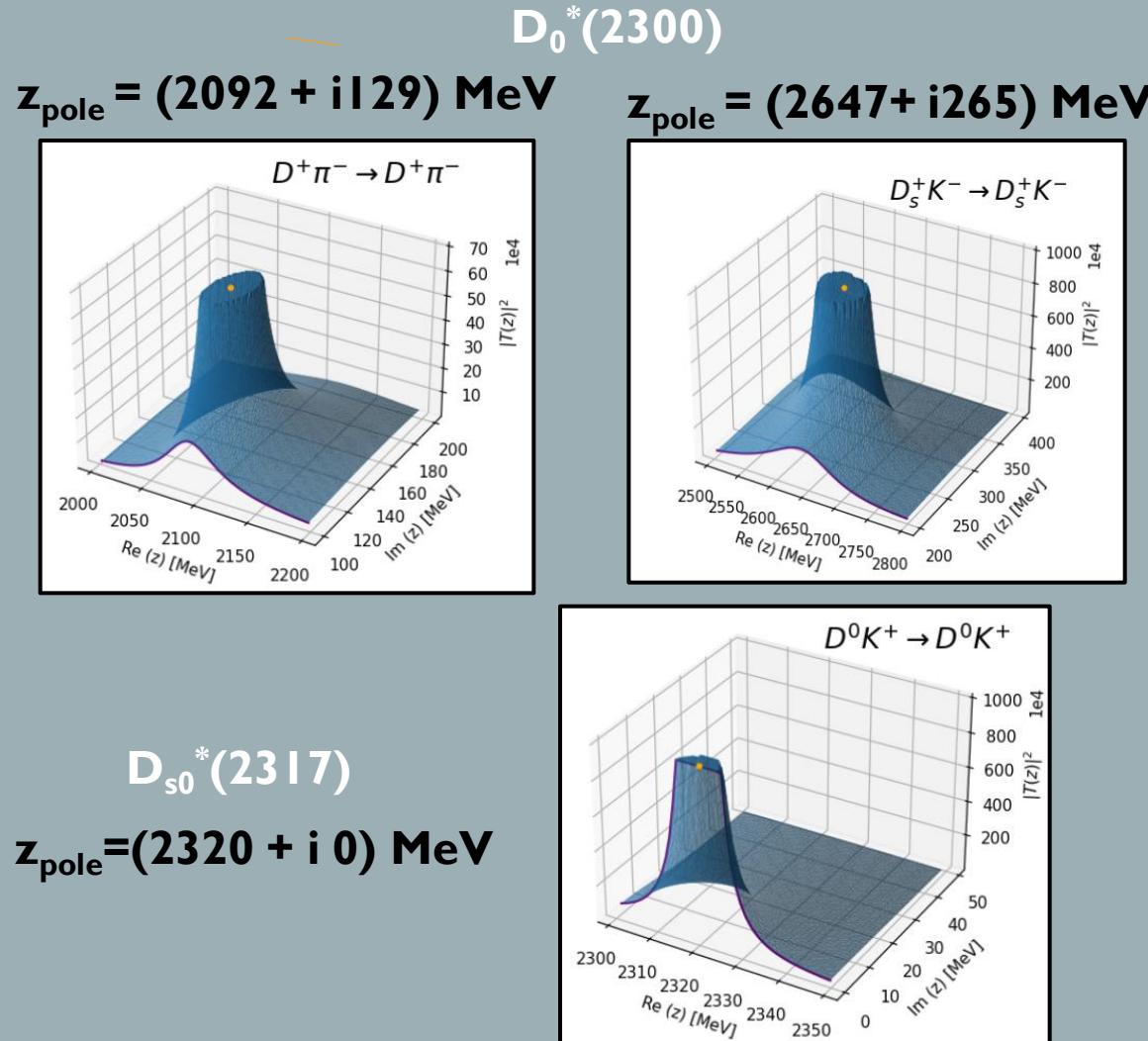


On-shell reduction: Oller, Oset, NPA620 (1997) 438; Oset, Ramos NPA635 (1998) 99

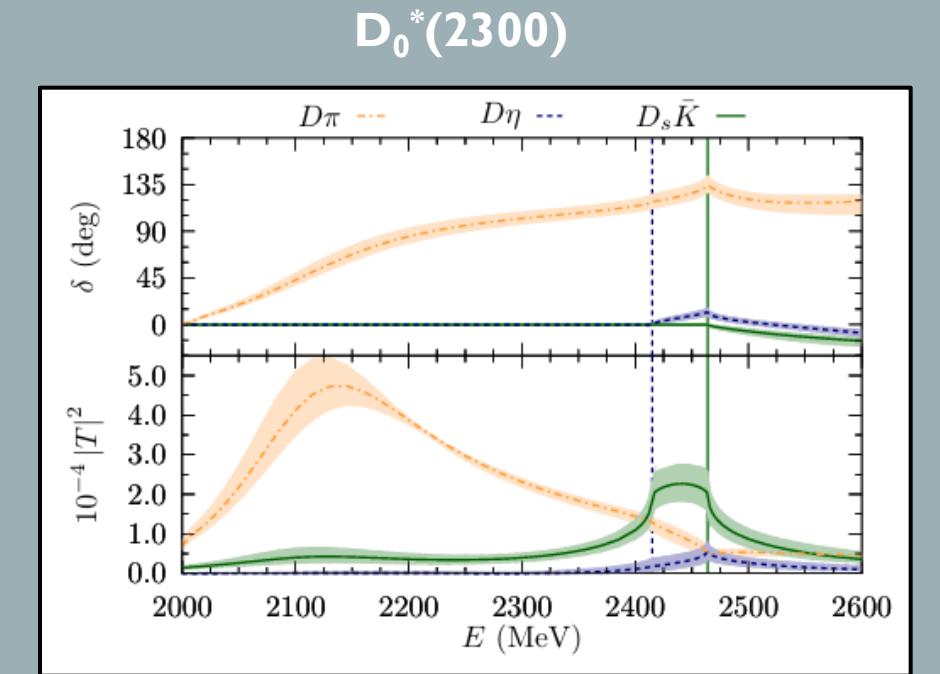
$$T = V(1 - VG)^{-1}$$

# Molecular states as poles of T matrix

JMT-R, Ramos, Tolos, PRD 108, 096008 (2023)



Albaladejo et al. PLB 767 (2017) 465



$M$ (MeV)	$\Gamma/2$ (MeV)	$ g_{D\pi} $	$ g_{D\eta} $	$ g_{D_s\bar{K}} $
$2105^{+6}_{-8}$	$102^{+10}_{-12}$	$9.4^{+0.2}_{-0.2}$	$1.8^{+0.7}_{-0.7}$	$4.4^{+0.5}_{-0.5}$
$2451^{+36}_{-26}$	$134^{+7}_{-8}$	$5.0^{+0.7}_{-0.4}$	$6.3^{+0.8}_{-0.5}$	$12.8^{+0.8}_{-0.6}$

Pole parameters

# Meson-baryon molecular states

## Meson-baryon states with open charm

$\Lambda_c(2595), \Lambda_c(2880), \Sigma_c(2800), \Xi_c(2970) \dots$

$$V_{ij}(s) = D_{ij} \frac{2\sqrt{s} - M_i - M_j}{4 f_i f_j} \sqrt{\frac{E_i + M_i}{2M_i}} \sqrt{\frac{E_j + M_j}{2M_j}}$$

$$T(s) = \frac{1}{1 - V(s)G(s)} V(s)$$

Contact s-wave interaction:

Lutz, Kolomeitsev, NPA730 (200) 110

Hofmann, Lutz, NPA763 (2005) 90

Mizutani, Ramos, PRC74, 065201 (2006)

He, Liu, PRD82:114029 (2010)

Romanets *et al.* PRD 85, 114032 (2012)

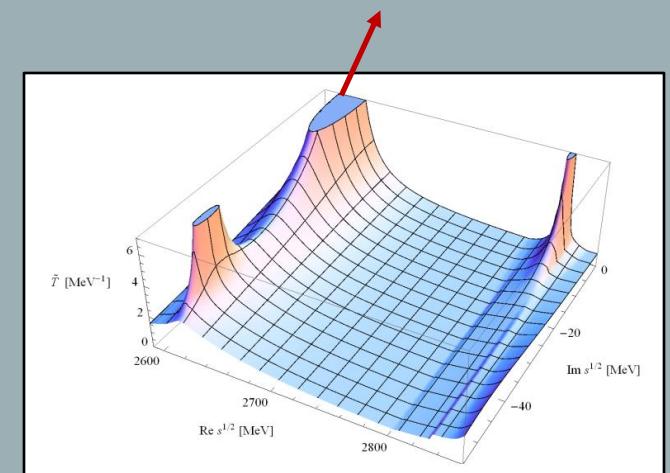
He *et al.*, EPJC51, 883 (2007)

Jimenez-Tejero *et al.* PRC80, 055206 (2009)

Jimenez-Tejero *et al.*, PRC84, 015208 (2010)

...

see Guo *et al.* RMP90, 015004 (2018)



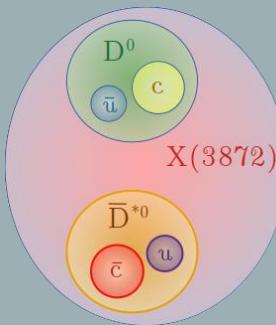
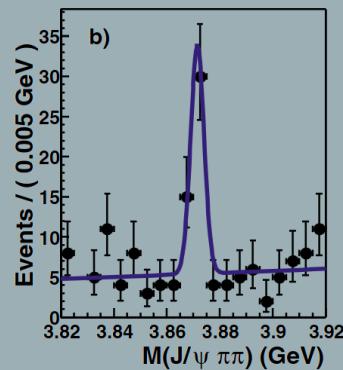
Romanets *et al.*  
PRD 85, 114032 (2012)

Also **hidden charm pentaquarks** candidates  $P_c(4380)$  &  $P_c(4450)$  also studied under the molecular assumption  $[\Sigma_c(2520) D]$  &  $[\chi_{c1} P]$  (among other possible interpretations), e.g.

Chen *et al.*, PRL 115, 172001 (2015); Mei  ner, Oller, PLB751 (2015) 59

# X(3872): Heavy-heavy molecular states

- X(3872)** [Belle Coll. PRL91, 262001 (2003)] seems to have strong coupling to  $D\bar{D}^*$  Törnqvist, ZPC61, 525 (1994)



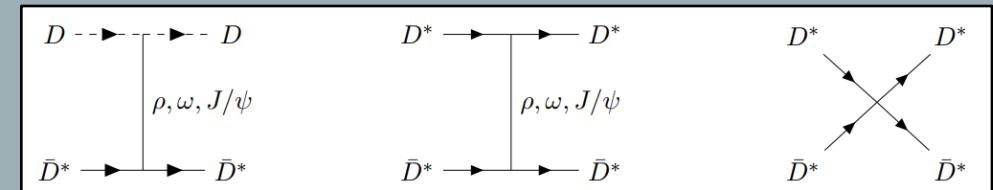
- Quantum number:  $I^{++}$  (LHCb coll., PRL110 (2013) 2220001)
- Nature still not clear:  $D\bar{D}^*$  but also conventional  $\chi_{c1}(2P)$ , tetraquark, hybrid, glueball...
- Mass very close to  $D\bar{D}^*$  threshold. Width extremely small

Molecular description: **Chiral SU(4)** Gamermann, Oset, EPJA33:119,2007 **Local Hidden Gauge** Montaña et al. (JMT-R) PRD107(2023)5, 054014

Local Hidden Gauge Lagrangian in SU(4)  
Molina, Oset, PRD80 (2009) 114013  
Molina et al. PRD80 (2009) 014025

$$\mathcal{L} = -\frac{1}{4}\langle V_{\mu\nu}V^{\mu\nu} \rangle + \frac{1}{2}m_V^2 \left\langle \left( V_\mu - \frac{i}{g}\Gamma_\mu \right)^2 \right\rangle$$

Montaña et al. (JMT-R) PRD107(2023)5, 054014



X(3872)

X(4014)

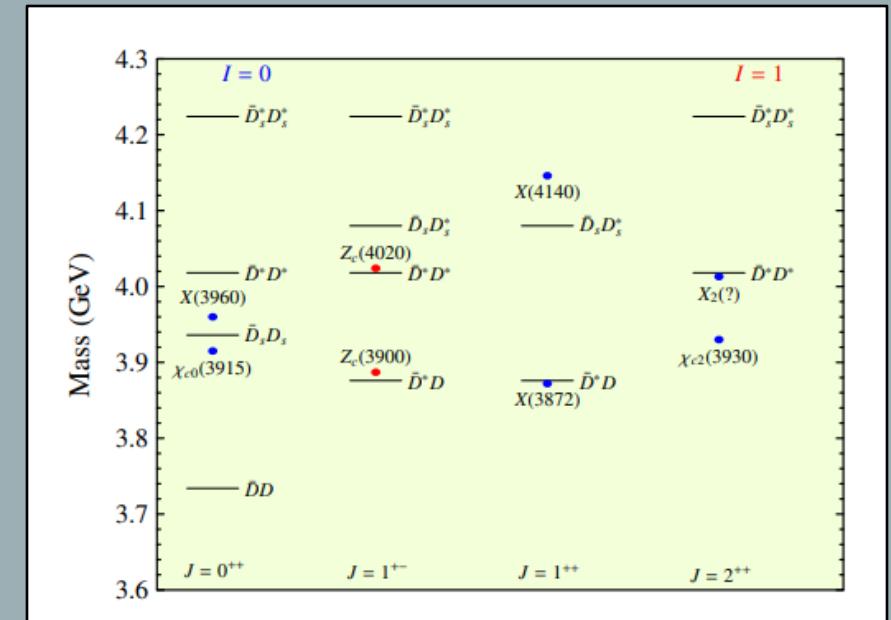
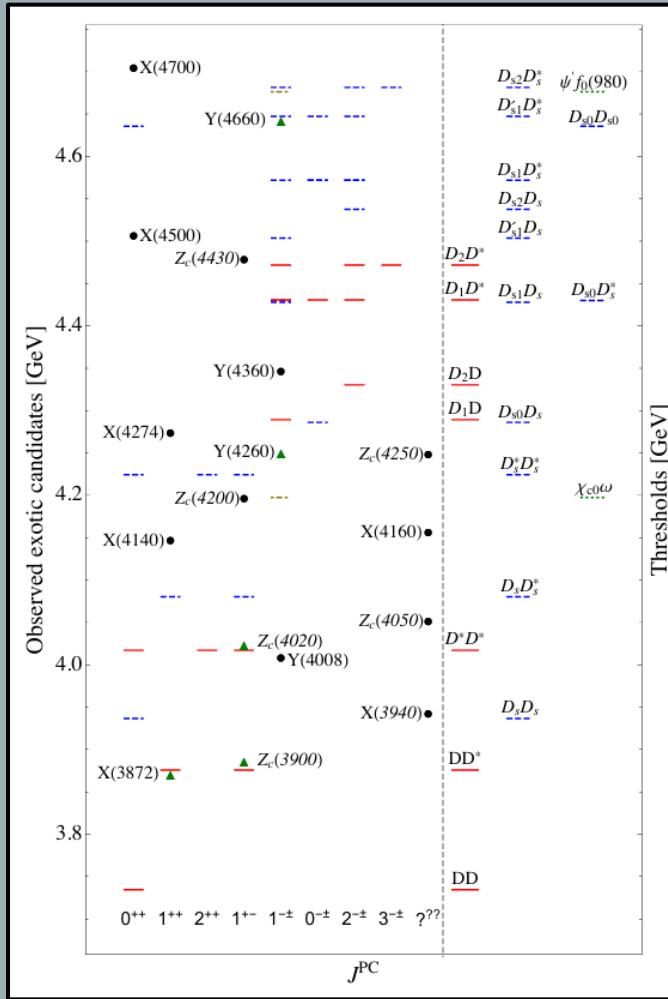
$$T(s) = \frac{1}{1 - V(s)G(s)} V(s)$$

$\Lambda$ (MeV)	State	Nearest threshold (MeV)	$\sqrt{z_p}$ (MeV)	Couplings (GeV)
567	$X(3872)$	$m_D + m_{\bar{D}^*} = 3875.80$	$3871.65 + i 0.00$	$ g_{D\bar{D}^*}  = 9.23$ $ g_{D_s\bar{D}_s^*}  = 3.98$
510	$X(4014)$	$m_{D^*} + m_{\bar{D}^*} = 4017.11$	$4014.31 + i 0.00$	$ g_{D^*\bar{D}^*}  = 8.56$ $ g_{D_s^*\bar{D}_s^*}  = 3.69$

# X,Y,Z: Heavy-heavy molecular states

# Plethora of heavy-quarkonium like states (+200):

State	$I^G(J^{PC})$	$M$ [MeV]	$\Gamma$ [MeV]	$S$ -wave threshold(s) [MeV]
$X(3872)$	$0^+(1^{++})$	$3871.69 \pm 0.17$	$< 1.2$	$D^{*+}D^- + c.c.(-8.15 \pm 0.20)$ $D^{*0}\bar{D}^0 + c.c.(0.00 \pm 0.18)$
$X(3940)$	$?^?(?^{??})$	$3942.0 \pm 9$	$37^{+27}_{-17}$	$D^*\bar{D}^*(-75.1 \pm 9)$
$X(4160)$	$?^?(?^{??})$	$4156^{+29}_{-25}$	$139^{+110}_{-60}$	$D^*\bar{D}^*(139^{+29}_{-25})$
$Z_c(3900)$	$1^+(1^{+-})$	$3886.6 \pm 2.4$	$28.1 \pm 2.6$	$D^*\bar{D}(10.8 \pm 2.4)$
$Z_c(4020)$	$1(?^?)$	$4024.1 \pm 1.9$	$13 \pm 5$	$D^*\bar{D}^*(7.0 \pm 2.4)$
$Y(4260)$	$?^?(1^{--})$	$4251 \pm 9$	$120 \pm 12$	$D_1\bar{D} + c.c.(-38.2 \pm 9.1)$ $\chi_{c0}\omega(53.6 \pm 9.0)$
$Y(4360)$	$?^?(1^{--})$	$4346 \pm 6$	$102 \pm 10$	$D_1\bar{D}^* + c.c.(-85 \pm 6)$
$Y(4660)$	$?^?(1^{--})$	$4643 \pm 9$	$72 \pm 11$	$\psi(2S)f_0(980)(-33 \pm 21)$ $\Lambda_c^+\Lambda_c^-(70 \pm 6)$
$Z_c(4430)^+$	$?(1^+)$	$4478^{+15}_{-18}$	$181 \pm 31$	$\psi(2S)\rho(17^{+15}_{-18})$
$Z_c(4200)^+$	$?(1^+)$	$4196^{+35}_{-32}$	$370^{+100}_{-32}$	
$Z_c(4050)^+$	$?(^?)$	$4051^{+24}_{-40}$	$82^{+50}_{-28}$	$D^*\bar{D}^*(34^{+24}_{-40})$
$Z_c(4250)^+$	$?(^?)$	$4248^{+19}_{-50}$	$177^{+120}_{-70}$	$\chi_{c1}\rho(-37^{+56}_{-56})$
$X(4140)$ (Aaij <i>et al.</i> , 2017a,b)	$0^+(1^{++})$	$4146.5 \pm 4.5^{+4.6}_{-2.8}$	$83 \pm 21^{+21}_{-14}$	$D_s\bar{D}_s^*(-66.1^{+4.9}_{-3.2})$
$X(4274)$ (Aaij <i>et al.</i> , 2017a,b)	$0^+(1^{++})$	$4273.3 \pm 8.3^{+17.2}_{-3.6}$	$56 \pm 11^{+8}_{-11}$	$D_s^*\bar{D}_s^*(-49.1^{+19.1}_{-9.1})$
$X(4500)$ (Aaij <i>et al.</i> , 2017a,b)	$0^+(0^{++})$	$4506 \pm 11^{+15}_{-15}$	$92 \pm 21^{+21}_{-15}$	$D_{s0}^*(2317)\bar{D}_{s0}^*(2317)(-129^{+16}_{-19})$
$X(4700)$ (Aaij <i>et al.</i> , 2017a,b)	$0^+(0^{++})$	$4700 \pm 10^{+14}_{-24}$	$120 \pm 31^{+42}_{-33}$	$D_{s0}^*(2317)\bar{D}_{s0}^*(2317)(69^{+17}_{-26})$
$Z_b(10610)$	$1^+(1^+)$	$10607.2 \pm 2.0$	$18.4 \pm 2.4$	$B\bar{B}^* + c.c.(4.0 \pm 3.2)$

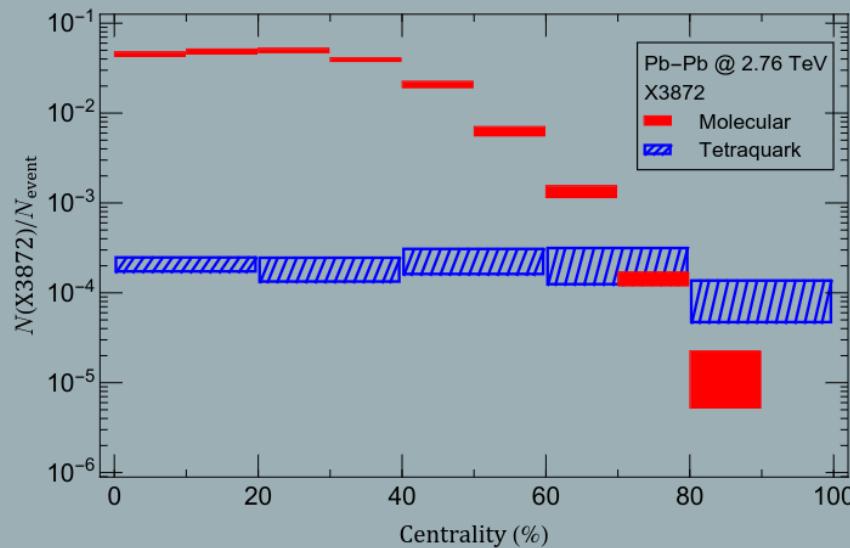


Liu et al., arXiv:2404.06399

# X(3872): Molecular vs Tetraquark

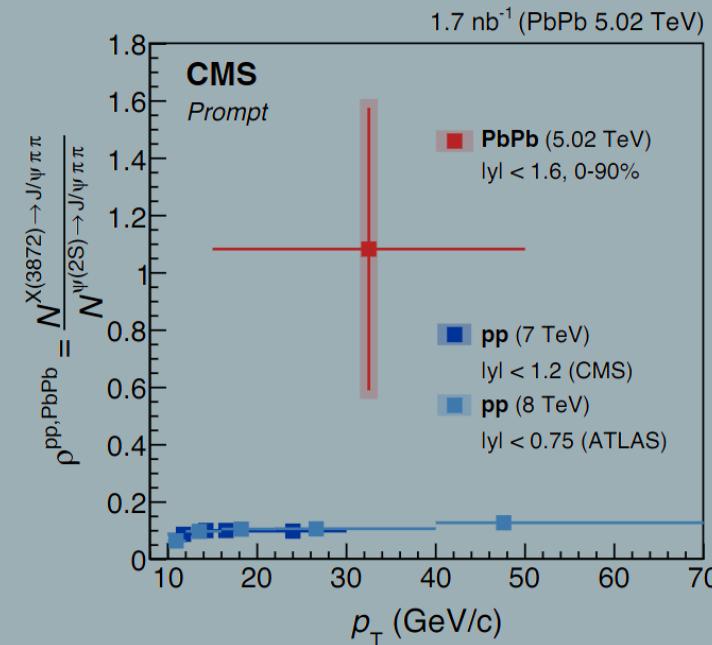
## Insights from Heavy-Ion Collisions

- Production of extended molecule ( $\sim 5$  fm) drastically depends on system's volume
- For tetraquark, compact state ( $\sim 0.5$  fm) it is independent of centrality



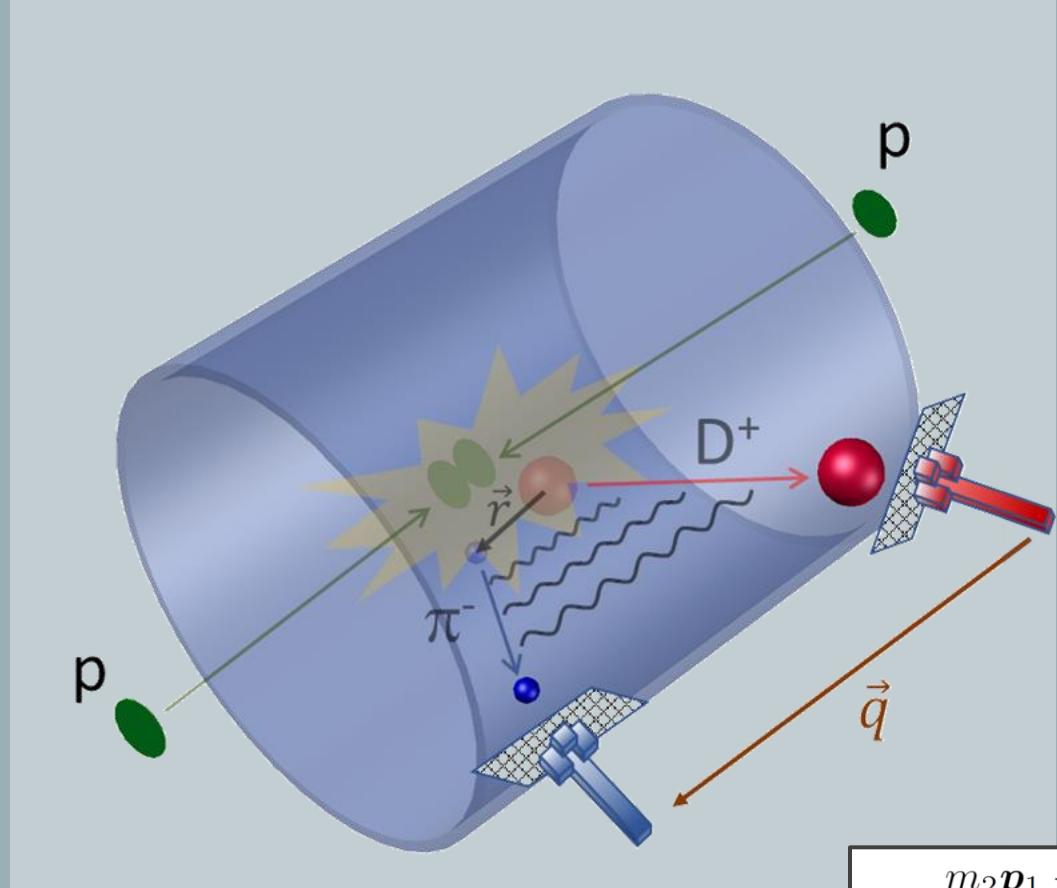
Zhang et al. PRL126, 012301 (2021)

First measurement of X(3872) in Pb-Pb collisions by CMS collaboration:



CMS collaboration PRL128, 032001 (2022)

# Femtoscopy in p+p collisions



$$q = \frac{m_2 \mathbf{p}_1 - m_1 \mathbf{p}_2}{m_1 + m_2}$$

Heinz, Jacak, ARNPS 49 (1999) 529-579

Lisa, Pratt, Wiedemann, ARNPS 55 (2005) 357

Fabbietti, Mantovani Sarti, Vazquez Doce, ARNPS 71, 377 (2021)

**Femtoscopy** can also help in identifying resonant states

Femtoscopy studies with charm in high multiplicity p+p collisions @  $s^{1/2}=13\text{ TeV}$ :

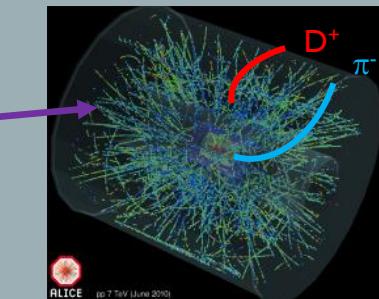
$\bar{D}N$ : ALICE coll., PRD 106 (2022) 052010

$D^{(*)}\pi, D^{(*)}K, D^{(*)}\bar{K}$ : ALICE coll, 2401.13541

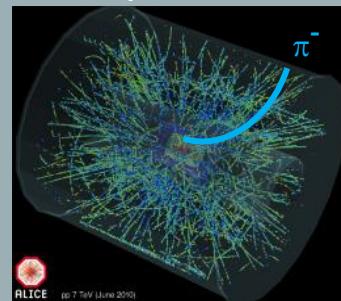
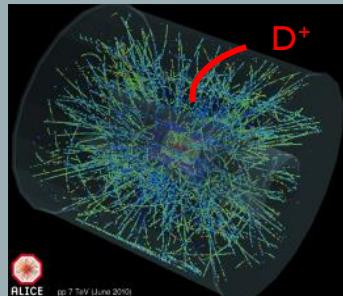
# Insights from femtoscopy

Pair Correlation Function

$$C(\mathbf{q}) = \mathcal{N} \frac{N_{\text{same}}(\mathbf{q})}{N_{\text{mixed}}(\mathbf{q})}$$



'Event mixing' technique



Koonin-Pratt formula

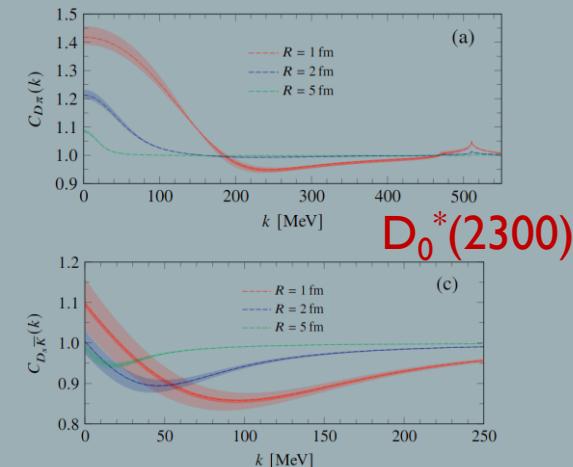
$$C(\mathbf{q}) = \int d^3r \sum_i w_i S_i(\mathbf{r}) |\Psi_i(\mathbf{q}; \mathbf{r})|^2$$

$C(\mathbf{q}) > 1$  : attraction  
 $C(\mathbf{q}) < 1$  : repulsion

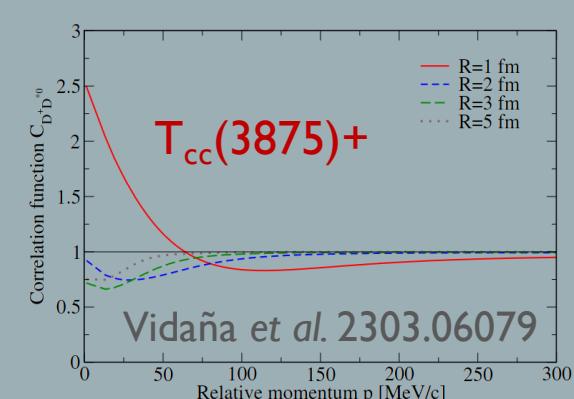
Koonin, PL.B, 70, 43 (1977)

Pratt, Csorgo, Zimanyi, PRC, 42, 2646(1990)

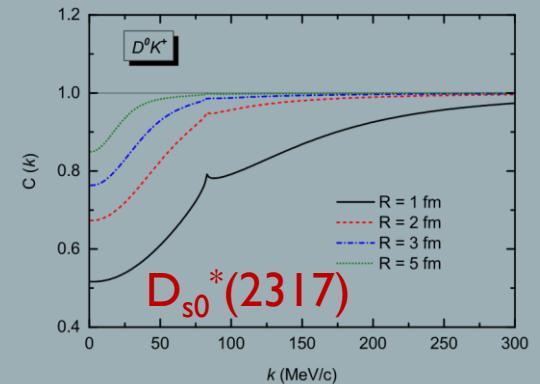
Resonances/bound present characteristic effects  
**Examples with charm:**



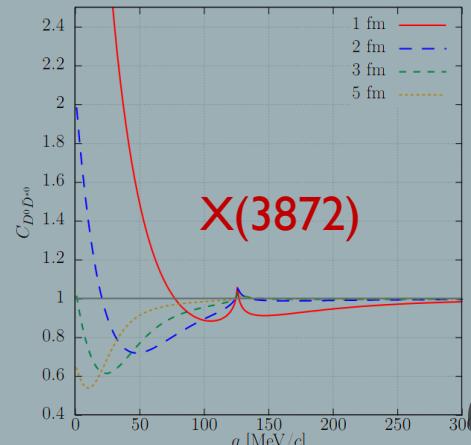
Albaladejo, Nieves, Ruiz Arriola,  
PRD108 (2023) 1, 014020



Liu, Lu, Geng, PRD107  
(2023) 7, 074019



Kamiya, Hyodo, Ohnishi  
EPJA58 (2022) 7, 131

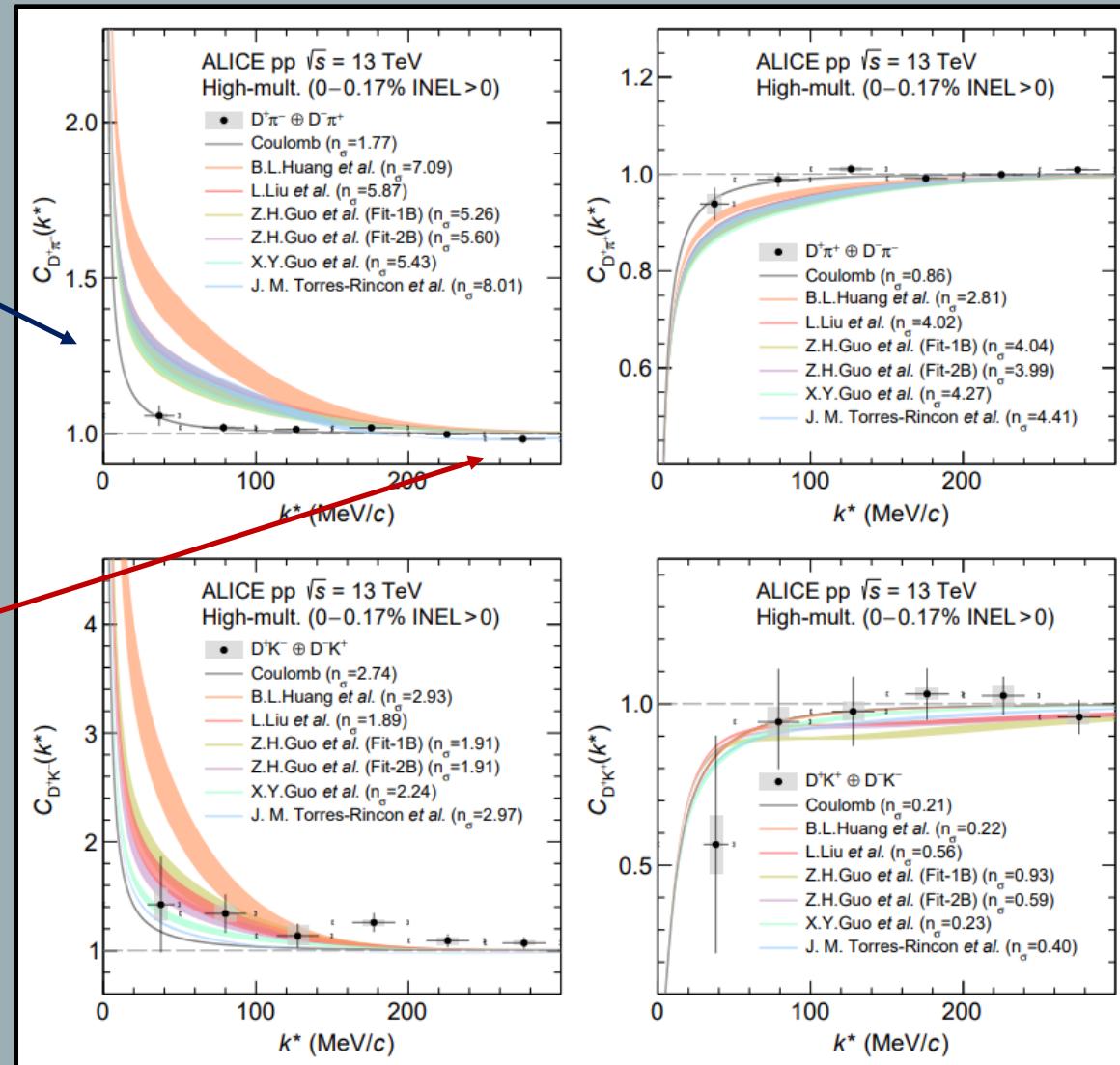


# D meson correlation functions

Strong deviations in  
 $D^+\pi^-$  channel!

but

Lower pole of  
 $D_0^*(2300)$   
makes depletion for  
 $q=250$  MeV/c



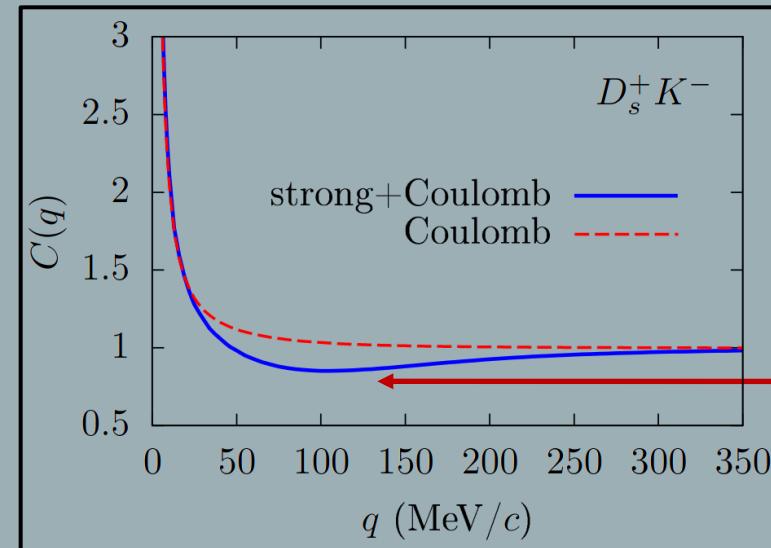
ALICE collaboration  
2401.13541

JMT-R, Ramos, Tolos,  
PRD 108, 096008 (2023)

**TROY** framework  
“T-matrix-based Routine  
for Hadron Femtoscopy”

# $D_s$ and $D^*$ meson correlation functions

One should look also  
at  $D_s^+ K^-$  channel

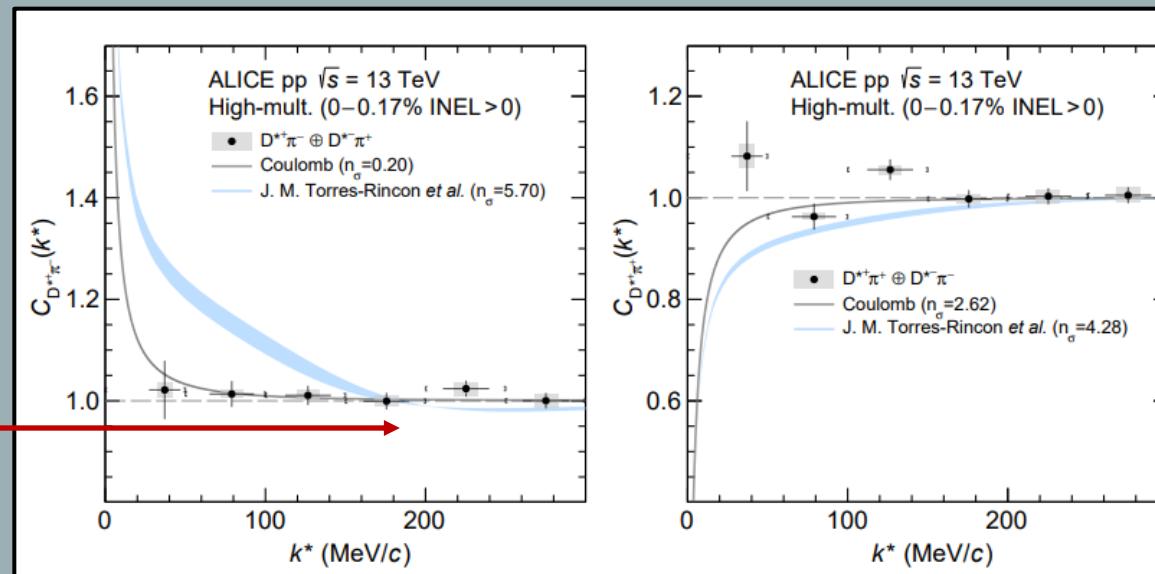


JMT-R, Ramos, Tolos,  
PRD 108, 096008 (2023)

Higher pole of  
 $D_0^*(2300)$  makes  
depletion around  
 $q=100$  MeV/c

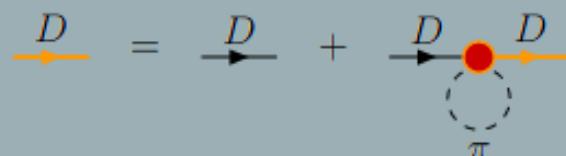
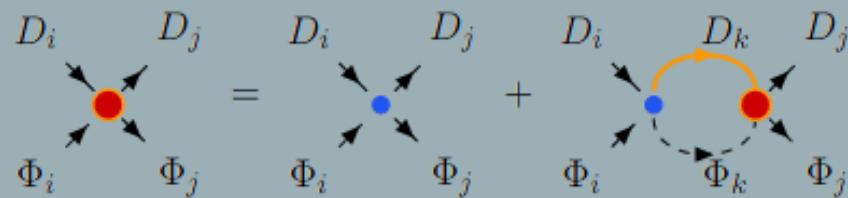
Similar situation for heavy-  
flavor partners due to HQSS

Lower pole  
of  $D_1^*(2460)$   
makes depletion for  
 $q=250$  MeV/c



ALICE collaboration  
2401.13541

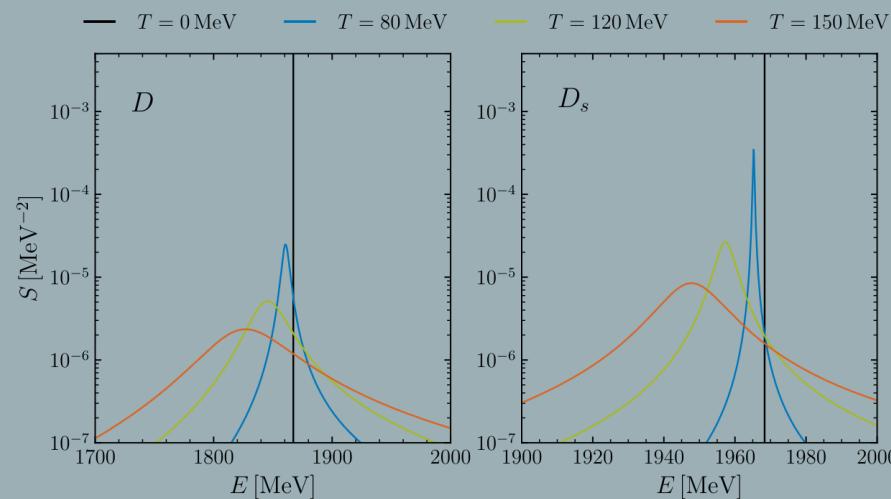
# Charm at finite temperature



$$S_D(E, \mathbf{q}) = -\frac{1}{\pi} \text{Im} \left( \frac{1}{E^2 - \mathbf{q}^2 - m_0^2 - \Pi_D(E, \mathbf{q})} \right)$$

## D & $D_s$ spectral functions

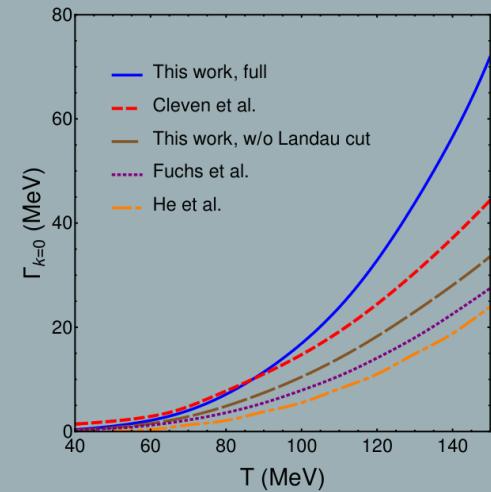
Montaña et al. (JMT-R),  
PLB 806 (2020) 135464  
&  
PRD 102 (2020) 096020



## D meson at finite temperature

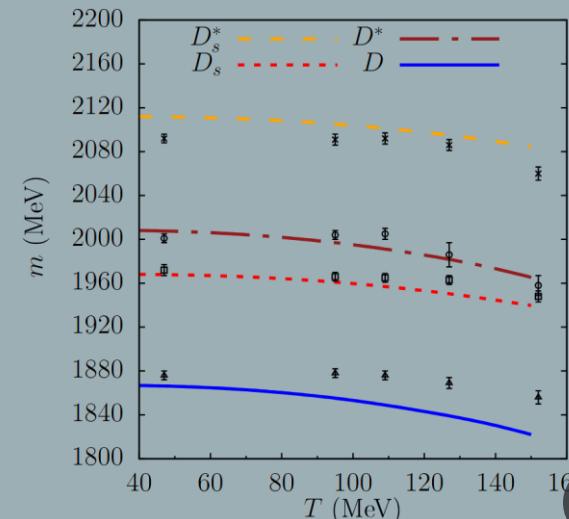
- Fuchs et al. PRC73,035204, (2006)  
He, Fries, Rapp, PLB701, 445 (2011)  
Ghosh, Mitra, Sarkar, NPA917:71 (2013)  
Cleven et al. PRC96, 045201 (2017)  
JMT-R et al. PRC105, 025203 (2022)

## D-meson thermal width

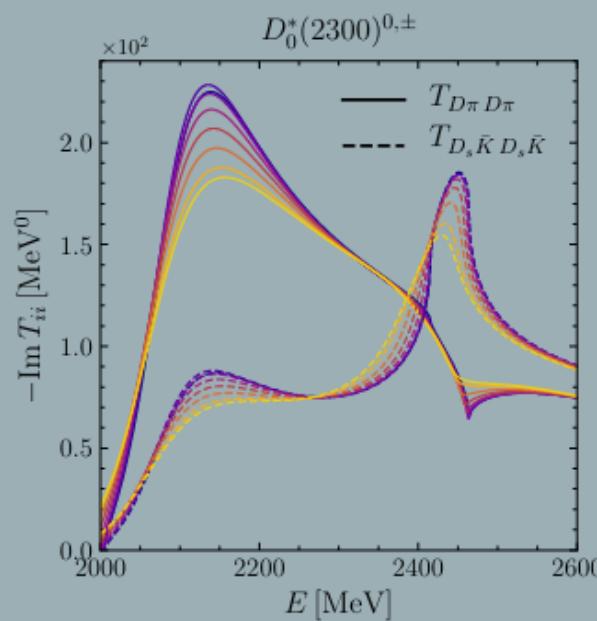


## Open charm meson masses

Lattice QCD data:  
Aarts et al. 2209.14681  
 $m_\pi = 239(1)$  MeV

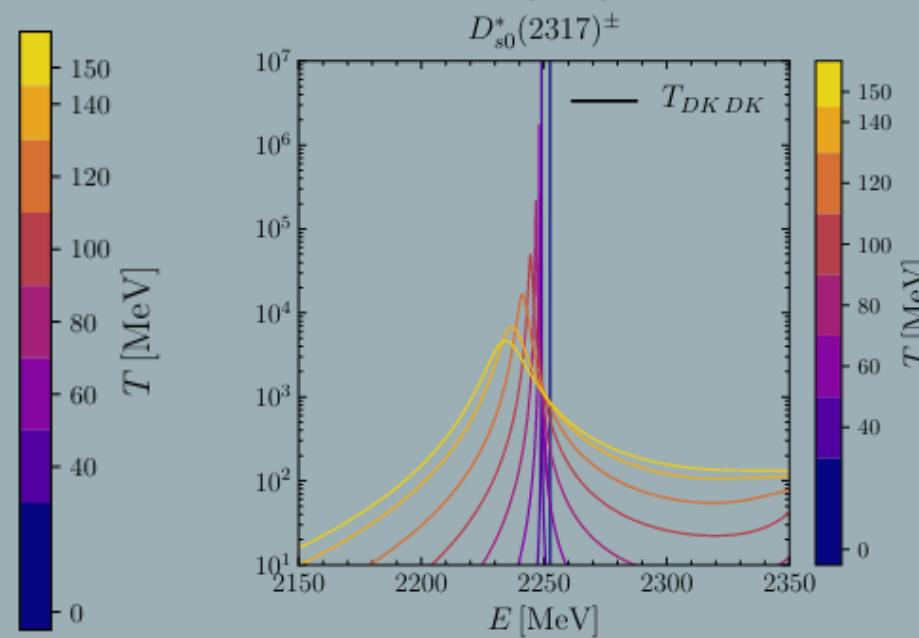


# Thermal evolution of charm molecular states

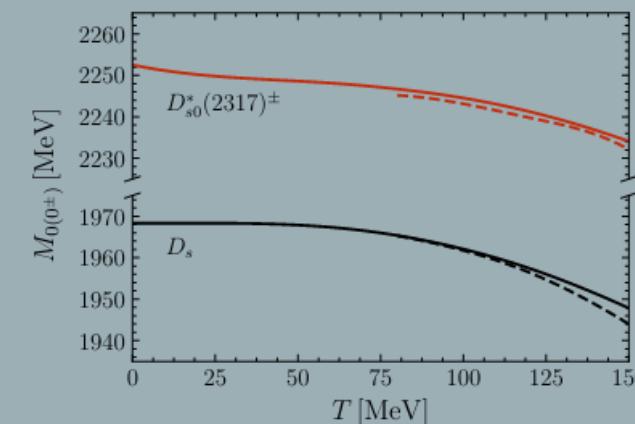
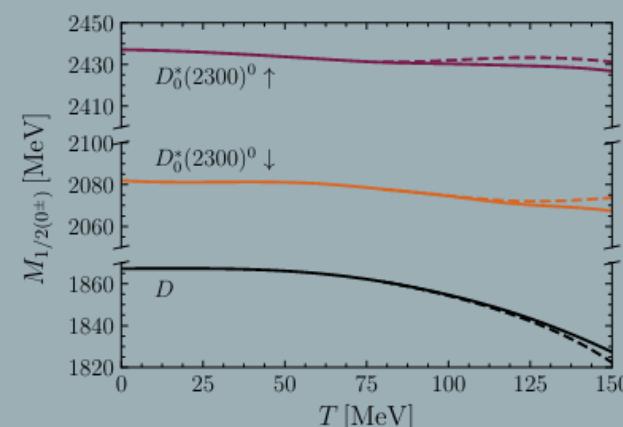
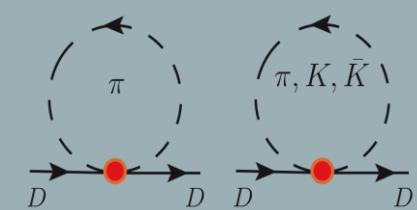


2 poles of **D<sub>0</sub>\***(2300) state  
Weak dependence on temperature

Montaña et al. (JMT-R),  
PLB 806 (2020) 135464  
&  
PRD 102 (2020) 096020



**D<sub>s0</sub>\***(2317)  
Acquires thermal  
broadening for typical  
freeze-out temperatures

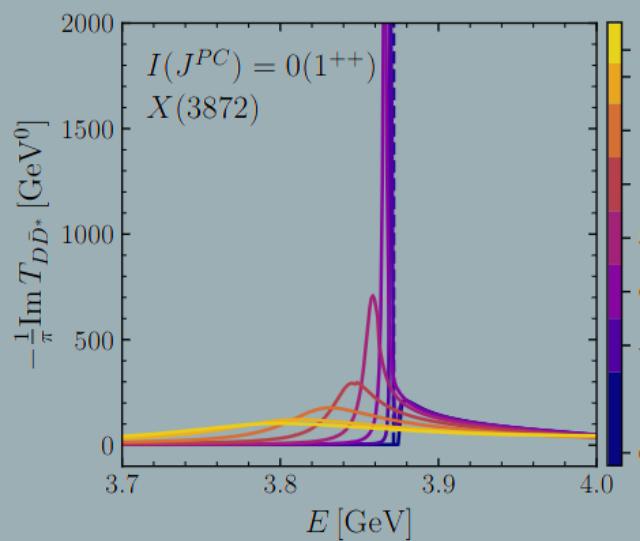
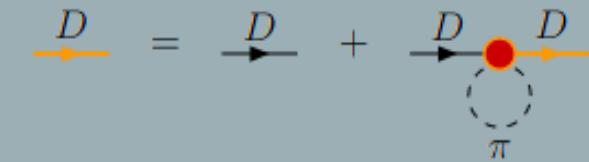


# X(3872): In-medium exotics

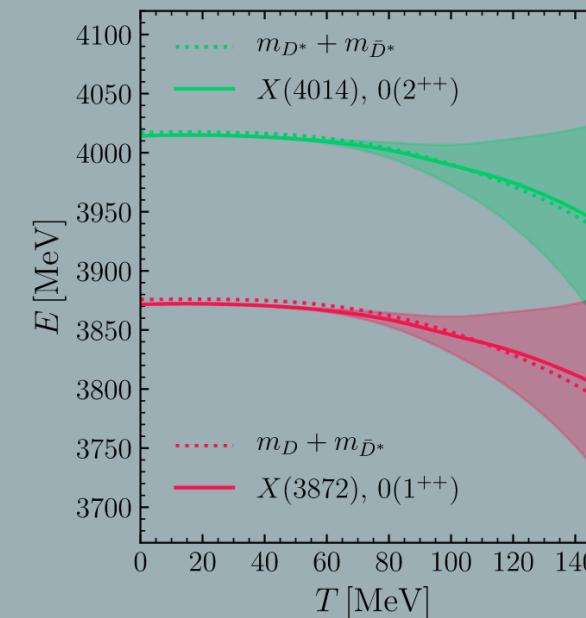
$$G(E, \mathbf{P}; T) = \int \frac{d^3 q}{(2\pi)^3} \int d\omega \int d\omega' \frac{S_1(\omega, \mathbf{q}; T) S_2(\omega', \mathbf{P} - \mathbf{q}; T)}{E - \omega - \omega' + i\epsilon} [1 + f(\omega; T) + f(\omega'; T)]$$

$$T(s) = \frac{1}{1 - V(s)G(s)}V(s)$$

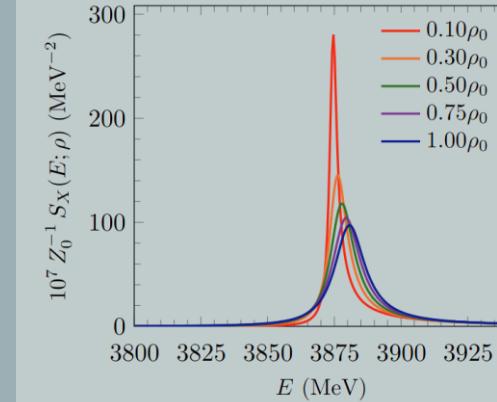
X(3872), X(4014) as molecules **melt down** around T=110 MeV  
 Modified thermal production at freeze out in RHICs?



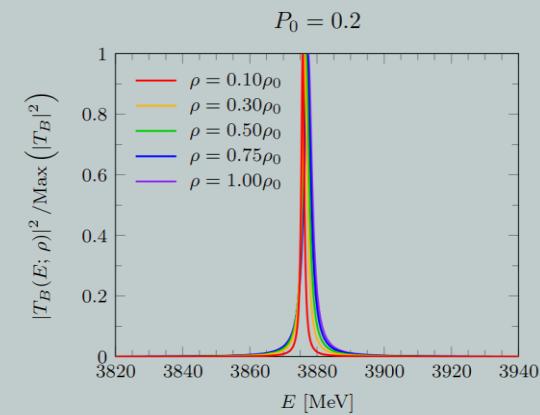
Montaña et al. (JMT-R), PRD 107, 054014 (2023)



X(3872) and  $T_{cc}(3875)^+$  also in dense medium



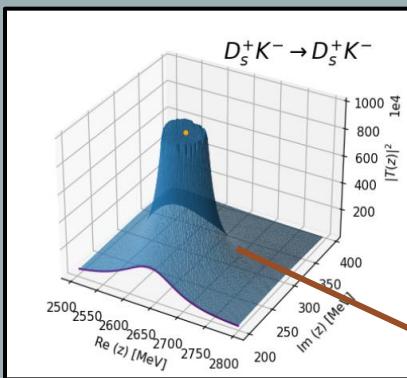
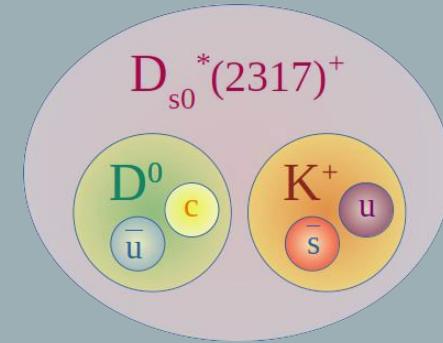
Albaladejo, Nieves, Tolos,  
 PRC 104 (2021) 3, 035203



Montesinos et al.,  
 PRC 108 (2023) 3, 035205

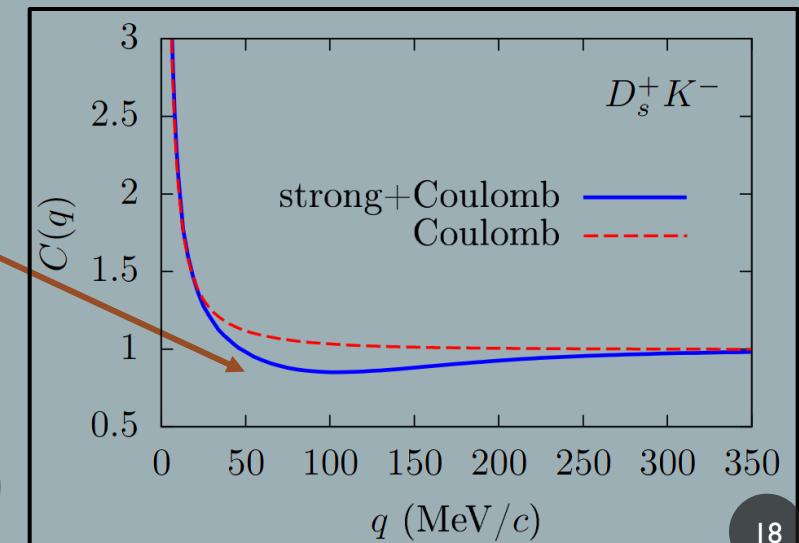
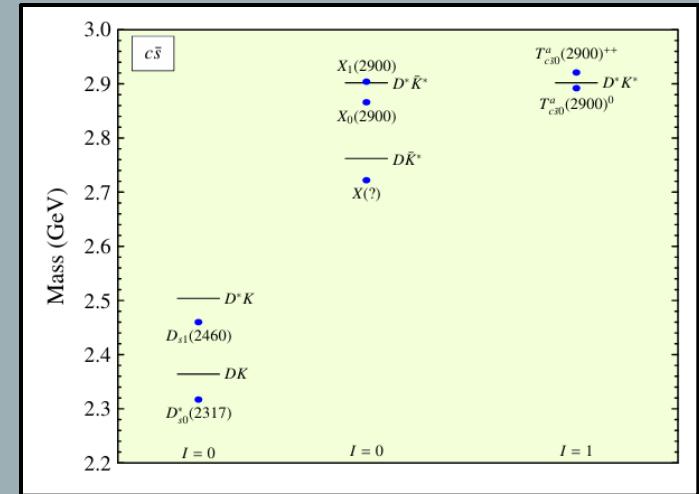
# Summary

1. Molecular state is a genuine interpretation for many of the seen charm exotic states
2. **Natural option for close-to-threshold states (weakly bound)**
3. Useful information from heavy-ion physics.  
**Femtoscopy correlation functions can help to identify resonant states**
4. Finite-temperature broadening can affect production and decay products in RHICs



JMT-R, Ramos, Tolos,  
PRD 108, 096008 (2023)

Liu et al., arXiv:2404.06399





# MOLECULAR STATES WITH CHARM: INSIGHTS FROM VACUUM & FINITE- TEMPERATURE ANALYSES



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Forschungsgemeinschaft



SQM 2024  
The 21<sup>st</sup> International Conference on Strangeness in Quark Matter  
3-7 June 2024, Strasbourg, France