

# Low Seesaw Scale Solution for $M_W$ and $(g - 2)_\mu$

by **Arturo de Giorgi (Madrid, IFT)**

based on **2211.03797** - *Fortschritte der Physik* (2023)

in collaboration with **L. Merlo (Madrid, IFT)**, **S. Pokorski (Warsaw U.)**



Contribution to: *57th Rencontres de Moriond 2023 - Electroweak Interactions & Unified Theories*

March 23, 2023



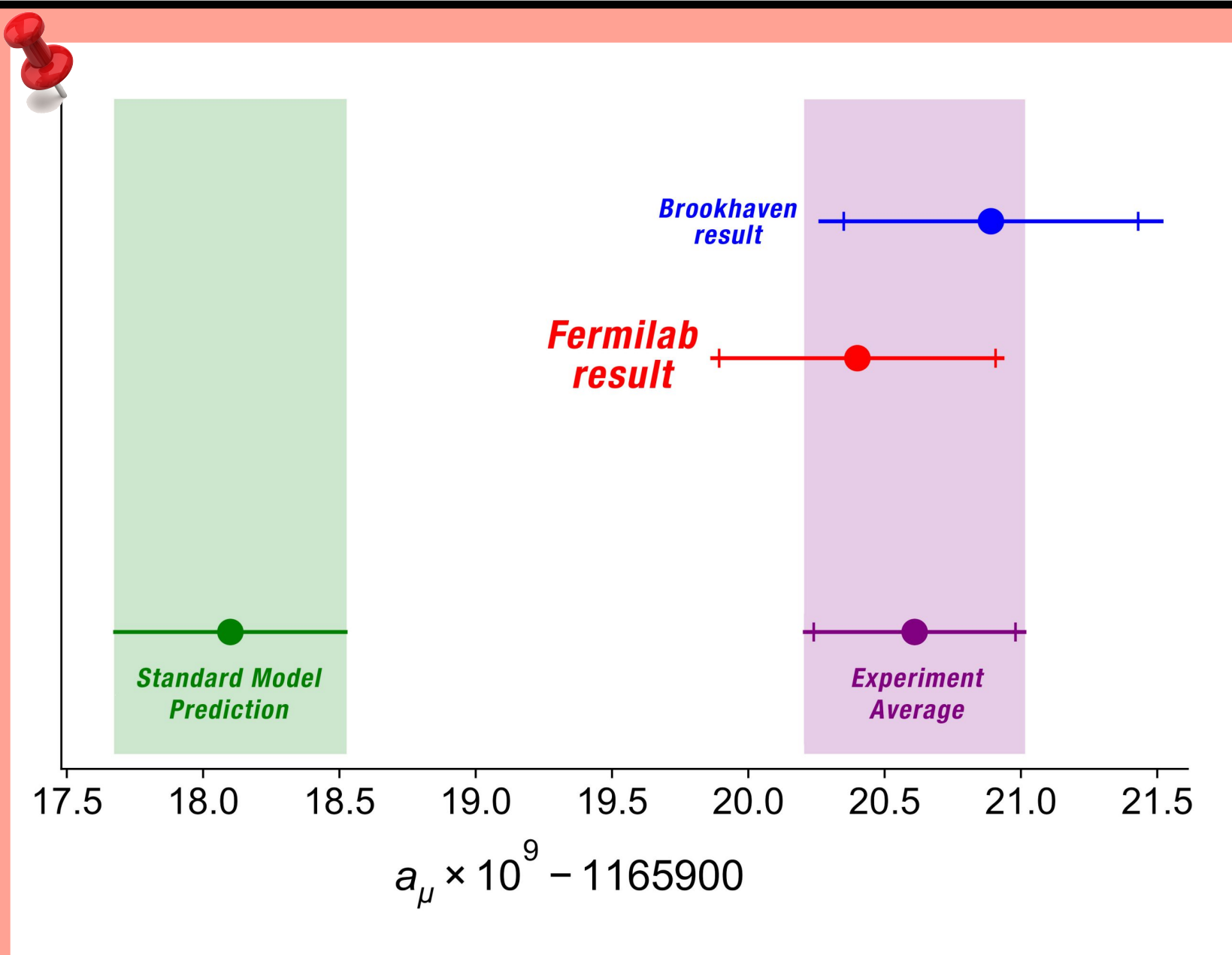
# Some Experimental Inputs

## $\nu$ -Masses

	NO	IO
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.41^{+0.21}_{-0.20}$	$7.41^{+0.21}_{-0.20}$
$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.507^{+0.026}_{-0.027}$	$-2.486^{+0.025}_{-0.028}$

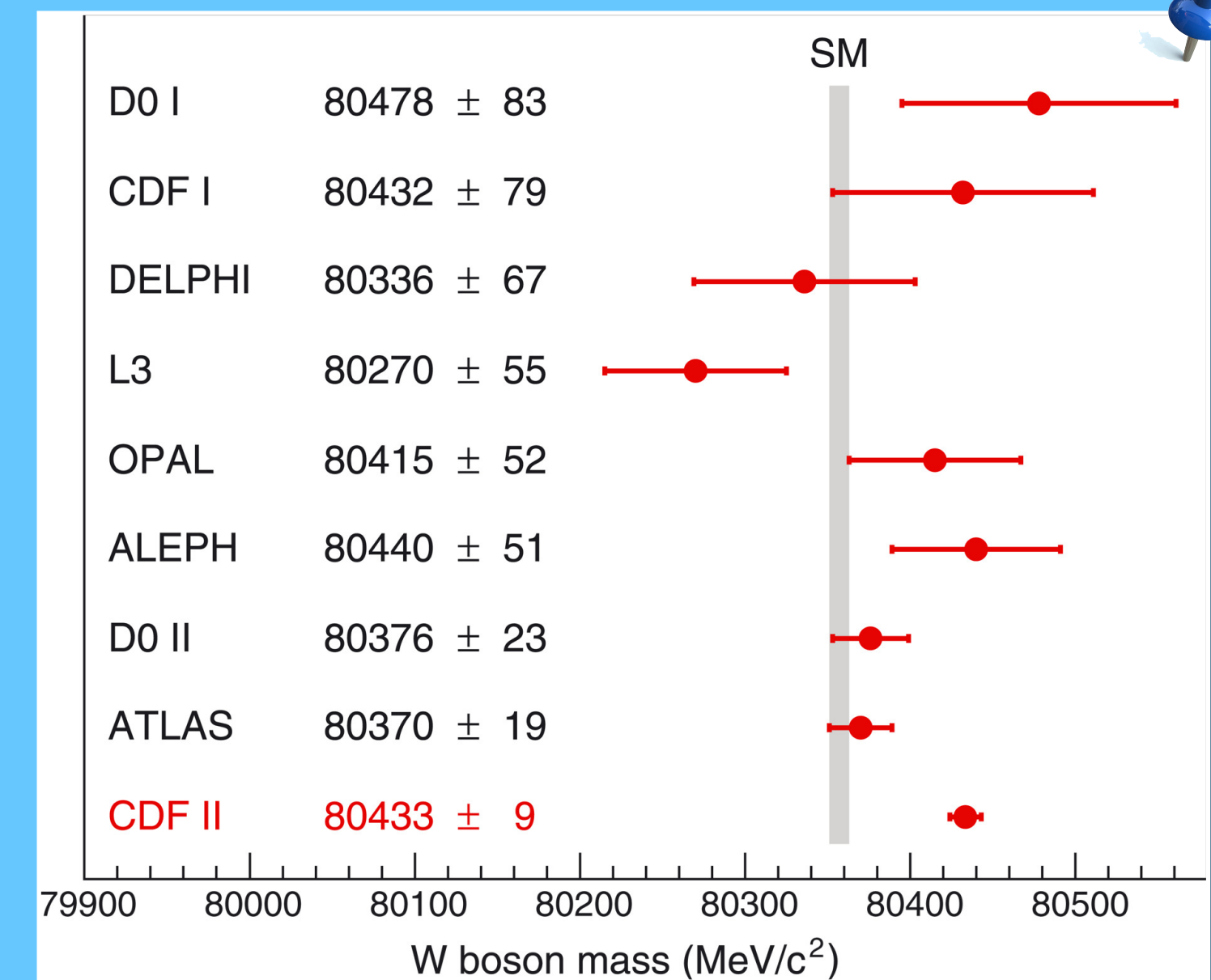
$\nu$ Fit Collaboration [2007.14792]

## $(g - 2)_\mu$



Muon  $g - 2$  Collaboration, Phys. Rev. Lett. 126 (2021)

## $M_W$



CDF Collaboration, Science 376 (2022), no. 6589 170–176.

# Some Experimental Inputs

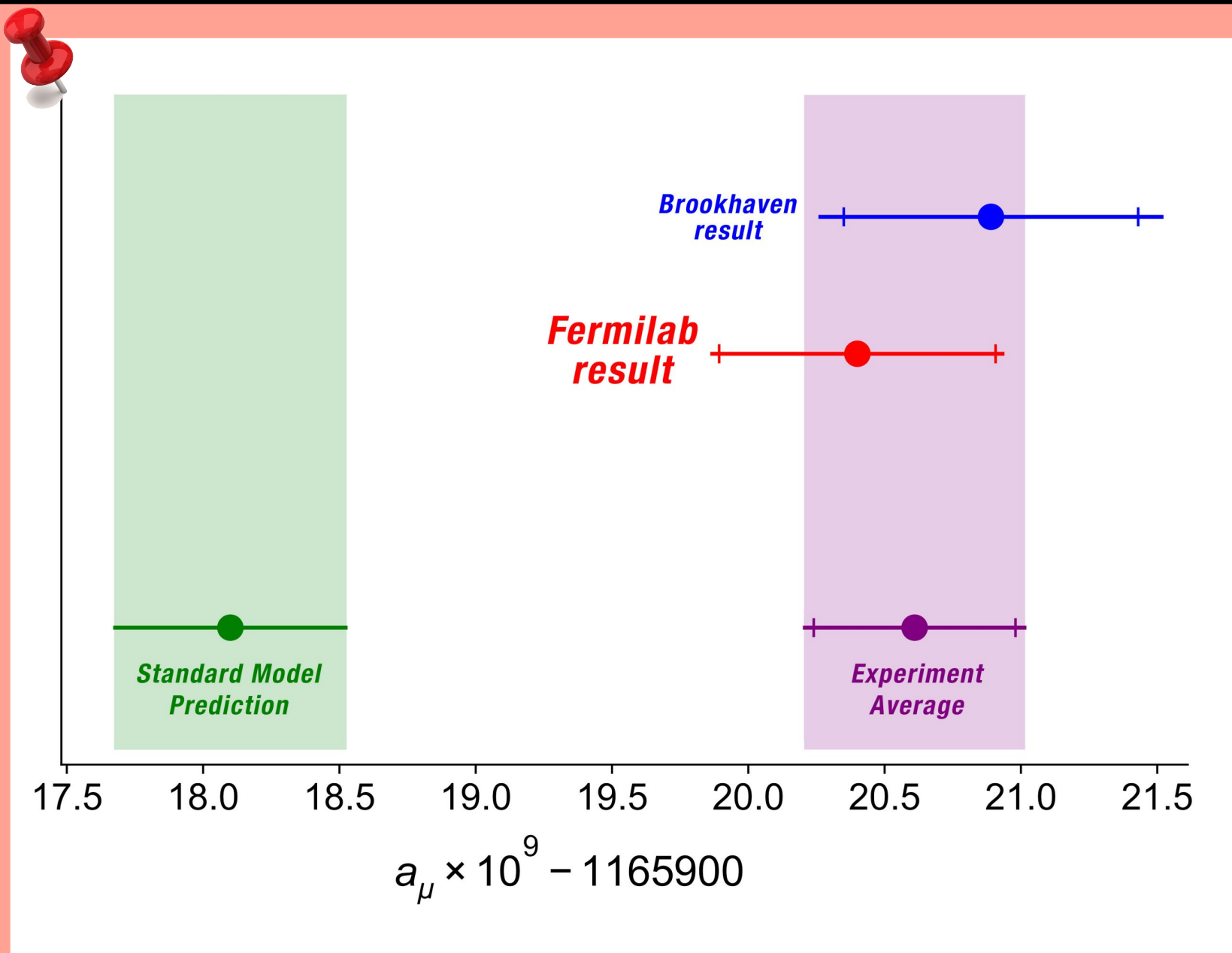
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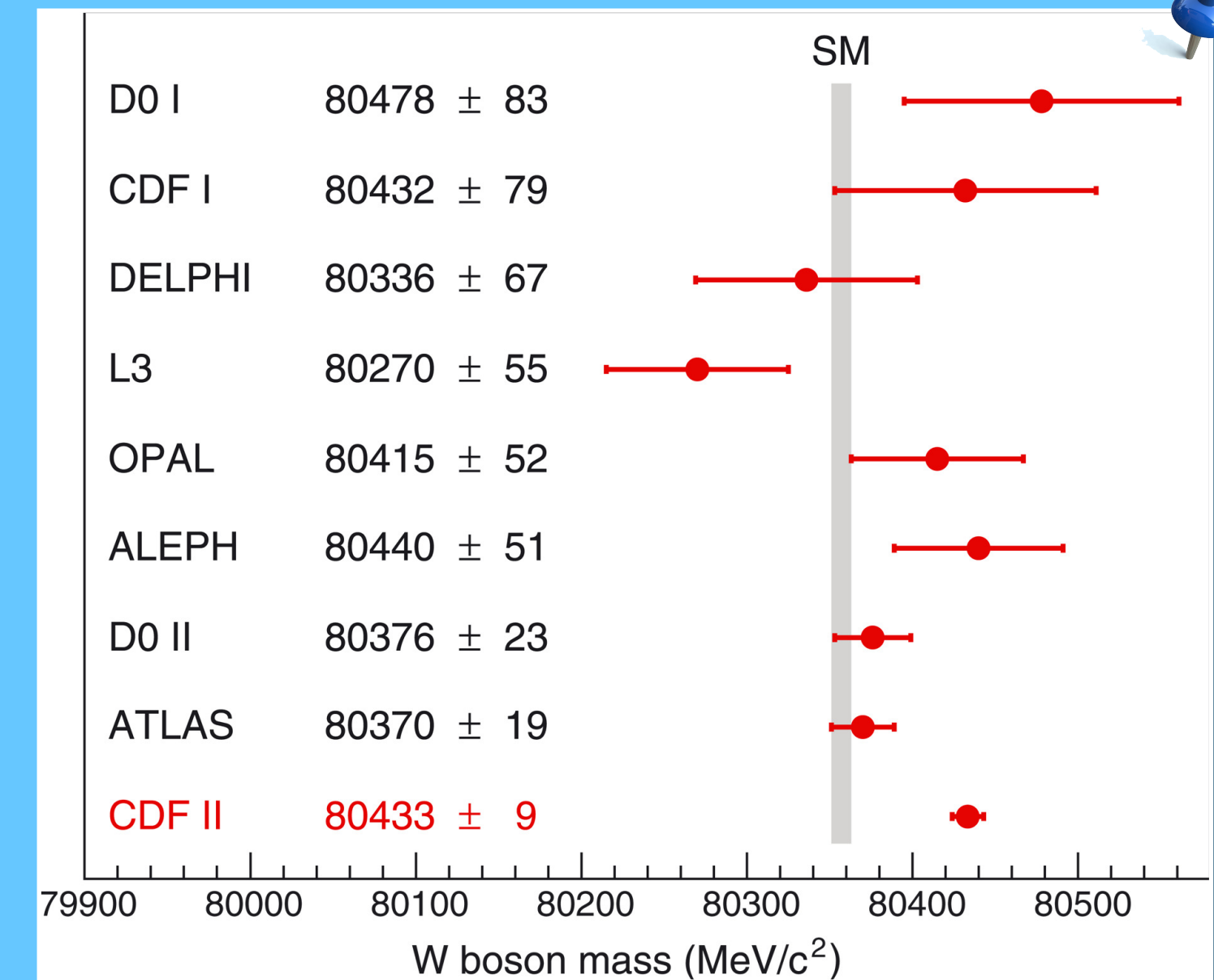
## NP in the Leptonic Sector?

### $(g - 2)_\mu$



Muon  $g - 2$  Collaboration, Phys. Rev. Lett. 126 (2021)

### $M_W$



CDF Collaboration, Science 376 (2022), no. 6589 170–176.

# A Minimal Extension

K. Kannike et al., JHEP 02 (2012) 106. [Erratum: JHEP 10, 136 (2012)].  
 R. Dermisek and A. Raval, Phys. Rev. D 88 (2013) 013017.  
 G. Arcadi et al., Phys. Rev. Lett. 127 (2021), no. 6 061802.  
 C.-T. Lu et al., JHEP 08 (2021) 073.  
 G. Guedes and P. Olgoso, JHEP 09 (2022) 181.

- **Only** sterile neutrinos?
  - $m_\nu$ ?
  - $M_W$ ?
  - $(g - 2)_\mu$ ?

$$\left(\frac{\delta a_\mu}{10^{-9}}\right) \sim \frac{1}{16\pi^2} |\Theta_{\mu N}|^2 G_F m_\mu^2 \sim \mathcal{O}(1) |\Theta_{\mu N}|^2$$

	$SU(2)_L$	$U(1)_Y$	$U(1)_L$
$\ell_L$	<b>2</b>	-1/2	1
$\mu_R$	1	1	1
$H$	<b>2</b>	+1/2	0
$N_R$	1	1	1
$S_R$	1	1	-1
$\psi_L$	<b>2</b>	-1/2	1
$\psi_R$	<b>2</b>	-1/2	1

**Minimal**  
extension in the  
leptonic sector?



**2 Vector-Like  
Leptons**  
coupling to  $\mu$

# Low Scale Seesaws

D. Wyler and L. Wolfenstein, Nucl. Phys. B 218 (1983) 205–214.  
 R. N. Mohapatra and J. W. F. Valle, Phys. Rev. D 34 (1986) 1642.  
 J. Bernabeu et al., Phys. Lett. B 187 (1987) 303–308.  
 M. Malinsky et al., Phys. Rev. Lett. 95 (2005) 161801.

Small Symmetry Breaking Parameters

$$\begin{aligned}
 -\mathcal{L}_Y = & \bar{\ell}_L H Y_\mu \mu_R + \bar{\ell}_L \tilde{H} Y_N N_R + \epsilon \bar{\ell}_L \tilde{H} Y_S S_R + \frac{1}{2} \mu' \bar{N}_R^c N_R + \frac{1}{2} \mu \bar{S}_R^c S_R + \Lambda \bar{N}_R^c S_R + \\
 & + Y_R \bar{\psi}_L H \mu_R + Y_V \bar{S}_R^c \tilde{H}^\dagger \psi_R + Y'_V \bar{\psi}_L \tilde{H} N_R + M_\psi \bar{\psi}_L \psi_R + M_L \bar{\ell}_L \psi_R + \text{h.c.},
 \end{aligned}$$

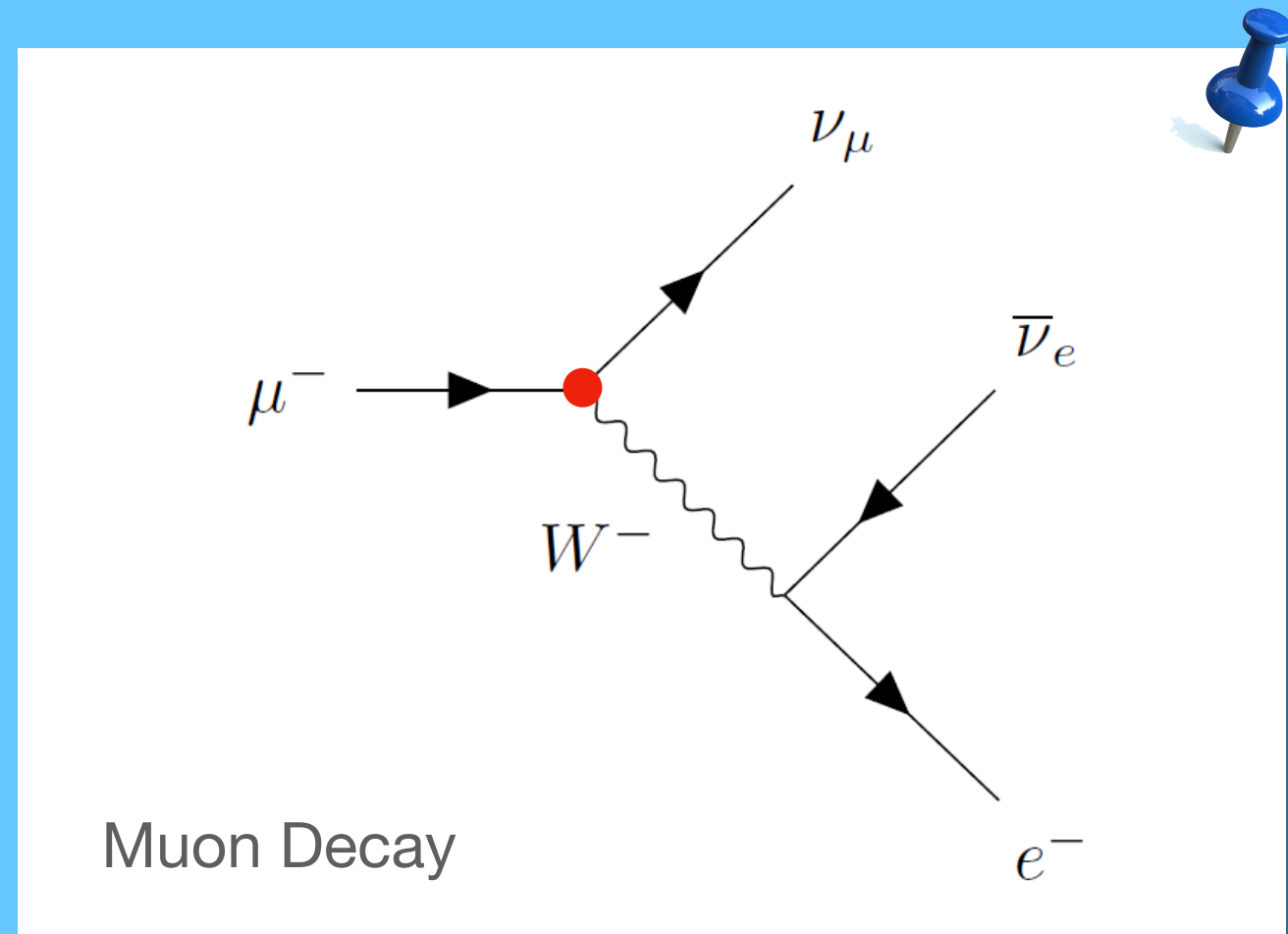
$$\chi \equiv (\nu_L, N_R^c, S_R^c, \psi_L^0, \psi_R^{0c})^T$$

$$-\mathcal{L}_Y \supset \frac{1}{2} \bar{\chi} \mathcal{M}_\chi \chi^c$$

$$\mathcal{M}_\chi = \begin{pmatrix} 0 & m_N & \epsilon m_S & 0 & M_L \\ m_N & 0 & \Lambda & m_{V'} & 0 \\ \epsilon m_S & \Lambda & \mu & 0 & m_V \\ 0 & m_{V'} & 0 & 0 & M_\psi \\ M_L & 0 & m_V & M_\psi & 0 \end{pmatrix}$$

$$m_\nu \simeq \frac{v^2}{2} \left[ \left( Y_N \frac{1}{\Lambda^T} \mu \frac{1}{\Lambda} Y_N^T \right) - \epsilon \left( Y_S \frac{1}{\Lambda} Y_N^T + Y_N \frac{1}{\Lambda^T} Y_S^T \right) \right] \quad \checkmark$$

$$M_W$$



$$G_F = G_\mu(1 + \Delta_G)$$

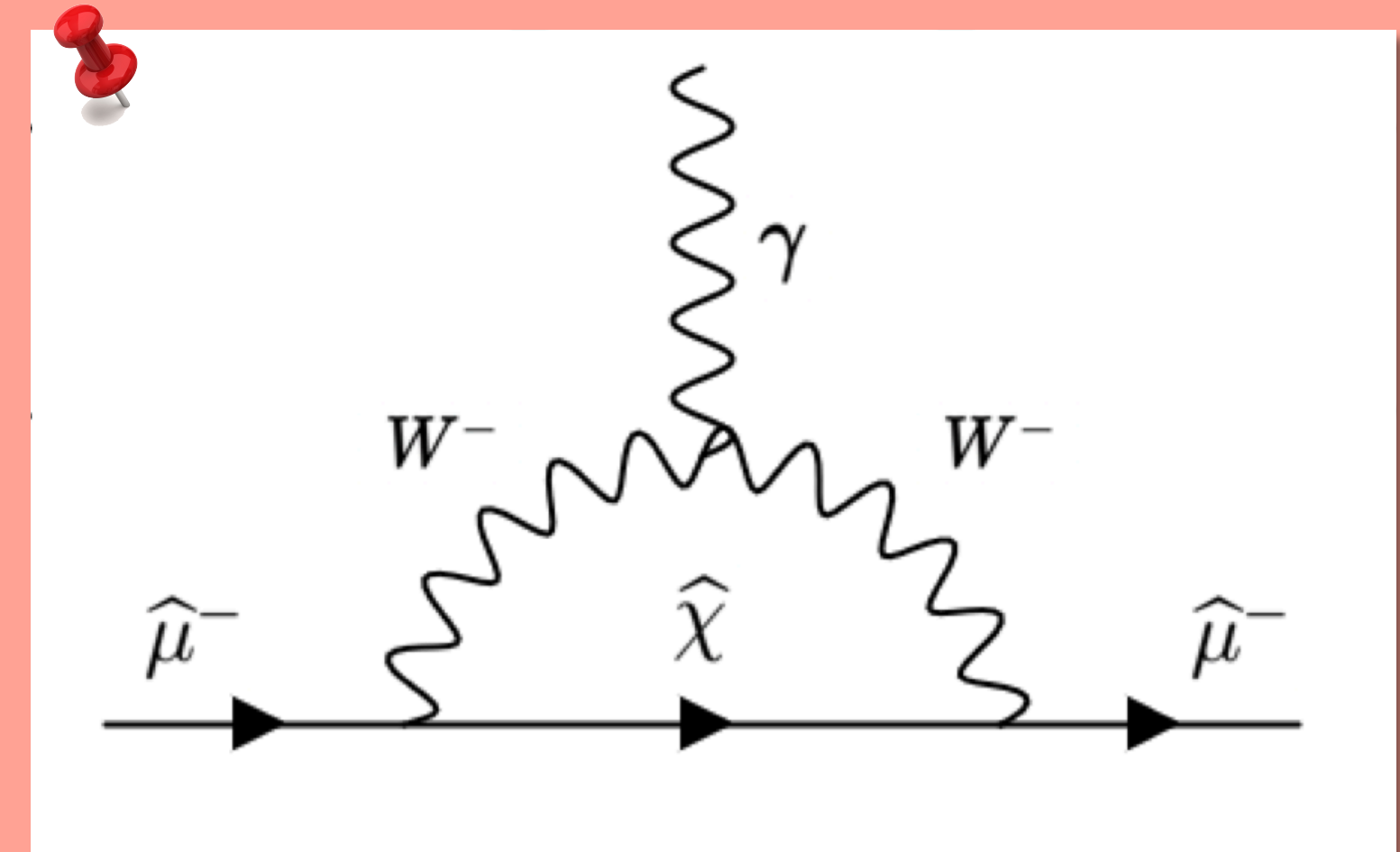
$$M_W = M_Z \sqrt{\frac{1}{2} + \sqrt{\frac{1}{4} - \frac{\pi \alpha (1 - \Delta_G)}{\sqrt{2} G_\mu M_Z^2 (1 - \Delta_r)}}}$$

$$\Delta_G \sim 5 \times 10^{-3}$$



M. Blennow et al., Phys. Rev. D 106 (2022), no. 7 073005.  
F. Arias-Aragon et al., JHEP 09 (2022) 210.

$$(g - 2)_\mu$$



What to expect? 

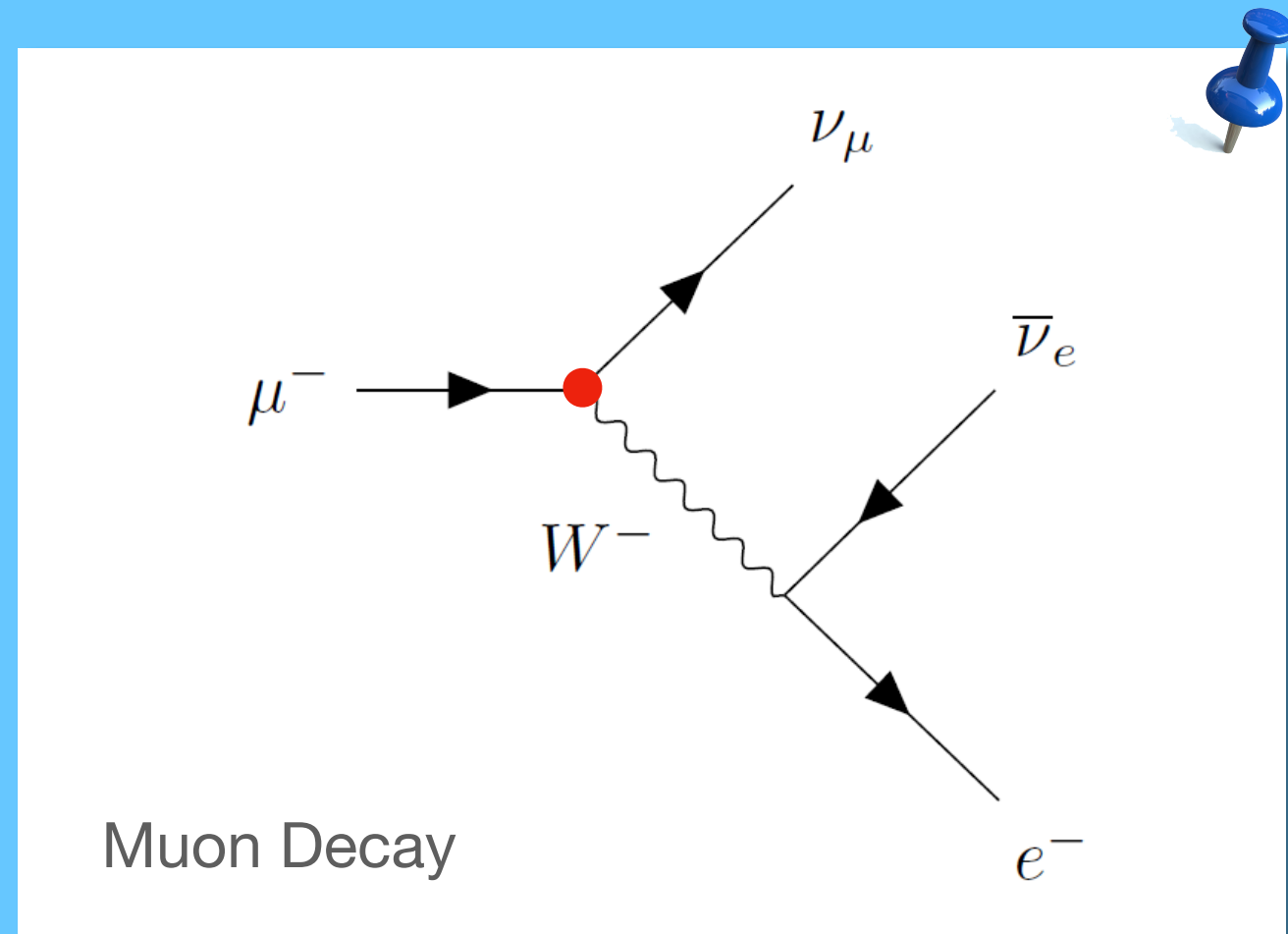
$$\delta a_\mu \sim \frac{Y_i^3}{16\pi^2} \frac{m_\mu}{v} \left[ \mathcal{O}\left(\frac{v^2}{M_\psi \Lambda}\right) + \mathcal{O}\left(\frac{v^2}{M_\psi \Lambda}\right)^2 \right]$$

$$M_\psi, \Lambda \sim \mathcal{O}(10) \text{ TeV}$$

$$M_\psi, \Lambda \sim \mathcal{O}(1) \text{ TeV}$$

N. Arkani-Hamed and K. Harigaya, JHEP 09 (2021) 025.  
N. Craig et al., JHEP 05 (2022) 079.  
L. Delle Rose et al., JHEP 05 (2022) 120.

$$M_W$$



$$G_F = G_\mu(1 + \Delta_G)$$

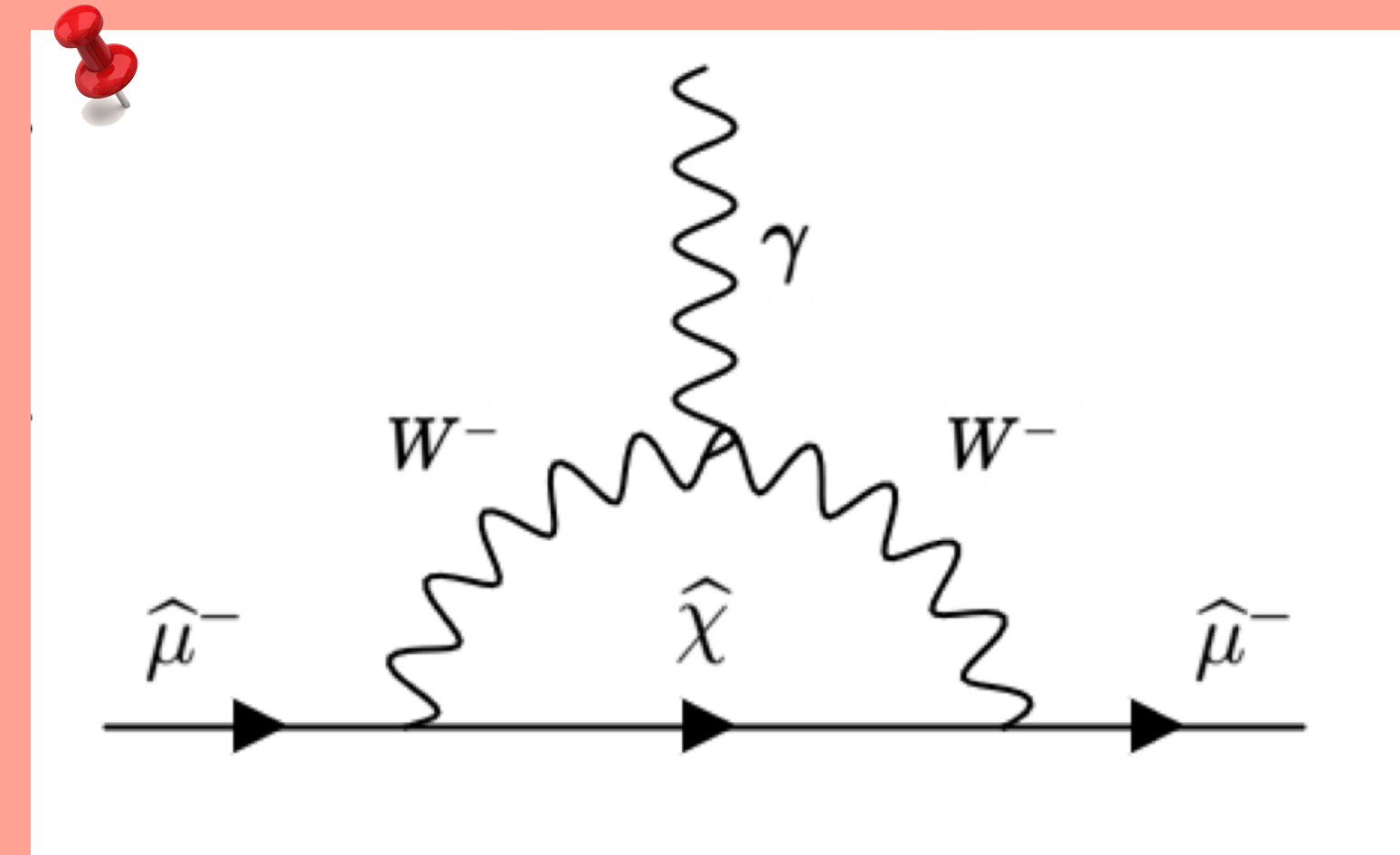
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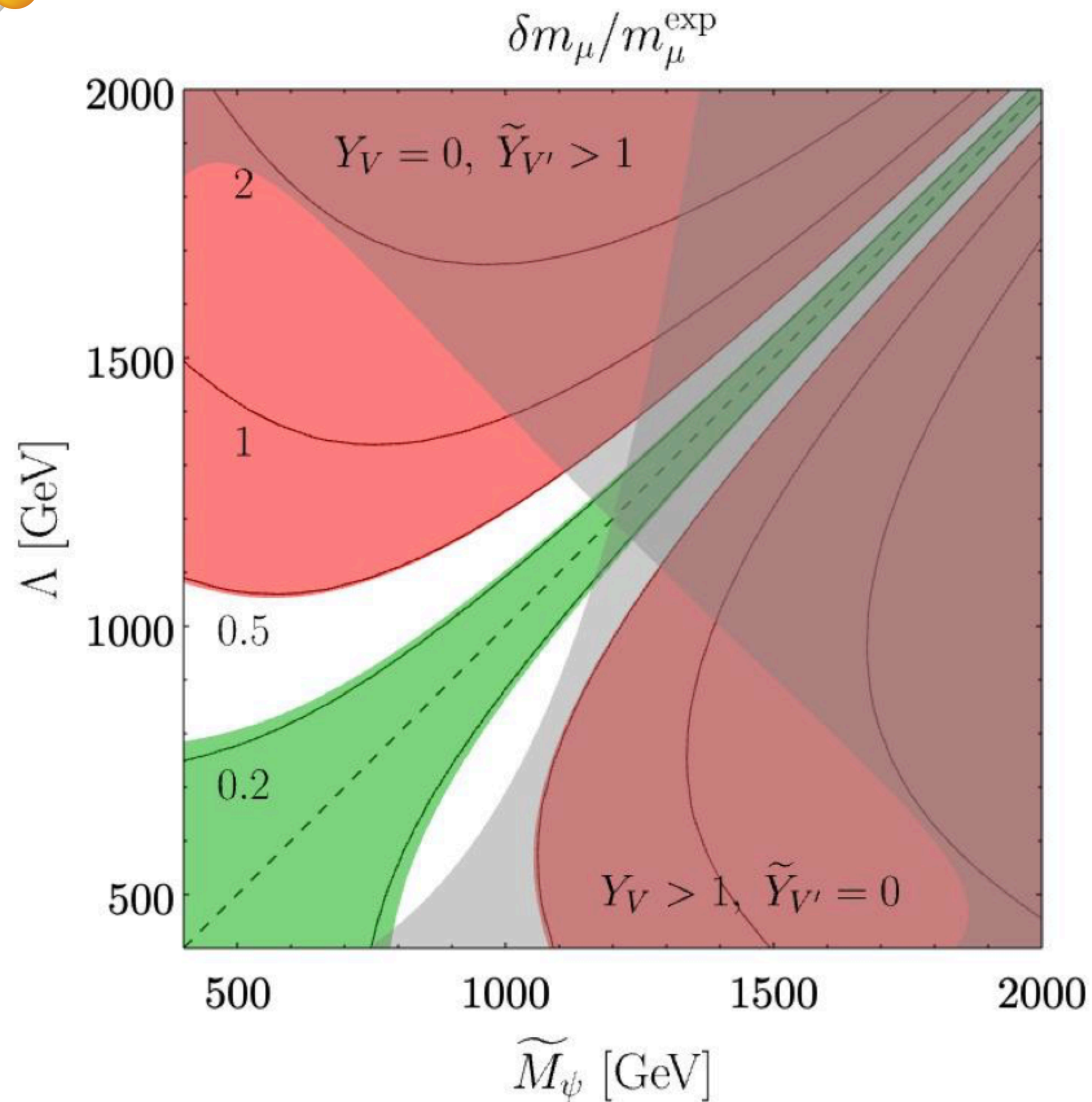
What to expect? 

$$\delta a_\mu \sim \frac{Y_i^3}{16\pi^2} \frac{m_\mu}{v} \left[ \mathcal{O}\left(\frac{v^2}{\Lambda}\right) + \mathcal{O}\left(\frac{v^2}{M_\psi \Lambda}\right)^2 \right]$$

$$M_\psi, \Lambda \sim \cancel{\mathcal{O}(10)} \text{ TeV} \quad M_\psi, \Lambda \sim \mathcal{O}(1) \text{ TeV}$$

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# Conclusions



- New particles:

	$SU(2)_L$	$U(1)_Y$	$U(1)_L$
$N_R$	1	1	1
$S_R$	1	1	-1
$\psi_L$	<b>2</b>	-1/2	1
$\psi_R$	<b>2</b>	-1/2	1

## 2 Vector-Like Leptons

- Possible **simultaneous** explanation of  $m_\nu$ ,  $(g - 2)_\mu$  and  $M_W$
- NP at  $\sim \mathcal{O}(1)$  TeV, or even lower!
- Very rich phenomenology



**Thank you!**