



Closing the window on WIMP Dark Matter

Dario Buttazzo

2107.09688, 2205.04486 in collaboration with
Bottaro, Costa, Franceschini, Panci, Redigolo, Vittorio



57th Rencontres de Moriond, EW session – La Thuile, 22.3.2023

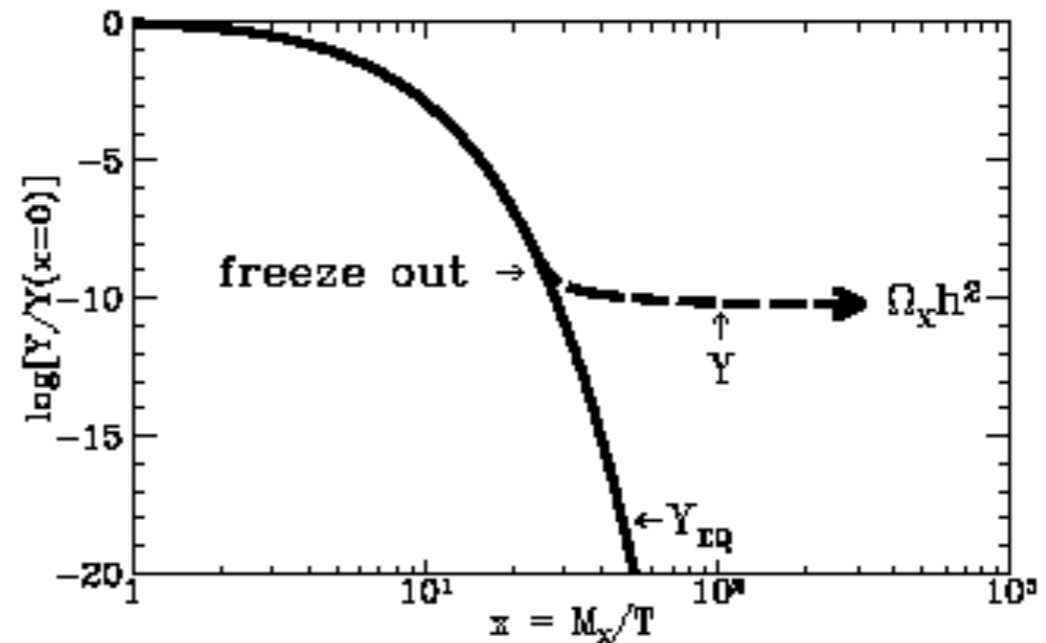
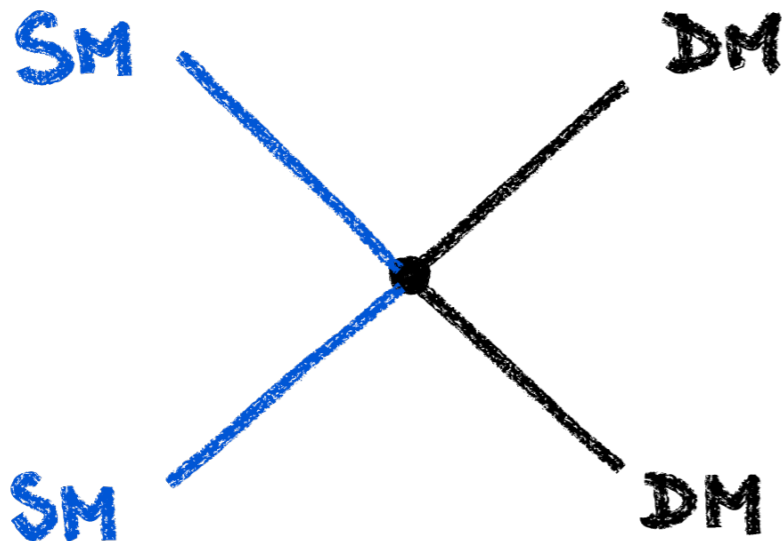
“Physicist searching for heavy WIMP Dark Matter on the mountains near La Thuile”
according to StableDiffusion AI

thanks to C. Cesarotti for the idea!



The case for WIMPs

- Production in early Universe: thermal freeze-out of $2 \rightarrow 2$ scatterings



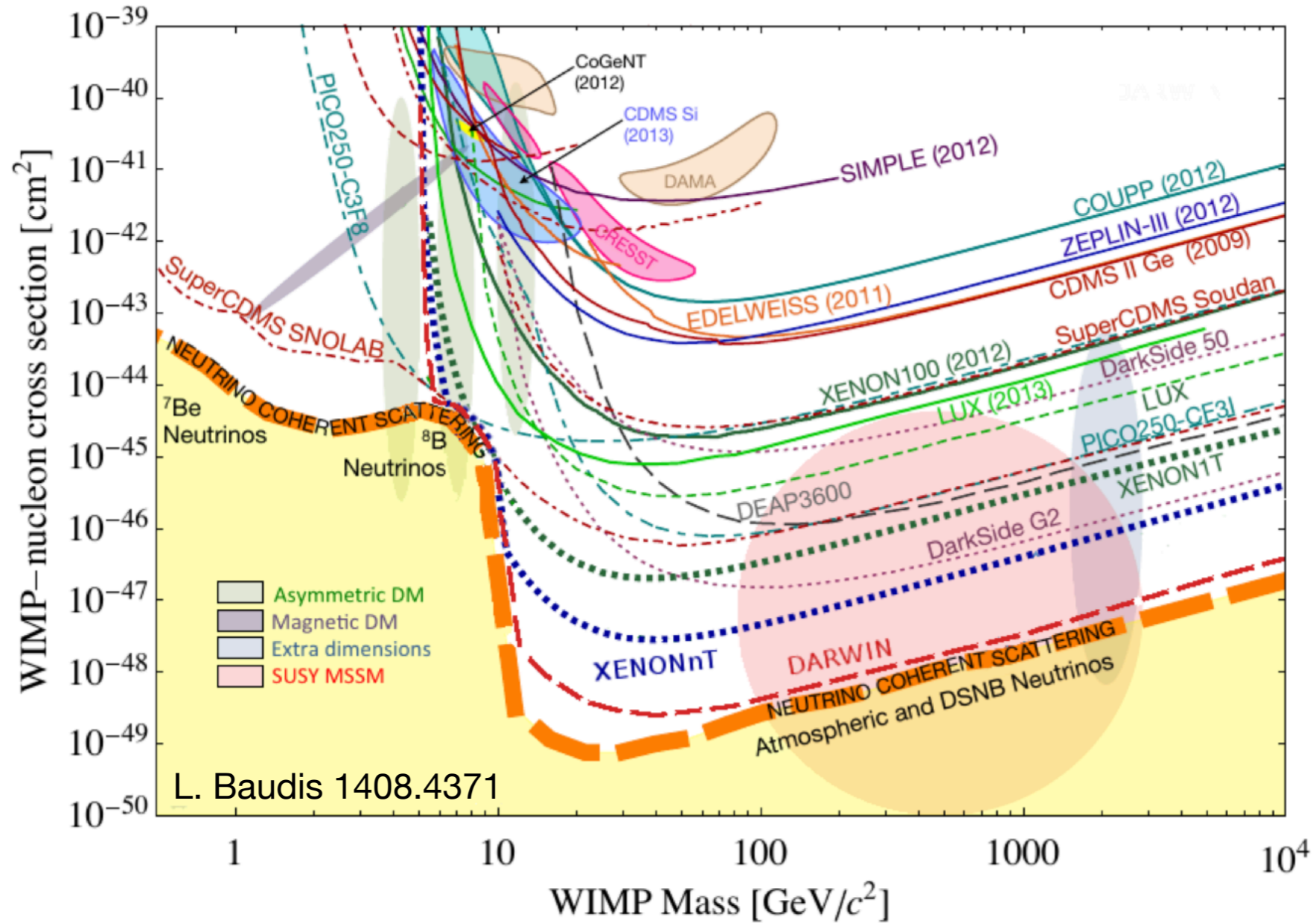
- For each value of the DM-SM coupling g_* the DM mass is predicted.

$$g_* \sim g_{EW} \Rightarrow M_{DM} \sim \text{TeV}$$

- WIMP miracle:** simple explanation for the observed Dark Matter abundance ($\Omega_{DM} \sim 0.26$) and a connection to naturalness of EW scale.

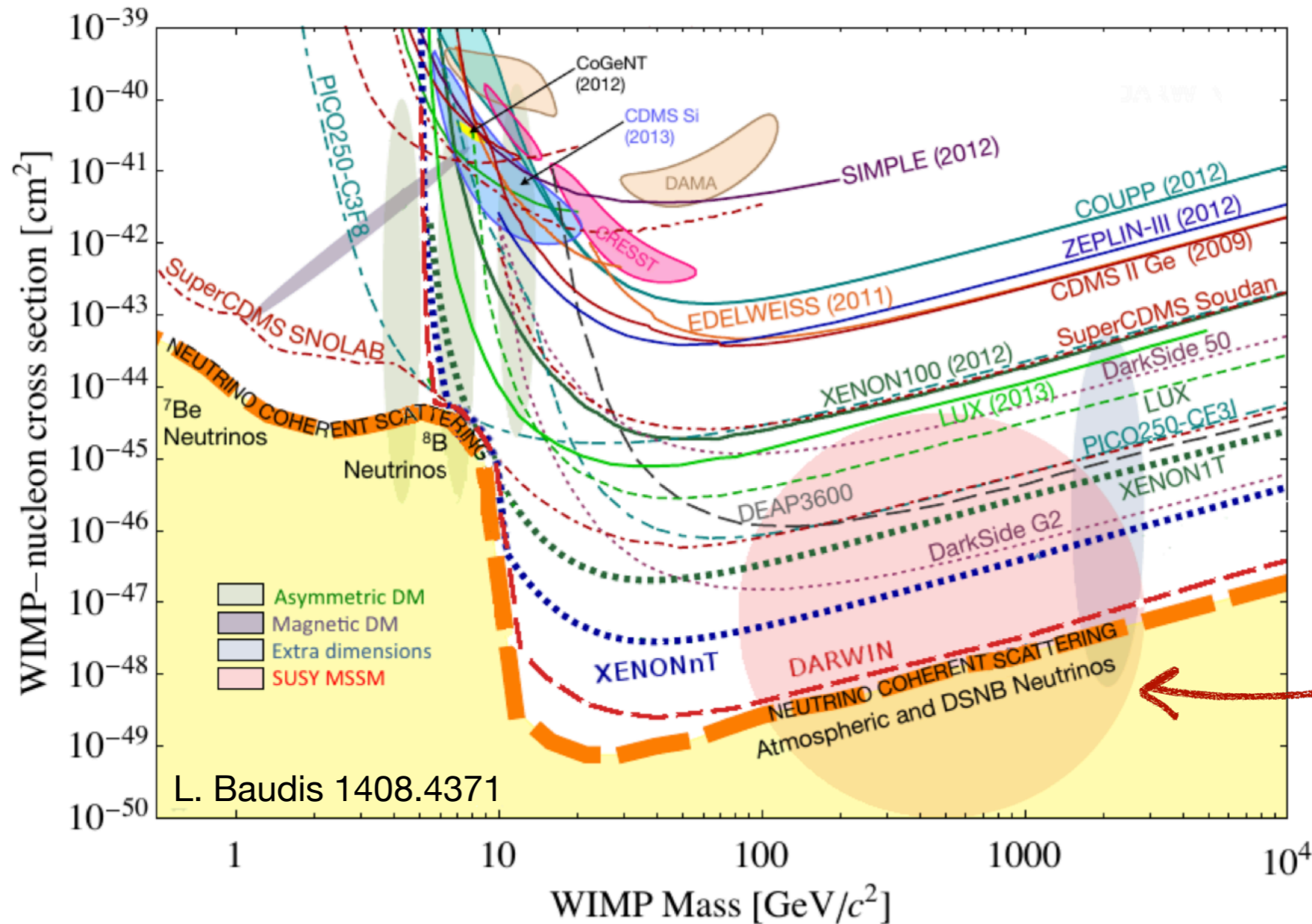
Ideal target for nuclear recoils & colliders!

Are WIMPs almost dead?



- ◆ Large fraction of the “standard” WIMP parameter space ruled out?

Are WIMPs almost dead?



WIMP param. space
in specific models
e.g. MSSM

- Large fraction of the “standard” WIMP parameter space ruled out?

Not quite yet...

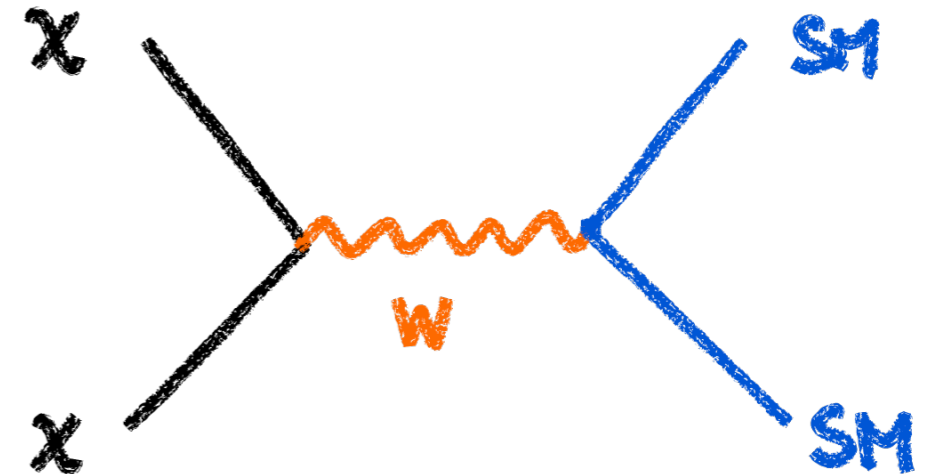
Which WIMP?

Consider generic EW multiplet: interacts w/ SM through W, Z

“Minimal Dark Matter”: Cirelli, Fornengo, Strumia 2005

- ◆ DM is the neutral component

$$\chi_n = (\dots, \chi^-, \chi^0, \chi^+, \dots)$$



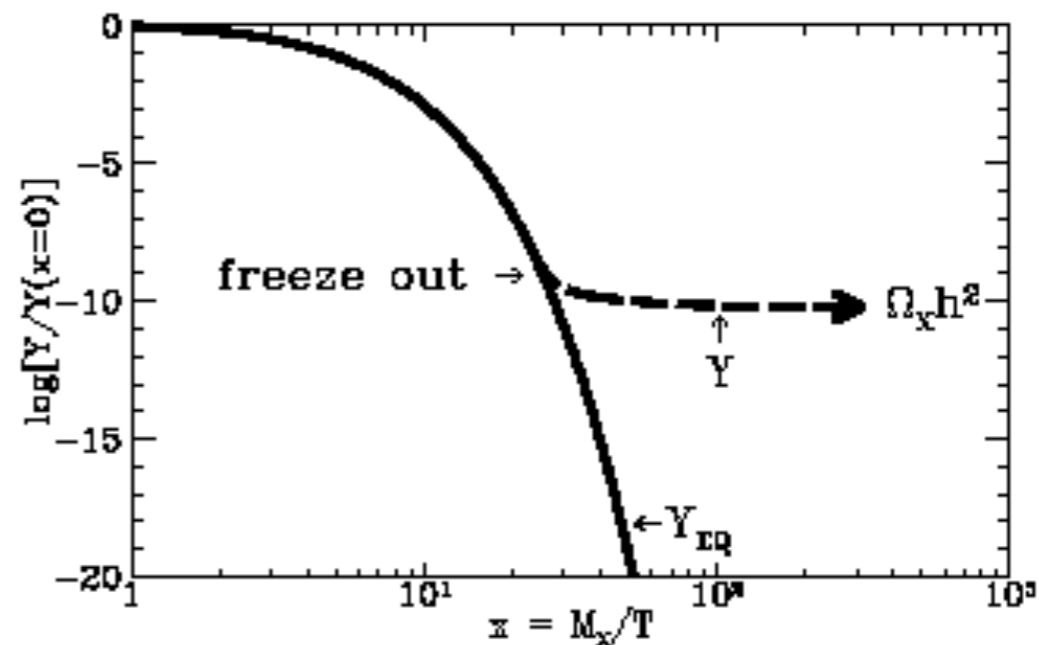
- ◆ DM needs to be stable: χ^0 lightest state
- ◆ Strong bounds from Direct Detection: no Z coupling @ tree-level
 - ▶ Real multiplet: $Y = 0$, n odd
 - ▶ Complex multiplet: $Y \neq 0$,
(mass splittings from higher-dimensional operators needed)
- ◆ Single parameter sets the DM abundance: mass M_{DM}

Which WIMP?

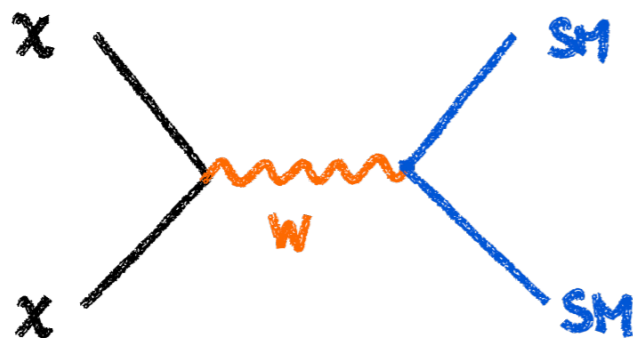
- ◆ Consider generic EW multiplet: interacts w/ SM through W, Z

$$\frac{dY}{dx} \propto \langle \sigma v \rangle (Y^2 - Y_{\text{eq}}^2)$$

which cross-section?



- ◆ Tree-level EW cross-section...

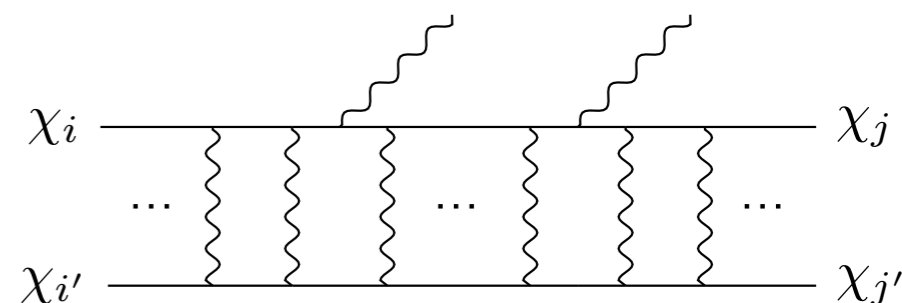


$$\langle \sigma v \rangle_0 = \frac{\pi \alpha_2^2 (2n^4 + 17n^2 - 19)}{16g_\chi M_\chi^2}$$

... is inaccurate!

Large non-perturbative, non-relativistic effects

- ▶ Sommerfeld enhancement
- ▶ Bound state formation



Bound state formation

- ◆ Coupled Boltzmann eq. for DM and bound states:

$$z \frac{dY_{\text{DM}}}{dz} = -\frac{2s}{H} \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle [Y_{\text{DM}}^2 - (Y_{\text{DM}}^{\text{eq}})^2] - \frac{2s}{Hz} \sum_{B_I} \langle \sigma_{B_I} v_{\text{rel}} \rangle \left[Y_{\text{DM}}^2 - (Y_{\text{DM}}^{\text{eq}})^2 \frac{Y_{B_I}}{Y_{B_I}^{\text{eq}}} \right],$$

$$z \frac{dY_{B_I}}{dz} = Y_{B_I}^{\text{eq}} \left\{ \frac{\langle \Gamma_{B_I, \text{break}} \rangle}{H} \left[\frac{Y_{\text{DM}}^2}{(Y_{\text{DM}}^{\text{eq}})^2} - \frac{Y_{B_I}}{Y_{B_I}^{\text{eq}}} \right] + \frac{\langle \Gamma_{B_I, \text{ann}} \rangle}{H} \left[1 - \frac{Y_{B_I}}{Y_{B_I}^{\text{eq}}} \right] + \sum_{B_J} \frac{\langle \Gamma_{B_I \rightarrow B_J} \rangle}{H} \left[\frac{Y_{B_J}}{Y_{B_J}^{\text{eq}}} - \frac{Y_{B_I}}{Y_{B_I}^{\text{eq}}} \right] \right\}$$

BS breakup in
thermal plasma
(negligible for
tight bound states)

annihilation

decay into other BS

Bound state formation

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- ◆ if BS decay/annihilate quickly

$$\frac{dY_{\text{DM}}}{dz} = -\frac{\langle \sigma_{\text{eff}} v_{\text{rel}} \rangle s}{Hz} (Y_{\text{DM}}^2 - Y_{\text{DM}}^{\text{eq},2})$$

$$\langle \sigma_{\text{eff}} v_{\text{rel}} \rangle \equiv S_{\text{ann}}(z) + \sum_{B_J} S_{B_J}(z)$$

Bound state formation

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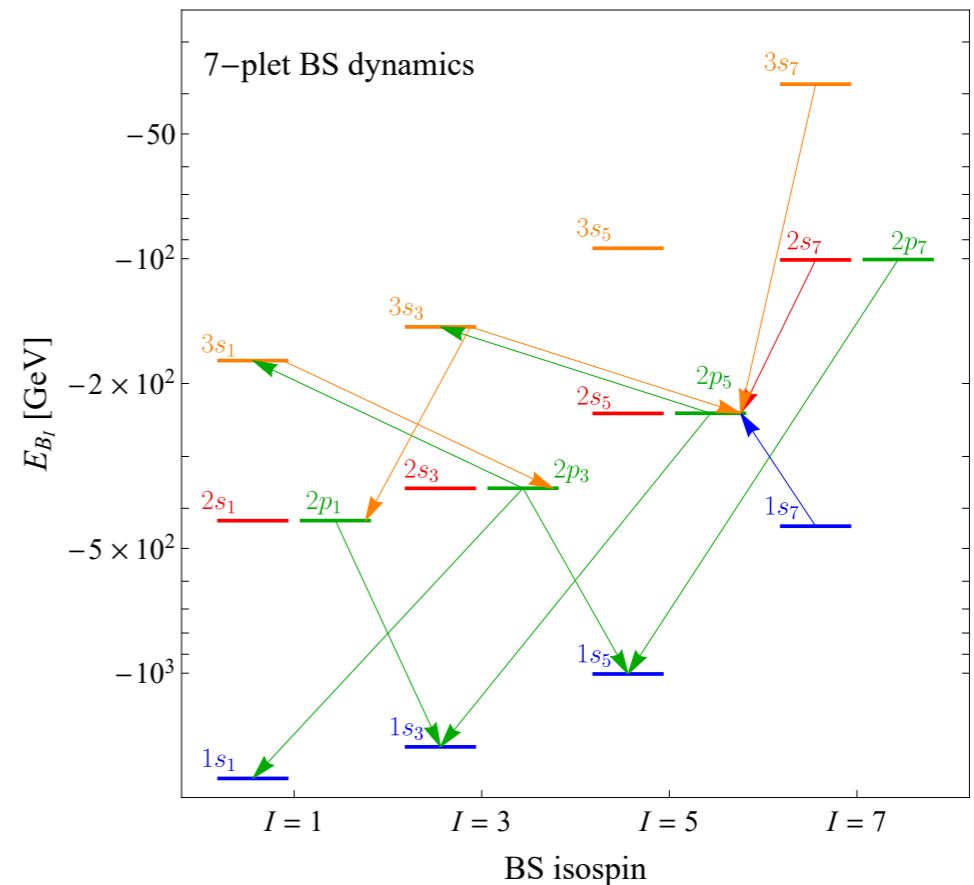
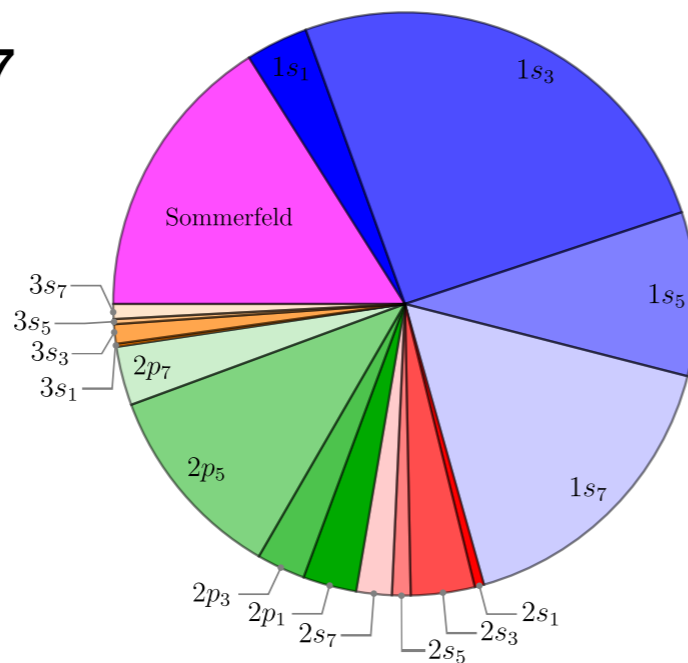
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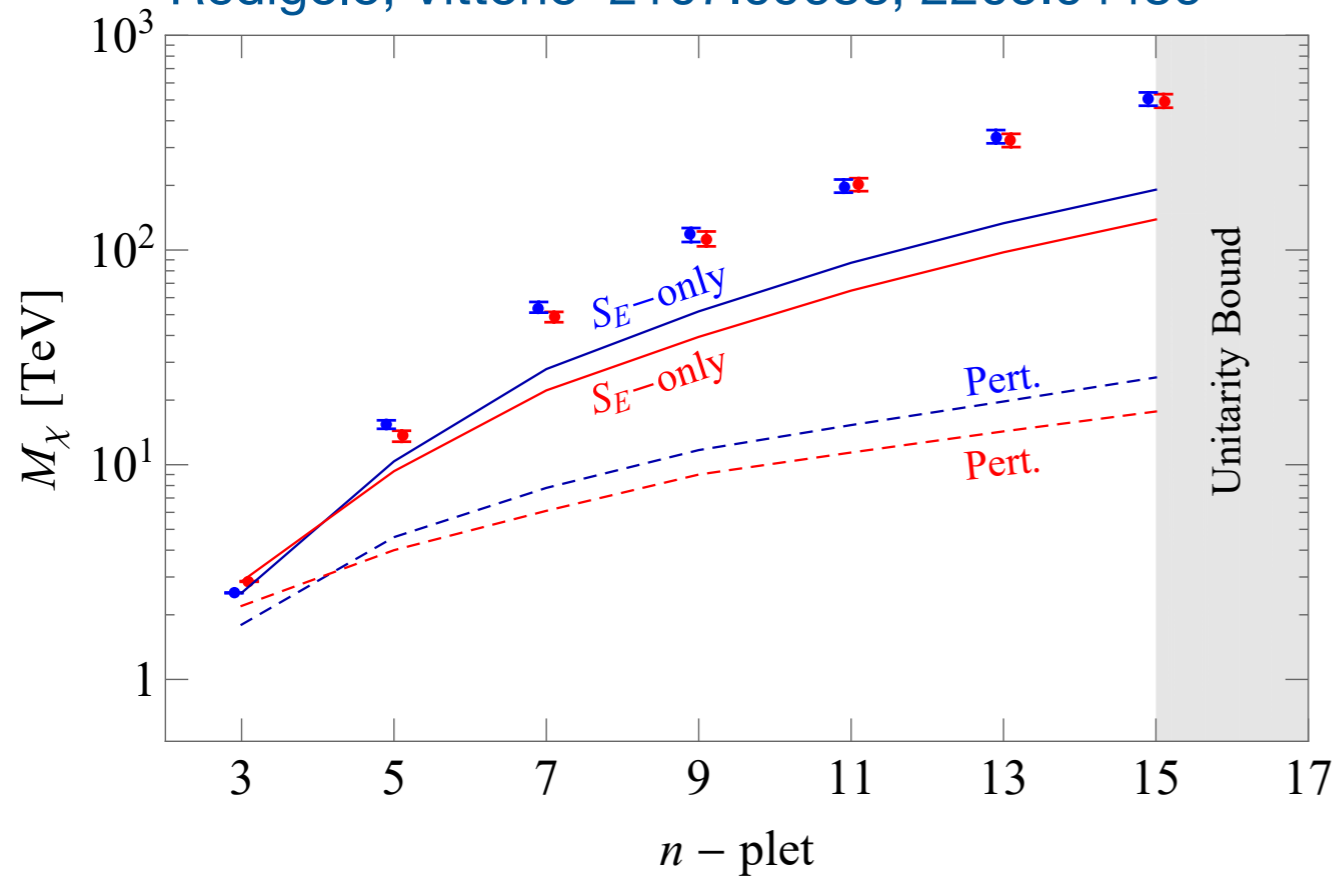
$$\langle \sigma_{\text{eff}} v_{\text{rel}} \rangle \equiv S_{\text{ann}}(z) + \sum_{B_J} S_{B_J}(z)$$

- ◆ Example: $n = 7$



Thermal freeze-out masses

Bottaro, DB, Costa, Franceschini, Panci,
Redigolo, Vittorio 2107.09688, 2205.04486

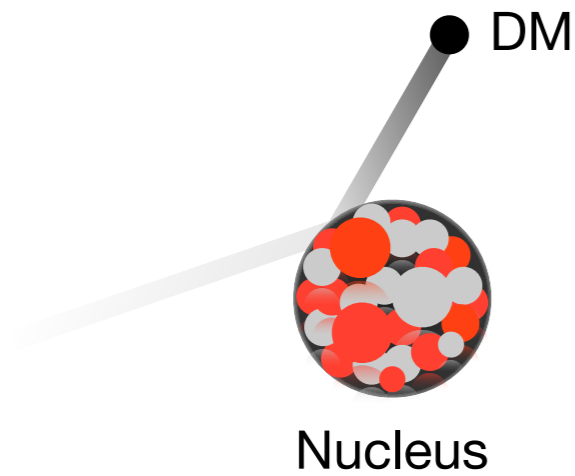


(and similar for scalars)

How do we probe these states?

	EW n-plet	Mass [TeV]
Majorana fermion	3_0	2.86
	5_0	13.6
	7_0	48.8
	9_0	113
	11_0	202
	13_0	324.6
Dirac fermion	$2_{1/2}$	1.08
	3_1	2.85
	$4_{1/2}$	4.8
	5_1	9.9
	$6_{1/2}$	31.8
	$8_{1/2}$	82
	$10_{1/2}$	158
	$12_{1/2}$	253

Direct detection

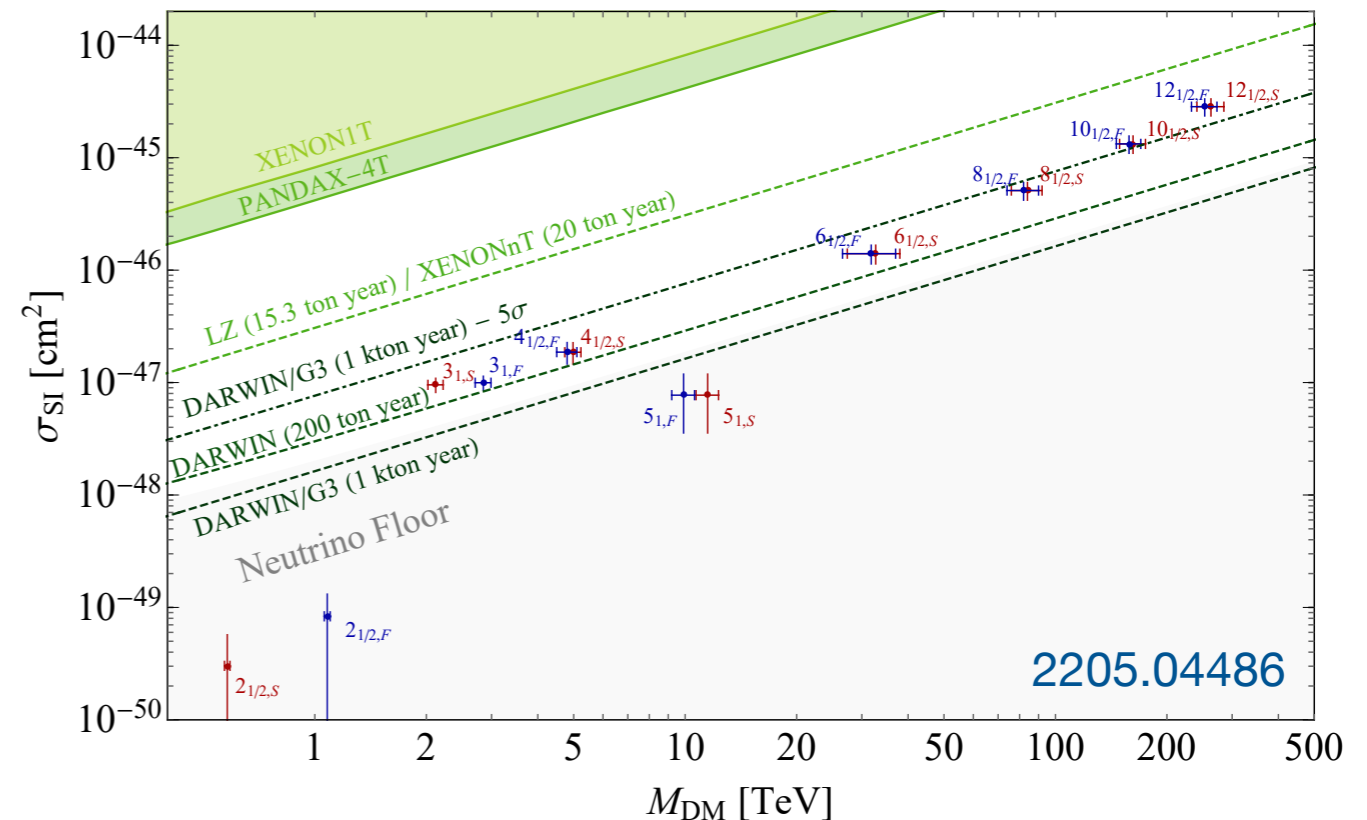
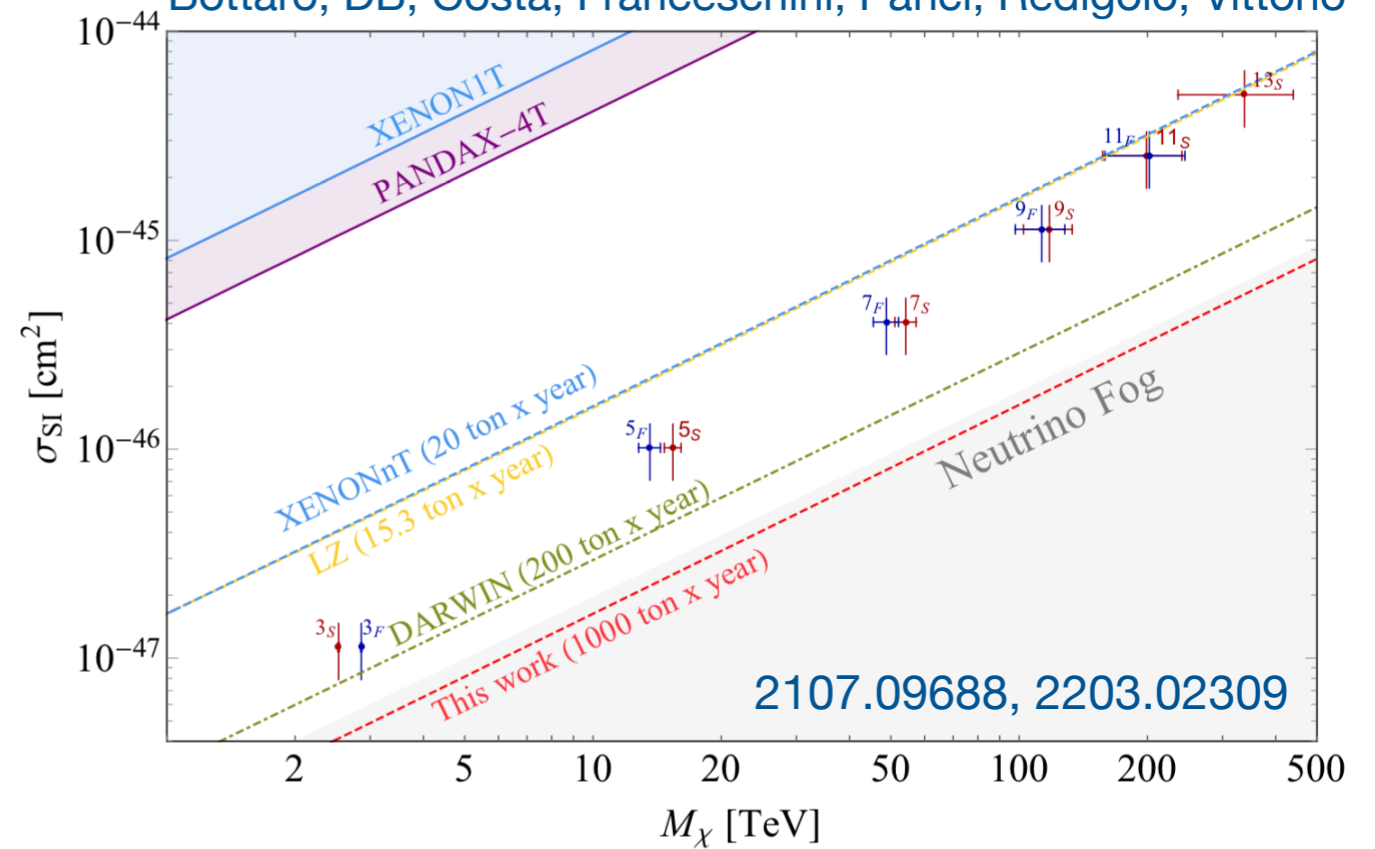


$$\mathcal{L}_{\text{eff}}^{\text{SI}} = \bar{\chi}\chi \left(f_q m_q \bar{q}q + f_G G_{\mu\nu}^a G^{\mu\nu,a} \right) + \frac{g_q}{M_\chi} (\bar{\chi} i \partial^\mu \gamma^\nu \chi) \mathcal{O}_{\mu\nu}^q$$

$$f_i \approx \frac{\alpha_{\text{EW}}^2}{m_{\text{EW}}^3} (n^2 - 1)$$

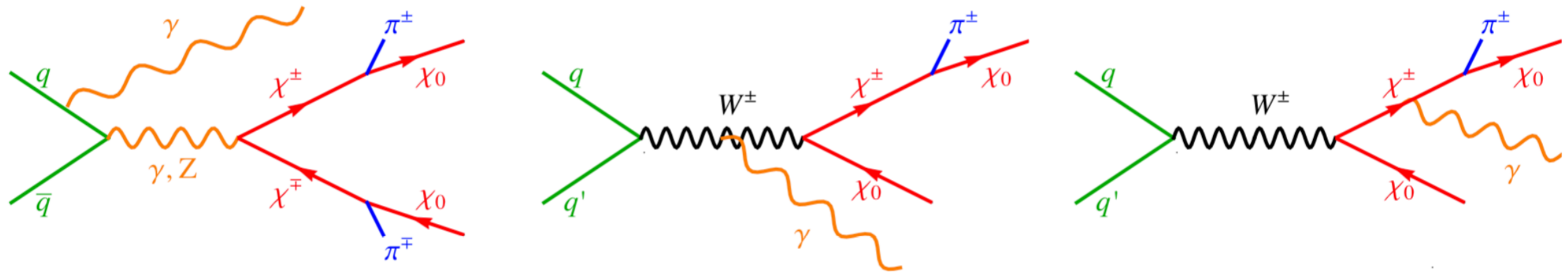
All WIMP candidates (except doublet!) above the neutrino floor, but need a very large exposure to be probed

Bottaro, DB, Costa, Franceschini, Panci, Redigolo, Vittorio



Colliders: missing energy searches

- ◆ $2 \rightarrow 2$ production of invisible χ pair + event tag, e.g. monophoton



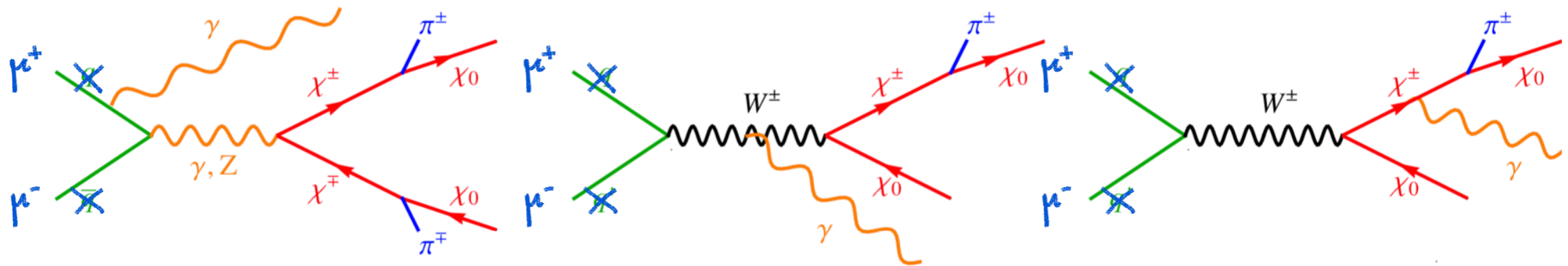
very difficult at hadron colliders: large backgrounds, and strong PDF suppression at high partonic c.o.m. energies (large invariant masses)

- ▶ LHC sensitive to DM masses $\sim O(100 \text{ GeV})$
- ▶ even at 100 TeV can't reach thermal freeze-out targets

Cirelli, Sala, Taoso 1407.7058

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Cirelli, Sala, Taoso 1407.7058

➡ Try with a high-energy lepton collider!



Missing mass searches at μ collider

— Want to know more?

2303.08533 2203.07964

2210.02591 2203.08033

2209.01318 2203.07224

2203.07256

2203.07261

2103.14043

1901.06150

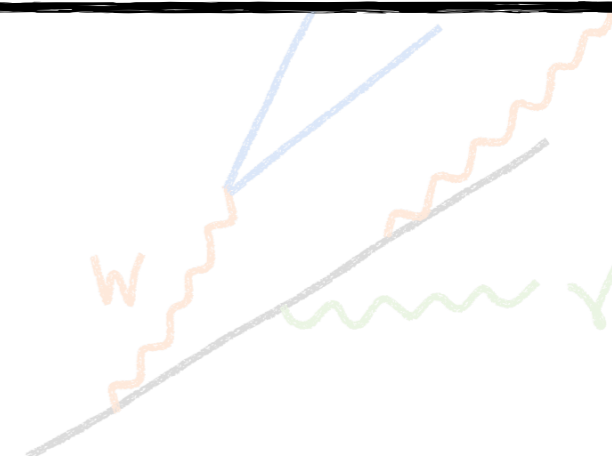
+ many more...



www.redbubble.com/people/muon-collider

Sudakov factor $\frac{1}{4\pi} \log^2(E/m_W) \approx 1$ for $E \sim 10$ TeV

- ▶ mono- γ , mono-W, mono-Z are all similar!
- ▶ multiple gauge boson emission



Missing mass searches at μ collider

$2 \rightarrow 2$ production of χ pair

- ◆ Full energy available

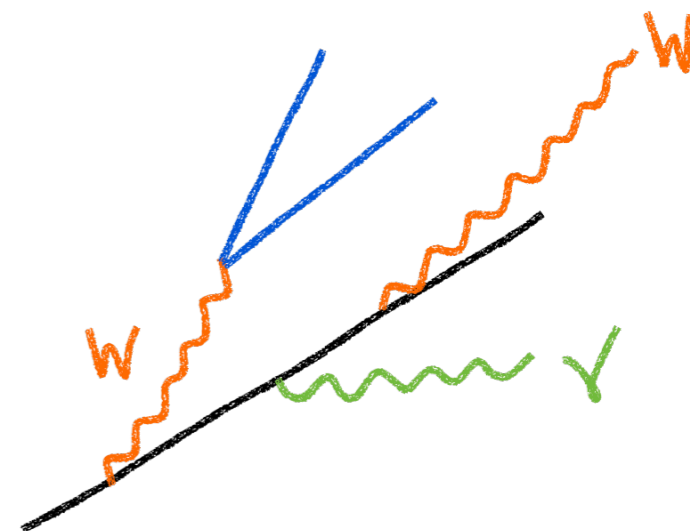
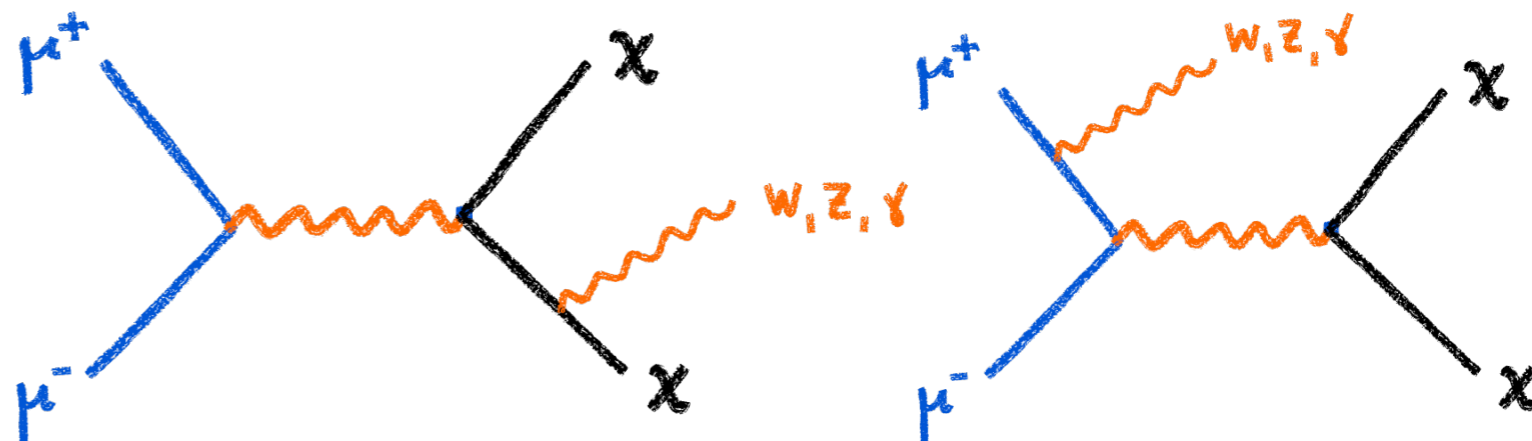
in the center of mass:

ability to discover particles **up to kinematical threshold** $\sqrt{s}/2$

- ◆ Full event reconstruction: **missing invariant mass** (not just pT)
- ◆ No QCD backgrounds: ideal for EW physics
- ◆ **EW radiation** becomes important at multi-TeV energies!

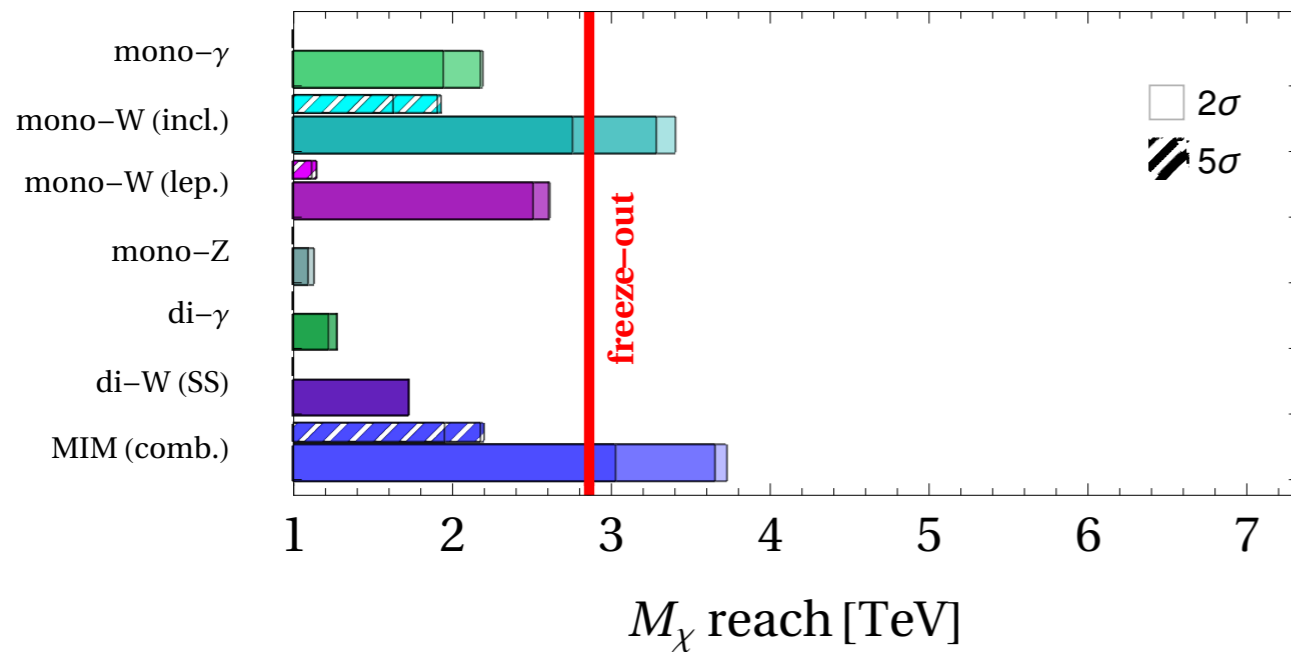
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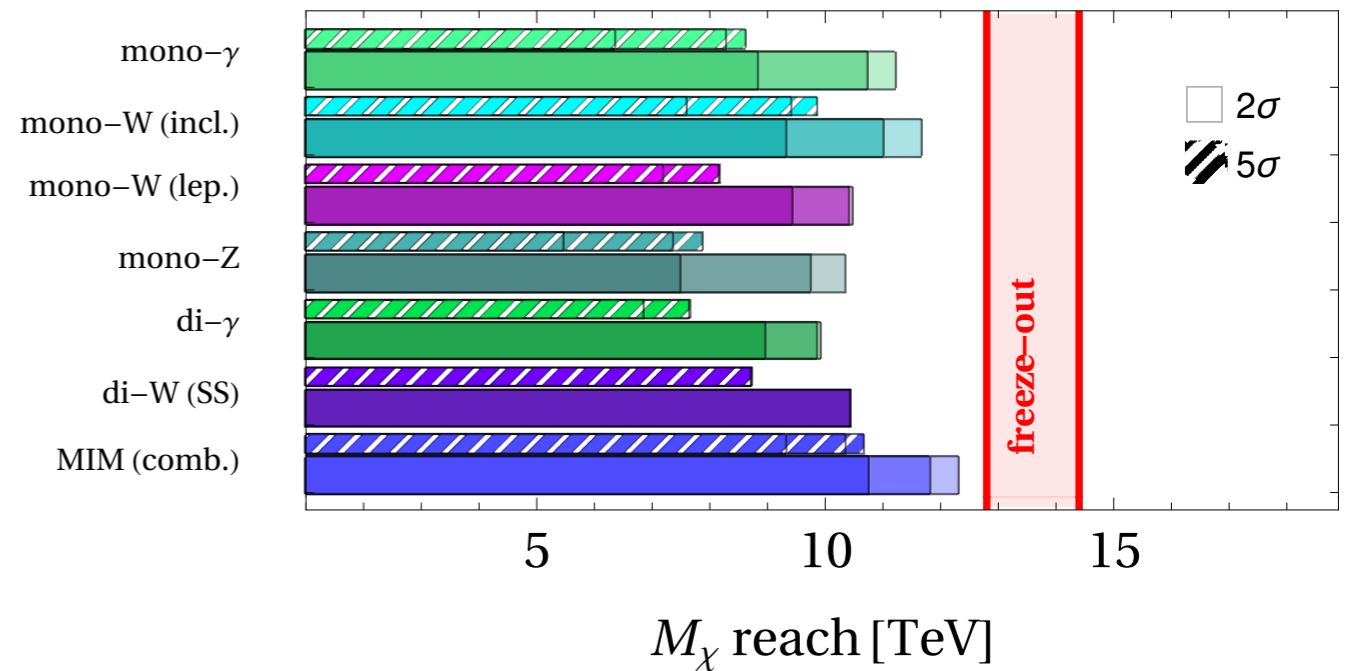


Missing mass searches at μ collider

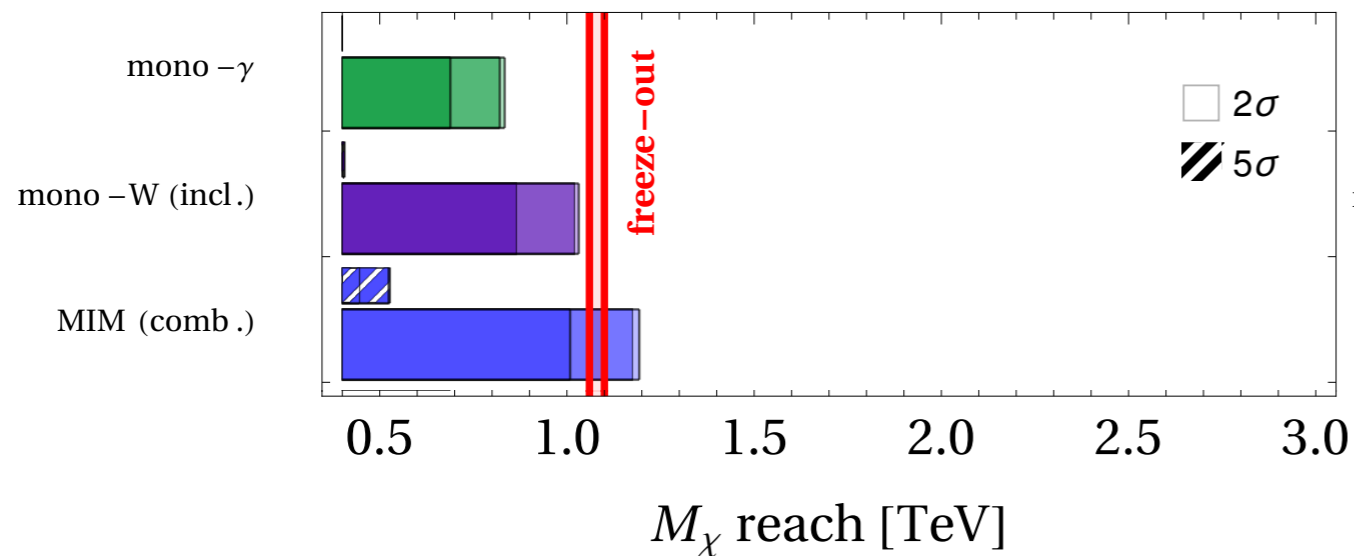
$\sqrt{s} = 14 \text{ TeV}, \mathcal{L} = 20 \text{ ab}^{-1}, \text{Majorana } 3\text{-plet}$



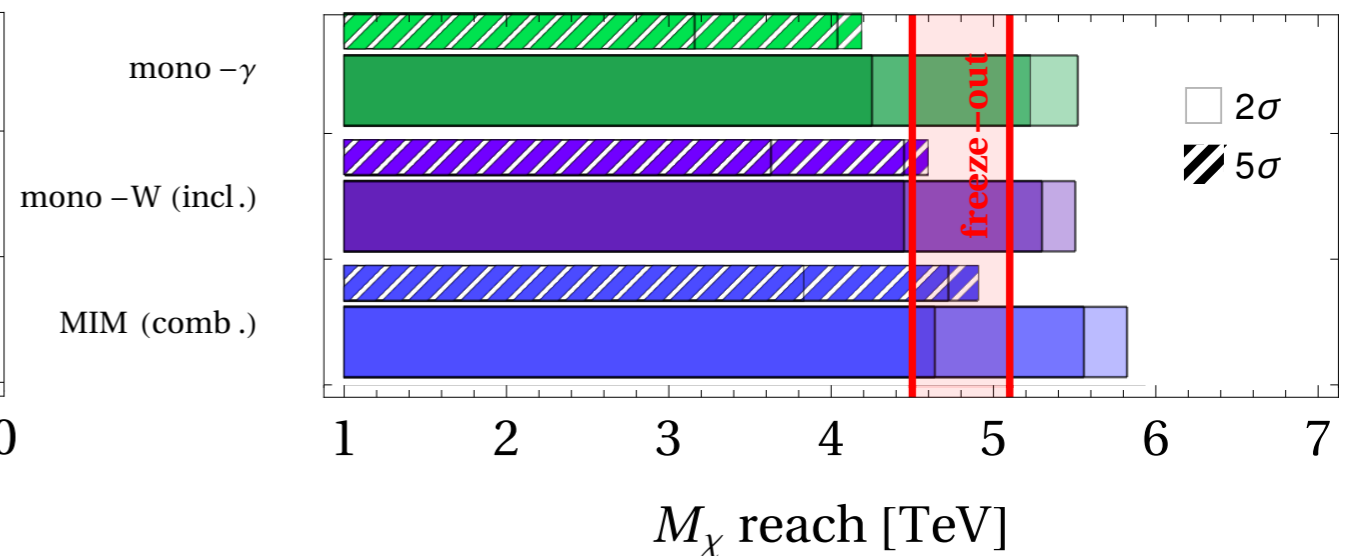
$\sqrt{s} = 30 \text{ TeV}, \mathcal{L} = 90 \text{ ab}^{-1}, \text{Majorana } 5\text{-plet}$



$\sqrt{s} = 6 \text{ TeV}, \mathcal{L} = 4 \text{ ab}^{-1}, \text{Dirac } 2_{1/2}$



$\sqrt{s} = 14 \text{ TeV}, \mathcal{L} = 20 \text{ ab}^{-1}, \text{Dirac } 4_{1/2}$



* shadings = different assumptions about systematic errors
typically low signal/background \rightarrow requires good control of systematics

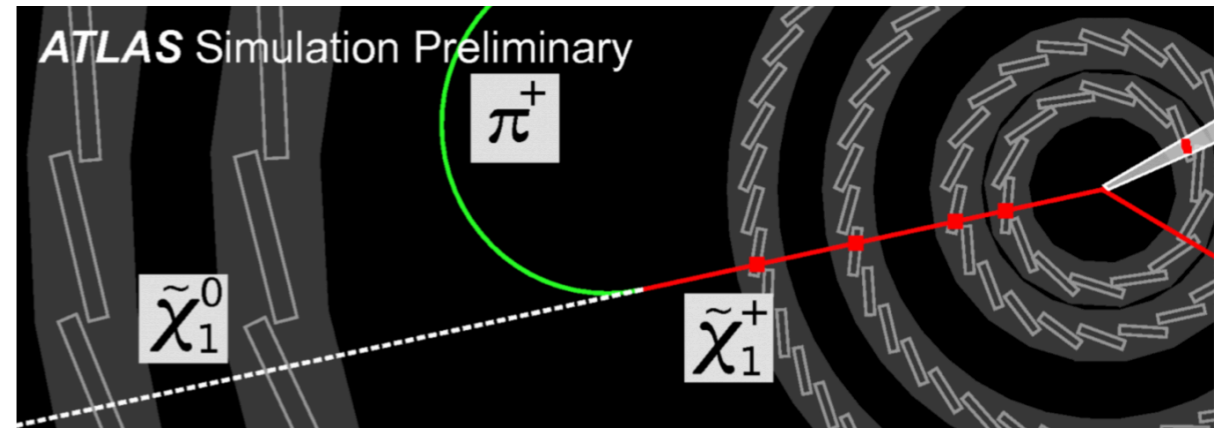
Mass splittings and disappearing tracks

- Dark Matter is part of a multiplet that includes also charged states

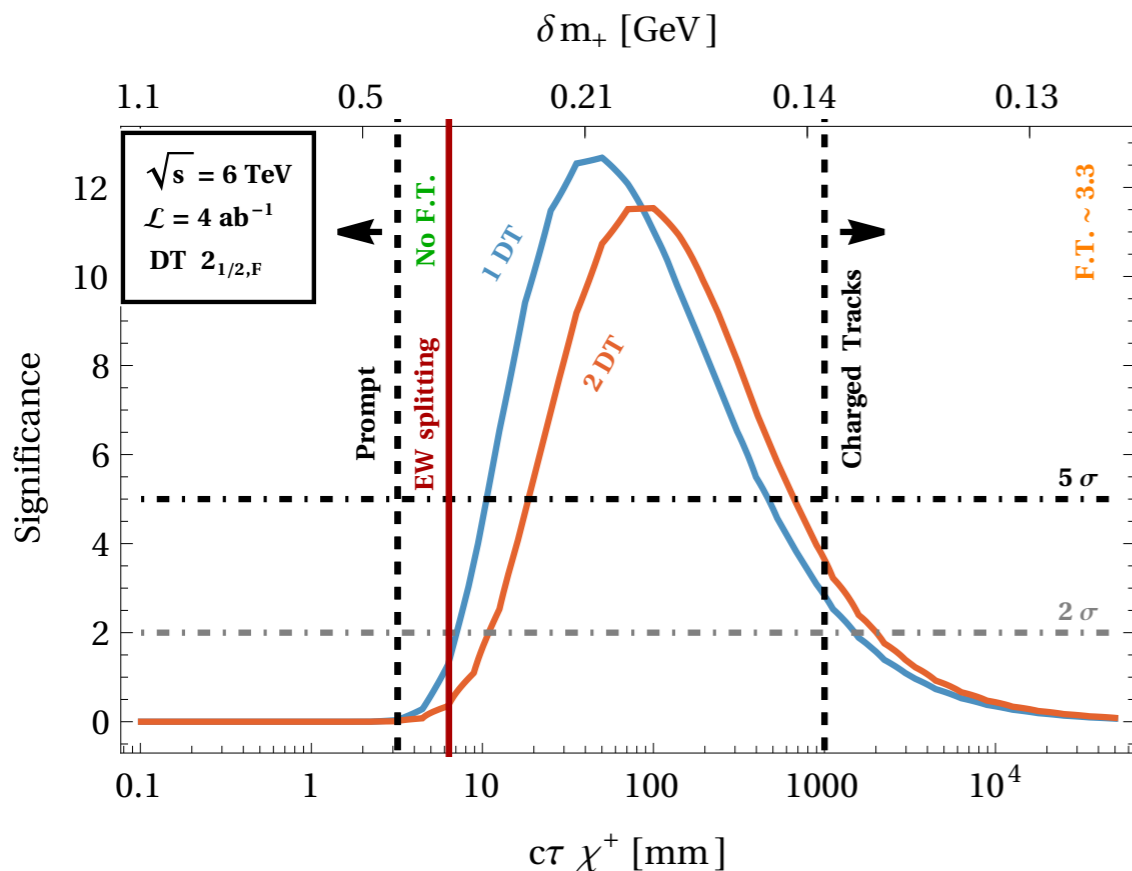
$$\chi_n = (\dots, \chi^-, \chi^0, \chi^+, \dots)$$

χ^\pm decays into DM inside the detector

- Look for the disappearing tracks of the charged particles to isolate the DM signal from the SM background (mainly neutrinos)



Capdevilla, Meloni, Simoniello, Zurita 2102.11292



- Real WIMPs ($Y = 0$): mass splitting fixed by gauge interactions

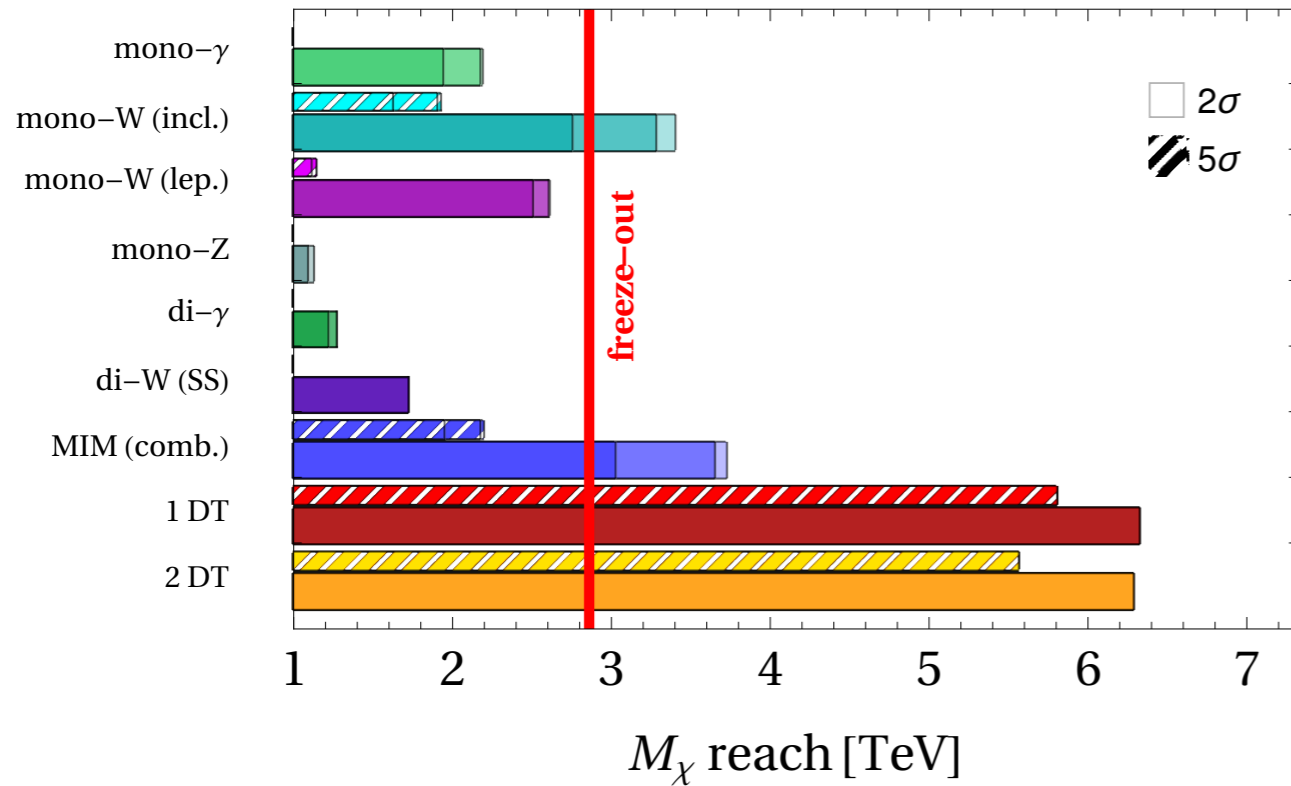
$$M_Q - M_0 \approx Q^2 \alpha_{\text{em}} m_W$$

$$c\tau_{\chi^\pm} \approx 50 \text{ cm} / (n^2 - 1)$$

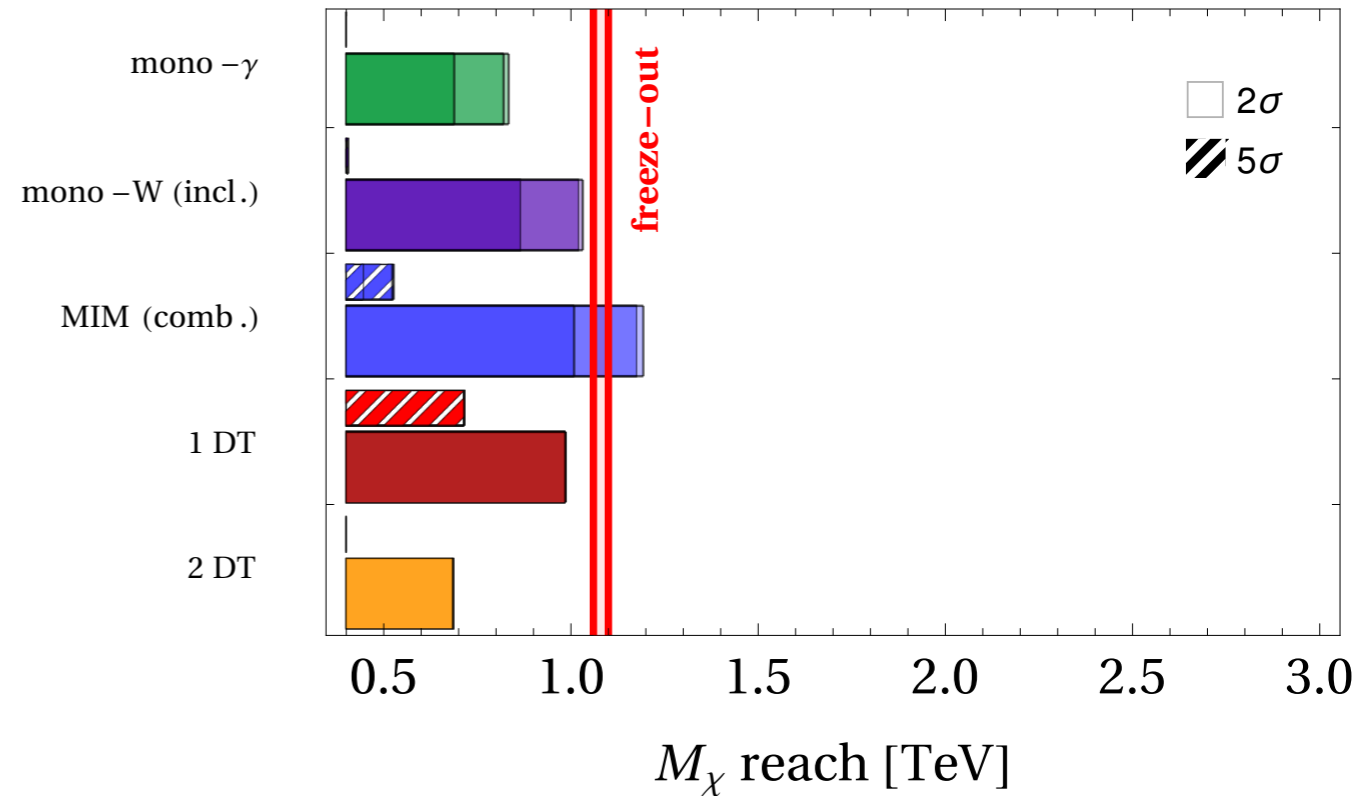
- Complex WIMPs: additional splitting needed to make DM stable

Disappearing tracks at μ collider

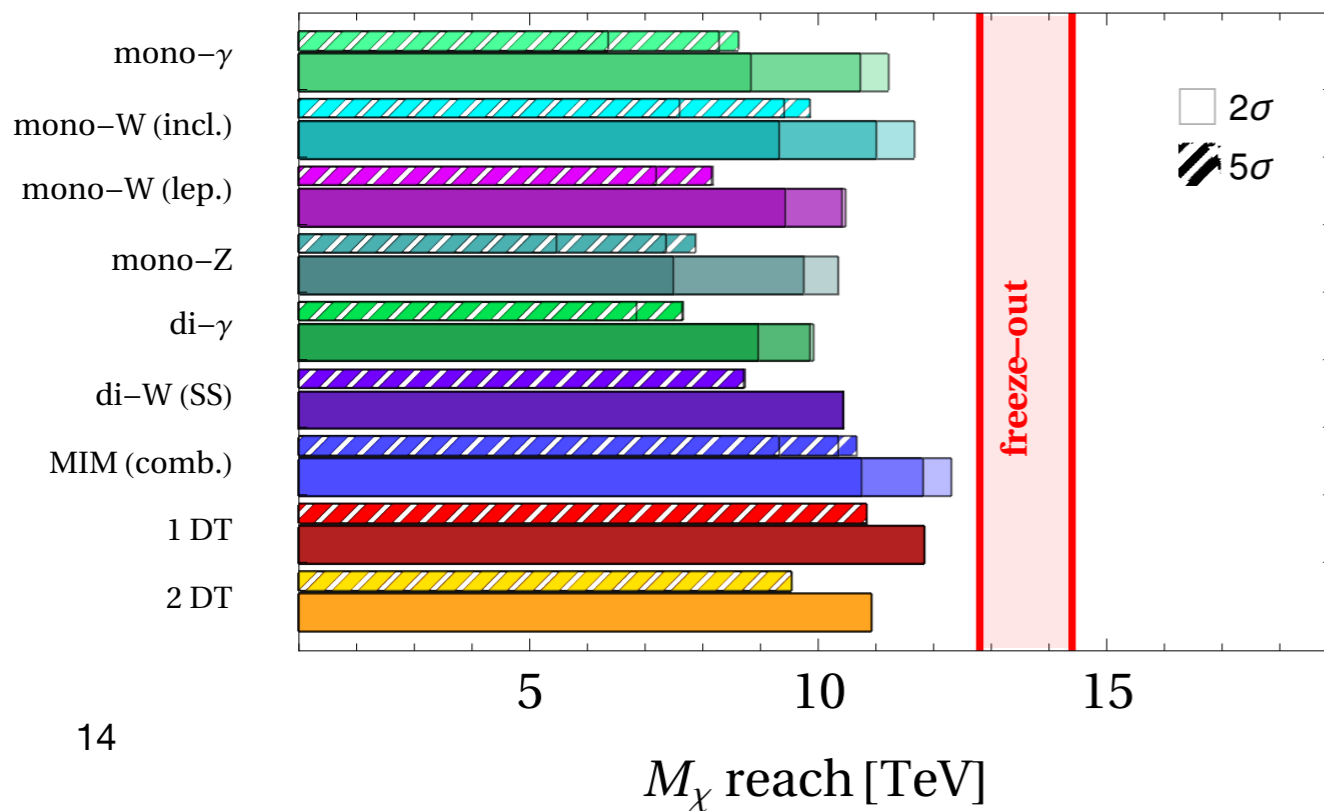
$\sqrt{s} = 14 \text{ TeV}$, $\mathcal{L} = 20 \text{ ab}^{-1}$, Majorana 3-plet



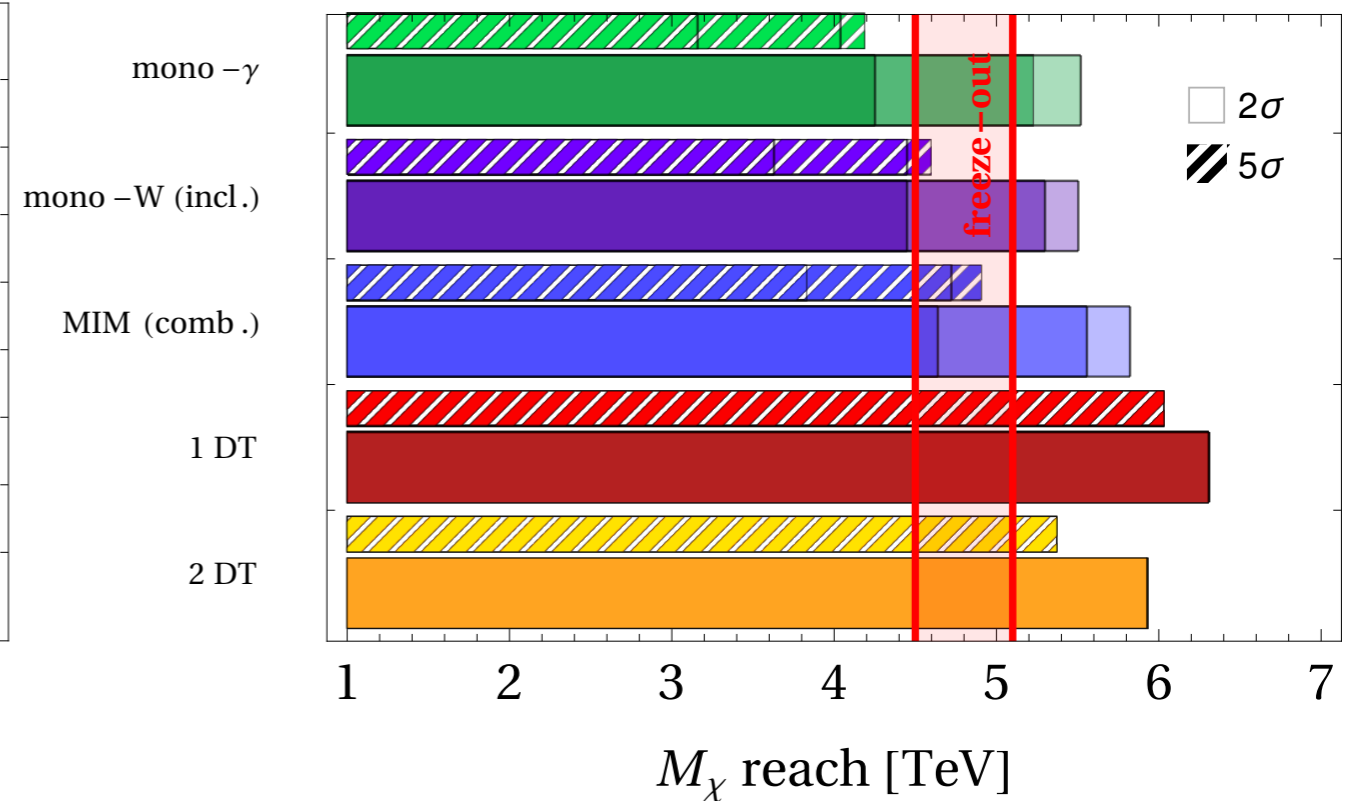
$\sqrt{s} = 6 \text{ TeV}$, $\mathcal{L} = 4 \text{ ab}^{-1}$, Dirac $2_{1/2}$



$\sqrt{s} = 30 \text{ TeV}$, $\mathcal{L} = 90 \text{ ab}^{-1}$, Majorana 5-plet

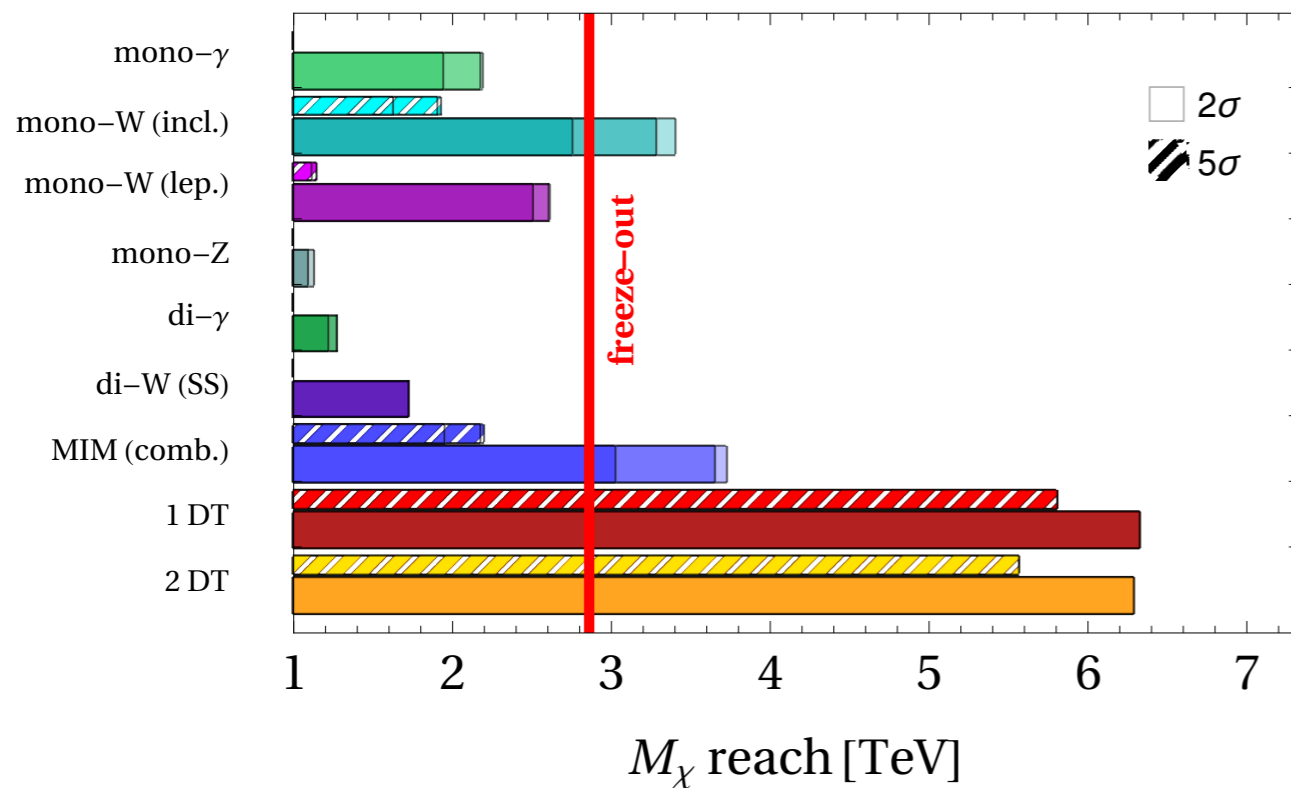


$\sqrt{s} = 14 \text{ TeV}$, $\mathcal{L} = 20 \text{ ab}^{-1}$, Dirac $4_{1/2}$

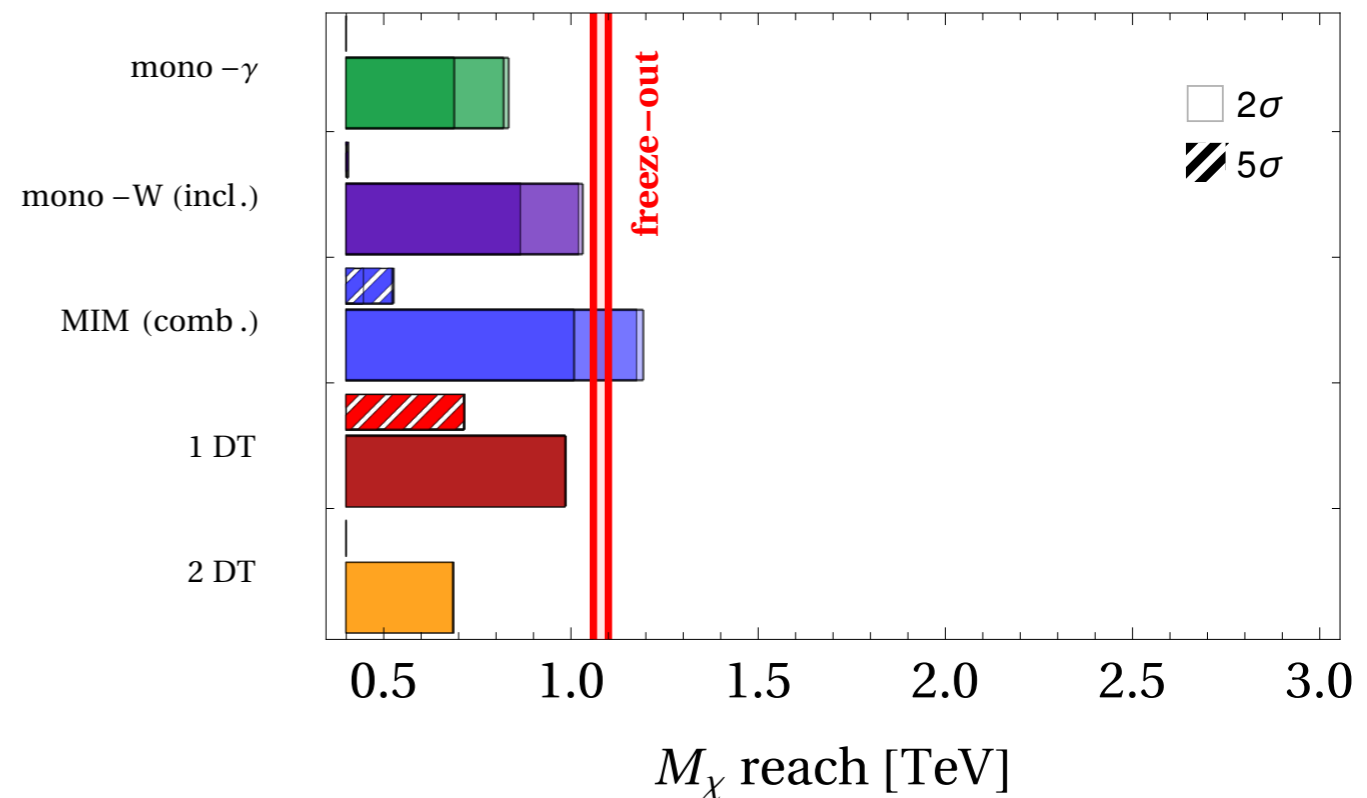


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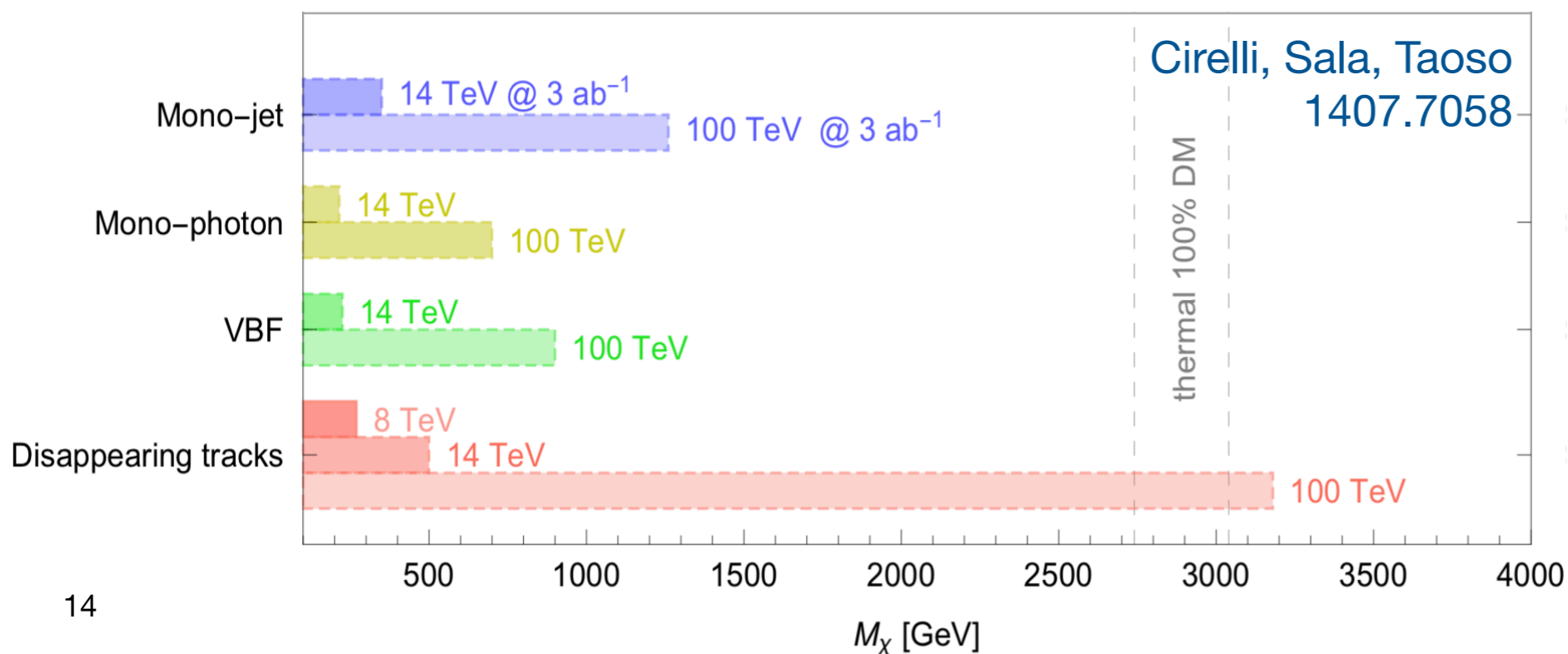
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$\sqrt{s} = 6 \text{ TeV}, \mathcal{L} = 4 \text{ ab}^{-1}, \text{Dirac } 2_{1/2}$



Majorana 3-plet at 100 TeV pp

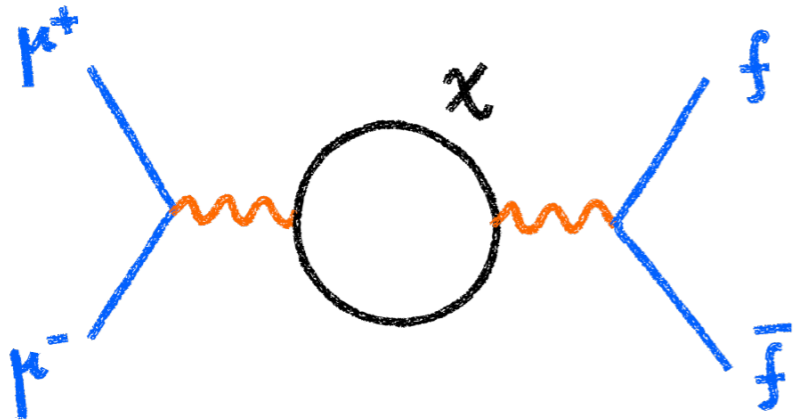


* disappearing tracks allow to probe the Wino also at FCC-hh

Indirect effects at colliders

- ♦ All EW multiplets contribute to high-energy $2 \rightarrow 2$ fermion scattering: effects that grow with energy, can be tested at μ collider or FCC-hh

Di Luzio, Gröber, Panico 1810.10993



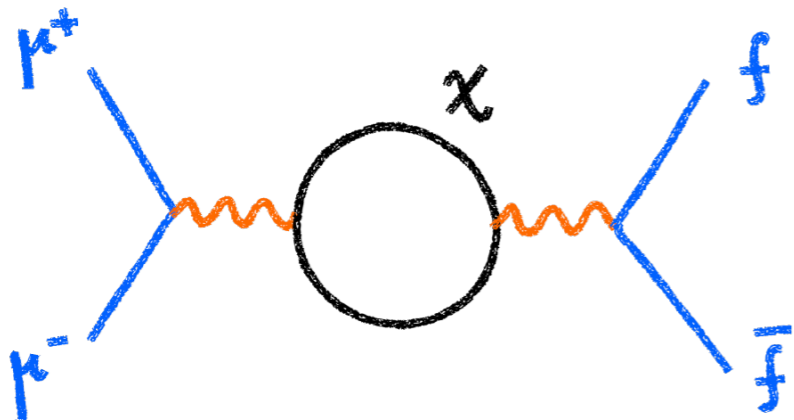
$$\hat{W} \approx 10^{-7} \times \left(\frac{1 \text{ TeV}}{M_{\text{DM}}} \right)^2 n^3 \propto 1/n^2$$

$$\hat{Y} \approx 10^{-7} \times \left(\frac{1 \text{ TeV}}{M_{\text{DM}}} \right)^2 Y^2 n \propto 1/n^4$$

Indirect effects at colliders

- ◆ All EW multiplets contribute to high-energy $2 \rightarrow 2$ fermion scattering: effects that grow with energy, can be tested at μ collider or FCC-hh

Di Luzio, Gröber, Panico 1810.10993



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- ◆ Complex multiplets need mass splittings from higher dim. operators

- ▶ Charged-neutral splitting (to make DM stable): $(\bar{\chi} T^a \chi) (H^\dagger \sigma^a H)$

- ▶ Inelastic splitting (suppress Z-induced scattering): $(\bar{\chi} (T^a)^{2Y} \chi^c) (H^{\dagger c} \sigma^a H)^{2Y}$

$$\hat{S} \approx 10^{-5} \times \left(\frac{1 \text{ TeV}}{M_{\text{DM}}} \right) \left(\frac{\delta M}{10 \text{ GeV}} \right) n^3, \quad \hat{T} \approx 10^{-5} \times \left(\frac{\delta M}{10 \text{ GeV}} \right)^2 n^3$$

can be tested at FCC-ee

Di Luzio, Gröber, Kamenik, Nardecchia 1505.00359

Indirect detection

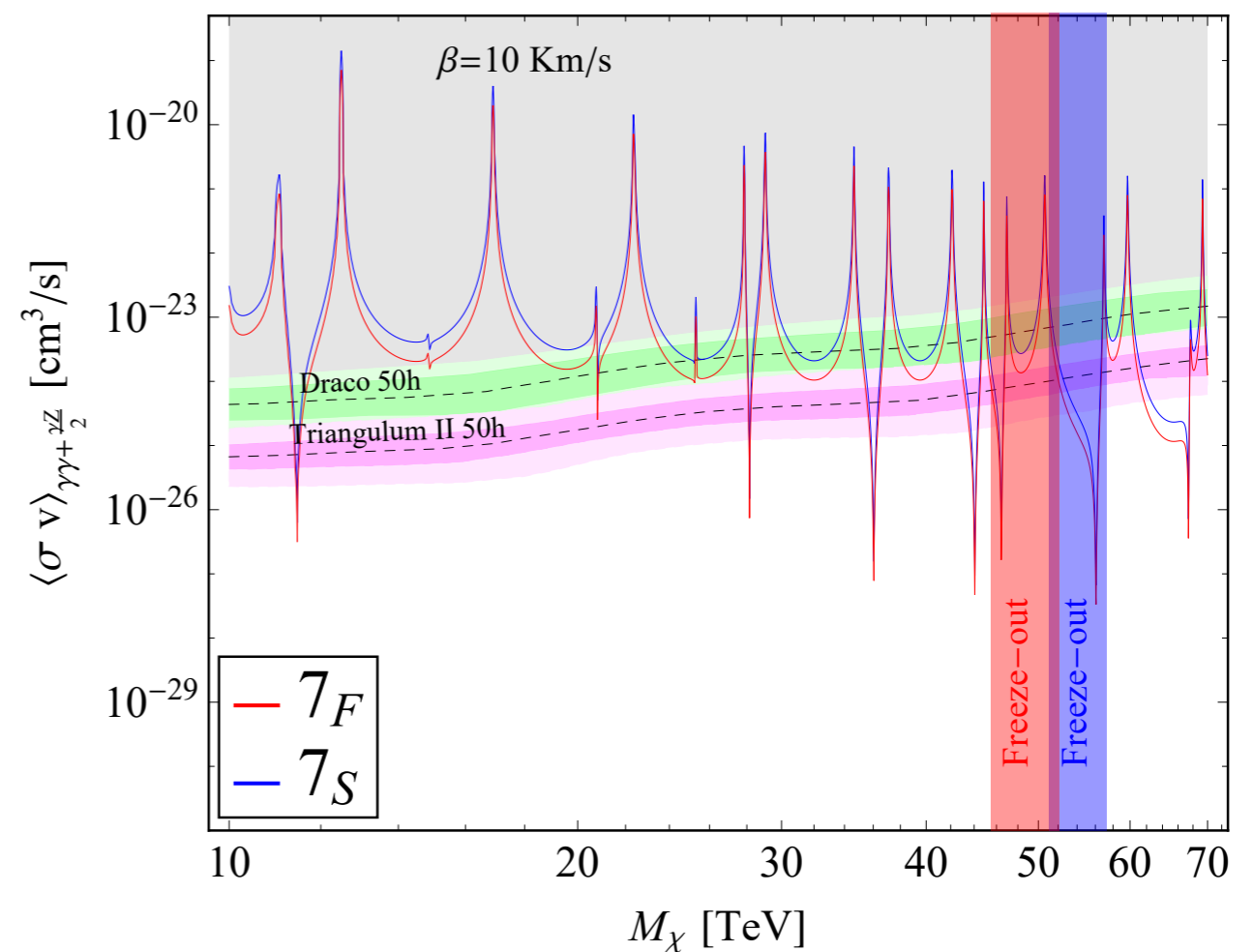
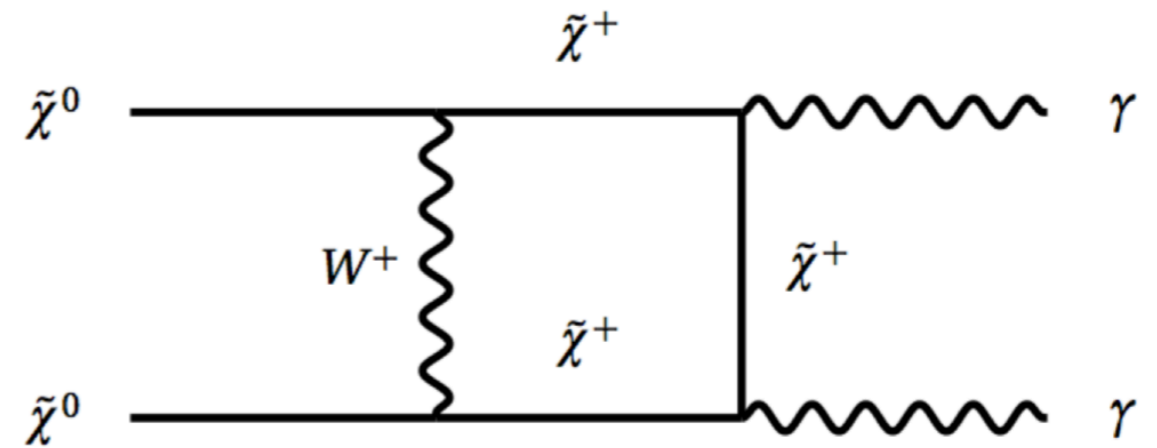
- Searches for high-energy gamma-ray lines with Cherenkov telescopes are a powerful constraint for high-mass WIMP DM

γ -ray line at $E_\gamma \approx M_\chi$

to be included:

- ▶ continuum
- ▶ bound-state contribution
- ▶ EW radiation

- Large multiplets are easily probed due to increased annihilation cross-section



- ◆ Thermal, weakly interacting Dark Matter generically points to multi-TeV mass scales. Not probed yet!
- ◆ Next-generation experiments needed to fully cover the parameter space:

large exposure
direct detection

high-energy
muon collider

indirect detection
gamma-ray lines

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large exposure
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*needs a
 μ -collider!*

Results: real WIMPs

DM spin	EW n-plet	M_χ (TeV)	$(\sigma v)_{\text{tot}}^{J=0} / (\sigma v)_{\text{max}}^{J=0}$	$\Lambda_{\text{Landau}} / M_{\text{DM}}$	$\Lambda_{\text{UV}} / M_{\text{DM}}$
Real scalar	3	2.53 ± 0.01	–	2.4×10^{37}	$4 \times 10^{24*}$
	5	15.4 ± 0.7	0.002	7×10^{36}	3×10^{24}
	7	54.2 ± 3.1	0.022	7.8×10^{16}	2×10^{24}
	9	117.8 ± 8.8	0.088	3×10^4	2×10^{24}
	11	199 ± 14	0.25	62	1×10^{24}
	13	338 ± 24	0.6	7.2	2×10^{24}
Majorana fermion	3	2.86 ± 0.01	–	2.4×10^{37}	$2 \times 10^{12*}$
	5	13.6 ± 0.8	0.003	5.5×10^{17}	3×10^{12}
	7	48.8 ± 2.7	0.019	1.2×10^4	1×10^8
	9	113 ± 9	0.07	41	1×10^8
	11	202 ± 14	0.2	6	1×10^8
	13	324.6 ± 23	0.5	2.6	1×10^8

$$\mathcal{L}_s \supset \frac{C_1^{(s)}}{\Lambda_{\text{UV}}^{n-4}} \chi (H^\dagger H)^{\frac{n-1}{2}} + \frac{C_2^{(s)}}{\Lambda_{\text{UV}}^{n-4}} \chi W_{\mu\nu} W^{\mu\nu} (H^\dagger H)^{\frac{n-5}{2}} + \dots + \frac{C_w^{(s)}}{\Lambda_{\text{UV}}^{n-4}} \chi (W_{\mu\nu} W^{\mu\nu})^{\frac{n-1}{4}} + \frac{C_{3\chi}^{(s)}}{\Lambda_{\text{UV}}} \chi^3 H^\dagger H,$$

$$\mathcal{L}_f \supset \frac{C_1^{(f)}}{\Lambda_{\text{UV}}^{n-3}} (\chi HL) (H^\dagger H)^{\frac{n-3}{2}} + \frac{C_2^{(f)}}{\Lambda_{\text{UV}}^{n-3}} (\chi \sigma^{\mu\nu} HL) W_{\mu\nu} (H^\dagger H)^{\frac{n-5}{2}} + \dots + \frac{C_w^{(f)}}{\Lambda_{\text{UV}}^{n-3}} (\chi HL) (W_{\mu\nu} W^{\mu\nu})^{\frac{n-3}{4}} + \frac{C_{3\chi}^{(f)}}{\Lambda_{\text{UV}}^3} \chi^3 HL,$$

Results: complex WIMPs

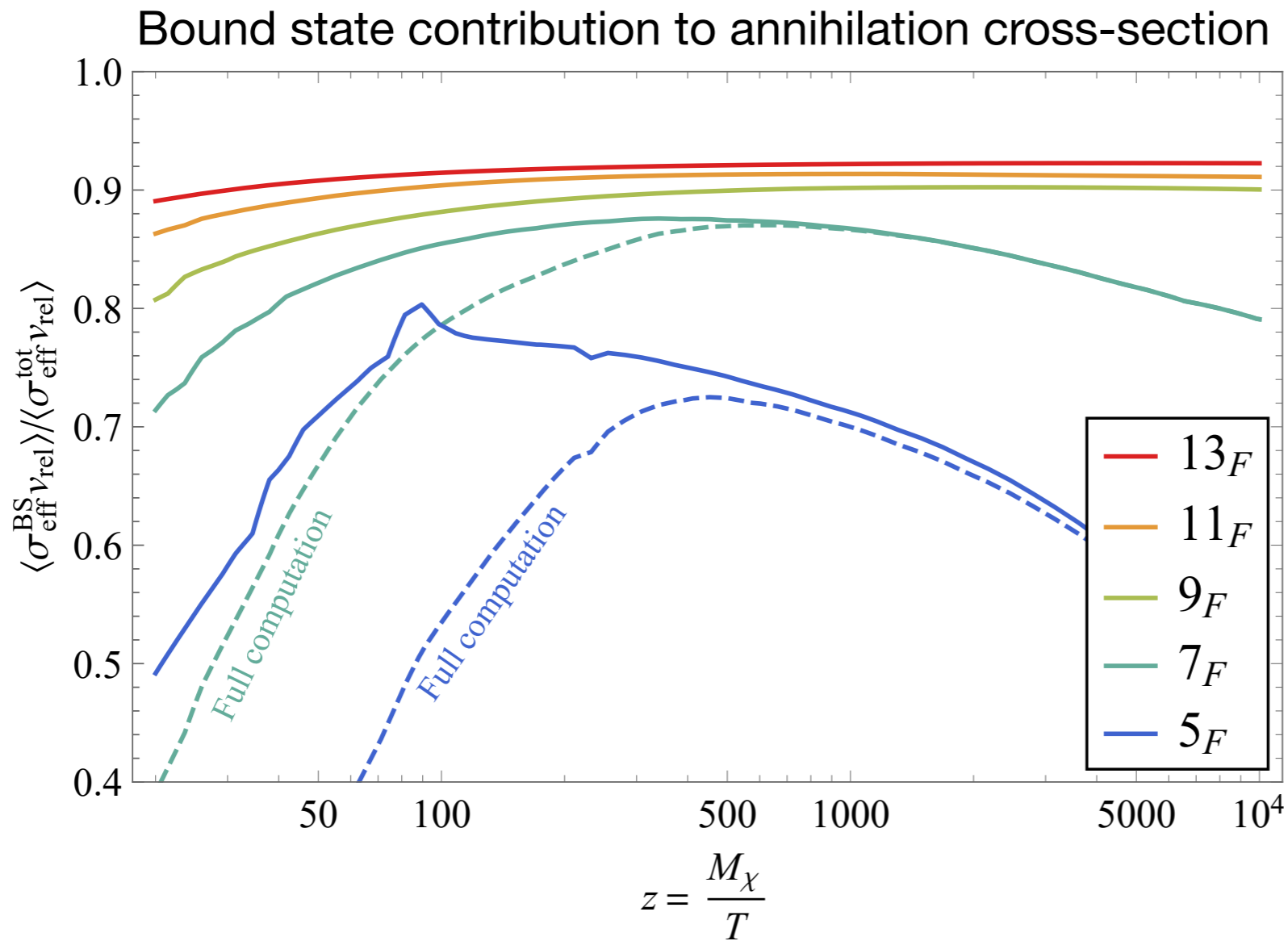
DM spin	n_Y	M_{DM} (TeV)	$\Lambda_{\text{Landau}}/M_{\text{DM}}$	$(\sigma v)_{\text{tot}}^{J=0}/(\sigma v)_{\text{max}}^{J=0}$	δm_0 [MeV]	$\Lambda_{\text{UV}}^{\text{max}}/M_{\text{DM}}$	δm_{Q_M} [MeV]
Dirac fermion	$2_{1/2}$	1.08 ± 0.02	$> M_{\text{Pl}}$	-	$0.22 - 2 \times 10^4$	10^7	$4.8 - 10^4$
	3_1	2.85 ± 0.14	$> M_{\text{Pl}}$	-	$0.22 - 40$	60	$312 - 1.6 \times 10^4$
	$4_{1/2}$	4.8 ± 0.3	$\simeq M_{\text{Pl}}$	0.001	$0.21 - 3 \times 10^4$	5×10^6	$20 - 1.9 \times 10^4$
	5_1	9.9 ± 0.7	3×10^6	0.003	$0.21 - 3$	25	$10^3 - 2 \times 10^3$
	$6_{1/2}$	31.8 ± 5.2	2×10^4	0.01	$0.5 - 2 \times 10^4$	4×10^5	$100 - 2 \times 10^4$
	$8_{1/2}$	82 ± 8	15	0.05	$0.84 - 10^4$	10^5	$440 - 10^4$
	$10_{1/2}$	158 ± 12	3	0.16	$1.2 - 8 \times 10^3$	6×10^4	$1.1 \times 10^3 - 9 \times 10^3$
	$12_{1/2}$	253 ± 20	2	0.45	$1.6 - 6 \times 10^3$	4×10^4	$2.3 \times 10^3 - 7 \times 10^3$
Complex scalar	$2_{1/2}$	0.58 ± 0.01	$> M_{\text{Pl}}$	-	$4.9 - 1.4 \times 10^4$	-	$4.2 - 7 \times 10^3$
	3_1	2.1 ± 0.1	$> M_{\text{Pl}}$	-	$3.7 - 500$	120	$75 - 1.3 \times 10^4$
	$4_{1/2}$	4.98 ± 0.25	$> M_{\text{Pl}}$	0.001	$4.9 - 3 \times 10^4$	-	$17 - 2 \times 10^4$
	5_1	11.5 ± 0.8	$> M_{\text{Pl}}$	0.004	$3.7 - 10$	20	$650 - 3 \times 10^3$
	$6_{1/2}$	32.7 ± 5.3	$\simeq 6 \times 10^{13}$	0.01	$4.9 - 8 \times 10^4$	-	$50 - 5 \times 10^4$
	$8_{1/2}$	84 ± 8	2×10^4	0.05	$4.9 - 6 \times 10^4$	-	$150 - 6 \times 10^4$
	$10_{1/2}$	162 ± 13	20	0.16	$4.9 - 4 \times 10^4$	-	$430 - 4 \times 10^4$
	$12_{1/2}$	263 ± 22	4	0.4	$4.9 - 3 \times 10^4$	-	$10^3 - 3 \times 10^4$

$$\mathcal{L}_D = \bar{\chi} (i\not{D} - M_\chi) \chi + \frac{y_0}{\Lambda_{\text{UV}}^{4Y-1}} \mathcal{O}_0 + \frac{y_+}{\Lambda_{\text{UV}}} \mathcal{O}_+ + \text{h.c.} ,$$

$$\mathcal{O}_0 = \frac{1}{2(4Y)!} (\bar{\chi} (T^a)^{2Y} \chi^c) \left[(H^{c\dagger}) \frac{\sigma^a}{2} H \right]^{2Y} ,$$

$$\mathcal{O}_+ = -\bar{\chi} T^a \chi H^\dagger \frac{\sigma^a}{2} H ,$$

Impact of bound state formation



$$\langle \sigma_{\text{eff}} v_{\text{rel}} \rangle \equiv S_{\text{ann}}(z) + \sum_{B_J} S_{B_J}(z)$$

$$S_{\text{ann}} = \sum_I \left\langle \sigma_{\text{ann}}^I v_{\text{rel}} \frac{2\pi\alpha_{\text{eff}}}{v_{\text{rel}}} \right\rangle$$

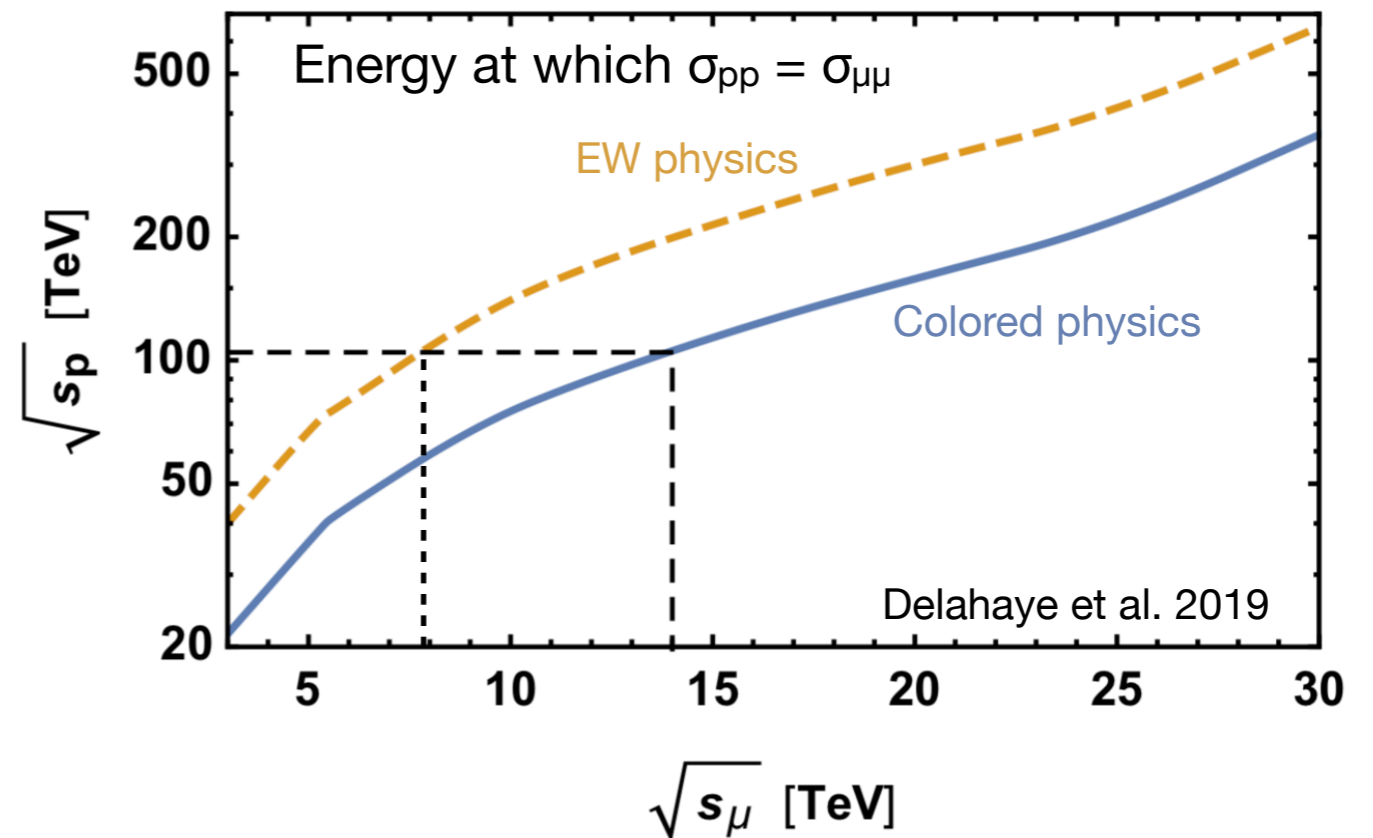
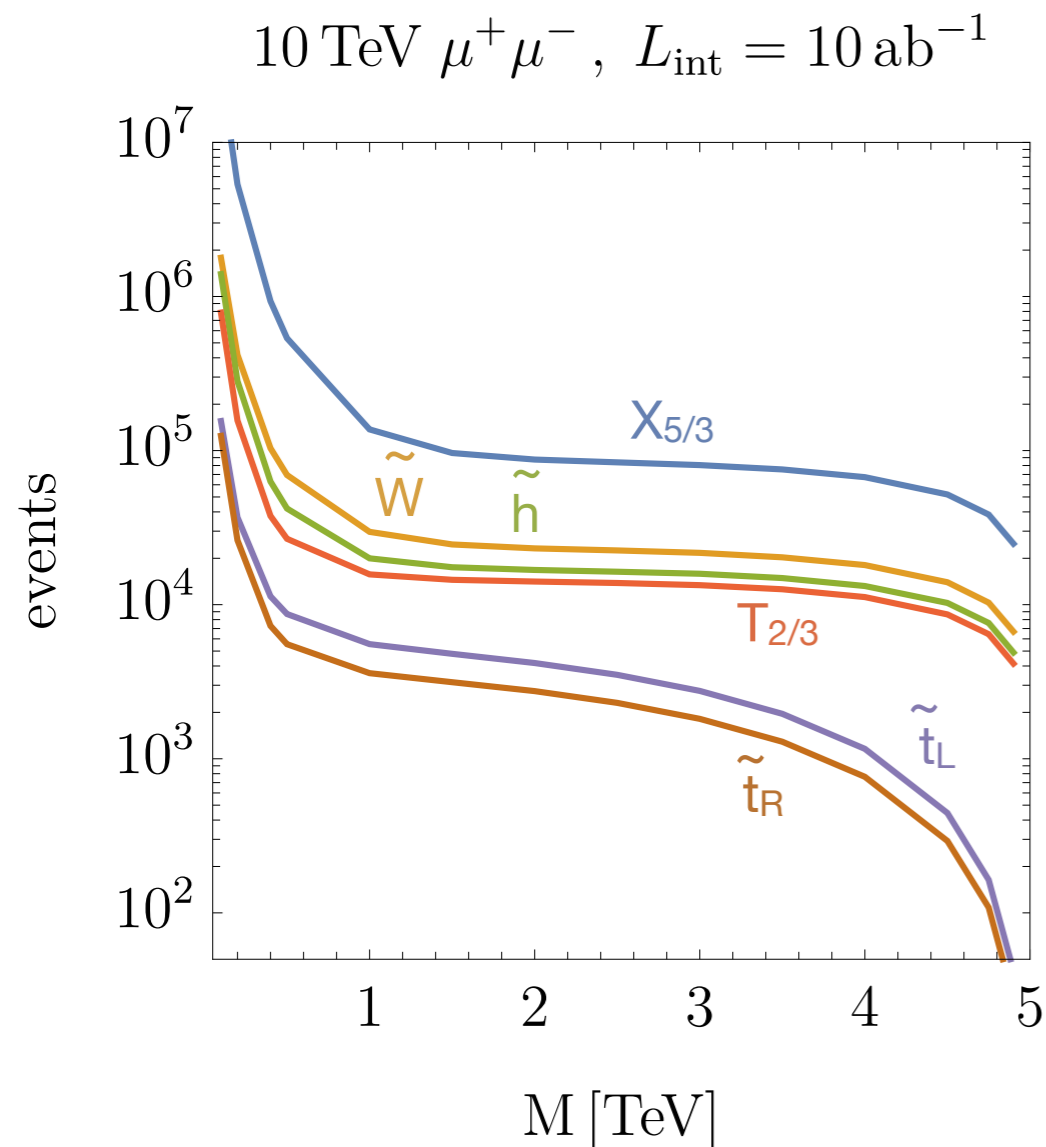
$$S_{B_J} = \sum_{I,l} \sigma_{B_J}^{I,l} \frac{2\pi\alpha_{\text{eff}}}{v_{\text{rel}}} R_J$$

branching ratio into SM

Sommerfeld

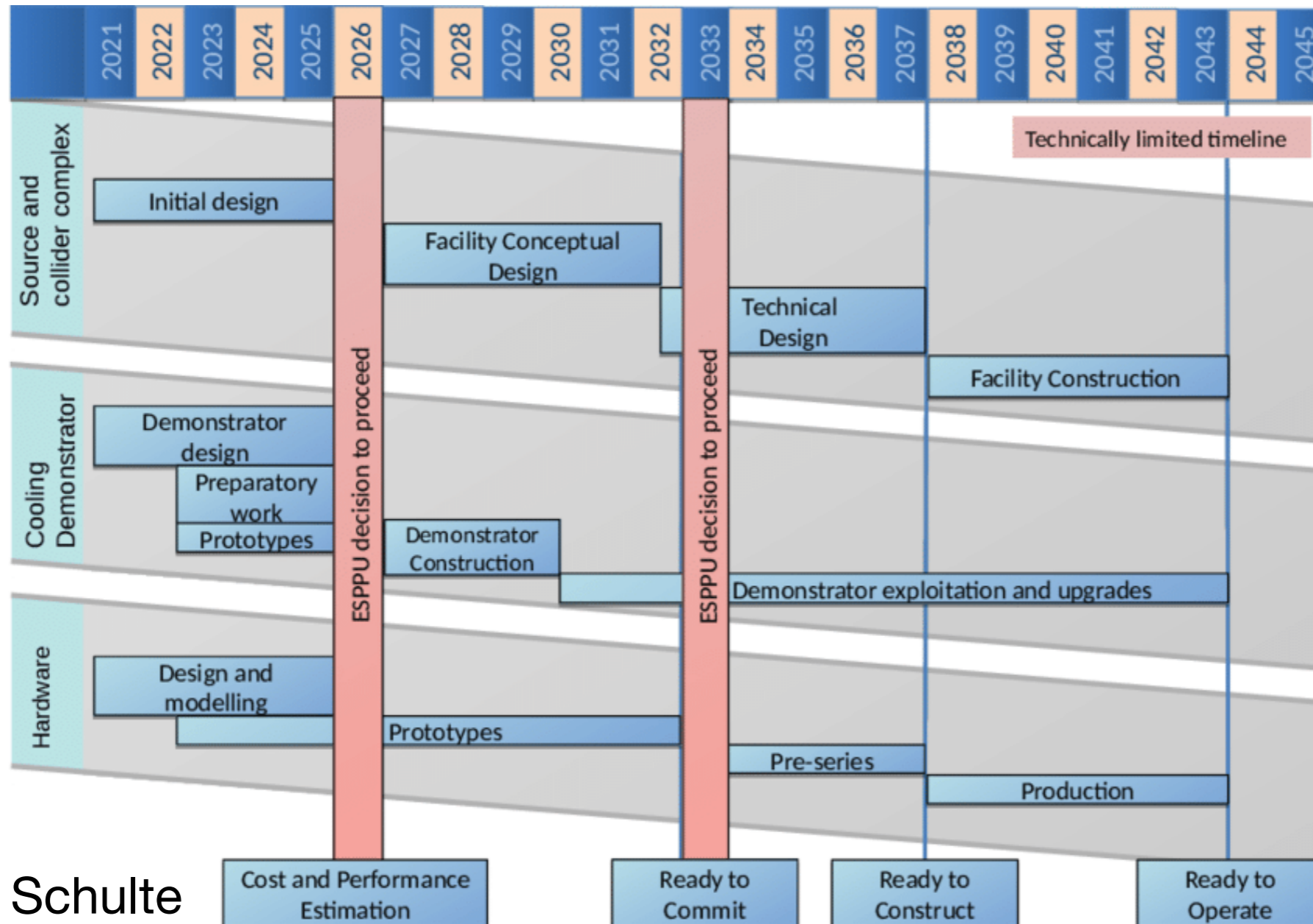
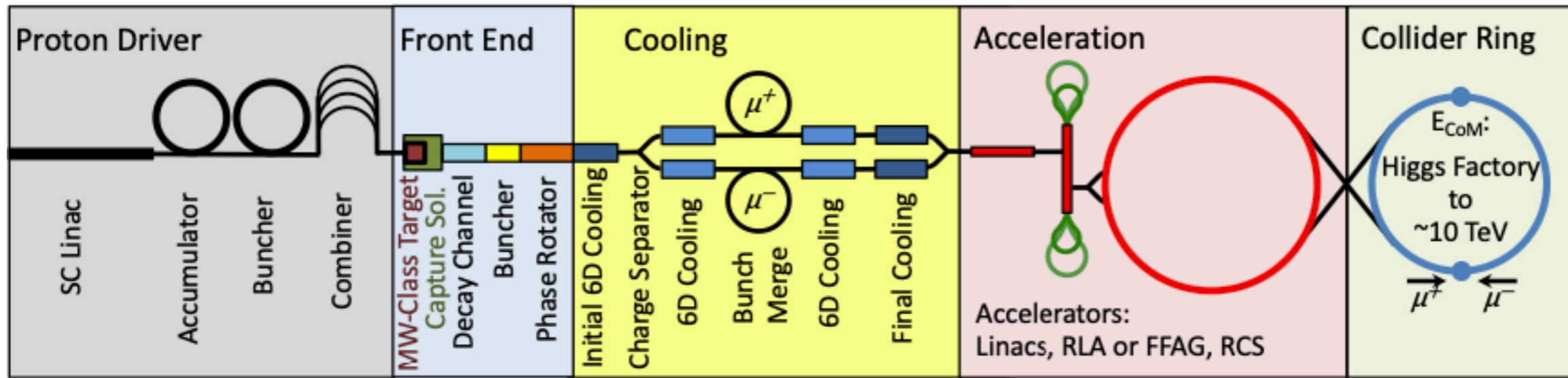
Muon collider physics: energy AND precision

- ◆ Pair-production of EW particles up to threshold



- ◆ Precision physics: Higgs boson physics comparable to Higgs factories
- ◆ High-energy probes: probe new physics at 100 TeV

Muon collider: possible timeline



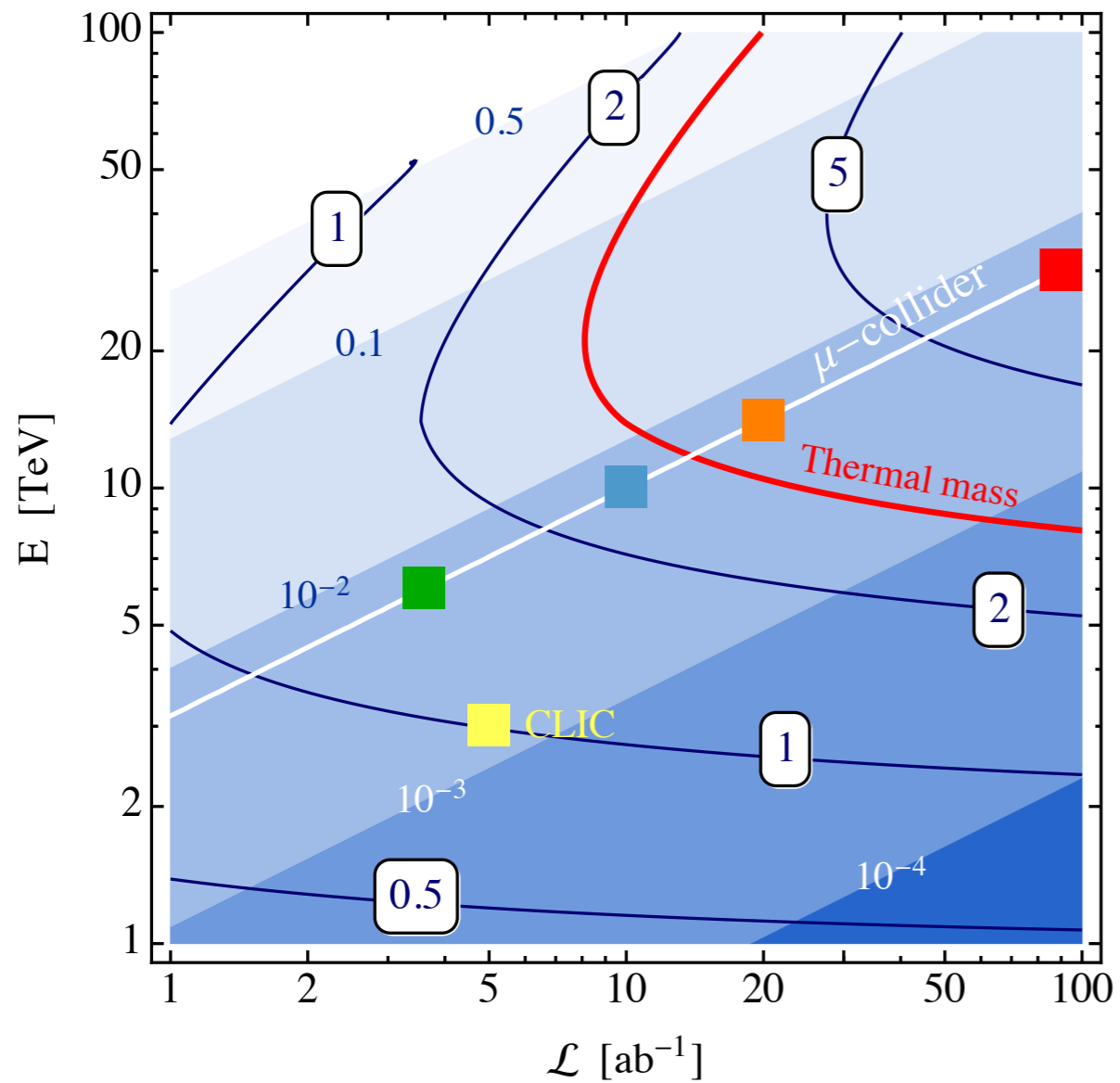
D. Schulte



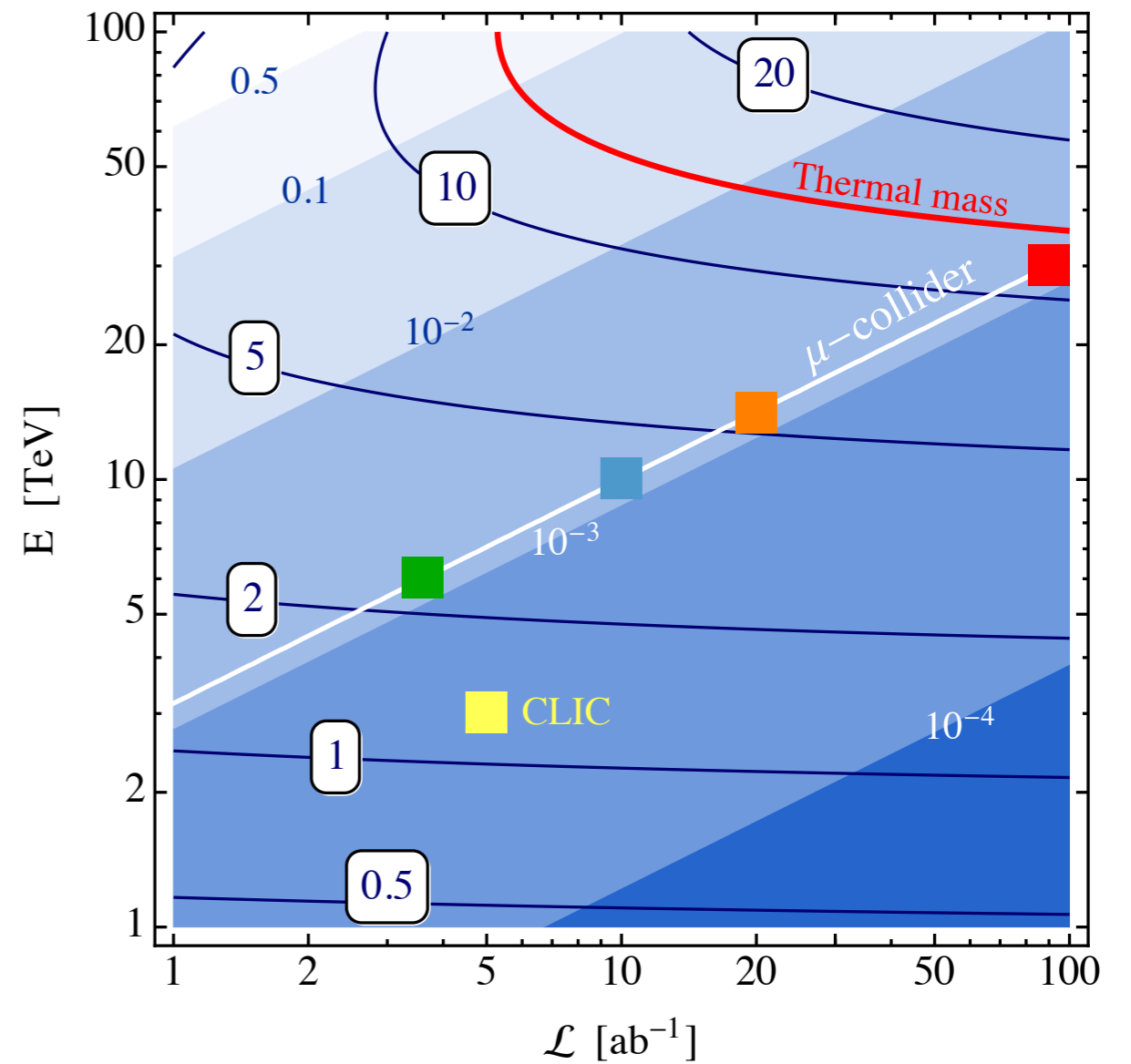
Reach at muon colliders

mono-W searches

Majorana 3-plet (Wino)



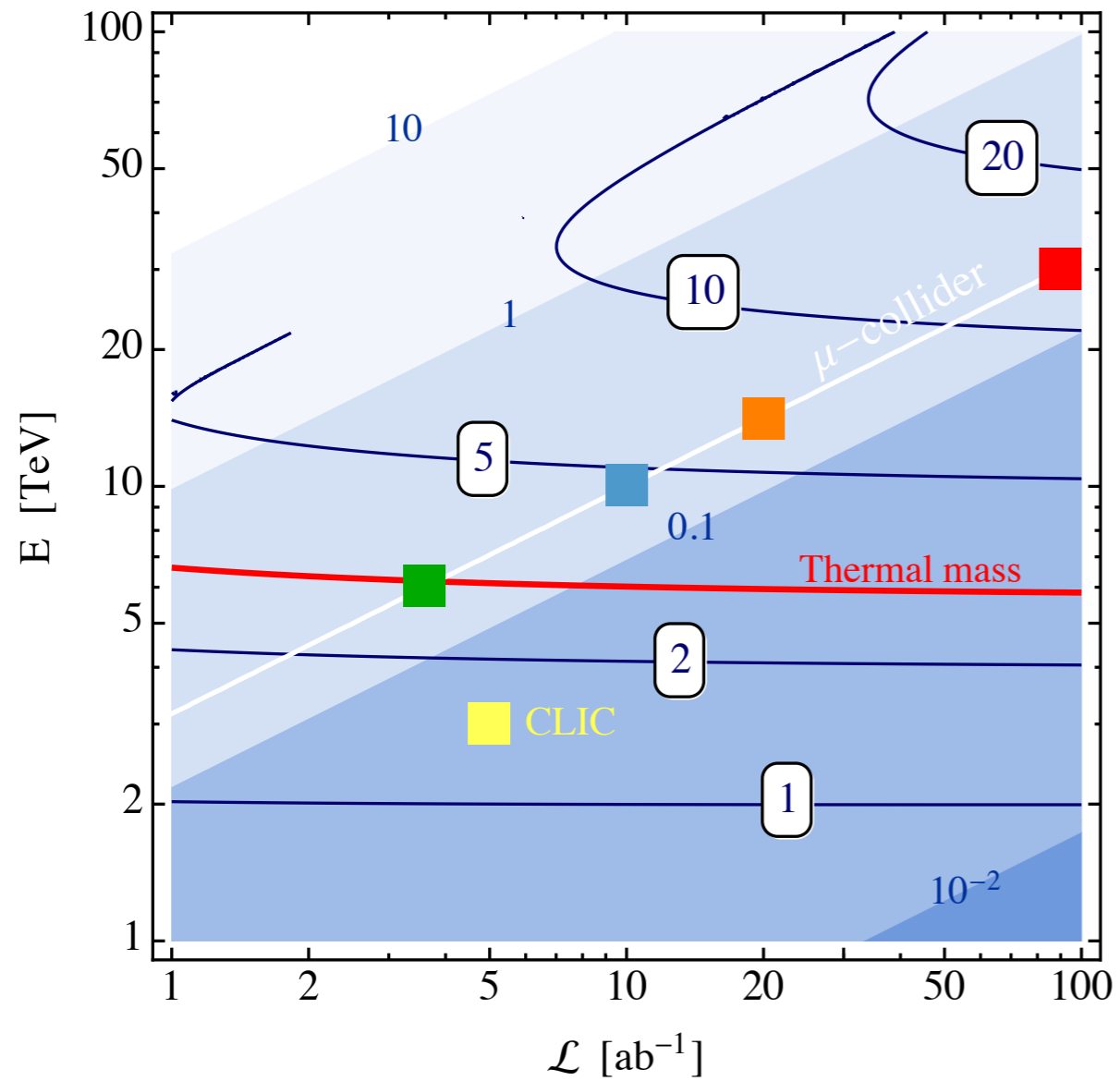
Majorana 5-plet (MDM)



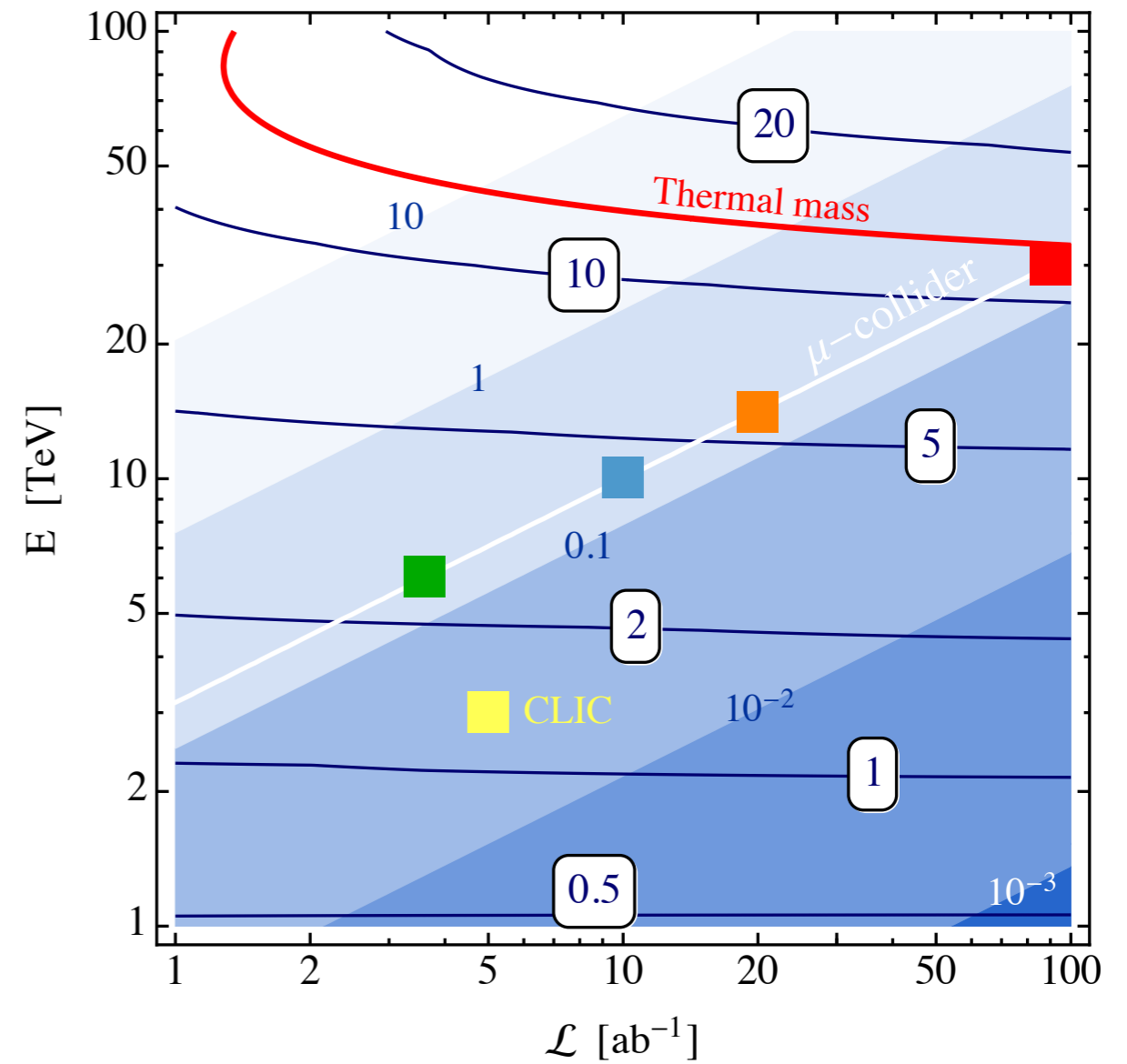
Reach at muon colliders

Disappearing track searches (mono- γ)

Majorana 3-plet (Wino)

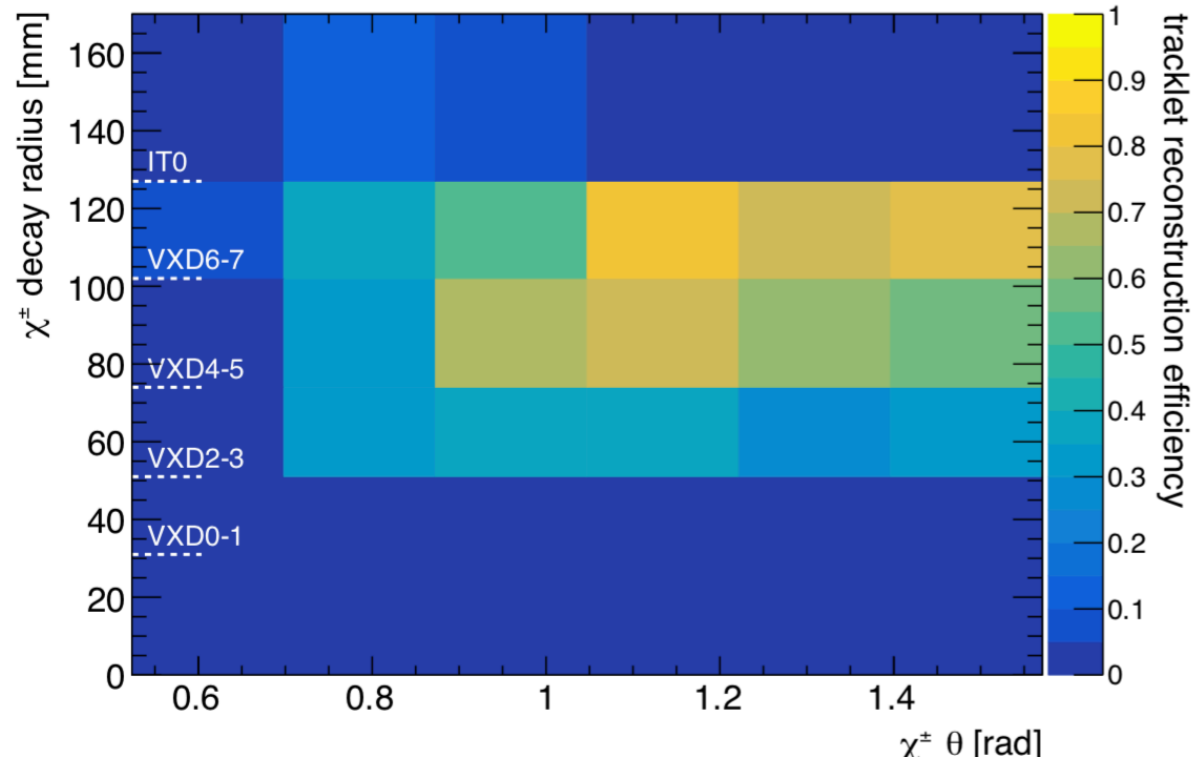


Majorana 5-plet (MDM)

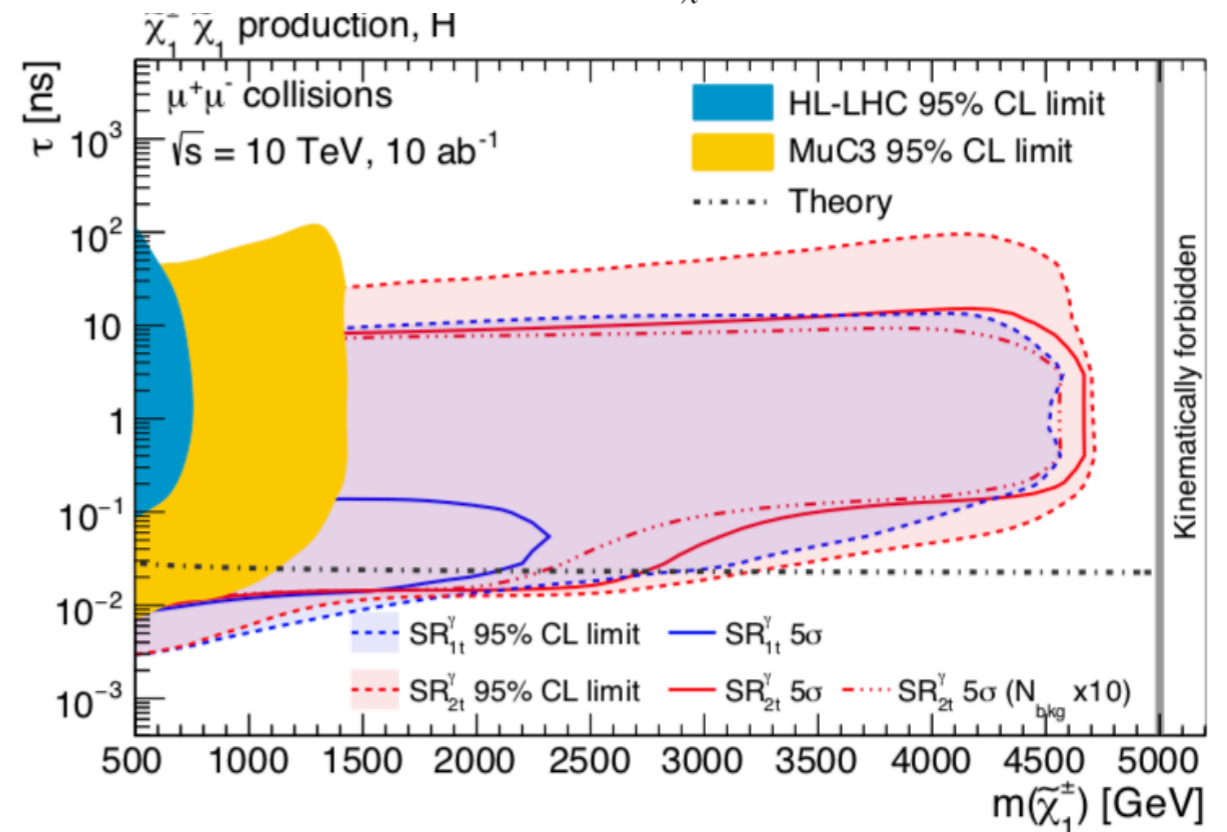
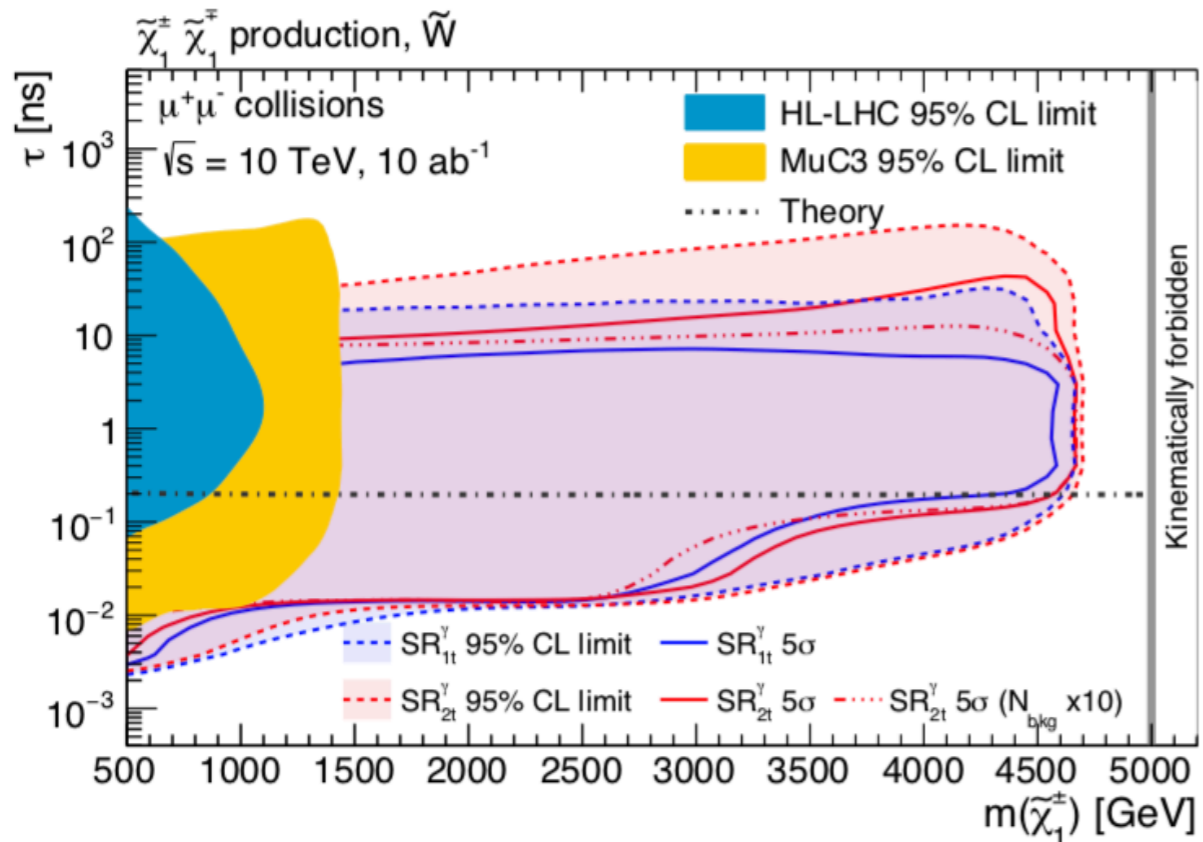
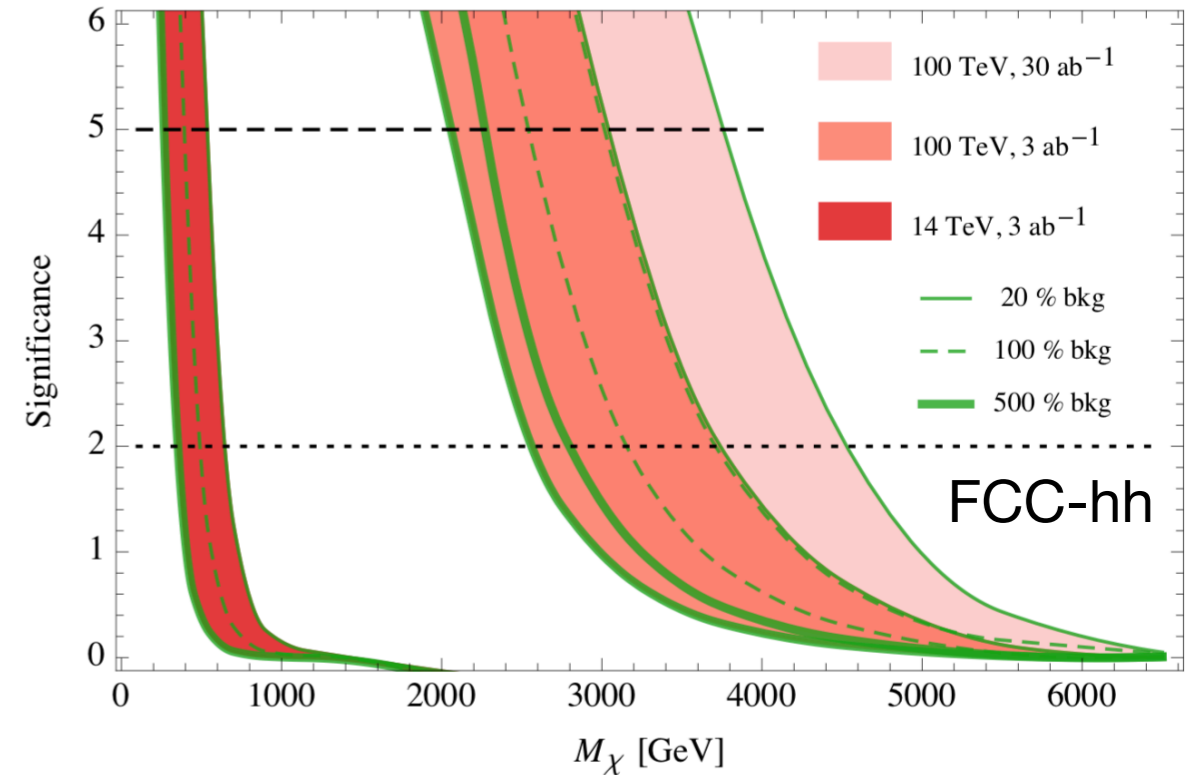


Disappearing tracks

Capdevilla, Meloni, Simoniello, Zurita 2102.11292

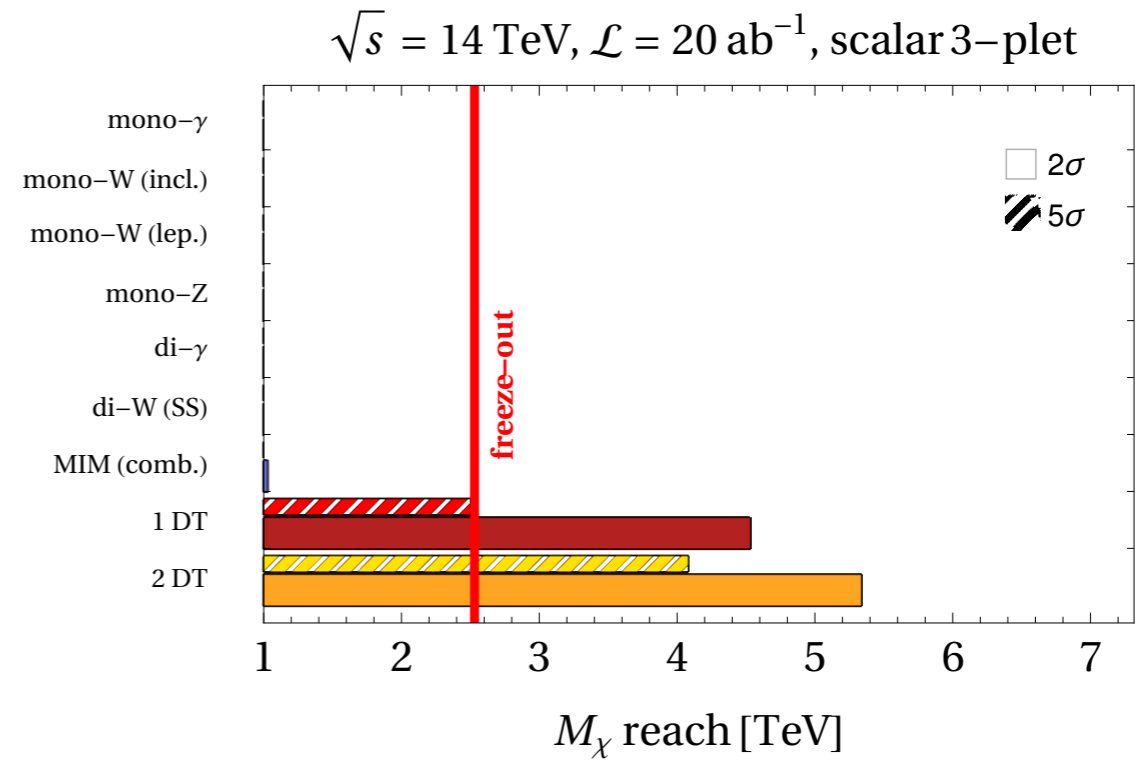
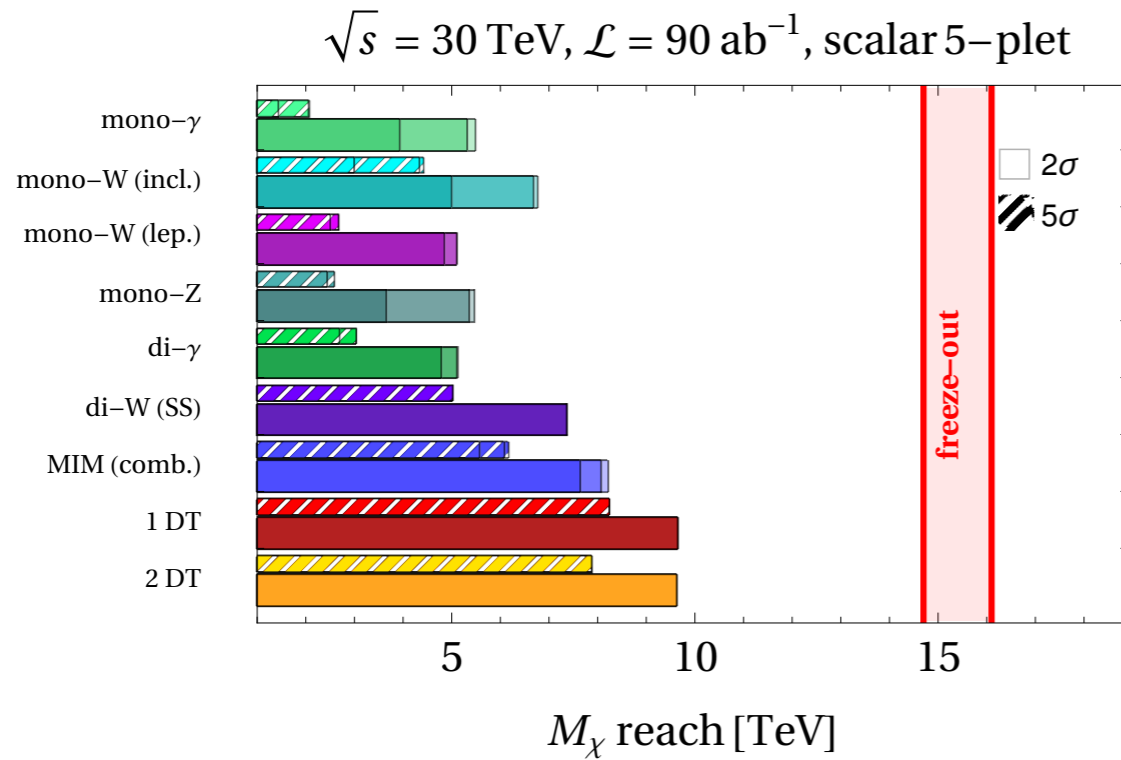


Cirelli, Sala, Taoso 1407.7058



Scalar WIMPs

- ◆ Scalars have lower cross-sections



- ◆ Higgs portal coupling
→ direct detection

