

EFT & Heavy Flavours : an experimentalist point of view

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Outline of the lectures

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- Introduction (context, EFT as seen from an experimentalist, LHCb)
- $B \rightarrow \ell^+ \ell^-$ what do we measure and how?
- $H_b \rightarrow H_s \ell^+ \ell^-$ what do we measure and how?

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- Why not electrons ?
- Some ideas to move forward

$B_{s/d} \rightarrow \mu^+ \mu^- :$

- clean prediction (relative precision $\sim 4 - 5 \%$)
- clean measurement for B_s ($\sim 10\%$) ; B_d not yet measured.

😊 clear road
 C_{10} constraint

$H_b \rightarrow H_s \mu^+ \mu^- :$

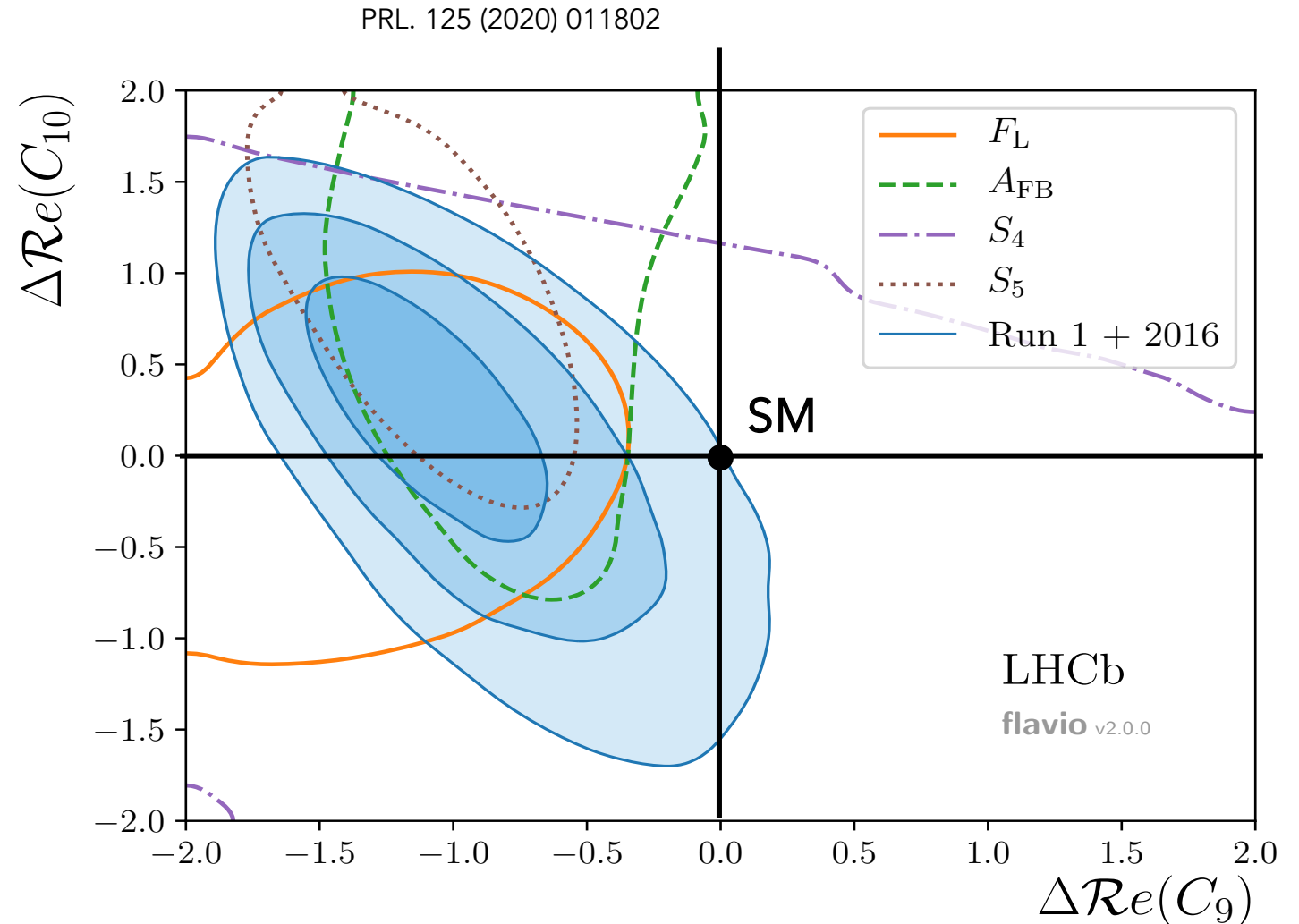
- clean measurements ($\sim 10\%$ on BR in various q^2 bins)
- TH predictions not very precise for the BR. Better for angular observables.
- How to mitigate/constraint the impact of non-local contributions ?

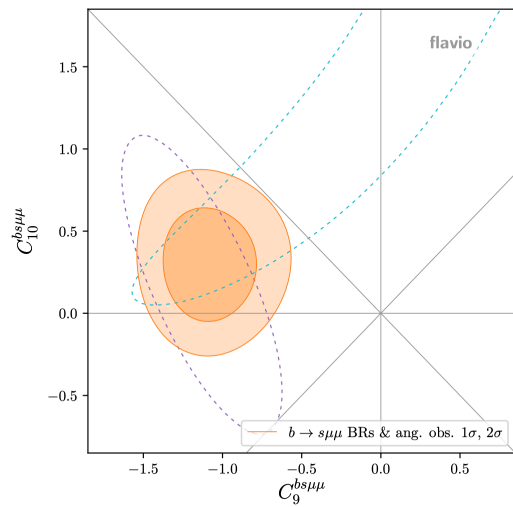
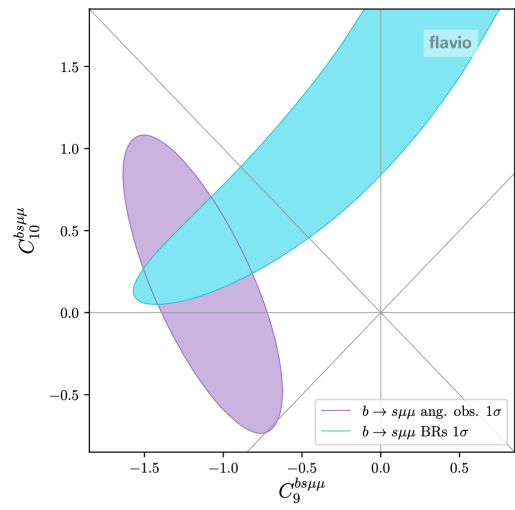
?????

$$C_i = C_i^{SM} + C_i^{NP}$$

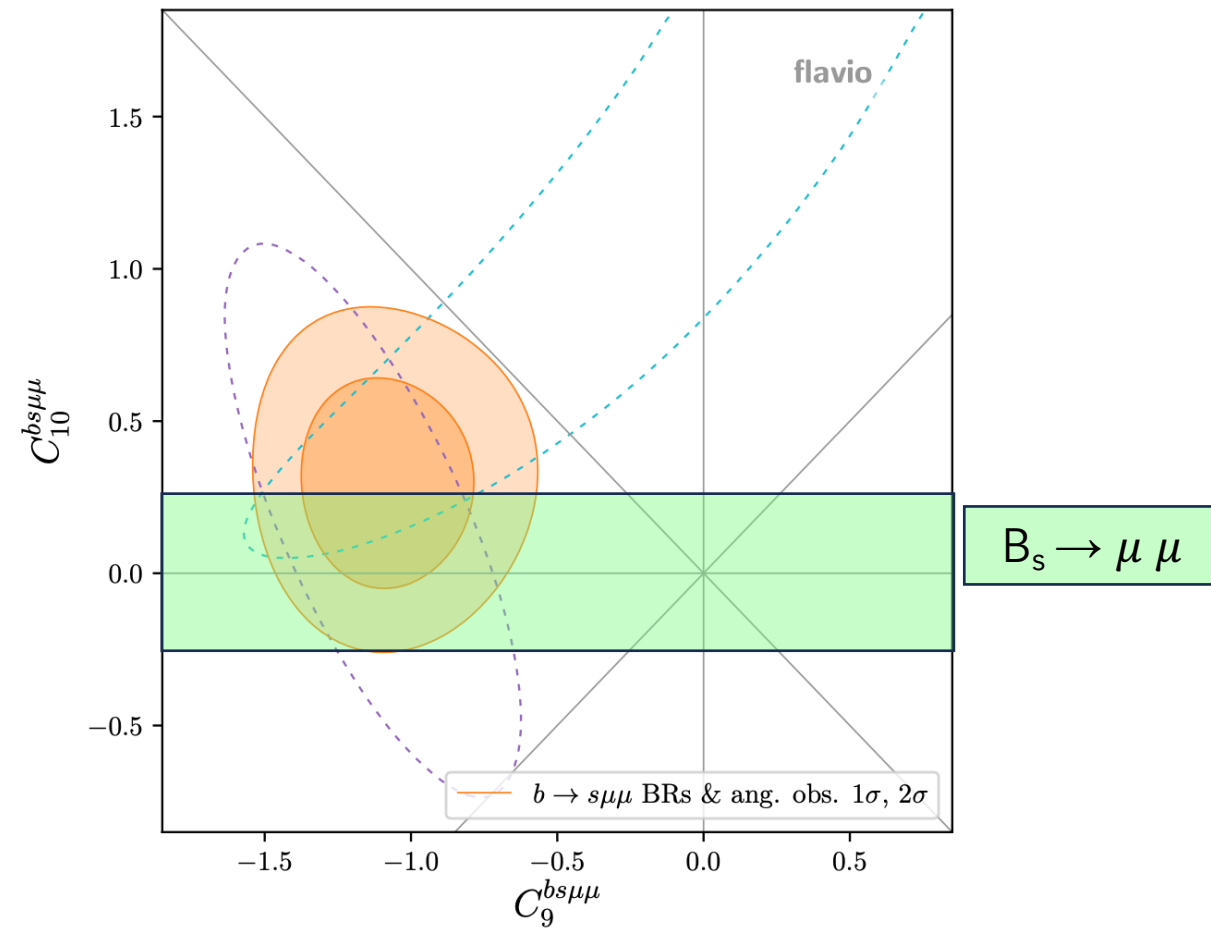
- In the SM Wilson coefficients are real, no necessarily the case for New Physics
- Many parameters fit... reduced configurations

$B \rightarrow K^* \mu \mu$ alone

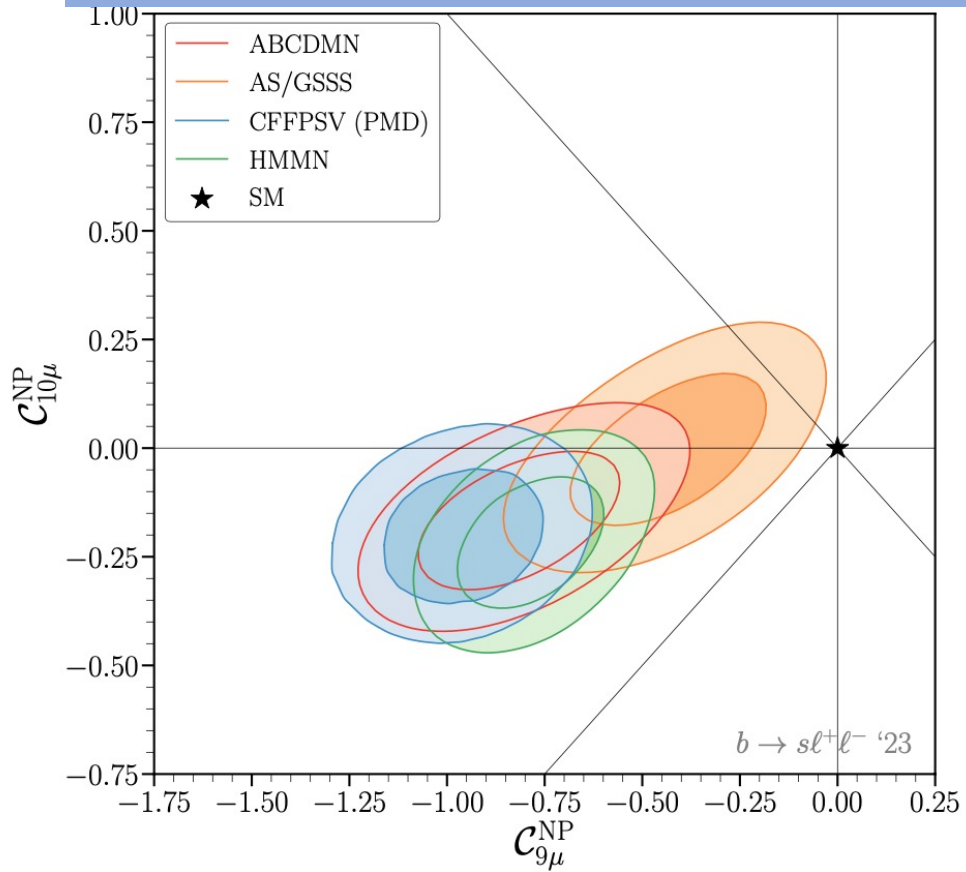




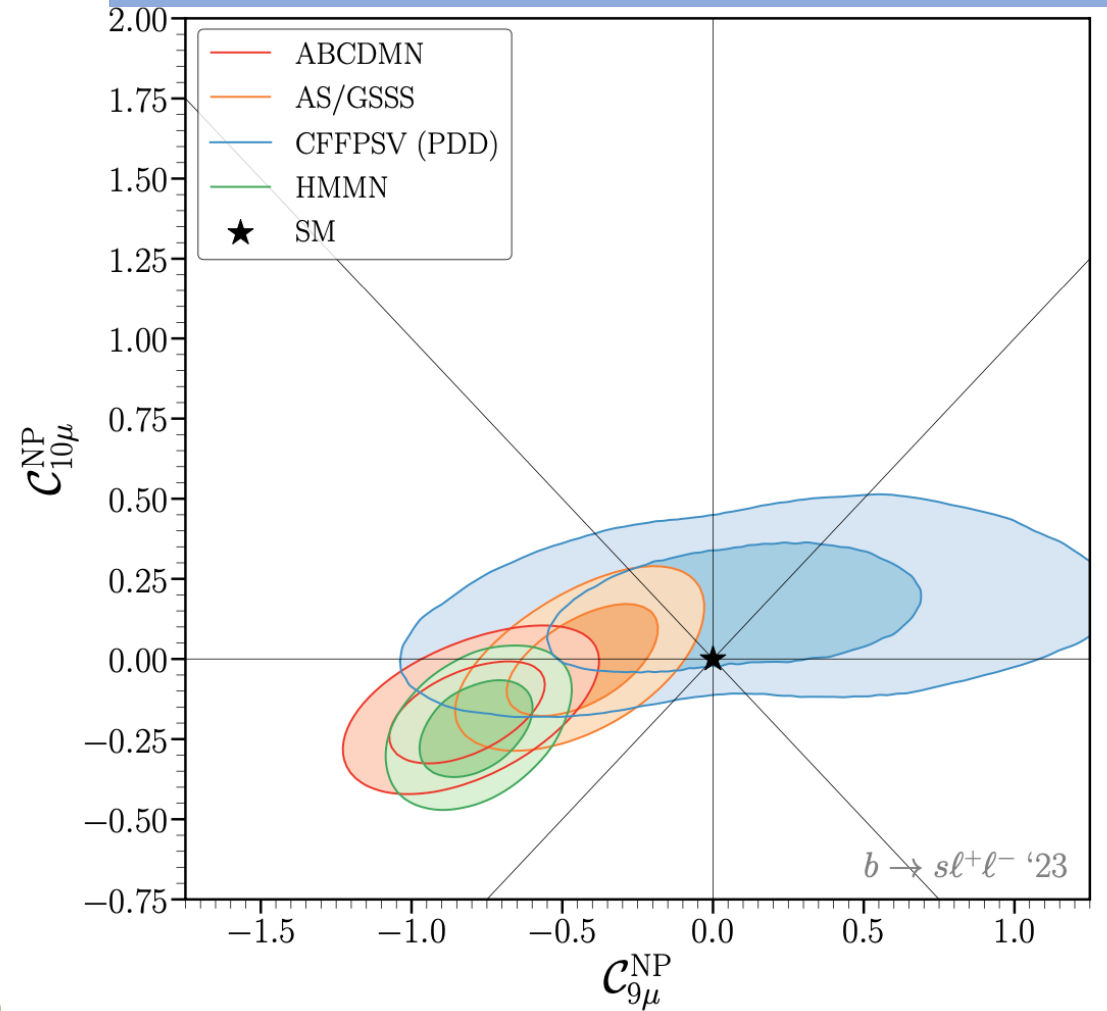
Adapted from plots from Peter Stangl La Thuile 2021



with TH input for the non-local contributions



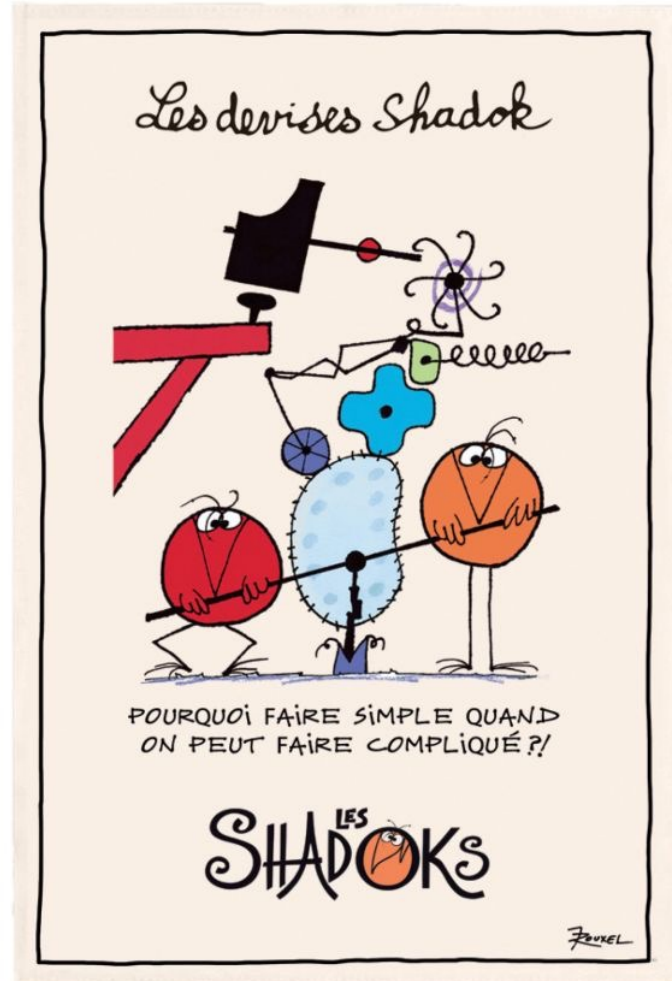
No TH input for the non-local contributions

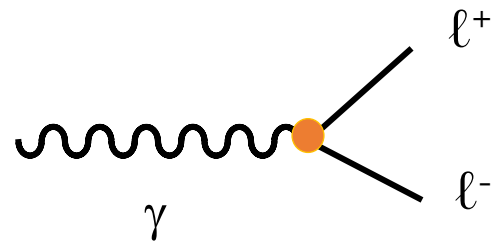
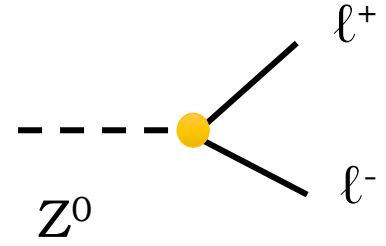
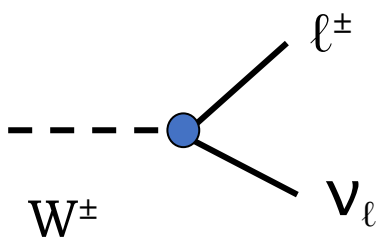


- ▶ **ABCDMN** (M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, M. Novoa-Brunet)
Statistical framework: χ^2 -fit, based on private code arXiv:2304.07330
- ▶ **AS / GSSS** (W. Altmannshofer, P. Stangl / A. Greljo, J. Salko, A. Smolkovic, P. Stangl)
Statistical framework: χ^2 -fit, based on public code `flavio` arXiv:2212.10497.
- ▶ **CFFPSV** (M. Ciuchini, M. Fedele, E. Franco, A. Paul, L. Silvestrini, M. Valli)
Statistical framework: Bayesian MCMC fit, based on public code `HEPfit` arXiv:2212.10516
- ▶ **HMMN** (T. Hurth, F. Mahmoudi, D. Martínez-Santos, S. Neshatpour)
Statistical framework: χ^2 -fit, based on public code `SuperIso` arXiv:23xx.xxxxxx

From B. Capdevila
FPCP 2023

Why not electrons ?

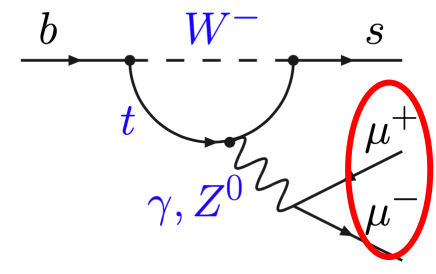
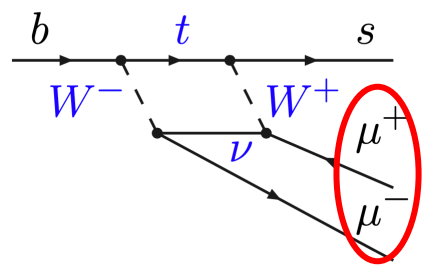




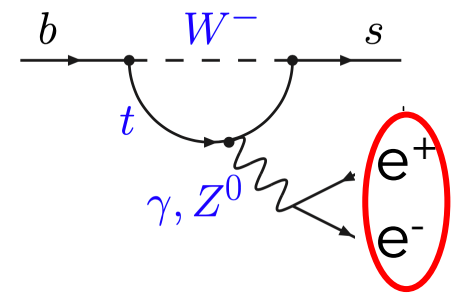
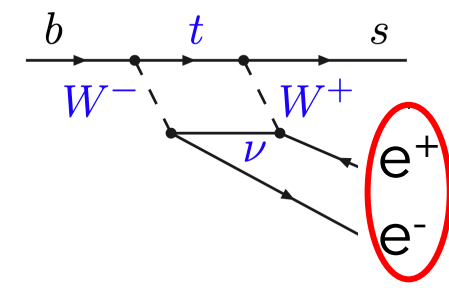
$\ell = e, \mu$ or τ

Only difference : kinematics (lepton masses)

SM

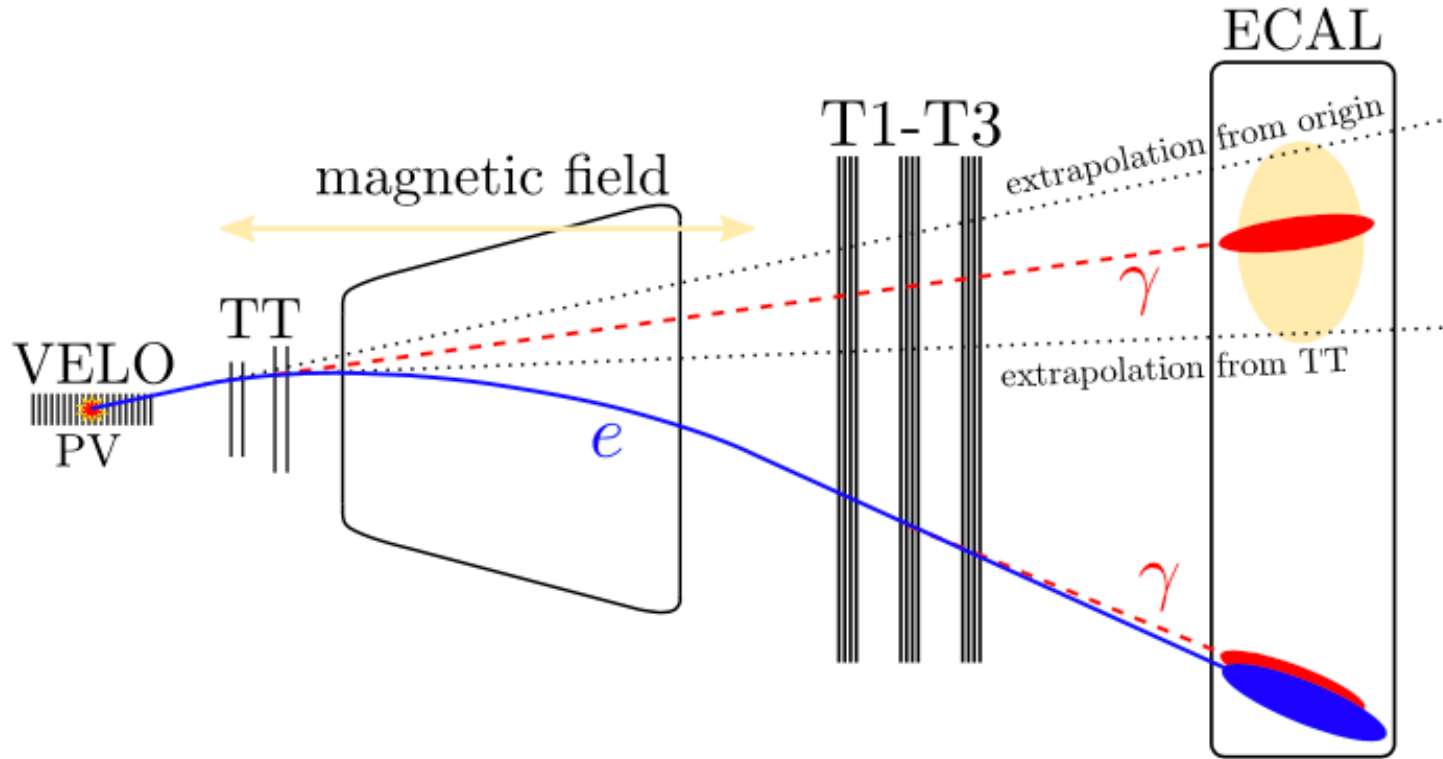


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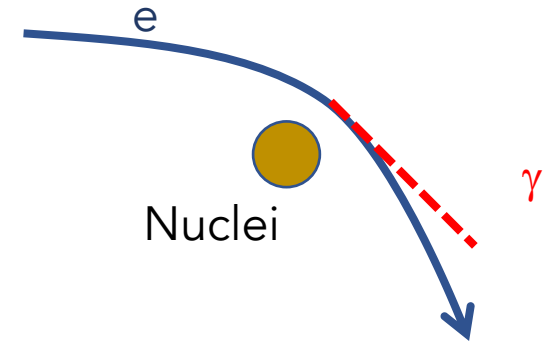


Let's use the electrons and double our statistics !

Electrons emit Bremsstrahlung



Energy loss $\propto E_e$
 Energy loss \propto material



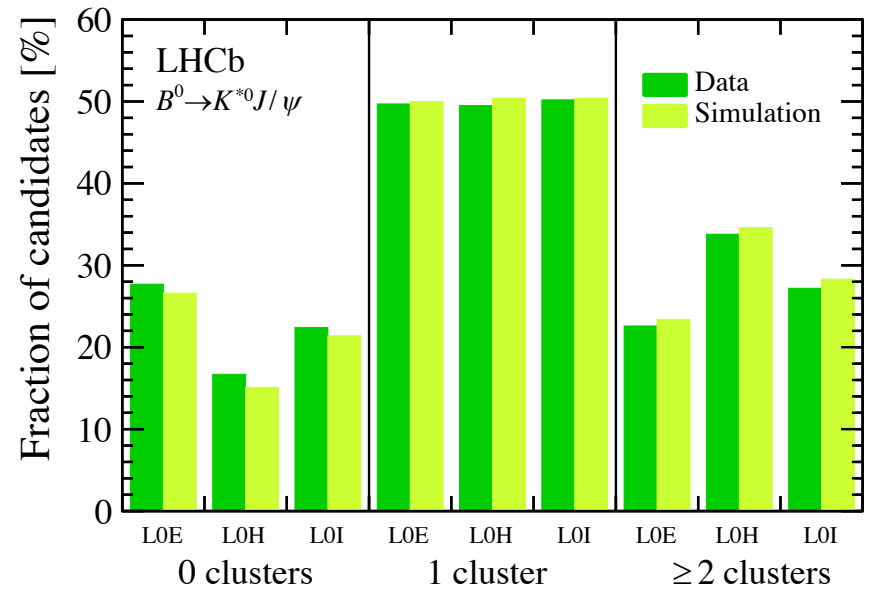
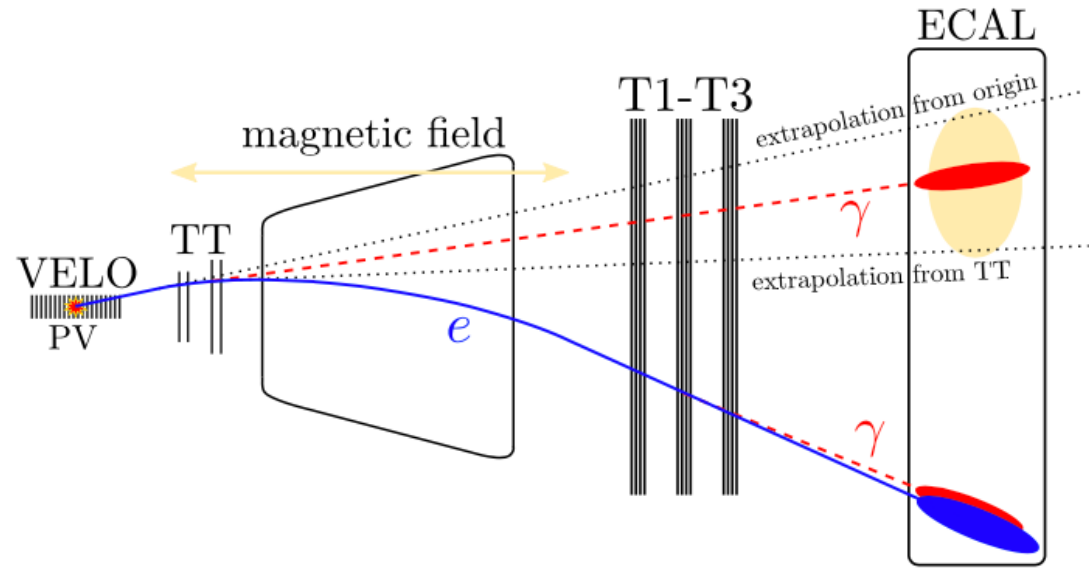
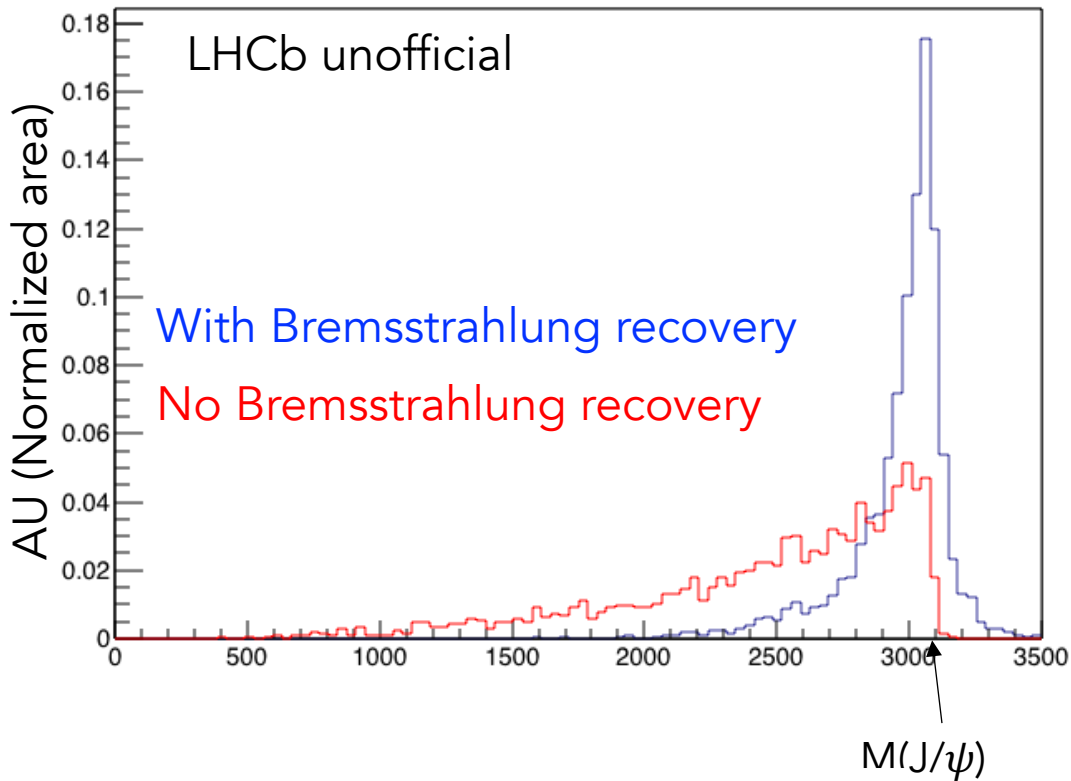
Before the magnet

- electron can be swept out (=lost !)
- kinematics are "wrong"

After the magnet

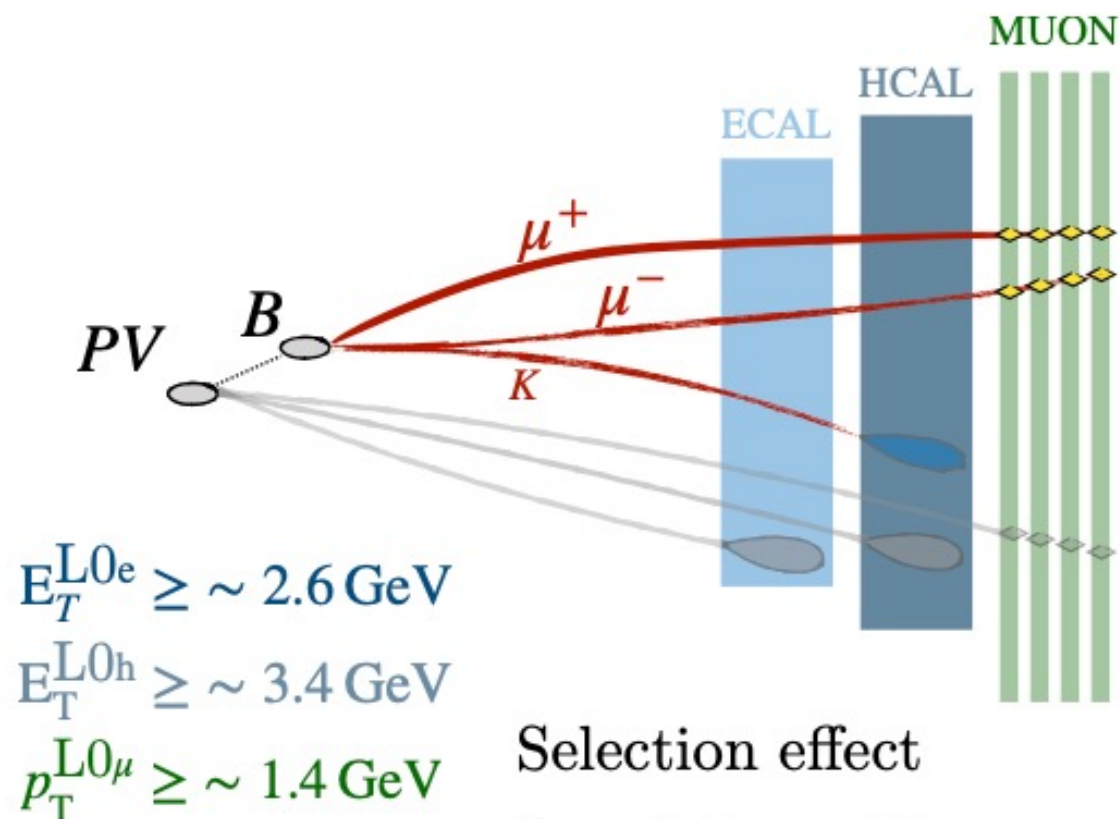
- not an issue

In both cases E/p is correct



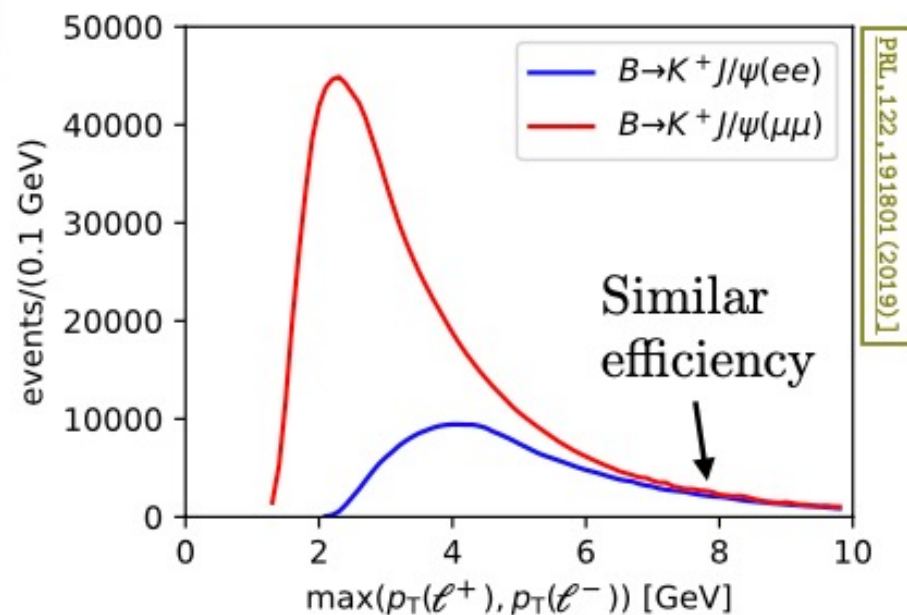
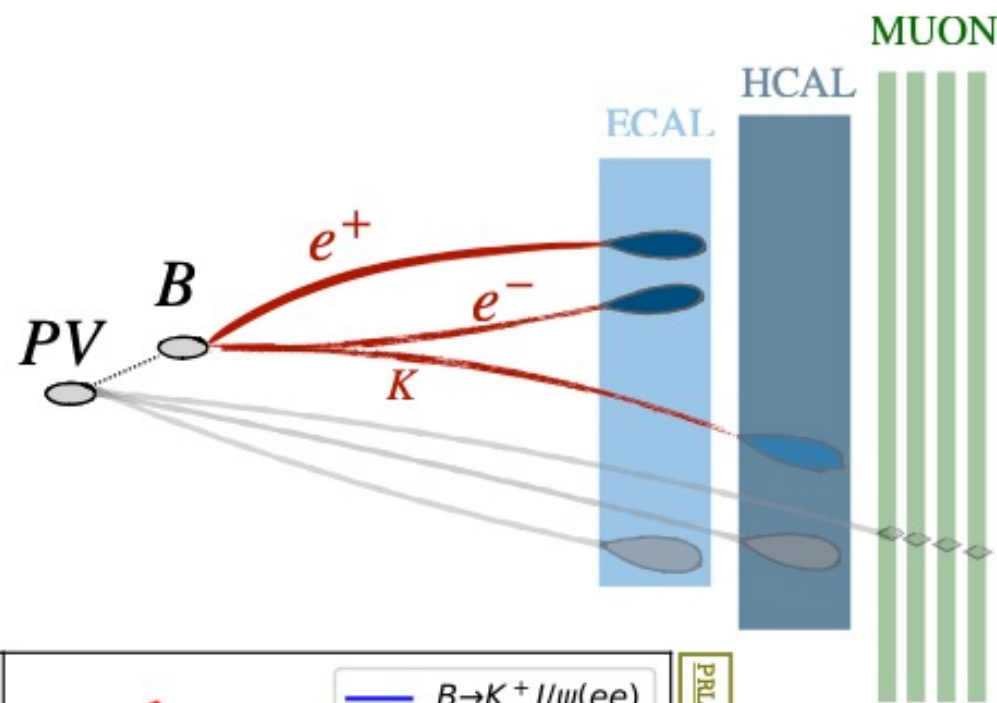
Bremsstrahlung recovery algorithm is $\sim 50\%$ efficient
 Well described in simulation

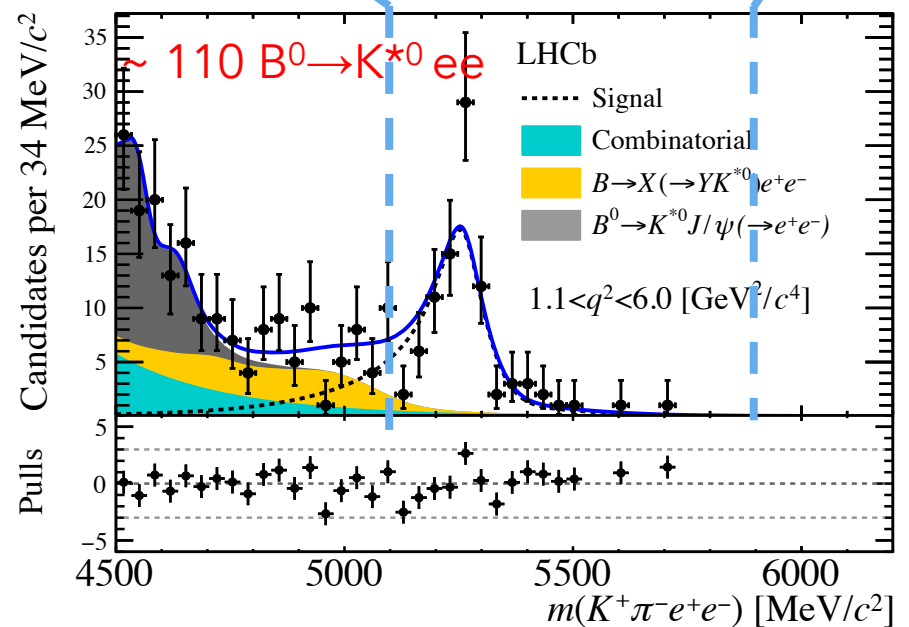
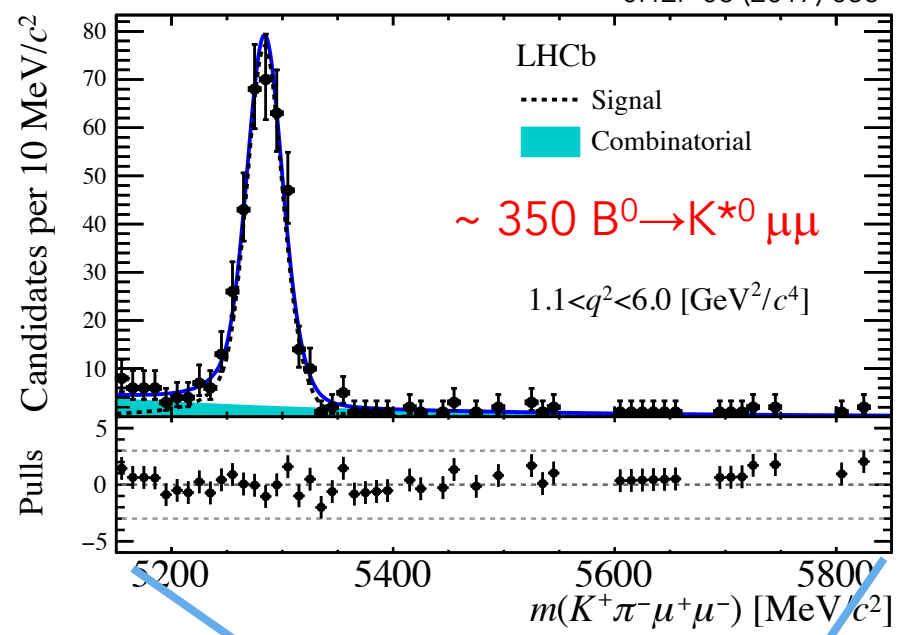
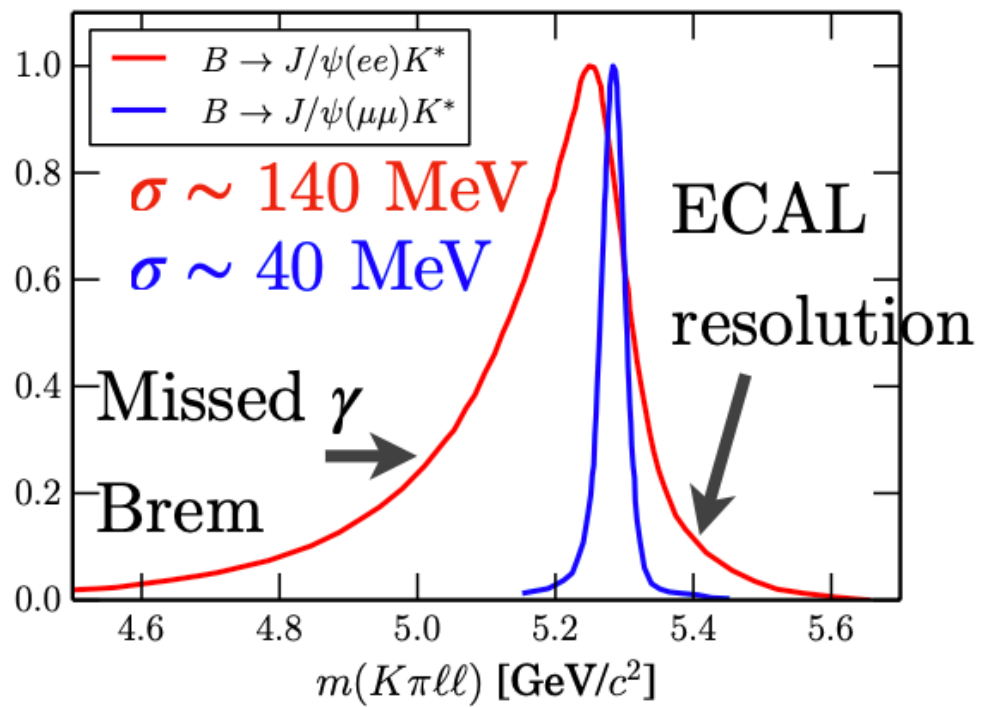
Hardware trigger is very different for electrons and muons



Selection effect
from L0e vs L0 μ

$$\sim \frac{1}{3}$$



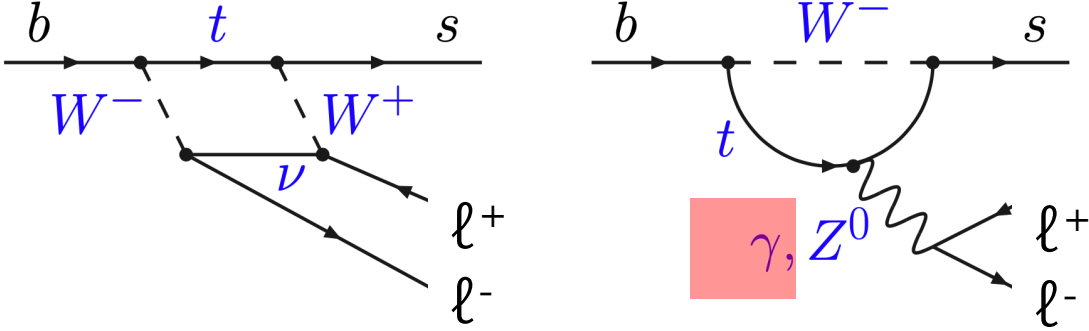


Using modes with electrons to increase the statistics is not the best idea

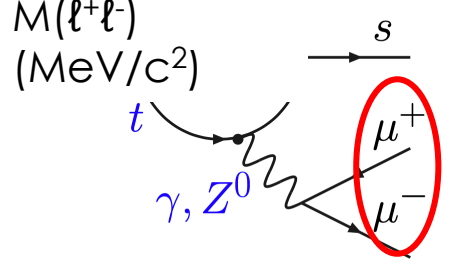
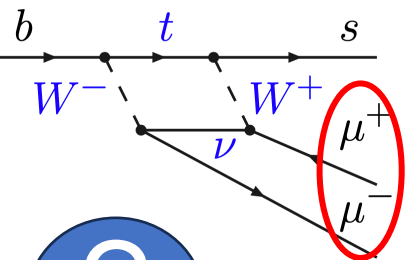
Use electrons for:

- measurements which cannot be done with muons

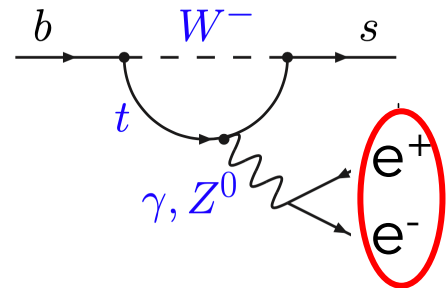
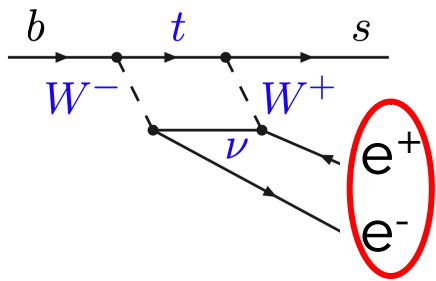
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- search for New Physics



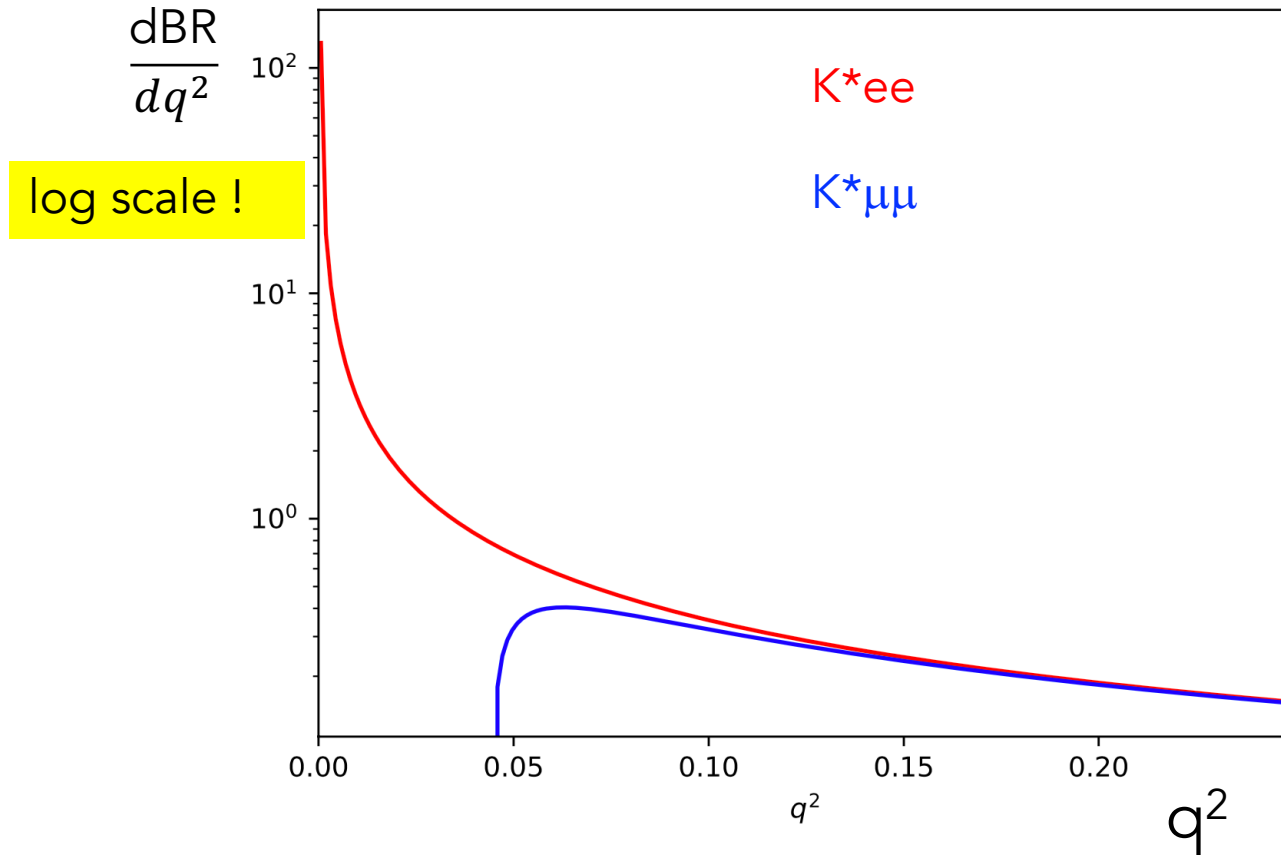
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2

1

$$B^0 \rightarrow K^{*0} \ell^+ \ell^- \times 10^6$$



Electrons should give us access to C_7 and C'_7 Wilson coefficients (photon pole) in a privileged manner

Going back to

$$s=q^2$$

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} =$$

$$\begin{aligned} & \frac{9}{32\pi} \left[I_1^s \sin^2\theta_K + I_1^c \cos^2\theta_K \right. \\ & + I_2^s \sin^2\theta_K \cos 2\theta_\ell + I_2^c \cos^2\theta_K \cos 2\theta_\ell \\ & + I_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + I_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi \\ & + I_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + I_6 \sin^2\theta_K \cos \theta_\ell \\ & + I_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + I_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi \\ & \left. + I_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi \right], \end{aligned}$$

$$\begin{aligned} I_1 = & \left\{ \frac{3}{4} [|A_{\perp L}|^2 + |A_{\parallel L}|^2 + (L \rightarrow R)] \left(1 - \frac{4m_l^2}{3s} \right) + \frac{4m_l^2}{s} \text{Re}(A_{\perp L} A_{\perp R}^* + A_{\parallel L} A_{\parallel R}^*) \right\} \sin^2\theta_{K^*} \\ & + \left\{ (|A_{0L}|^2 + |A_{0R}|^2) + \frac{4m_l^2}{s} [|A_t|^2 + 2\text{Re}(A_{0L} A_{0R}^*)] \right\} \cos^2\theta_{K^*}, \end{aligned} \quad (\text{A.6a})$$

$$I_2 = \left(1 - \frac{4m_l^2}{s} \right) \left[\frac{1}{4} (|A_{\perp L}|^2 + |A_{\parallel L}|^2) \sin^2\theta_{K^*} - |A_{0L}|^2 \cos^2\theta_{K^*} + (L \rightarrow R) \right], \quad (\text{A.6b})$$

$$I_3 = \frac{1}{2} \left(1 - \frac{4m_l^2}{s} \right) \left[(|A_{\perp L}|^2 - |A_{\parallel L}|^2) \sin^2\theta_{K^*} + (L \rightarrow R) \right], \quad (\text{A.6c})$$

$$I_4 = \frac{1}{\sqrt{2}} \left(1 - \frac{4m_l^2}{s} \right) \left[\text{Re}(A_{0L} A_{\parallel L}^*) \sin 2\theta_{K^*} + (L \rightarrow R) \right], \quad (\text{A.6d})$$

$$I_5 = \sqrt{2} \left(1 - \frac{4m_l^2}{s} \right)^{1/2} \left[\text{Re}(A_{0L} A_{\perp L}^*) \sin 2\theta_{K^*} - (L \rightarrow R) \right], \quad (\text{A.6e})$$

$$I_6 = 2 \left(1 - \frac{4m_l^2}{s} \right)^{1/2} \left[\text{Re}(A_{\parallel L} A_{\perp L}^*) \sin^2\theta_{K^*} - (L \rightarrow R) \right], \quad (\text{A.6f})$$

$$I_7 = \sqrt{2} \left(1 - \frac{4m_l^2}{s} \right)^{1/2} \left[\text{Im}(A_{0L} A_{\parallel L}^*) \sin 2\theta_{K^*} - (L \rightarrow R) \right], \quad (\text{A.6g})$$

$$I_8 = \frac{1}{\sqrt{2}} \left(1 - \frac{4m_l^2}{s} \right) \left[\text{Im}(A_{0L} A_{\perp L}^*) \sin 2\theta_{K^*} + (L \rightarrow R) \right], \quad (\text{A.6h})$$

$$I_9 = \left(1 - \frac{4m_l^2}{s} \right) \left[\text{Im}(A_{\parallel L}^* A_{\perp L}) \sin^2\theta_{K^*} + (L \rightarrow R) \right]. \quad (\text{A.6i})$$

Going back to

$$s=q^2$$

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} =$$

$$\begin{aligned} & \frac{9}{32\pi} \left[I_1^s \sin^2 \theta_K + I_1^c \cos^2 \theta_K \right. \\ & + I_2^s \sin^2 \theta_K \cos 2\theta_\ell + I_2^c \cos^2 \theta_K \cos 2\theta_\ell \\ & + I_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + I_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi \\ & + I_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + I_6 \sin^2 \theta_K \cos \theta_\ell \\ & + I_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + I_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi \\ & \left. + I_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right], \end{aligned}$$

$$4m_l^2 \ll q^2$$

$$\begin{aligned} I_1 = & \left\{ \frac{3}{4} [|A_{\perp L}|^2 + |A_{\parallel L}|^2 + (L \rightarrow R)] \left(1 - \frac{4m_l^2}{3s} \right) + \frac{4m_l^2}{s} \text{Re}(A_{\perp L} A_{\perp R}^* + A_{\parallel L} A_{\parallel R}^*) \right\} \sin^2 \theta_{K^*} \\ & + \left\{ (|A_{0L}|^2 + |A_{0R}|^2) + \frac{4m_l^2}{s} [|A_{\perp L}|^2 + |A_{\parallel L}|^2 + 2\text{Re}(A_{0L} A_{0R}^*)] \right\} \cos^2 \theta_{K^*}, \end{aligned} \quad (\text{A.6a})$$

$$I_2 = \left(1 - \frac{4m_l^2}{s} \right) \left[\frac{1}{4} (|A_{\perp L}|^2 + |A_{\parallel L}|^2) \sin^2 \theta_{K^*} - |A_{0L}|^2 \cos^2 \theta_{K^*} + (L \rightarrow R) \right], \quad (\text{A.6b})$$

$$I_3 = \frac{1}{2} \left(1 - \frac{4m_l^2}{s} \right) \left[(|A_{\perp L}|^2 - |A_{\parallel L}|^2) \sin^2 \theta_{K^*} + (L \rightarrow R) \right], \quad (\text{A.6c})$$

$$I_4 = \frac{1}{\sqrt{2}} \left(1 - \frac{4m_l^2}{s} \right) \left[\text{Re}(A_{0L} A_{\parallel L}^*) \sin 2\theta_{K^*} + (L \rightarrow R) \right], \quad (\text{A.6d})$$

$$I_5 = \sqrt{2} \left(1 - \frac{4m_l^2}{s} \right)^{1/2} \left[\text{Re}(A_{0L} A_{\perp L}^*) \sin 2\theta_{K^*} - (L \rightarrow R) \right], \quad (\text{A.6e})$$

$$I_6 = 2 \left(1 - \frac{4m_l^2}{s} \right)^{1/2} \left[\text{Re}(A_{\parallel L} A_{\perp L}^*) \sin^2 \theta_{K^*} - (L \rightarrow R) \right], \quad (\text{A.6f})$$

$$I_7 = \sqrt{2} \left(1 - \frac{4m_l^2}{s} \right)^{1/2} \left[\text{Im}(A_{0L} A_{\parallel L}^*) \sin 2\theta_{K^*} - (L \rightarrow R) \right], \quad (\text{A.6g})$$

$$I_8 = \frac{1}{\sqrt{2}} \left(1 - \frac{4m_l^2}{s} \right) \left[\text{Im}(A_{0L} A_{\perp L}^*) \sin 2\theta_{K^*} + (L \rightarrow R) \right], \quad (\text{A.6h})$$

$$I_9 = \left(1 - \frac{4m_l^2}{s} \right) \left[\text{Im}(A_{\parallel L}^* A_{\perp L}) \sin^2 \theta_{K^*} + (L \rightarrow R) \right]. \quad (\text{A.6i})$$

At low q^2 (FF simplification)

$$\hat{s} = \frac{q^2}{m_B^2}$$

$$A_{\perp L,R} = \sqrt{2} N m_B (1 - \hat{s}) \left[(C_9^{\text{eff}} \mp C_{10}) + \frac{2\hat{m}_b}{\hat{s}} (C_7^{\text{eff}} + C_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*}),$$

$$A_{\parallel L,R} = -\sqrt{2} N m_B (1 - \hat{s}) \left[(C_9^{\text{eff}} \mp C_{10}) + \frac{2\hat{m}_b}{\hat{s}} (C_7^{\text{eff}} - C_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*}),$$

$$A_{0L,R} = -\frac{N m_B}{2\hat{m}_{K^*} \sqrt{\hat{s}}} (1 - \hat{s})^2 \left[(C_9^{\text{eff}} \mp C_{10}) + 2\hat{m}_b (C_7^{\text{eff}} - C_7^{\text{eff}'}) \right] \xi_{\parallel}(E_{K^*}),$$

Definition of observables:

$$F_L(q^2) = \frac{|A_0|^2}{|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2}$$

“clean”

$$A_T^{(\text{re})}(q^2) = \frac{2 \text{Re}[A_{\parallel}^L(q^2) A_{\perp}^{L*}(q^2) - A_{\parallel}^R(q^2) A_{\perp}^{R*}(q^2)]}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2}$$

$$A_T^{(2)}(q^2) = \frac{|A_{\perp}(q^2)|^2 - |A_{\parallel}(q^2)|^2}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2}$$

$$A_T^{(\text{im})}(q^2) = \frac{2 \text{Im}[A_{\parallel}^L(q^2) A_{\perp}^{L*}(q^2) + A_{\parallel}^R(q^2) A_{\perp}^{R*}(q^2)]}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2},$$

At low q^2 (FF simplification)

$$\hat{s} = \frac{q^2}{m_B^2}$$

$q^2 \rightarrow 0$

$$A_{\perp L,R} = \sqrt{2} N m_B (1 - \cancel{\beta}) \left[(\cancel{C_9^{\text{eff}} + C_{10}}) + \frac{2\hat{m}_b}{\hat{s}} (C_7^{\text{eff}} + C_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*}),$$

$$A_{\parallel L,R} = -\sqrt{2} N m_B (1 - \cancel{\beta}) \left[(\cancel{C_9^{\text{eff}} + C_{10}}) + \frac{2\hat{m}_b}{\hat{s}} (C_7^{\text{eff}} - C_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*}),$$

$$A_{0L,R} = -\frac{N m_B}{2\hat{m}_{K^*} \sqrt{\hat{s}}} (1 - \cancel{\beta})^2 \left[(\cancel{C_9^{\text{eff}} + C_{10}}) + 2\hat{m}_b (C_7^{\text{eff}} - C_7^{\text{eff}'}) \right] \xi_{\parallel}(E_{K^*}),$$

Definition of observables:

“clean”

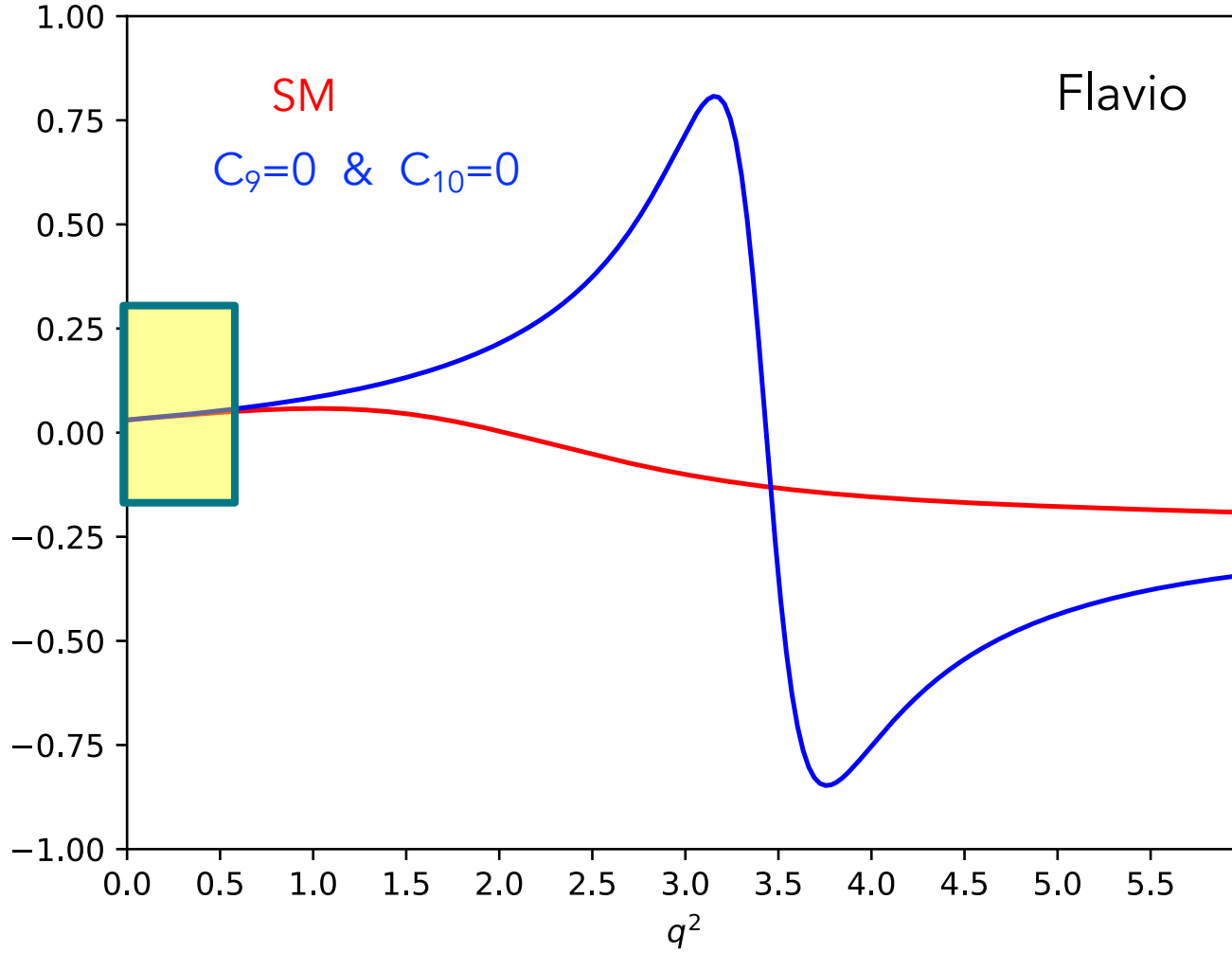
$$A_T^{(\text{re})}(q^2) = \frac{2 \text{Re}[A_{\parallel}^L(q^2) A_{\perp}^{L*}(q^2) - A_{\parallel}^R(q^2) A_{\perp}^{R*}(q^2)]}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2}$$

$$A_T^{(2)}(q^2) = \frac{|A_{\perp}(q^2)|^2 - |A_{\parallel}(q^2)|^2}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2} \quad \text{sensitive to the photon polarisation}$$

$$A_T^{(\text{im})}(q^2) = \frac{2 \text{Im}[A_{\parallel}^L(q^2) A_{\perp}^{L*}(q^2) + A_{\parallel}^R(q^2) A_{\perp}^{R*}(q^2)]}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2},$$

$$F_L(q^2) = \frac{|A_0|^2}{|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2}$$

A_T^2 for $B^0 \rightarrow K^{*0} e^+ e^-$



$$A_T^{(2)}(q^2) = \frac{|A_{\perp}(q^2)|^2 - |A_{\parallel}(q^2)|^2}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2}$$

$$I_1 = \left\{ \frac{3}{4} [|A_{\perp L}|^2 + |A_{\parallel L}|^2 + (L \rightarrow R)] \left(1 - \frac{4m_l^2}{3s} \right) + \frac{4m_l^2}{s} \text{Re}(A_{\perp L} A_{\perp R}^* + A_{\parallel L} A_{\parallel R}^*) \right\} \sin^2 \theta_{K^*} \\ + \left\{ (|A_{0L}|^2 + |A_{0R}|^2) + \frac{4m_l^2}{s} [|A_t|^2 + 2\text{Re}(A_{0L} A_{0R}^*)] \right\} \cos^2 \theta_{K^*},$$

$$I_2 = \left(1 - \frac{4m_l^2}{s} \right) \left[\frac{1}{4} (|A_{\perp L}|^2 + |A_{\parallel L}|^2) \sin^2 \theta_{K^*} - |A_{0L}|^2 \cos^2 \theta_{K^*} + (L \rightarrow R) \right],$$

$$I_3 = \frac{1}{2} \left(1 - \frac{4m_l^2}{s} \right) \left[(|A_{\perp L}|^2 - |A_{\parallel L}|^2) \sin^2 \theta_{K^*} + (L \rightarrow R) \right],$$

$$I_4 = \frac{1}{\sqrt{2}} \left(1 - \frac{4m_l^2}{s} \right) \left[\text{Re}(A_{0L} A_{\parallel L}^*) \sin 2\theta_{K^*} + (L \rightarrow R) \right],$$

$$I_5 = \sqrt{2} \left(1 - \frac{4m_l^2}{s} \right)^{1/2} \left[\text{Re}(A_{0L} A_{\perp L}^*) \sin 2\theta_{K^*} - (L \rightarrow R) \right],$$

$$I_6 = 2 \left(1 - \frac{4m_l^2}{s} \right)^{1/2} \left[\text{Re}(A_{\parallel L} A_{\perp L}^*) \sin^2 \theta_{K^*} - (L \rightarrow R) \right],$$

$$I_7 = \sqrt{2} \left(1 - \frac{4m_l^2}{s} \right)^{1/2} \left[\text{Im}(A_{0L} A_{\parallel L}^*) \sin 2\theta_{K^*} - (L \rightarrow R) \right],$$

$$I_8 = \frac{1}{\sqrt{2}} \left(1 - \frac{4m_l^2}{s} \right) \left[\text{Im}(A_{0L} A_{\perp L}^*) \sin 2\theta_{K^*} + (L \rightarrow R) \right],$$

$$I_9 = \left(1 - \frac{4m_l^2}{s} \right) \left[\text{Im}(A_{\parallel L}^* A_{\perp L}) \sin^2 \theta_{K^*} + (L \rightarrow R) \right].$$

$$A_T^{(2)}(q^2) = \frac{|A_{\perp}(q^2)|^2 - |A_{\parallel}(q^2)|^2}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2}$$

$$A_T^{(\text{im})}(q^2) = \frac{2 \text{Im}[A_{\parallel}^L(q^2) A_{\perp}^{L*}(q^2) + A_{\parallel}^R(q^2) A_{\perp}^{R*}(q^2)]}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2},$$

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} = \frac{9}{32\pi} \left[\begin{aligned} &I_1^s \sin^2 \theta_K + I_1^c \cos^2 \theta_K \\ &+ I_2^s \sin^2 \theta_K \cos 2\theta_\ell + I_2^c \cos^2 \theta_K \cos 2\theta_\ell \\ &+ I_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + I_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi \\ &+ I_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + I_6 \sin^2 \theta_K \cos \theta_\ell \\ &+ I_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + I_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi \\ &+ I_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \end{aligned} \right],$$

+

$$\tilde{\phi} \equiv \begin{cases} \phi & \text{if } \phi \geq 0 \\ \phi + \pi & \text{if } \phi < 0 \end{cases}$$

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} = \frac{9}{32\pi} \left[\begin{aligned} &I_1^s \sin^2 \theta_K + I_1^c \cos^2 \theta_K \\ &+ I_2^s \sin^2 \theta_K \cos 2\theta_\ell + I_2^c \cos^2 \theta_K \cos 2\theta_\ell \\ &+ I_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + \cancel{I_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi} \\ &+ \cancel{I_5 \sin 2\theta_K \sin \theta_\ell \cos \phi} + I_6 \sin^2 \theta_K \cos \theta_\ell \\ &+ \cancel{I_7 \sin 2\theta_K \sin \theta_\ell \sin \phi} + \cancel{I_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi} \\ &+ I_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \end{aligned} \right],$$

Important simplification of the formulae without loss of precision on what we are interested in: the photon polarisation (C₇ and C'₇)

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\cos\theta_\ell d\cos\theta_K d\tilde{\phi}} = \frac{9}{16\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\
+ \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell - F_L \cos^2 \theta_K \cos 2\theta_\ell \\
+ (1 - F_L) A_T^{Re} \sin^2 \theta_K \cos \theta_\ell \\
+ \frac{1}{2}(1 - F_L) A_T^{(2)} \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\tilde{\phi} \\
\left. + \frac{1}{2}(1 - F_L) A_T^{Im} \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\tilde{\phi} \right].$$

$$F_L(q^2) = \frac{|A_0|^2}{|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2}$$

$$A_T^{(re)}(q^2) = \frac{2\text{Re}[A_{\parallel}^L(q^2)A_{\perp}^{L*}(q^2) - A_{\parallel}^R(q^2)A_{\perp}^{R*}(q^2)]}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2}$$

$$A_T^{(2)}(q^2) = \frac{|A_{\perp}(q^2)|^2 - |A_{\parallel}(q^2)|^2}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2}$$

$$A_T^{(im)}(q^2) = \frac{2\text{Im}[A_{\parallel}^L(q^2)A_{\perp}^{L*}(q^2) + A_{\parallel}^R(q^2)A_{\perp}^{R*}(q^2)]}{|A_{\perp}(q^2)|^2 + |A_{\parallel}(q^2)|^2},$$

$$A_T^{(2)}(q^2 \rightarrow 0) = \frac{2\text{Re}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2}$$

$$A_T^{Im}(q^2 \rightarrow 0) = \frac{2\text{Im}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2}$$

They vanish for
purely left-handed
polarisation

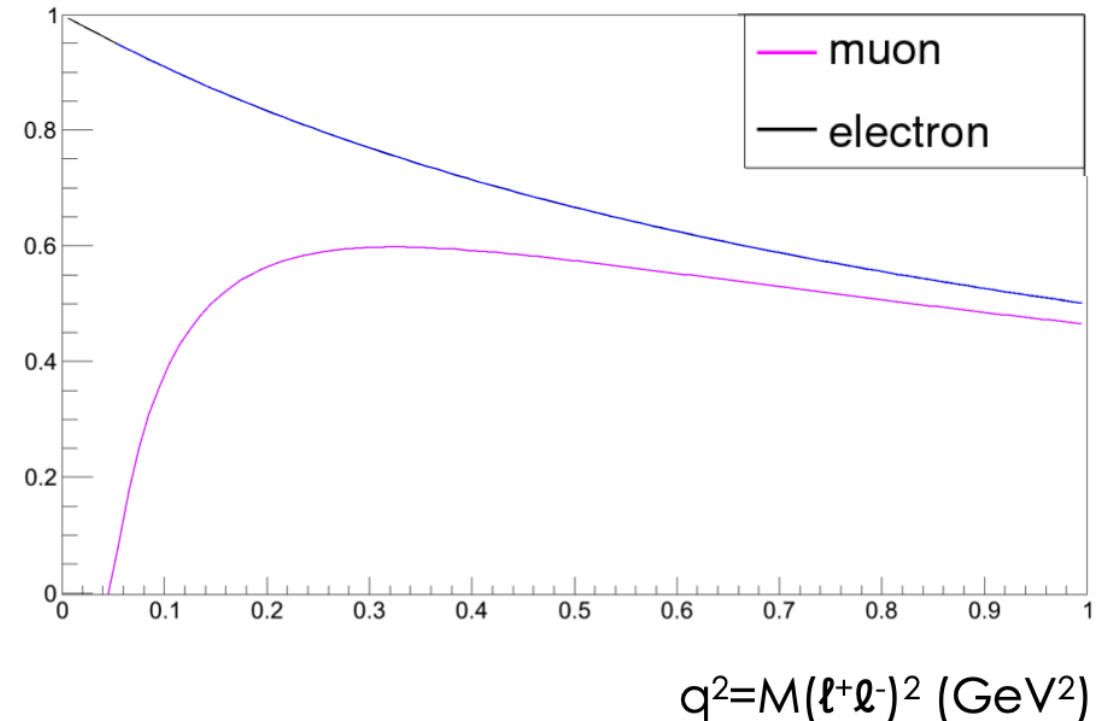
Beyond the yields, the precision on A_T^2 and A_T^{lm} is driven by $(1-F_L)$

$$\frac{9}{16\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\
+ \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell - F_L \cos^2 \theta_K \cos 2\theta_\ell \\
+ (1 - F_L) A_T^{Re} \sin^2 \theta_K \cos \theta_\ell \\
+ \frac{1}{2}(1 - F_L) A_T^{(2)} \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\tilde{\phi} \\
\left. + \frac{1}{2}(1 - F_L) A_T^{lm} \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\tilde{\phi} \right].$$

$$(1 - F_L)$$

$$(1 - F_L) \frac{1 - x}{1 + \frac{x}{2}}$$

$$x = \frac{4m_\ell^2}{q^2}$$

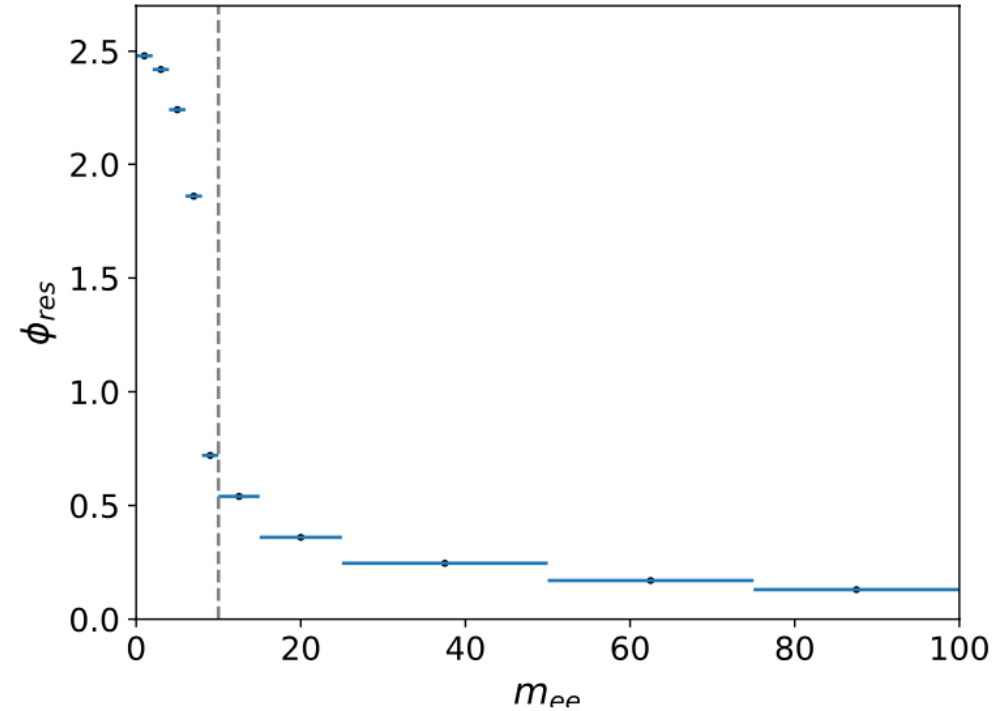
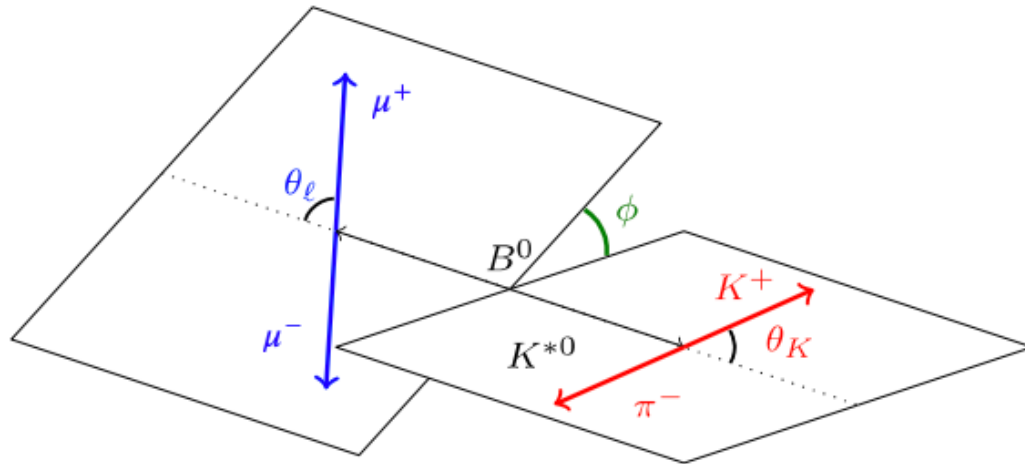


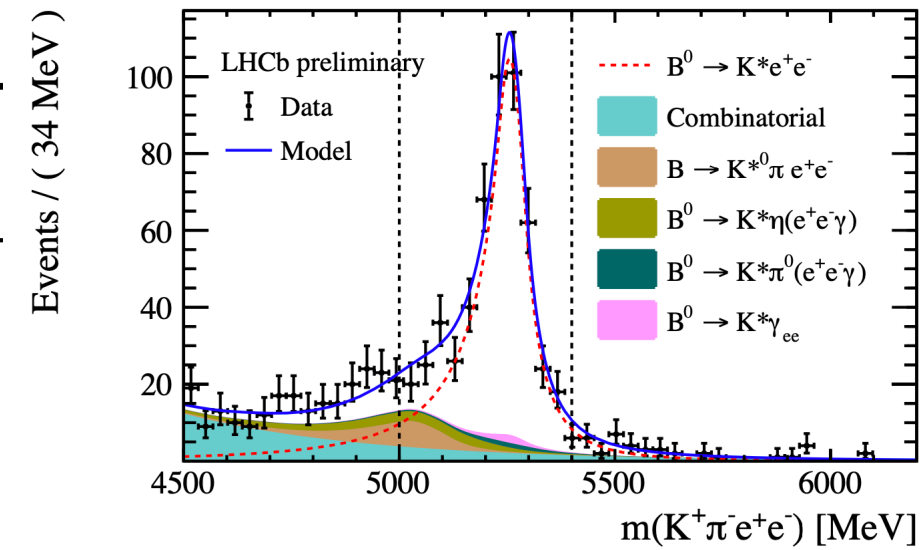
Given the experimental challenges, going above 0.5 GeV² with the electrons channel is not meaningful.

Lower Boundary In principle, can go to the threshold $m_{(ee)} = 2m_e \sim 1\text{MeV}/c^2$

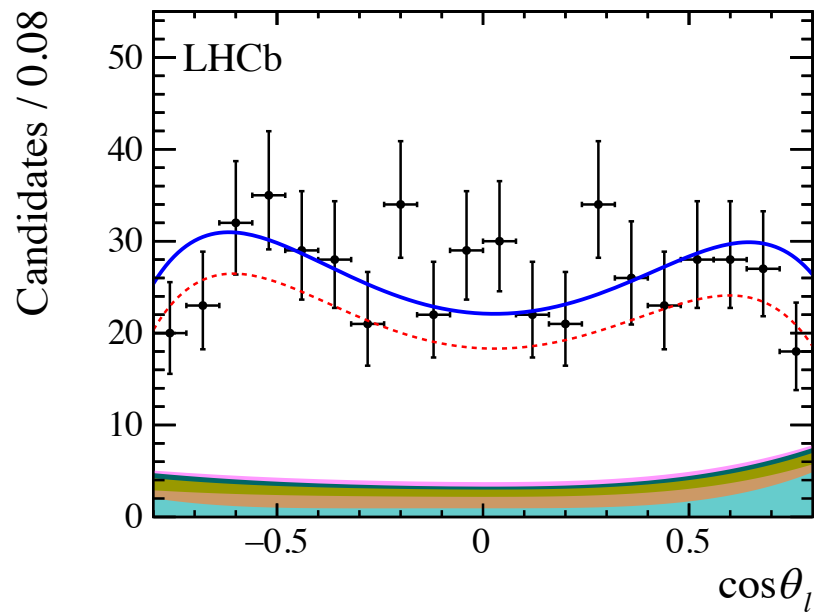
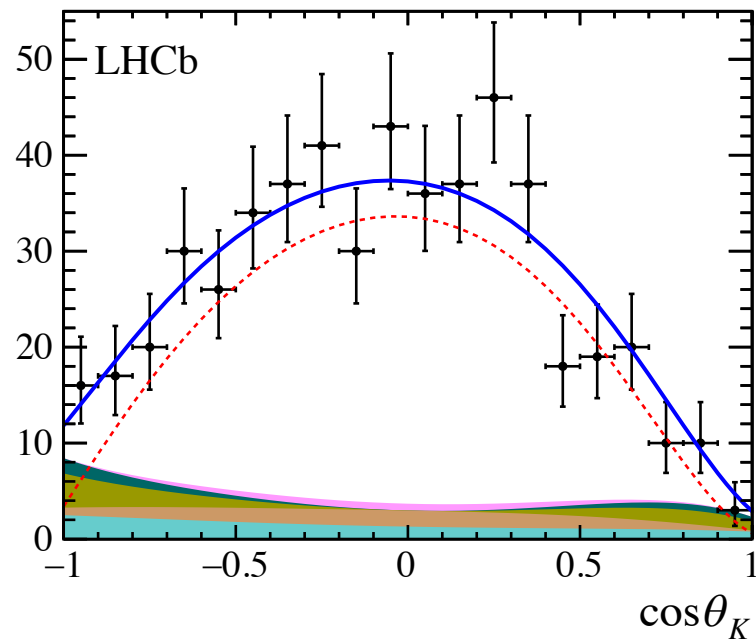
- Angle between leptons gets very small
- Bad resolution on ϕ
- Worse measurement of observables of interest

→ Cut at 10 MeV serves as a veto to converted γ

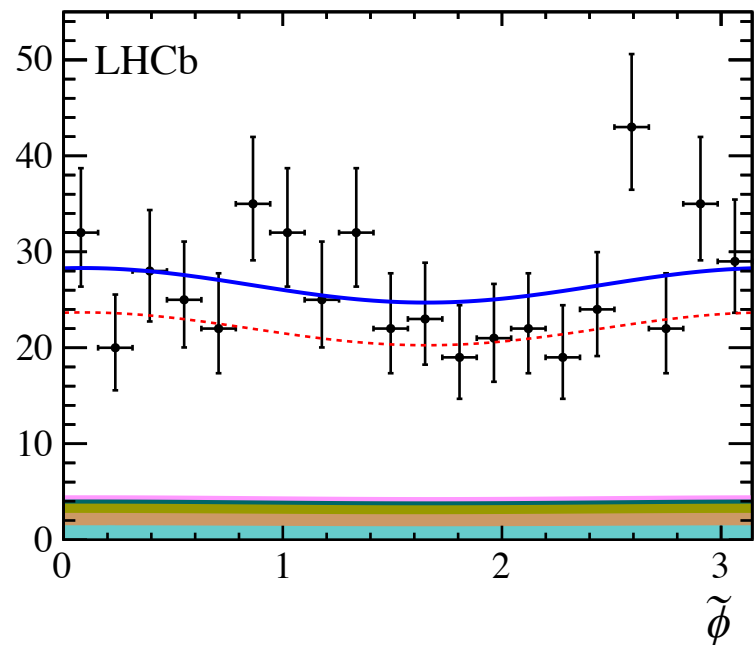




Candidates / 0.1



Candidates / 0.05 π



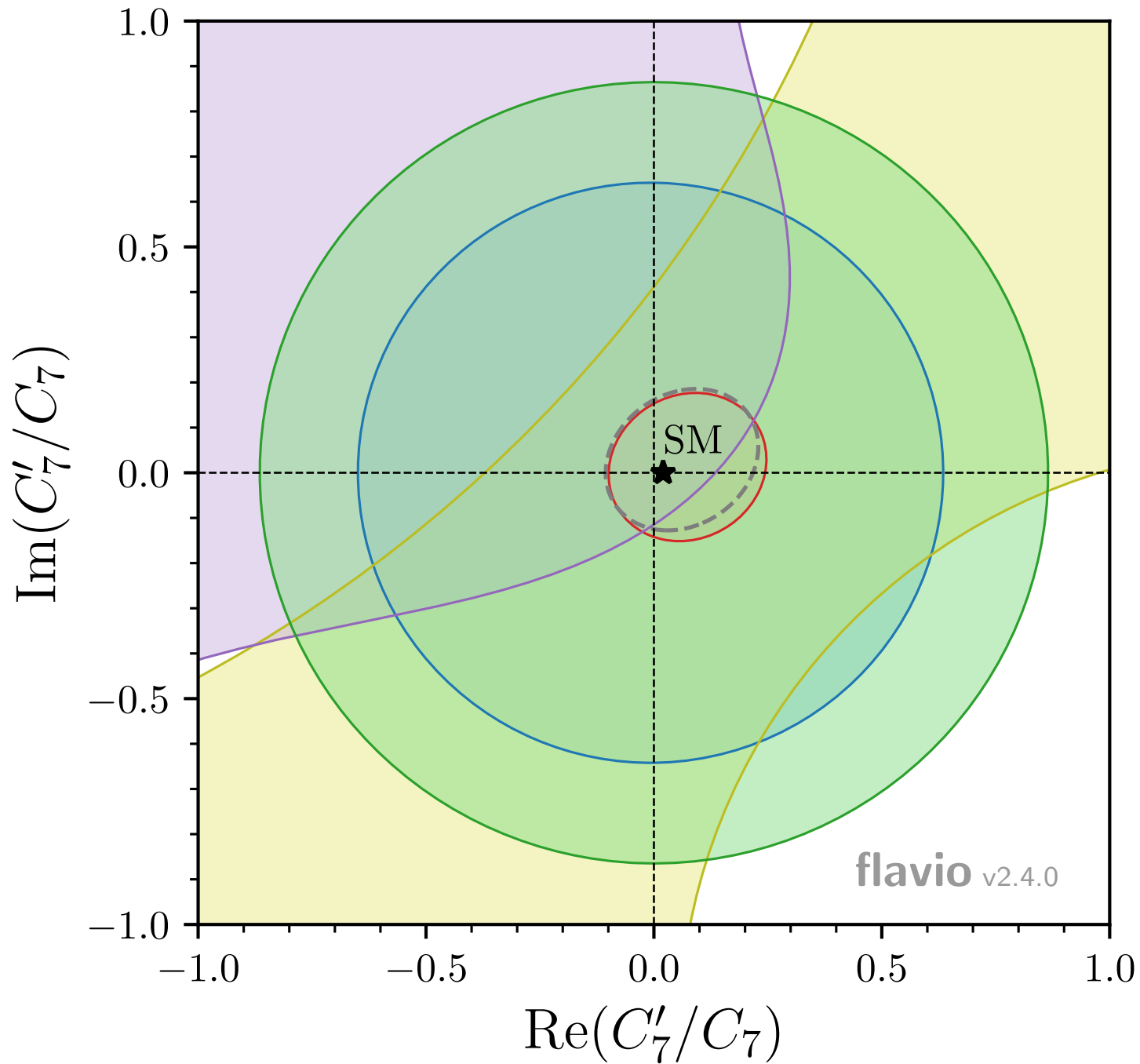
$$\begin{aligned}
F_L &= 0.044 \pm 0.026 \pm 0.014, \\
A_T^{\text{Re}} &= -0.06 \pm 0.08 \pm 0.02, \\
A_T^{(2)} &= +0.11 \pm 0.10 \pm 0.02, \\
A_T^{\text{Im}} &= +0.02 \pm 0.10 \pm 0.01,
\end{aligned}$$

$$\begin{aligned}
F_L(\text{SM}) &= 0.051 \pm 0.013, \\
A_T^{\text{Re}}(\text{SM}) &= -0.0001 \pm 0.0004, \\
A_T^{(2)}(\text{SM}) &= 0.033 \pm 0.020, \\
A_T^{\text{Im}}(\text{SM}) &= -0.00012 \pm 0.00034.
\end{aligned}$$

In good agreement with the SM predictions

$$\begin{aligned}
A_T^{(2)}(q^2 \rightarrow 0) &= \frac{2\text{Re}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2} \\
A_T^{\text{Im}}(q^2 \rightarrow 0) &= \frac{2\text{Im}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2}
\end{aligned}$$

5% precision on the photon polarization in $b \rightarrow s\gamma$ transitions. Dominated by statistical uncertainties



Constraints at 2σ

- $\mathcal{B}(B \rightarrow X_s \gamma)$
- $B^0 \rightarrow K^{*0} e^+ e^-$
- $B^0 \rightarrow K_S^0 \pi^0 \gamma$
- $B_s^0 \rightarrow \phi \gamma$
- $\Lambda_b \rightarrow \Lambda \gamma$ $\Lambda_b \rightarrow \Lambda \gamma : \alpha_\gamma \sim \frac{1 - |C'_7/C_7|^2}{1 - |C_7/C_7|^2}$
- - - Global

$$C_7^{\text{SM}} = -0.2915$$

2

Branching Fractions

Angular observables

Lepton Flavour Universality
observables:
Branching Fractions ratios
angular observables ratios

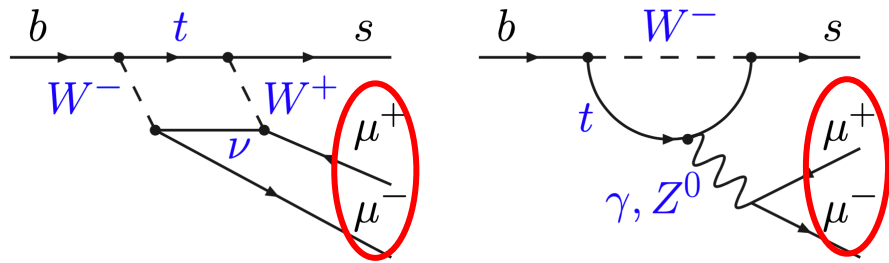
theoretical
cleanness

Results in the $b \rightarrow s\mu\mu$ transitions:

- Extremely clean experimentally
- Large statistics
- not in perfect agreement with SM predictions (but uncertainties on these predictions due to non-local contributions which are hard to estimate)

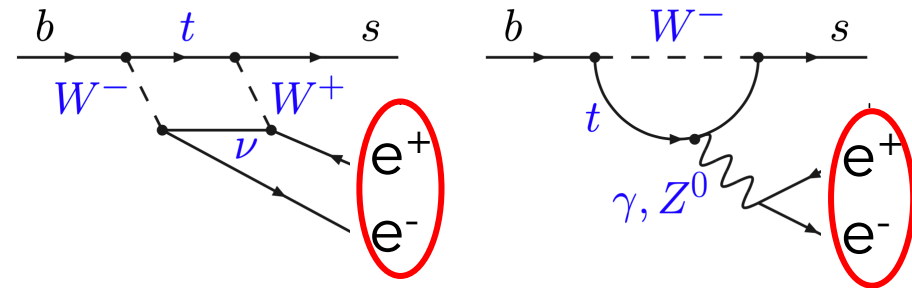
Lepton Flavour Universality tests in $b \rightarrow s \ell \ell$ transitions

$\ell = e, \mu$



?

=



In the SM only difference : kinematics (lepton masses)

Any ratio of observables in principle

Start with the simplest (?) one: ratio of branching fractions

$$R_{H_s} = \frac{\int \frac{d\Gamma(B \rightarrow H_s \mu^+ \mu^-)}{dq^2} dq^2}{\int \frac{d\Gamma(B \rightarrow H_s e^+ e^-)}{dq^2} dq^2} \stackrel{SM}{\approx} 1$$

← $B^{+,0}, B_s, \Lambda_b$
← $K, K^*, \phi, \rho K \dots$

Practically at LHCb:

$$R_H = \frac{N(B \rightarrow H \mu^+ \mu^-)}{N(B \rightarrow H e^+ e^-)} \times \frac{\epsilon(B \rightarrow H e^+ e^-)}{\epsilon(B \rightarrow H \mu^+ \mu^-)} + r_{J/\psi} = \frac{BR(B \rightarrow H J/\psi(\mu^+ \mu^-))}{BR(B \rightarrow H J/\psi(e^+ e^-))} = 1$$

Yields from mass fits

Efficiencies from
MC & data
calibration samples

well tested LFU in J/ψ modes

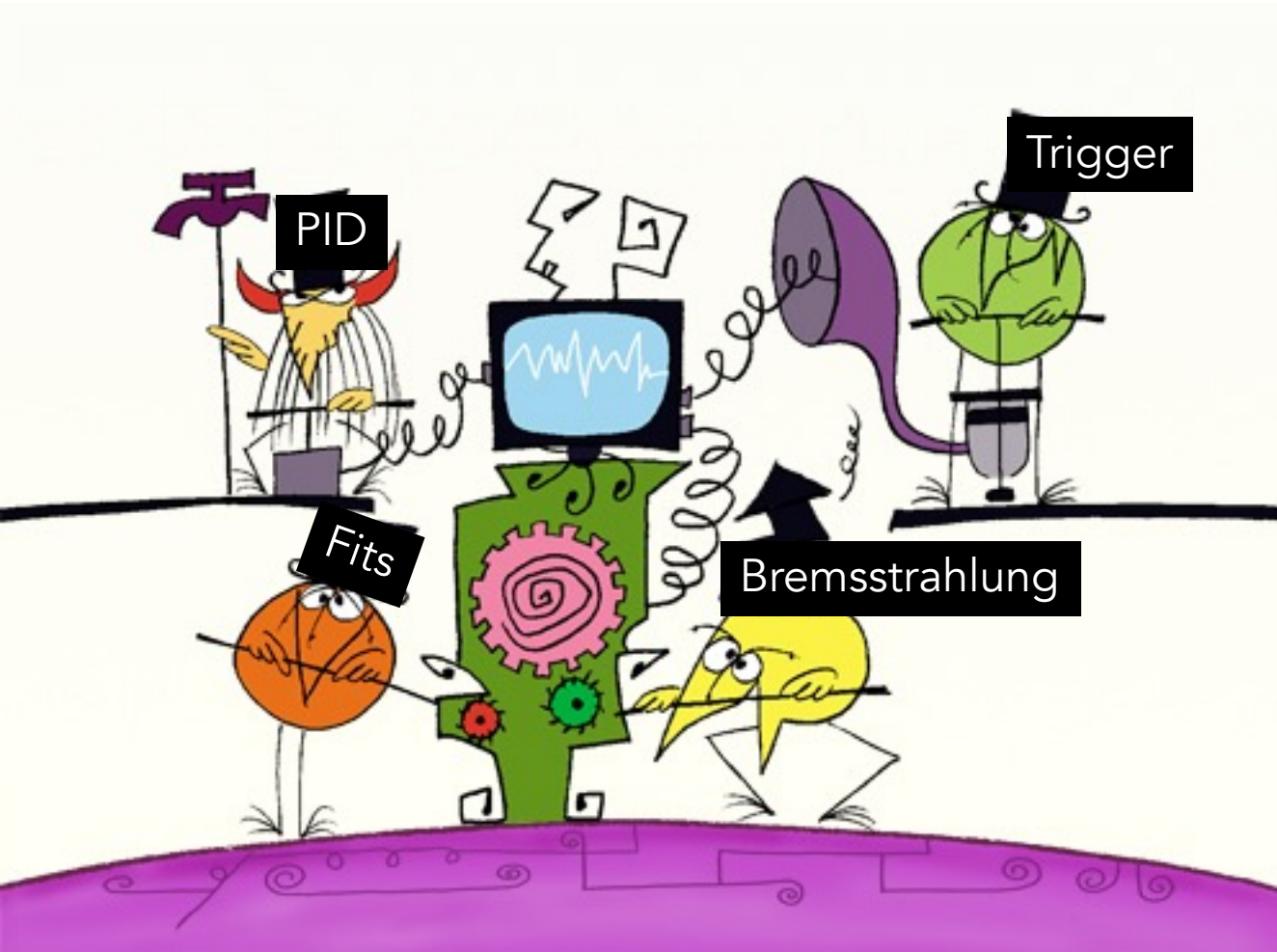
H = K, K*, pK ...

⇒ Use of the double ratio using the resonant channels

$$R_H = \frac{\frac{N(B \rightarrow H \mu^+ \mu^-)}{N(B \rightarrow H J/\psi(\mu^+ \mu^-))}}{\frac{N(B \rightarrow H e^+ e^-)}{N(B \rightarrow H J/\psi(e^+ e^-))}} \times \frac{\frac{\epsilon(B \rightarrow H e^+ e^-)}{\epsilon(B \rightarrow H J/\psi(e^+ e^-))}}{\frac{\epsilon(B \rightarrow H \mu^+ \mu^-)}{\epsilon(B \rightarrow H J/\psi(\mu^+ \mu^-))}}$$

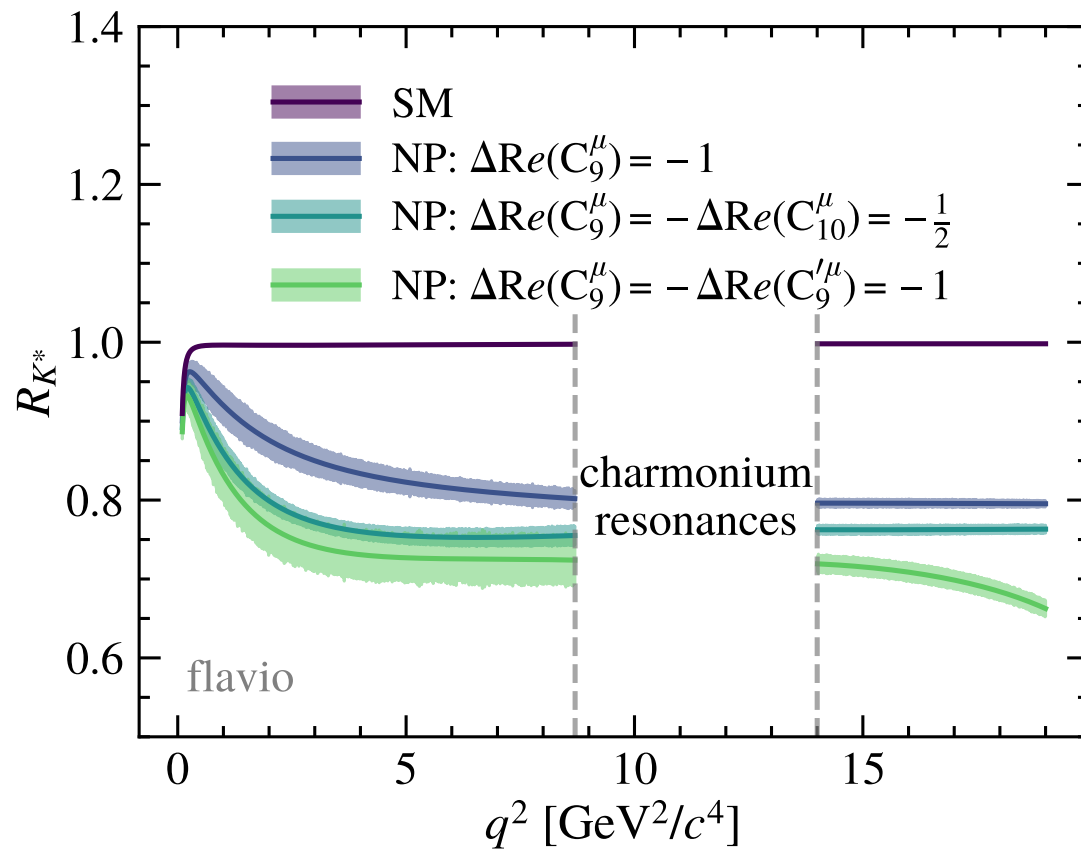
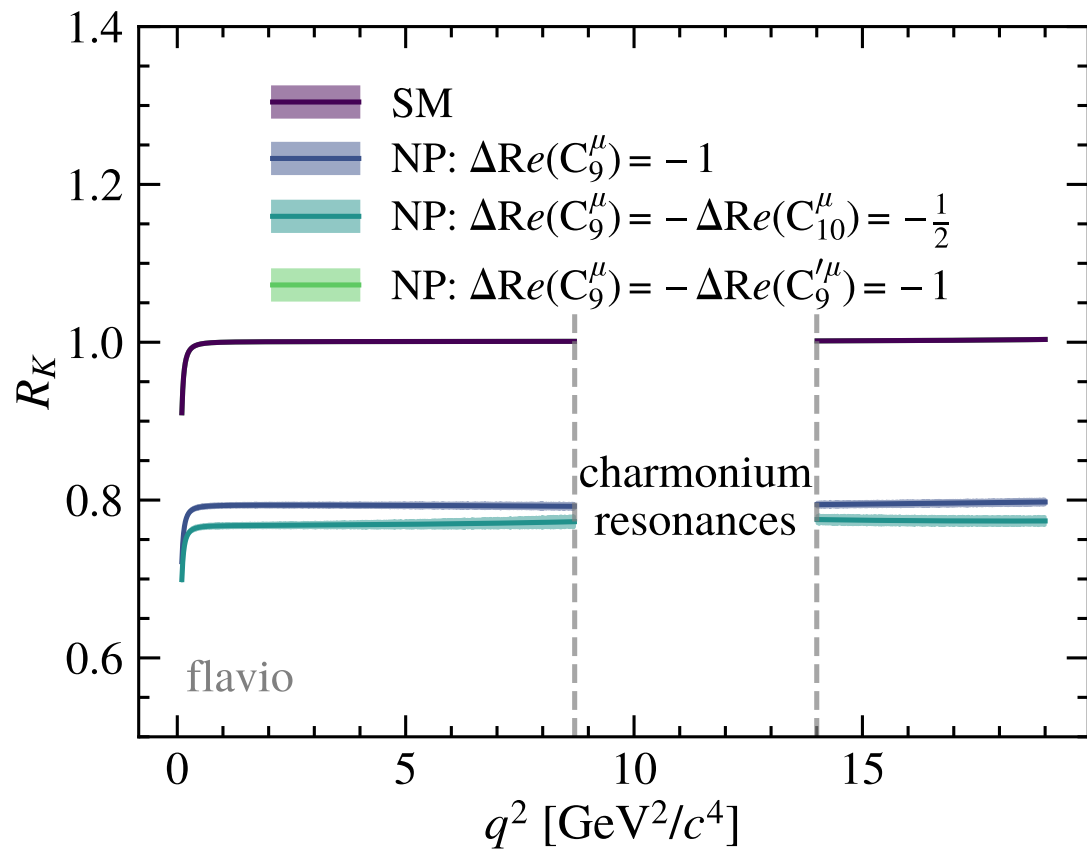
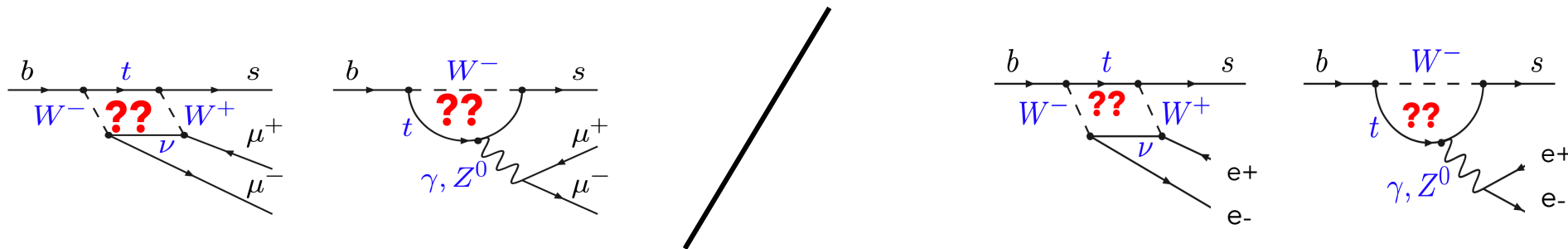
⇒ cancels out most of the systematics due to e/μ differences

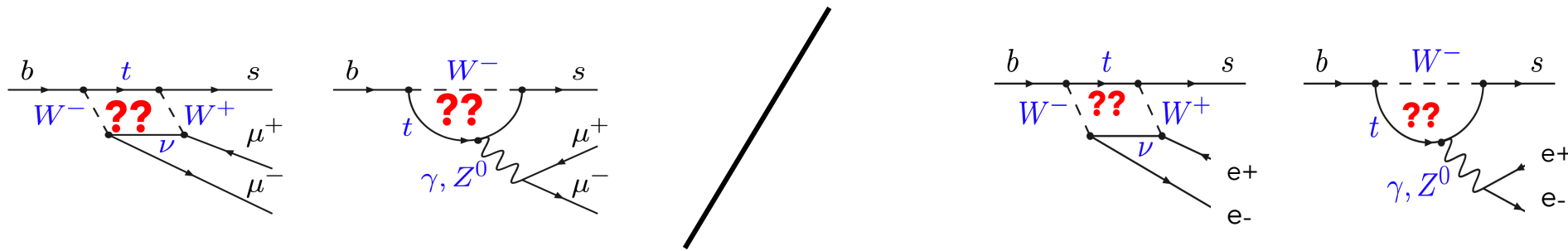
⇒ the R_x analysis



Simultaneous fit of

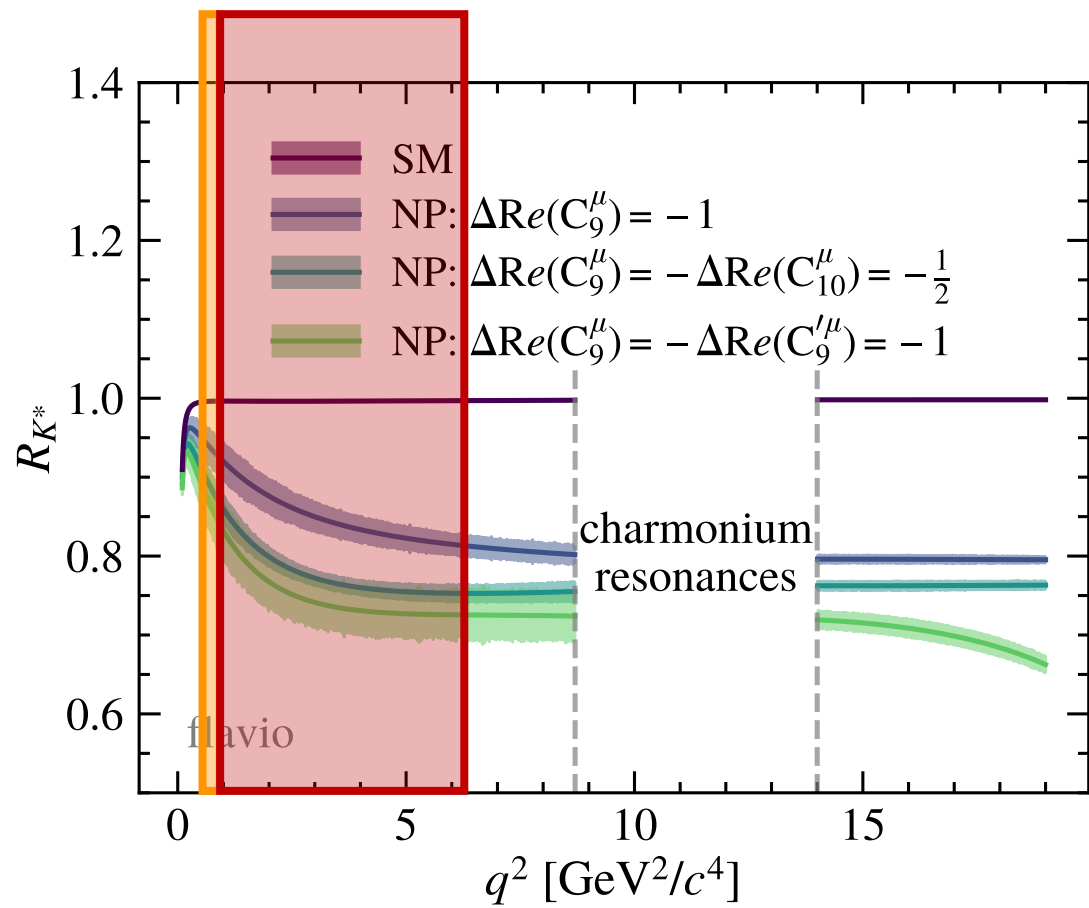
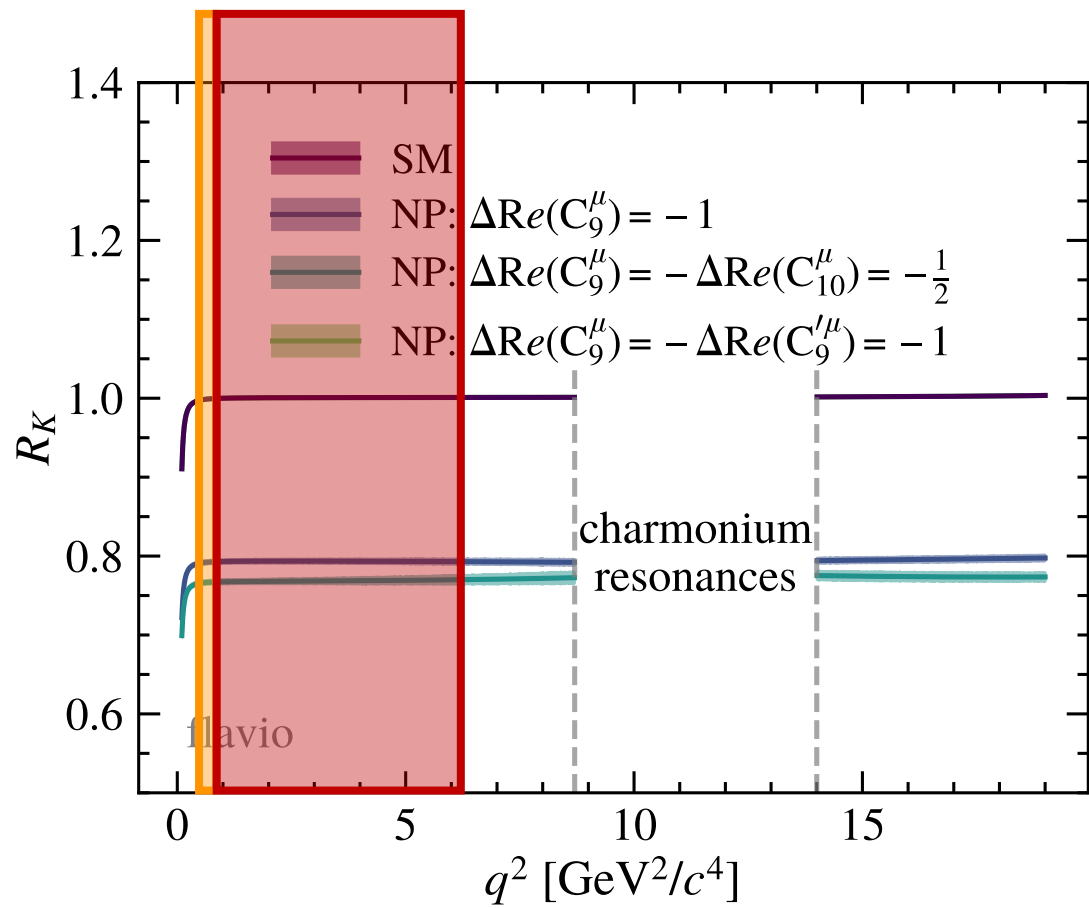
- $B \rightarrow K \ell \ell$ and $B \rightarrow K^* \ell \ell$
- in 2 kinematical regions (low and central- q^2)





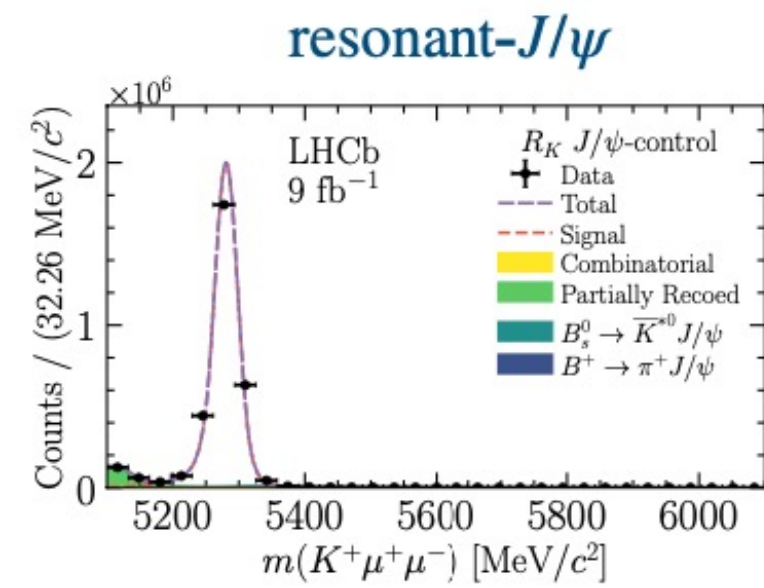
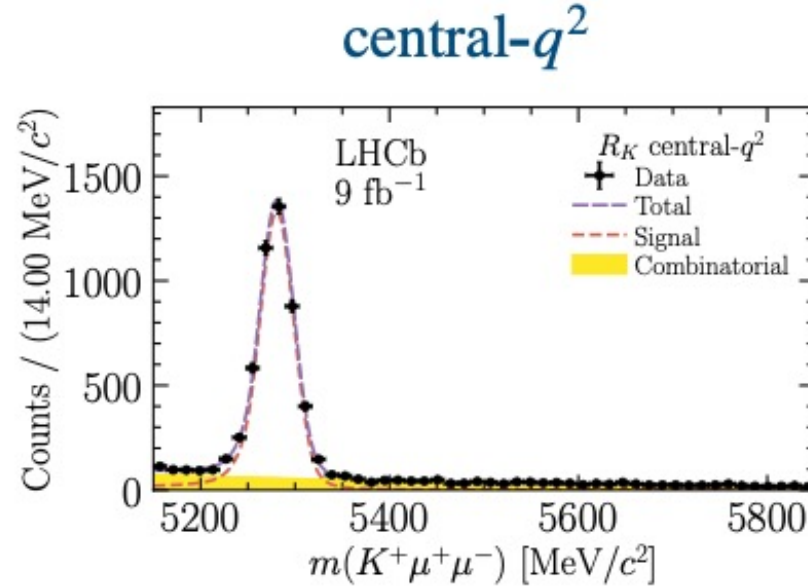
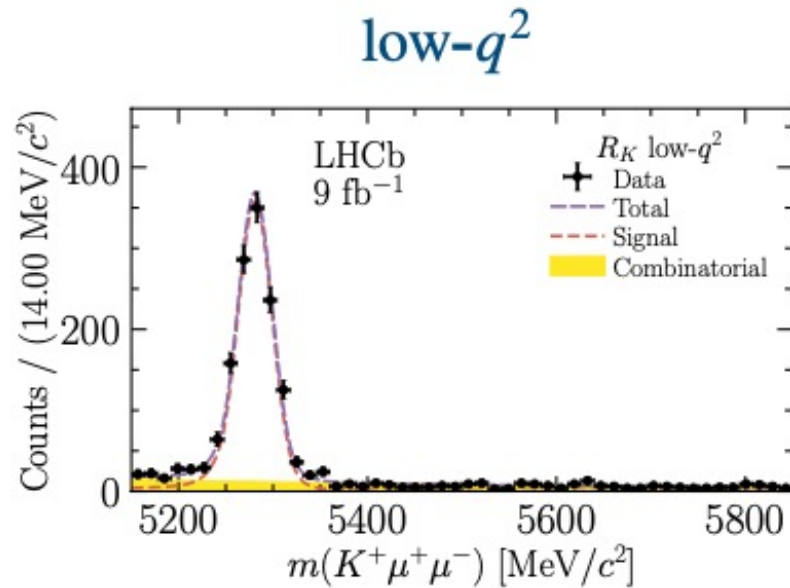
low- q^2

central- q^2

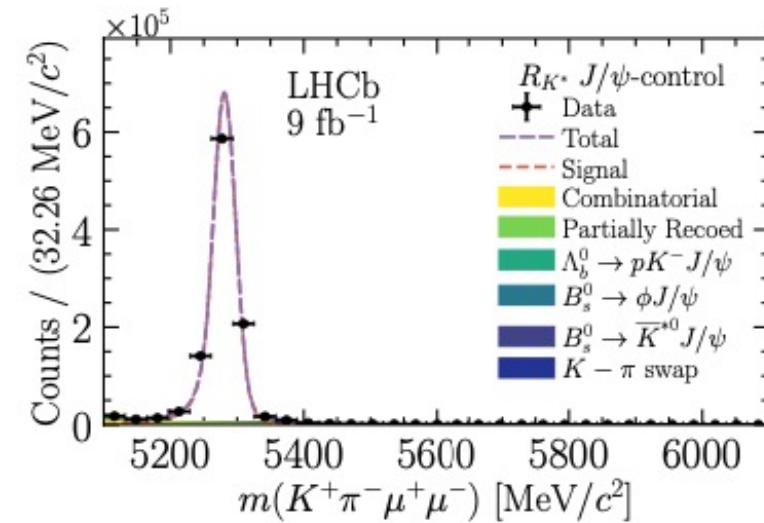
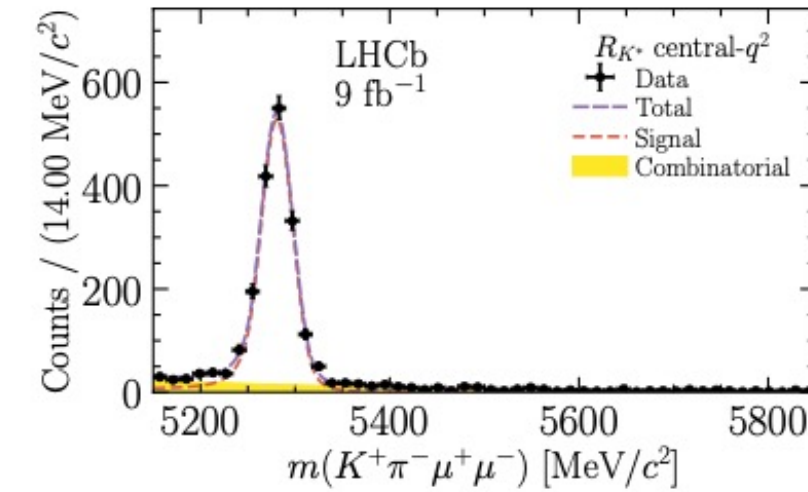
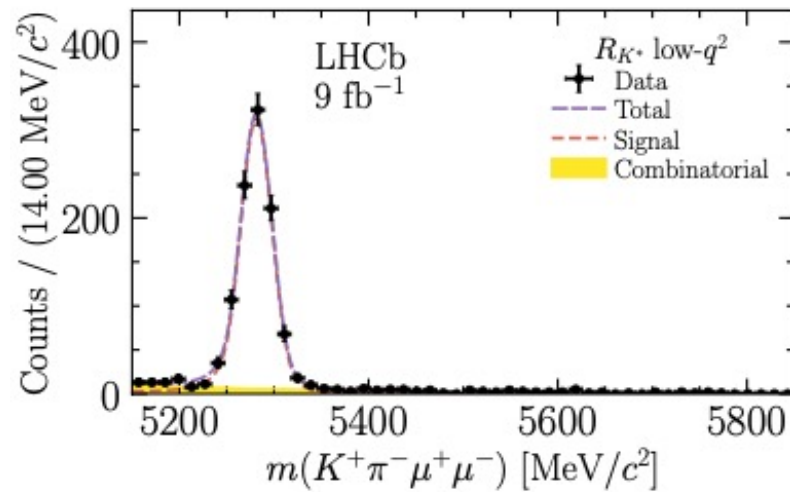


Simultaneous fit for R_x extraction: muon modes

B^+

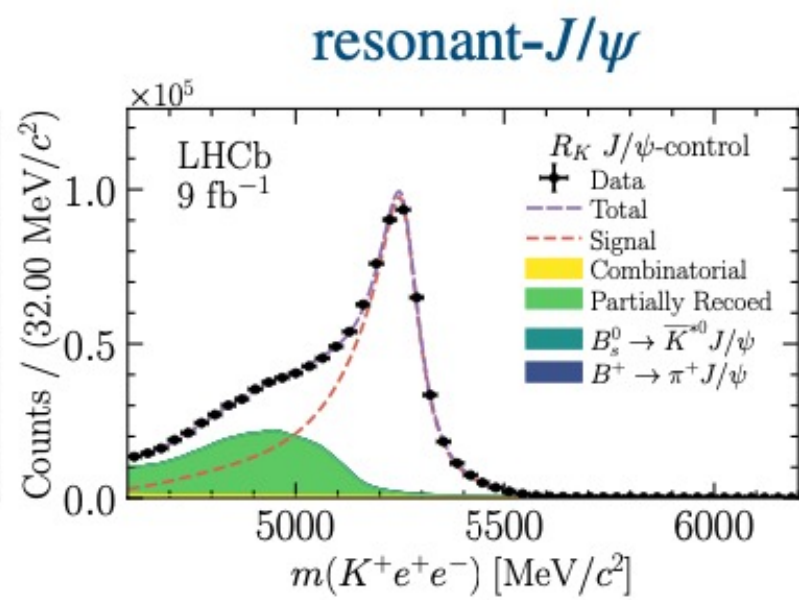
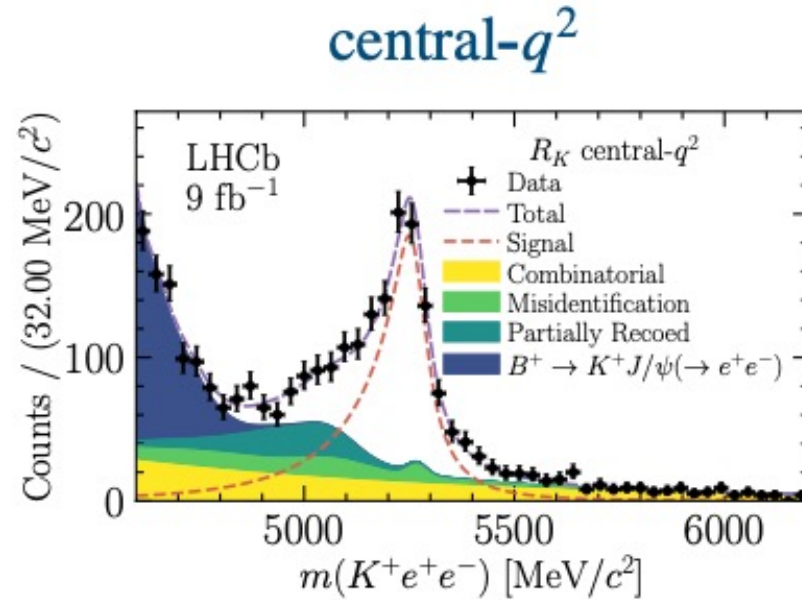
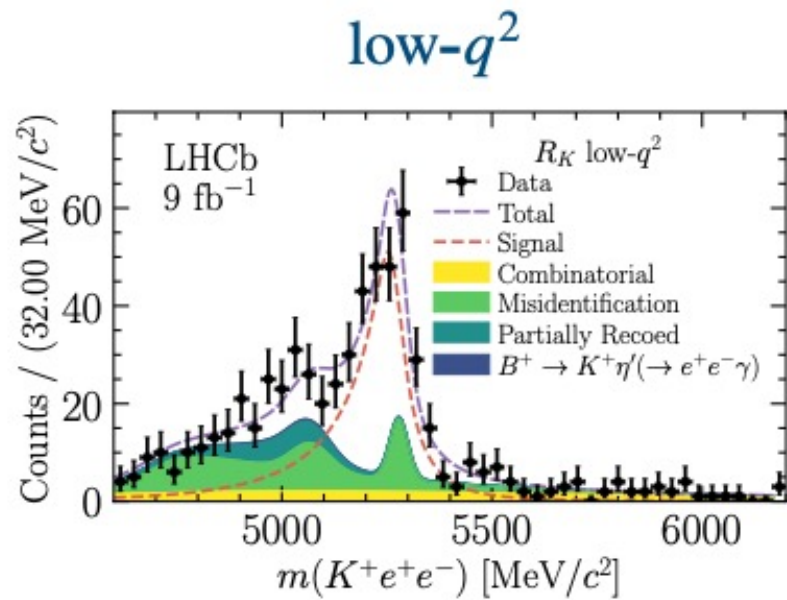


B^0

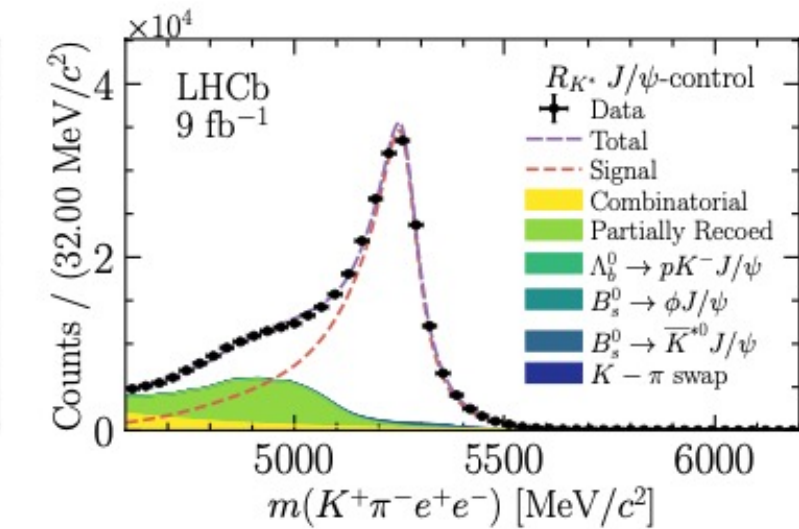
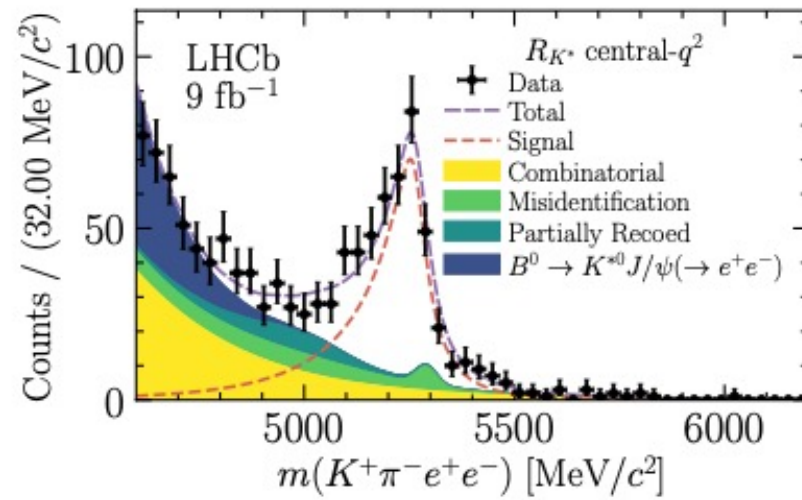
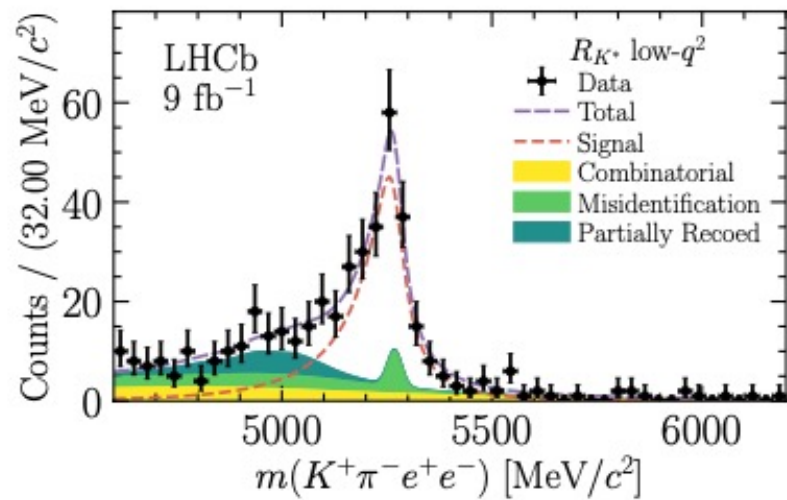


Simultaneous fit for R_x extraction: electron modes

B^+



B^0



A factor ~ 4 in yields between electron and muon modes

Measured yields from simultaneous fit to R_X

| LU observable | Muon ($\times 10^3$) | Electron ($\times 10^3$) |
|--------------------------|--|--|
| low- q^2 R_K | 1.25 ± 0.04 | 0.305 ± 0.024 |
| low- q^2 R_{K^*} | 1.001 ± 0.034 | 0.247 ± 0.022 |
| central- q^2 R_K | 4.69 ± 0.08 | 1.19 ± 0.05 |
| central- q^2 R_{K^*} | 1.74 ± 0.05 | 0.443 ± 0.028 |
| J/ψ R_K | $(2.964 \pm 0.002) \times 10^3$ | $(7.189 \pm 0.015) \times 10^2$ |
| J/ψ R_{K^*} | $(9.733 \pm 0.010) \times 10^2$ | $(2.517 \pm 0.009) \times 10^2$ |

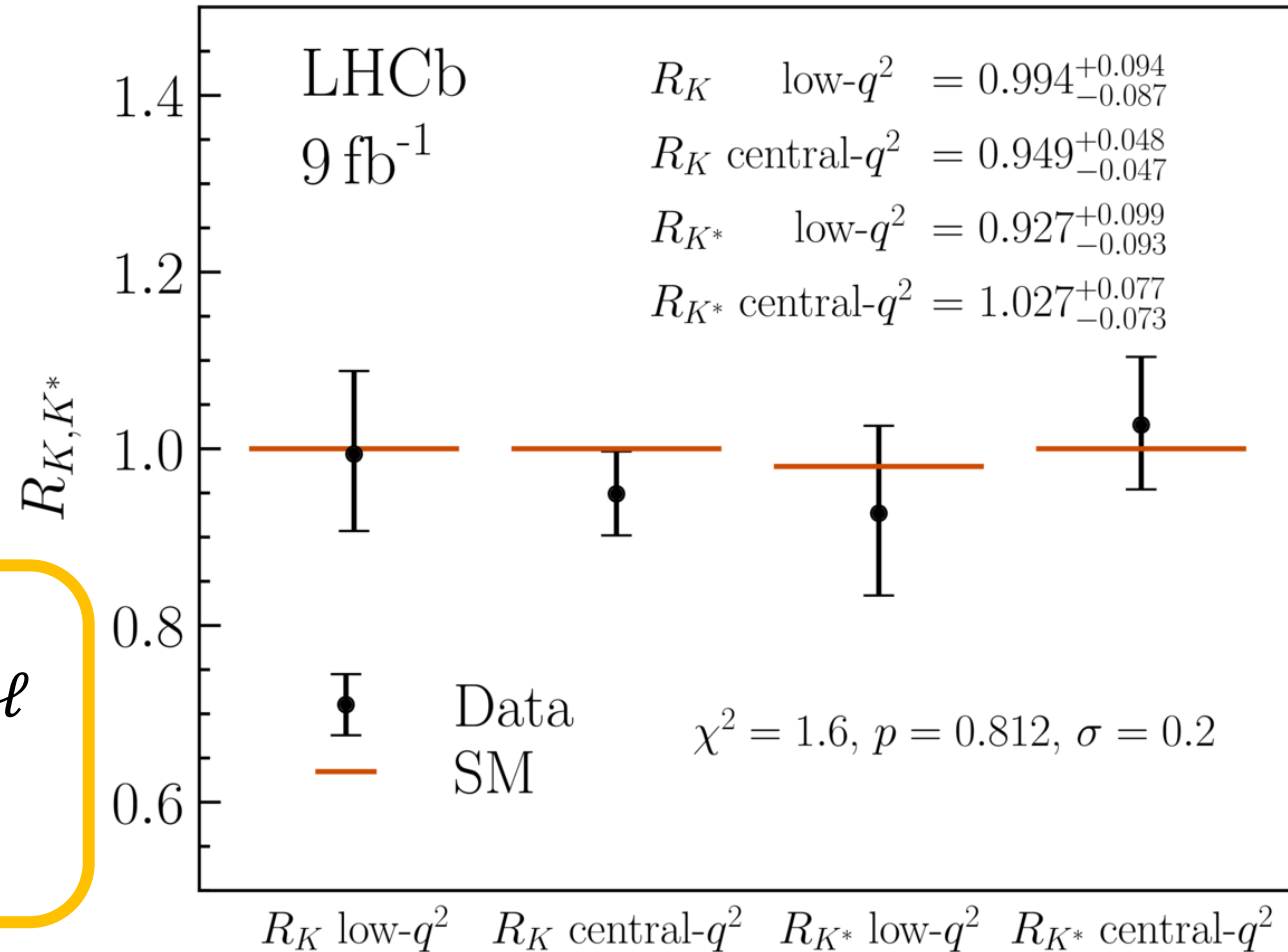
Results

$$\text{low-}q^2 \begin{cases} R_K & = 0.994^{+0.090}_{-0.082} \text{ (stat)} \quad ^{+0.029}_{-0.027} \text{ (syst)}, \\ R_{K^*} & = 0.927^{+0.093}_{-0.087} \text{ (stat)} \quad ^{+0.036}_{-0.035} \text{ (syst)}, \end{cases}$$

$$\text{central-}q^2 \begin{cases} R_K & = 0.949^{+0.042}_{-0.041} \text{ (stat)} \quad ^{+0.022}_{-0.022} \text{ (syst)}, \\ R_{K^*} & = 1.027^{+0.072}_{-0.068} \text{ (stat)} \quad ^{+0.027}_{-0.026} \text{ (syst)}, \end{cases}$$

First or most precise test of LFU in $b \rightarrow s \ell \ell$

Compatible with the SM at 0.2σ



To include Lepton Flavour Universality measurements in global fits:

$$C_i = C_i^{SM} + C_i^{NP}$$

$$i = 7, 9, 10$$



$$\left[\begin{array}{l} C_{i,e} = C_i^{SM} + C_{i,e}^{NP} \\ C_{i,\mu} = C_i^{SM} + C_{i,\mu}^{NP} \end{array} \right.$$

Some remarks:

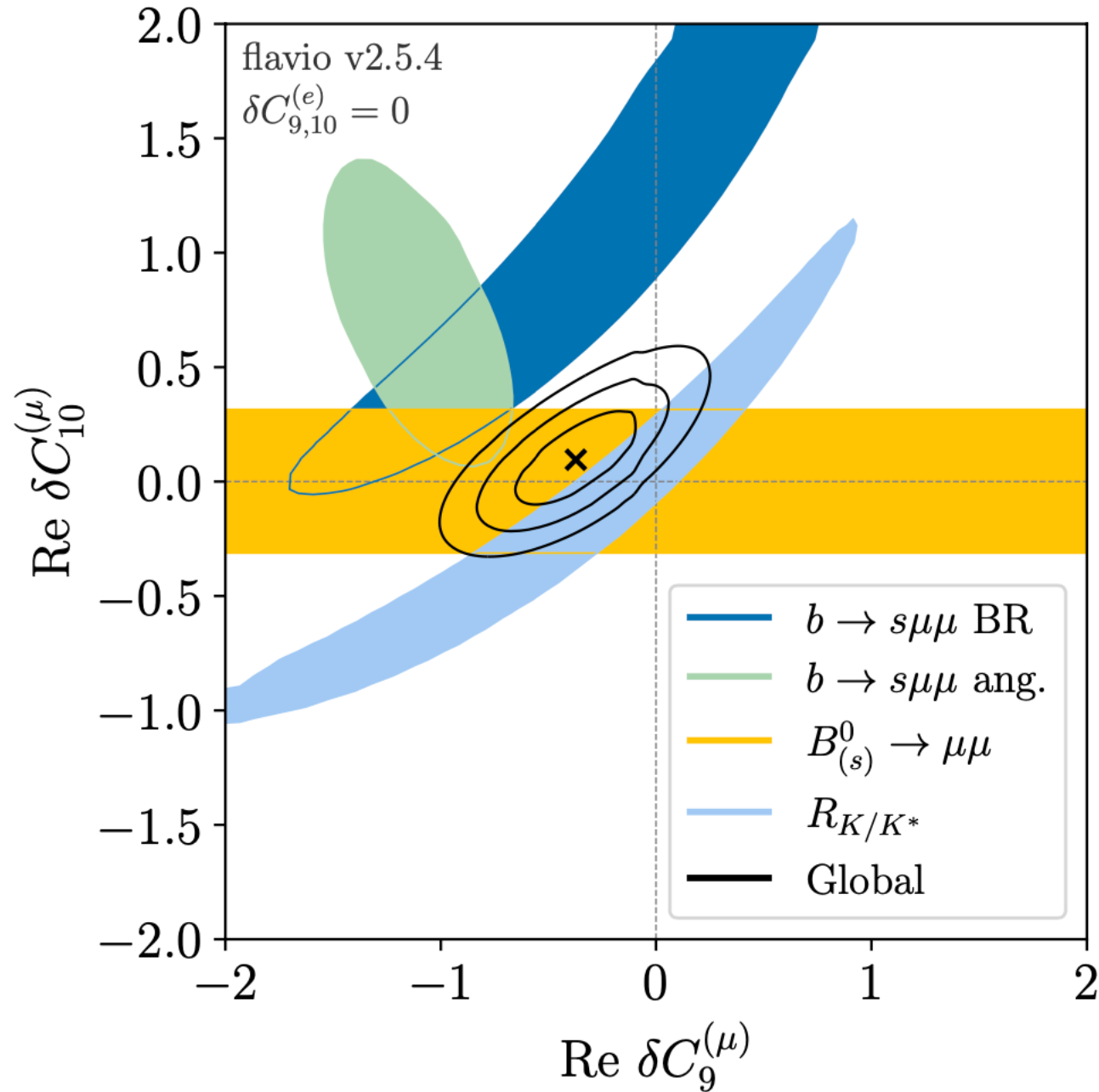
- $C_7^{(\prime)}$ strongly constrained from radiative decays and $K^* \rightarrow e\bar{e}$ (very low- q^2)
- C_9^{\prime} and C_{10}^{\prime} contributions disfavoured by $R_K \sim R_{K^*}$...

Some assumptions can be made:

- NP in muon modes only
- NP only in C_9
- ...

no NP in electrons

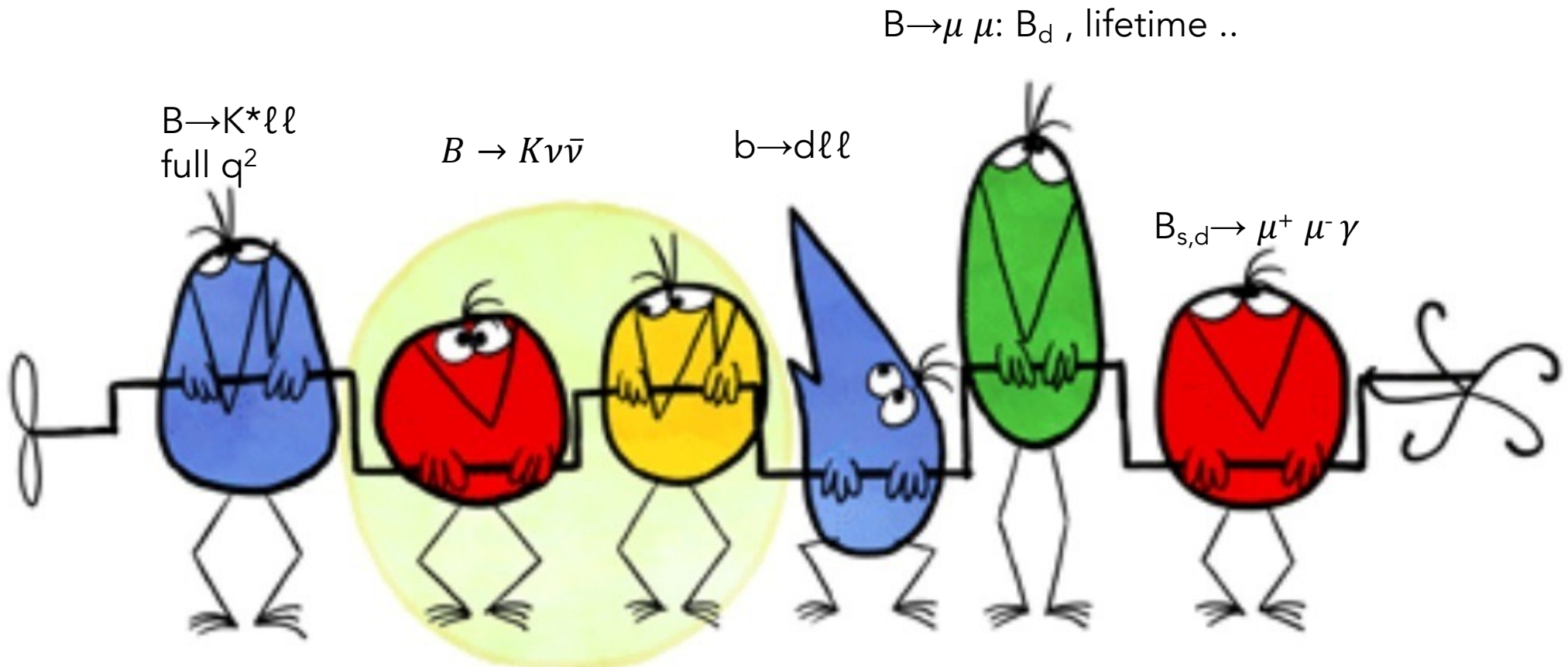
C_9 and C_{10} real



from Camille Normand
PhD thesis (2023)

Disfavours a large
shift on C_{10}

Some ideas to move forward



$$B_{s,d} \rightarrow \mu^+ \mu^-$$

- More observables
- $B_{s,d} \rightarrow \mu^+ \mu^- \gamma$

and more stat !

More observables (one example)

$$\mathcal{B}(B_s^0 \rightarrow \ell^+ \ell^-) = \frac{1 + y_s \mathcal{A}_{\Delta\Gamma}}{1 - y_s^2} \times \mathcal{B}(B_s^0 \rightarrow \ell^+ \ell^-)_{t=0}$$

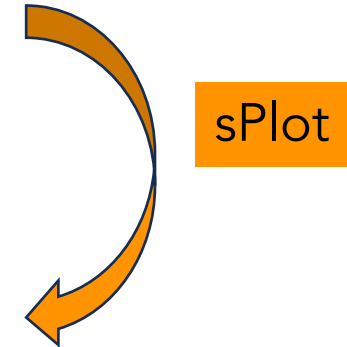
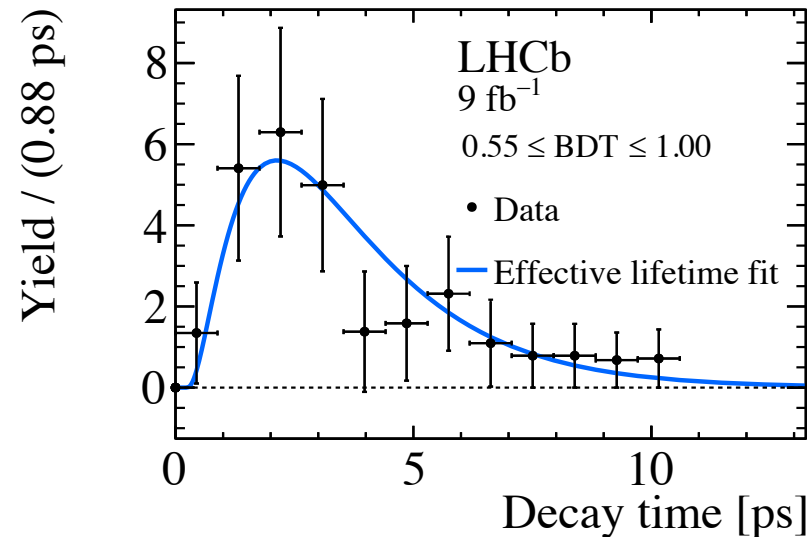
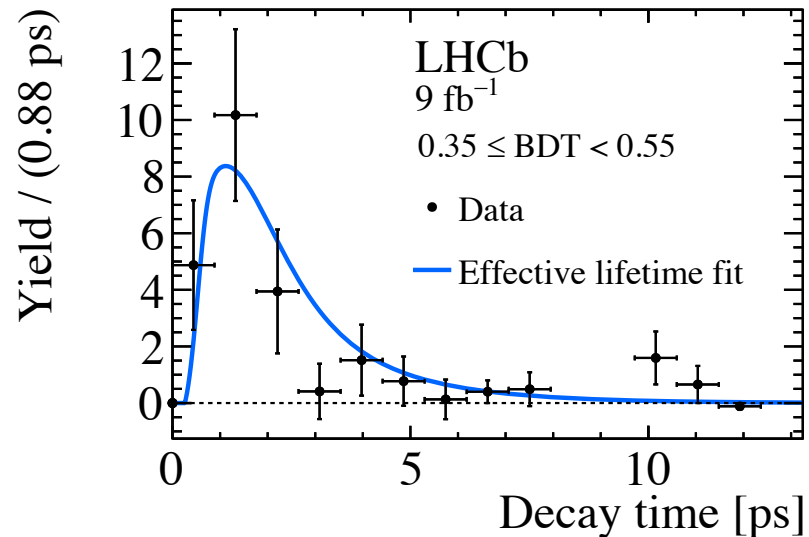
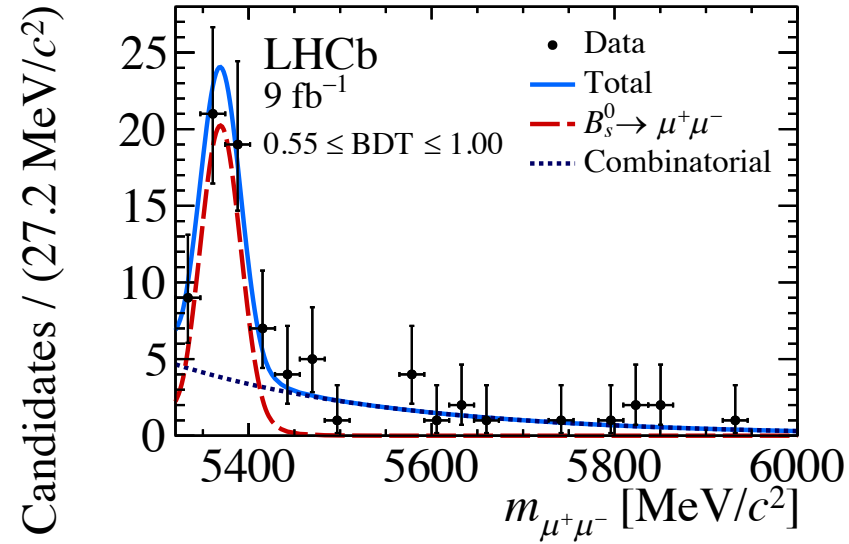
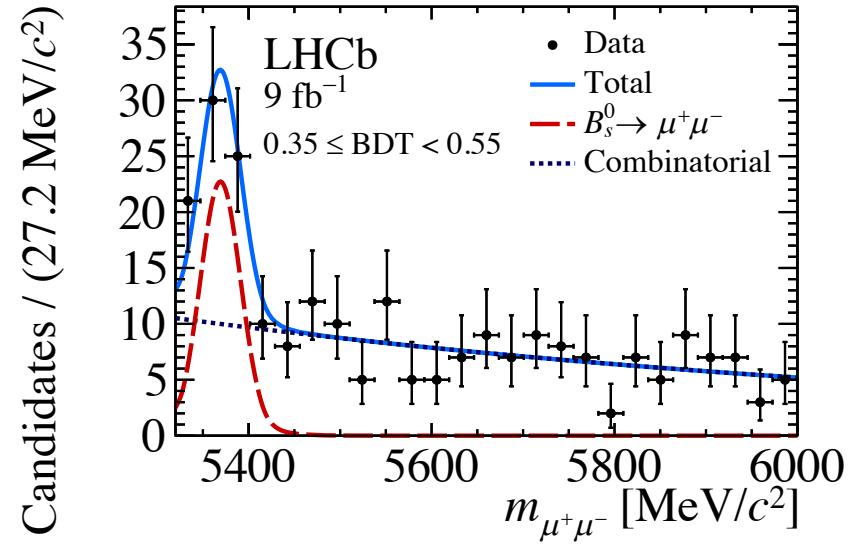
NP ? NP ?

$$\mathcal{B}(B_{(s)}^0(t) \rightarrow \ell^+ \ell^-)_{t=0} \propto \left(1 - \frac{4m_\ell^2}{m_B^2}\right) |C_S - C'_S|^2 + \left| (C_P - C'_P) + 2\frac{m_\ell}{m_B^2} (C_{10} - C'_{10}) \right|^2$$

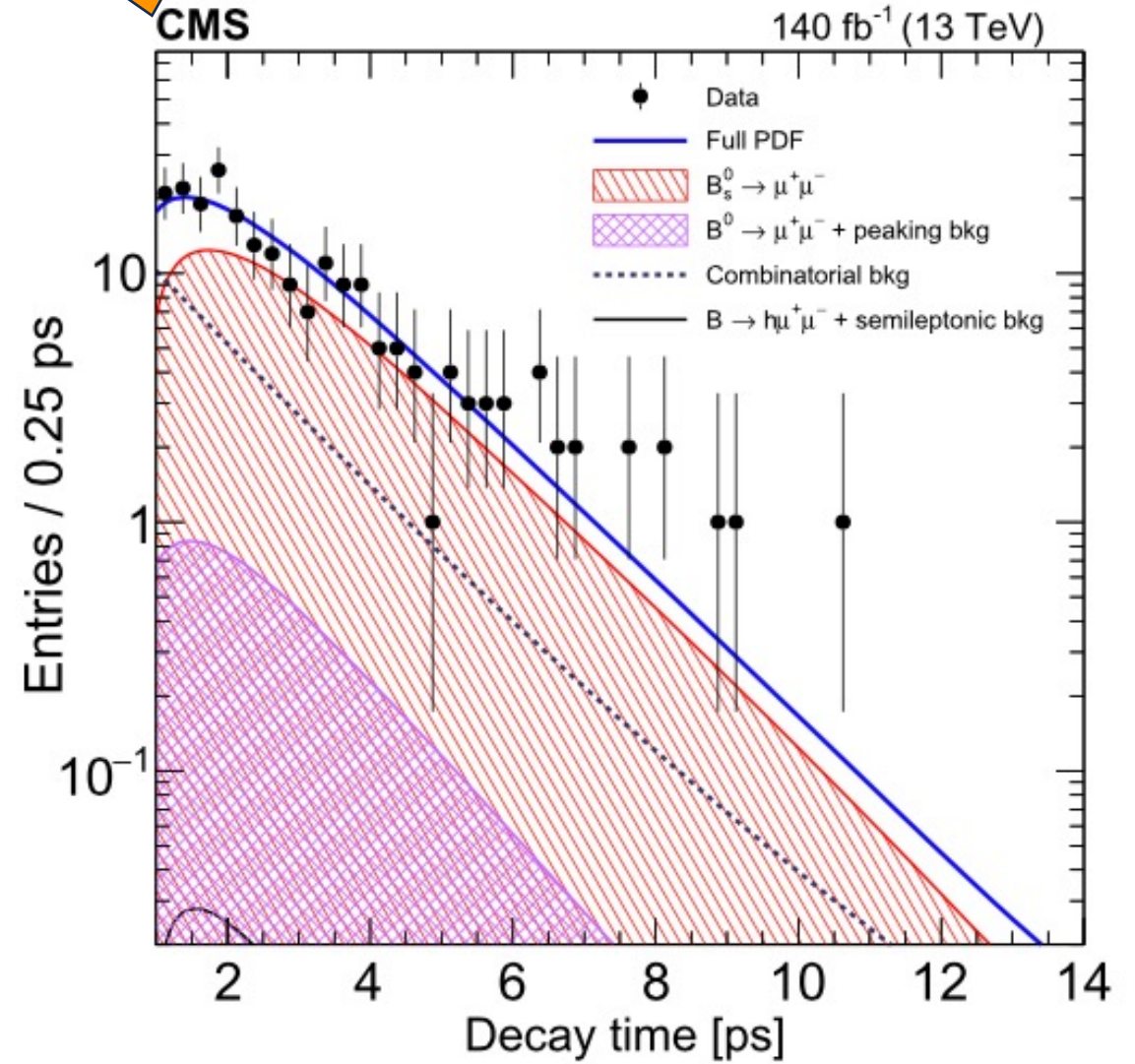
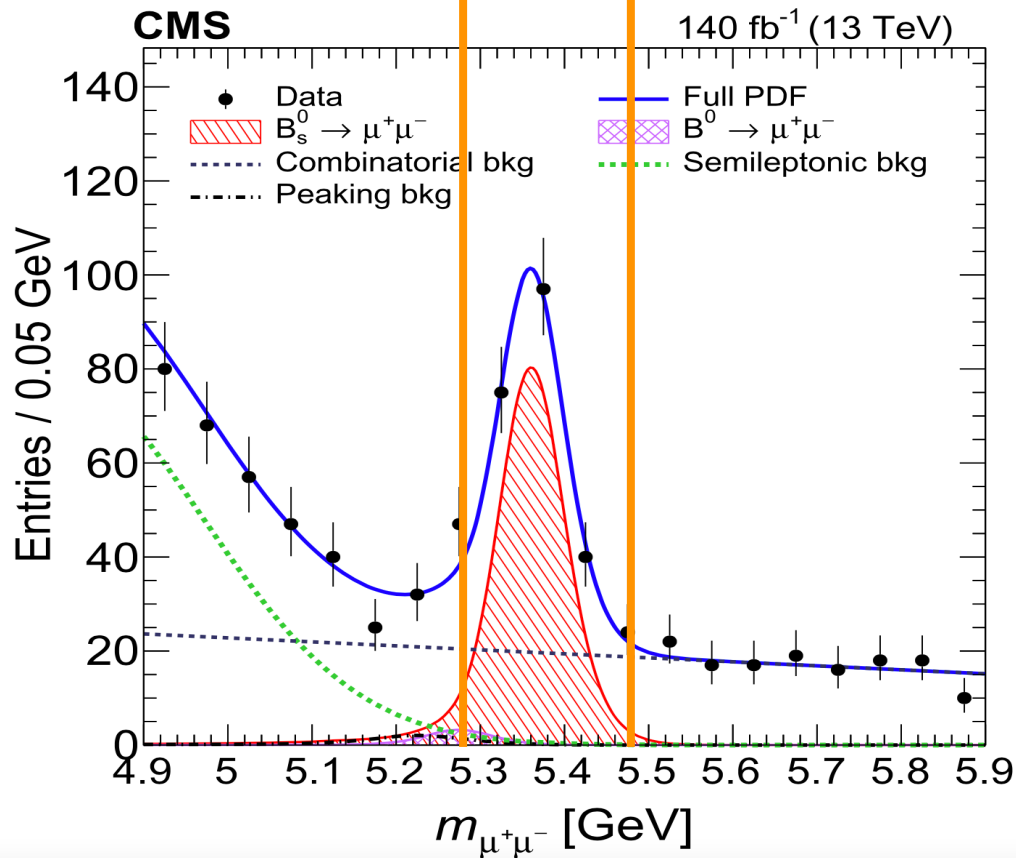
An additional variable : the effective lifetime

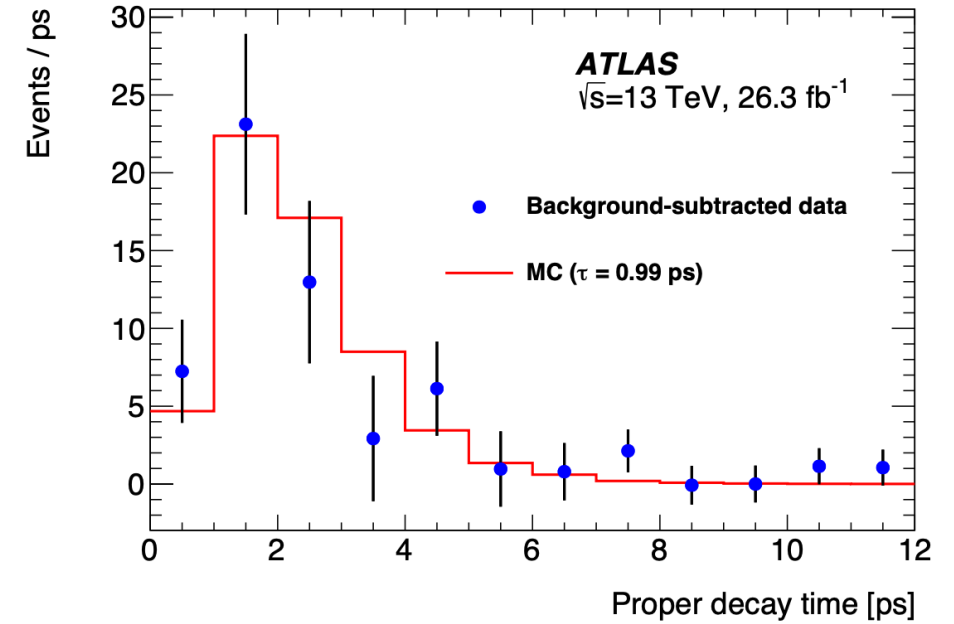
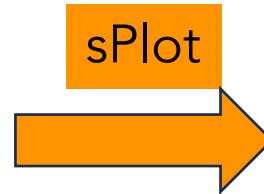
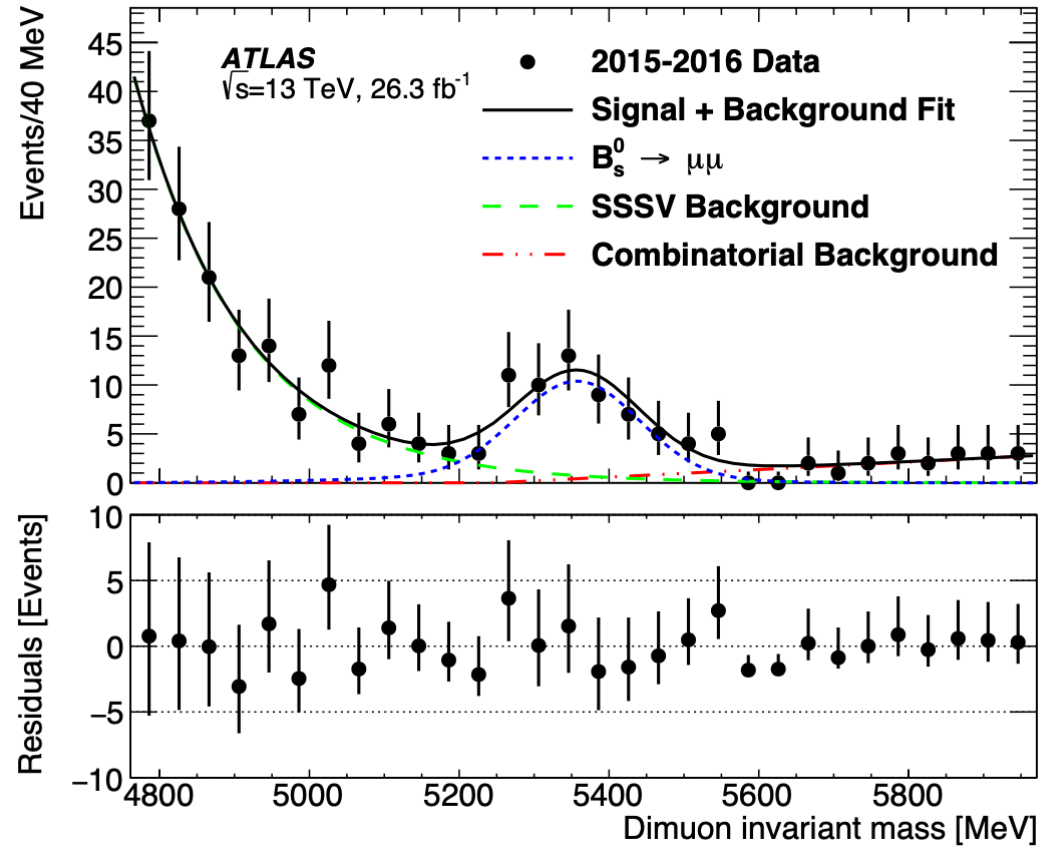
$$\tau_{\mu^+\mu^-} \equiv \frac{\int_0^\infty t \Gamma(B_s(t) \rightarrow \mu^+ \mu^-) dt}{\int_0^\infty \Gamma(B_s(t) \rightarrow \mu^+ \mu^-) dt} = \frac{\tau_{B_s^0}}{1 - y_s^2} \left[\frac{1 + 2A_{\Delta\Gamma_s}^{\mu\mu} y_s + y_s^2}{1 + A_{\Delta\Gamma_s}^{\mu\mu} y_s} \right]$$

Enough statistics to start measuring the effective lifetime:



3D (dimuon invariant mass, decay time, and decay time uncertainty) Maximum Likelihood fit





Effective lifetime results:

$$2.07 \pm 0.29 \pm 0.03 \text{ ps}$$

LHCb

$$1.83^{+0.23}_{-0.20} \text{ (stat)}^{+0.04}_{-0.04} \text{ (syst)} \text{ ps.}$$

CMS

$$0.99^{+0.42}_{-0.07} \text{ (stat.)} \pm 0.17 \text{ (syst.) ps}$$

ATLAS

NB :

$$\tau_L = 1.423 \pm 0.005 \text{ ps and } \tau_H = 1.620 \pm 0.007 \text{ ps}$$

| Lifetime | Value [ps] |
|--|-----------------------------|
| $\tau_{B_s^0 \rightarrow J/\psi \phi}$ | $1.480 \pm 0.011 \pm 0.005$ |

JHEP 04 (2014) 114
<1 % relative precision

Will play a role in future

What to expect with HL-LHC?

LHCb

$BR(B_d \rightarrow \mu^+ \mu^-)$ still dominated by statistical uncertainty

$BR(B_s \rightarrow \mu^+ \mu^-)$: stat ~ 1.8 % syst ~ 4 % (f_s/f_d)

$BR(B_d \rightarrow \mu^+ \mu^-) / BR(B_s \rightarrow \mu^+ \mu^-)$: much more precisely predicted.

Measurement precision $\sim 10\%$

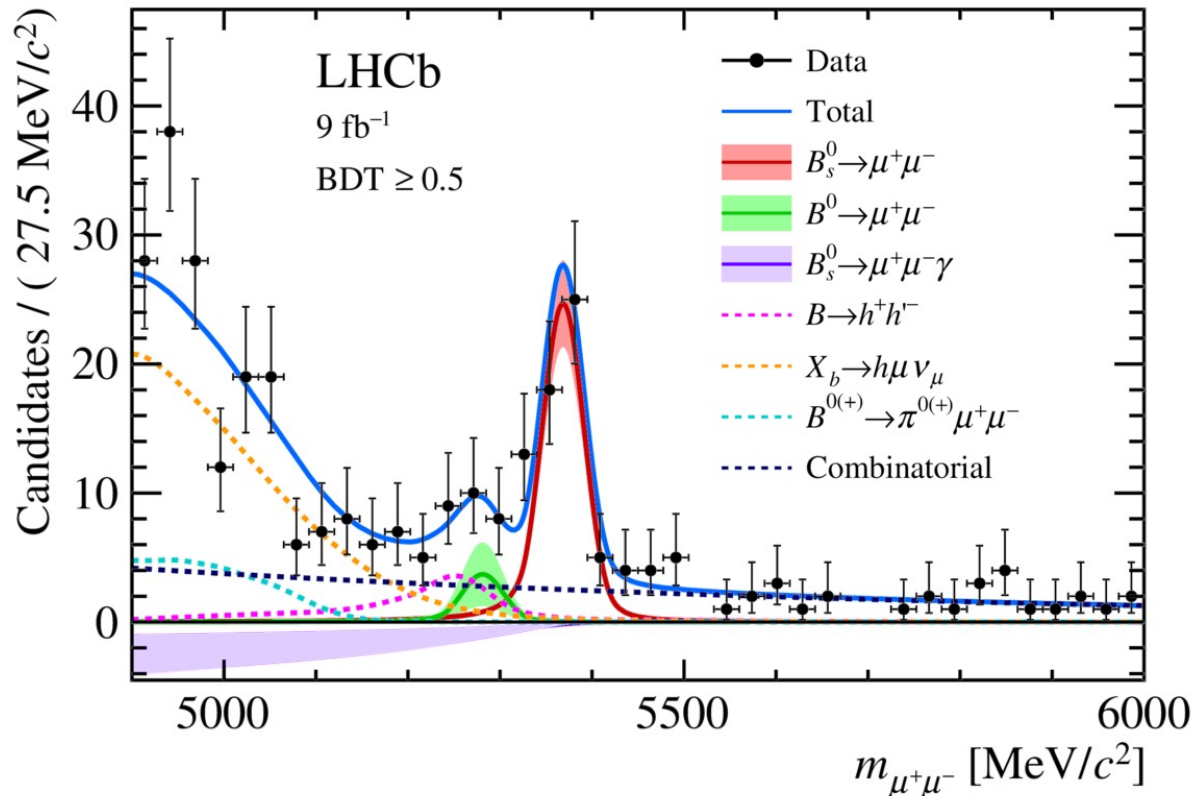
Additional observables:

- effective lifetime $\tau_{\mu\mu}$ precision for LHCb : 8% for 23 fb⁻¹ and 2 % with 300 fb⁻¹
- time dependent CP asymmetry (sensitive to NP phase) . Accessible only to LHCb with 300 fb⁻¹

$$B_{s,d} \rightarrow \mu^+ \mu^- \gamma$$

When the photon is soft: test of the high- q^2 region (above $\psi(2S)$). Do not try to reconstruct it !

Nice interplay with the $B \rightarrow V \mu^+ \mu^-$ where the low- q^2 (below J/ψ) is exhibiting tensions with predictions



$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^- \gamma) < 2.0 \times 10^{-9} \text{ at } 95\% \text{ CL}$$

$$m_{\mu\mu} > 4.9 \text{ GeV}/c^2$$

Need for a dedicated analysis going lower in $m_{\mu^+ \mu^-}$

An analysis targeting the low- q^2 (energetic photon) ?

In any case: **experimentally challenging !**

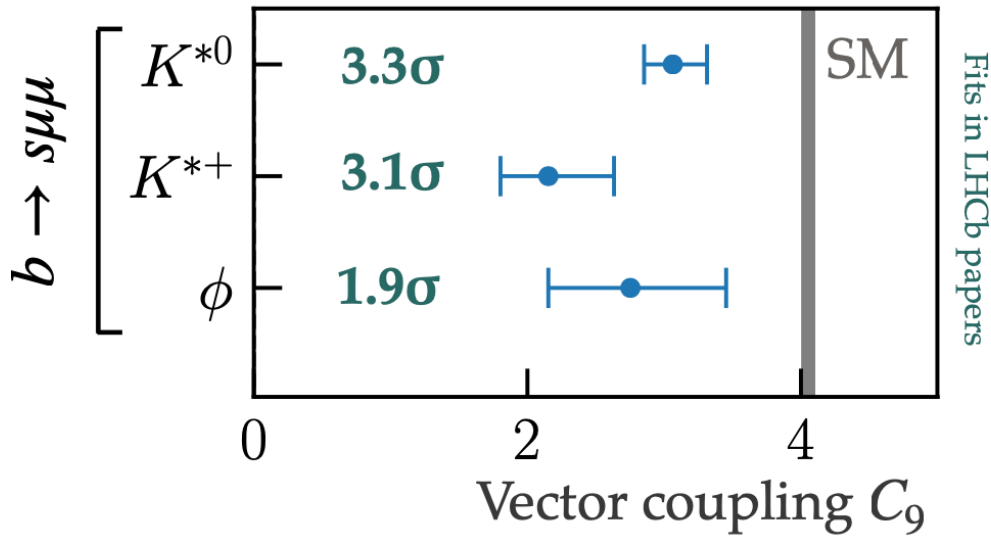
and predictions very sensitive to FF

$$H_b \rightarrow H_{s,d} \ell^+ \ell^-$$

- Constraining the non-local contribution from data ?
- More observables
- $b \rightarrow d \ell^+ \ell^-$

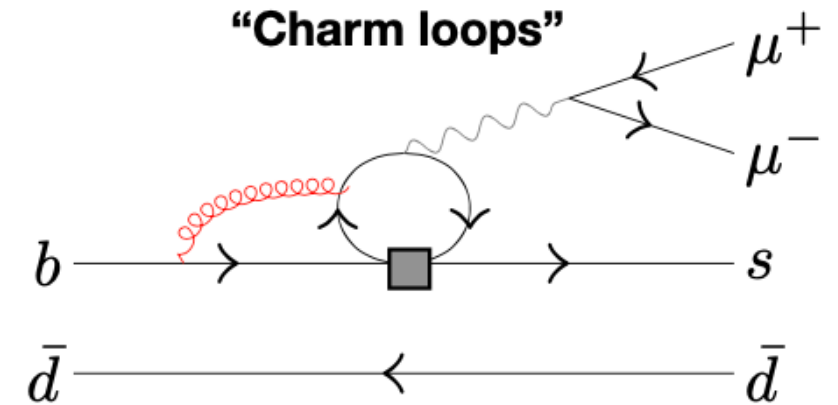
and more stat !

Constraining the non-local contribution from data ?

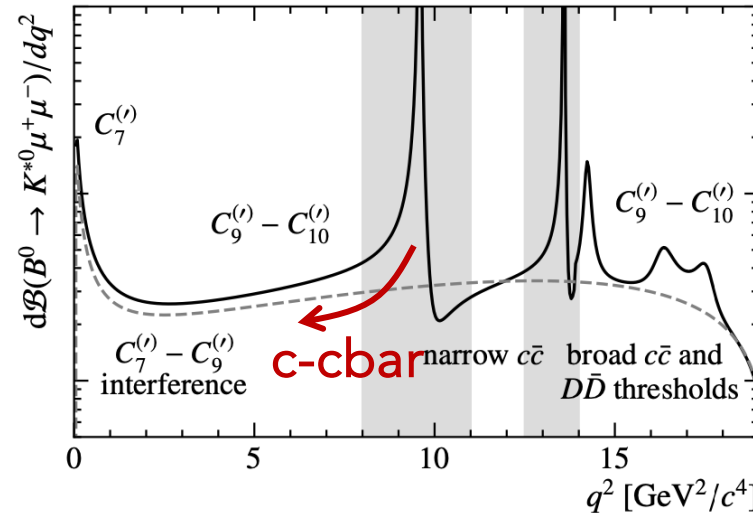


From Martino Borsato (SUSY2022)

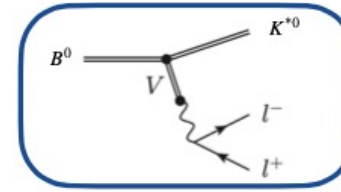
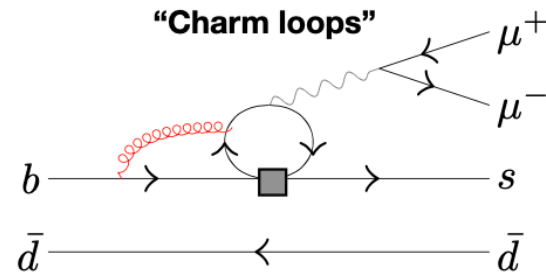
but :



would act as a shift on C_9

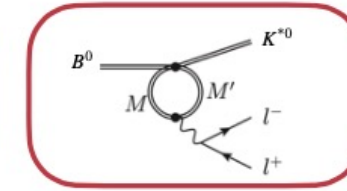


Lively theoretical debate on the estimate of these non-local effects



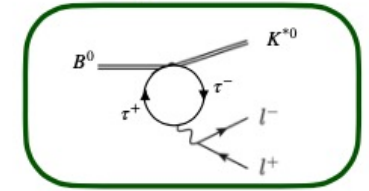
1-particle contributions

Includes:
 $\omega(782)$, $\psi(2S)$,
 $\rho(770)$, $\psi(3770)$,
 $\phi(1020)$, $\psi(4040)$,
 J/ψ , $\psi(4160)$



2-particle contributions

Includes:
 $D\bar{D}$,
 $D^*\bar{D}$,
 $D^*\bar{D}^*$



Tau loop contribution

C. Cornella, G. Isidori, M. König, S. Liechti, P. Owen, N. Serra [[Eur.Phys.J.C 80 \(2020\) 12, 1095](#)]

- Computation of the exchange of one soft gluon (seems to increase more the tension)
- Problem: the phase difference between the long-distance charm contribution and the short-distance physics
 - nuisance parameters in the global fits
 - **estimate from data fits** (next two slides)

Various possibilities (most of them on their way for $B^0 \rightarrow K^* \mu \mu$)

$$A_\lambda^{L,R} = A_\lambda^{L,R,Local} + H_\lambda(q^2)$$

$$C_9^{eff,\lambda}(q^2) = C_9^\mu + G_\lambda(q^2)$$

Model Independent

Model Dependent

Binned

Unbinned

Extract the angular observables from a 4D fit $(M, \vec{\Omega})$

Extract an amplitude ansatz ($A^{L,R}(q^2)$ modelled by polynomials) from a 4D fit $(q^2, \vec{\Omega})$

Extract $C_{9,10}^{(l)}$ + non-local contributions modelled by polynomials from a 4D fit $(q^2, \vec{\Omega})$

Extract $C_{9,10}^{(l)}$ C_9^τ + non-local contributions (magnitudes & phases) from a 4D fit $(q^2, \vec{\Omega})$

Estimate using data: $B \rightarrow K \mu \mu$

$$C_9^{\text{eff}} = C_9 + Y(q^2)$$

$$C_9^{\text{eff}} = C_9 + \sum_j \eta_j e^{i\delta_j} A_j^{\text{res}}(q^2)$$

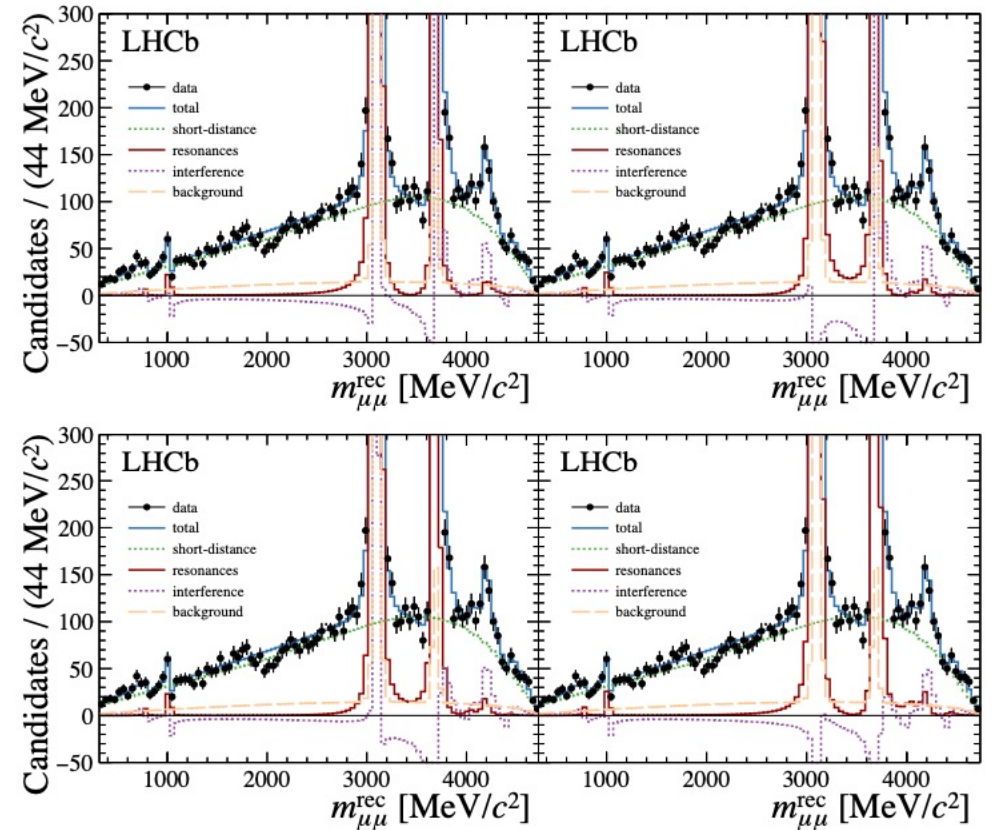
magnitude of the
resonance

phase of the
resonance wrt C_9

- Resonances added as relativistic BW
Branching ratios of $B_+ \rightarrow VK_+$ constrained from the PDG (assuming factorization)
- Form-factors constrained from lattice QCD ([Bailey et al., Phys.Rev.D 93 \(2016\) 2, 025026](#))
- Contribution of $D^{(*)}D^{(*)}$ ignored

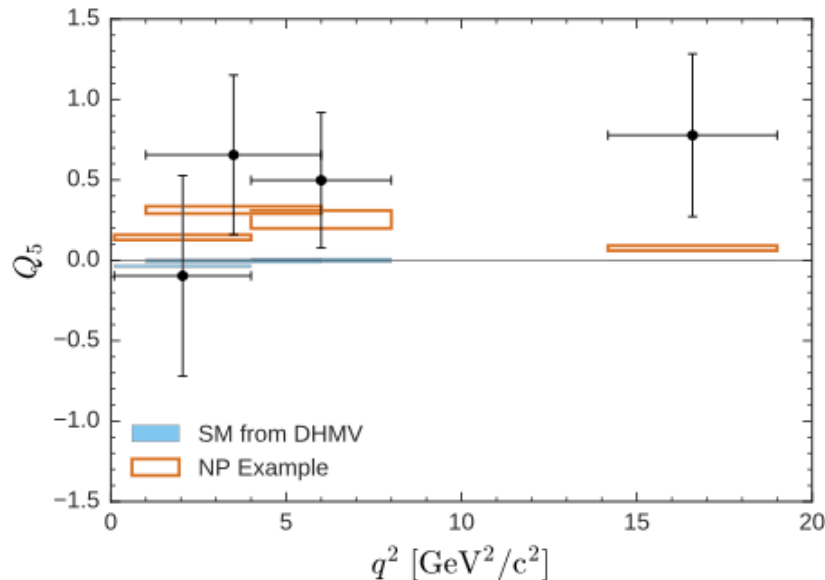
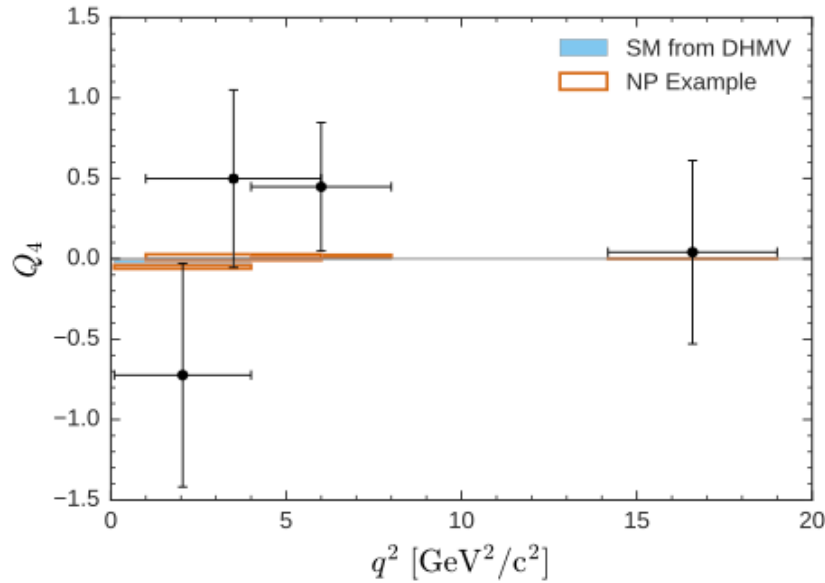
4 ambiguities

interference with the rare mode far from the pole is small
can be improved with more contributions



More observables, more modes

Belle PRL 118 (2017) 111801



Dataset

$\sigma(Q_5)$
 $1 < m_{\ell^+\ell^-}^2 < 6 \text{ GeV}^2/c^4$

Belle [32] ($\sim 0.7 \text{ ab}^{-1}$)

~ 0.5

LHCb (9 fb^{-1})

$\sim 0.1 - 0.15 ?$

Belle-II (25 ab^{-1})

~ 0.05

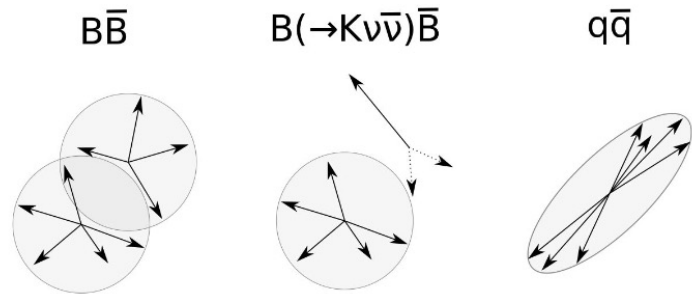
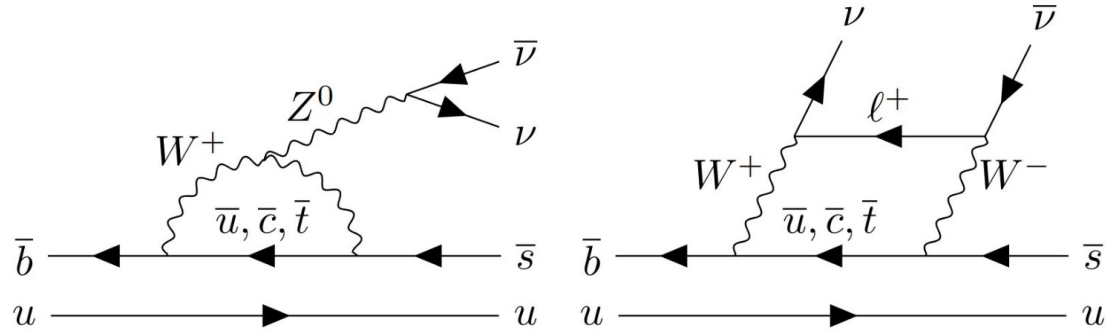
LHCb (23 fb^{-1})

$\sim 0.05 - 0.1 ?$

Are angular observables the same in $b \rightarrow s \mu \mu$ and $b \rightarrow s e e$?

- non-local contributions should be the same
- New Physics a priori different

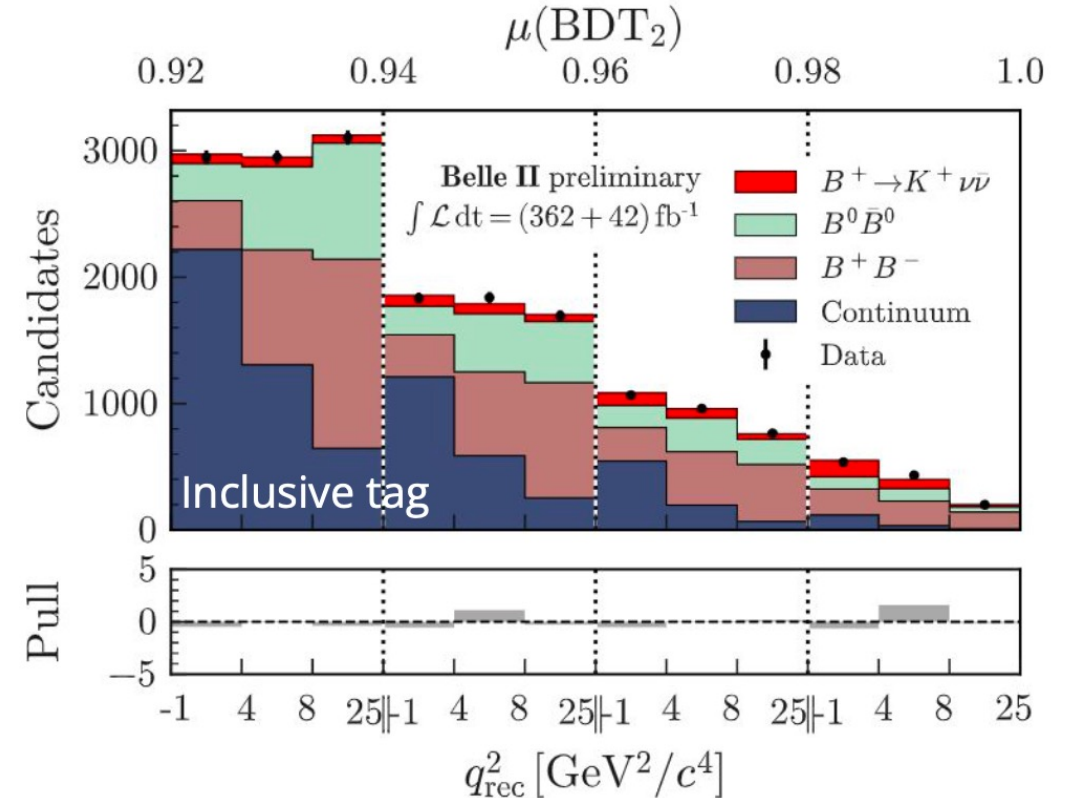
$B \rightarrow K \nu \bar{\nu}$

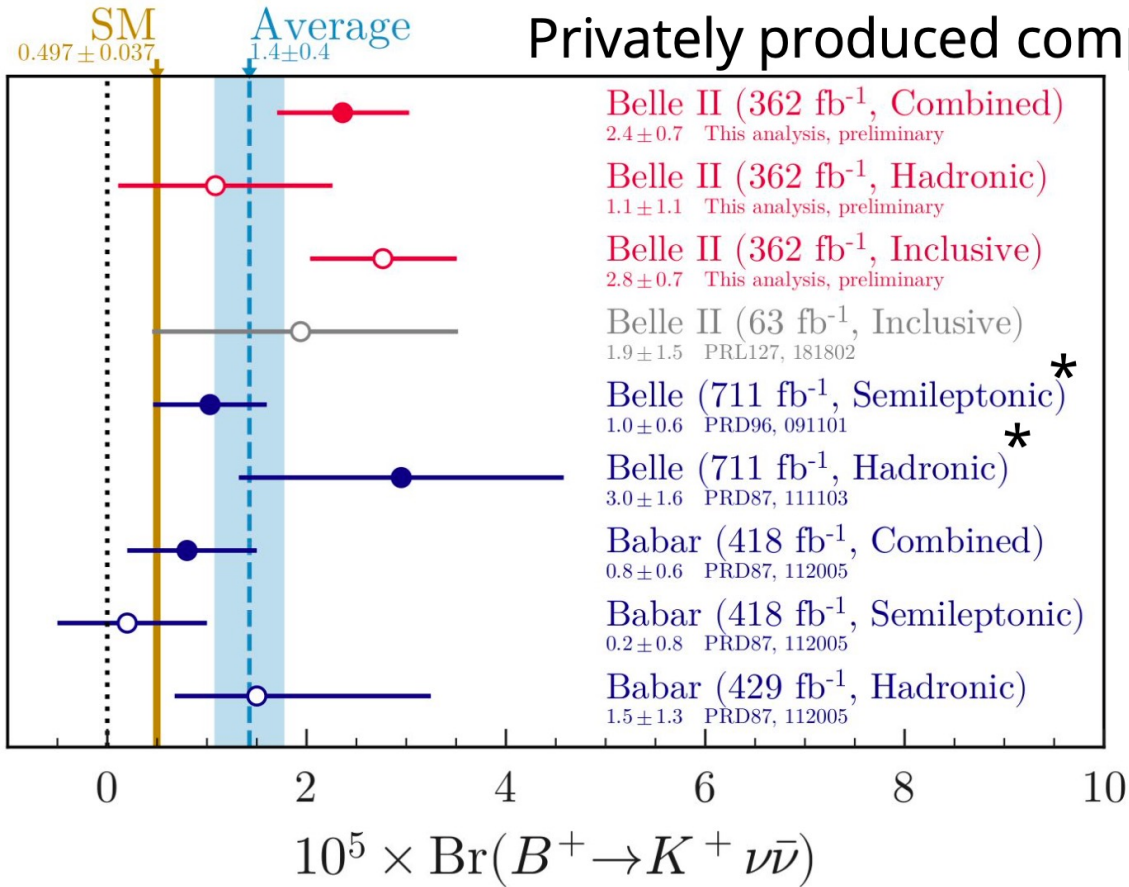


q^2 computed for the 2 neutrinos from K^+ recoil
 global analysis using general event information (2 BDT)
 Fit in bins of $q^2 \times$ BDT bins

Precisely predicted in the SM

$$B(B \rightarrow K^+ \nu \bar{\nu}) = (5.6 \pm 0.4) \times 10^{-6} \quad (\text{arXiv:2207.13371})$$



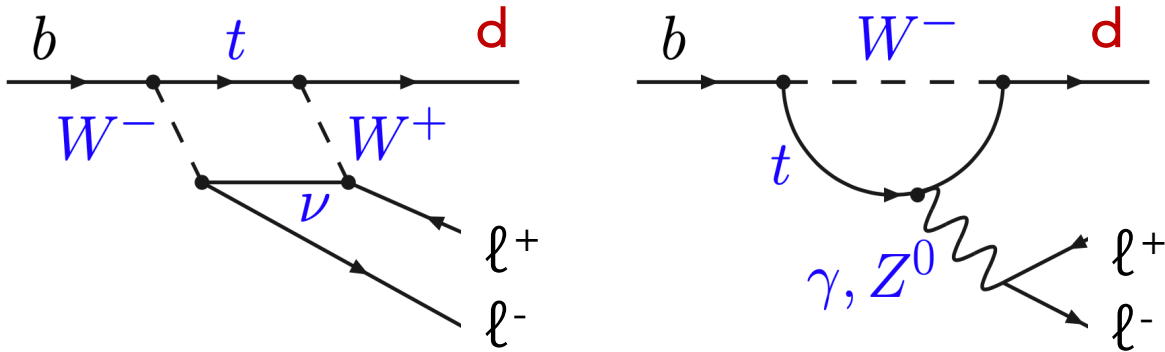


Not in significant tension with the SM

$$b \rightarrow d \ell^+ \ell^-$$

$$H_b \rightarrow H_d \ell^+ \ell^-$$

$$B_d \rightarrow \ell^+ \ell^-$$



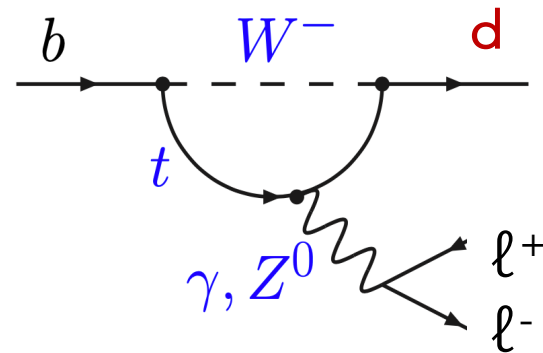
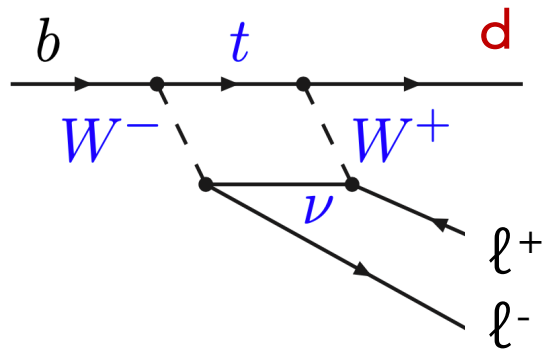
In the SM suppressed by $\left| \frac{V_{td}}{V_{ts}} \right|^2 \sim 0.04$

Rare modes are even more rare

But New Physics can couple differently: important to check

$B_d \rightarrow \ell^+ \ell^-$ "automatically" done (same final state)

What about $H_b \rightarrow H_d \ell^+ \ell^-$?



$$B^+ \rightarrow K \ell \ell$$

$$B^+ \rightarrow \pi \ell \ell$$

| $b \rightarrow s \ell^+ \ell^-$ | $b \rightarrow d \ell^+ \ell^-$ |
|------------------------------------|------------------------------------|
| $B^+ \rightarrow K \ell \ell$ | $B^+ \rightarrow \pi \ell \ell$ |
| $B^0 \rightarrow K_S \ell \ell$ | $B^0 \rightarrow \pi^0 \ell \ell$ |
| $B^0 \rightarrow K^{*0} \ell \ell$ | $B^0 \rightarrow \rho^0 \ell \ell$ |
| $B_s \rightarrow \phi \ell \ell$ | $B_s \rightarrow K^{*0} \ell \ell$ |

In most of the cases $b \rightarrow d \ell^+ \ell^-$ transitions are experimentally and theoretically more challenging than $b \rightarrow s \ell^+ \ell^-$

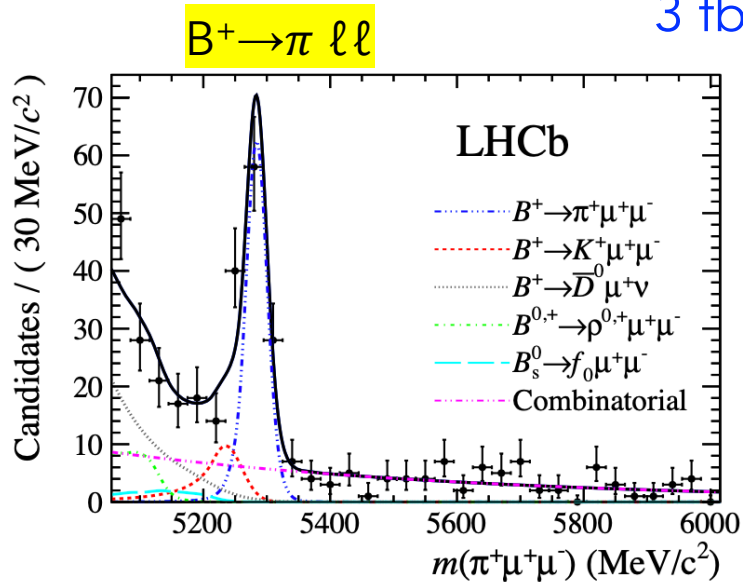
| | |
|---------------------------------|---------------------------------|
| $b \rightarrow s \ell^+ \ell^-$ | $b \rightarrow d \ell^+ \ell^-$ |
| $B^+ \rightarrow K \ell \ell$ | $B^+ \rightarrow \pi \ell \ell$ |

JHEP 10 (2015) 034

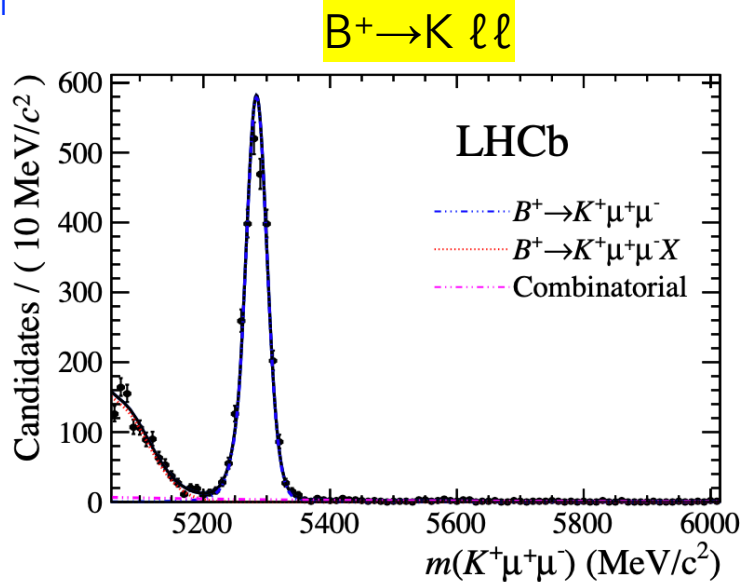
$$\mathcal{B}(B^\pm \rightarrow \pi^\pm \mu^+ \mu^-) = (1.83 \pm 0.24 \pm 0.05) \times 10^{-8}$$

full q^2 range (but J/ψ and $\psi(2S)$)

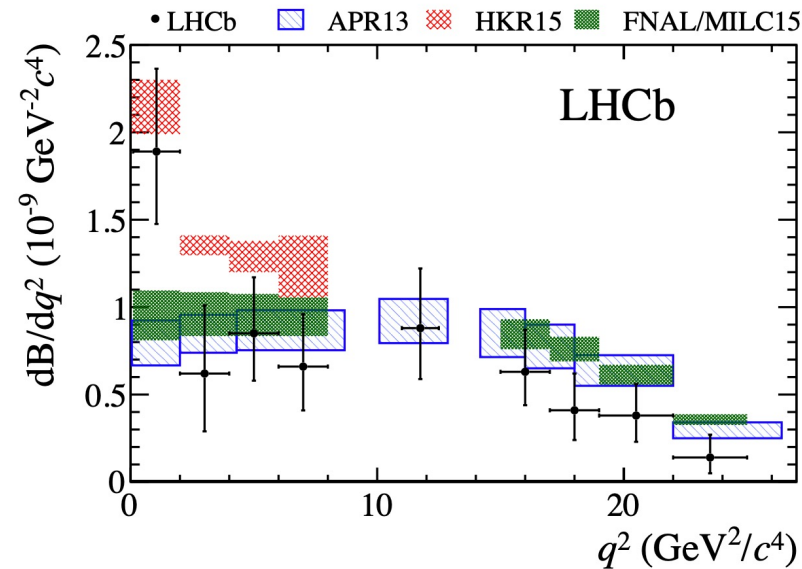
3 fb⁻¹



94 ± 12

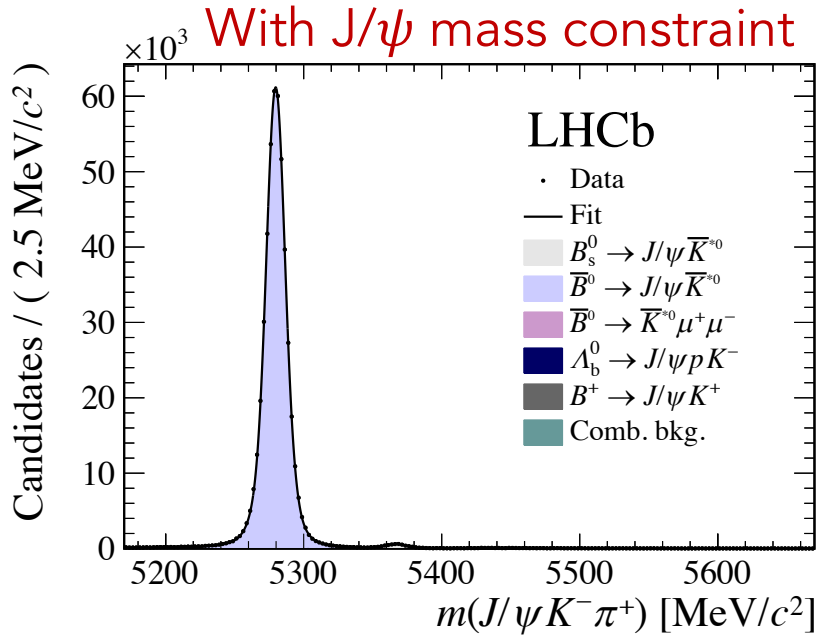


2922 ± 55

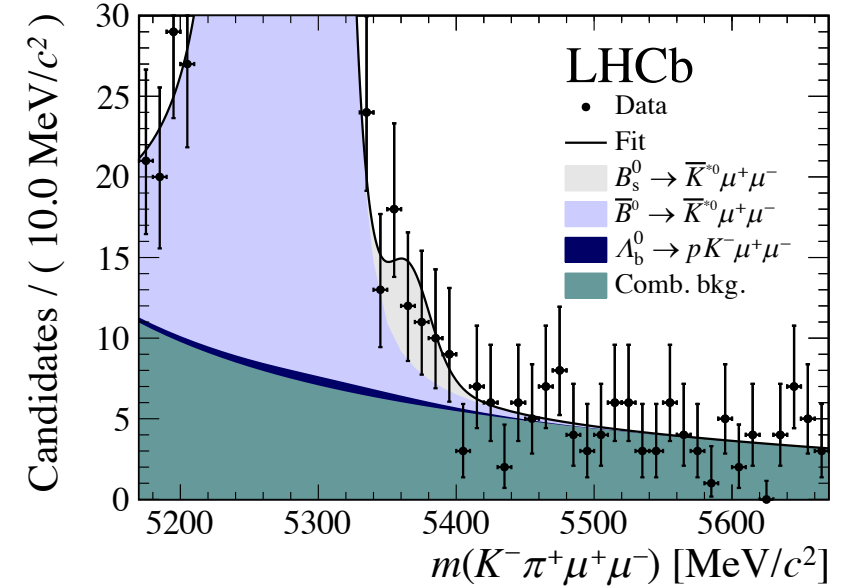
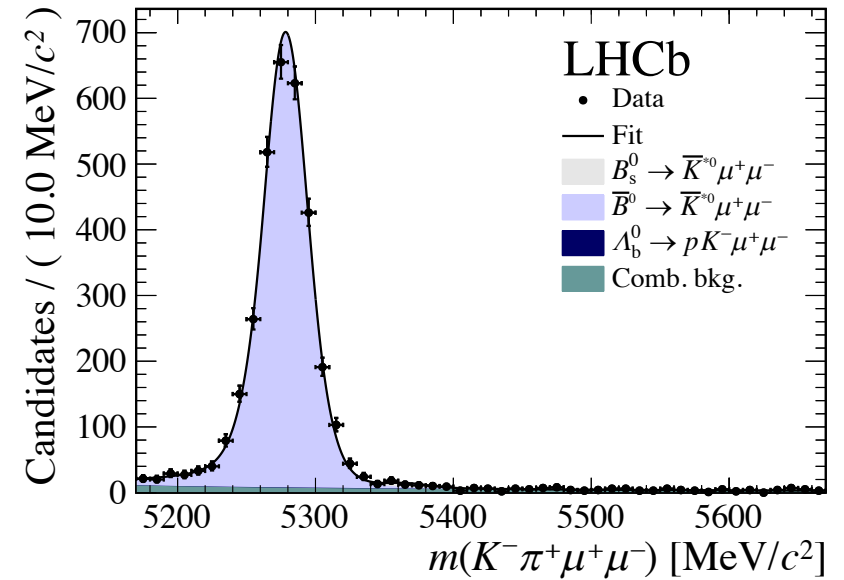
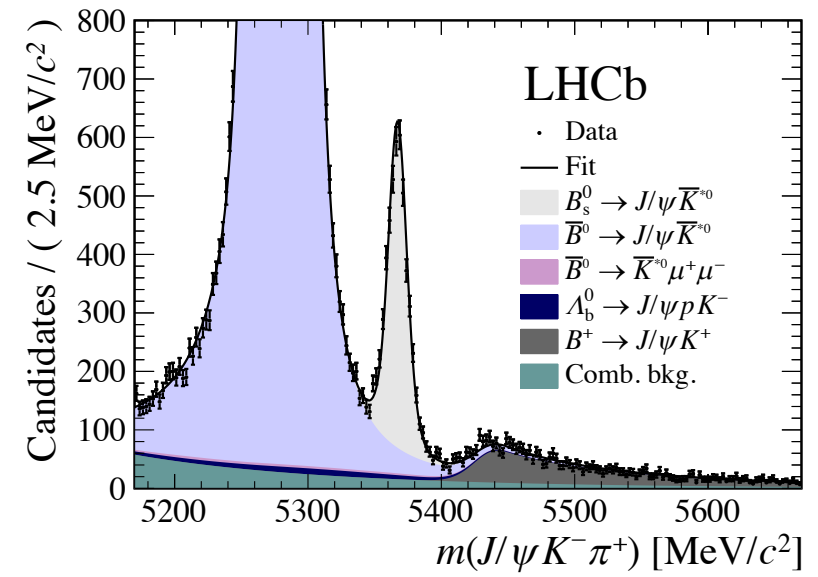


| | |
|----------------------------------|------------------------------------|
| $b \rightarrow s \ell^+ \ell^-$ | $b \rightarrow d \ell^+ \ell^-$ |
| $B_s \rightarrow \phi \ell \ell$ | $B_s \rightarrow K^{*0} \ell \ell$ |

$$\mathcal{B}(B_s^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-) = [2.9 \pm 1.0 (\text{stat}) \pm 0.2 (\text{syst}) \pm 0.3 (\text{norm})] \times 10^{-8}$$



4.6 fb⁻¹



Will not work with electrons

Conclusion

Les devises Shadok



EN ESSAYANT CONTINUELLEMENT
ON FINIT PAR RÉUSSIR. DONC:
PLUS ÇA RATE, PLUS ON A
DE CHANCES QUE ÇA MARCHÉ.

- Experimentalists are more and more using EFT 'language' (specially useful for analyses with a lot of observables)
- A shift in C_9 ($b \rightarrow s \mu\mu$ branching fractions and (some) angular parameters). Situation unclear... Experiments & theory progressing together
- $B_s \rightarrow \mu\mu$ is compatible with the SM: no obvious sign of NP in C_{10}
- No sign of large Lepton Flavour Universality violation in $b \rightarrow s \ell\ell$
- Photon polarization in $b \rightarrow s \gamma$ transitions compatible with SM expectation

**When SM agreement it is at the ~5%
precision, tests statistically limited**

→ More data and more analyses !

Stay tuned

Many thanks to J. Rouxel & JP
Couturier for the Shadoks

- 5 to 10% precision (stat dominated)



Looking back in the mirror

VOLUME 6, NUMBER 10

PHYSICAL REVIEW LETTERS

MAY 15, 1961

DECAY PROPERTIES OF K_2^0 MESONS*

D. Neagu, E. O. Okonov, N. I. Petrov, A. M. Rosanova, and V. A. Rusakov
Joint Institute of Nuclear Research, Moscow, U. S. S. R.
(Received April 20, 1961)

1961

Combining our data with those obtained in reference 7, we set an upper limit of 0.3% for the relative probability of the decay $K_2^0 \rightarrow \pi^- + \pi^+$. Our results on the charge ratio and the degree of the 2π -decay forbiddenness are in agreement with each other and provide no indications that time-reversal invariance fails in K^0 decay.

Experiment stopped

In 1964 CP violation discovery:
 $(2.0 \pm 0.4) 10^{-3}$

Physical Review Letters, vol. 13, n° 4, 1964, p. 138

Backup slides

Why don't you look at $B_s \rightarrow ee$?

SM prediction

more helicity suppression !

$$\mathcal{B}(B_s^0 \rightarrow e^+e^-) = (8.60 \pm 0.36) \times 10^{-14}$$

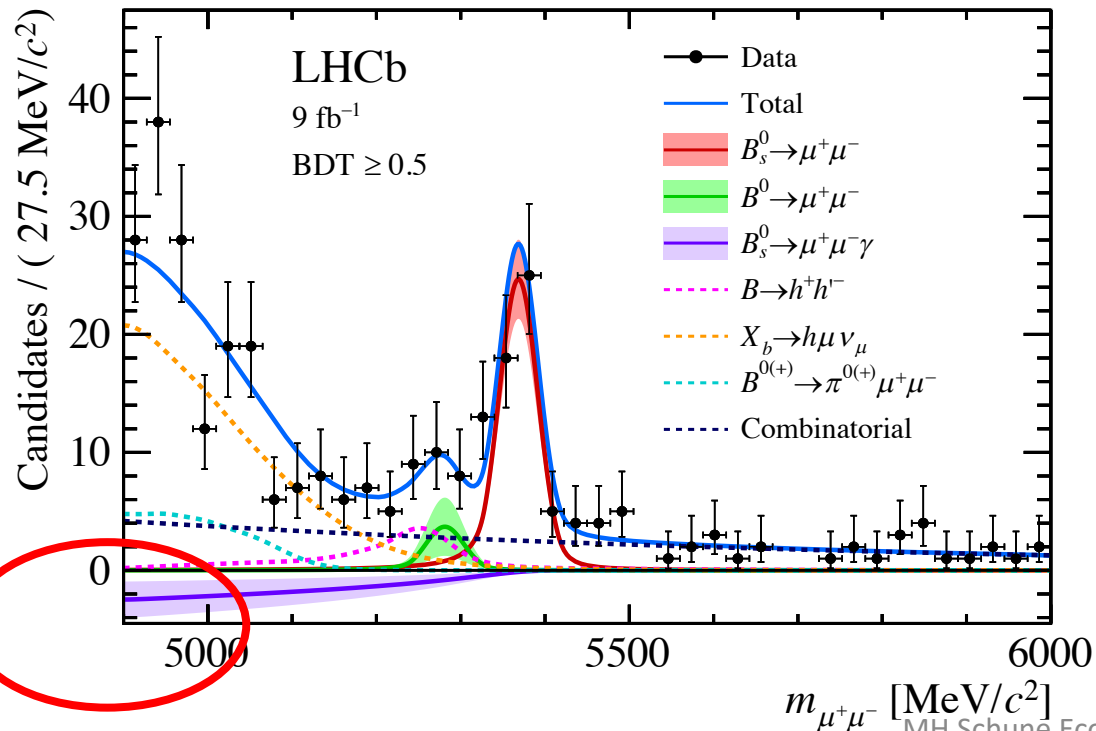
$$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) = (3.66 \pm 0.14) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow e^+e^-) = (2.41 \pm 0.13) \times 10^{-15}$$

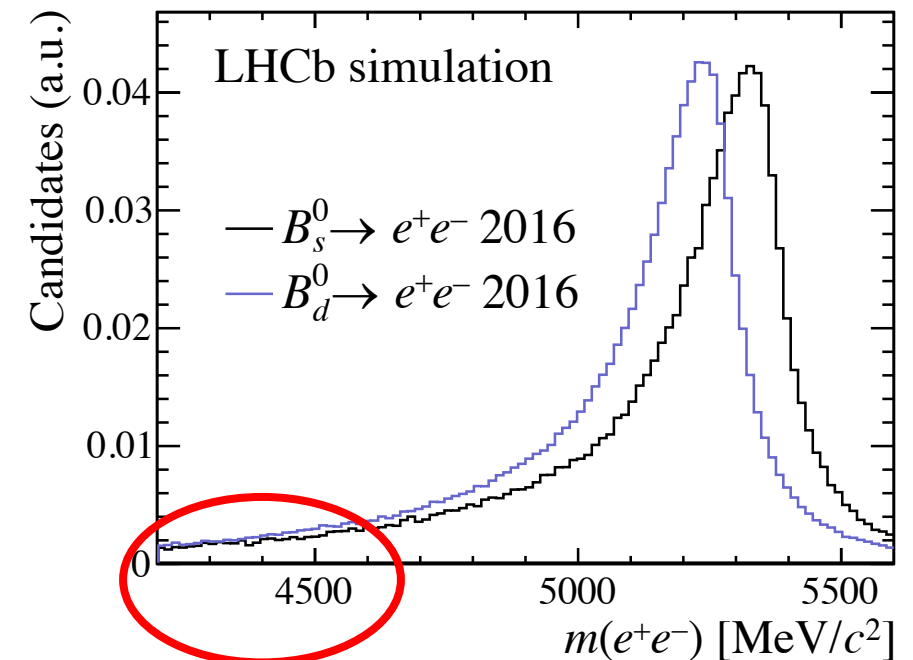
$$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-) = (1.03 \pm 0.05) \times 10^{-10}$$

But electrons emit Bremsstrahlung photons

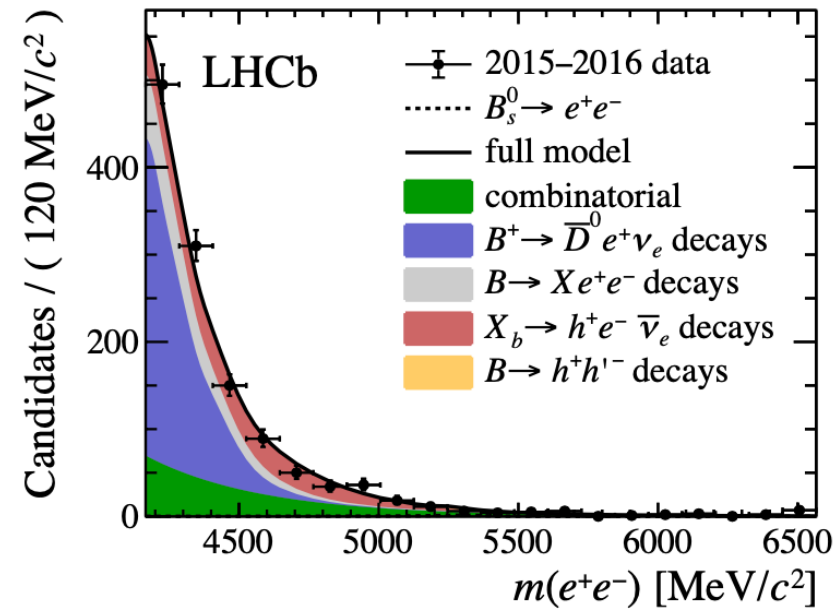
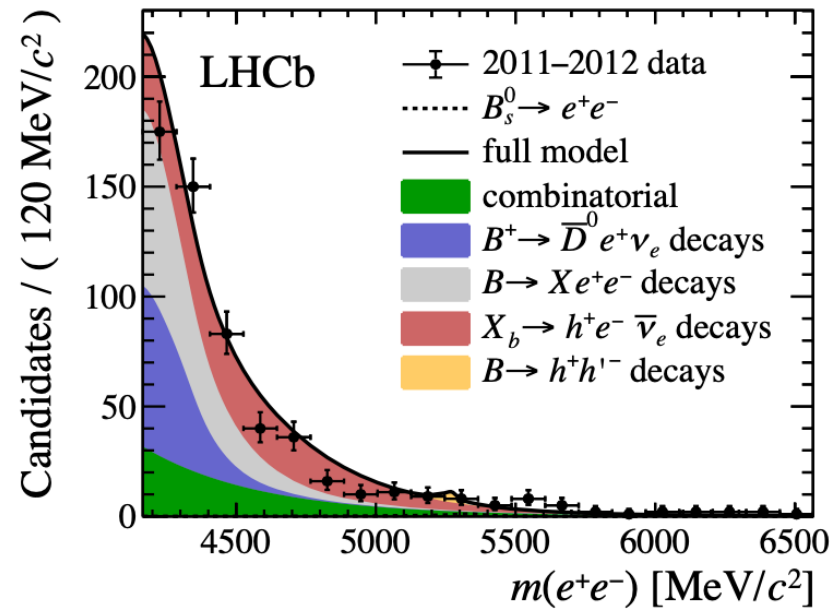
$\mu\mu$



ee



Not enough mass resolution to separate B_d from B_s



$$\mathcal{B}(B_s^0 \rightarrow e^+e^-) < 9.4 (11.2) \times 10^{-9} \text{ at } 90 (95) \% \text{ confidence level} \quad (5 \text{ fb}^{-1})$$

5 orders of magnitude wrt to SM

The top quark at an $e^+ e^-$ collider with $\sqrt{s}=10$ GeV in 1987 !

$e^+ e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ at $\sqrt{s} = 10.58$ GeV

Production of coherent $B\bar{B}$ pairs

First hint of a really large m_{top} !

Argus Collaboration
Phys Lett B 192 p454

$B^0 \rightarrow D^{*-} \mu^+ \nu$

$B^0 \rightarrow D^{*-} \mu^+ \nu$

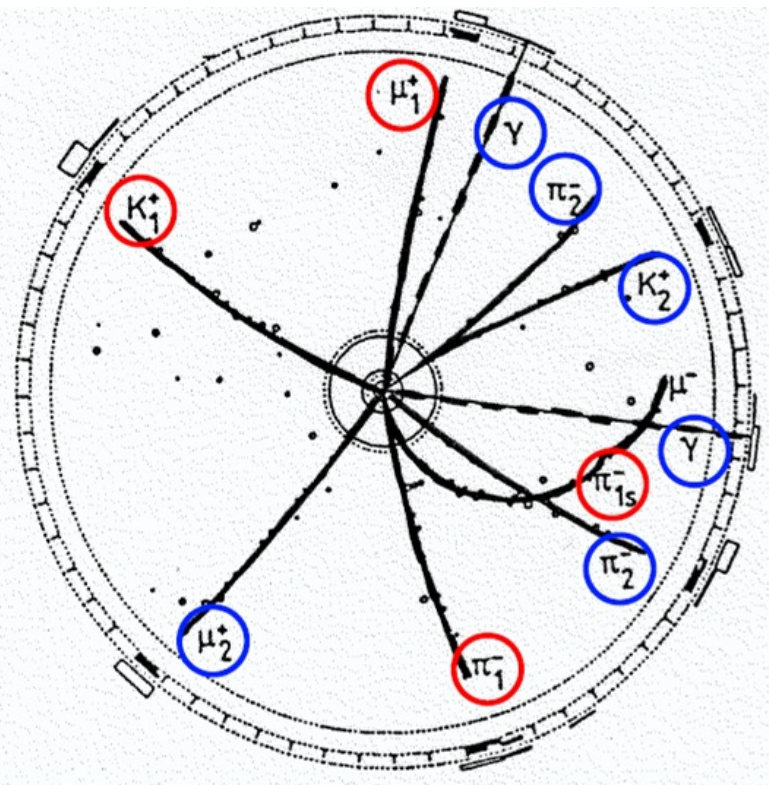
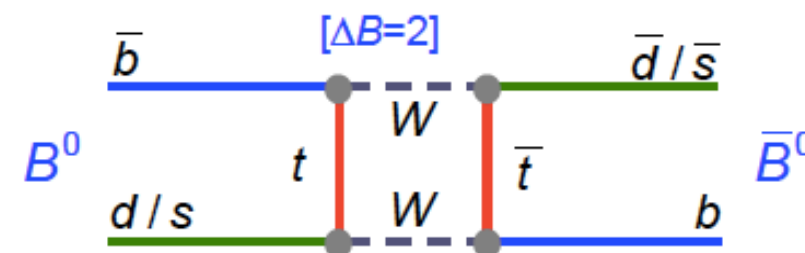


Fig. 11: The fully reconstructed ARGUS event [26]
 $e^+ e^- \rightarrow \Upsilon(4S) \rightarrow B^0 \bar{B}^0 \rightarrow B^0 B^0$
 as the first evidence for the occurrence of $B^0 \bar{B}^0$ oscillations.
 $B^0 \rightarrow D_1^{*-} \mu_1^+ \nu$, \leftarrow
 $D_1^{*-} \rightarrow \pi_1^- \bar{D}^0$, $\bar{D}^0 \rightarrow K_1^+ \pi_1^-$.
 $\bar{B}^0 \rightarrow B^0 \rightarrow D_2^{*-} \mu_2^+ \nu$, \leftarrow
 $D_2^{*-} \rightarrow \pi^0 D_2^-$,
 $\pi^0 \rightarrow \gamma \gamma$, $D_2^- \rightarrow K_2^+ \pi_2^- \pi_2^-$.

$$\Delta m_B \approx 0.00002 \cdot \left(\frac{m_t}{\text{GeV}/c^2} \right)^2 \text{ps}^{-1}$$

$$\approx 0.5 \text{ps}^{-1}$$

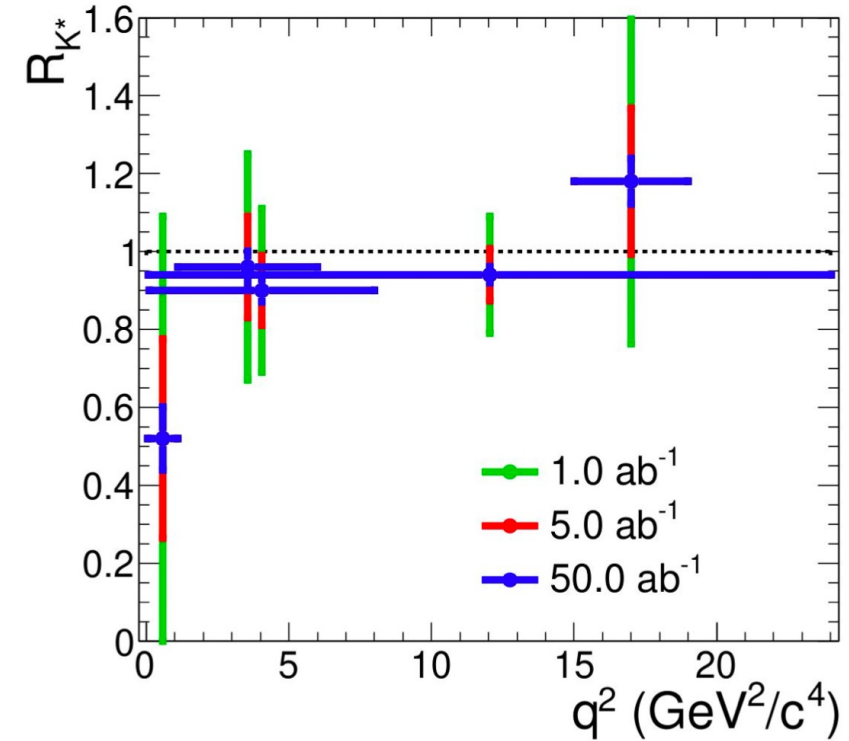
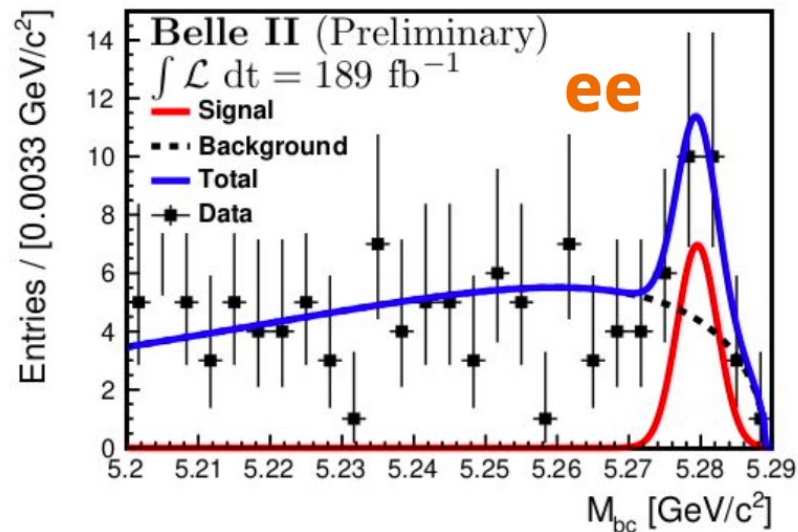
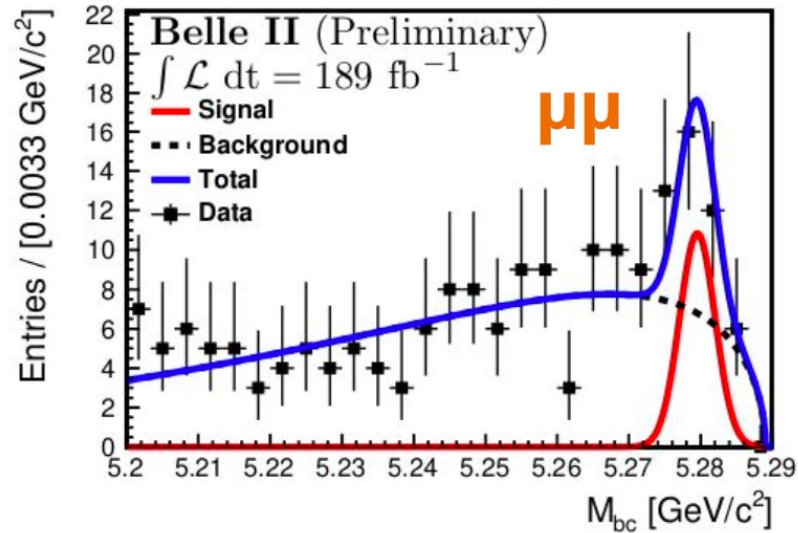
$$\Rightarrow m_t > 50 \text{ GeV}$$



Belle-II prospects on $R(K)$ and $R(K^*)$

$R(K^*)$ status

$\sim 3\%$ precision for q^2 bin [1-6] for 50 ab^{-1} of data



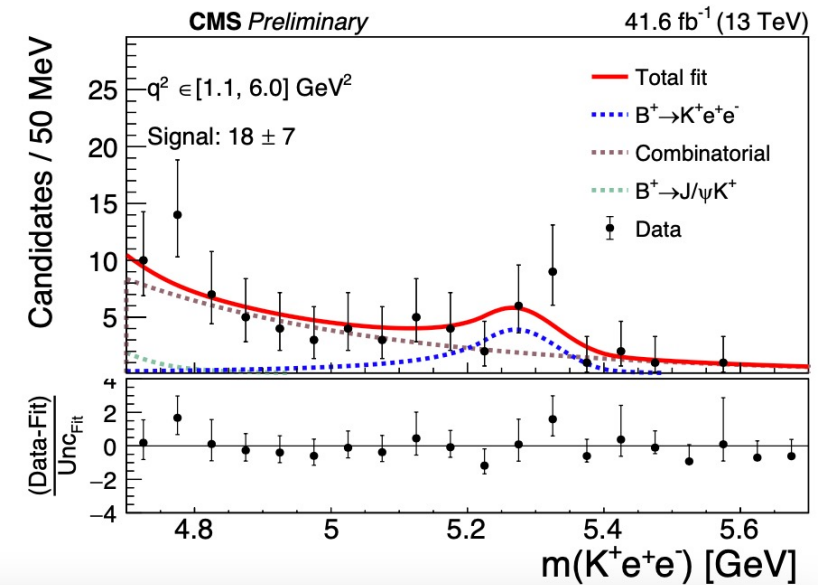
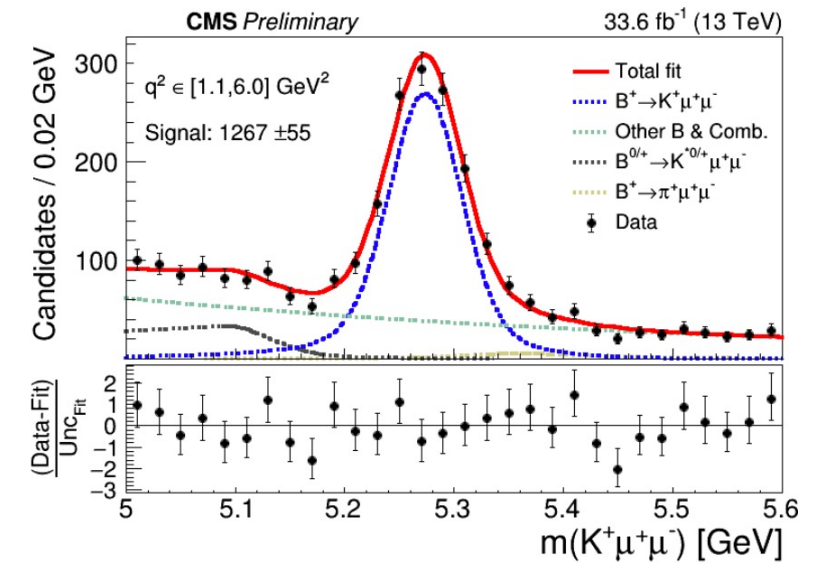
(ee) and ($\mu\mu$) similar !

$R(K)$ in the $1.1 < q^2 < 6.0 \text{ GeV}^2$ range

$$R_K = \frac{BF(B \rightarrow \mu\mu K)}{BF(B \rightarrow J/\psi K, J/\psi \rightarrow \mu\mu)} / \frac{BF(B \rightarrow ee K)}{BF(B \rightarrow J/\psi K, J/\psi \rightarrow ee)}$$

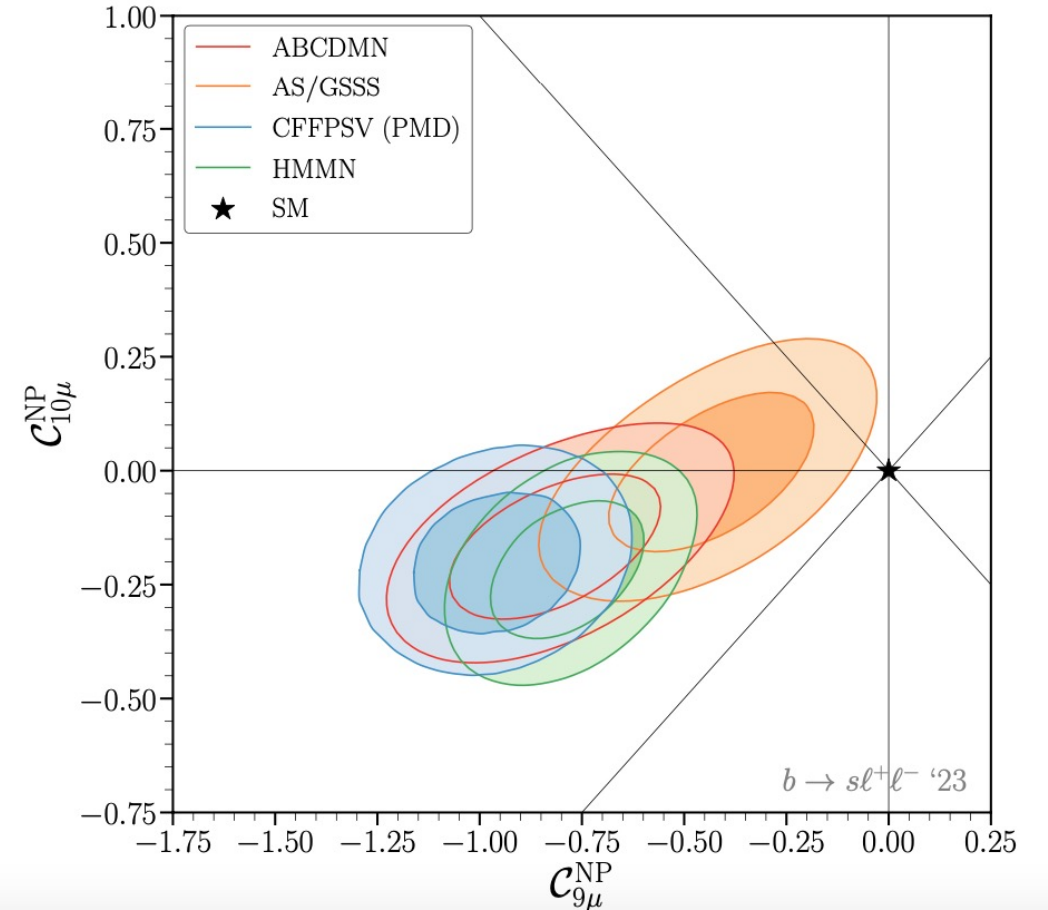
$$R(K) = 0.78_{-0.23}^{+0.46} (\text{stat})_{-0.05}^{+0.09} (\text{syst})$$

In agreement with SM



- Several fitters, they differs by:
 - Choice of experimental inputs
 - Form factors modelling
 - Treatment on non-local nuisance parameters
 - Statistical frameworks

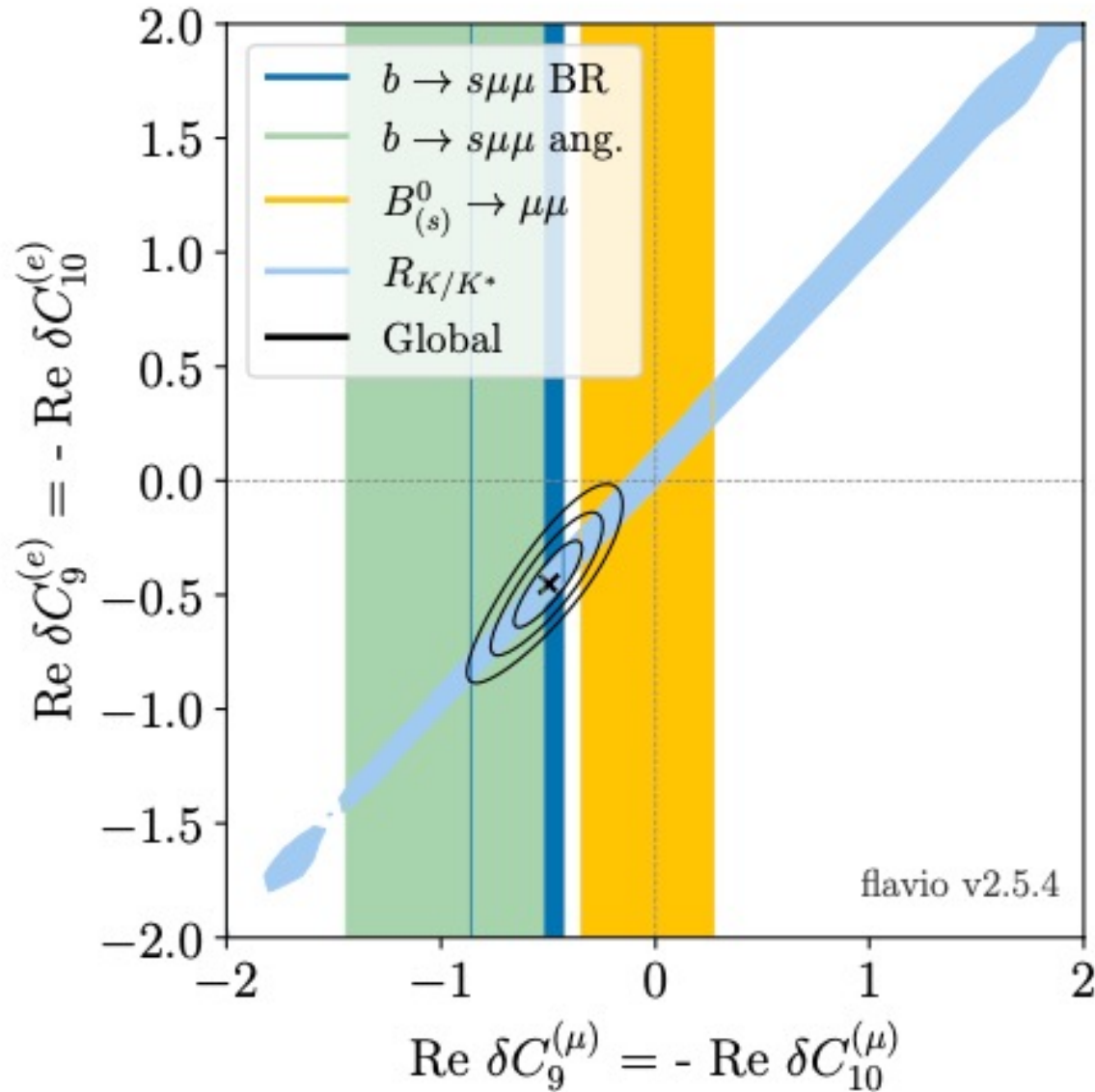
2-dimensional global fits



From B Capdevila FPCP2023

$$\delta C_9^{(\ell)} = -\delta C_{10}^{(\ell)} \equiv \delta C_{LL}^{(\ell)}/2 \quad \text{NP in e and } \mu$$

from Camille Normand
PhD thesis (2023)



shifts in Wilsons Coefficients
should be the same for
electrons and muons

What to expect with HL-LHC?

Additional observables:

- effective lifetime $\tau_{\mu\mu}$ precision for LHCb : 8% for 23 fb^{-1} and 2 % with 300 fb^{-1}
- time dependent CP asymmetry (sensitive to NP phase) . Accessible only to LHCb with 300 fb^{-1}

| Experiment | Scenario | $\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$ | $\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)$ |
|------------|----------------------------------|--|--|
| | | stat + syst % | stat + syst % |
| LHCb | 23 fb^{-1} | 8.2 | 33 |
| LHCb | 300 fb^{-1} | 4.4 | 9.4 |
| CMS | 300 fb^{-1} | 12 | 46 |
| CMS | 3 ab^{-1} | 7 | 16 |
| ATLAS | Run 2 | 22.7 | 135 |
| ATLAS | 3 ab^{-1} Conservative | 15.1 | 51 |
| ATLAS | 3 ab^{-1} Intermediate | 12.9 | 29 |
| ATLAS | 3 ab^{-1} High-yield | 12.6 | 26 |

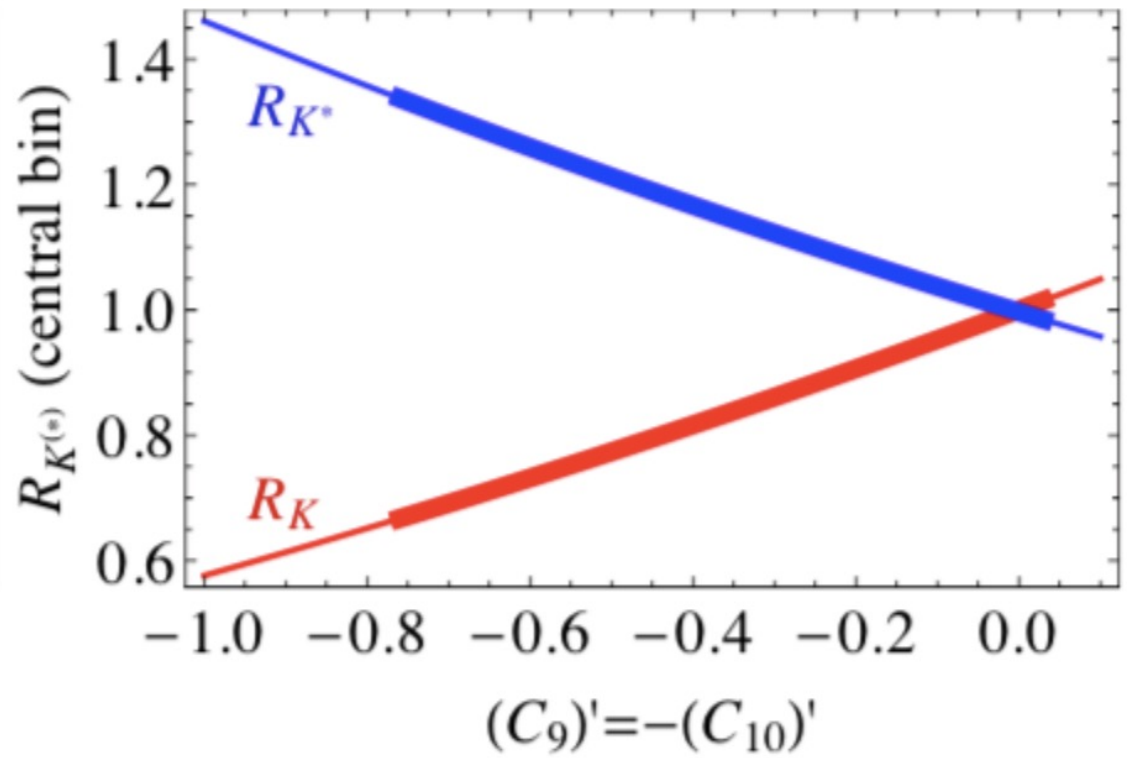
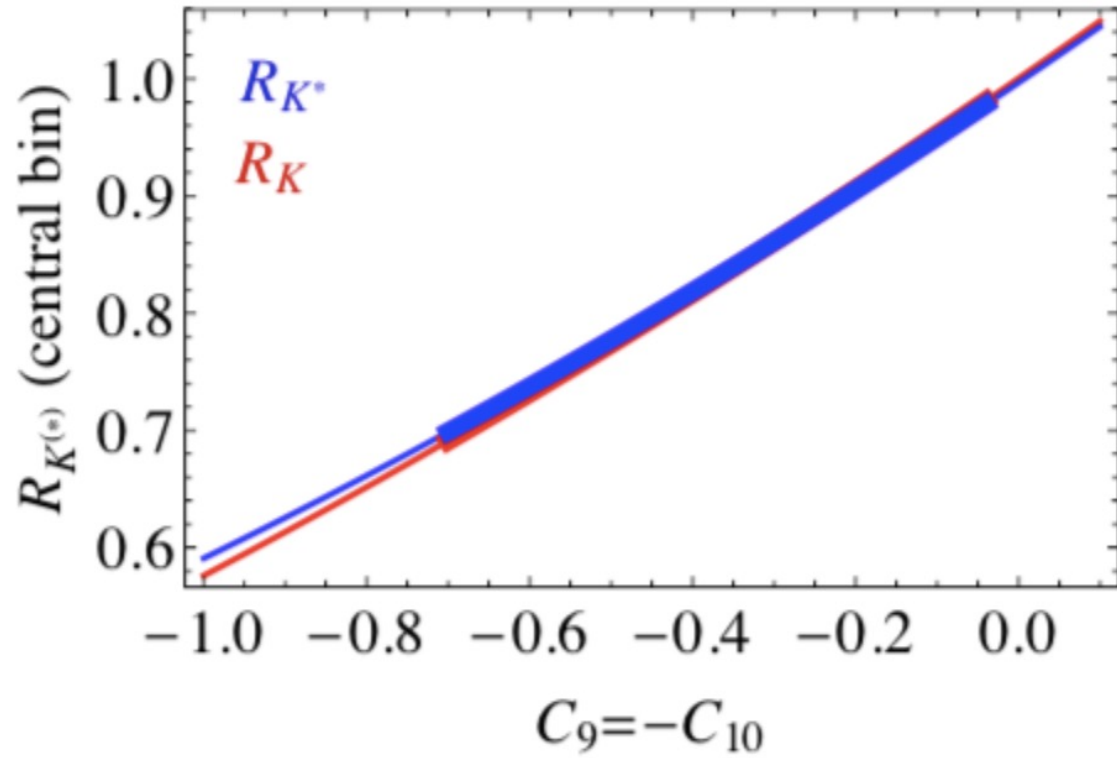
LHCb

$\text{BR}(B_d \rightarrow \mu^+ \mu^-)$ still dominated by statistical uncertainty

$\text{BR}(B_s \rightarrow \mu^+ \mu^-)$: stat ~ 1.8 % syst ~ 4 % (f_s/f_d)

$\text{BR}(B_d \rightarrow \mu^+ \mu^-) / \text{BR}(B_s \rightarrow \mu^+ \mu^-)$: much more precisely predicted.

Measurement precision $\sim 10\%$



From Damir Becirevic (Gif 2018)