A visualization of the cosmic web, showing a complex network of filaments and clusters of galaxies. The filaments are represented by thin, glowing blue lines, while the clusters are shown as bright, yellow and orange spots. The background is a deep blue.

# Numerical simulations for interpreting large-scale structure data

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**Silvia Bonoli**



**Nate Bastian**

- **3 staff**
- **6 PhD**
- **6 Postdocs**
  
- **Galaxy formation**
- **Black Holes & AGN/Quasars**
- **Star and clusters formation**
- **Large-scale structure**



**Donostia-San Sebastian, Spain**



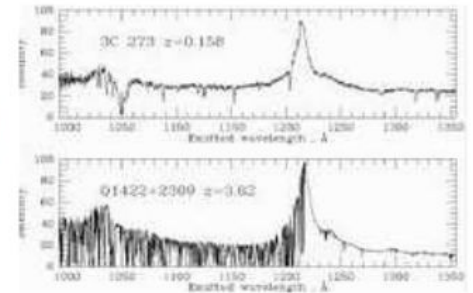
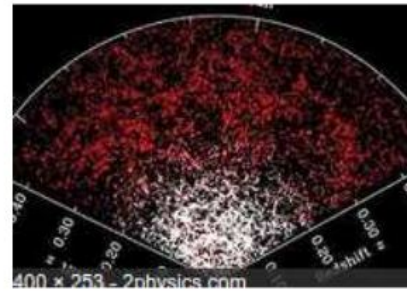
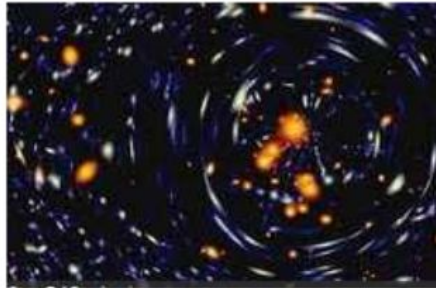
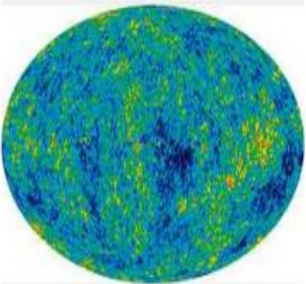
# Our current understanding of structure formation in the Universe:

**General Relativity**

**Dark Matter**

**Dark Energy**

**Inflation**



# Despite the progress, there are questions about each of the fundamental ingredients of LCDM

**Gravity Law**

**GR, Galileon, f(R)?**

**Accelerated  
Expansion**

**DE, coupled, w(z)?**

**Dark Matter**

**Temperature,  
Neutrinos, Quantum?**

**Initial Conditions  
Inflation  
Single/multi-field?**

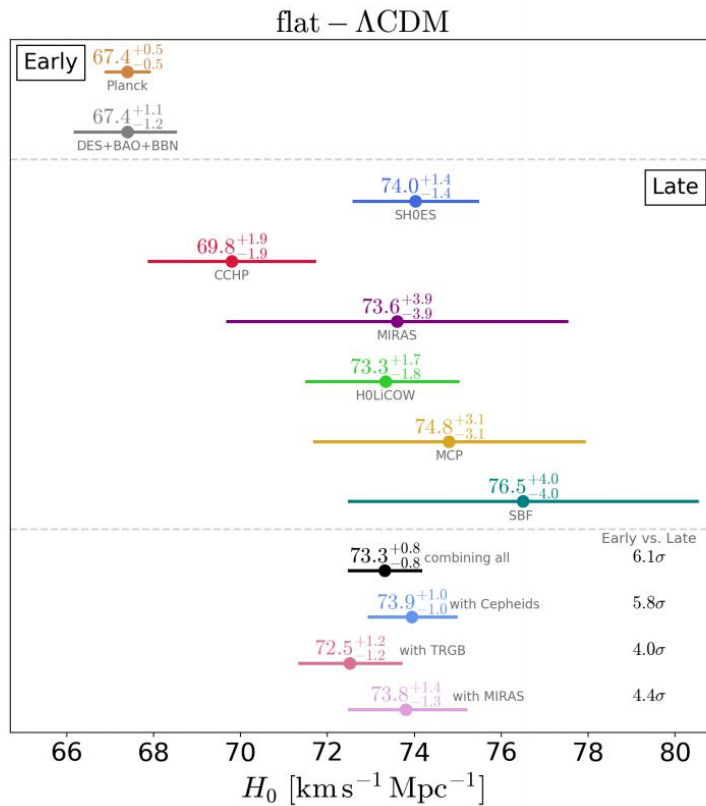
No deviations have  
from the simplest  
LCDM model been  
detected so far

$\Omega_K$ .....	$-0.0096 \pm 0.0061$
$\Sigma m_\nu$ [eV] .....	$< 0.241$
$N_{\text{eff}}$ .....	$2.89^{+0.36}_{-0.38}$
$r_{0.002}$ .....	$< 0.101$

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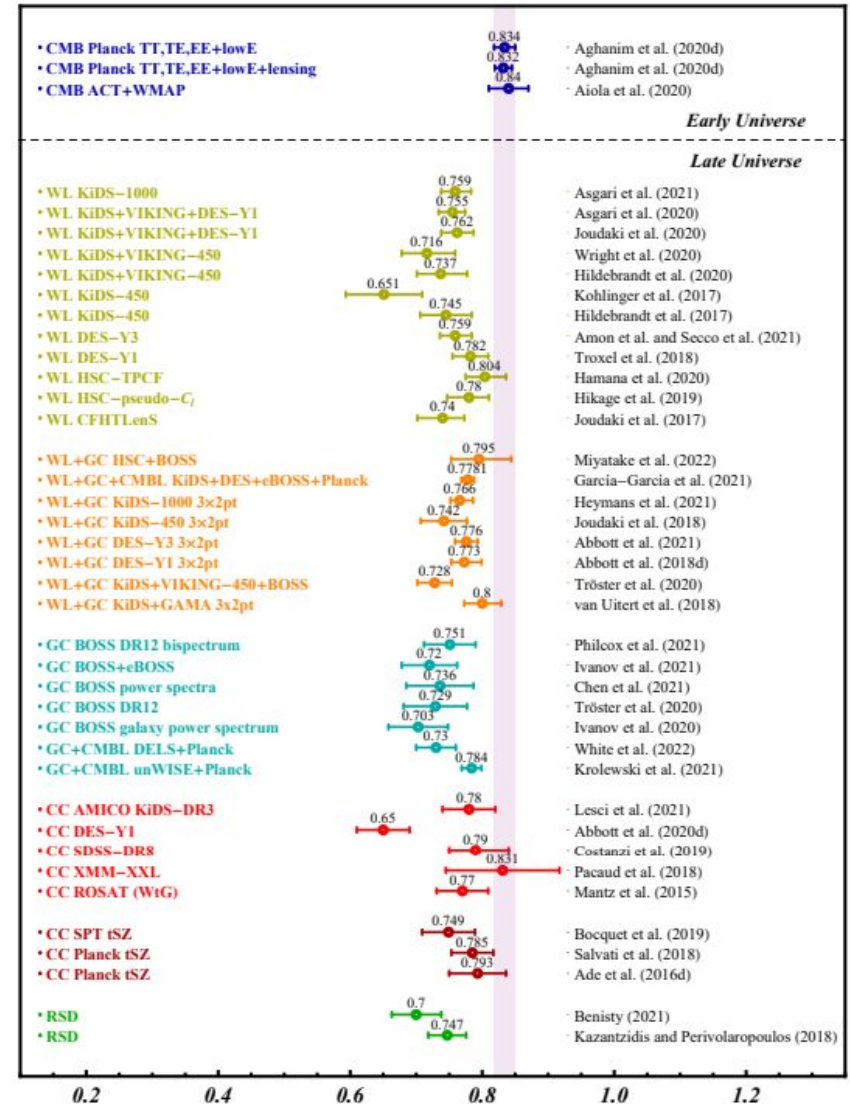
# Tensions between the low-z universe and CMB expectations

## Hubble Parameter



Verde et al 2019, Vagnozzi et al 2021

## Structure Parameter



# The era of precision cosmology for Large-scale structure data

2019-2030:

SKA  
SQUARE KILOMETER ARRAY

WFIRST  
WIDE-FIELD INFRARED SURVEY TELESCOPE  
ASTROPHYSICS • DARK ENERGY • EXOPLANETS

Euclid  
consortium

LSST  
Large Synoptic Survey Telescope

CHIME

MAVE

J-PAS  
Javalambre PAU Astrophysical Survey

eBOSS

ENERGY  
INSTRUMENT

ROSITA

CMB-S4  
Next Generation CMB Experiment

4  
MOST

Lensing

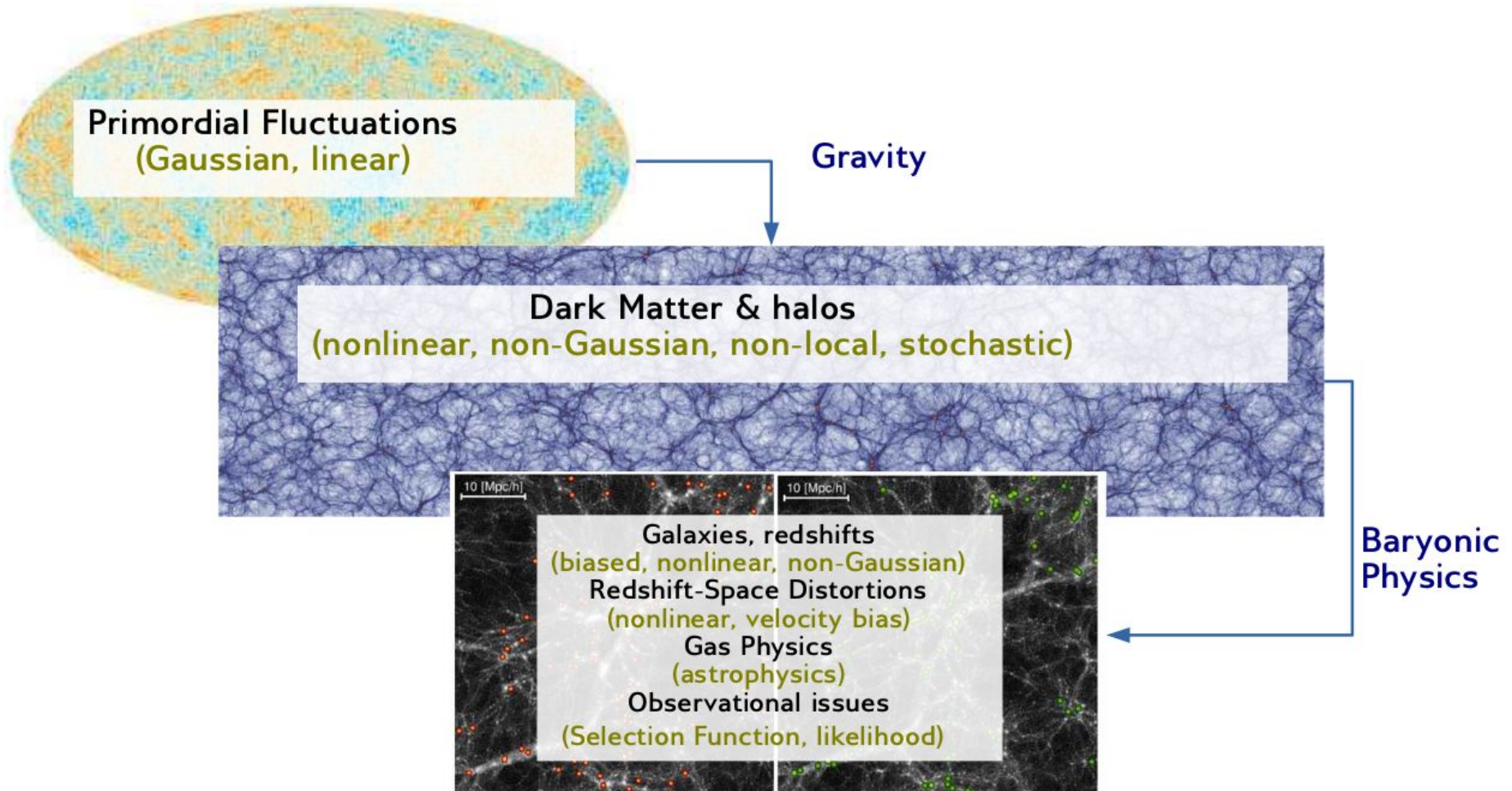
SZ-IM

Clustering

Clusters

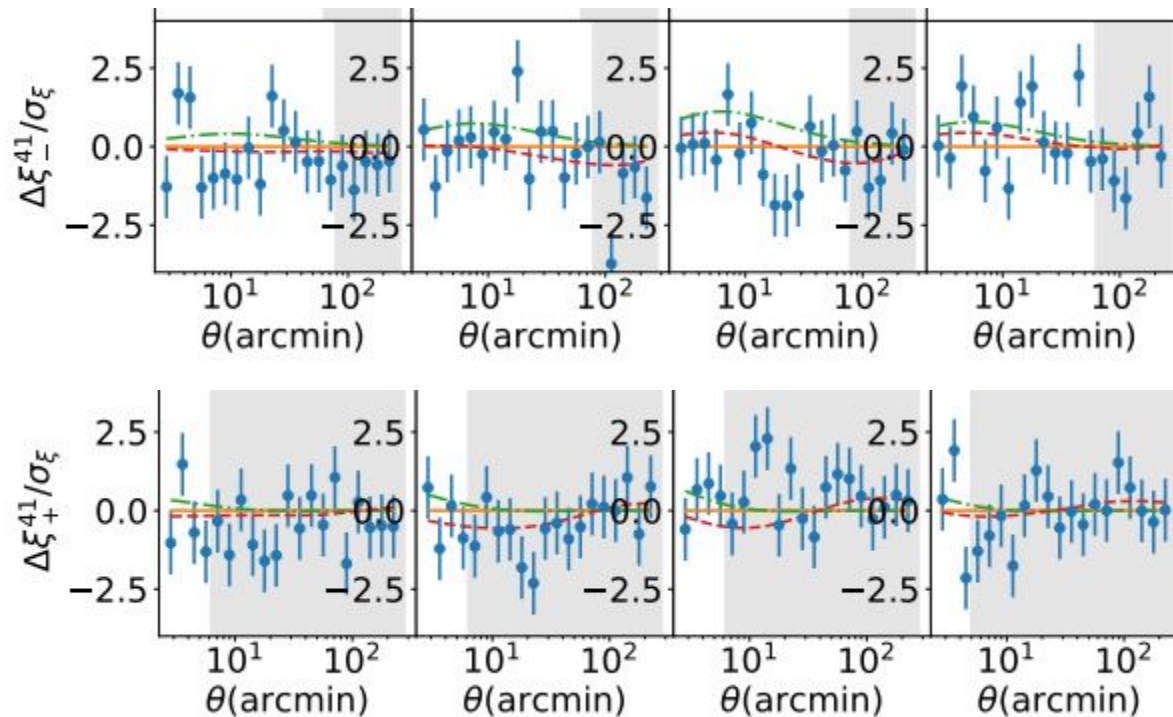


# Exploiting current and future LSS data is a very hard problem.



# Cosmology from weak gravitational lensing

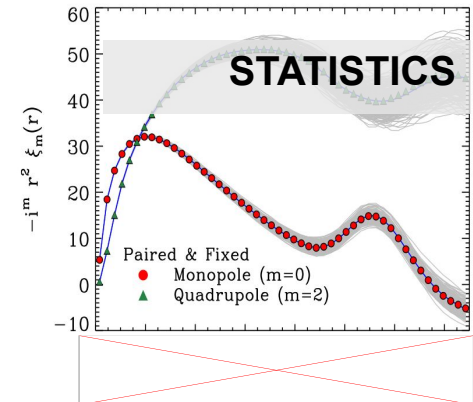
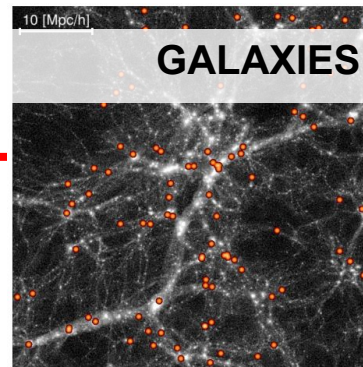
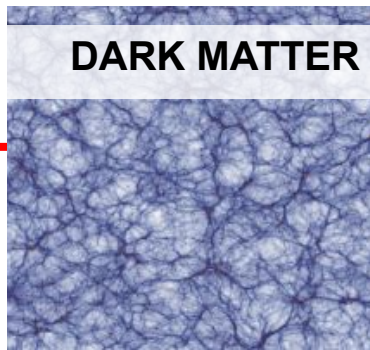
Current analyses are restricted by nonlinearities and gas physics



- Non linear matter power spectrum
- Galaxy Bias
- Baryonic effects
- Intrinsic Alignments

Chen+ 2022

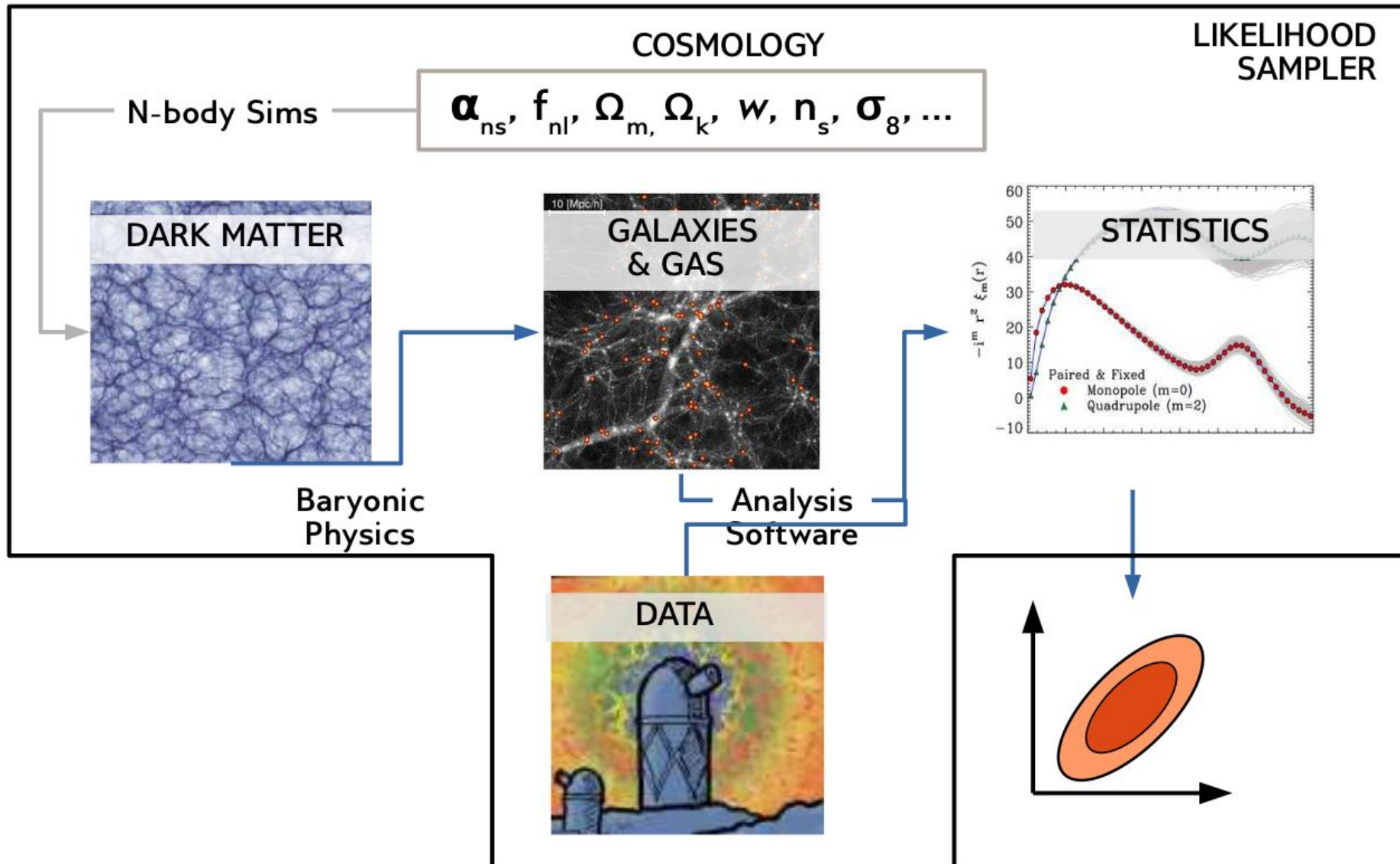




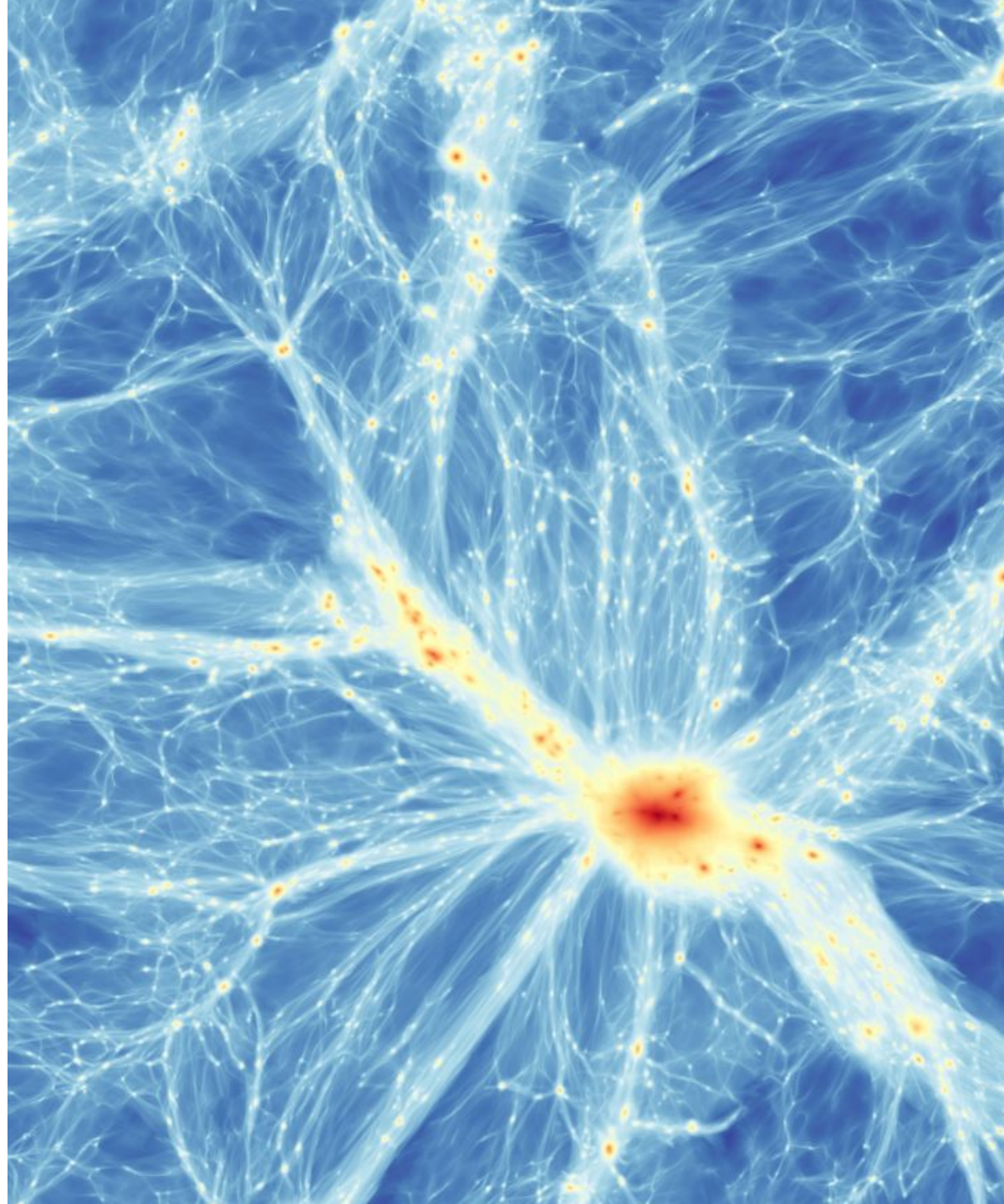
**How do we unlock the full power of late-universe measurements?**

# Simulations as LSS theory

Employing precise and physical structure formation models



# GRAVITY AND DARK MATTER FIELD





# The Vlasov-Poisson (aka collisionless Boltzmann)

Simplest case: DM is initially smooth, cold, classical, and collisionless

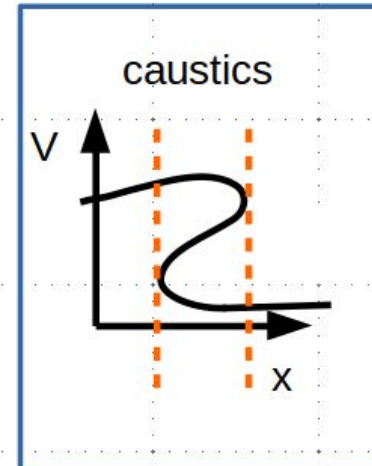
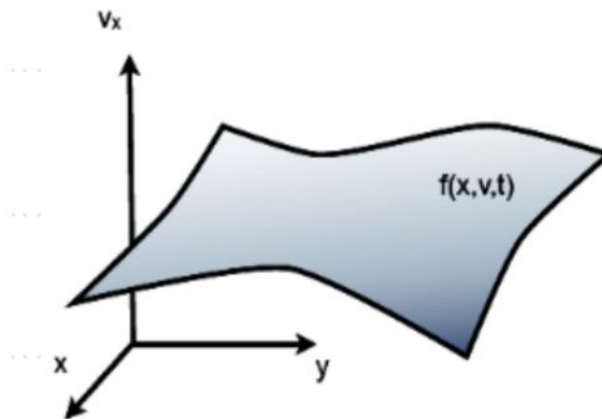
## The Vlasov-Poisson Equation

$$0 = \frac{df}{dt} = \frac{\partial f}{\partial t} + \frac{\mathbf{v}}{a^2} \cdot \frac{\partial f}{\partial \mathbf{v}} - \frac{\partial f}{\partial \mathbf{x}} \frac{\partial \Phi}{\partial \mathbf{x}}$$

$$\nabla^2 \Phi = \frac{4\pi G}{a} \int f d^3 v.$$

## CDM Sheet Properties

- phase-space is conserved along characteristics
- It can never tear
- It can never intersect



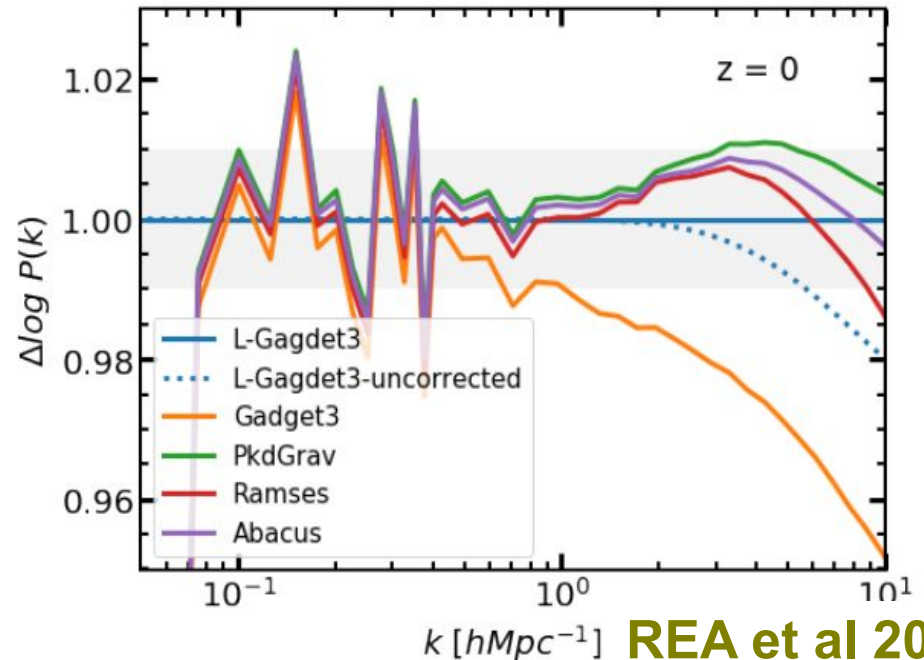
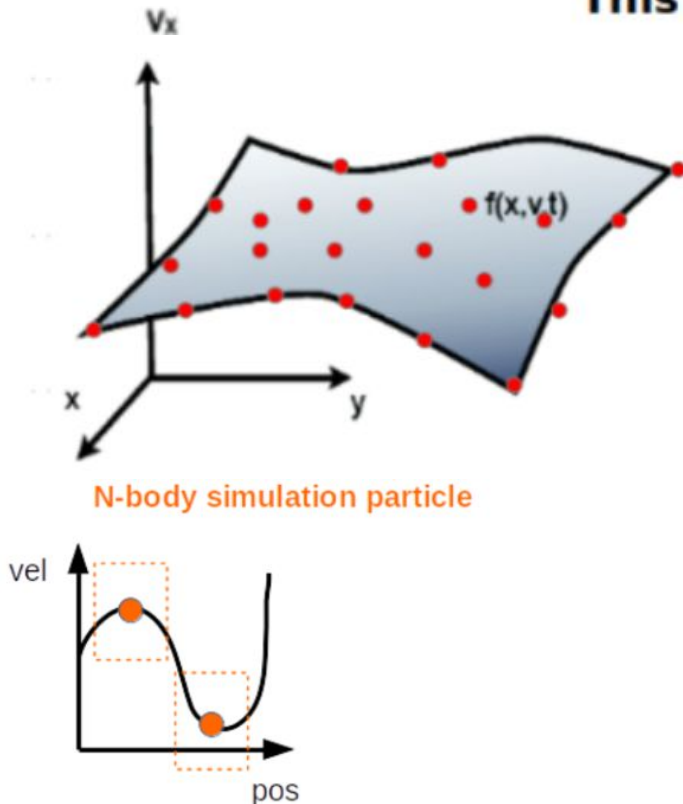
# Solving Vlasov-Poisson via MC sampling

Currently, the most accurate solution is discretizing the distribution function

$$\dot{\mathbf{x}}_c = \frac{\mathbf{v}_c}{a^2}$$
$$\dot{\mathbf{v}}_c = -\nabla_{\mathbf{x}}\phi|_{\mathbf{x}_c}$$

The solution yields the equation of motions of the Hamiltonian of classical mechanics

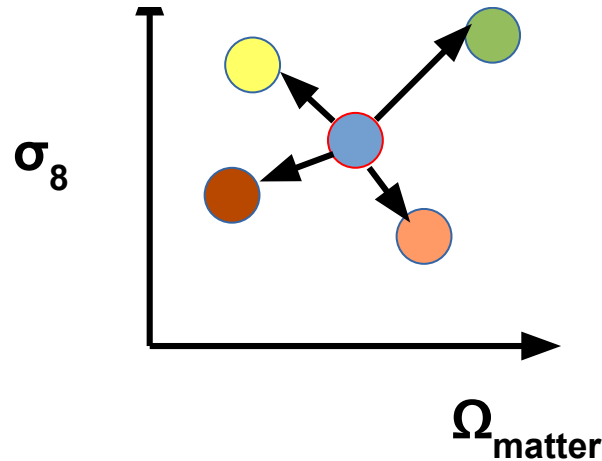
This is the correct solution as N goes to infinity



# How to sample the cosmo-parameter space?

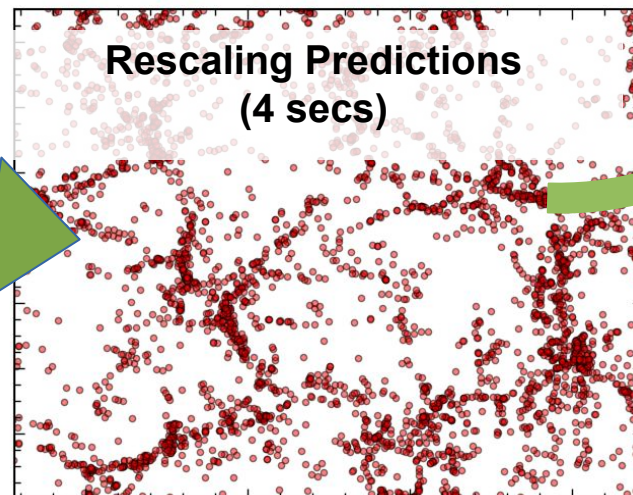
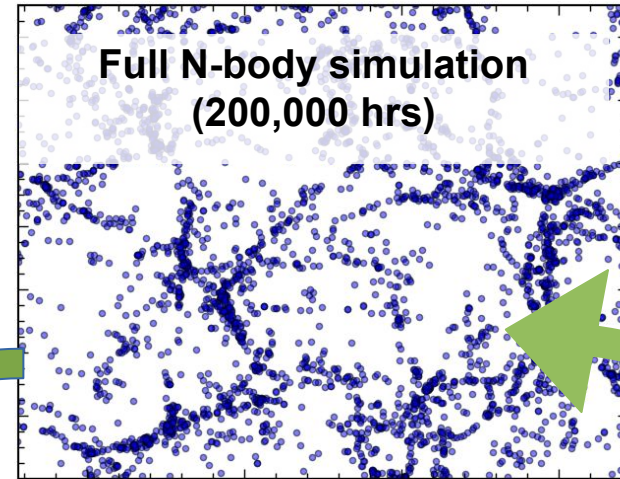
Rescaling modifies the outputs of simulation to mimic other cosmologies

Angulo & White (2010)  
Angulo & Hilbert (2015)  
Ruiz et al (2011)  
Renneby, Hilbert, Angulo (2018)



20 kpc error  
in the position  
of objects

200 Mpc



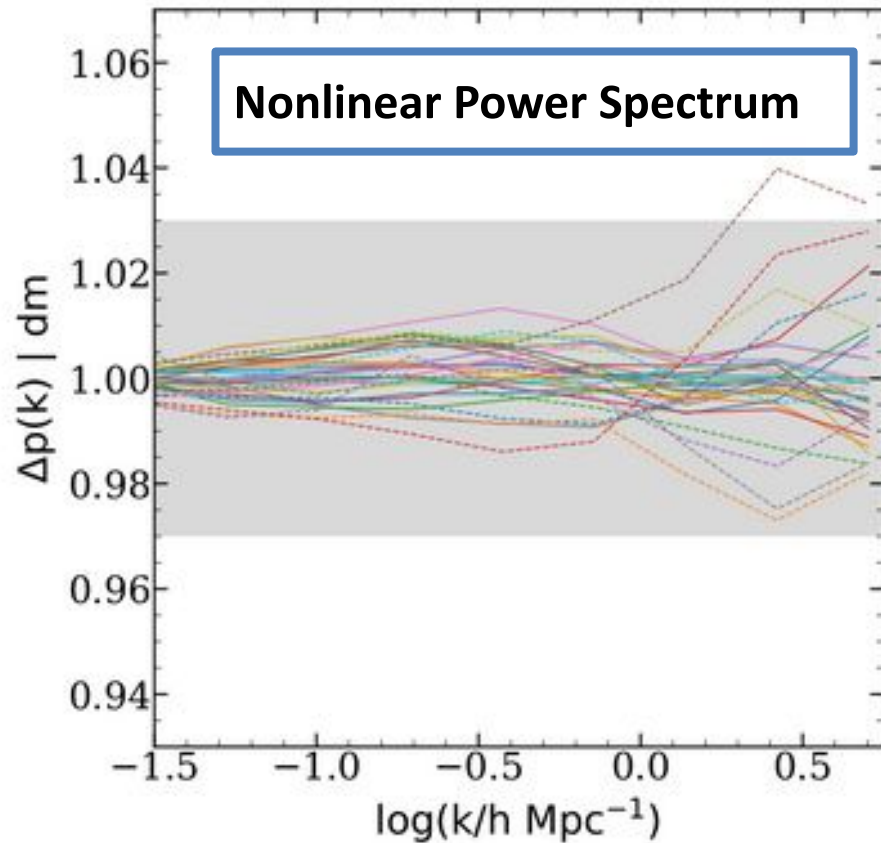
8 orders of  
Magnitude  
faster

Validated for:

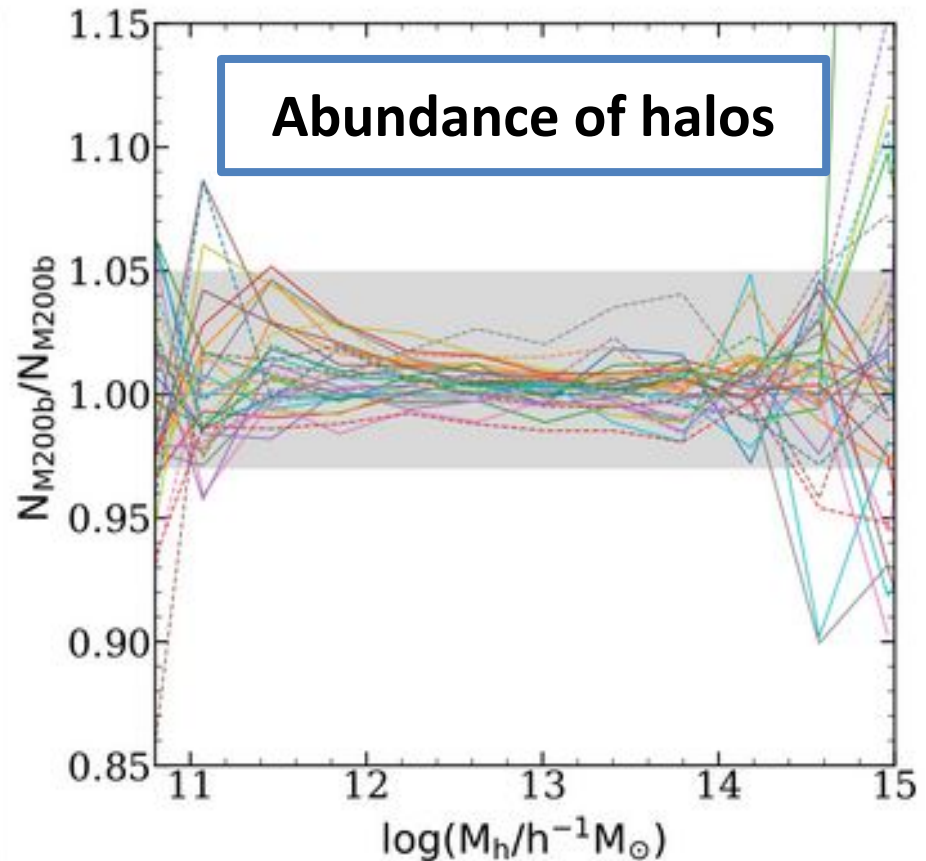
- real/redshift-space
- correlation function/power spectra
- 3-point correlation functions
- (sub)halo mass function
- abundance of voids
- different redshifts/cosmologies



# Accuracy in predicting the nonlinear distribution of matter and collapsed objects



Contreras, Angulo, et al (2020)



Ondaro, Angulo, et al (2021)

Region of  $\sim 10$ -sigma around Planck's best fit values, including massive neutrinos and dynamical dark energy

# Bacco simulations: The challenge of predicting the nonlinear mass field at the 1%

---



<http://goo.gl/RCSDwp>

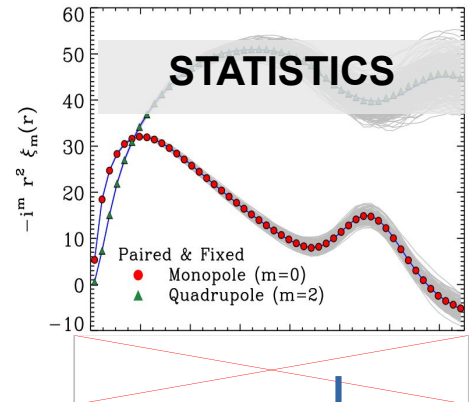
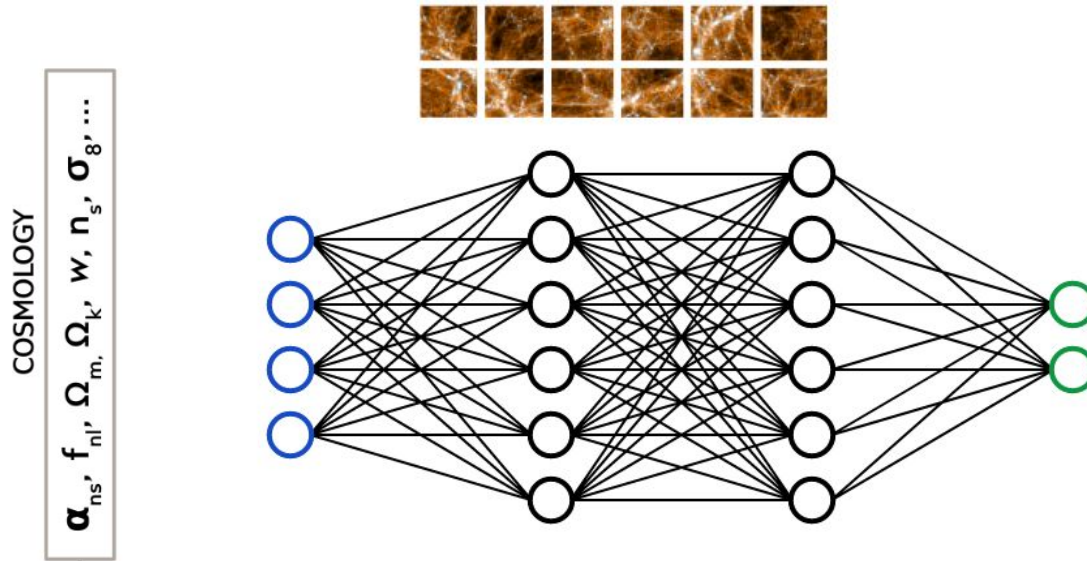
- New SubFind
- Merger Trees (100 outputs)
- 1% agreement with other codes up to  $k \sim 10 \text{ h/Mpc}$
- Phase-space tessellations
- Orphan tracking

---

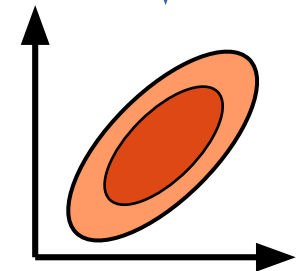
6 simulations: 2000 Mpc with  $4320^3$  particles;  
Paired-Fixed 2LPT ICs; 100 outputs; halos  $\sim 10^{10} \text{ Msun/h}$

# Constraining Cosmology and Astrophysics

Feed-forward neural networks trained on 10,000 combinations of cosmology and astrophysics

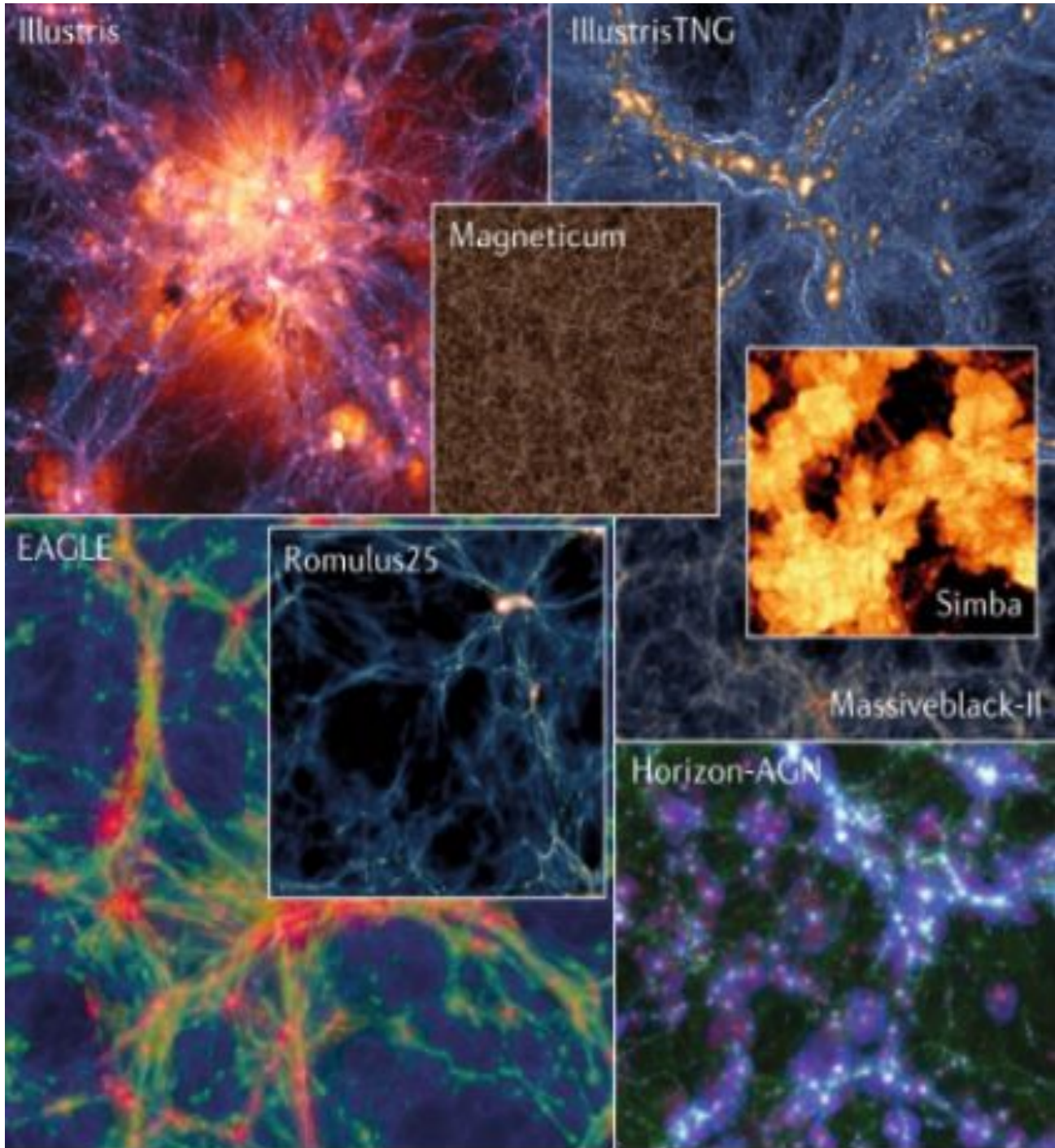


- (Non) linear matter power spectrum
- Baryonic effects
- Galaxy correlation functions
- Halo Mass function
- Perturbative bias in real & redshift space
- Linear theory

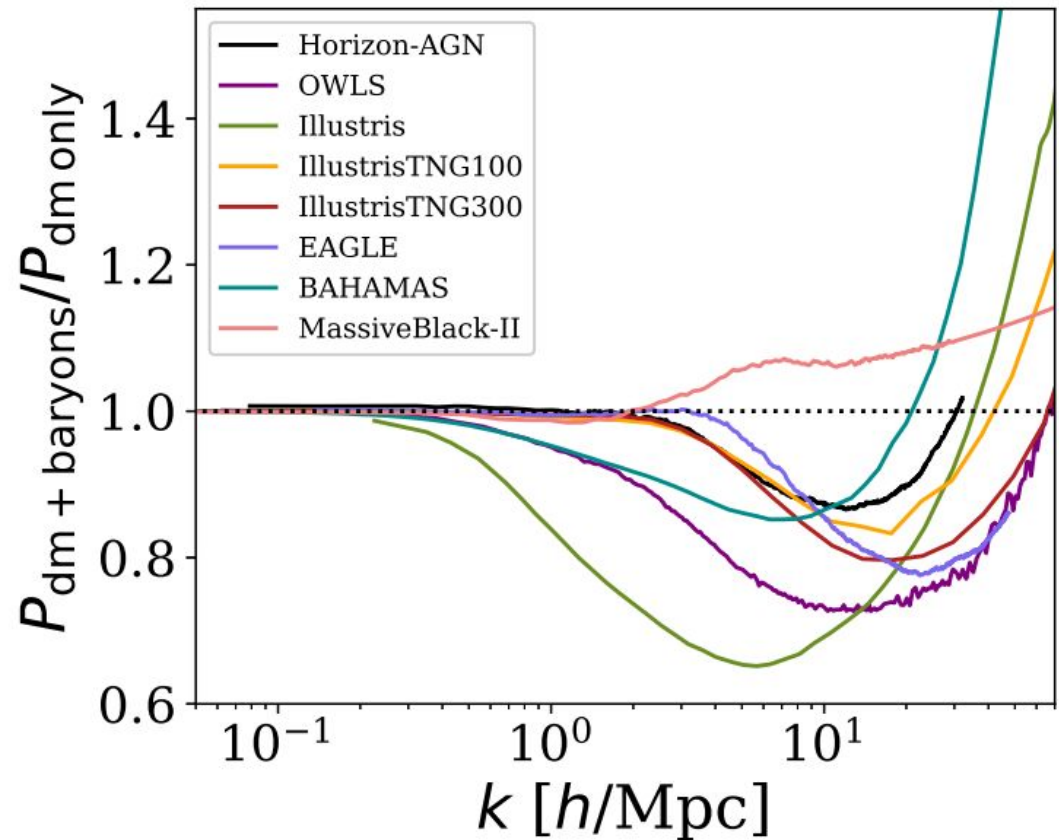
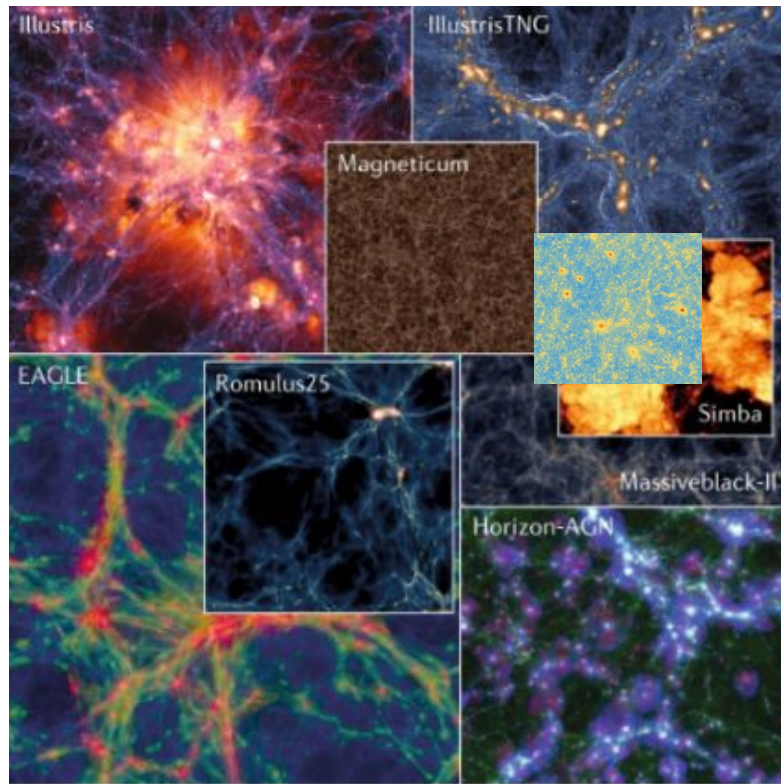




# Gas and hydro forces



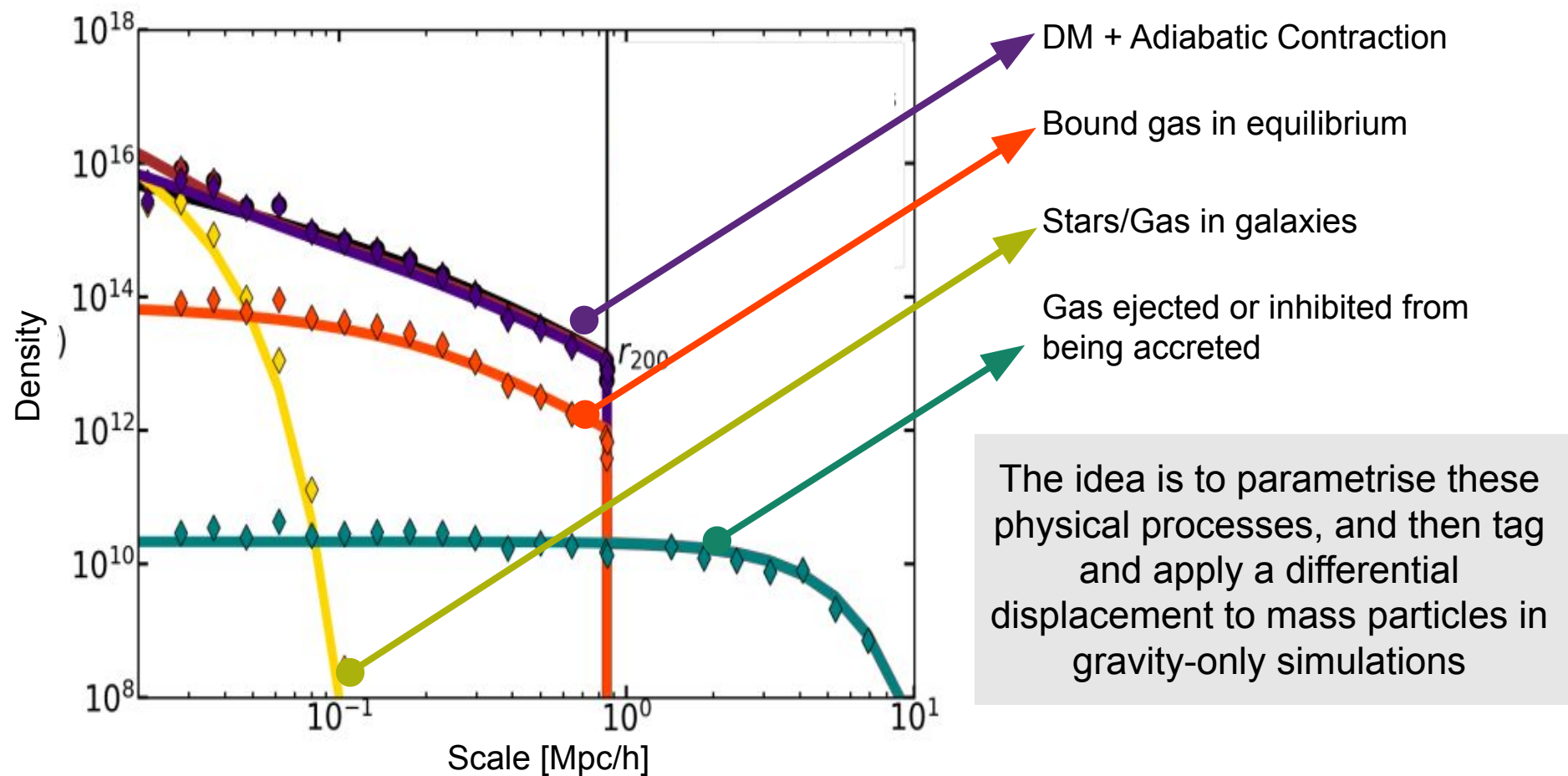
# Hydrodynamical forces and galaxy formation is important to predict the large-scale structure of a given cosmology



Chisari et al (2019)

# Modelling the baryonic effects on the matter clustering

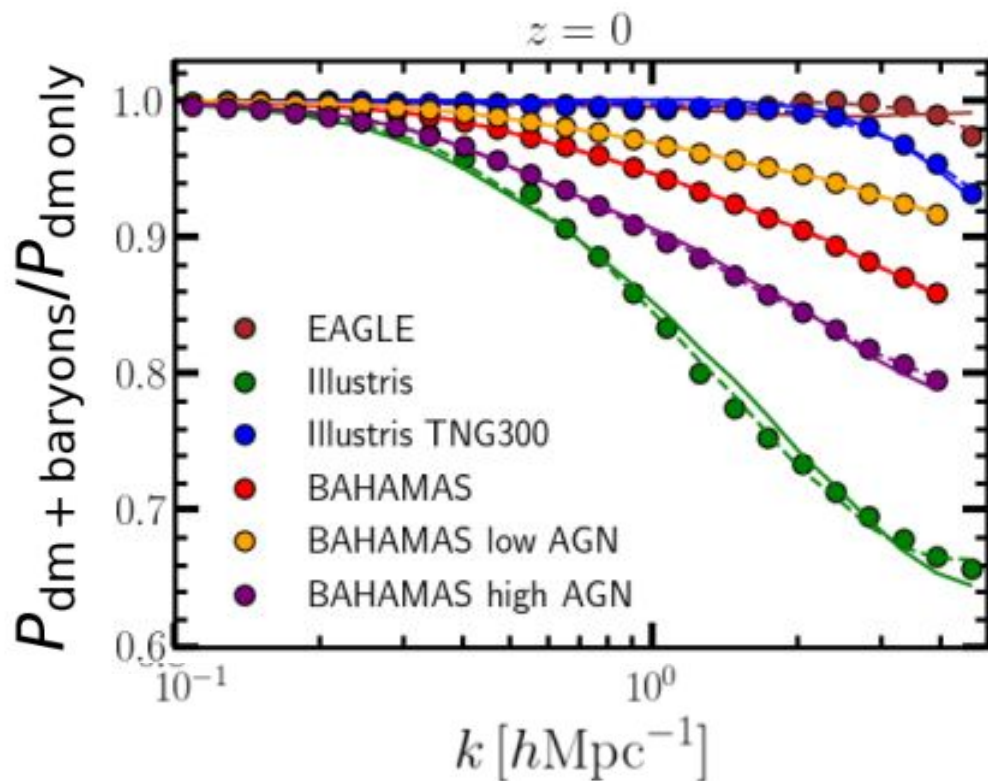
Arico, REA+ (2020,2021); Schneider+(2017, 2019)





# Modelling the baryonic effects on the matter clustering

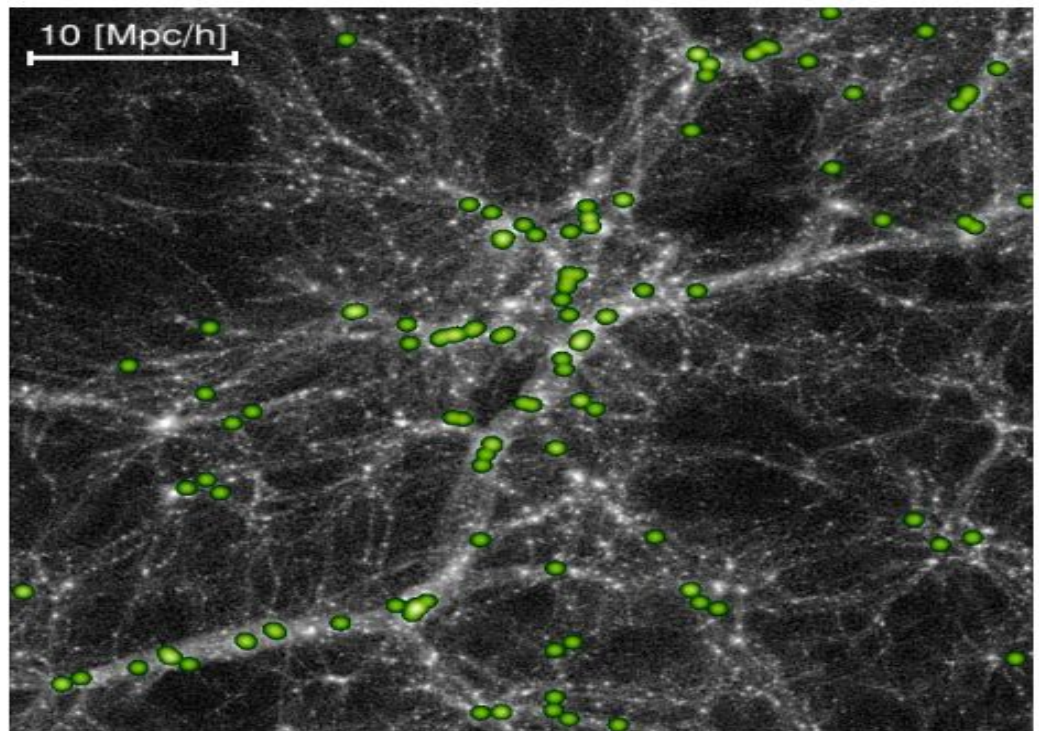
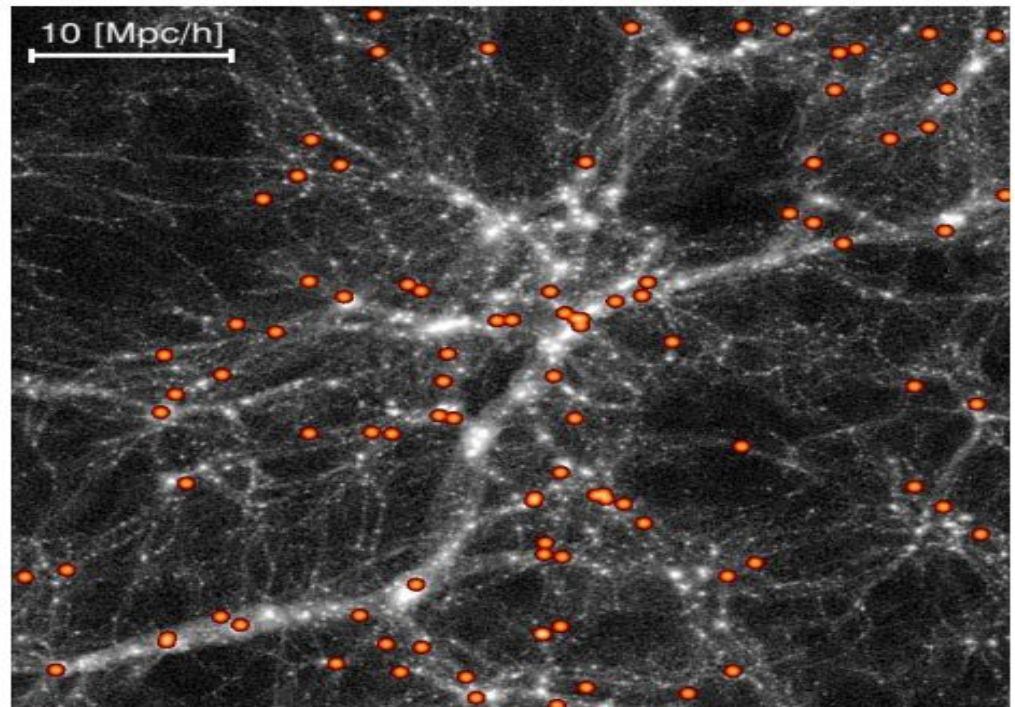
The impact of baryons can be reproduced to  $\sim 1\%$  accuracy on 7 different state-of-the-art hydrodynamical simulations



1. Fast & flexible 3D predictions
2. It can be calibrated with observations
3. It does not depend on any specific simulation
4. Also validated for WL peaks and bispectrum and at high redshift

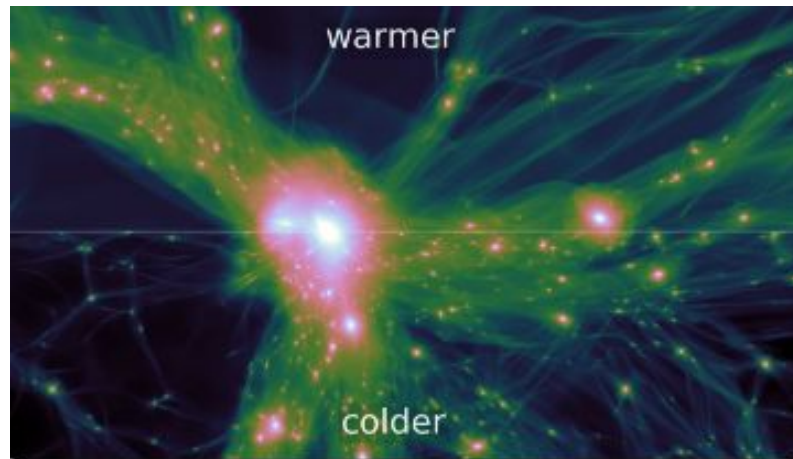
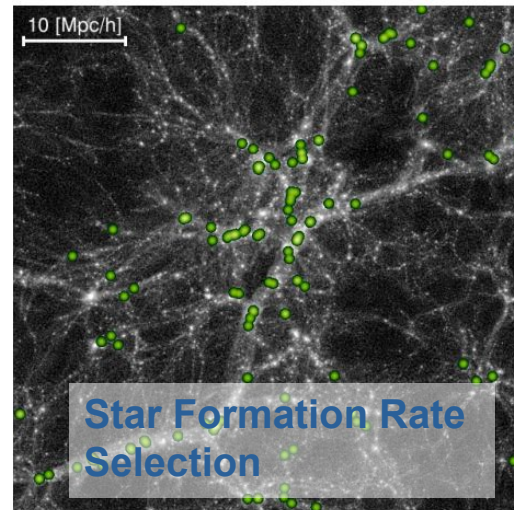
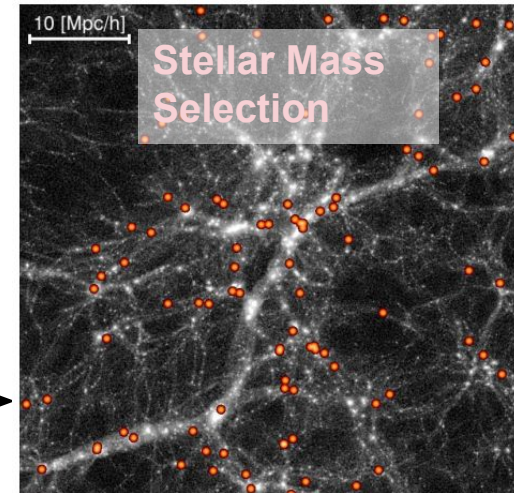
Arico, Angulo, et al (2019, 2020, 2021);

# GALAXIES



# How to efficiently model galaxies in DM sims?

- Halo Occupation Distribution Models
- **(Extended) Subhalo Abundance Matching**
- Empirical Modelling
- Semi-Analytic Galaxy Formation

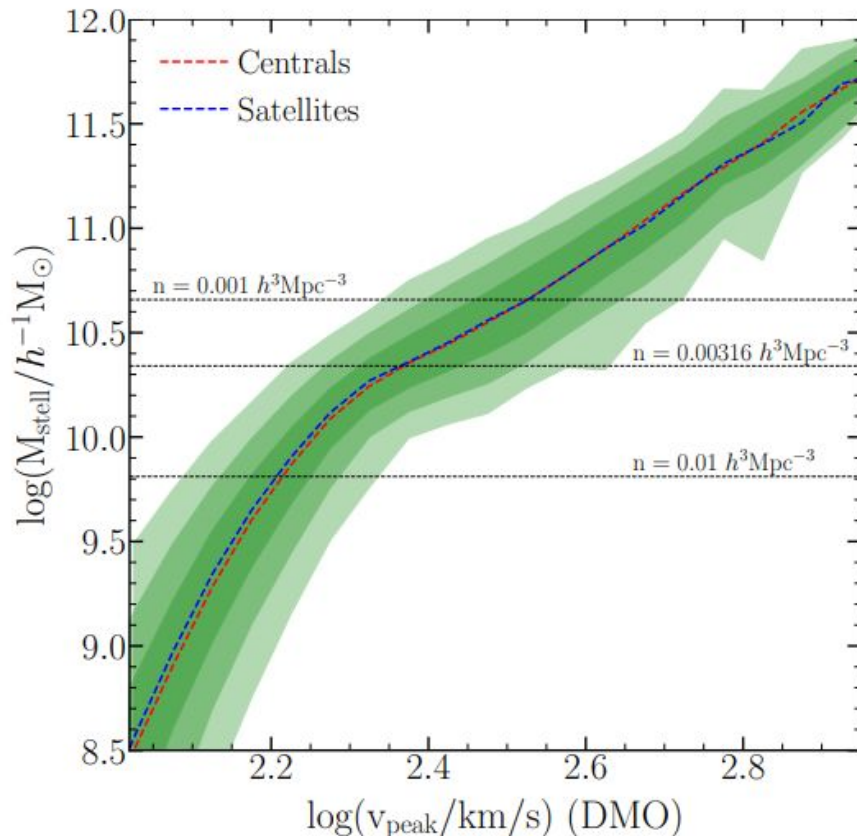


Contreras, REA, Zennaro (2020)  
Contreras, REA, et al (2021)  
Contreras, REA, MTNG (2022)



# SHAMe: Subhalo Abundance Matching Extended

Goal: Flexible and efficient model to fit all available sims



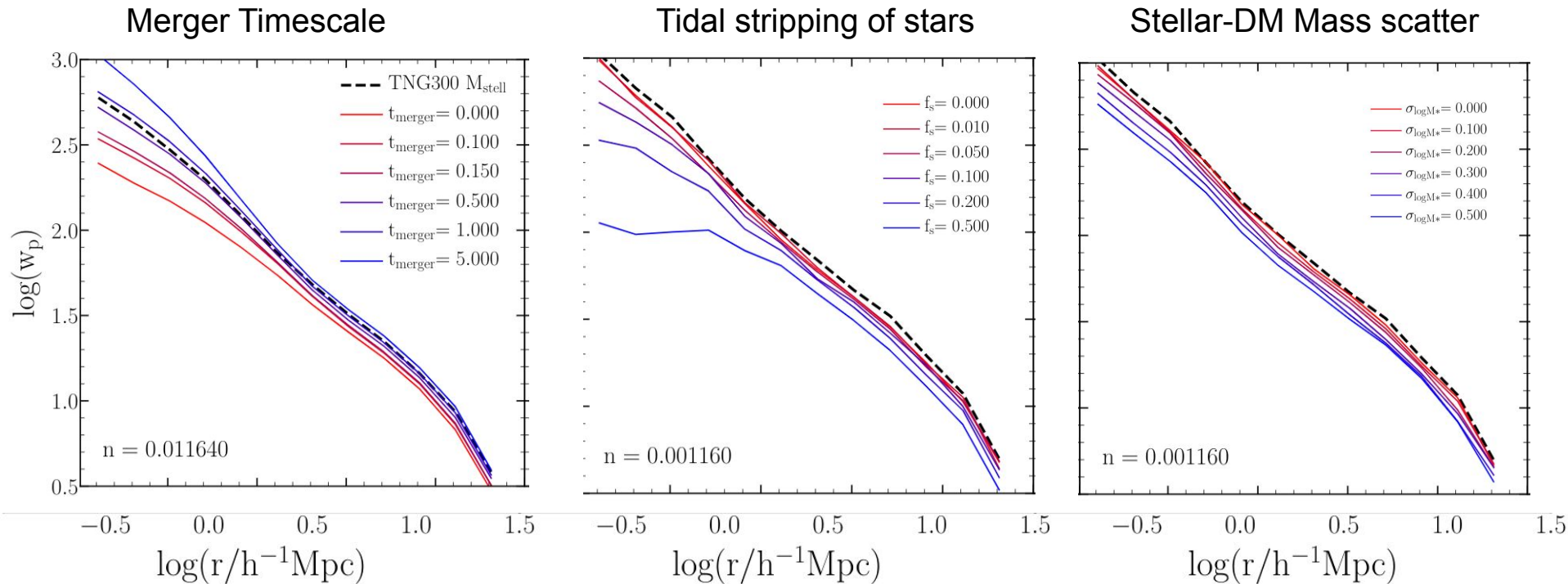
## Subhalo Abundance Matching

1. Describes the Mhalo-Mstar and clustering of galaxies in observational and simulated data
2. Fails in redshift space
3. Incorrect environmental dependence
4. Incorrect stripping and disruption

## extended Subhalo Abundance Matching (alla Emerge/UniverseMachine)

1. Model for the stripping of stars
2. Predictions for Star Formation Rates
3. Model for dynamical friction (orphan tracking)
4. Flexible degree of assembly bias

# The impact of astrophysics in the spatial distribution of galaxies



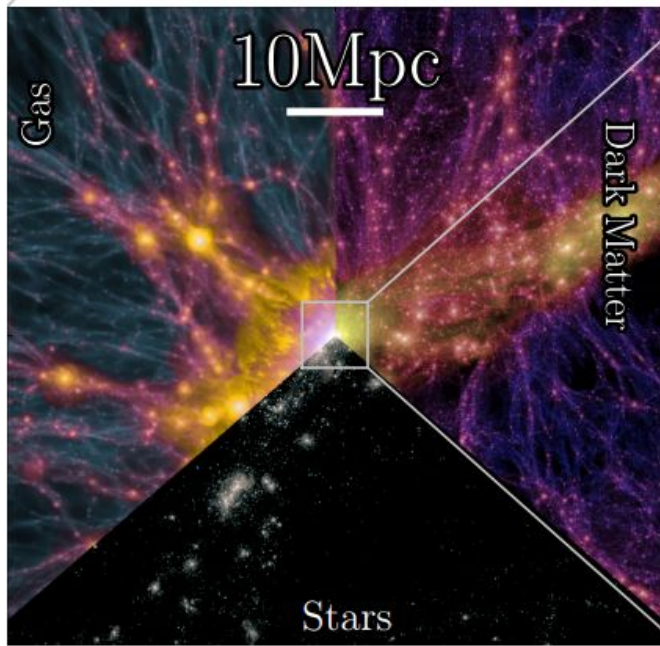
## Validated for:

- redshift space multipoles
- 3-point correlation functions
- Amount of assembly bias
- k-Nearest neighbours
- Stellar Mass and SFR galaxy selections

**Contreras, Angulo, et al (2021)**

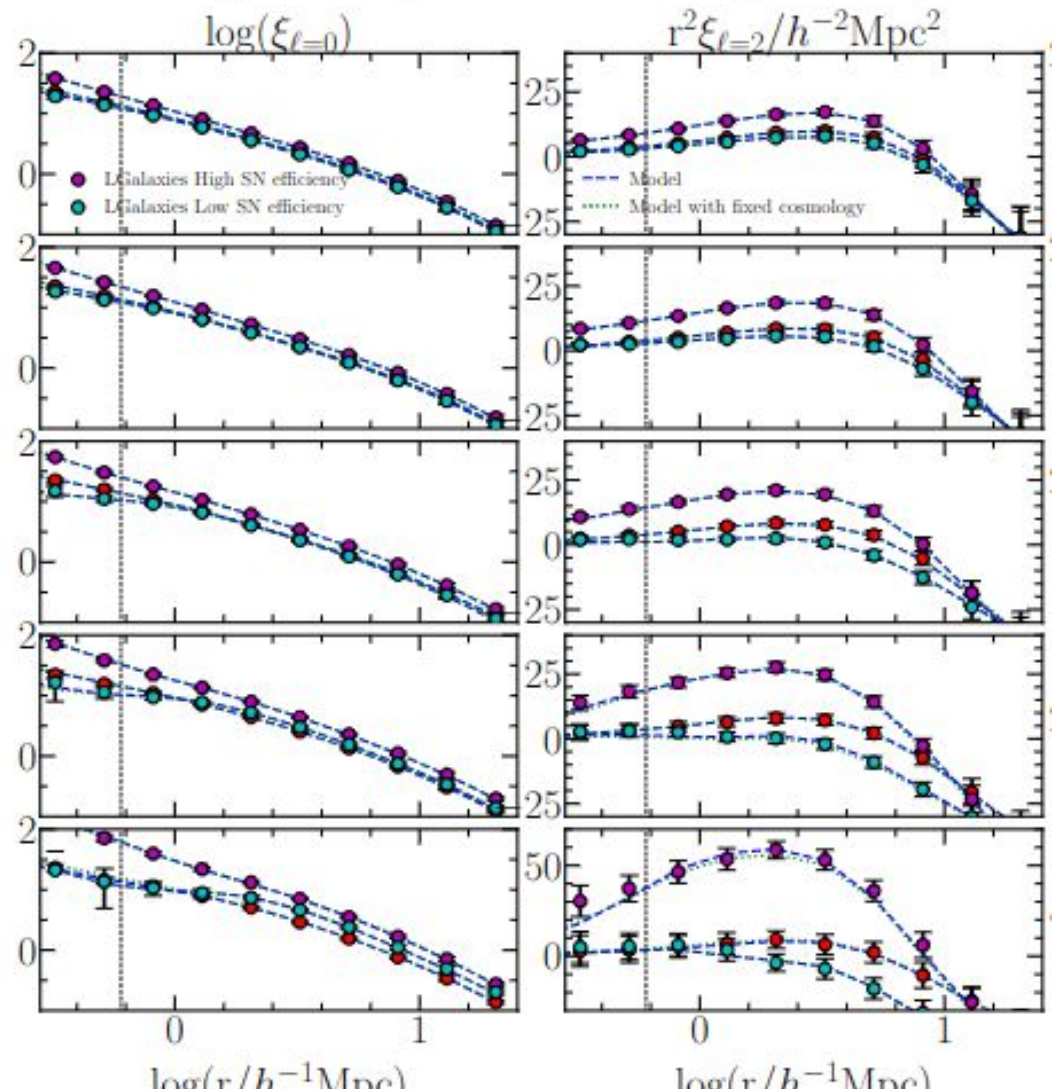
# SHAMe meets Millennium-TNG hydro simulation

SHAMe is able to describe the redshift-space clustering of MTNG galaxies



$L = 740 \text{ Mpc}$   
(similar volume to SDSS main)  
Same resolution as TNG300  
4 additional SAM catalogues  
4 number densities

Contreras, REA+ (2022)





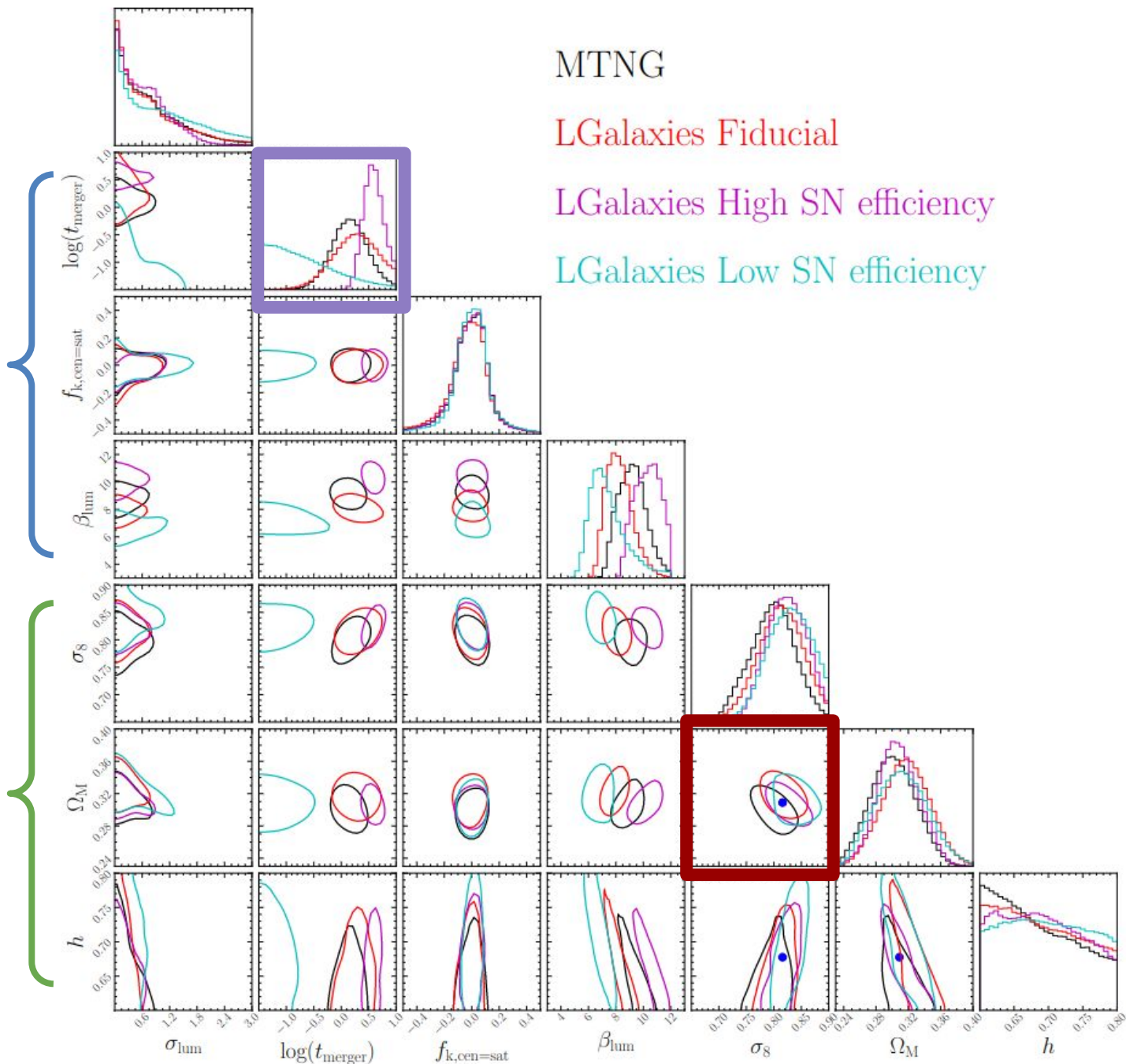
MTNG

LGalaxies Fiducial

LGalaxies High SN efficiency

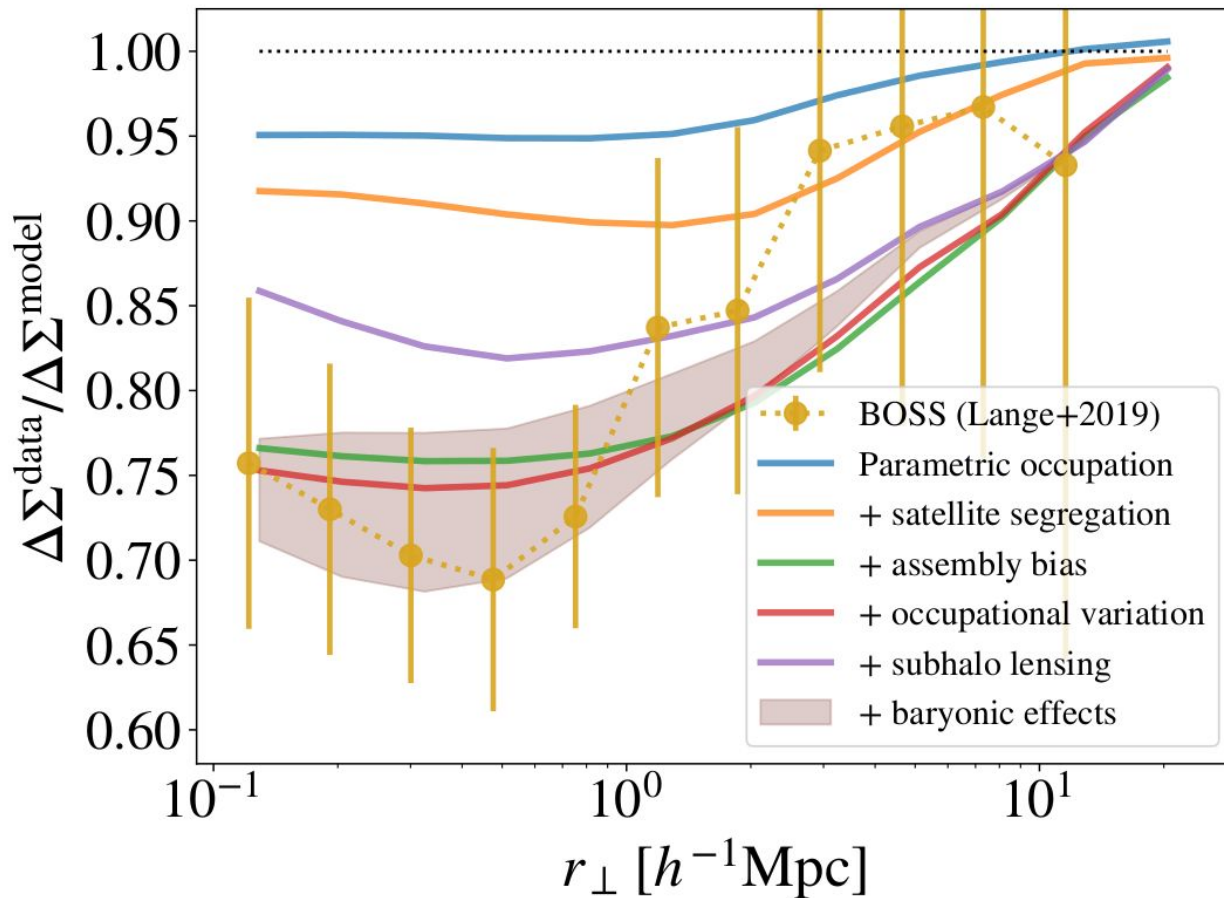
LGalaxies Low SN efficiency

Astrophysical  
Parameters



# “Lensing is low” tension

HOD modelling lead to artificial tensions in clustering and gg-lensing



# BACCO's Hybrid bias expansion

A rigorous model that is agnostic to selection effects and gas-physics

---

The galaxy overdensity field, can be written as a function of matter (and velocity) statistics

$$\delta_g(\mathbf{x}, \tau) = \mathcal{F}[\Phi, \Phi_v],$$

Which can then be written perturbatively up to a given order. Specifically, in Lagrangian coordinates:

$$1 + \delta_g(\mathbf{q}) = 1 + b_1^L \delta(\mathbf{q}) + b_2^L \delta^2(\mathbf{q}) + b_{s^2}^L s^2(\mathbf{q}) + b_{\nabla^2 \delta}^L \nabla_{\mathbf{q}}^2 \delta(\mathbf{q}) + \dots,$$

$$1 + \delta_g(\mathbf{x}) = \int d^3 \mathbf{q} \delta^D(\mathbf{x} - \mathbf{q} - \boldsymbol{\psi}(\mathbf{q})) (1 + \delta_g(\mathbf{q}))$$

Additionally, the displacement field can be computed perturbatively

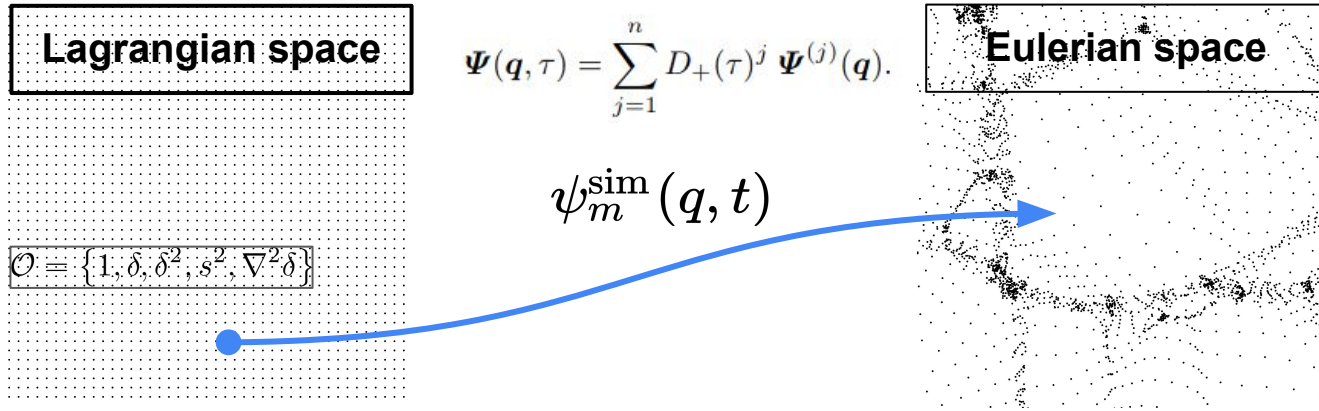
$$\boldsymbol{\Psi}(\mathbf{q}, \tau) = \sum_{j=1}^n D_+(\tau)^j \boldsymbol{\Psi}^{(j)}(\mathbf{q}).$$

**However, perturbative approaches break at  $\sim 0.1$  h/Mpc – potentially neglecting 100x modes**

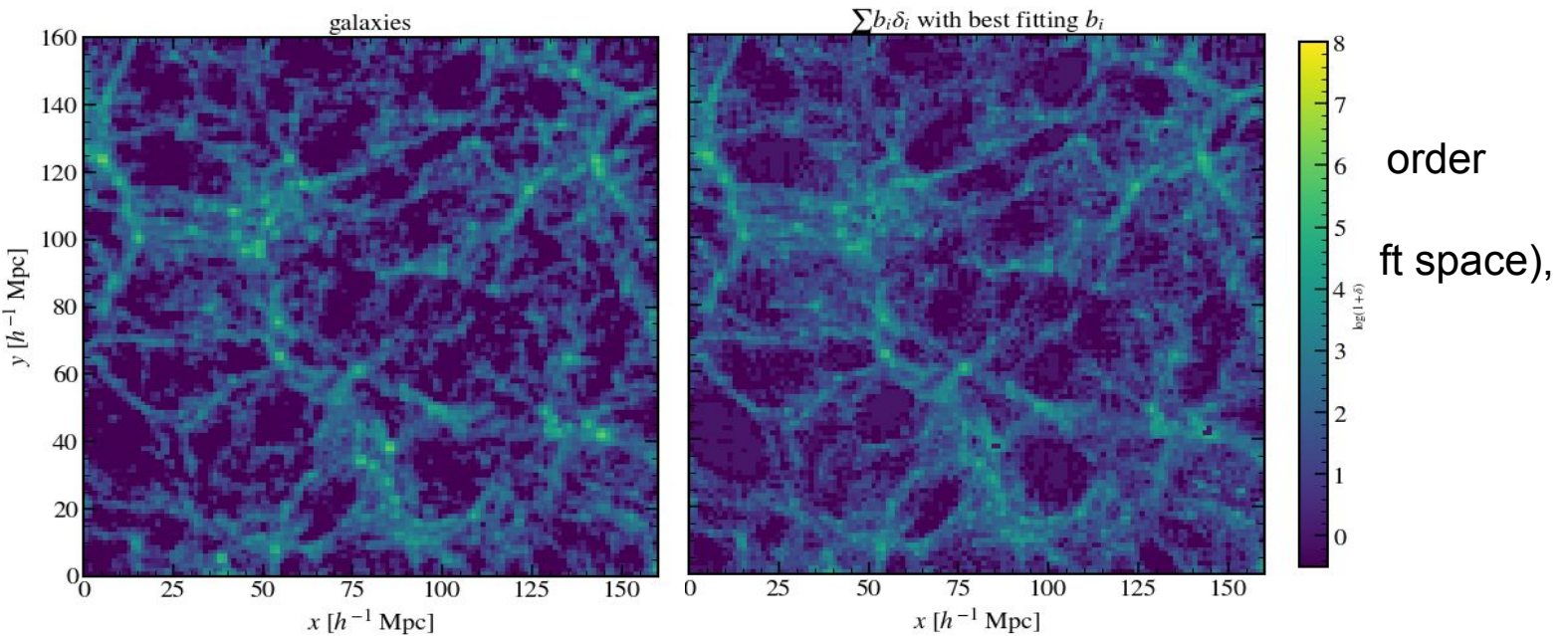


# Alternative approach: Hybrid bias expansion

Combining numerical and perturbative worlds (M. Pellejero & M. Zennaro)



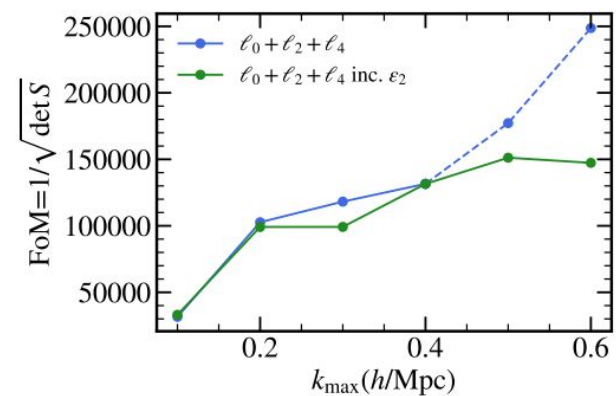
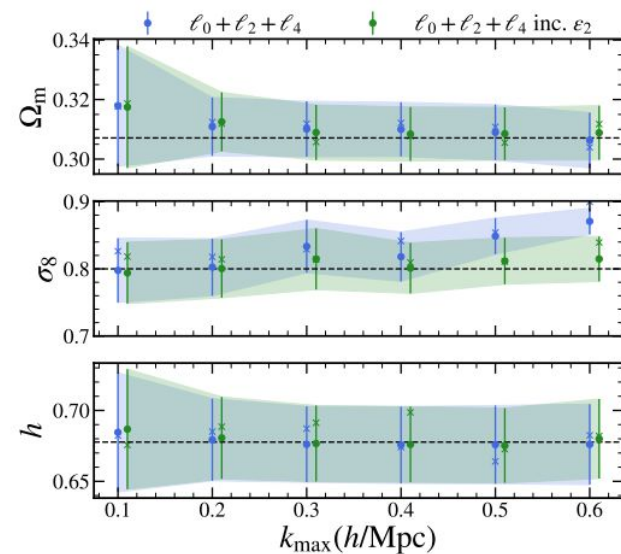
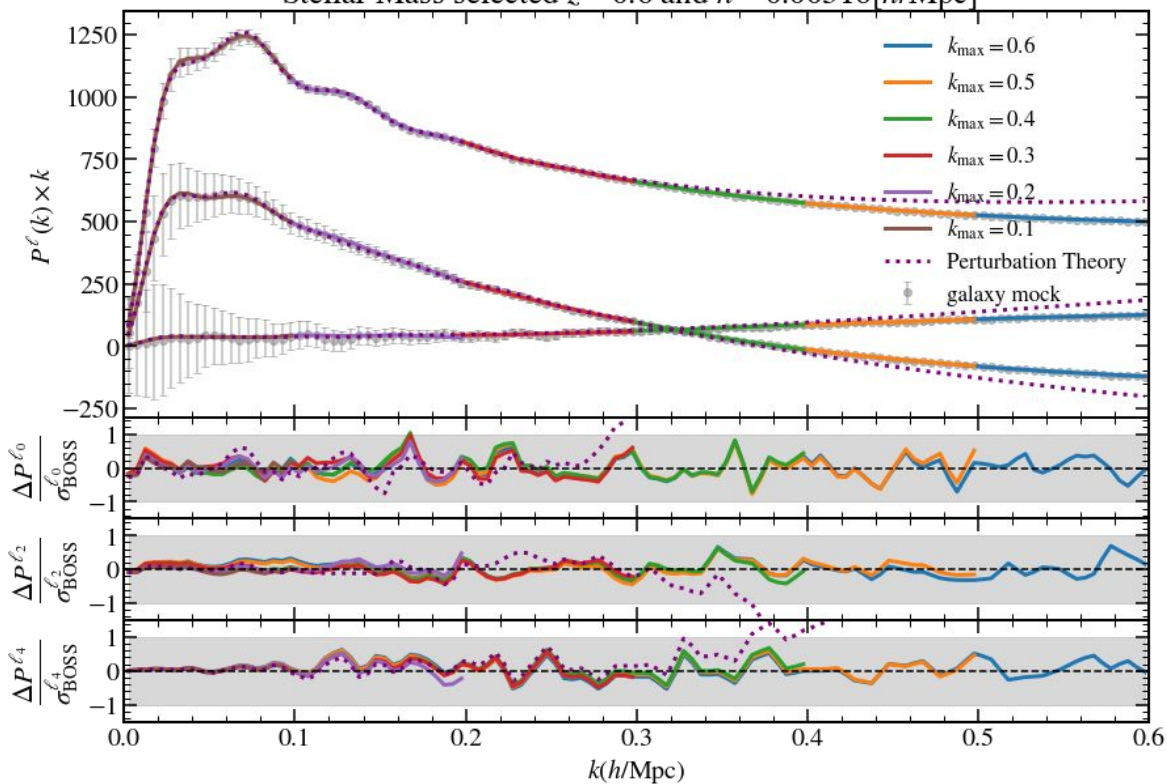
The uncertainty  
The transition  
can be p



# BACCO's Hybrid bias expansion in z-space

Fits to the 300 official BOSS mock catalogues

Stellar Mass selected  $z=0.6$  and  $\bar{n}=0.00316[h/\text{Mpc}]^3$



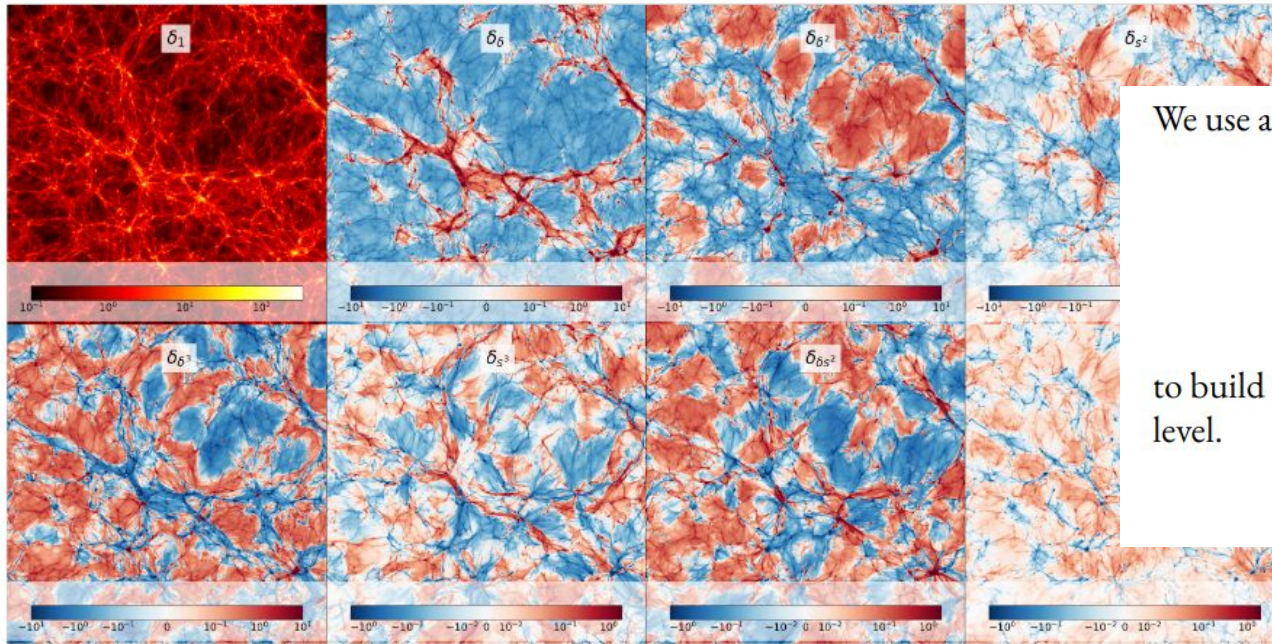
Zennaro, REA, + (2021,2022)

Pellejero-Ibañez, RA+ (2021,2022)



# Describing galaxies at the “field level”

Galaxy field is built by combining all 8 terms that appear at 3rd order



We use a third order bias model

$$\begin{cases} \text{1st Order} & \delta \\ \text{2nd Order} & \delta^2, s^2 \\ \text{3rd Order} & \delta^3, s^3, s^2\delta \\ \text{Non-Local} & \nabla^2\delta \end{cases}$$

to build a model for biased tracers at the field level.

$$\delta_{h,det} = \sum_i b_i \mathcal{O}_i$$

$$-2\ln\mathcal{P}(\delta_g|\delta_{g,det}) = \int_{|\mathbf{k}|<\Lambda} \frac{d^3\mathbf{k}}{(2\pi)^3} \left[ \frac{|\delta_g(\mathbf{k}) - \delta_{g,det}(\mathbf{k})|^2}{P_\epsilon(k)} + \ln(2\pi P_\epsilon(k)) \right].$$



Francisco Maion

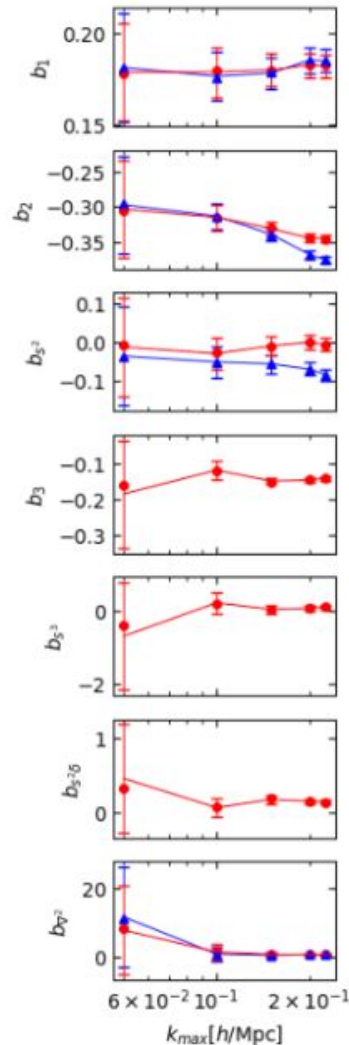


# Describing galaxies at the “field level”

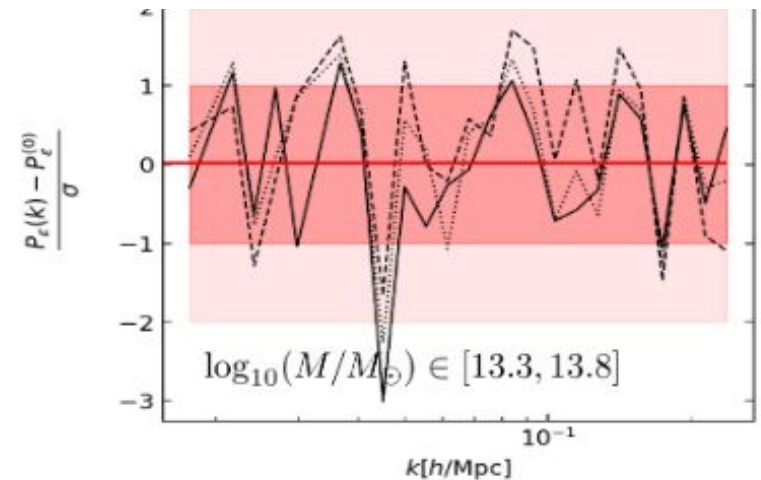
In the most extreme test – fixed phases and cosmology – every single pixel is compatible with stochastic noise up to  $k=0.25$  h/Mpc

Bias parameters measured from galaxy mock created using SHAMe method (Contreras et. al (2021))

2nd order bias  
3rd order bias



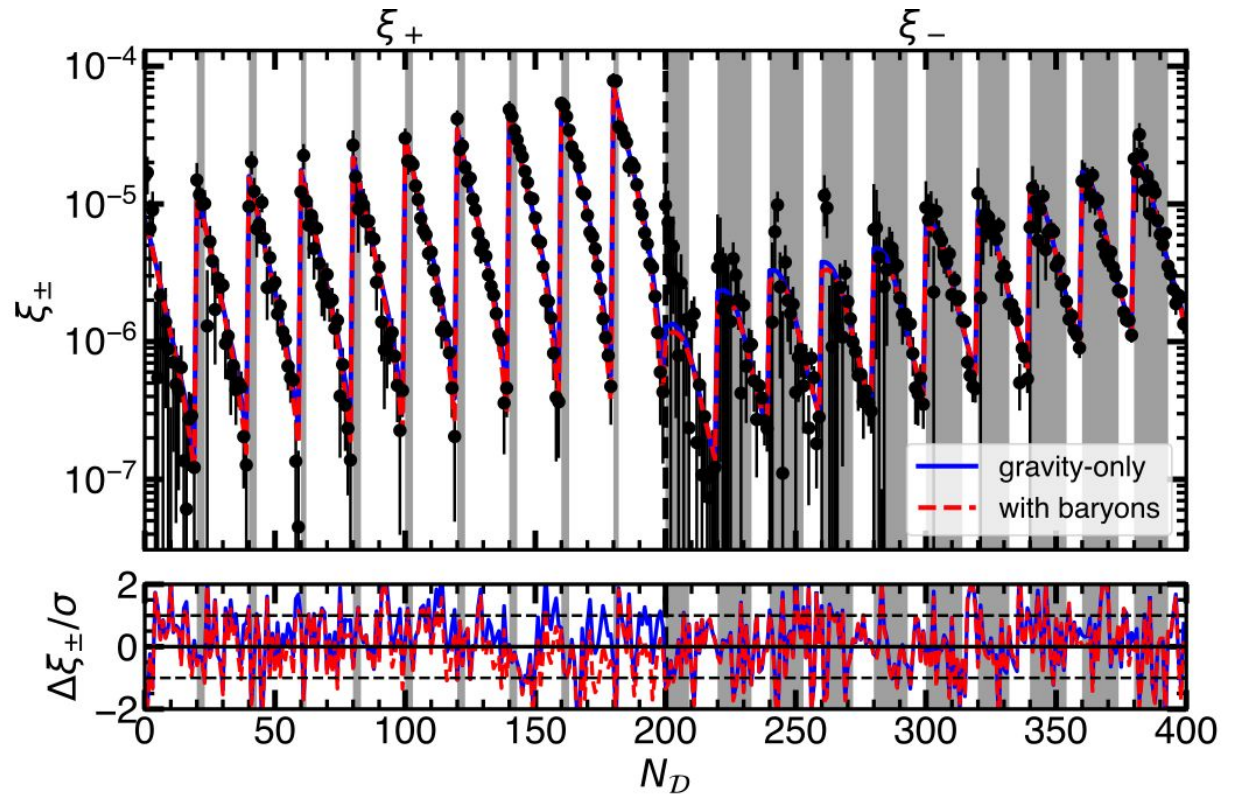
$$P_{\epsilon}(k) = |\delta_h - \delta_{h,det}|^2$$



1. Extension to redshift space
2. Quantification in constraining power
3. Combination with ML techniques

# Exploring the S8 tension

## Constraints on cosmology and baryons from small scales



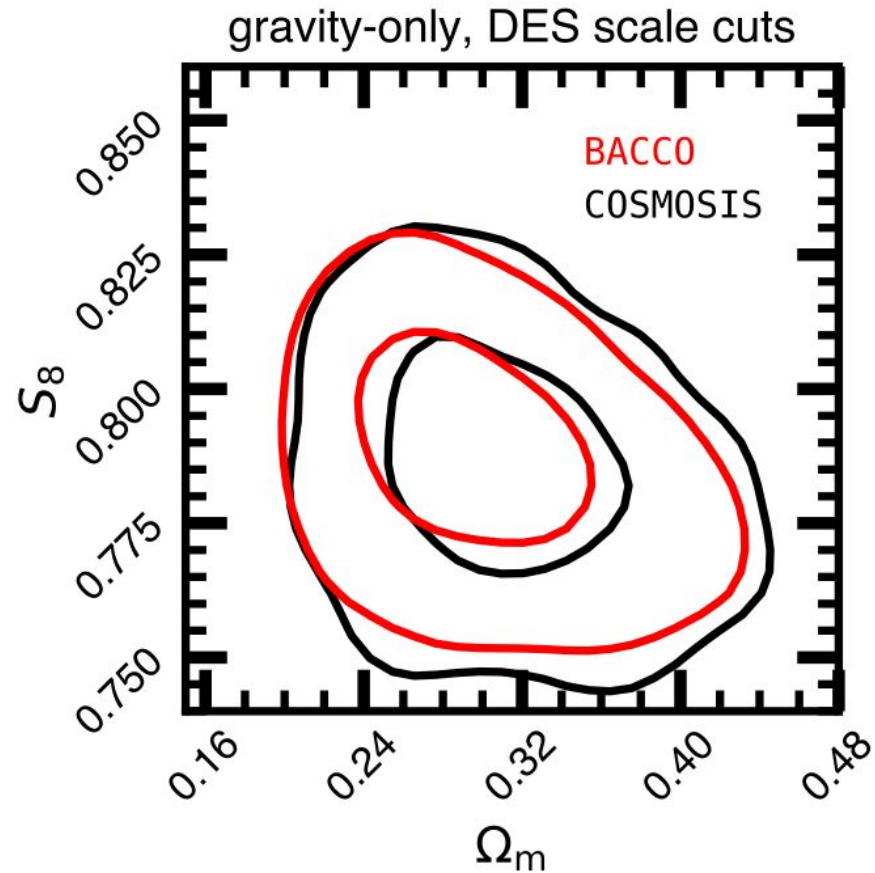
Arico, REA+ (2023)

DES Y3 Cosmic shear correlation functions  $\xi_{\pm}$ ,  
all angular scales  $\theta \in [2.5, 250]$  arcmins.

# Exploring the S8 tension

## Constraints on cosmology and baryons from small scales

- Independent pipeline written from scratch (0.4s in a laptop)
- More accurate Pnl – BACCOemu
- Explicit baryon model via baryonification
- All scales in shear
- No shear ratios
- NLA intrinsic alignment

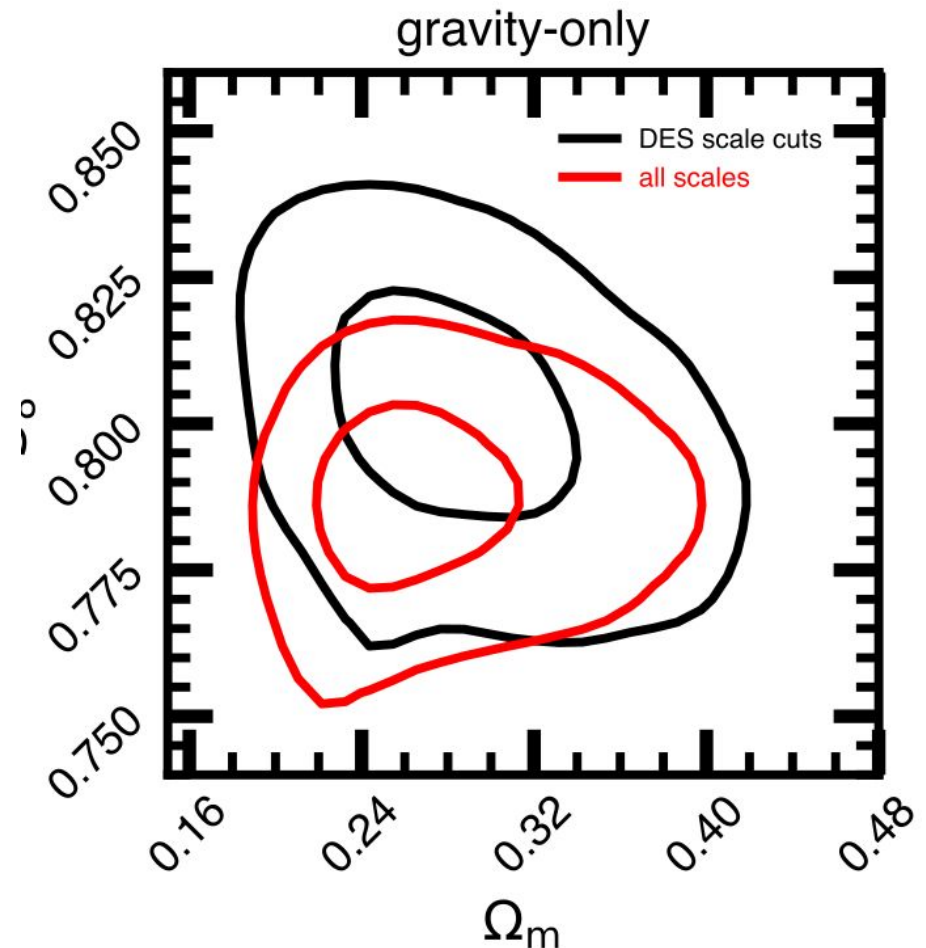




# Exploring the S8 tension

## Constraints on cosmology and baryons from small scales

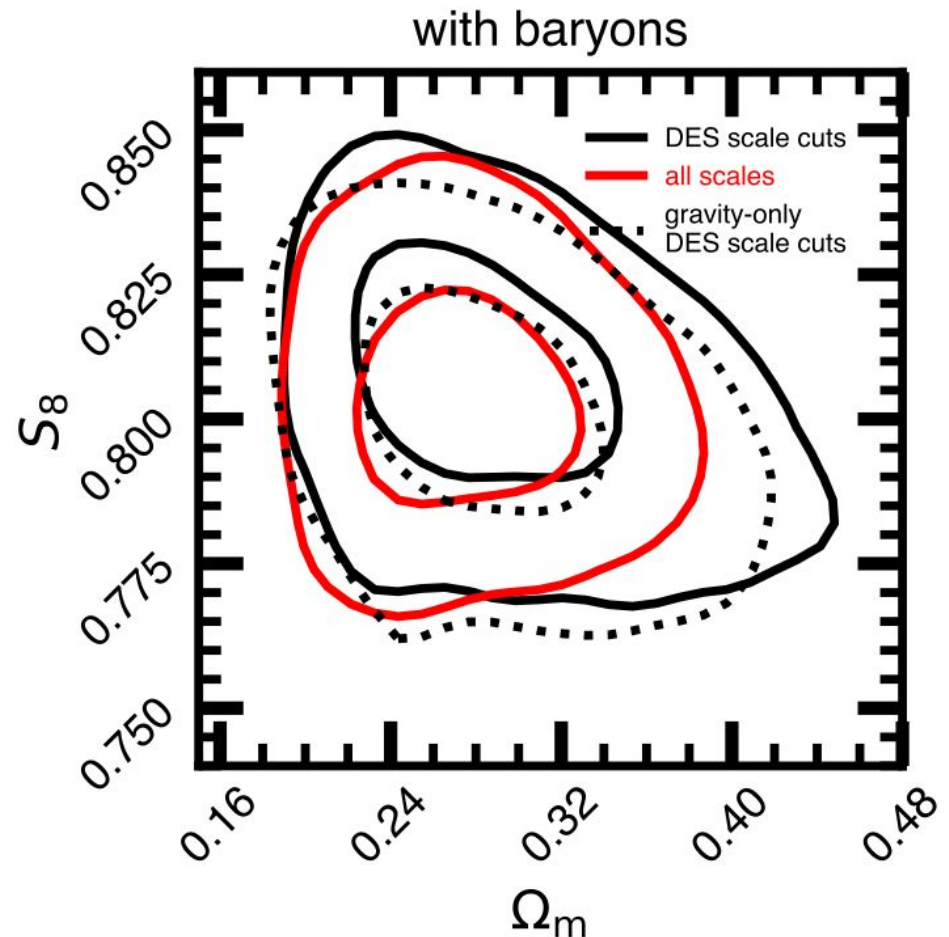
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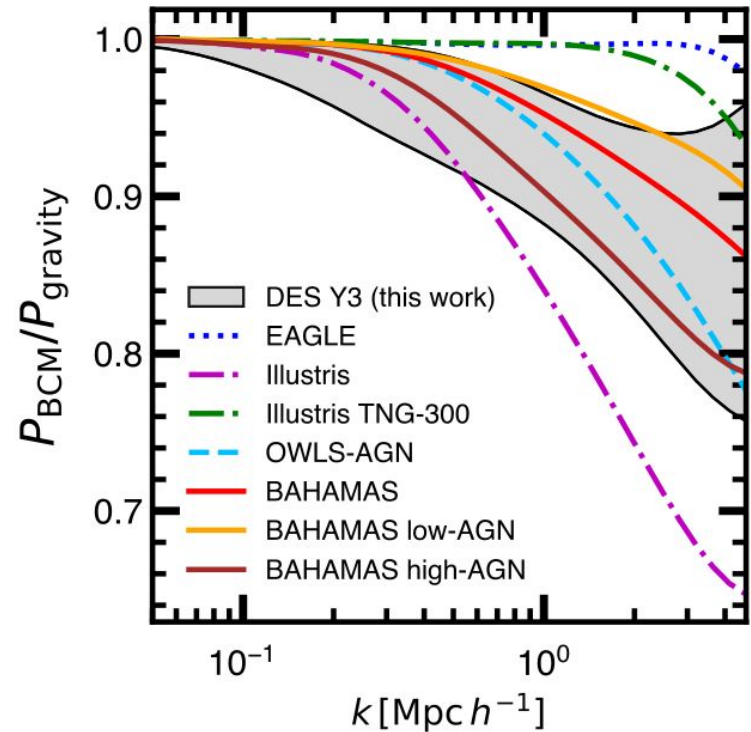
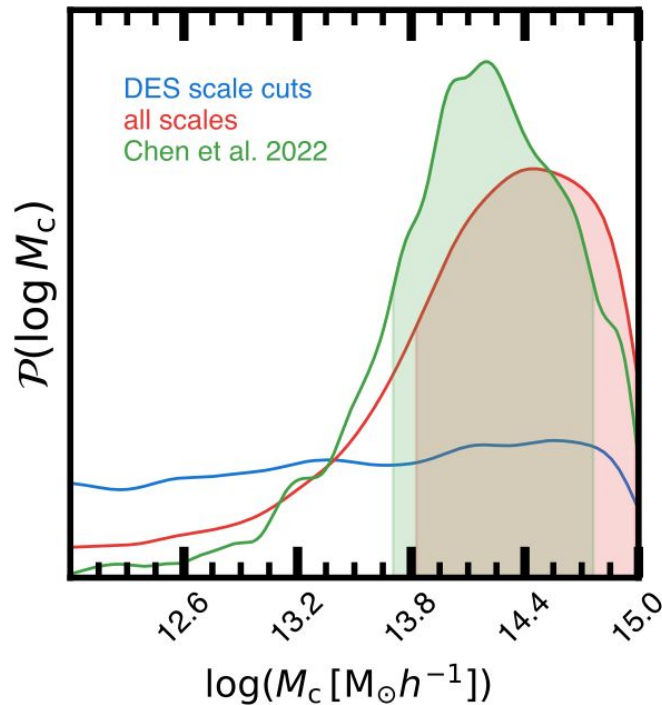
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# Exploring the S8 tension

Results on baryons. Halo mass for which half of the gas is lost due to feedback



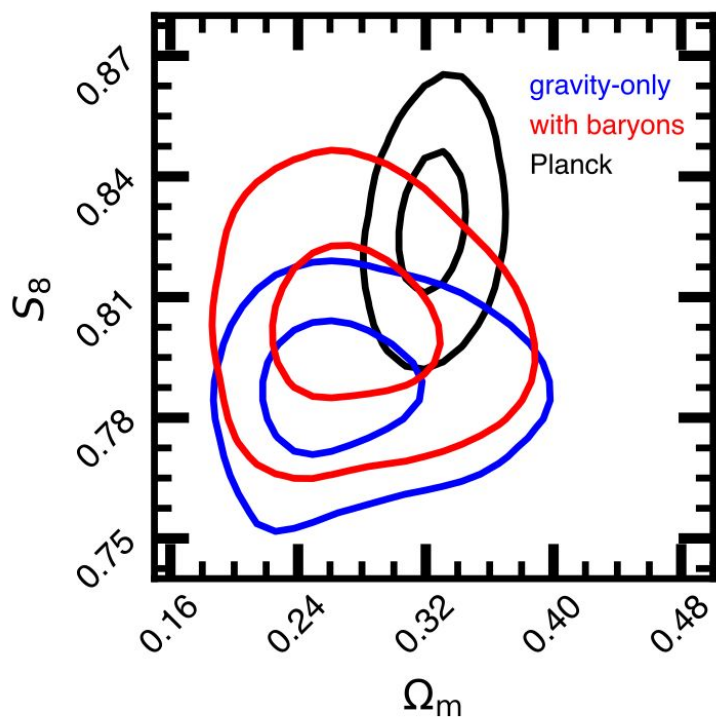
Arico, REA + (2023)

$$\log M_c = 14.38^{+0.60}_{-0.56} \log(h^{-1} M_\odot)$$

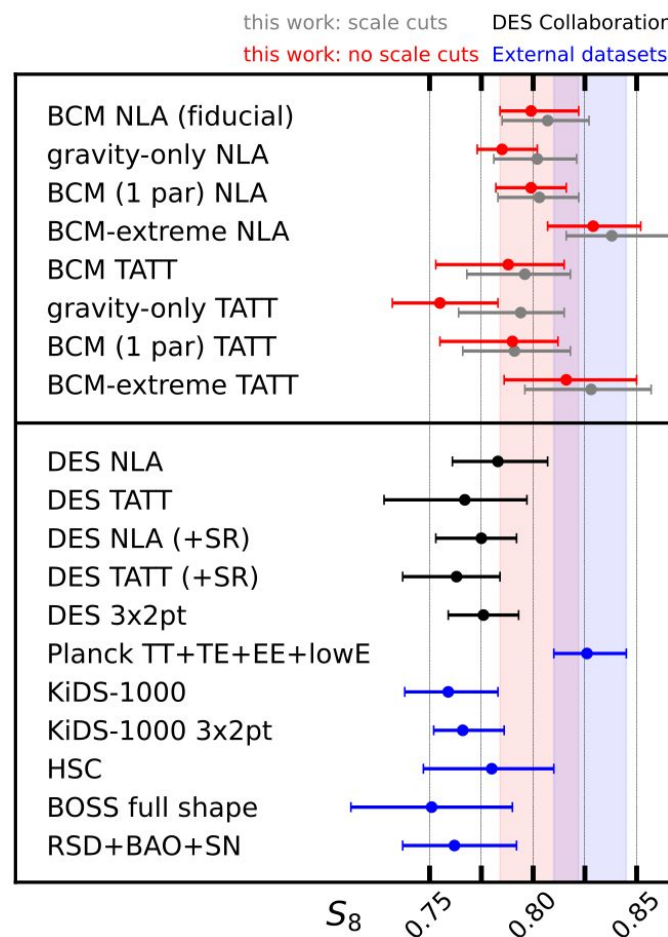


# Exploring the S8 tension

## 0.9 sigma tension with Planck for our fiducial case

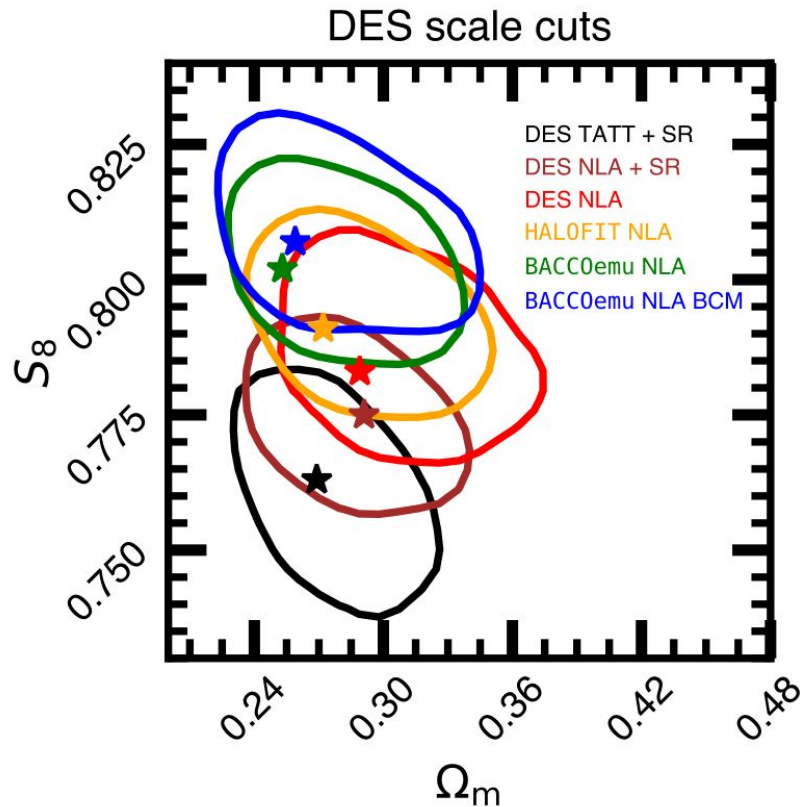


0.9 $\sigma$  tension with Planck in our fiducial case



# Exploring the $S_8$ tension

## Differences with respect to the DES collaboration results



Disagreement in  $S_8$

Our fiducial - DES fiducial  $1.4\sigma$

TATT-NLA  $0.4 - 0.7\sigma$

Shear ratios  $0.1 - 0.3\sigma$

Pipeline/priors  $\approx 0.2\sigma$

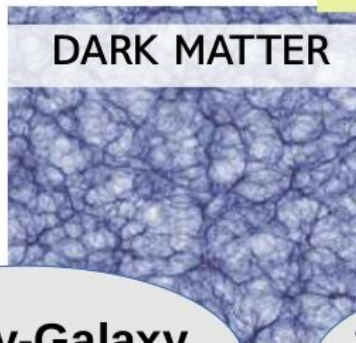
Non-linearities  $0.4 - 0.5\sigma$

Baryons  $\approx 0.2\sigma$

# Simultaneous modelling of LSS data

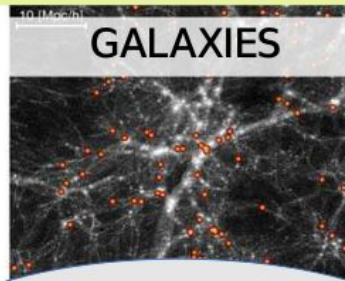
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**Lensing**



**Galaxy-Galaxy  
Lensing**

**Clustering  
Clusters**



**tSZ – shear – Galaxy  
Cross Correlations**

**SZ  
Intensity  
Mapping**



**Clusters in X-rays,  
SZ, optical, lensing**

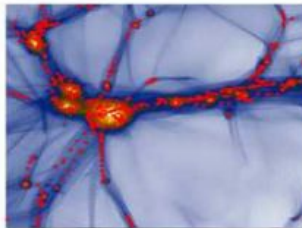
Improvements feedback into a more accurate modelling and better cosmological inferences



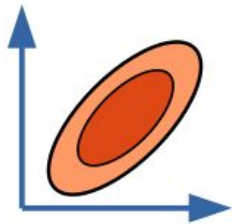
# Numerical simulations for interpreting large scale structure data



Upcoming large galaxy surveys pose multiple challenges in data analyses and theory



Simulation-based approaches and new summary statistics are providing new options



All these together could offer a robust and accurate path to discovering new physics

# <http://bacco.dipic.org/>



## COSMOLOGY WITH BACCO: MAXIMISING DISCOVERY WITH GALAXY SURVEYS

The BACCO project is a simulation framework specially designed to provide highly-accurate predictions for the distribution of mass, galaxies, and gas as a function of cosmological parameters

### baccoemu 0.3

```
pip install baccoemu
```