



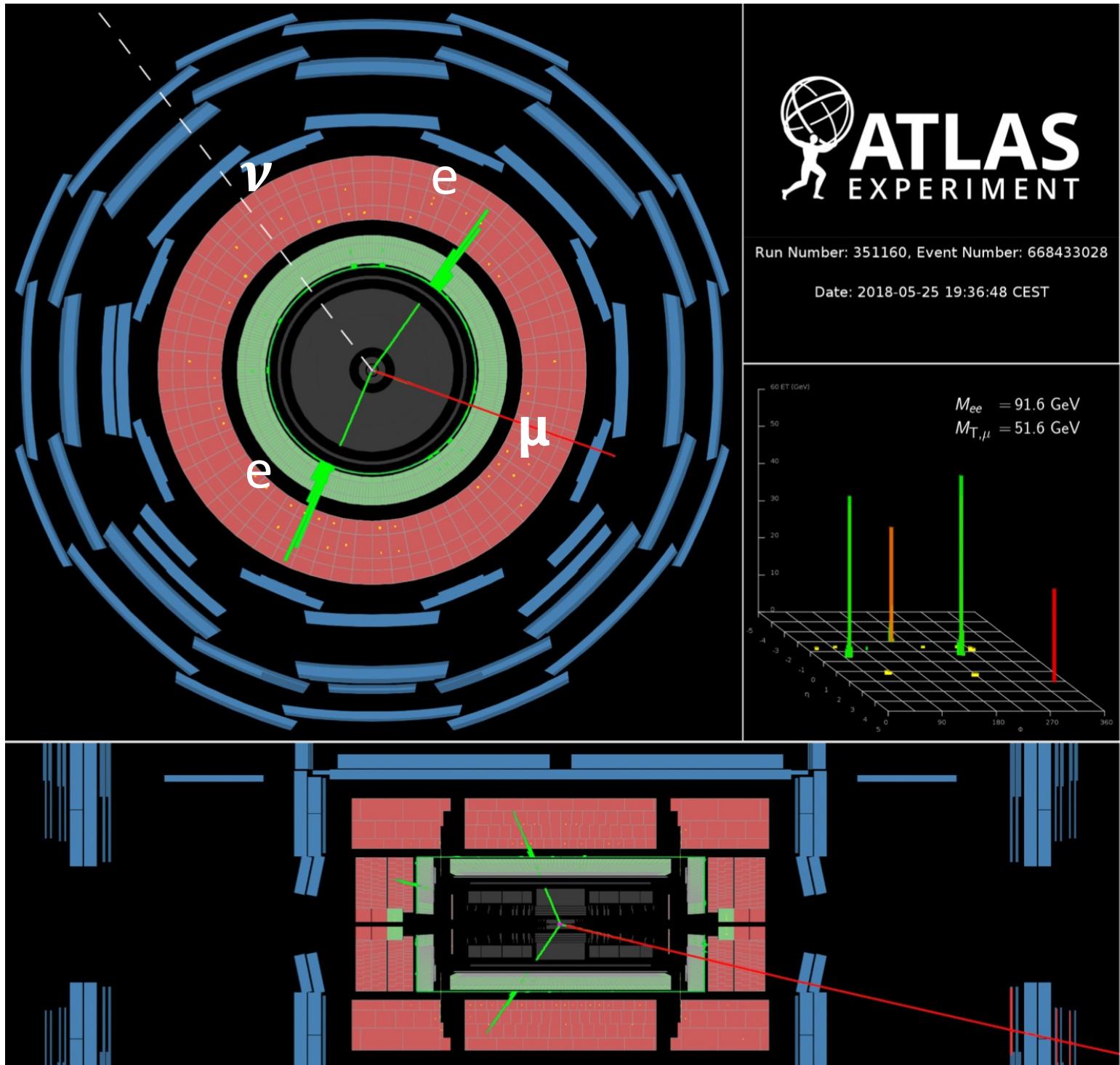
A computing exercise using ROOT

Aim: give a taste of data analysis @ LHC

- What is ROOT ?
 - ROOT is an object-oriented C++ analysis package
 - User-compiled code can be called to produce 1-d, 2-d, and 3-d graphics and histograms...



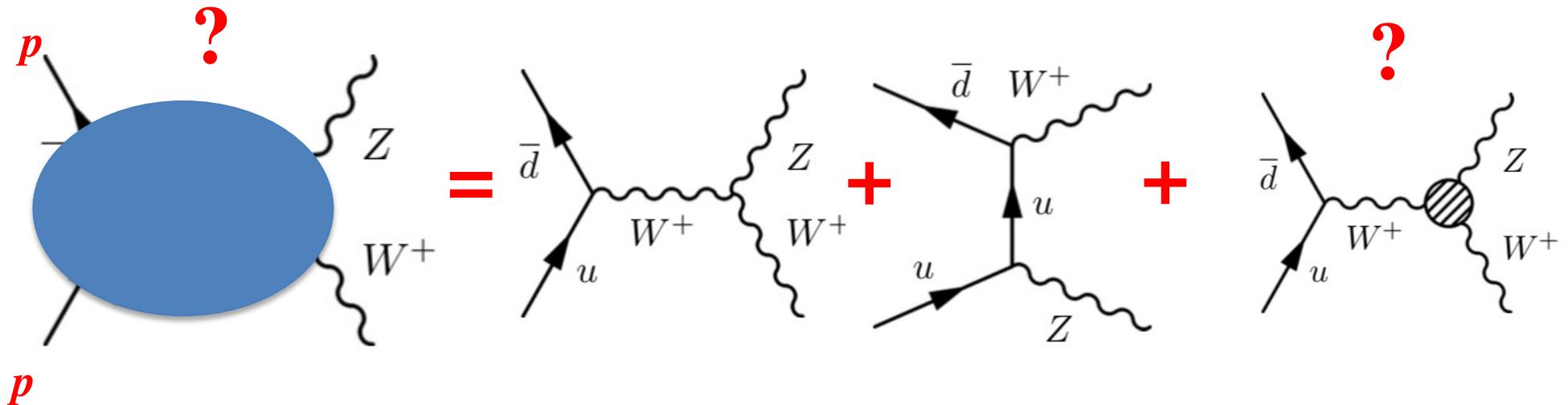
<https://root.cern.ch>



Hands-on on diboson physics



topic @ LHC



Test of SM
(measure interaction probability)

Discover New Physics
(look inside the blob)

Advantage of accelerator physics: controlled and known initial conditions



→ most of things discovered about fundamental interactions so far thanks to accelerator physics

Outline of the presentation

- Kinematic variables used in the analysis of $p - p$ collisions
- Useful relations
- Concept of invariant mass (example: ‘inclusive’ Z boson production)
- Example of analysis in $p - p$ collisions :
 - * Signal: Production of a W and a Z $p - p \rightarrow W Z X$
 - * Background: Production of a pair of top-antitop
- Example: Macro.C

p = proton

X = additional
undetected
particles

(X) =
part1, part2, part3, ...

In all the following slides we assume the speed of the light

c=1

$p - p$ = proton - proton

Variables used in the analysis of p - p collisions

A particle (Z, W, e+, e-, etc ...) is described by its **four-momentum**:

$$\tilde{p} = (E, p_x, p_y, p_z)$$

The particle mass is $m = \sqrt{E^2 - p_x^2 - p_y^2 - p_z^2}$

When dealing with p - p collisions the following variables are used:

For **each** particle (Z, W, e+, e-, etc ...):

- 1. Transverse momentum/energy : $p_T = p \sin \theta$ $E_T = E \sin \theta$

- 2. Rapidity

$$Y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$$

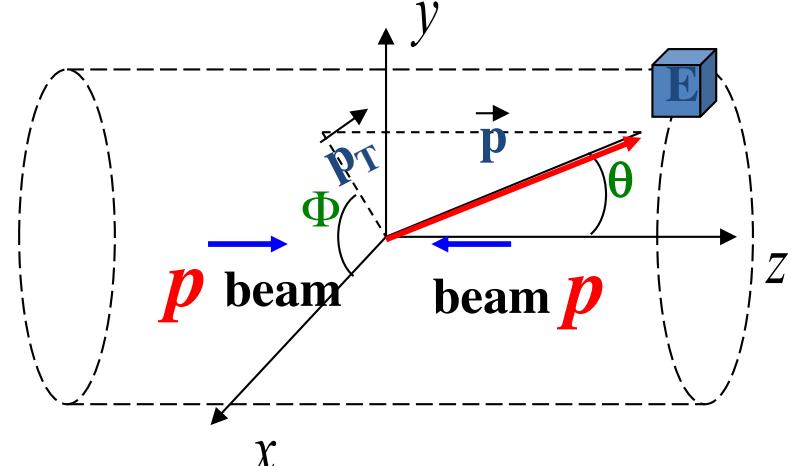
or Pseudorapidity

$$\eta = -\ln (\tan \frac{\theta}{2})$$

Why?

- 3. Azimuthal angle

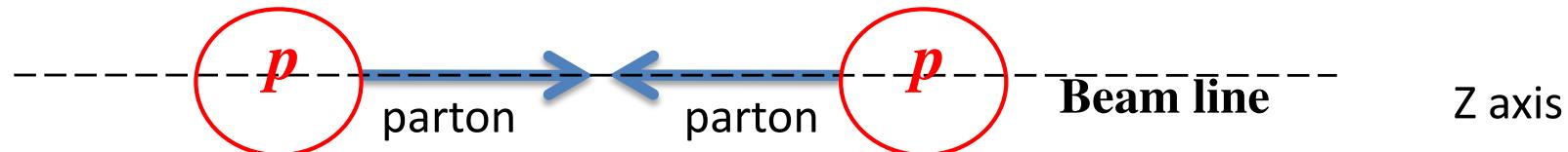
$$\Phi$$



Variables used in the analysis of $p - p$ collisions

Why p_T, Y ?

Many reasons (p = proton).



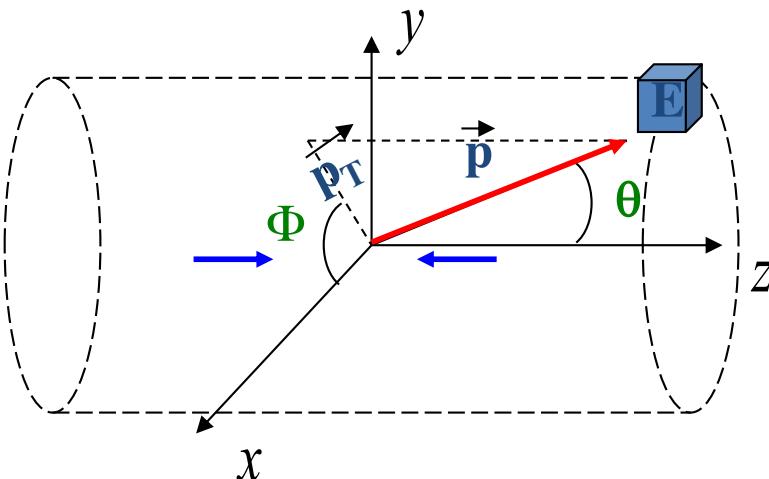
1. p_T and ΔY are invariants for Lorentz transformations along the z axis 
2. The **longitudinal momentum of a initial partons is ‘unknown’**, while we know that $\vec{p}_T^{\text{initial parton}} \sim 0$
→ Exploit momentum conservation **in the plane \perp to the beam** using *transverse* quantities → Example:

$$\sum_{\text{initial partons}} \vec{p}_T = \sum_{\text{vis}^{\text{fin}}} \vec{p}_T + \sum_{\text{invis}^{\text{fin}}} \vec{p}_T \approx 0 \quad \rightarrow \text{Allows to evaluate the } p_T \text{ of not detected (v) particles}$$

$$\sum_{\text{invis}^{\text{fin}}} \vec{p}_T = - \sum_{\text{vis}^{\text{fin}}} \vec{p}_T \quad |\sum_{\text{invis}} p_T| \text{ is the “missing } E_T \text{”}$$

3. The “interesting” physics is due to **hard scattering processes** → **high p_T particles** (selection of high p_T particles ensures “interesting” physics)

Useful relations



$$p_T = p \sin \theta$$

$$p_x = p_T * \cos(\Phi);$$

$$p_y = p_T * \sin(\Phi);$$

$$p_z = E * \tanh(\eta);$$

$$\eta = -\ln(\tan \frac{\theta}{2})$$

NB:

- $m \ll E \rightarrow Y \approx \eta$ (η doesn't require particle identification)
- $m \ll E \rightarrow p_T \approx E_T \quad E_T = E \sin \theta$

Concept of *invariant* mass M_A

Particle A decays to B and C

$$A \rightarrow B \ C$$

$$M_A^2 = \tilde{p}_A^2 = (\tilde{p}_B + \tilde{p}_C)^2$$

The invariant mass is the same in all frames of reference related by Lorentz transformations

Concept of *invariant mass*: inclusive Z boson production

$p - p \rightarrow Z (X)$

With $Z \rightarrow e+e-$

(X) = part1, part2, part3, ...

Invariant mass M_{ee} of ee system from the 4-momentum conservation

(it allows to measure the Z mass, M_Z):

Very ‘clean’ events (low bkg)!!

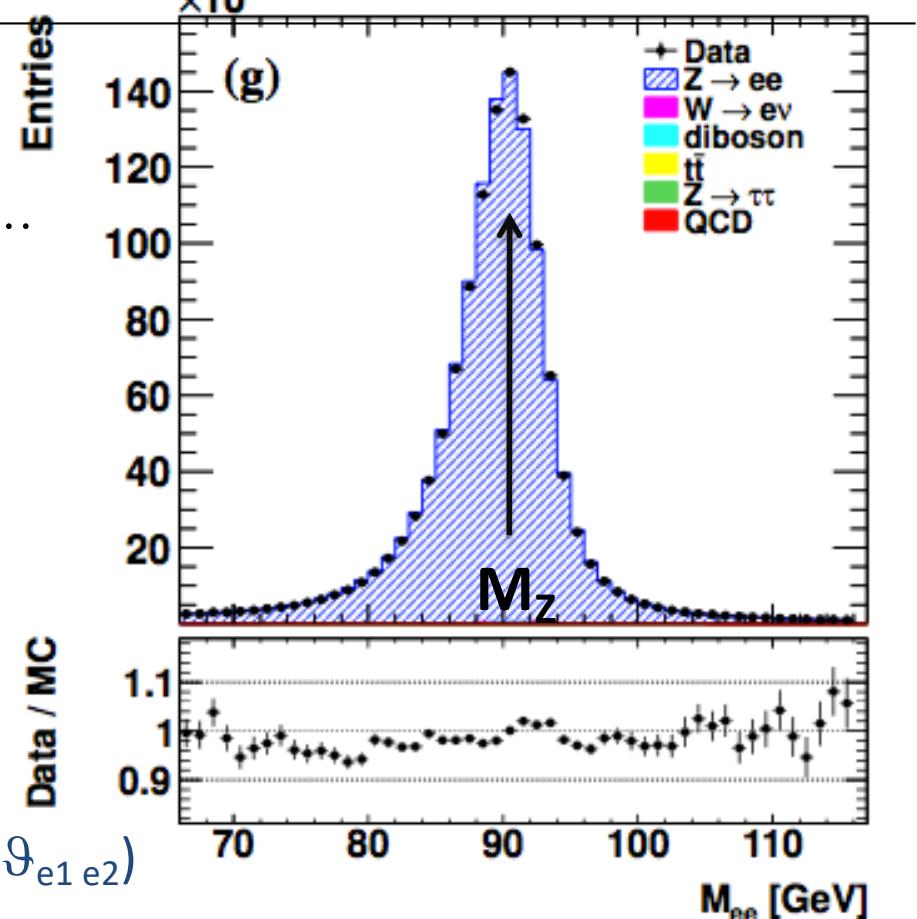
$$\tilde{p}_Z^2 = (\tilde{p}_{e1} + \tilde{p}_{e2})^2$$

$$M_{ee}^2 = (\tilde{p}_{e1} + \tilde{p}_{e2})^2 \approx 2 (E_{e1} E_{e2} - |\vec{p}_{e1}| |\vec{p}_{e2}| \cos \vartheta_{e1 e2})$$

$$M_{ee} \approx \sqrt{2 E_{e1} E_{e2} (1 - \cos \vartheta_{e1 e2})}$$

(the electron mass is neglected)

Why M_{ee} gives a distribution and not a single value?



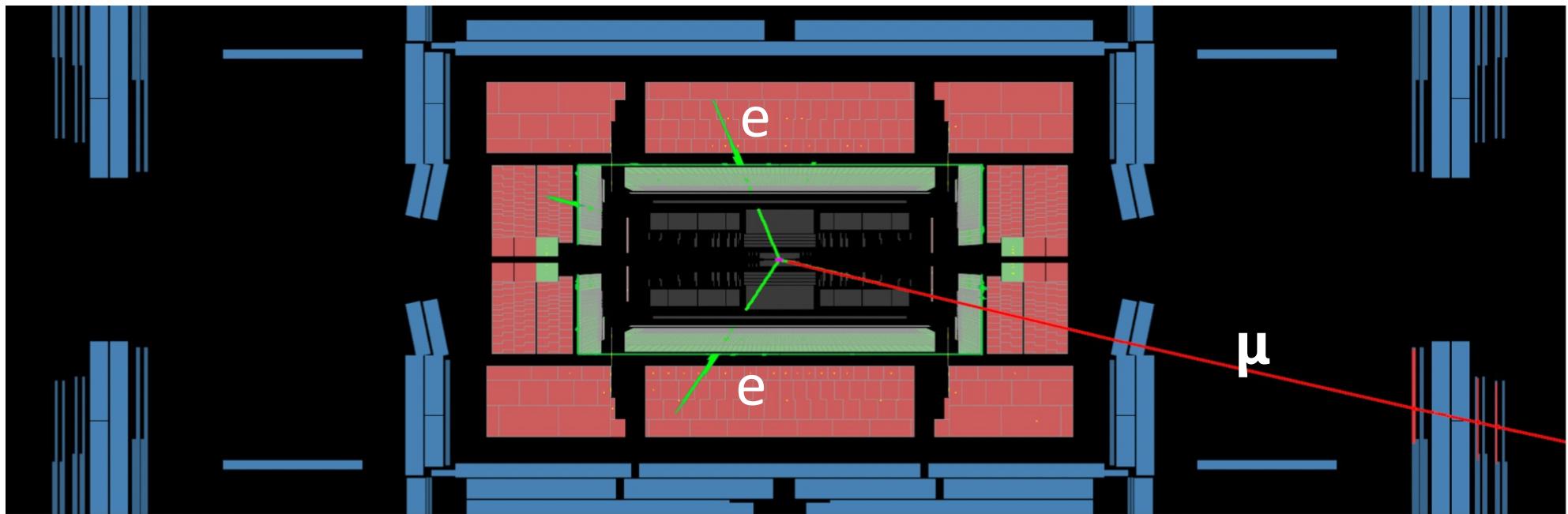
1. $\Delta E * \Delta t > \hbar/2$ $\Delta m * \tau > \hbar/2$

$\Gamma * \tau > \hbar/2$

width

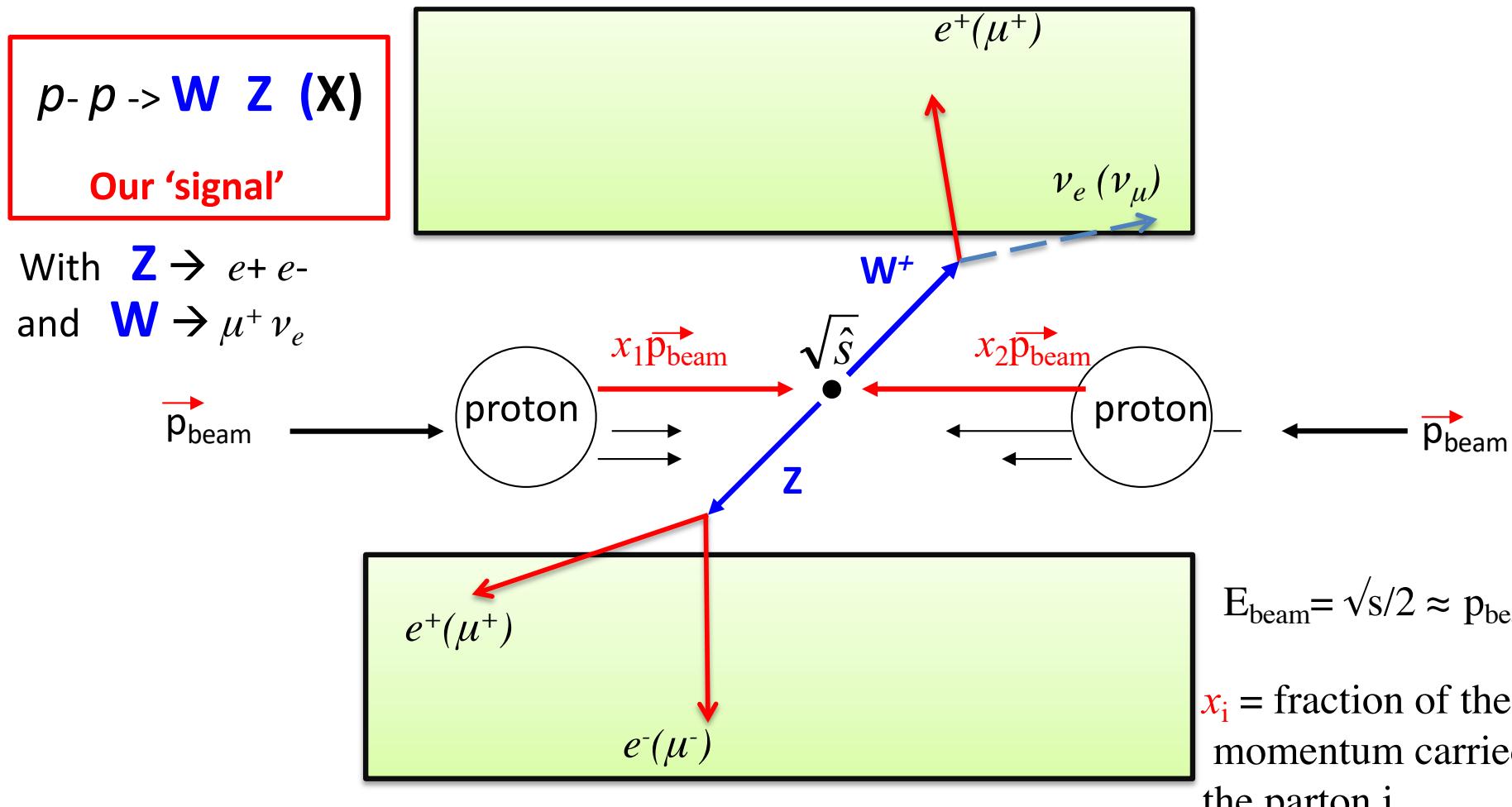
lifetime

2. Experimental resolution



Our signal : production of a W and a Z (decaying leptonically)

p - p ‘hard’ collisions in the $q_1 \bar{q}_2$ center of mass:



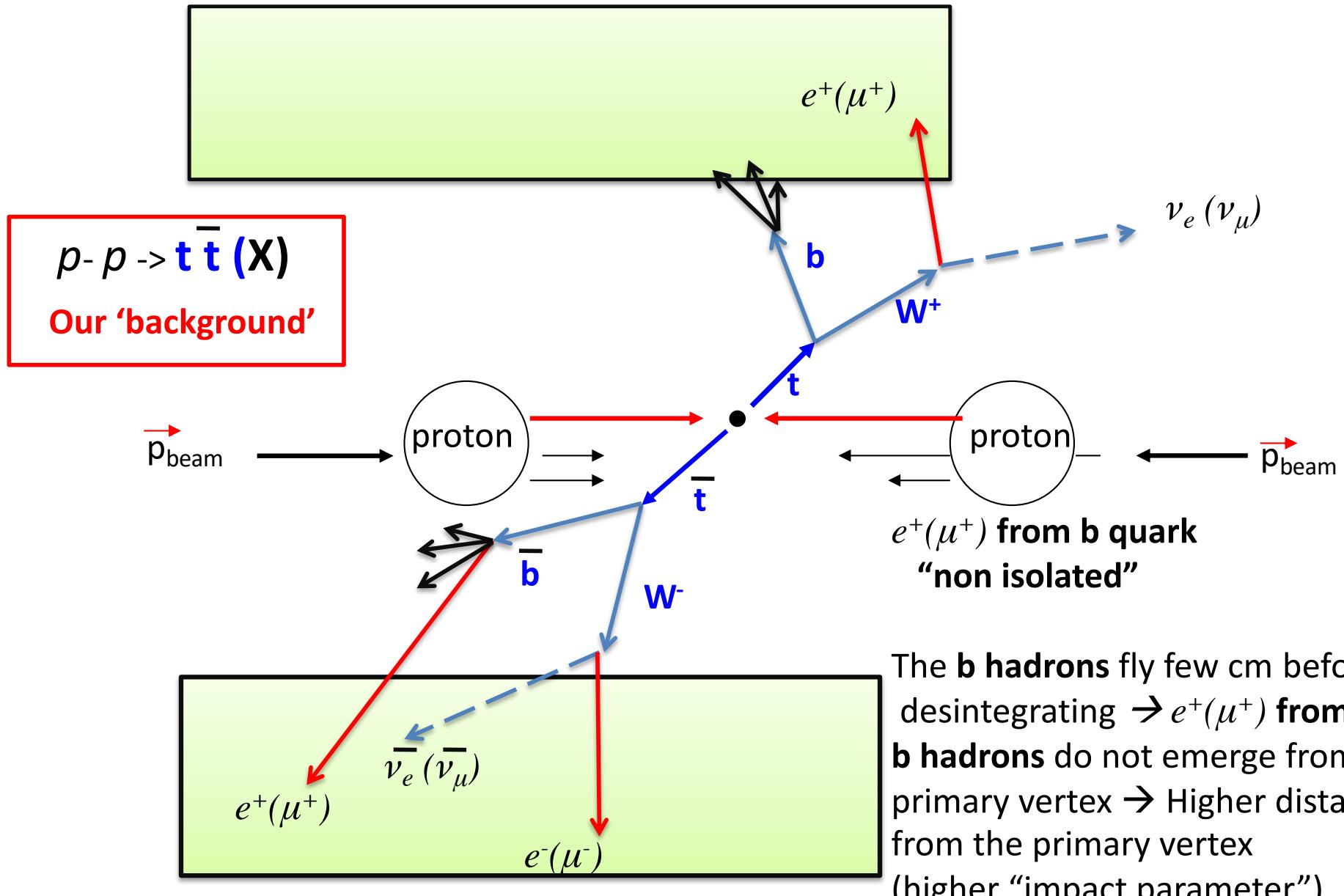
Kinematics of p - p collisions

$$0 < x_{1,2} < 1$$

* 4-mom of the initial partons : [$(x_1+x_2)E_{\text{beam}}, 0, 0, (x_1-x_2) p_{\text{beam}}$]

Our background: Production of a pair of top-antitop

p - p ‘hard’ collisions. In the $\bar{q}_1 q_2$ center of mass:



Aim of the exercise (**note, this are the first steps of an analysis**):

- 1) look at some important variables,
- 2) build the Z invariant mass,
- 3) how one can discriminate between the 'signal' and the 'background' ?

You will have:

GRASPA2023explanation.pptx.pdf (this slides)

Exercise2023.pdf (what we ask to do)

Selected_All_EEM.root (« data file » (simulated data))

macro.C (draft of an analysis program)

macro_final.C (solution: final analysis program)

<https://root.cern.ch/root/html/doc/guides/primer/ROOTPrimer.html>

1) The **input file** containing the physics: **Selected_All_EEM.root**

==== MOST ENERGETIC LEPTON FROM THE Z

Br 4 :pt1 : pt1

Br 5 :eta1 : eta1

Br 6 :phi1 : phi1

Br 7 :E1 : E1

==== SECOND ENERGETIC LEPTON FROM THE Z

Br 8 :pt2 : pt2

Br 9 :eta2 : eta2

Br 10 :phi2 : phi2

Br 11 :E2 : E2

==== LEPTON FROM W

Br 12 :pt3 : pt3

Br 13 :eta3 : eta3

Br 14 :phi3 : phi3

Br 15 :E3 : E3

List of variables given per each collision event (kinematics of the final state leptons)

2) Instructions to make the computing exercise : **Exercise2023.pdf**



COMPUTING EXERCISE

Study of the production of a pair of gauge bosons (W and Z) at the LHC

The data to analyse are organised into a '**Root n-tuple**' which we will provide to you. The Root n-tuple is a file containing information about the kinematics of "events", each resulting from a **proton-proton interaction**.

These events have three leptons (electrons or muons) and are of two kinds:

- 1) **SIGNAL EVENTS**: corresponding to $pp \rightarrow W Z X$ with both bosons disintegrating leptonically (X stands for non identified generic particles),
- 2) **BACKGROUND EVENTS**: top-antitop events $pp \rightarrow t\bar{t}X$.

We remind that the leptonic decays of the W and Z are:

$$W \rightarrow \ell\nu \text{ and } Z \rightarrow \ell^+\ell^- \text{ with } \ell = e \text{ or } \mu.$$

3) A skeleton of an analysis program using ROOT: **macro.C**

```
#include "TCanvas.h"
#include "TROOT.h"
#include "TFile.h"
#include "TTree.h"
#include "TBrowser.h"
#include "TH2.h"
#include "TRandom.h"

void tree1r()
{
    // Read Selected_All_EEM.root file
    //Root file
    TFile *f = new TFile("Selected_All_EEM.root");

    // Signal events
    TTree *sig = (TTree*)f->Get("WZSignal");
    Double_t pt1, eta1, phi1, E1;
    Double_t pt2, eta2, phi2, E2;
    Double_t pt3, eta3, phi3, E3;
    Double_t MZ, MET, trackd0cutWMu, TrackIsoWMu;
    Double_t Weight;

    //get some variables for SIGNAL EVENTS
    sig->SetBranchAddress("pt1",&pt1);
```

Example of analysis program

macro.C

23/07/2013 00:21

```
#include "TCanvas.h"
#include "TRoot.h"
#include "TFile.h"
#include "TTree.h"
#include "TBrowser.h"
#include "TH2.h"
#include "TRandom.h"

void tree1r()
{
    // Read Selected_All_EEM.root file
    //Root file
    TFile *f = new TFile("Selected_All_EEM.root");

    // Signal events
    TTree *sig = (TTree*)f->Get("WZSignal");
    Double_t pt1, eta1, phi1, E1;
    Double_t pt2, eta2, phi2, E2;
    Double_t pt3, eta3, phi3, E3;
    Double_t MZ, MET, trackd0cutWMu, TrackIsowmu;
    Double_t Weight;

    //get some variables for SIGNAL EVENTS
    sig->SetBranchAddress("pt1",&pt1);
    sig->SetBranchAddress("eta1",&eta1);
    sig->SetBranchAddress("phi1",&phi1);
    sig->SetBranchAddress("E1",&E1);
    sig->SetBranchAddress("MZ",&MZ);
    sig->SetBranchAddress("Weight",&Weight);
    // add other variables ...
```

Header files

Open the input file

Access the Signal info

**Define the name
variables per each SIGNAL lepton**

```

////get some variables for BACKGROUND EVENTS
TTree *ttbar = (TTree*)f->Get("ttbar");
Double_t pt1_bkg, eta1_bkg, phi1_bkg, E1_bkg;
Double_t MZ_bkg;
Double_t Weight_bkg;

//get some variables for ttbar
ttbar->SetBranchAddress("pt1",&pt1_bkg);
ttbar->SetBranchAddress("eta1",&eta1_bkg);
ttbar->SetBranchAddress("phi1",&phi1_bkg);
ttbar->SetBranchAddress("E1",&E1_bkg);
ttbar->SetBranchAddress("MZ",&MZ_bkg);
ttbar->SetBranchAddress("Weight",&Weight_bkg);
// add other variables ...

//create two histograms (for sig and ttbar)
TH1F *h_MZ      = new TH1F("h_MZ","MZ distribution All events",40,65,115);
TH1F *h_MZ_bkg   = new TH1F("h_MZ_bkg","MZ distribution BKG",40,65,115);
TH1F *h_MZ_sig   = new TH1F("h_MZ_sig","MZ distribution SIG",40,65,115);

//read all SIGNAL entries and fill the histograms
Int_t nentries = (Int_t)sig->GetEntries();

for (Int_t i=0;i<nentries_bkg;i++) {
    ttbar->GetEntry(i);
    h_MZ_bkg->Fill(MZ_bkg,Weight_bkg);
    h_MZ->Fill(MZ_bkg,Weight);
}

```

Access the background info

**Define the name
variables per each bkg lepton**

Loop on events

Page 1 of 2

```
// example how Draw and save histograms  
TCanvas *c = new TCanvas();  
c->cd();  
h_MZ_sig->Draw();  
h_MZ_bkg->SetLineColor(kRed);  
h_MZ_bkg->Draw("same");  
  
c->Print("test_MZ.eps");  
}
```

```
void macro()  
{  
    tree1r();  
}
```

Draw and save histograms

Main program

To start root you may type:

root -l

root [1] .x macro.C

and look at what you get

Useful in-line commands:

```
TFile f("Selected_All_EEM.root");
f.ls();
WZSignal->Scan();
WZSignal->Print();
```

Where to find help:

[https://root.cern.ch/root/html/doc/guides/primer\(ROOTPrimer.pdf](https://root.cern.ch/root/html/doc/guides/primer(ROOTPrimer.pdf)

Have fun !!



W(jj) Z (jj)

jj = J (1 fat jet)

Another example: search for di-boson resonances

- Is there something hiding in the data, waiting to be discovered?

