



On the Exotic String Landscape

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Based on: 2309.15152 with

Yuta Hamada
Kaan Baykara
Cumrun Vafa

+ work in progress

Nov. 2023



String Landscape



Geometric string
constructions do
lots of the heavy
lifting!



CY3

Swampland

Landscape

String Pheno

String QFT

Geometric

String Landscape



Geometric

String Landscape

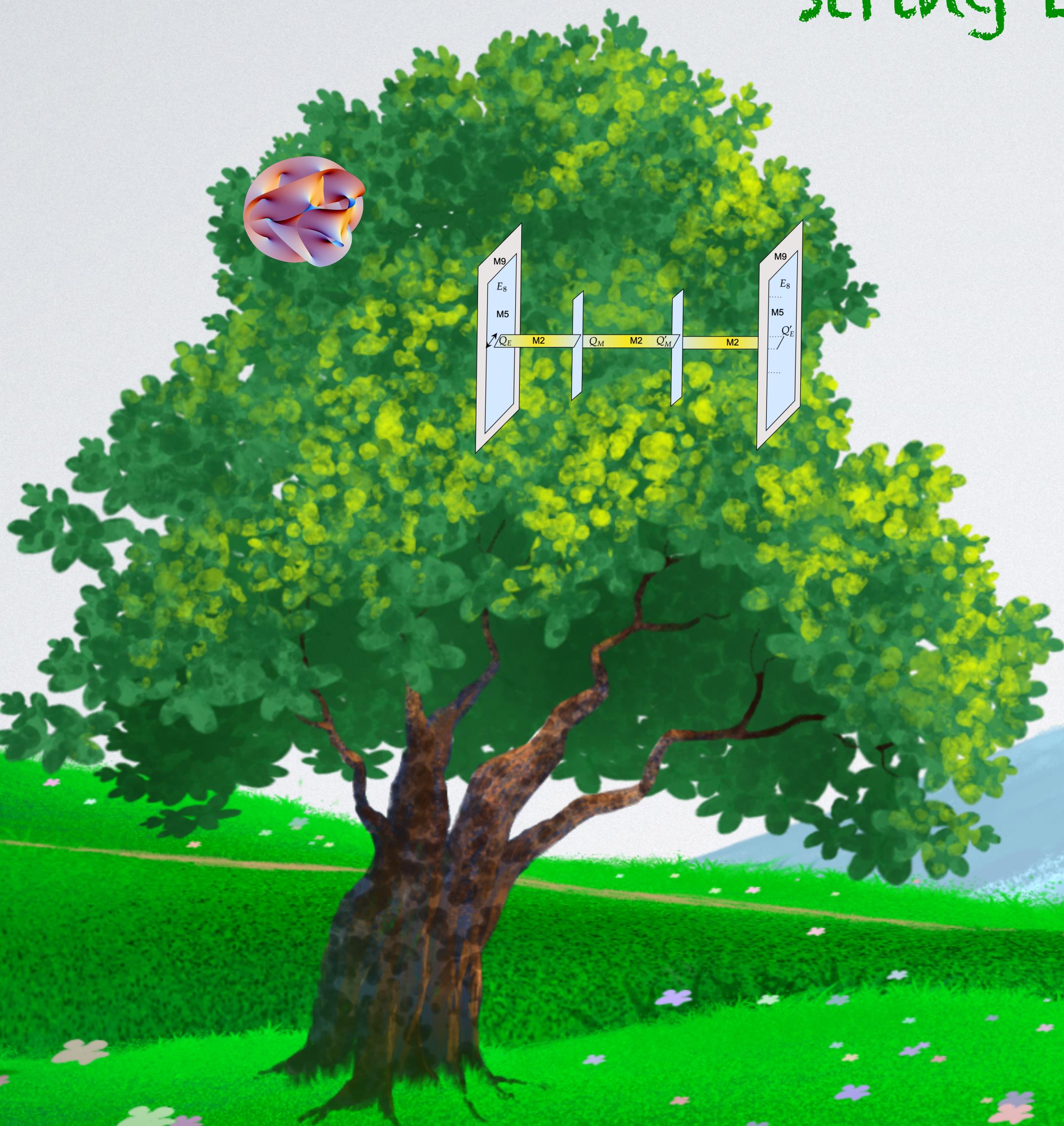


Non-geometric



Geometric

String Landscape



Today

Non-geometric



Geometric

String Landscape



Connections?

Non-geometric

Today

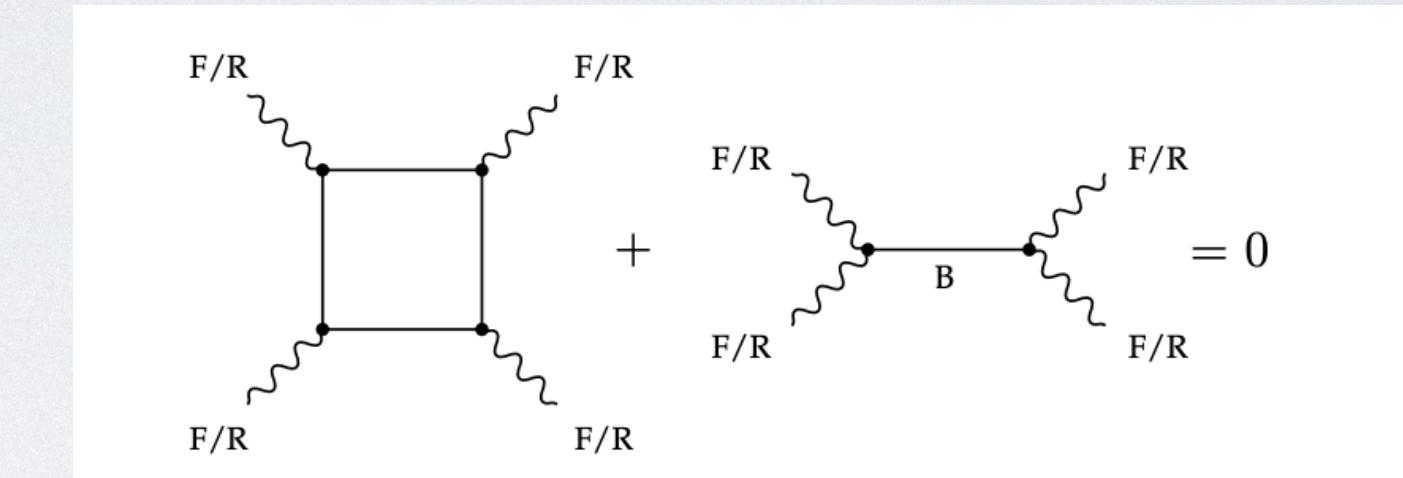
6d $\mathcal{N} = 1$ Supergravity theories

Super-multiplets:

Supergravity-multiplet	$(g_{\mu\nu}, B_{\mu\nu}, \psi_\mu^-)$
Tensor-multiplet(T)	$(B_{\mu\nu}, \phi, \chi^+)$
Vector-multiplet(V)	(A_μ, λ^-)
Hyper-multiplet(H)	$(4h, \psi^+)$

}

Chiral fields contribute to gauge/gravitational anomalies
Cancelled by the **Green-Schwarz-Sagnotti Mechanism**



Anomaly polynomial factorizes as:

$$I_8 = \frac{1}{2} \Omega_{\alpha\beta} X_4^\alpha X_4^\beta$$

$$X^\alpha = \frac{1}{2} a^\alpha \text{tr} R^2 + \sum_i b_i^\alpha \left(\frac{2}{\lambda_i} \text{tr} F_i^2 \right)$$

$\Omega_{\alpha\beta}$ symmetric of signature (1,T)

$$a^\alpha, b_i^\alpha \in \mathbb{R}^{1,T}$$

Anomaly Cancellation:

$$R^4 : H - V = 273 - 29T$$

$$F^2 R^2 : a \cdot b_i = \frac{1}{6} \lambda_i (A_{Adj}^i - \sum_R n_R^i A_R^i) \in \mathbb{Z}$$

$$F^4 : 0 = B_{Adj}^i - \sum_R n_R^i B_R^i$$

$$(F^2)^2 : b_i \cdot b_i = \frac{1}{3} \lambda_i^2 (\sum_R n_R^i C_R^i - C_{Adj}^i) \in \mathbb{Z}$$

$$(R^2)^2 : a \cdot a = 9 - T \in \mathbb{Z}$$

$$F_i^2 F_j^2 : b_i \cdot b_j = \sum_{R,S} \lambda_i \lambda_j n_{RS}^{ij} A_R^i A_S^j \in \mathbb{Z}, \quad i \neq j$$

A_R, B_R, C_R group theory coefficients

$$\text{tr}_R F^2 = A_R \text{tr} F^2, \quad \text{tr}_R F^4 = B_R \text{tr} F^4 + C_R (\text{tr} F^2)^2$$

n_R^i = hypers in number of in R

[Taylor, Kumar, Morison,....]

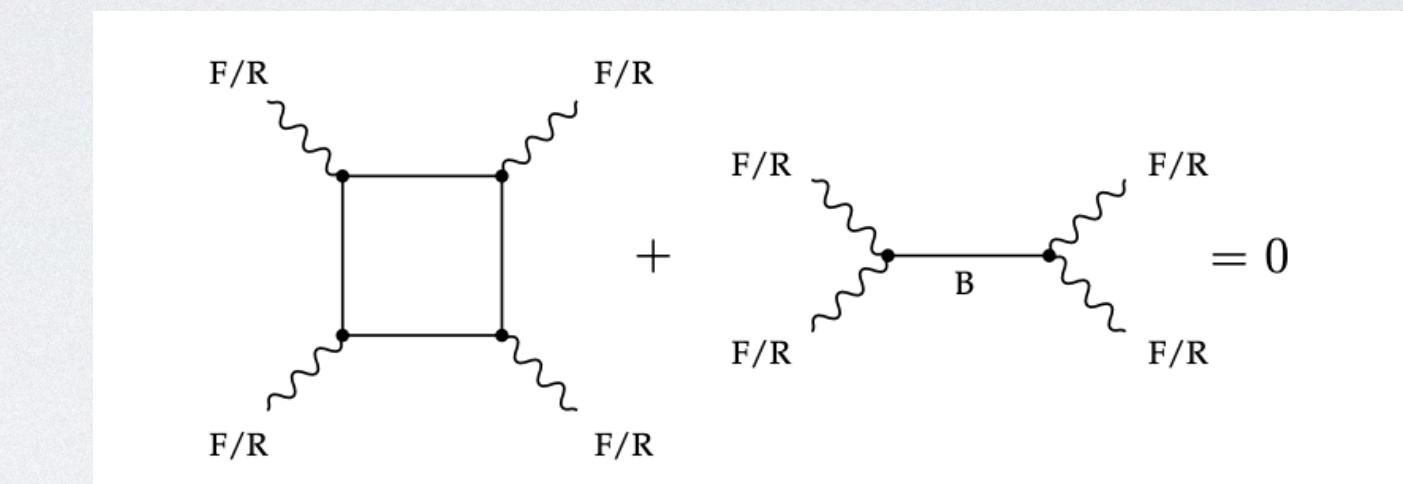
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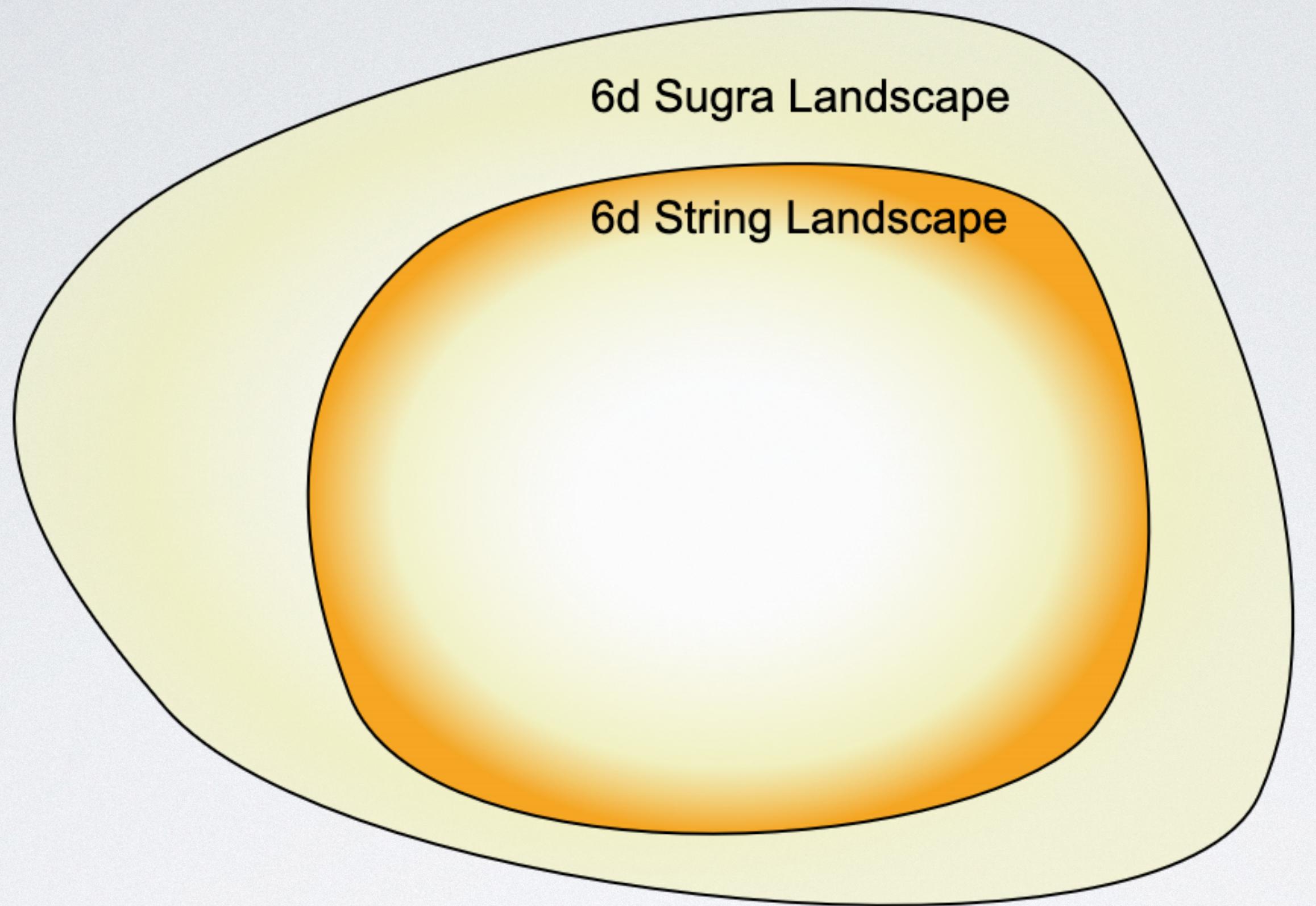
[Taylor, Kumar, Morison,....]

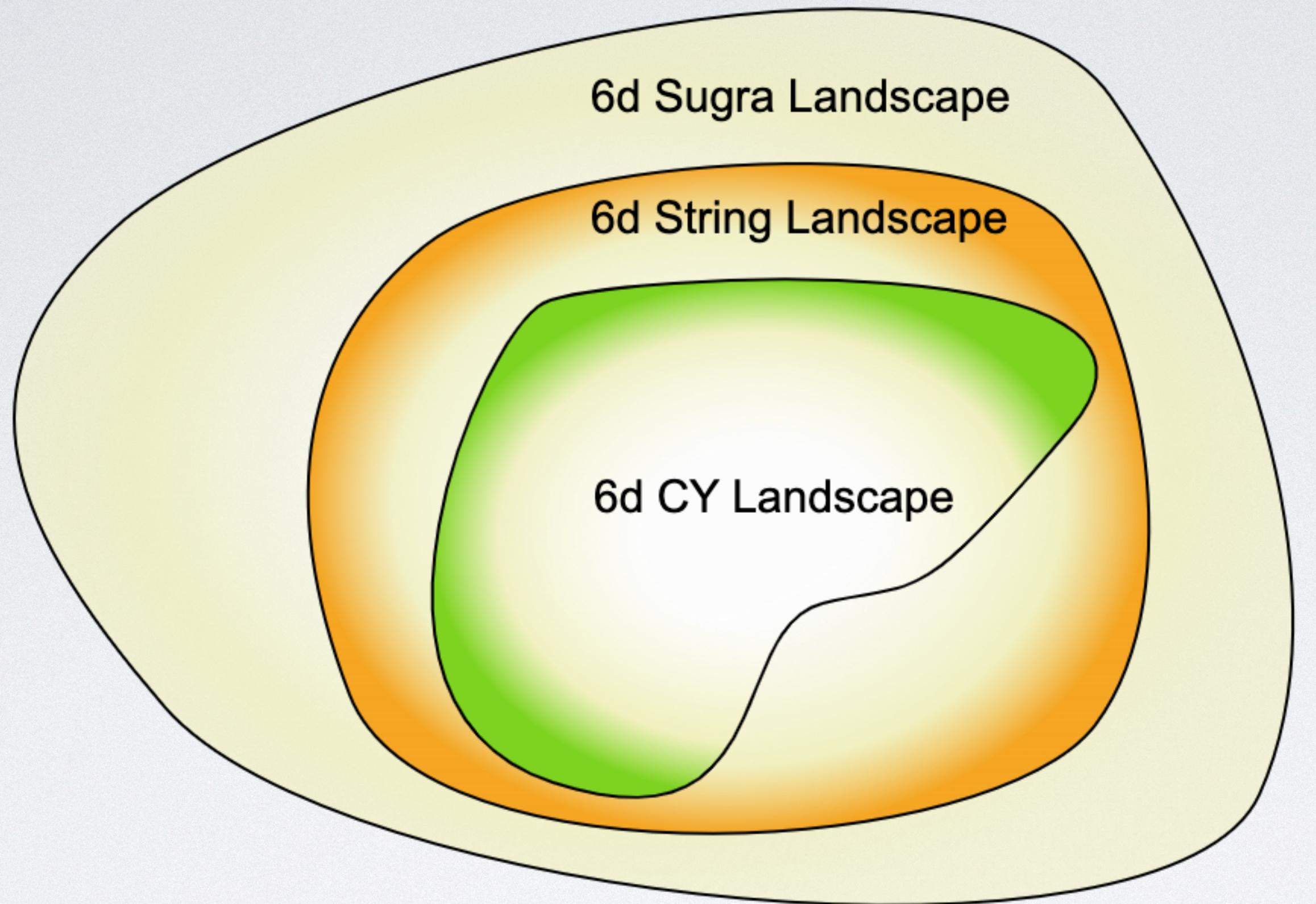
6d Sugra Landscape

[Morrison, ,Kumar, Taylor,.....09'/10'/.]

[Kim, Shiu, Vafa 19'] [Lee,Weigand 19']

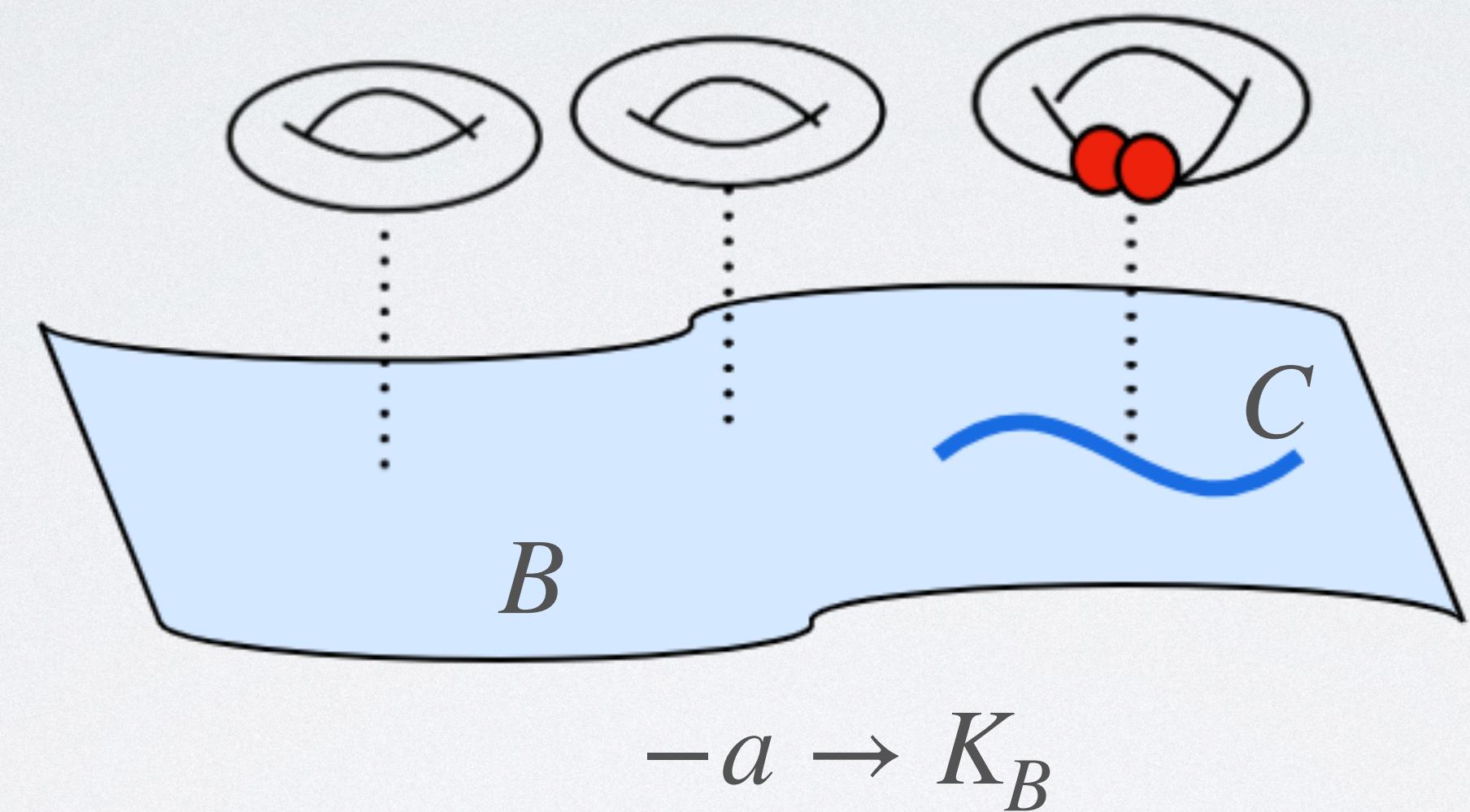
[HCT, Vafa 21'] [Hamada, Loges 23']





6d $\mathcal{N} = 1$ Supergravity

Large Class: F-theory on elliptic Calabi-Yau threefold

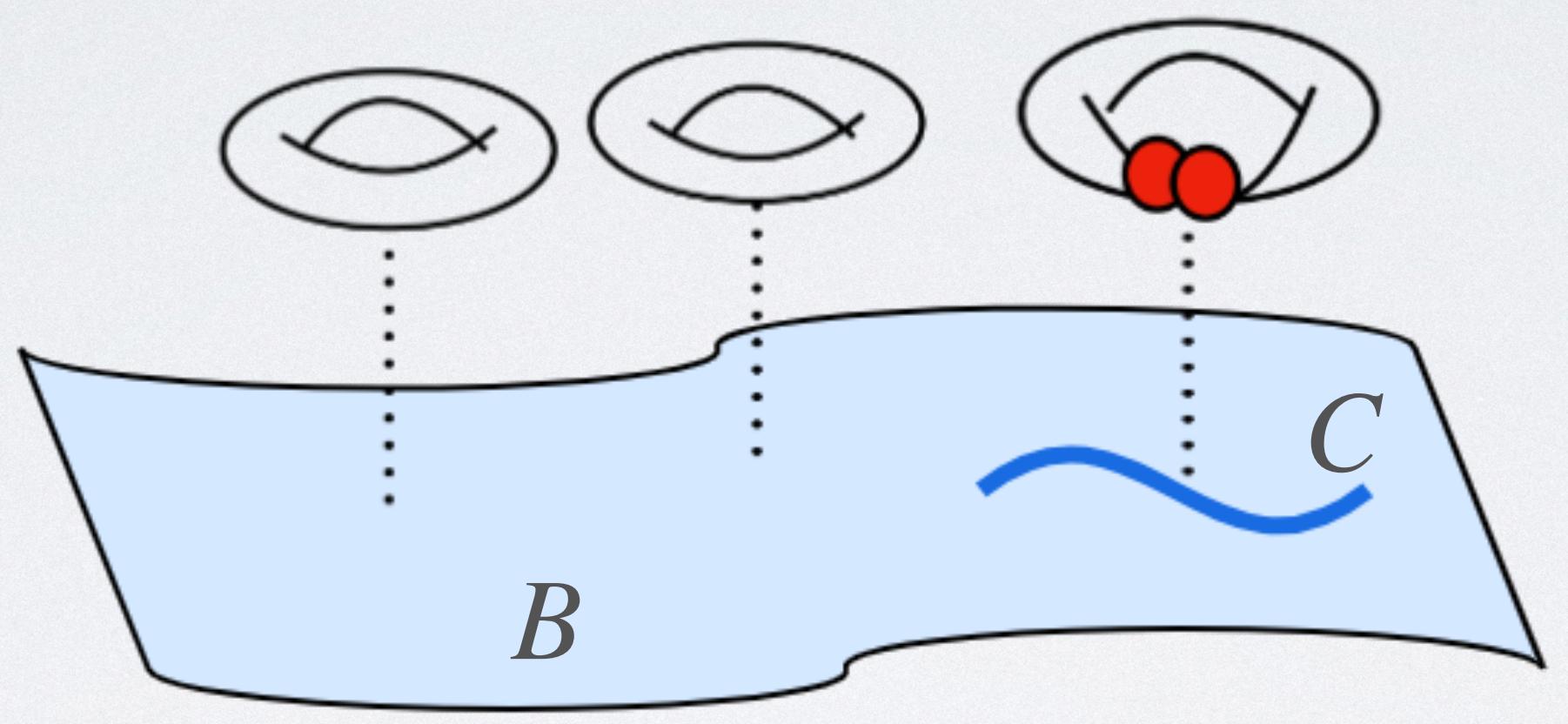


Kodaira Condition:

$$-12a = \sum_i \nu_i b_i + Y$$

6d $\mathcal{N} = 1$ Supergravity

Large Class: F-theory on elliptic Calabi-Yau threefold



$$-a \rightarrow K_B$$

$$b \rightarrow C$$

As a supergravity condition

$$B_2^a \wedge \left(\frac{1}{2} a^\alpha \text{tr} R^2 + \sum_i b_i^a \left(\frac{2}{\lambda_i} \text{tr} F_i^2 \right) \right)$$

Gravitational Instanton charge

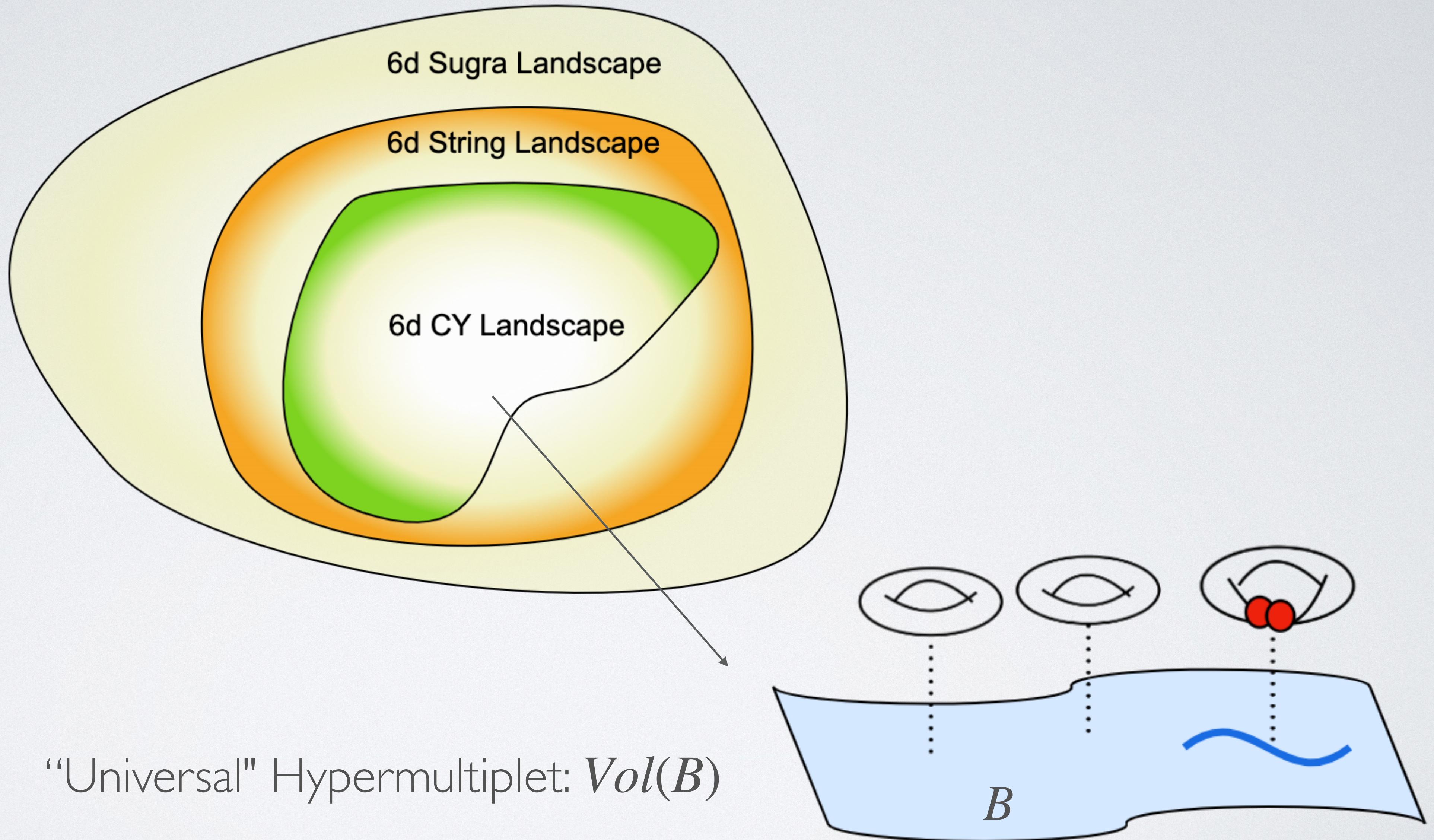
Gauge Instanton charge

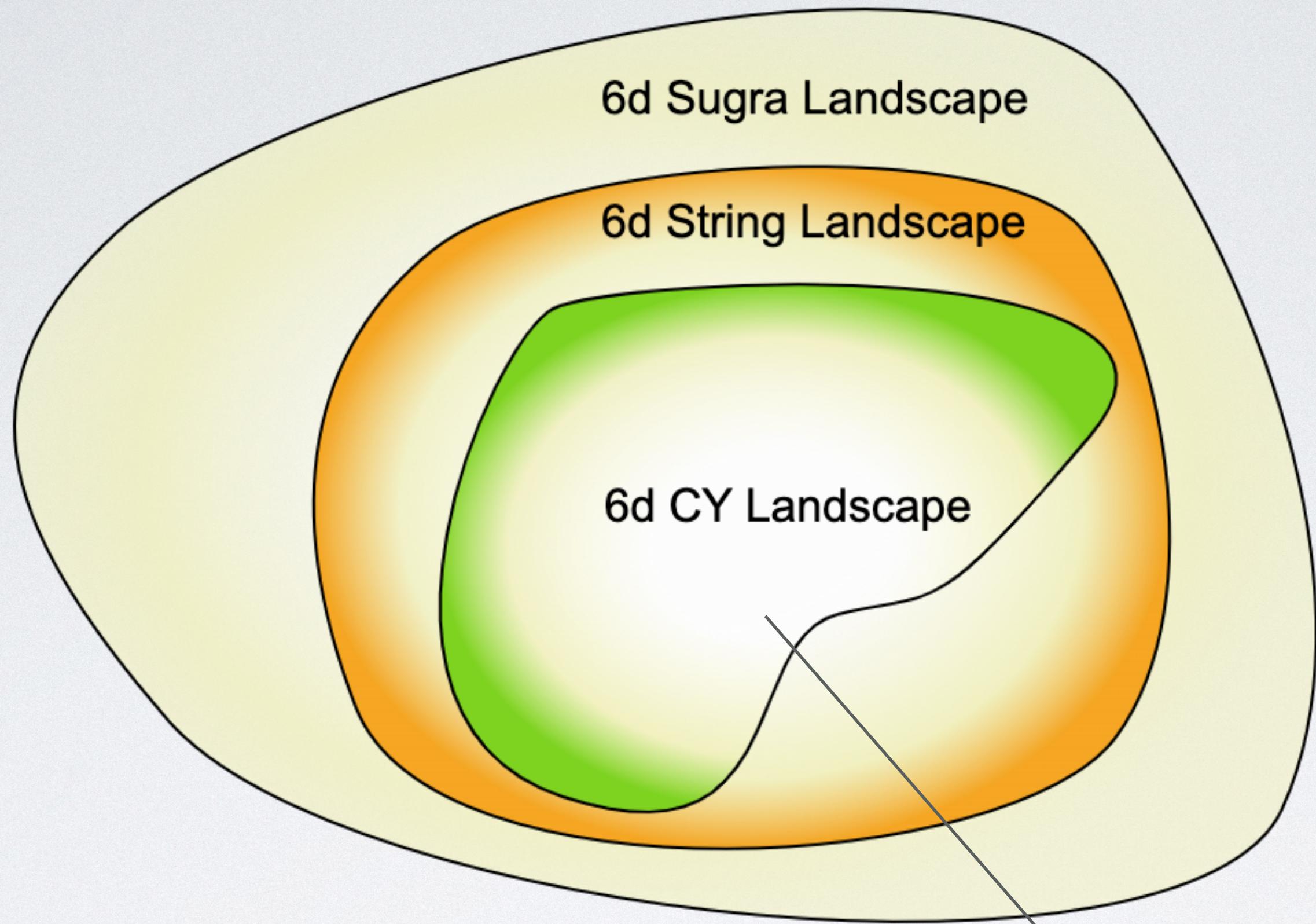
Kodaira Condition:

$$-12a = \sum_i \nu_i b_i + Y \quad \xrightarrow[J \cdot Y \geq 0]{} \quad 12 J \cdot a \geq \sum_i \nu_i J \cdot b_i$$

T_{-a}

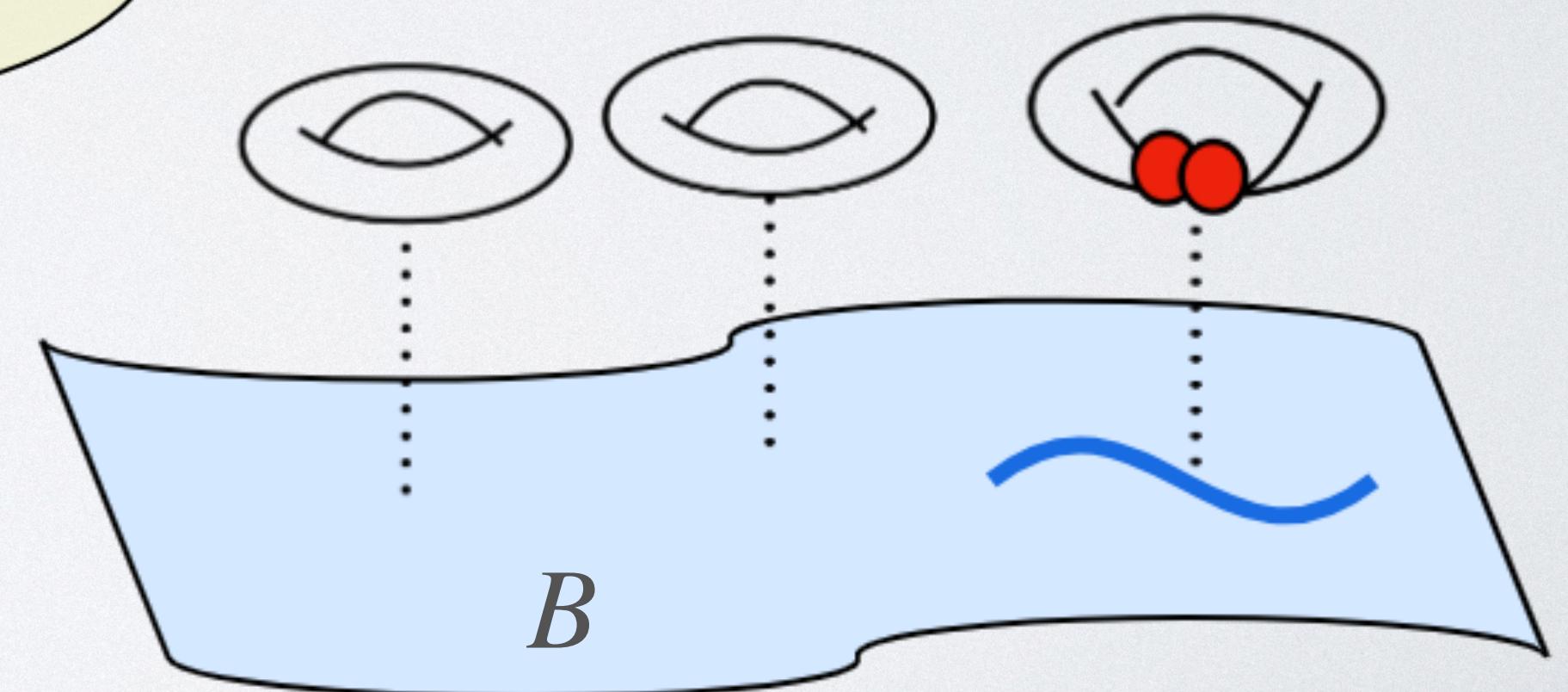
T_{b_i}

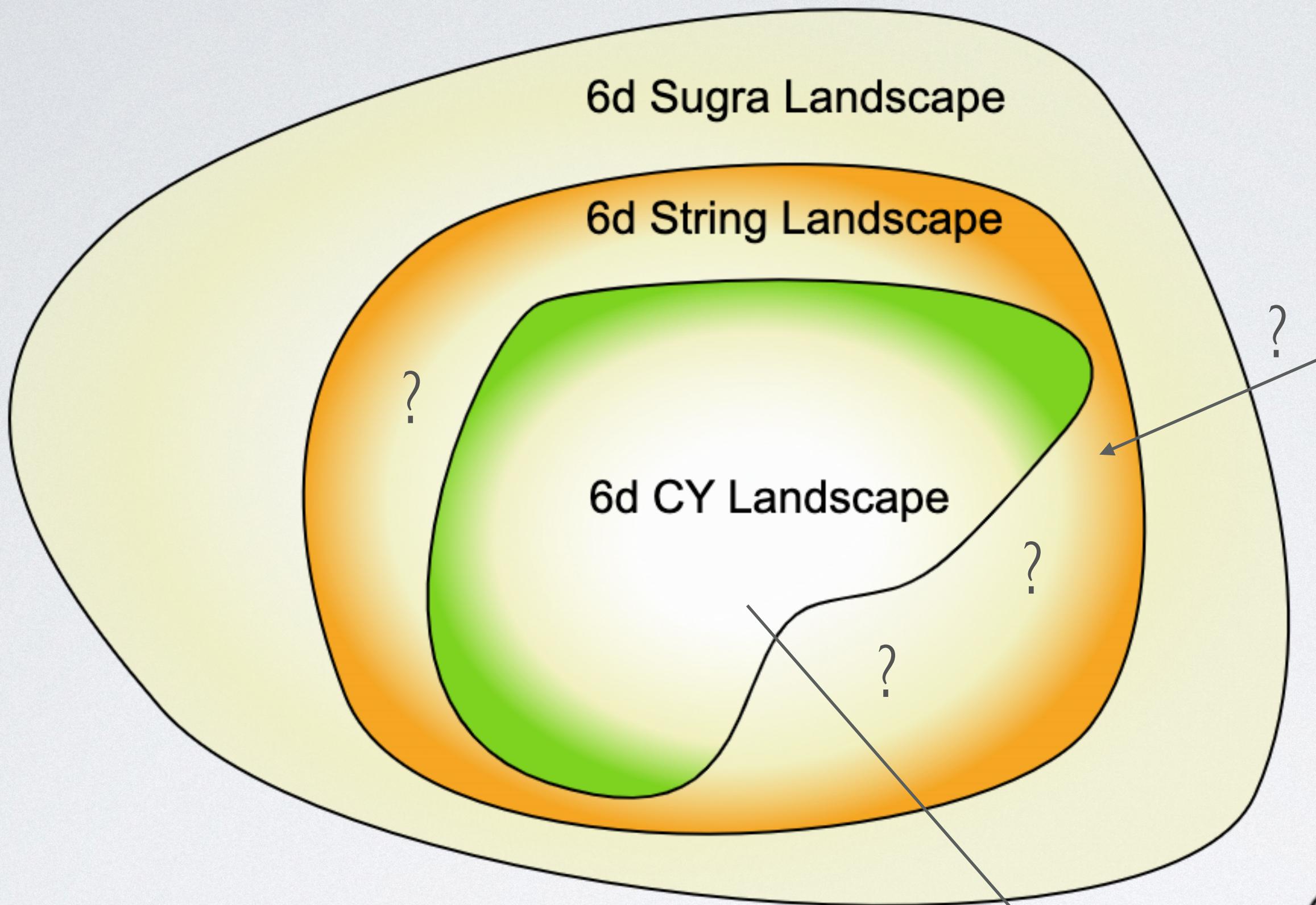




What is special about the “universal” hyper?

“Universal” Hypermultiplet: $Vol(B)$

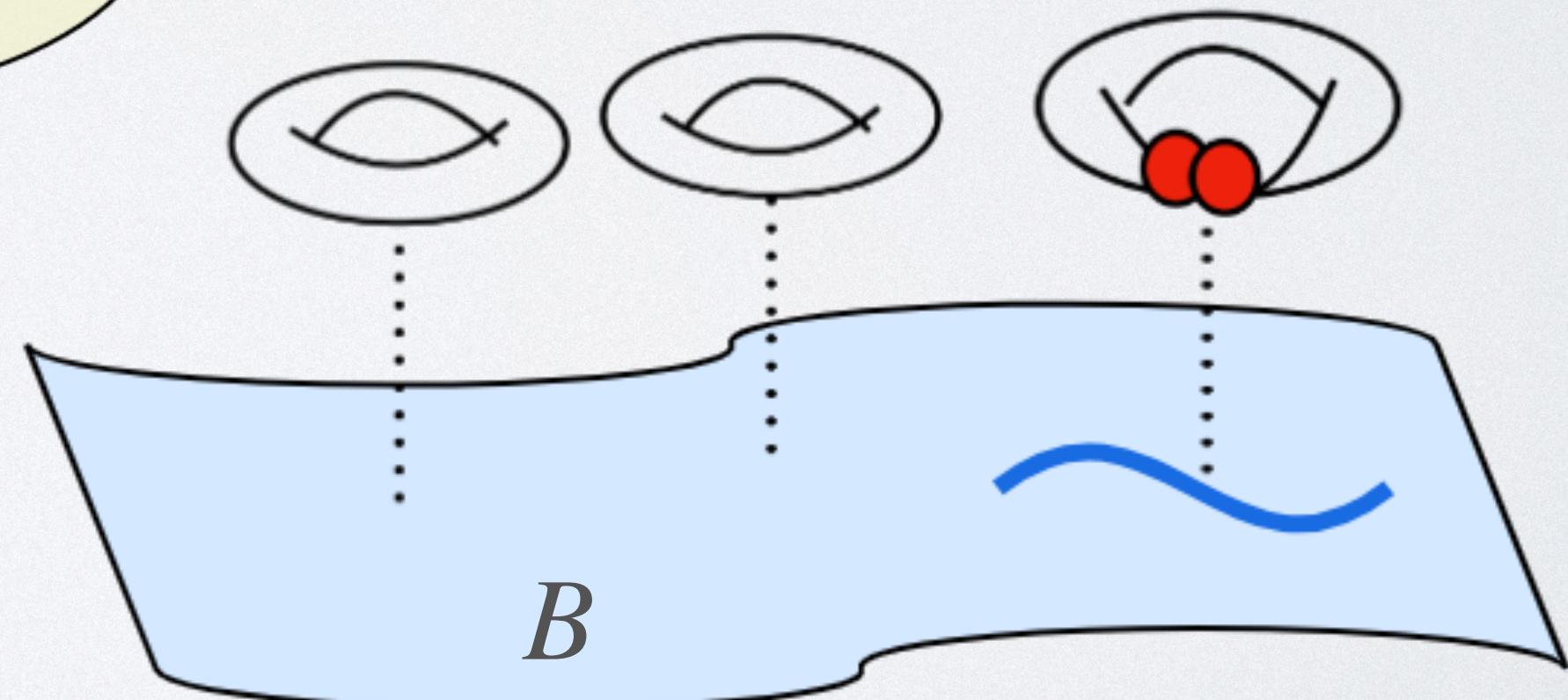


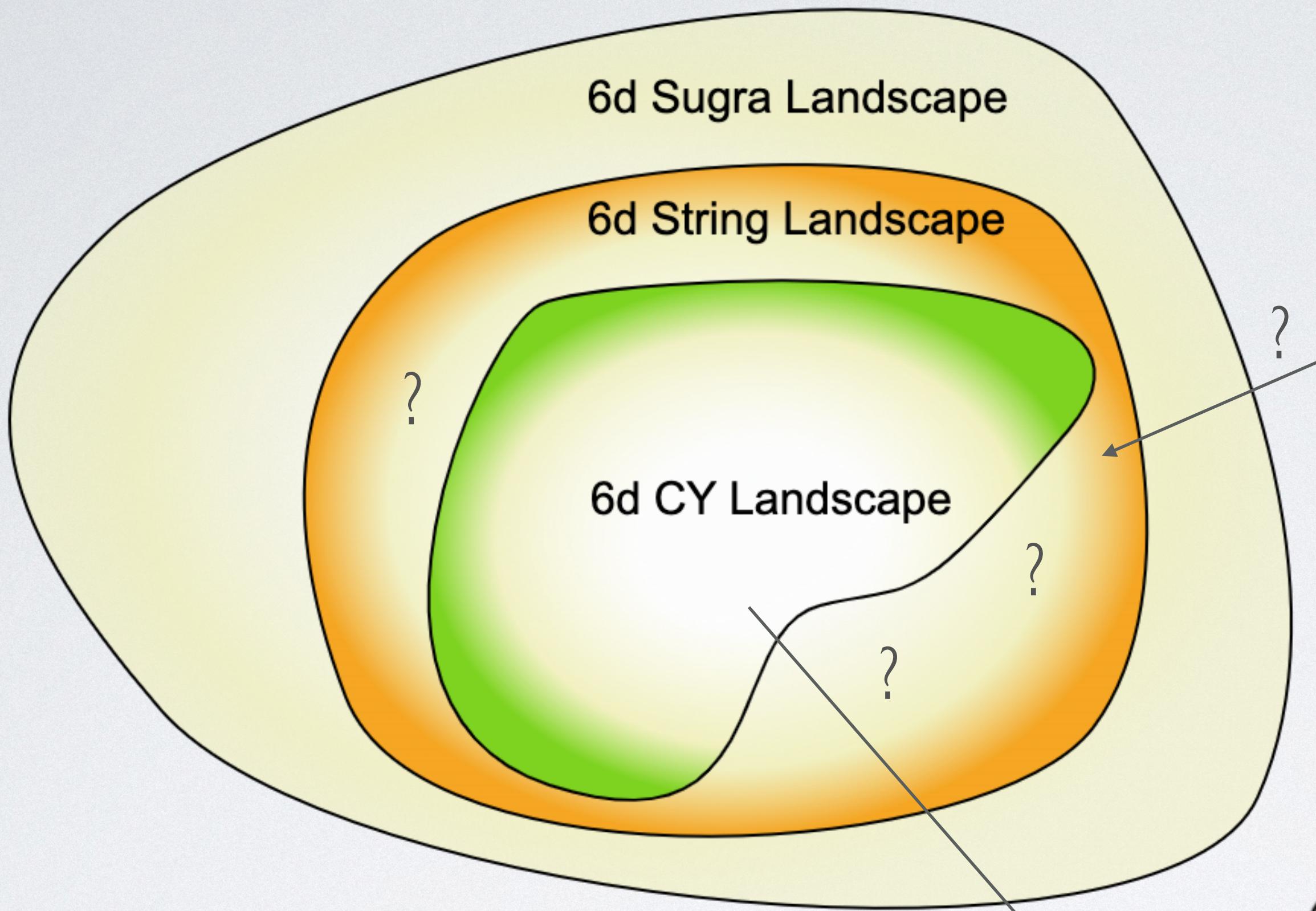


“Universal” Hypermultiplet: $Vol(B)$

$$R^4 : H_{neutral} + H_{charged} - V = 273 - 29T$$

Anomalies permit: $H_{neutral} = 0$



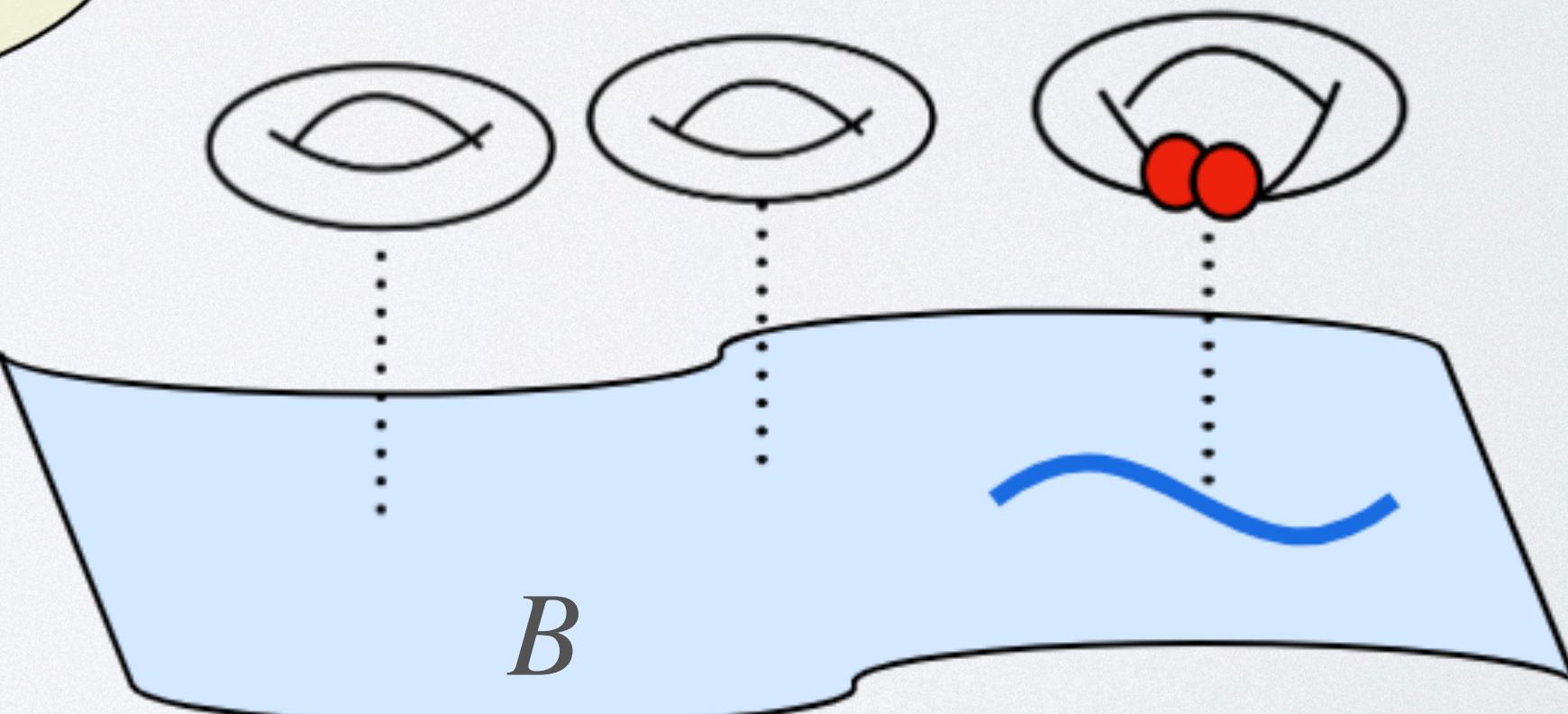


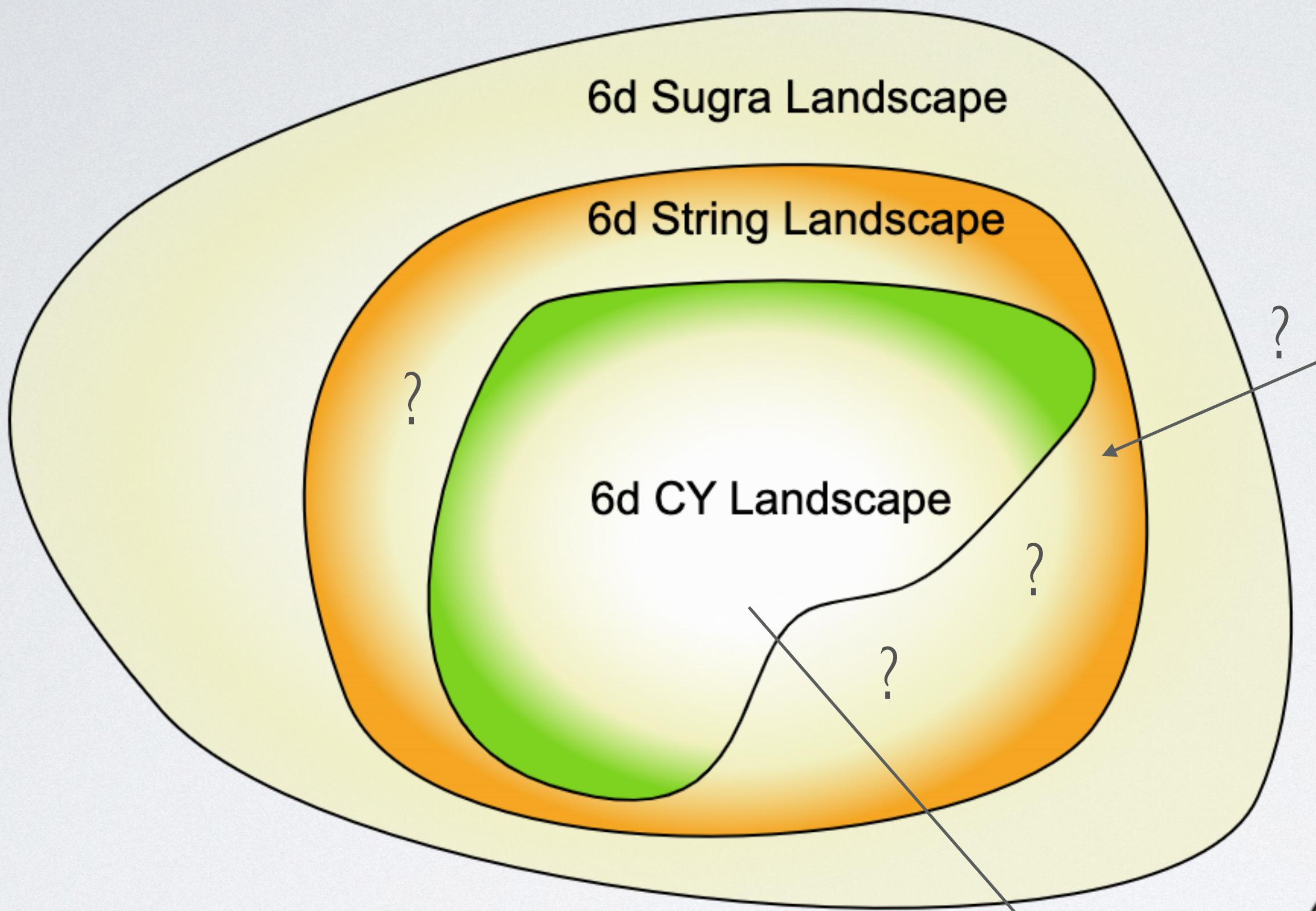
What is special about the “universal” hyper?

Nothing!

$$R^4 : H_{neutral} + H_{charged} - V = 273 - 29T$$

Anomalies permit: $H_{neutral} = 0$





$$R^4 : H_{neutral} + H_{charged} - V = 273 - 29T$$

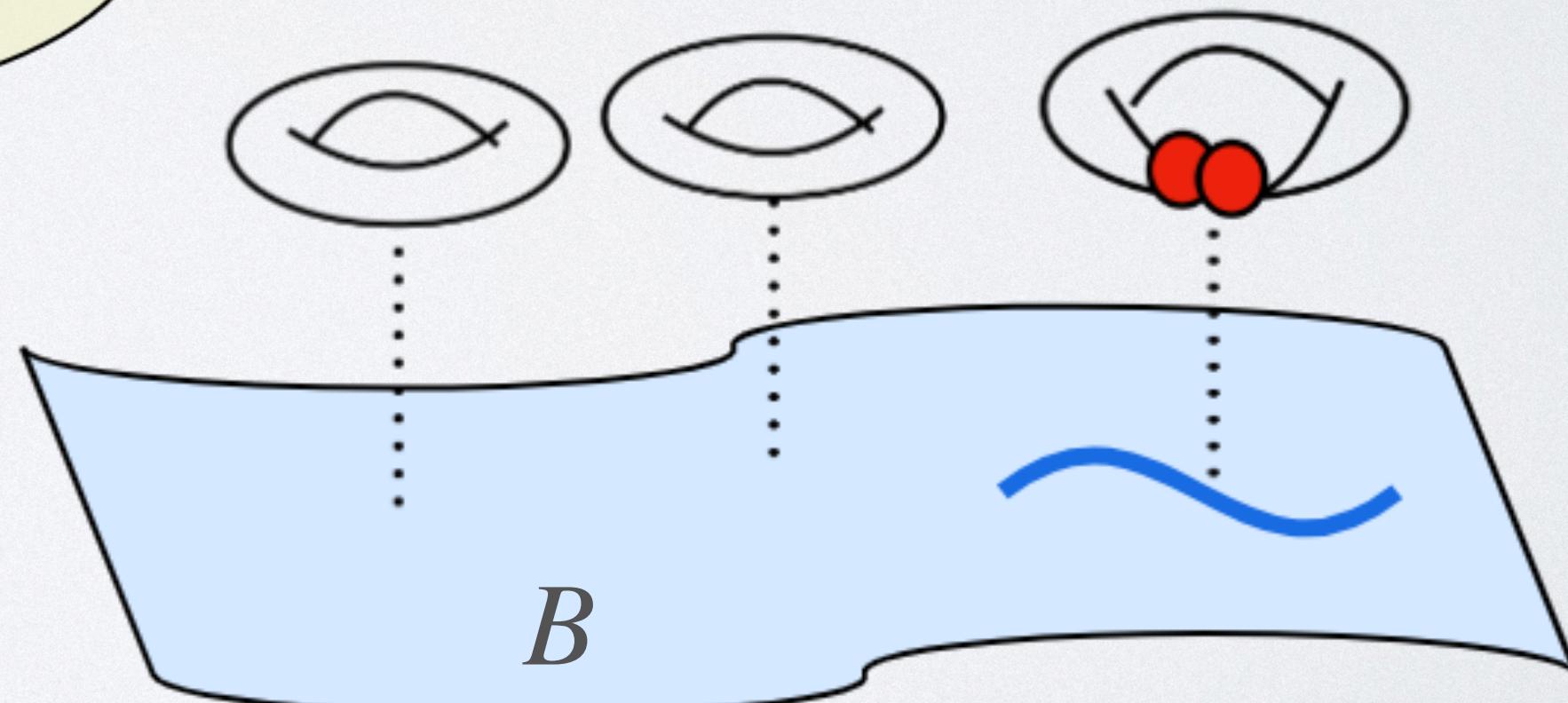
Anomalies permit: $H_{neutral} = 0$

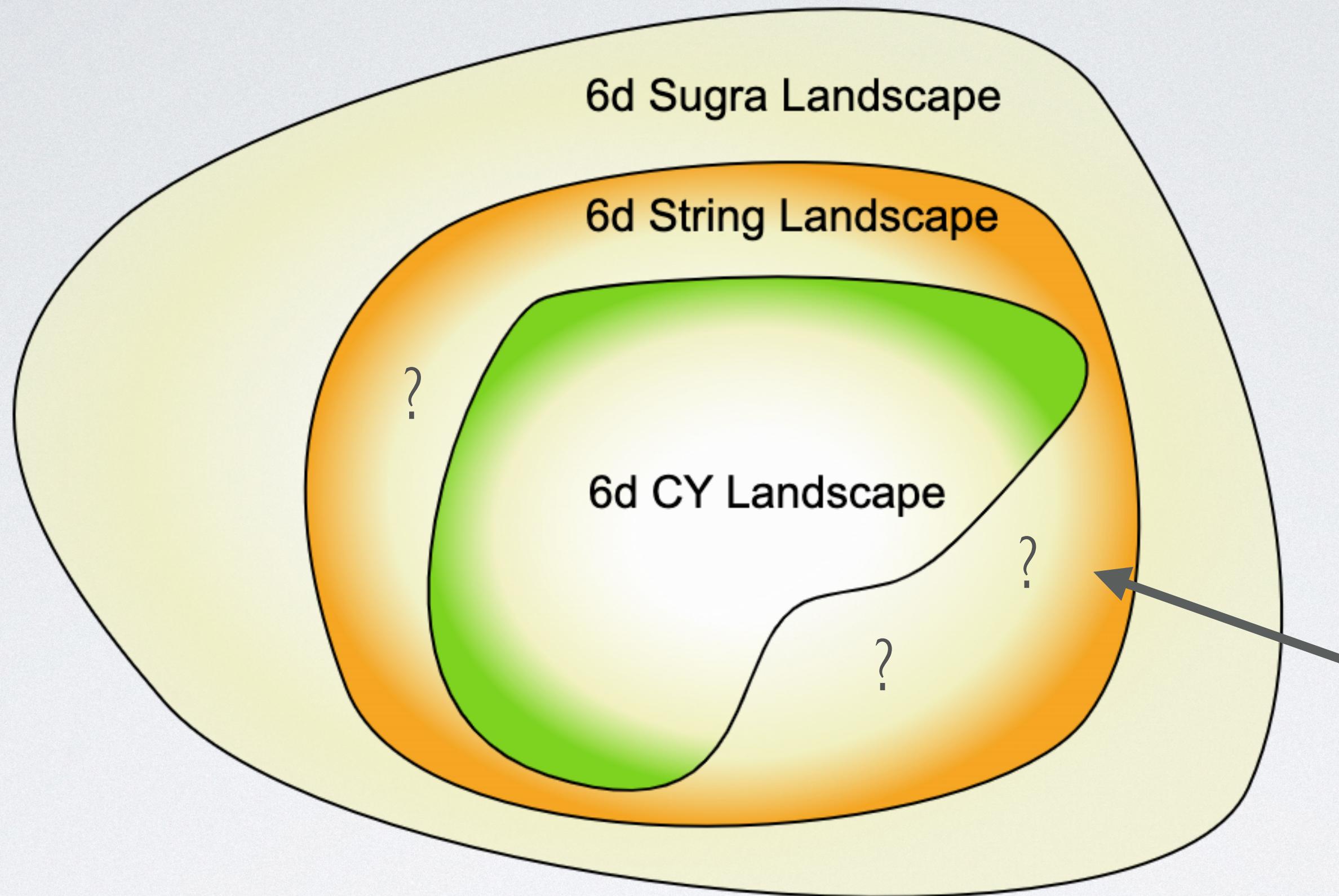
Can it become charged?

What is special about the “universal” hyper?

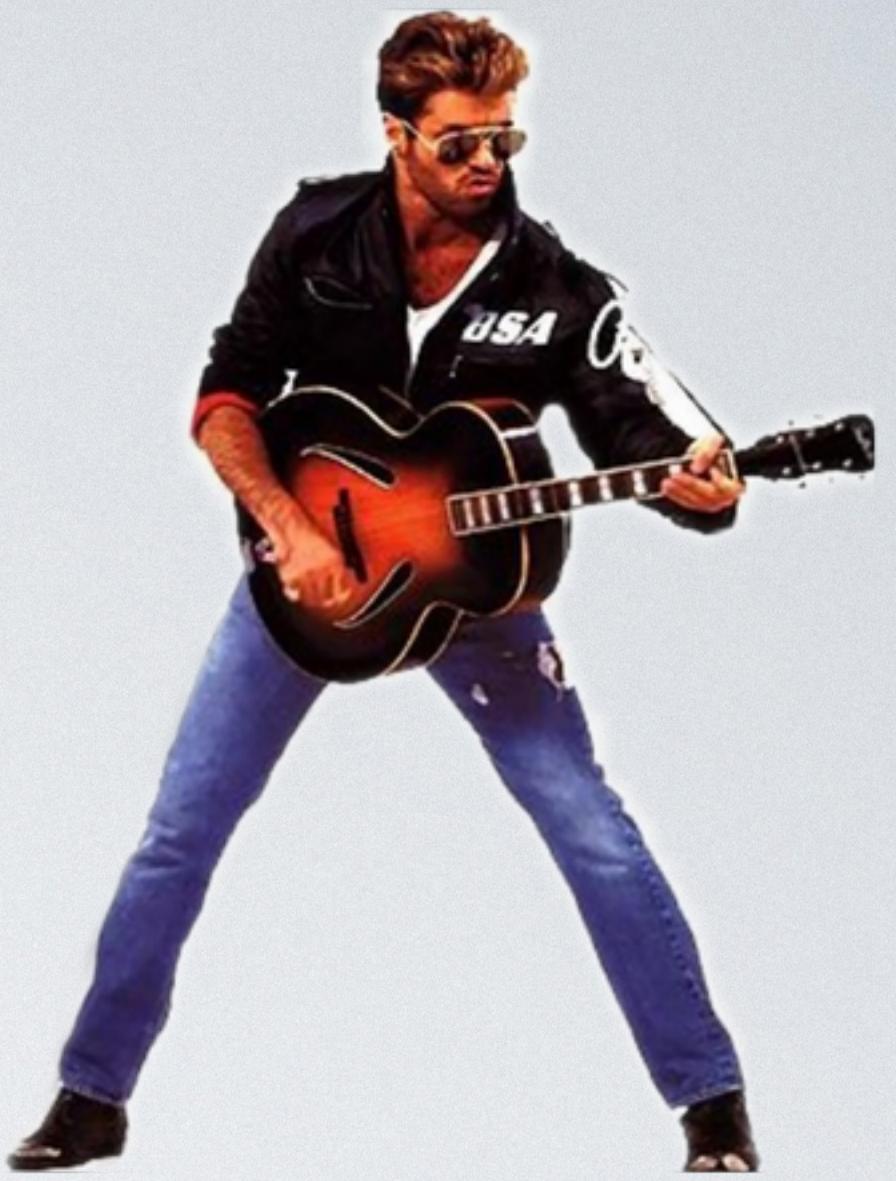
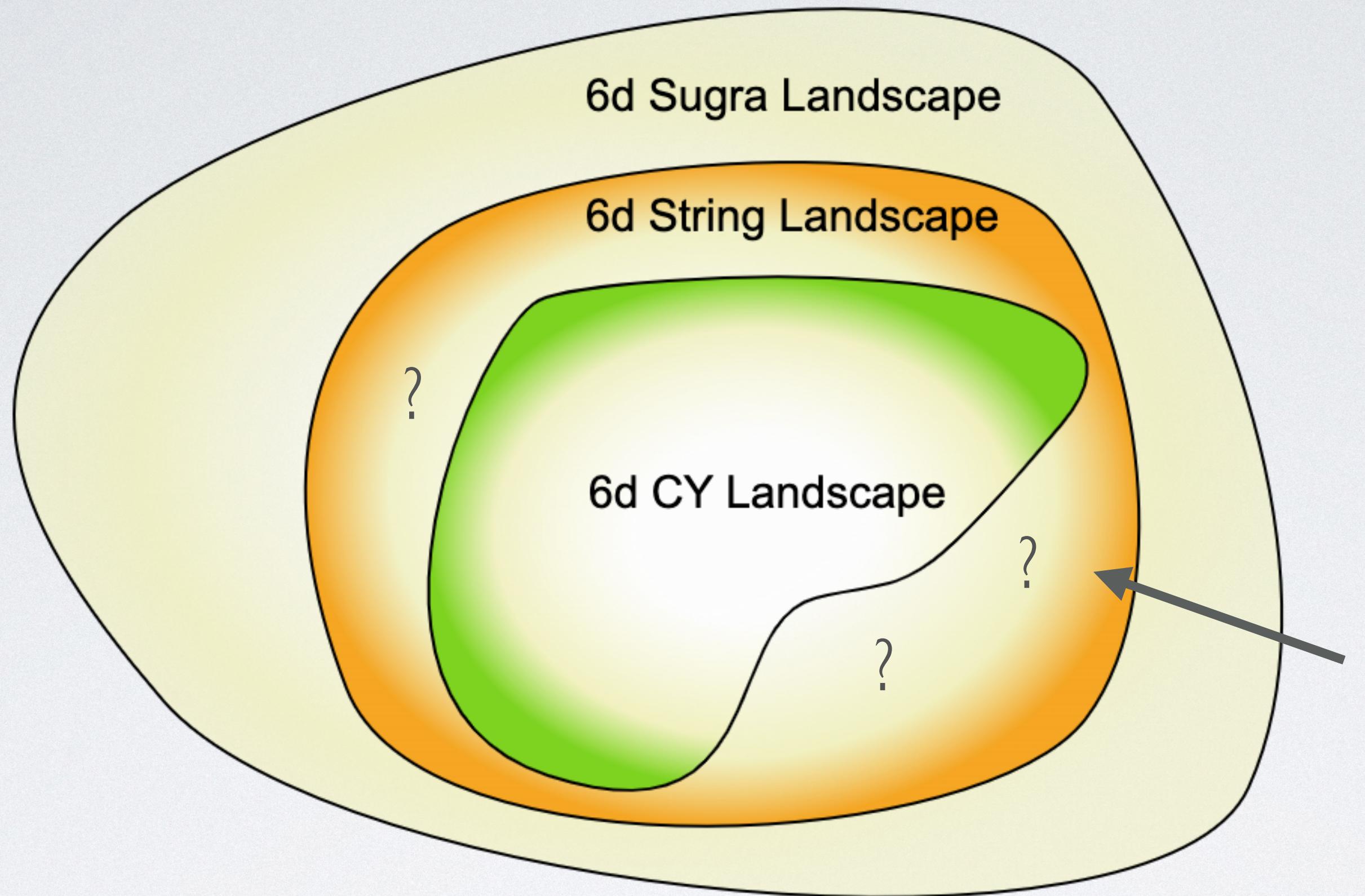
Nothing!

“Universal” Hypermultiplet: $Vol(B)$





"A different corner"



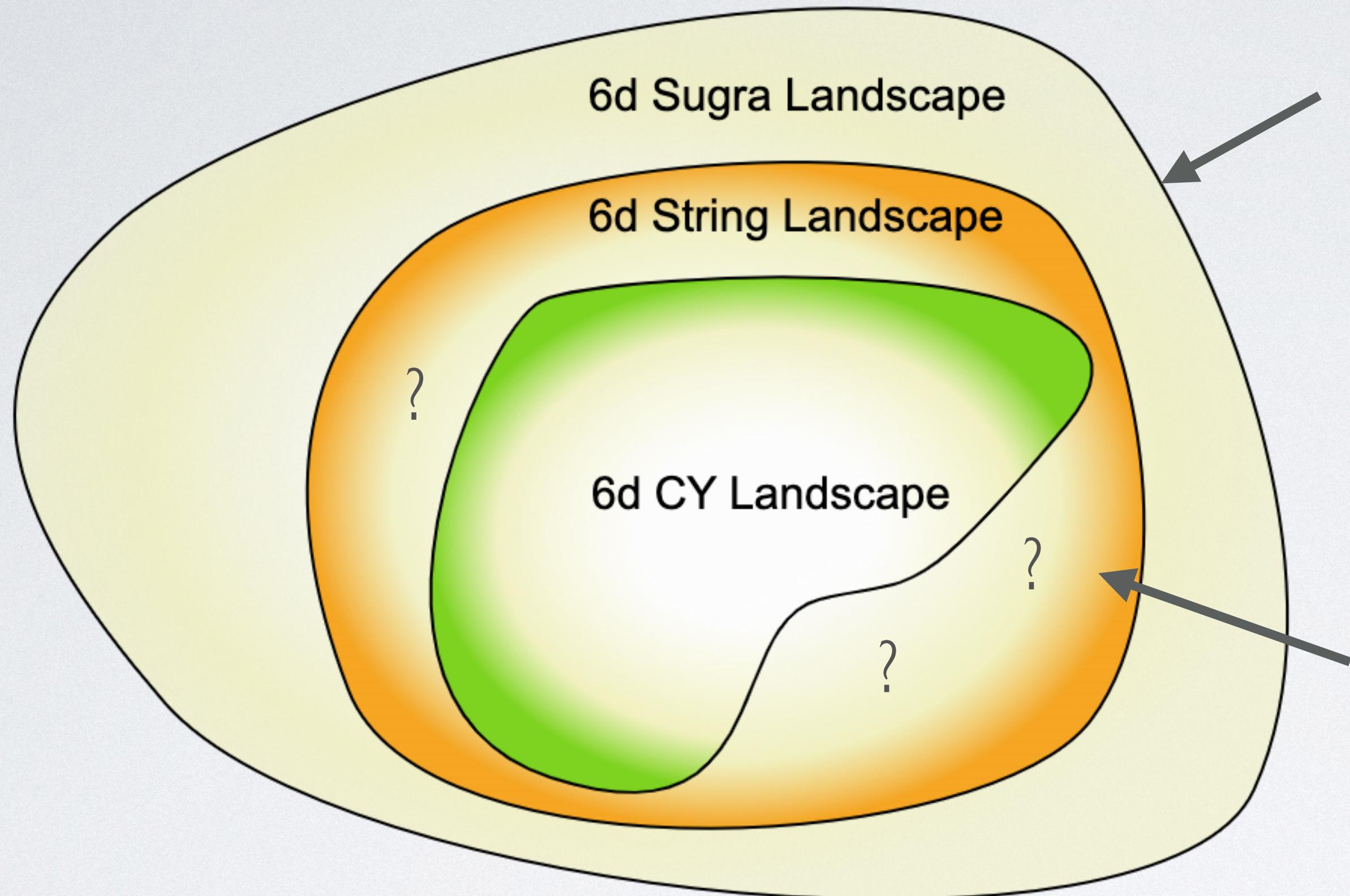
“A different corner”

Non-geometric models

**Asymmetric
Orbifolds**

$$H_{neutral} = 0$$

Sugra Questions



- Find universal consistency conditions

Is the Kodaira condition a Sugra condition ?

$$12 J \cdot a \geq \sum_i \nu_i J \cdot b_i$$

Non-geometric models

Asymmetric Orbifolds

Connection to geometry ?

Sugra Questions

- Find universal consistency conditions

Is the Kodaira condition a Sugra condition ?

Or

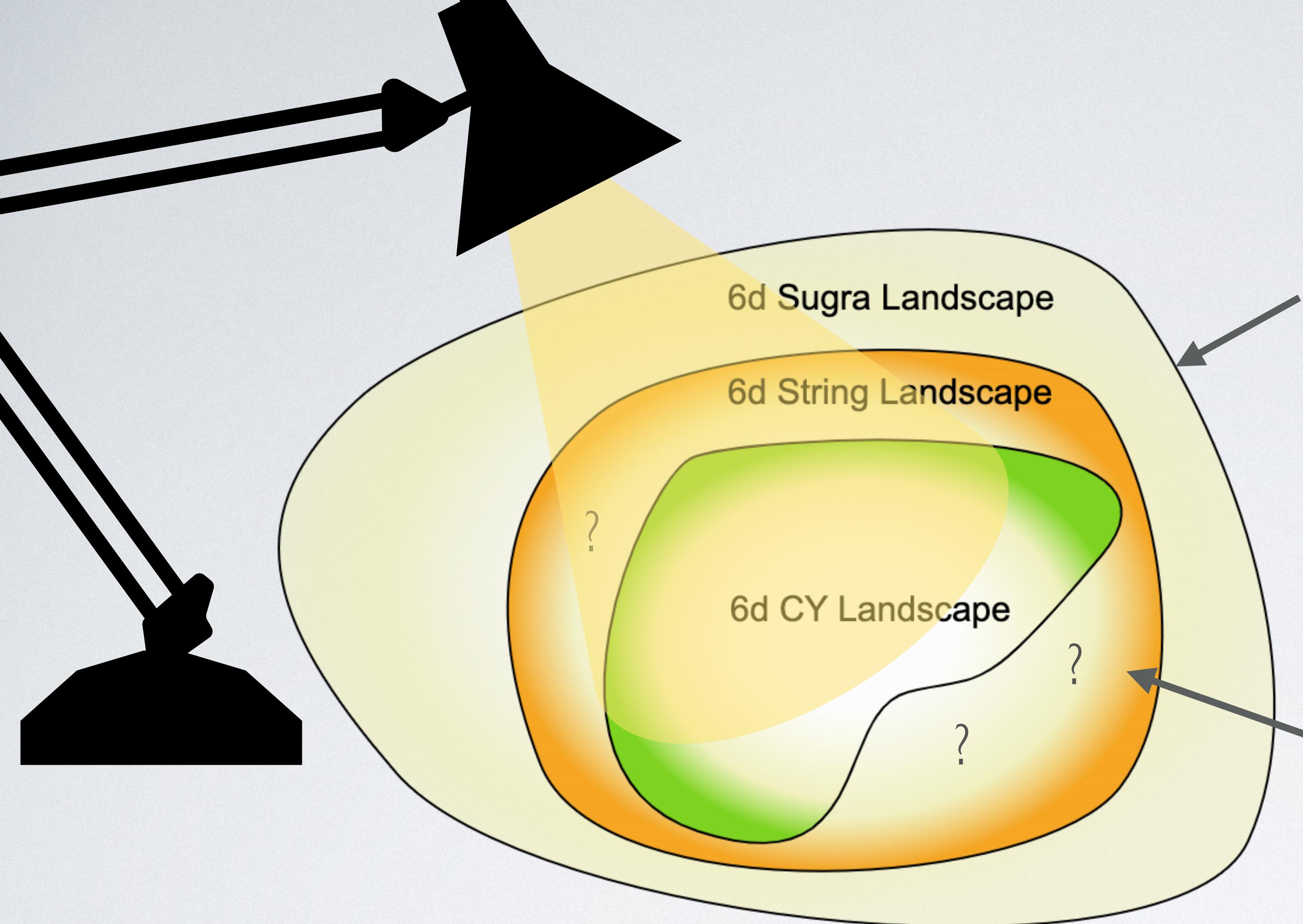
a CY Lamppost effect?

$$12 J \cdot a \geq \sum_i \nu_i J \cdot b_i$$

Non-geometric models

Asymmetric Orbifolds

Connection to geometry ?



Abelian Orbifolds

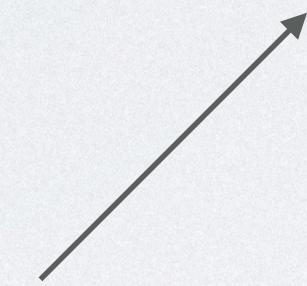
- Choose the starting point: IIA, IIB, Heterotic
- Choose even self-dual lattice: $\Gamma^{D,D}(\mathfrak{g}) = \{(p_L, p_R) | p_L \in \Lambda_W(\mathfrak{g}), p_R \in \Lambda_W(\mathfrak{g}), p_L - p_R \in \Lambda_R(\mathfrak{g})\}$

$$\Gamma^{D,D}(\mathfrak{g}) + \Gamma^{16,0}(E_8 \times E_8)$$

Abelian Orbifolds

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$$\Gamma^{D,D}(\mathfrak{g}) + \Gamma^{16,0}(E_8 \times E_8)$$



Lattice Automorphisms/crystallographic symmetries on T^D

Abelian Orbifolds

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 $\Gamma^{D,D}(\mathfrak{g}) + \Gamma^{16,0}(E_8 \times E_8)$
 - Choose the twist: $[g_L, g_R] = [\exp(2\pi i \phi_L), \exp(2\pi i \phi_R)]$
 - Choose the shift: (v_L, v_R)
- $|p_L, p_R\rangle \rightarrow e^{2\pi i(p_L \cdot v_L - p_R \cdot v_R)} |g_L \cdot p_L, g_R \cdot p_R\rangle$

Abelian Orbifolds

- Choose the starting point: IIA, IIB, Heterotic

- Choose even self-dual lattice: $\Gamma^{D,D}(\mathfrak{g}) = \{(p_L, p_R) | p_L \in \Lambda_W(\mathfrak{g}), p_R \in \Lambda_W(\mathfrak{g}), p_L - p_R \in \Lambda_R(\mathfrak{g})\}$

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$$\left. \begin{array}{c} \\ \\ \end{array} \right\} |p_L, p_R\rangle \rightarrow e^{2\pi i(p_L \cdot v_L - p_R \cdot v_R)} |g_L \cdot p_L, g_R \cdot p_R\rangle$$

$$R = L$$

**Symmetric
Orbifolds**

[Dixon, Harvey, Vafa, Witten 85'/86']

$$R \neq L$$

**Asymmetric
Orbifolds**

[Narain, Sarmadi, Vafa 87']

Abelian Orbifolds

- Choose the starting point: IIA, IIB, Heterotic
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$$\Gamma^{D,D}(\mathfrak{g}) + \Gamma^{16,0}(E_8 \times E_8)$$

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- Choose the shift: $v_{L,R}$

$$R = L$$

**Symmetric
Orbifolds**

$$R \neq L$$

**Asymmetric
Orbifolds**

Type II Asymmetric Orbifold

6d

$$\Gamma^{4,4}(D_4) = \{(p_L, p_R) \mid p_L \in \Lambda_W(D_4), p_R \in \Lambda_W(D_4), p_L - p_R \in \Lambda_R(D_4)\}$$

Type II Asymmetric Orbifold

6d

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$\mathcal{N} = 1$

$$[\exp(2\pi i \phi_L), \exp(2\pi i \phi_R)]$$

Preserve 8 supercharges

Break all right moving SUSY

$$\phi_R = (-1)^{F_R}$$

Type II Asymmetric Orbifold

6d

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Preserve 8 supercharges

Break all right moving SUSY

$$\phi_R = (-1)^{F_R}$$

$$\phi_L = \left(\frac{1}{2}, \frac{1}{2}\right)$$

Break half left moving SUSY

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6d

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Break half left moving SUSY

Spectrum

T
9

V
 $U(1)^{12}$

$$(\underline{\pm 1, 0, 0, 0}, 0^8) + (\pm, \pm, \pm, \pm, 0^8) \frac{1}{2} + (\underline{\pm, \mp, \mp, \mp}, 0^8) \frac{1}{2} + (\underline{-, -, +, +}, 0^8) \frac{1}{2}$$

$H_{charged}$

$H_{neutral}$

0

Type II Asymmetric Orbifold

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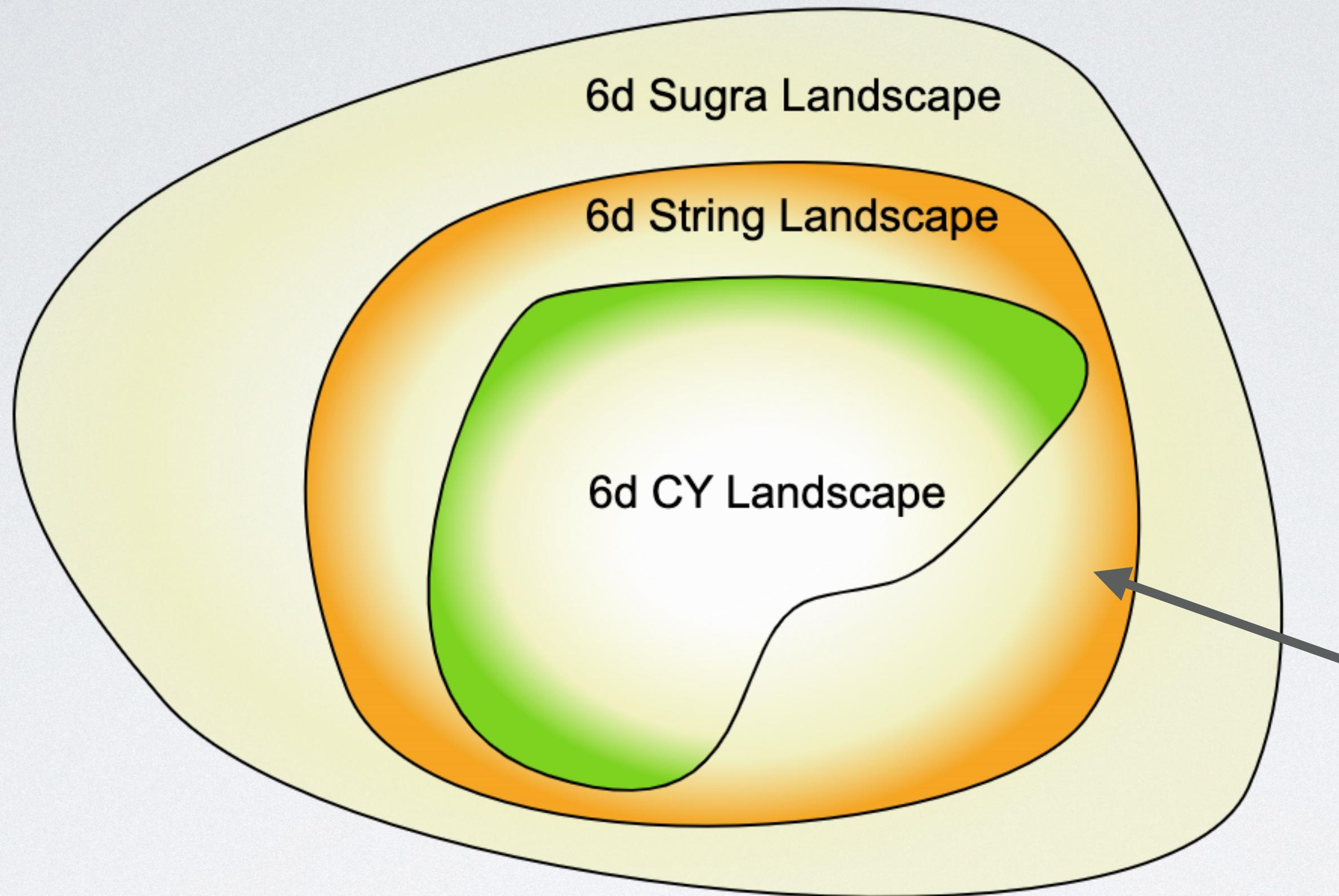
$$\phi_L = \left(\frac{1}{2}, \frac{1}{2}\right)$$

Break half left moving SUSY

$$\begin{matrix} & g_s \\ T & V \\ 9 & U(1)^{12} \end{matrix}$$

Spectrum

$$\begin{aligned} H_{charged} &= (\underline{\pm 1, 0, 0, 0}, 0^8) + (\pm, \pm, \pm, \pm, 0^8) \frac{1}{2} + (\underline{\pm, \mp, \mp, \mp}, 0^8) \frac{1}{2} + (\underline{-, -, +, +}, 0^8) \frac{1}{2} \\ H_{neutral} &= 0 \end{aligned}$$

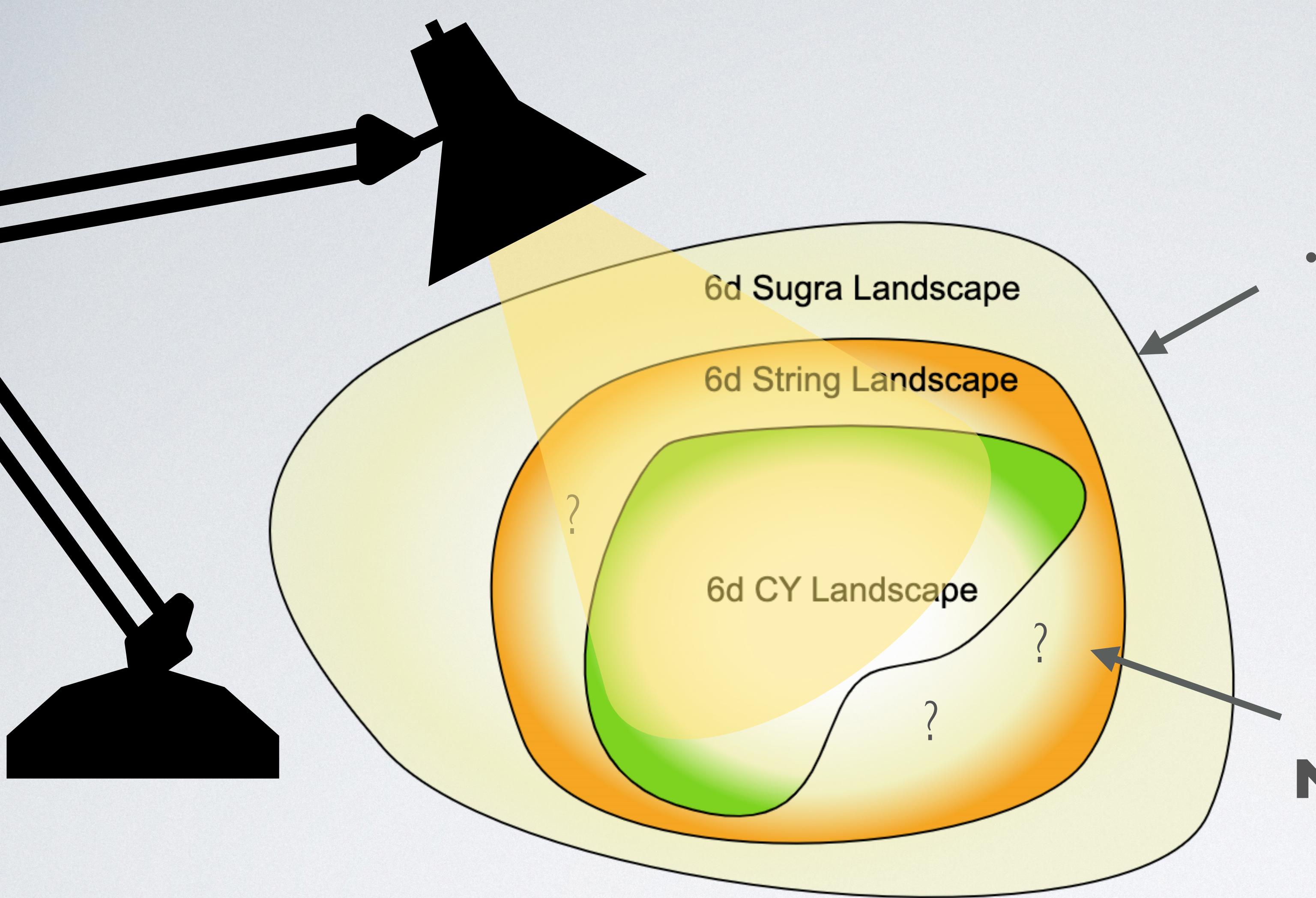


Non-geometric models

**Asymmetric
Orbifolds**



$$H_{neutral} = 0$$



Swampland Questions

- Find universal consistency conditions

Is the Kodaira condition a Sugra condition ?

Or

a Lamppost effect?

$$12 J \cdot a \geq \sum_i \nu_i J \cdot b_i$$

Non-geometric models

✓ **Asymmetric
Orbifolds**



Connection to geometry ?

Heterotic Asymmetric Orbifold

6d

$$\Gamma^{4,4}(A_2 \oplus A_2) + 2\Gamma^{8,0}(E_8)$$

$\mathcal{N} = 1$

$$[\exp(2\pi i\phi_L), \exp(2\pi i\phi_R)]$$

Preserve 8 supercharges

Break half right moving SUSY

$$\phi_R = \left(\frac{2}{3}, \frac{2}{3}\right) \quad \phi_L = (0,0)$$

$$V_L = \frac{1}{3}(1^6, 0^2; 0^8)$$

Heterotic Asymmetric Orbifold

6d

$$\Gamma^{4,4}(A_2 \oplus A_2) + 2\Gamma^{8,0}(E_8)$$

$\mathcal{N} = 1$

$$[\exp(2\pi i\phi_L), \exp(2\pi i\phi_R)]$$

Preserve 8 supercharges

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$$V_L = \frac{1}{3}(1^6, 0^2; 0^8)$$

Spectrum

T

V

1

$$E_6 \times SU(3) \times E_8 \times SU(3)^2$$

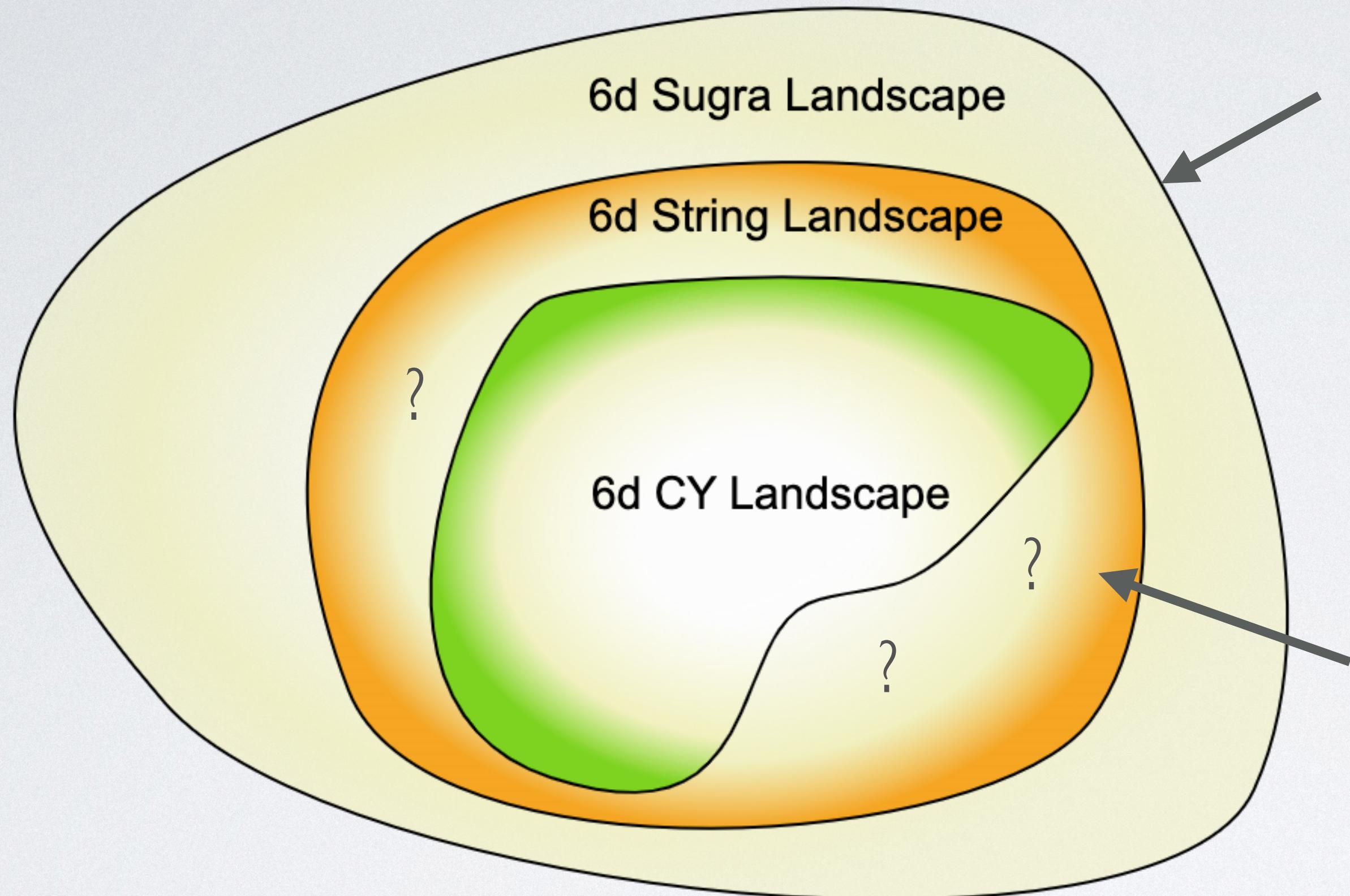
$H_{charged}$

$$\begin{aligned} & 2(27, 3, 1, 1, 1) + (27, 1, 1, \underline{3}, 1) + (27, 1, 1, \bar{3}, 1) \\ & + (1, 3, 1, 3, 3) + (1, 3, 1, \underline{3}, \bar{3}) + (1, 3, 1, \bar{3}, \bar{3}) \end{aligned}$$

$H_{neutral}$

0

Sugra Questions



- Find universal consistency conditions

Is the Kodaira condition a Sugra condition ?
Or
a Lamppost effect?

$$12 J \cdot a \geq \sum_i \nu_i J \cdot b_i$$

Non-geometric models

✓ **Asymmetric Orbifolds**



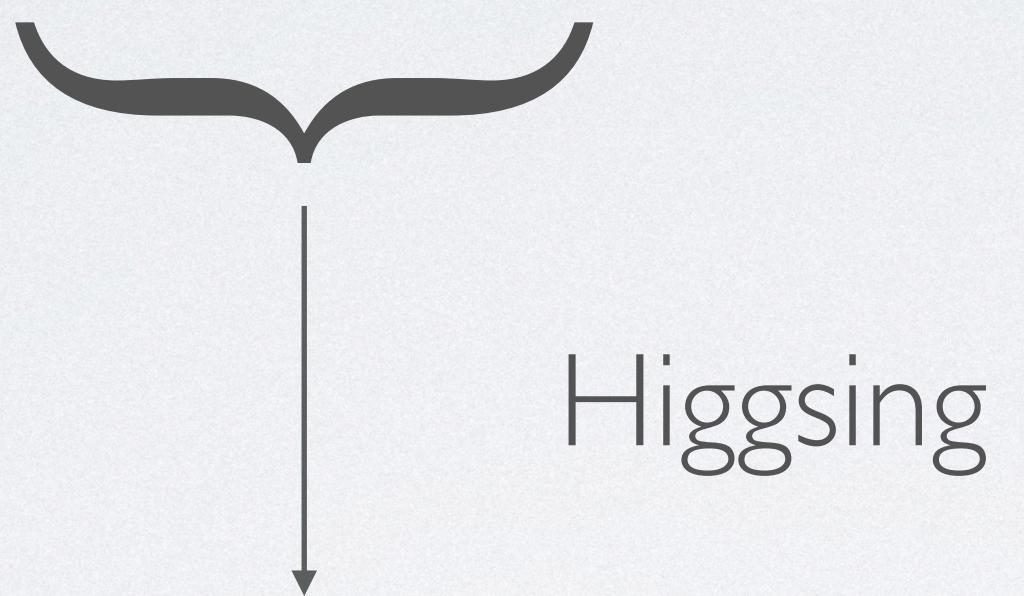
Connection to geometry ?

Heterotic Asymmetric Orbifold

Spectrum

T	V	$H_{charged}$	$H_{neutral}$
-----	-----	---------------	---------------

1	$E_6 \times SU(3) \times E_8 \times SU(3)^2$	$2(27, 3, 1, 1, 1) + (27, 1, 1, \underline{3}, \underline{1}) + (27, 1, 1, \bar{\underline{3}}, \underline{1})$ $+ (1, 3, 1, 3, 3) + (1, 3, 1, \underline{3}, \bar{\underline{3}}) + (1, 3, 1, \bar{\underline{3}}, \bar{\underline{3}})$	0
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T	V	$H_{charged}$	$H_{neutral}$
1	E_8	0	492

Heterotic Asymmetric Orbifold

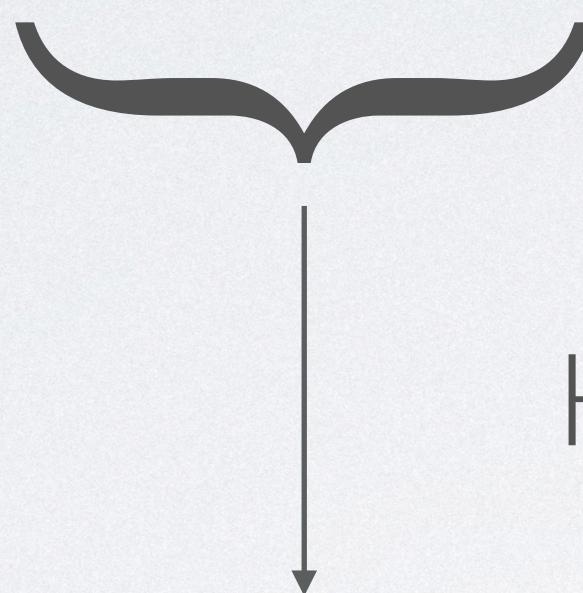
Spectrum

T	V	$H_{charged}$	$H_{neutral}$
-----	-----	---------------	---------------

$$1 \quad E_6 \times SU(3) \times E_8 \times SU(3)^2$$

$$\begin{aligned} & 2(27, 3, 1, 1, 1) + (27, 1, 1, \underline{3}, \underline{1}) + (27, 1, 1, \bar{\underline{3}}, \underline{1}) \\ & + (1, 3, 1, 3, 3) + (1, 3, 1, \underline{3}, \bar{\underline{3}}) + (1, 3, 1, \bar{\underline{3}}, \bar{\underline{3}}) \end{aligned}$$

$$0$$



Higgsing

T	V	$H_{charged}$	$H_{neutral}$
-----	-----	---------------	---------------

$$1 \quad E_8$$

$$0$$

$$492$$

Familiar?

Heterotic Asymmetric Orbifold

Spectrum

T	V	$H_{charged}$	$H_{neutral}$
-----	-----	---------------	---------------

$$1 \quad E_6 \times SU(3) \times E_8 \times SU(3)^2$$

$$2(27, 3, 1, 1, 1) + (27, 1, 1, \underline{3}, \underline{1}) + (27, 1, 1, \bar{\underline{3}}, \underline{1})$$

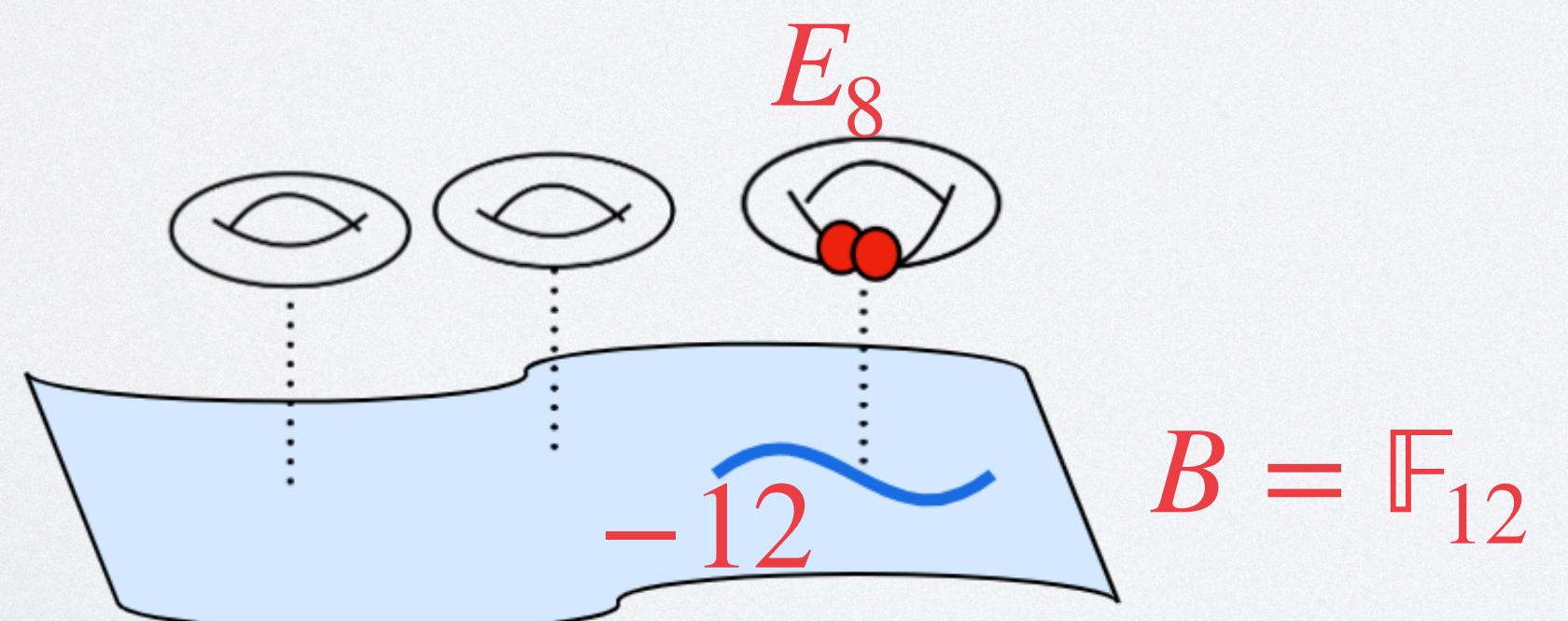
$$+ (1, 3, 1, 3, 3) + (1, 3, 1, \underline{3}, \bar{\underline{3}}) + (1, 3, 1, \bar{\underline{3}}, \bar{\underline{3}})$$



Higgsing
↓

T	V	$H_{charged}$	$H_{neutral}$
-----	-----	---------------	---------------

$$1 \quad E_8 \quad 0 \quad 492$$



Heterotic Asymmetric Orbifold

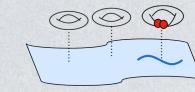
T	V	$H_{charged}$	$H_{neutral}$
1	$E_6 \times SU(3) \times E_8 \times SU(3)^2$	$2(27, 3, 1, 1, 1) + (27, 1, 1, \underline{3}, \underline{1}) + (27, 1, 1, \bar{\underline{3}}, \underline{1})$ $+(1, 3, 1, 3, 3) + (1, 3, 1, \underline{3}, \bar{\underline{3}}) + (1, 3, 1, \bar{\underline{3}}, \bar{\underline{3}})$	0
↓ Higgsing			
Calabi-Yau threefold with base \mathbb{F}_{12}			
T	V	$H_{charged}$	$H_{neutral}$
1	E_8	0	492
↓ Duality			
Heterotic on K3 with Instanton number (0,24)			

[9505105]

Kachru,Vafa

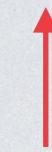
T^2
4d

Transitions

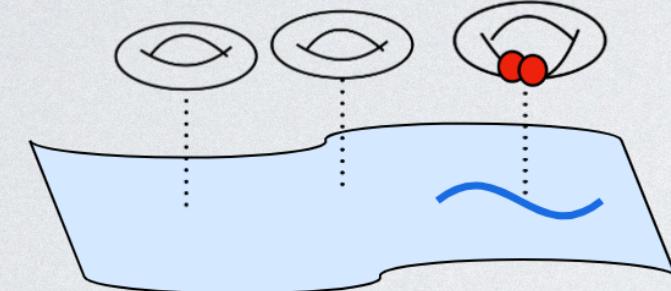


Conifold like

$g_S \rightarrow \infty$



$Vol(B) \rightarrow 0$



Calabi-Yau threefold with base \mathbb{F}_{12}



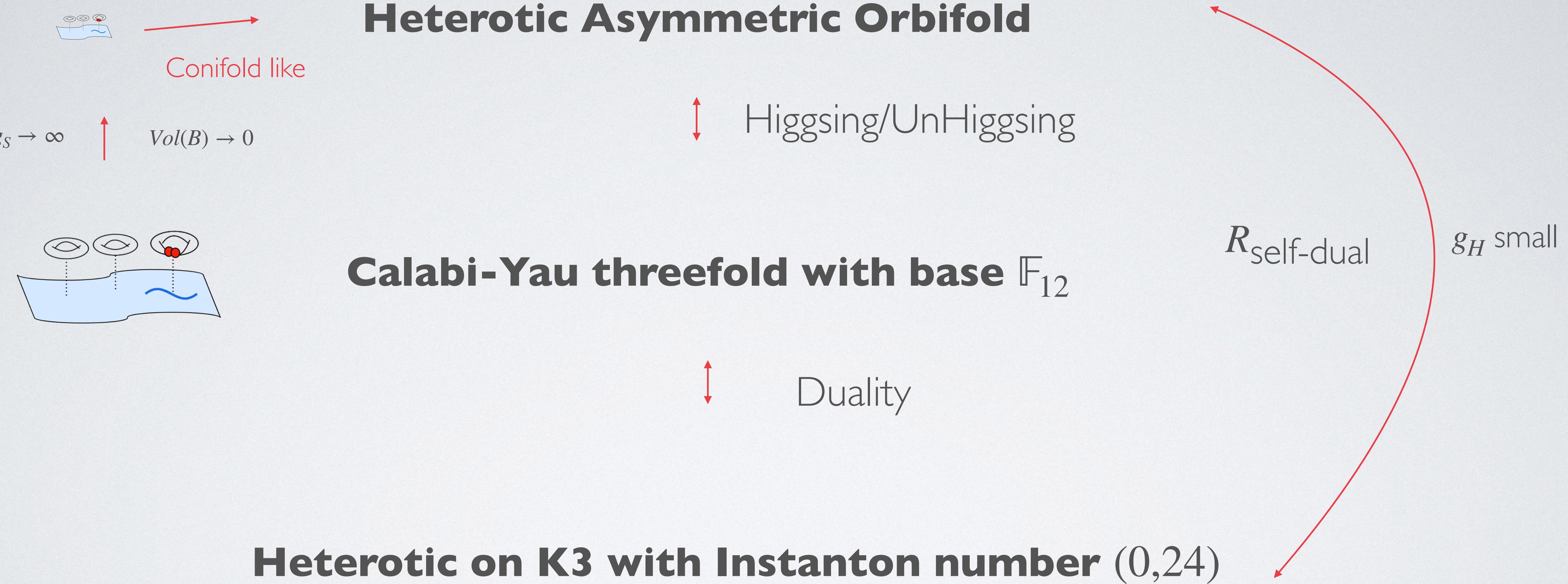
Higgsing/UnHiggsing



Duality

Heterotic on K3 with Instanton number (0,24)

Transitions



$$\Gamma^{4,4}(D_4)$$

$$\phi_R = (-1)^{F_R} \quad \phi_L = (\frac{1}{2}, \frac{1}{2})$$

Type II AO

$$\Gamma^{4,4}(A_2 \oplus A_2) + 2\Gamma^{8,0}(E_8)$$

$$\phi_R = (\frac{2}{3}, \frac{2}{3})$$

$$V_L = \frac{1}{3}(1^6, 0^2; 0^8)$$

Heterotic AO1

$$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$$

$$\phi_R = (\frac{1}{2}, \frac{1}{2})$$

$$V_L = \frac{1}{2}(1^2, 0^6; 1^2, 0^6)$$

Heterotic AO2

$$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$$

$$\phi_R = (\frac{1}{2}, \frac{1}{2})$$

$$E_8 \leftrightarrow E_8$$

Heterotic AO3

$$\Gamma^{4,4}(D_4)$$

$$\phi_R = (-1)^{F_R} \quad \phi_L = (\frac{1}{2}, \frac{1}{2})$$

Type II AO

$$U(1)^{12} + H_c$$

$$\Gamma^{4,4}(A_2 \oplus A_2) + 2\Gamma^{8,0}(E_8)$$

$$\phi_R = (\frac{2}{3}, \frac{2}{3})$$

$$\phi_L = (0,0)$$

$$V_L = \frac{1}{3}(1^6, 0^2; 0^8)$$

Heterotic AO1

$$E_6 \times SU(3) \times E_8 \times SU(3)^2 + H_c$$

$$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$$

$$\phi_R = (\frac{1}{2}, \frac{1}{2})$$

$$\phi_L = (0,0)$$

$$V_L = \frac{1}{2}(1^2, 0^6; 1^2, 0^6)$$

Heterotic AO2

$$E_7 \times SU(2) \times E_7 \times SU(2) \times SO(8) + H_c$$

$$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$$

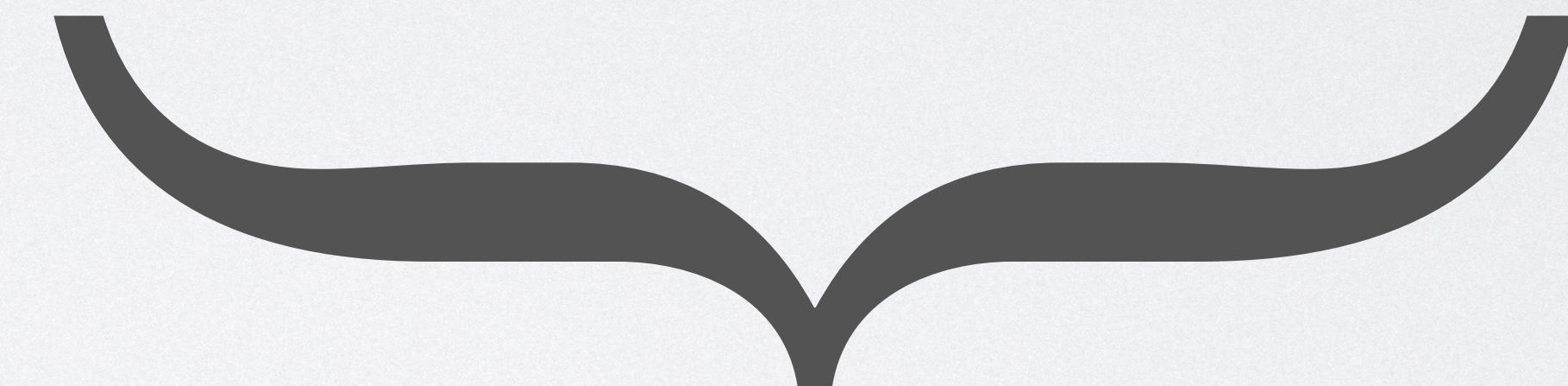
$$\phi_R = (\frac{1}{2}, \frac{1}{2})$$

$$\phi_L = (0,0)$$

$$E_8 \leftrightarrow E_8$$

Heterotic AO3

$$E_8 \times SO(8) + H_c$$



Kodaira  condition

$$\Gamma^{4,4}(D_4)$$

$$\phi_R = (-1)^{F_R} \quad \phi_L = (\frac{1}{2}, \frac{1}{2})$$

Type II AO

$$U(1)^{12} + H_c$$

$$\Gamma^{4,4}(A_2 \oplus A_2) + 2\Gamma^{8,0}(E_8)$$

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Heterotic AO1

$$E_6 \times SU(3) \times E_8 \times SU(3)^2 + H_c$$



$$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$$

$$\phi_R = (\frac{1}{2}, \frac{1}{2})$$

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Heterotic AO2

$$E_7 \times SU(2) \times E_7 \times SU(2) \times SO(8) + H_c$$



$$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$$

$$\phi_R = (\frac{1}{2}, \frac{1}{2})$$

$$\phi_L = (0,0)$$

$$E_8 \leftrightarrow E_8$$

Heterotic AO3

$$E_8 \times SO(8) + H_c$$



Calabi-Yau dP_9

Calabi-Yau \mathbb{F}_{12}

Calabi-Yau \mathbb{F}_0

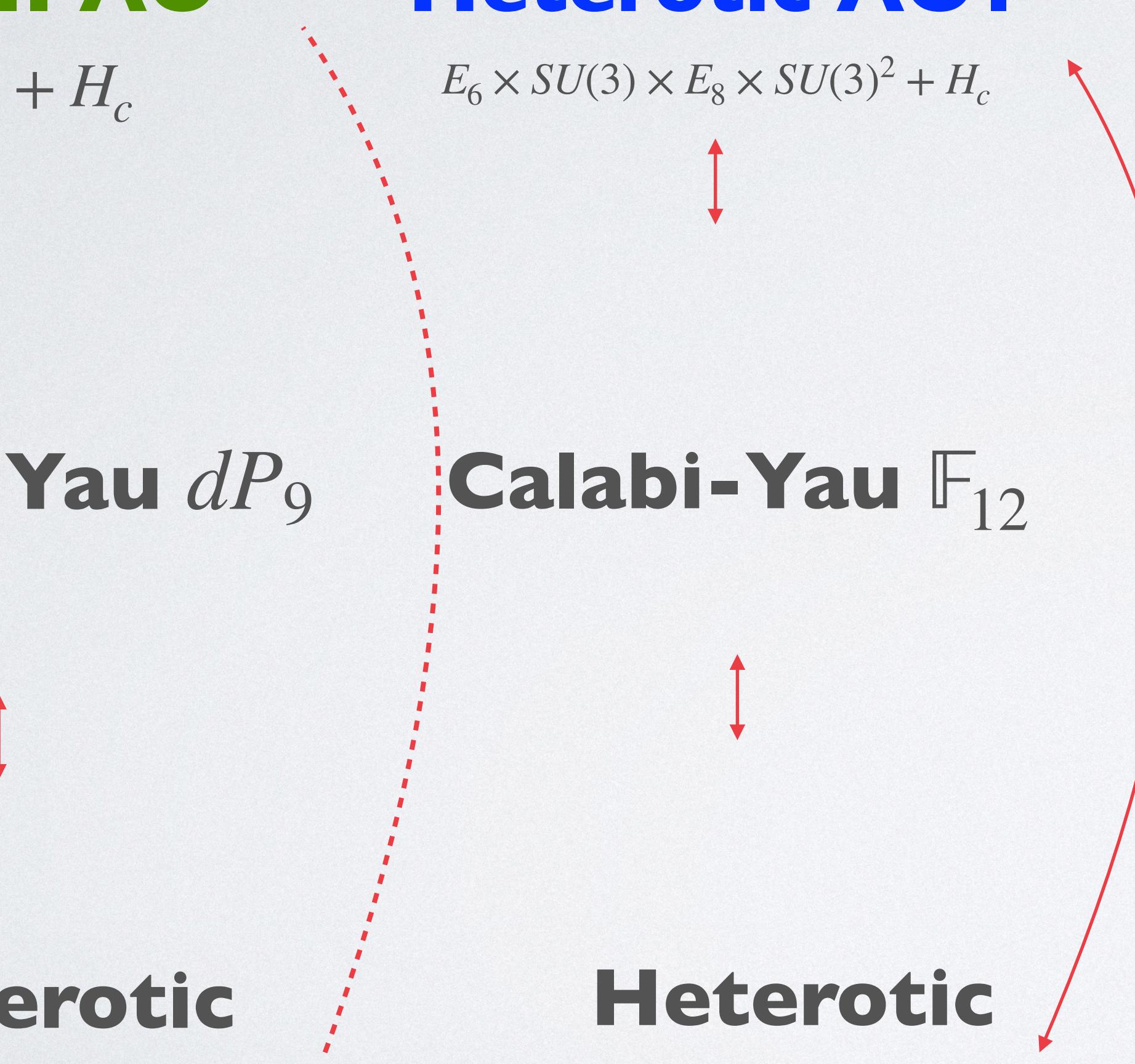
Calabi-Yau \mathbb{F}_3

**Heterotic
K3+ NS5 branes**

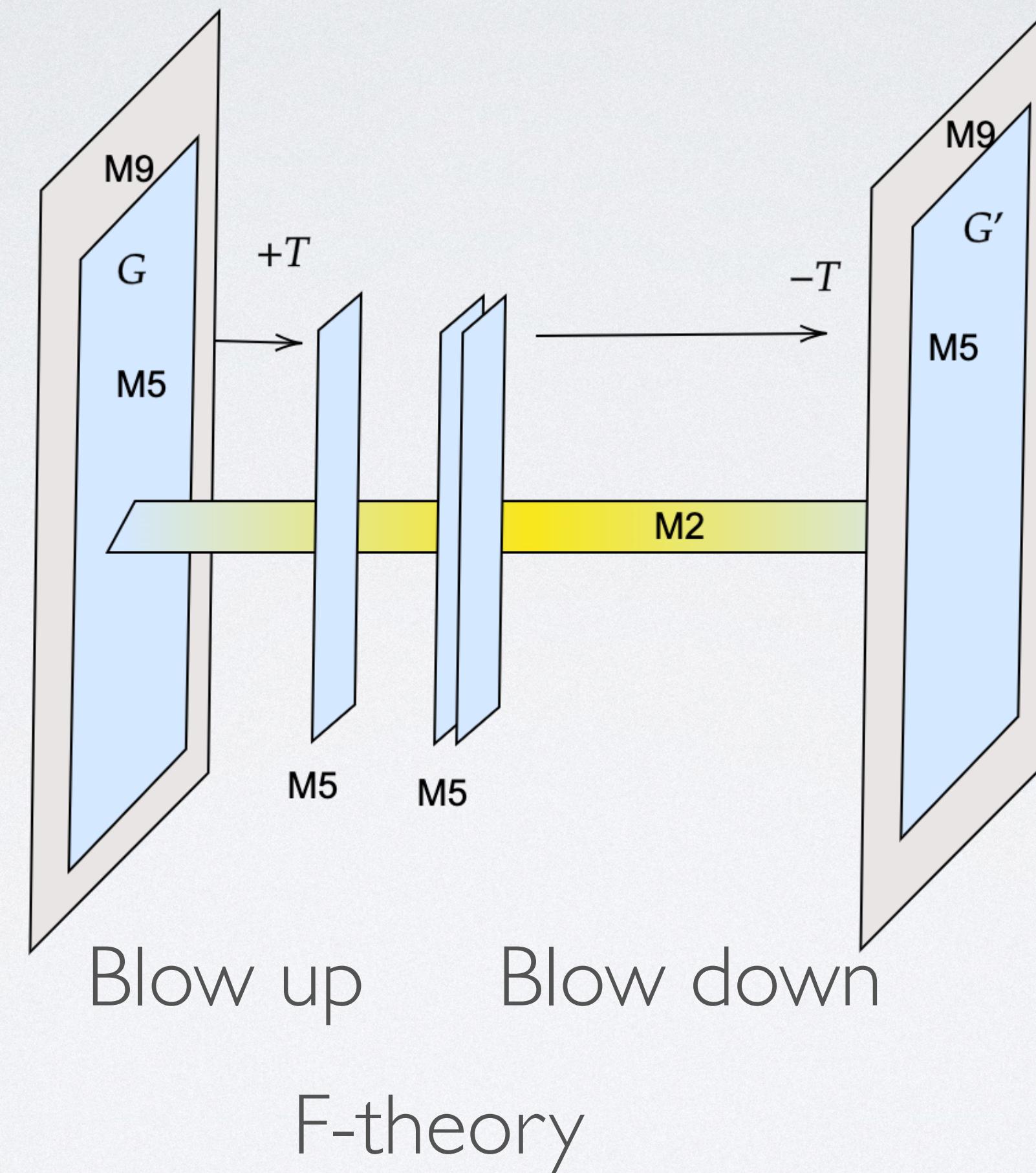
**Heterotic
K3 (0,24)**

**Heterotic
K3 (12,12)**

**Heterotic
K3 (9,15)**



M-theory on $K3 \times S^1/\mathbb{Z}_2$ Transitions



Type II AO

$$U(1)^{12} + H_c$$

Calabi-Yau dP_9

Heterotic
K3+ NS5 branes

Heterotic AO1

$$E_6 \times SU(3) \times E_8 \times SU(3)^2 + H_c$$

Calabi-Yau \mathbb{F}_{12}

Heterotic
K3 (0,24)

Heterotic AO2

$$E_7 \times SU(2) \times E_7 \times SU(2) \times SO(8) + H_c$$

Calabi-Yau \mathbb{F}_0

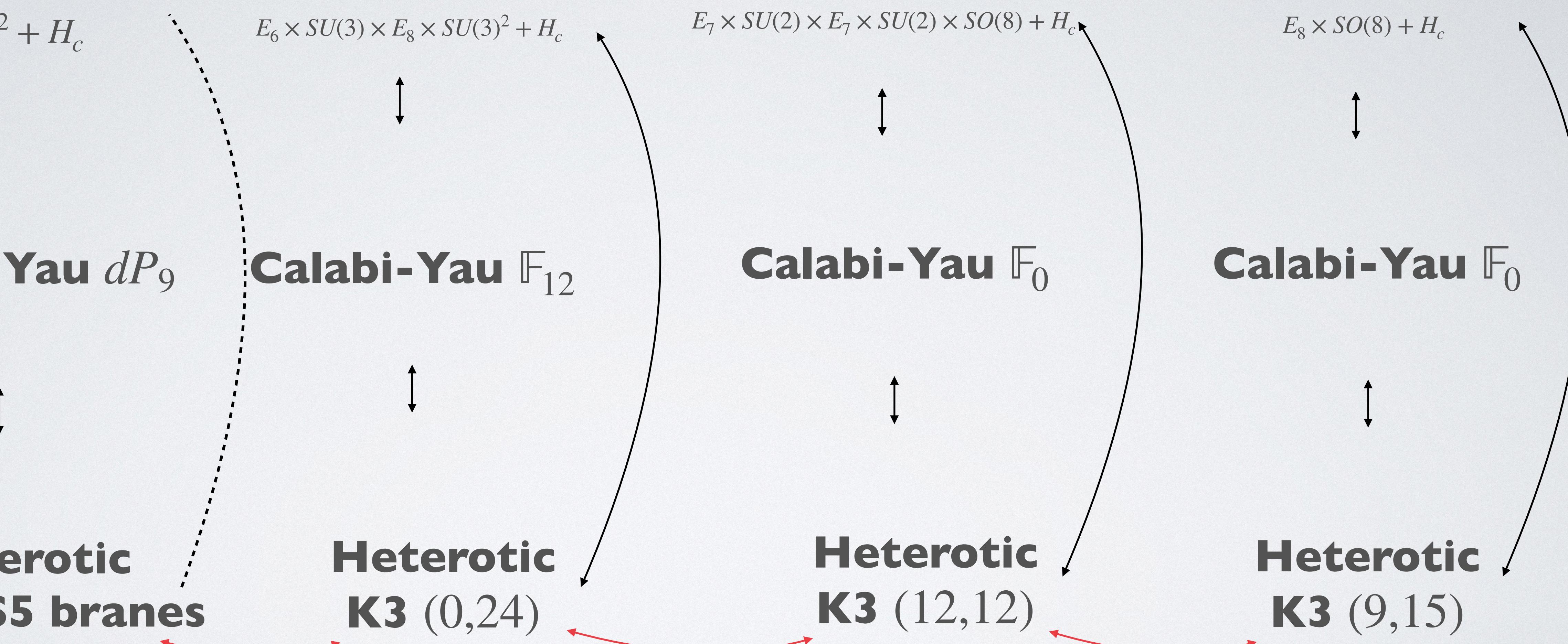
Heterotic
K3 (12,12)

Heterotic AO3

$$E_8 \times SO(8) + H_c$$

Calabi-Yau \mathbb{F}_0

Heterotic
K3 (9,15)



Consider theories on S^1 with Wilson lines

6d

Type II AO

$$U(1)^{12} + H_c$$
$$T = 9$$

5d on Coulomb branch

Heterotic AO1

$$E_6 \times SU(3) \times E_8 \times SU(3)^2 + H_c$$
$$T = 1$$

$$U(1)^{22}$$

Heterotic AO2

$$E_7 \times SU(2) \times E_7 \times SU(2) \times SO(8) + H_c$$
$$T = 1$$



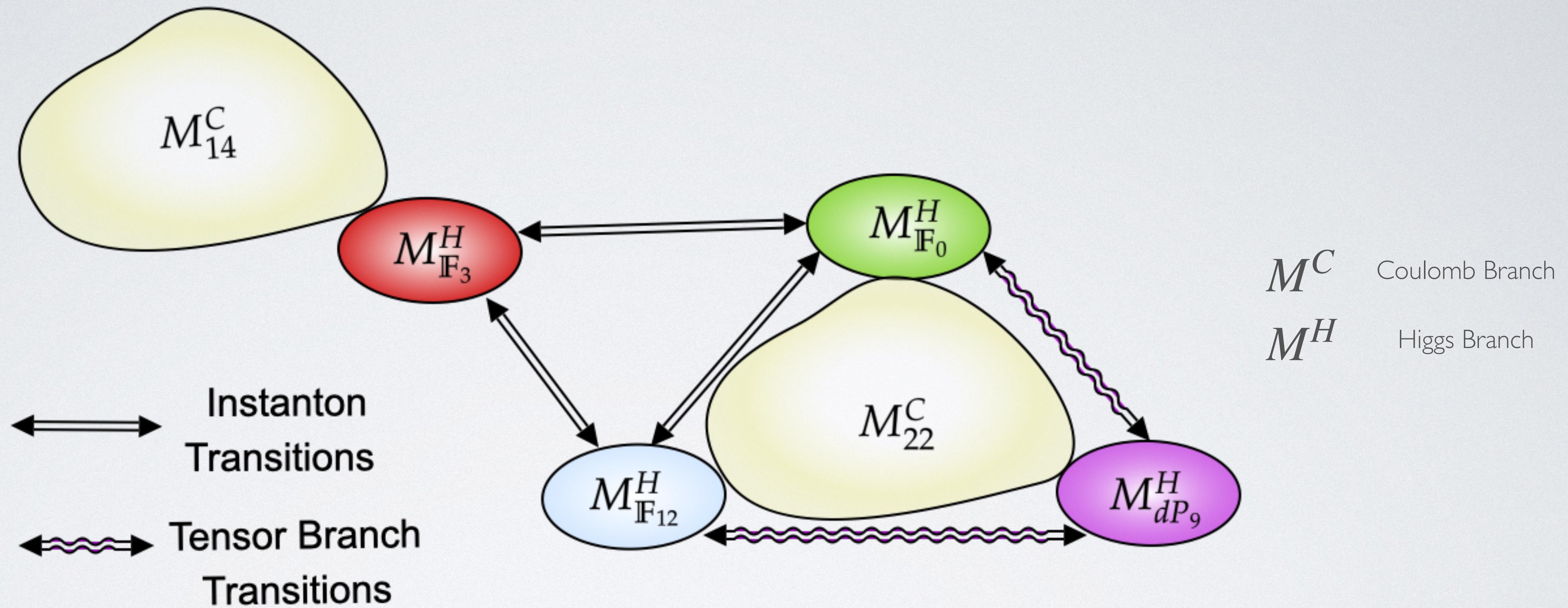
Heterotic AO3

$$E_8 \times SO(8) + H_c$$
$$T = 1$$

$$U(1)^{14}$$



Connectedness of String Vacua



More 5d models with no hypers ?

Freely Acting Orbifolds

Type II AO

$$\Gamma^{5,5} = \Gamma^{4,4} + \Gamma^{1,1}$$

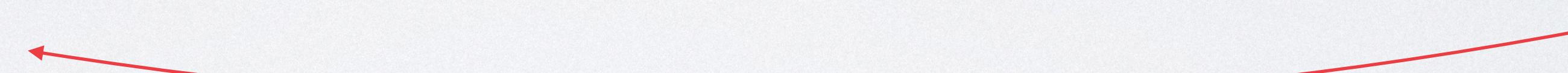
$$\begin{array}{ccc} \uparrow & & \uparrow \\ \mathbb{Z}_N \text{ twist} & & \text{Shift} \end{array}$$

Heterotic AO

$$\Gamma^{21,5} = \Gamma^{20,4} + \Gamma^{1,1}$$

$$\begin{array}{ccc} \uparrow & & \uparrow \\ \mathbb{Z}_N \text{ twist} & & \text{Shift} \end{array}$$

Twisted sectors become massive



Similar examples

[Gkoumtoumis, Hull, Stemerdink, Vandoren 23']

More 5d models with no hypers ?

rank	type	lattice + $\Gamma^{1,1}$	twist	order
2	II	$\Gamma^{4,4}(D_4)$	$\phi_L = (\frac{1}{6}, \frac{3}{6})$ $\phi_R = (\frac{1}{4}, \frac{1}{4})$	12
4	II	$\Gamma^{4,4}(D_4)$	$\phi_L = (0, \frac{2}{3})$ $\phi_R = (\frac{1}{4}, \frac{1}{4})$	12
6	II	$\Gamma^{4,4}(A_2 \times A_2)$	$\phi_L = (1, 0)$ $\phi_R = (\frac{1}{3}, \frac{1}{3})$	6
8	II	$\Gamma^{4,4}(D_4)$	$\phi_L = (\frac{1}{2}, 0)$ $\phi_R = (\frac{1}{4}, \frac{1}{4})$	4
12	Het	$2\Gamma^{2,2}(A_2) + 2\Gamma^{8,0}(E_8)$	$\phi_R = (\frac{1}{6}, \frac{1}{6})$ $\Gamma^{2,2}(A_2) \leftrightarrow \Gamma^{2,2}(A_2)$ $\Gamma^{8,0}(E_8) \leftrightarrow \Gamma^{8,0}(E_8)$ $V_L = (0^8; 0^8)$	12
14	Het	$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$	$\phi_L = (0, 0)$ $\phi_R = (\frac{1}{4}, \frac{1}{4})$ $\Gamma^{8,0}(E_8) \leftrightarrow \Gamma^{8,0}(E_8)$ $V_L = (0^8; 0^8)$	4
		Model 4 on S^1 , Coulomb branch		
20	Het	$2\Gamma^{2,2}(A_2) + 2\Gamma^{8,0}(E_8)$	$\phi_R = (\frac{1}{6}, \frac{1}{6})$ $\Gamma^{2,2}(A_2) \leftrightarrow \Gamma^{2,2}(A_2)$ $V_L = (0^8; 0^8)$	12
22	Het	$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$	$\phi_L = (0, 0)$ $\phi_R = (\frac{1}{2}, \frac{1}{2})$ $V_L = (0^8; 0^8)$	2
		Model 1, 2, 3 on S^1 , Coulomb branch		

More 5d models with no hypers ?

Observations

- Even Rank ?

rank	type	lattice + $\Gamma^{1,1}$	twist	order
2	II	$\Gamma^{4,4}(D_4)$	$\phi_L = (\frac{1}{6}, \frac{3}{6})$ $\phi_R = (\frac{1}{4}, \frac{1}{4})$	12
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12	Het	$2\Gamma^{2,2}(A_2) + 2\Gamma^{8,0}(E_8)$	$\phi_R = (\frac{1}{6}, \frac{1}{6})$ $\Gamma^{2,2}(A_2) \leftrightarrow \Gamma^{2,2}(A_2)$ $\Gamma^{8,0}(E_8) \leftrightarrow \Gamma^{8,0}(E_8)$ $V_L = (0^8; 0^8)$	12
14	Het	$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$	$\phi_L = (0, 0)$ $\phi_R = (\frac{1}{4}, \frac{1}{4})$ $\Gamma^{8,0}(E_8) \leftrightarrow \Gamma^{8,0}(E_8)$ $V_L = (0^8; 0^8)$	4
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22	Het	$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$	$\phi_L = (0, 0)$ $\phi_R = (\frac{1}{2}, \frac{1}{2})$ $V_L = (0^8; 0^8)$	2
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More 5d models with no hypers ?

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		Model 1, 2, 3 on S^1 , Coulomb branch		

- Even Rank ?

[Gkoumtoumis, Hull, Stemerdink, Vandoren 23']

- $r < 26 - d + 1$?

[Kim, HCT,Vafa 19']

More 5d models with no hypers ?

Observations

rank	type	lattice + $\Gamma^{1,1}$	twist	order
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22	Het	$\Gamma^{4,4}(D_4) + 2\Gamma^{8,0}(E_8)$	$\phi_L = (0, 0)$ $\phi_R = (\frac{1}{2}, \frac{1}{2})$ $V_L = (0^8; 0^8)$	2
		Model 1, 2, 3 on S^1 , Coulomb branch		

- Even Rank ?

- $r < 26 - d + 1?$
For H=0

- $r = 0??????$
[Mizoguchi 01']

More 5d models with no hypers ?

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rank	type	lattice + $\Gamma^{1,1}$	twist	order
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- $r < 26 - d + 1$?
- $r = 0??????$

No scalars so not a perturbative string theory



More 5d models with no hypers ?

Observations

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		Model 1, 2, 3 on S^1 , Coulomb branch		

- Even Rank ?

- $r < 26 - d + 1$?

- $r = 0??????$

No scalars so not a perturbative string theory

Maybe strong coupling of 4d with one vector?



Abelian Orbifolds

Observations

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string theory

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Abelian Orbifolds

Observations

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- $r < 26 - d + 1?$
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No scalars so not a perturbative
string theory

Maybe strong coupling of 4d
with one vector?

Maybe strong coupling of 3d
with two vectors?



3d models with no hypers and two vectors

- Find 4d orbifold with untwisted sector: (4d $\mathcal{N} = 2$ Gravity) + 1(Vector)

3d models with no hypers and two vectors

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- Put the theory on S^1 with a shift: twisted sectors massive

3d models with no hypers and two vectors

- Find 4d orbifold with untwisted sector: (4d $\mathcal{N} = 2$ Gravity) + 1(Vector)
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- Resulting theory: (3d $\mathcal{N} = 4$ Gravity) + 2(Vectors)

3d models with no hypers and two vectors

- Find 4d orbifold with untwisted sector: (4d $\mathcal{N} = 2$ Gravity) + 1(Vector)
- Put the theory on S^1 with a shift: twisted sectors massive
- Resulting theory: (3d $\mathcal{N} = 4$ Gravity) + 2(Vectors)

$$\Gamma^{6,6}(E_6)$$

$$\phi_L = \left(0, \frac{2}{3}, \frac{2}{3}\right) \quad \phi_R = \left(\frac{1}{9}, \frac{2}{9}, \frac{4}{9}\right)$$

3d models with no hypers and two vectors

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$$\Gamma^{6,6}(E_6)$$

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Could this be our theory?

3d models with no hypers and two vectors

- Find 4d orbifold with untwisted sector: (4d $\mathcal{N} = 2$ Gravity) + 1(Vector)
- Put the theory on S^1 with a shift: twisted sectors massive
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$$\Gamma^{6,6}(E_6)$$

$$\phi_L = \left(0, \frac{2}{3}, \frac{2}{3}\right) \quad \phi_R = \left(\frac{1}{9}, \frac{2}{9}, \frac{4}{9}\right)$$

Does the theory go to 4d or 5d?

Emergent string conjecture: Infinite distance limit decompactifies or string limit

[Lee, Lerche, Weigand 19']

3d models with no hypers and two vectors

- Find 4d orbifold with untwisted sector: (4d $\mathcal{N} = 2$ Gravity) + 1(Vector)
- Put the theory on S^1 with a shift: twisted sectors massive
- Resulting theory: (3d $\mathcal{N} = 4$ Gravity) + 2(Vectors)

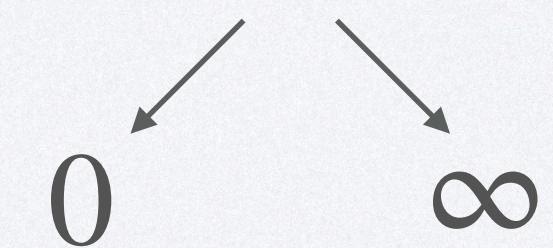
$$\Gamma^{6,6}(E_6)$$

$$\phi_L = \left(0, \frac{2}{3}, \frac{2}{3}\right) \quad \phi_R = \left(\frac{1}{9}, \frac{2}{9}, \frac{4}{9}\right)$$

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Two non-compact scalars: R_{S^1} and g_s



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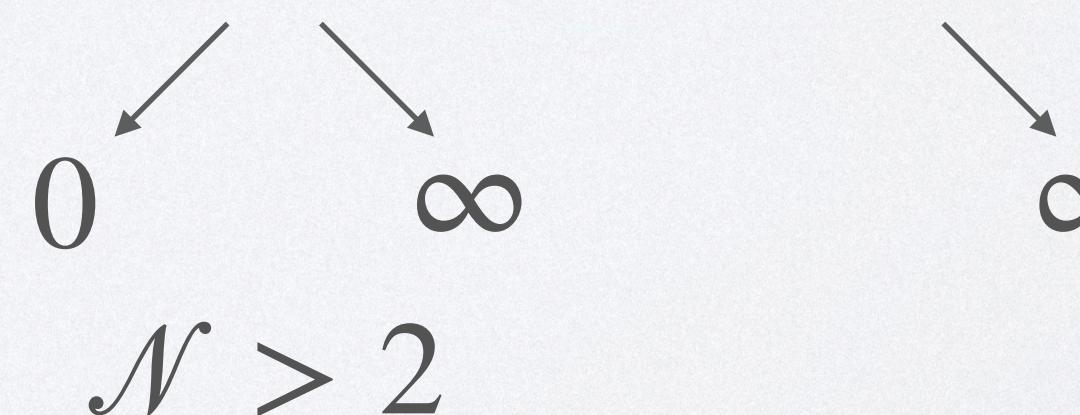
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Two non-compact scalars:

R_{S^1} and g_s



We need to compute
the instanton corrections

Abelian Orbifolds

- Choose the starting point: IIA, IIB, Heterotic
- Choose even self-dual lattice: $\Gamma^{D,D}(\mathfrak{g}) = \{(p_L, p_R) \mid p_L \in \Lambda_W(\mathfrak{g}), p_R \in \Lambda_W(\mathfrak{g}), p_L - p_R \in \Lambda_R(\mathfrak{g})\}$

$$\Gamma^{D,D}(\mathfrak{g}) + \Gamma^{16,0}(E_8 \times E_8)$$

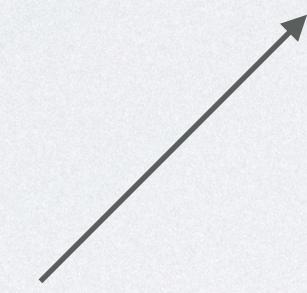


Lattice Automorphisms/crystallographic symmetries of T^D

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Are there such automorphisms that act crystallographically on $\Gamma^{D,D}$ but not T^D ?

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Lattice Automorphisms/crystallographic symmetries of T^D

Are there such automorphisms that act crystallographically on $\Gamma^{D,D}$ but not T^D ?

Yes!

[Harvey, Moore, Vafa 87']

Quasicrystalline Compactifications

- Choose the starting point: IIA, IIB, Heterotic
- Find automorphisms that act crystallographically in $2d$ but not d
- Build even self-dual lattice $\Gamma^{D,D}$

Quasicrystalline Compactifications

Q	6d	$\Gamma^{4,4}$	Twist	Known
16	$1G + 21T$	$2\Gamma_C^{2,2}$	$\mathbb{Z}_{12} : \{1/12, 1/12\}, \{5/12, 5/12\}$	K3
8	$1G + 9T + 8V + 20H$	$\Gamma_C^{4,4}$	$\mathbb{Z}_{20} : \{1/20, 3/20\}, \{7/20, 9/20\}$	$CY3 \rightarrow dP9$

Freely Acting

Q	5d	Lat.+ $\Gamma^{1,1}$	Twist
16	$1G + 1V$	$2\Gamma_C^{2,2}$	$\mathbb{Z}_{12} : \{1/12, 1/12\}, \{5/12, 5/12\}$
0	$1G + 4V + 2F + 3S_R$ $1G + 3V + 2S_R$ $1G + 3V + 2F + 2S_R$	$\Gamma_C^{4,4}$ $\Gamma_C^{4,4}$ $\Gamma_C^{4,4}$	$\mathbb{Z}_{20} : \{1/20, 3/20\}, \{7/20, 9/20\}$ $\mathbb{Z}_{30} : \{1/30, 11/30\}, \{7/30, 13/30\}$ $\mathbb{Z}_{30} : \{1/30, 7/30\}, \{11/30, 13/30\}$

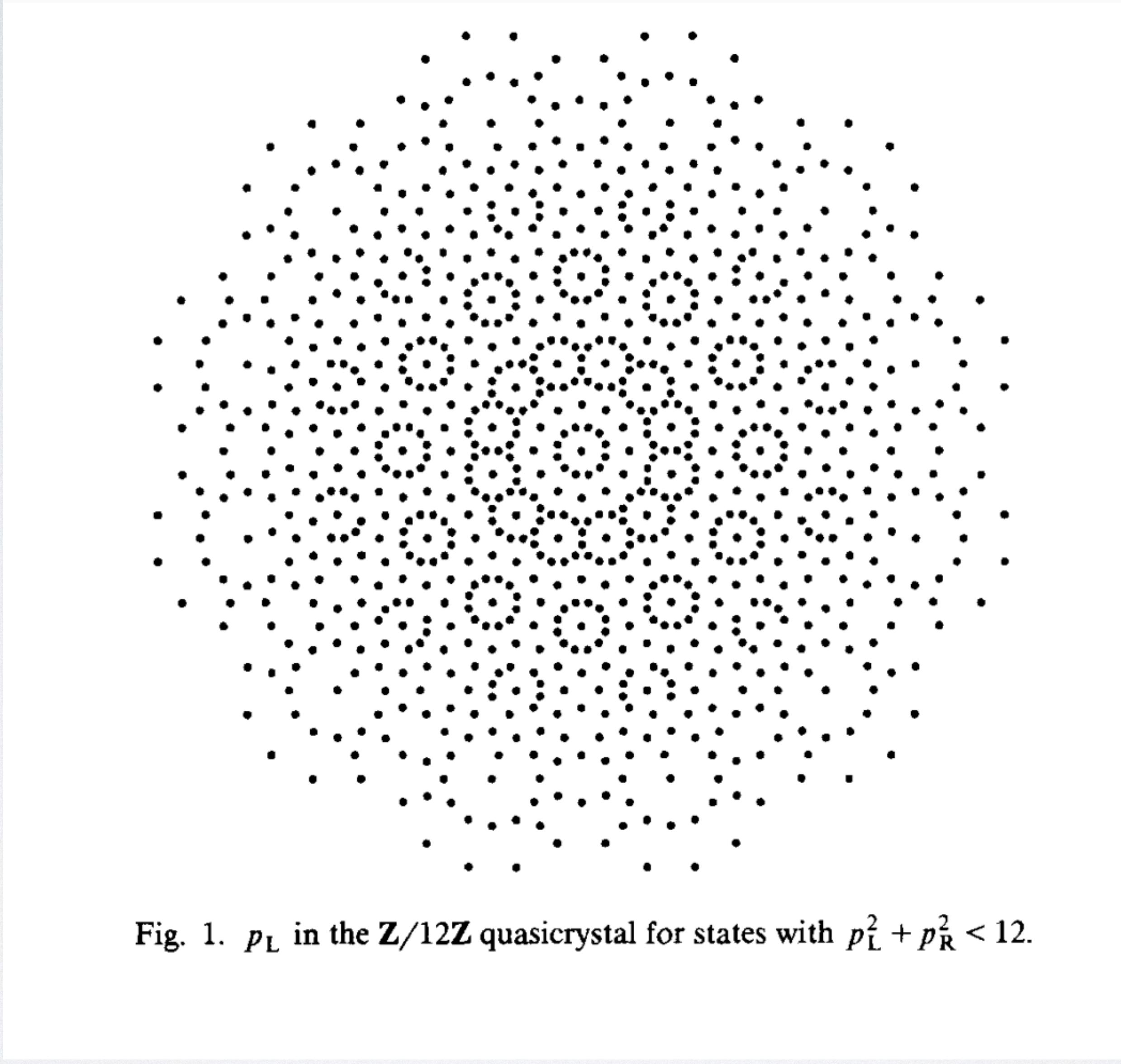
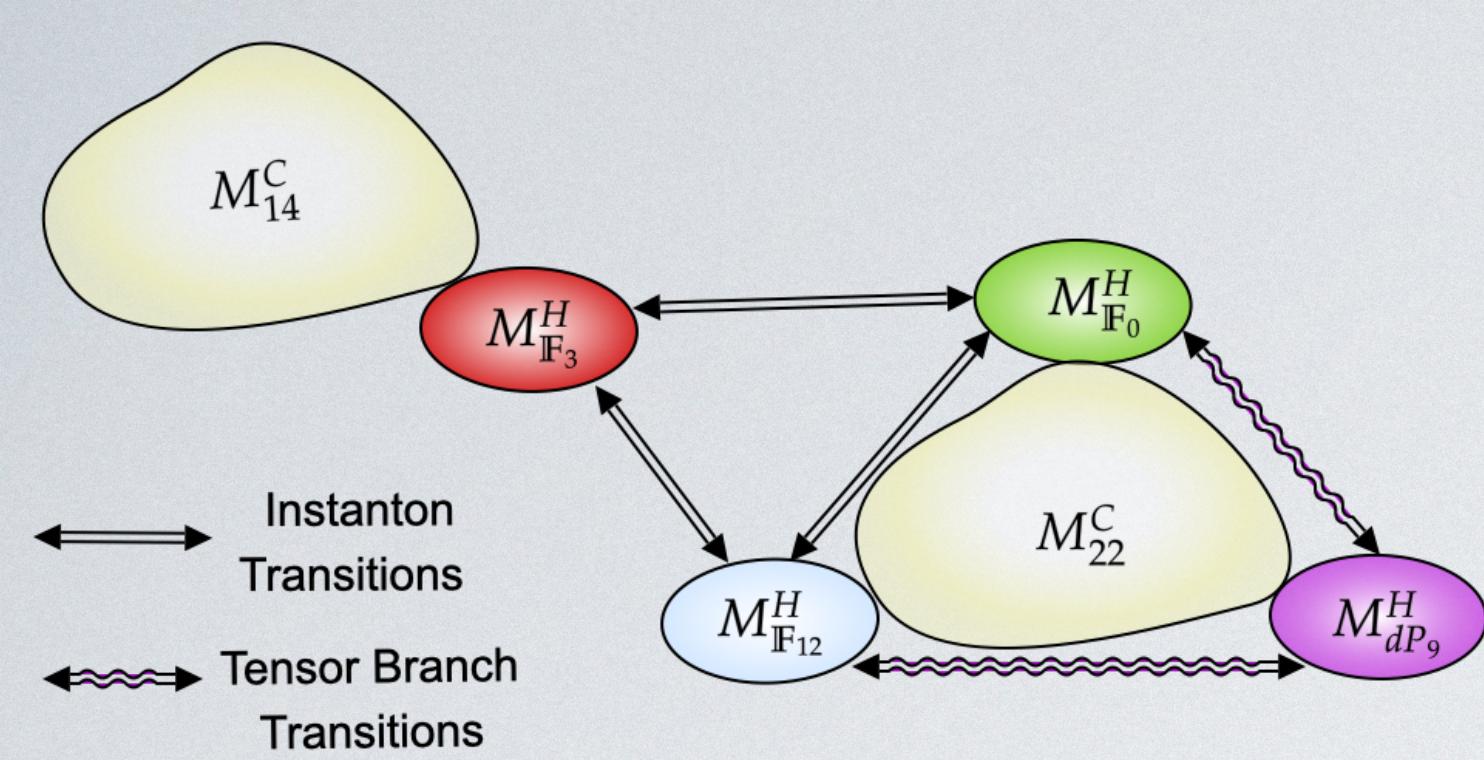


Fig. 1. p_L in the $\mathbf{Z}/12\mathbf{Z}$ quasicrystal for states with $p_L^2 + p_R^2 < 12$.

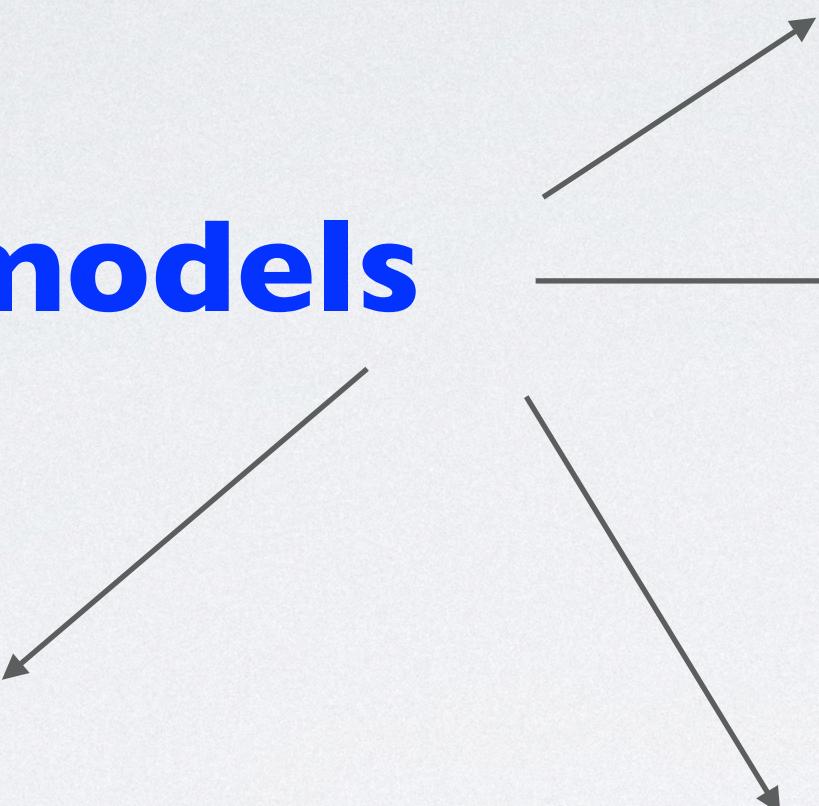
Summary and future direction



Understanding the boundary
of the string landscape

- **Non-geometric models**

Good testing
ground for Swampland conjectures



Where is the 5d $\mathcal{N} = 1$?
Compute corrections?

They kill moduli: important for realistic non-susy models
Other like $SO(16) \times SO(16)$ string theory?

- Any new ideas for non-geometric string constructions?



Thank you very much
for listening!