

PBH from domain wall networks

Motivated by PTA signal

Yann Gouttenoire



Axion ++ conference in Annecy

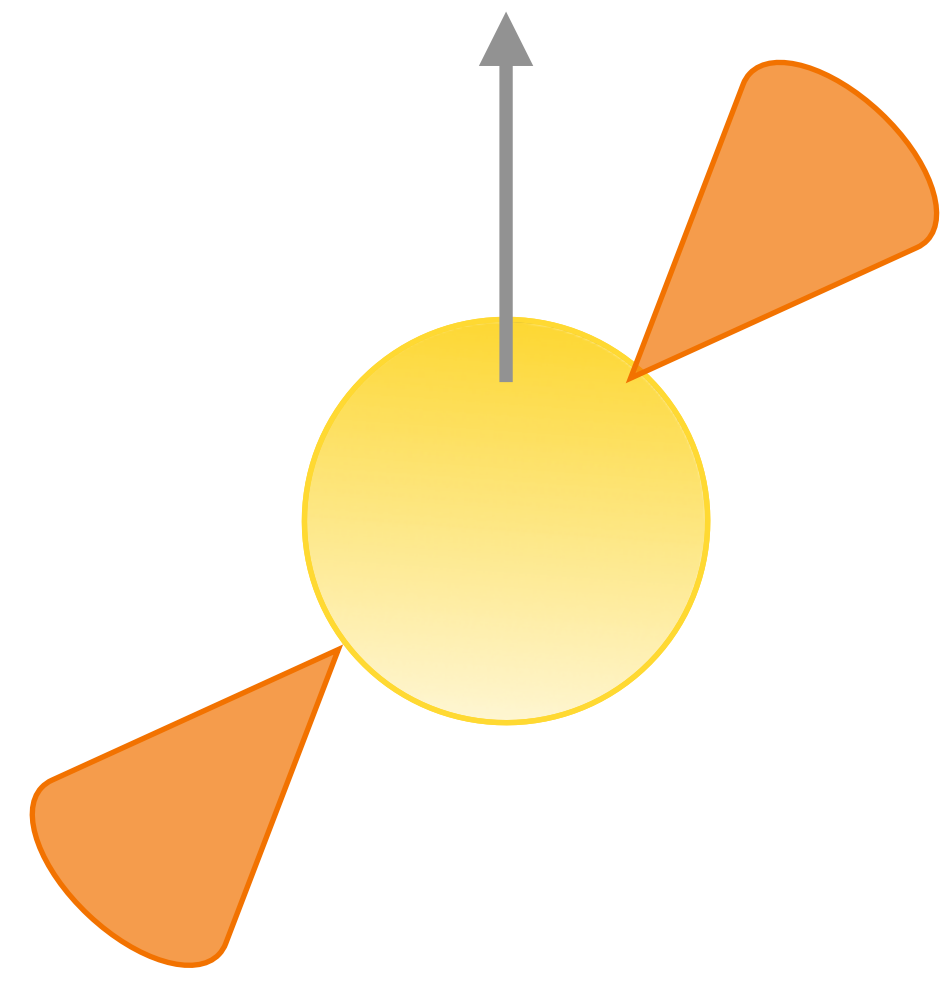
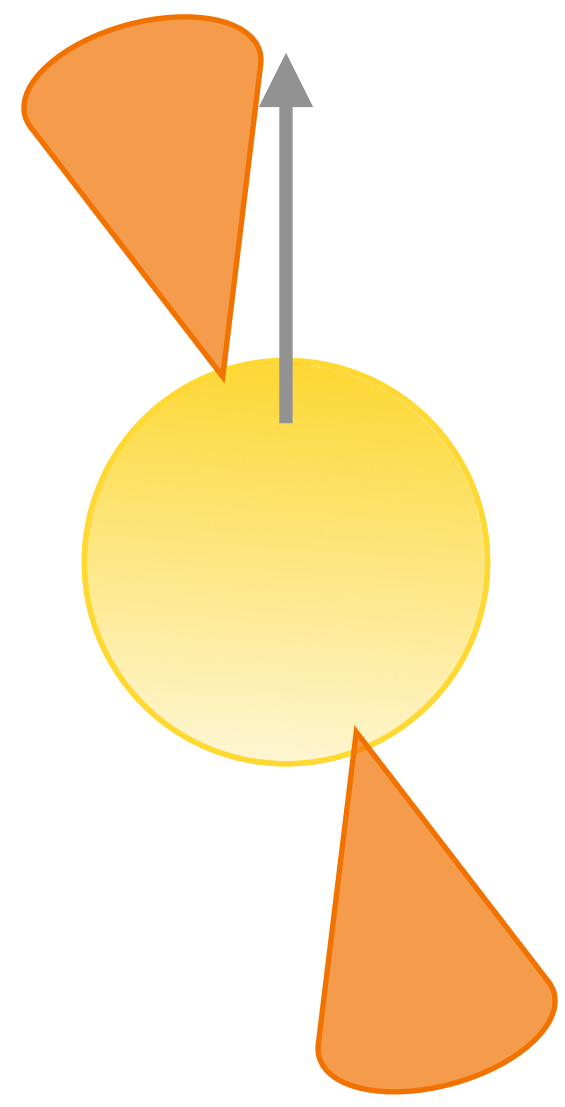
27th September 2023

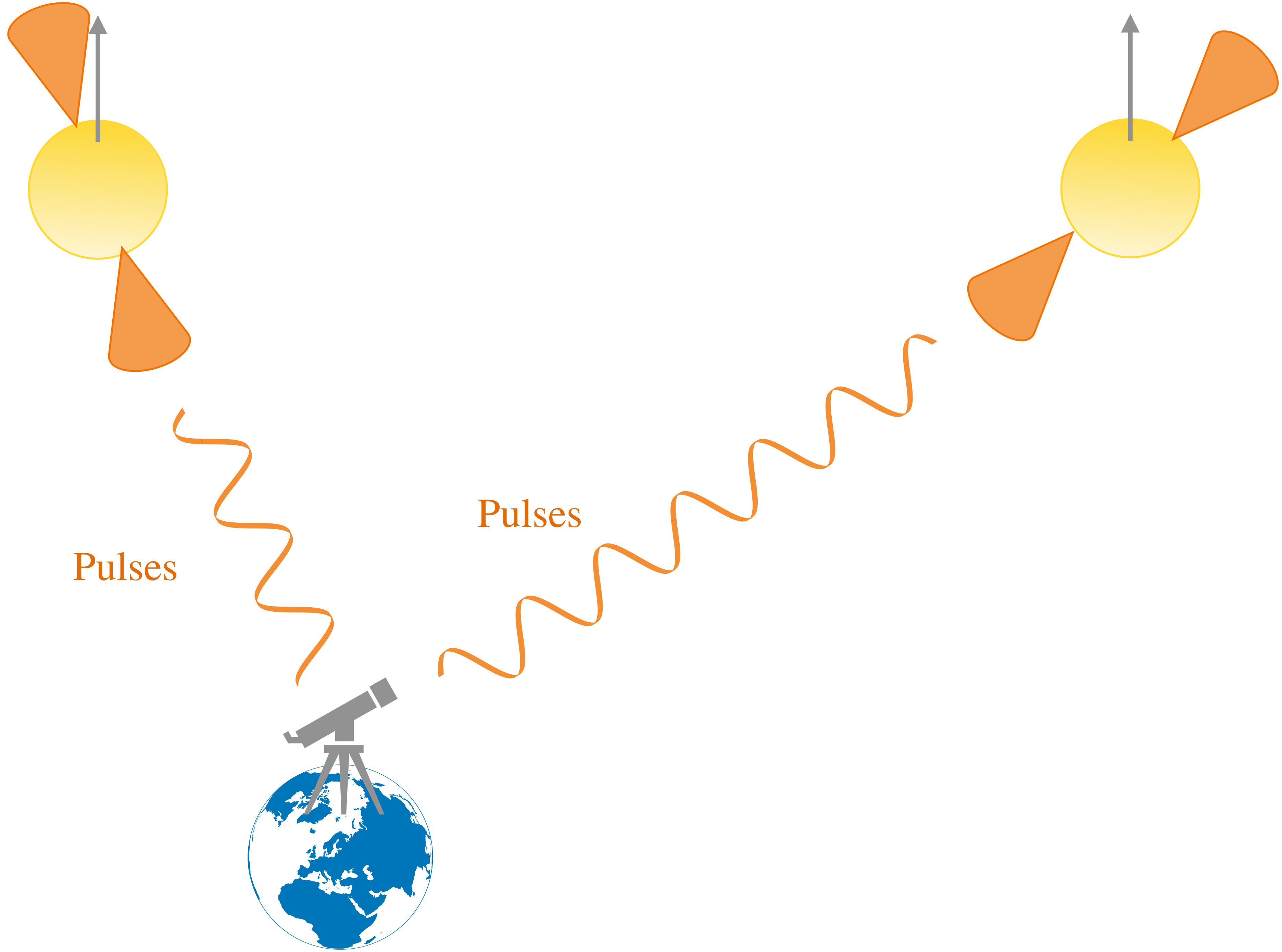
Postdoc in Tel Aviv U.

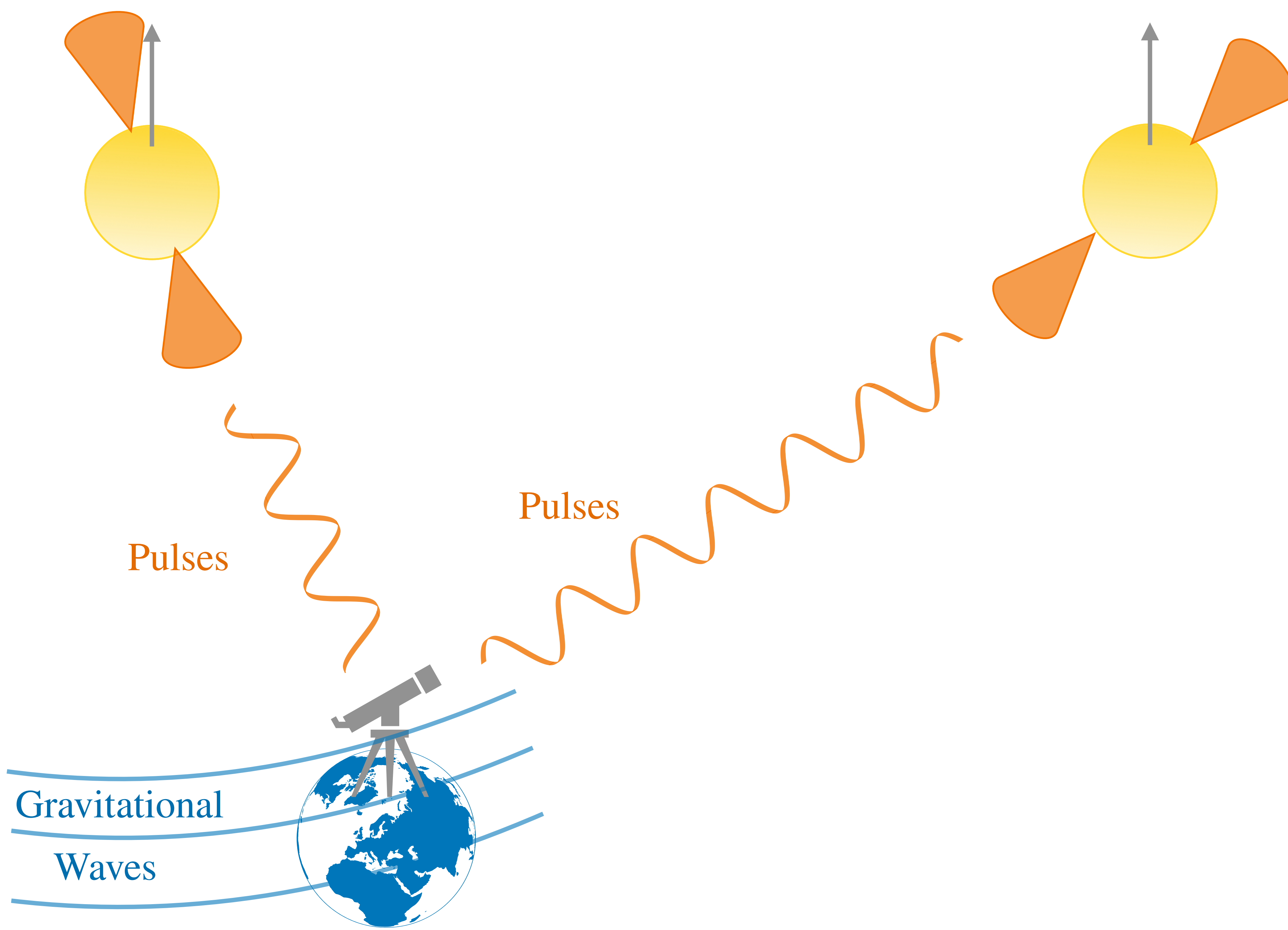


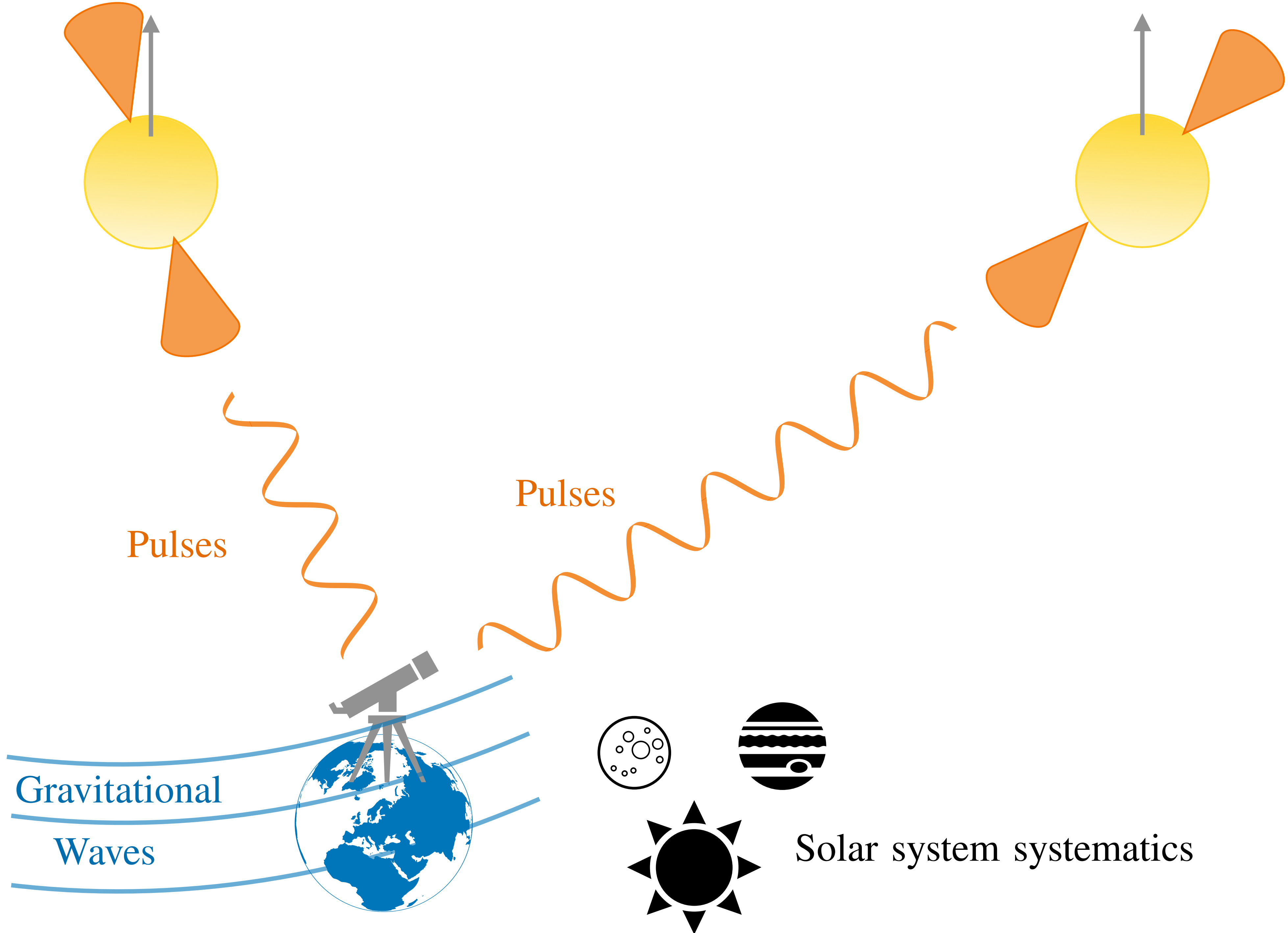
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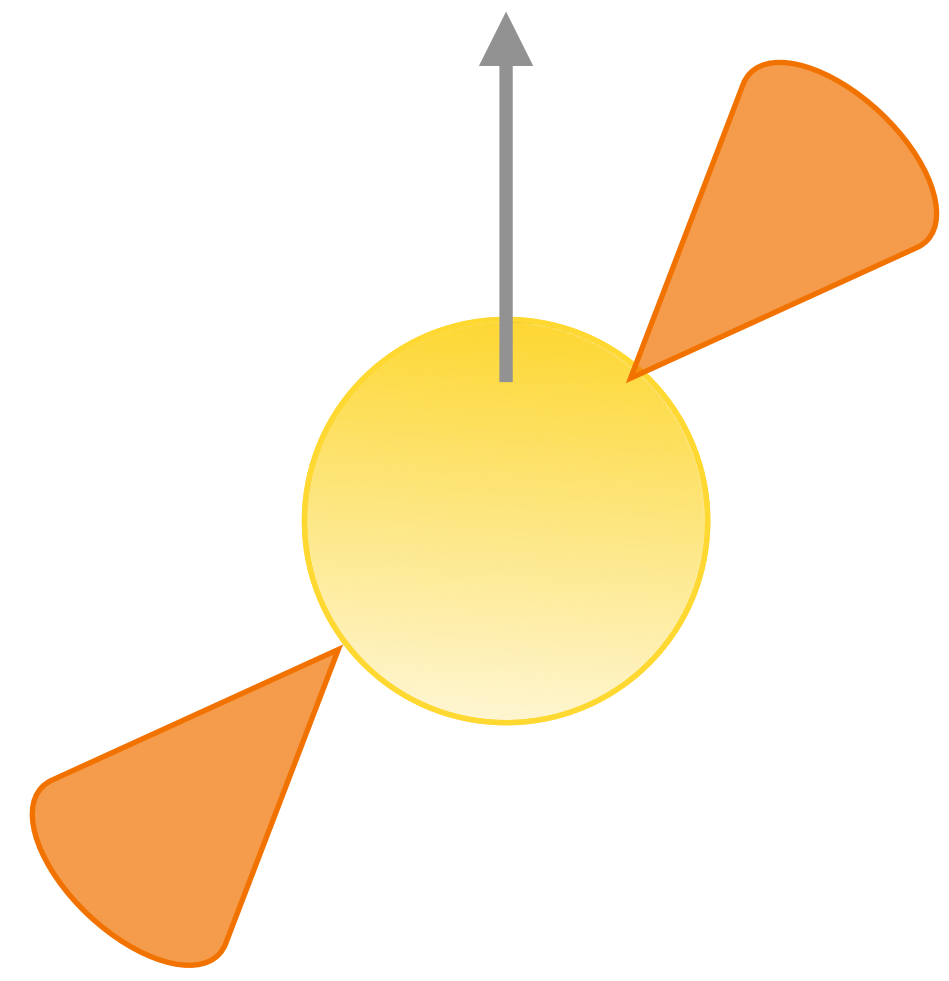
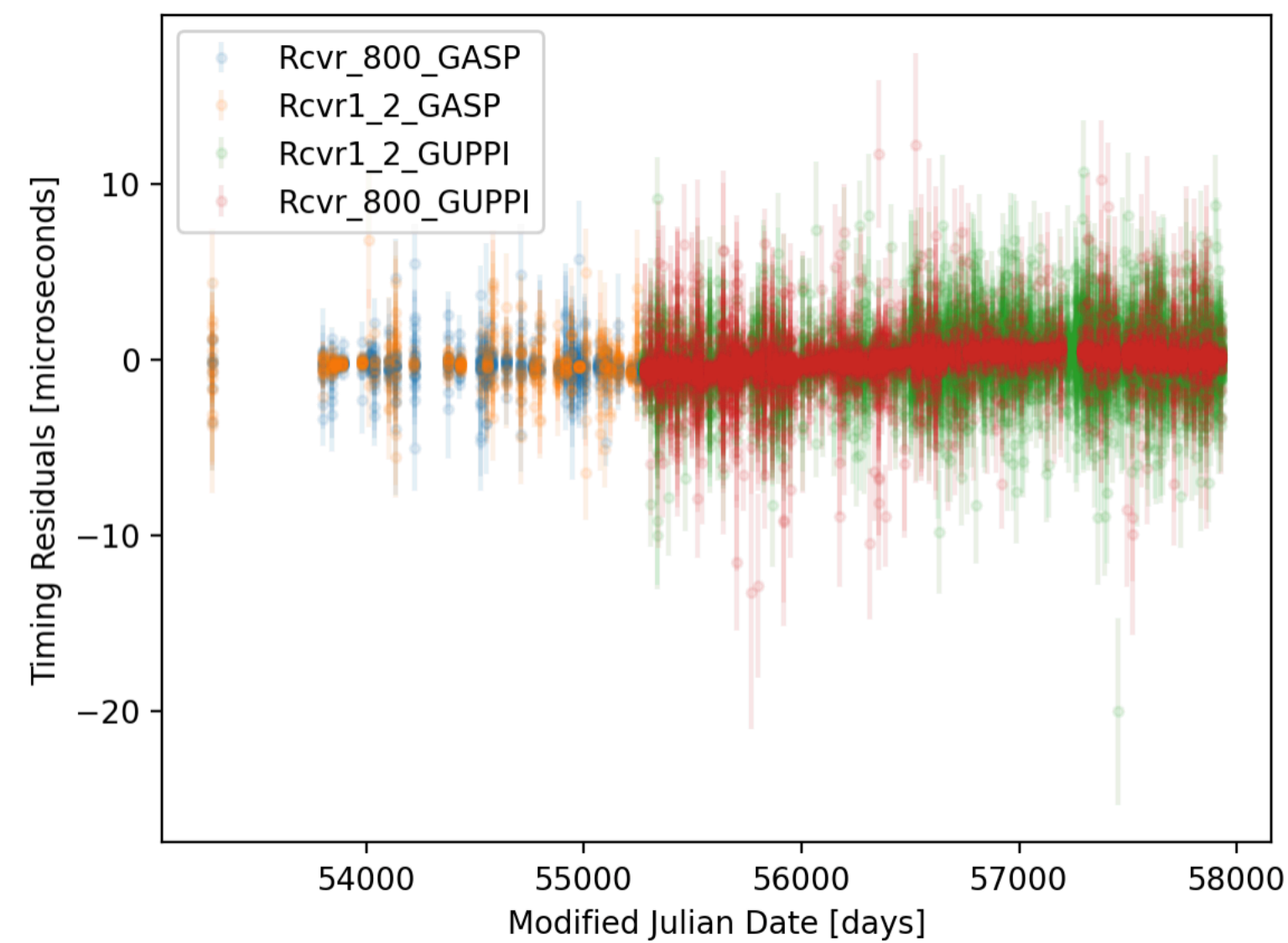
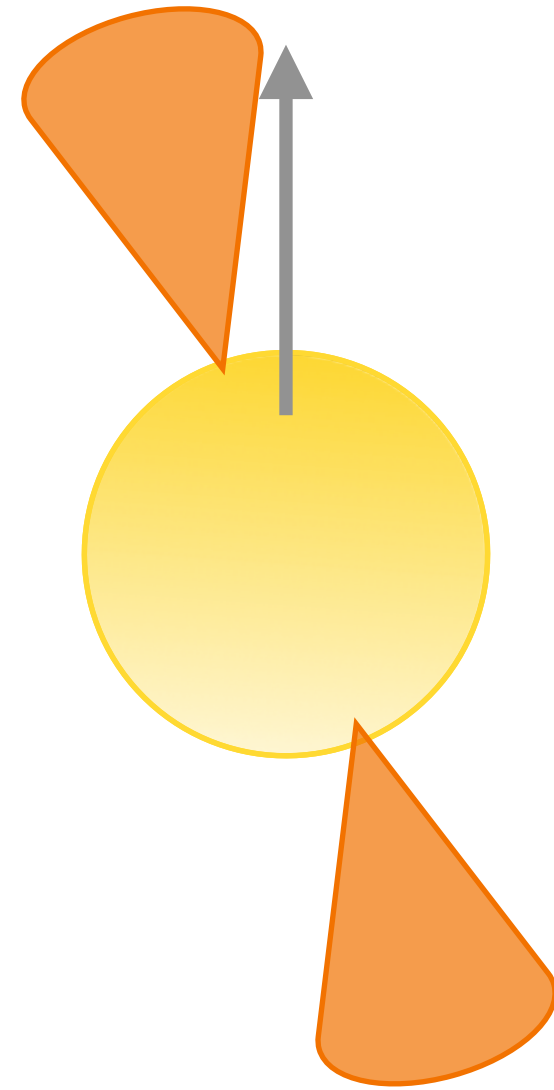








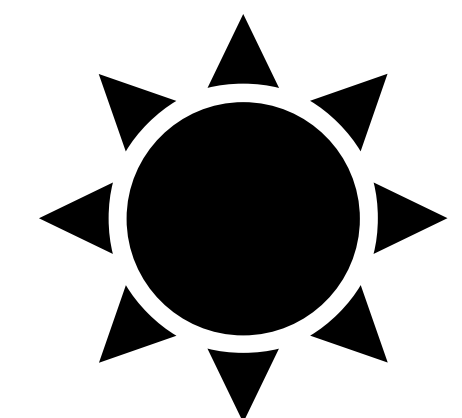
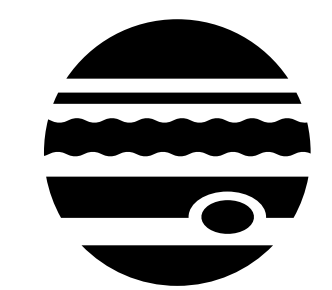
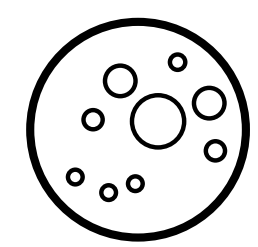
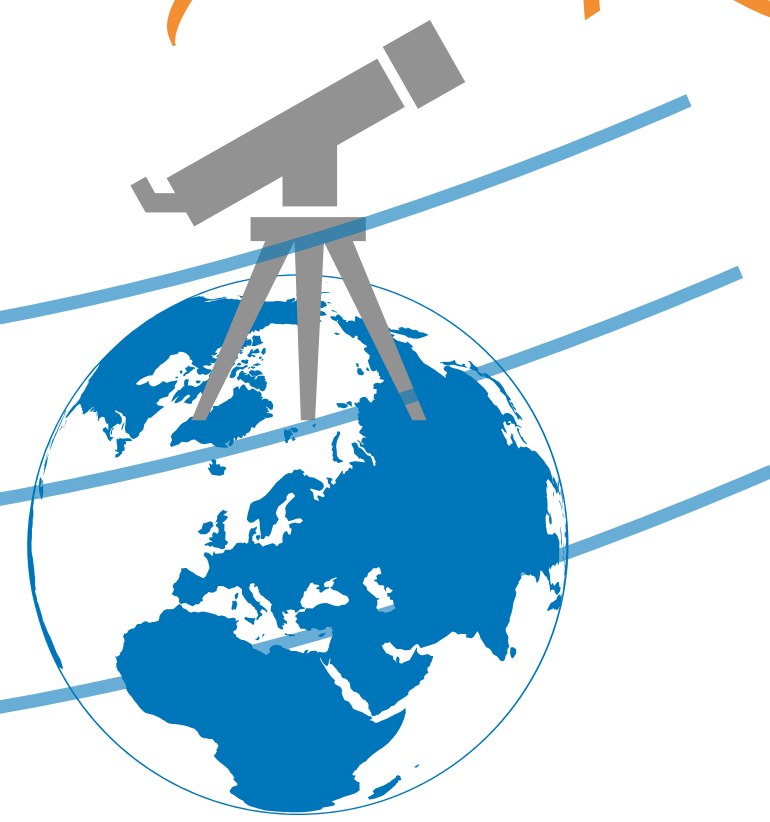




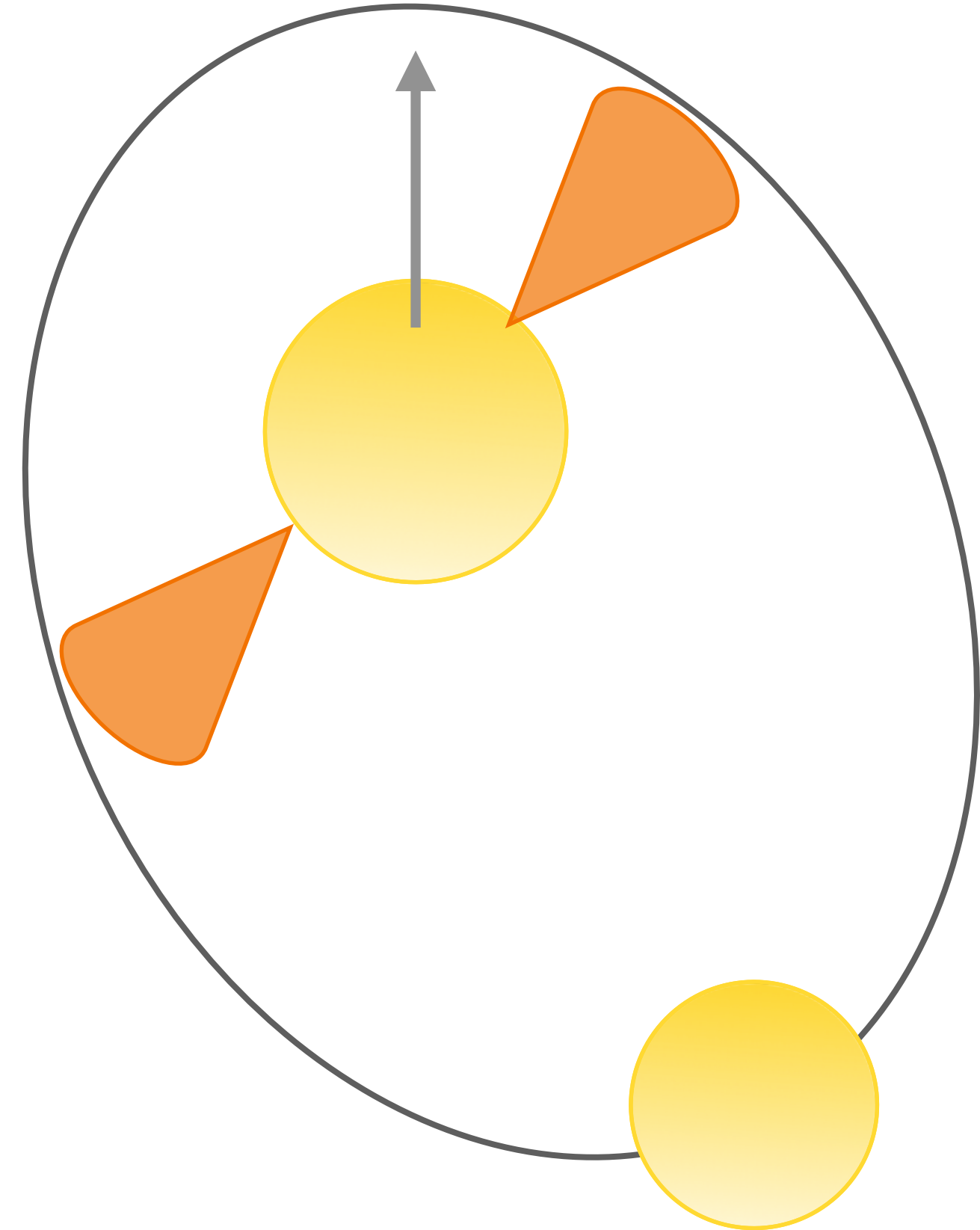
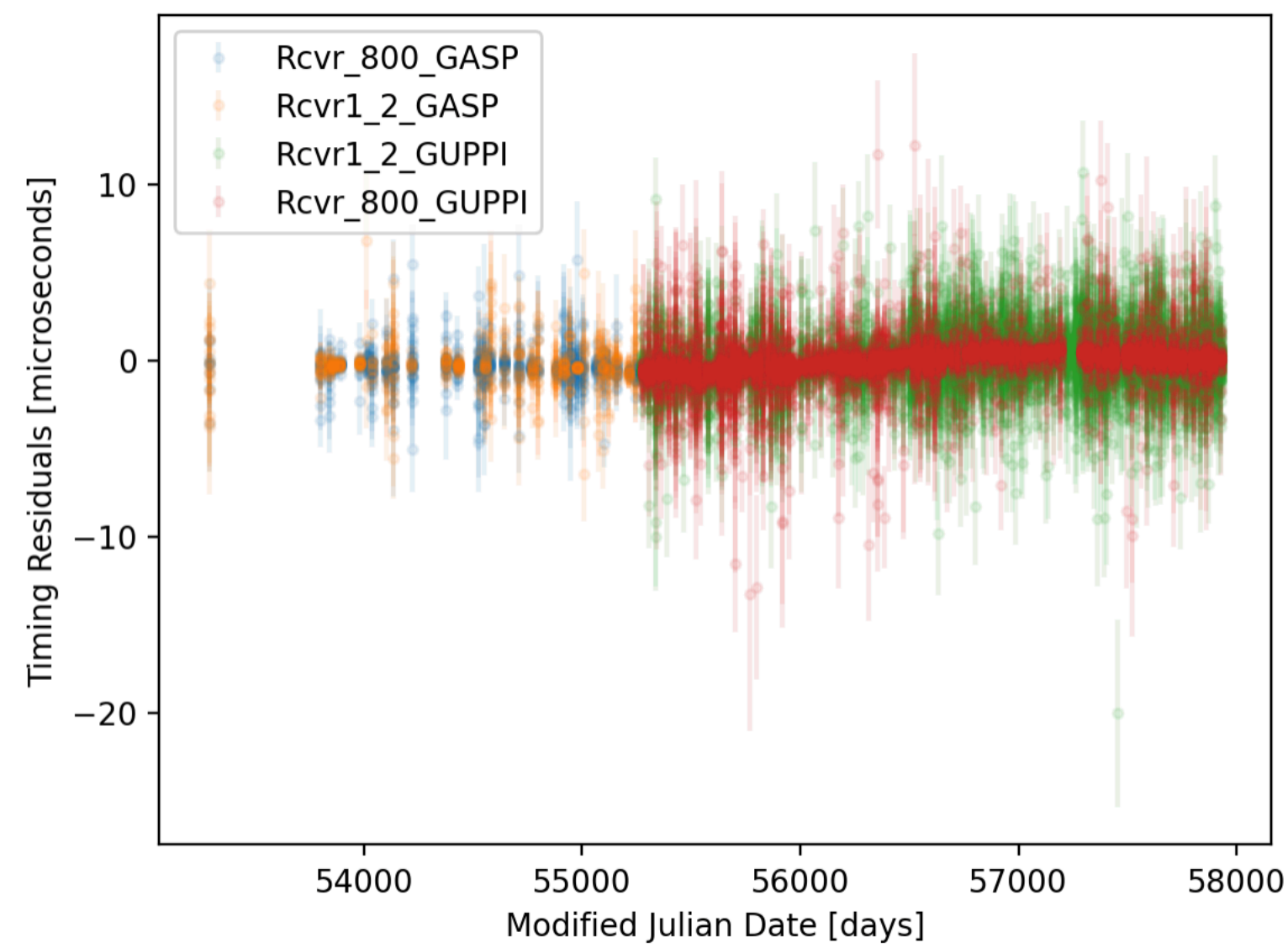
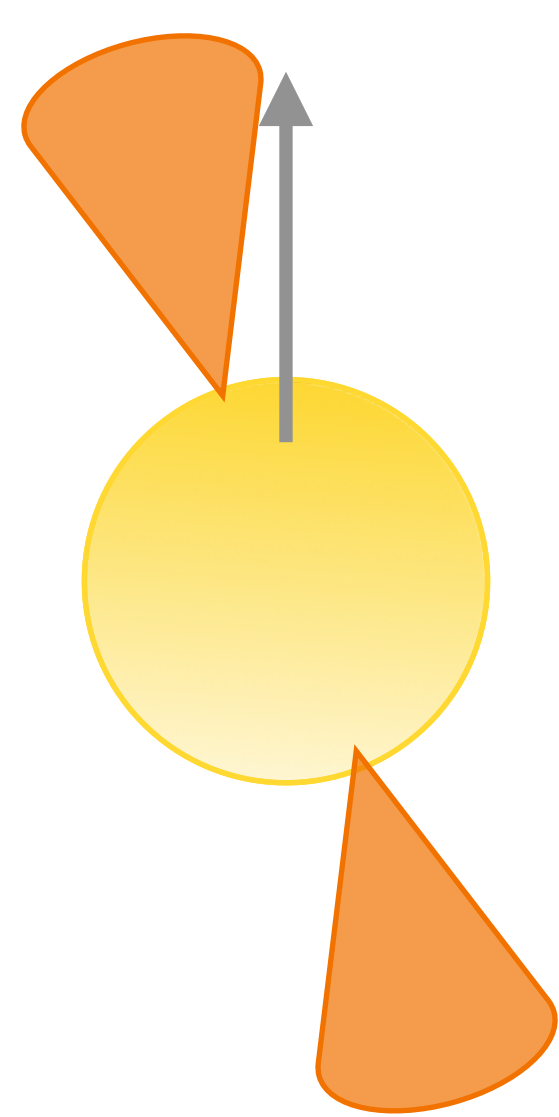
Pulses

Pulses

Gravitational
Waves



Solar system systematics

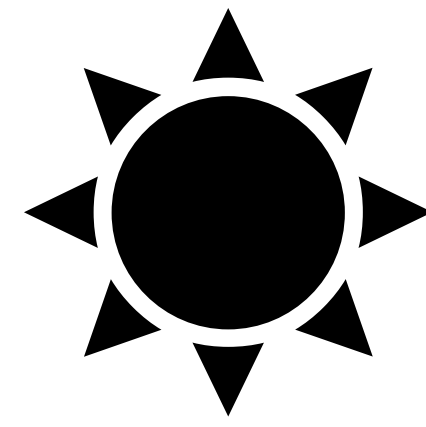
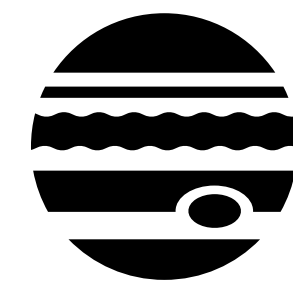
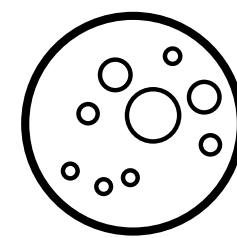


Pulses

Pulses

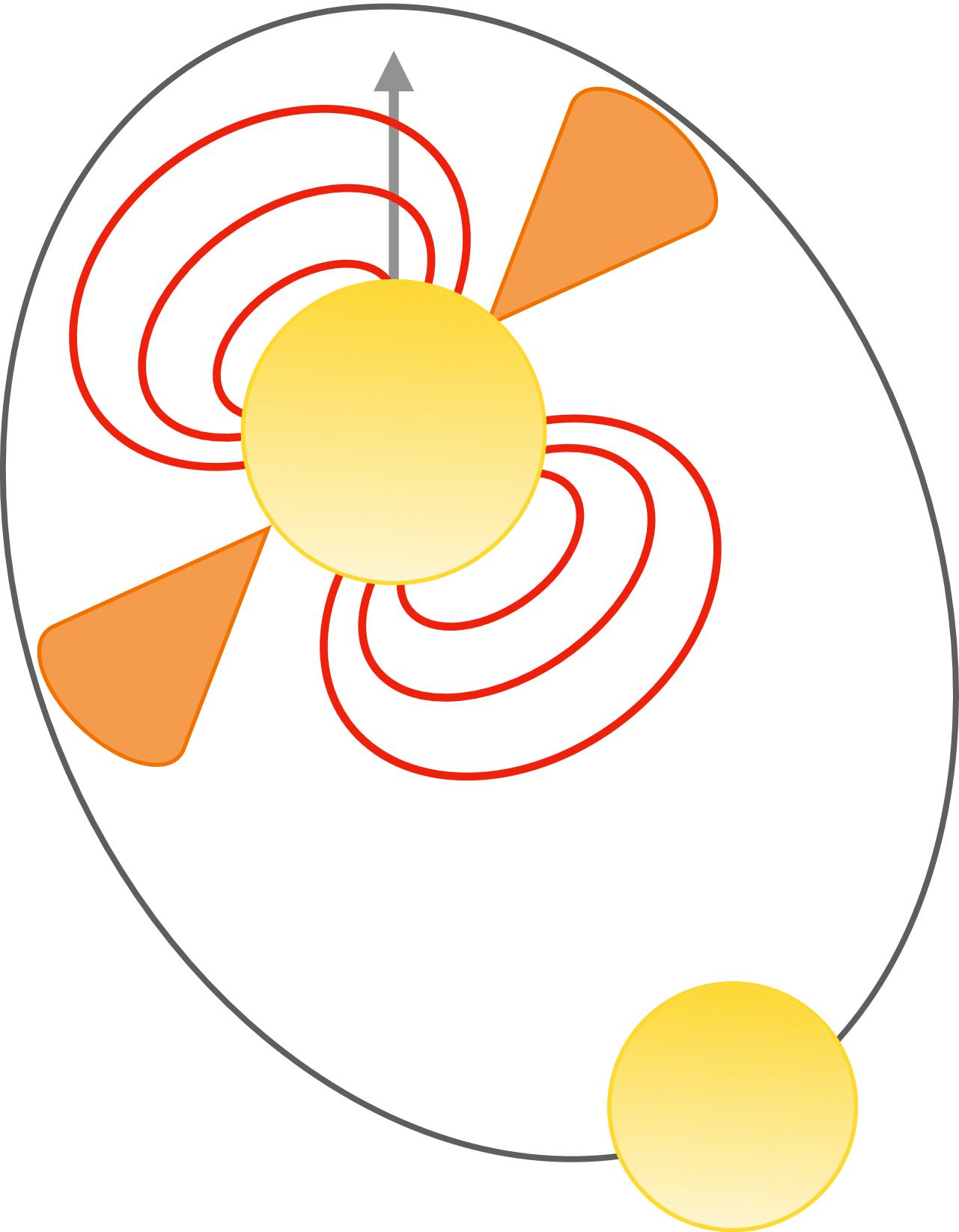
Pulsar companion systematics

Gravitational Waves



Solar system systematics

Pulsar red noise
(e.g. magnetosphere fluctuation)

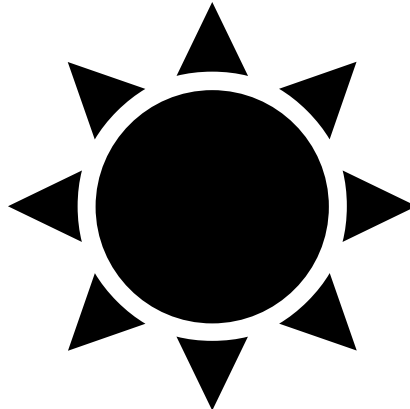
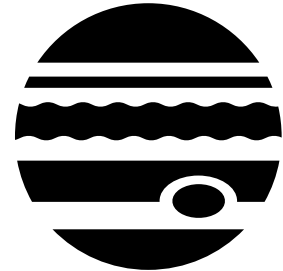
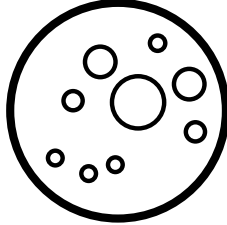


Pulsar companion systematics

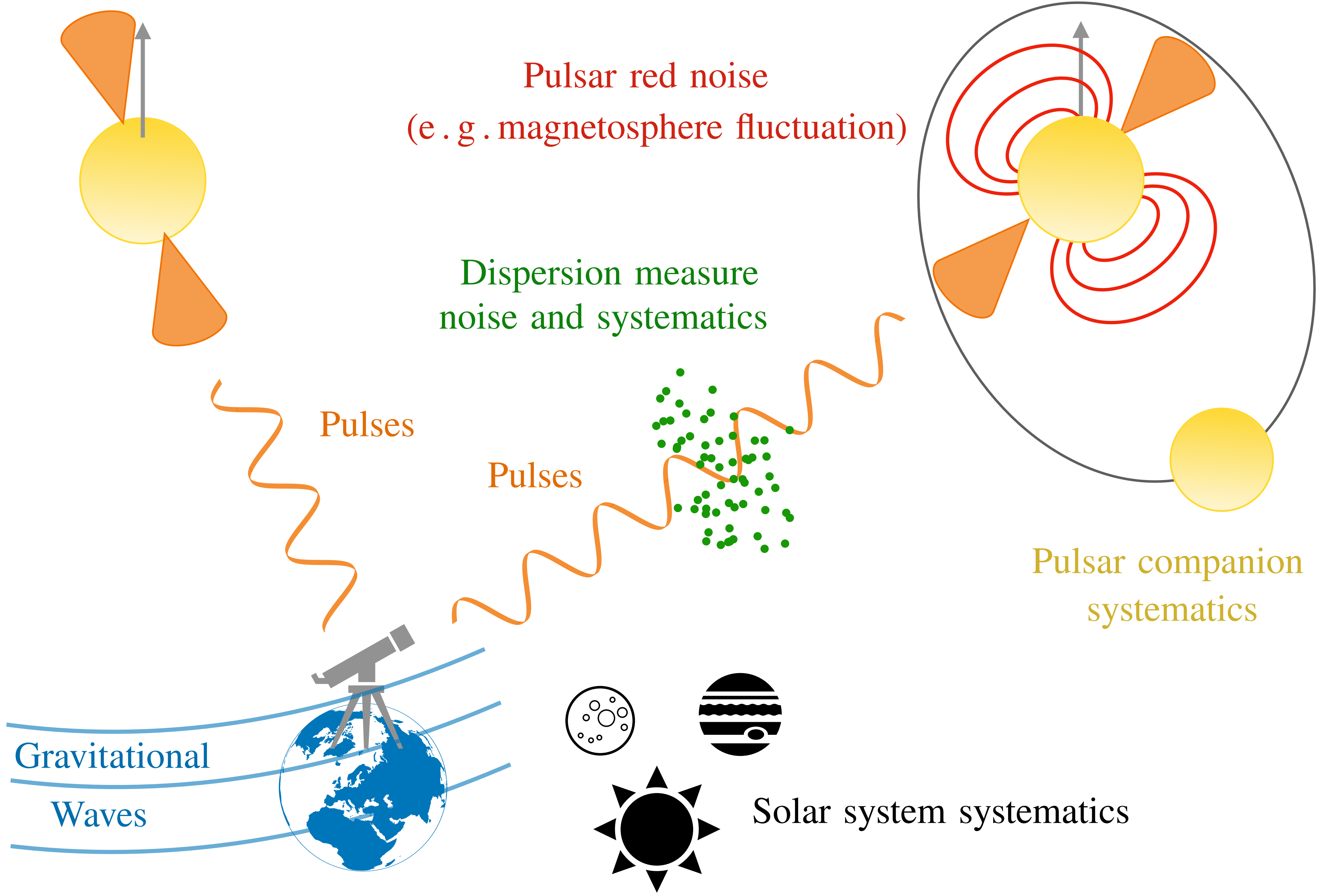
Pulses

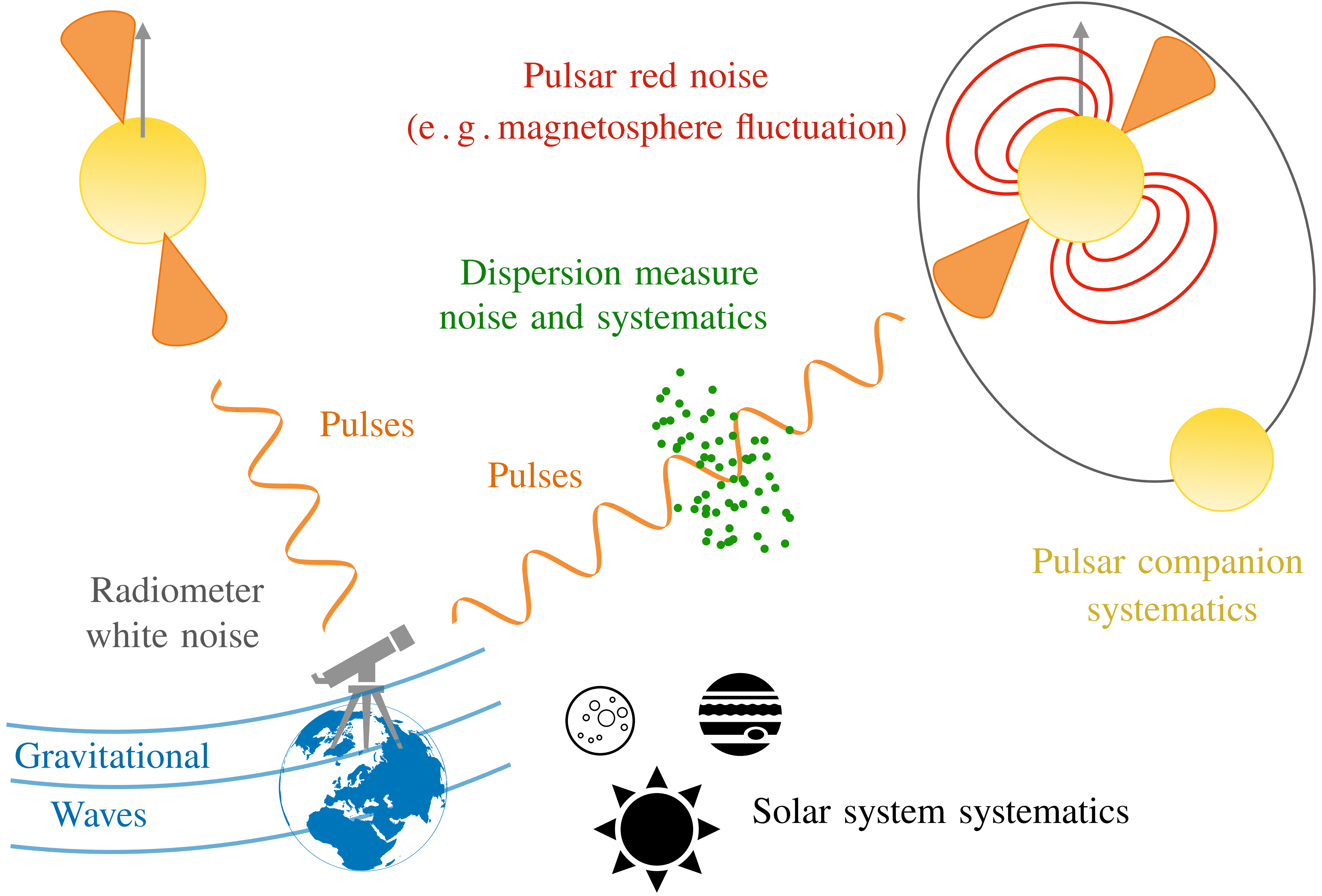
Pulses

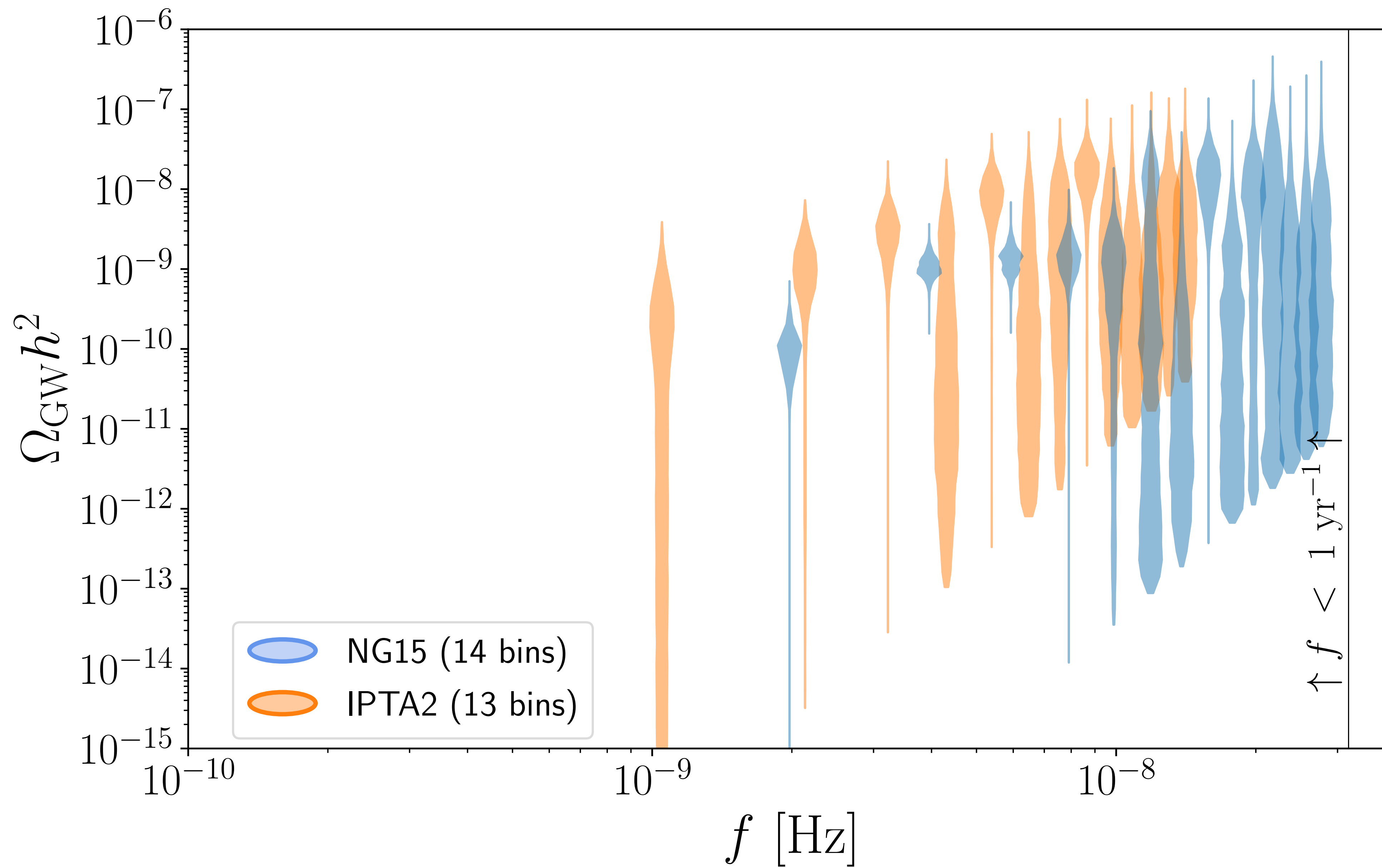
Gravitational Waves



Solar system systematics

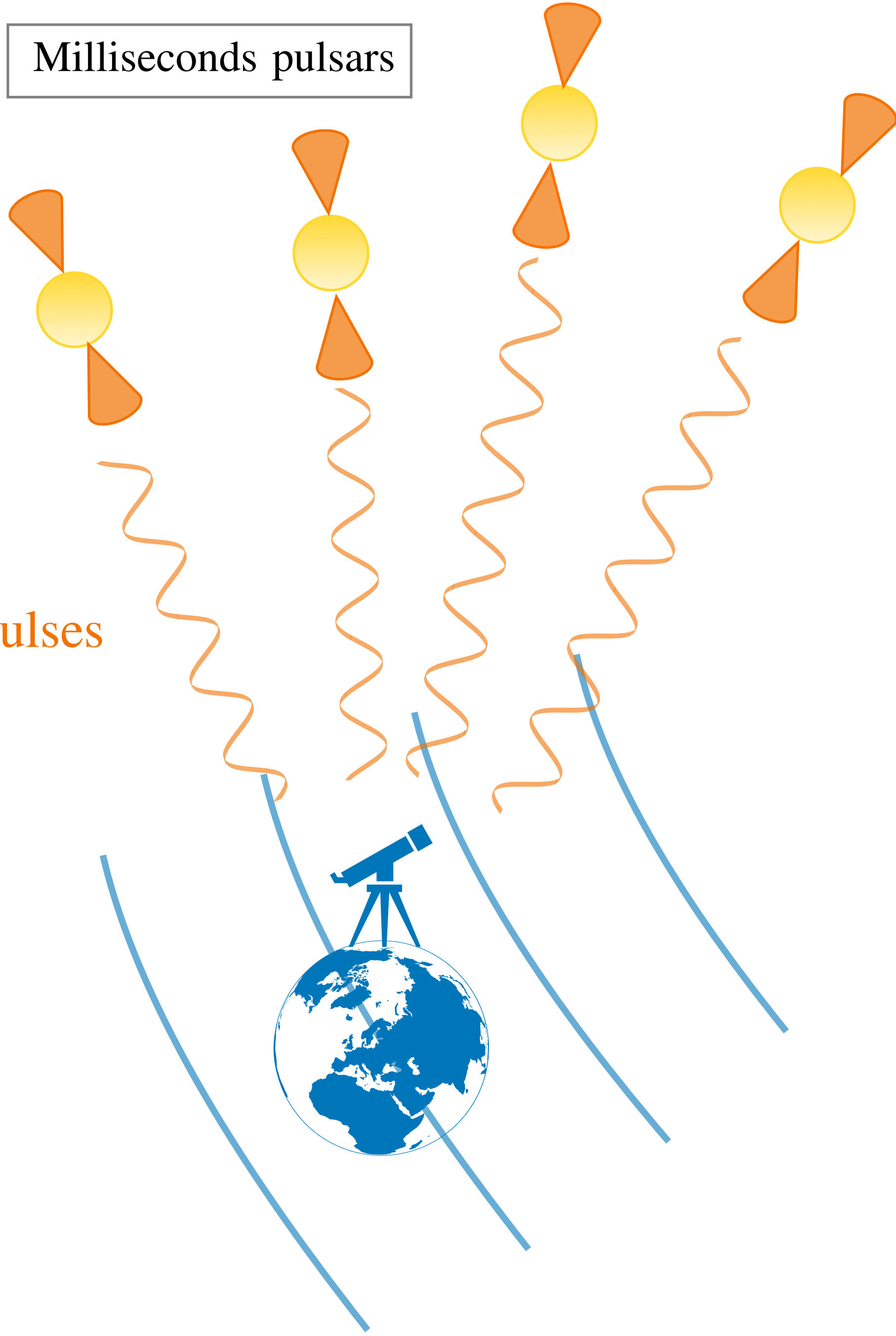






Milliseconds pulsars

Pulses



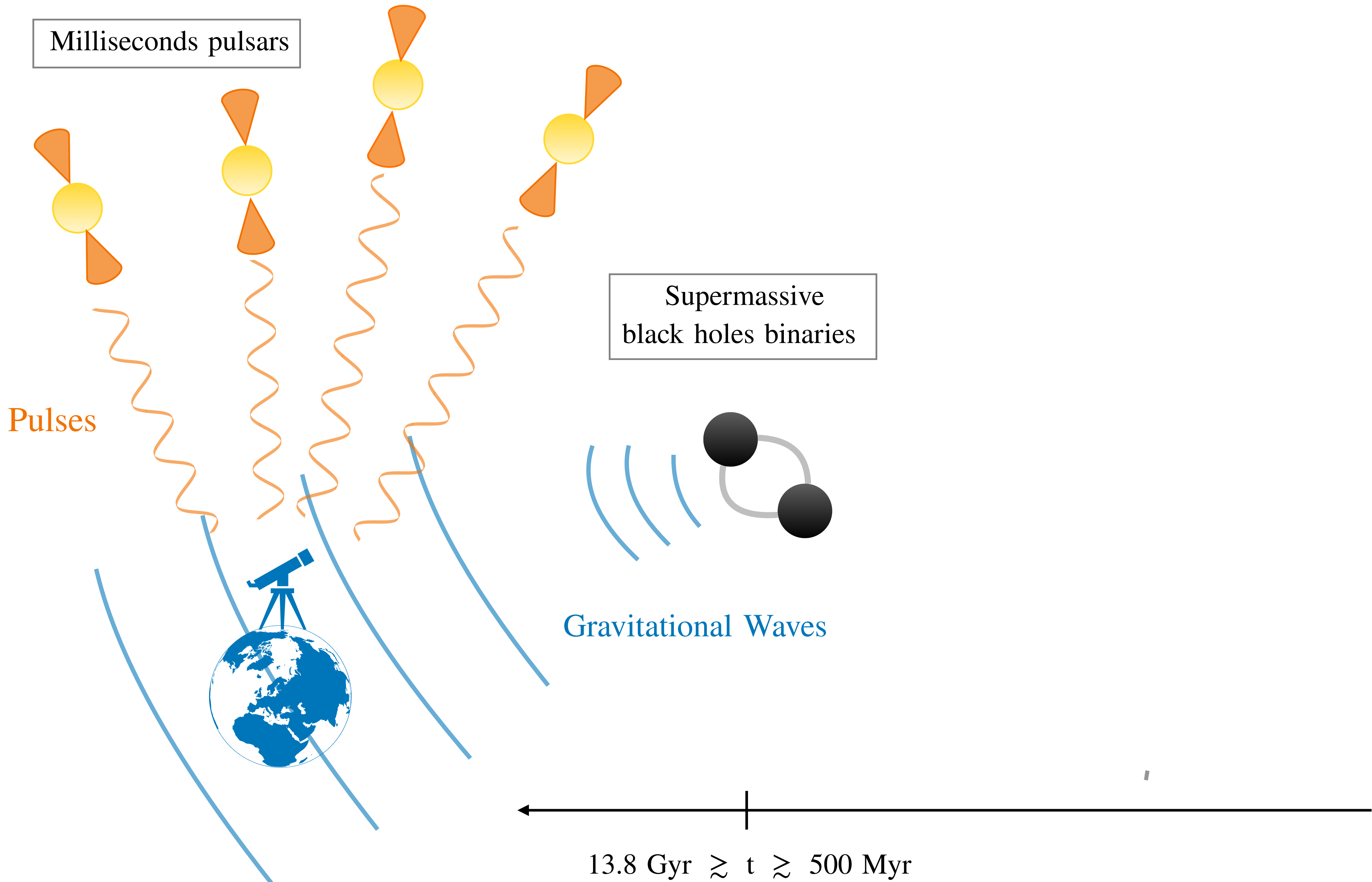
Milliseconds pulsars

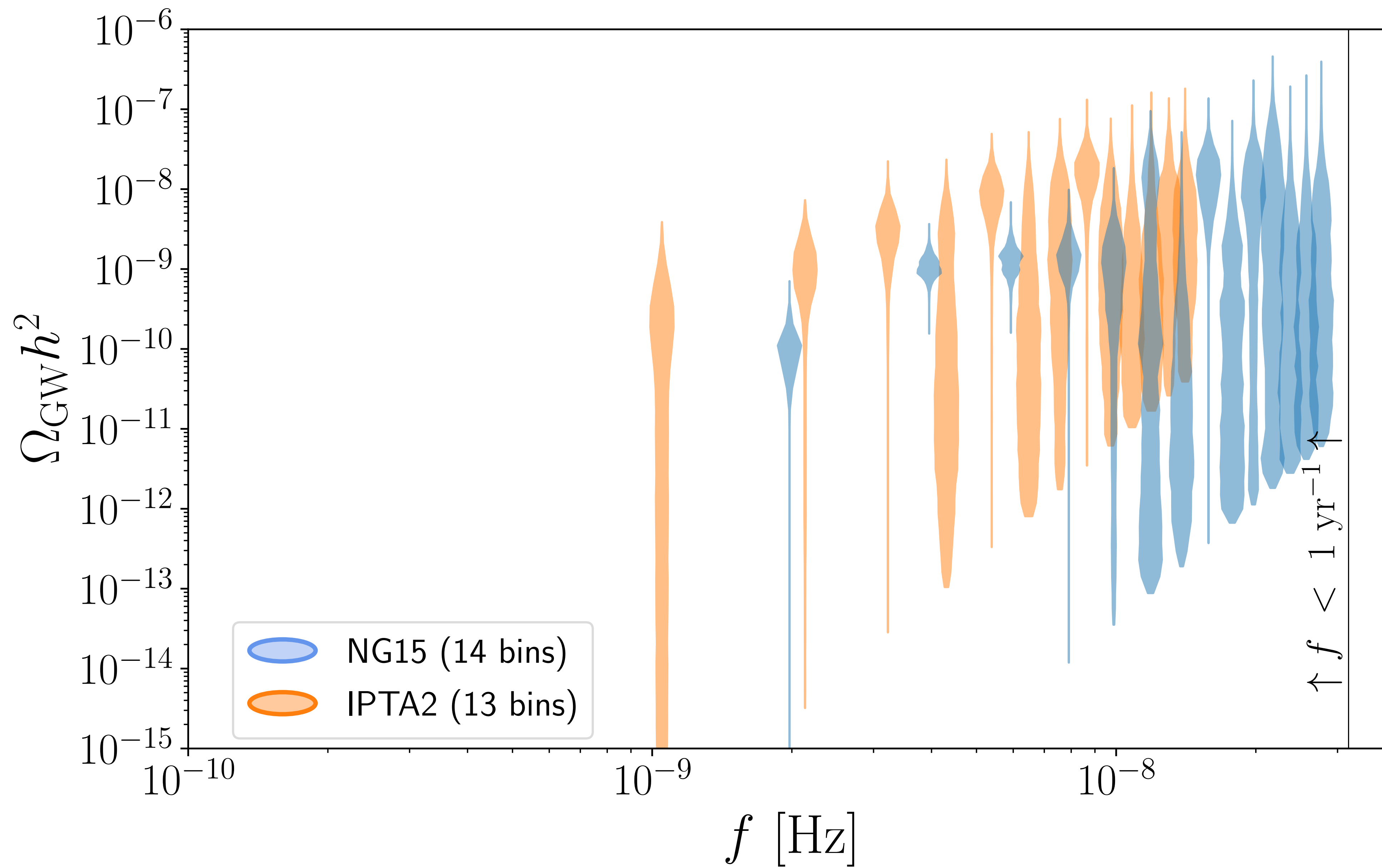
Supermassive
black holes binaries

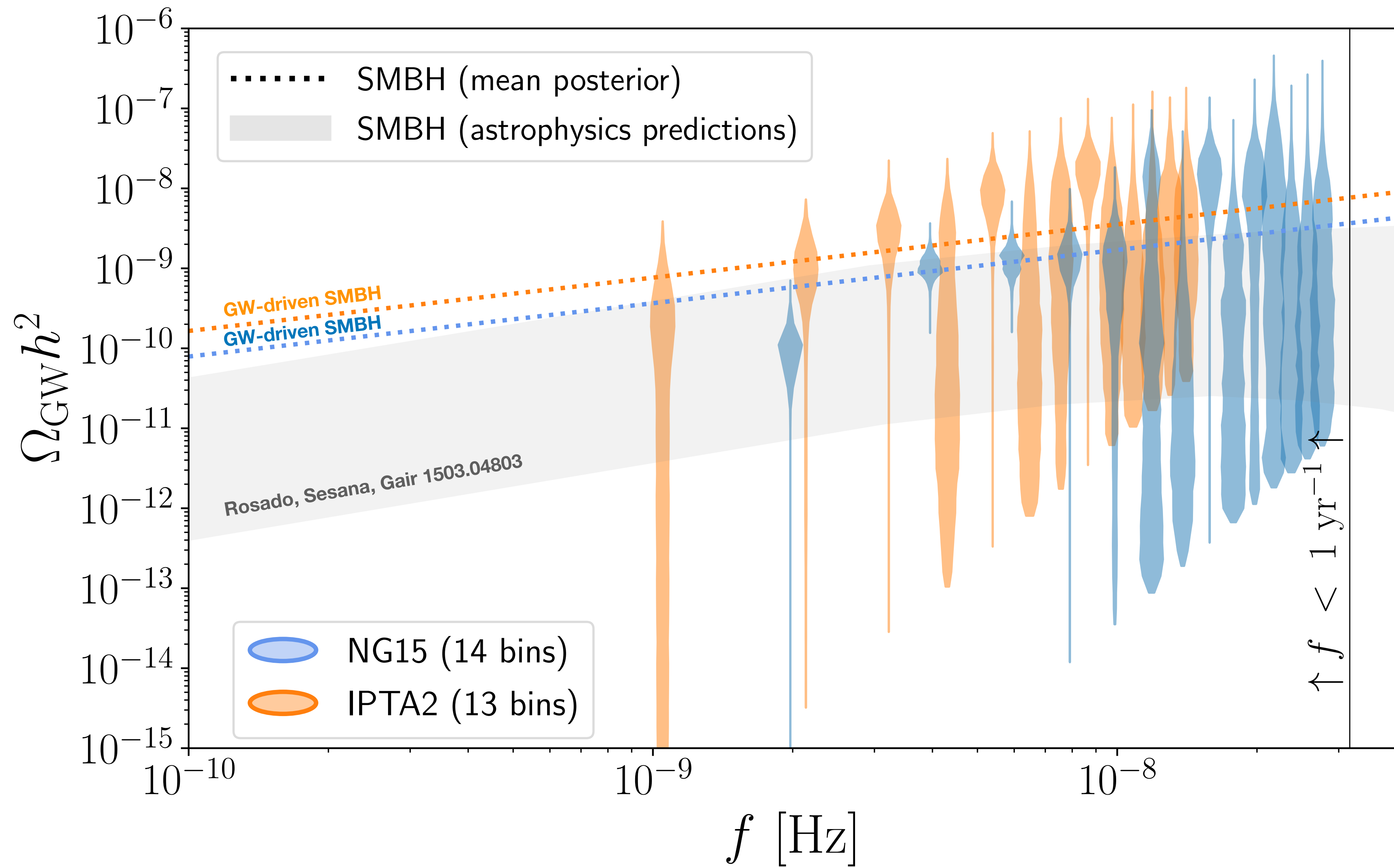
Pulses

Gravitational Waves

13.8 Gyr \gtrsim t \gtrsim 500 Myr







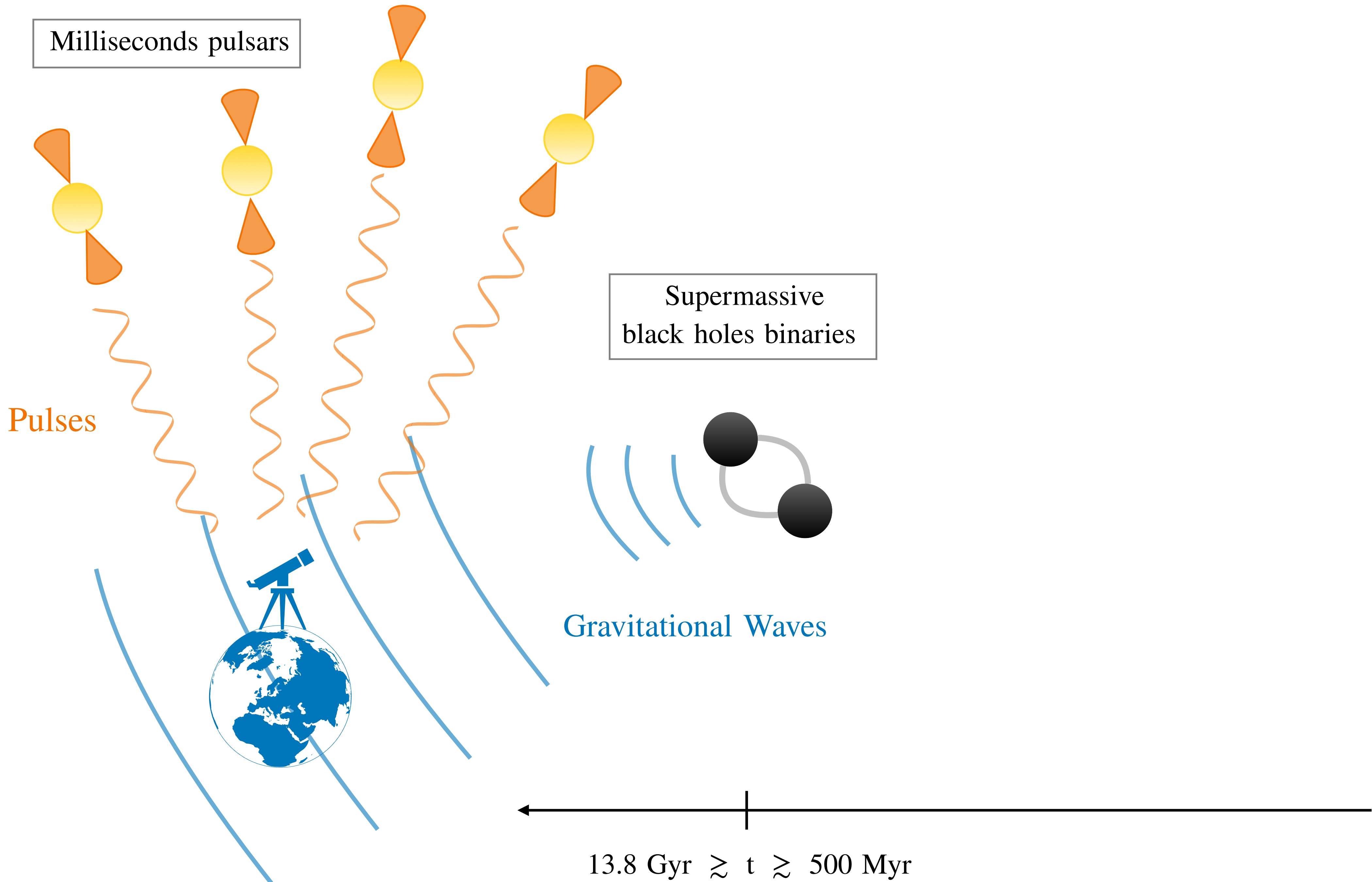
Milliseconds pulsars

Supermassive
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Pulses

Gravitational Waves

13.8 Gyr \gtrsim t \gtrsim 500 Myr



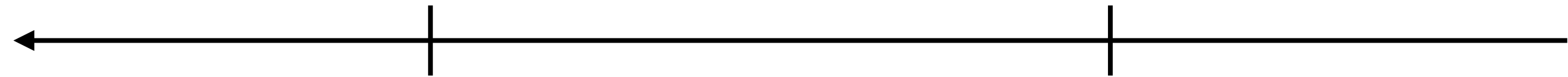
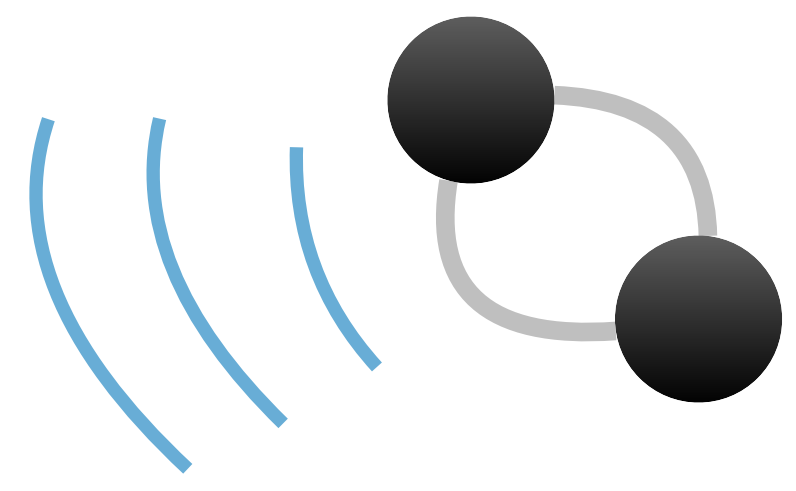
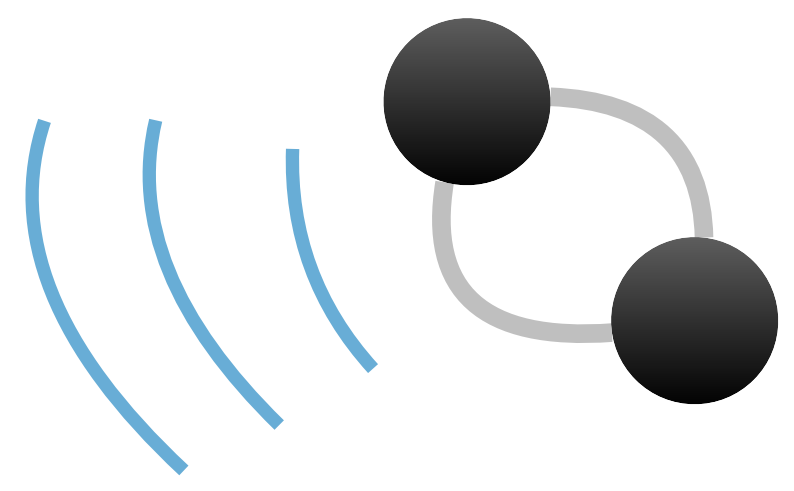
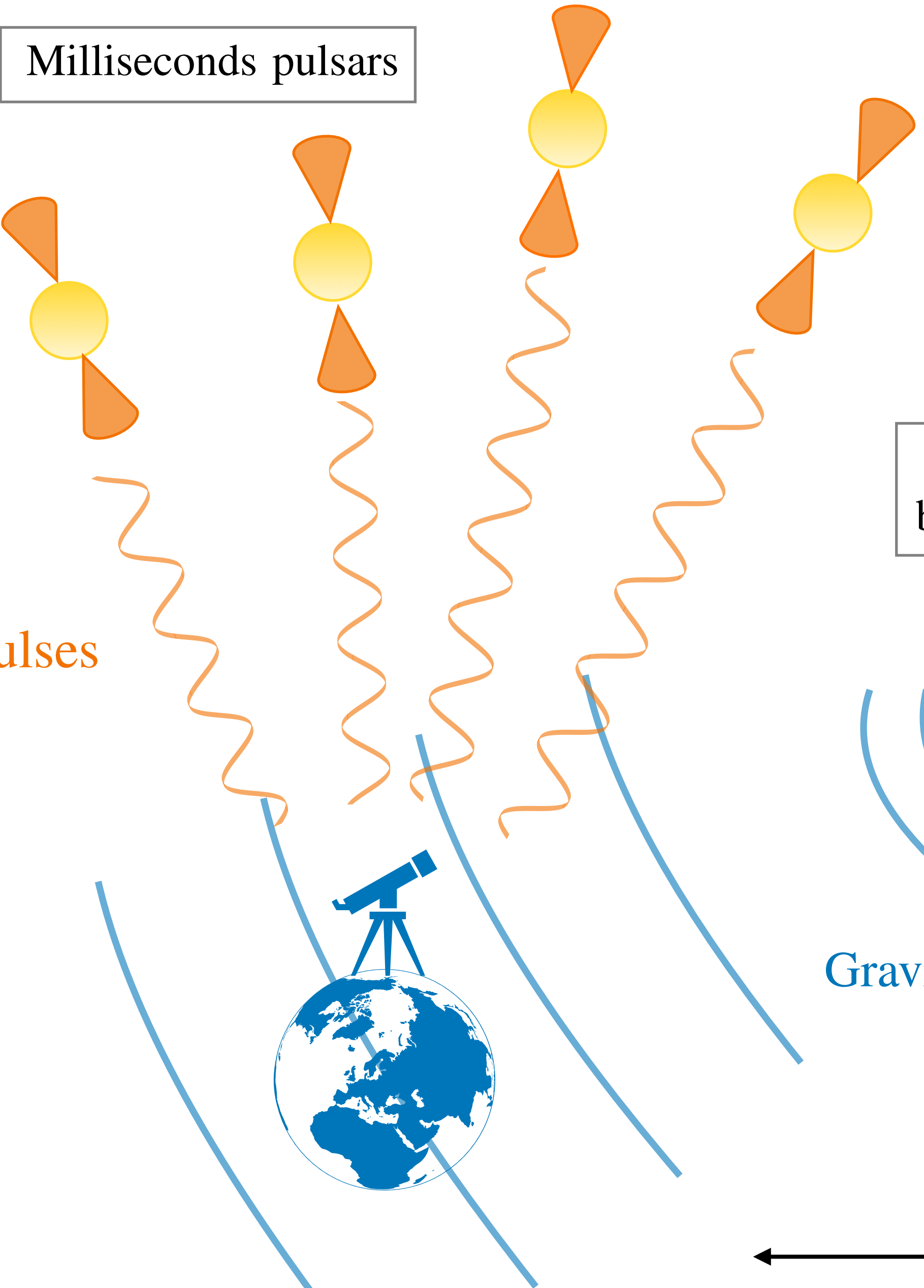
Milliseconds pulsars

Supermassive
PBH binaries

Supermassive
black holes binaries

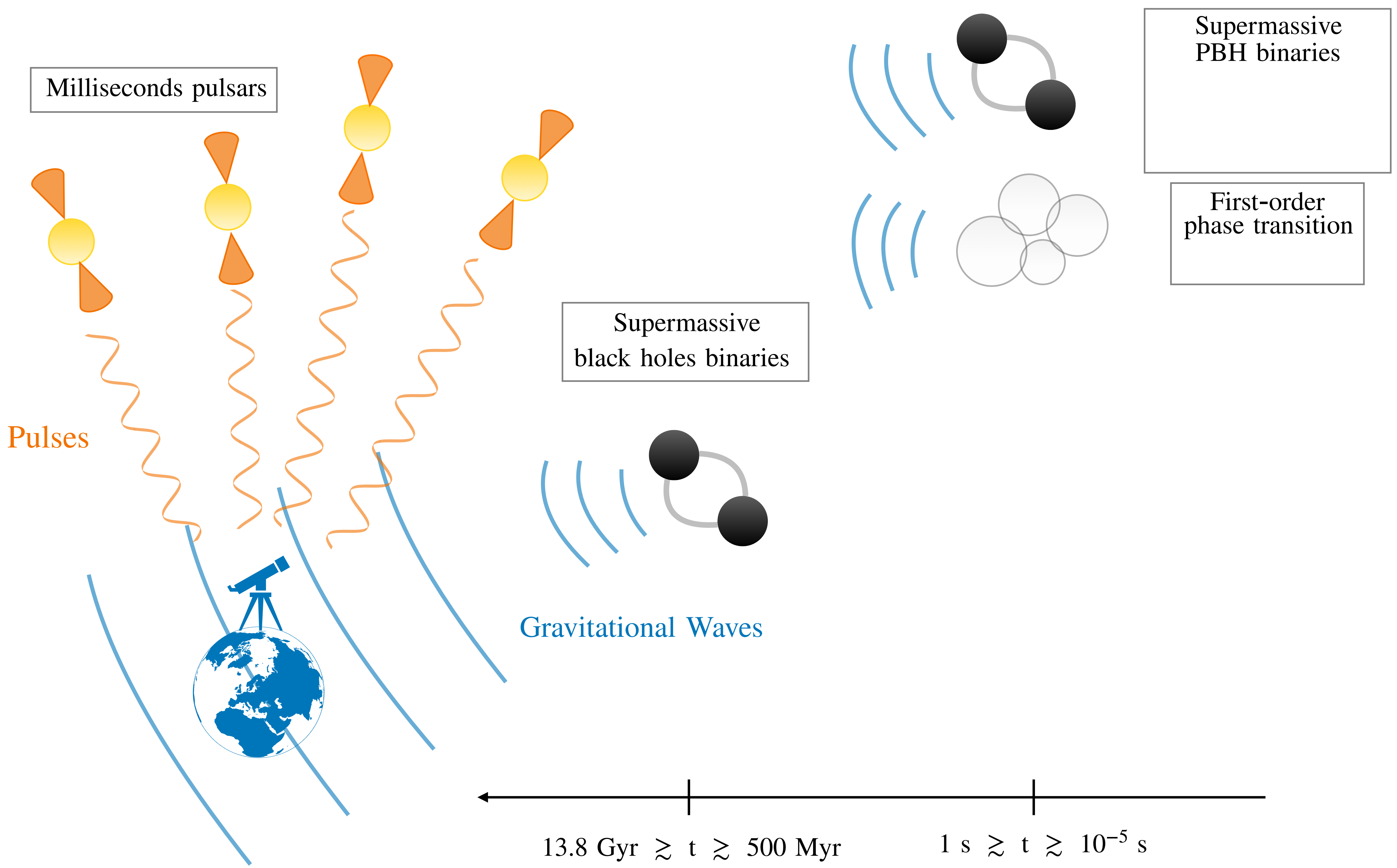
Pulses

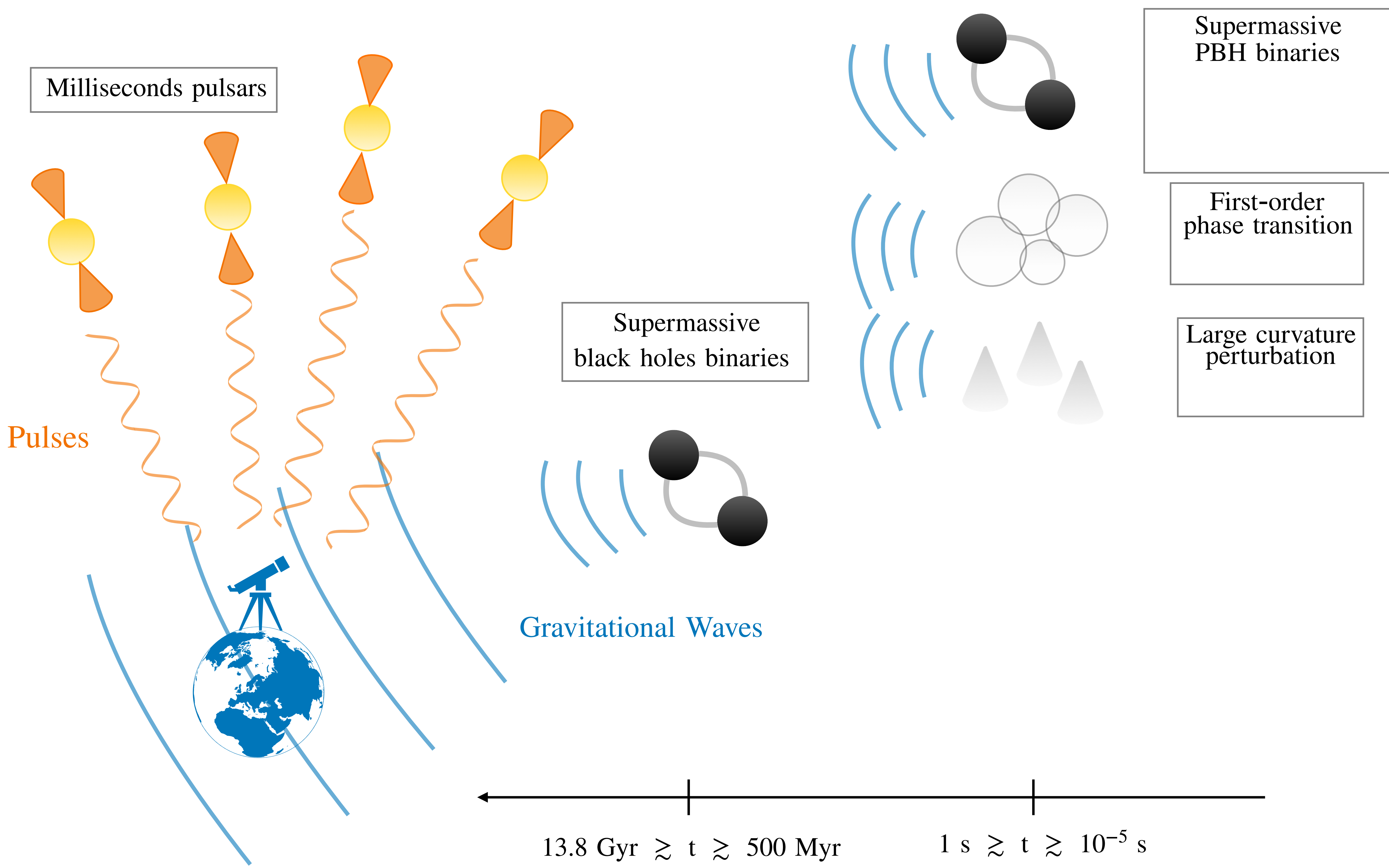
Gravitational Waves

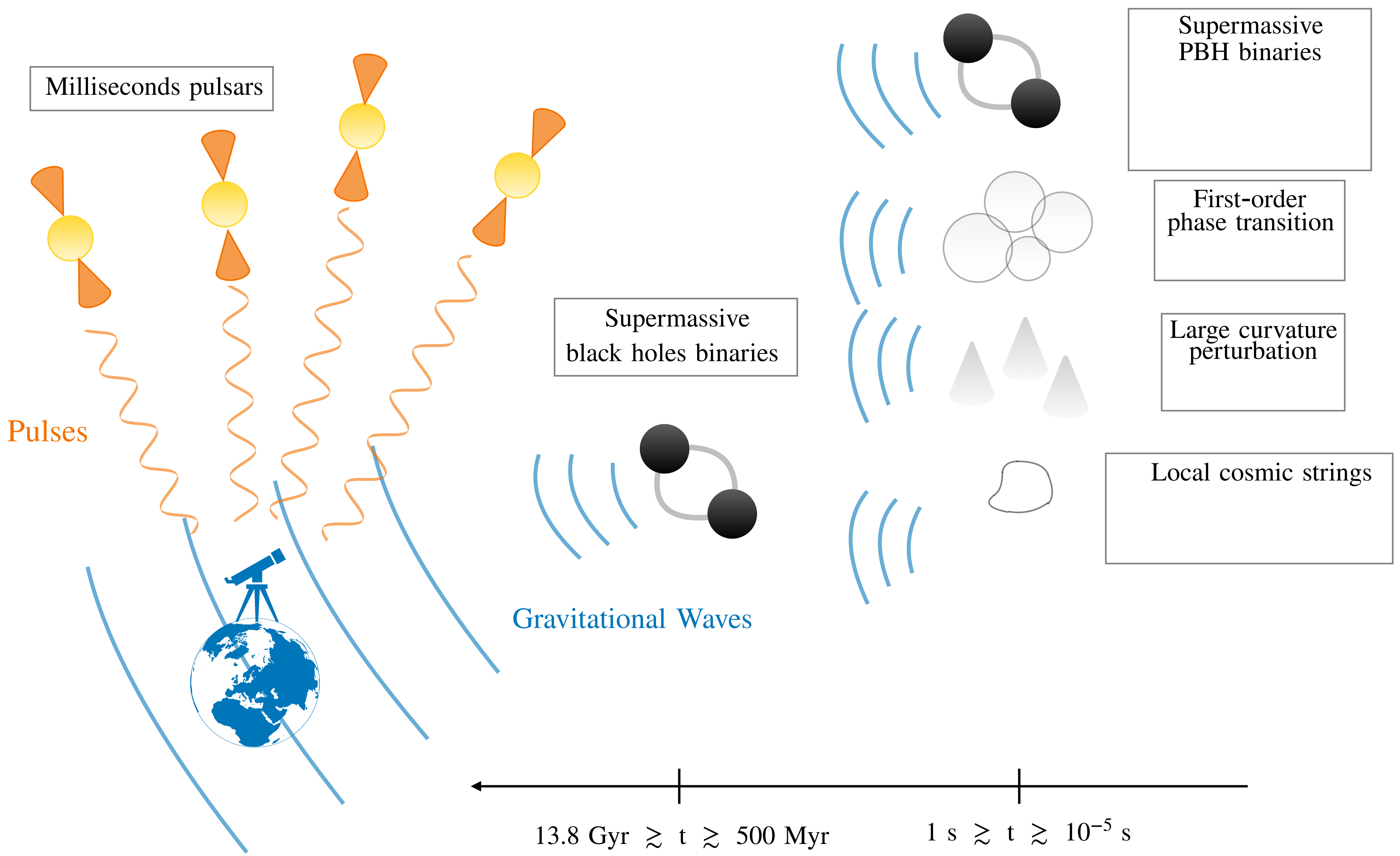


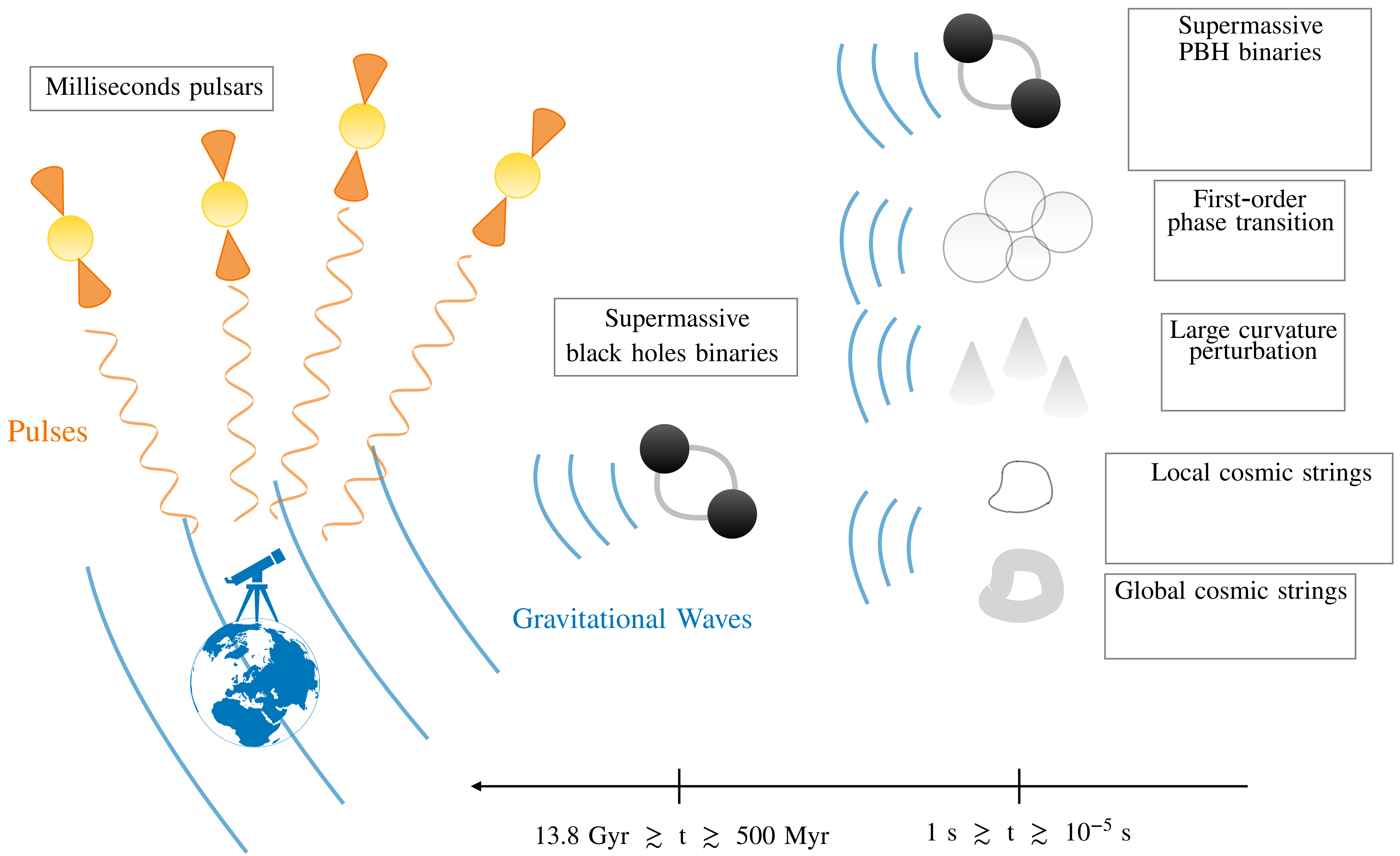
13.8 Gyr \gtrsim t \gtrsim 500 Myr

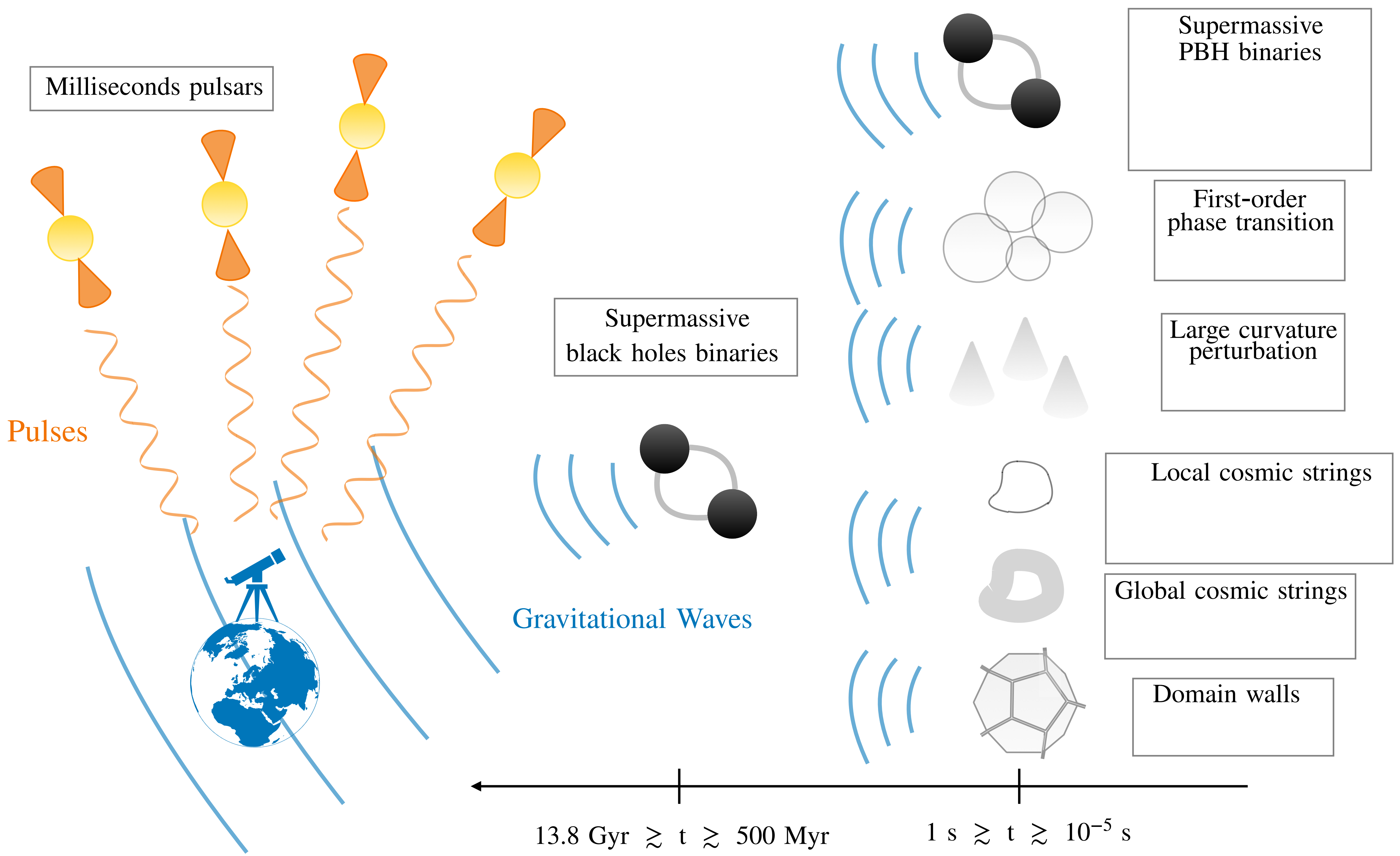
1 s \gtrsim t \gtrsim 10⁻⁵ s

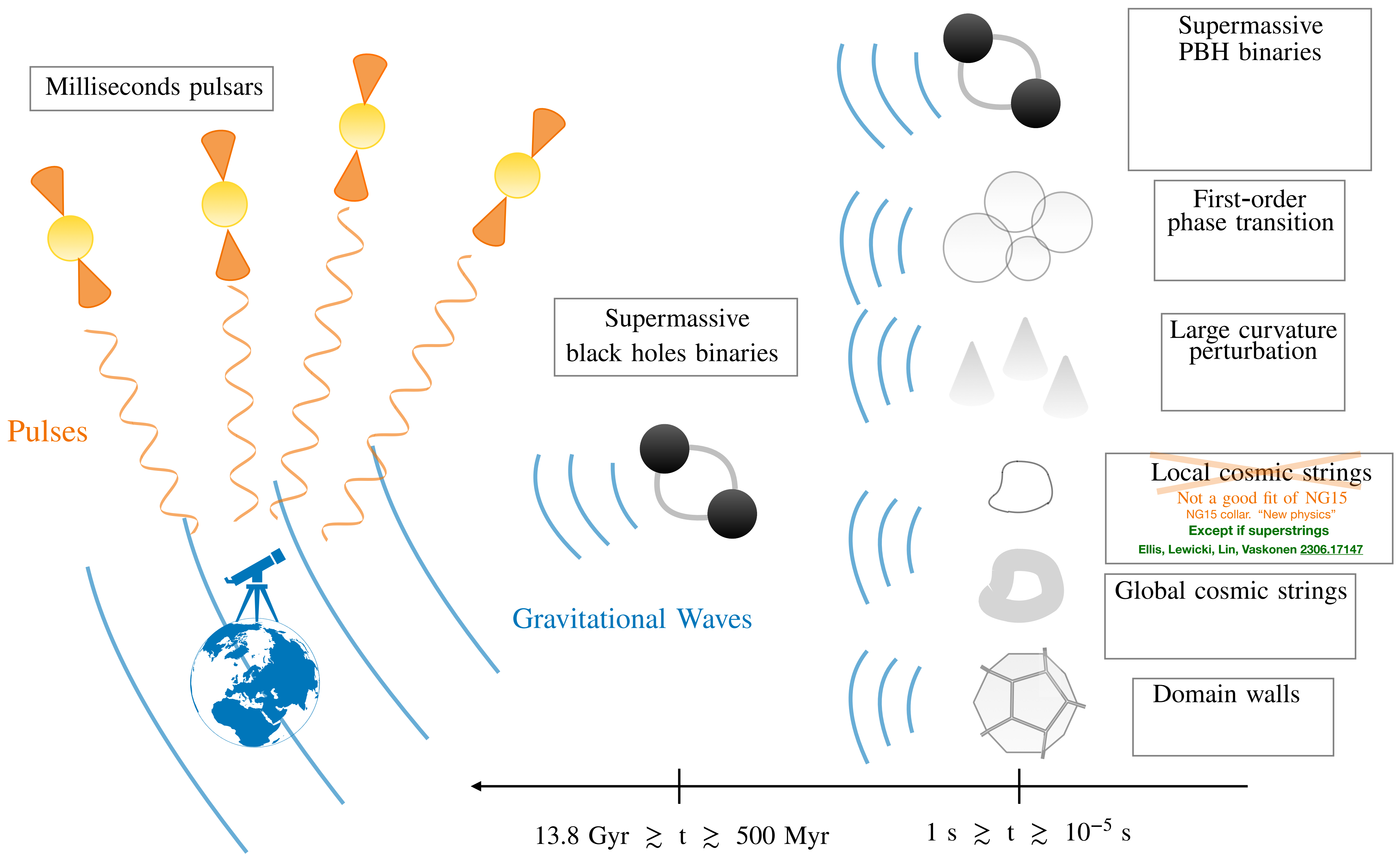


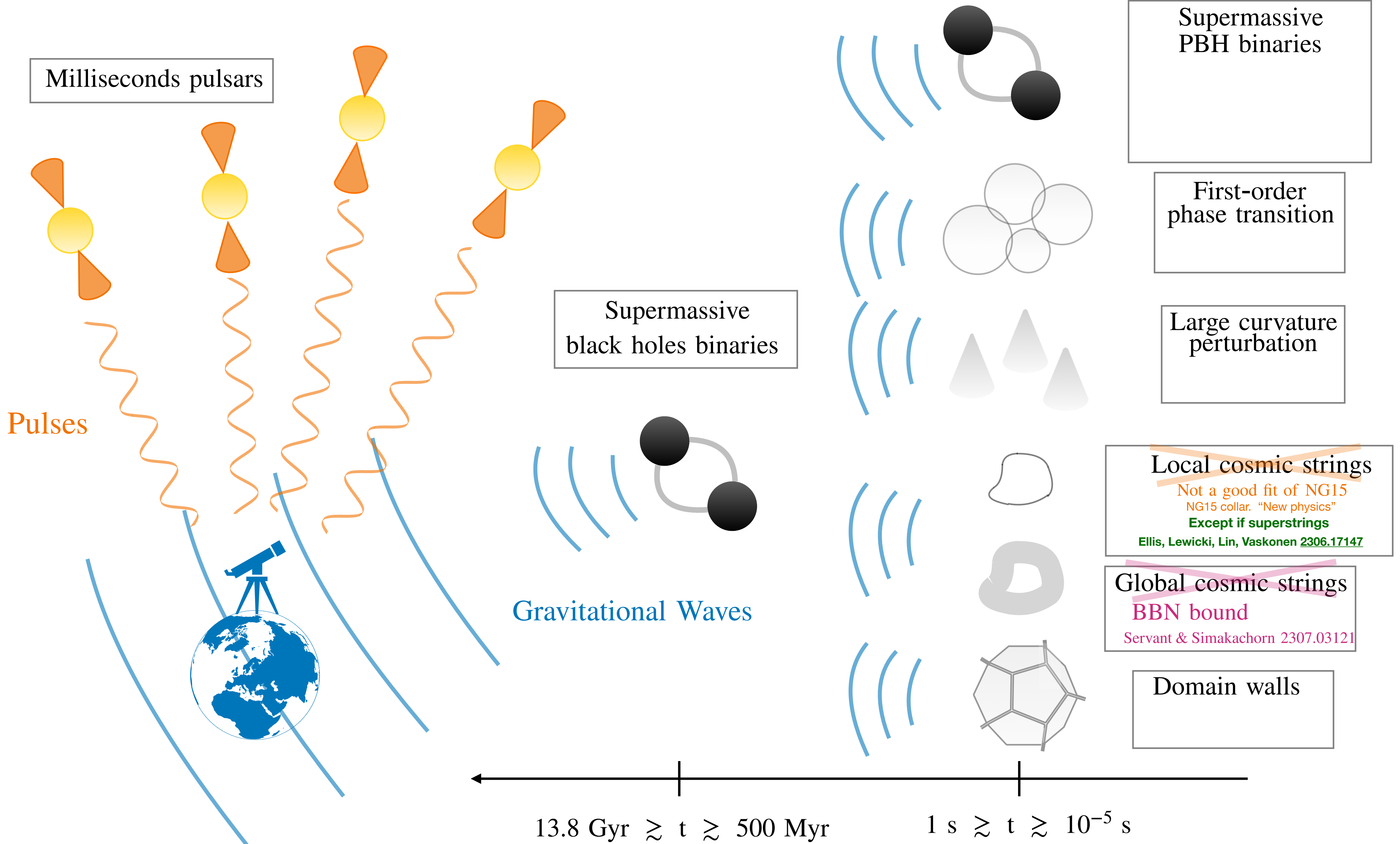


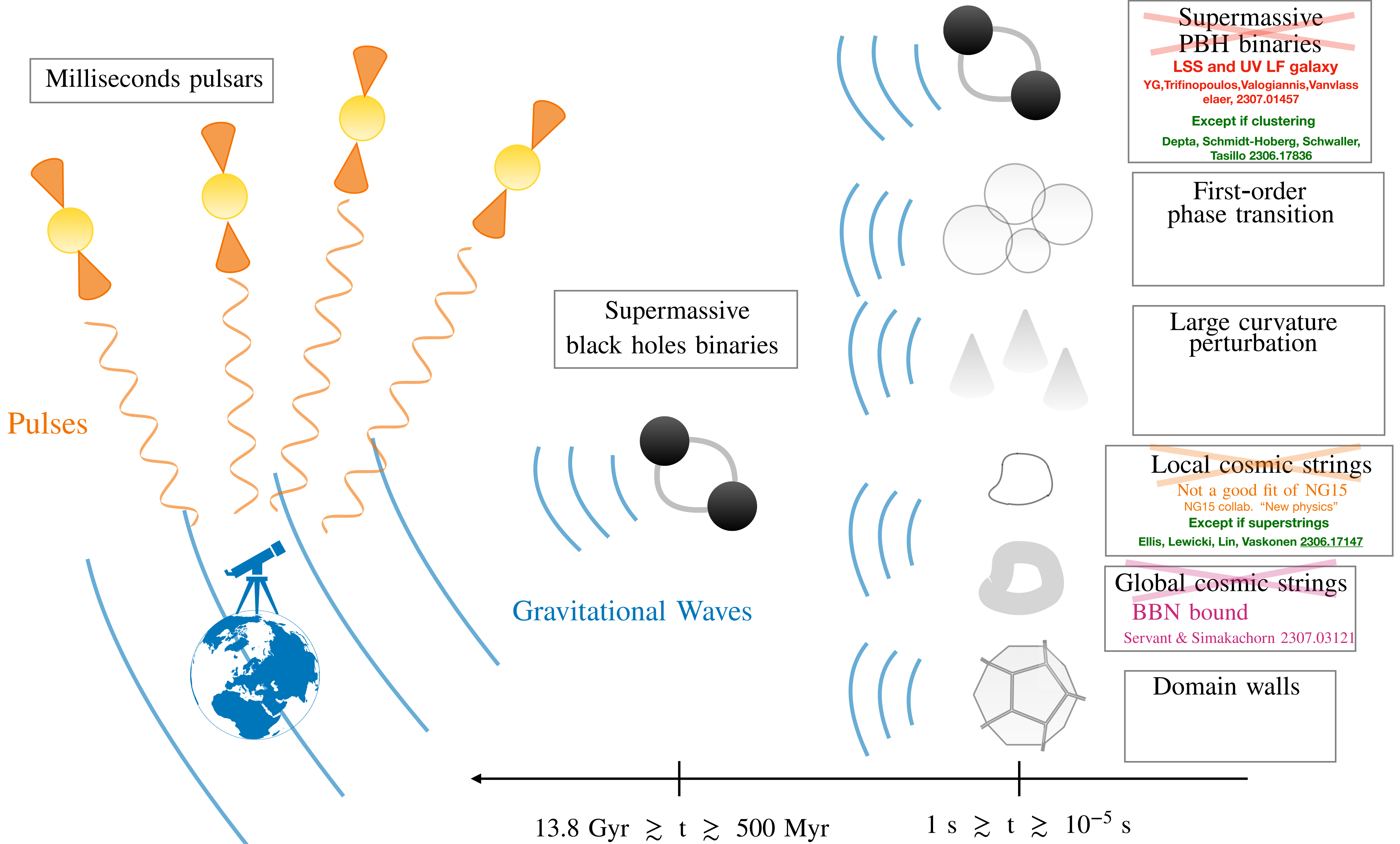












Milliseconds pulsars

Pulses

Supermassive black holes binaries

Gravitational Waves

~~Supermassive PBH binaries~~
LSS and UV LF galaxy
 YG, Trifinopoulos, Valogiannis, Vanvlasselaer, 2307.01457
 Except if clustering
 Depta, Schmidt-Hoberg, Schwaller, Tasillo 2306.17836

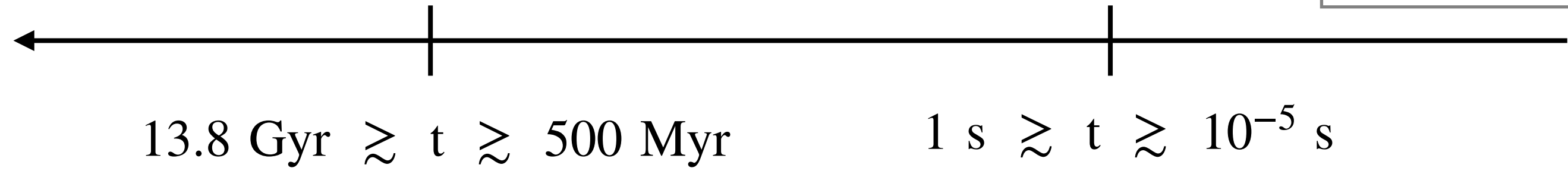
First-order phase transition

Large curvature perturbation

~~Local cosmic strings~~
 Not a good fit of NG15
 NG15 collab. "New physics"
 Except if superstrings
 Ellis, Lewicki, Lin, Vaskonen 2306.17147

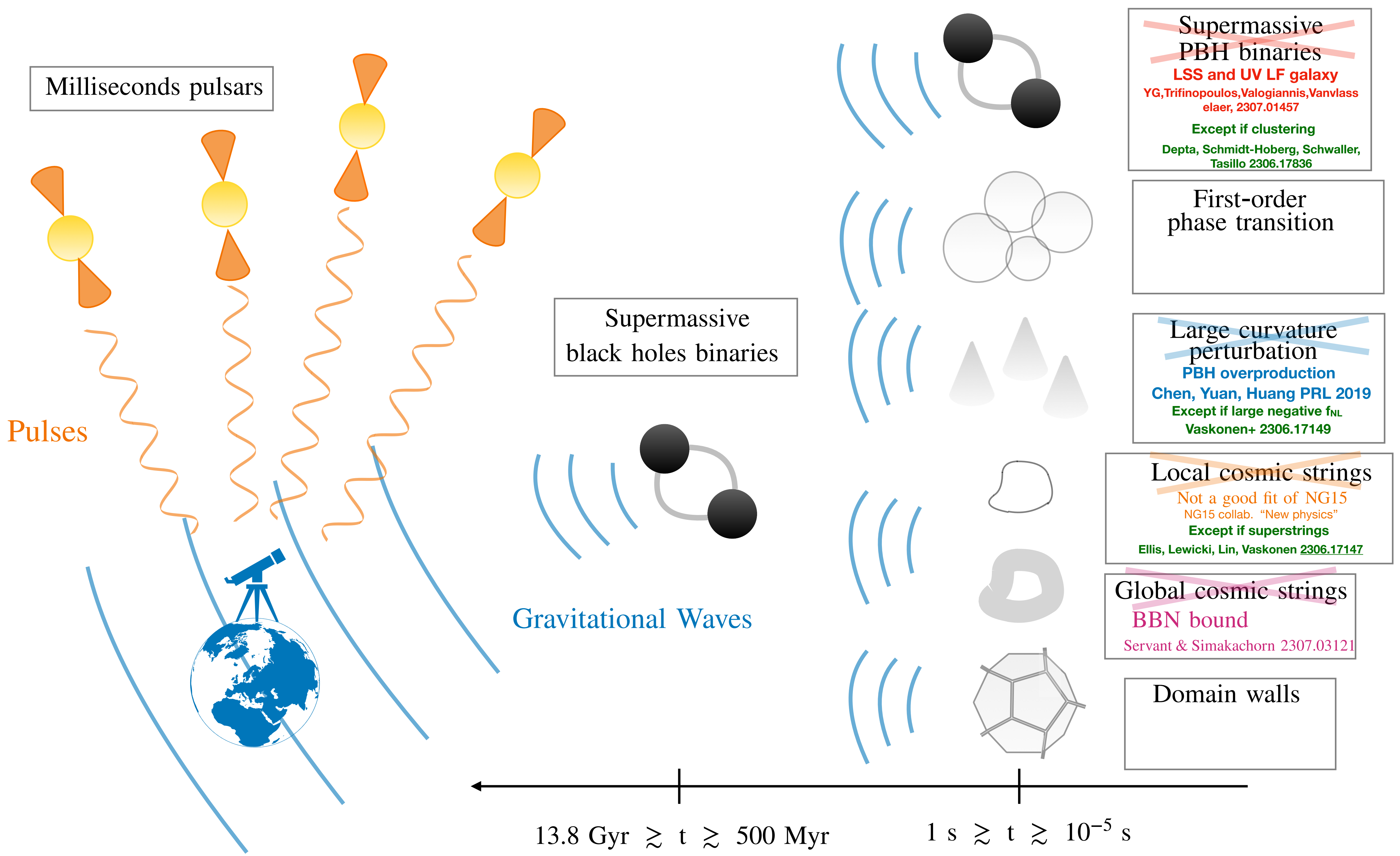
~~Global cosmic strings~~
BBN bound
 Servant & Simakachorn 2307.03121

Domain walls



13.8 Gyr \gtrsim t \gtrsim 500 Myr

1 s \gtrsim t \gtrsim 10^{-5} s



~~Supermassive PBH binaries~~
LSS and UV LF galaxy
 YG, Trifinopoulos, Valogiannis, Vanvlasselaer, 2307.01457
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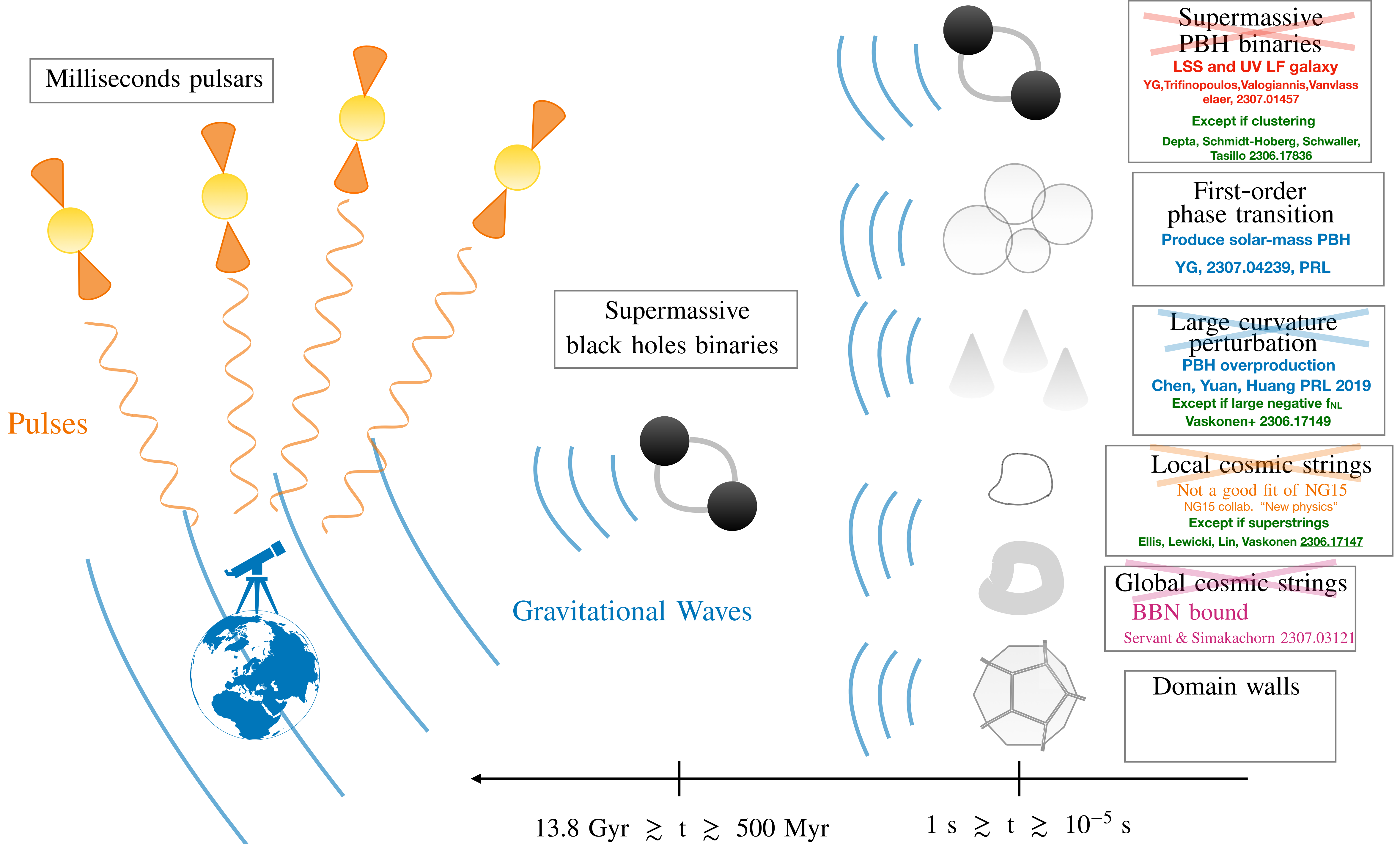
First-order phase transition

~~Large curvature perturbation~~
PBH overproduction
 Chen, Yuan, Huang PRL 2019
 Except if large negative f_{NL}
 Vaskonen+ 2306.17149

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Domain walls



Milliseconds pulsars

Pulses

Supermassive black holes binaries

Gravitational Waves

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LSS and UV LF galaxy
 YG, Trifinopoulos, Valogiannis, Vanvlasselaer, 2307.01457
 Except if clustering
 Depta, Schmidt-Hoberg, Schwaller, Tasillo 2306.17836

First-order phase transition
 Produce solar-mass PBH
 YG, 2307.04239, PRL

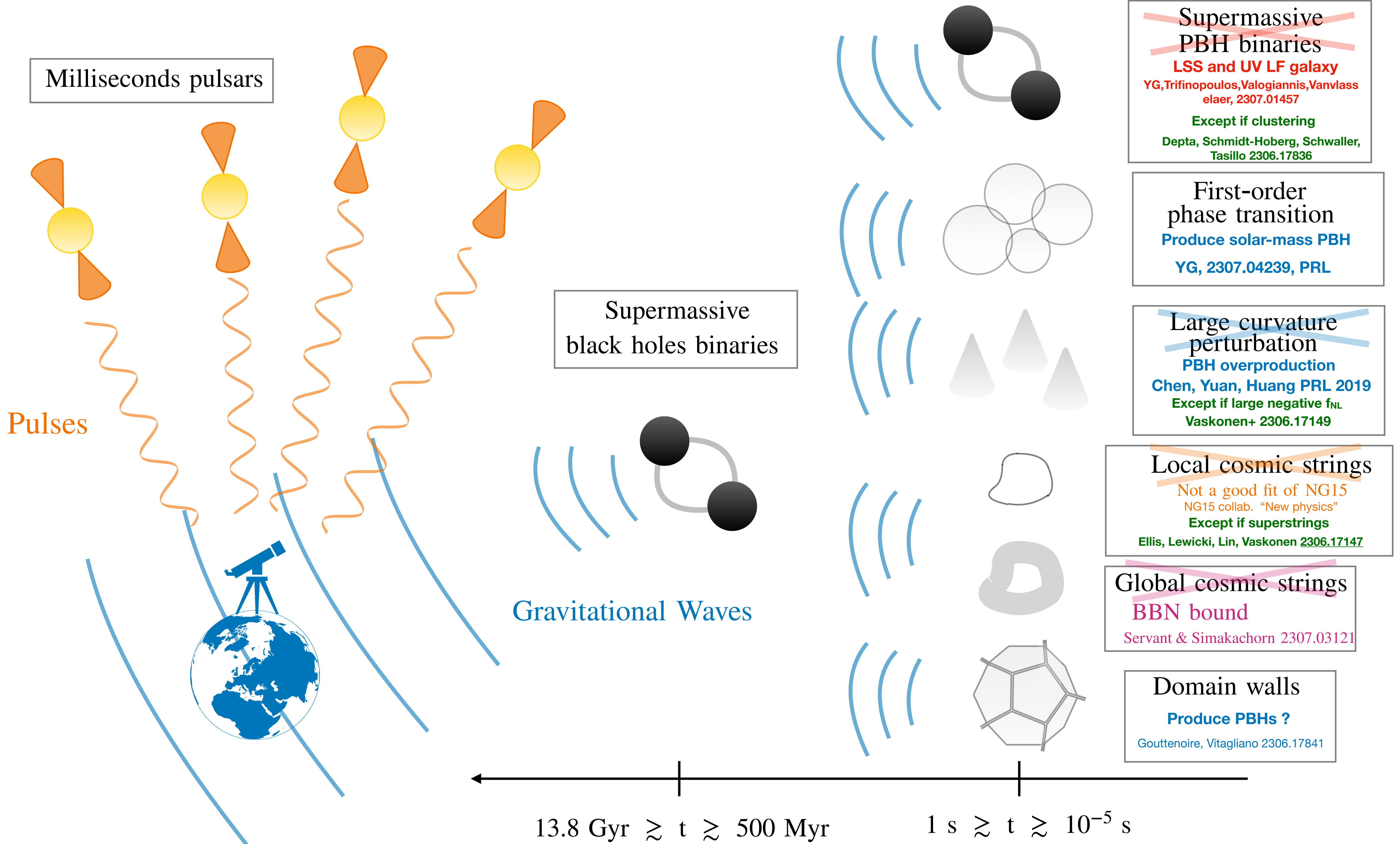
~~Large curvature perturbation~~
 PBH overproduction
 Chen, Yuan, Huang PRL 2019
 Except if large negative f_{NL}
 Vaskonen+ 2306.17149

~~Local cosmic strings~~
 Not a good fit of NG15
 NG15 collab. "New physics"
 Except if superstrings
 Ellis, Lewicki, Lin, Vaskonen 2306.17147

~~Global cosmic strings~~
 BBN bound
 Servant & Simakachorn 2307.03121

Domain walls





Milliseconds pulsars

Pulses

Supermassive black holes binaries

Gravitational Waves

~~Supermassive PBH binaries~~
LSS and UV LF galaxy
 YG, Trifinopoulos, Valogiannis, Vanvlasselaer, 2307.01457
 Except if clustering
 Depta, Schmidt-Hoberg, Schwaller, Tasillo 2306.17836

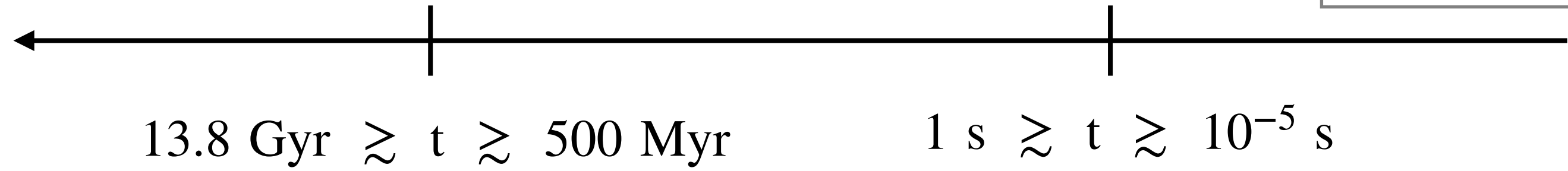
First-order phase transition
Produce solar-mass PBH
 YG, 2307.04239, PRL

~~Large curvature perturbation~~
PBH overproduction
 Chen, Yuan, Huang PRL 2019
 Except if large negative f_{NL}
 Vaskonen+ 2306.17149

~~Local cosmic strings~~
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 Ellis, Lewicki, Lin, Vaskonen 2306.17147

~~Global cosmic strings~~
BBN bound
 Servant & Simakachorn 2307.03121

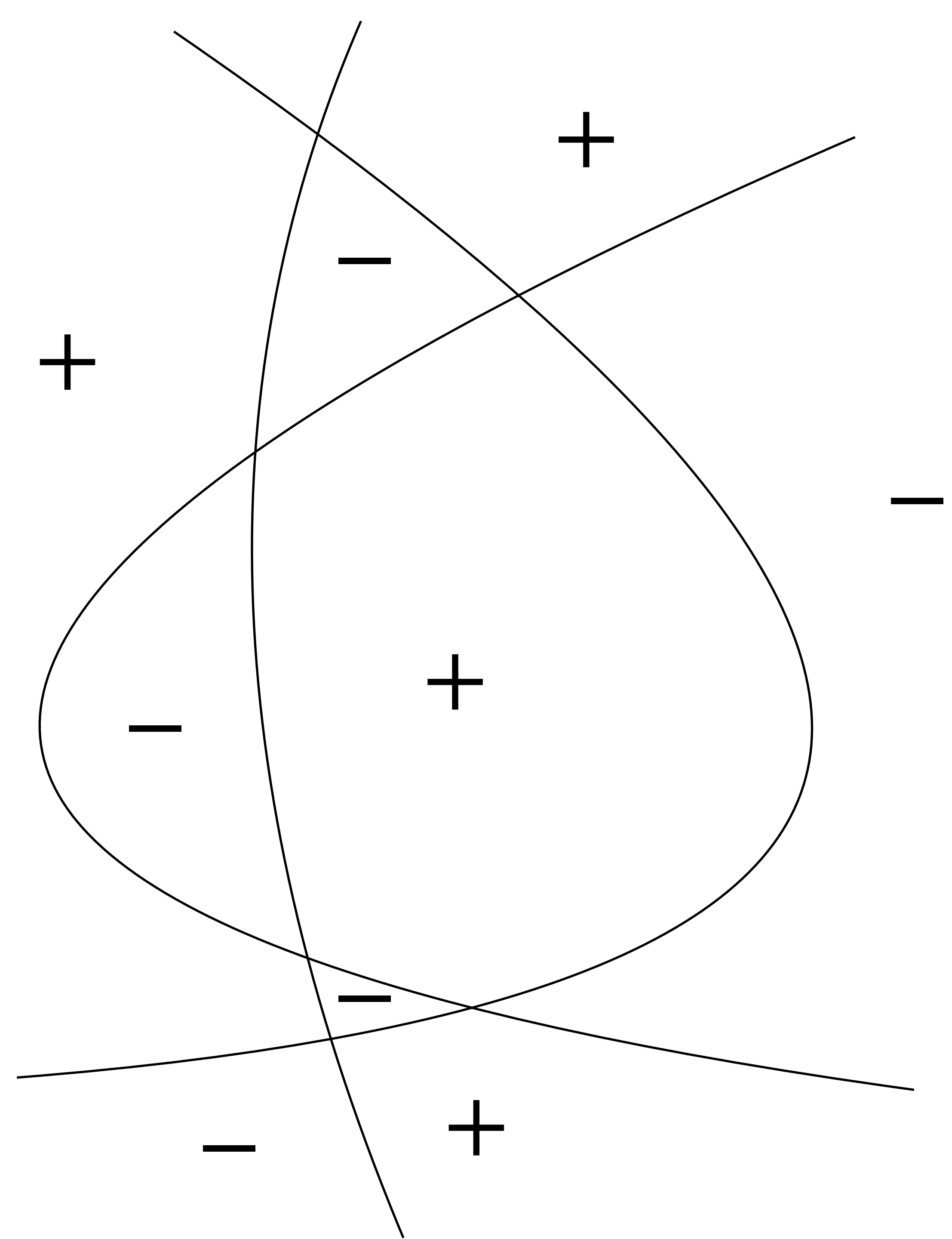
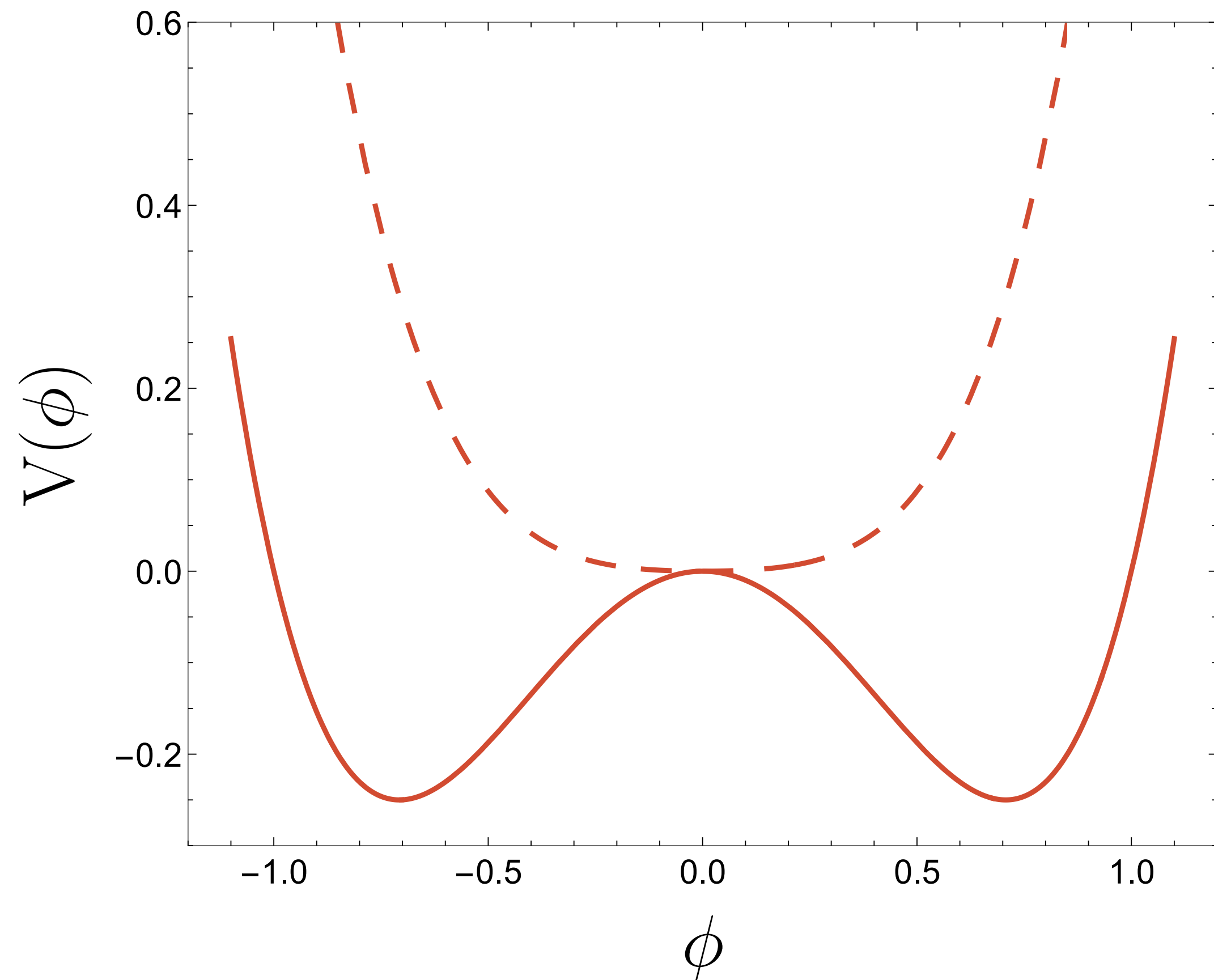
Domain walls
Produce PBHs ?
 Gouttenoire, Vitagliano 2306.17841



Formation of Domain Wall

$$V(\phi) = \lambda(\phi^2 - v_\phi^2)^2$$

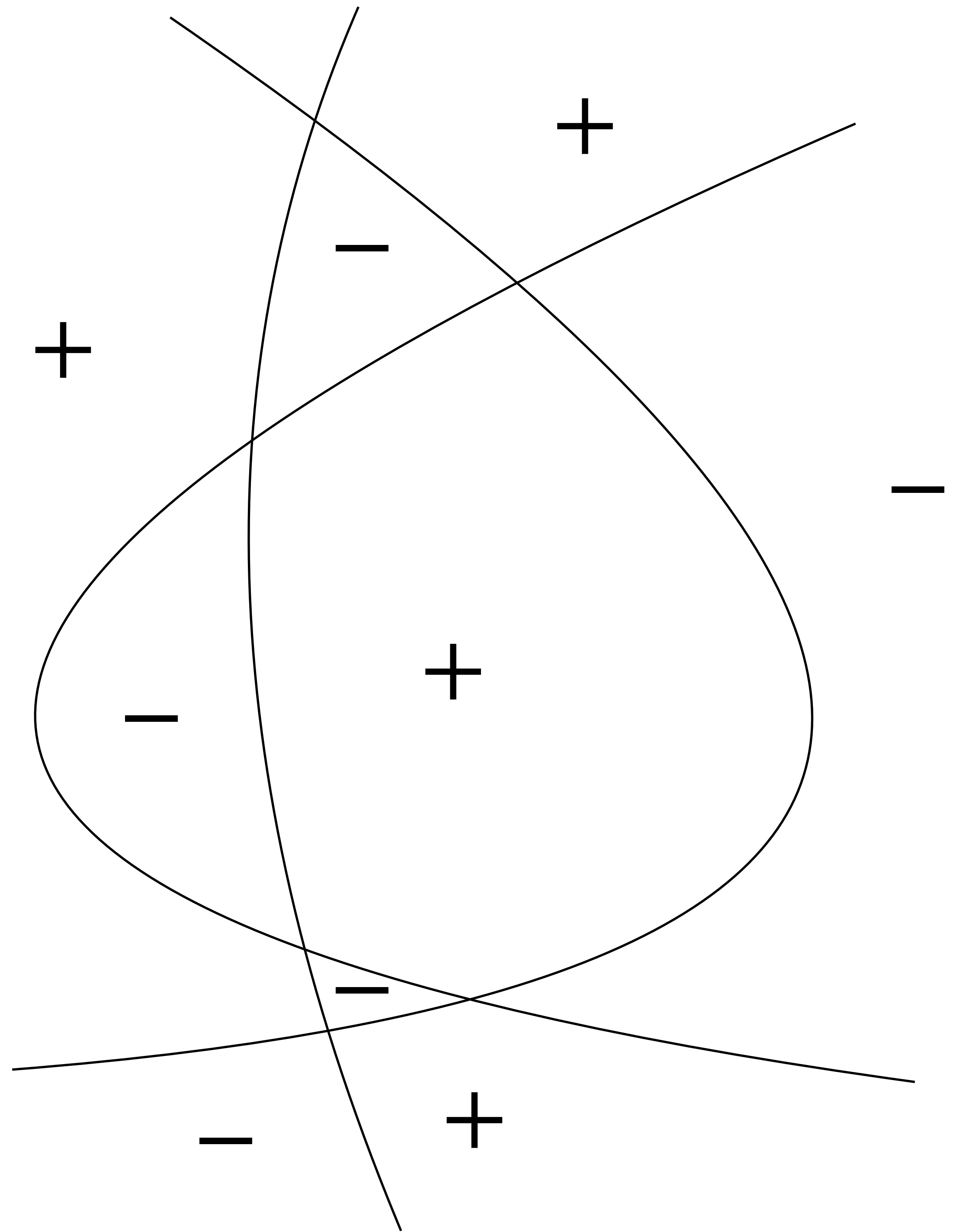
Break \mathbb{Z}_2



Formation of Domain Wall

Scaling regime : $R \simeq t$

$$\rho_{\text{DW}} \simeq \frac{\sigma}{R} \simeq \frac{\sigma}{t}$$

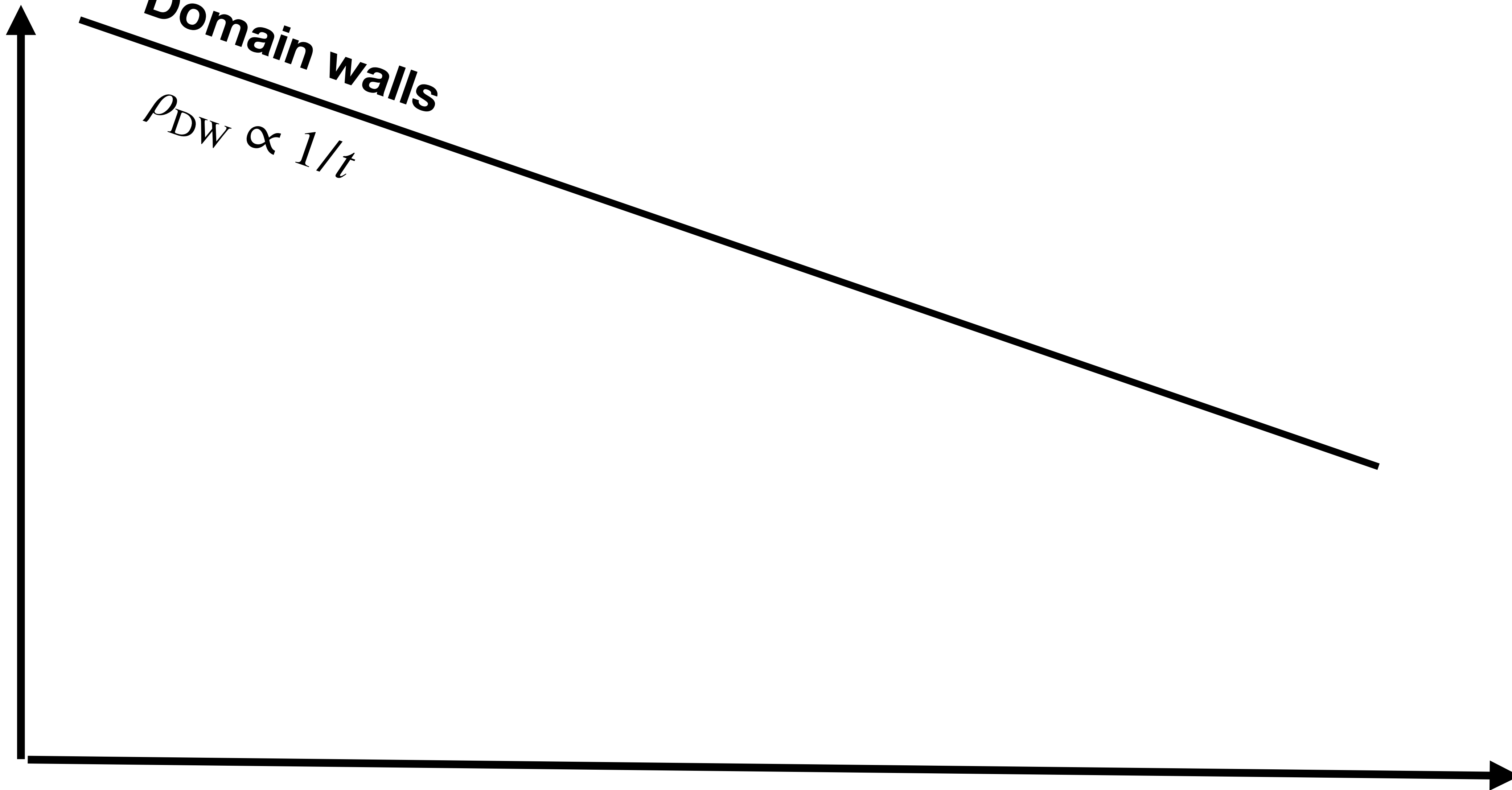


Energy density

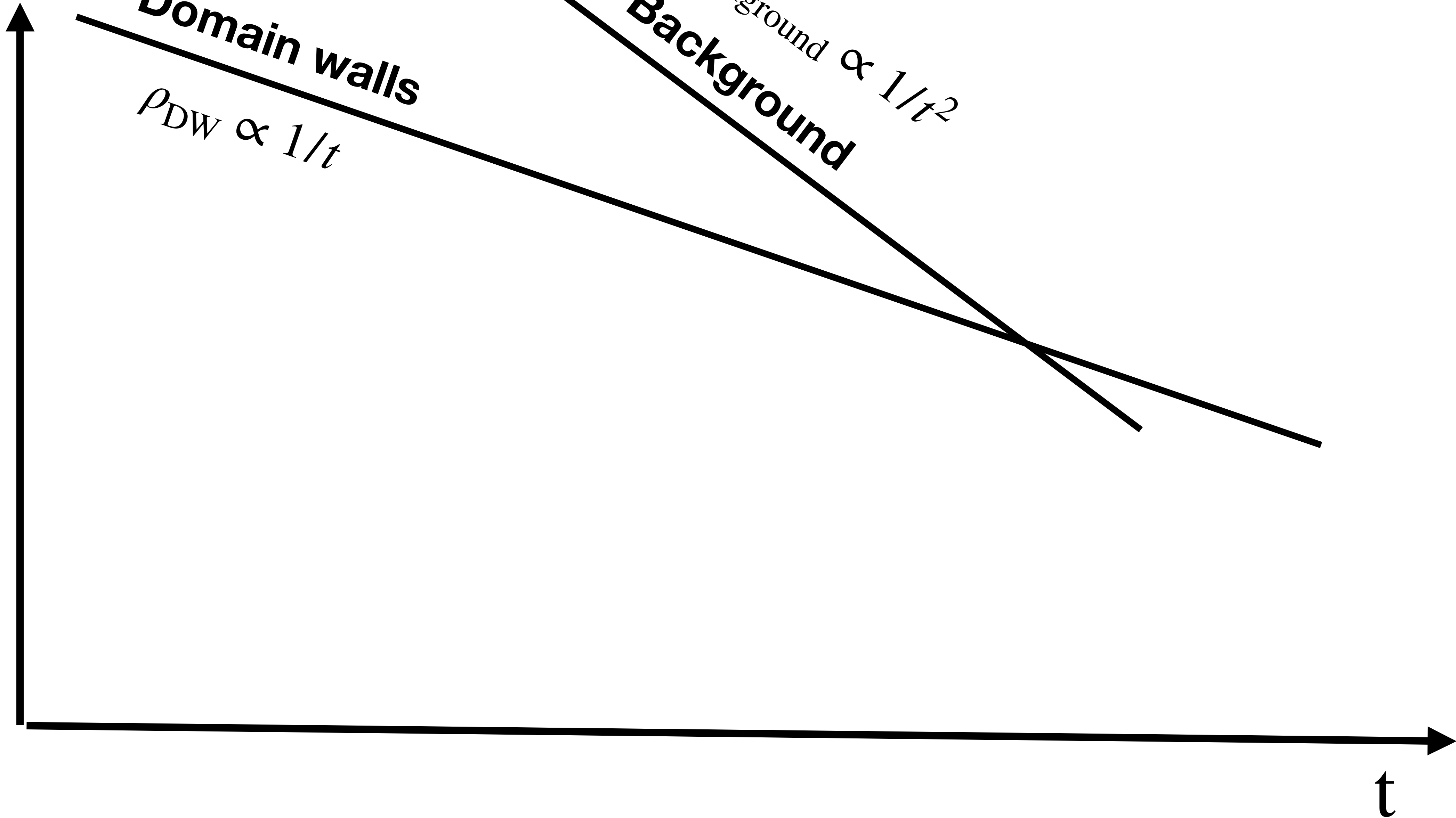
Domain walls

$$\rho_{DW} \propto 1/t$$

t



Energy density



Energy density

Domain walls

$$\rho_{DW} \propto 1/t$$

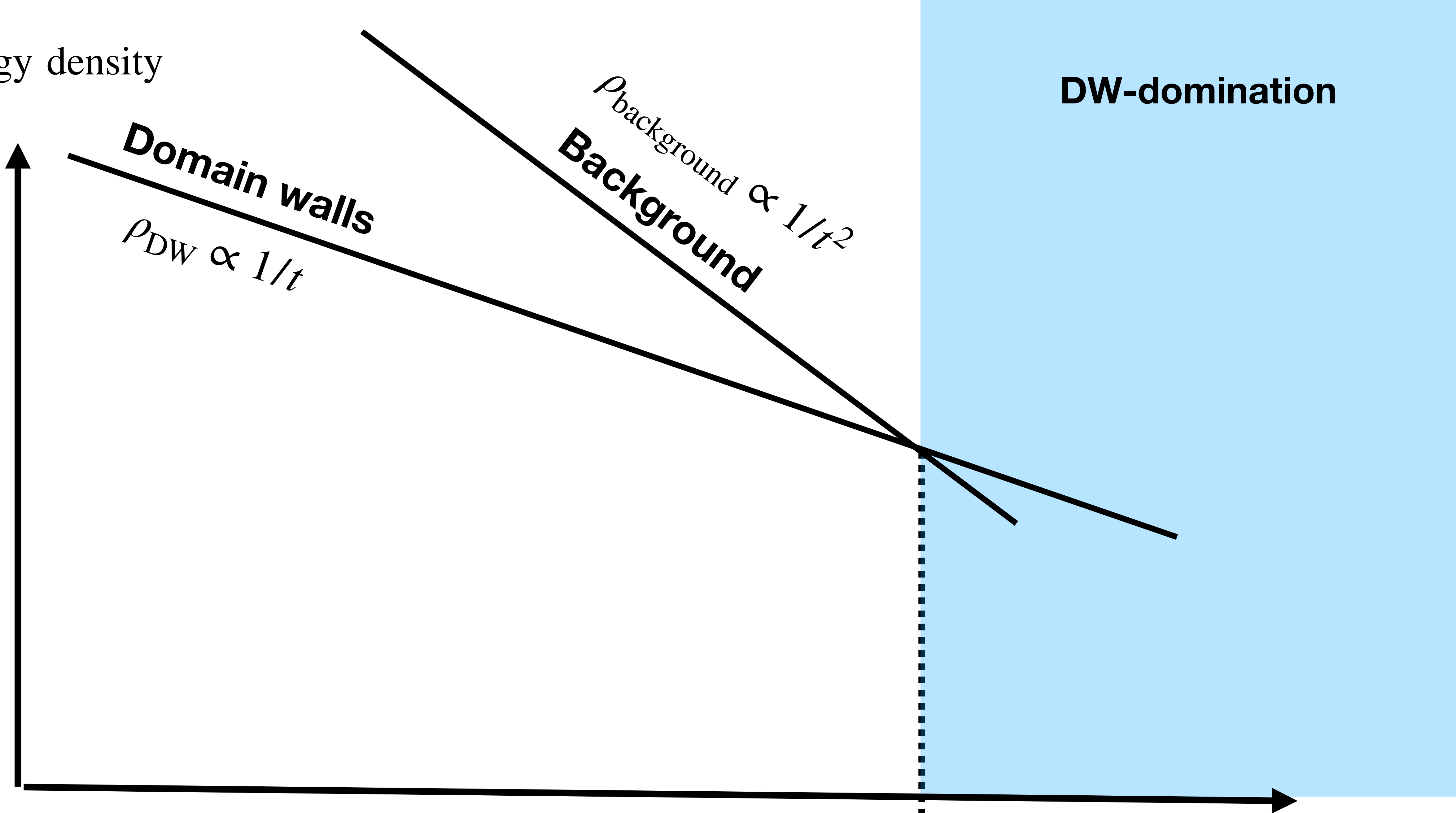
Background

$$\rho_{\text{background}} \propto 1/t^2$$

DW-domination

t_{dom}

t



Energy density

Domain walls

$$\rho_{DW} \propto 1/t$$

Background

$$\rho_{\text{background}} \propto 1/t^2$$

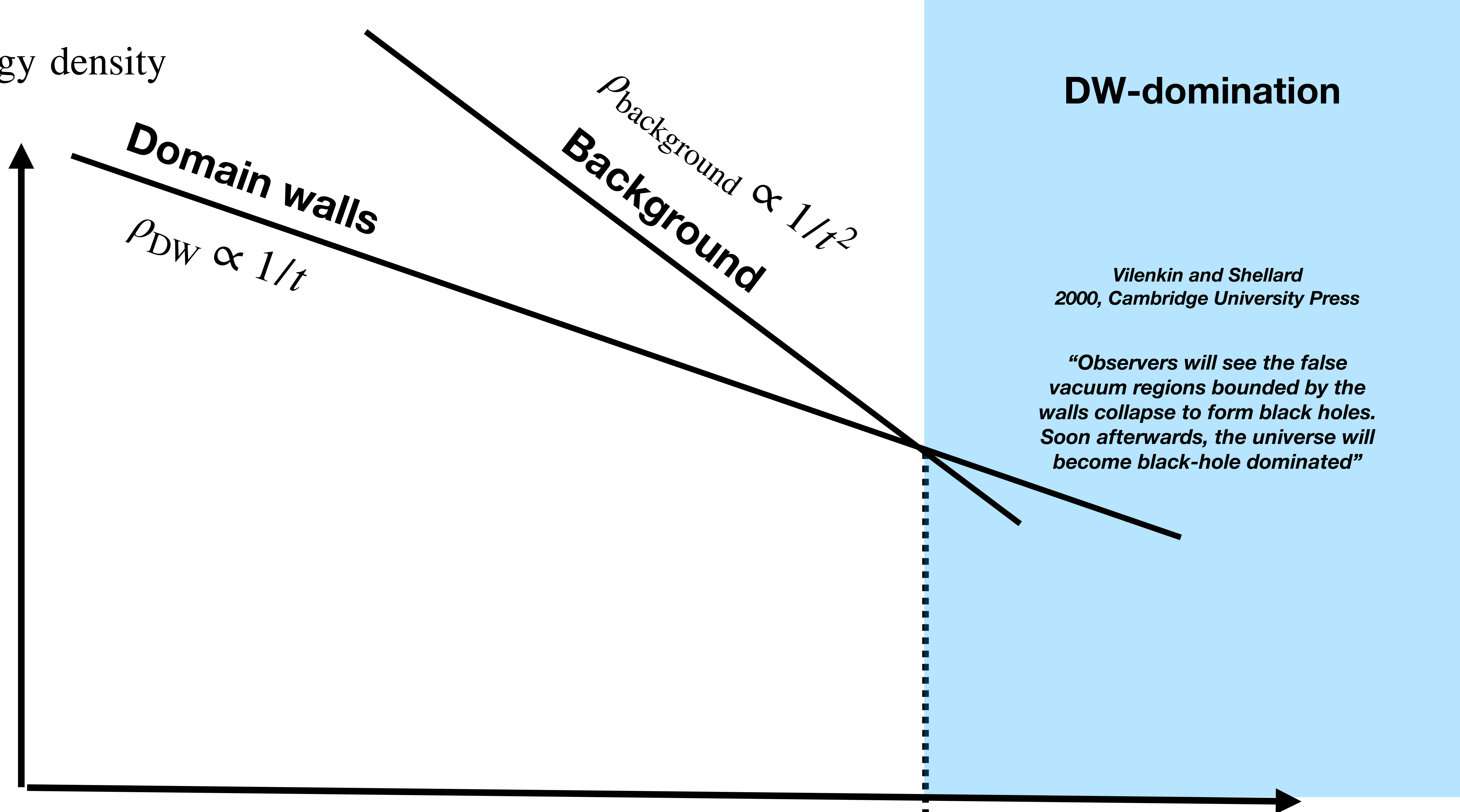
DW-domination

*Vilenkin and Shellard
2000, Cambridge University Press*

*“Observers will see the false
vacuum regions bounded by the
walls collapse to form black holes.
Soon afterwards, the universe will
become black-hole dominated”*

t_{dom}

t



Energy density

Domain walls

$$\rho_{DW} \propto 1/t$$

Background

$$\rho_{\text{background}} \propto 1/t^2$$

DW-domination

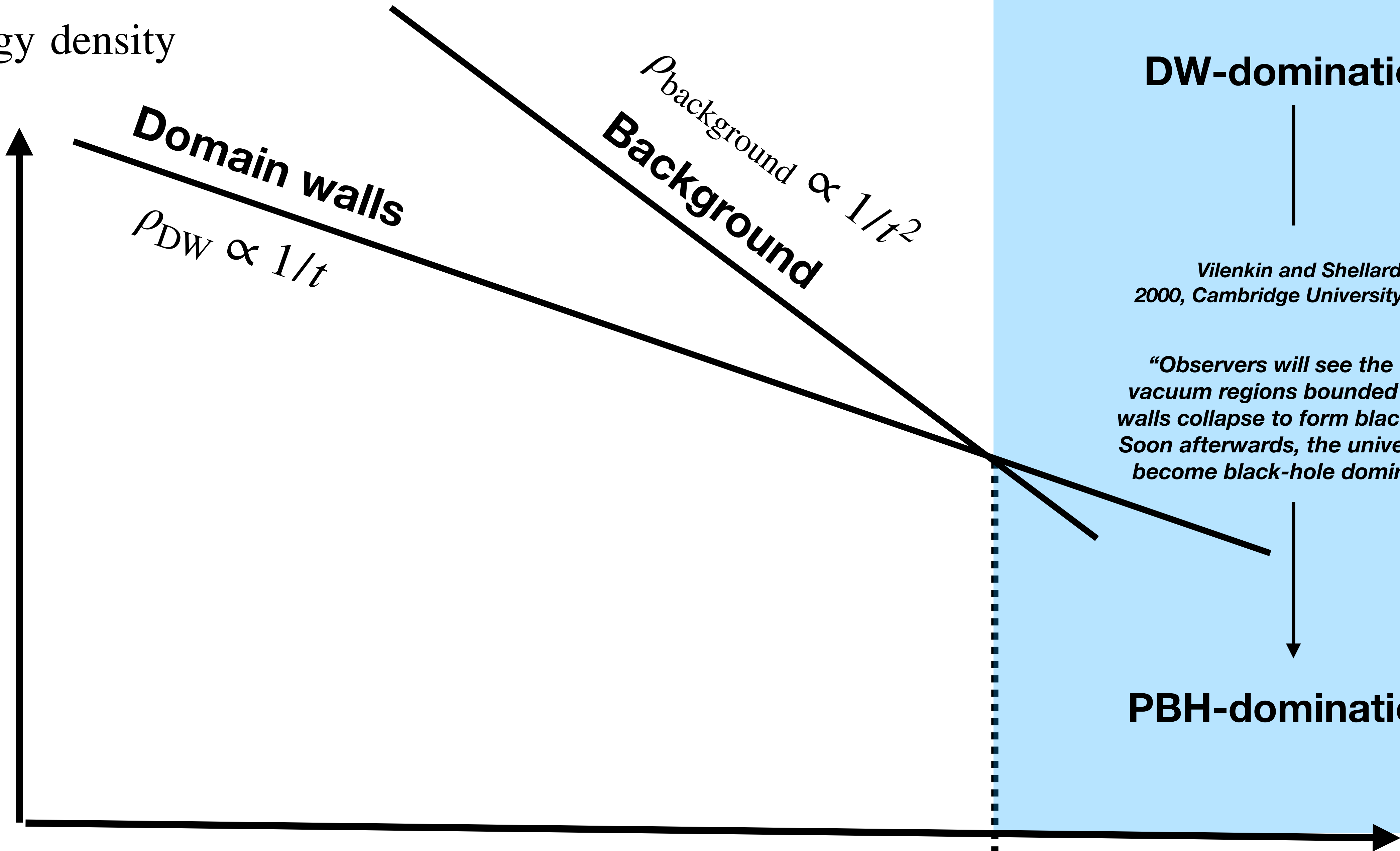
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“Observers will see the false vacuum regions bounded by the walls collapse to form black holes. Soon afterwards, the universe will become black-hole dominated”

PBH-domination

t_{dom}

t



Energy density

Domain walls

$$\rho_{\text{DW}} \propto 1/t$$

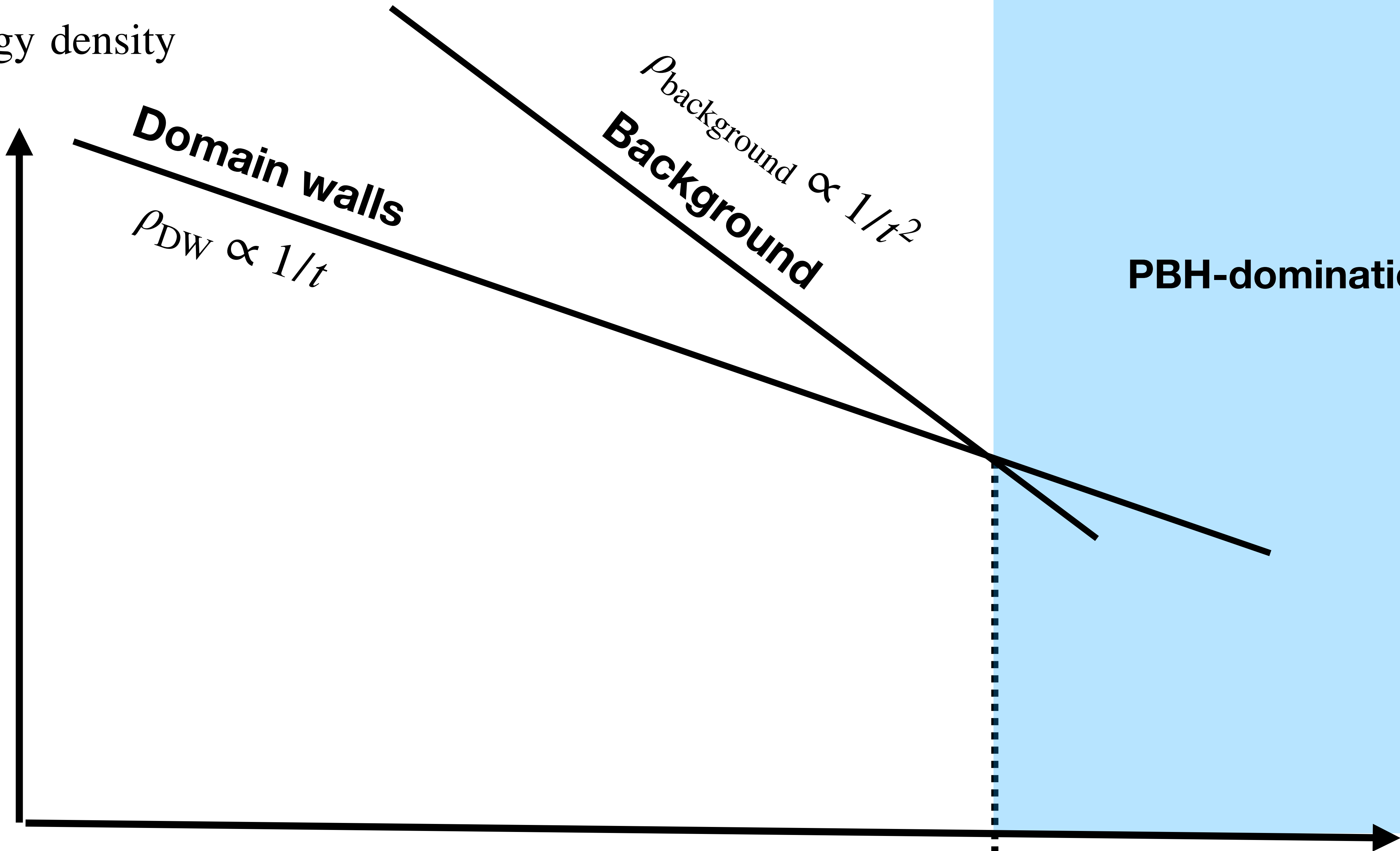
Background

$$\rho_{\text{background}} \propto 1/t^2$$

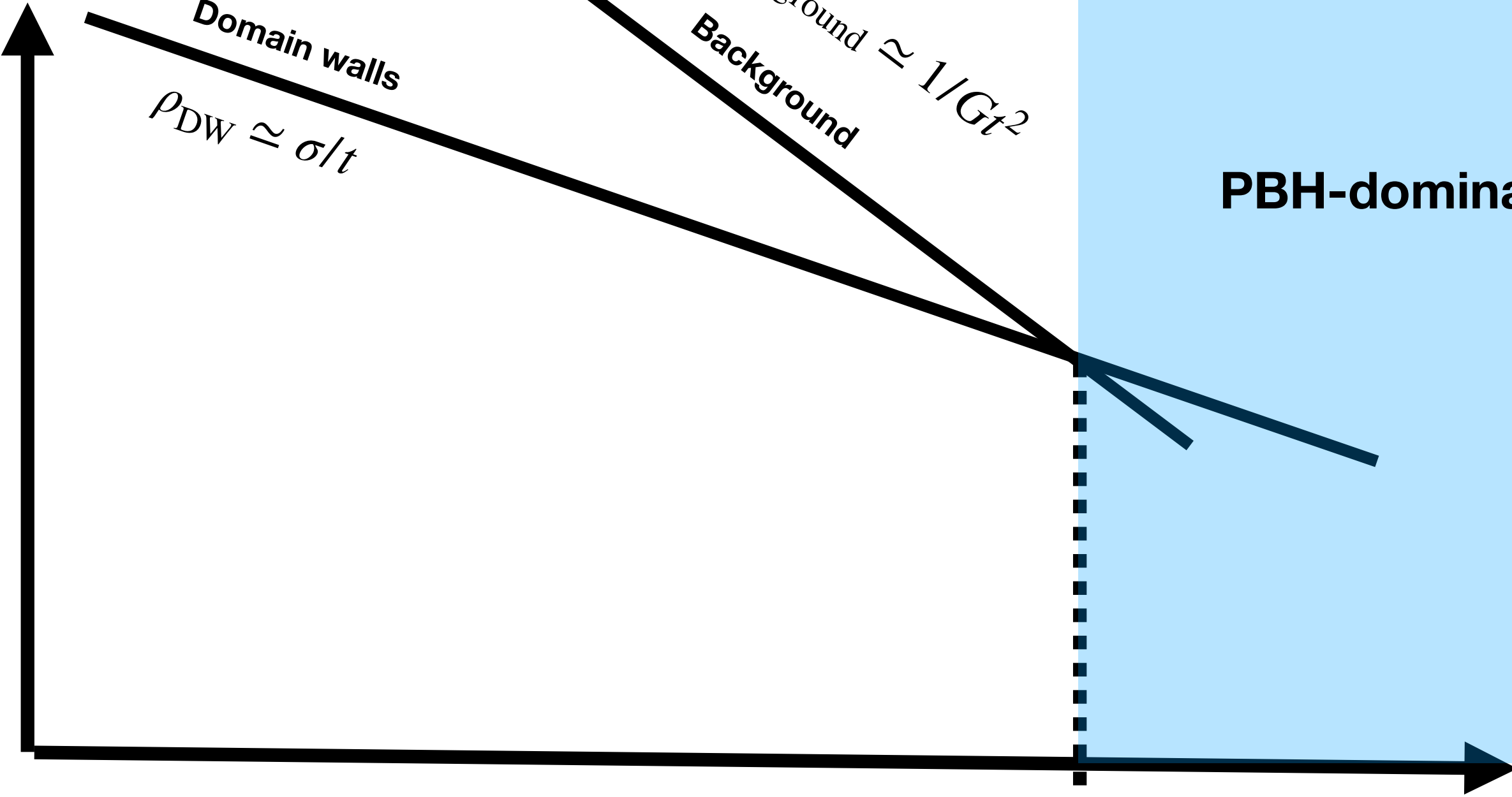
PBH-domination

t_{dom}

t



Energy density



Domain walls

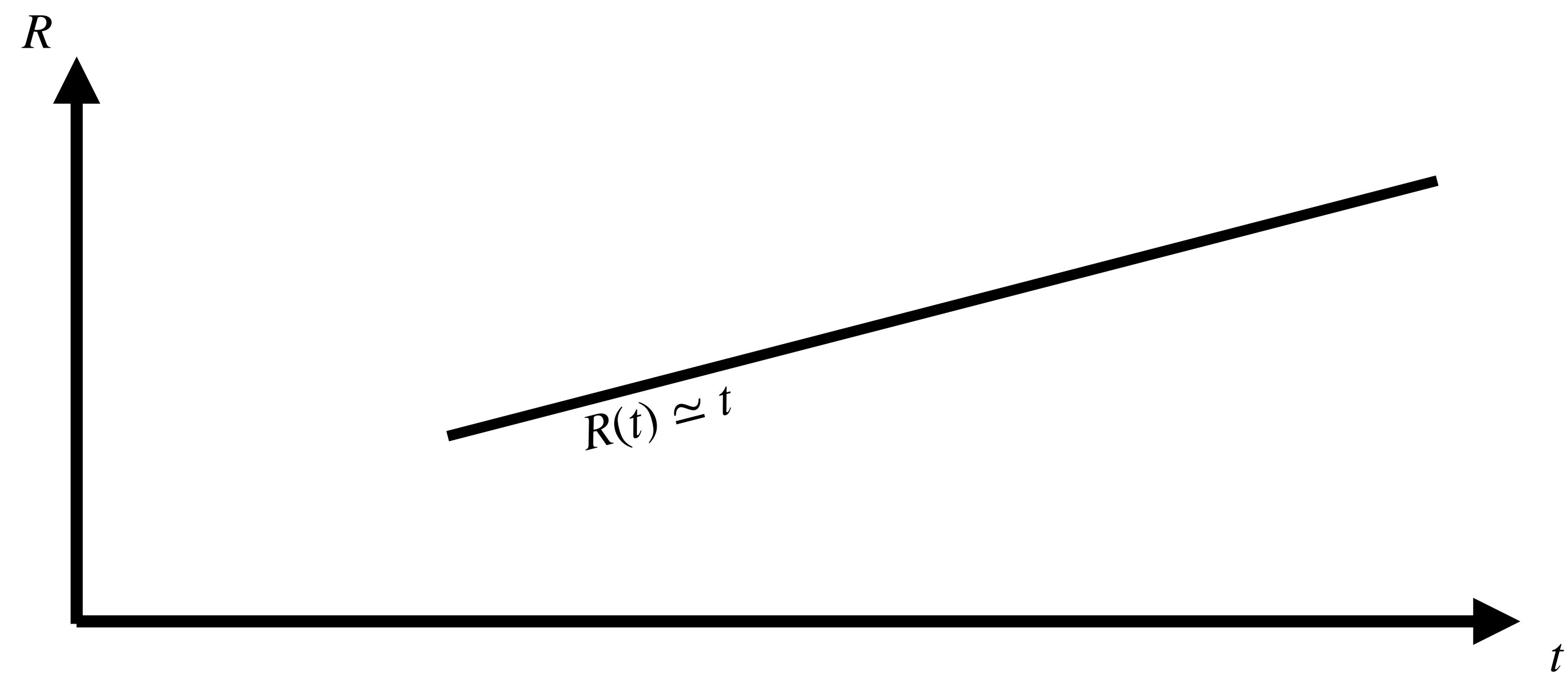
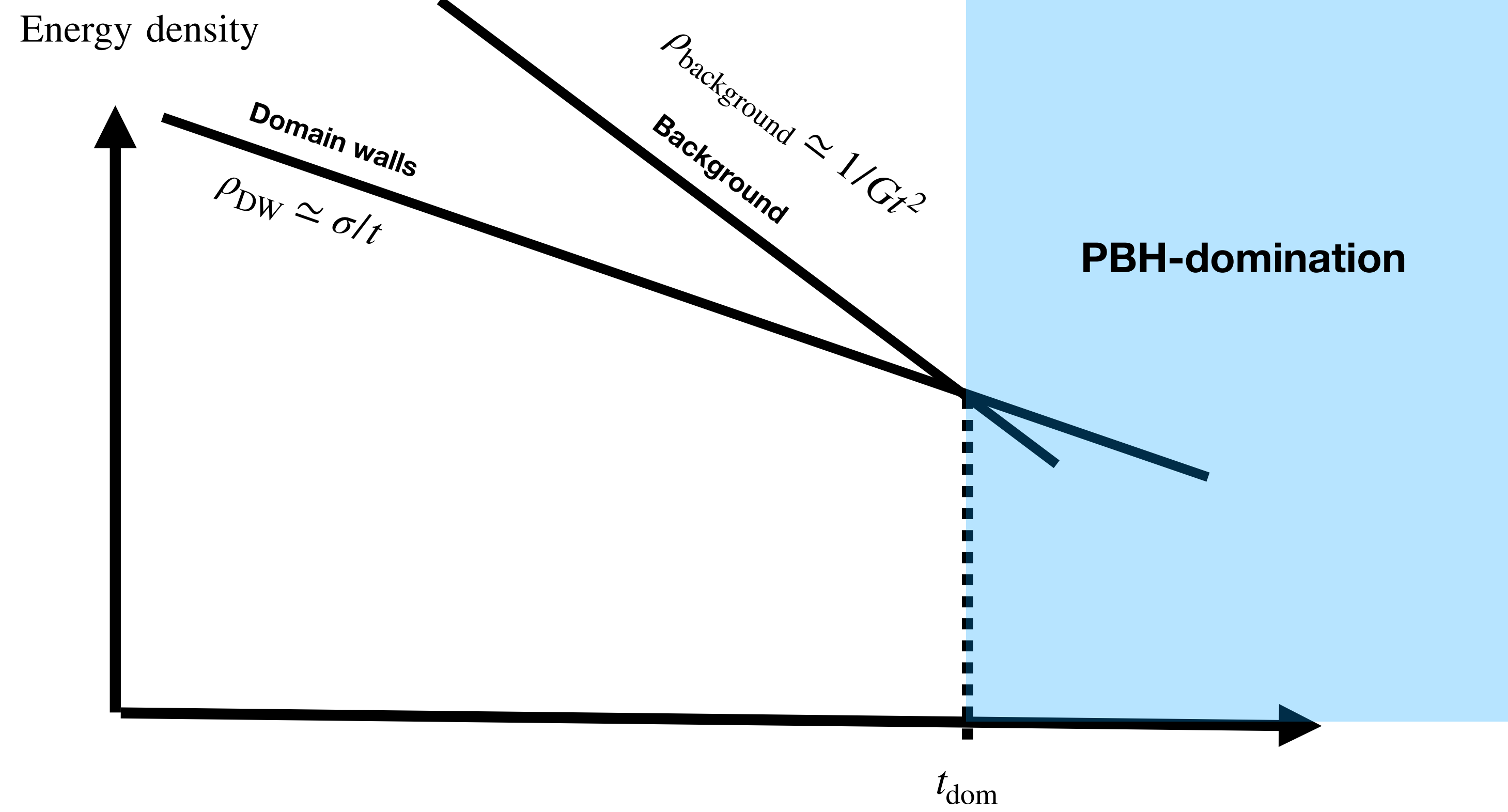
$$\rho_{DW} \simeq \sigma/t$$

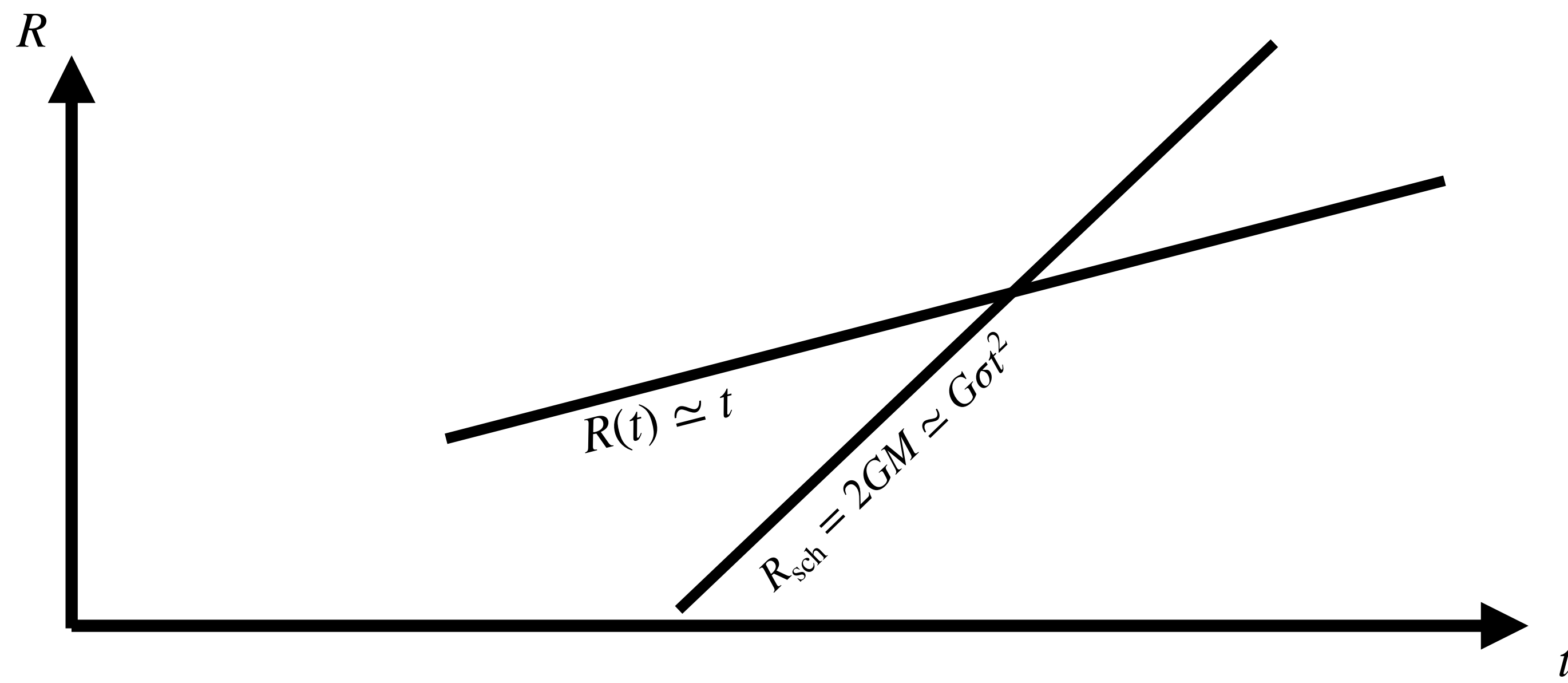
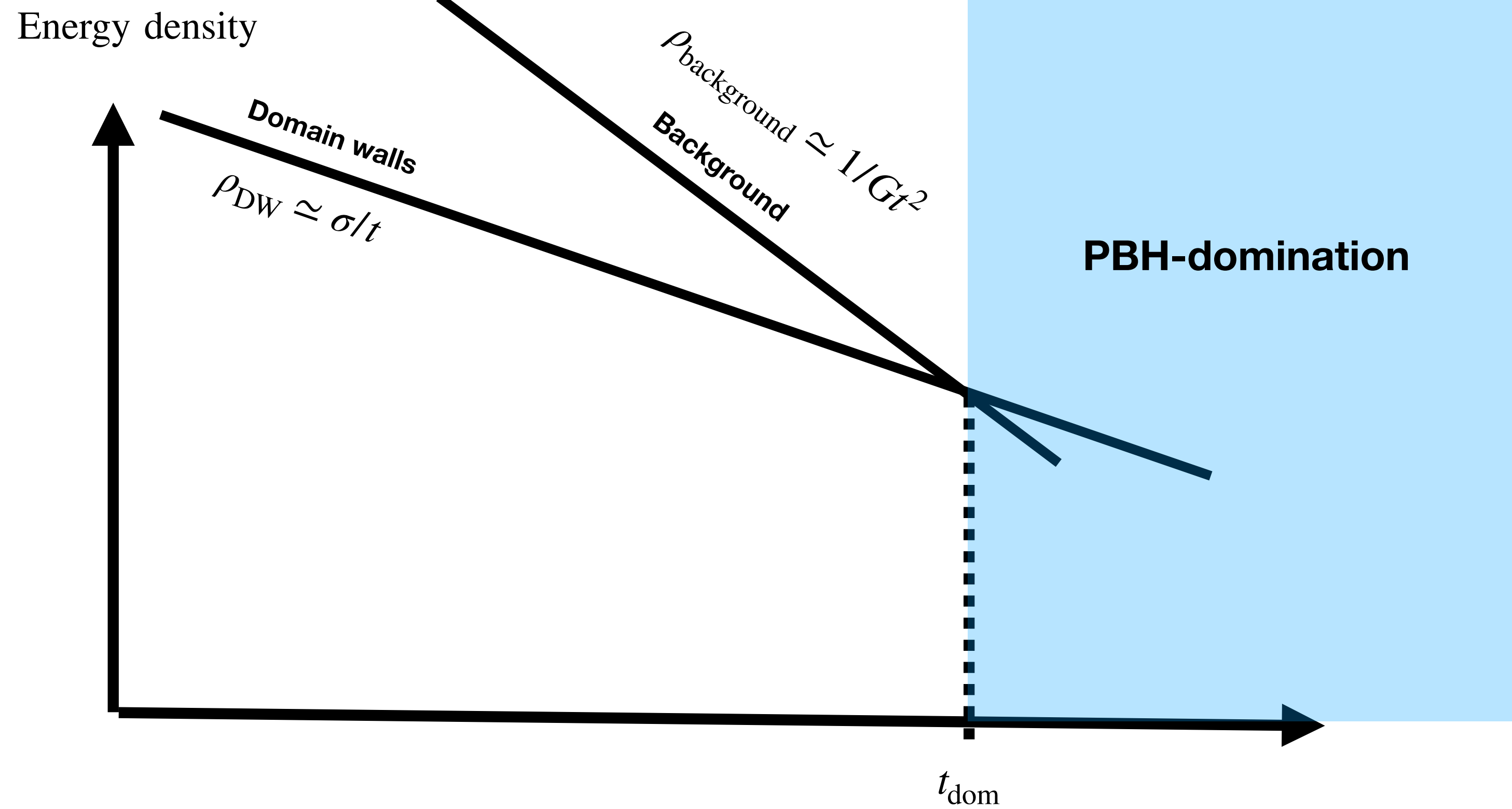
$\rho_{\text{background}} \simeq 1/Gt^2$

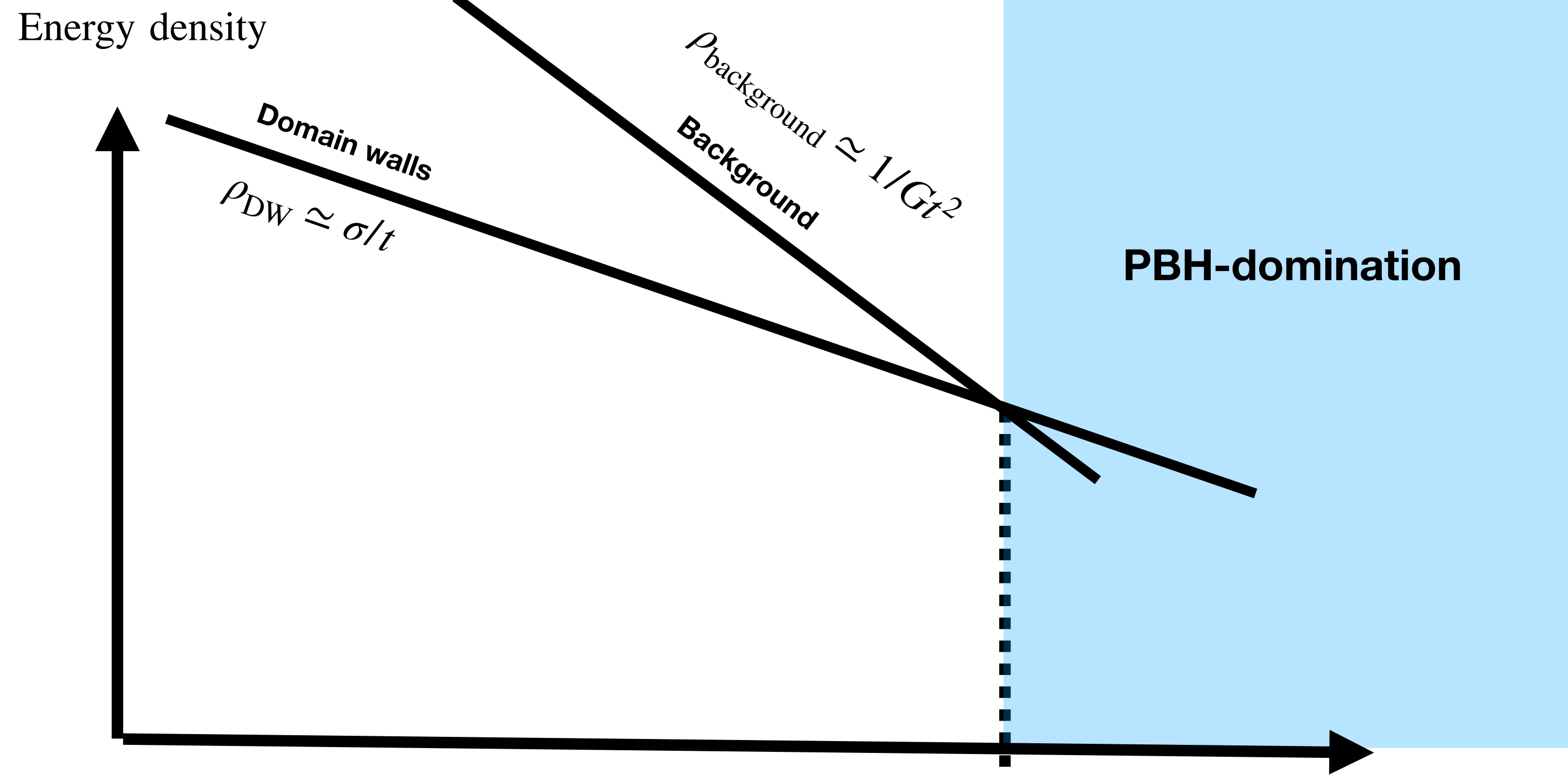
Background

PBH-domination

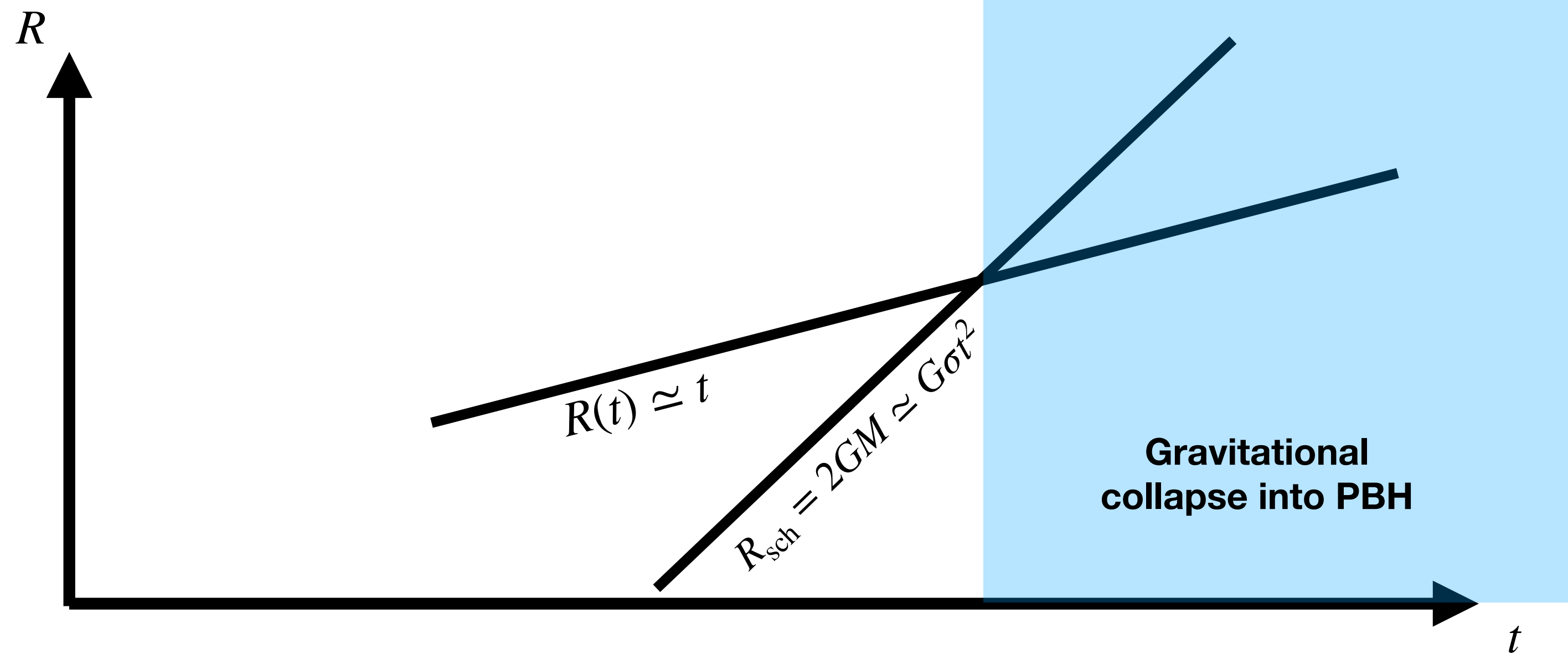
t_{dom}







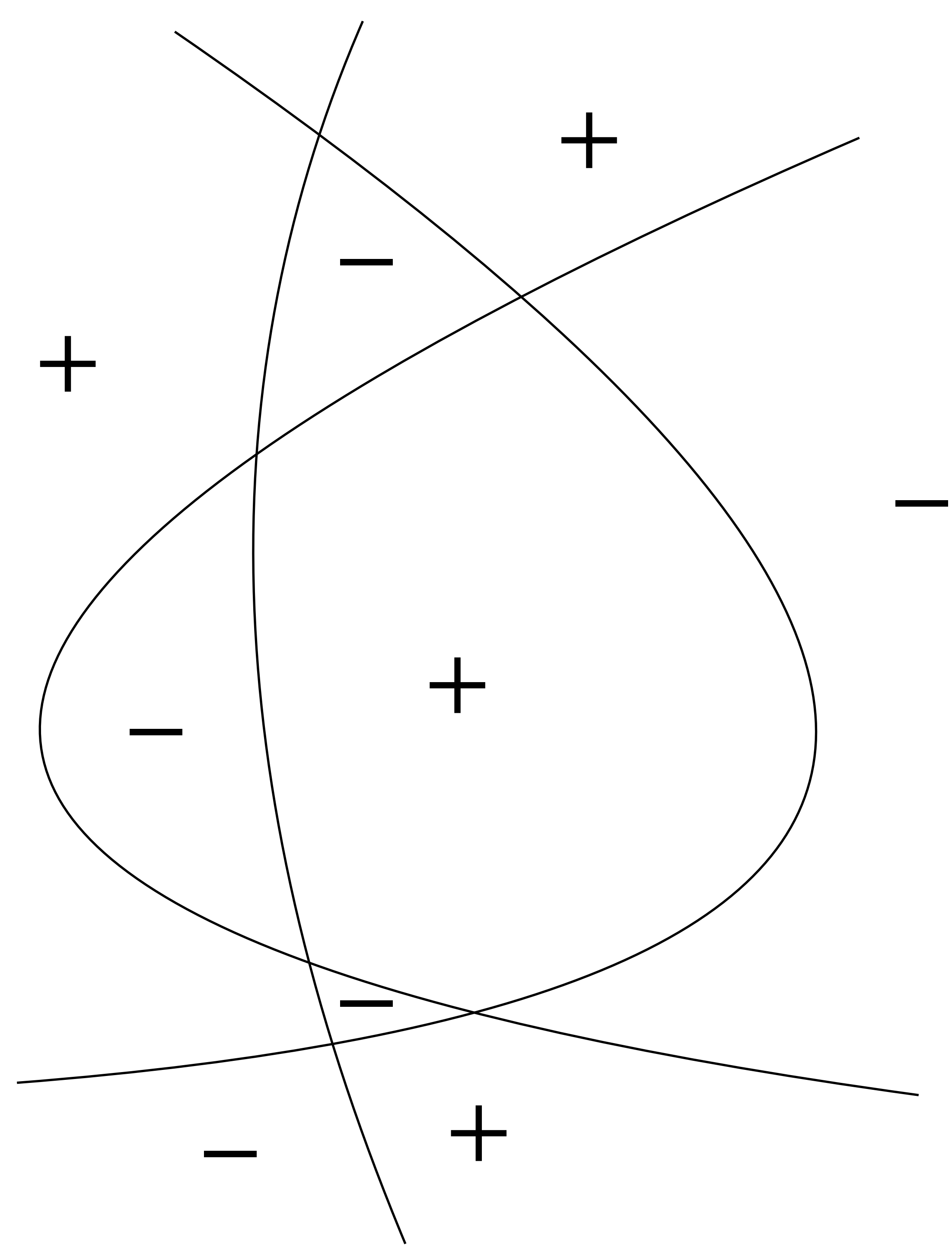
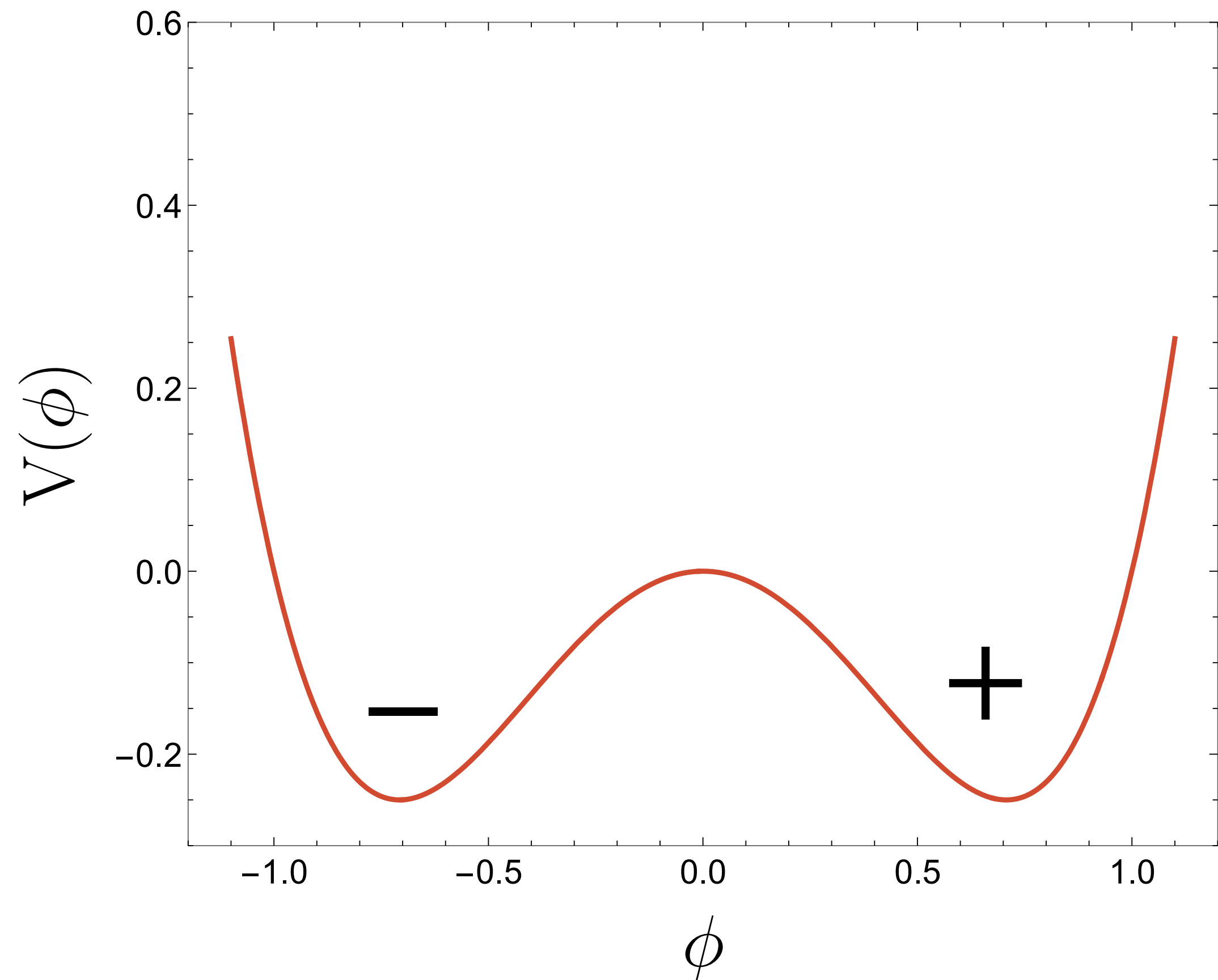
t_{dom}



Formation of Domain Wall

$$V(\phi) = \lambda(\phi^2 - v_\phi^2)^2$$

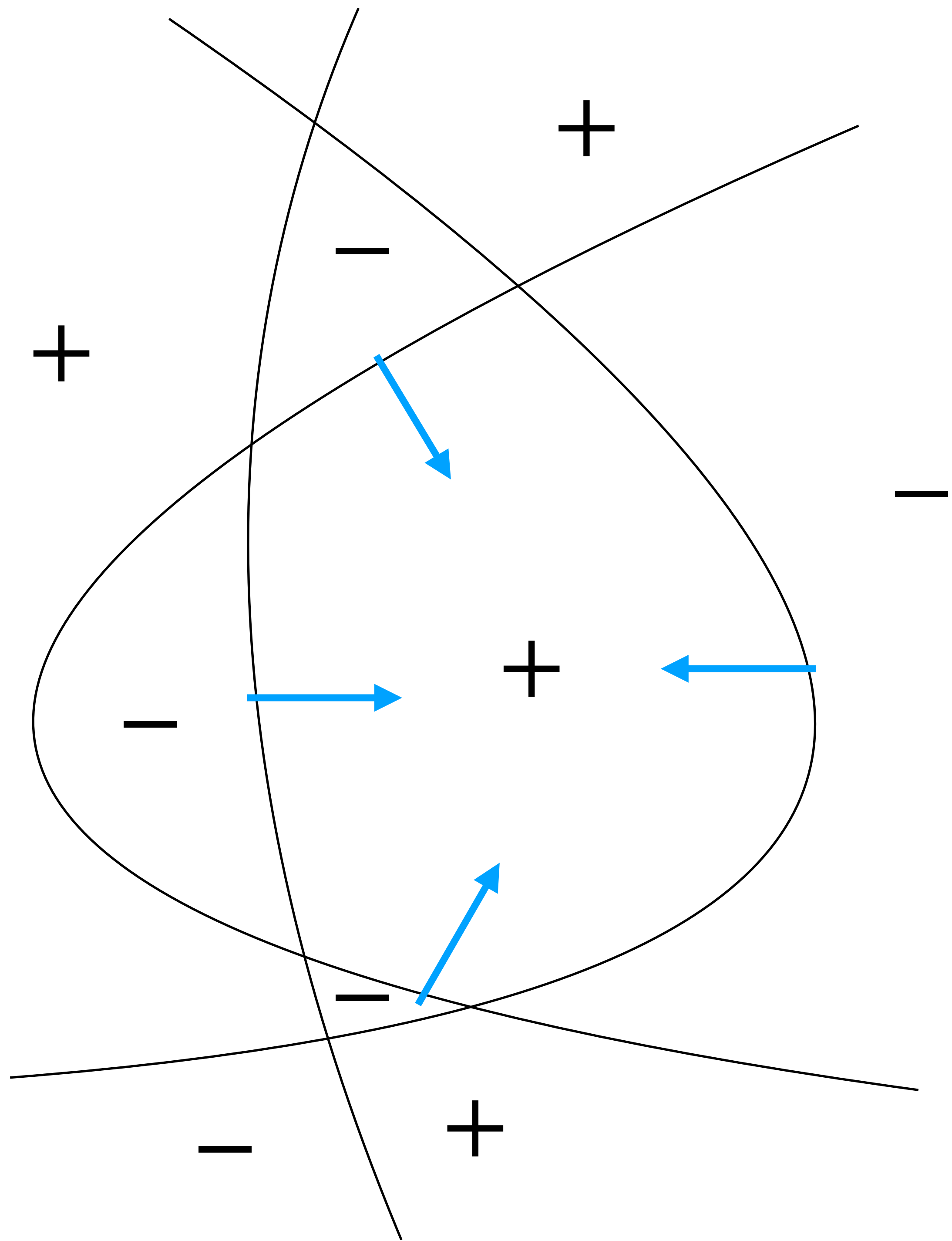
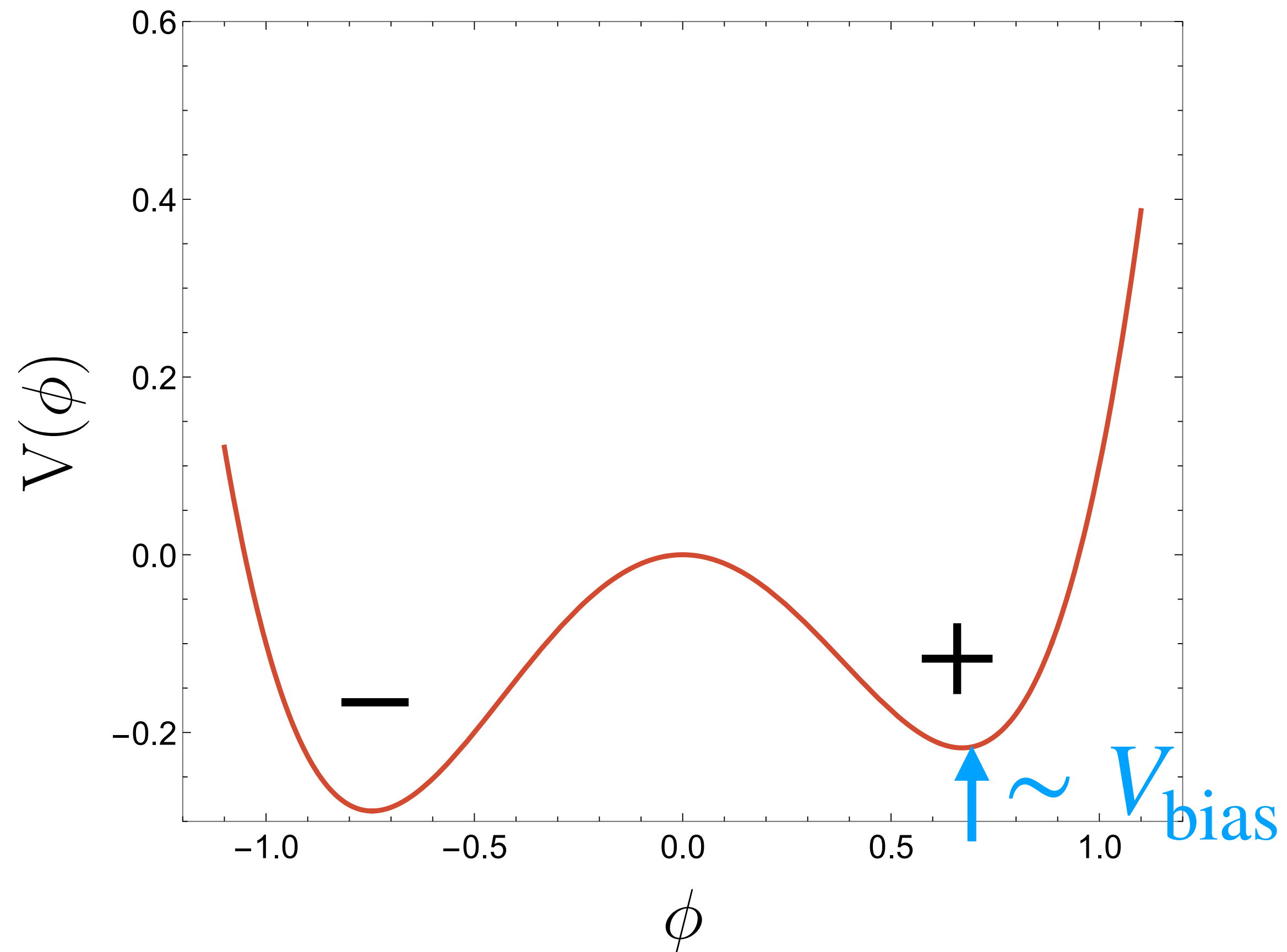
Break \mathbb{Z}_2



Formation of Domain Wall

$$V(\phi) = \lambda(\phi^2 - v_\phi^2)^2 + \epsilon\phi^3$$

Break \mathbb{Z}_2



Energy density

Domain walls

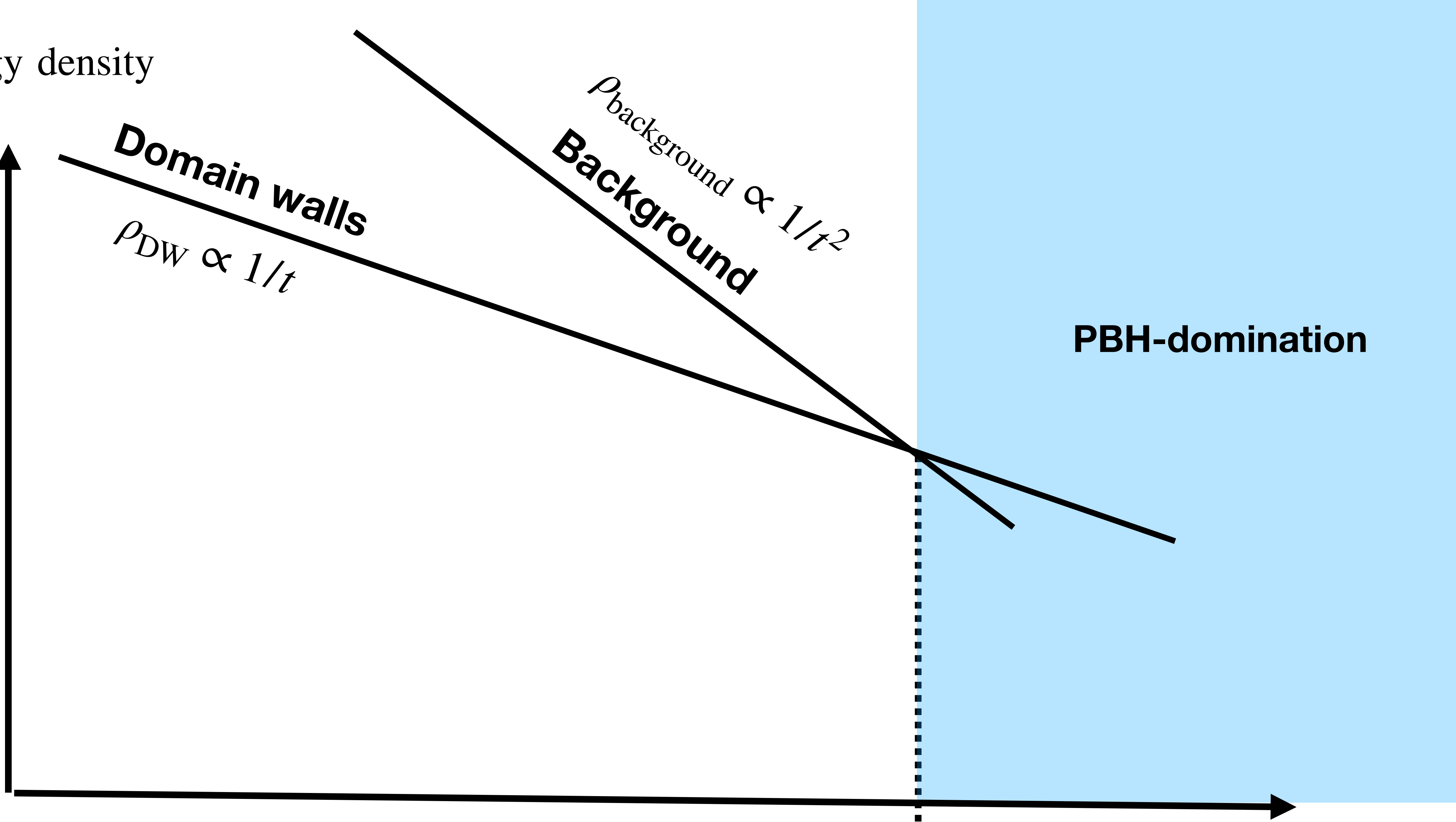
$$\rho_{\text{DW}} \propto 1/t$$

Background

$$\rho_{\text{background}} \propto 1/t^2$$

PBH-domination

t_{dom}



Energy density

Domain walls

$$\rho_{DW} \propto 1/t$$

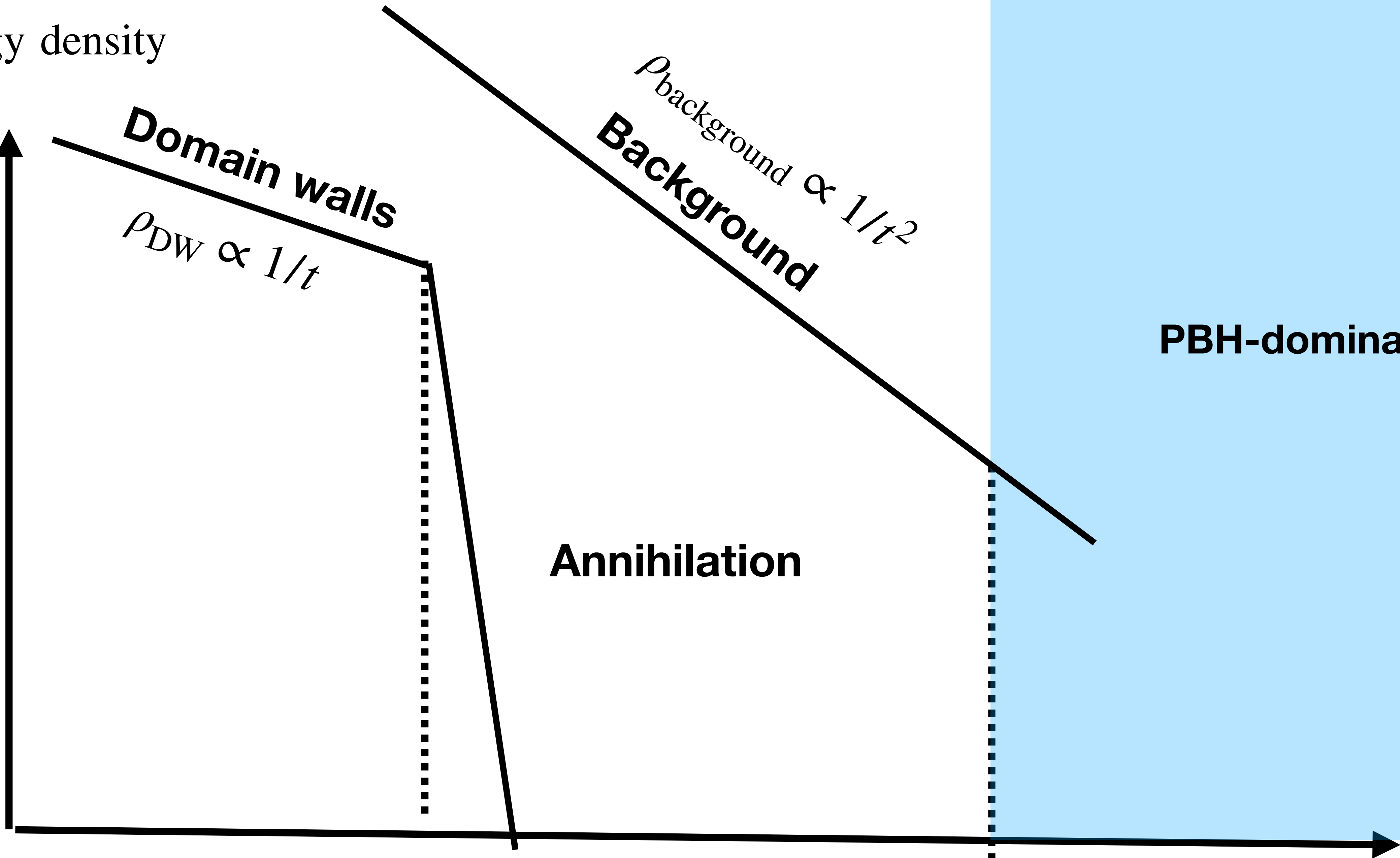
$\rho_{\text{background}} \propto 1/t^2$
Background

PBH-domination

Annihilation

t_{ann}

t_{dom}



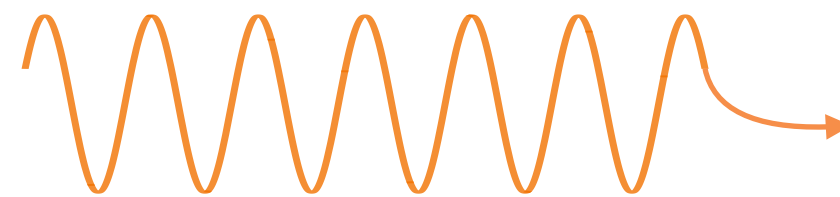
Energy density

Domain walls

$$\rho_{\text{DW}} \propto 1/t$$

$\rho_{\text{background}} \propto 1/t^2$
Background

Gravitational waves

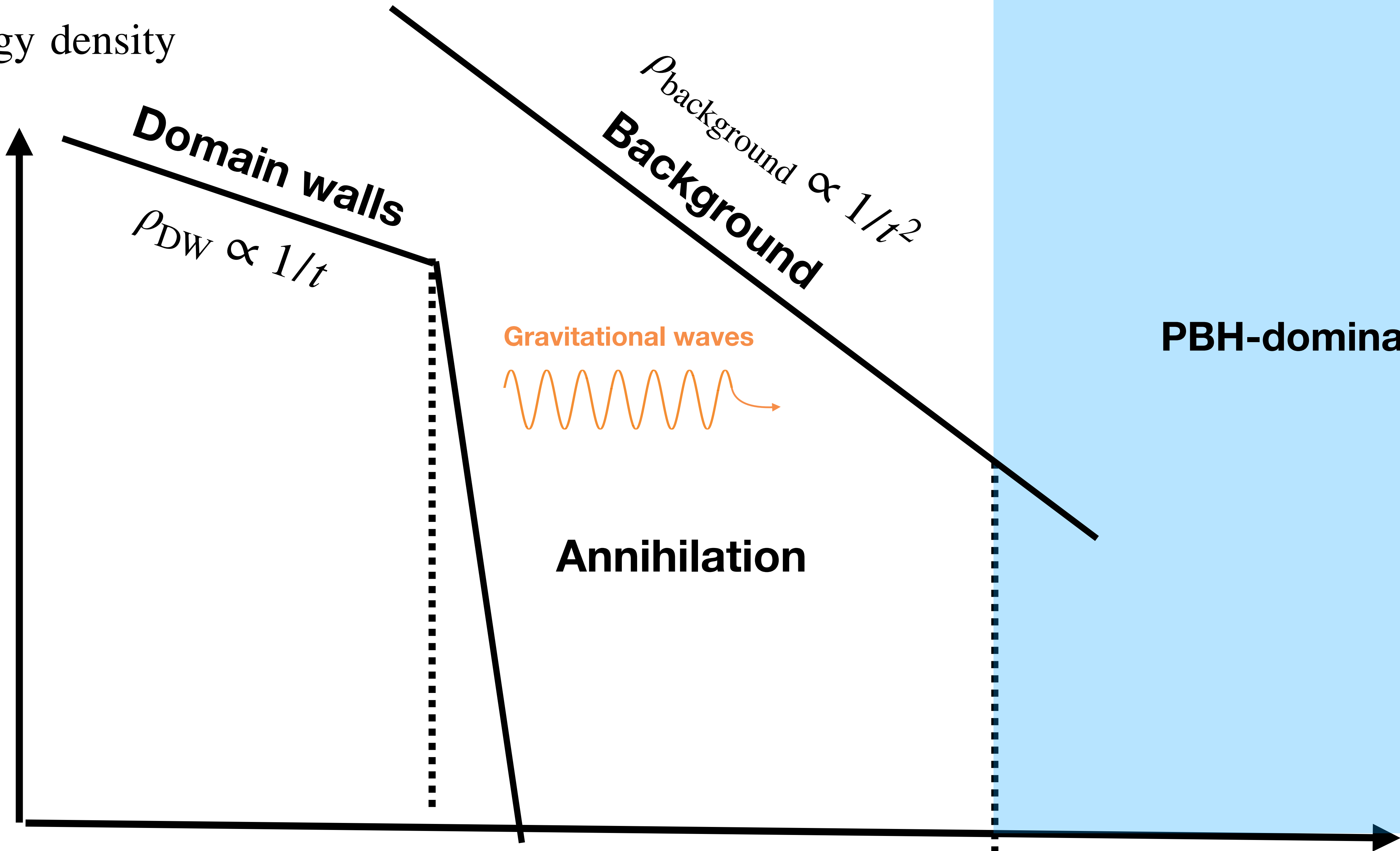


Annihilation

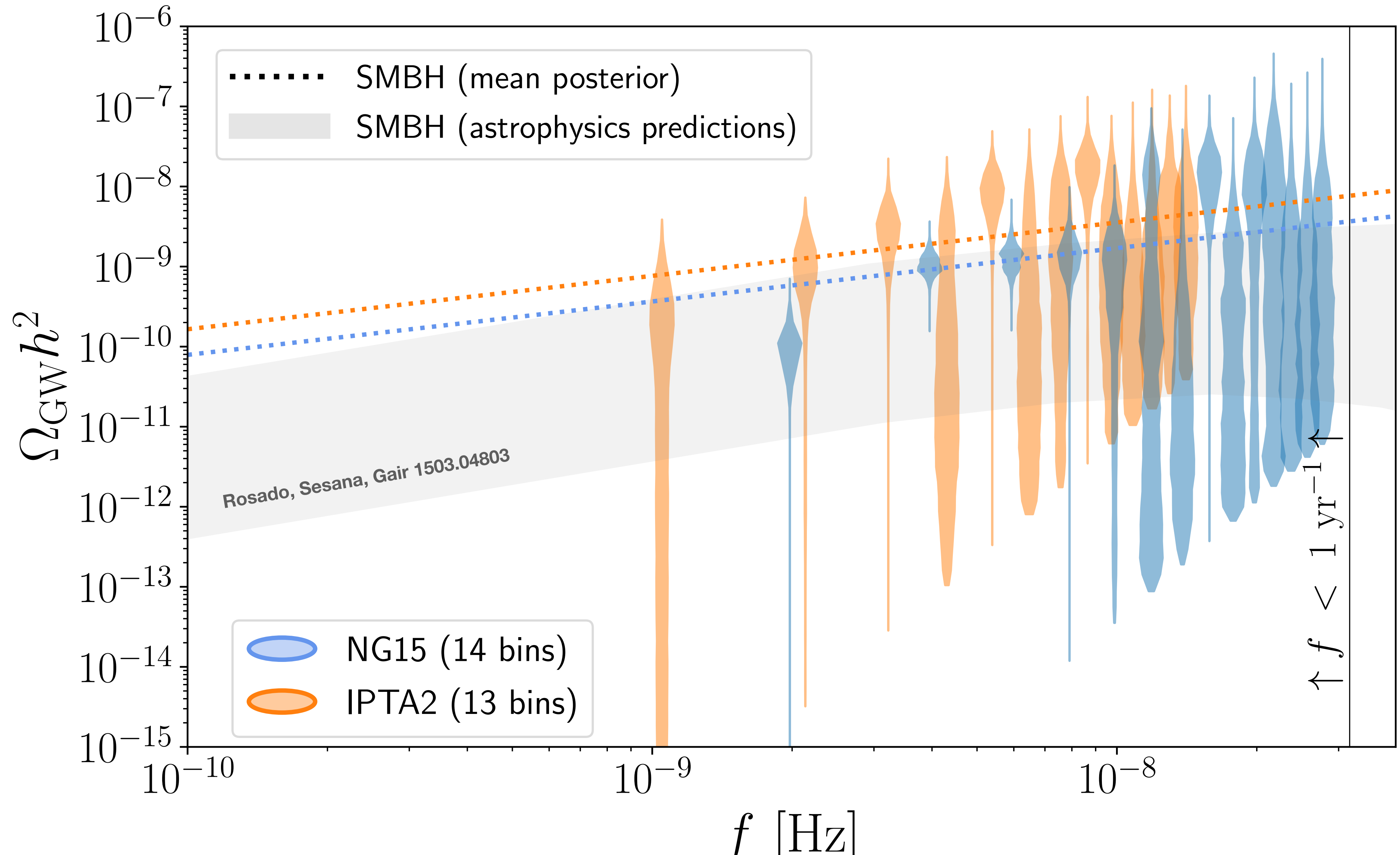
PBH-domination

t_{ann}

t_{dom}

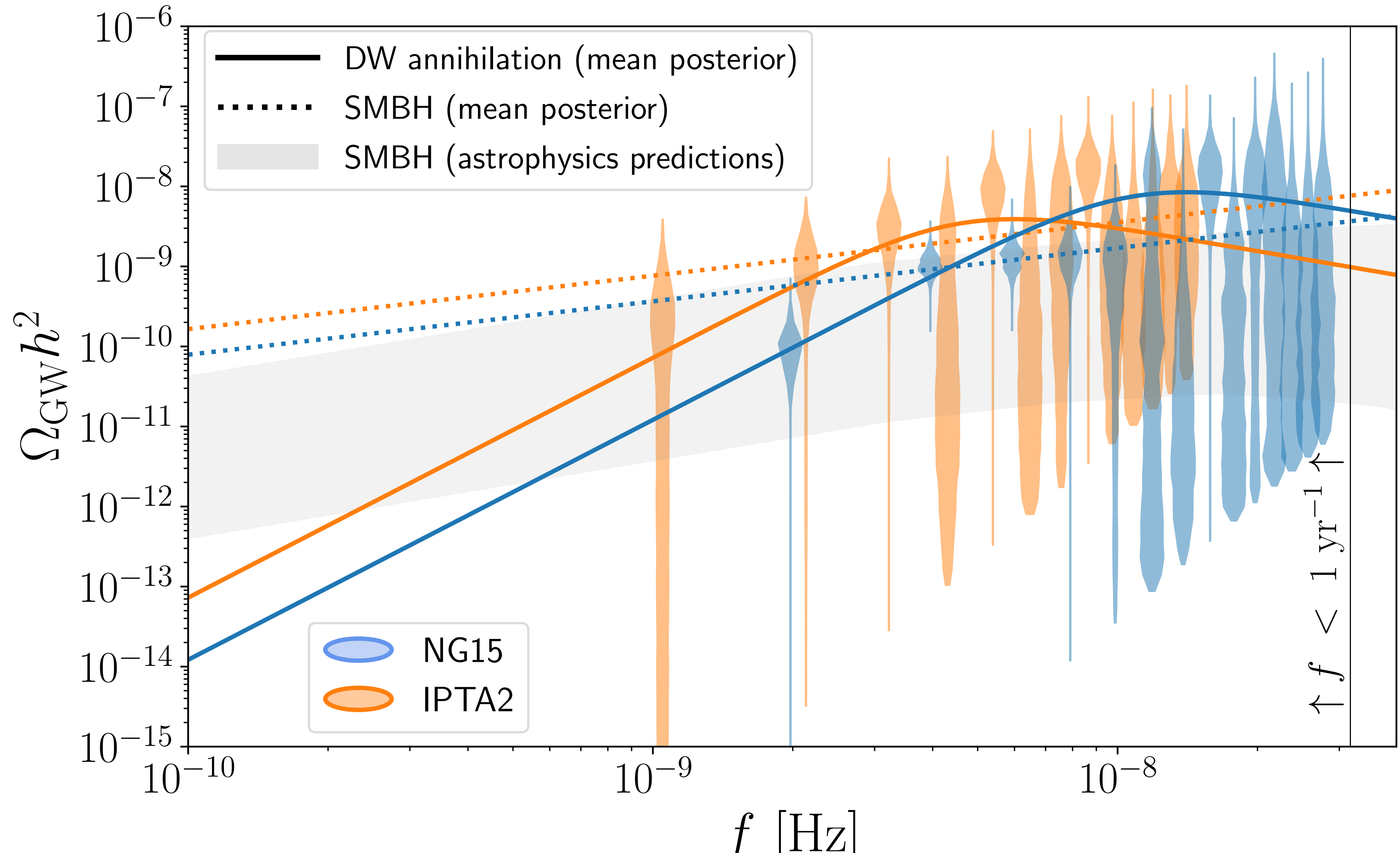


GW from DW annihilation in Pulsar Timing arrays



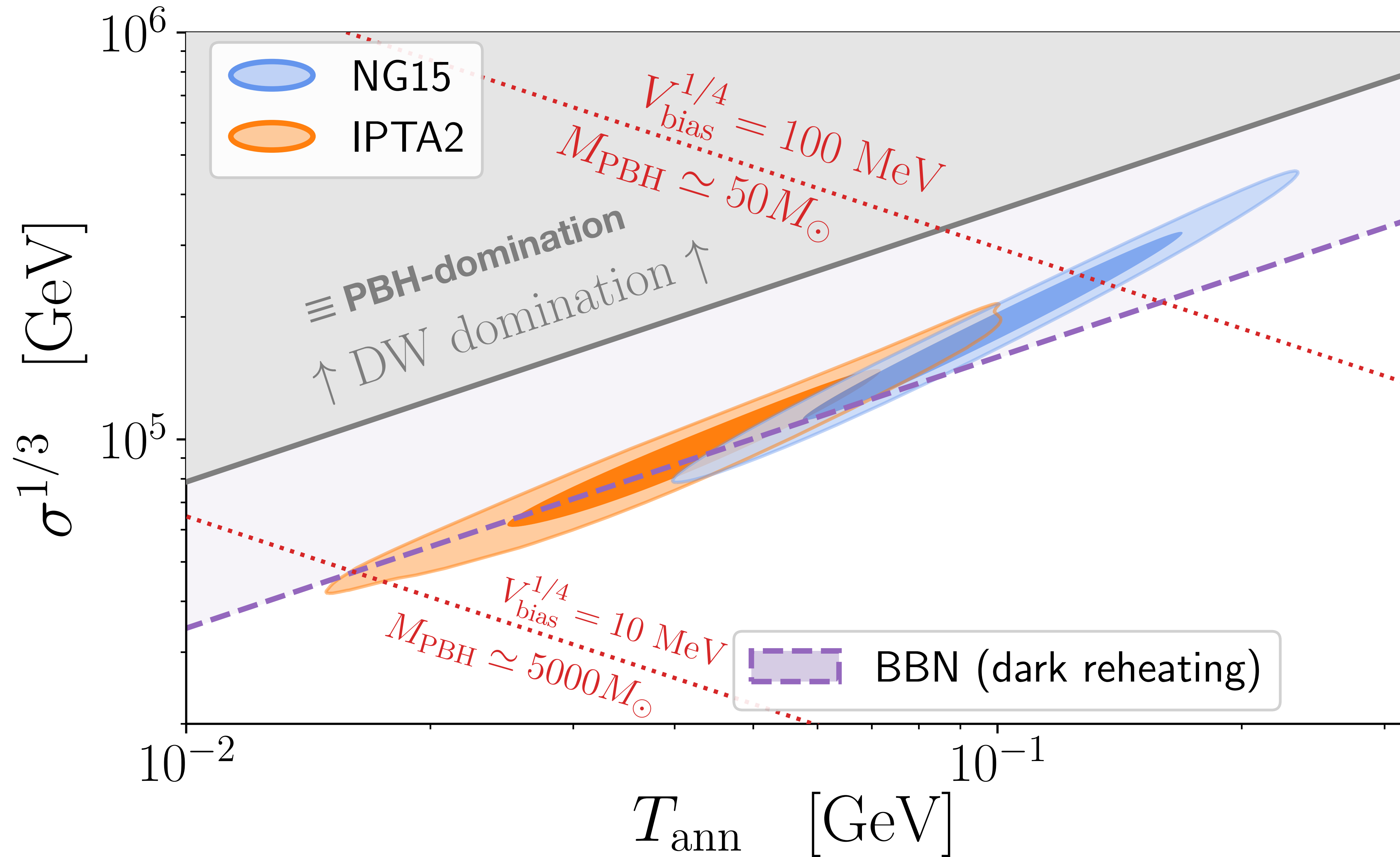
GW from DW annihilation in Pulsar Timing arrays

YG, E. Vitagliano, 2306.17841



GW from DW annihilation in Pulsar Timing arrays

YG, E. Vitagliano, 2306.17841



Energy density

Domain walls

$$\rho_{\text{DW}} \propto 1/t$$

Background

$$\rho_{\text{background}} \propto 1/t^2$$

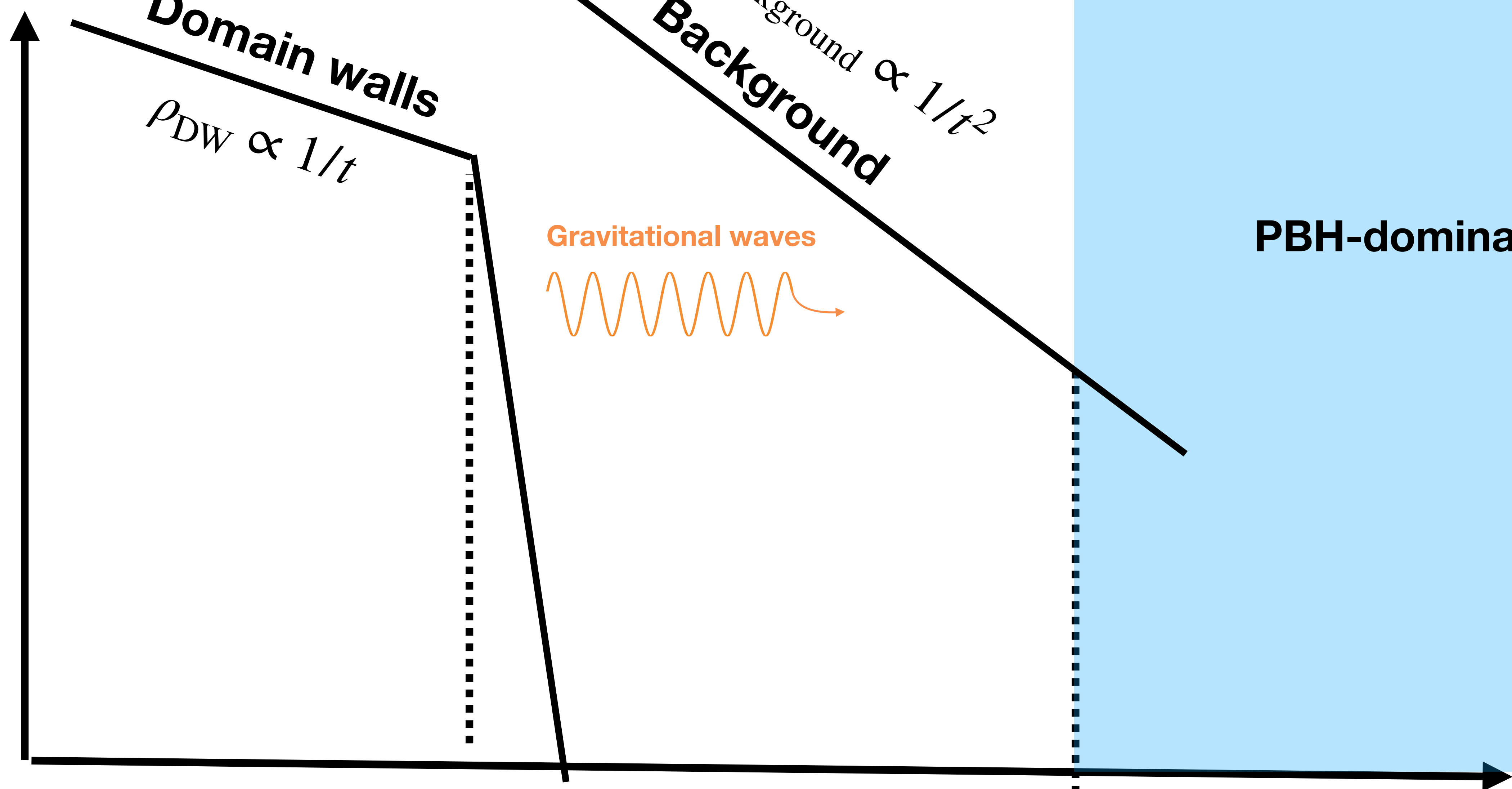
Gravitational waves



PBH-domination

t_{ann}

t_{dom}



Energy density

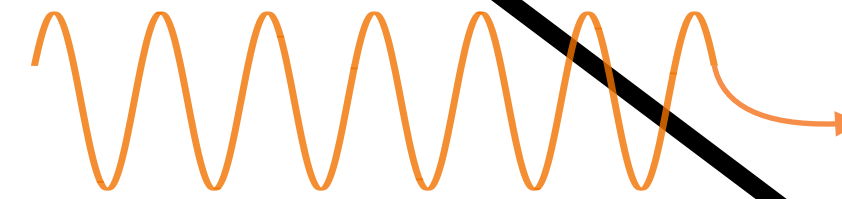
Domain walls

$$\rho_{\text{DW}} \propto 1/t$$

Background

$$\rho_{\text{background}} \propto 1/t^2$$

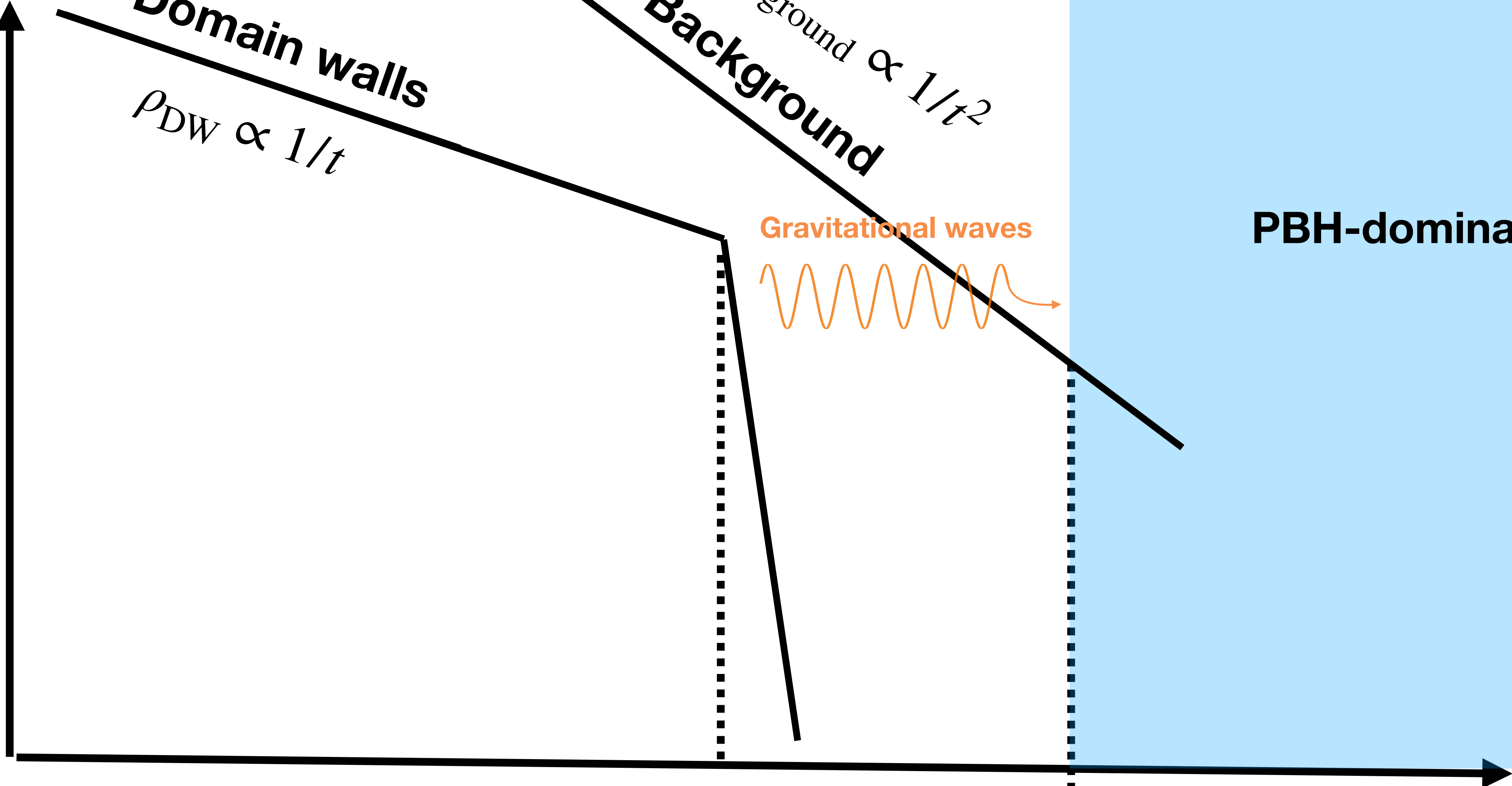
Gravitational waves

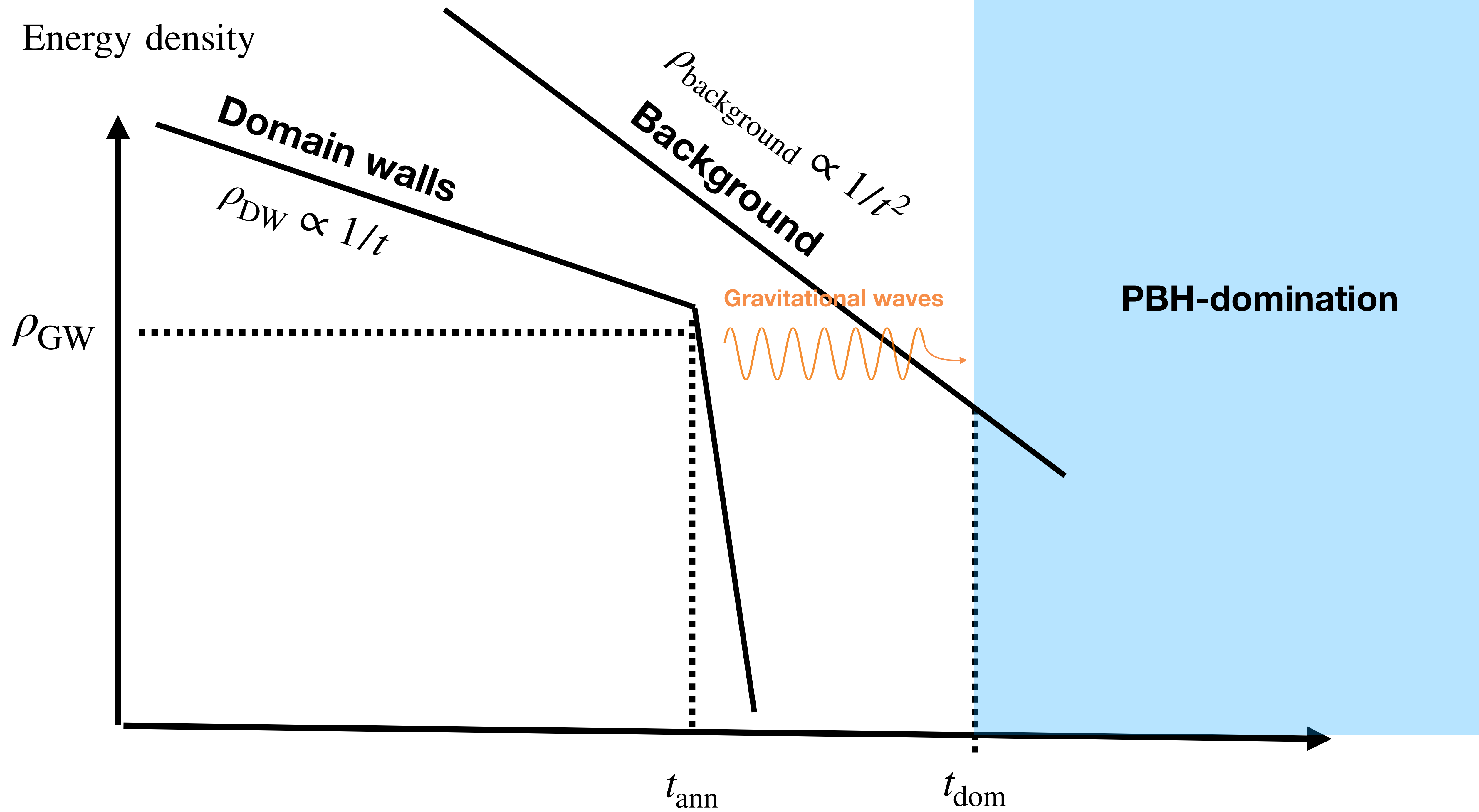


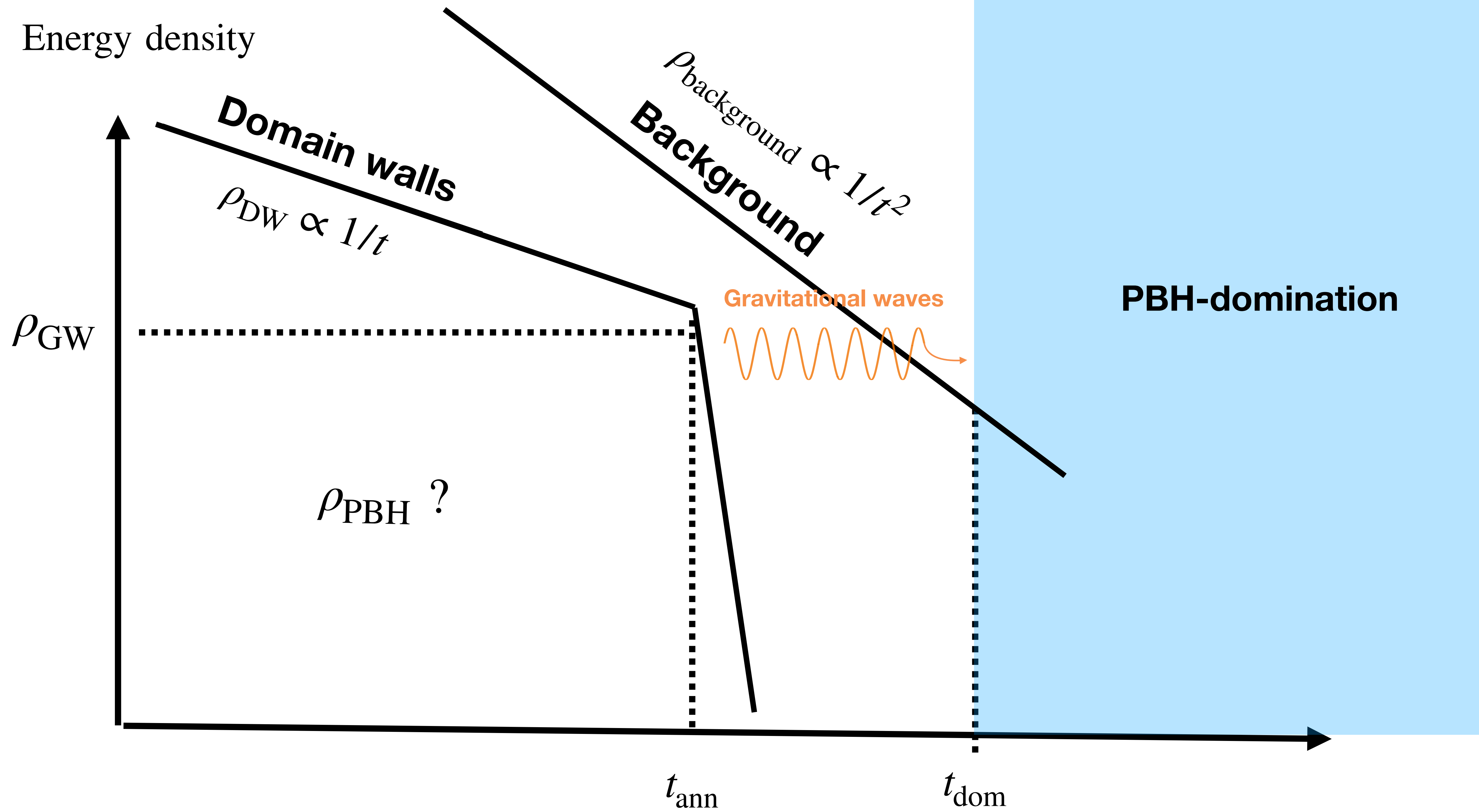
PBH-domination

t_{ann}

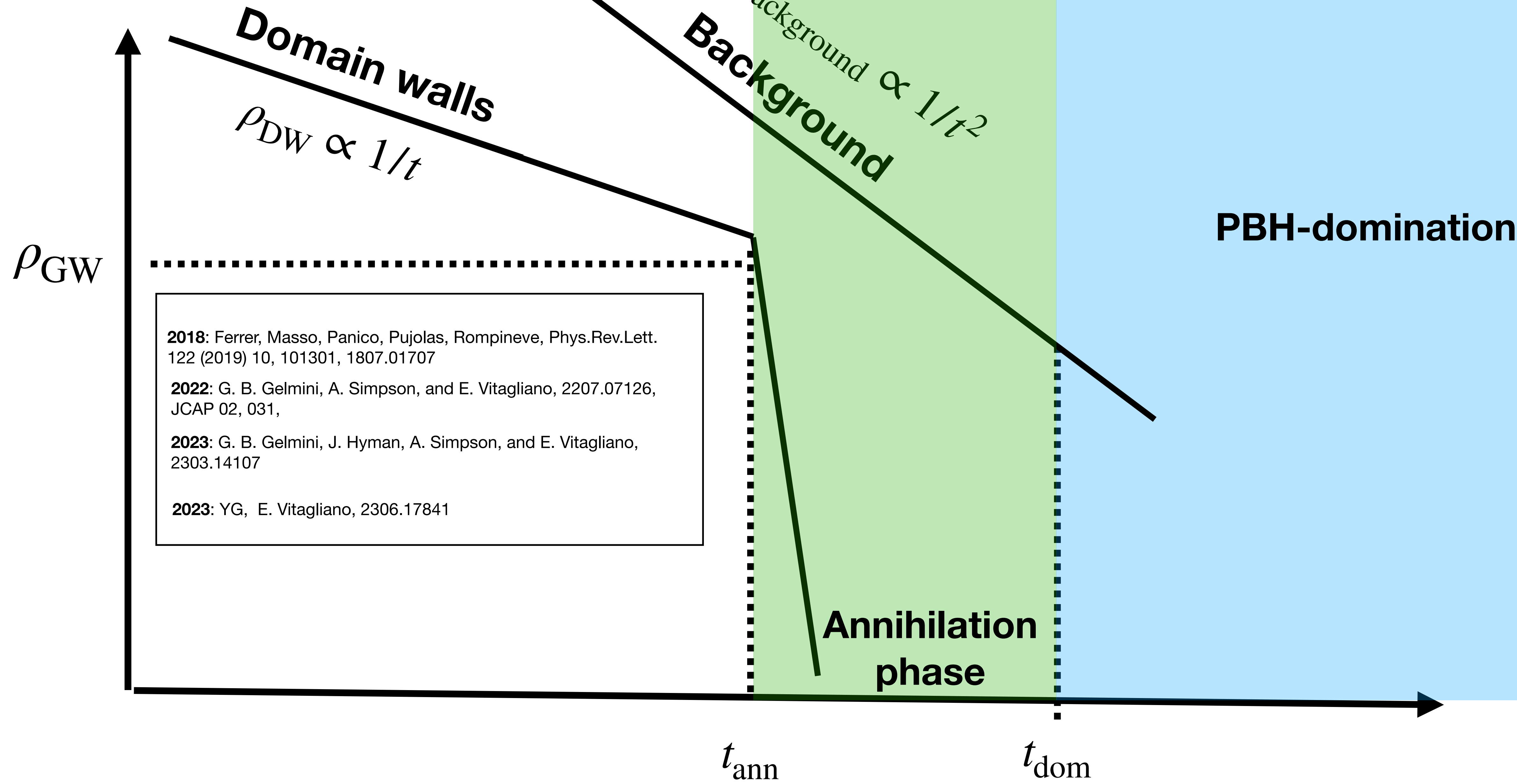
t_{dom}







Energy density



Domain walls
 $\rho_{DW} \propto 1/t$

$\rho_{background} \propto 1/t^2$
Background

PBH-domination

Annihilation phase

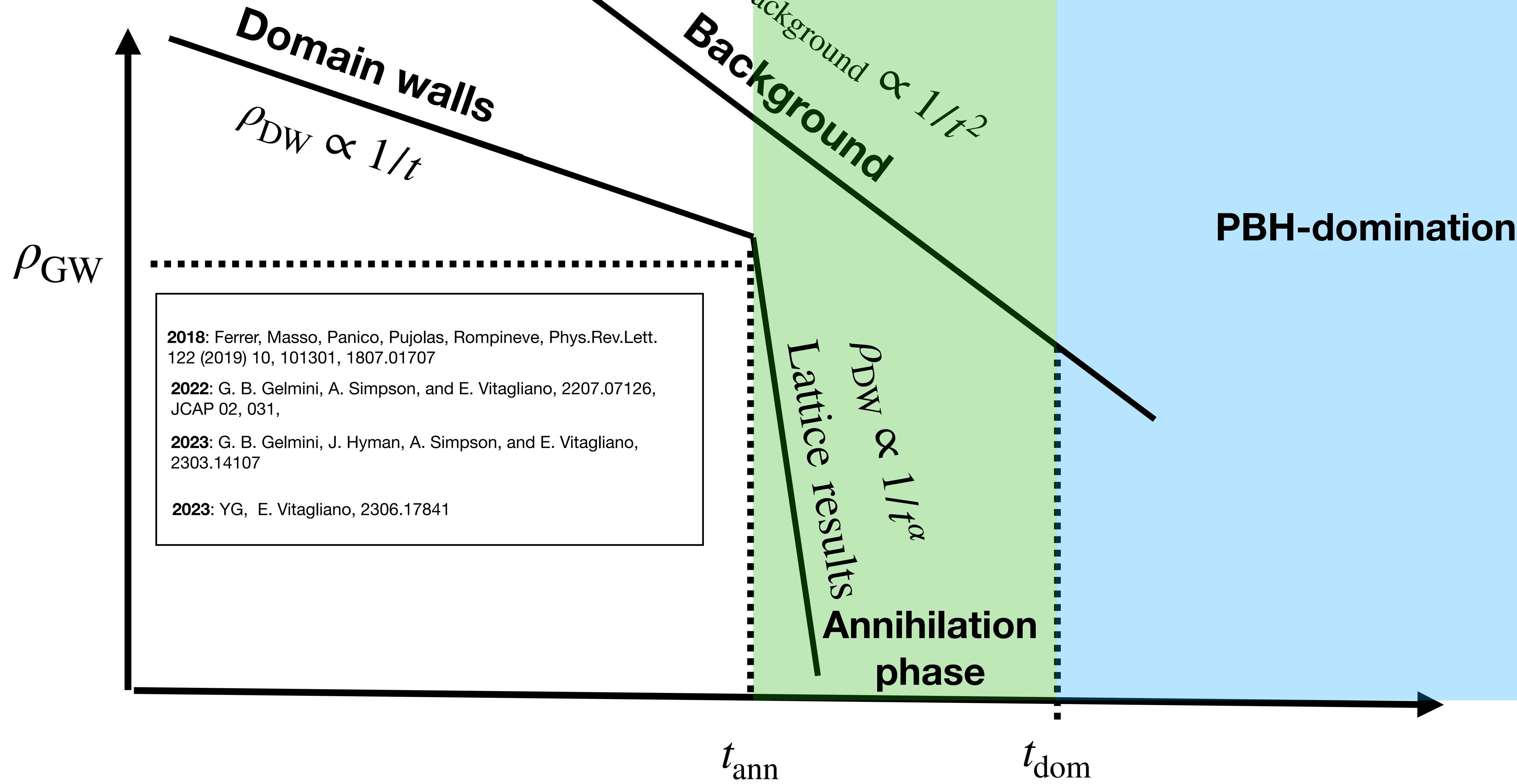
2018: Ferrer, Masso, Panico, Pujolas, Rompineve, Phys.Rev.Lett. 122 (2019) 10, 101301, 1807.01707
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2023: G. B. Gelmini, J. Hyman, A. Simpson, and E. Vitagliano, 2303.14107
2023: YG, E. Vitagliano, 2306.17841

t_{ann}

t_{dom}

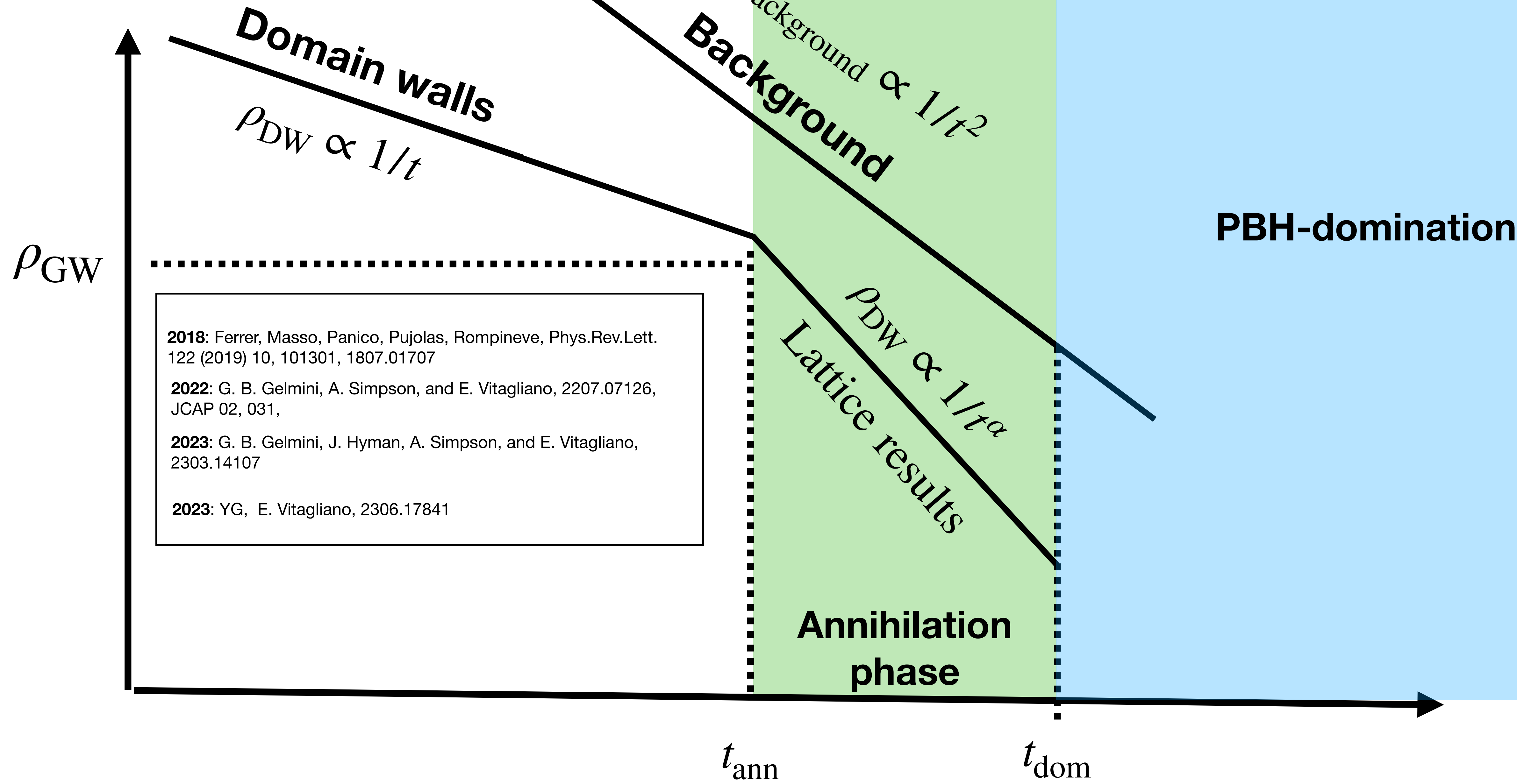
ρ_{GW}

Energy density

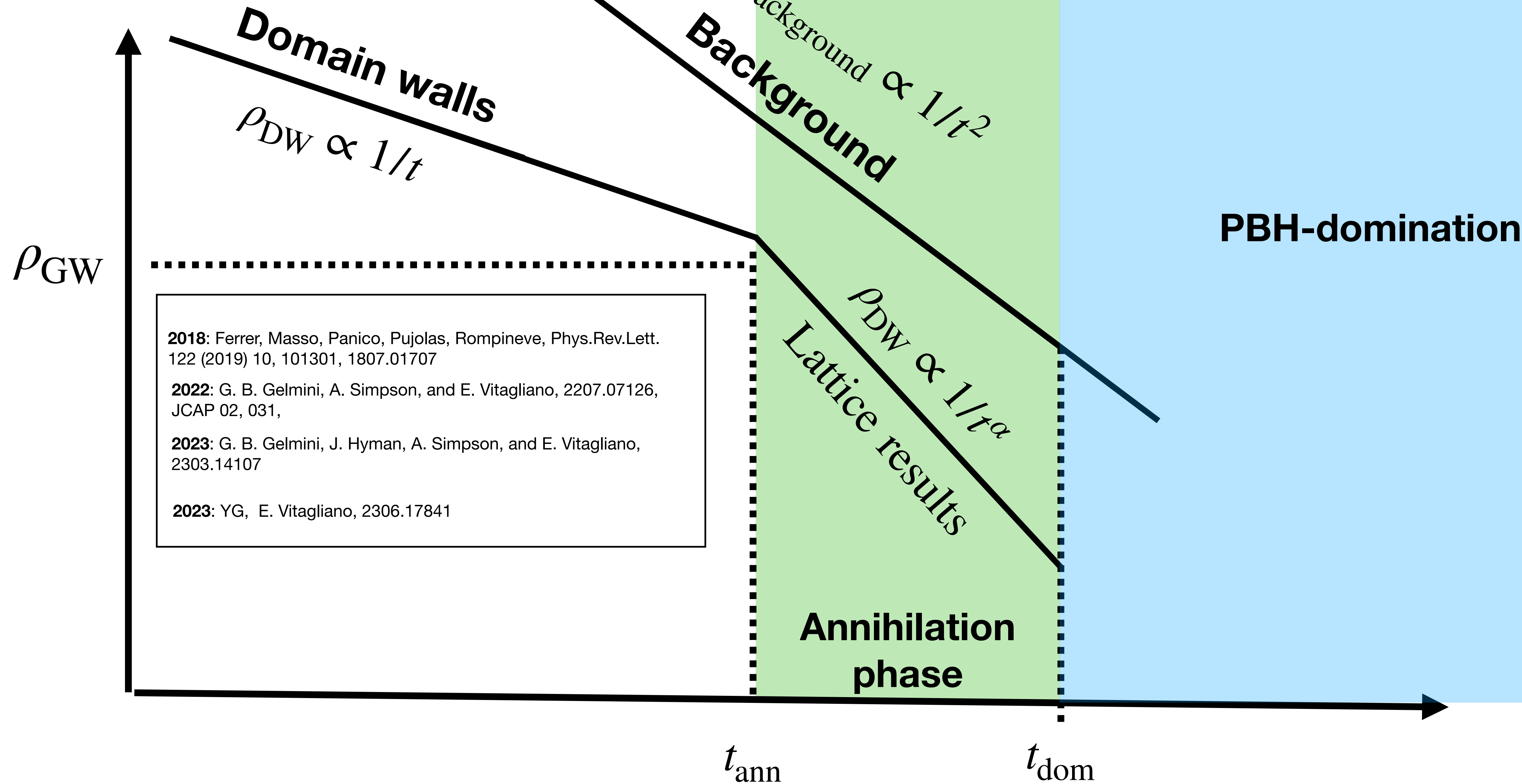


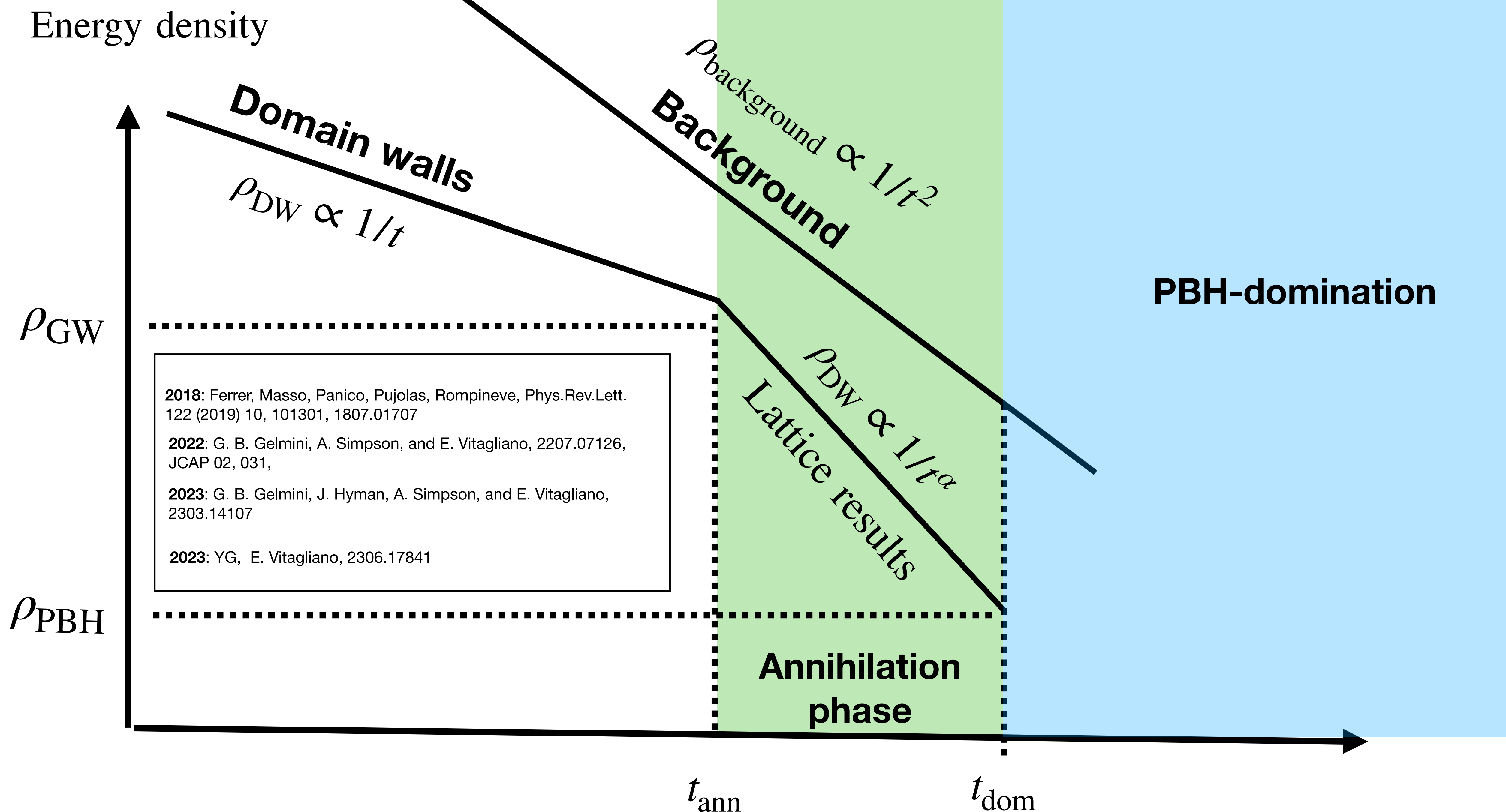
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Energy density



Energy density





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Energy density



Domain walls
 $\rho_{DW} \propto 1/t$

$\rho_{DW} \propto 1/t$

ρ_{PBH}



$\rho_{background} \propto 1/t^2$
Background

$\rho_{DW} \propto 1/t^\alpha$

Annihilation phase

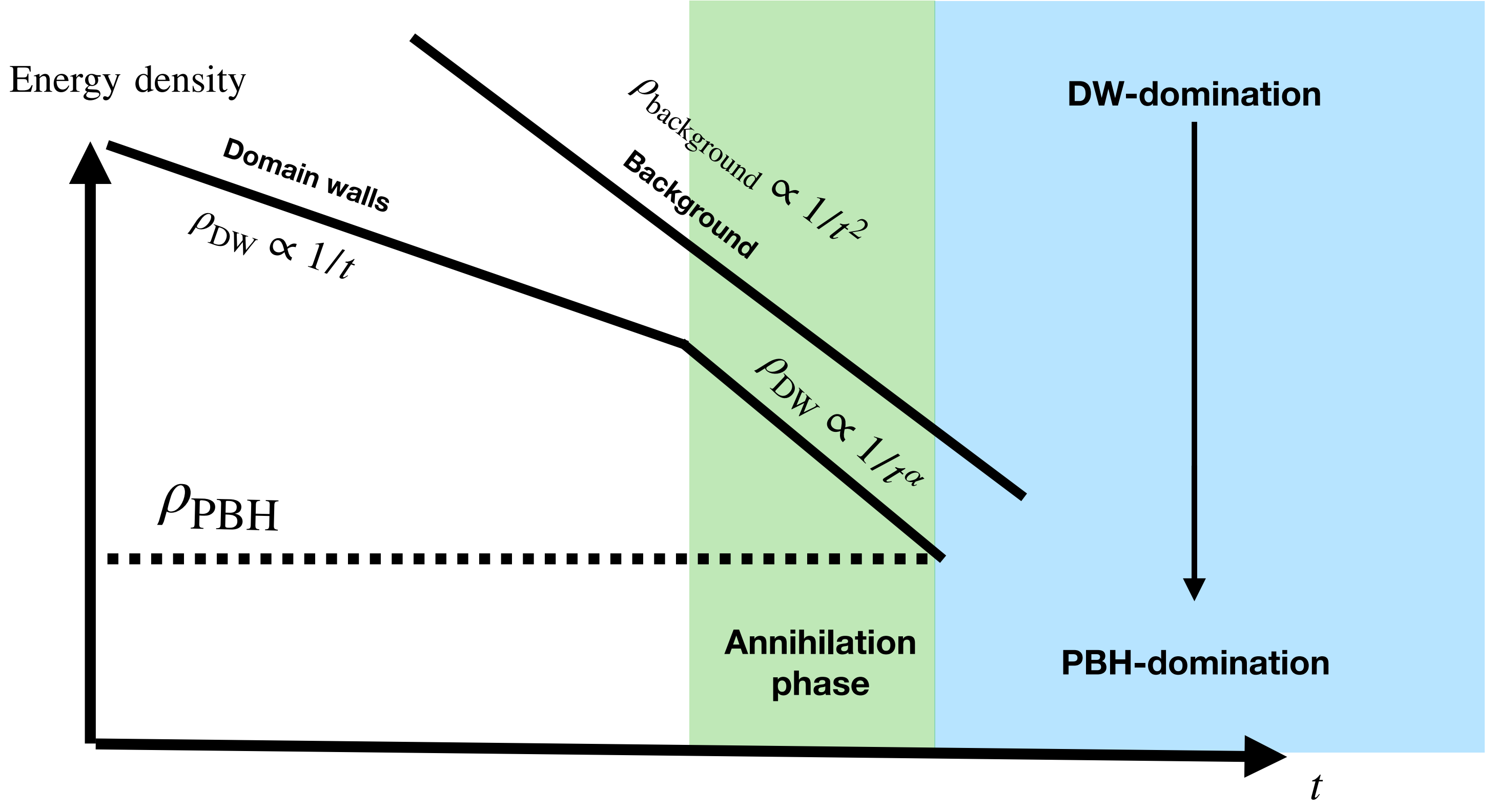
DW-domination



PBH-domination



t



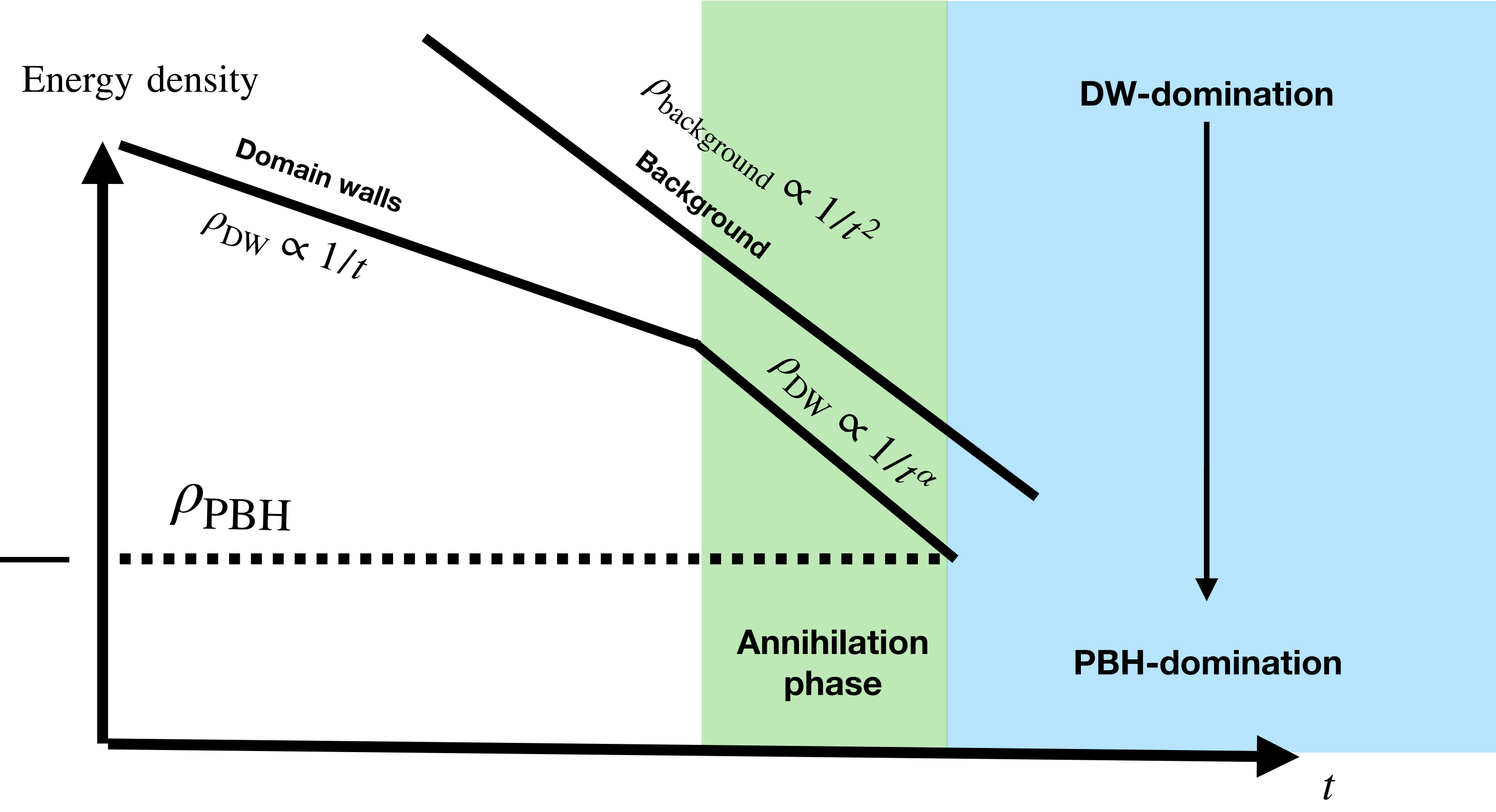
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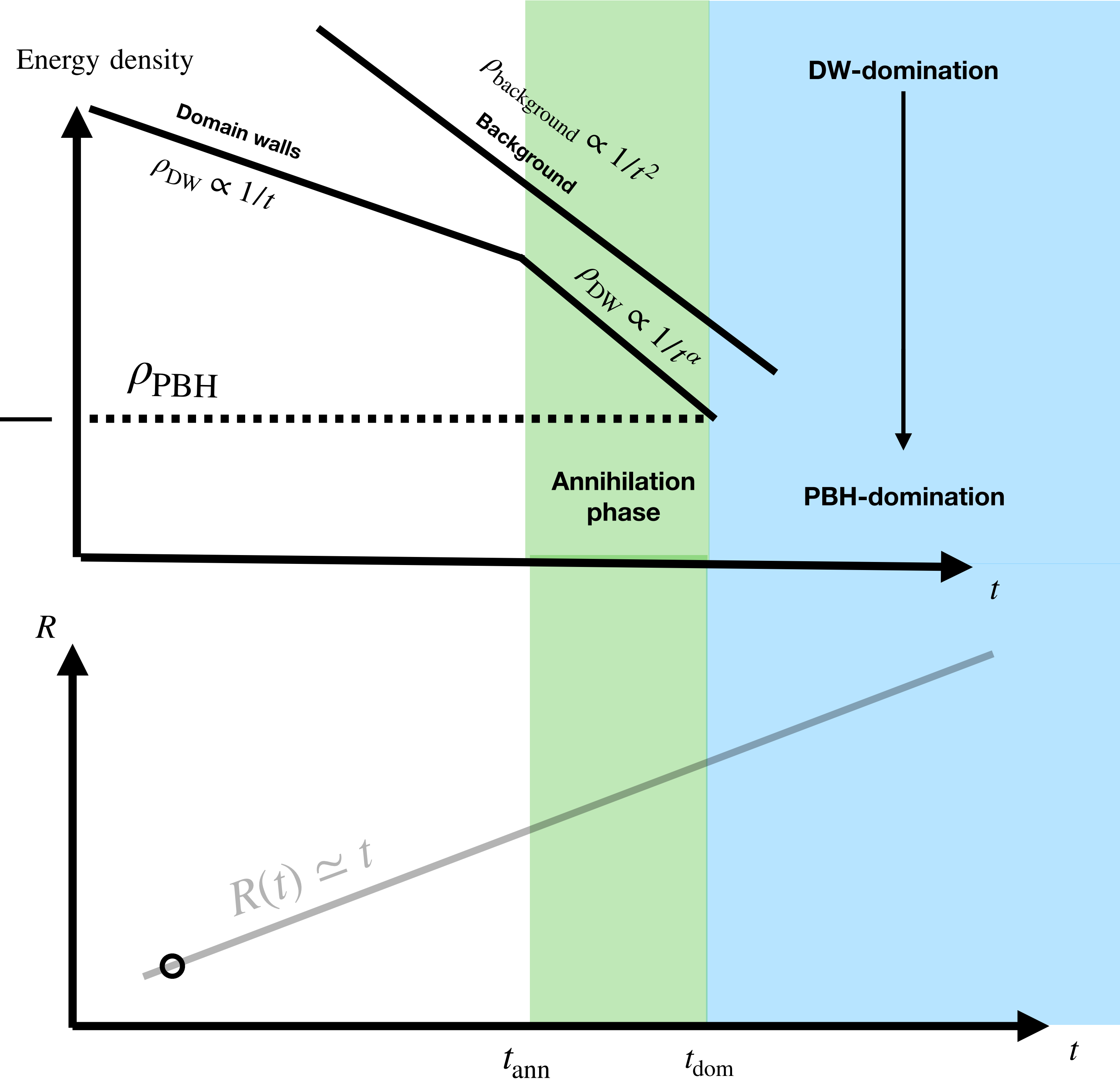
2023: YG, E. Vitagliano, 2306.17841

Assumption: $R(t) \simeq t$



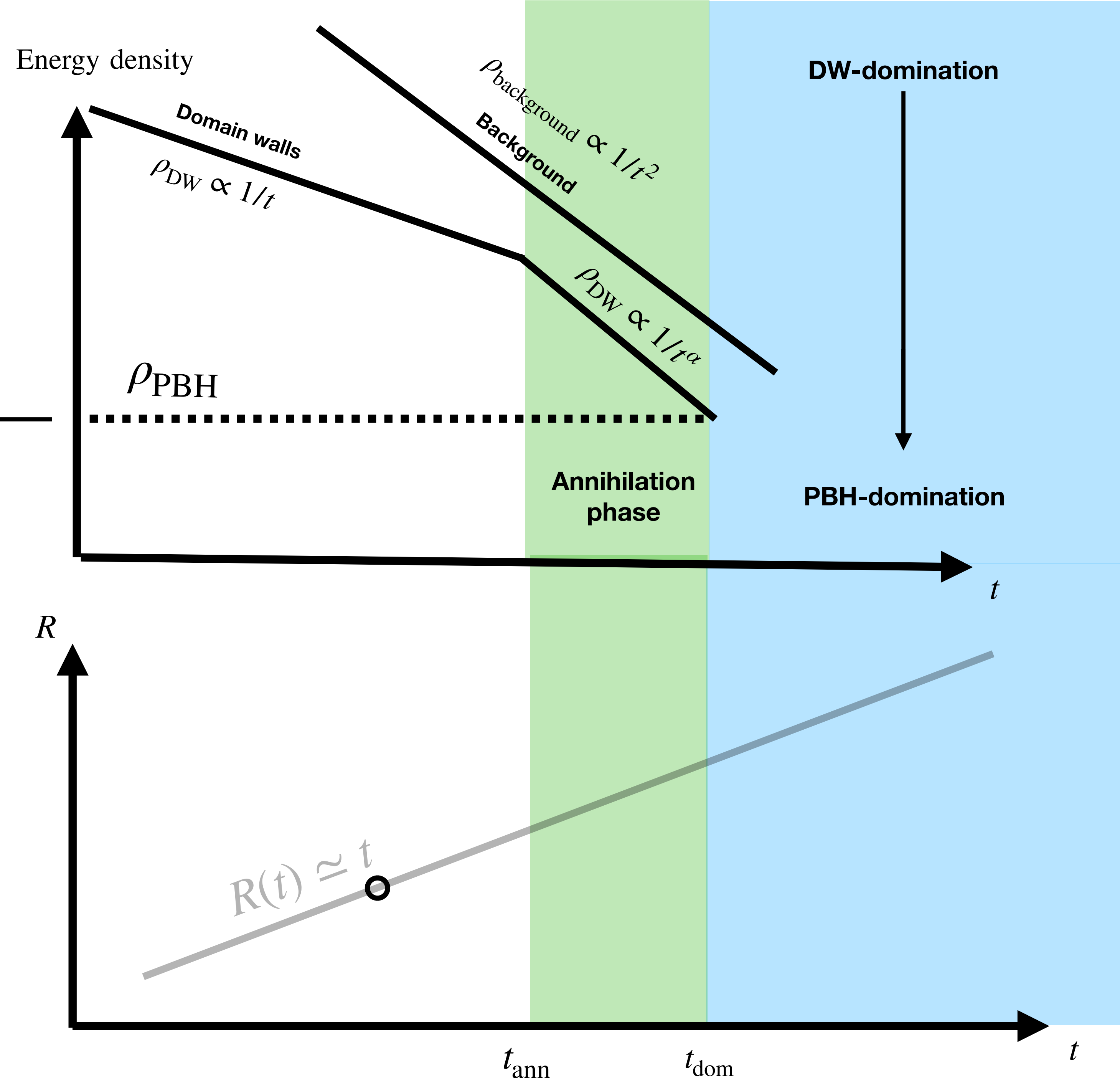
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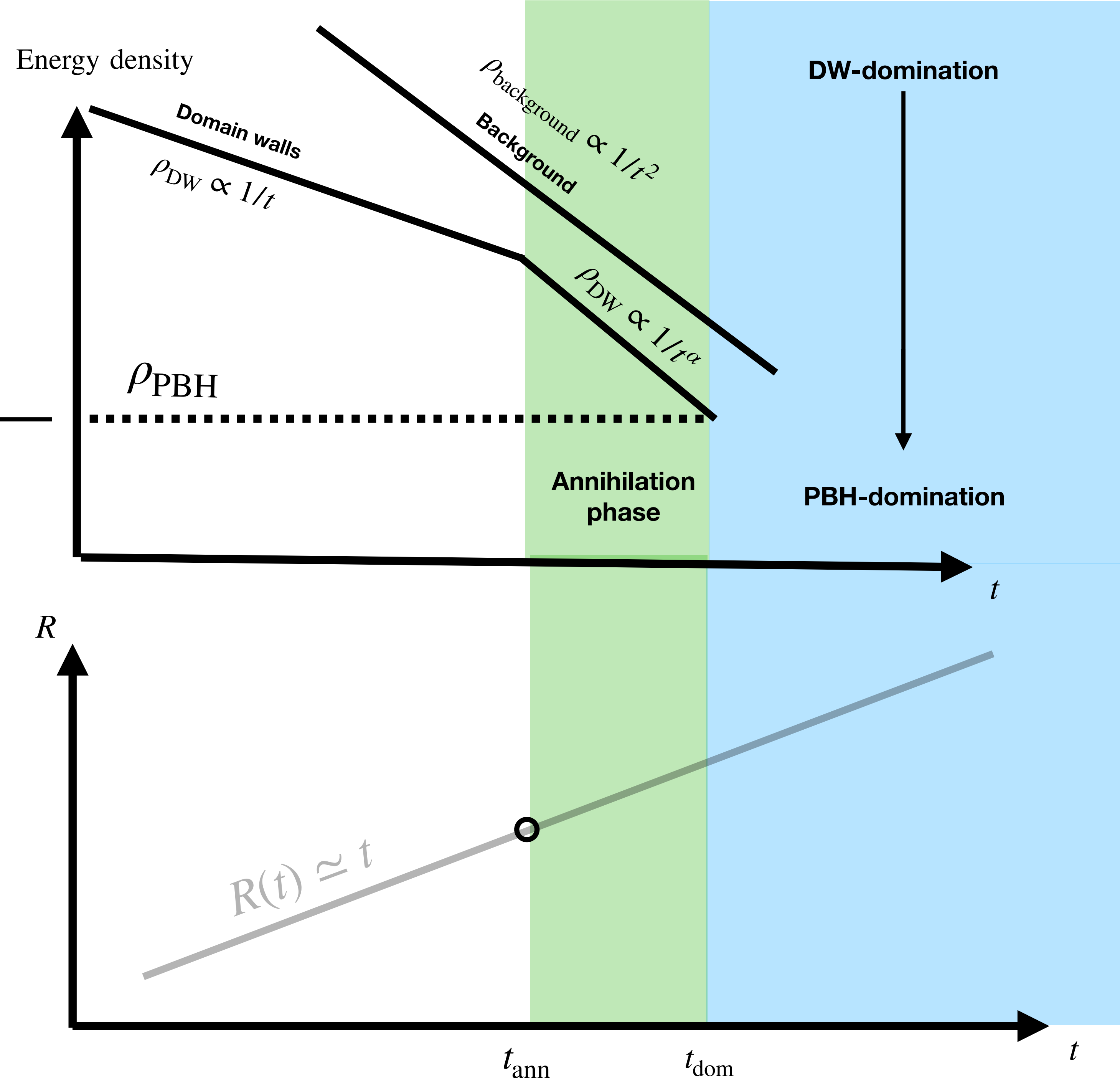
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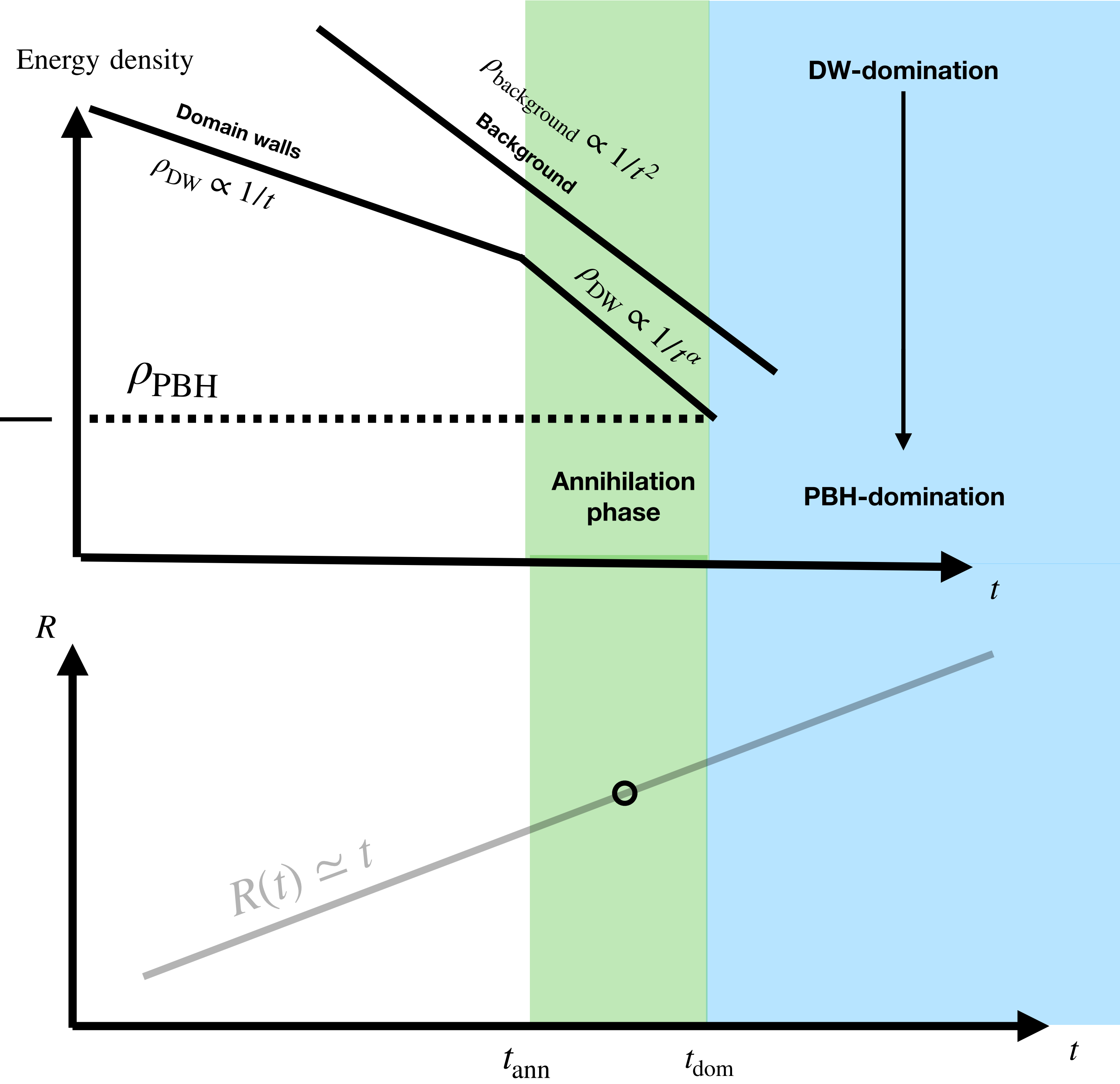
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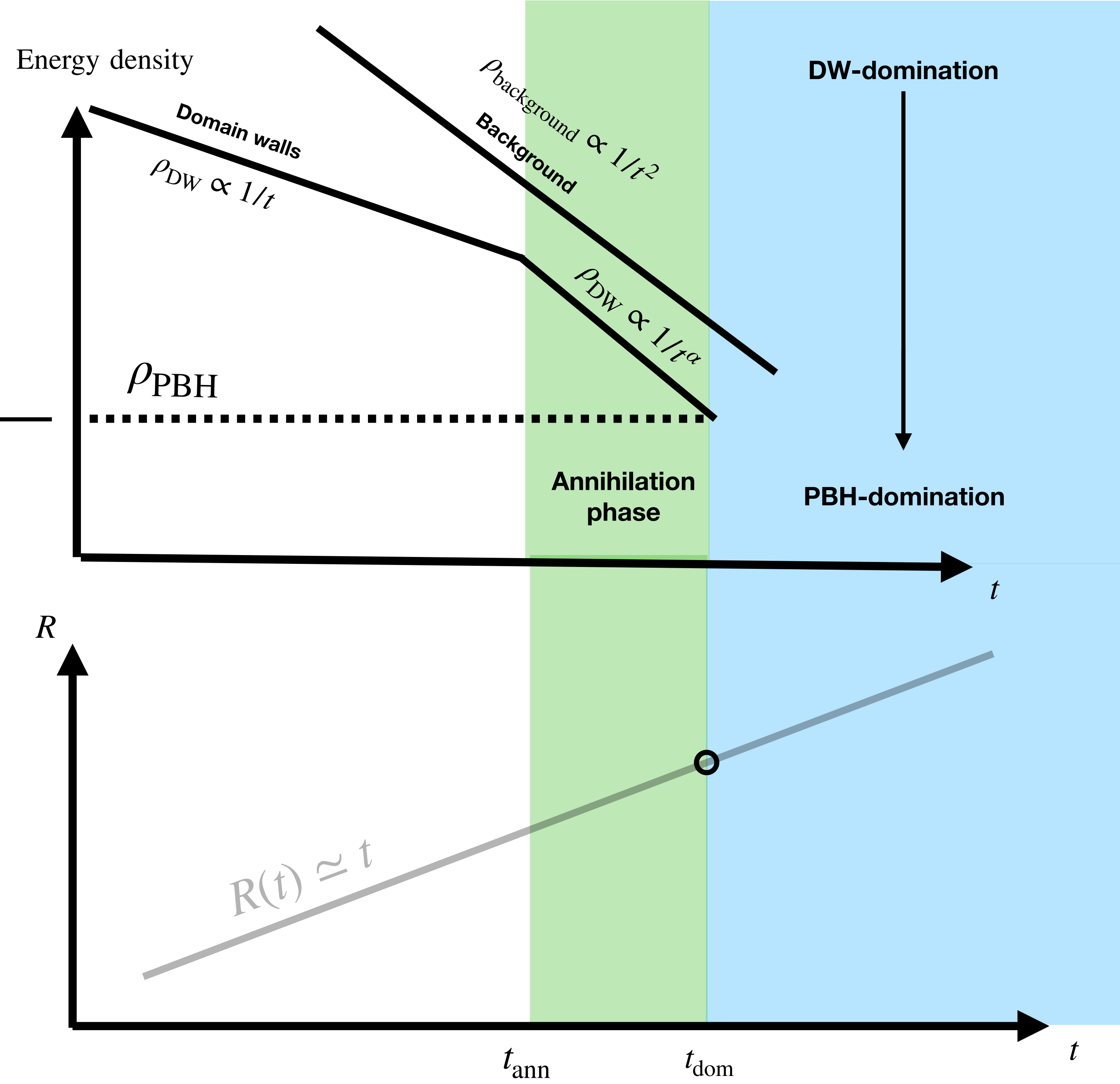
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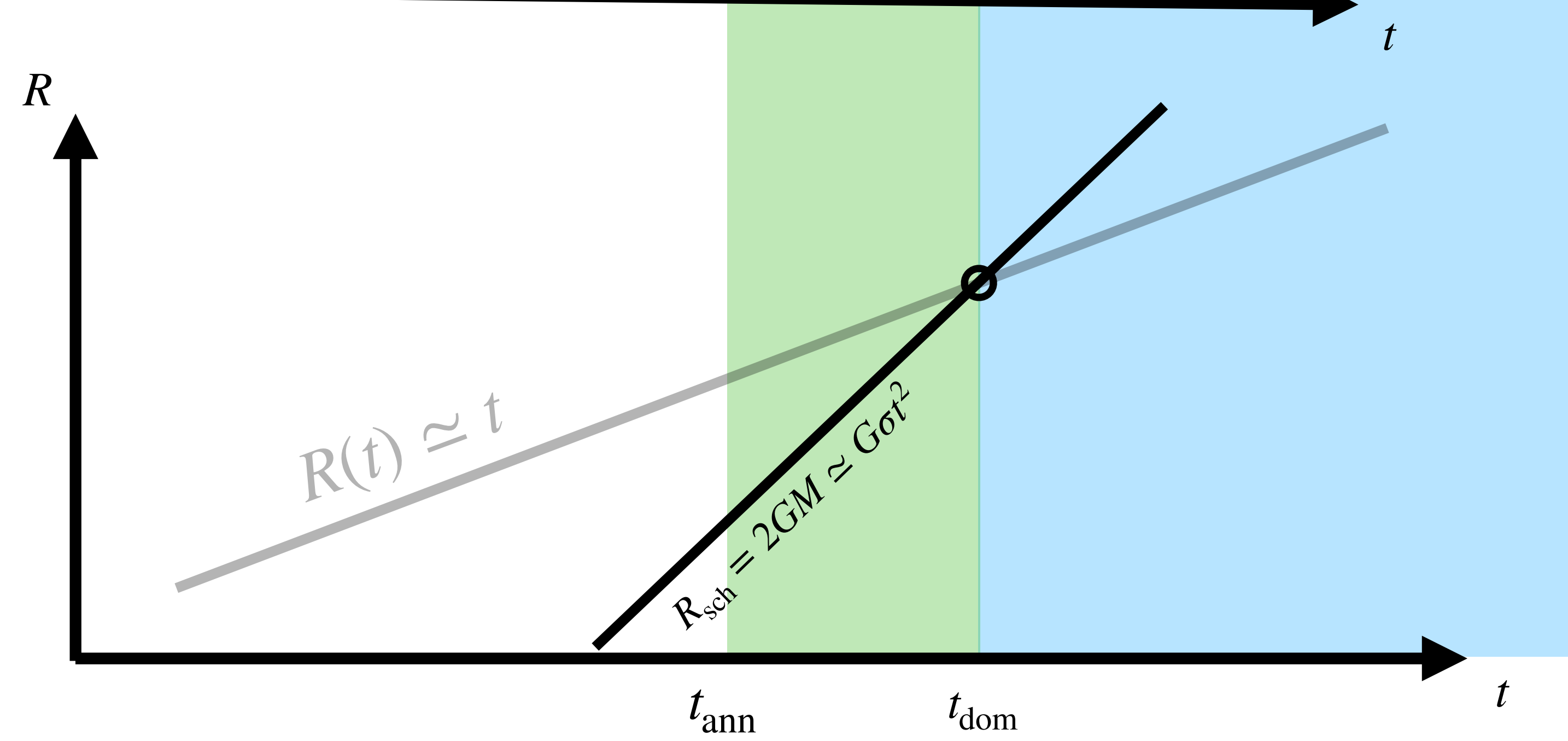
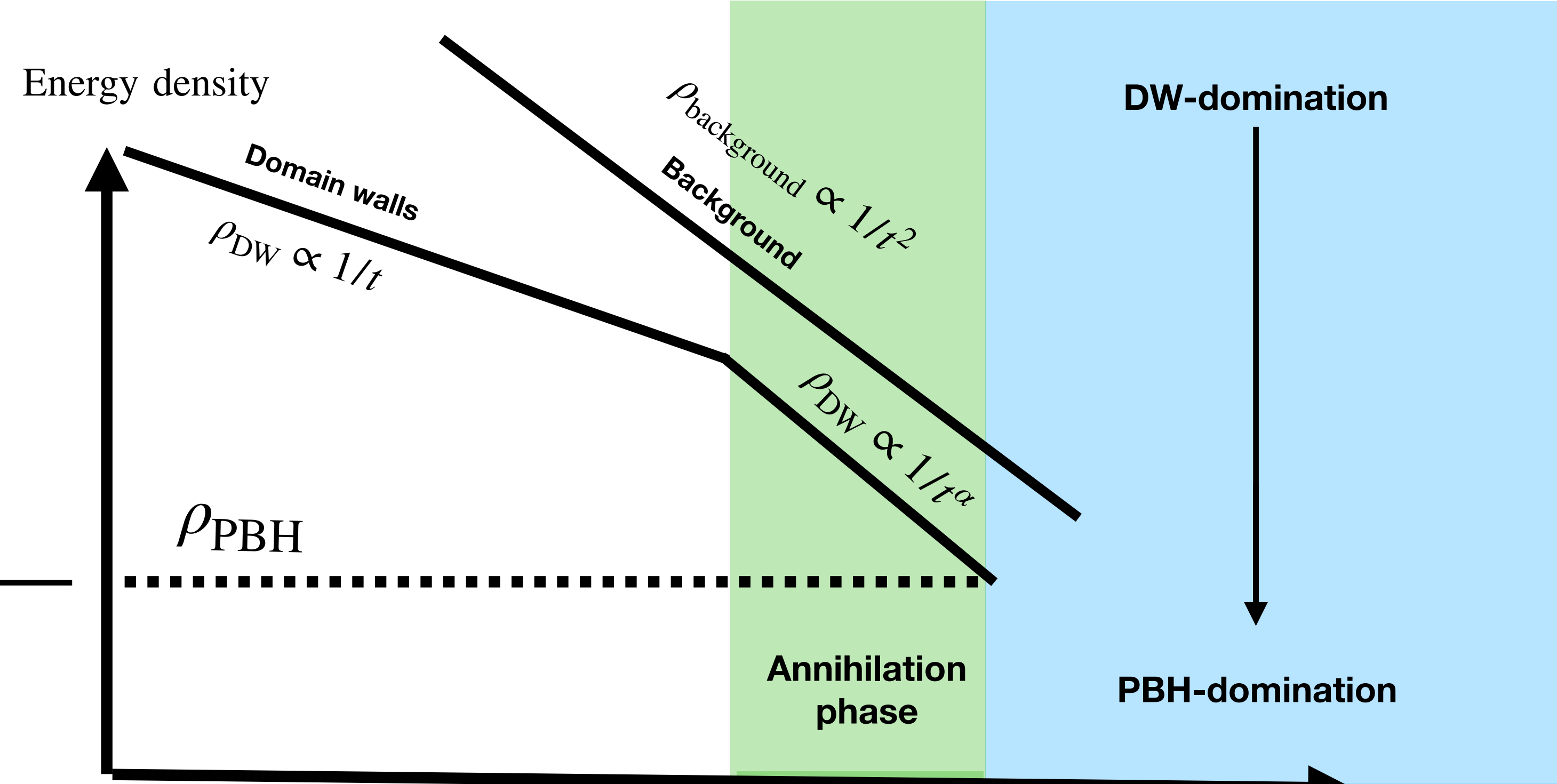
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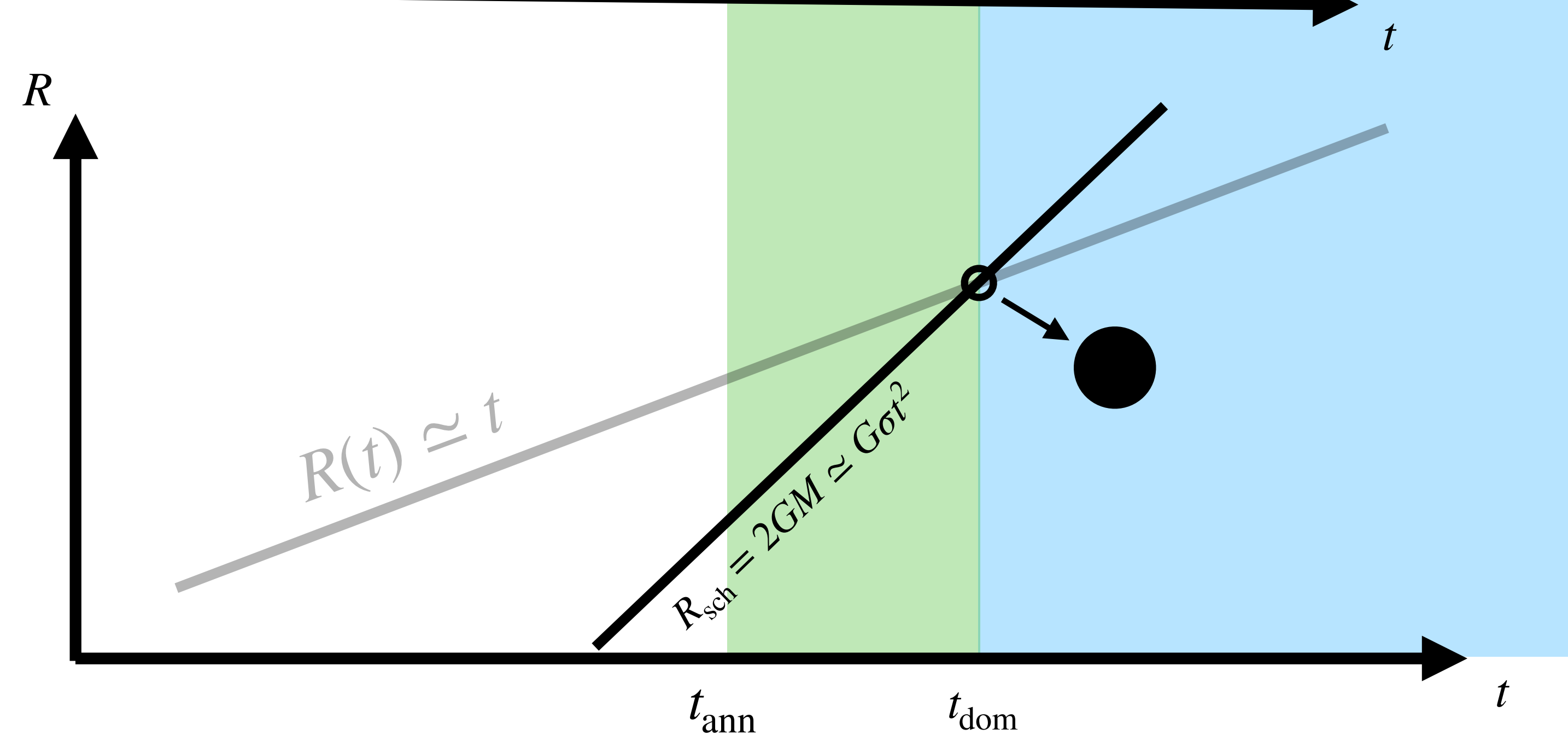
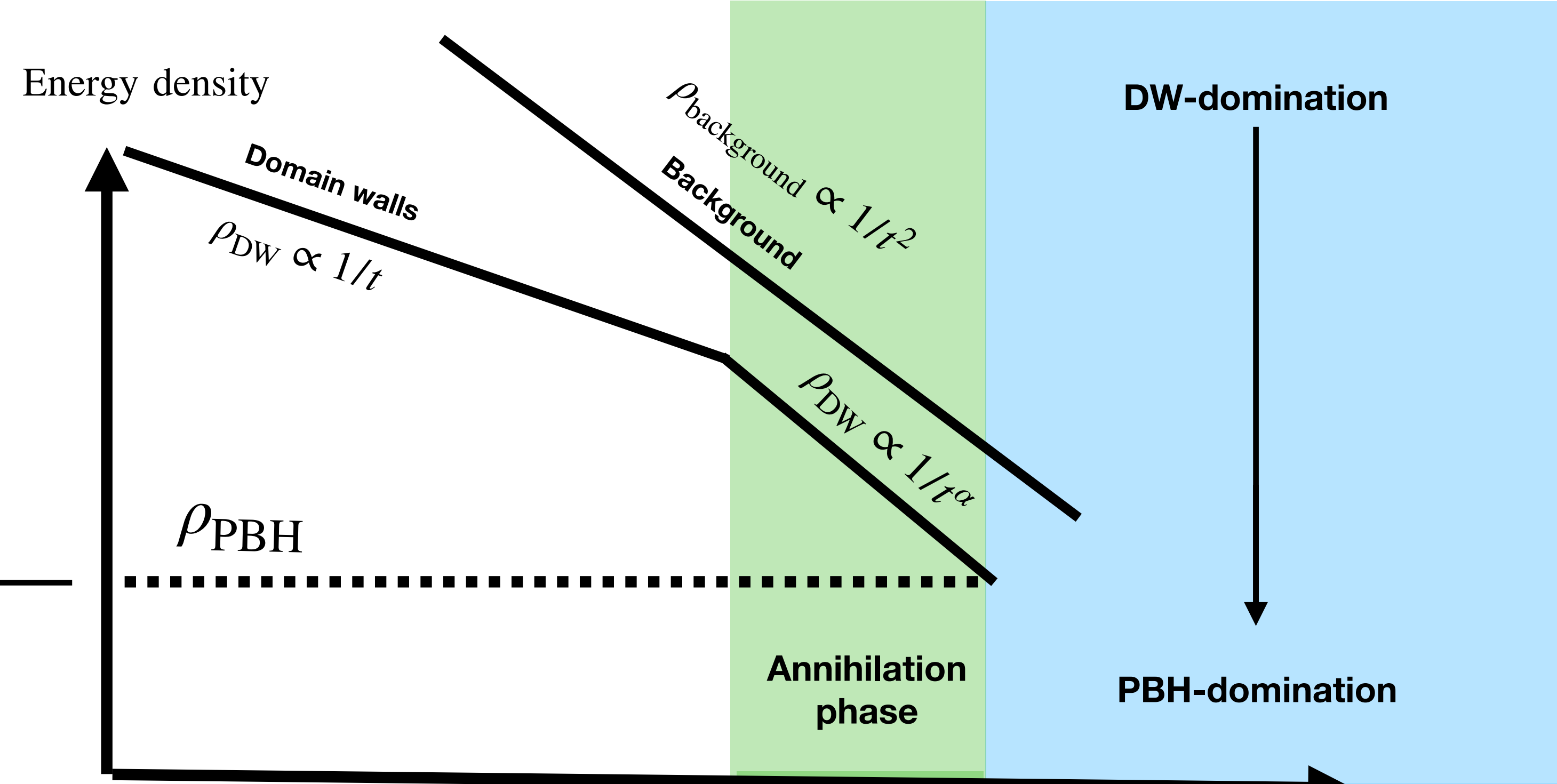
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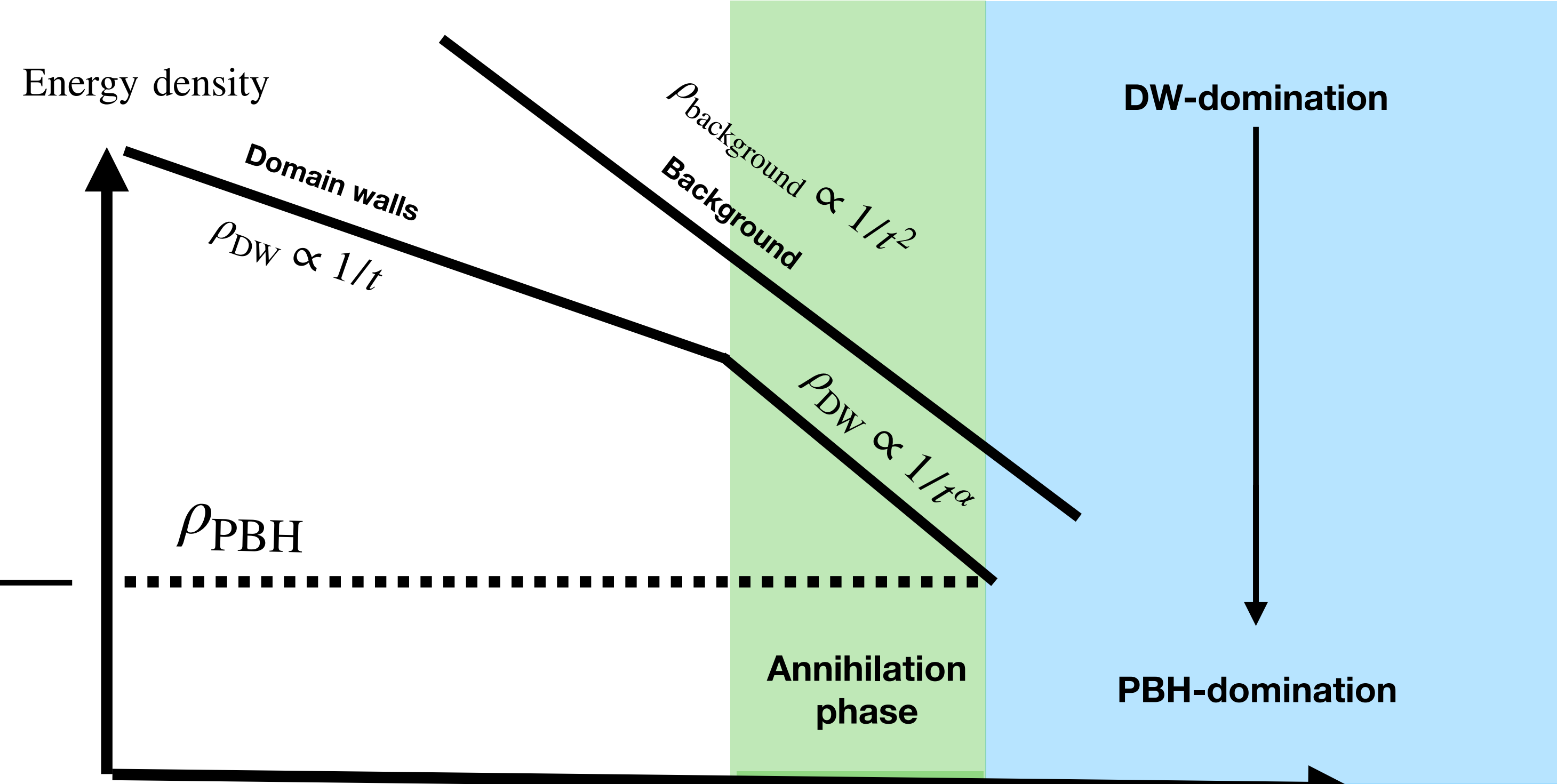


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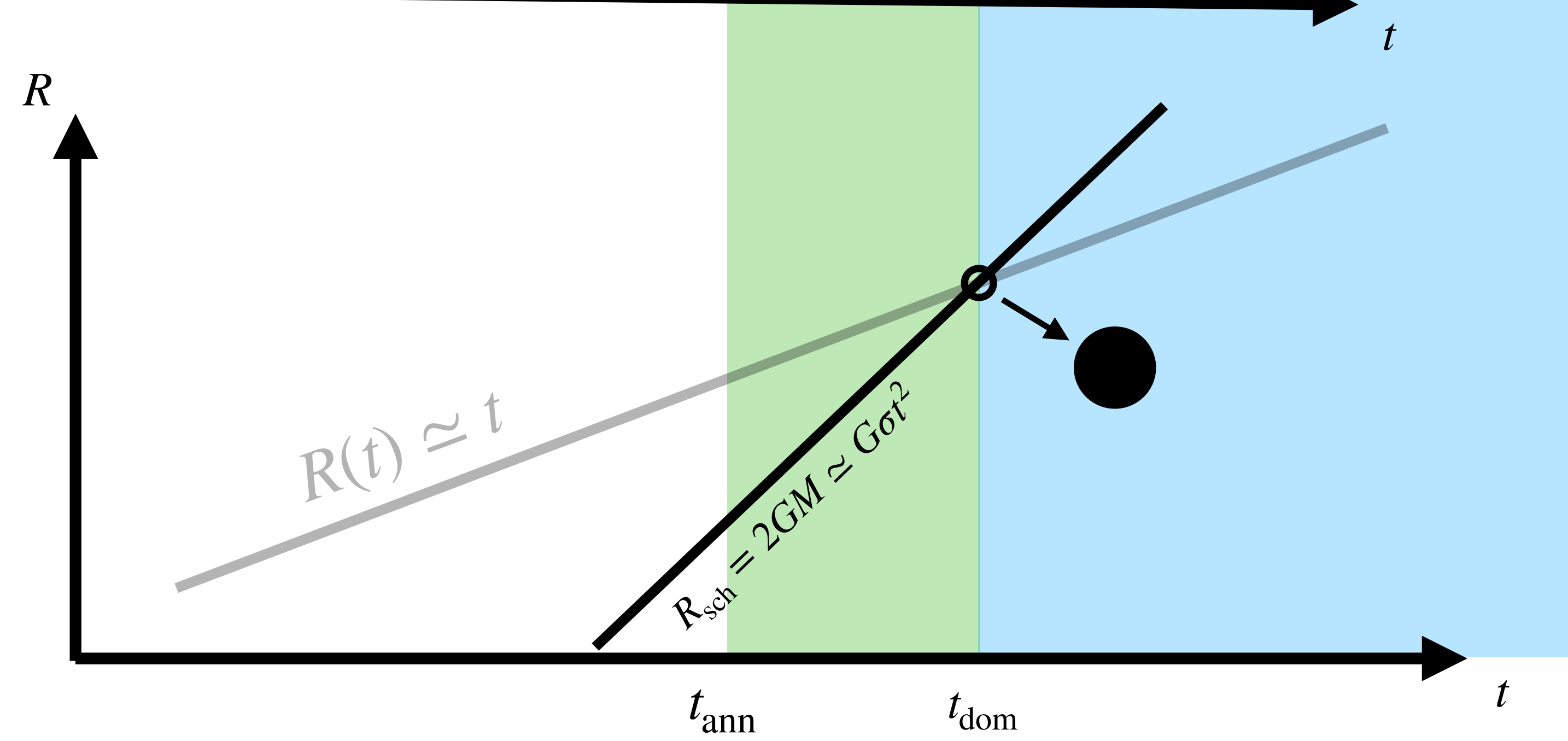
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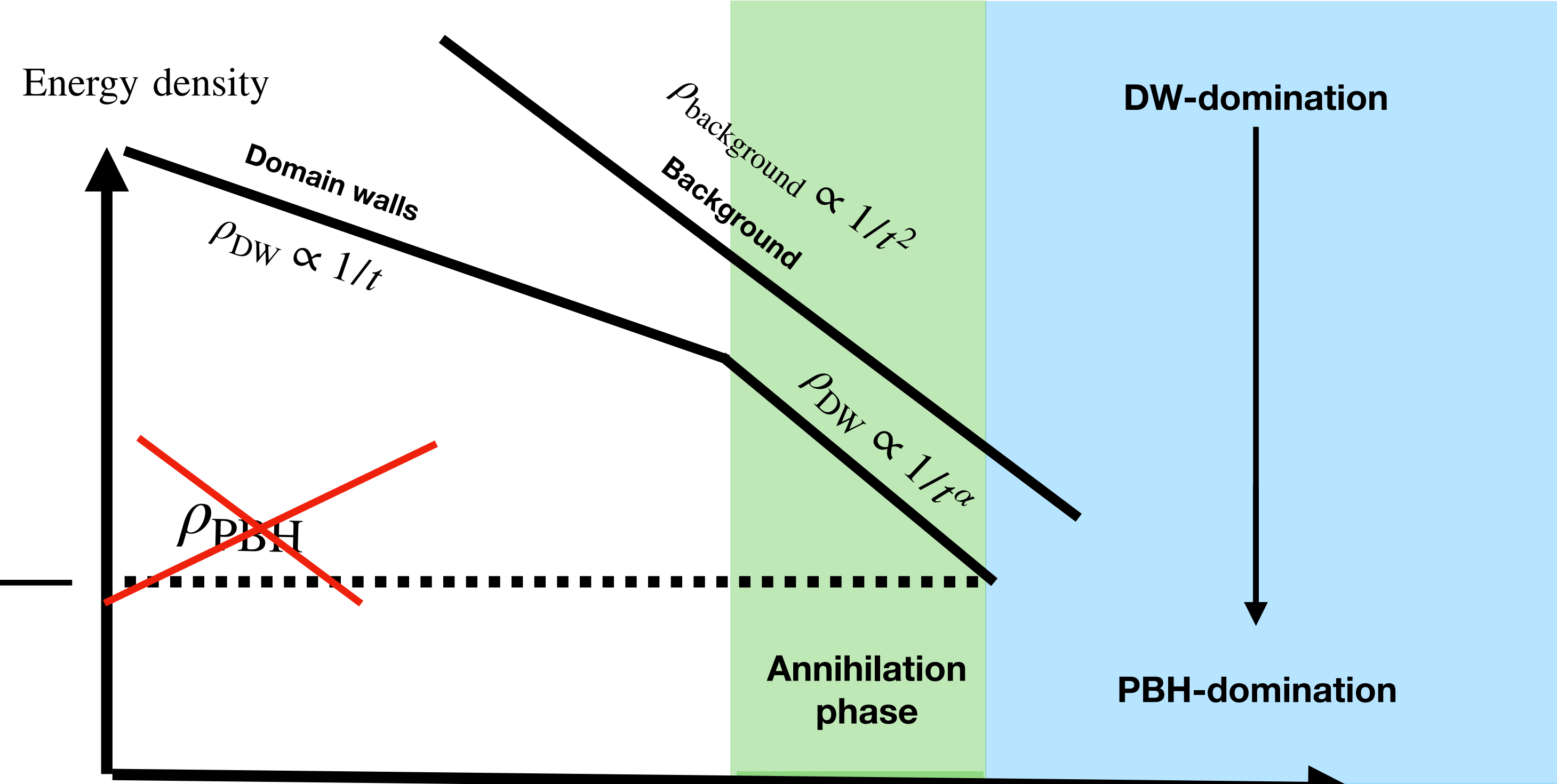
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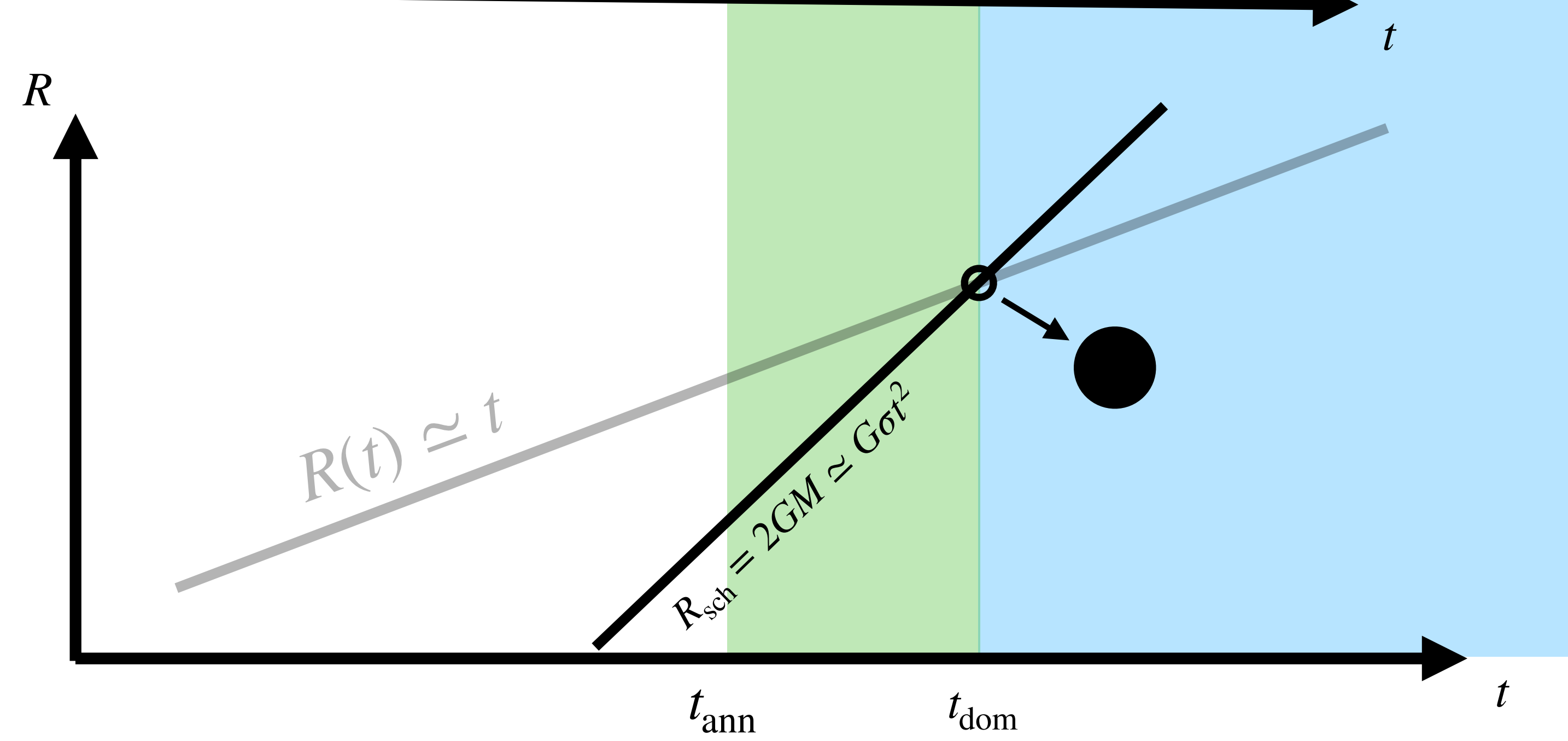
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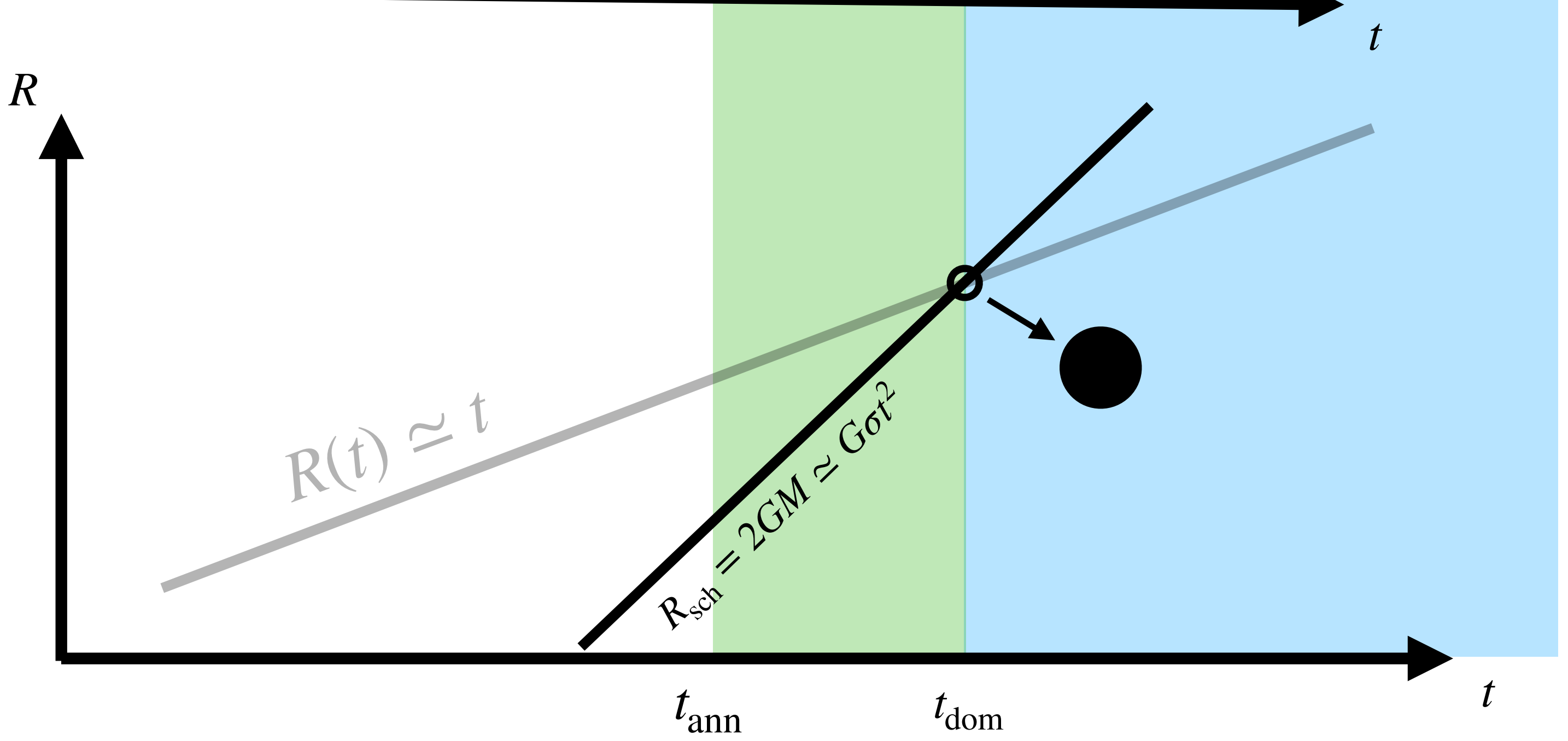
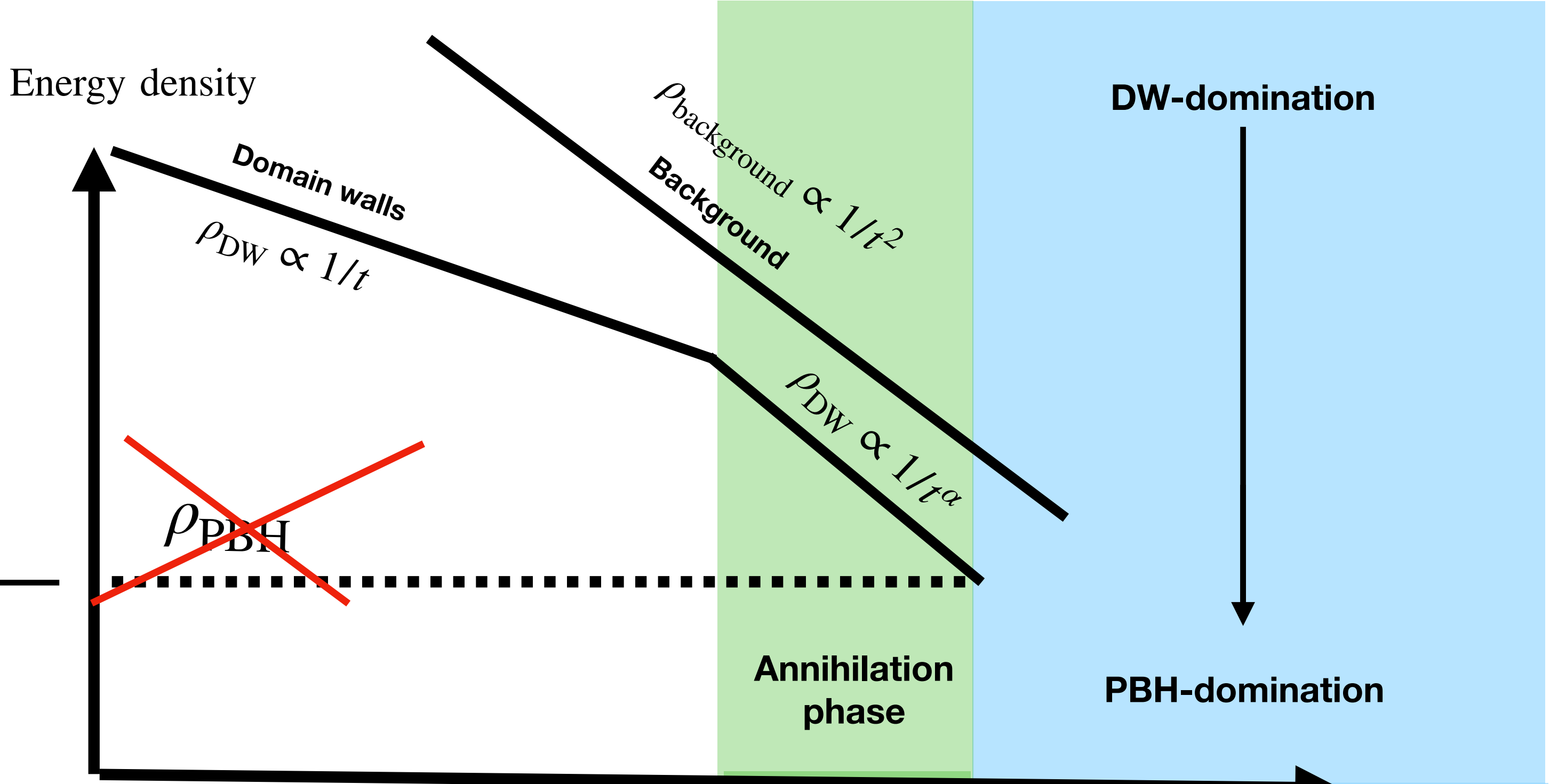
~~2018: Ferrer, Masso, Panico, Pujolas, Rompineve, Phys.Rev.Lett. 122 (2019) 10, 101304, 1807.01707~~

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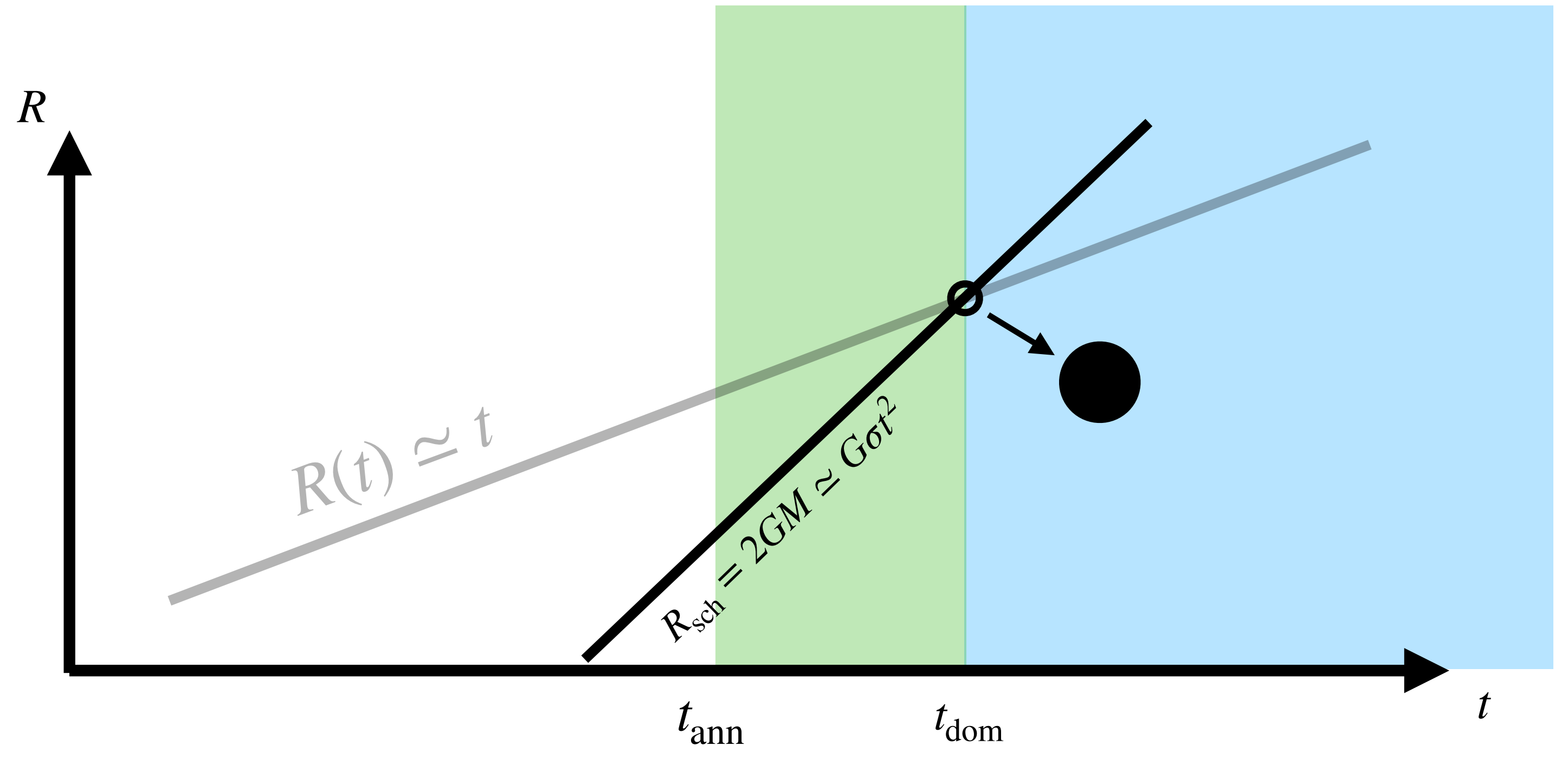
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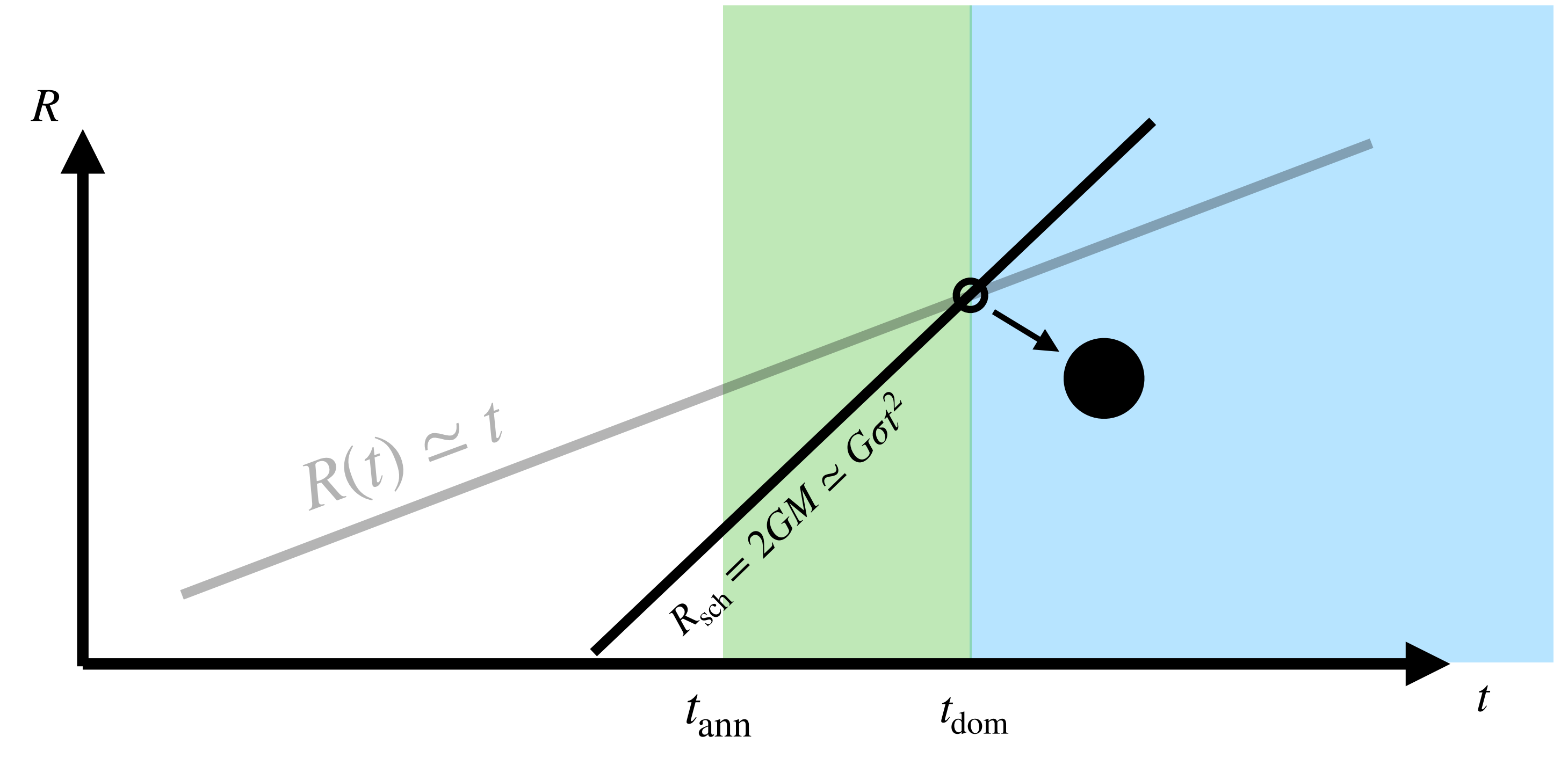


~~Assumption: $R(t) \simeq t$~~



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Go back to basics:

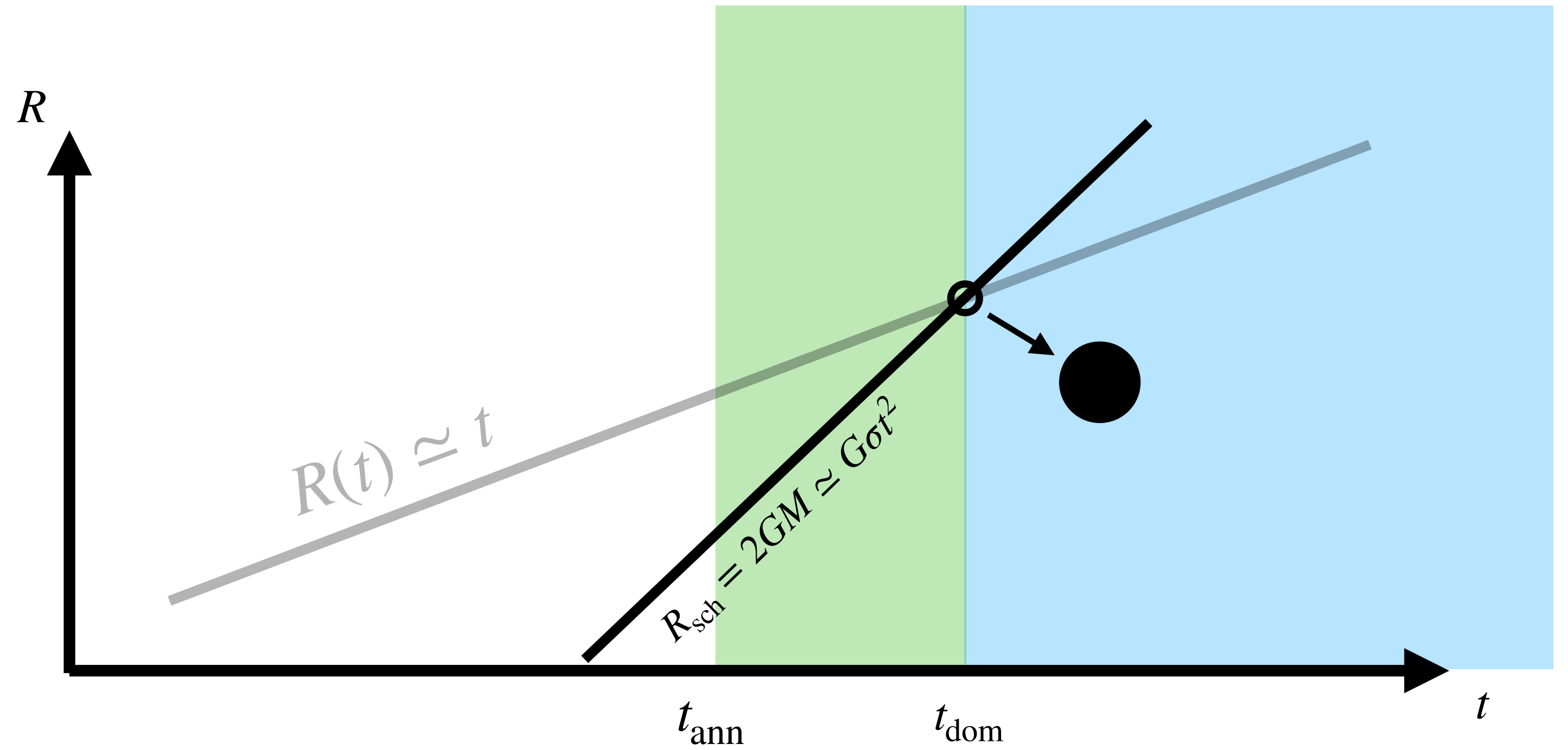


~~Assumption: $R(t) \simeq t$~~

Go back to basics:

$$\ddot{\chi} + (4 - 3a^2\dot{\chi}^2)H\dot{\chi} + \frac{2}{a^2\chi}(1 - a^2\dot{\chi}^2) = - \left(\frac{V_{\text{bias}}}{\sigma} + 6\pi\sigma \right) \frac{(1 - a^2\dot{\chi}^2)^{3/2}}{a}$$

$$R(t) = a(t)\chi(t)$$

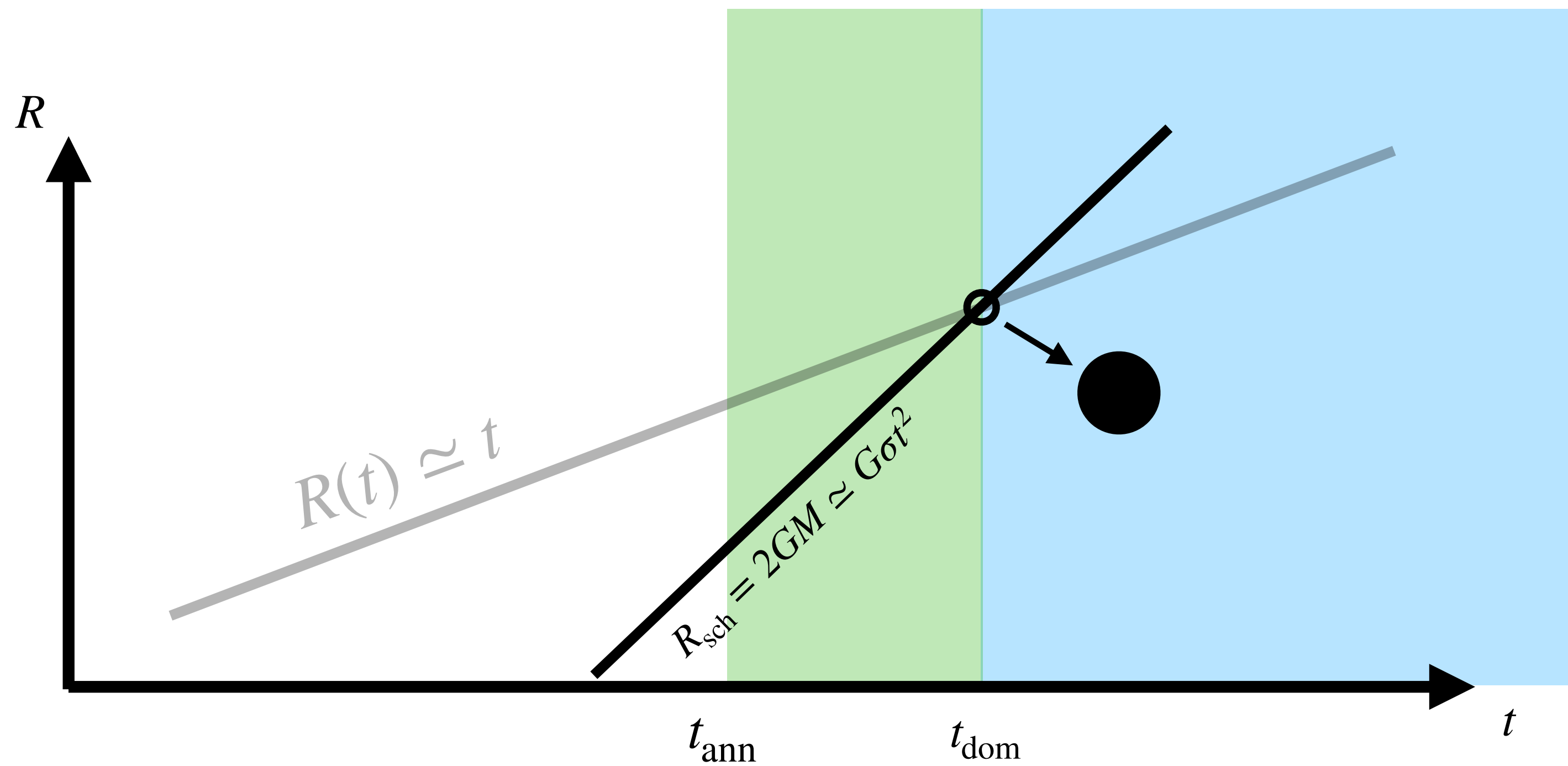
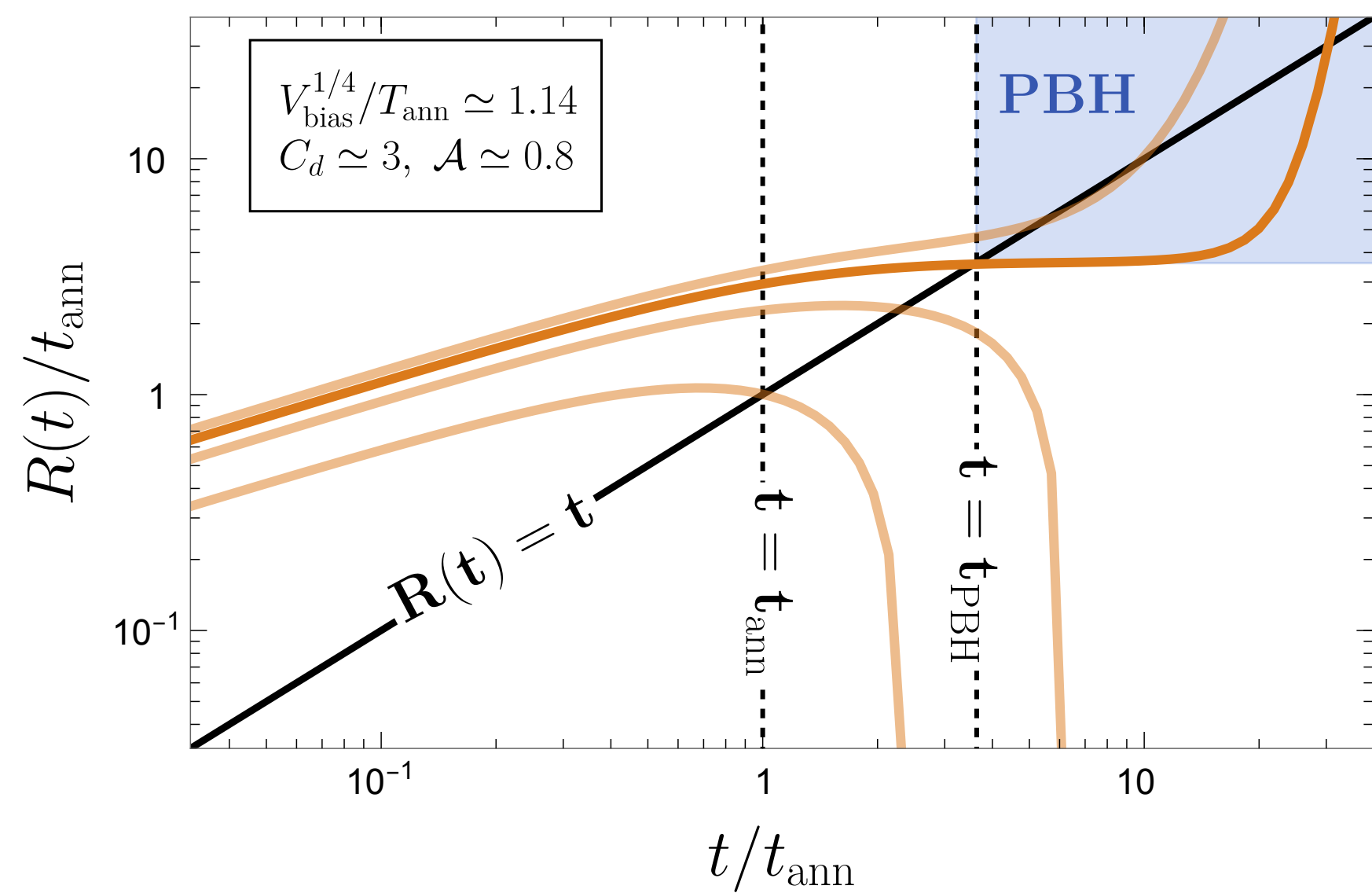


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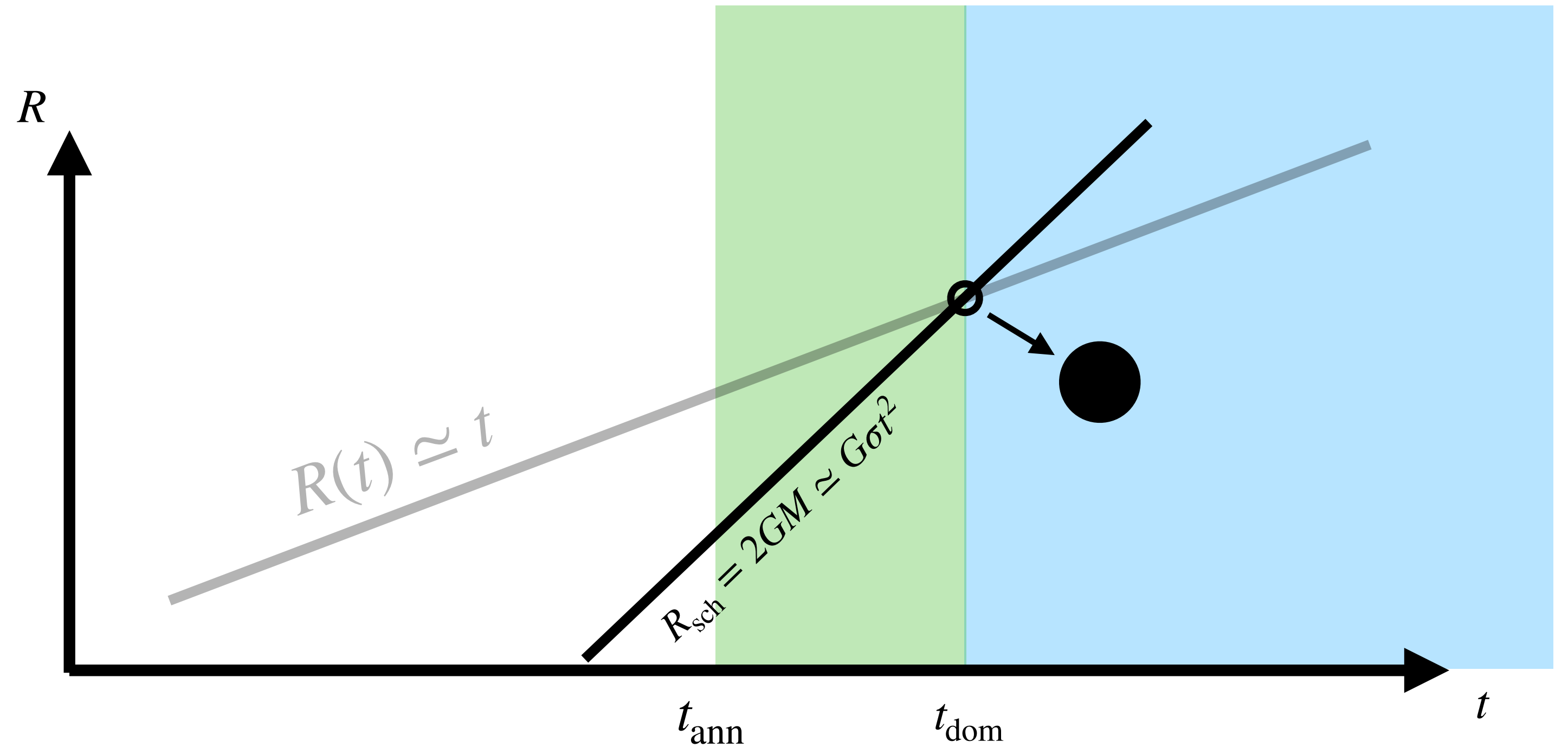
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$$R(t) = a(t)\chi(t)$$

Result:

$$R(t) \propto \begin{cases} a(t), & \text{if } R > t, \\ e^{-\Gamma t}, & \text{if } R < t. \end{cases}$$



~~Assumption: $R(t) \simeq t$~~

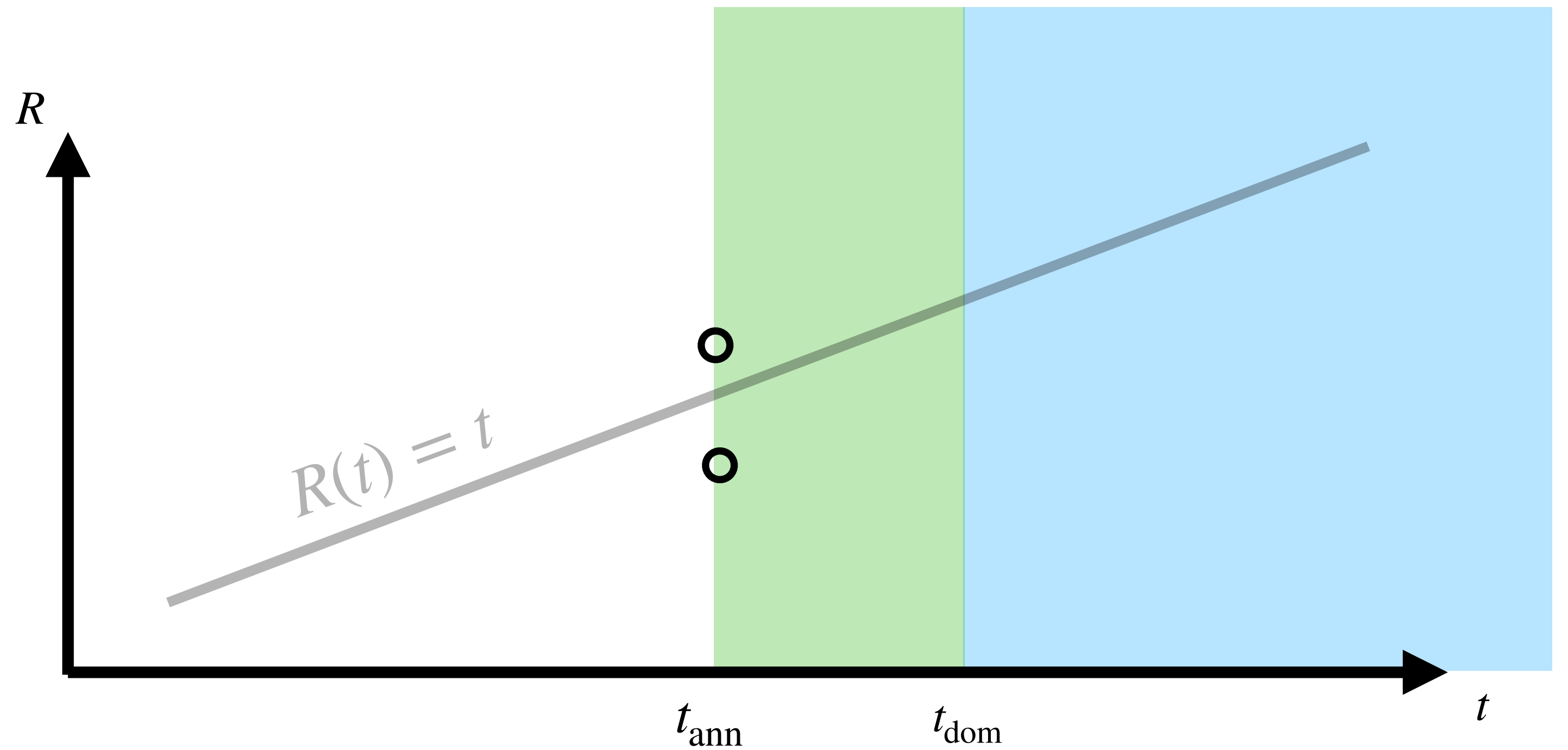
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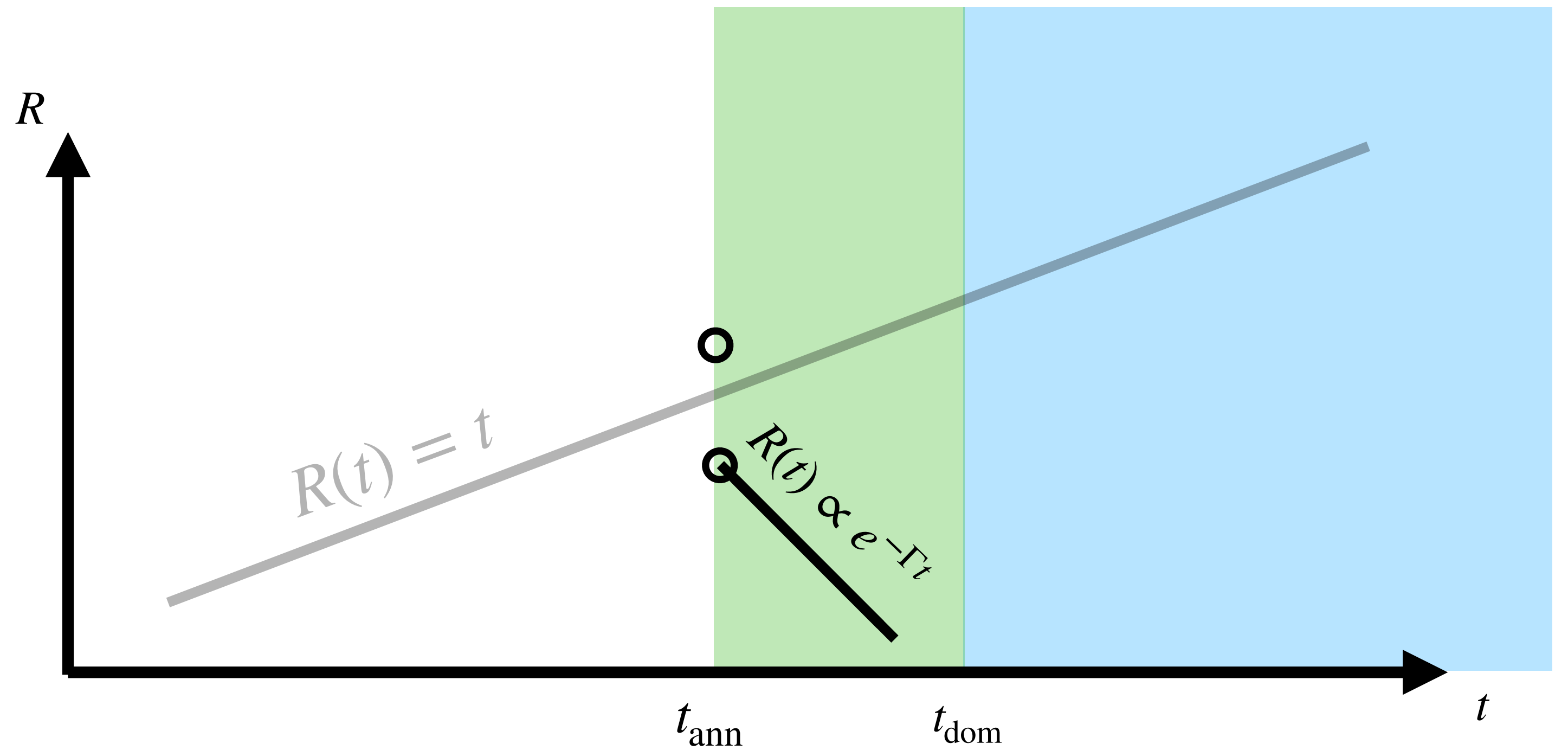
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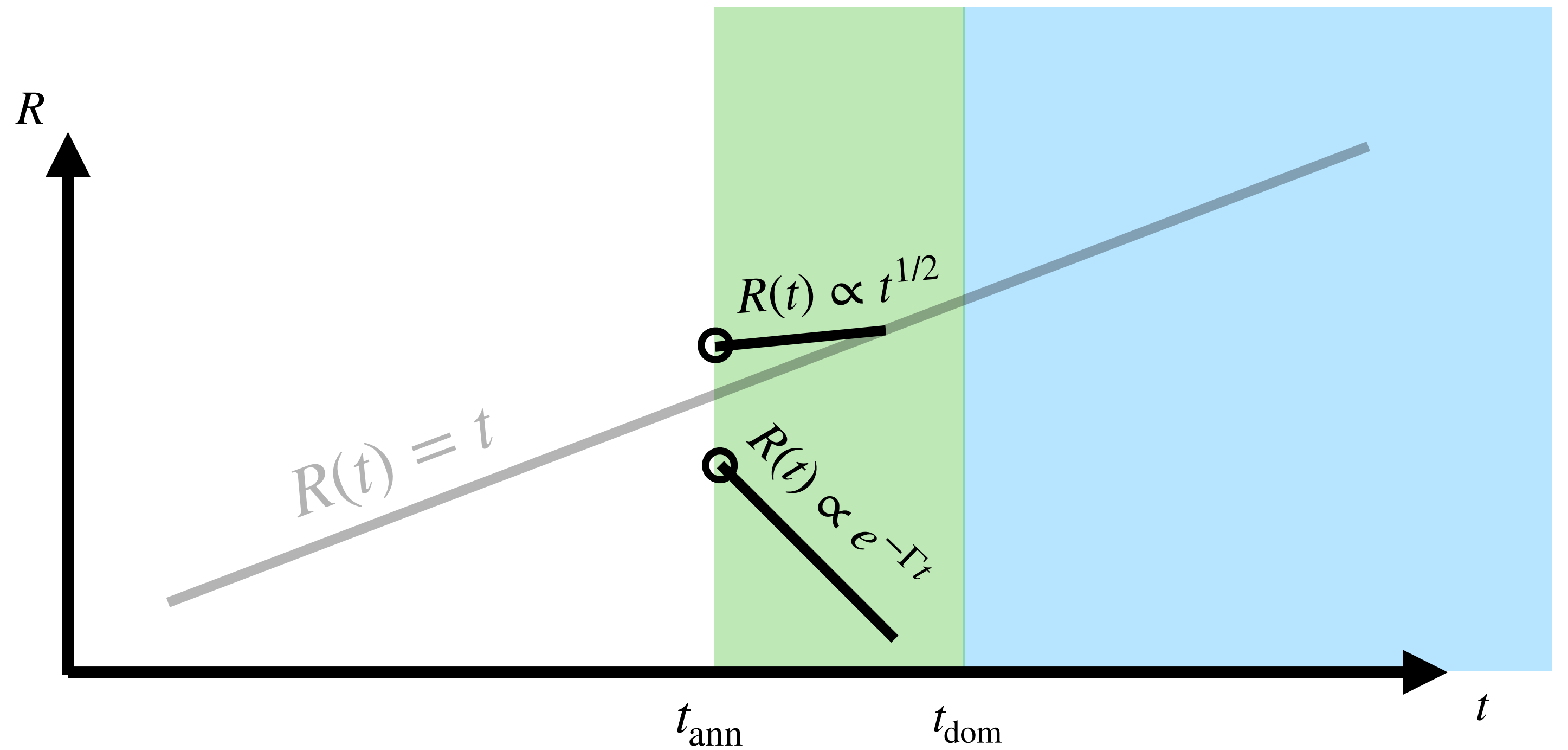
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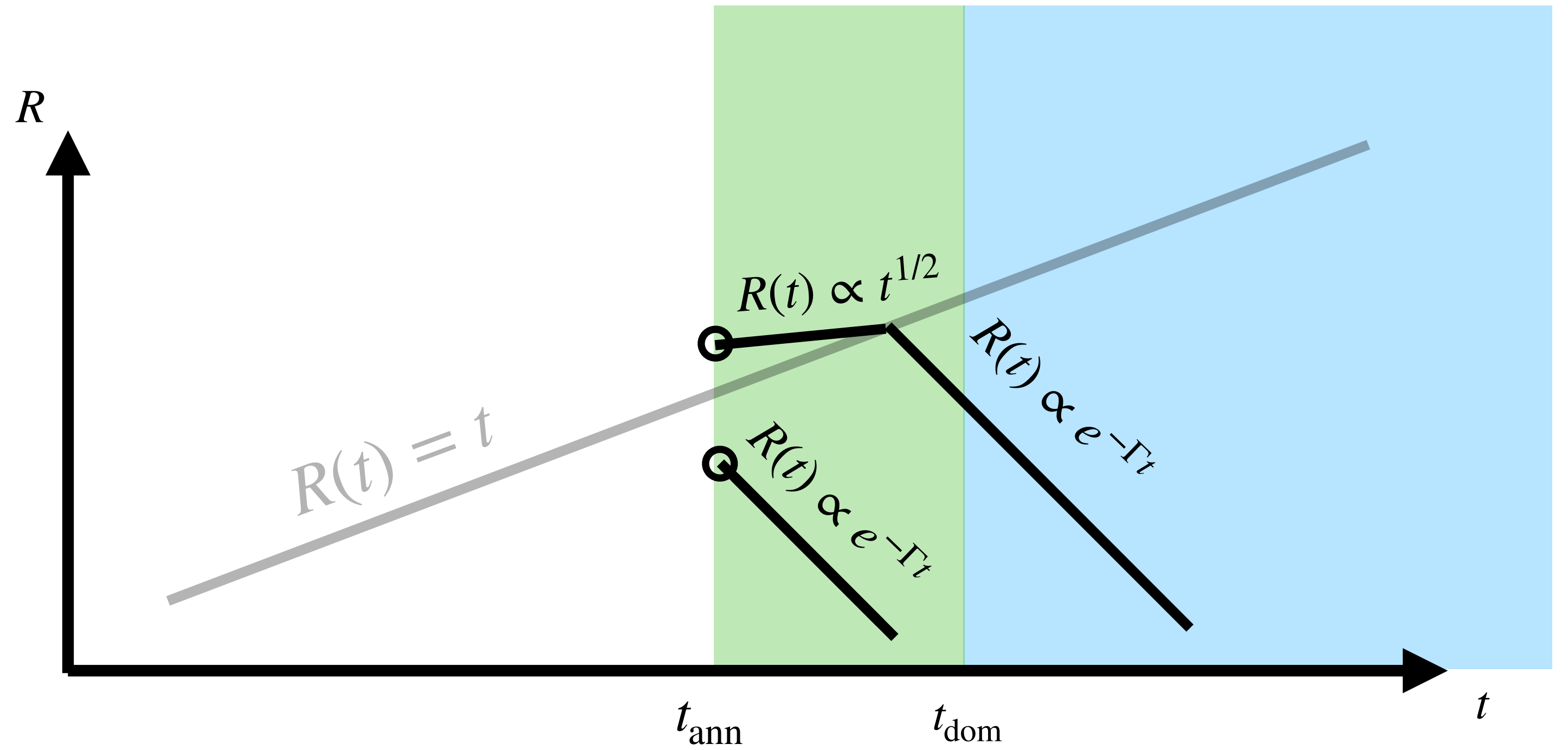
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Scaling regime: $\langle R(t) \rangle \simeq t$ ✓

~~Assumption: $R(t) \simeq t$~~

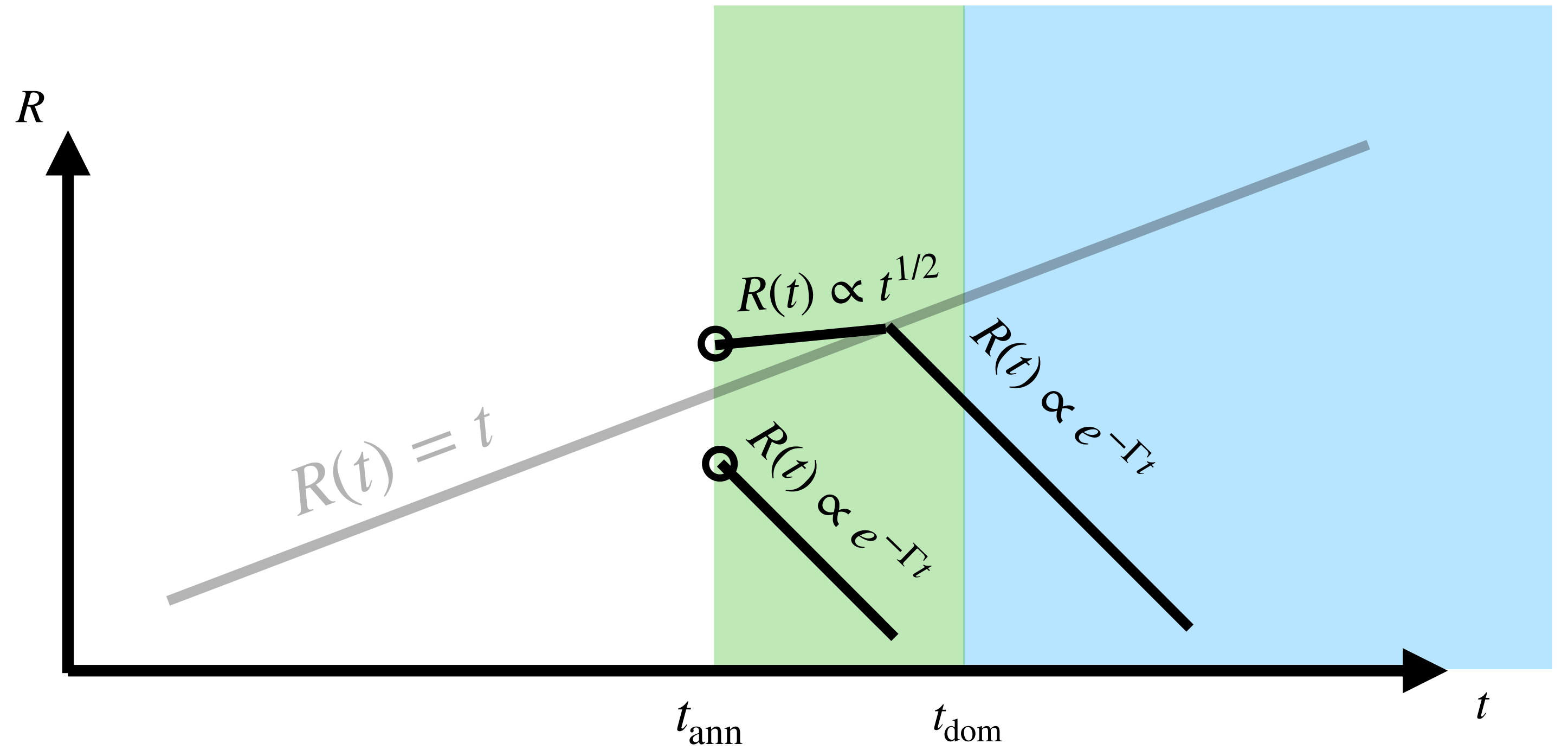
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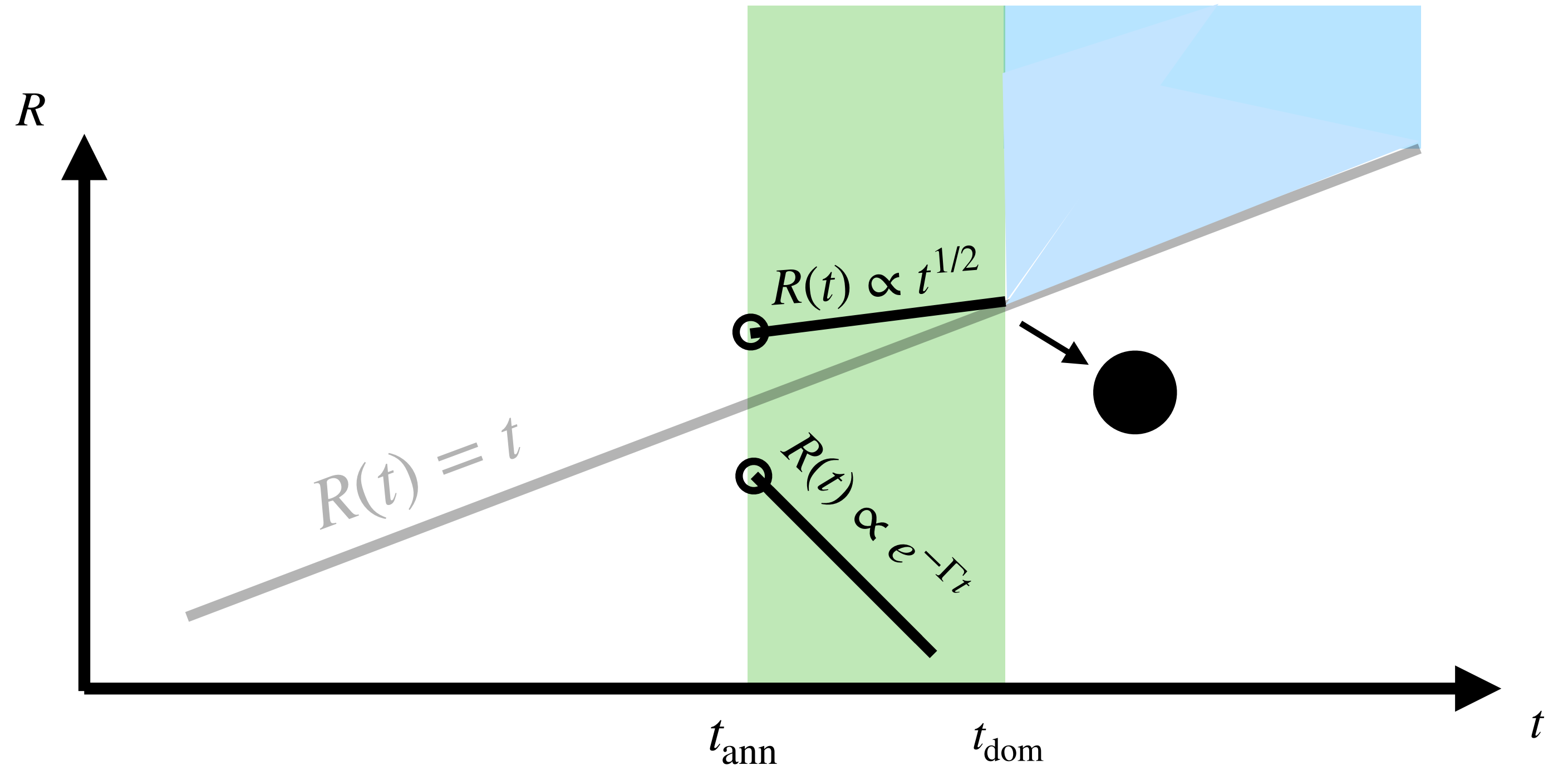
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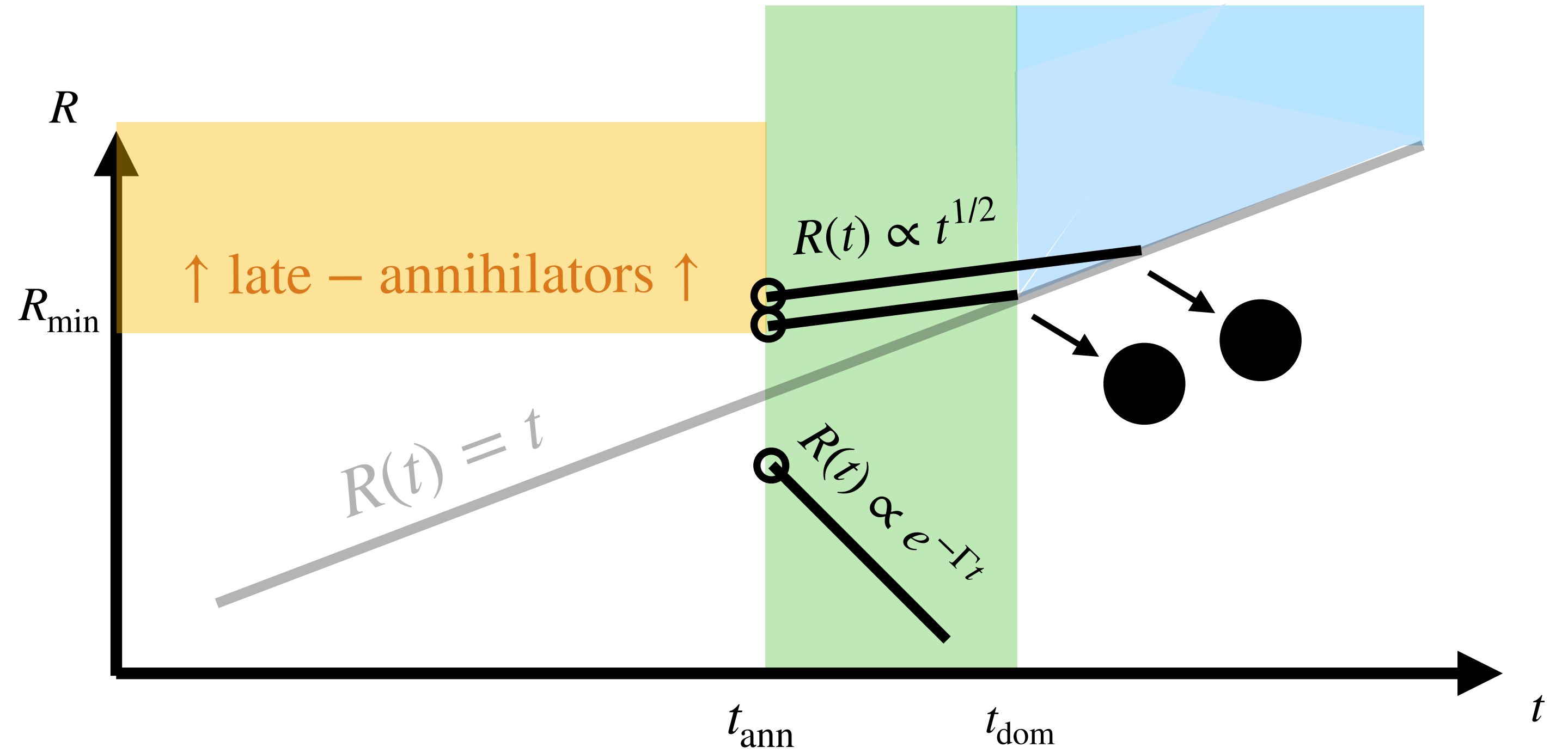
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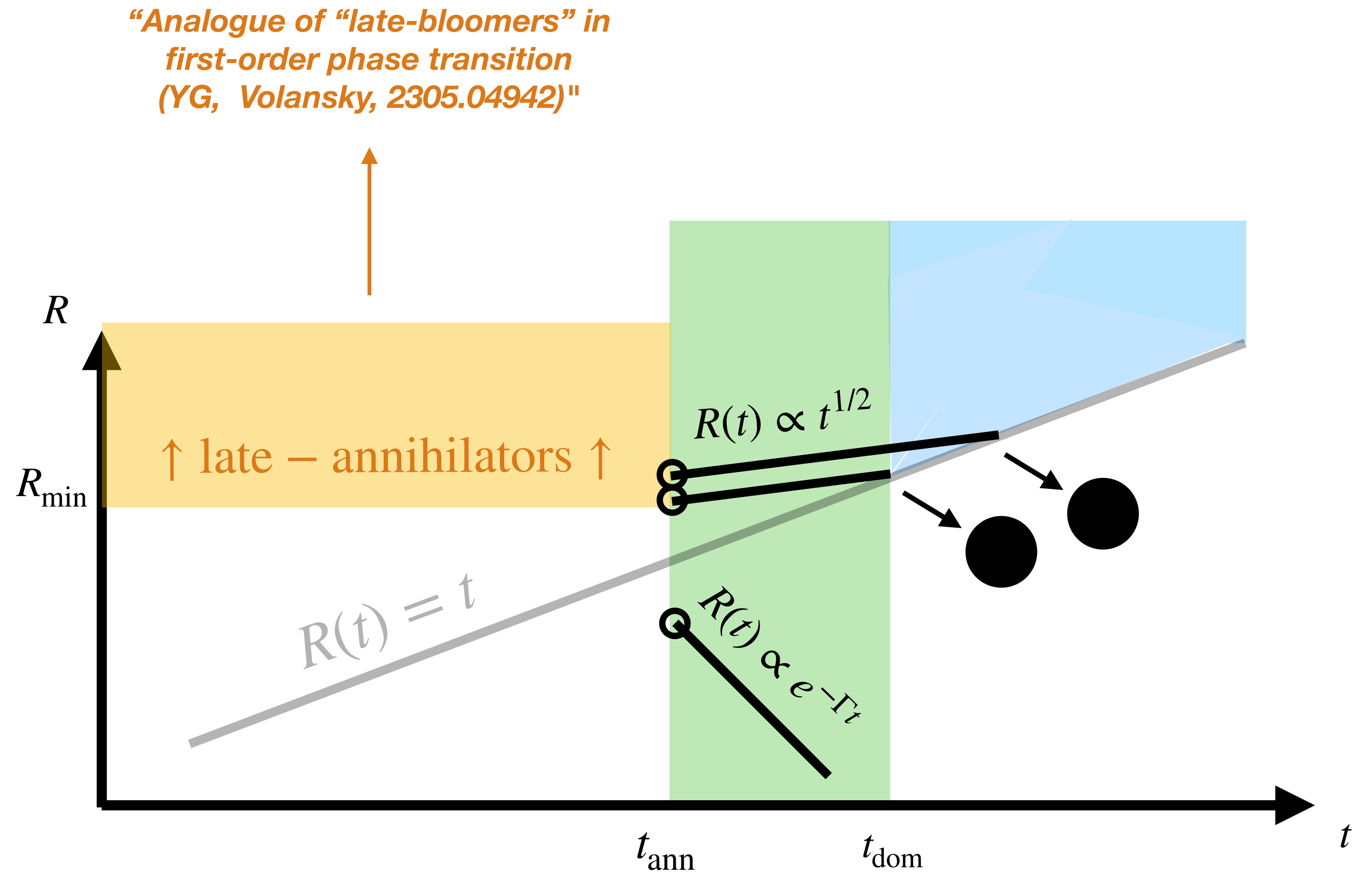
Go back to basics:

$$\ddot{\chi} + (4 - 3a^2\dot{\chi}^2)H\dot{\chi} + \frac{2}{a^2\chi}(1 - a^2\dot{\chi}^2) = - \left(\frac{V_{\text{bias}}}{\sigma} + 6\pi\sigma \right) \frac{(1 - a^2\dot{\chi}^2)^{3/2}}{a}$$

$$R(t) = a(t)\chi(t)$$

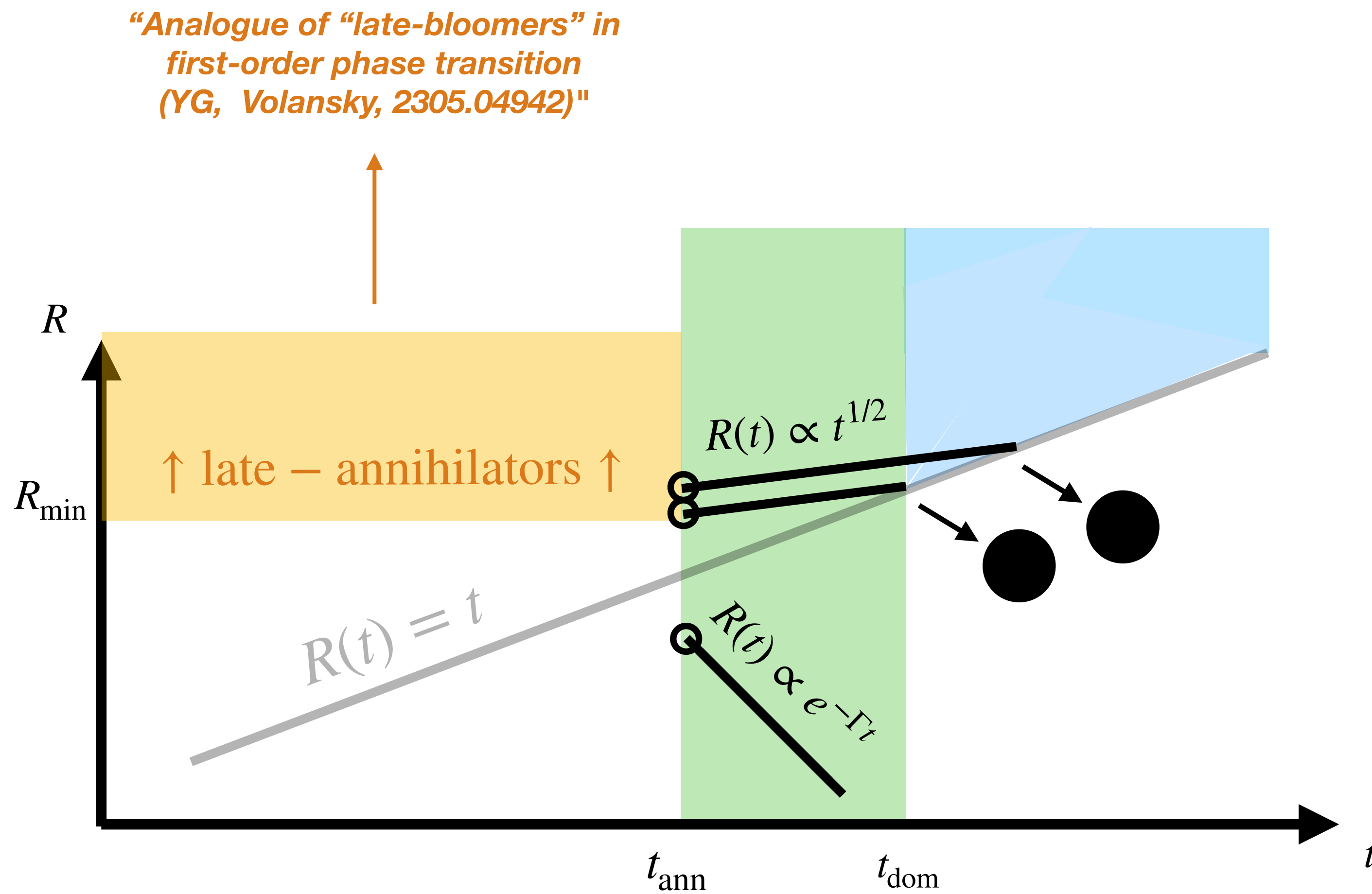
Result:

$$R(t) \propto \begin{cases} a(t), & \text{if } R > t, \\ e^{-\Gamma t}, & \text{if } R < t. \end{cases}$$



PBH abundance:

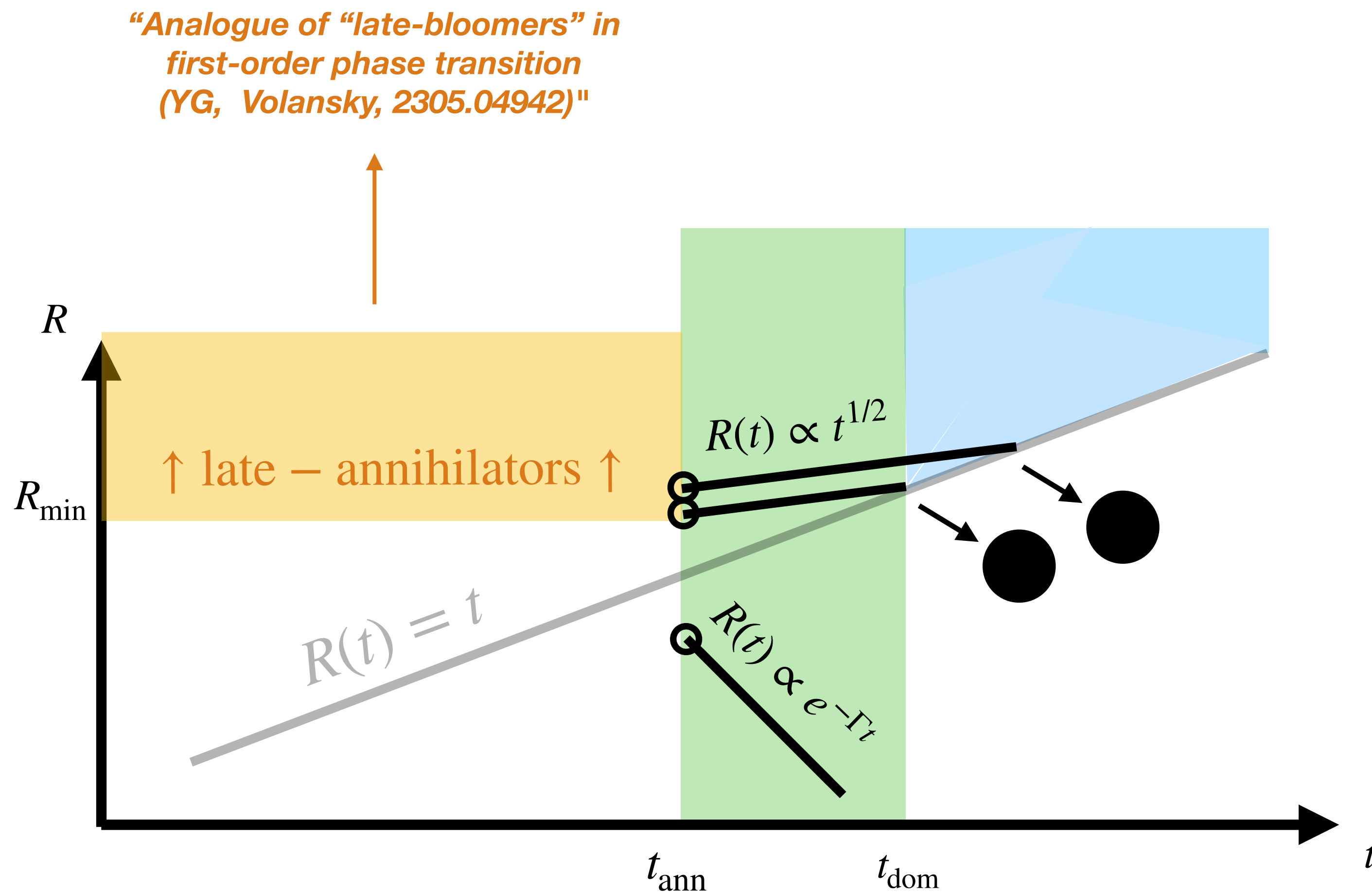
$$f_{\text{PBH}} \simeq \mathcal{F} \times \left(\frac{T_{\text{dom}}}{T_{\text{eq}}} \right)$$



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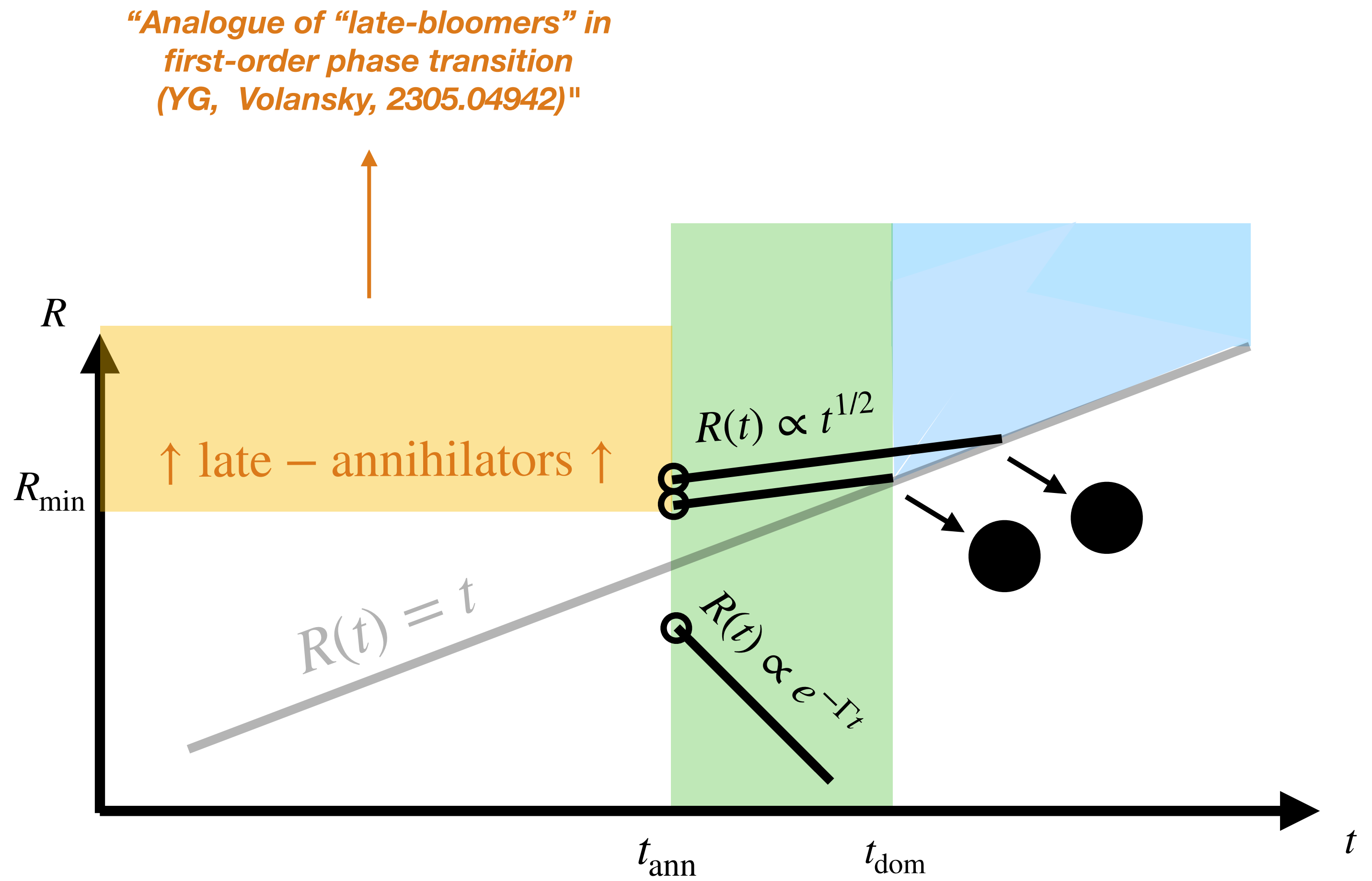


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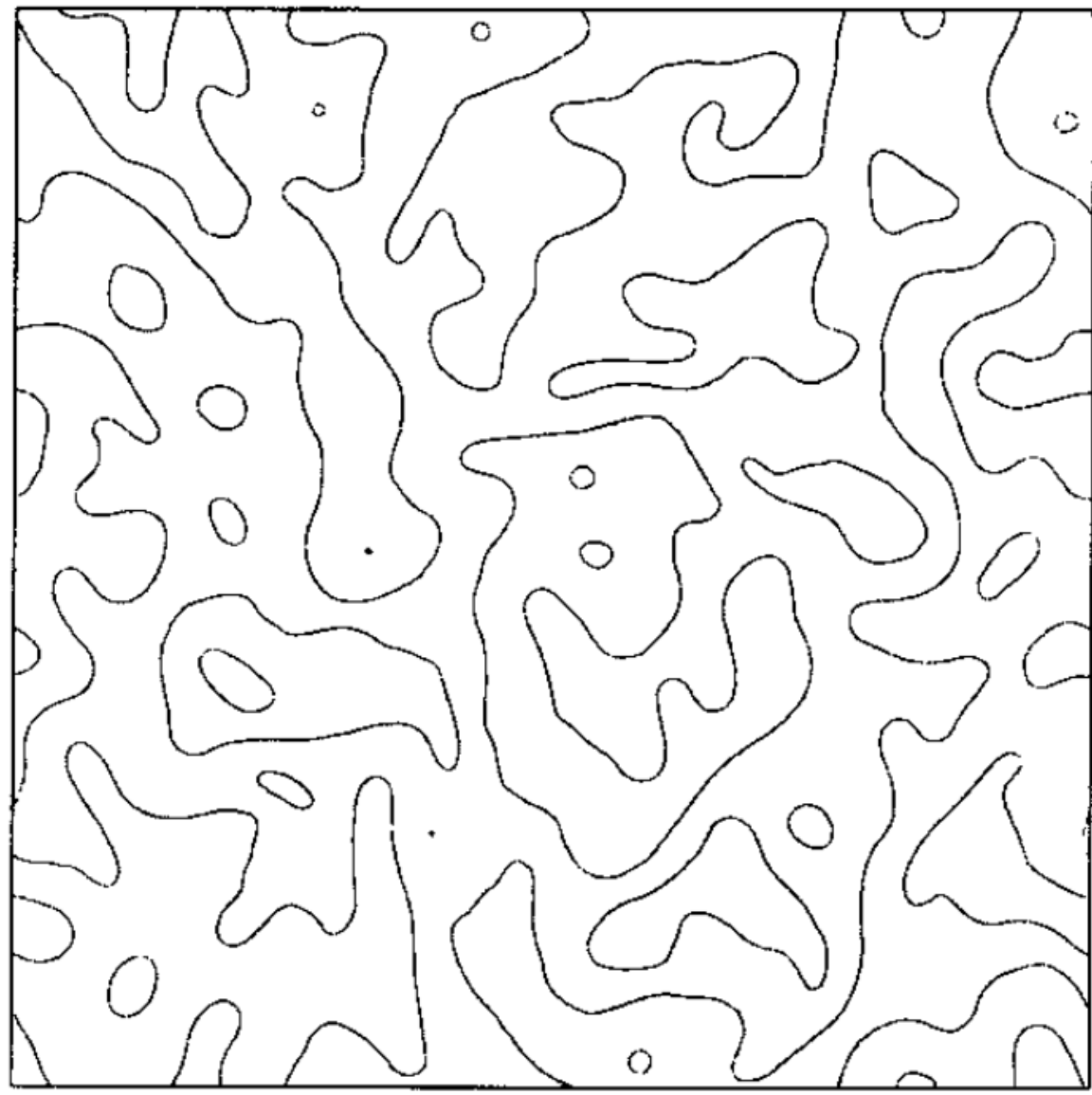
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↑ Late-annihilators fraction

Redshift factor

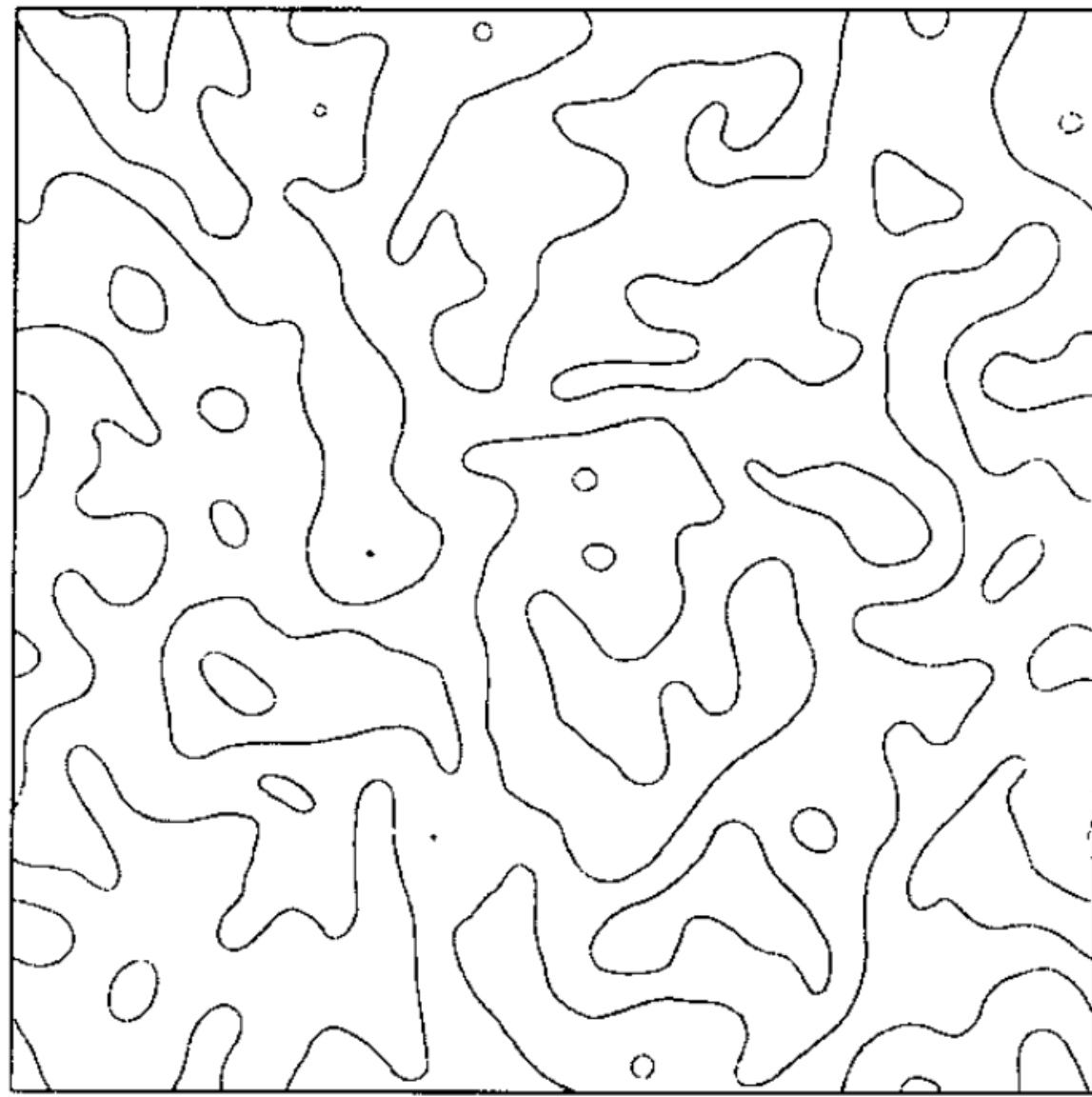


Abundance of late-annihilators \mathcal{F}



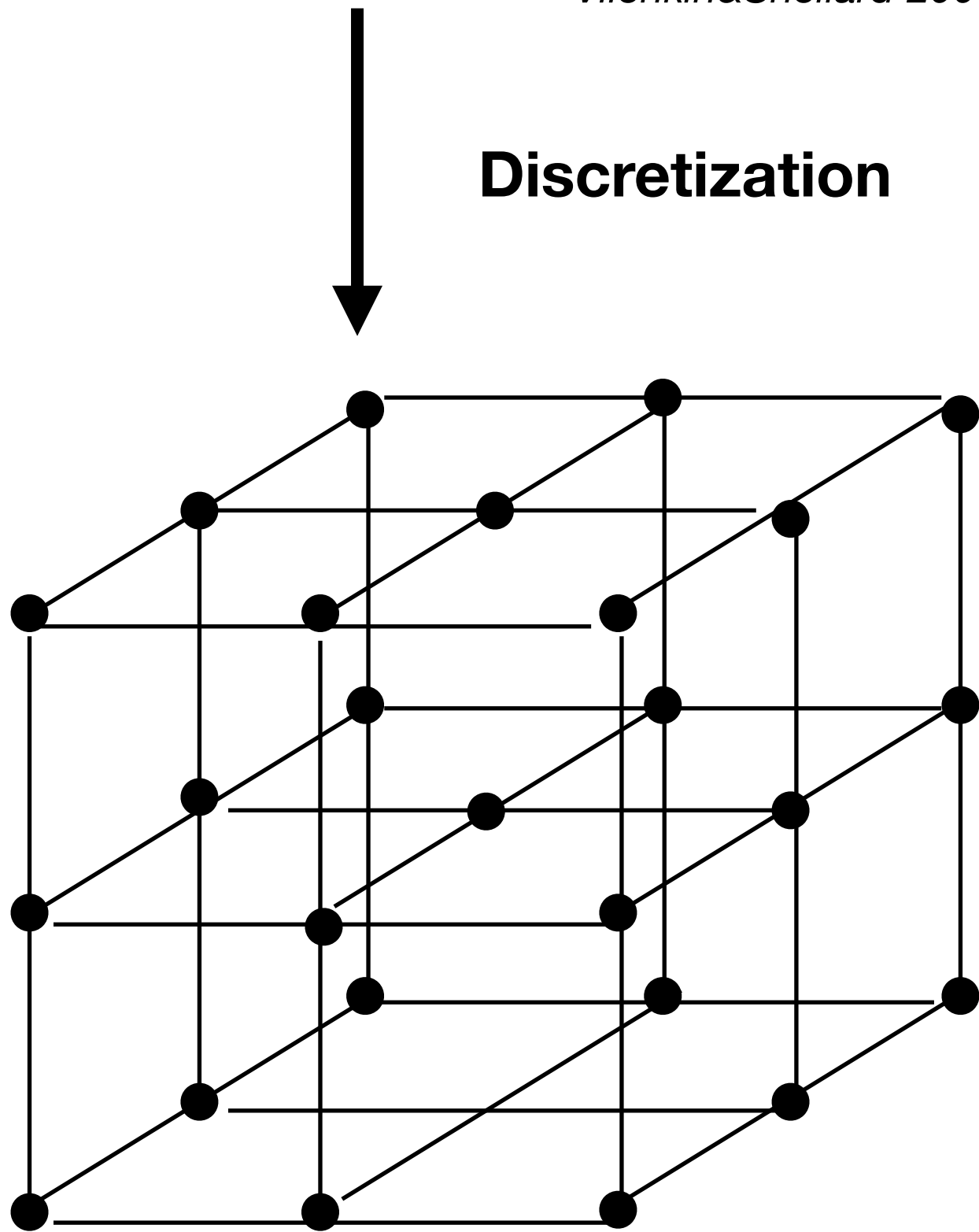
Vilenkin&Shellard 2000

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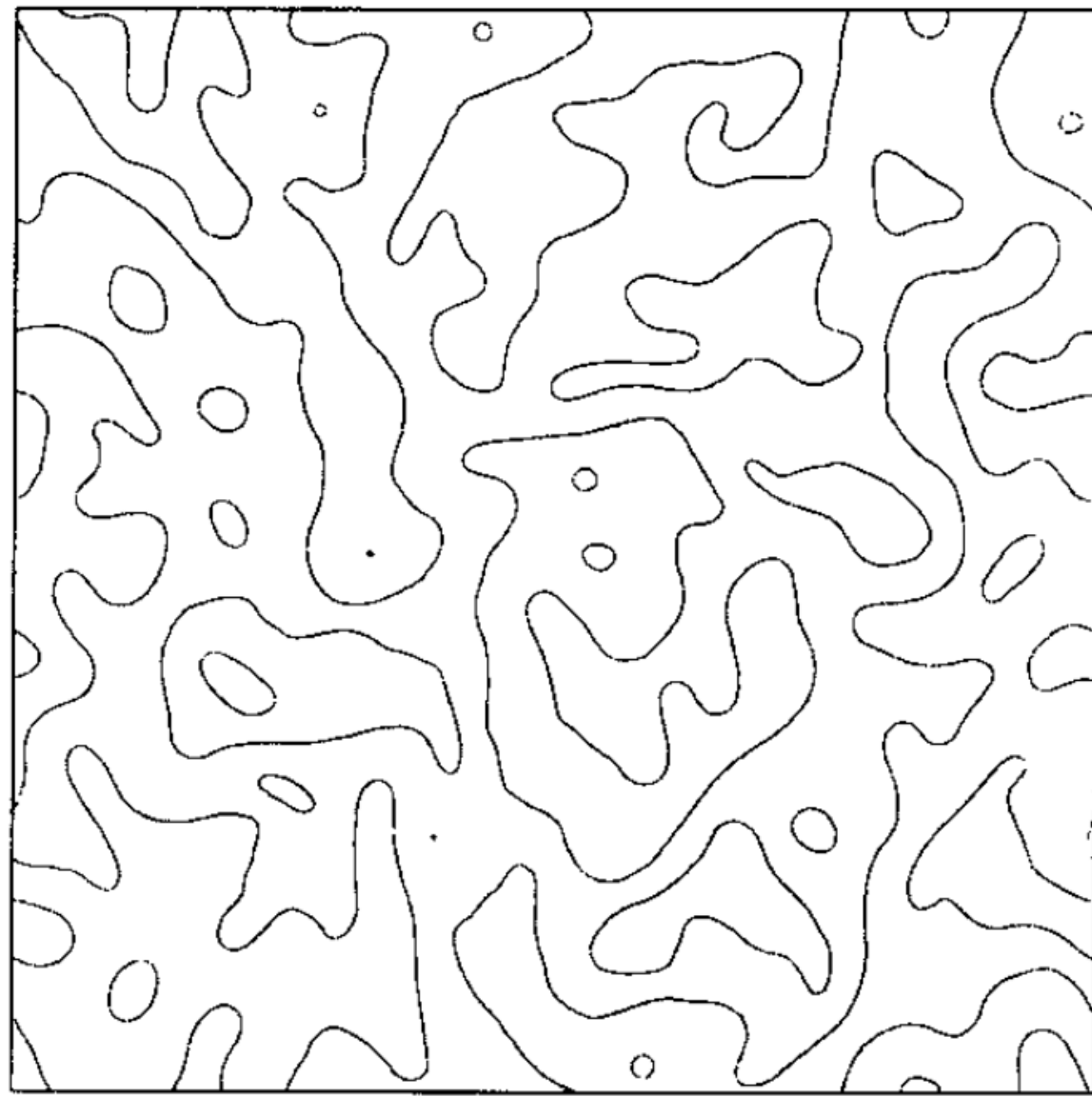
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Discretization



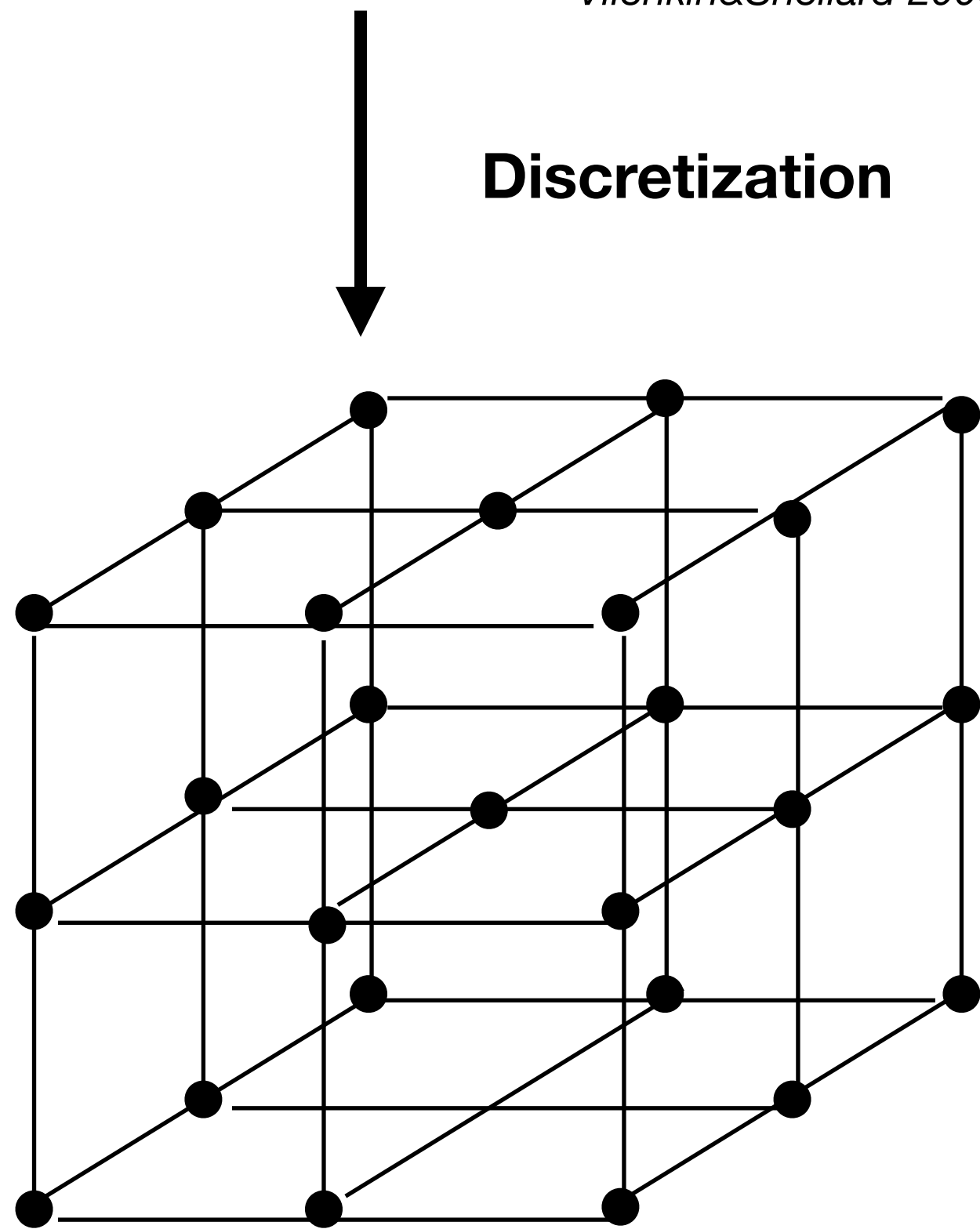
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Percolation theory on a lattice:



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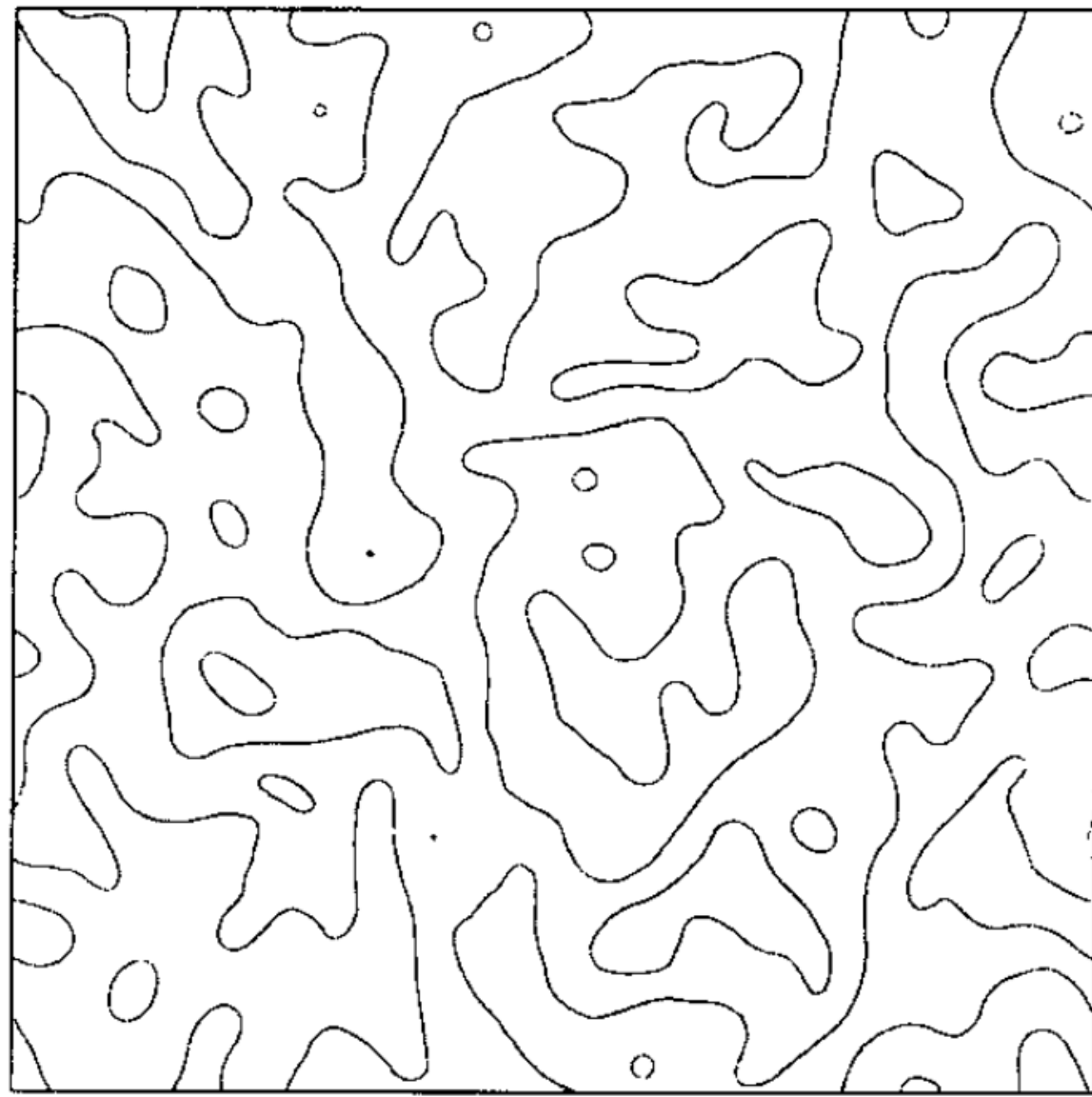
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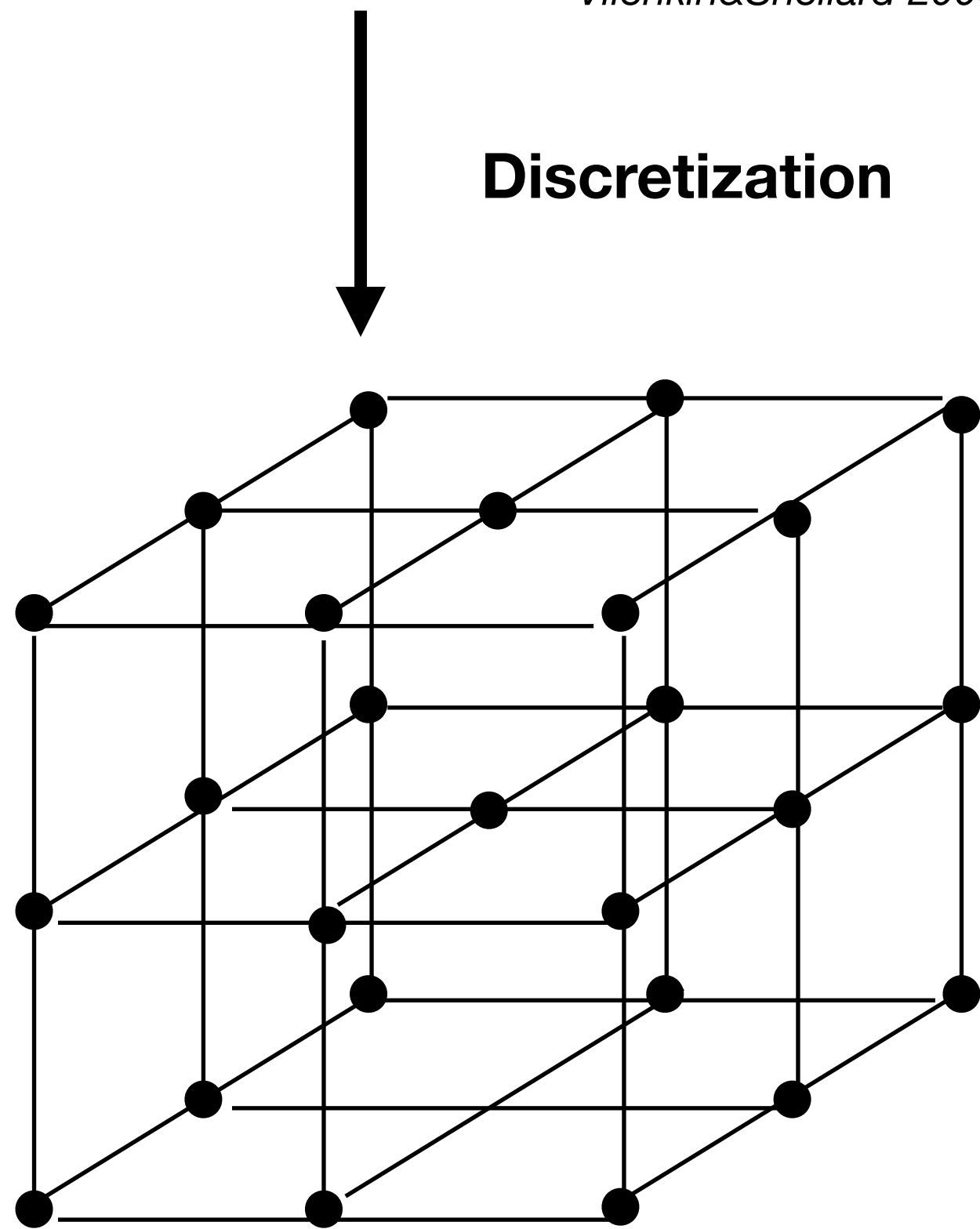
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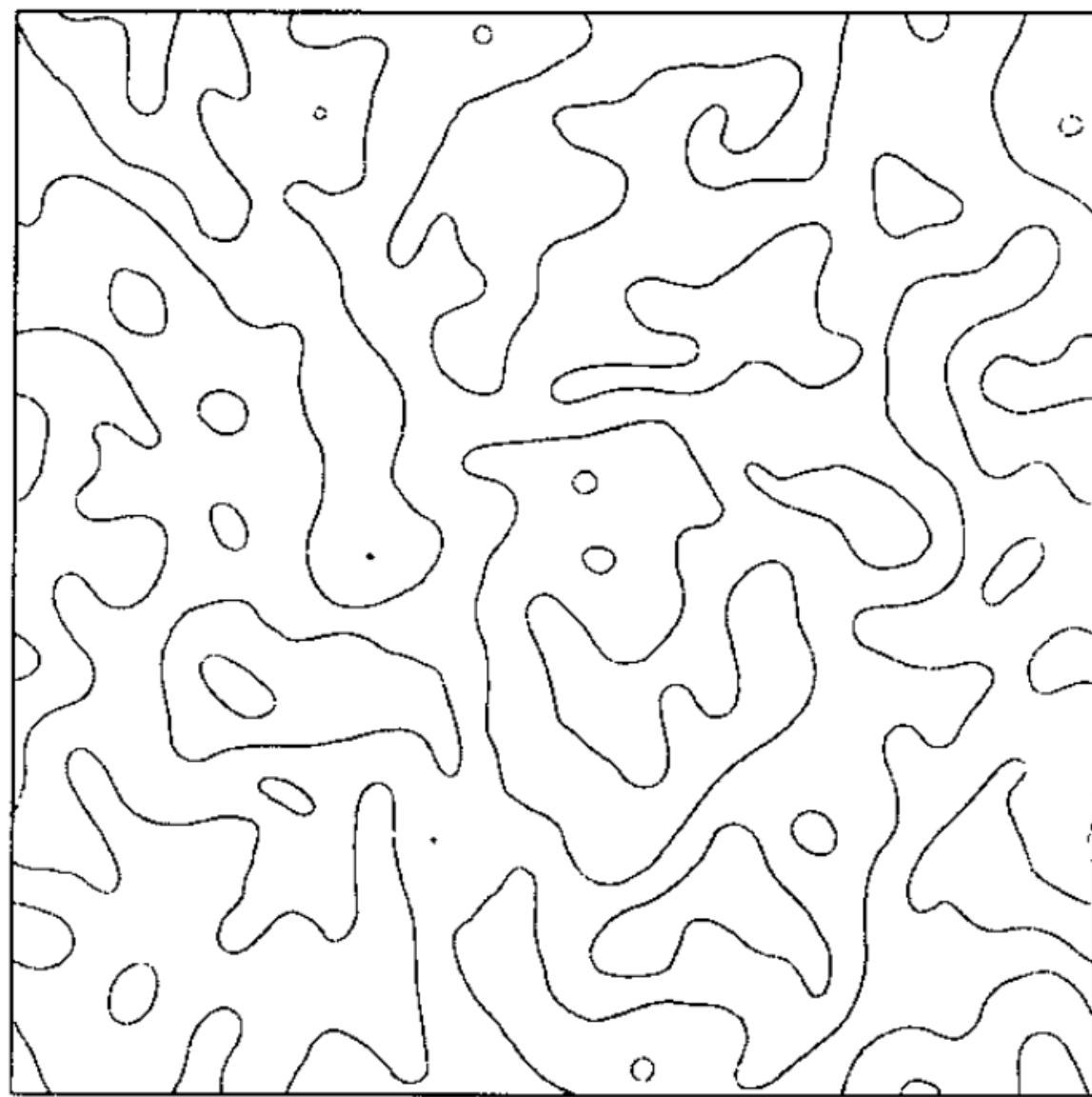


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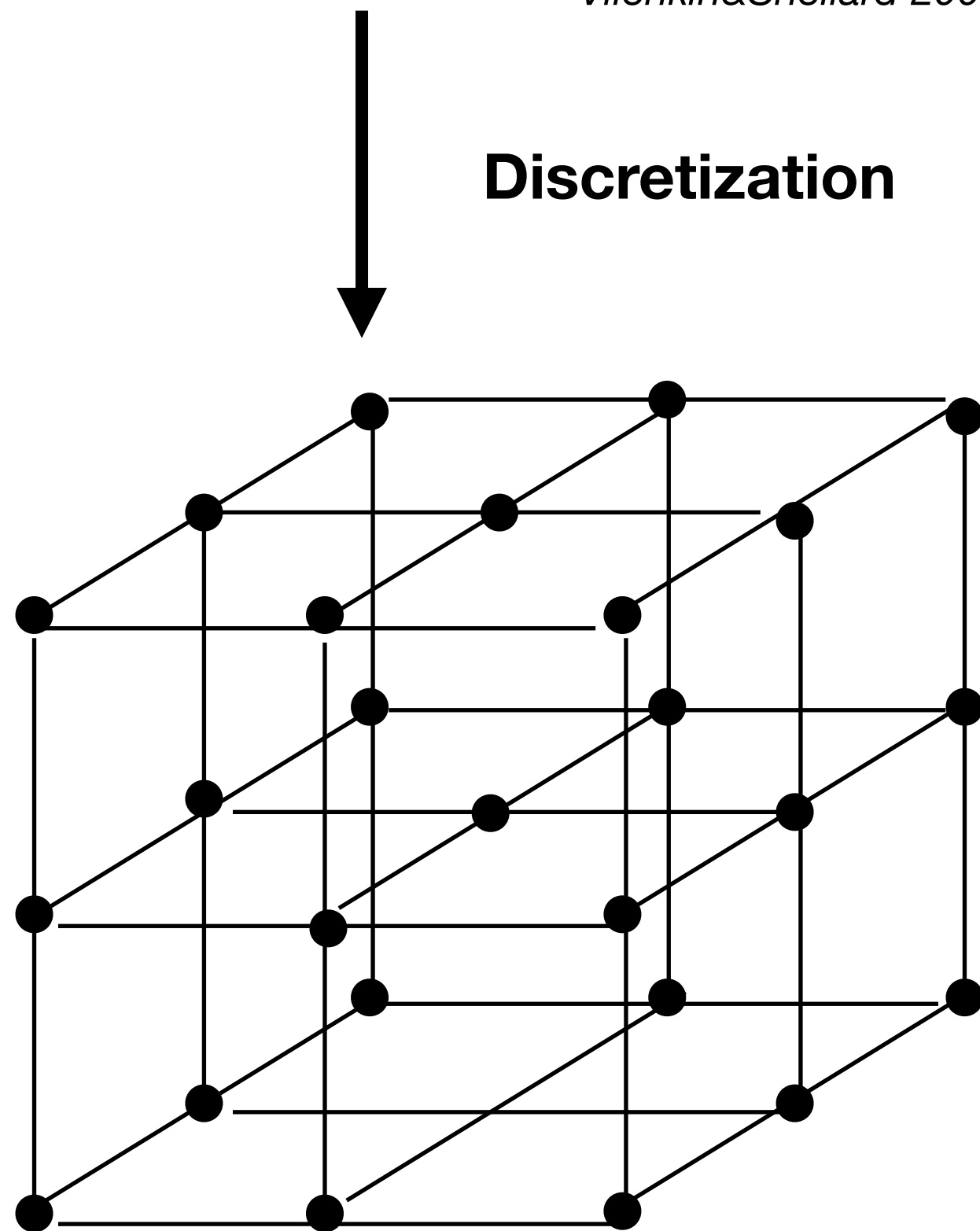
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Vilenkin&Shellard 2000

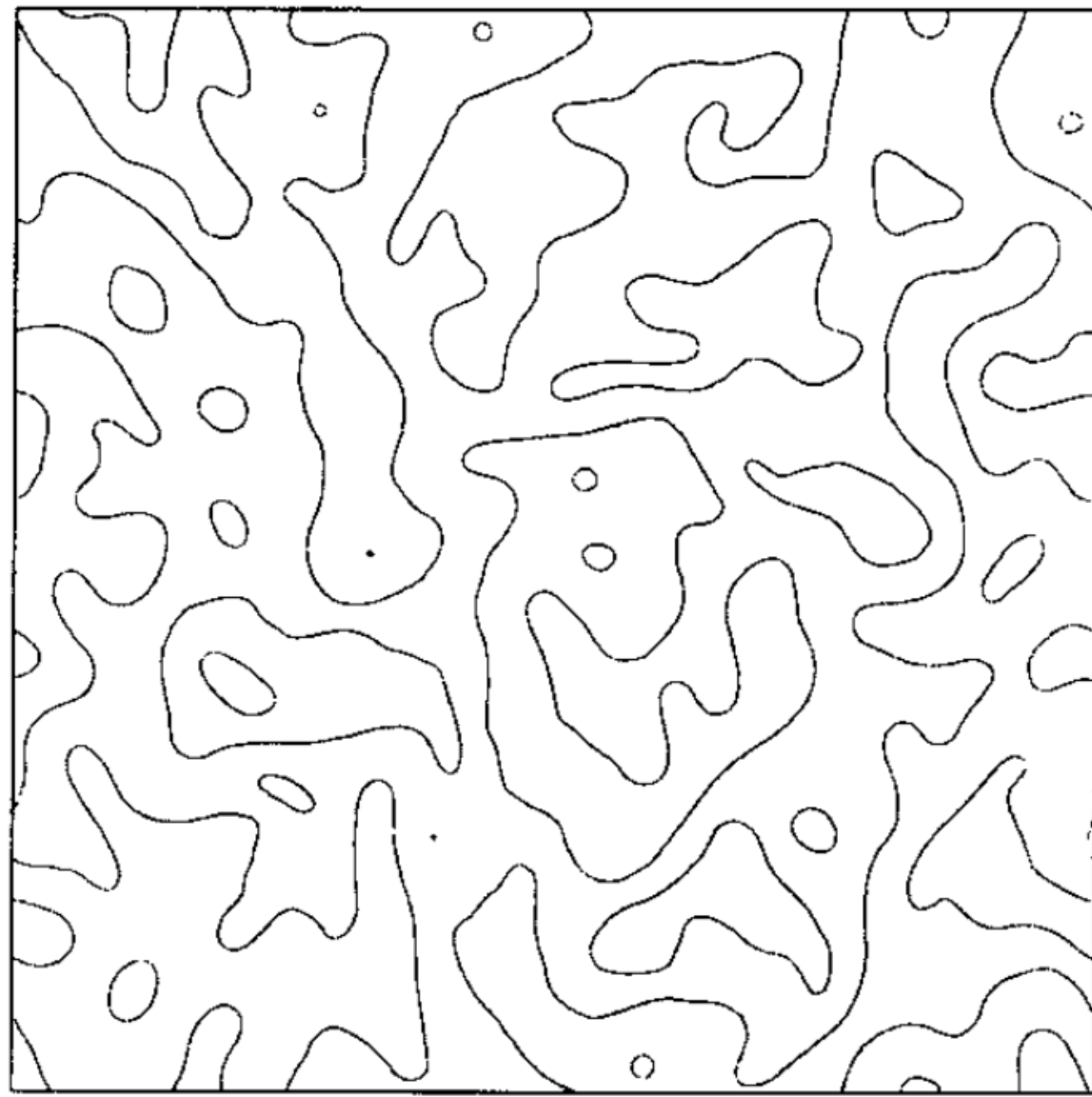
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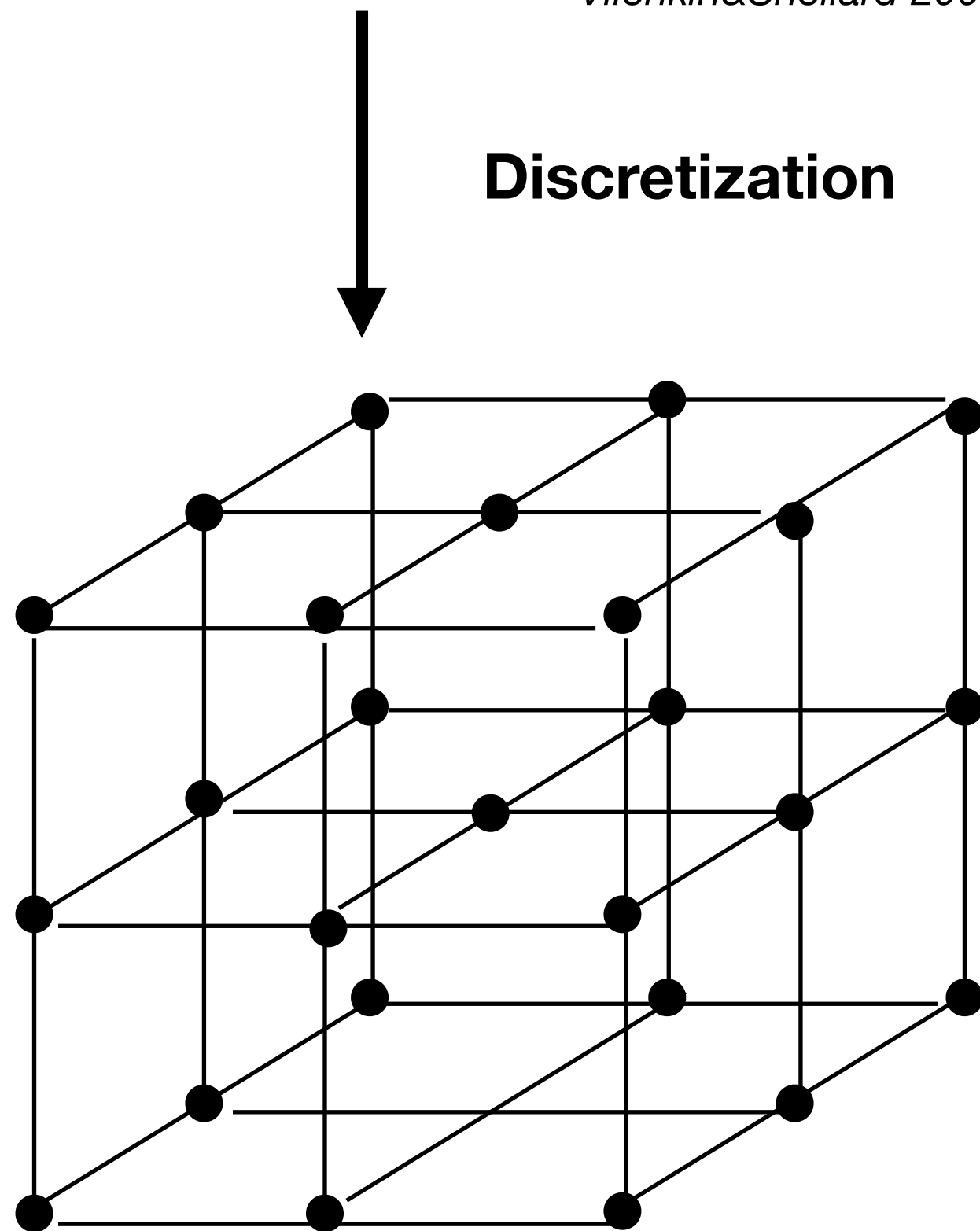
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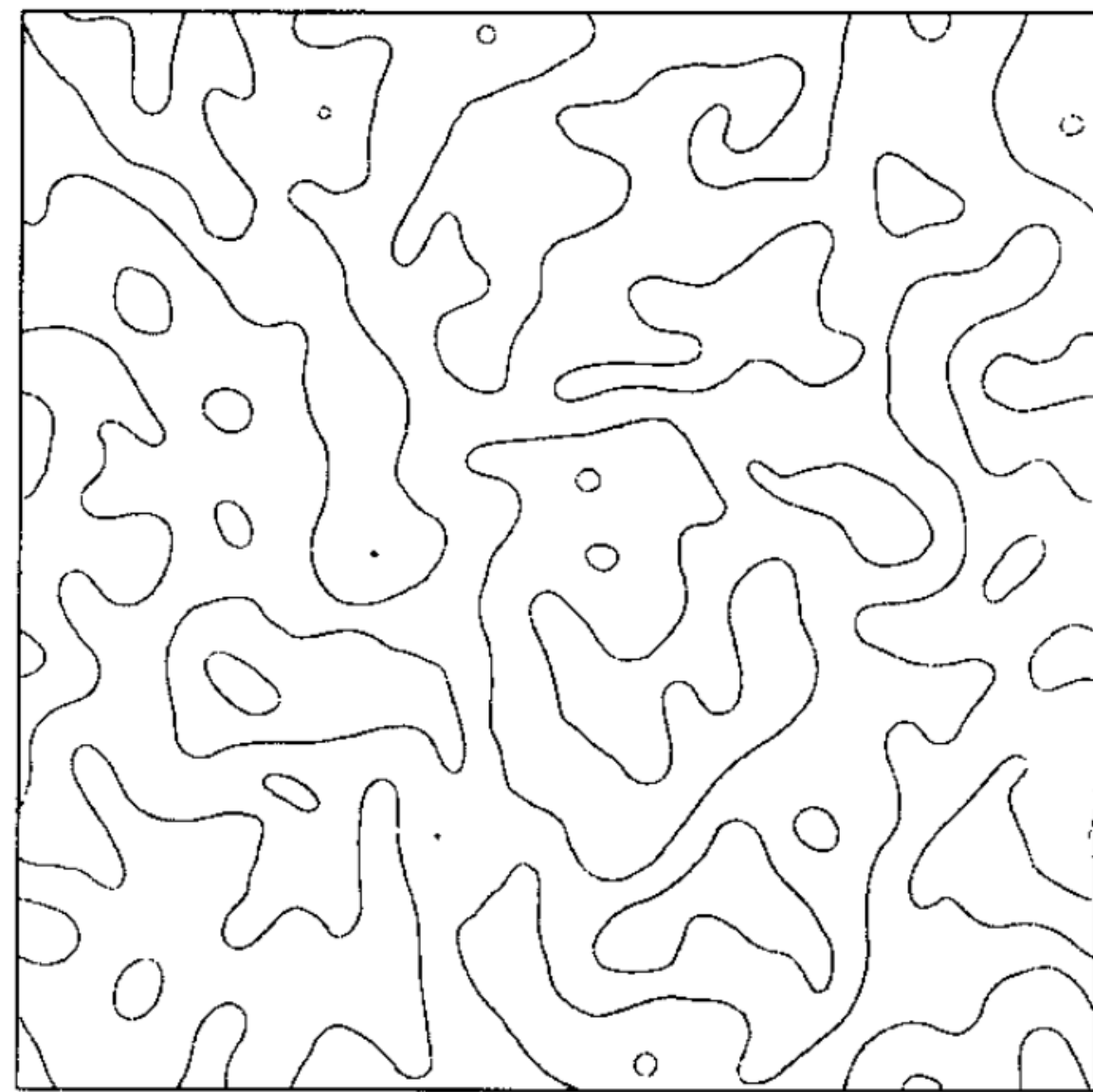


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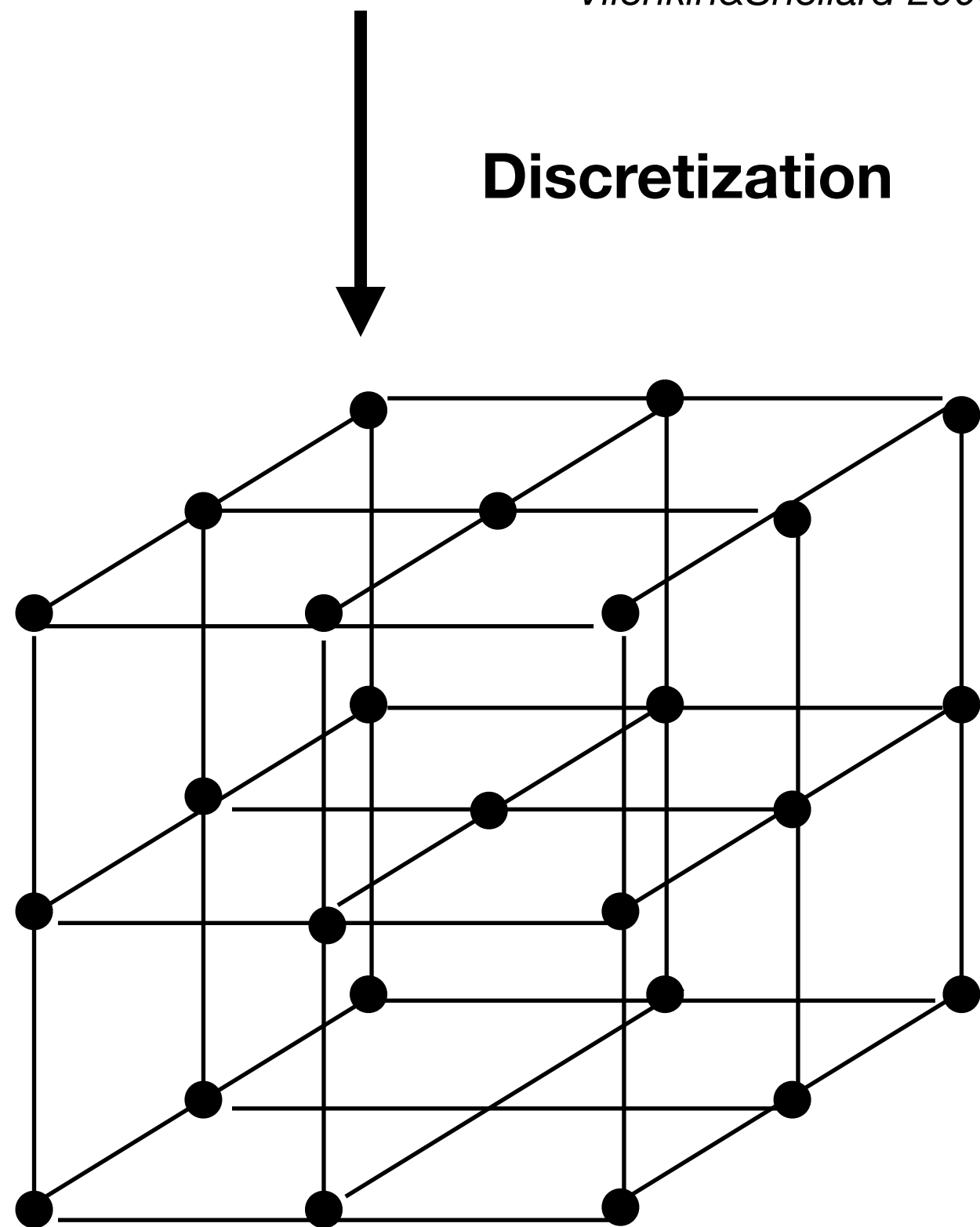
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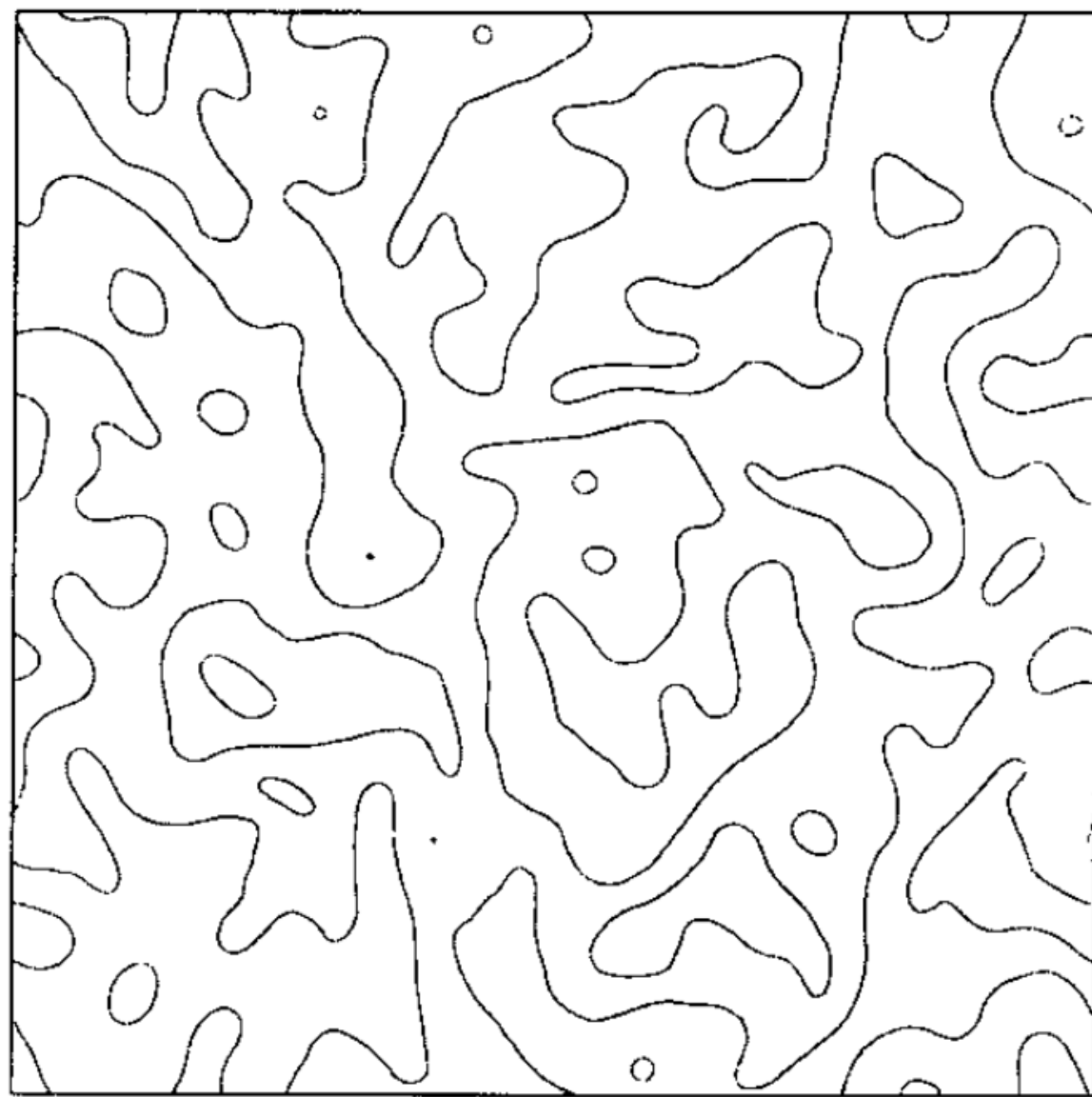
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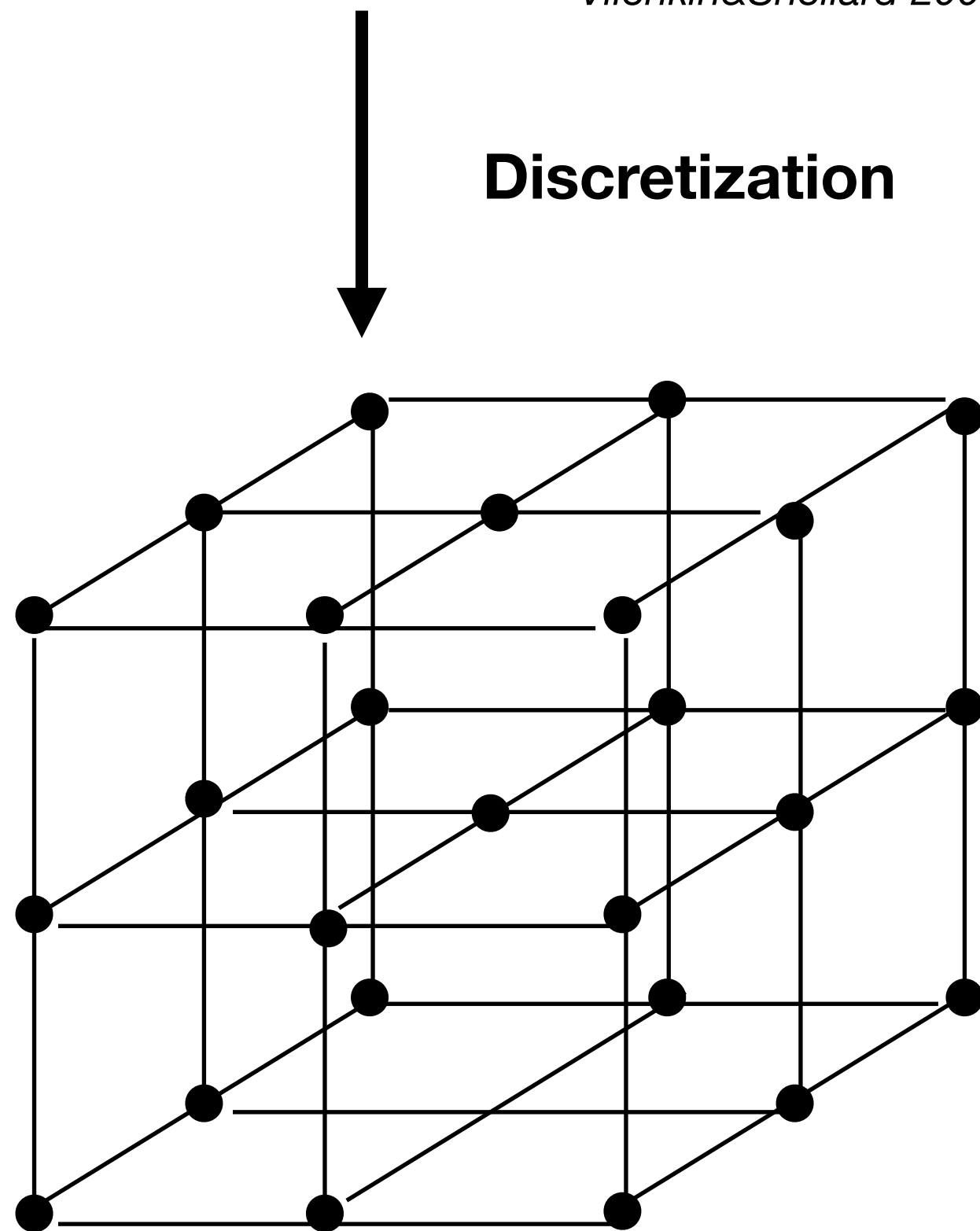
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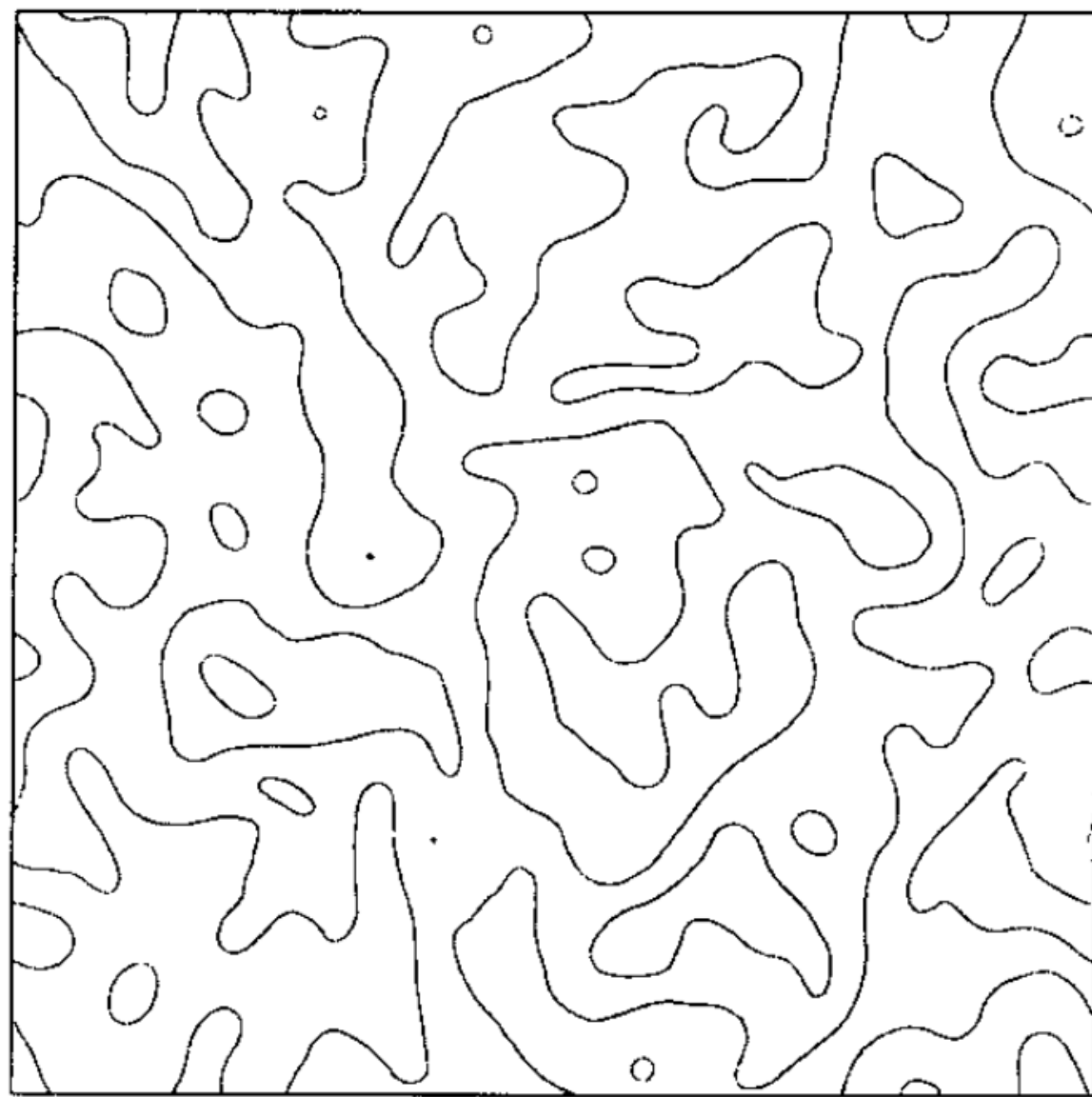
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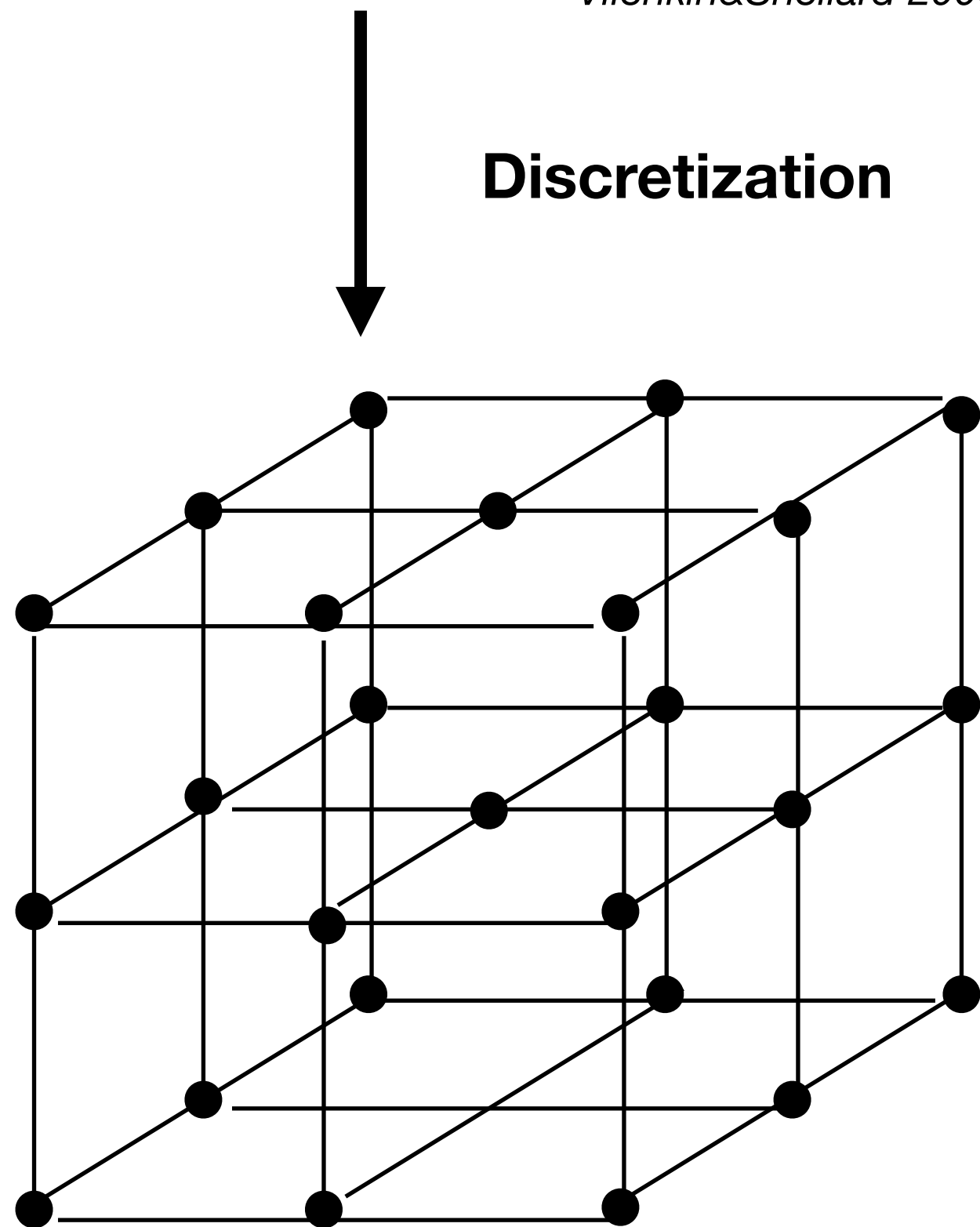
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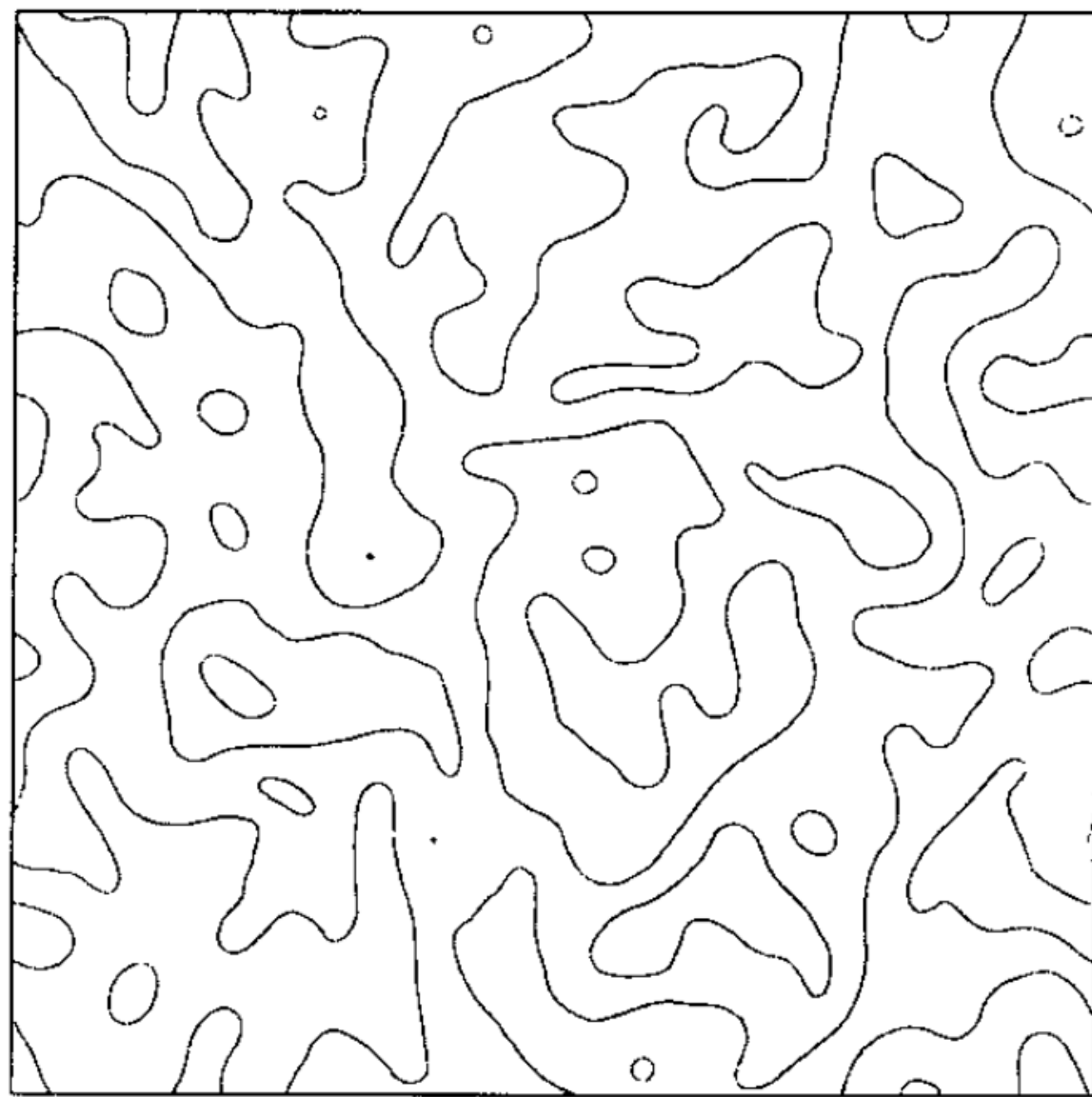
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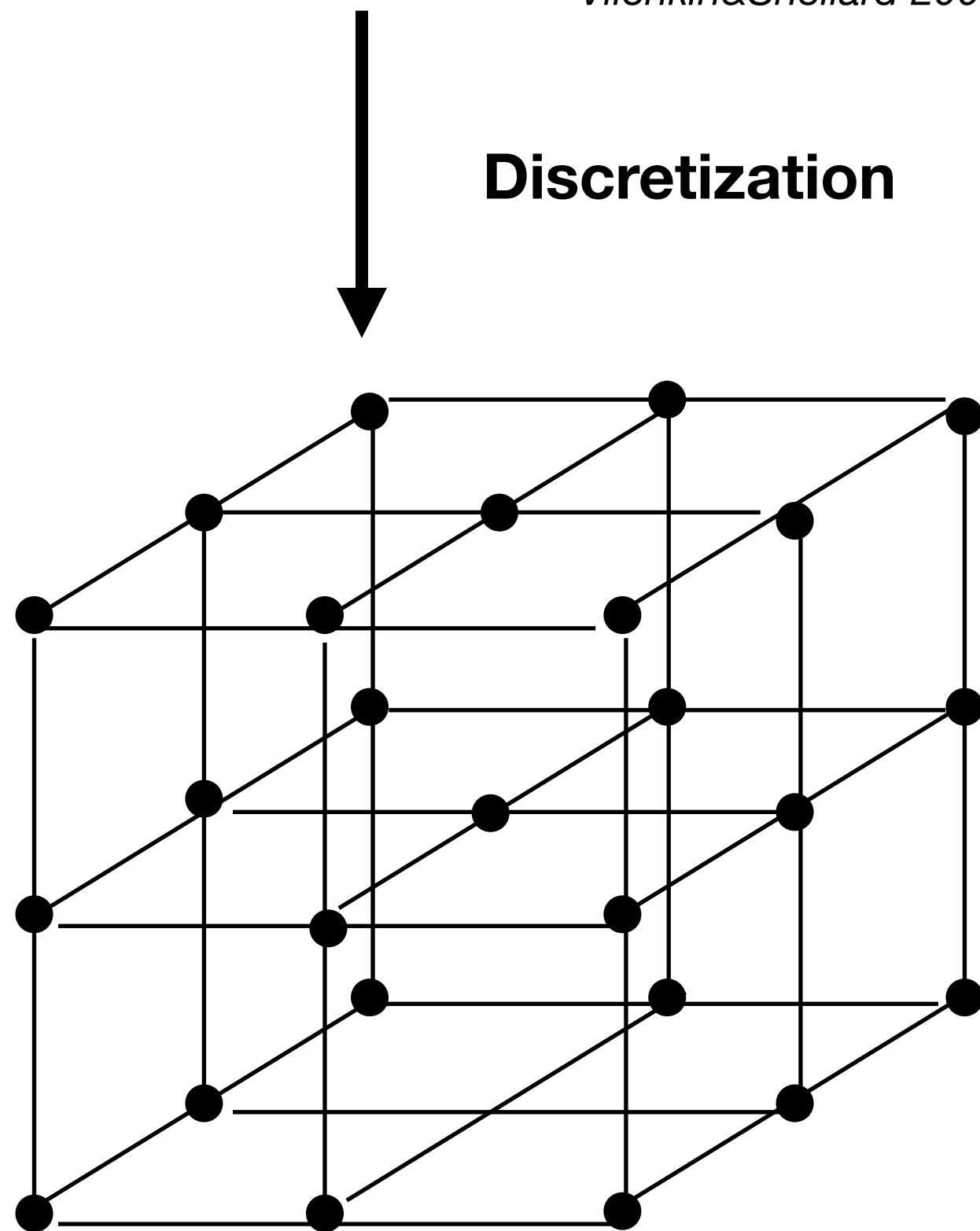
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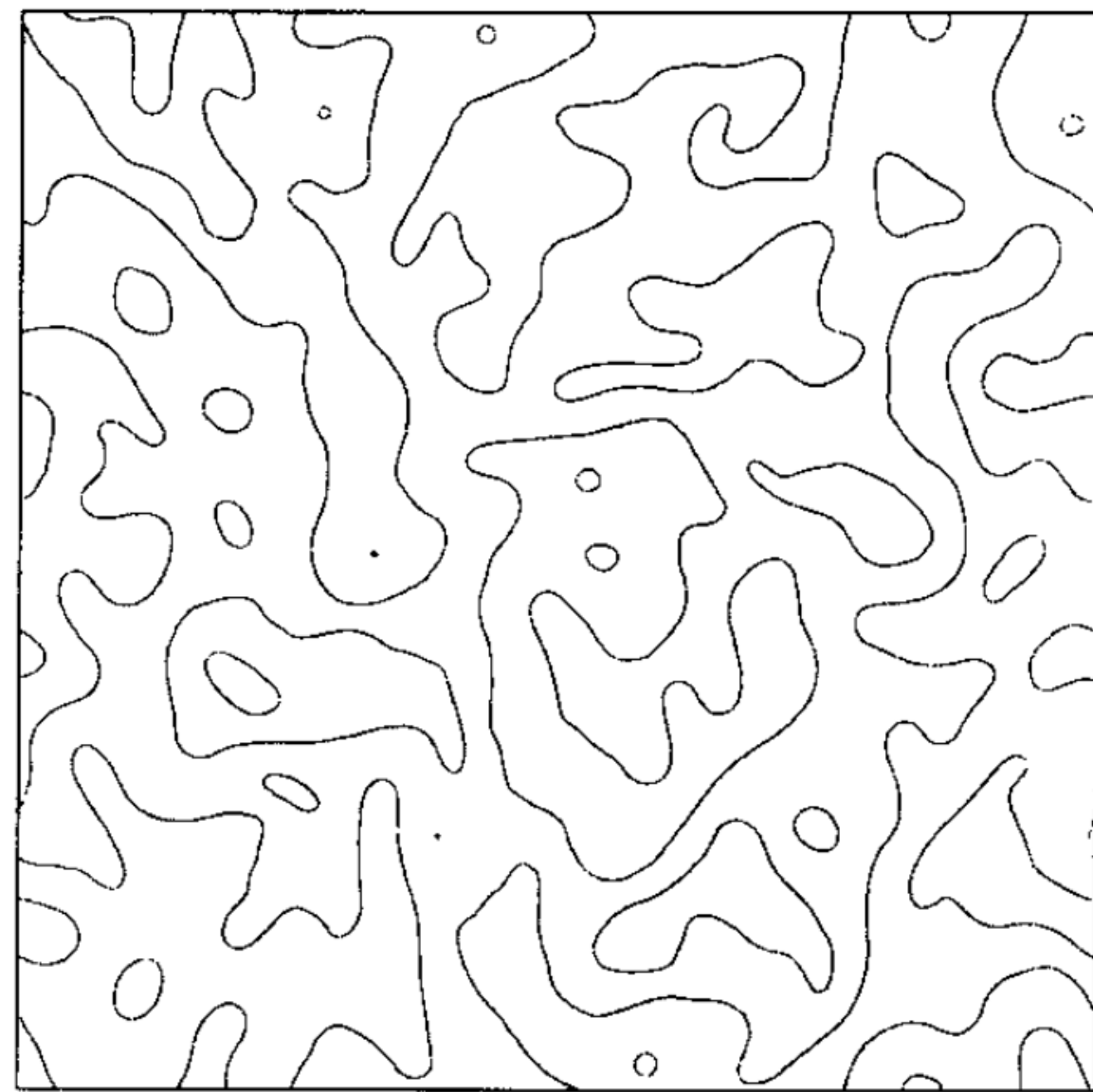
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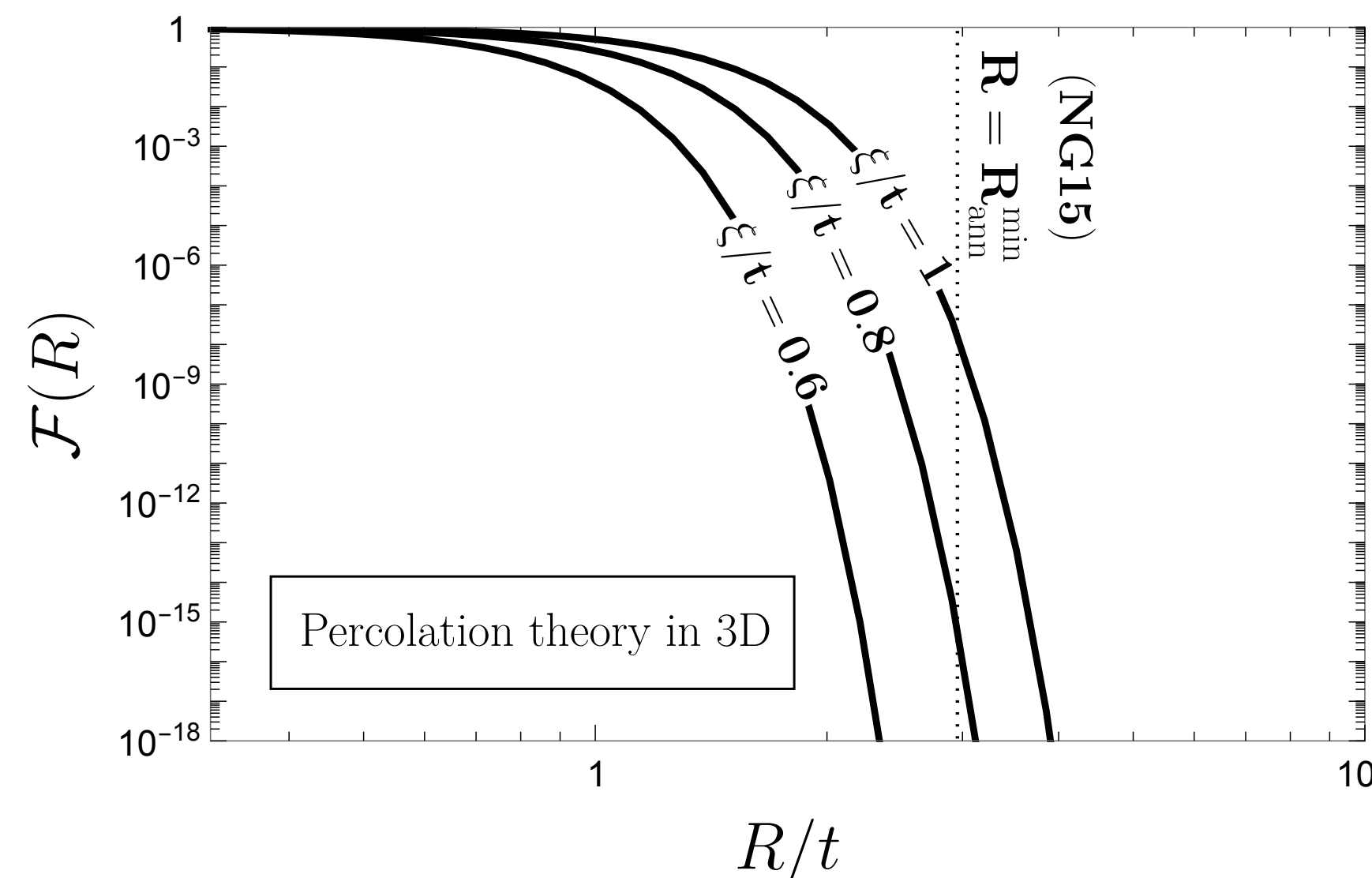
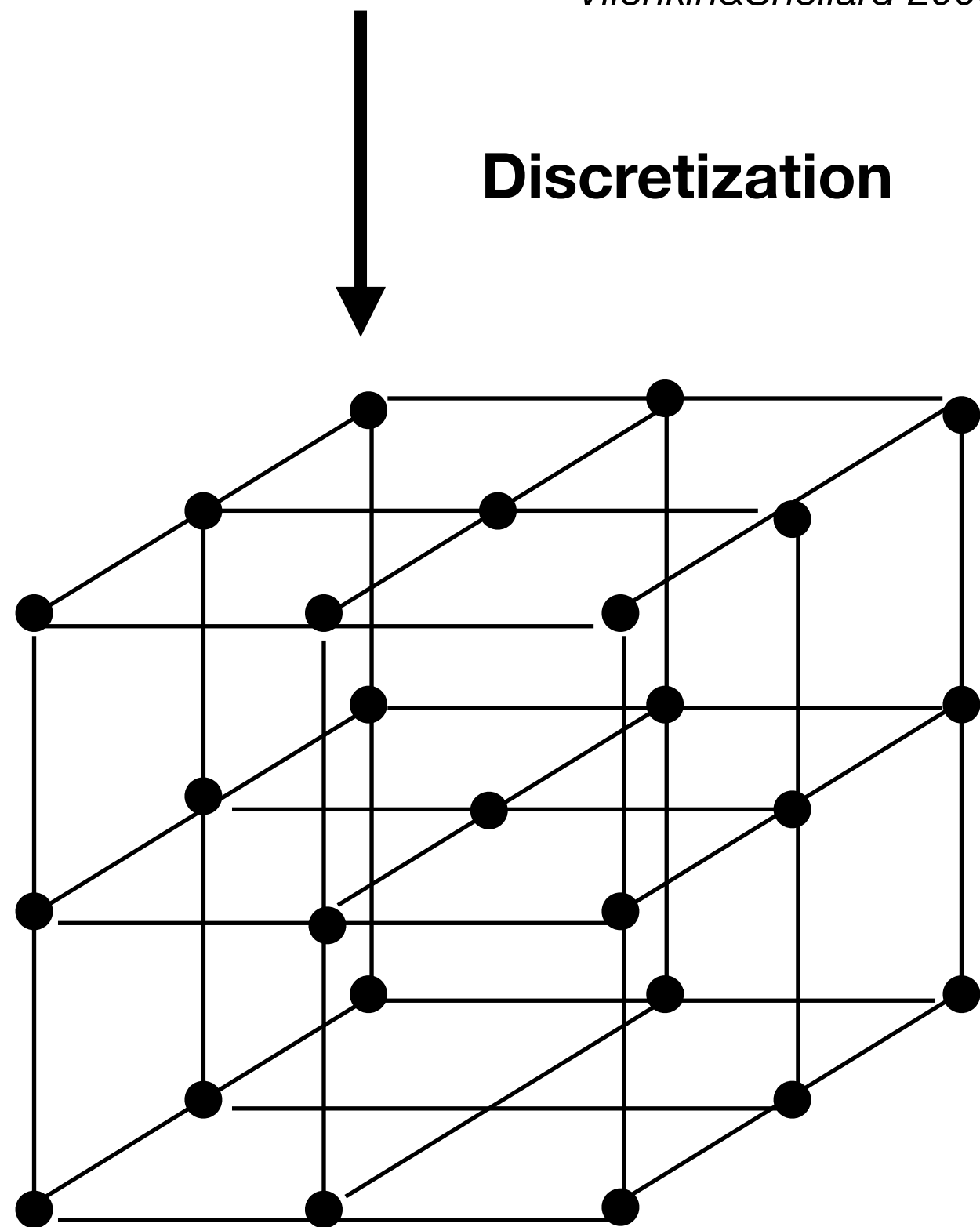
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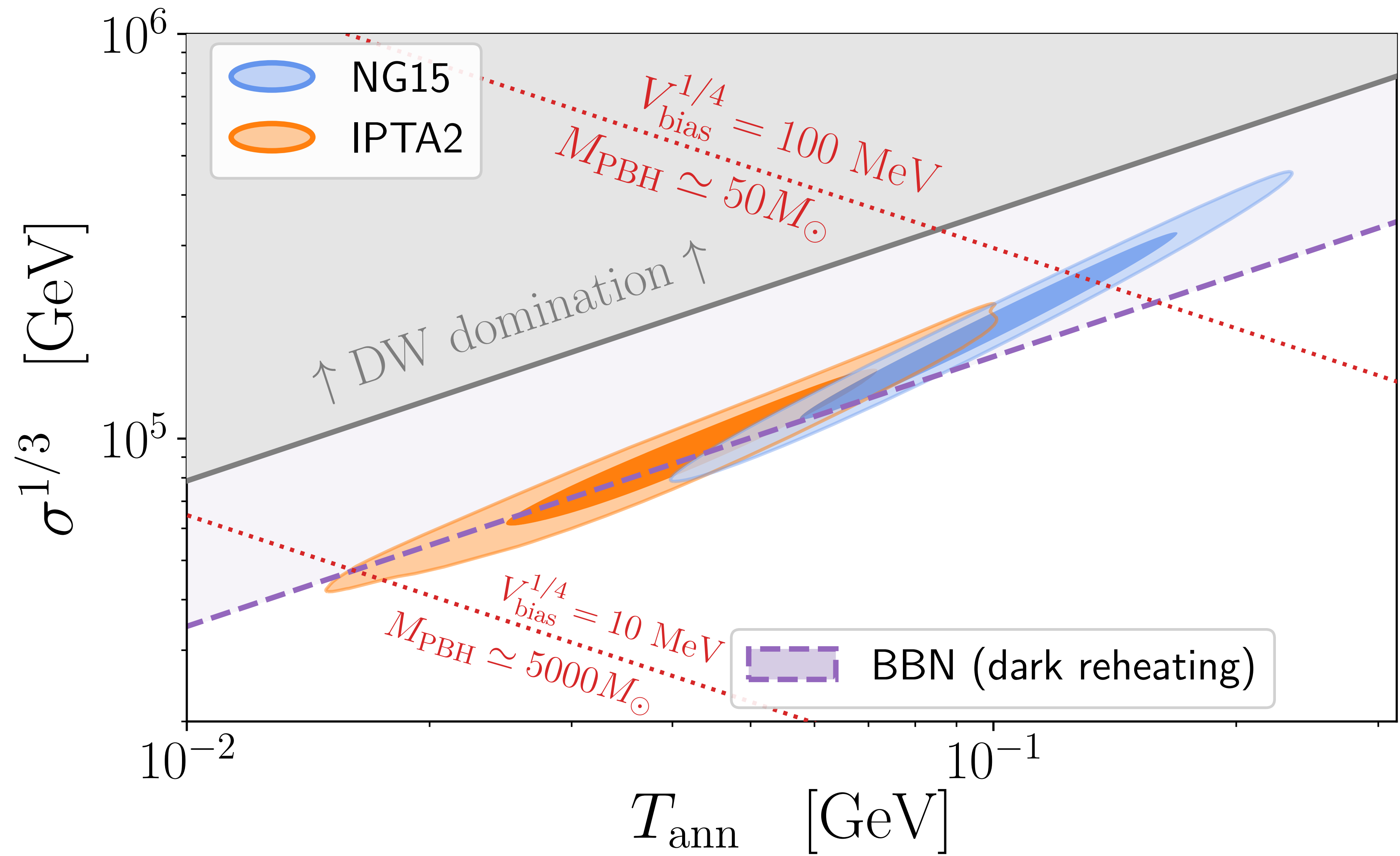
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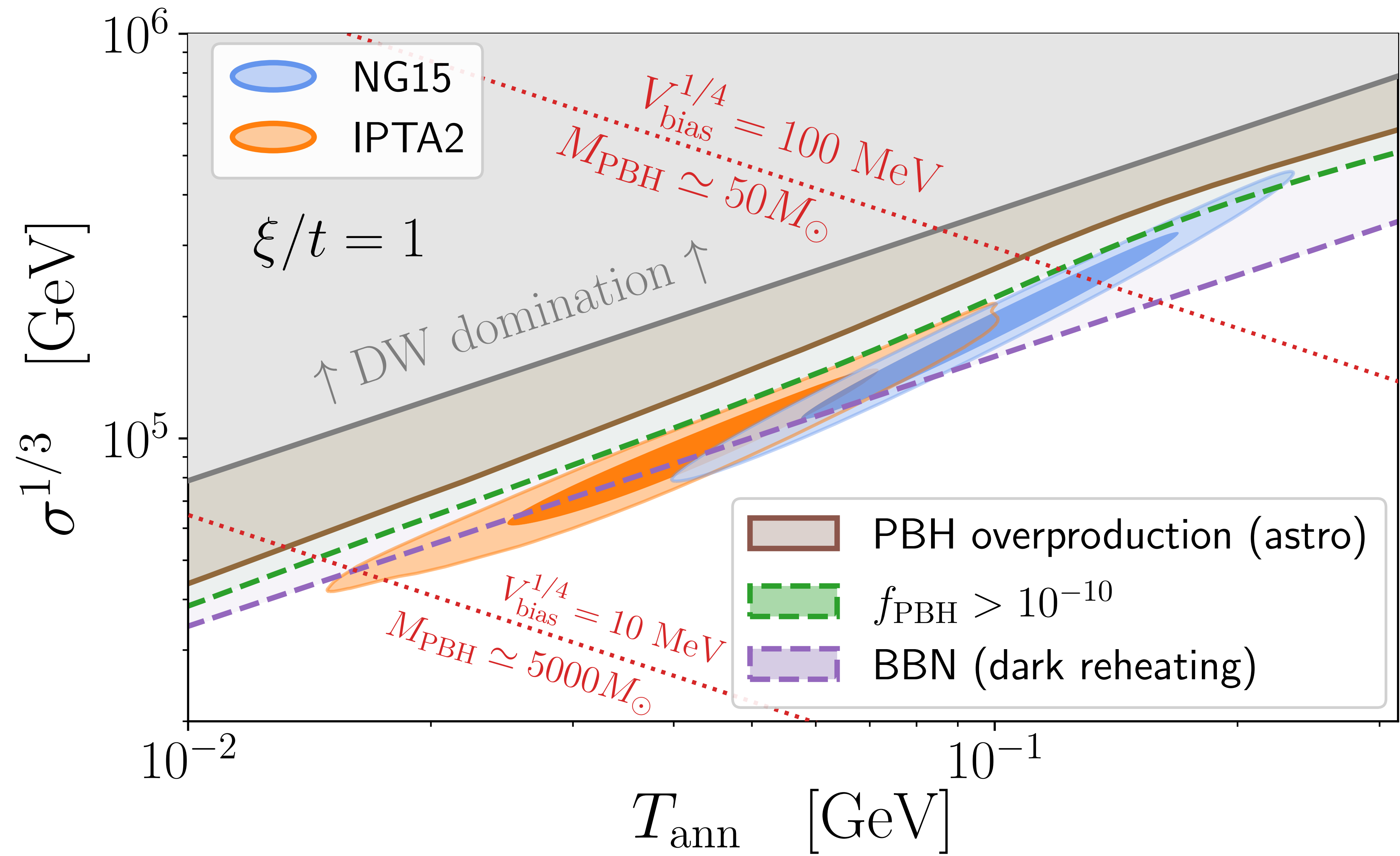


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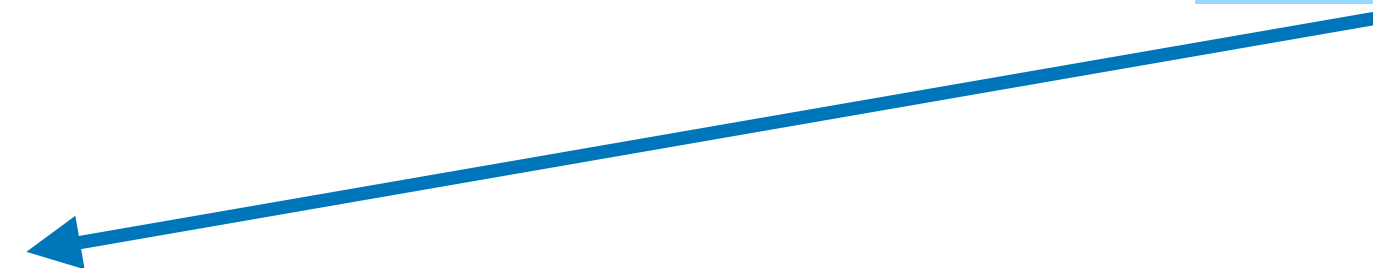
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Outlooks: Many applications beyond PTA

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