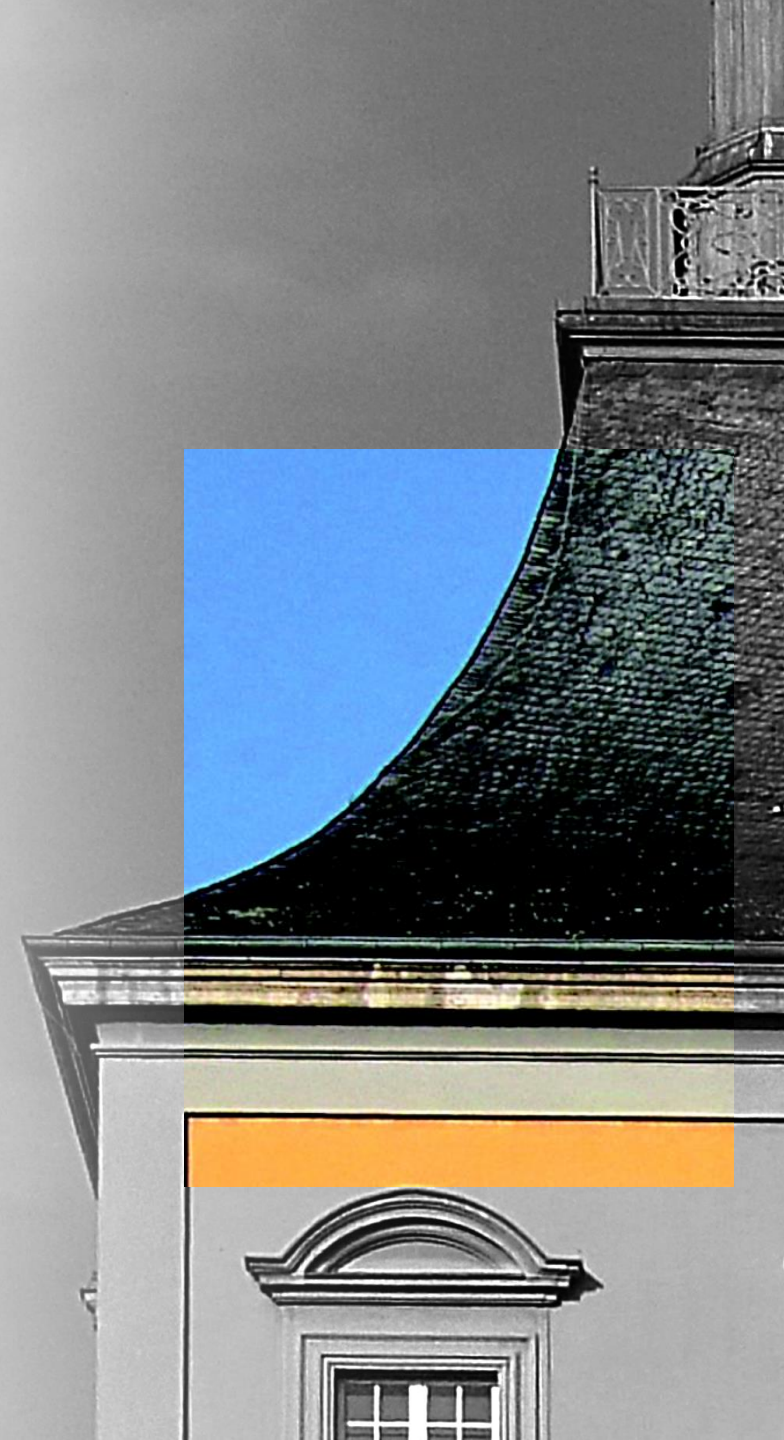


# RAY TRACING FOR BABYIAXO WITH REST

Johanna von Oy

Axion++ workshop

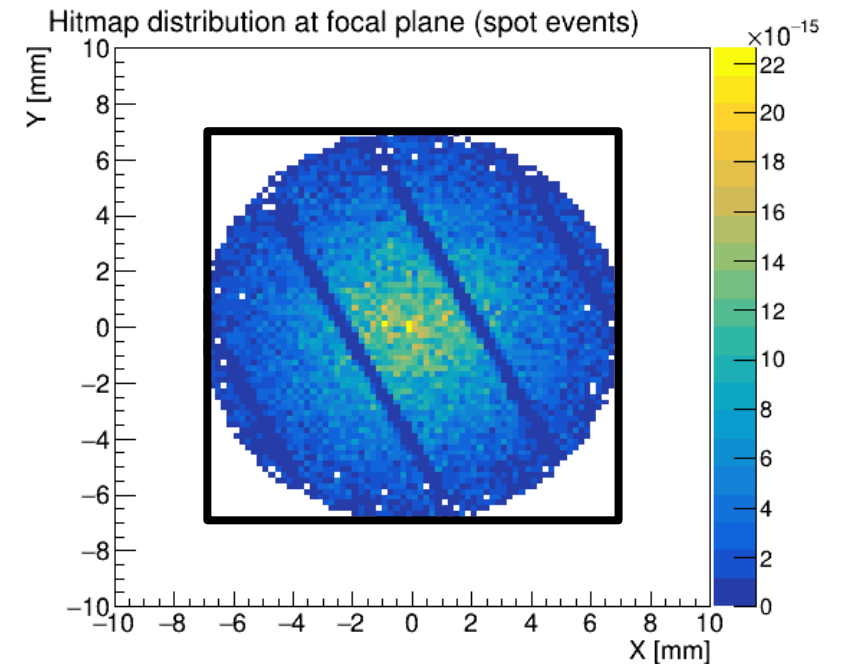
26.09.23



# BABYIAXO AT DESY

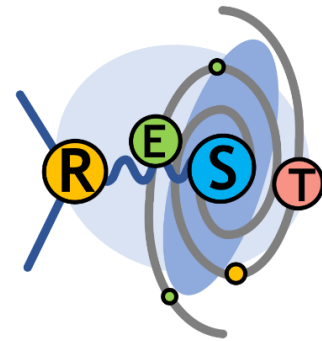


- BabyIAXO will be built at DESY
- Until then: simulations through ray tracing



## MOTIVATION RAY TRACER AND REST

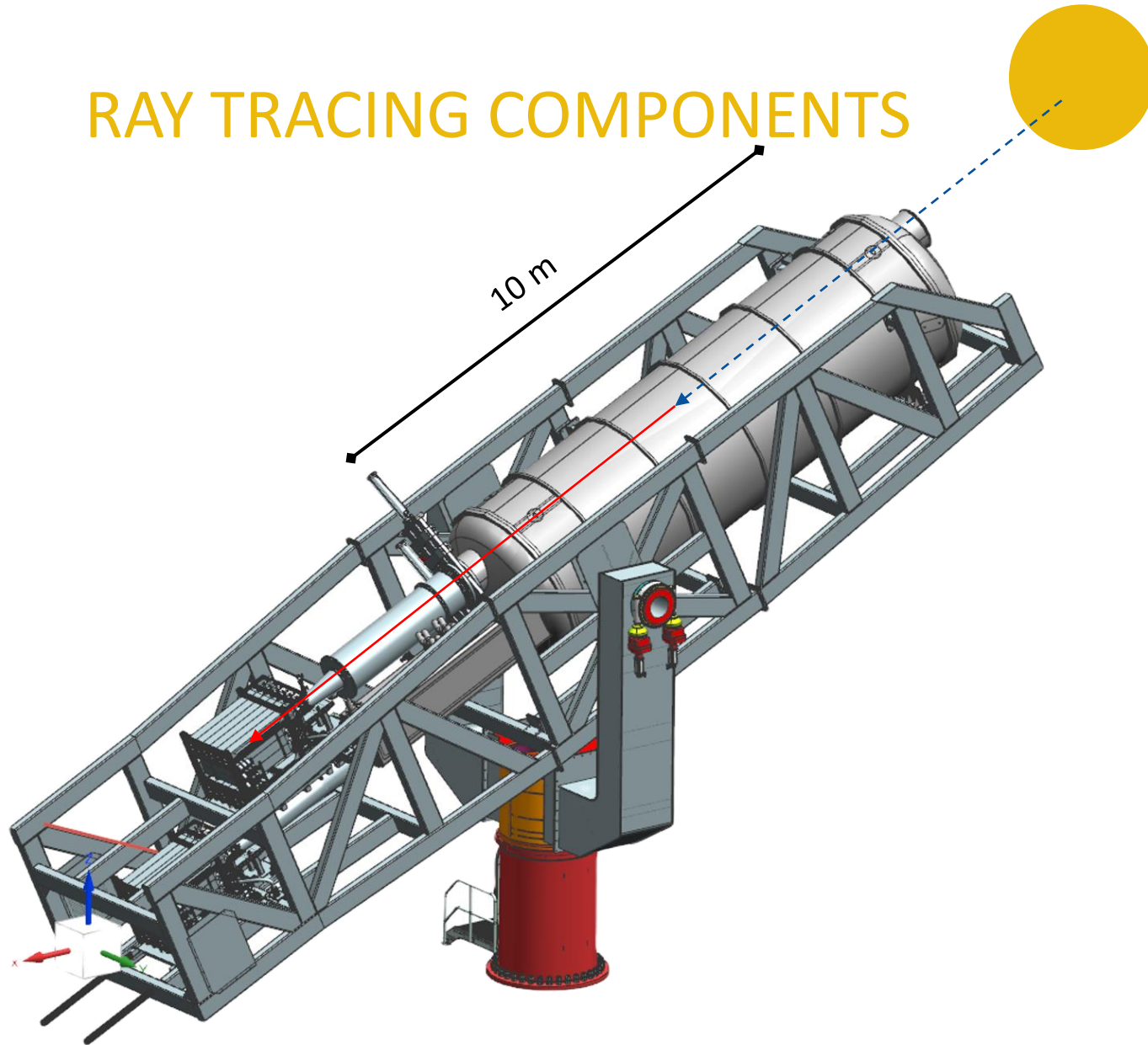
- Adjust the axion model to compare the simulation with future results
- Adjust the position of the telescope components to understand their acceptance range



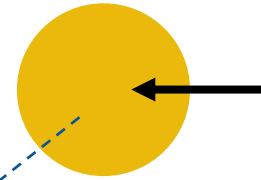
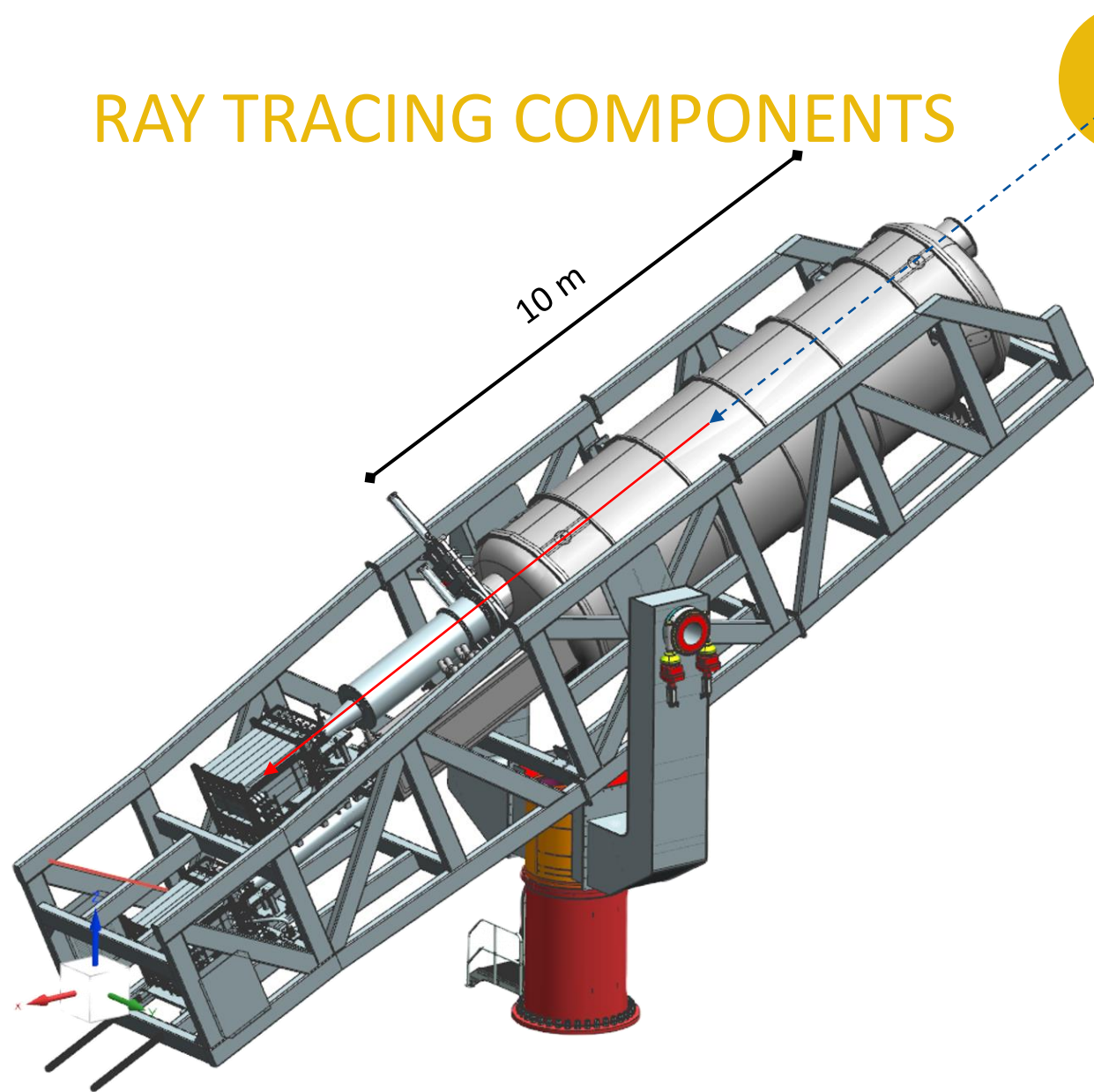
Rare Event  
Searches Toolkit  
software

- Mainly written in C++ and fully integrated with ROOT I/O interface
- Contains other libraries for data processing and analysis

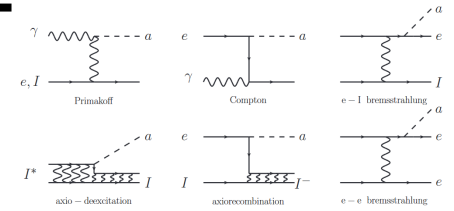
# RAY TRACING COMPONENTS



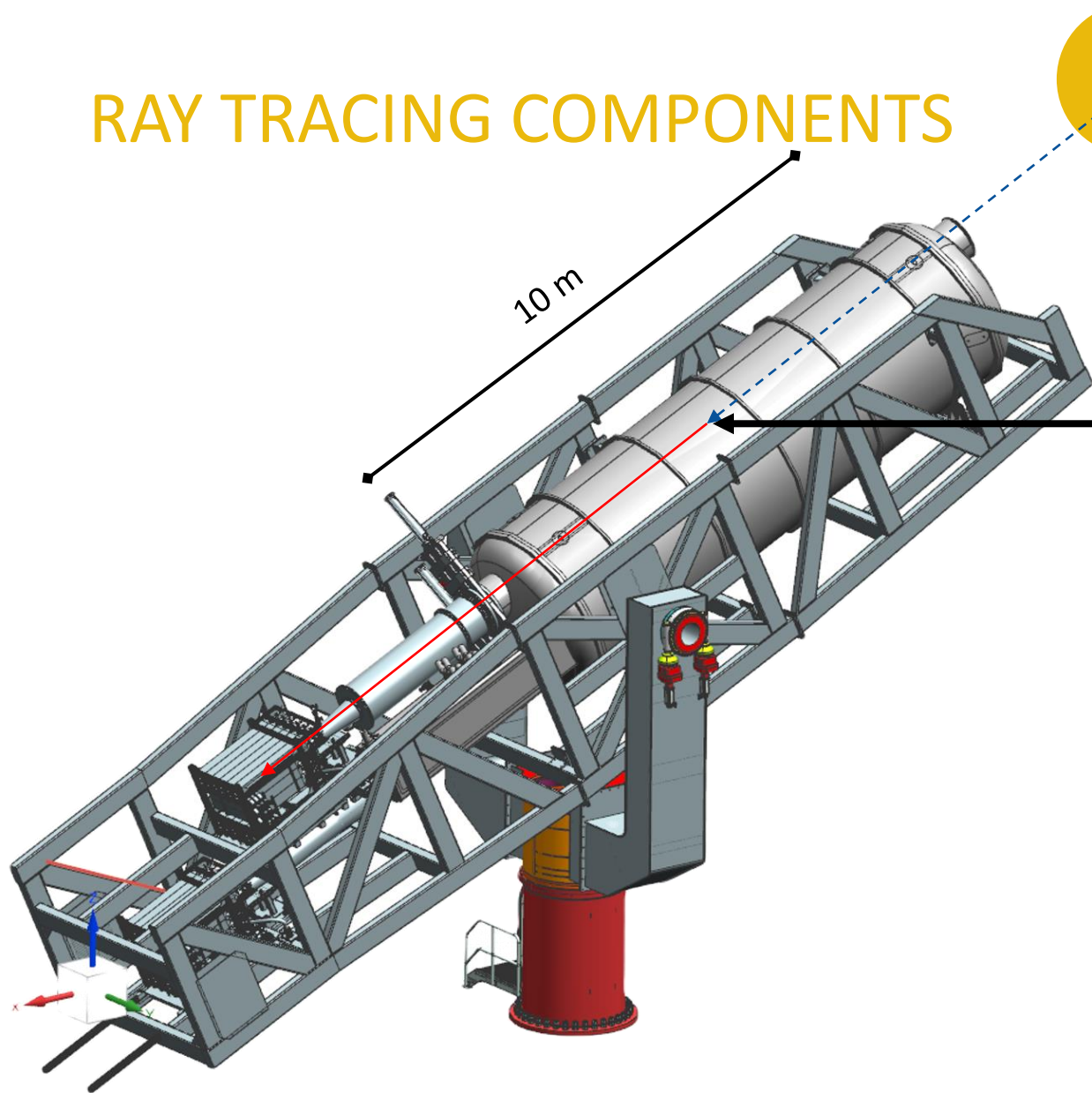
# RAY TRACING COMPONENTS



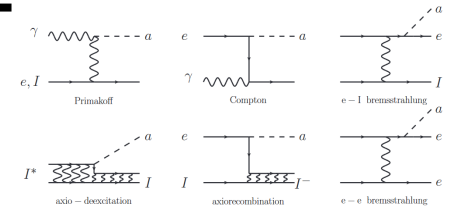
Axion production  
in the sun



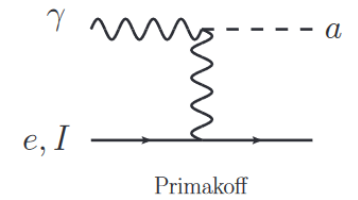
# RAY TRACING COMPONENTS



Axion production in the sun

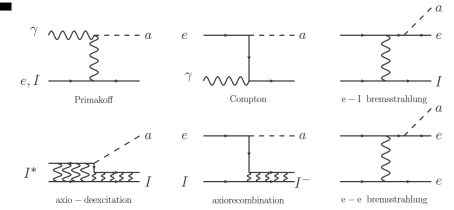
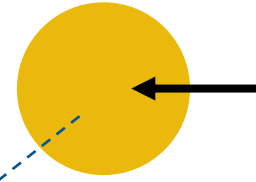


Axions couple to photons in magnetic field

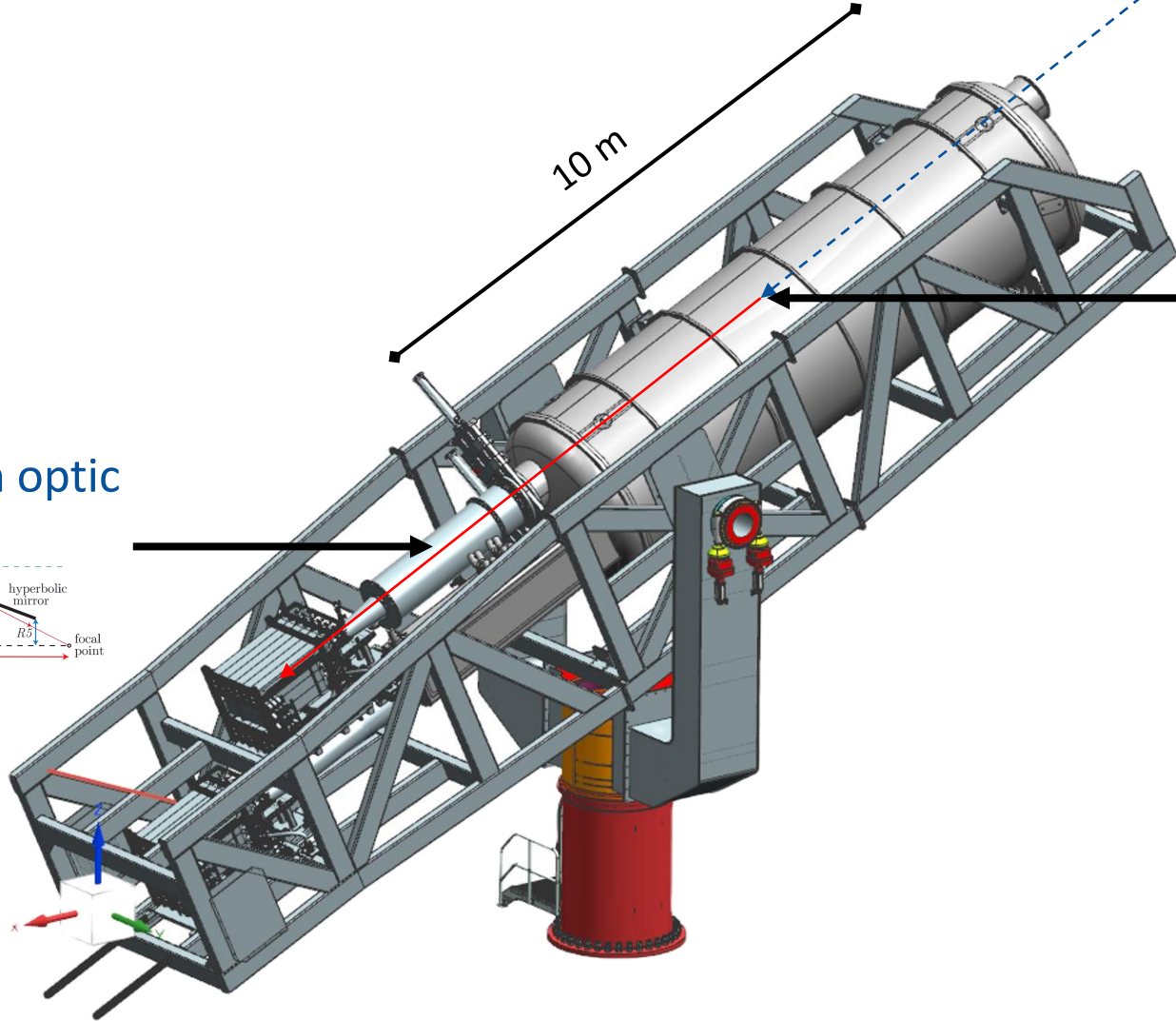
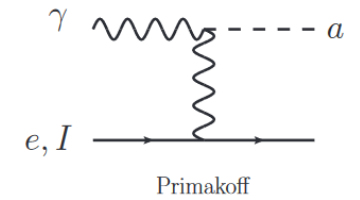


# RAY TRACING COMPONENTS

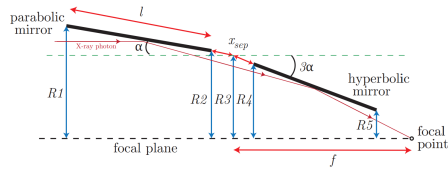
Axion production in the sun



Axions couple to photons in magnetic field

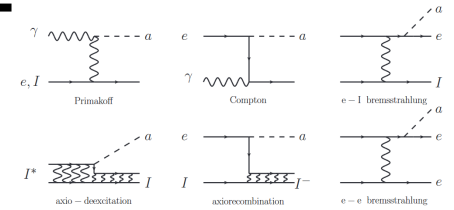
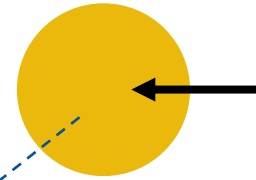


Focus of X-rays in optic

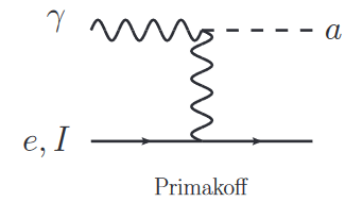


# RAY TRACING COMPONENTS

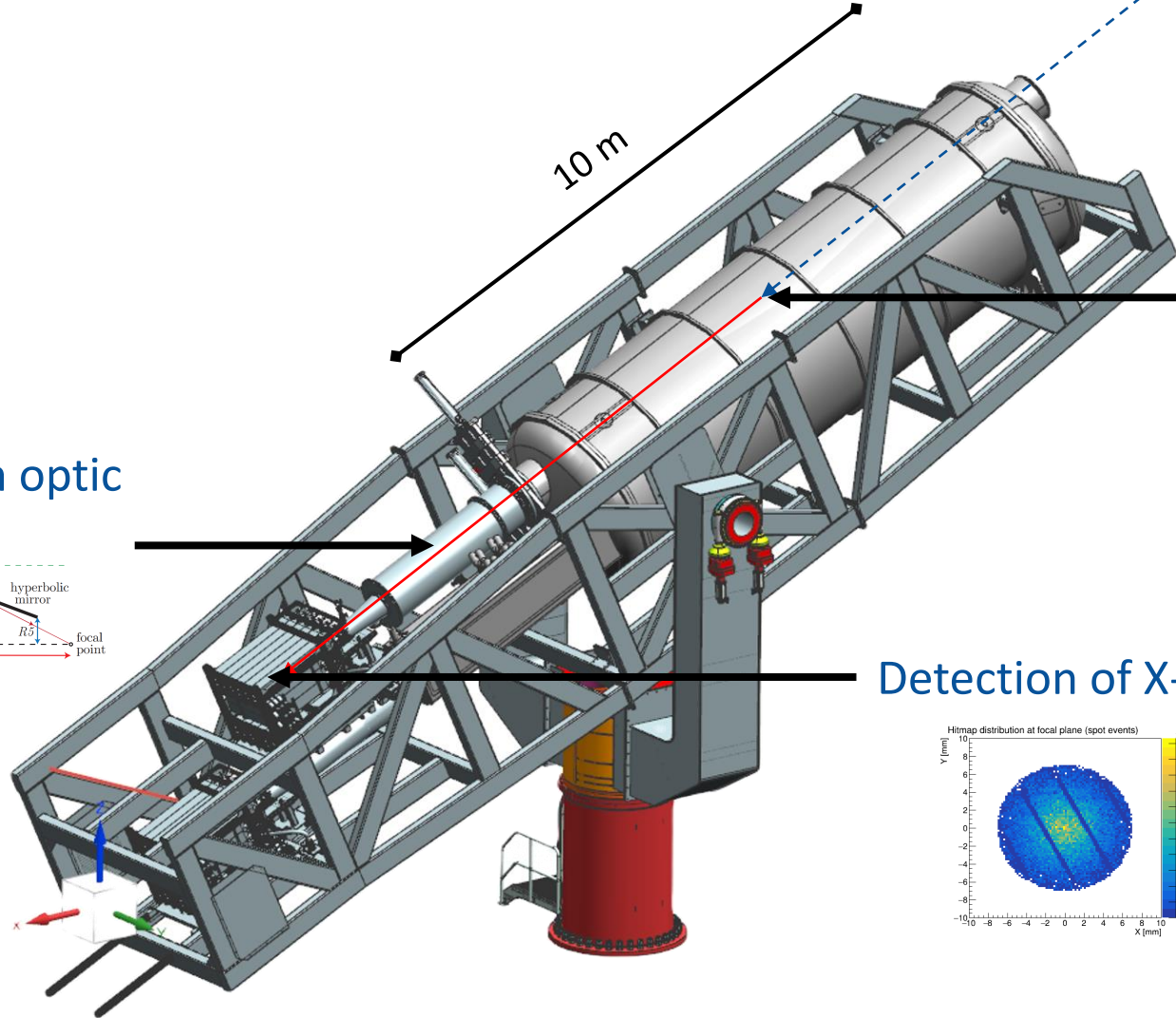
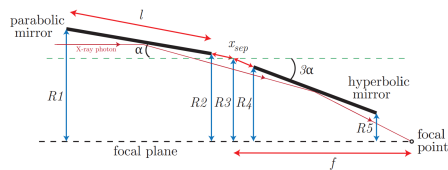
Axion production in the sun



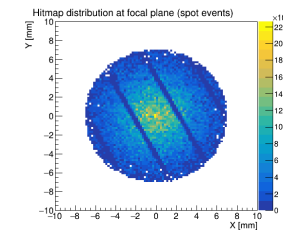
Axions couple to photons in magnetic field



Focus of X-rays in optic

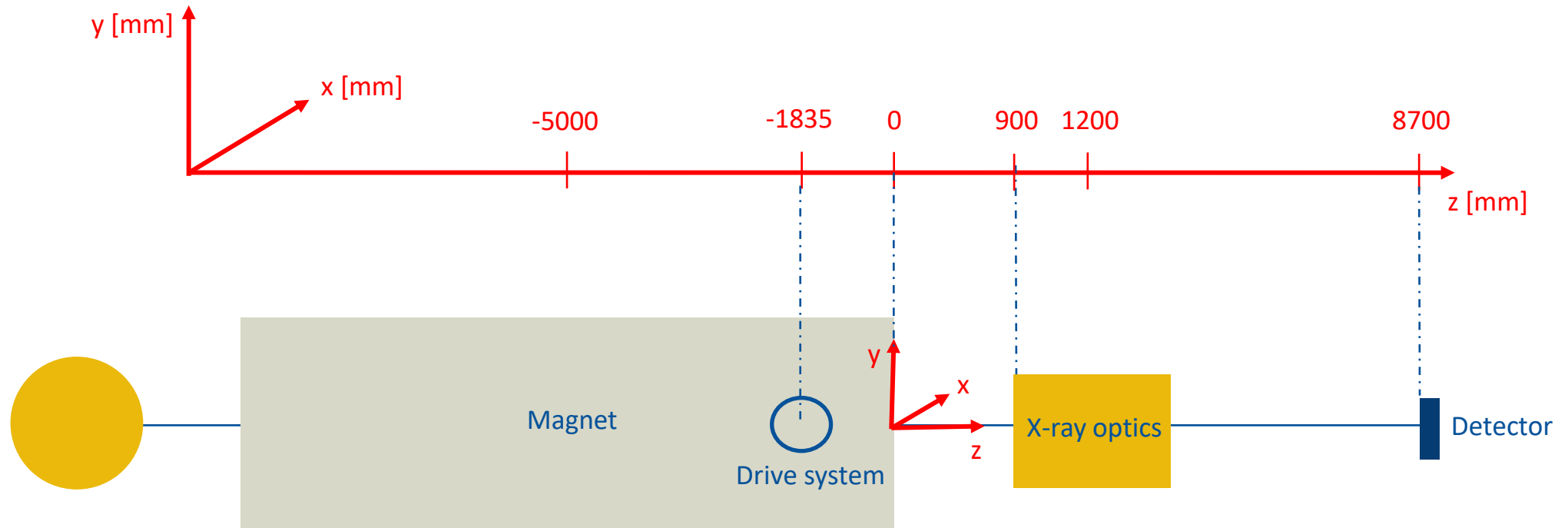


Detection of X-rays

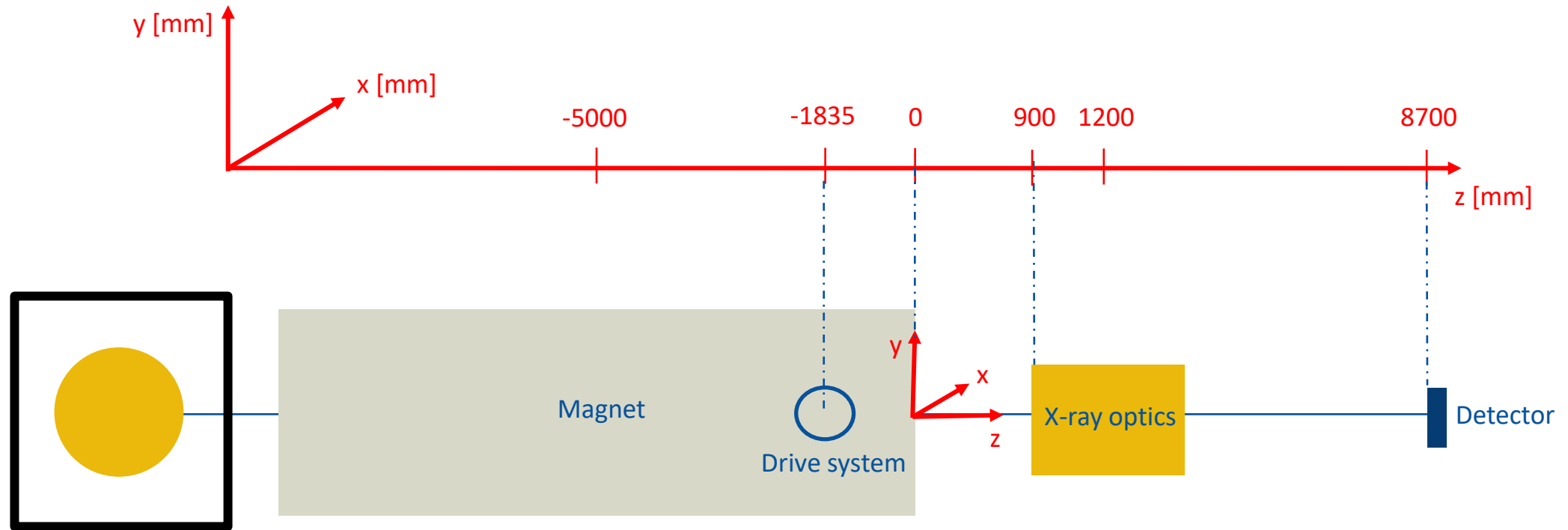




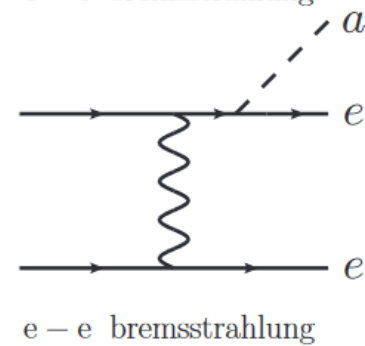
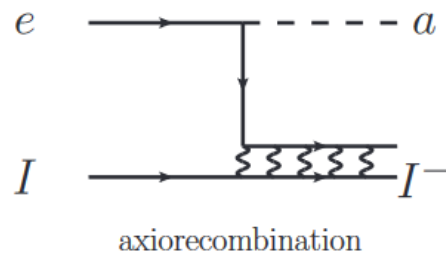
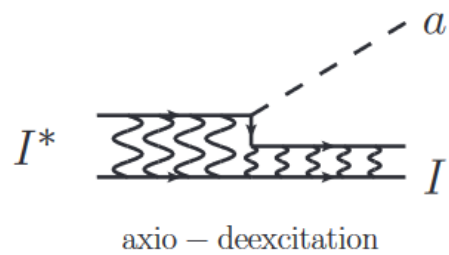
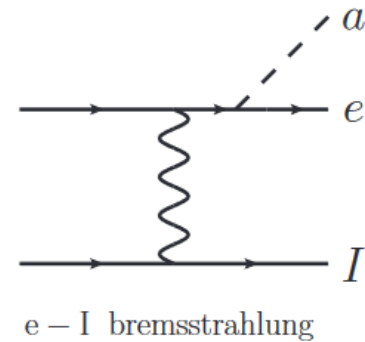
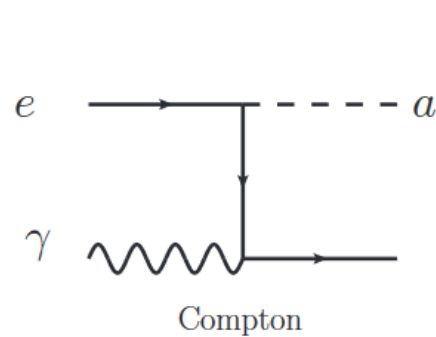
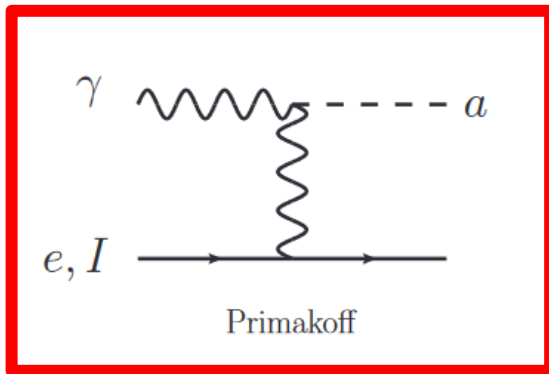
# BABYIAXO SETUP



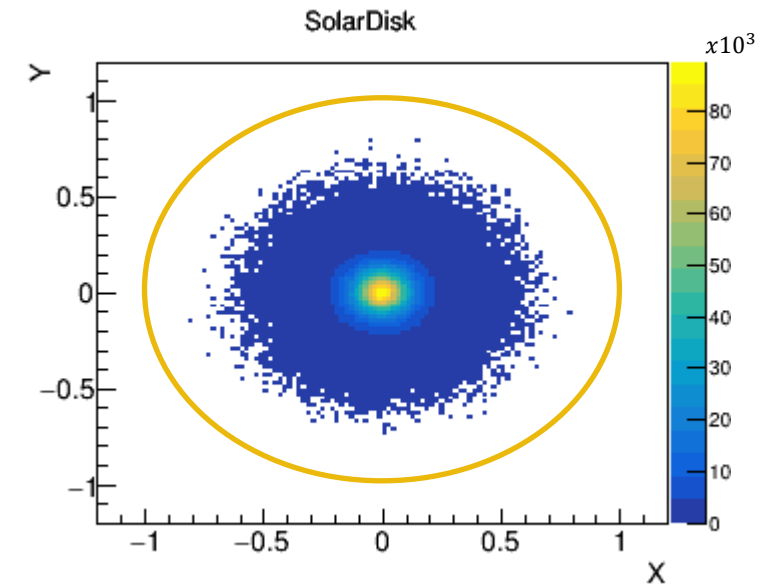
# BABYIAXO – SOLAR AXIONS



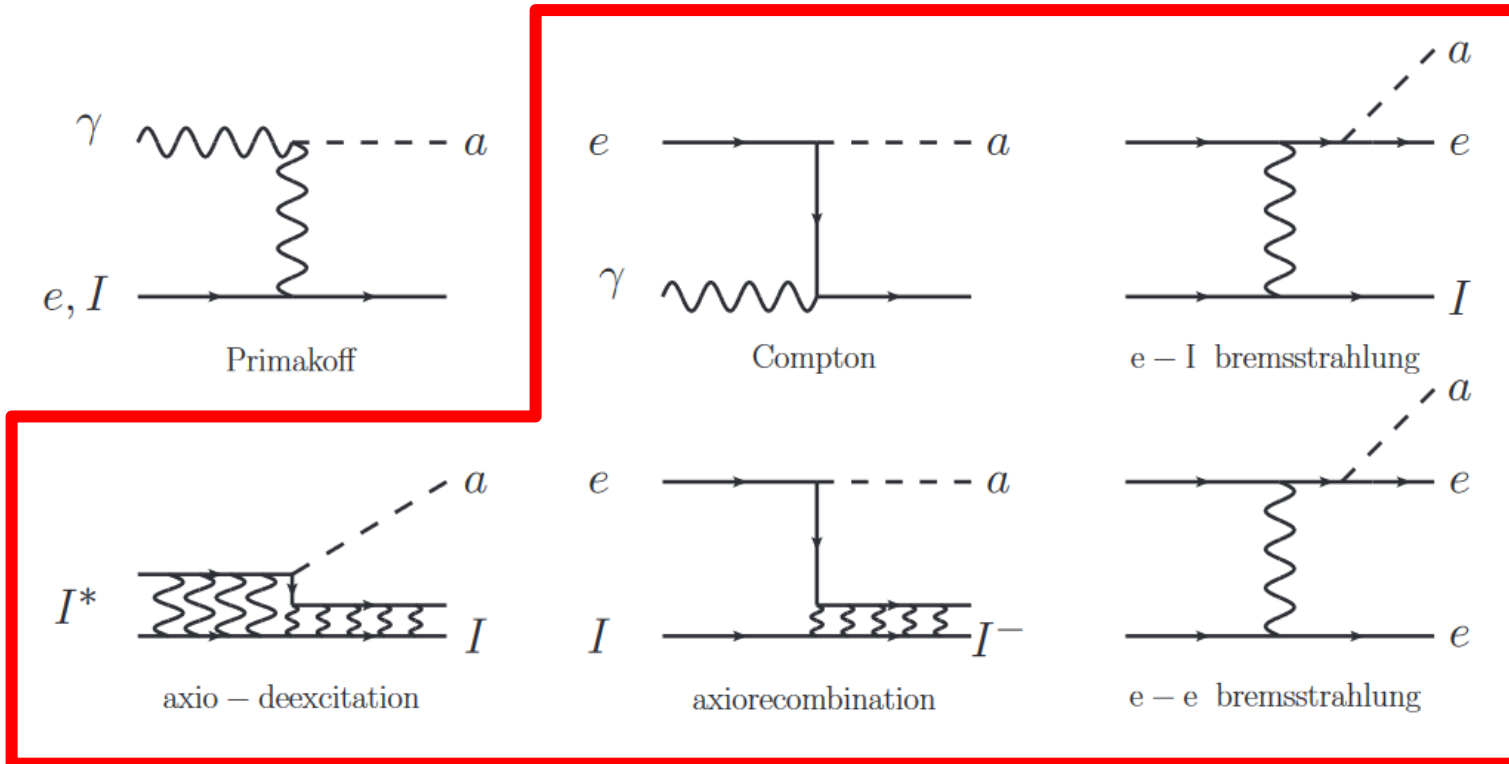
# SOLAR AXIONS – RADIAL DISTRIBUTION



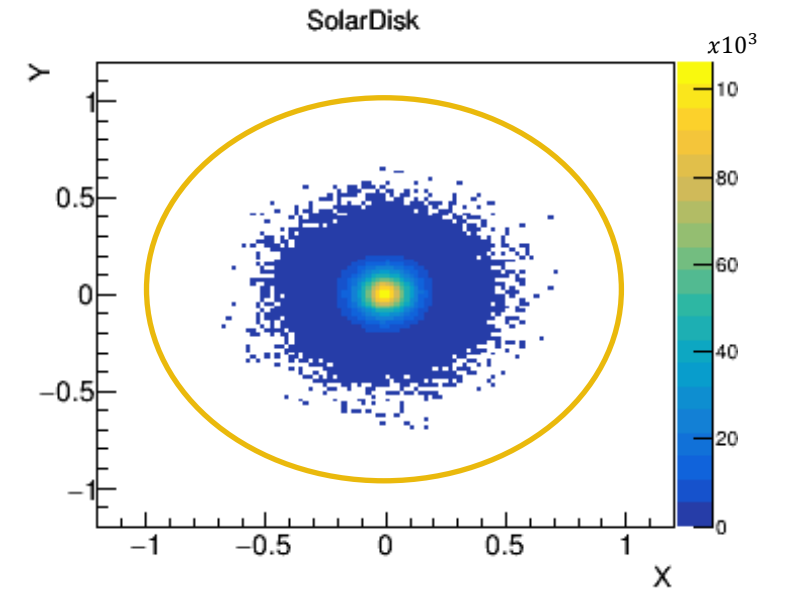
Radial distribution of Primakoff axion flux in sun



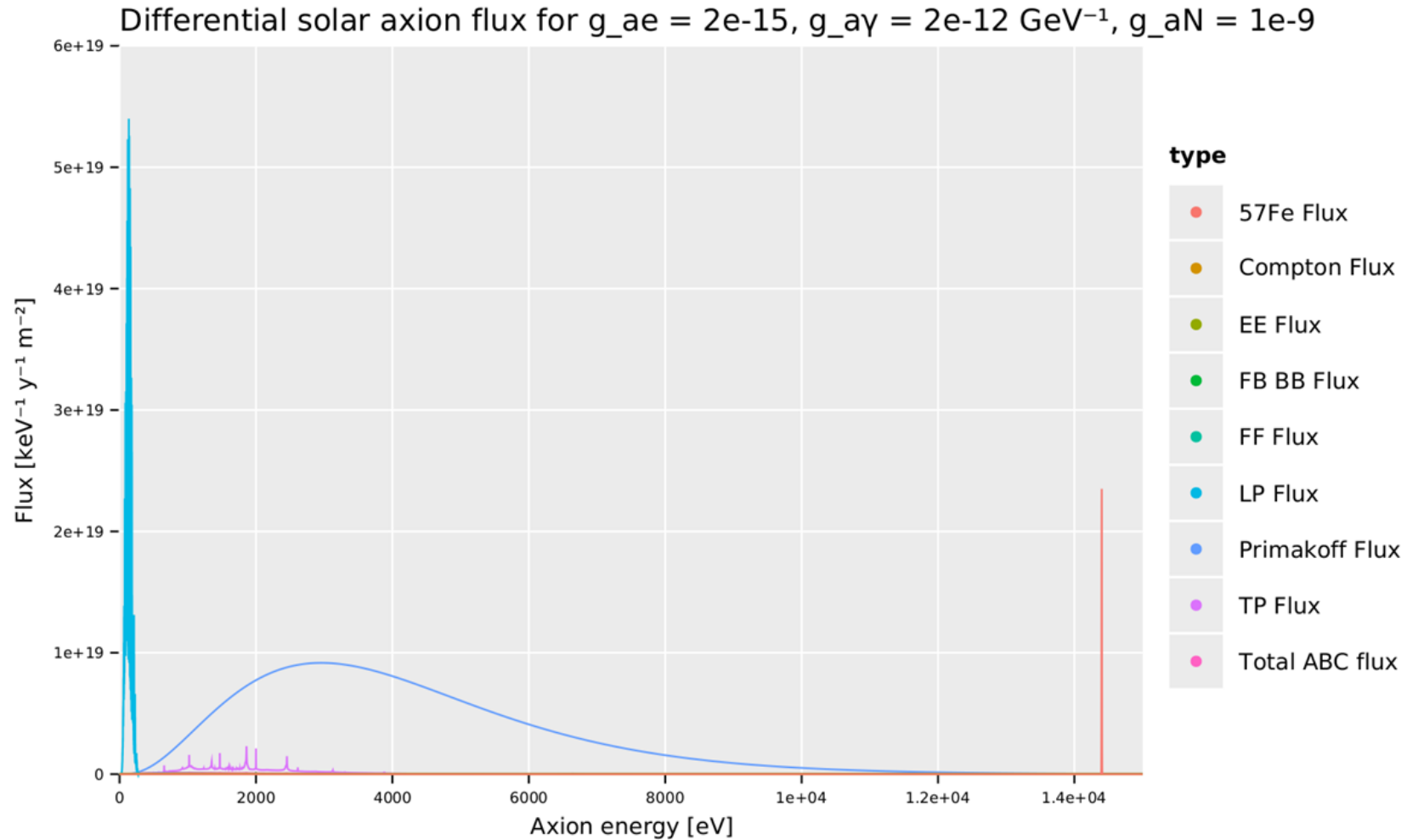
# SOLAR AXIONS – RADIAL DISTRIBUTION



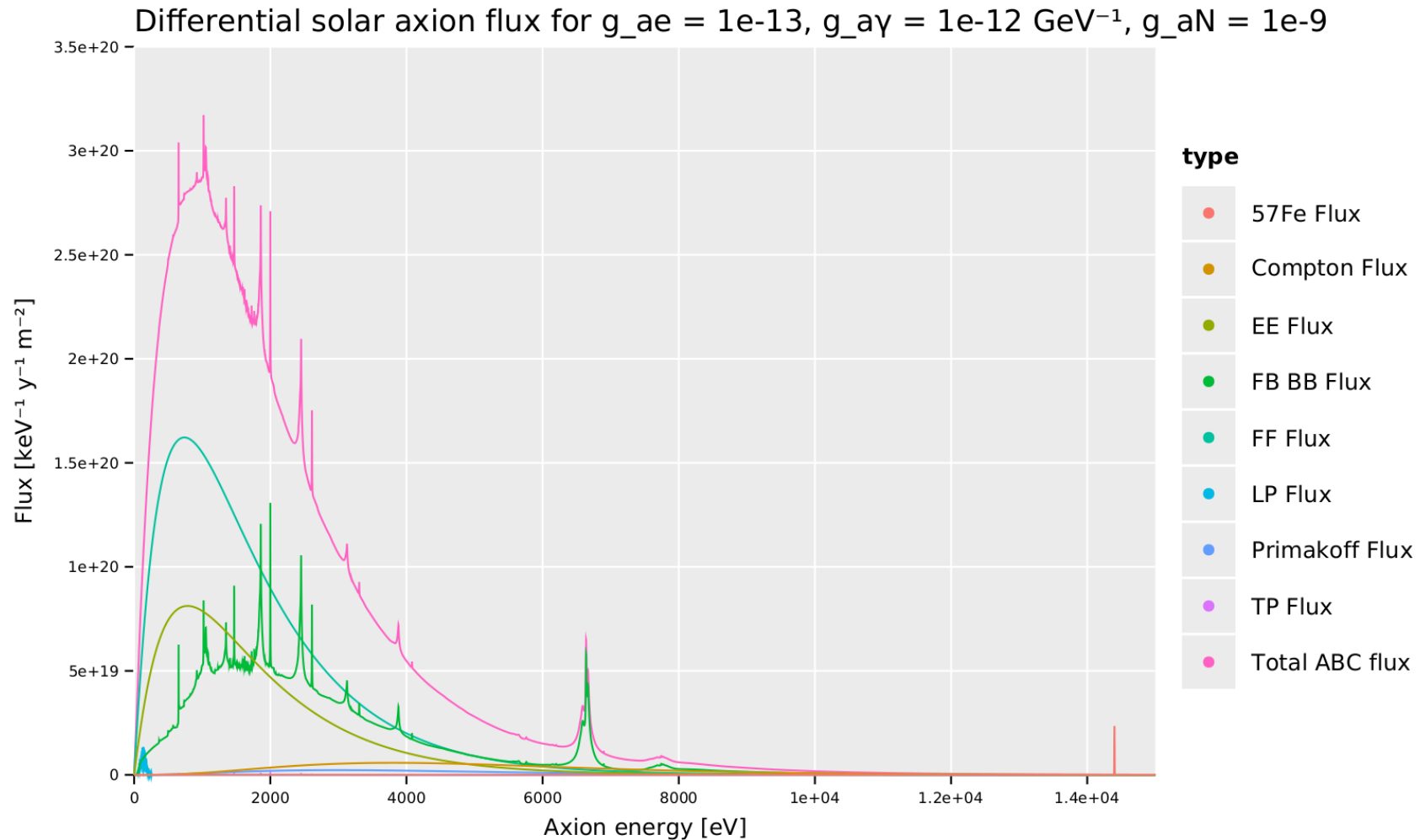
Radial distribution of ABC axion flux in sun



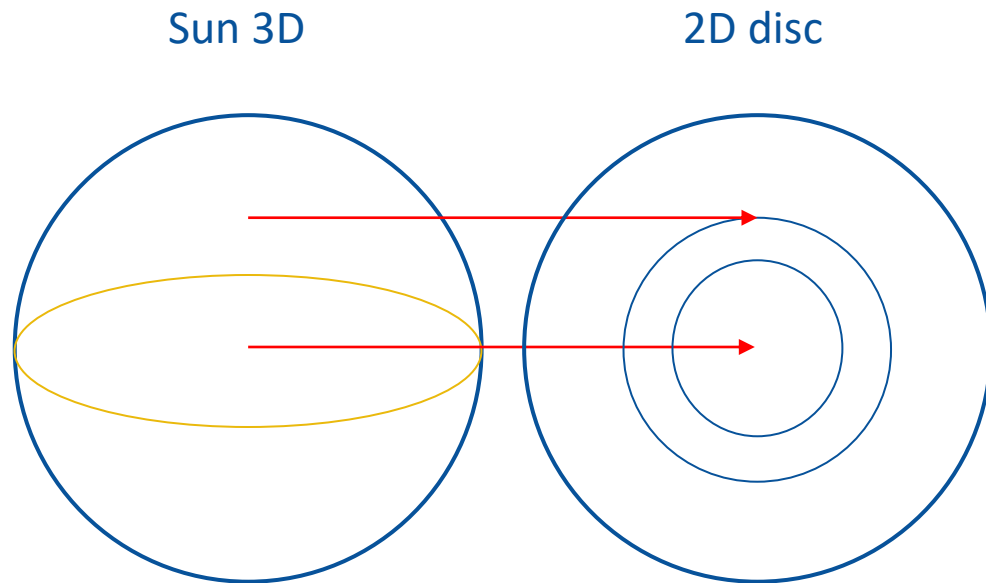
# SOLAR AXION – KSVZ ENERGY DISTRIBUTION



# SOLAR AXION – DFSZ ENERGY DISTRIBUTION

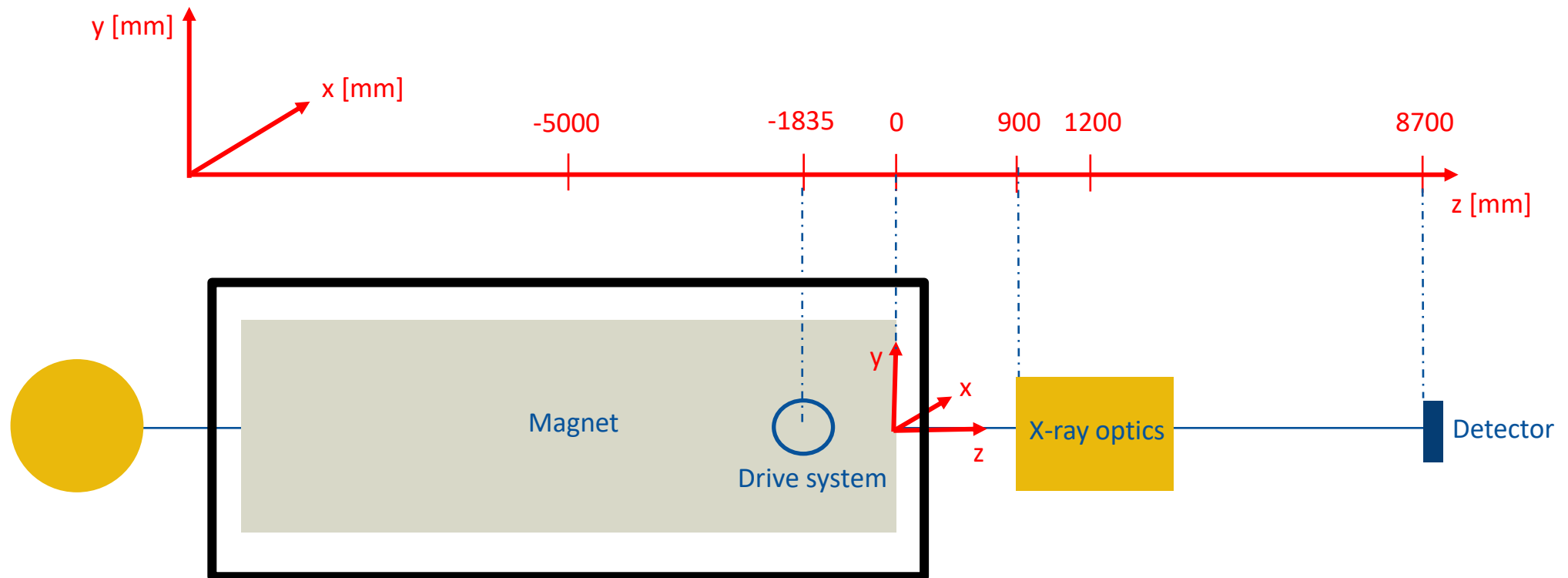


# GENERATING AXIONS FROM THE SUN



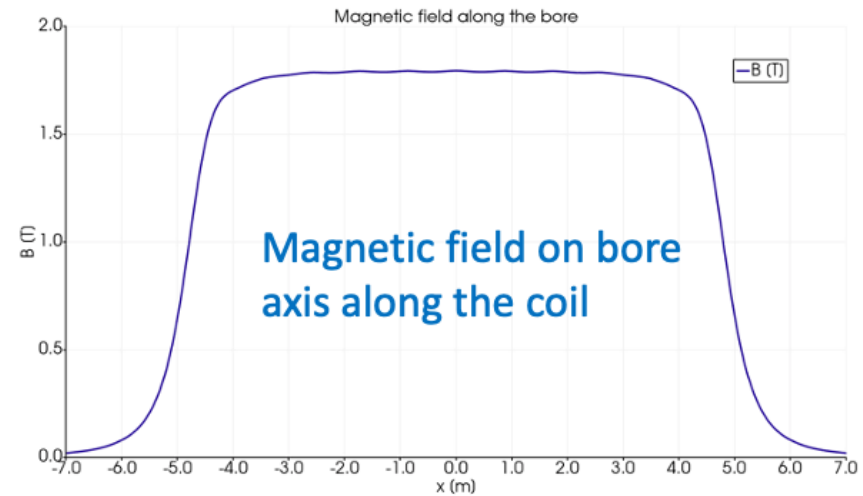
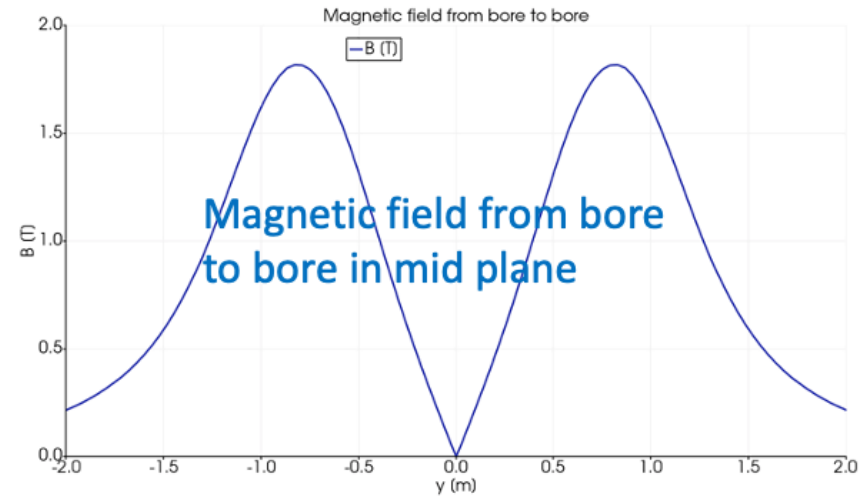
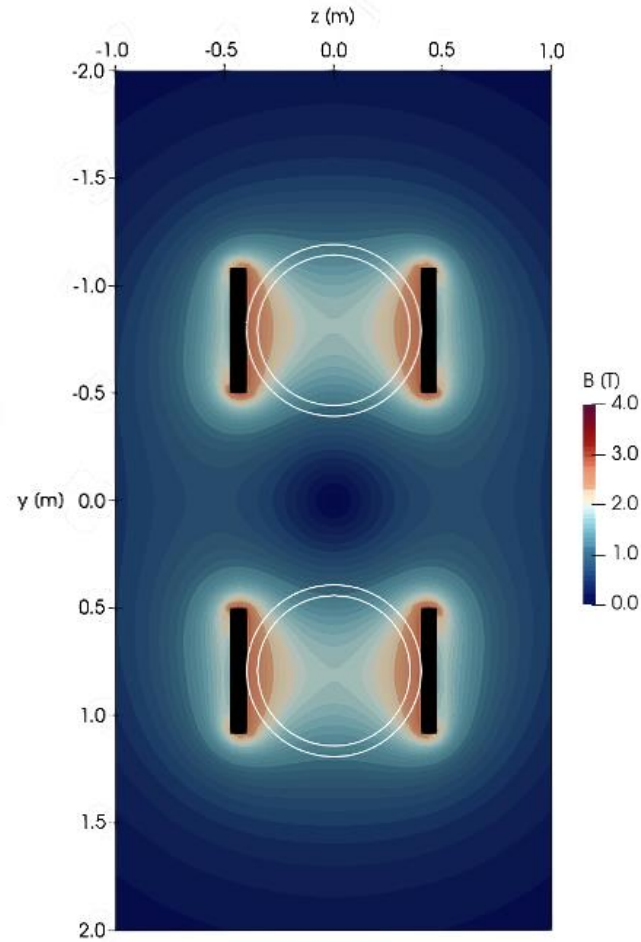
1. Integrate over the sun for each radius
2. Get random radius and energy for each axion biased by the calculated flux

# BABYIAXO – THE MAGNET

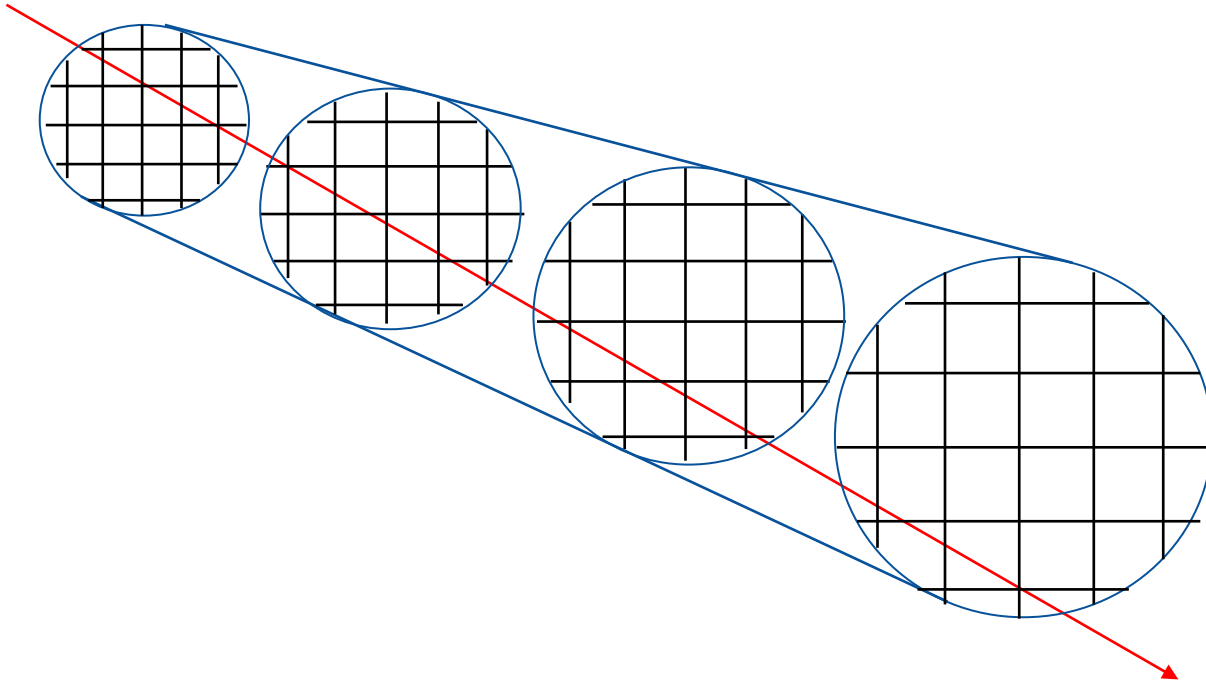




# MAGNETIC FIELD



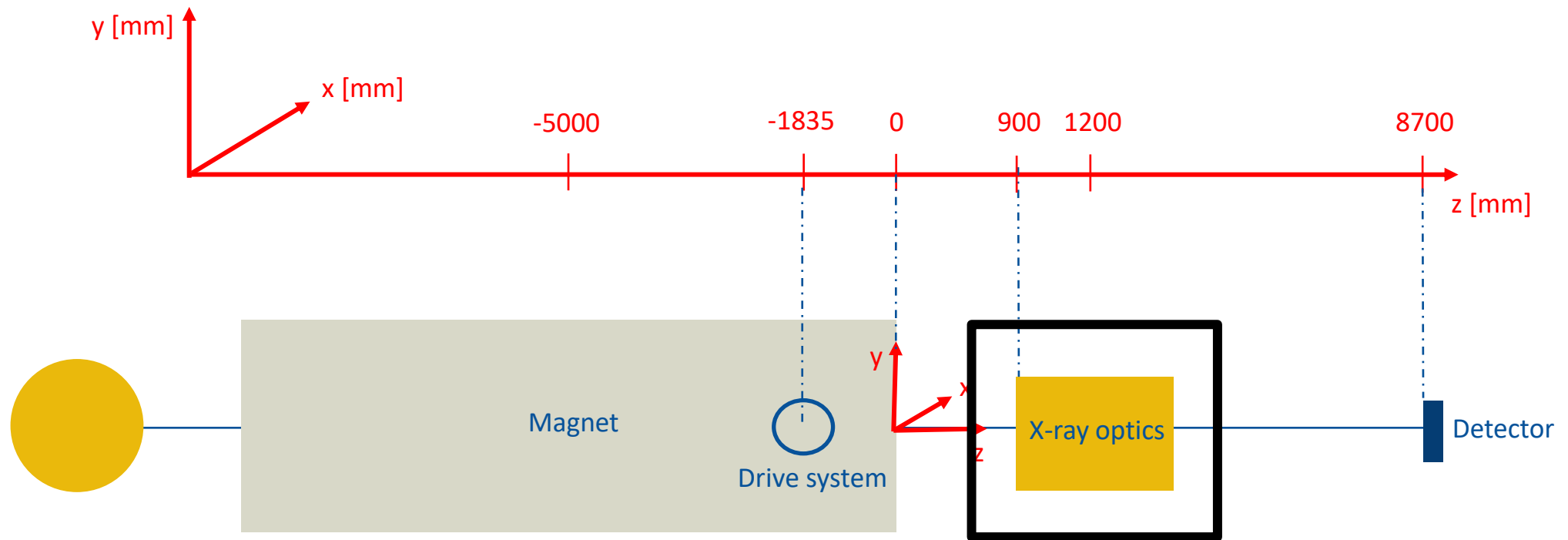
# MAGNETIC FIELD IMPLEMENTATION



1. Get magnetic field on grid-vector intersection points
2. Integrate magnetic field over vector
3. Photon production probability:

$$P_{a \rightarrow \gamma} = \frac{1}{4} (g_{a\gamma} BL)^2$$

# BABYIAXO – X-RAY OPTICS

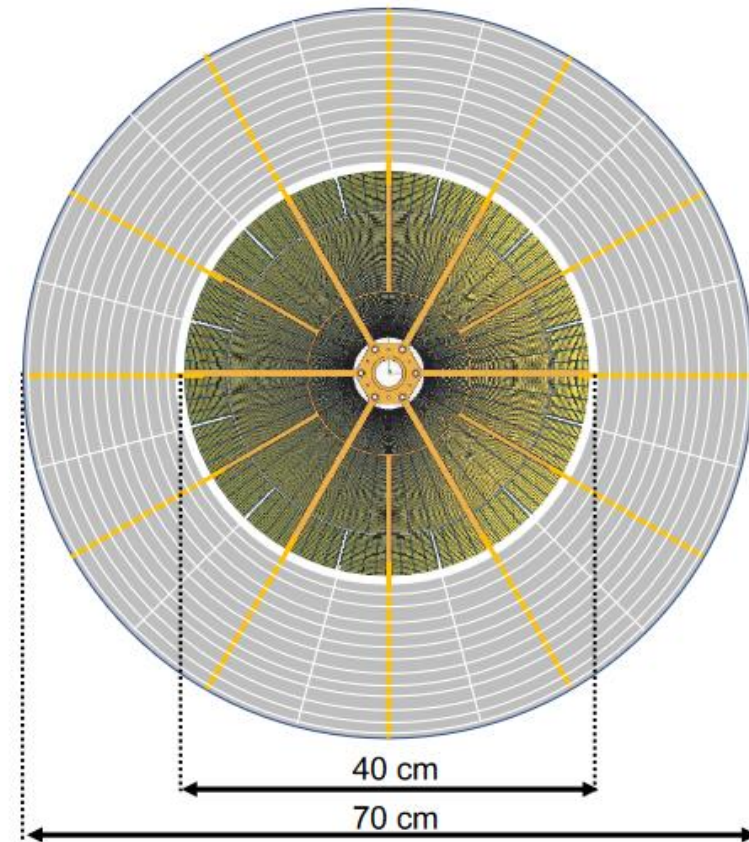


# X-RAY OPTICS

The XMM optics built for the XMM-Newton space mission

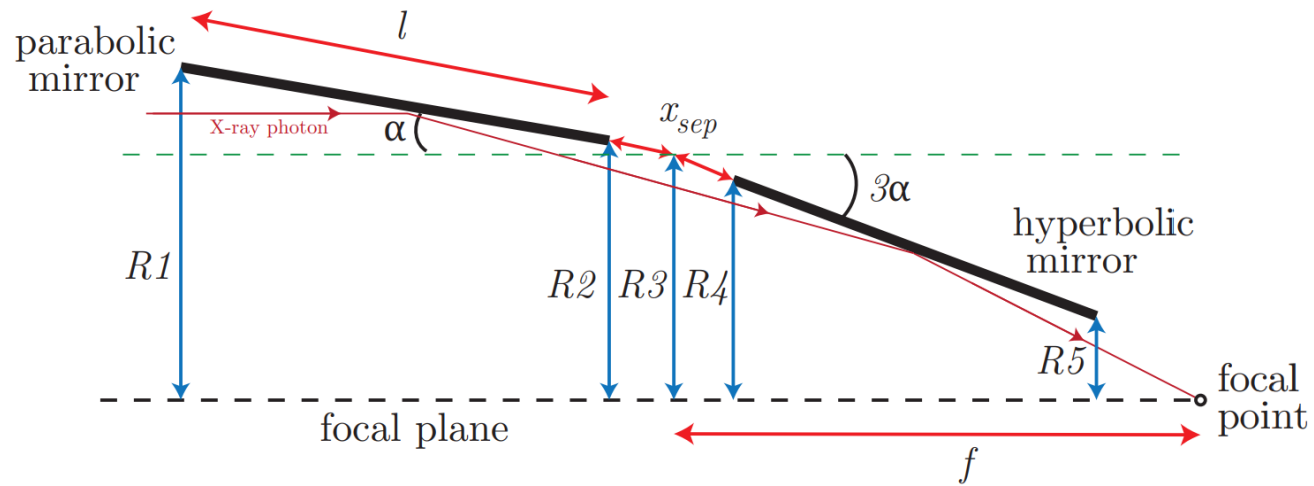


The custom BabyIAXO optics consisting of an inner optics and an outer optics



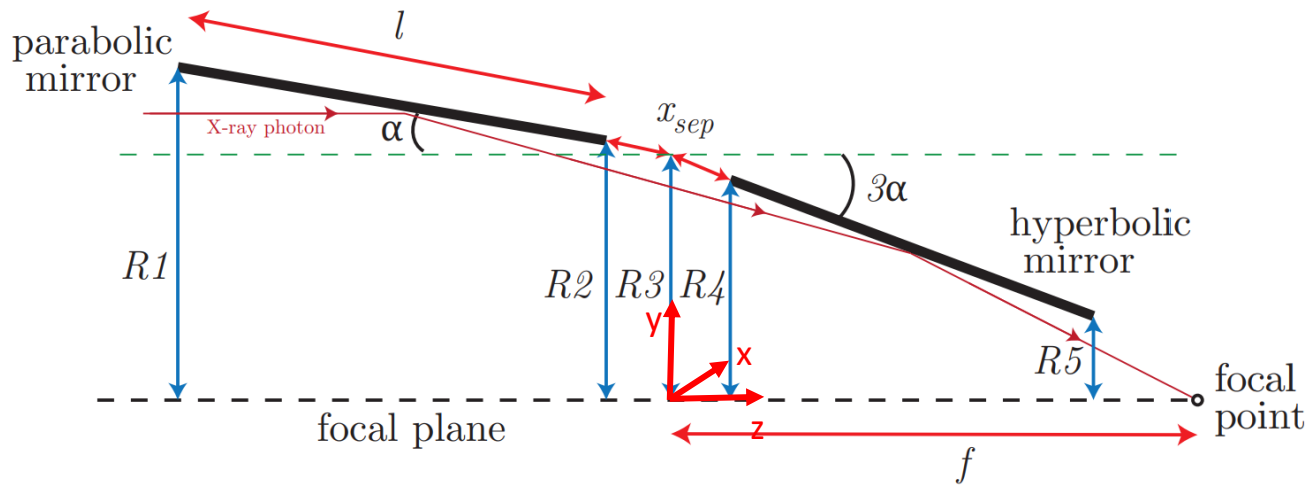
IAXO collaboration 2020, arXiv:2010.12076

A Wolter I optic principle from the side



1. Find interaction point
2. Turn X-ray vector in regards to the respective normal vector

A Wolter I optic principle from the side



1. Find interaction point
2. Turn X-ray vector in regards to the respective normal vector

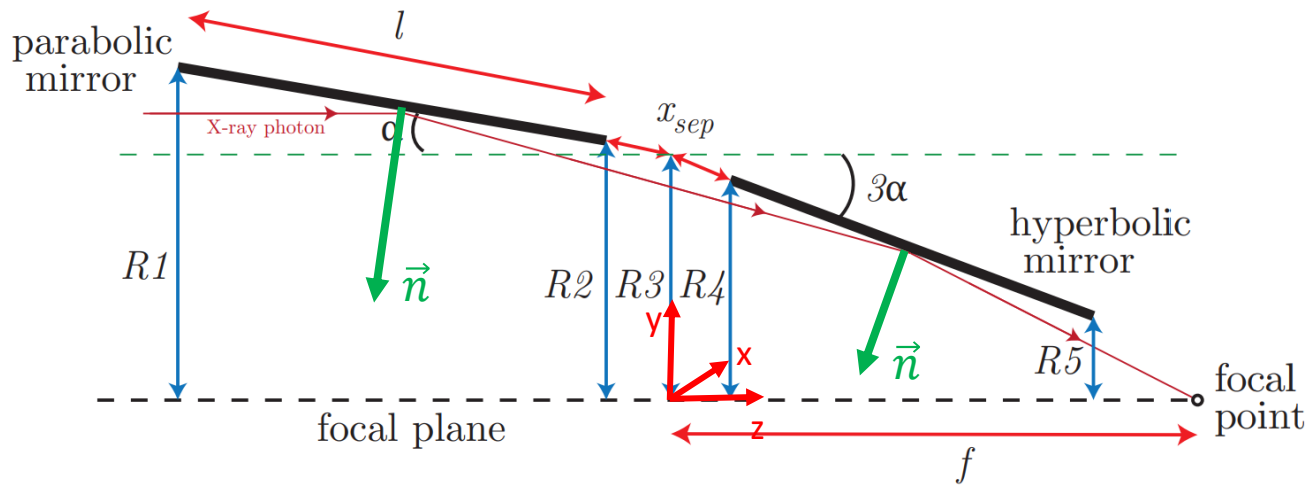
Wolter I: Parabolic mirror function

$$R^2(z) = R3^2 - R3 \cdot 2 \cdot \tan(\alpha) \cdot z$$

Wolter I: Hyperbolic mirror function

$$R^2(z) = R3^2 - R3 \cdot 2 \cdot \tan(3\alpha) \cdot \left( z + \frac{z^2}{f + R3 \cdot \cot(2\alpha)} \right)$$

A Wolter I optic principle from the side



1. Find interaction point
2. Turn X-ray vector in regards to the respective normal vector

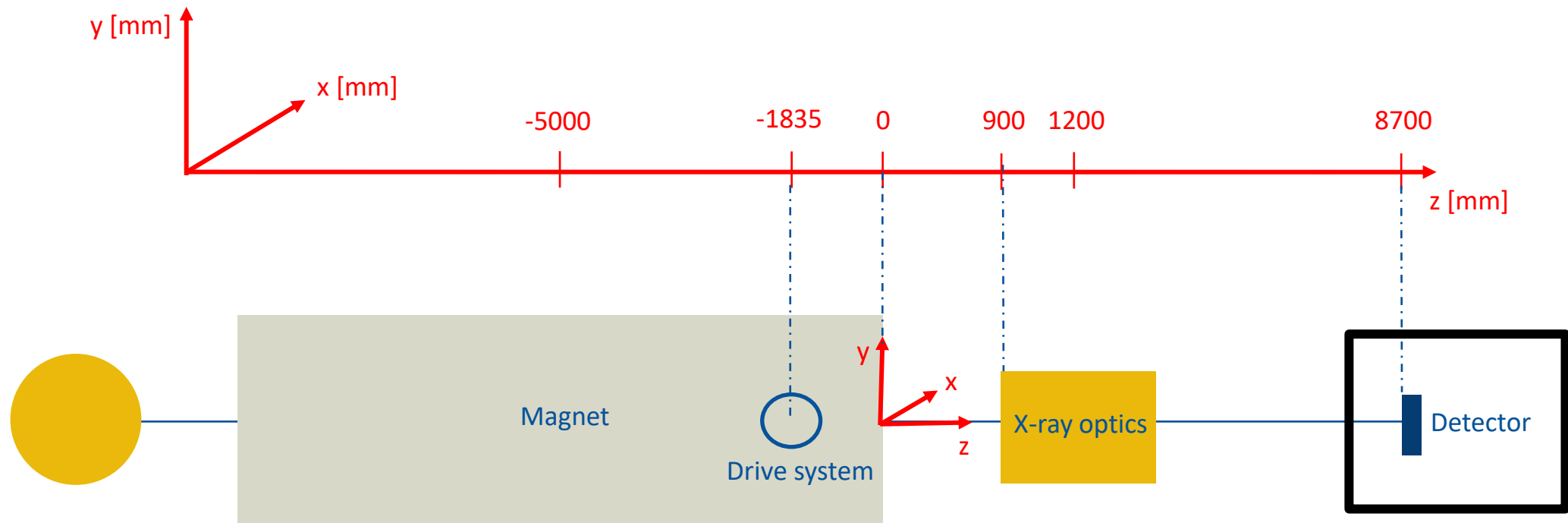
Wolter I: Parabolic mirror function

$$R^2(z) = R3^2 - R3 \cdot 2 \cdot \tan(\alpha) \cdot z$$

Wolter I: Hyperbolic mirror function

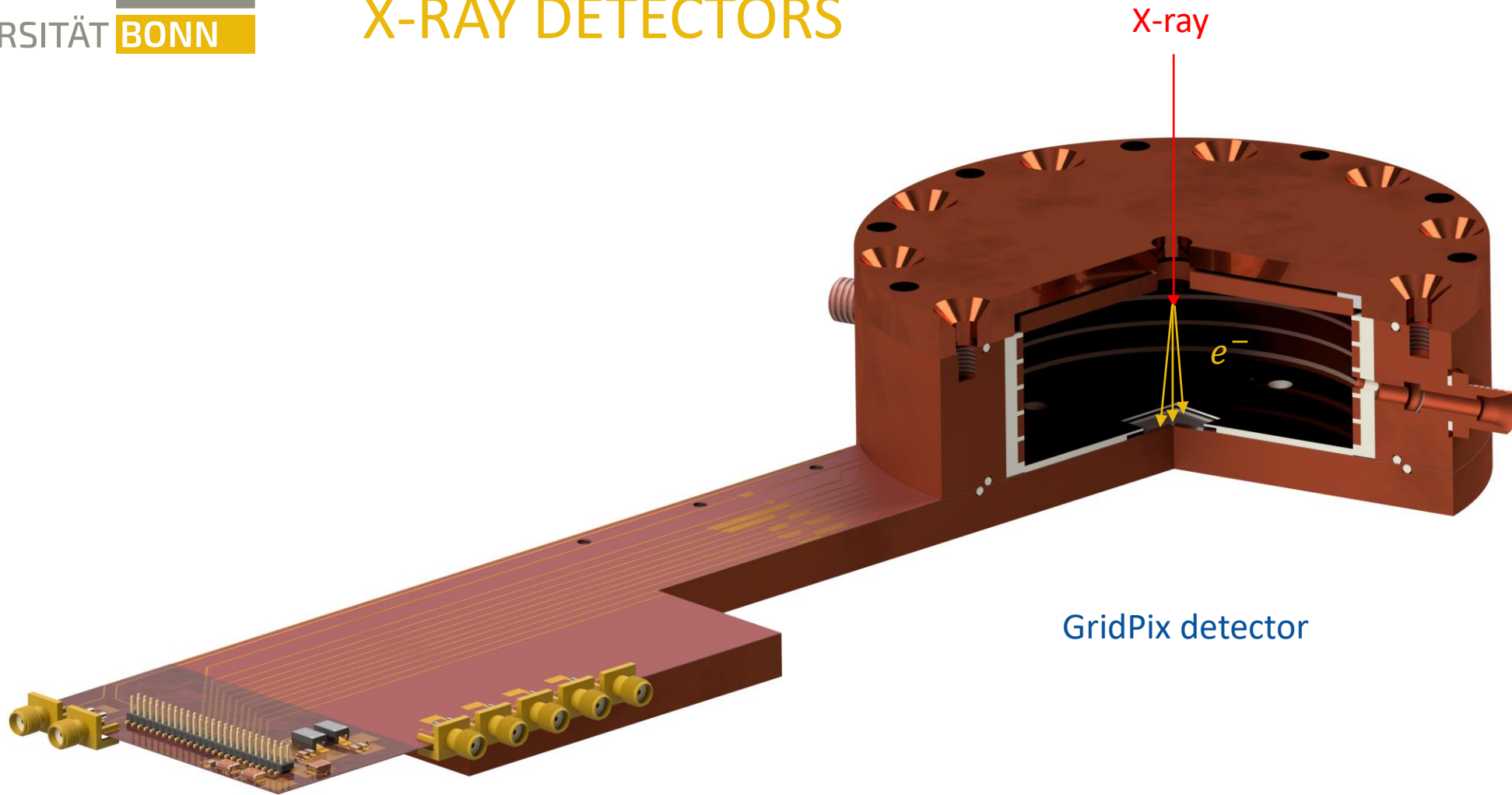
$$R^2(z) = R3^2 - R3 \cdot 2 \cdot \tan(3\alpha) \cdot \left( z + \frac{z^2}{f + R3 \cdot \cot(2\alpha)} \right)$$

# BABYIAXO – DETECTORS





# X-RAY DETECTORS



# DETECTOR WINDOWS AND MASKS

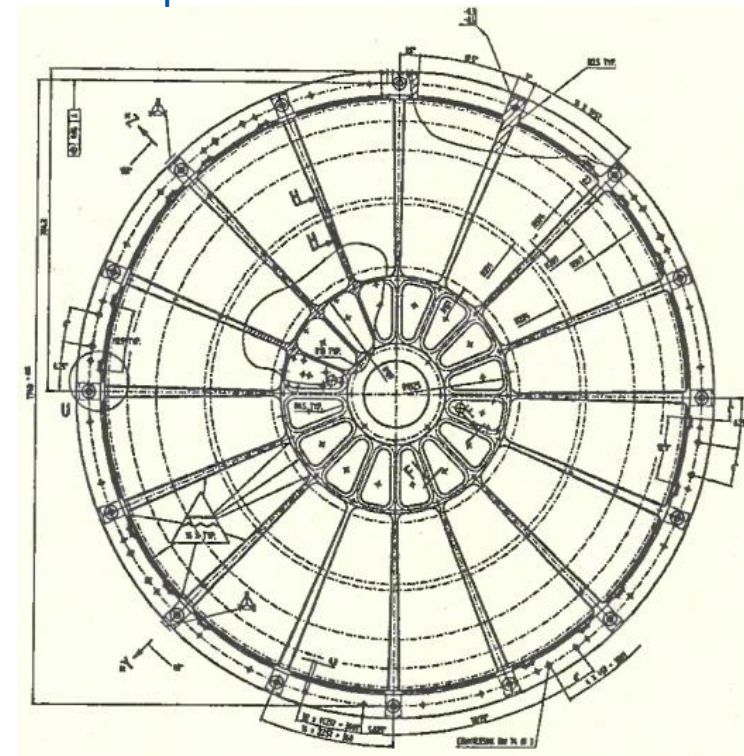
Mylar window



A vacuum tight Si<sub>3</sub>N<sub>4</sub> window

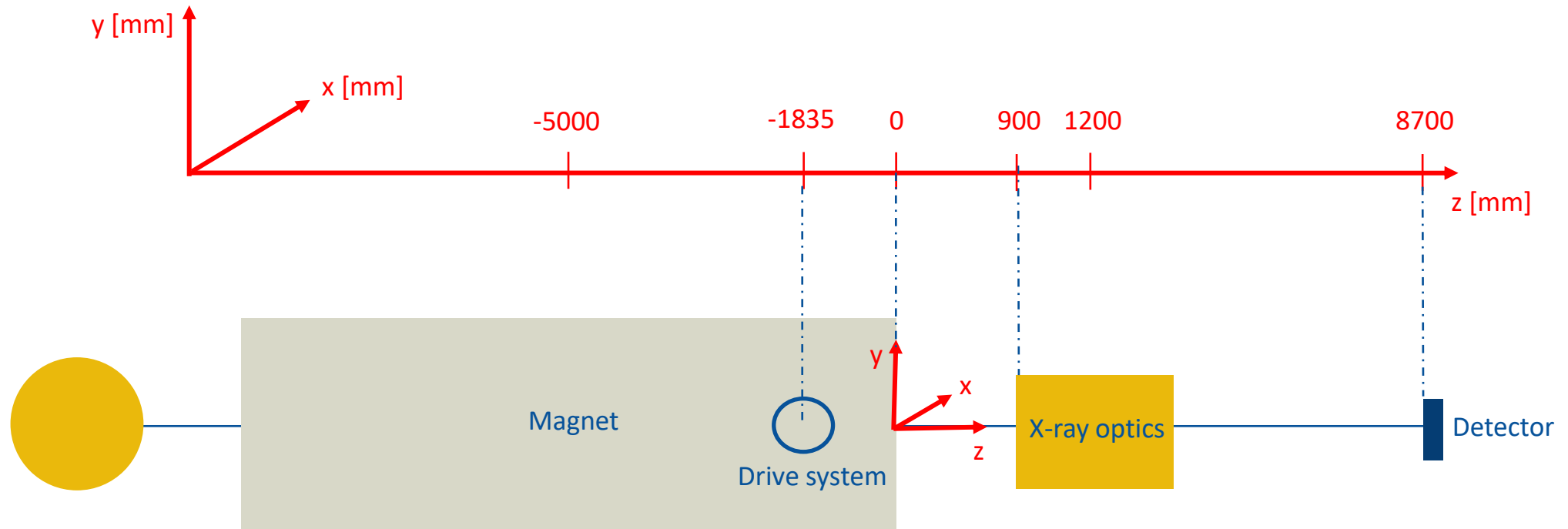


The spider structure in front of the XMM optics



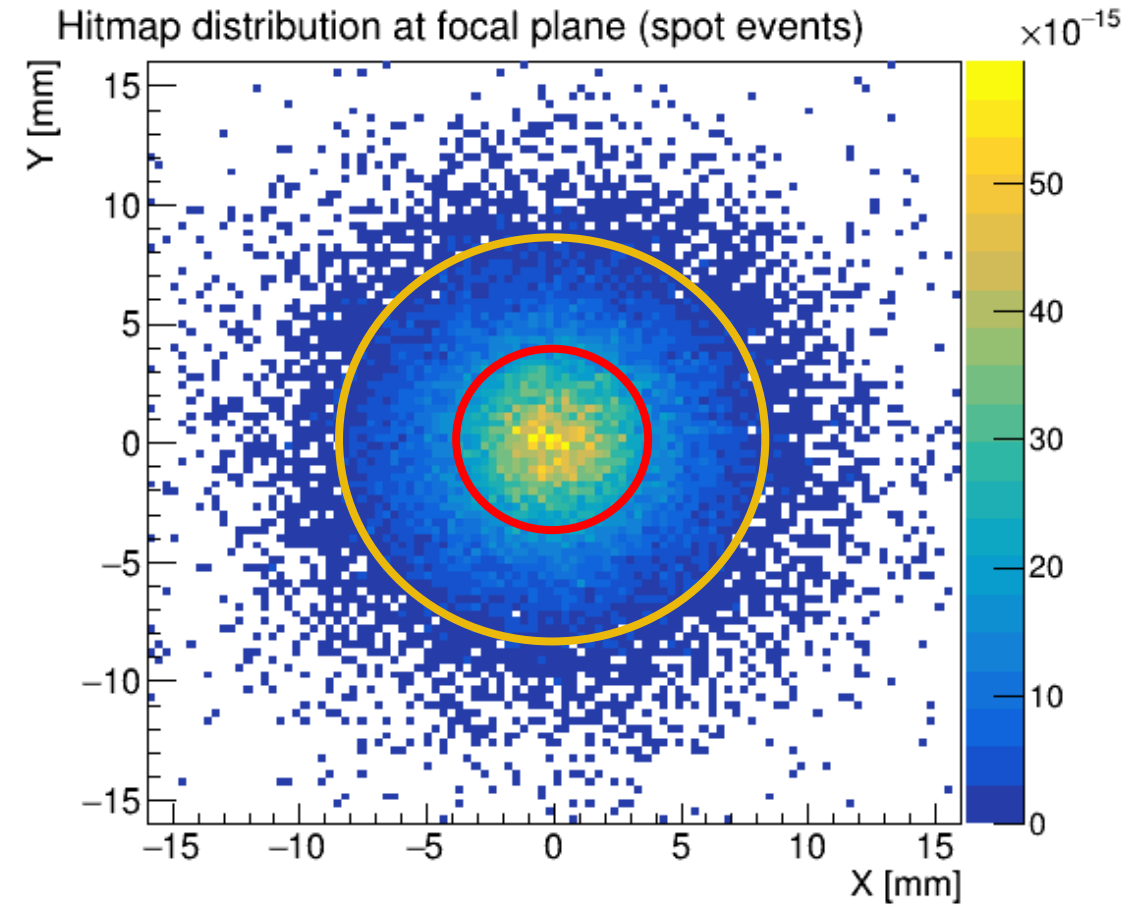
1. Get energy dependent transmission probability of different materials
2. Create a geometric mask

# BABYIAXO – PERFECT ALIGNMENT



## RESULTS PERFECT ALIGNMENT

- Run with 100 000 events
- Solar flux: Primakoff
- Vacuum stage
- Optics: XMM optics
- Results here done with REST v2.3.15



HEW=7.83mm W90=16.83mm  
HEW=3.59' W90=7.714'

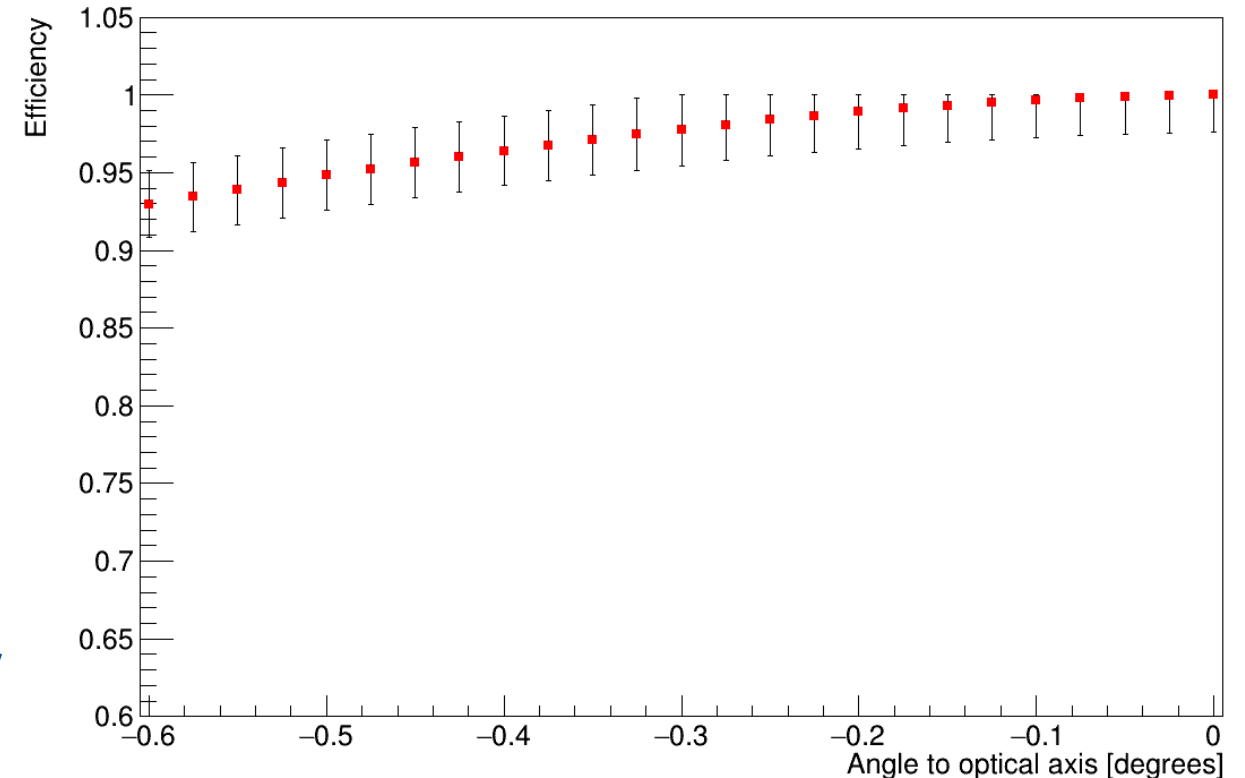
## 1. Internal:

- Individual rotation of magnet and optics around their own center
- Magnet, optics and detector displacement

## 2. External:

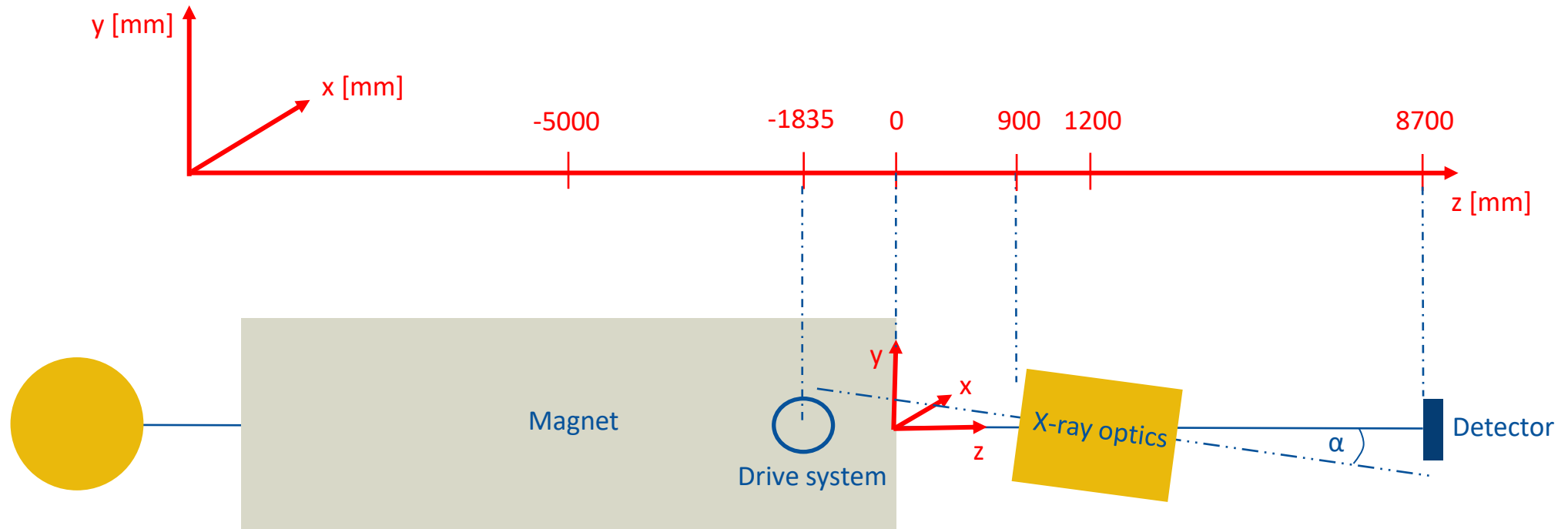
- Misalignment effects due to gravity

Relative Efficiency Comparison



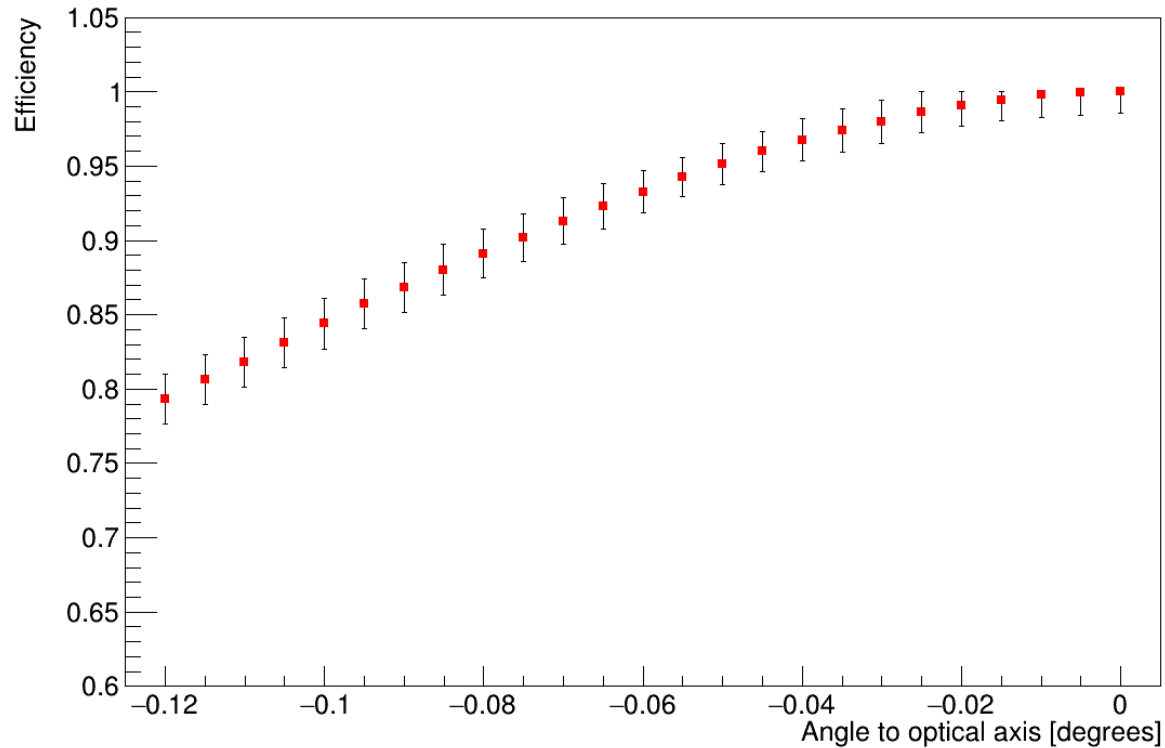
Internal magnet rotation downwards

# INTERNAL ROTATION X-RAY OPTICS

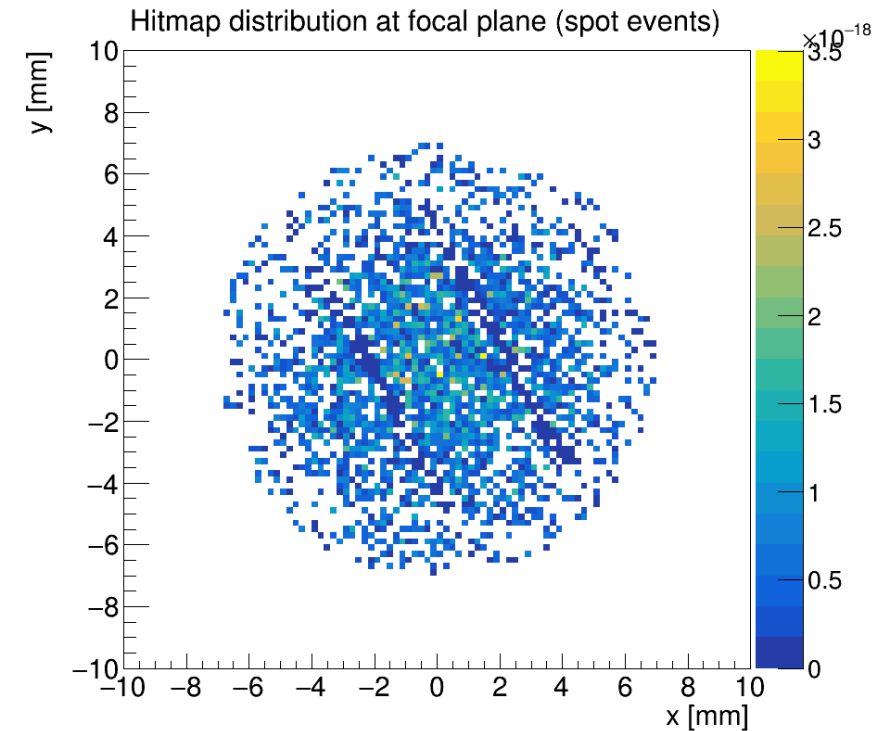


# INTERNAL OPTICS ROTATION

Relative Efficiency Comparison



Internal optics rotation downwards



Optics rotation around its center by  $0.12^\circ$

## RESULTS INTERNAL

Individual acceptance magnet	
Rotation $\alpha_{pitch}(99\%)$ [°]	Rotation $\alpha_{yaw}(99\%)$ [°]
-0.19	-0.13
Deviation $y(99\%)$ [mm]	Deviation $x(99\%)$ [mm]
-24.76	-17.77

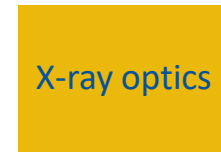




## RESULTS INTERNAL

Individual acceptance magnet	
Rotation $\alpha_{pitch}$ (99%) [°]	Rotation $\alpha_{yaw}$ (99%) [°]
-0.19	-0.13
Deviation $y$ (99%) [mm]	Deviation $x$ (99%) [mm]
-24.76	-17.77

Individual acceptance XMM optics	
Rotation $\alpha_{pitch}$ (99%) [°]	Rotation $\alpha_{yaw}$ (99%) [°]
-0.021	-0.017
Deviation $y$ (99%) [mm]	Deviation $x$ (99%) [mm]
-1.09	-1.02



## RESULTS INTERNAL

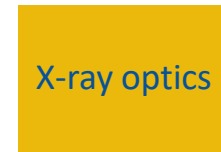
Individual acceptance magnet	
Rotation $\alpha_{pitch}$ (99%) [°]	Rotation $\alpha_{yaw}$ (99%) [°]
-0.19	-0.13
Deviation $y$ (99%) [mm]	Deviation $x$ (99%) [mm]
-24.76	-17.77

Individual acceptance XMM optics	
Rotation $\alpha_{pitch}$ (99%) [°]	Rotation $\alpha_{yaw}$ (99%) [°]
-0.021	-0.017
Deviation $y$ (99%) [mm]	Deviation $x$ (99%) [mm]
-1.09	-1.02

Individual acceptance detector	
$y$ (99%) GridPix window [mm]	$x$ (99%) GridPix window [mm]
-1.04	-1.06
$y$ (99%) Micromegas window [mm]	$x$ (99%) Micromegas window [mm]
-1.22	-1.25



Magnet

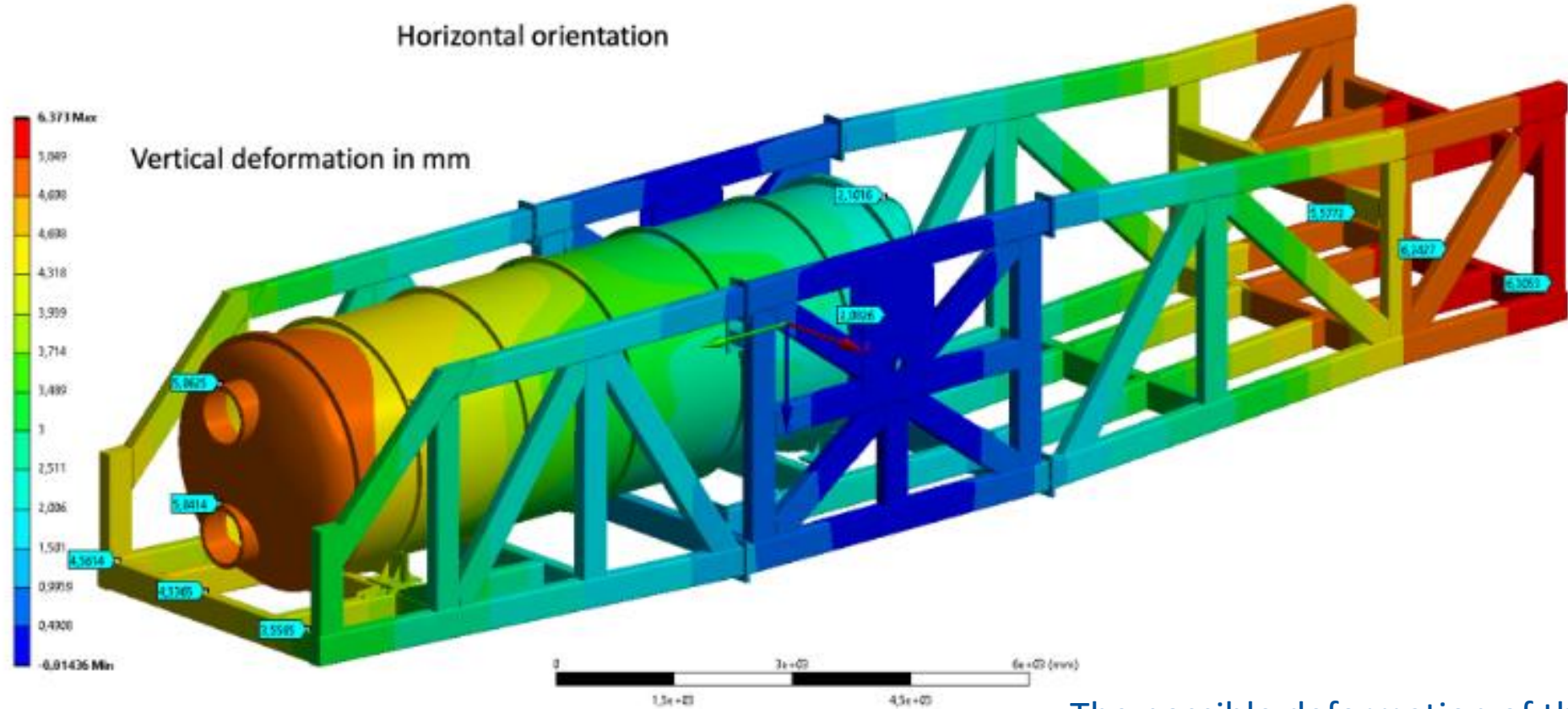


X-ray optics



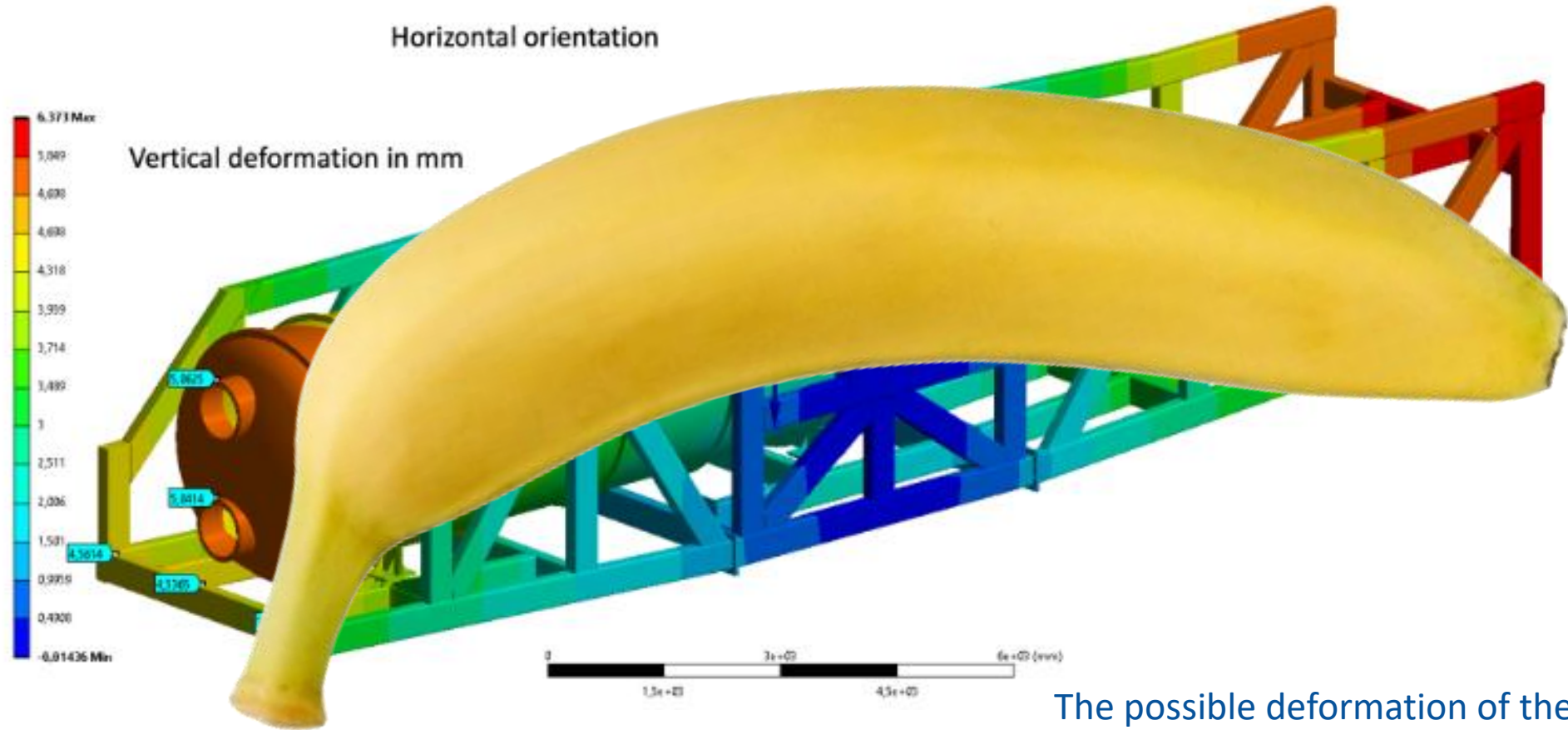
Detector

# POSSIBLE GRAVITATIONAL EFFECTS



The possible deformation of the setup due to gravity at  $0^\circ$

# POSSIBLE GRAVITATIONAL EFFECTS



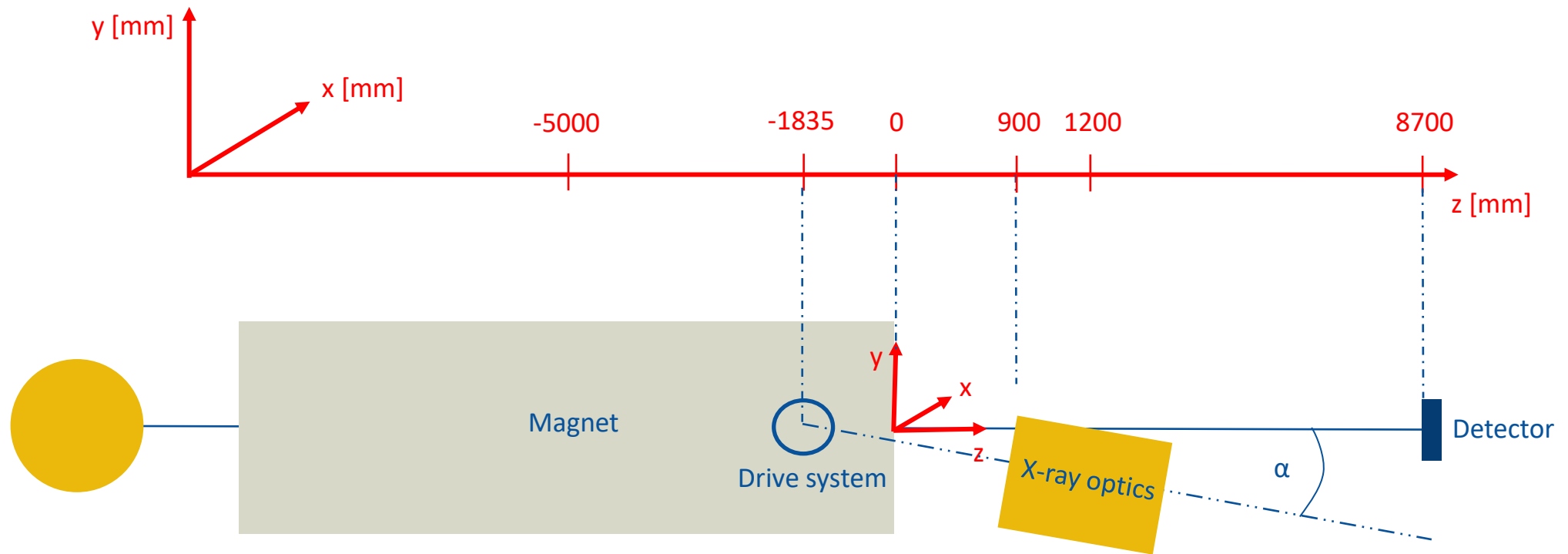
The possible deformation of the setup due to gravity at 0°

## POSSIBLE GRAVITATIONAL EFFECTS

Support Frame Deformations (mm)						
Magnet side						
Tilt	Ansys <sup>a)</sup>	Ansys <sup>b)</sup>	Comsol	RStab	Average	Std Dev
0°	4.5	4.1	3.9	4.9	4.4	0.4
25°	4.6	3.9	3.8	4.9	4.3	0.5
-25°	3.5	3.6	3.3	3.8	3.5	0.2
$\Delta(25 - 0)$	0.1	-0.2	-0.1	0.0	-0.1	0.1
$\Delta(-25 - 0)$	-1.0	-0.5	-0.6	-1.1	-0.8	0.3
Detector side						
Tilt	Ansys <sup>a)</sup>	Ansys <sup>b)</sup>	Comsol	RStab	Average	Std Dev
0°	6.2	6.0	5.9	4.8	5.8	0.1
25°	4.4	5.3	4.3	3.0	4.3	0.4
-25°	6.4	5.6	6.1	5.3	5.9	0.4
$\Delta(25 - 0)$	-1.8	-0.7	-1.6	-1.8	-1.5	0.5
$\Delta(-25 - 0)$	0.2	-0.4	0.2	0.5	0.1	0.3

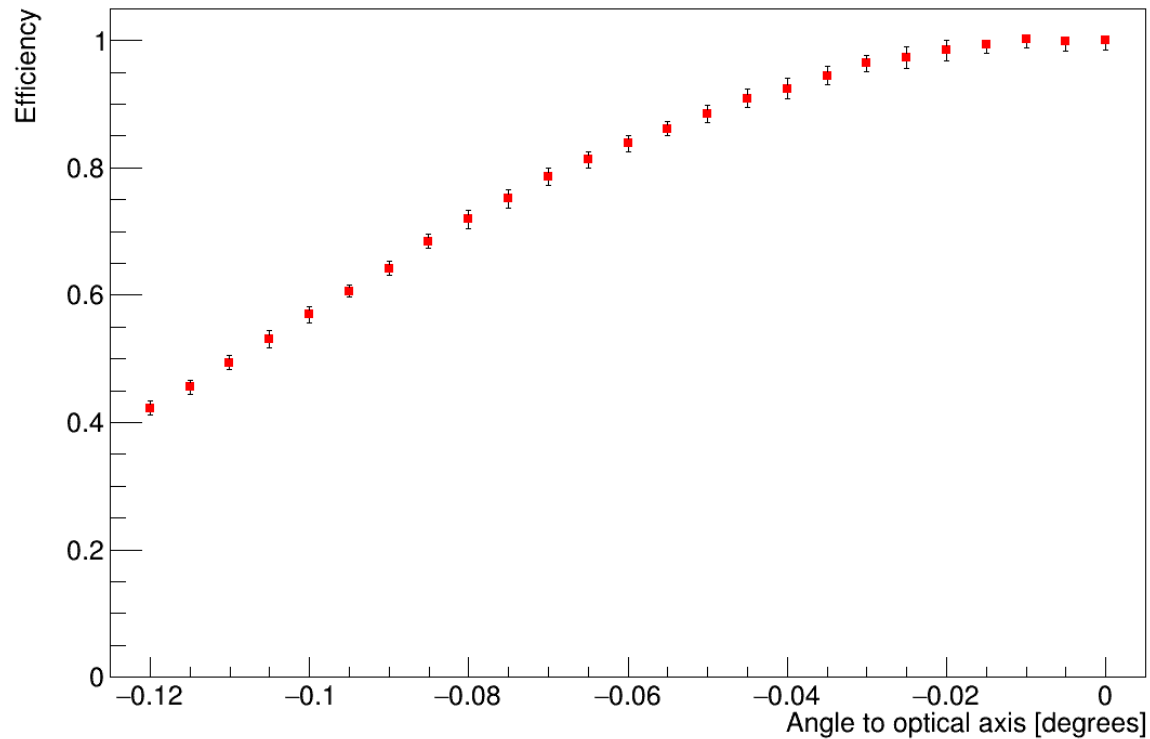
The possible deformation of the setup due to gravity

# DEFORMATION DUE TO GRAVITY ONLY OPTICS

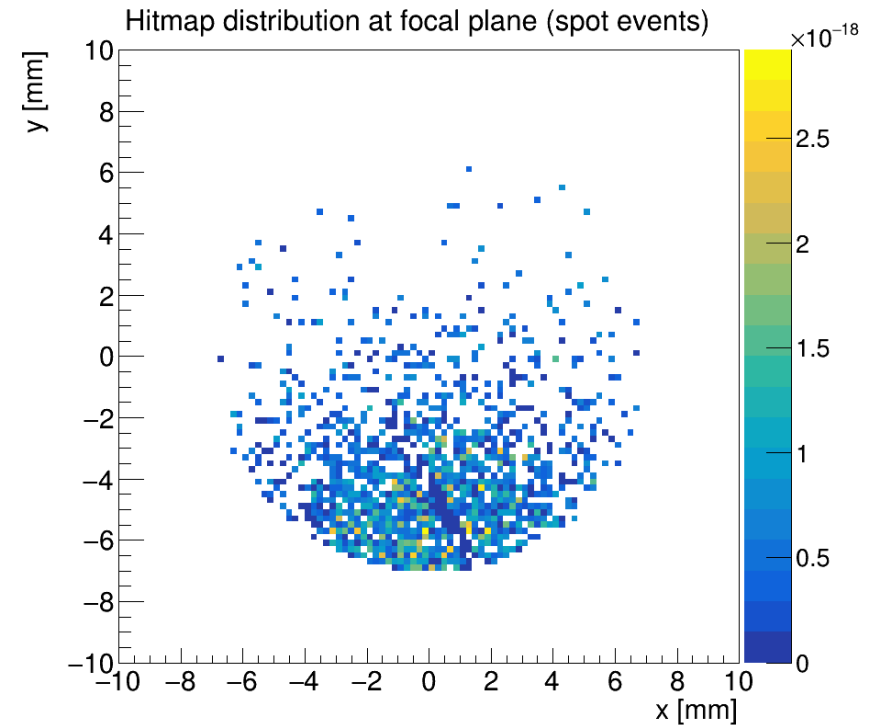


# DEFORMATION DUE TO GRAVITY ONLY OPTICS

Relative Efficiency Comparison

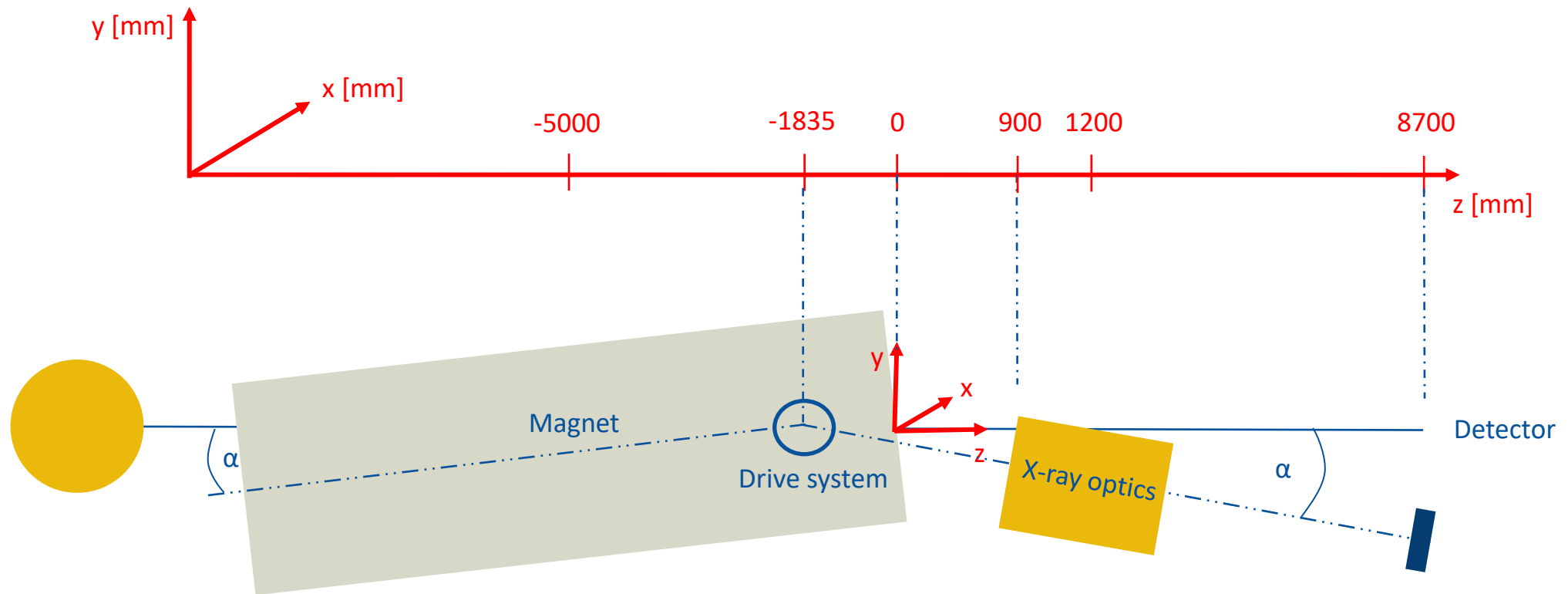


Optics rotation around the systems center



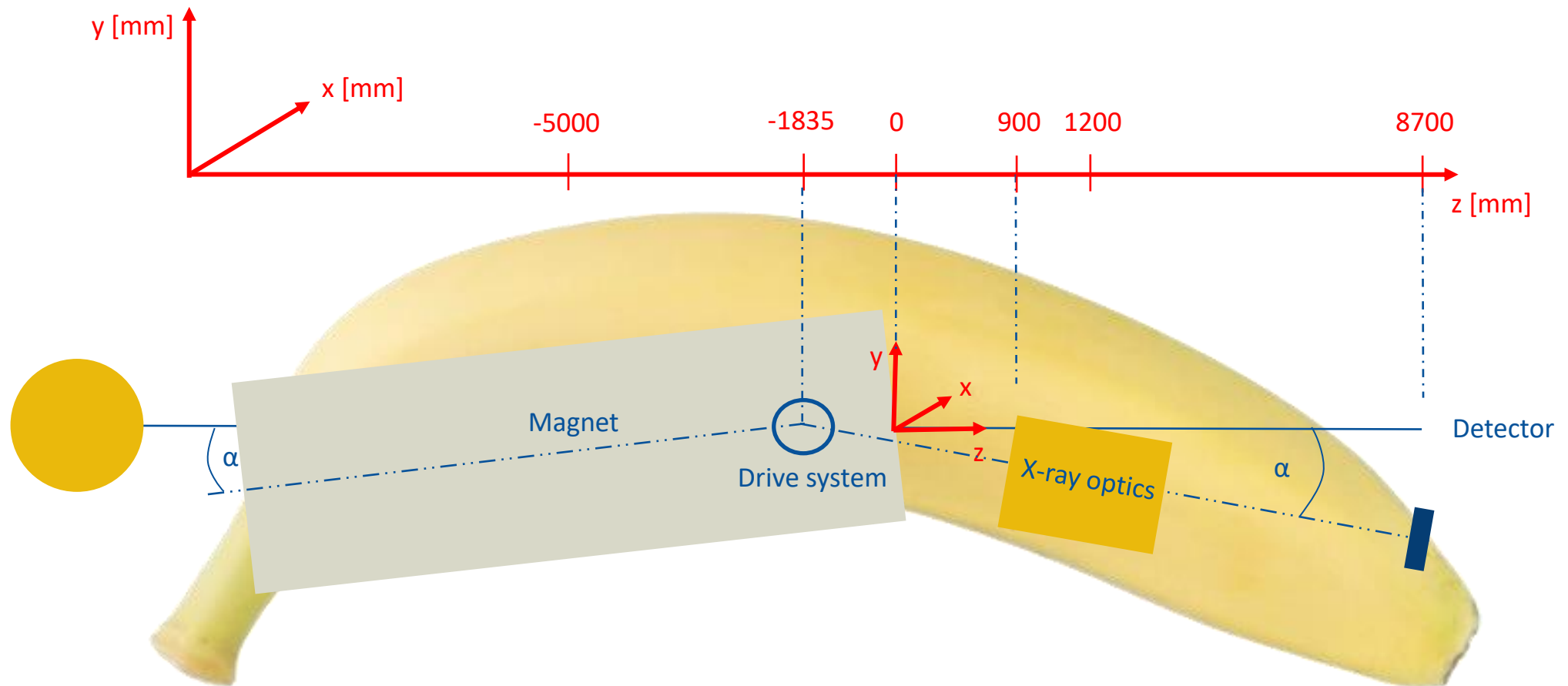
Optics rotation around system center by  $0.12^\circ$

# DEFORMATION DUE TO GRAVITY



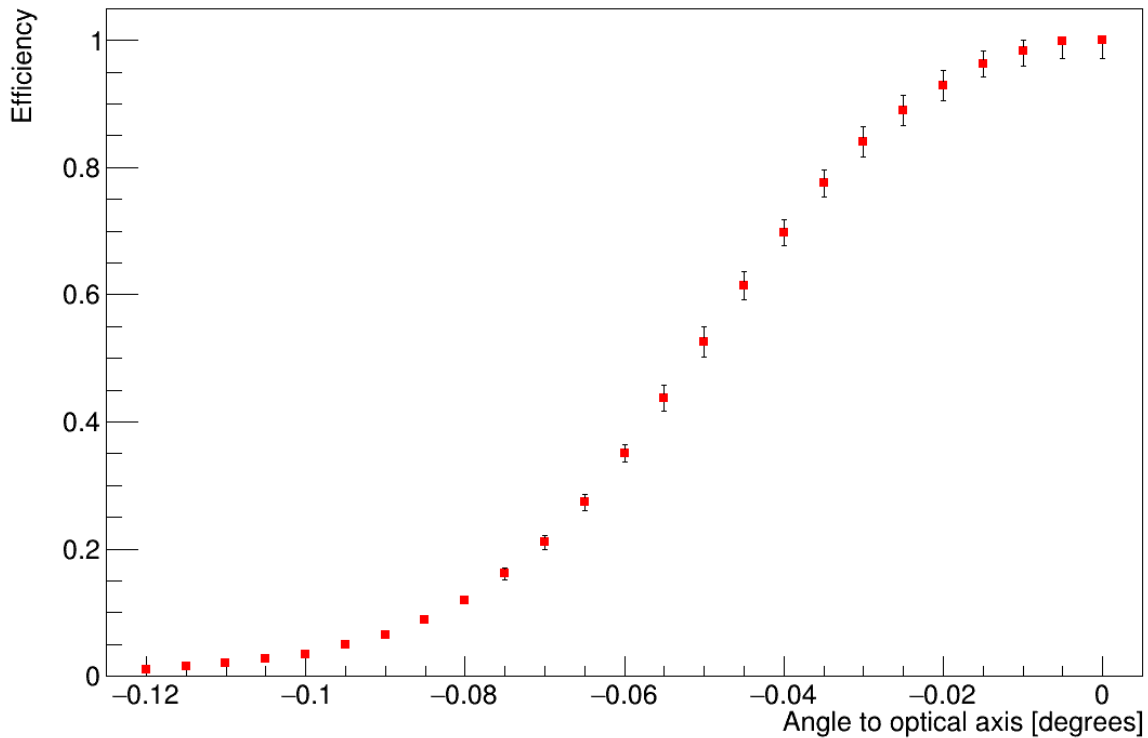


# DEFORMATION DUE TO GRAVITY



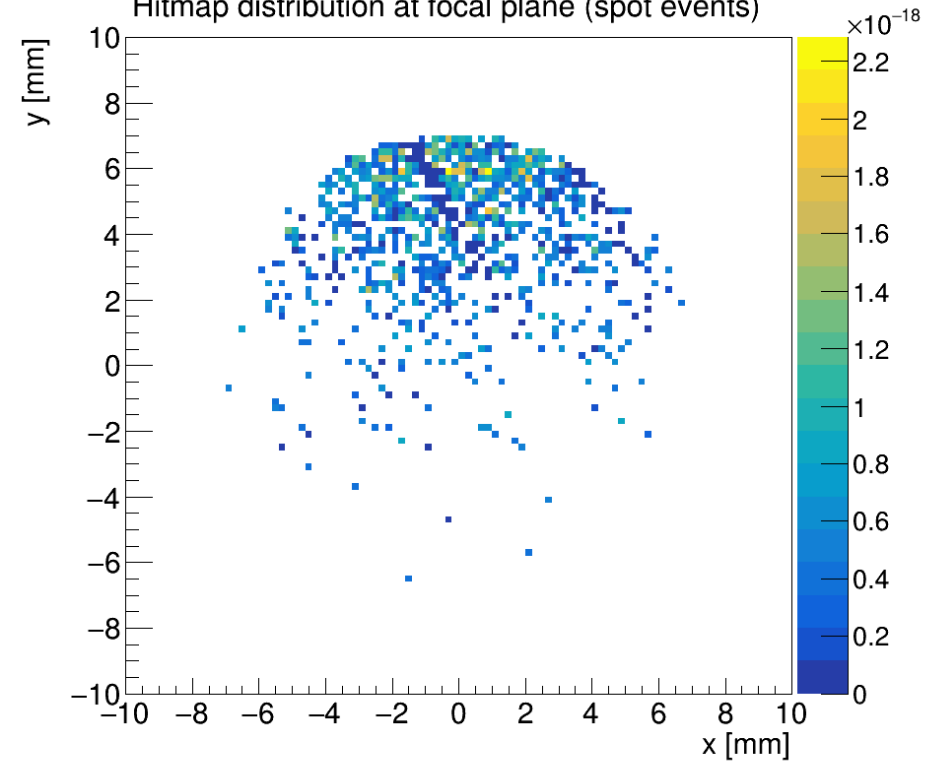
# DEFORMATION DUE TO GRAVITY

Relative Efficiency Comparison



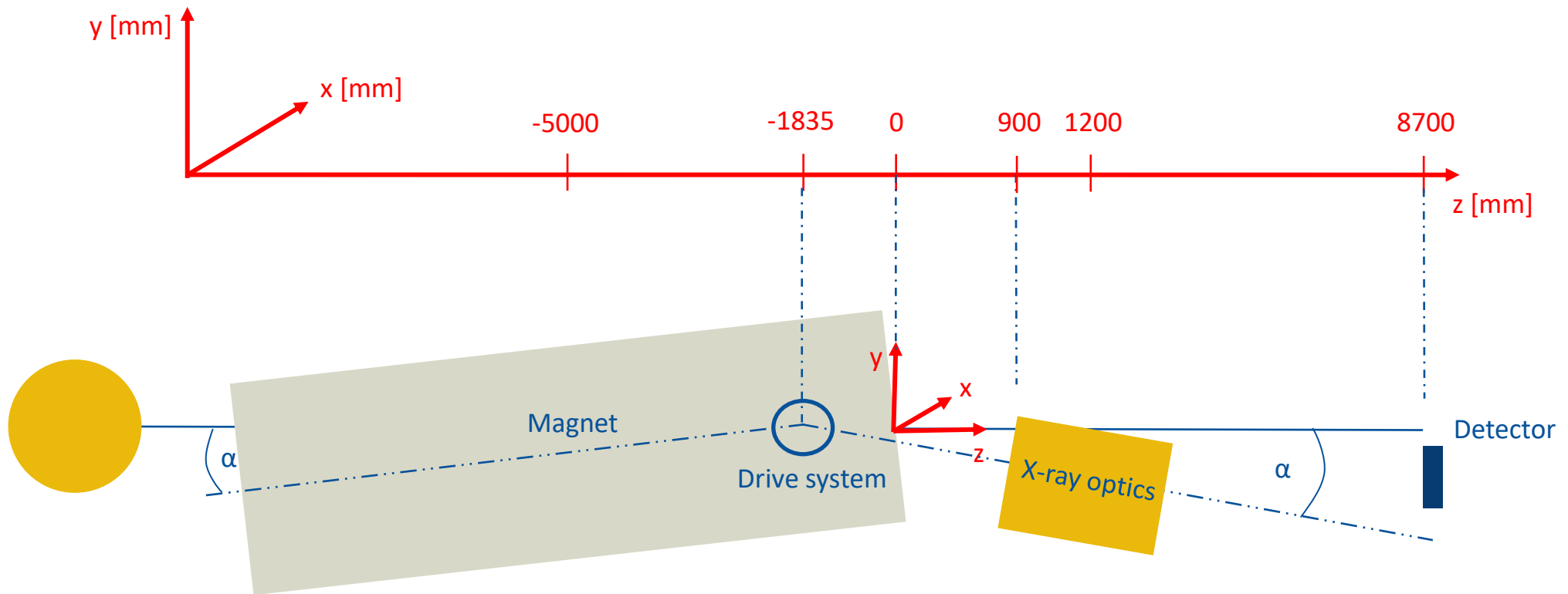
System rotation banana shaped

Hitmap distribution at focal plane (spot events)



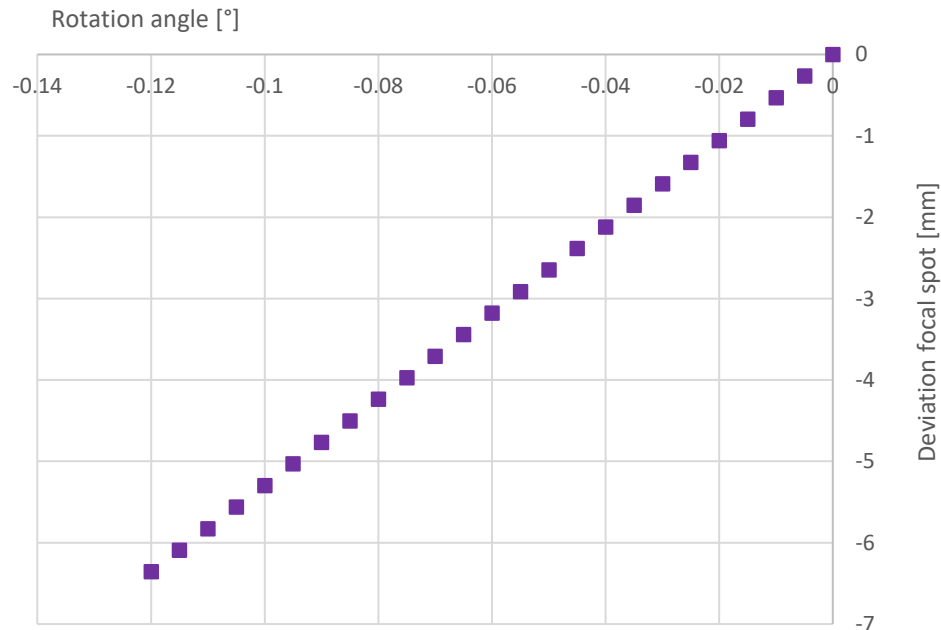
Focal plane distribution of the system rotation by 0.06°

# DEFORMATION DUE TO GRAVITY WITH DETECTOR CORRECTION

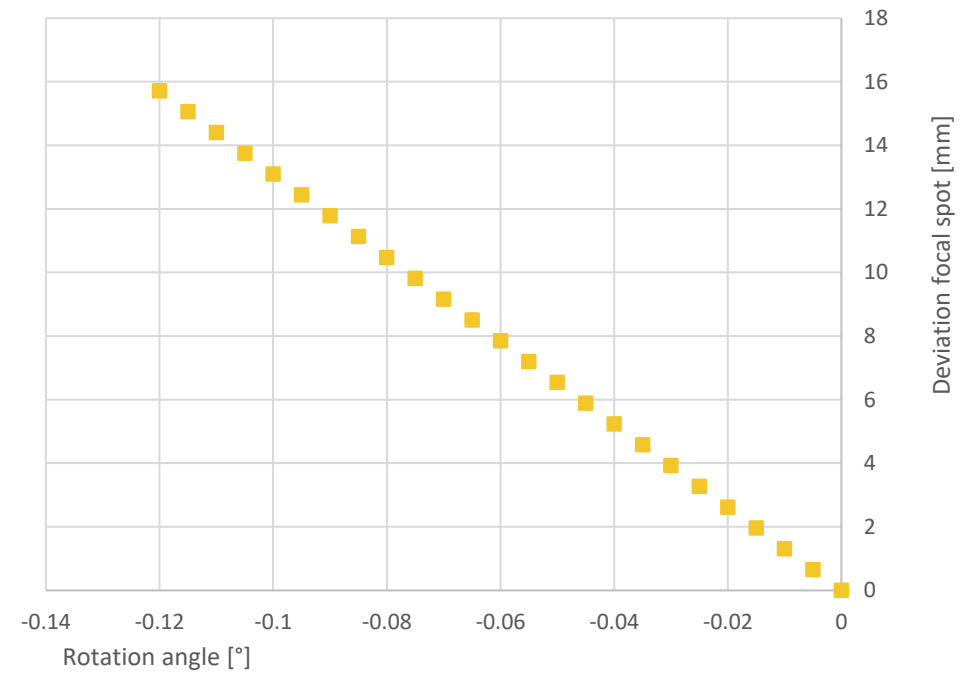


# DEFORMATION DUE TO GRAVITY – DETECTOR CORRECTION

Detector correction from the original position

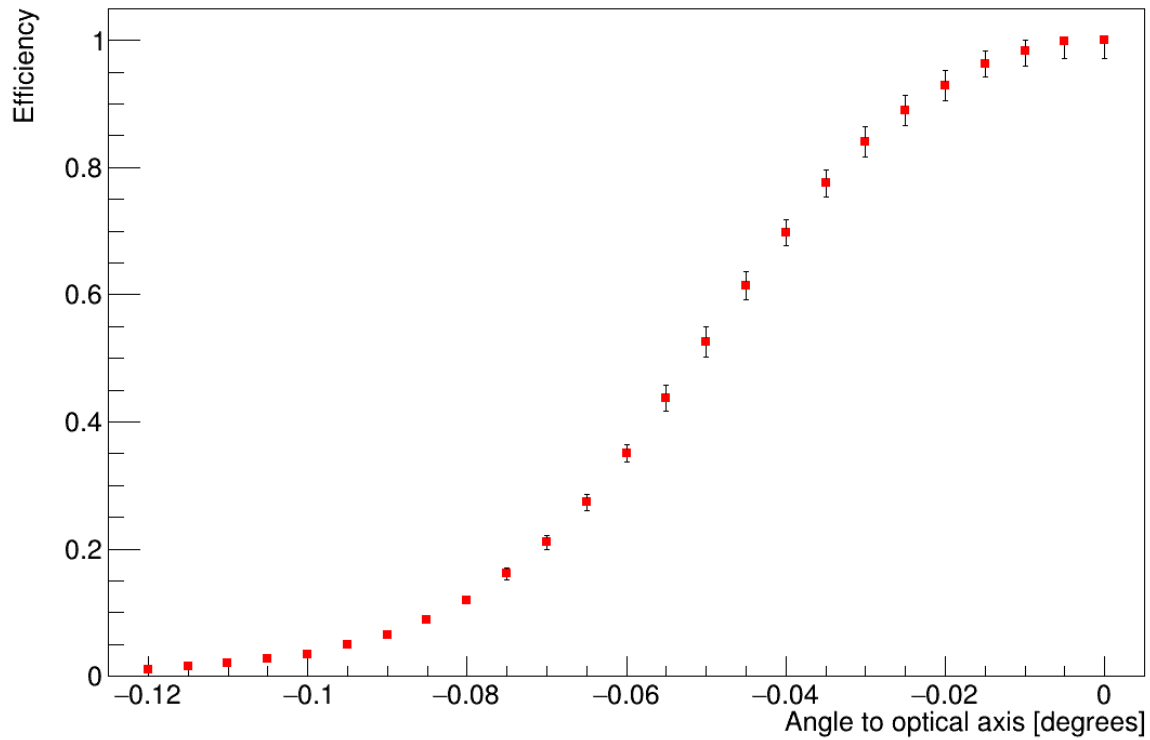


Detector correction from the support structure



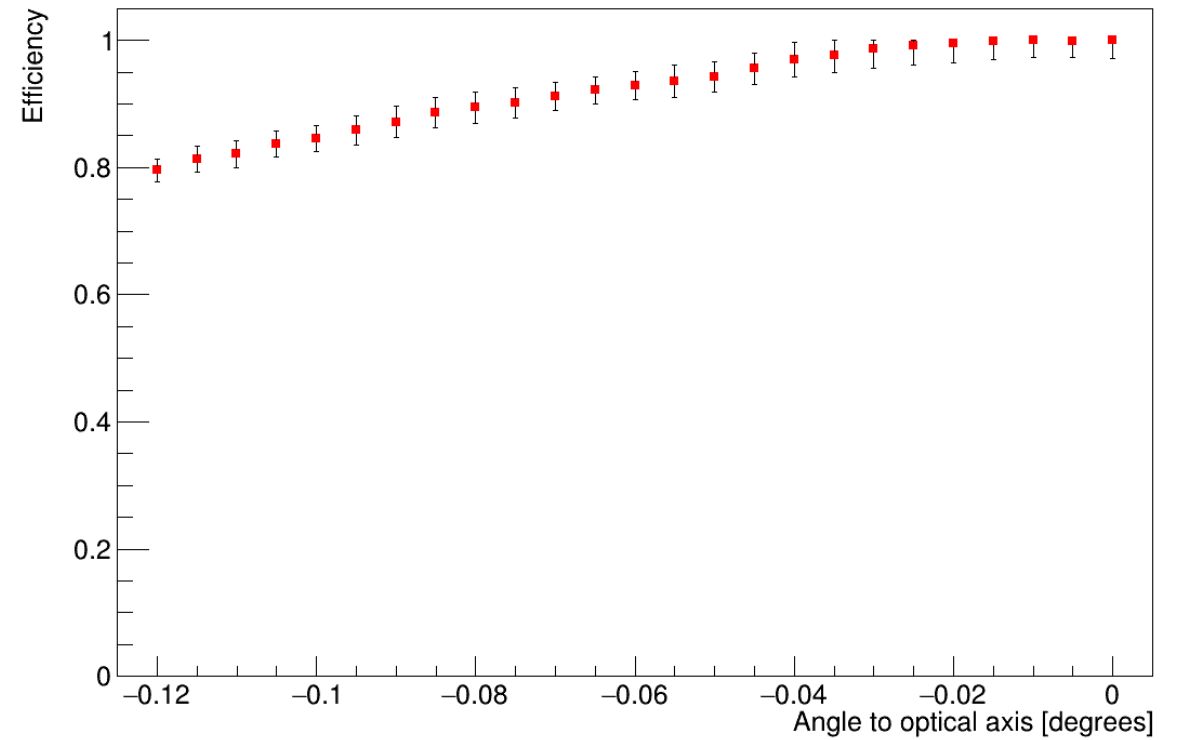
# DEFORMATION DUE TO GRAVITY

Relative Efficiency Comparison



System rotation banana shaped

Relative Efficiency Comparison



System rotation banana shaped corrected detector

# RESULTS DEFORMATION DUE TO GRAVITY

Magnet side				
	Magnet	Magnet and optics	All	Detector corrected
$\alpha(99\%)$ [°]	-0.19	-0.016	-0.01	-0.025
$\Delta y(99\%)$ [mm]	-27.25	-2.23	-1.39	-3.58
$\alpha(95\%)$ [°]	x	-0.035	-0.018	-0.049
$\Delta y(95\%)$ [mm]	x	-4.94	-2.58	-7.00

Detector side				
	XMM optics	Magnet and optics	All	Detector corrected
$\alpha(99\%)$ [°]	-0.0175	-0.016	-0.01	-0.025
$\Delta y(99\%)$ [mm]	-3.22	-2.87	-1.8	-4.61
$\alpha(95\%)$ [°]	x	-0.035	-0.018	-0.049
$\Delta y(95\%)$ [mm]	x	-6.38	-3.33	-9.03

# RESULTS DEFORMATION DUE TO GRAVITY

## Support Frame Deformations (mm)

Magnet side							[mm]
Tilt	Ansysis <sup>a)</sup>	Ansysis <sup>b)</sup>	Comsol	RStab	Average	Std Dev	Detector corrected
0°	4.5	4.1	3.9	4.9	4.4	0.4	-0.025
25°	4.6	3.9	3.8	4.9	4.3	0.5	-3.58
-25°	3.5	3.6	3.3	3.8	3.5	0.2	-0.049
$\Delta(25 - 0)$	0.1	-0.2	-0.1	0.0	-0.1	0.1	-7.00
$\Delta(-25 - 0)$	-1.0	-0.5	-0.6	-1.1	-0.8	0.3	

Detector side							[mm]
Tilt	Ansysis <sup>a)</sup>	Ansysis <sup>b)</sup>	Comsol	RStab	Average	Std Dev	Detector corrected
0°	6.2	6.0	5.9	4.8	5.8	0.1	-0.025
25°	4.4	5.3	4.3	3.0	4.3	0.4	-4.61
-25°	6.4	5.6	6.1	5.3	5.9	0.4	-0.049
$\Delta(25 - 0)$	-1.8	-0.7	-1.6	-1.8	-1.5	0.5	-9.03
$\Delta(-25 - 0)$	0.2	-0.4	0.2	0.5	0.1	0.3	

# REST RAYTRACER COLLABORATION

Solar axion flux  
implemented by:  
Sebastian Hoof  
Lennert Thormahlen  
Maurizio Gianotti

Solar flux:  
<https://github.com/sebhoof/SolarAxionFlux>

Magnetic field  
implemeted by:  
Kresimir Jakovcic  
Nikolay Bikovskiy



Ray tracer

<https://github.com/rest-for-physics/axionlib>

X-ray optics  
implemented by:  
Javier Galán  
Johanna von Oy

Detector windows and  
masks implemented  
by:  
Javier Galán  
Johanna von Oy



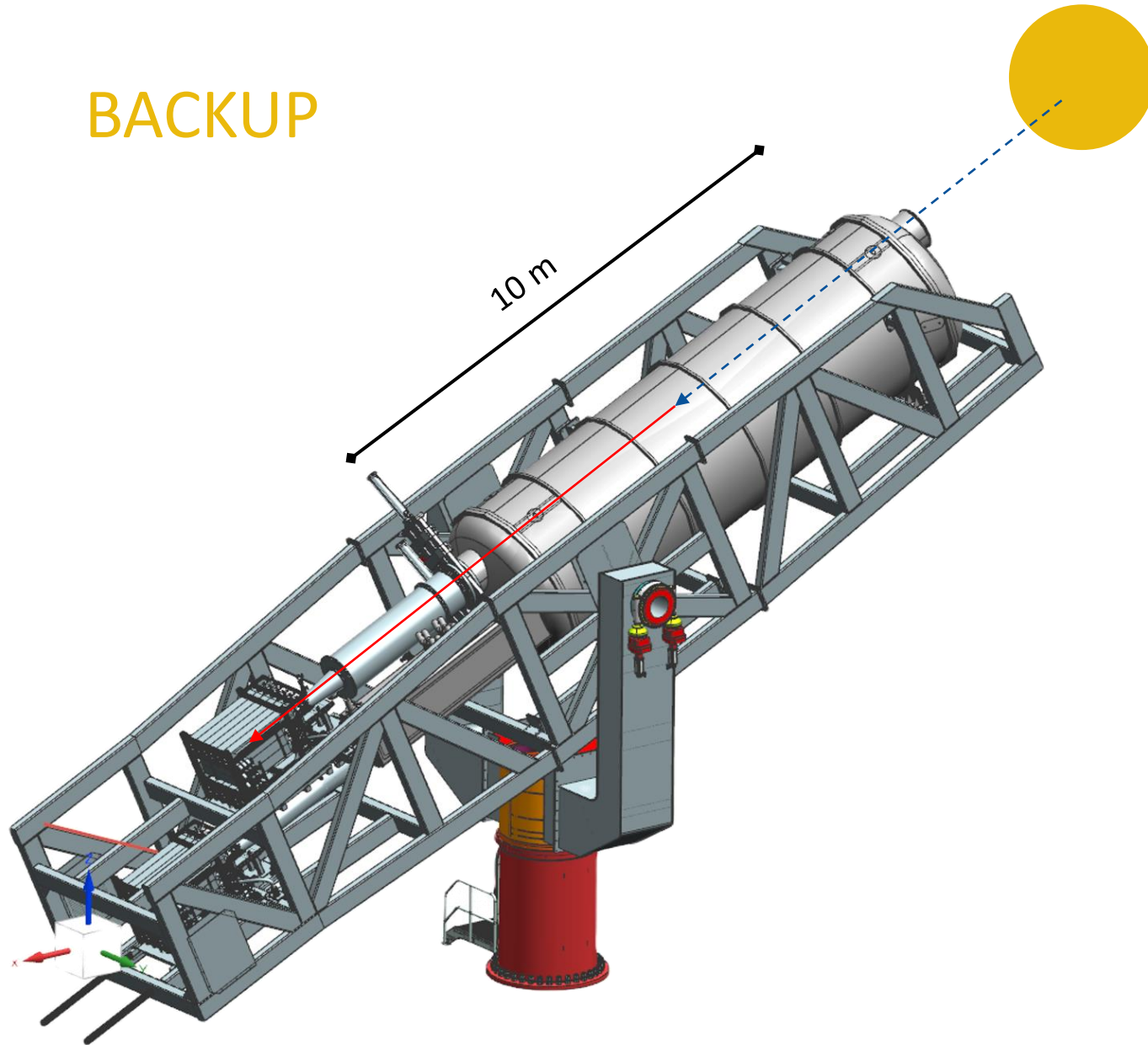
# SUMMARY

BabyIAXO simulated by the REST ray tracer:

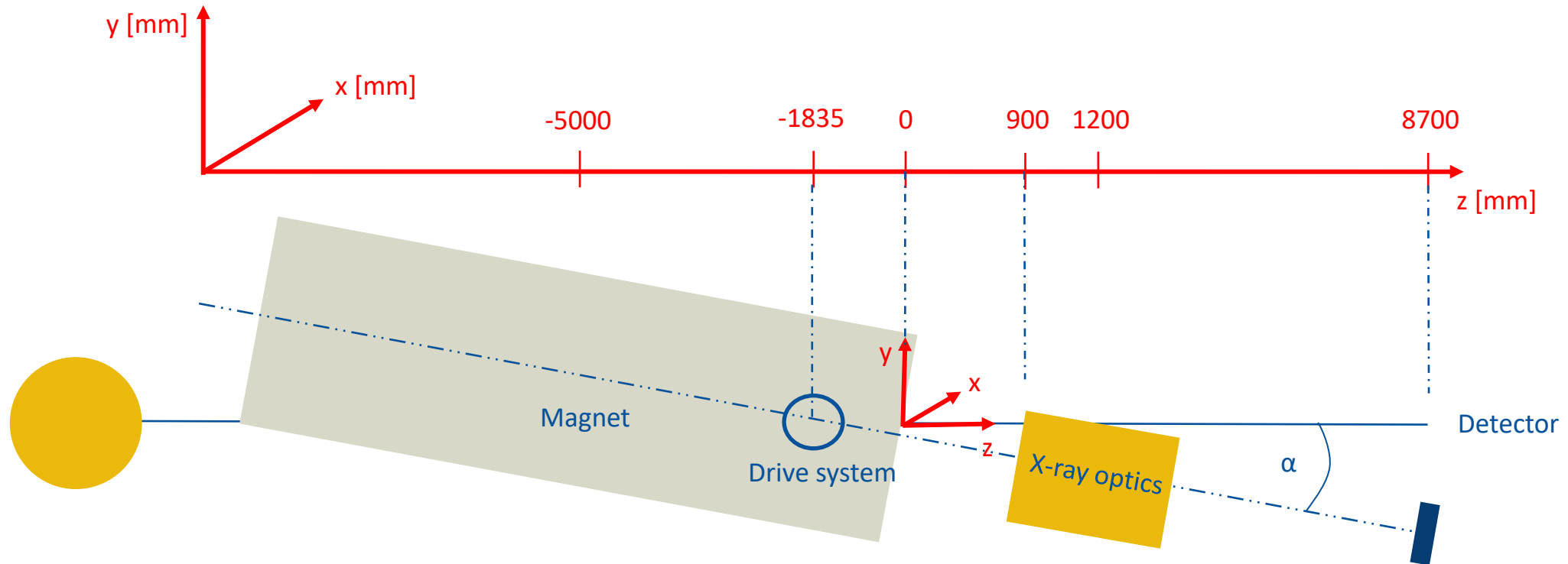
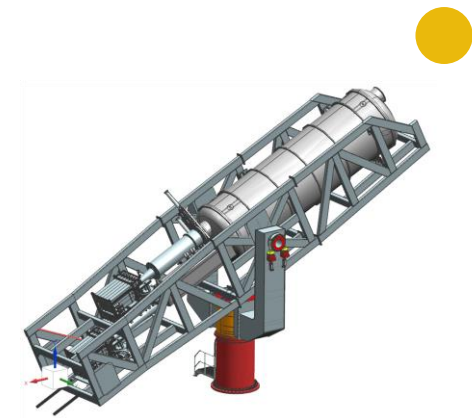
- Overview of acceptances of individual components: magnet, optics, detector
- Simulation of worst-case scenario due to gravitational effects
- Solution through detector movement



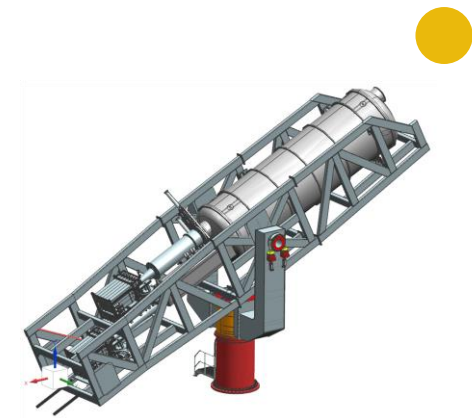
# BACKUP



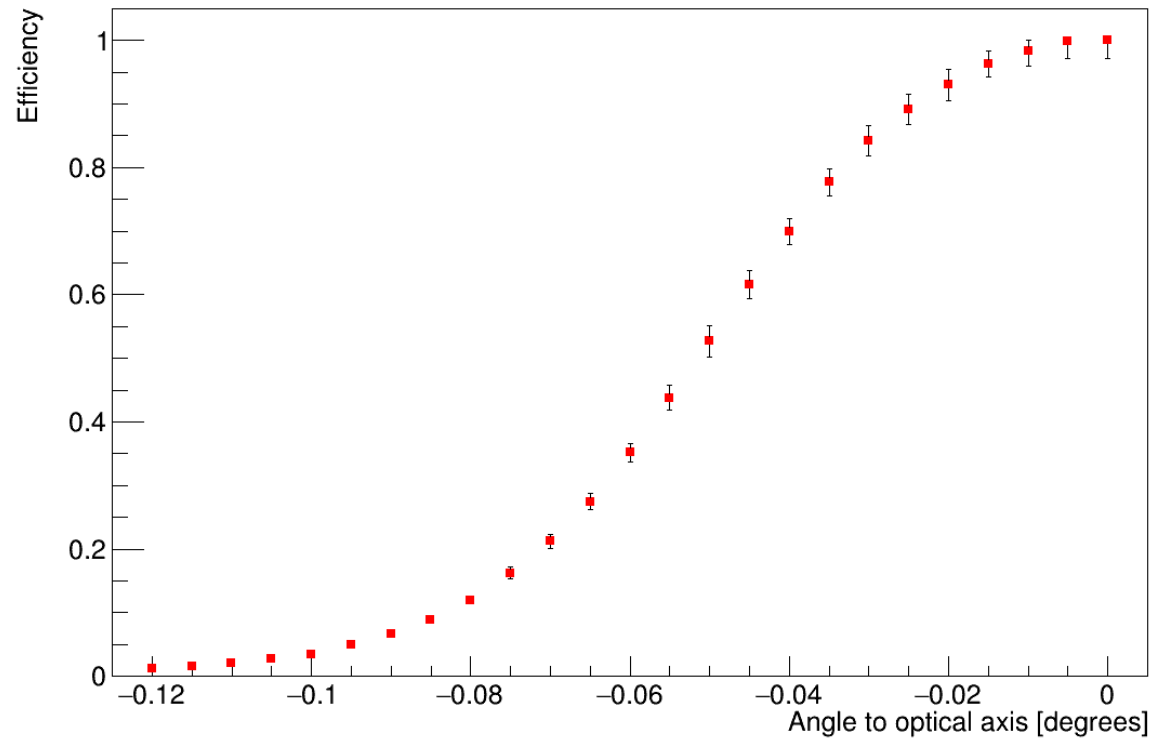
# OVER ROTATION



# OVER ROTATION

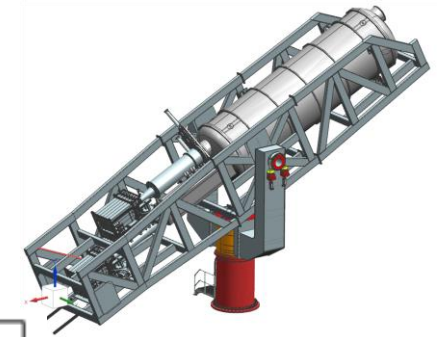


Relative Efficiency Comparison



System rotation downwards

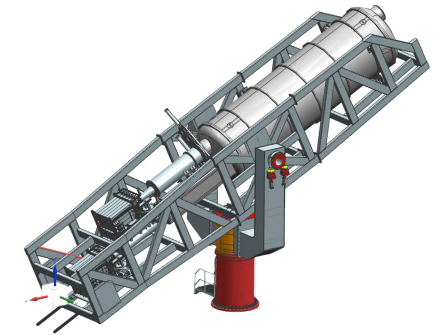
# RESULTS DEFORMATION DUE TO GRAVITY



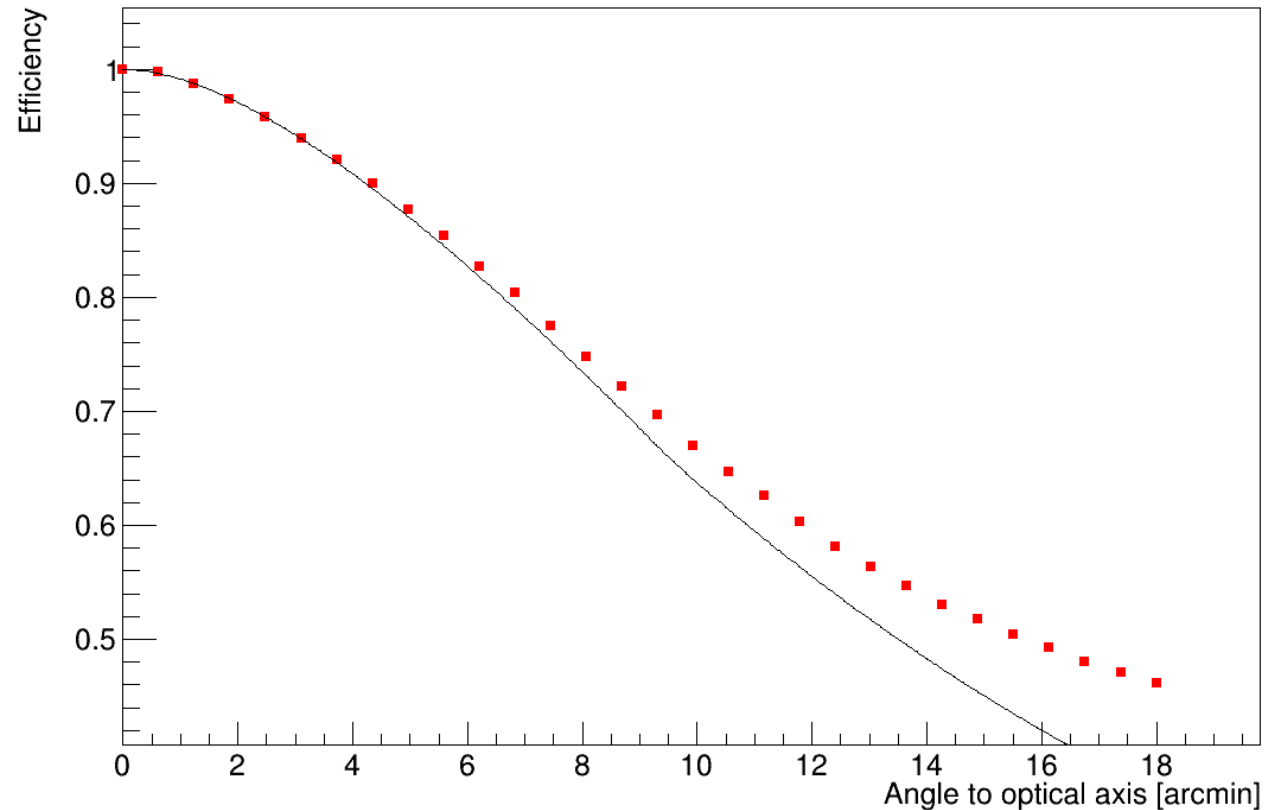
Magnet side				
	Magnet	Magnet and optics	All	Detector corrected
$\alpha(99\%)$ [°]	-0.19	-0.016	-0.01	-0.025
$\Delta y(99\%)$ [mm]	-27.25	-2.23	-1.39	-3.58
$\alpha(95\%)$ [°]	x	-0.035	-0.018	-0.049
$\Delta y(95\%)$ [mm]	x	-4.94	-2.58	-7.00

Detector side				
	XMM optics	Magnet and optics	All	Detector corrected
$\alpha(99\%)$ [°]	-0.0175	-0.016	-0.01	-0.025
$\Delta y(99\%)$ [mm]	-3.22	-2.87	-1.8	-4.61
$\alpha(95\%)$ [°]	x	-0.035	-0.018	-0.049
$\Delta y(95\%)$ [mm]	x	-6.38	-3.33	-9.03

# EFFICIENCY OF THE XMM AT 0.03 KEV

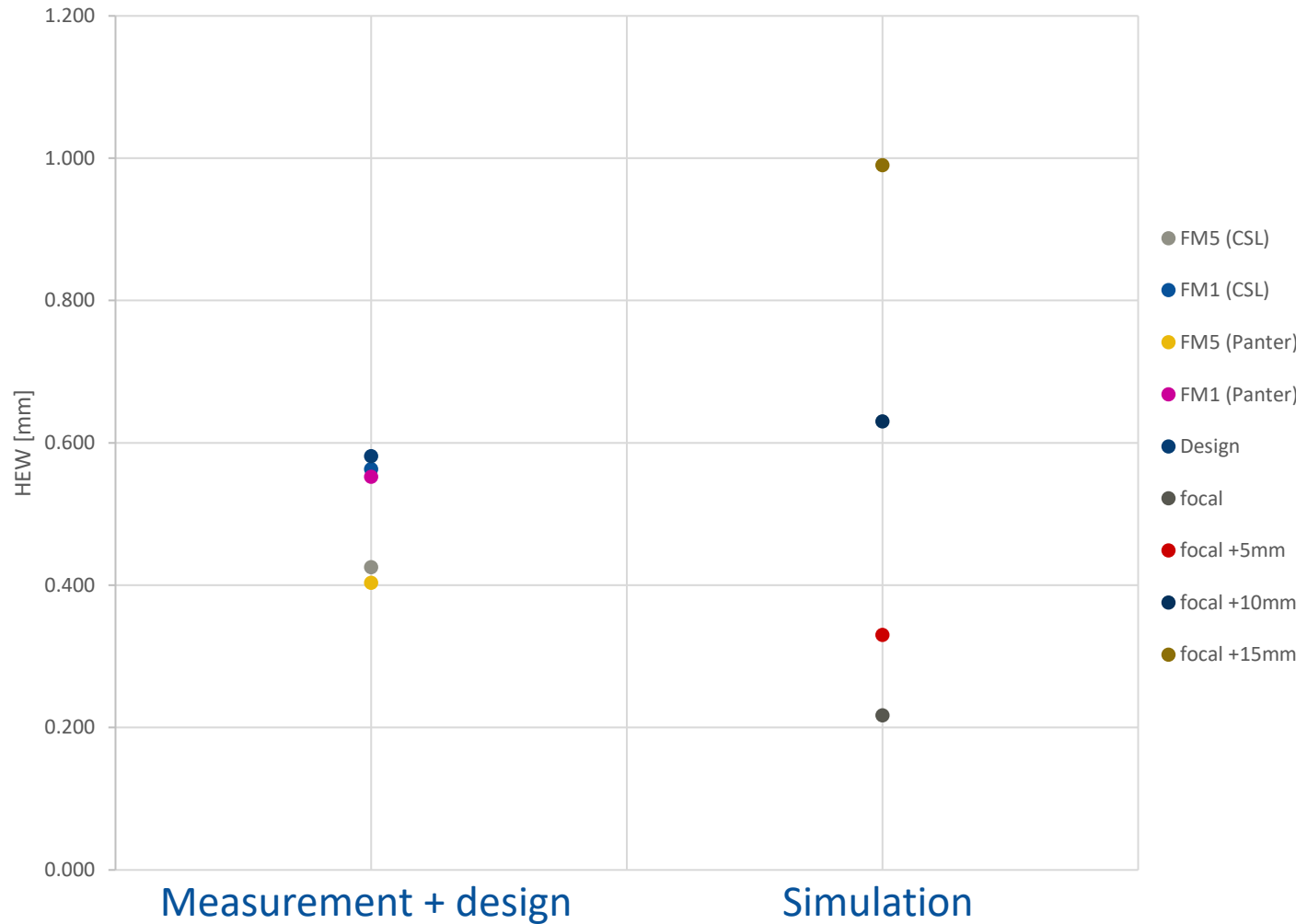
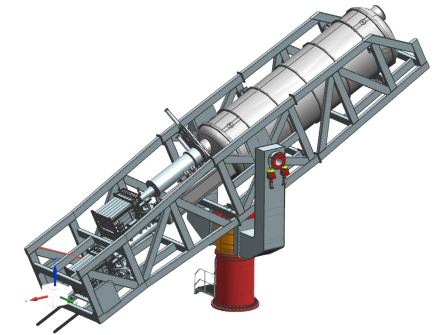


## Geometrical Acceptance



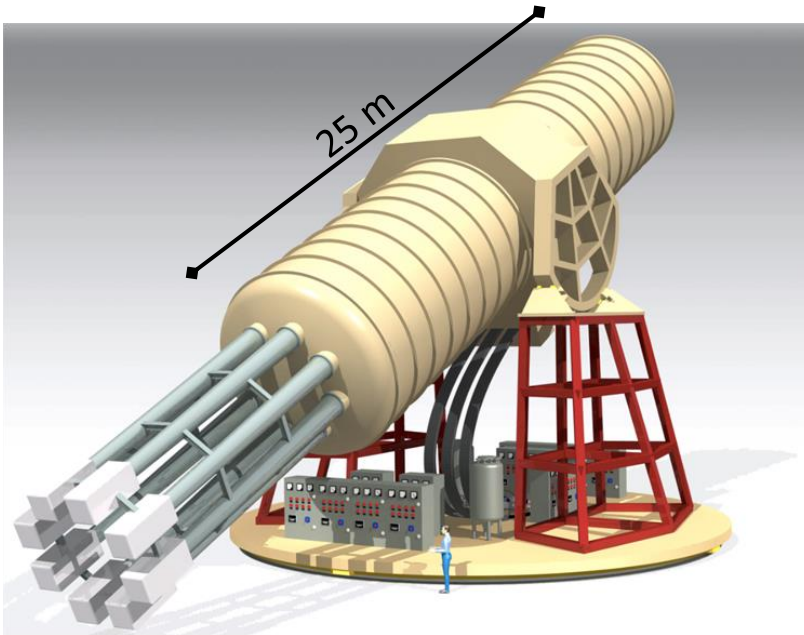
- Off axis test with an EUV source at Centre Spatial de Liège (CSL) in 1998 (black line)
- Rotation of the XMM optics in the ray tracer at 0.03 keV (red dots)

# HEW: EXPERIMENT VS SIMULATION



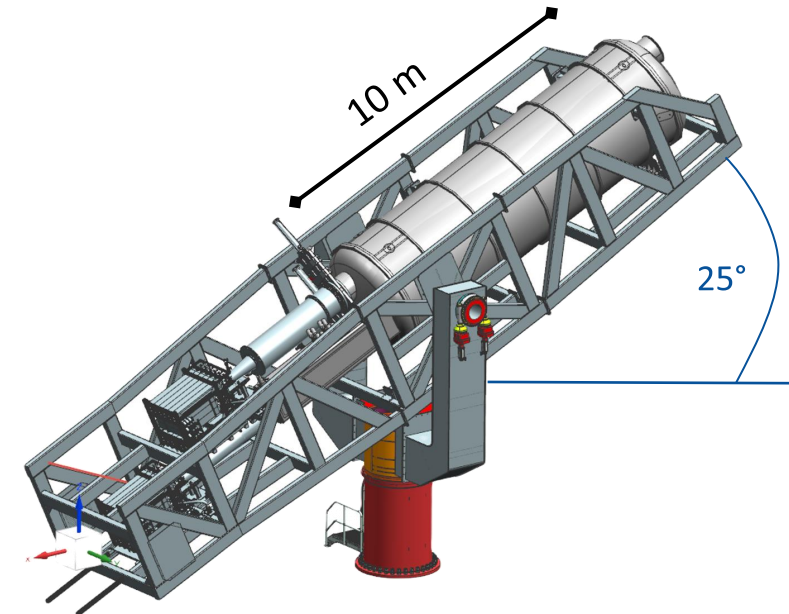
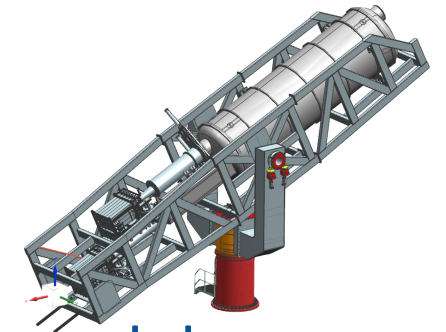
- HEW: Diameter of a circle that includes half of the signal information
- Experimental data from CSL and Panter in the 90s

## IAXO VS. BABXIAXO



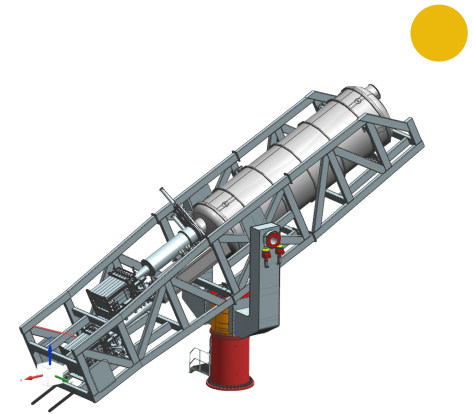
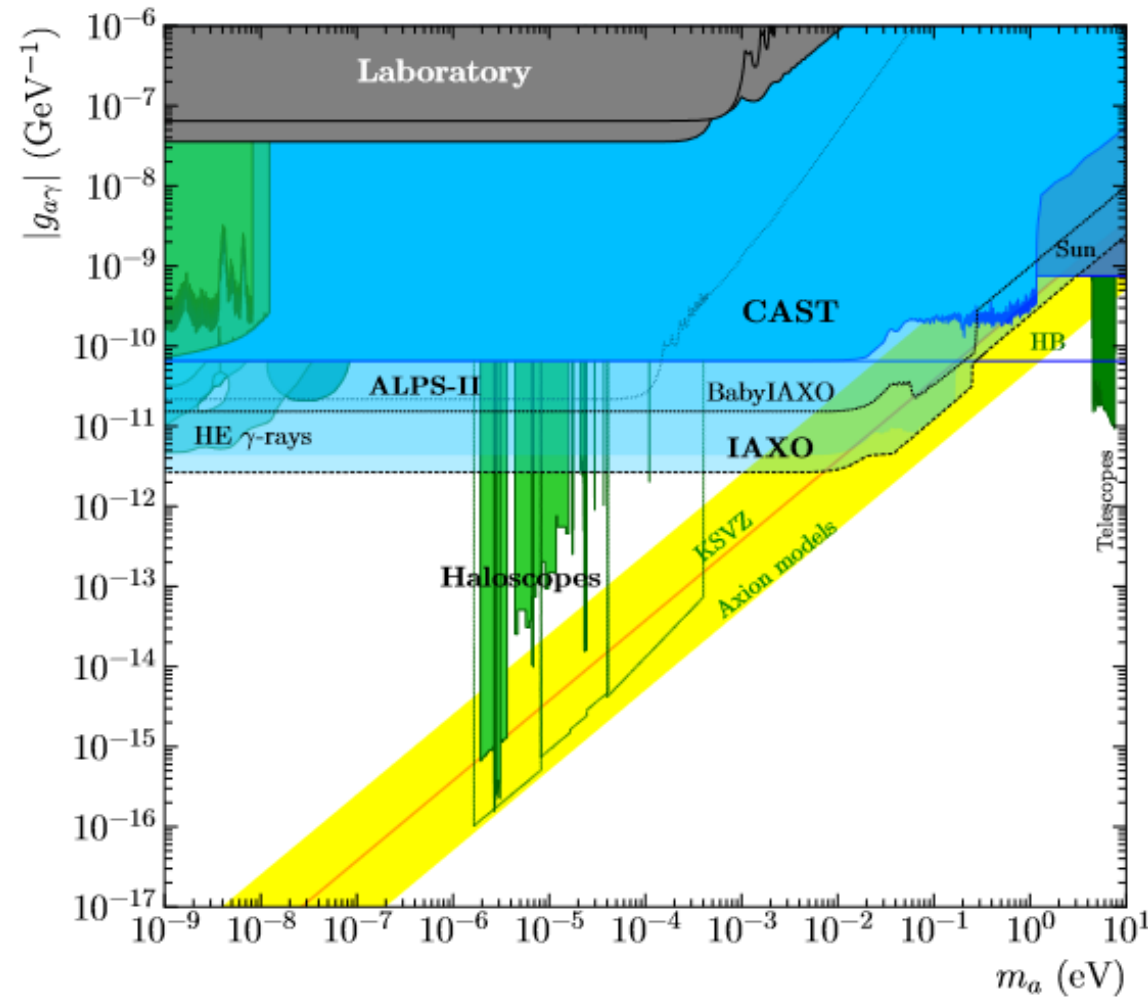
- 25m long magnet
- 8 bores with optics and detectors
- Peak magnetic field of 5.4 T

- 10m long magnet
- 2 bores with optics and detectors
- Peak magnetic field of 3.2 T





# IAXO VS. BABYIAXO



IAXO collaboration 2020, arXiv:2010.12076

# RESULTS PERFECT ALIGNMENT

- Run with 100 000 events
- Solar flux: Primakoff
- Vacuum stage
- Optics: XMM optics
- GridPix window
- Results here done with REST v2.3.1!

