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Baruch MEERSON - Fluctuations of “Brownian bees” and of some other interacting particle systems with reset

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The “Brownian bees” model, suggested by J. Berestycki, E. Brunet, J. Nolen, and S. Penington, is a new member of a family of Brunet-Derrida particle systems which mimic some aspects of biological selection. Like other Brunet-Derrida systems, the Brownian bees can be also considered as a system of interacting particles with reset. The model describes an ensemble of N independent branching Brownian particles. When a particle branches into two particles, the particle farthest from the origin is eliminated so as to keep the number of particles constant. In the limit of $N \rightarrow \infty$, the coarse-grained particle density is governed by the solution of a free boundary problem for a simple reaction-diffusion equation. At long times the particle density approaches a spherically symmetric steady-state solution with a compact support. We studied fluctuations of the “swarm of bees” due to the random character of the branching Brownian motion in the limit of large but finite N , and we focused on the fluctuations of the swarm radius $l(t)$ in 1d [1]. We found that the autocorrelation function of $l(t)$ in the steady state, $g(\tau)$, exhibits a logarithmic scaling with $\tau=t_1-t_2$, which corresponds to a $1/f$ noise in the frequency domain. The variance of $l(t)$ exhibits an anomalous scaling $(1/N) \ln N$ with N . These anomalies appear because a broad range of spatial scales contribute to the fluctuations. I will also briefly consider another model - an N -particle system with reset of the farthest particle to the origin [2] - which shares these anomalies.

[1] M. Siboni, P. Sasorov and B. Meerson, Fluctuations of a swarm of Brownian bees. Phys. Rev. E 104, 054131 (2021).

[2] O. Vilik, M. Assaf and B. Meerson, Fluctuations and first-passage properties of systems of Brownian particles with reset. Phys. Rev. E 106, 024117 (2022).

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