New elements on the search for high frequency gravitational waves with haloscopes (resonant cavities)

Based on arXiv:2303.06006

With Aurélien Barrau (LPSC), Juan Garcia Bellido (IFT) and Thierry Grenet (Néel institute).

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High frequency gravitational waves



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High frequency gravitational waves



Review paper: N. Aggarwal et. al., arXiv:2011.12414

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What is a haloscope?

Haloscope: experiment searching for axion dark matter in our galactic halo

Axion DM behaves like a classical oscillating field



Credits: Raphael Cervantes, University of Washington



Credits: https://cajohare.github.io/AxionLimits/

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Different possible configurations Field RF-cavity dia. Warm dia. Frequency GrAHal 43 T 34 mm 20 mm 11.5 GHz For this study: 50 mm 6.76 GHz 40 T 34 mm GrAHal platform taken 27 T 170 mm 86 mm 2.67 GHz as a benchmark 375 mm 0.79 GHz 17.5 T 291 mm Grenoble Axion Haloscopes 675 mm 9.5 T 800 mm 0.34 GHz Ideal for a haloscope T. Grenet et. al., arXiv:2110.14406

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Axion electrodynamics

•
$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}^2 - A_{\mu}J^{\mu} + \frac{1}{2}(\partial_{\mu}a\partial^{\mu}a - m^2a^2) + \frac{g_{a\gamma\gamma}}{4}aF_{\mu\nu}\tilde{F}^{\mu\nu}$$
 Axion-photons
coupling
• $\partial_{\mu}F^{\mu\nu} = J^{\nu} + g_{a\gamma\gamma}(\partial_{\mu}a)\tilde{F}^{\mu\nu} \longrightarrow \vec{\nabla} \times \vec{B} = \frac{\partial \vec{E}}{\partial t} + \vec{j} - g_{a\gamma\gamma}\left(\vec{B}\frac{\partial a}{\partial t} + \vec{\nabla}a \times \vec{E}\right)$ (Maxwell-Ampère)
Generated current: $\vec{j}_a = -g_{a\gamma\gamma}\left(\vec{B}\frac{\partial a}{\partial t} + \vec{\nabla}a \times \vec{E}\right)$ Current aligned along \vec{B}

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• Power extracted from the cavity:
$$P_{signal} \propto g_{a\gamma\gamma}^2 B^2 Q V \frac{\rho_a}{m_a} \sim 10^{-22} \,\mathrm{W} \longrightarrow \mathrm{To} \text{ be amplified!}$$

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• Noise: $P_{noise} \propto T_{sys}$

4 key ingredients for a good haloscope: High magnetic fields Good cavity (high QV) Good amplifiers Low temperatures

Axion electrodynamics

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4 key ingredients
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Low temperatures

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GW electrodynamics

Einstein-Maxwell action:

$$S_{EM} = \int d^4x \sqrt{-g} \left(-\frac{1}{4} g^{\mu\alpha} g^{\nu\beta} F_{\mu\nu} F_{\alpha\beta} \right)$$

 $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu} , \ |h_{\mu\nu}| \ll 1$

$$S_{EM} = -\frac{1}{4} \int d^4x \sqrt{-g} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2} \int d^4x \partial_\nu \left[\frac{\tilde{h}}{2} F^{\mu\nu} + h^{\nu}_{\alpha} F^{\alpha\mu} - h^{\mu}_{\alpha} F^{\alpha\nu} \right] A_{\mu} + \mathcal{O}\left(h^2\right)$$

Effective current:
$$j_{\text{eff}}^{\mu} = \partial_{\nu} \left(\frac{\tilde{h}}{2} F^{\mu\nu} + h_{\alpha}^{\nu} F^{\alpha\mu} - h_{\alpha}^{\mu} F^{\alpha\nu} \right)$$

Result from Berlin, Blas et. al., arXiv:2112.11465



Current dependent to the GW direction of propagation

 \neq Axionic current!

• <u>GW signal extracted from the cavity</u>

Result from Berlin et. al., arXiv:2112.11465

$$P_{\text{sign,GW}} = \frac{1}{2} Q \omega_g^3 V_{\text{cav}}^{5/3} \left(\eta_n h_0 B_0\right)^2$$

Coupling coefficient between the effective current and the cavity modes

$$\eta_n \equiv \frac{\left|\int_{V_{\text{cav}}} d^3 \vec{x} \vec{E}_n^{\star} \cdot \hat{j}_{+,\times}\right|}{V_{\text{cav}}^{1/2} \left(\int_{V_{\text{cav}}} d^3 \vec{x} |\vec{E}_n|^2\right)^{1/2}}$$



Signal to Noise ratio estimated by the radiometer equation:

$$\mathrm{SNR} \simeq \frac{P_{\mathrm{sig}}}{k_B T_{\mathrm{sys}}} \sqrt{\frac{t_{\mathrm{eff}}}{\Delta \nu}}$$

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• Focus on binary systems of (light) black holes A. Barrau, J.G. Bellido, T. Grenet, K. M, arXiv:2303.06006

> Working at fixed frequency (~ GHz) does not fix the masses!



 ν : resonant frequency of the detector

 τ : time to merger





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$$SNR \simeq \frac{P_{sig}}{k_B T_{sys}} \sqrt{\frac{t_{eff}}{\Delta \nu}} + P_{sign,GW} = \frac{1}{2} Q \omega_g^3 V_{cav}^{5/3} \left(\eta_n h_0 B_0\right)^2$$

 $SNR > 1 \Rightarrow$ Sensitivity estimates:

Grenoble Axion Haloscopes

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$$h > 4.7 \times 10^{-22} \times \left(\frac{0.34 \text{ GHz}}{\nu}\right)^{\frac{5}{4}} \left(\frac{0.1}{\eta}\right) \left(\frac{9 \text{ T}}{B_0}\right) \left(\frac{5.01 \times 10^{-1} \text{ m}^3}{V_{\text{cav}}}\right)^{\frac{5}{6}} \left(\frac{10^5}{Q}\right)^{\frac{3}{4}} \left(\frac{T_{\text{sys}}}{0.3 \text{ K}}\right)^{\frac{1}{2}} \left(\frac{1 \text{ s}}{t_{\text{eff}}}\right)^{\frac{1}{4}}$$

$$\Leftrightarrow h > 1.5 \times 10^{-21} \times \left(\frac{2.67 \text{ GHz}}{\nu}\right)^{\frac{5}{4}} \left(\frac{0.1}{\eta}\right) \left(\frac{27 \text{ T}}{B_0}\right) \left(\frac{1.83 \times 10^{-3} \text{ m}^3}{V_{\text{cav}}}\right)^{\frac{5}{6}} \left(\frac{10^5}{Q}\right)^{\frac{3}{4}} \left(\frac{T_{\text{sys}}}{0.4 \text{ K}}\right)^{\frac{1}{2}} \left(\frac{1 \text{ s}}{t_{\text{eff}}}\right)^{\frac{1}{4}}$$

$$\Leftrightarrow h > 4.8 \times 10^{-21} \times \left(\frac{11.47 \text{ GHz}}{\nu}\right)^{\frac{5}{4}} \left(\frac{0.1}{\eta}\right) \left(\frac{43 \text{ T}}{B_0}\right) \left(\frac{4.93 \times 10^{-5} \text{ m}^3}{V_{\text{cav}}}\right)^{\frac{5}{6}} \left(\frac{10^5}{Q}\right)^{\frac{3}{4}} \left(\frac{T_{\text{sys}}}{1.0 \text{ K}}\right)^{\frac{1}{2}} \left(\frac{1 \text{ s}}{t_{\text{eff}}}\right)^{\frac{1}{4}}$$

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Extremely encouraging

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Extremely encouraging

But ...

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What about this value?

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Extremely encouraging

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What about this value?

Hypothesis made:

The signal must remain coherent and located in the experimental frequency bandwidth during at least 1s

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Is it really possible?

• The frequency of GWs coming from binary systems drifts with time $\dot{f}(\nu) = \frac{96}{5}\pi^{\frac{8}{3}} \left(\frac{G\mathcal{M}_c}{c^3}\right)^{\frac{5}{3}} \nu^{\frac{11}{3}}$

• Time during which the signal drifts in the frequency sensitivity bandwidth: $t_{\Delta\nu} \sim \frac{\Delta\nu}{\dot{f}(\nu)} = \frac{\nu}{Q\dot{f}(\nu)}$

$$t_{\Delta\nu} \sim \frac{5}{96} \pi^{-\frac{8}{3}} \nu^{-\frac{8}{3}} Q^{-1} \left(\frac{G\mathcal{M}_c}{c^3}\right)^{-\frac{5}{3}}$$



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$$\mathrm{SNR} \simeq \frac{P_{\mathrm{sig}}}{k_B T_{\mathrm{sys}}} \sqrt{\frac{t_{\mathrm{eff}}}{\Delta \nu}} > 1$$

3 different regimes:

1) Effective time given by the signal frequency drift through the frequency bandwidth of the cavity

$$> 2.0 \times 10^{-21} \times \left(\frac{2.67 \text{ GHz}}{\nu}\right)^{\frac{7}{12}} \left(\frac{0.1}{\eta}\right) \left(\frac{27 \text{ T}}{B_0}\right) \left(\frac{1.83 \times 10^{-3} \text{m}^3}{V_{\text{cav}}}\right)^{\frac{5}{6}} \left(\frac{10^5}{Q}\right)^{\frac{1}{2}} \left(\frac{T_{\text{sys}}}{0.4 \text{ K}}\right)^{\frac{1}{2}} \left(\frac{\mathcal{M}c}{10^{-14} M_{\odot}}\right)^{\frac{5}{12}}$$

 $t_{\rm eff} = t_{\Delta \nu}$

2) Effective time limited by the duration of the experiment Very small chirp masses The signal would spend "more time than available" within the cavity bandwidth $t_{\Delta\nu} > t_{\max} \Rightarrow t_{eff} = t_{\max}$ $h > 5.3 \times 10^{-22} \times \left(\frac{2.67 \text{ GHz}}{\nu}\right)^{\frac{5}{4}} \left(\frac{0.1}{n}\right) \left(\frac{27 \text{ T}}{B_0}\right) \left(\frac{1.83 \times 10^{-3} \text{ m}^3}{V_{exv}}\right)^{\frac{5}{6}} \left(\frac{10^5}{Q}\right)^{\frac{3}{4}} \left(\frac{T_{sys}}{0.4 \text{ K}}\right)^{\frac{1}{2}} \left(\frac{60 \text{ s}}{t_{max}}\right)^{\frac{1}{4}}$

3) Effective time limited by the sampling rate *Highest chirp masses accessible*

The time spent by the signal within the experimental bandwidth is smaller than the inverse sampling frequency $t_{\rm eff} = t_{\Delta\nu}^2/t_{\rm min}$

$$h > 3.3 \times 10^{-18} \times \left(\frac{2.67 \text{ GHz}}{\nu}\right)^{\frac{1}{6}} \left(\frac{0.1}{\eta}\right) \left(\frac{27 \text{ T}}{B_0}\right) \left(\frac{1.83 \times 10^{-3} \text{ m}^3}{V_{\text{cav}}}\right)^{\frac{5}{6}} \left(\frac{T_{\text{sys}}}{0.4 \text{ K}}\right)^{\frac{1}{2}} \left(\frac{\mathcal{M}c}{10^{-9}M_{\odot}}\right)^{\frac{5}{6}}$$

Strain sensitivity



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Accessible distance



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Number of expected events



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Take away message:

Time analyses are mandatory to derive realistic estimates

Not a small correction but a huge effect

Drastically reduces the sensitivity, thus the accessible distance

• Possibilities to increase the signal:

- Coupling to different modes in the cavity
- Eccentric orbits \longrightarrow Boost the emitted power by a factor

$$F(e) = (1 - e^2)^{-7/2} \left(1 + \frac{73}{24}e^2 + \frac{37}{96}e^4\right)$$

Generation of controlled gravitational waves from high-power twisted light

The action of gravity on light is well known and has been extensively studied over the past century but the converse - i.e. the way light acts as a source of gravity - remains, to a large extent, unexplored.

Based on arXiv:2309.04191

With E. Atonga (Oxford Univ.), R. Aboushelbaya (Oxford Univ.),A. Barrau (LPSC), C. Lin (Jagiellonian Univ.),P. Norreys (Oxford Univ.), et. al.



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Region where twisted light is generated

$$\begin{split} E_x &= \frac{E_0}{2} \left[J_{l+1}(\beta\rho) \sin(\omega t - k_z z + (l+1)\phi) - J_{l-1}(\beta\rho) \sin(\omega t - k_z z + (l-1)\phi) \right] , \\ E_y &= -\frac{E_0}{2} \left[J_{l+1}(\beta\rho) \cos(\omega t - k_z z + (l+1)\phi) + J_{l-1}(\beta\rho) \cos(\omega t - k_z z + (l-1)\phi) \right] , \\ E_z &= 0 , \\ B_x &= \cos(\alpha) \frac{E_0}{2} \left[J_{l+1}(\beta\rho) \cos(\omega t - k_z z + (l+1)\phi) + J_{l-1}(\beta\rho) \cos(\omega t - k_z z + (l-1)\phi) \right] , \\ B_y &= \cos(\alpha) \frac{E_0}{2} \left[J_{l+1}(\beta\rho) \sin(\omega t - k_z z + (l+1)\phi) - J_{l-1}(\beta\rho) \sin(\omega t - k_z z + (l-1)\phi) \right] , \\ B_z &= \sin(\alpha) \frac{E_0}{c} J_l(\beta\rho) \cos(\omega t - k_z z + l\phi) , \end{split}$$

Stress-energy tensor

$$T^{\mu\nu} = \left(\frac{u \mid \vec{N}/c}{\vec{N}/c \mid -\sigma_{i,j}} \right)$$

with $\begin{aligned} u &= \frac{\epsilon_0 c}{2} (E^2 + c^2 B^2) , & \text{Electromagnetic field energy density} \\ \vec{N} &= \frac{\vec{E} \times \vec{B}}{\mu_0} , & \text{Poynting vector} \\ \sigma_{ij} &= \epsilon_0 c (E_i E_j + c^2 B_i B_j) - u \delta_{i,j} . & \text{Maxwell tensor} \end{aligned}$

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$$\begin{split} \bar{h}_{\mu\nu}^{TT} &= \bar{h}_{\mu\nu}^{D,TT} + \bar{h}_{\mu\nu}^{ZZ,TT} + \bar{h}_{\mu\nu}^{+,TT} + \bar{h}_{\mu\nu}^{+,TT} + \bar{h}_{\mu\nu}^{+,TT} \\ \bar{h}_{\mu\nu}^{D,TT} &= \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \cos^2(\theta) \left[1 - \cos(2\theta)\right] & 0 & \cos(\theta) \sin(\theta) \left[\cos(2\theta - 1\right] & \sin^2(\theta) \sin(\theta) \left[\cos(2\theta - 1\right] & \sin^2(\theta) \left[1 - \cos(2\theta)\right] & 0 & \frac{1}{2} & \sin^2(\theta) \left[1 - \cos(2\theta)\right] & 0 & \frac{1}{2} & \sin^2(\theta) \left[1 - \cos(2\theta)\right] & 0 & \frac{1}{2} & \sin^2(\theta) \left[1 - \cos(2\theta)\right] & 0 & \frac{1}{2} & \frac{1}{2} & \sin^2(\theta) \left[1 - \cos(2\theta)\right] & \frac{1}{2} & \frac{1}{2} & \sin^2(\theta) \left[1 - \cos(2\theta)\right] & \frac{1}{2} & \frac{1}{2$$

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Beaming effect towards the half-cone angle as the frequency increases

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In definitive

- Estimations performed with current (Laser MegaJoule, National Ignition Facility) and forthcoming (Station of Extreme Light) facilities.
- The optical setup provides a very good control over the GWs properties (frequency, direction of emission, polarisation states)
 Beaming effect towards the half-cone angle alpha
- Generated strains too low to be observed in a near future $h > 10^{-20}$ for current laser systems and $h > 10^{-27}$ with future generation facilities

→ In the 10¹² - 10¹⁹ Hz range G. Vacalis, G. Marocco et. al.. arXiv: 2301.08163

• Are high-power twisted lights, the highest sources of gravitational strain produced by humankind?

Strain produced by Spinlaunch suborbital accelerator ~ 100 times bigger But probably the highest sources of power radiated through GWs:

Close to the pulse:
$$\frac{dP}{d\Omega} \sim 9.4 \times 10^{-5} \text{ W.m}^{-2}$$

10 meters away: $\frac{dP}{d\Omega} \sim 1.9 \times 10^{-17} \text{ W.m}^{-2}$ $\frac{dP_{SL}}{d\Omega} \sim 1.1 \times 10^{-35} \text{ W.m}^{-2}$



https://www.spinlaunch.com/

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Thank you!