String theory, from the landscape to the swampland

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String theory

- A remarkable theory of quantum gravity, calculable
- Second superstring revolution ('95): unique theory!







Multiple solutions







Simplest exemple





Observable world

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 T_6



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supersymmetric spectrum no cosmological constant Massless scalars (moduli)

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M₆ : R_{mn}=0 Ricci-flat

Calabi-Yau manifolds



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Landscape of possibles 4d universes

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The problem of **bottom-up**: are we really in the landscape? Or did we fall into the swampland ?





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Black holes $M \ge Q$

 \Rightarrow extremal black holes cannot decay: remnants

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EFT breaks down when $\Delta \phi \to \infty$

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de Sitter space is in the swampland!!

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The potential satisfies $|\nabla V| \ge cV$ with c > 0 (O(1) in Planck units)

or

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If so, dark energy comes from quintessence field(s)

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uses non-perturbative ingredients

Demonstrated to have instabilities with unclear end-points

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Beautiful and still largely unexplored landscape

Transplanckian Censorship Conjecture

• The expansion of the universe must slow down before all Planckian modes are stretched beyond the Hubble size

Two implications:

- no dS close to boundaries of moduli space, where

$$\frac{|\nabla V|}{V} \ge \frac{2}{\sqrt{(d-1)(d-2)}}$$

- dS can exist inside the bulk, if short lived

$$\tau \le \frac{1}{H} \log \frac{M_P}{H}$$