Gravitational wave data analysis Part I





MaNiTou 2nd summer school on Gravitational Waves

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Introduction



From data...

... to science



GW191103_012549 GW191105_143521 GW191109_010717 GW191113_071753 GW191126_115259 GW191127_050227 GW191129_134029 GW191204_110529 GW191204_171526 GW191215_223052 GW191216_213338 *GW191219_163120* GW191222_033537 GW191230_180458 *GW200105_162426* GW200112_155838 GW200115_042309 GW200128_022011 GW200129_065458 GW200202_154313 GW200208_130117 GW200208_222617 GW200209_085452 GW200210_092254 GW200216_220804 GW200219_094415 GW200220_061928 GW200220_124850 GW200224_222234 GW200225_060421 GW200302_015811 GW200306_093714 GW200308_173609* GW200311_115853 GW200316_215756 GW200322_091133

Introduction



Data & signal models

Realistic data and signal:

- Data quality for real detectors
- Data cleaning
- Glitch analysis and removal
- Full CBC signals, waveform modelling
- Continuous waves analysis
- Unmodeled signals (bursts)
- Stochastic backgrounds

Our scope:

- Idealized detector: stationary Gaussian noise
- Simplified CBC signals

Science products

Full science products:

- Realistic detections, confidence and classification
- Realistic parameter estimation
- Evidence computation and model comparison
- Production of catalogs
- Cosmological analyses
- Population analyses
- Tests of GR analyses

Our scope:

- Simplified detection with matched filtering
- Simplified parameter estimation



Introduction

$Data = Response \cdot Signal + Noise$



- deterministic signals, waveform models models approx. GR background(s)

Noise

- stochastic process
- need modelling
- idealized process vs data artefacts ?



Part I

- GW signals: the basics
- Noise as a stochastic process
- Introducing matched filtering
- Towards real CBC searches
- Other signals: continuous waves, stochastic backgrounds

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GW Signals: polarizations and strain



Response of an interferometer: $h = F_+h_+ + F_\times h_\times$

 $F_{+,\times}(\theta,\phi,\psi)$ pattern functions, depend on sky and polarization



GW Signals: Compact Binary Coalescences - Fact sheet

Inspiral: analytical Merger/Ringdown: numerical





- Chirp mass: $\mathcal{M}_c = \frac{m_1^{3/3} m_2^{3/3}}{(m_1 + m_2)^{1/5}}$
- Inspiral frequency: $\omega_{\rm orb}(t) = \left(\frac{G\mathcal{M}_c}{c^3}\right)^{-5/8} \left(\frac{5}{256}\frac{1}{t_{\perp}-t}\right)^{3/8}$
- BBH scale invariance: $G = c = 1 \qquad \begin{array}{cc} t \to t/M & f \to Mf \\ & h \to rh/M \end{array}$
- End of inspiral: $r_{\rm ISCO} = 6M \ f_{\rm ISCO} = 1/6^{3/2}/(\pi M)$
- Effect of cosmology: $M \rightarrow (1+z)M \quad 1/r \rightarrow 1/d_L$





The Fourier domain



GW Signals: CBC parameter space



For CBC: 15+2+2 parameters

- intrinsic: 2 masses, 2*3 spin vectors
- distance: |
- time of coales¢en¢e?) |
- direction to the observer: 2 angles $D_{\ell*}^{\ell*}$ (α if β in ℓ observer's frame: 2 angles
 - polarization angle: I angle
 - +eccentricity, periastron: 2
 - +tidal deformabilities BNS: 2

(0, 0, 0, 0, 5) = (0, 0, 0, 0, 5)



 m_2

- BBH: massive, merger-ringdown
- BNS: inspiral dominated, tidal effects
- NSBH: high mass ratio, tidal effects ?

へい

 m_1

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- How to understand noise as a stochastic process ?
- Ergodicity, stationarity, Gaussianity ?



Noise autocorrelation:

$$C(t,t') = \langle n(t)n(t') \rangle$$

Stationary white noise:

Flat spectrum

Noise



- How to model real noise ?
- Ergodicity, stationarity, Gaussianity ?

Noise autocorrelation: $C(t, t') = \langle n(t)n(t') \rangle$

$$P_n = \lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{T/2} |n(t)|^2 dt$$

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In the Fourier domain:

$$n_T(t) \equiv \chi_{[-T/2,T/2]} n(t)$$

$$P_n = \lim_{T \to +\infty} \frac{1}{T} \int_{-\infty}^{+\infty} dt \, n_T(t)^2$$

$$= \lim_{T \to +\infty} \frac{1}{T} \int_{-\infty}^{+\infty} df \, |\tilde{n}_T(f)|^2$$

$$= \int_{0}^{+\infty} df \, S_n(f)$$

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Noise Power Spectral Density (I-sided):

$$S_n(f) \equiv \lim_{T \to +\infty} \frac{2}{T} |\tilde{n}_T(f)|^2$$

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Noise Power Spectral Density (I-sided):

$$S_n(f) \equiv \lim_{T \to +\infty} \frac{2}{T} |\tilde{n}_T(f)|^2$$

In the stationary case: $\langle \rangle \sim \frac{1}{T} \int dt$ $C(t, t') = \langle n(t)n(t') \rangle$ $C(t, t') = C(0, t' - t) \equiv C(t' - t)$

Noise PSD as the FT of the autocorrelation:

$$\frac{1}{2}S_n(f) = \int d\tau C(\tau) e^{-2i\pi f\tau}$$

the two definitions correspond

Noise PSD



- Different processes dominate red/white/blue noise
- PSD from real LVK data: lines, drifts over time
- PSD estimation method: average over segments (Welch)





$$C(t, t') = \langle n(t)n(t') \rangle$$
$$C(t, t') \equiv C(t - t')$$

$$\langle \tilde{n}(f)\tilde{n}^*(f')\rangle = \int dt \int dt' \, e^{2i\pi ft} e^{-2i\pi ft} e^{-2$$

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 $2i\pi f't' \langle n(t)n(t') \rangle$

$$\begin{split} \langle \tilde{n}(f)\tilde{n}^*(f')\rangle &= \int dt \int dt' \, e^{2i\pi ft} e^{-2i\pi f't'} \langle n(t)n(t')\rangle \\ &= \int dt \int d\tau \, e^{2i\pi ft} e^{-2i\pi f'(t+\tau)} \langle n(t)n(t+\tau)\rangle \end{split}$$

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$$e^{-2i\pi f't'} \langle n(t)n(t') \rangle$$

$$\begin{split} \langle \tilde{n}(f)\tilde{n}^*(f')\rangle &= \int dt \int dt' \, e^{2i\pi ft} e^{-2i\pi} \\ &= \int dt \int d\tau \, e^{2i\pi ft} e^{-2i\pi} \\ &= \int d\tau \, C(\tau) e^{-2i\pi f'\tau} \int d\tau \, e^{2i\pi f'\tau} \int d\tau \, e^{-2i\pi f'\tau}$$

$$C(t, t') = \langle n(t)n(t') \rangle$$

$$C(t, t') \equiv C(t - t')$$

$$e^{-2i\pi f't'} \langle n(t)n(t') \rangle$$

$$e^{-2i\pi f'(t+\tau)} \langle n(t)n(t+\tau) \rangle$$

 $\int dt \, e^{2i\pi(f-f')t}$

$$\begin{split} \langle \tilde{n}(f)\tilde{n}^{*}(f')\rangle &= \int dt \int dt' e^{2i\pi ft} e^{-2it} \\ &= \int dt \int d\tau \, e^{2i\pi ft} e^{-2i\tau} \\ &= \int d\tau \, C(\tau) e^{-2i\pi f'\tau} \int d\tau \, C(\tau) e^{-2i\pi f'\tau} \int d\tau \, C(\tau) e^{-2i\pi f'\tau} \, d\tau \, C(\tau) e^{-2i\pi f'\tau} \end{split}$$

$$(t, t') = \langle n(t)n(t') \rangle$$

$$(t, t') \equiv C(t - t')$$

$$2i\pi f't' \langle n(t)n(t') \rangle$$

$$2i\pi f'(t+\tau) \langle n(t)n(t+\tau) \rangle$$

C(

$$dt \, e^{2i\pi(f-f')t}$$

 $e^{-2i\pi f' au}$

A consequ

Equence of noise stationarity:
$$C(t,t') = \langle n(t)n(t') \rangle$$

 $C(t,t') \equiv C(t-t')$
 $\langle \tilde{n}(f)\tilde{n}^*(f') \rangle = \int dt \int dt' e^{2i\pi ft} e^{-2i\pi f't'} \langle n(t)n(t') \rangle$
 $= \int dt \int d\tau e^{2i\pi ft} e^{-2i\pi f'(t+\tau)} \langle n(t)n(t+\tau) \rangle$
 $= \int d\tau C(\tau) e^{-2i\pi f'\tau} \int dt e^{2i\pi(f-f')t}$
 $= \delta(f-f') \int d\tau C(\tau) e^{-2i\pi f'\tau}$
 $= \delta(f-f') \frac{1}{2} S_n(f)$
Noise stationindependential

ationarity means lence in Fourier domain !

In practice, stationarity is always approximate...

Gaussian noise



In Fourier domain (DFT):

$$p(\tilde{\mathbf{n}}) = \frac{1}{\sqrt{(2\pi)^N \det \tilde{\boldsymbol{\Sigma}}}} \exp\left[-\frac{1}{2}\tilde{\mathbf{n}}^T \cdot \tilde{\boldsymbol{\Sigma}}^{-1}\right]$$



Gaussian noise



$$p(\tilde{\mathbf{n}}) = \frac{1}{\sqrt{(2\pi)^N \det \tilde{\boldsymbol{\Sigma}}}} \exp\left[-\frac{1}{2}\tilde{\mathbf{n}}^T \cdot \tilde{\boldsymbol{\Sigma}}^{-1}\right]$$

From NxN to N !

 $\cdot \tilde{\mathbf{n}}$

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$$\frac{1}{T} \int dt \, h(t) s(t) = \frac{1}{T} \int dt \, h(t)^2 + \frac{1}{T} \int dt \, h$$

coherent
 $\sim \text{const}$ incoh
 $\sim 1/T$





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coherent
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 $\sim 1/T$

In signal:

In noise:

$$\hat{s} \equiv \int dt W(t) s(t) \quad \hat{n} \equiv \int dt W(t) n(t)$$
$$S = \langle \hat{s} \rangle \qquad N^2 = \langle \hat{n}^2 \rangle$$





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$$S = \int dt W(t)h(t)$$
$$= \int df \tilde{W}^*(f)\tilde{h}(f)$$

L(t)n(t)



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Build filter W(t) to optimize S/N

$$S = \int dt W(t)h(t)$$
$$= \int df \tilde{W}^*(f)\tilde{h}(f)$$

$$N^{2} = \langle \int dt \, dt' \, W(t) W(t') n(t) n(t') \rangle$$

$$\frac{1}{T} \int dt \, h(t) s(t) = \frac{1}{T} \int dt \, h(t)^2 + \frac{1}{T} \int dt \, h(t) n(t)$$

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= $\int df df' \tilde{W}^*(f)\tilde{W}(f')\langle \tilde{n}(f)\tilde{n}^*(f') \rangle$

$$\frac{1}{T} \int dt h(t)s(t) = \frac{1}{T} \int dt h(t)^2 + \frac{1}{T} \int dt h(t)n(t)$$

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= $\int df df' \tilde{W}^*(f)\tilde{W}(f')\langle \tilde{n}(f)\tilde{n}^*(f') \rangle$
= $\int df df' \tilde{W}^*(f)\tilde{W}(f')\frac{1}{2}S_n(f)\delta(f - f')$



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= $\int df df' \tilde{W}^*(f)\tilde{W}(f')\frac{1}{2}S_n(f)\delta(f - \int df \frac{1}{2}S_n(f)|\tilde{W}(f)|^2$



$$(a|b) \equiv 4 \operatorname{Re} \int_{0}^{+\infty} \frac{df}{S_n(f)} \tilde{a}(f) \tilde{b}^*(f)$$

Redefine:
$$\tilde{u}(f) \equiv \frac{1}{2} S_n(f) \tilde{W}(f)$$

•	
•	

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Simpler expressions:

$$S = (u|h) \qquad N^2 = (u|u)$$
$$\frac{S}{N} = \frac{(u|h)}{\sqrt{(u|u)}}$$

Optimization, Wiener filter:

$$u \propto \tilde{h}$$

 $\tilde{W}(f) \equiv 2\tilde{h}(f)/S_n(f)$

•	
•	

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Using the Wiener filter on data:

$$N^2 = (h|h)$$
$$\hat{s} = (h|s)$$

Matched filter SNR:

$$\rho = \frac{\hat{s}}{N} = \frac{(h|s)}{\sqrt{(h|h)}}$$

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In noise: $\rho \sim \mathcal{N}(0, 1)$ For signal: $\rho \sim \mathcal{N}(\overline{\rho}, 1)$ (perfect template) $\overline{\rho} = \sqrt{(h|h)}$ optimal SNR



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In practice, multiple templates and optimize over time and phase

 $\tilde{h}_{\Delta t,\Delta\phi}(f) = e^{-2i\pi f\Delta t} e^{i\phi} \tilde{h}(f)$



Whitening, band-passing



Whitening, band-passing





Matched filtering example

Try a fixed template



See also GWOSC tutorials [https://gwosc.org]

Optimization over phase and 2 polarizations: $\rho^2 = \rho_{\rm c}^2 + \rho_{\rm p}^2$ Distribution (chi2, noncentered): $R \equiv \rho^2$ $p(R|\overline{R}) = \frac{1}{2}e^{-(R+\overline{R})/2}I_0\left(\sqrt{R\overline{R}}\right)$ $p(R|0) = \frac{1}{2}e^{-R/2}$

Rough estimates:

- templates in bank: $\sim 10^5$
- values of time / yr: $\sim 10^{10}$
- for a FAR ~ I/yr: $\rho_t \sim 8$ $ho_t \sim 5.5$ two det.

single det.



Thresholding: tradeoff between false alarms and false dismissals

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Match with nearest template: $(h_t|h)$ max $\Delta t, \phi \sqrt{(h_t|h_t)} \sqrt{(\overline{h|h})}$

- Effectualness criterion: match > 0.97
- Methods to build a template bank: geometric (metric based on match), stochastic, hybrid
- Trade-off between effectualness (template bank size) and FAR
- Simplified physics (no precession)

 10^{3}



Templates are more orthogonal at low masses, with many wave cycles



 Calibration: the output strain is the results of a complex control loop



• Calibration is in part stochastic: amplitude and phase splines, with nodes randomly distributed in envelope

Real data and artefacts: glitches, non-stationarity



Real data and artefacts: glitches, non-stationarity



- Glitches: strong non-stationary, non-Gaussian events
- SNR alone would be dominated by glitches
- Need more robust significance metric

aussian events ches

Real data: data quality, data cleaning



• Data cleaning (removal of noise lines)







• Glitch gating or removal (BayesWave)







Signal consistency and ranking statistic

PyCBC

Penalization of large residuals: computed on n freq. bands, χ^2 with $\nu = 2n - 2$ d.o.f.

$$\hat{\rho} = \rho \times \begin{cases} 1 & \chi^2 \leq \nu \\ \left[\frac{1}{2} + \frac{1}{2}(\chi^2/\nu)^3\right]^{-1/6} & \chi^2 > \nu \end{cases}$$

GstLAL

Consistency between time series and autocorrelation of template

- Idea: use a ranking statistic for all foreground/ background events
- Tradeoff between false alarm and false dismissals
- Can use different ranking statistics !







Significance of coincident triggers: time slides



- False Alarm Rate: with and without signal

- Rank all triggers with ranking statistic of choice
- From rank of trigger False Alarm Rate (over time of extended data)
- Cumulative distribution of IFAR: N=T/IFAR
- Consistency, does not say how sensitive the search is



Sensitivity and p_astro



$$P_{1}(x \mid \vec{x}) = \int_{0}^{\infty} \vec{x}$$

Unmodeled search for bursts

- Time-frequency domain: wavelets (cWB, BayesWave)
- Exploit direction-dependent detector response: signal reconstruction
- Background estimation challenging, introduce chirp morphology, vetoes

Detection statistic:

$$\eta_c = \sqrt{rac{2E_c}{(1+E_n/E_c)}}$$
 E_c coherent E_n residual n

Generic transient search

Looking for generic transients

Overview of search pipelines

Online analysis:

- minimize latency
- limited data quality/calibration • final data quality/calibration information information
- send alerts based on FAR • use p astro > 0.5 for catalogs

- Offline analysis:
- run on ~Iweek chunks

- Outside groups:
- PyCBC
- Princeton

CBC detections

GRAVITATIONAL WAVE \square DETECTIONS – SINCE 2015 – -----OzGrav-

ARC Centre of Excellence for Gravitational Wave Discovery

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Continuous waves

Long-lived quasi-monochromatic signals: modulated response

$$F_{+}, F_{\times} \to F_{+}(t), F_{\times}(t)$$

$$\tau(t) = t + \frac{\vec{r}(t) \cdot \vec{n}}{c} + \Delta_{E\odot} - \Delta_{S\odot}$$

- Targeted/directed search: known pulsars, galactic center
- All-sky coherent search untractable !
- Semi-coherent searches required

$$\mathbf{h}(t, \mathbf{x}) = \sum_{A=+,\times} \int df \int d^2 \mathbf{n} \, \tilde{h}_A(f, \mathbf{n}) \mathbf{e}_A(\mathbf{n}) e^{-2i\pi f(t-\mathbf{n}\cdot\mathbf{x}/c)} \qquad \Omega_{\rm GW}(f) = \frac{f}{\rho_c} \frac{\mathrm{d}\rho_{\rm GW}}{\mathrm{d}f}$$

- Isotropic
- Stationary
- Gaussian ? 'Pop-corn' ?

- Main target: CBC background
- Backgrounds of cosmological origin
- Check for correlations between detectors (magnetic)

Superposition of signal(s) from all directions: Energy density spectrum of GW background:

Cross-Correlation between detectors: $\hat{C}^{IJ}(f) = \frac{2}{T} \frac{\operatorname{Re}[\tilde{s}_{I}^{\star}(f)\tilde{s}_{J}(f)]}{\gamma_{IJ}(f)S_{0}(f)}$

