

Federal University of Santa Catarina

# Exclusive photoproduction of light vector mesons with a holographic wave function model.

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and Haimon Trebien

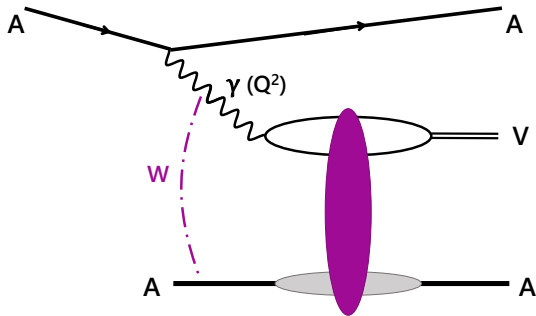


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# Light vector meson photoproduction in nuclear targets

# Coherent production

In the coherent vector meson photoproduction, the nucleus target remains intact.

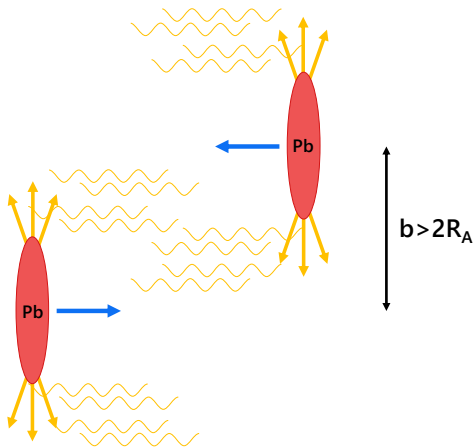


The rapidity differential cross section for the  $AA \rightarrow AVA$  process can be factorized:

$$\frac{d\sigma^{AA \rightarrow AVA}}{dy} = \int d^2b \frac{\omega dN_\gamma(\omega, b)}{d\omega} \frac{d\sigma^{\gamma A \rightarrow VA}(\omega, b)}{d^2b} + (y \rightarrow -y).$$

# Photon flux and ultraperipheral collisions

An ultraperipheral collision between two nuclei is defined as the one in which the impact parameter exceeds the sum of the nuclei radius.



# Photon flux and ultraperipheral collisions

The photon flux at  $b$  emitted by the projectile nucleus, and excluding strong interaction between the colliding ions, is :

$$\omega \frac{dN_\gamma(\omega, b)}{d\omega} = \int d^2 b_\gamma \frac{\omega N_\gamma(\omega, b_\gamma)}{d\omega d^2 b_\gamma} \exp \left( -\sigma_{\text{NN}}^{\text{tot}} \int d^2 b' T_A(b') T_A(|\vec{b}_{AA} - \vec{b}'|) \right). \quad (1)$$

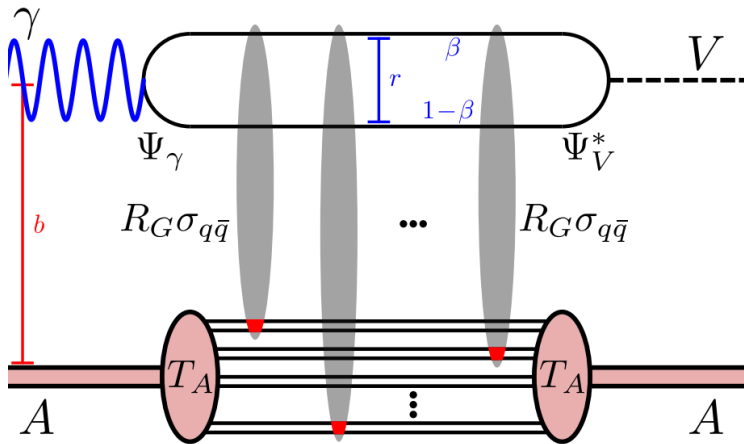
The Weizsäcker-Williams method calculated for a punctual charge is used to calculate the  $b$ -dependent photon flux:

$$\frac{\omega d^3 N_\gamma(\omega, b_\gamma)}{d\omega d^2 b_\gamma} = \frac{Z^2 \alpha_{\text{em}} \omega^2}{\pi^2 \gamma^2} K_1^2 \left( \frac{b_\gamma \omega}{\gamma} \right), \quad (2)$$

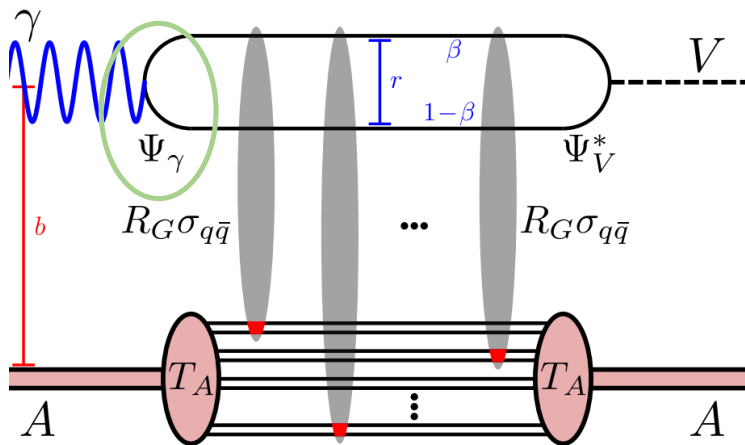
The Woods-Saxon distribution for the lead nuclear density was used in the thickness function

$$T_A(b) = \int_{-\infty}^{+\infty} dz \rho_A(b, z). \quad (3)$$

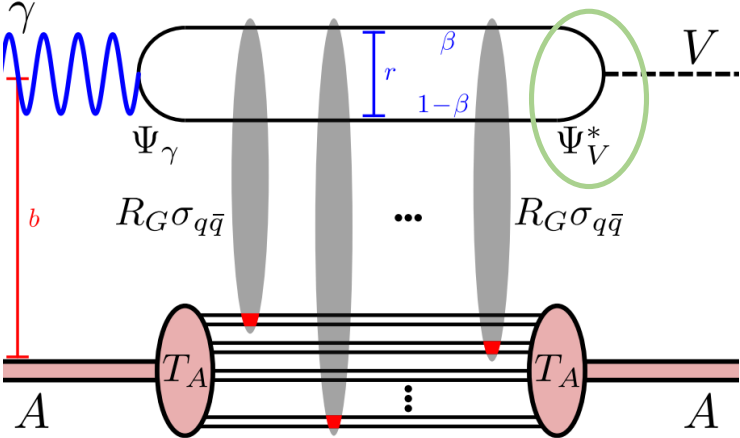
# Color dipole approach



# Photon wave function



# Vector meson wave function





# Vector meson wave function

## AdS/QCD holographic model

It is considered a semiclassical approximation, which enables the scalar part to be factorized

$$\psi(\beta, \zeta, \varphi) = e^{iL\varphi} X(\beta) \frac{\phi(\zeta)}{\sqrt{2\pi\zeta}},$$

with  $\zeta^2 = \beta(1 - \beta)r^2$ .

The hadronic LF wave function is found by solving a relativistic equation, equal to the Schrodinger equation, with the effective confinement potential

$$U(\zeta, J) = \kappa^4 \zeta^2 + 2\kappa^2(J - 1)$$

$$\left( -\frac{d^2}{d\zeta^2} - \frac{1 - 4L^2}{4\zeta^2} + U(\zeta) \right) \phi(\zeta) = M^2 \phi(\zeta)$$

The solutions, fully relativistic, have the shape of the HO wave functions, while the eigenvalues are given by

$$M^2 = 4\kappa^2 \left( n + \frac{J}{2} + \frac{L}{2} \right).$$

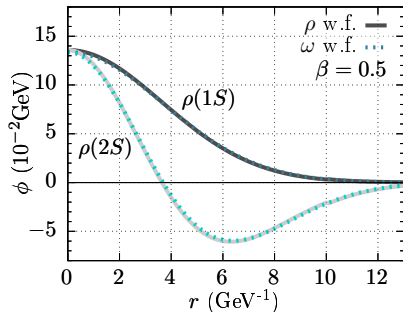
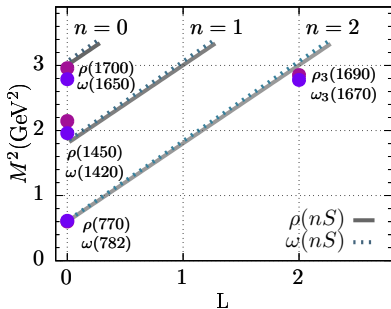
Mass dependent  $\kappa$

$$\kappa = \frac{M_{V(n=0)}}{\sqrt{2}}$$

# Vector meson wave function

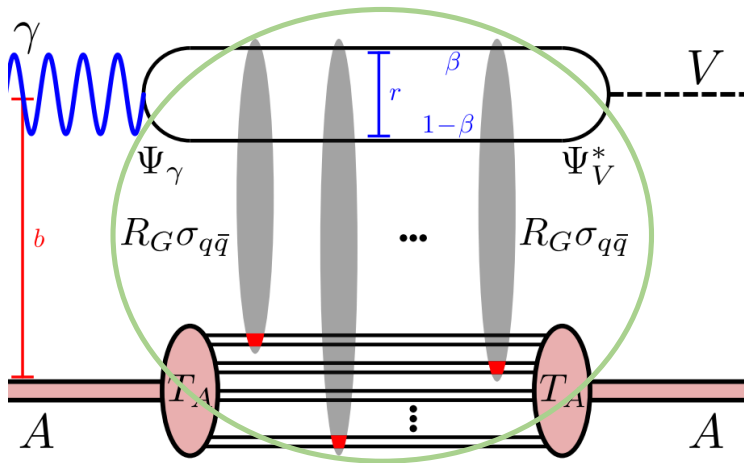
## AdS/QCD holographic model

The left panel shows the mass spectroscopy of  $\rho$  and  $\omega$  vector mesons.



The right panel presents the LF wave functions for the  $\rho$  vector meson at ground and excited states.

# Dipole-nucleus cross section



Glauber-Gribov model

# Coherent production

The total cross sections for the  $\gamma A \rightarrow VA$  process is

$$\frac{d\sigma^{\gamma A \rightarrow VA}(\omega, b)}{d^2b} = \left| \int d\beta d^2r \Psi_V^* \Psi_\gamma(\beta, r) \left( 1 - e^{-\sigma_{q\bar{q}}(x, r) T_A(b)/2} \right) \right|^2$$

The GBW model was used to describe the dipole cross section  $\sigma_{q\bar{q}}$ .

## Corrections

### 1 Real part

$$\sigma_{q\bar{q}}(x, r) \Rightarrow \sigma_{q\bar{q}}(x, r) \left( 1 - i \frac{\pi}{2} \lambda \right)$$

### 2 Skewness

$$R_g(\lambda) = \frac{2^{2\lambda+3}}{\sqrt{\pi}} \frac{\Gamma(\lambda + 5/2)}{\Gamma(\lambda + 4)}$$

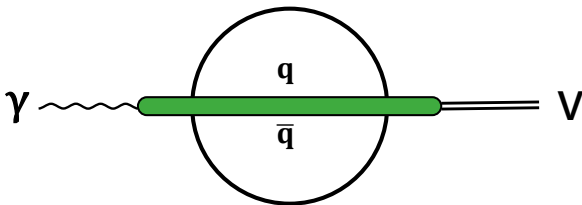
$$\lambda = \frac{\partial \ln \sigma_{q\bar{q}}(x, r)}{\partial \ln(1/x)}$$

# Coherence length

At high energies, the  $q\bar{q}$  pair lifetime, called coherence length, is defined as

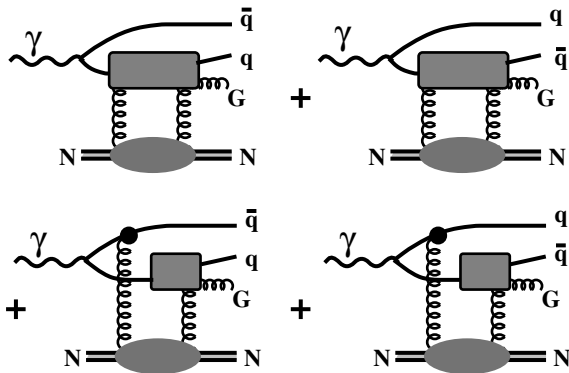
$$l_c = \frac{2\omega'}{M_V^2}. \quad (4)$$

The dipole model considers it to be much bigger than the nucleus radius.



# Higher states

At high energies, we need to consider that the photon can split into higher states with gluons  $|q\bar{q}g\rangle, |q\bar{q}gg\rangle, \dots$



[Kopeliovich, Schafer and Tarasov, Phys. Rev. D 62 054022, 2000]

This is taken into account in the dipole-proton cross section.

# Gluon shadowing

The infinite lifetime approximation fails for higher Fock states

↔ reduction of the  $\gamma A$  cross section.

↔ effect called **gluon shadowing**.

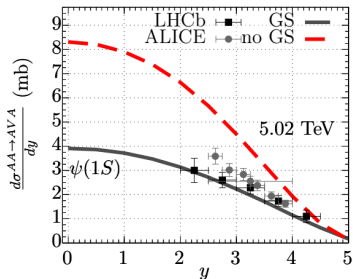
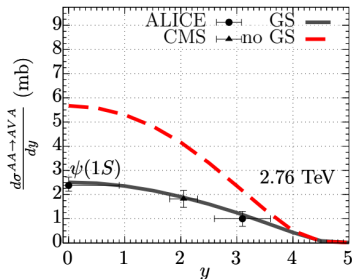
It is possible to rescale the dipole cross section by the factor  $R_G$

$$\sigma_{q\bar{q}}(r, x) \rightarrow \sigma_{q\bar{q}}(r, x)R_G(x, \mu^2).$$

# Gluon shadowing for heavy vector mesons

In the heavy vector meson case it is calculated with EPPS16 and a factorization scale  $\mu = M_V/2$ .

[Henkels, E.G.O., Pasechnik, Trebien, Phys. Rev. D 102, 014024 (2020)].



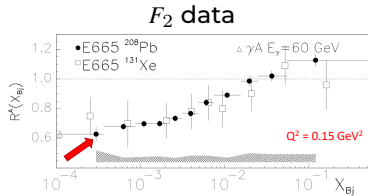
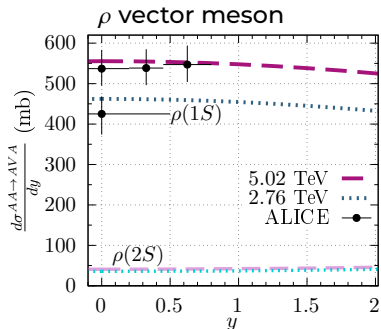
The evolution does not reach the light vector meson scale.

We do not have gluon shadowing for smaller scales

↪ This is a **PROBLEM**.



# Gluon shadowing extraction



[Data taken from the Fermilab E665 Collaboration,  
Z.Phys.C 67 (1995) 403-410]

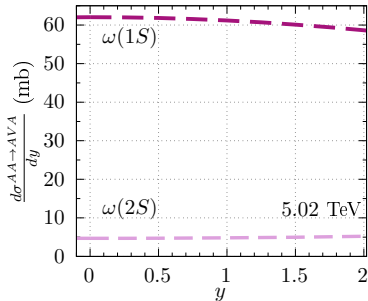
$$\frac{F_2^A}{AF_2^P} = 0.537$$

The available data led to an optimal value for the gluon shadowing

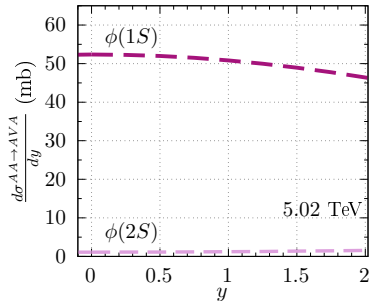
$$R_G = 0.85$$

# Coherent photoproduction predictions

$\omega$  vector meson



$\phi$  vector meson

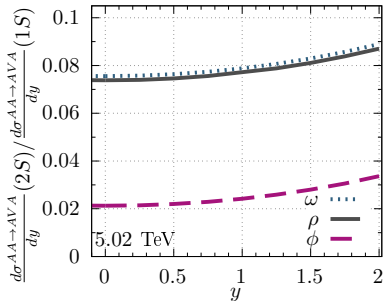


We used the same  $R_G = 0.85$  factor to make predictions for other light vector mesons.

Measurements can bring information about the  $R_G$  scale dependence.

# 2S to 1S ratio predictions

$\rho$ ,  $\omega$ , and  $\phi$  vector mesons



Predictions for the ratio between the excited state cross section and its corresponding ground state cross section.

This can be a tool for finding the best dipole cross section model.

# Conclusion

# Conclusion

- **Light vector meson** photoproduction: **small hard scales  $Q^2$** .
- The **Glauber-Gribov** approach is used for nuclear targets.
- The inclusion of **gluon shadowing**  $R_g$  is necessary.
- By fitting  $\rho(1S)$  **UPC ALICE** and  $F_2$  data, we effectively obtain:  **$R_g = 0.85$** .
- We make **predictions**:  $\rho(2S)$ ,  $\omega(1S, 2S)$ , and  $\phi(1S, 2S)$ .
- The **ratio** between excited and ground state cross sections depend on **vector meson wavefunctions** and probe the **dipole cross section**.

## See more:

Poster 'Photoproduction of light meson using holographic models' - Haimon Trebien

# Acknowledgments



Thank you!





# EXTRA SLIDES

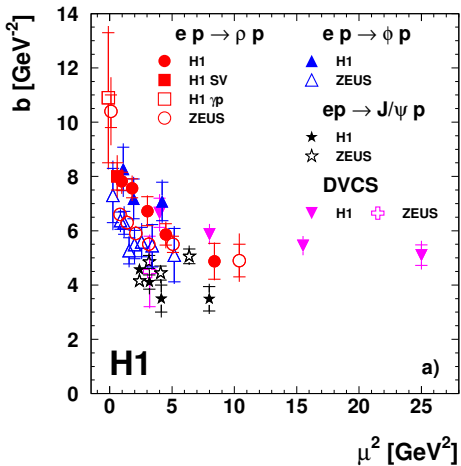
The slope parameter for heavy vector mesons takes the form:

$$B(W, Q^2) \approx B_0 + 4\alpha'(0) \ln\left(\frac{W}{W_0}\right) - B_1 \ln\left(\frac{Q^2 + M_V^2}{M_{J/\Psi}^2}\right), \quad (5)$$

while the one for light vector mesons is given by:

$$B = N \left[ 14.0 \left( \frac{1\text{GeV}^2}{Q^2 + M_V^2} \right)^{0.2} + 1 \right], \quad (6)$$

# Slope parameter



# Color dipole parametrizations

without impact parameter dependence

## 1 GBW

It has the form:

$$\sigma_{q\bar{q}}(x, r) = \sigma_0 \left( 1 - e^{-\frac{r^2 Q_s^2(x)}{4}} \right), \quad (7)$$

with saturation scale defined as  $Q_s^2(x) = Q_0^2 \left( \frac{x_0}{x} \right)^\lambda$ .

## 2 KST

It includes corrections for small  $\hat{s} \equiv W^2$ .

$$\sigma_{q\bar{q}}(r, \hat{s}) = \sigma_0(\hat{s}) \left[ 1 - e^{-r^2/R_0^2(\hat{s})} \right]. \quad (8)$$

In this case, the  $\hat{s}$ -dependence appears in  $\sigma_0(\hat{s})$  and  $R_0(\hat{s})$ , which are given by

$$R_0(\hat{s}) = 0.88 \text{fm} (s_0/\hat{s})^{0.14}, \quad \sigma_0(\hat{s}) = \sigma_{\text{tot}}^{\pi P}(\hat{s}) \left( 1 + \frac{3R_0^2(\hat{s})}{8 \langle r_{\text{ch}}^2 \rangle_\pi} \right). \quad (9)$$

# Color dipole parametrizations with impact parameter dependence

## 3 bSat

The partial dipole amplitude is

$$N(x, \mathbf{r}, \mathbf{b}) = 1 - \exp\left(-\frac{\pi^2}{2N_c} r^2 \alpha_s(\mu^2) x g(x, \mu^2) T(b)\right) \quad (10)$$

with the following scale dependence  $\mu^2 = 4/r^2 + \mu_0^2$ .

## 4 BK

The BK evolution equation is given by

$$\frac{\partial N(r, b, Y)}{\partial Y} = \int d\mathbf{r}_1 K(r, r_1, r_2) (N(r_1, b_1, Y) + N(r_2, b_2, Y) - N(r, b, Y) - N(r_1, b_1, Y) N(r_2, b_2, Y)) . \quad (11)$$

Gluon recombination effects are taken into account in the non-linear term

# Color dipole parametrizations

## 5 bCGC

It is the interpolation of solutions for the BFKL and the BK :

$$N(x, \mathbf{r}, \mathbf{b}) = \begin{cases} N_0 \left( \frac{r Q_s}{2} \right)^{2[\gamma_s + (1/(\eta\Lambda Y)) \ln(2/rQ_s)]} & rQ_s \leq 2 \\ 1 - e^{-\mathcal{A} \ln^2(\mathcal{B} r Q_s)} & rQ_s > 2 \end{cases} . \quad (12)$$

The  $b$ -dependence is introduced in the saturation scale

$$Q_s \equiv Q_s(x, b) = \left( \frac{x_0}{x} \right)^{\Lambda/2} \left[ \exp \left( -\frac{b^2}{2B_{\text{CGC}}} \right) \right]^{1/(2\gamma_s)} . \quad (13)$$

