Chirality and Wobbling in Atomic Nuclei, July 10 - July 14, 2023, Huizhou, China

The evolution of the chiral symmetry in cesium isotopes

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Duo Chen, Jian Li, et. al., The evolution of the chiral symmetry in cesium isotopes, Eur. Phys. J. A (2023) 59:142





Chirality in Nature

Chirality exists commonly in nature.



Elementary Particles



DNA & Spiral Shells



Molecules & Human Body



Chirality in Nuclear World

>> Chirality in atomic nucleus

• In 1997, Frauendorf and Meng suggested for the first time the occurrence of chirality in nuclear physics.

S. Frauendorf and J. Meng, Nucl. Phys. A 617, 131 (1997)

Triaxially deformed doubly odd nuclei can rotate in a left-handed and right-handed geometrical configuration, and manifest the chiral symmetry breaking in the intrinsic frame.



Chiral operator: $\chi = TR_{y}(\pi)$;

$$\begin{array}{l} \chi | \mathcal{L} \rangle = | \mathcal{R} \rangle; \\ \chi | \mathcal{R} \rangle = | \mathcal{L} \rangle. \end{array}$$



• Experimental signal of nuclear chirality----Chiral doublet bands: Two near degenerate $\Delta I = 1$ bands



S. Frauendorf and J. Meng, Nucl. Phys. A 617, 131 (1997)

Restoration of breaking symmetry in laboratory frame

 $|IM + \rangle = \frac{1}{\sqrt{2}} (|\mathcal{R}\rangle + |\mathcal{L}\rangle)$ $|IM - \rangle = \frac{i}{\sqrt{2}} (|\mathcal{R}\rangle - |\mathcal{L}\rangle)$

132₁ a

130

134_D

In 2001, the chiral nuclei were firstly reported. K. Starosta et al., Phys. Rev. Lett. 86, 971 (20)

5 February 2001

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PHYSICAL REVIEW LETTERS

Chiral Doublet Structures in Odd-Odd N = 75 Isotones: Chiral Vibrations

K. Starosta,^{1,*} T. Koike,¹ C. J. Chiara,¹ D. B. Fossan,¹ D. R. LaFosse,¹ A. A. Hecht,² C. W. Beausang,² M. A. Caprio,² J. R. Cooper,² R. Krücken,² J. R. Novak,² N. V. Zamfir,^{2,†} K. E. Zyromski,² D. J. Hartley,³ D. L. Balabanski,^{3,‡} Jing-ye Zhang,³ S. Frauendorf,⁴ and V. I. Dimitrov^{4,‡}
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136Pm

> The history of chirality in ¹³⁴Pr

✓ The doublet bands in 134Pr(previously observed by Petrache et al. in 1996) were discussed by Frauendorf and Meng in 1997.





S. Frauendorf and J. Meng, Nucl. Phys. A 617, 131 (1997)



✓ However, the chirality in 134Pr was later contradicted by the papers of Tonev et al. and Petrache et al. both in 2006.



134

15 20 Spin (h) In Fig. 1(c) the energy signature staggering is illustrated as a function of spin. At low spins the signature staggering in band 1 is larger than that in band 2. Above spin 18 the signature staggering of band 2 becomes large, while that of band 1 becomes very small. If two bands are chiral partners, the signature staggering should be equal.

positive-parity bands [1]. The experimental B(E2) values

are larger in Band 1 than in Band 2 whereas the B(M1)

values are slightly larger in Band 2 than in Band 1. The



✓ In 2011, a paper by Timar et al. in which other chiral candidates in 134Pr are proposed

PHYSICAL REVIEW C 84, 044302 (2011)

Medium- and high-spin band structure of the chiral-candidate nucleus ¹³⁴Pr

J. Timár,¹ K. Starosta,^{2,3} I. Kuti,¹ D. Sohler,¹ D. B. Fossan,² T. Koike,^{2,4} E. S. Paul,⁵ A. J. Boston,⁵ H. J. Chantler,⁵ M. Descovich,⁵ R. M. Clark,⁶ M. Cromaz,⁶ P. Fallon,⁶ I. Y. Lee,⁶ A. O. Macchiavelli,⁶ C. J. Chiara,^{2,7,8} R. Wadsworth,⁹ A. A. Hecht,¹⁰ D. Almehed,¹¹ and S. Frauendorf¹¹



Band 3 is newly identified in the present work. This $\Delta I = 1$ band has positive parity, and it decays through several M1and E2 transitions to bands 1 and 2. It has an alignment value of around $8\hbar$, which corresponds to a two-quasiparticle configuration. These facts indicate that its configuration is $\pi h_{11/2} \nu h_{11/2}$, similar to the configuration of bands 1 and 2. The observed B(M1)/B(E2) ratios of band 3 are two to three times larger than the corresponding ratios of band 1 and are close to the B(M1)/B(E2) ratios of band 2 near the $17\hbar$ spin region. This suggests a similarity between bands 2 and 3, which might indicate that the two bands are chiral partners. In this context, it may be informative to inspect also the signature splittings of the three $\pi h_{11/2} \nu h_{11/2}$ bands. In the



0.7



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¹³⁴Pr: Small tilting \rightarrow still the best candidate for chiral symmetry. -----Radu Budaca's report



>>> Experimental progress

In the past two decades, more than 50 chiral doublet candidate nuclei have been reported in the mass number A approximately equal to 80, 100, 130 and 190 region.







- Ster
- ? Some nuclei with doublet bands
- ? Neighboring nuclei of chiral candidates;
- ? The border of chiral island/isotope chain or isotone chain;







- ? Some nuclei with doublet bands
- ? Neighboring nuclei of chiral candidates;
- ? The border of chiral island/isotope chain or isotone chain;

Cs isotopes: perfect candidates

Isotopes	Exp.	Theor.
^{122,124,126,128,130,132} Cs		
^{125,127,129,131} Cs	Doublet bands	\checkmark
^{121,123} Cs	Doublet bands	
^{120,133,134} Cs	Only one band	







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- ? Neighboring nuclei of chiral candidates;
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Cs isotopes: perfect candidates

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^{121,123} Cs	Doublet bands	
^{120,133,134} Cs	Only one band	

Motivation: to study the evolution of the chiral symmetry in the Cs isotopes.

> Theoretical approaches for nuclear chirality

- Theoretical methods:
- Particle plus rotor model(PRM) S.Frauendorf and J. Meng, Nucl. Phys. A (1997) B. Qi et al. Phys. Lett. B (2009) Q. B. Chen et al. Phys. Lett. B (2018)
 A reflection-asymmetric triaxial (RAT) + PRM Y. Y. Wang et al. Phys. Lett. B (2019); Phys. Rev. C (2020)
- Project shell model (PSM)
 F. Q. Chen et al., Phys. Rev. C (2017)
 Y. K. Wang et al. PRC (2019)
- > Interacting boson fermion-fermion model (IBFFM) D. Tonev et al. Phys. Rev. Lett. (2006)
- Tilted axis cranking model (TAC) S.Frauendorf and J. Meng, Nucl. Phys. A (1997) S. Frauendorf, Nucl. Phys. A (2000)
 TAC + the random phase approximation (RPA) S. Mukhopadhyay et al. Phys. Rev. Lett. (2007) Daniel Almehed et al. Phys. Rev. C (2017)
 3D-TAC + Covariant density functional theory (CDFT) P. W. Zhao, Phys. Lett. B (2017)
- The advantages of **3DTAC-CDFT**
- > Self-consistent and microscopic investigations, no additional parameter beyond a well-determined functional
- Full account of polarization effects
- Self-consistent treatment of the nuclear currents
- This previous work of nuclear chirality by 3DTAC-CDFT :
- ¹⁰⁶Rh P. W. Zhao, Phys. Lett. B (2017).
 ¹⁰⁶Ag P. W. Zhao Y. K. Wang, and Q. B. Chen. Phys. Rev. C (2019)
 ¹⁰²⁻¹⁰⁷Rh J. Peng and Q. B. Chen Phys. Rev. C (2022)



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- Theoretical methods:
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 Y. K. Wang et al. PRC (2019)
- > Interacting boson fermion-fermion model (IBFFM) D. Tonev et al. Phys. Rev. Lett. (2006)
- Tilted axis cranking model (TAC) S.Frauendorf and J. Meng, Nucl. Phys. A (1997) S. Frauendorf, Nucl. Phys. A (2000)
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 3D-TAC + Covariant density functional theory (CDFT) P. W. Zhao, Phys. Lett. B (2017)
- The advantages of 3DTAC-CDFT
- > Self-consistent and microscopic investigations, no additional parameter beyond a well-determined functional
- Full account of polarization effects
 3DTAC-CDFT will be adopted to study the nuclear chirality in Cs isotopes.

^{102–107}Rh

▶ ¹⁰⁶Rh *P. W. Zhao, Phys. Lett. B* (2017).

¹³⁵Nd J. Peng and Q. B. Chen, Phys. Lett. B (2020) Y.P. Wang and J. Meng Phys. Lett. B (2023)</sup>

J. Peng and O. B. Chen Phys. Rev. C (2022)

¹⁰⁶Ag P. W. Zhao Y. K. Wang, and Q. B. Chen. Phys. Rev. C (2019)

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Isotope	Valence nucleons	Unpaired nucleons	References
¹²⁰ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^7 (g_{7/2}/d_{5/2})^8$	$\pi h^1_{11/2} {\otimes} \nu h^{-1}_{11/2}$	Y. Liu et al, PRC 58 (1998) C. B. Moon et al, NPA 696 (2001)
¹²¹ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^7 (g_{7/2}/d_{5/2})^9$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1} g_{7/2}^{-1}$	C. B. Moon et al, JKPS, Vol. 38, (2001)
¹²² Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^7 (g_{7/2}/d_{5/2})^{10}$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1}$	Y. N. U, J. Meng et al, JPG. 31 (2005)
¹²³ Cs	$\pi g_{7/2}^4 h_{11/2}^1 \otimes \nu h_{11/2}^7 (g_{7/2}/d_{5/2})^{11}$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1} g_{7/2}^{-1}$	K. Singh et al, EPJA 24, 359 (2004)
¹²⁴ Cs	$\pi g_{7/2}^4 h_{11/2}^1 \otimes \nu h_{11/2}^7 (g_{7/2}/d_{5/2})^{12}$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1}$	J. B. Lu et al, PRC 62, 057304 (2002) Y. Dong et al, CPL Vol. 26, 082101 (2009) S. Y. Wang et al, B. Qi, PRC 82, 027303 (2010)
¹²⁵ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^7 (g_{7/2}/d_{5/2})^{13}$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1} g_{7/2}^{-1}$	K. Singh et al, EPJA 27, 321324 (2006) J. Li, PRC 97, 034306 (2018) R. Guo et al, PRC 100, 034328 (2019)
¹²⁶ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^7 (g_{7/2}/d_{5/2})^{14}$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1}$	L. X. Feng et al, CPL 19 1779 (2002) S. Y. Wang et al, PRC 74, 017302 (2006) S. Y. Wang et al, PRC 75, 024309 (2007)
¹²⁷ Cs	$\pi g_{7/2}^4 h_{11/2}^1 \otimes \nu h_{11/2}^7 (s_{1/2}/d_{3/2})^1$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1} (s_{1/2}/d_{3/2})^1$	Y. Liang et al, PRC VOL 42, (1990) J. Li , PRC 97, 034306 (2018) R. Guo et al, PRC 100, 034328 (2019)





Isotope	Valence nucleons	Unpaired nucleons	References
¹²⁸ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^7 (s_{1/2}/d_{3/2})^2$	$\pi h_{11/2}^1 \! \otimes \! \nu h_{11/2}^{-1}$	T. Koike et al, PRC 67, 044319 (2003) E. Grodner et al, PRL 97, 172501 (2006) Qi Bin et al, CPC, 33 (2009) F. Q. Chen ,Q. B. Chen et al, PRC 96, 051303 (2017)
¹²⁹ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^9 (s_{1/2}/d_{3/2})^1$	$\pi h^1_{11/2} {\otimes} \nu h^{-1}_{11/2} (s_{1/2}/d_{3/2})^1$	Z. Y. Xin et al, CPL 26, 092301 (2009) J. Li , PRC 97, 034306 (2018) R. Guoet al, PRC 100, 034328 (2019)
¹³⁰ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^9 (s_{1/2}/d_{3/2})^2$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1}$	K. Starosta et al, PRL 86, 6 (2001) J. Peng, J. Meng et al, PRC 68, 044324 (2003) F. Q. Chen et al, PLB 785 (2018)
¹³¹ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^9 (s_{1/2}/d_{3/2})^3$	$\pi h^1_{11/2} {\otimes} \nu h^{-1}_{11/2} (s_{1/2}/d_{3/2})^1$	S. Sihotra et al, PRC 78, 034313 (2008) J. Li , PRC 97, 034306 (2018) R. Guo et al, PRC 100, 034328 (2019)
¹³² Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^9 (s_{1/2}/d_{3/2})^4$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1}$	T. Koike et al, PRC 67, 044319 (2003) G. Rainovski et al, PRC 68, 024318 (2003)
¹³³ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^9 (s_{1/2}/d_{3/2})^5$	$\pi h_{11/2}^1 \otimes \nu h_{11/2}^{-1} (s_{1/2}/d_{3/2})^1$	S. Biswas et al, PRC 95, 064320 (2017) Q. Xu et al, EPJA 54, 83 (2018)
¹³⁴ Cs	$\pi g_{7/2}^4 h_{11/2}^1 {\otimes} \nu h_{11/2}^9 (s_{1/2}/d_{3/2})^6$	$\pi h^1_{11/2} {\otimes} \nu h^{-1}_{11/2}$	T. Koike et al, PRC 67, 044319 (2003) H. Pai et al, PRC 84, 041301(R) (2011)

Single proton and neutron Routhians in ^{120–134}Cs



Single proton and neutron Routhians near the Fermi surface in $^{120-134}$ Cs as a function of the neutron number based on the fixed configuration with rotational frequency 0.3 MeV.

Evolution of polar angle \theta and azimuth angle \phi

The evolution of the polar angle θ and azimuth angle ϕ for the total angular momentum J as driven





zÎlong

- Polar angle θ: similar behavior in ^{120–134}Cs, i.e., increase with the rotational frequency and always larger than 50°.
- ✓ Azimuth angle ϕ :
- ¹²¹⁻¹³³Cs: zero at low rotational frequencies; become nonzero above the so-called critical frequency $\omega_{crit} \phi \Rightarrow$ the transition from planar to aplanar rotation.
- ^{120,134}Cs: always zero.



- The proton angular momentum comes mainly from the particles in the $h_{11/2}$ orbit, which aligns along the s axis;
- \checkmark The neutron hole in the h11/2 orbit and neutrons in low-j orbits (gd)/(sd) give substantial contributions to the neutron angular momentum, which leads to large components both in l axis and s axis.
- Higher spin states in the band are created by aligning the neutron angular momentum toward the s axis, while the proton \checkmark angular momentum keeps unchanged in the *s* axis

> Angular momenta along s, m and l axis in ^{124,125,126}Cs



For ¹²¹⁻¹³³Cs

It should be emphasized that the angular momentum contribution from proton part is approximately along the s axis at low rotational frequency. Therefore, the angular momentum components along 1 axis and m axis are mainly from neutron part.

Contributions of the valence neutrons in the $h_{11/2}$, (gd) and (sd) orbits to the total angular momenta along the s, m and l axis in 124,125,126 Cs

Figure 4 shows that the angular momentum increment of the (gd) orbits along the *s* and *l* axis will become smaller from ¹²⁴Cs to ¹²⁶Cs and the angular momentum increment along the *m*-axis will become larger. The similar behavior exists with the (gd) or (sd) orbits from ¹²⁰Cs to ¹³⁴Cs. So, we speculate that the angular momentum increment of the (gd) or (sd) orbits along the *s* and *l* axis will become smaller with the increasing of the neutron number and the angular momentum increment along the *m*-axis will become larger.

Rotational excitation energies in ^{120–134}Cs



 \checkmark The experimental excitation energies of the lower band can be reproduced well.

 \checkmark To describe the partner band, one needs to go beyond the mean-field calculations.



✓ The calculated values of spin I (ω) agree well with the experimental data for ^{120–123}Cs, and overestimate the data for ^{124–127,129–131,133}Cs, much higher than the experimental data for ^{128,132,134}Cs





The 3DTAC-CDFT results for ${}^{121,123,125-134}$ Cs show good agreements with the data, while the calculation overestimates the data for 120,122,124 Cs. For ${}^{121-133}$ Cs, a smooth falling behavior in the planar rotation, and the falling tendency slows down above the critical frequency ω_{crit} .

Evolutions of deformation parameters β and γ



✓ It could be found that β and γ are stable and there is only slight change with the increasing rotational frequency in $^{120-134}Cs$

- \checkmark Triaxial deformation in ¹³⁴Cs is approximately zero, and it further indicates no chirality in ¹³⁴Cs
- ✓ ¹²⁰Cs: the existence of chirality can not be completely obtained only based on the high-j particle-hole configurations plus stable triaxial deformation





A fully self-consistent and microscopic investigation for the evolution of chirality in the cesium isotopes ^{120–134}Cs has

- been performed with the 3DTAC-CDFT.
- ✓ $^{121-133}$ Cs: transition from the planar rotation to the chiral rotation has been obtained
- ✓ 120,124 Cs: only planar rotation, borders
- ✓ ¹¹⁹Cs: do not support the chirality built on a configuration with three protons $\pi g_{9/2}^{-1} h_{11/2}^2$