

0^+ to 0^+ Ft values:

CKM unitarity test and search for scalar currents



Bertram Blank
LP2i Bordeaux

- **Super-allowed $0^+ - 0^+$ β decay**
- **Search for scalar currents**

2nd Rencontre PhyNuBE:
Clustering and Symmetries in Nuclear physics
March 26 – 31, 2023

● ● ● Standard model of weak interaction

● Hamiltonian: Lorentz invariance

J.D. Jackson et al, Nucl. Phys. 4 (1957) 206
M. González-Alonso et al., Prog. Part. Nucl. Phys. 104, 165 (2019)

hadronic terms

leptonic terms

$$\begin{aligned}
 H = & \left(\overline{\psi}_p \gamma_\mu \psi_n \right) \left(C_V \overline{\psi}_e \gamma_\mu \psi_\nu + C'_V \overline{\psi}_e \gamma_\mu \gamma_5 \psi_\nu \right) \\
 & + \left(\overline{\psi}_p \gamma_\mu \gamma_5 \psi_n \right) \left(C_A \overline{\psi}_e \gamma_\mu \gamma_5 \psi_\nu + C'_A \overline{\psi}_e \gamma_\mu \psi_\nu \right) \\
 & + \left(\overline{\psi}_p \psi_n \right) \left(C_S \overline{\psi}_e \psi_\nu + C'_S \overline{\psi}_e \gamma_5 \psi_\nu \right) \\
 & + \frac{1}{2} \left(\overline{\psi}_p \sigma_{\lambda\mu} \psi_n \right) \left(C_T \overline{\psi}_e \sigma_{\lambda\mu} \psi_\nu + C'_T \overline{\psi}_e \sigma_{\lambda\mu} \gamma_5 \psi_\nu \right) + \text{Hermitian conj.}
 \end{aligned}$$

Initial wave function
current
final wave function

(pseudo-scalar term omitted...)

● Standard model: V-A theory

- $C_S = C'_S = C_T = C'_T = C_p = C'_p = 0$
- Maximal violation of parity: $C_V = C'_V$ and $C_A = C'_A$
- Time-reversal symmetry: C_V, C'_V, C_A, C'_A real

● Beyond standard model physics (new physics “NP”)

- search for new particles (HEP), deviation from theory in nuclear β decay

Weak-interaction studies with nuclear beta decay

Ft-values

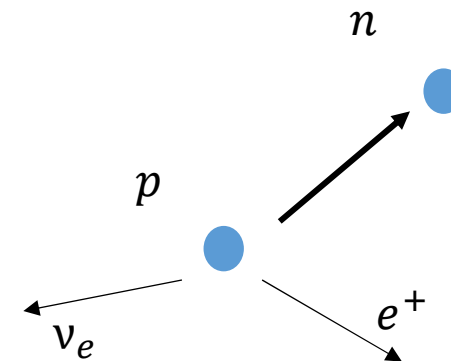
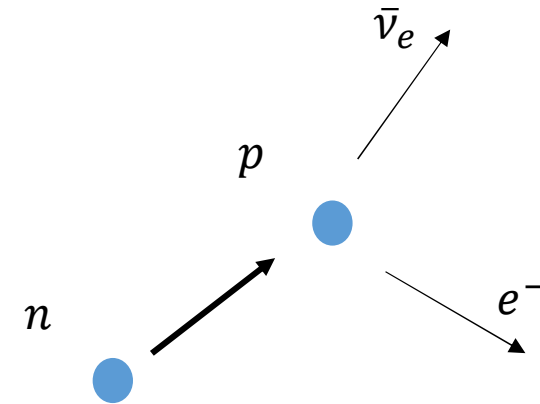
- Super-allowed Fermi decays
 - $0^+ - 0^+$
 - Mirror beta decay

Beta correlation coefficients

- $a_{\beta\nu}$
- A_{β}
- B_{ν}

Shape of the beta energy spectrum

→ Aim for a precision $\leq 10^{-3}$



• • • The nuclear laboratory



β-decay probability

$$\frac{dW(\mathbf{J})}{dE_e d\Omega_e d\Omega_\nu} = dW_0 \times \xi \left\{ 1 + a \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} + \frac{\langle \mathbf{J} \rangle}{J} \cdot \left[A \frac{\mathbf{p}_e}{E_e} + (B + b_B \frac{m_e}{E_e}) \frac{\mathbf{p}_\nu}{E_\nu} + D \frac{\mathbf{p}_e \times \mathbf{p}_\nu}{E_e E_\nu} \right] \right\}$$

β-ν correlation coefficient
CP conserving
Access to C_S and C_T quadratically

Fierz interference term
CP conserving
Access to C_S and C_T linearly

« D » coefficient
CP violating
Access to C_A, C_A', C_V, C_V' linearly



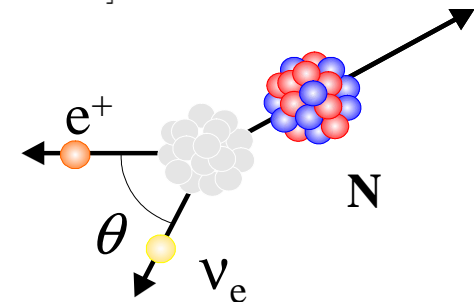
$$\frac{dW(\mathbf{J})}{dE_e d\Omega_e d\Omega_\nu} = dW_0 \times \xi \left\{ 1 + a \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} \right\}$$

for aligned spins only

$$\xi = |M_F|^2 [|C_V|^2 + |C_V'|^2 + |C_S|^2 + |C_S'|^2] - \frac{1}{3} |M_{GT}|^2 [|C_A|^2 + |C_A'|^2 + |C_T|^2 + |C_T'|^2]$$

Standard model: V-A theory

- Only vector and axial-vector: $C_S = C_S' = C_T = C_T' = 0$
- Maximal violation of parity: $C_V = C_V'$ and $C_A = C_A'$
- Time-reversal symmetry: C_V, C_V', C_A, C_A' real

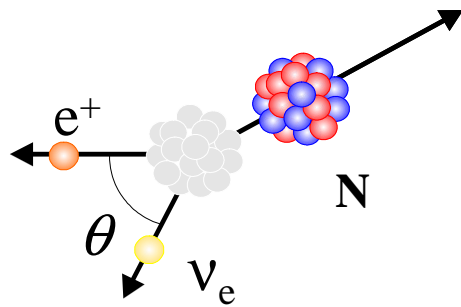


Beyond standard model physics (new physics “NP”)

- search for new particles (HEP), deviation from theory of nuclear β decay

• • • The nuclear laboratory: search for « beyond SM » physics

β-decay probability



$$dW = \boxed{dW_0} \left(1 + \boxed{a} \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + \boxed{b} \frac{m_e}{E_e} \right)$$

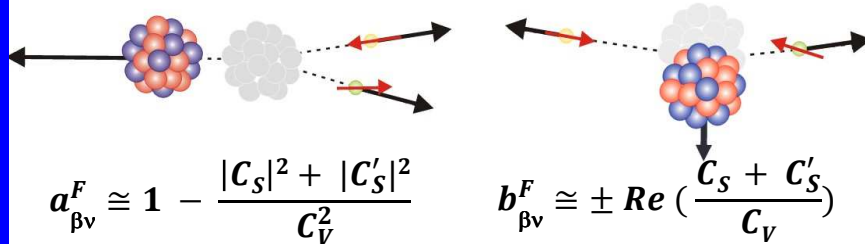
phase space factor

β-ν angular correlation coefficient

Fierz interference term = 0 (SM)

pure Fermi transitions ΔJ=0

⇒ S=0 : spin of leptons anti-parallel



$$a_{\beta\nu}^F \cong 1 - \frac{|C_S|^2 + |C'_S|^2}{C_V^2}$$

$$b_{\beta\nu}^F \cong \pm \text{Re} \left(\frac{C_S + C'_S}{C_V} \right)$$

SM: vector current

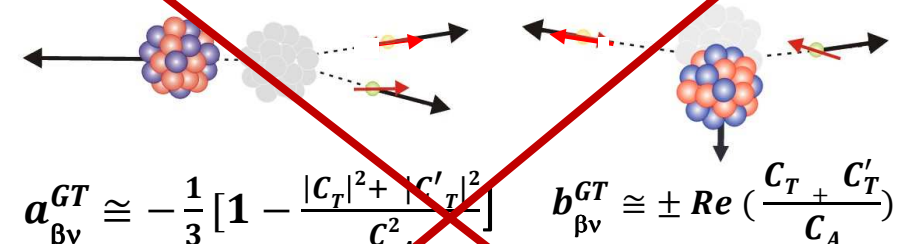
- Preferred emission angle: $\theta = 0^\circ$
- Maximum recoil energy

NP: scalar current

- Preferred emission angle: $\theta = 180^\circ$
- Minimum recoil energy

pure Gamow-Teller transitions

⇒ S=1 : spin of leptons parallel



$$a_{\beta\nu}^{GT} \cong -\frac{1}{3} \left[1 - \frac{|C_T|^2 + |C'_T|^2}{C_A^2} \right]$$

$$b_{\beta\nu}^{GT} \cong \pm \text{Re} \left(\frac{C_T + C'_T}{C_A} \right)$$

NP: tensor current

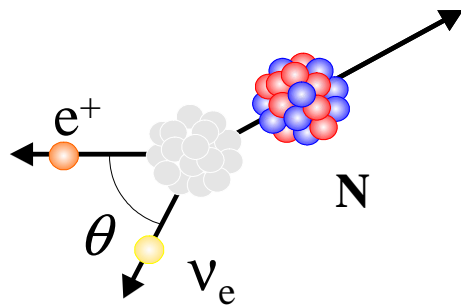
- Preferred emission angle: $\theta = 0^\circ$
- Maximum recoil energy

SM: axial-vector current

- Preferred emission angle: $\theta = 180^\circ$
- Minimum recoil energy

• • • The nuclear laboratory: search for « beyond SM » physics

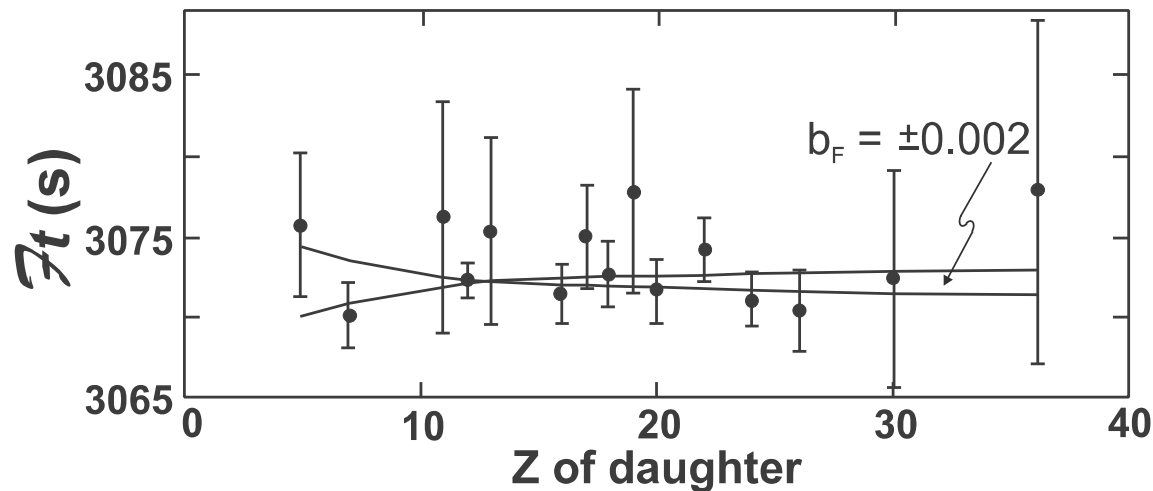
β-decay probability



$$dW = \boxed{dW_0} \left(1 + \boxed{a} \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + \boxed{b} \frac{m_e}{E_e} \right)$$

phase space factor
β-ν angular correlation coefficient
Fierz interference term = 0 (SM)

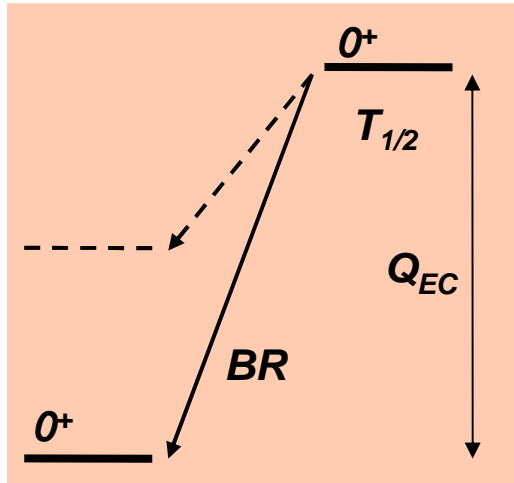
→ indirect effect on Ft values: $\mathcal{F}t \sim b \left\langle \frac{m_e}{E_e} \right\rangle$





$0^+ - 0^+$ super-allowed β -decay probability

• • • Nuclear beta decay: $0^+ - 0^+$



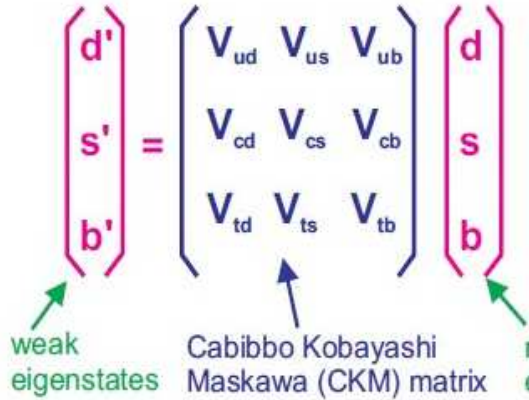
$0^+ \rightarrow 0^+$:

$$Ft = ft (1 + \delta_R') (1 - \delta_c + \delta_{NS}) = \frac{K}{G_V^2 (1 + \Delta_R) \langle M_F \rangle^2} = \text{const}$$

$f(Z, Q_{EC}) \sim 1.5\%$

$f(\text{nucl. structure}) \sim 0.3-1.5\%$

$f(\text{weak interaction}) \sim 2.4\%$



Obtain precise value of G_V^2

Determine V_{ud}^2

Test CKM unitarity

$$V_{ud}^2 = G_V^2 / G_\mu^2$$

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1$$

→ 1 – 3 σ tension

Precision measurements required: 10^{-3}

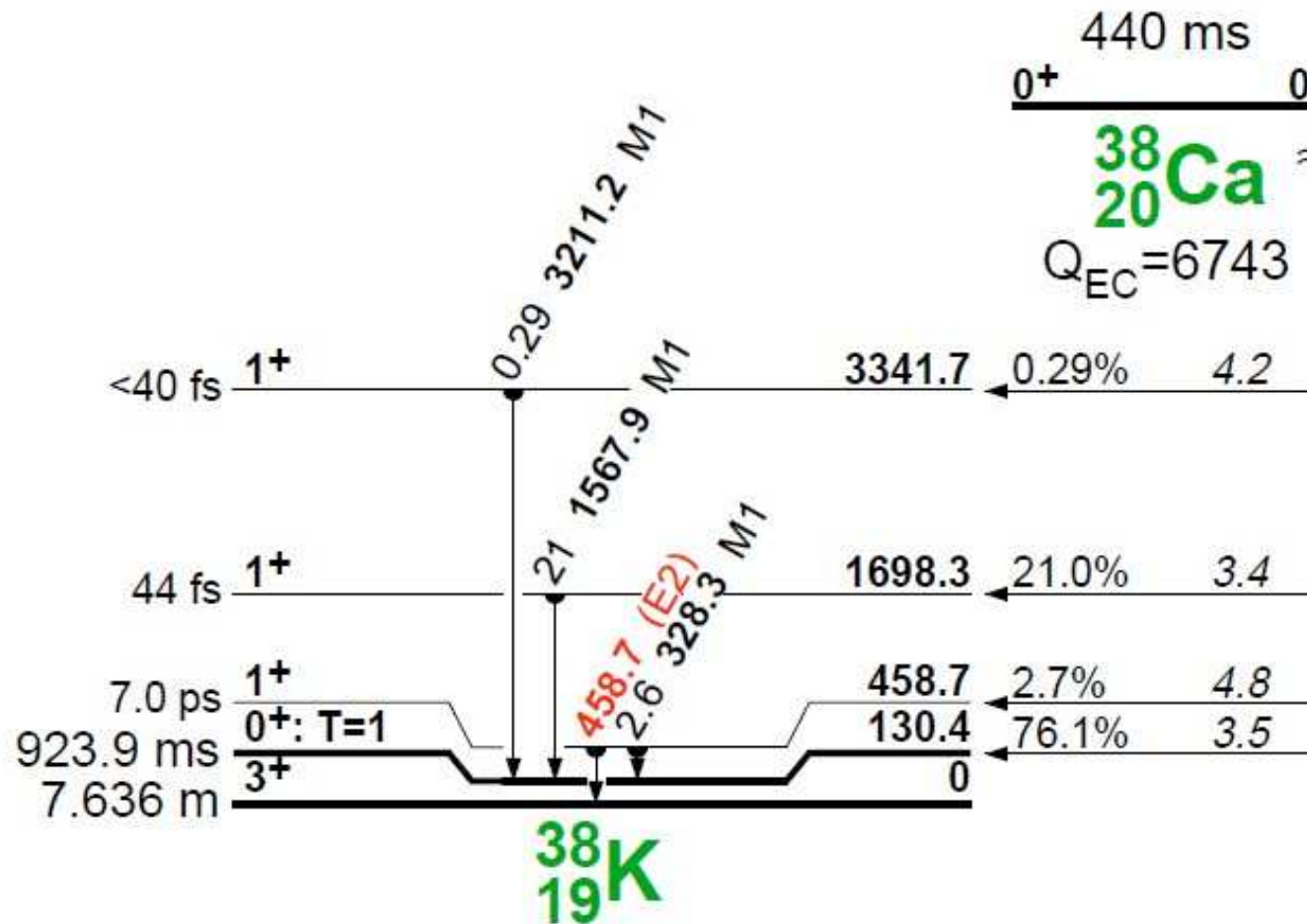
✓ Q_{EC} → mass measurements: $f \sim Q_{EC}^5$

✓ $T_{1/2}, BR$ → β -decay studies: $t = T_{1/2} / BR$



$0^+ - 0^+ \beta$ decay: ^{38}Ca

Super-allowed Fermi transitions for $T_z = -1$



- many decay channels open
- strong non-analog transitions
- high precision of γ efficiency needed \rightarrow 0.1%

● ● ● ^{38}Ca production at GANIL/LISE3

GANIL / LISE3 experiments

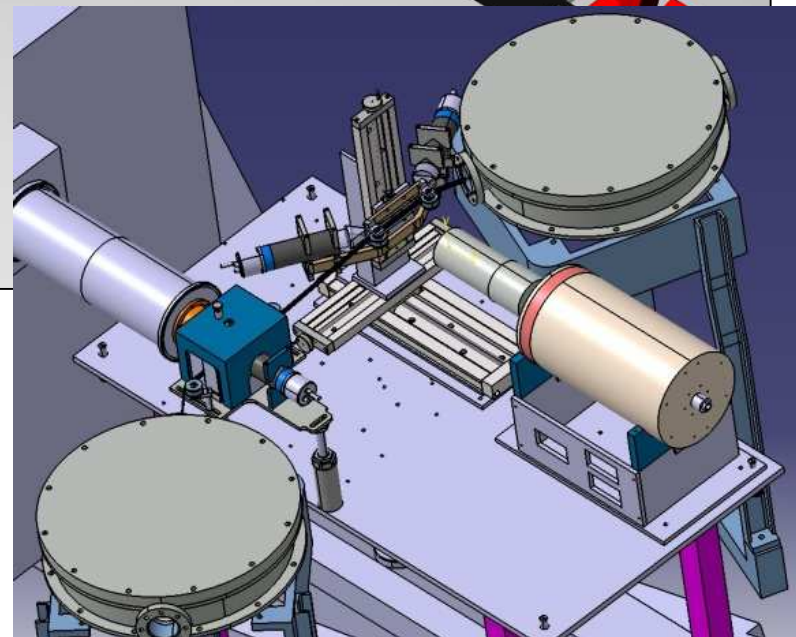
Primary Beam:
 ^{40}Ca @ 50 MeV/A

Production Target :
 $^{\text{nat}}\text{Ni}$ 90 μm

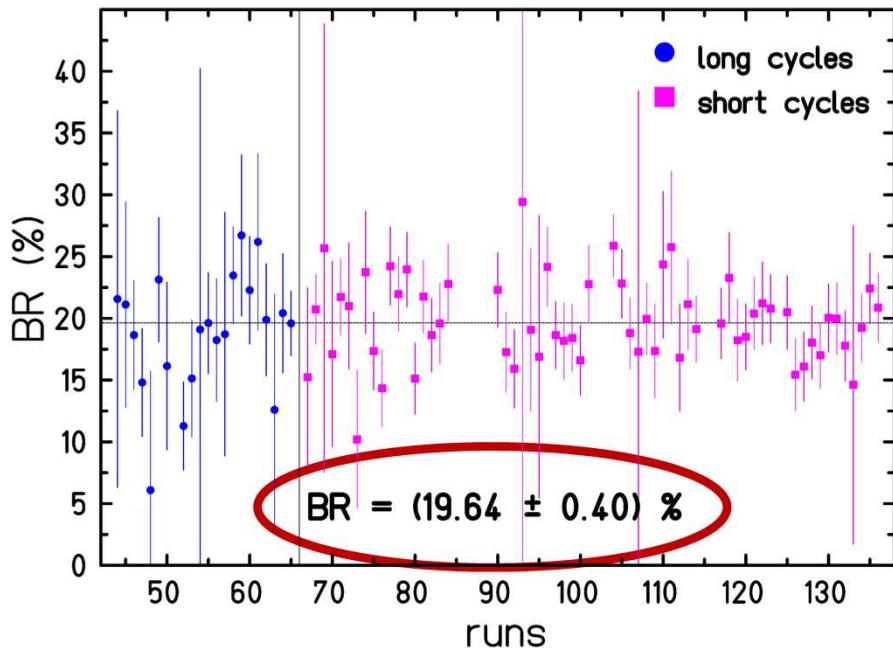
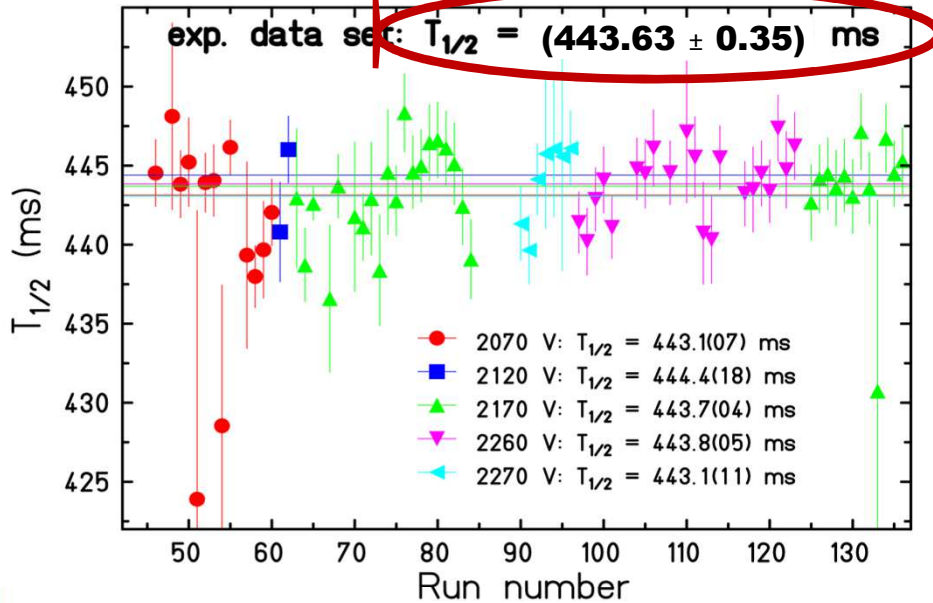
LISE3 Spectrometer

Detection Set-up

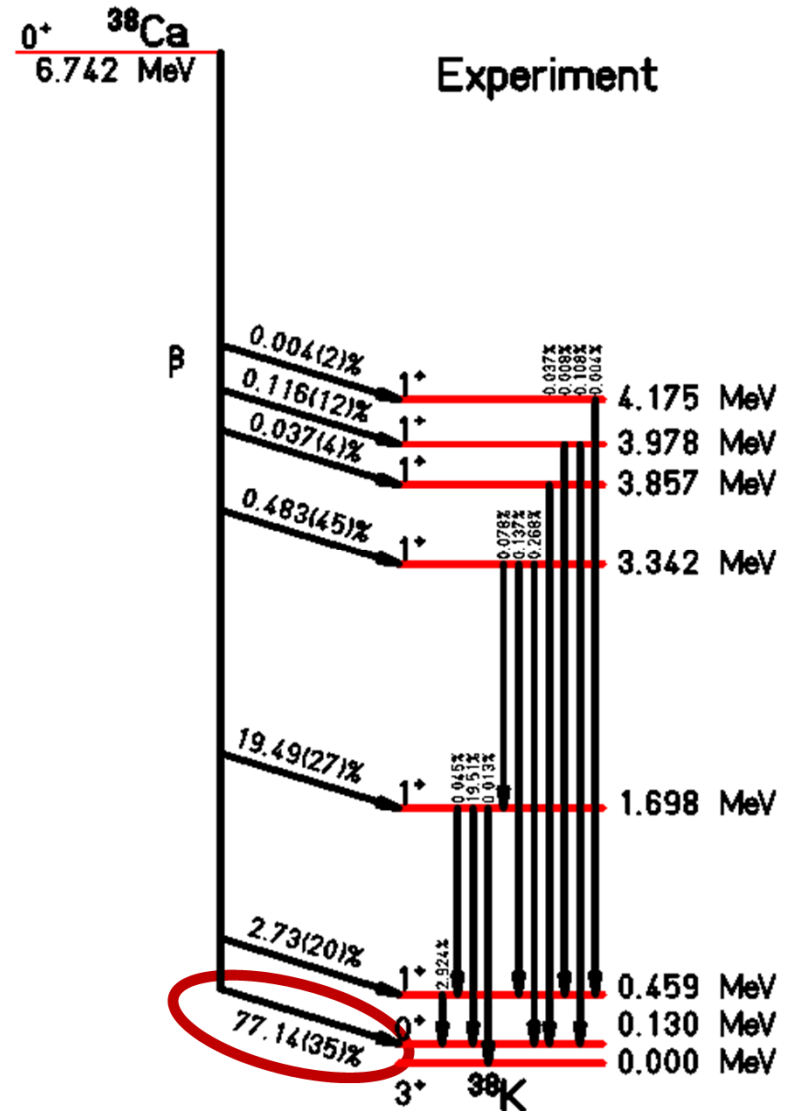
- 10^4 ^{38}Ca / s
- 99.5 % purity
- Contaminants:
 - ^{37}K : 0.12 %
 - ^{36}Ar (stable): 0.11 %
 - ^{35}Cl (stable): 0.09 %
 - ^{34}S (stable): 0.14 %



● ● ● ³⁸Ca branching ratios and half-life



Present work and Anderson et al.



● ● ● ^{38}Ca : result

• half-life:

Kavanagh <i>et al.</i> [26]	Gallmann <i>et al.</i> [27]	Zioni <i>et al.</i> [28]	Wilson <i>et al.</i> [29]	Blank <i>et al.</i> [20]	Park <i>et al.</i> [5]	Present	Average
470(20)	439(12)	450(70)	430(12)	443.8(19)	443.77(36)	443.63(35)	443.70(25)

→→ 443.70(25) ms

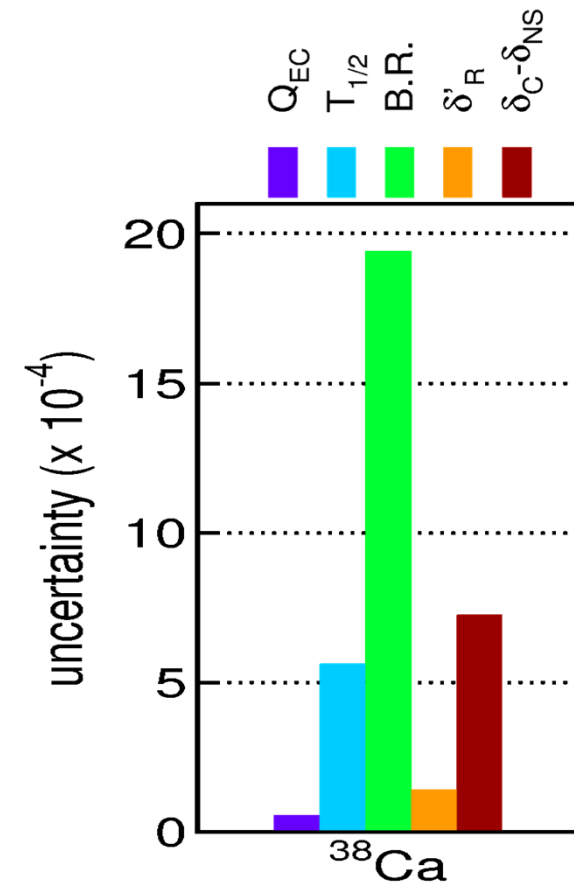
• BR ($0^+ - 0^+$): present: 77.09(35) %
Park et al.: 77.28(16) %

→→ 77.25(15) %

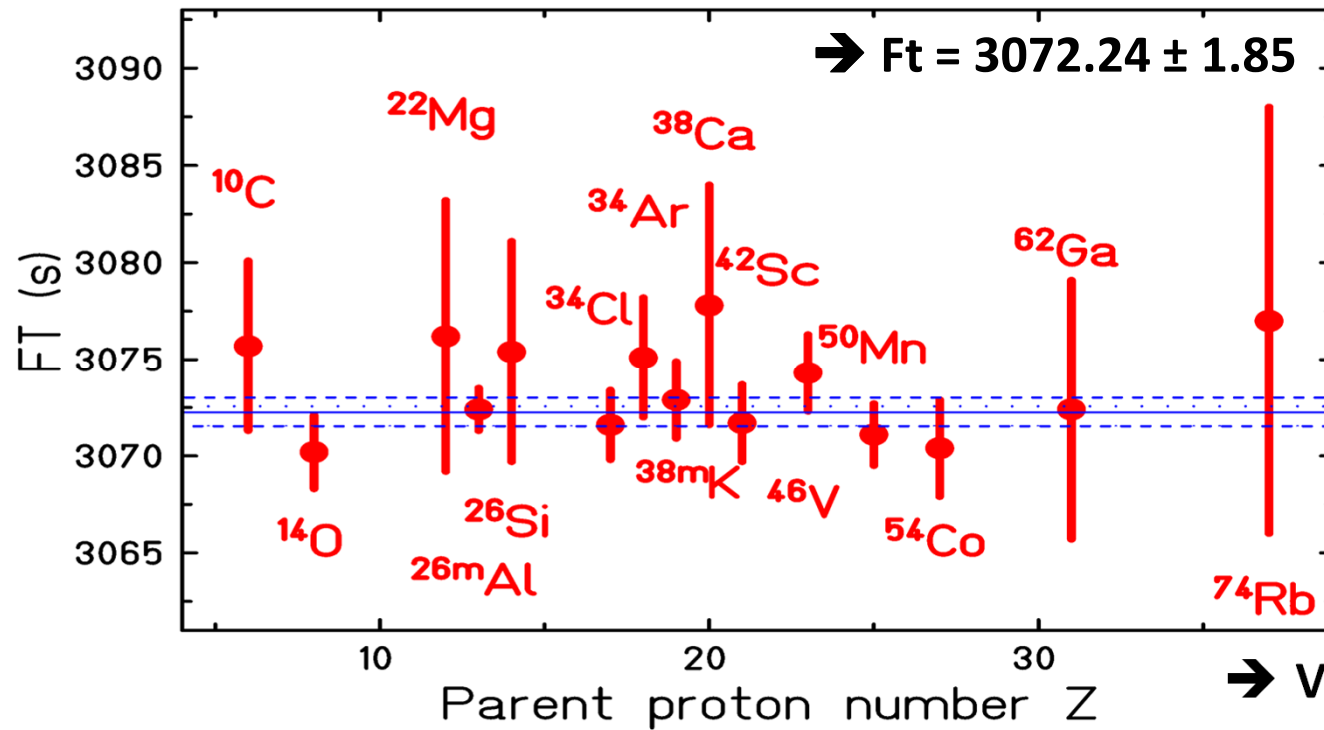
• Q value: Eronen et al.: 6612.11(7) keV

→ $ft = 3063.3(62) \text{ s}$

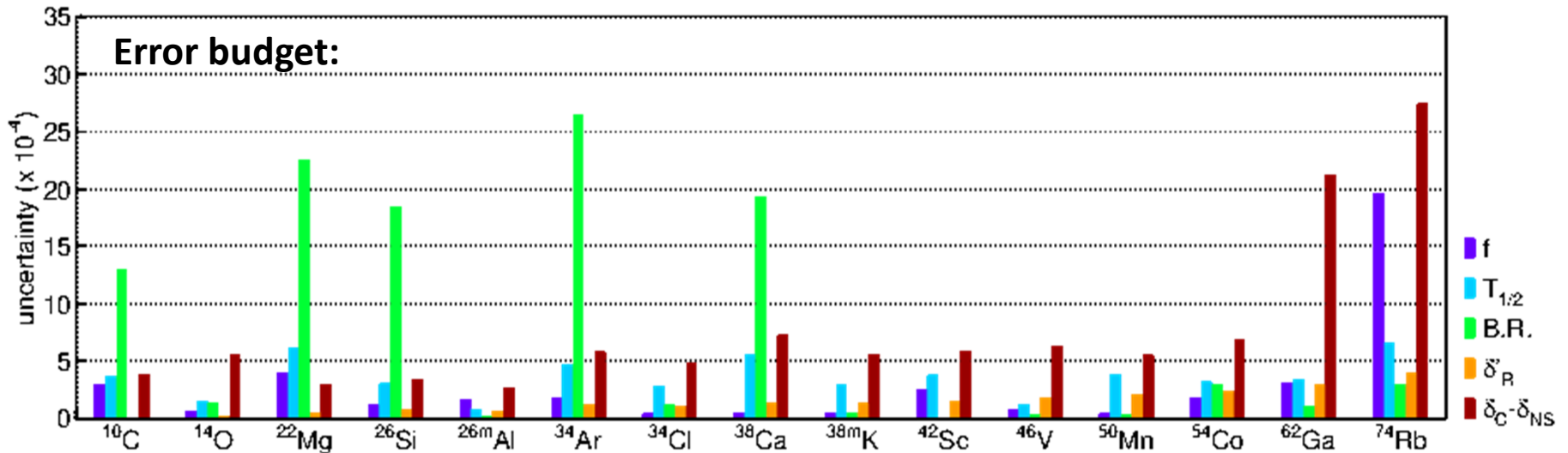
→ $\overline{ft} = 3077.5(67) \text{ s}$



● ● ● $0^+ \rightarrow 0^+$ decays: present status



- 15 nuclei
- other nuclei under study:
 - ^{18}Ne
 - ^{30}S
 - ^{42}Ti
 - ^{58}Zn
 - + heavier to come



● ● ● V_{ud} from different source and unitarity of CKM matrix

$0^+ - 0^+$ decays: $V_{ud} = 0.9740 \pm 0.0005$

mirror decays: $V_{ud} = 0.9742 \pm 0.0009$

neutron decay: $V_{ud} = 0.9743 \pm 0.0006$

→ →

$$V_{ud} = 0.9741 \pm 0.0004$$

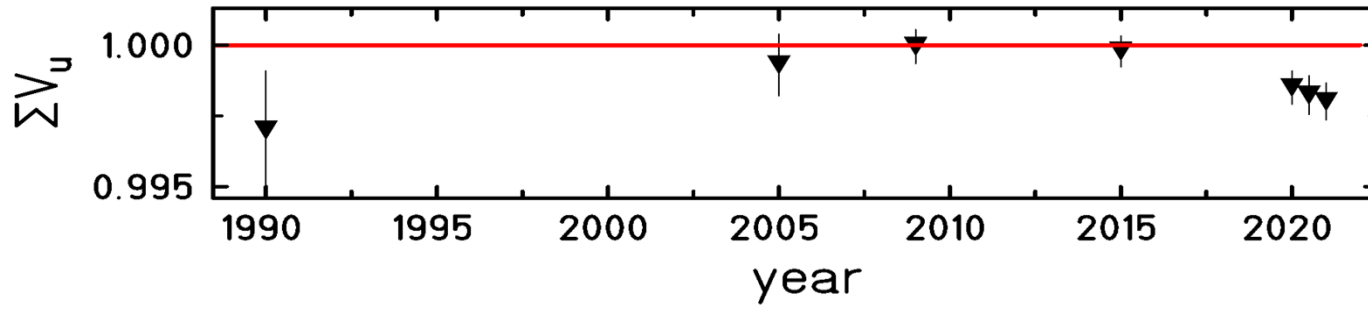
$$V_{us} = 0.2243 \pm 0.0005$$

$$V_{ub} = (3.94 \pm 0.36) \times 10^{-3}$$

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.9992 \pm 0.0007 \rightarrow 1.1\sigma$$

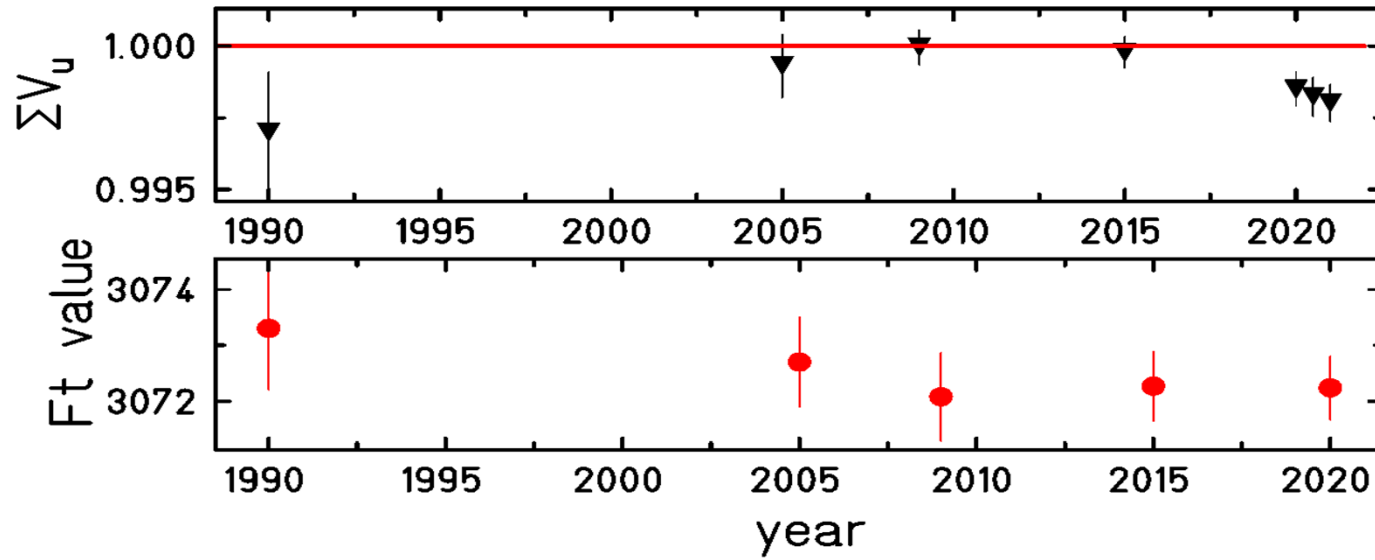
but also 3.1σ (see Hardy & Towner 2020)

● ● ● Evolution of ΣV_u , F_t , V_{ud} , V_{us} and Δ_R



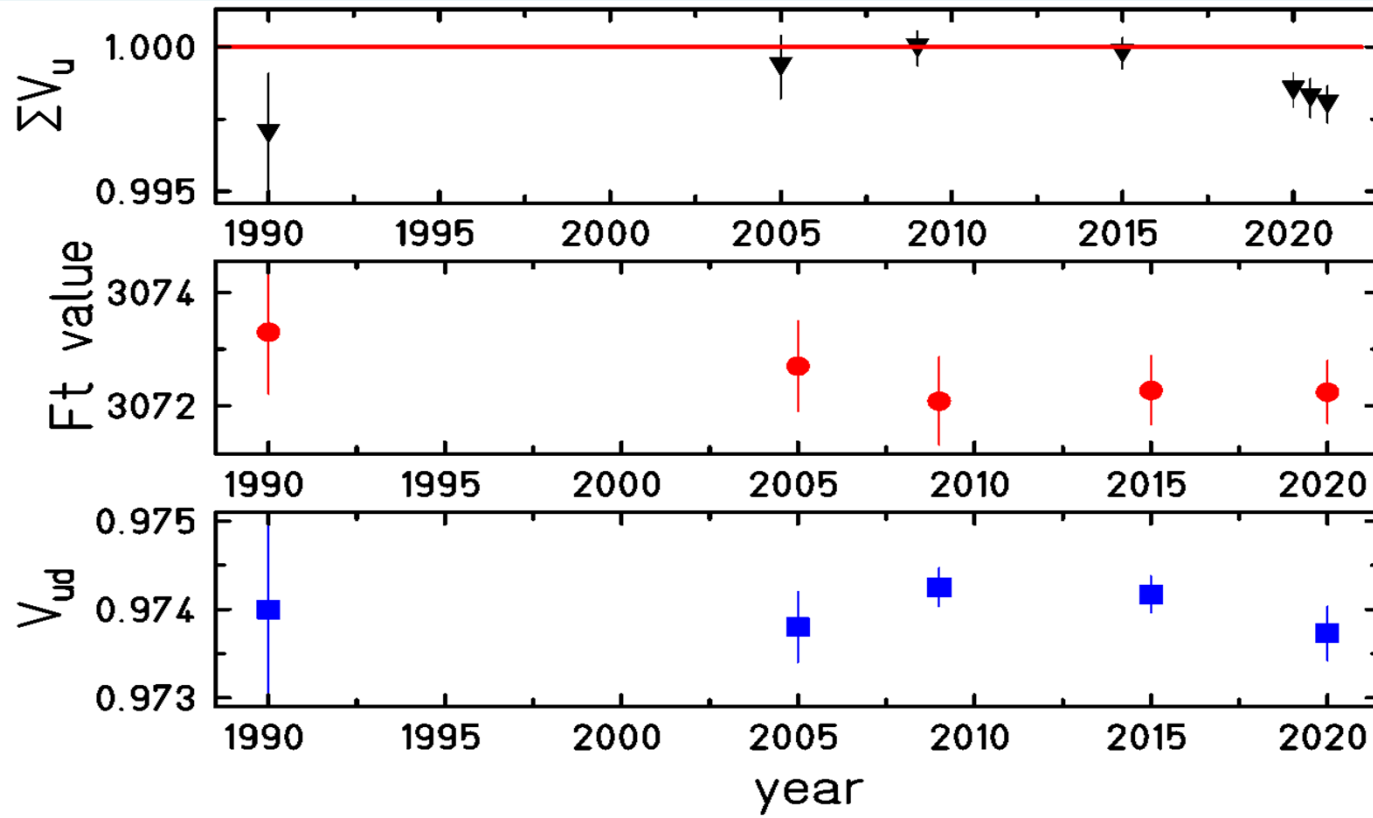
Hardy & Towner

● ● ● Evolution of ΣV_u , F_t , V_{ud} , V_{us} and Δ_R



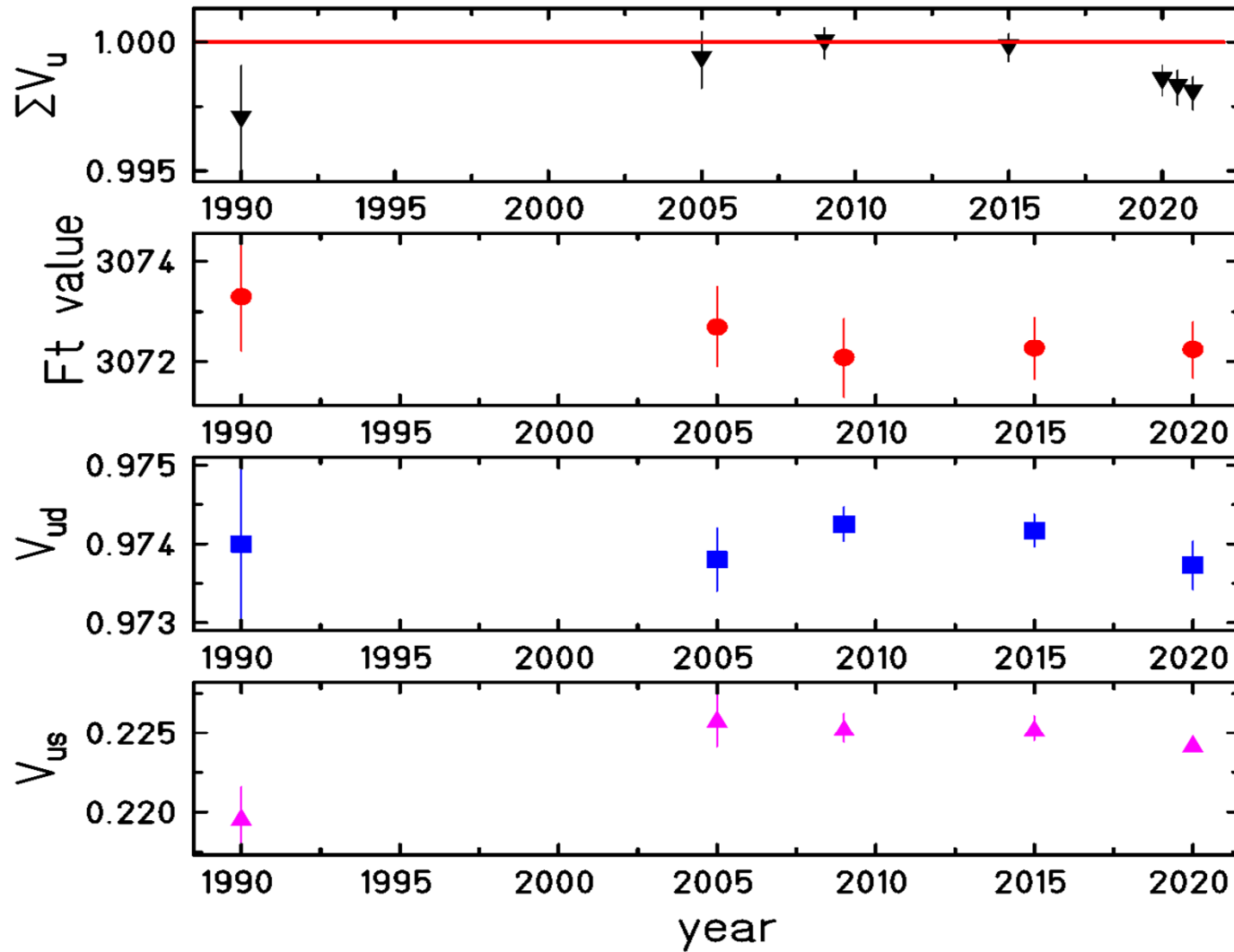
Hardy & Towner

● ● ● Evolution of ΣV_u , F_t , V_{ud} , V_{us} and Δ_R



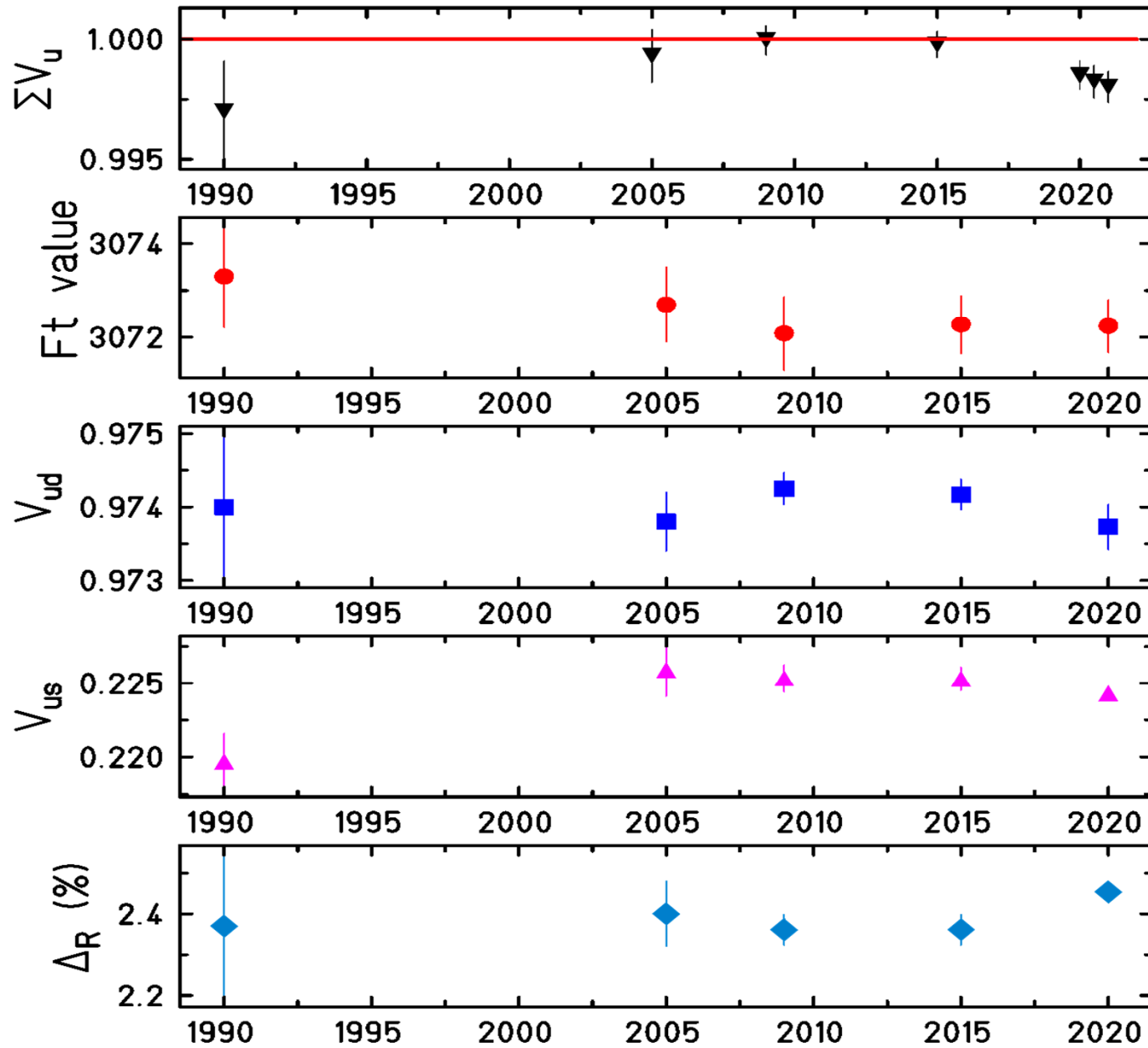
Hardy & Towner

● ● ● Evolution of ΣV_u , Ft , V_{ud} , V_{us} and Δ_R



Hardy & Towner

● ● ● Evolution of ΣV_u , Ft , V_{ud} , V_{us} and Δ_R

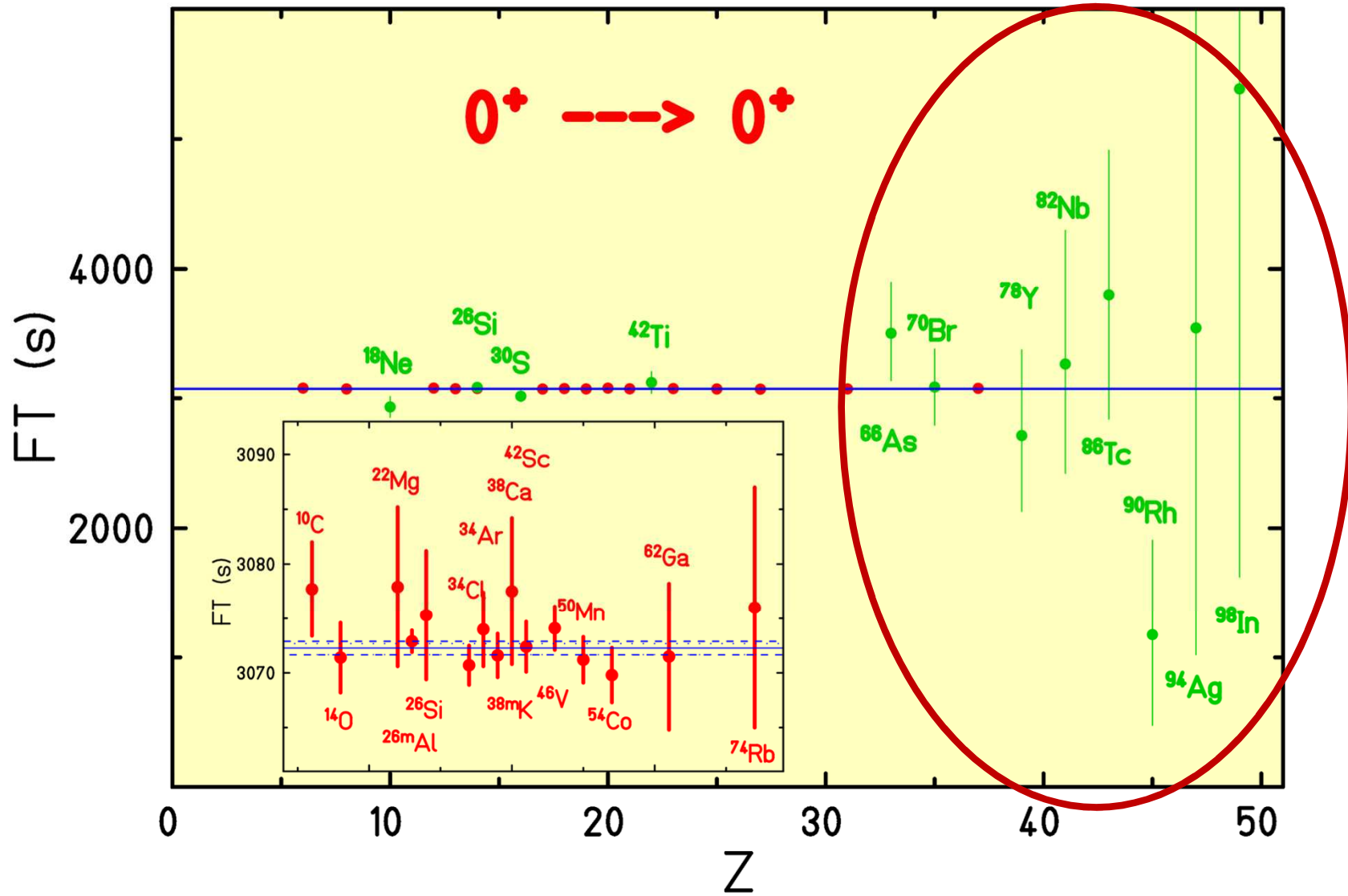


Hardy & Towerer



Future measurements at GANIL

● ● ● Heavy $T_z = 0$ nuclei



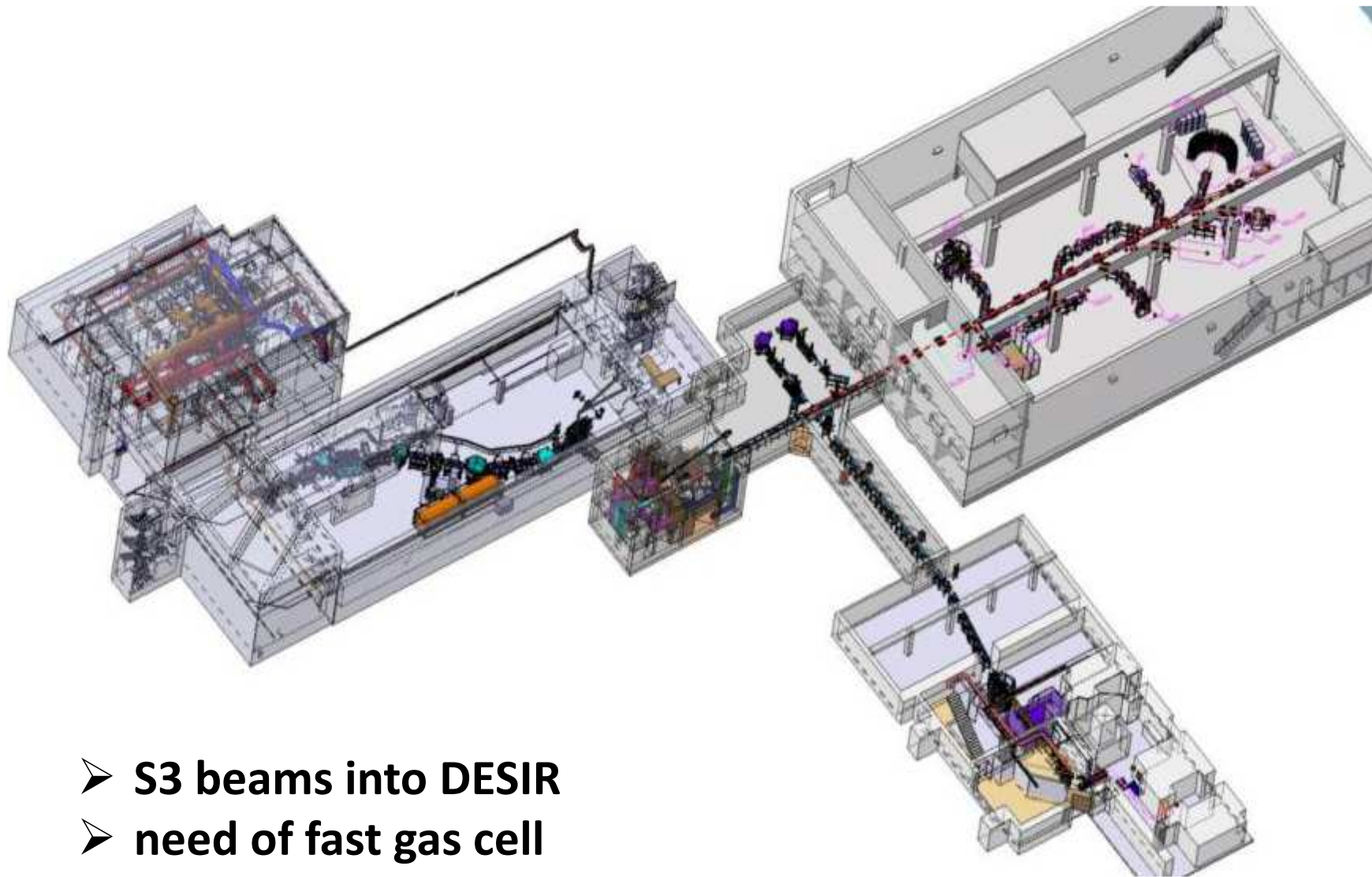
➤ test CVC on a much larger basis

● ● ● Heavy $T_z = 0$ nuclei: production at S3-LEB

isotope	half-life (ms)	rate day I (pps)	rate day II (pps)	rate A/Q=7 (pps)	rate A/Q=7 fast cell (20ms) (pps)
^{66}As	95.77(23)	75	450	750	4000
^{70}Br	79.1(8)	200	400	400	3000
^{74}Rb	64.78(3)	100	150	150	2000
^{78}Y	54(5)	10	10	15	300
^{82}Nb	50(5)	1.5	1.5	3	70
^{86}Tc	55(6)	1.5	1.5	3	50
^{90}Rh	15(7)	3e-4	4e-4	7e-4	30
^{94}Ag	37(18)	0.6	0.7	1	90
^{98}In	37(5)	5e-4	6e-4	1e-3	7e-2

➔ test CVC over a larger range of Z

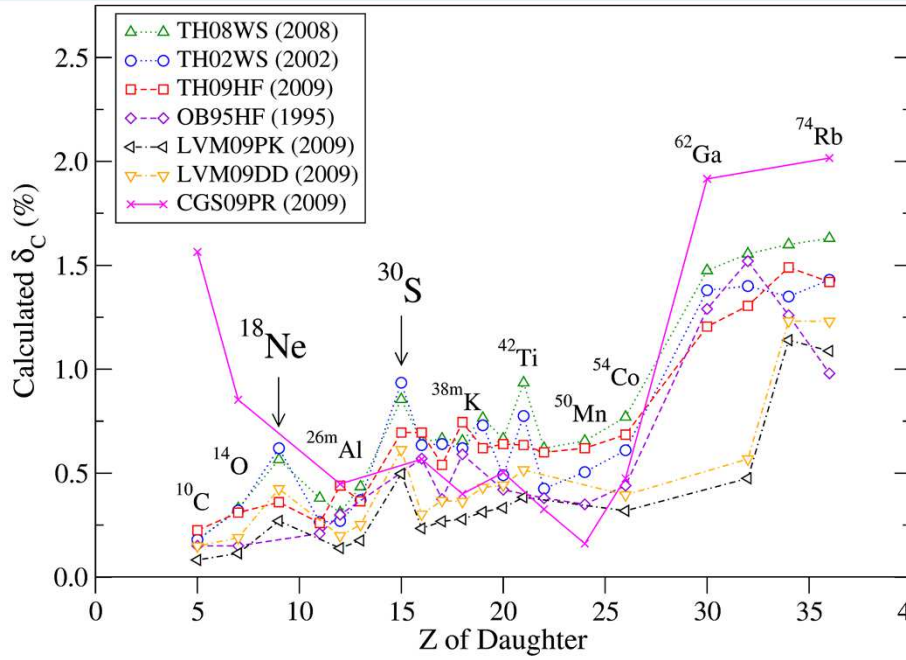
● ● ● S3-LEB + DESIR



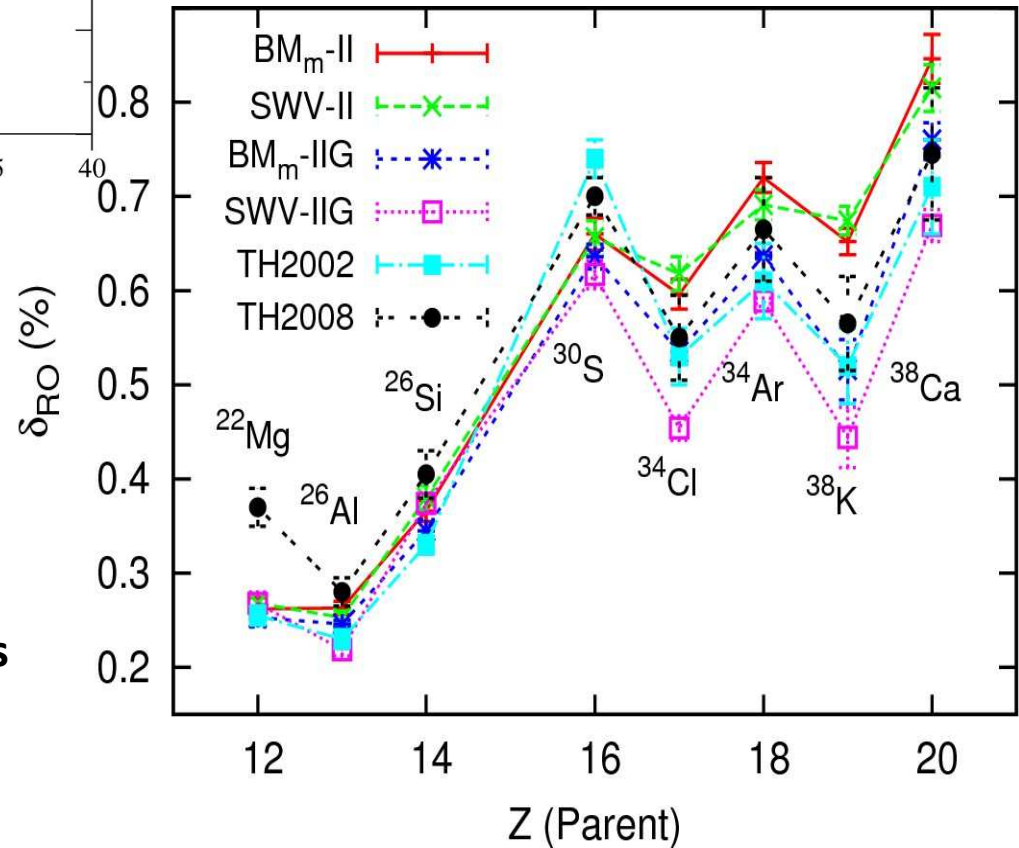
- S3 beams into DESIR
- need of fast gas cell
- purification with HRS + MR-TOF-MS or PIPERADE
- best place world-wide to do this

● ● ● $0^+ \rightarrow 0^+$ decays: new theoretical corrections for δ_c

N. Smirnova, Y. Lam, L. Xayavong et al.



previous calculations



new calculations



Search for scalar contributions

• • • $0^+ \rightarrow 0^+$ decays: limits on exotic currents

- standard model assumption: only vector current

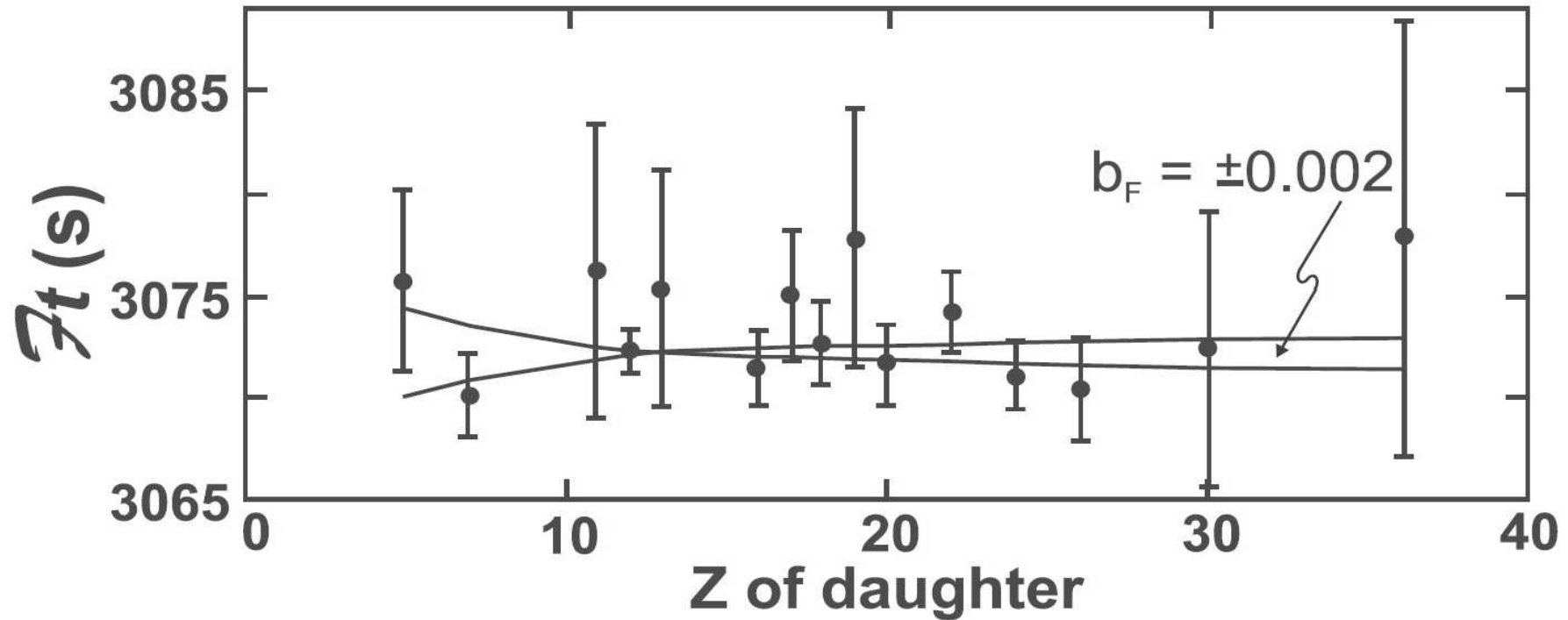
$$dW = dW_0 \left(1 + a \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} \right)$$

- if scalar currents, we obtain for \mathcal{F}_t

$$dW = dW_0 \left(1 + a \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} \right)$$

- $\mathcal{F}_t \rightarrow \mathcal{F}_t * \left(1 + \frac{y b_F}{\langle W \rangle} \right)$, $y^2 = 1 - Z^2 \alpha^2$
- limit on scalar current from term in \mathcal{F}_t function: $(1 + b_f y / \langle W \rangle)$

• • • $0^+ \rightarrow 0^+$ decays: limits on exotic currents

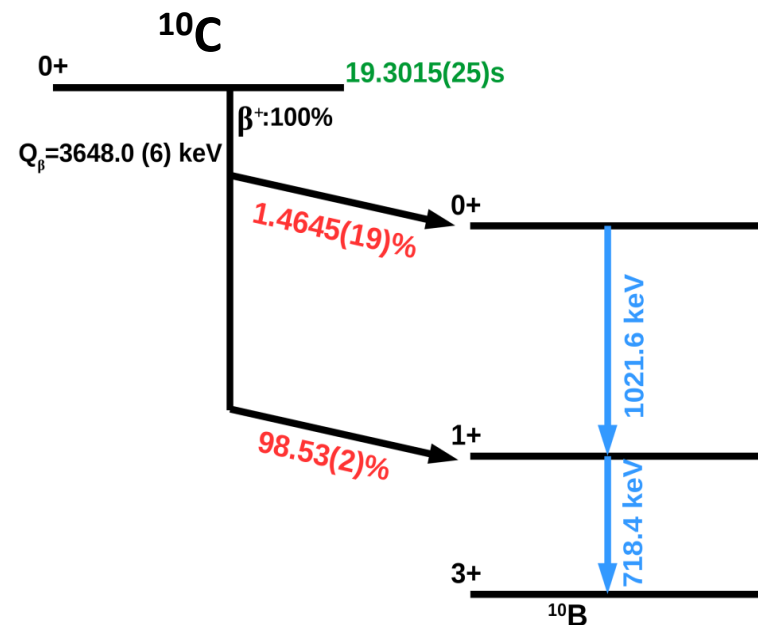
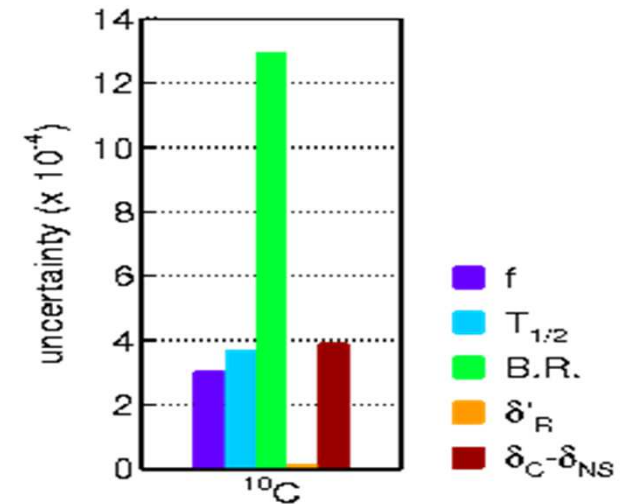


- from β decay: $b_F = 0.0000 \pm 0.0020 \sim \left(\frac{C_s + Cs'}{C_V} \right)$
- ➔➔ improve on low- Z nuclei

● ● ● $0^+ \rightarrow 0^+$ decays: ^{10}C error budget

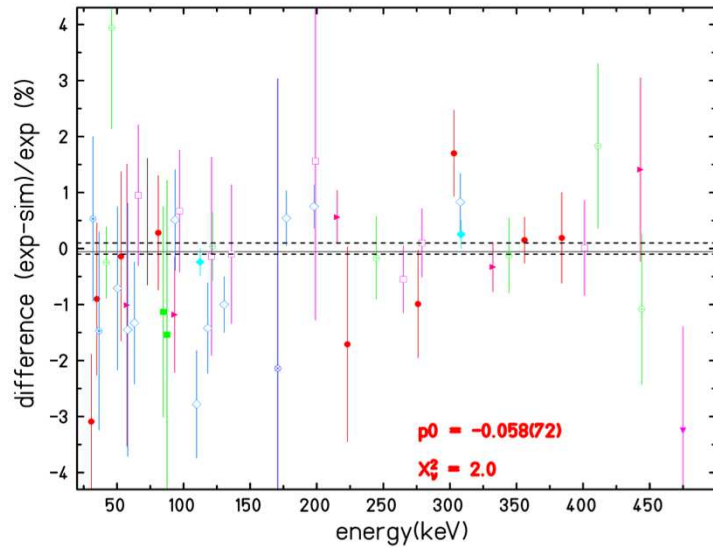
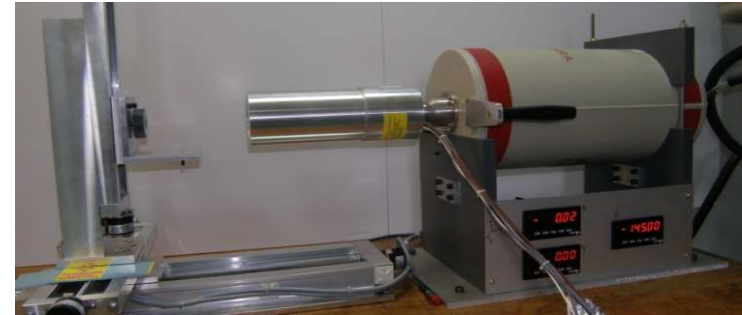
- BR by far largest error
- two precise measurements:
 - Savard et al.: 1.4625(25)%
(PRL 74 (1995) 1521)
 - Fujikawa et al.: 1.4665(38)%
(PLB 449 (1999) 6)
- measurements with Ge multi-detector array

our approach:
re-measuring the BR of ^{10}C
with out precisely calibrated
Germanium detector



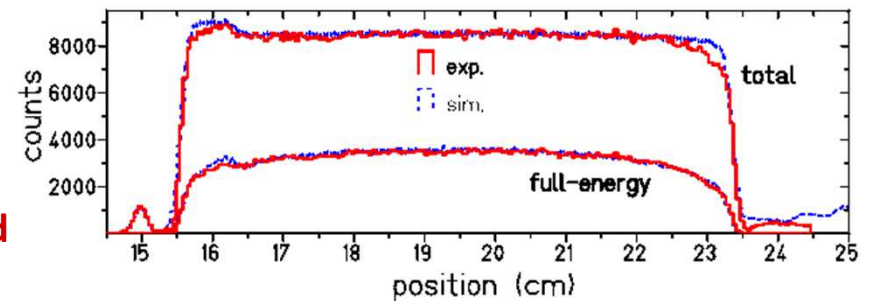
● ● ● Calibration of germanium detector

- $\Delta\epsilon_{\text{rel}} = 0.1\%$, $\Delta\epsilon_{\text{abs}} = 0.15\%$
- calibration programme of a HP Ge detector:
 - x-ray photography of detector
 - scan of the crystal at CSNSM Orsay
 - source measurements at CENBG, IPNO, ISOLDE
 - MC simulations: CYLTRAN, GEANT4



X-ray
photography

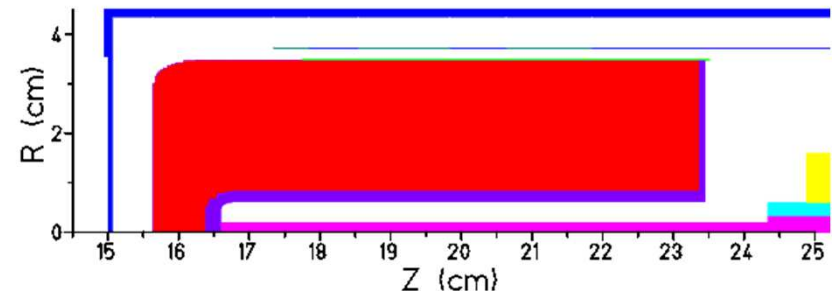
Scan at
CSNSM:
 ^{137}Cs
strongly
collimated



Relative detection efficiency:

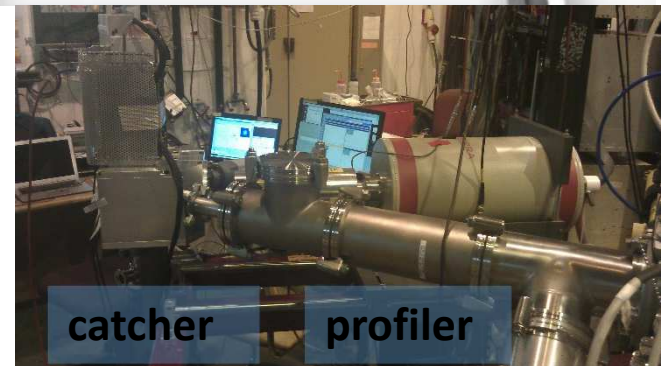
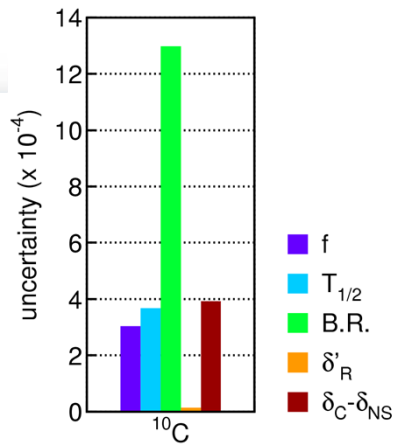
^{24}Na , ^{27}Mg , ^{48}Cr , ^{56}Co , ^{60}Co , ^{66}Ga , ^{75}Se , ^{88}Y , ^{109}Cd ,
 ^{133}Ba , ^{134}Cs , ^{137}Ce , ^{152}Eu , ^{169}Yb , ^{180}Hf , ^{207}Bi

Peak/total: ^{22}Na , ^{38}K , ^{41}Ar , ^{51}Cr , ^{54}Mn , ^{57}Co , ^{58}Co , ^{60}Co ,
 ^{65}Zn , ^{85}Sr , ^{137}Cs ...ISOLDE, IPNO sources

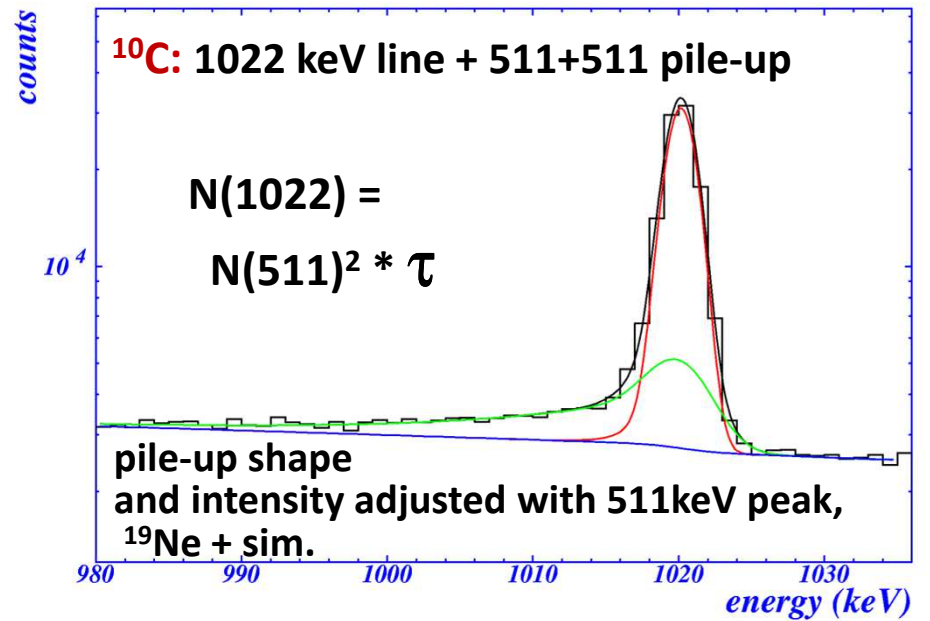
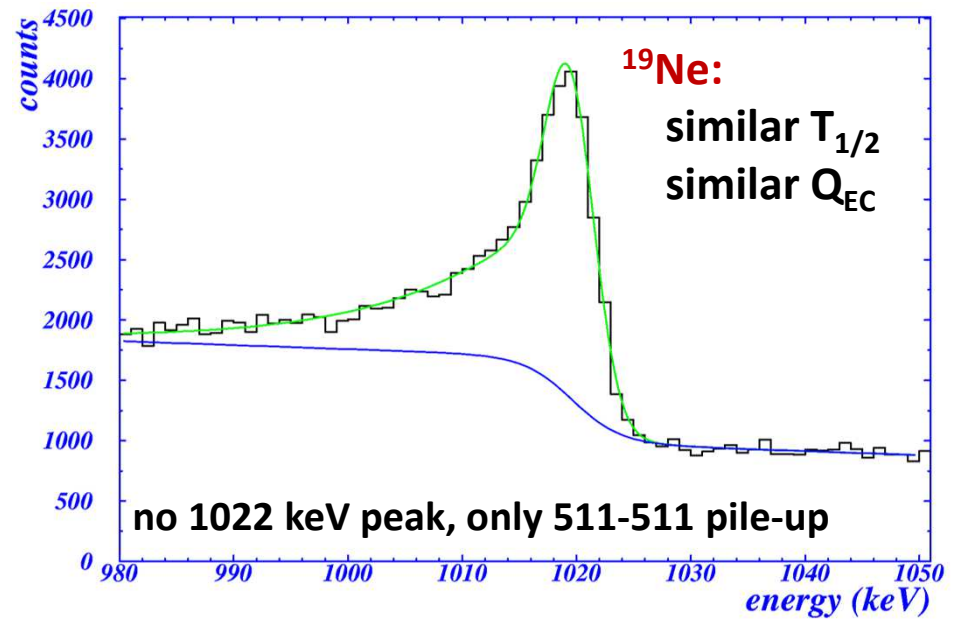
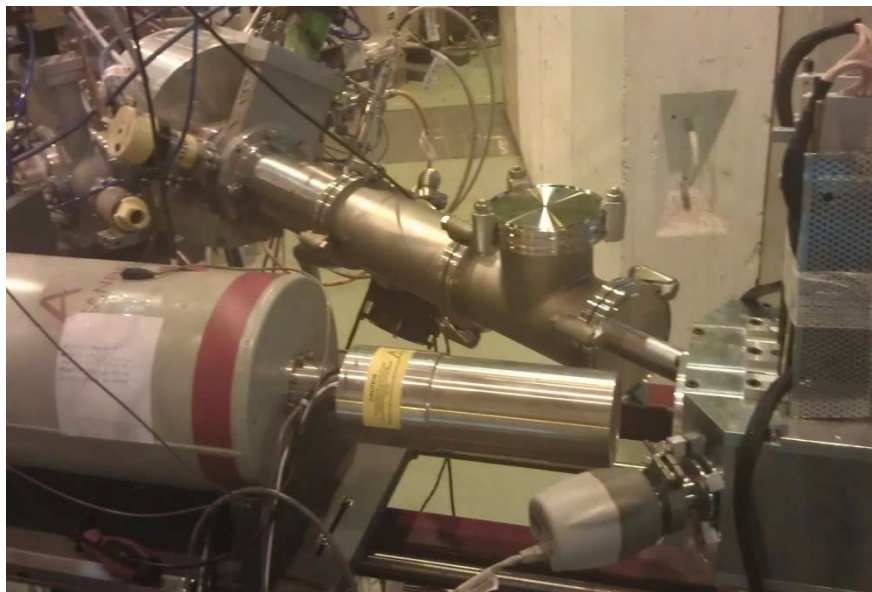
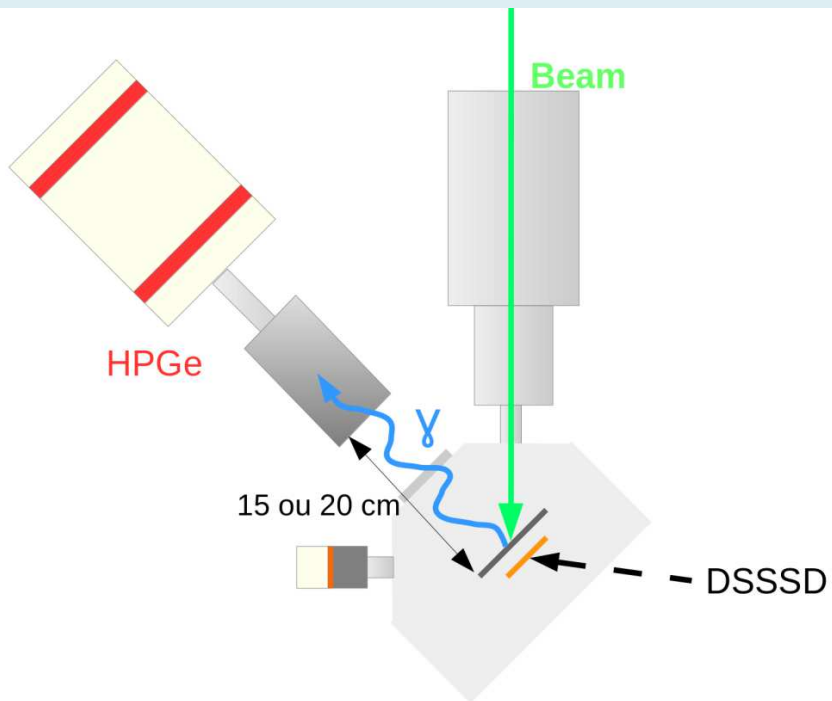


● ● ● ^{10}C measurement at ISOLDE

Proton beam at 1.4 GeV and $2\mu\text{A}$
 Target: CaO
 Source: VADIS

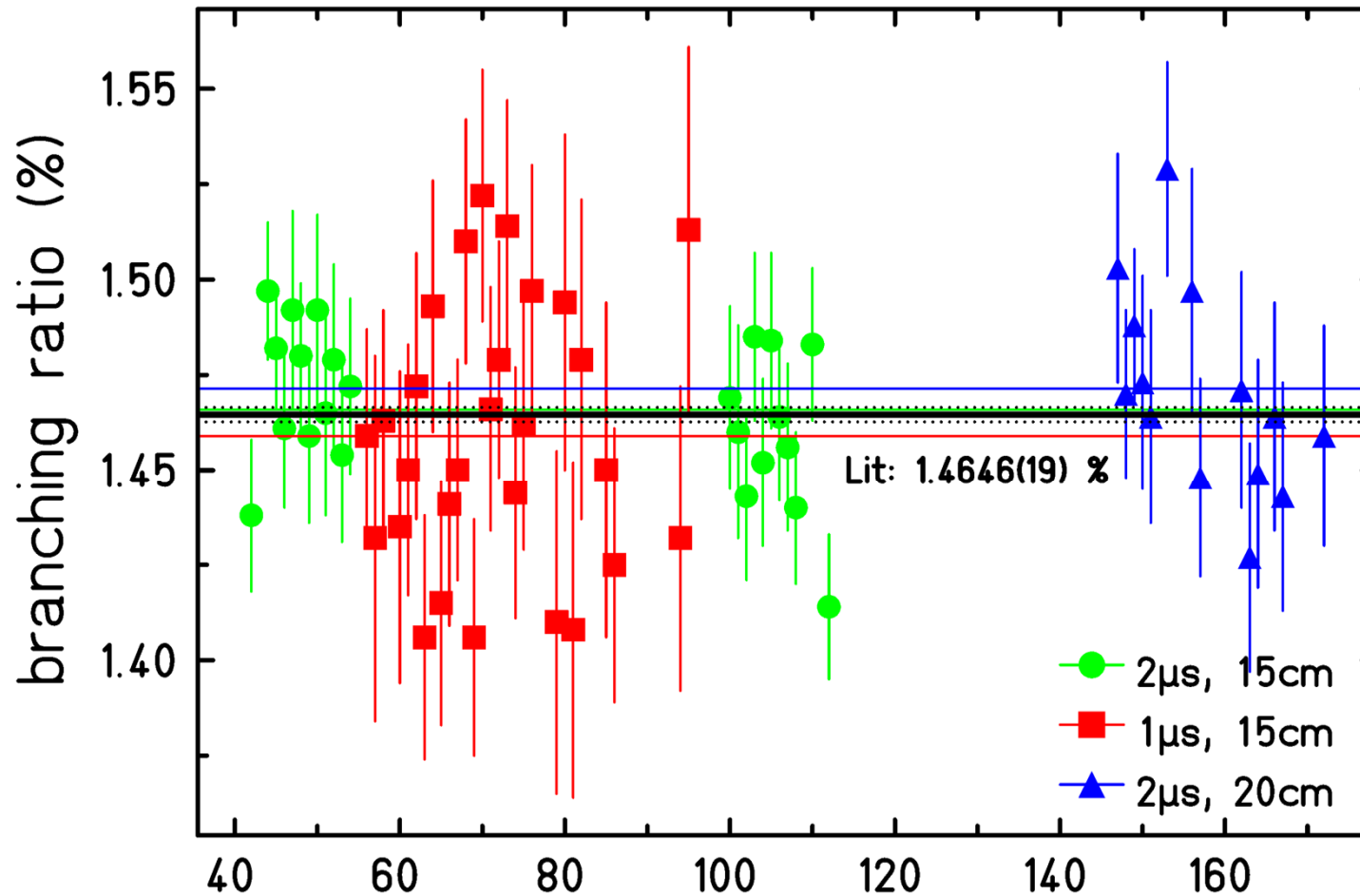


• • • ^{10}C experimental set-up and analysis procedure



● ● ● Super-allowed branching ratio of ^{10}C

Blank et al., EPJA56 (2020) 156



next attempt:

Final result:

Literature:

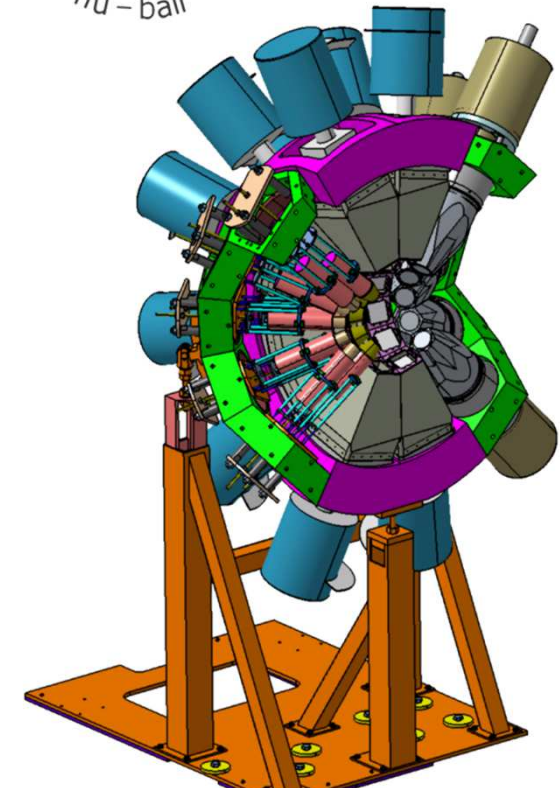
• higher statistics: difficult...

• higher purity: MR-ToF selection

statistics: 0.0039 %

pile-up: 0.0030 %

● ● ● ^{10}C measurement at ALTO/Orsay



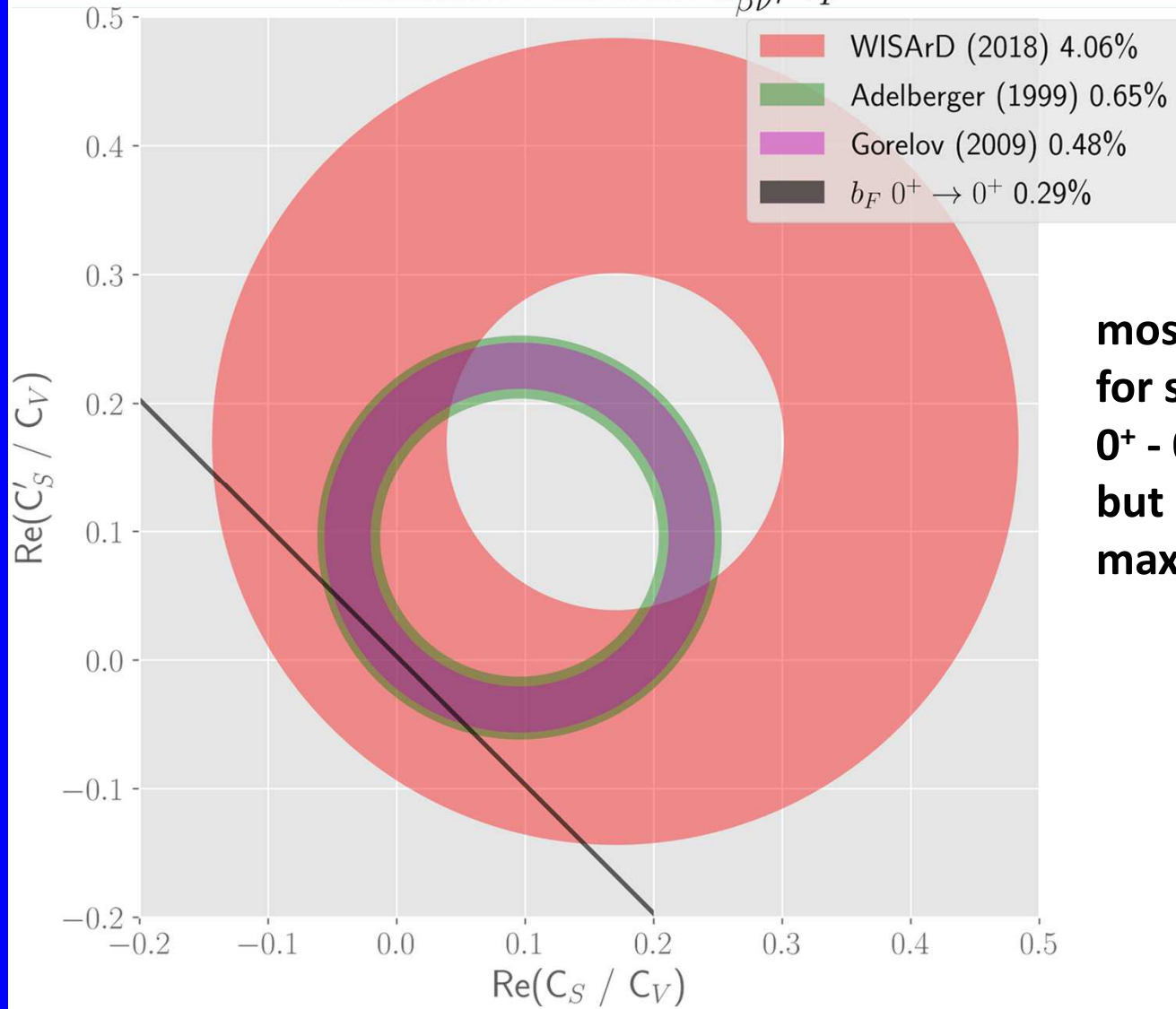
Scientific Manager: M. Lebois
Technical Manager: B. Genolini

100 Ge crystals: 5.5% @ 1 MeV
18 LaBr₃: 1.5% @ 1 MeV

data under analysis.... ...also statistics limited

● ● ● Conclusions

Exclusion Plot from $\tilde{a}_{\beta\nu}^F, b_F$



**most stringent limits
for scalar currents from
 $0^+ - 0^+$ β decay,
but only in model with
maximal parity violation**

● ● ● Conclusions

- most stringent limits for scalar currents from $0^+ - 0^+$ β decay, but only in model with maximal parity violation
 - if no parity violation for scalar currents, no sensitivity
- need for improved Ft values for light nuclei ^{10}C , ^{14}O
- interest in heavier $0^+ - 0^+$ decays to improve CVC condition
- more efforts needed from theory to better define corrections

Thanks for your attention