

Clustering away from stability using quasifree knockout reactions

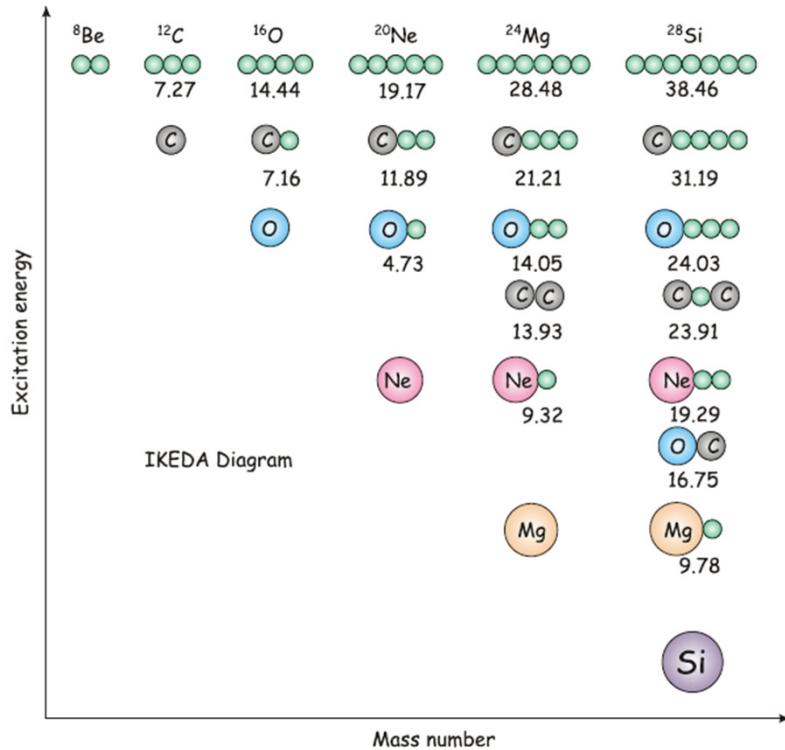
D.Beaumel
IJCLab, Orsay

- Introduction
 - Ikeda and beyond
 - Clustering in neutron rich nuclei towards the dripline
 - Beyond alpha clustering
- Cluster Knockout reactions
- First results on neutron-rich Be isotopes
alpha clustering vs triton clustering
- Neutral clusters : recent results on tetraneutron and outlooks

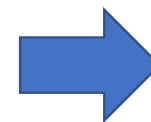
Clustering in light nuclei

The Ikeda diagram

For $N=Z=2n$ "alpha-conjugate" nuclei



- Cluster structure typically occurs close to cluster decay thresholds
- Based on properties of some near threshold states
 - ✓ Rotational bands with molecule-like structure
 - ✓ Very large moment of inertia
 - ✓ Large alpha-decay widths



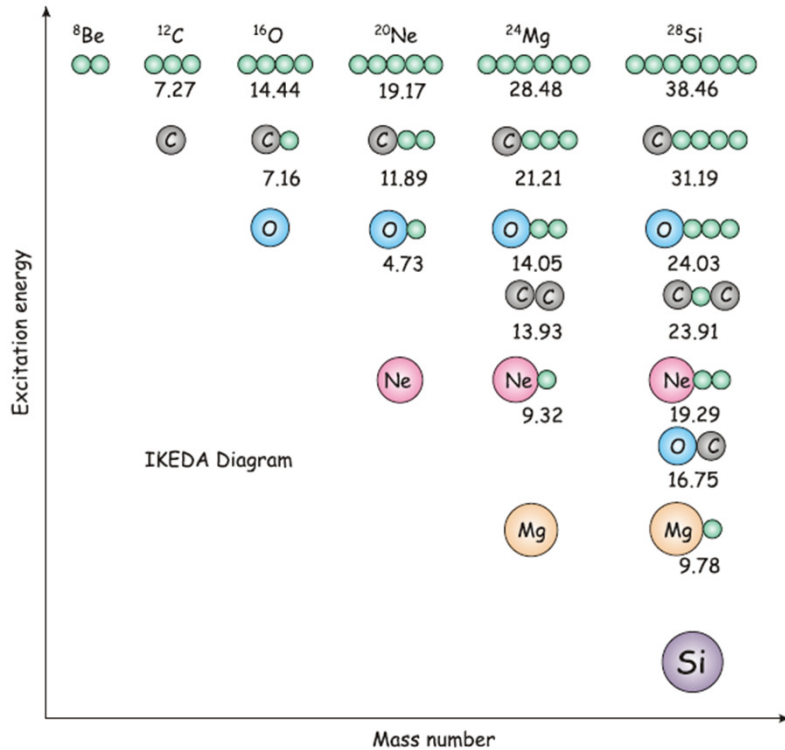
Unified picture of clustering

K.Ikeda, N.Takigawa, H.Horiuchi, **PTP (1968)**

Clustering in light nuclei

The Ikeda diagram

For $N=Z=2n$ "alpha-conjugate" nuclei



K.Ikeda, N.Takigawa, H.Horiuchi, *PTP* (1968)

Case of ^8Be

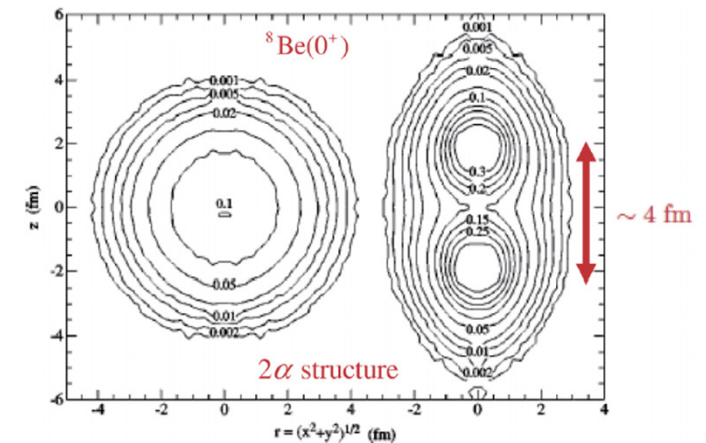
- Cluster state is the ground-state (specific case)
- Recognized as alpha-cluster state in the late 50's
 - Rotational levels, large moment of inertia

ab initio calculations for ^8Be

R.B. Wiringa, S.C.Pieper, J.Carlsson, V.R. Pandharipande, *PRC* 62 (2000)

Green's function Monte-Carlo

nucleon-nucleon interaction: 2-body (AV18) + 3-body (Urbana IX)

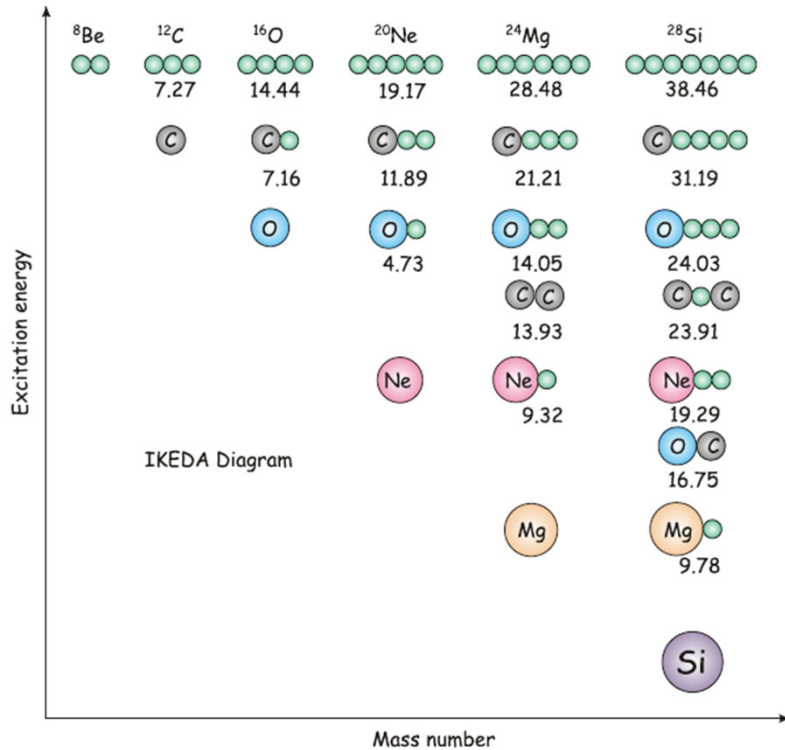


- $0+, 2+, 4+$ sequence in ^8Be well-reproduced by calc.
- For precise properties, need take into account continuum coupling

Clustering in light nuclei

The Ikeda diagram

For $N=Z=2n$ "alpha-conjugate" nuclei



IKEDA Diagram

K.Ikeda, N.Takigawa, H.Horiuchi, **PTP (1968)**

The Hoyle state in ^{12}C

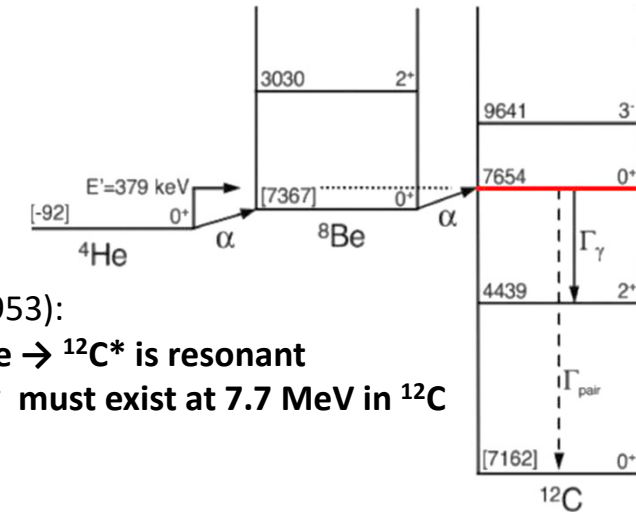
Synthesis of elements heavier in ^4He (no stable isotopes $A=5,8$)

Fusion of 3α in ^{12}C in 2 steps:

- $\alpha + \alpha \leftrightarrow {}^8\text{Be}$
 $\tau({}^8\text{Be}) = 9.7 \times 10^{-17} \text{ s}$
- $\alpha + {}^8\text{Be} \rightarrow {}^{12}\text{C}^*$



Fred Hoyle (1915 - 2001)



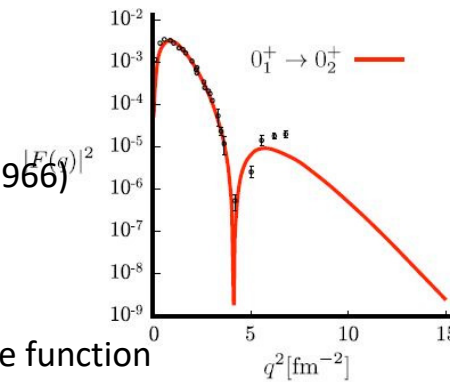
F.Hoyle (1953):

- ✓ $\alpha + {}^8\text{Be} \rightarrow {}^{12}\text{C}^*$ is resonant
- ✓ a $J^\pi=0^+$ must exist at 7.7 MeV in ^{12}C

Cluster Structure of the Hoyle state

- Large radius needed to reproduce its width (Barker and Treacy, NP1962)
→ **Large degree of alpha clustering**
- Suggested as linear alpha chain (Morinaga, PL1966)
- Recently: Study of decay modes
- Description as an alpha condensate

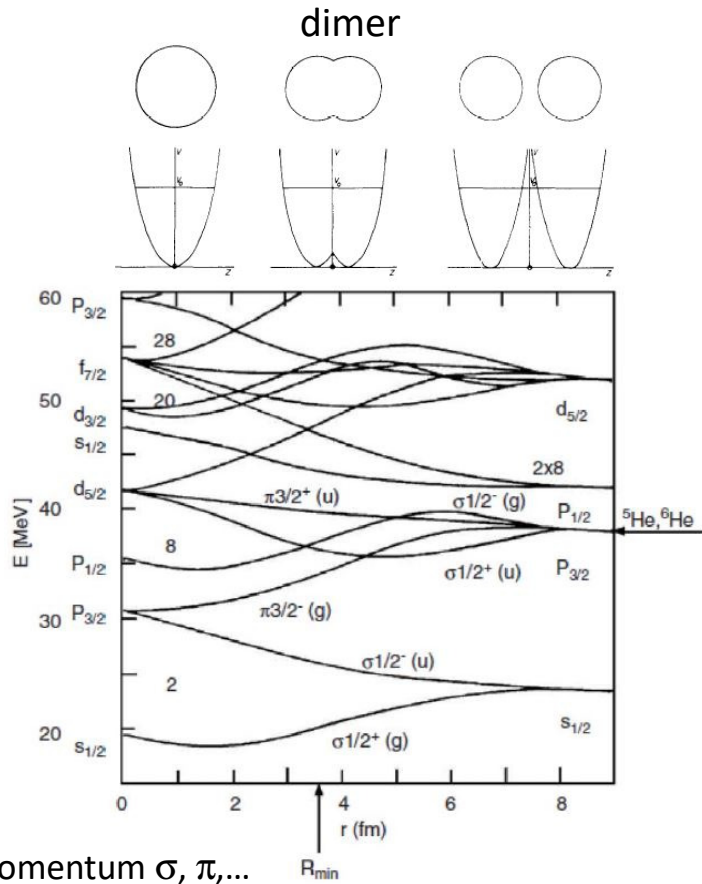
Tohsaki, Horiuchi, Schuck, Röpke (THSR) wave function
Volume [Hoyle state] = 3~4 times x Vol [GS]
Also: FMD calculations



Adding neutrons to $N=Z$ core

Two-center Shell Model

Scharnweber, Greiner, Mosel, Nucl.Phys. A164(1971)
 Von Oertzen, Z.Phys. A357, 355 (1997)



Angular momentum σ, π, \dots

Spin projection, parity

Generalization : dimers \rightarrow polymers

Antisymmetrized Molecular Dynamics

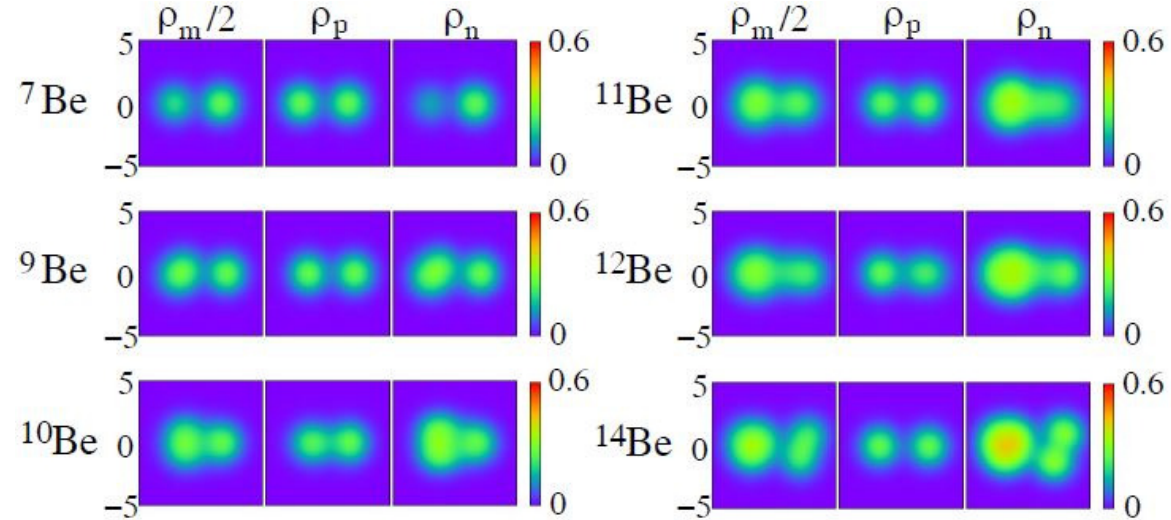
No assumption of preformed clusters

Early calculations for Be and B cases

Kanada-En'yo, Horiuchi, Ono, PRC 52, 628 (1995)

Kanada-En'yo, Horiuchi, PTP 142, 205(2001)

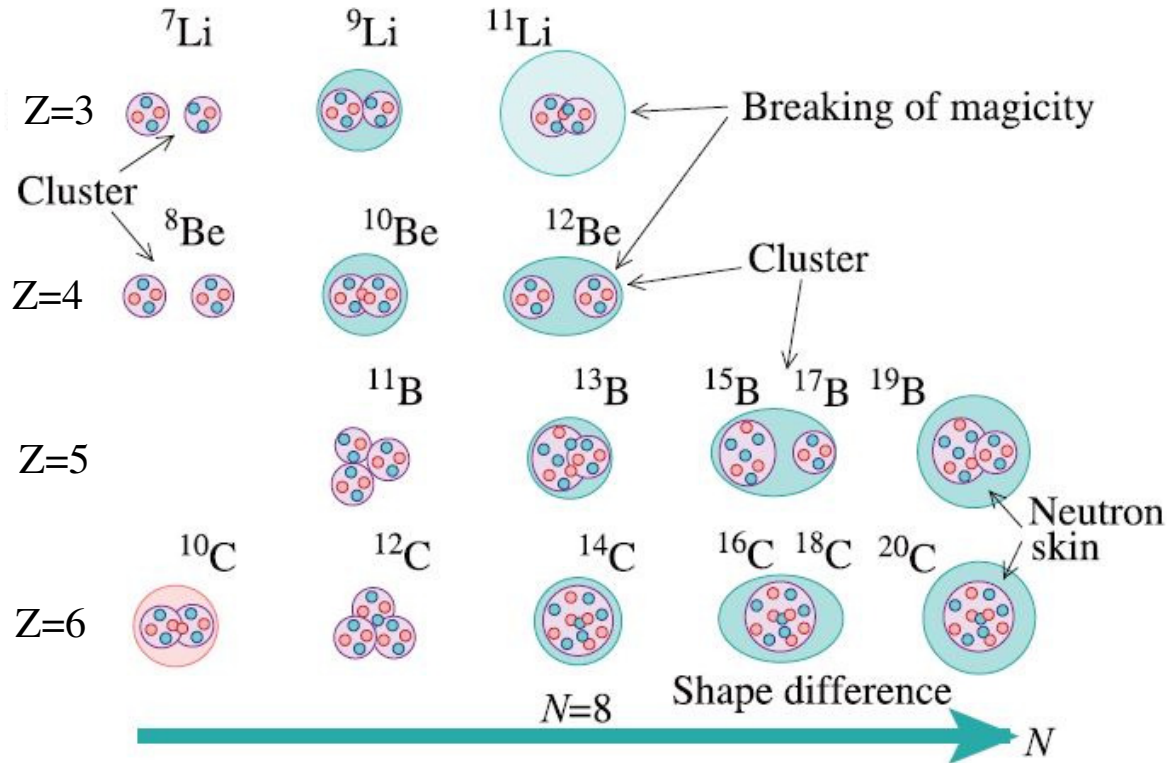
Recent calculations for Be ground-states



Kanada-Enyo, PRC91, 014315(2015)

Clustering in light neutron-rich nuclei

GROUND-STATES !



Antisymmetrized Molecular Dynamics (AMD)

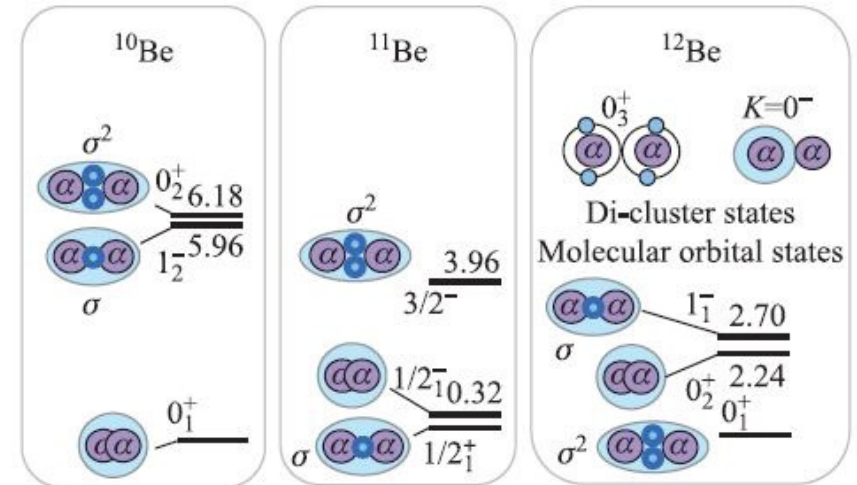
Y.Kanada-En'yo, H.Horiuchi, Front. Phys. 13 (2018)

When Adding neutrons to $N=Z$ nuclei:

Various Molecular structures

Neutron orbiting around the core of clusters for low-lying states including the ground-state

Case of neutron rich Be



π orbit \leftrightarrow p-orbit in SM limit – reduce clustering

σ orbit \leftrightarrow sd intruder configuration – enhance clustering

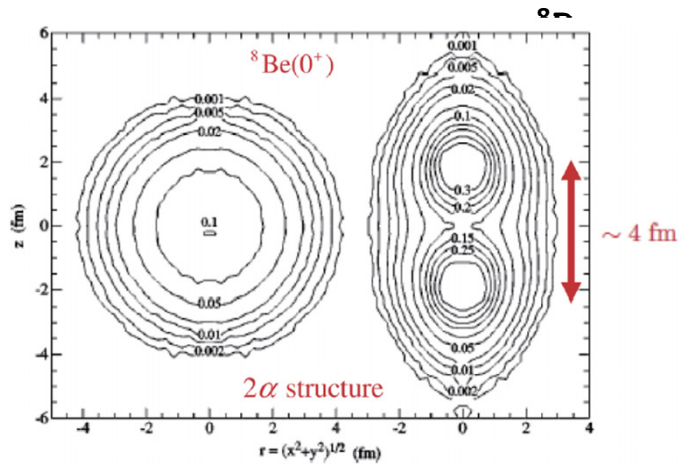
Calls for direct evidence of Molecular structure !

Calculations from first principles for Be isotopes

QMC calculation for ^8Be

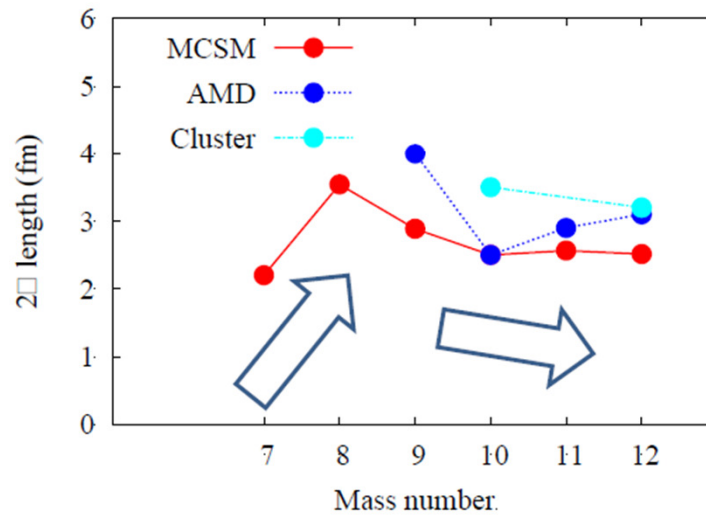
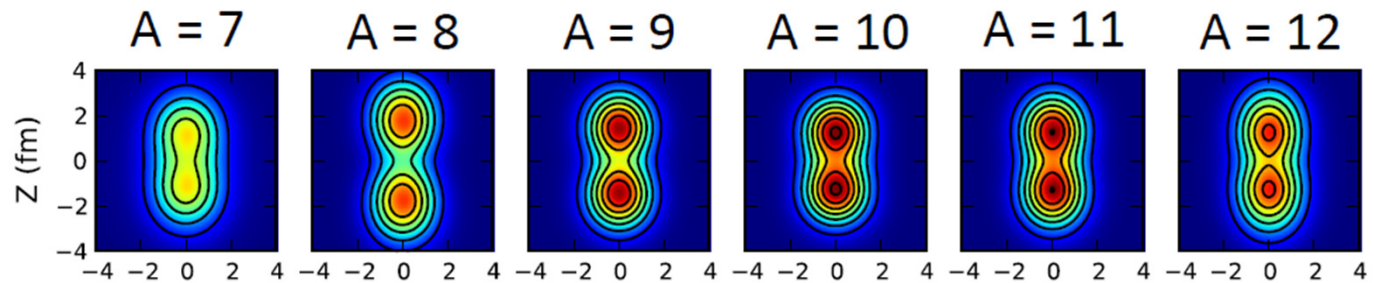
R.B. Wiringa, S.C. Pieper, J. Carlson,
V.R. Pandharipande
Phys. Rev. C 62 (2000)

Quantum Monte-Carlo
AV18 + Urbana IX

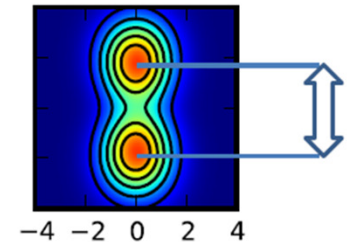


Rotational band well reproduced

Be isotopes in no-core Monte-Carlo Shell Model



Definition:
Distance btw the positions of
each highest proton density



Courtesy T. Abe (2019)

AMD: Y. Kanada-En'yo, *Phys. Rev. C* 68, 014319 (2003)

Cluster: M. Ito & K. Ikeda, *Rep. Prog. Phys.* 77, 096301 (2014)

Calculations from first principles for Be isotopes

QMC calculation for ^8Be

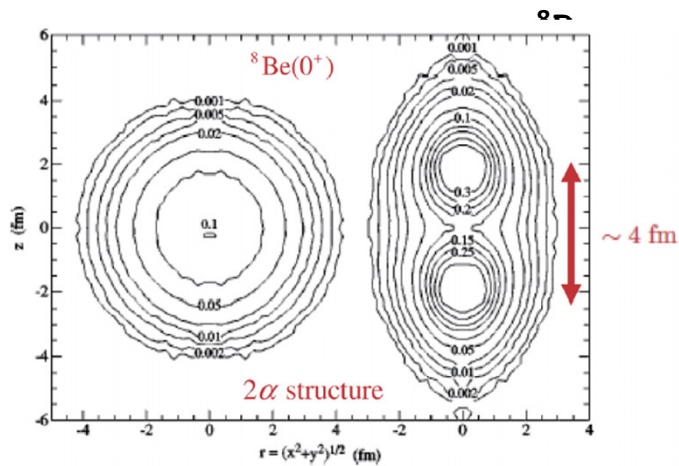
R.B. Wiringa, S.C. Pieper, J. Carlson,

V.R. Pandharipande

Phys. Rev. C 62 (2000)

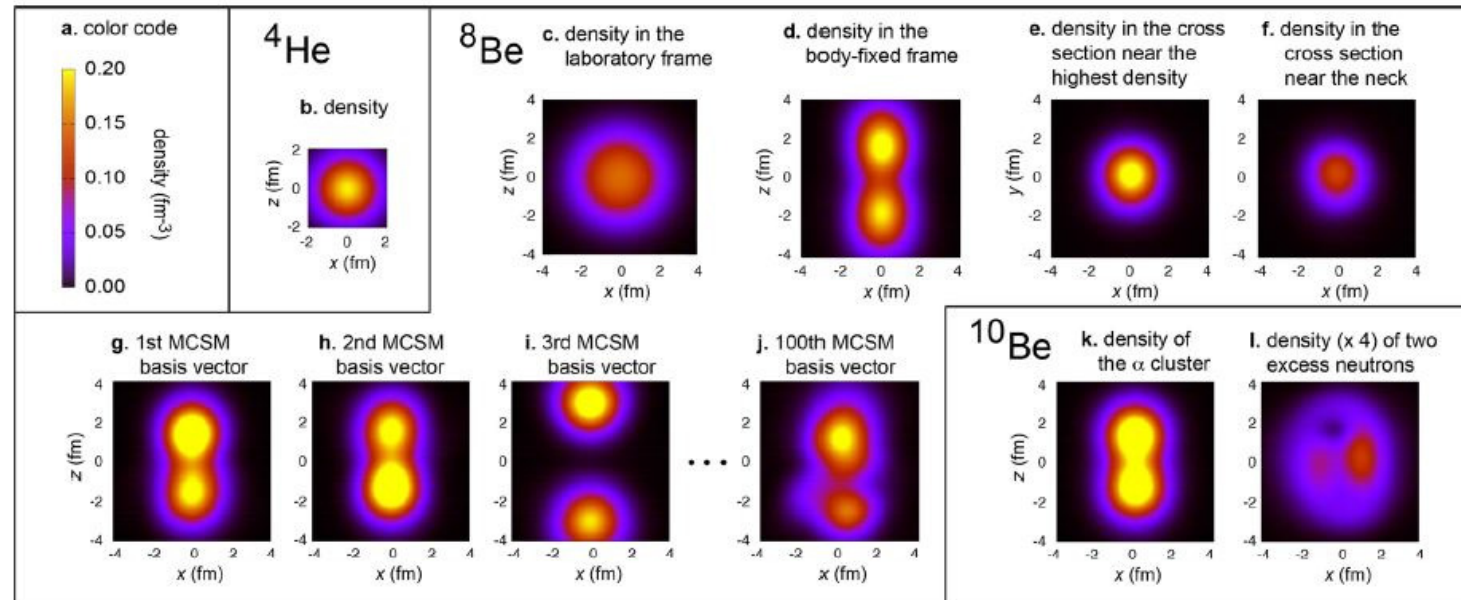
Quantum Monte-Carlo

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Be isotopes in no-core Monte-Carlo Shell Model

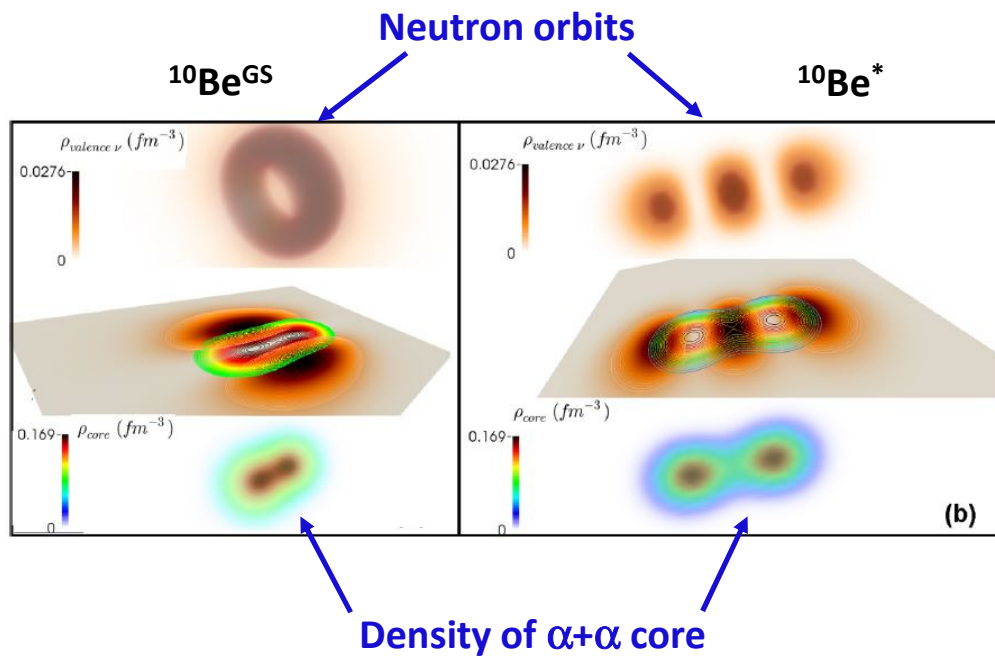


T.Otsuka, T.Abe et al., Nature comm. 2022

Density Functional Theory studies for clustering in light nuclei

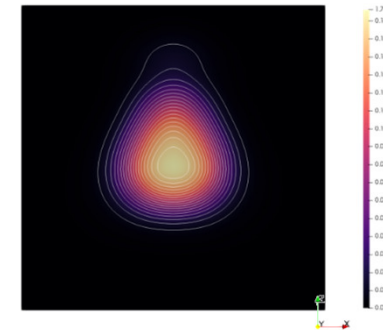
DDME2 relativistic functional in rel. HB calculations

J.P.Ebran, E.Khan, T.Niksic, D.Vretenar, PRC90 (2014)

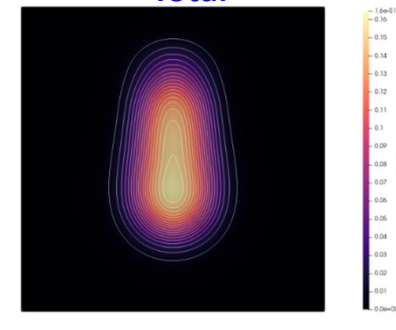


Recent calculations for ^{12}Be
Rel. HB with DD-PC1 + projected GCM

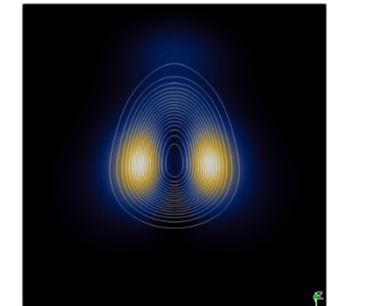
^{12}Be GS
Total



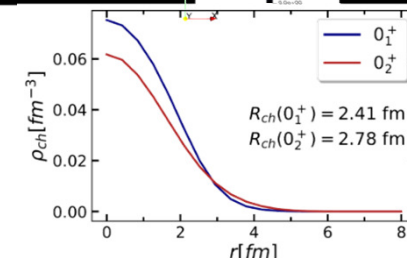
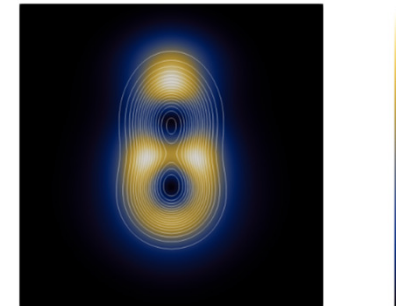
^{12}Be G(0_2^+)
Total



Valence neutrons

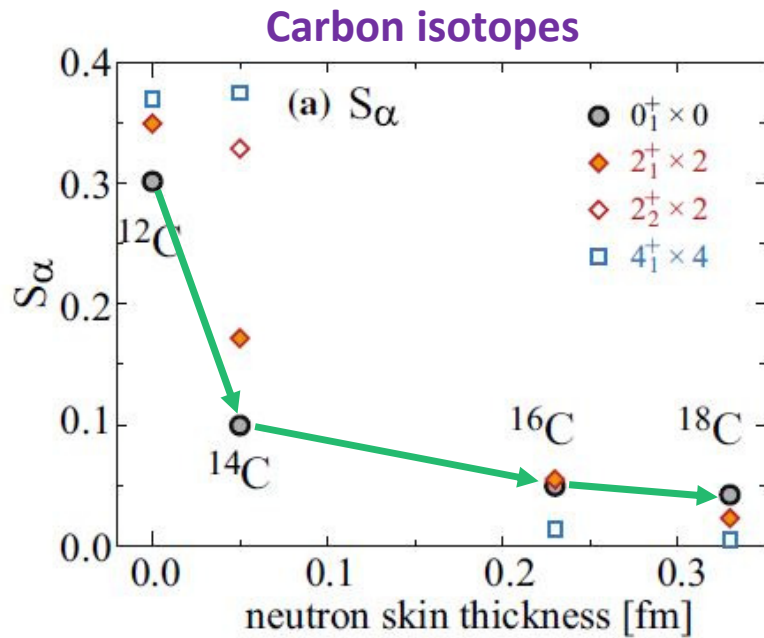


Valence neutrons



J.P.Ebran, et al.

Clustering evolution towards the dripline



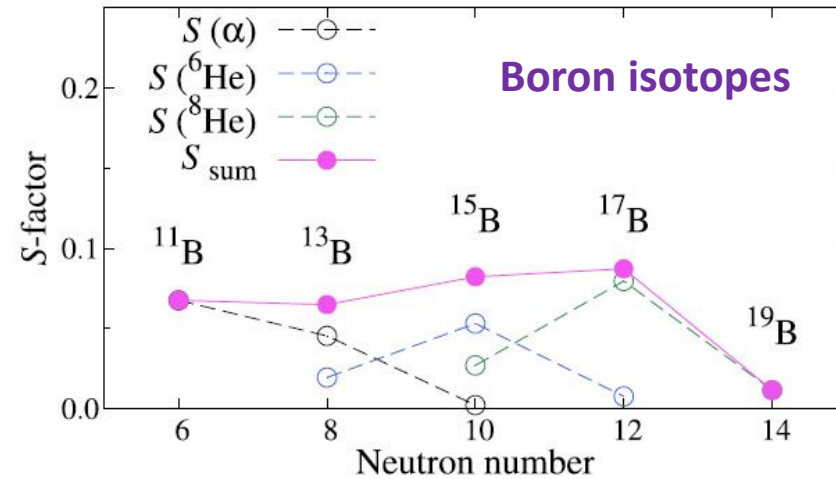
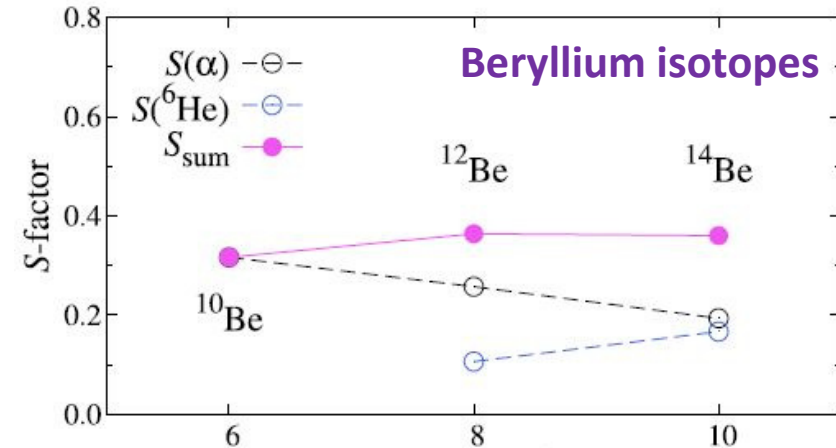
Q. Zhao, Y. Suzuki, J. He, B. Zhou, M. Kimura,
EPJA 157 (2021)

AMD calculations using Gogny D1S functional

Hindrance effect due to neutron skin ?

Alternative interpretations

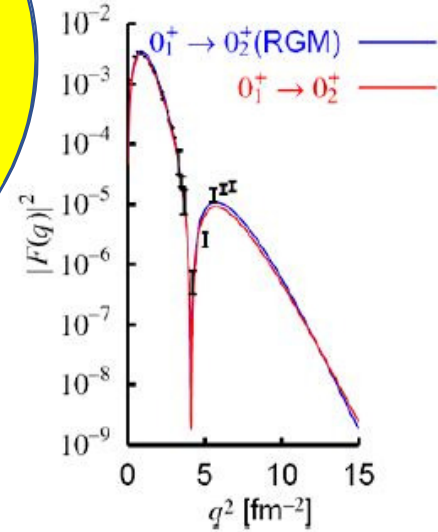
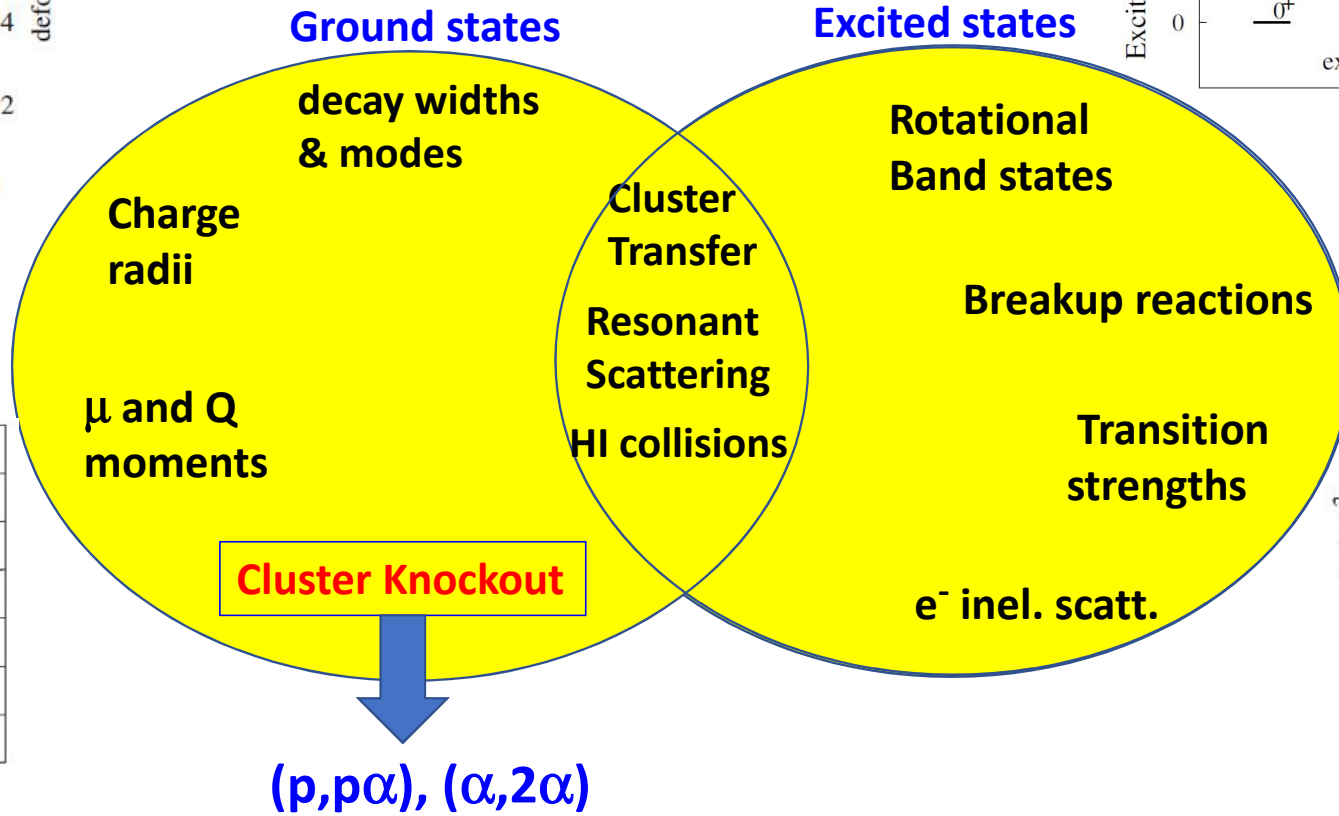
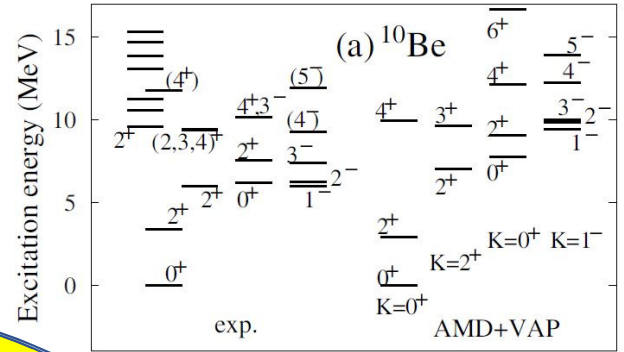
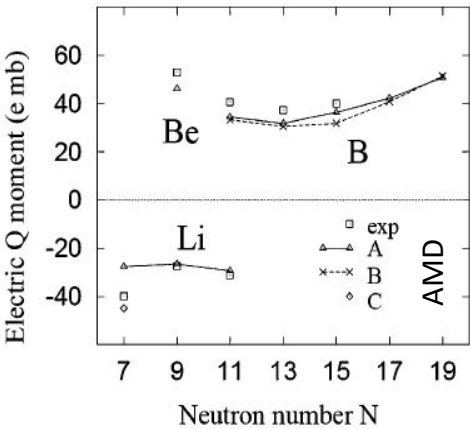
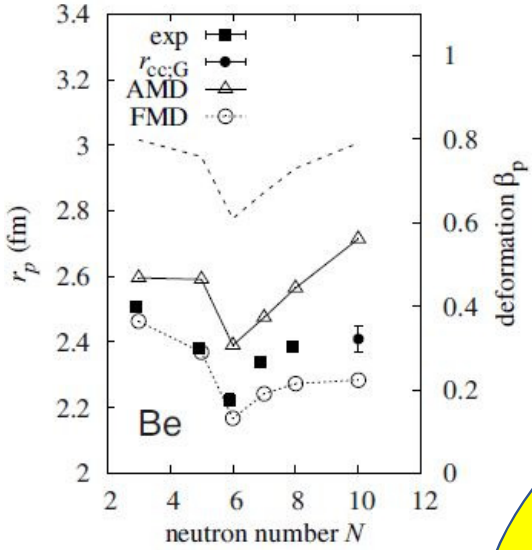
- Neutron single-particle configurations
- Relationship between α -clustering and α -threshold



H.Motoki, et al, PTEP (2022)113D01 - AMD calculations using Gogny D1S

- Hindrance of α clustering
- Development of ^6He clustering

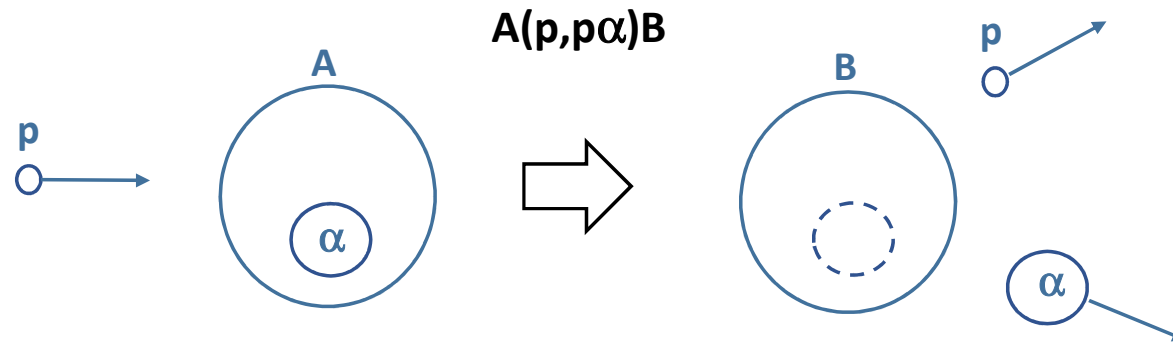
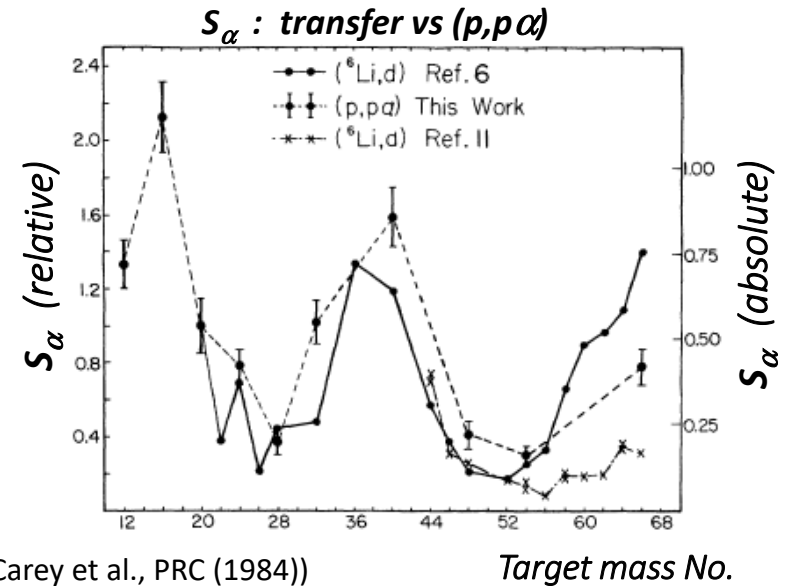
Experimental investigations of clustering



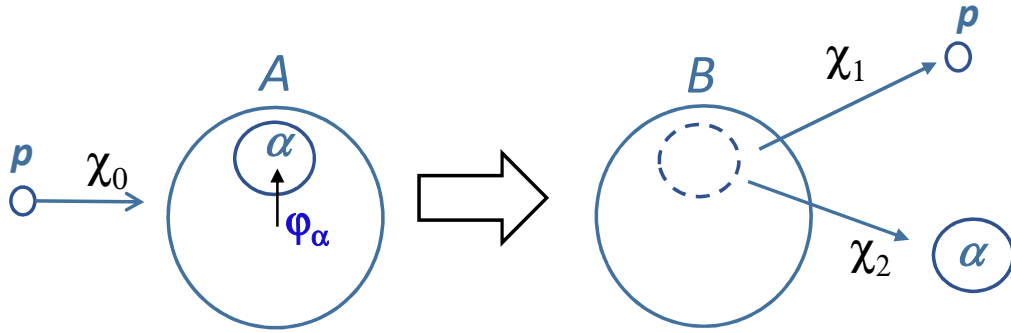
$(p,p\alpha), (\alpha,2\alpha)$

Cluster knockout reactions

- Direct reaction
 - ✓ short reaction time ($\sim 10^{-22}$ s)
 - ✓ one-step dominant
- (e,e'p), (p,2p) and (p,pn) for nucleons
(p,p α), (α ,2 α) for alpha cluster
- Well-studied since the 70's with proton and alpha beams on stable targets
- Incident p energy : 100~400 MeV
($\lambda \sim 0.5$ -0.25fm)
- *Peripheral* reaction
- Extraction of spectroscopic factors S_α
- **Recently: new analysis procedure**



Measurement of $(p,p\alpha)$ reactions



- **Excitation energy spectrum of the residue**
conservation laws \rightarrow 6 degrees of freedom (e.g. (\vec{p}_1, \vec{p}_2))

$$E_B = E_A + E_0 - E_1 - E_2$$

$$p_B = (p_A^2 + p_1^2 + p_2^2 - 2p_A p_1 \cos \theta_1 - 2p_A p_2 \cos \theta_2 + 2p_1 p_2 \cos \theta_{1-2})^{1/2}$$

$$m_B^* = \sqrt{E_B^2 - p_B^2}$$

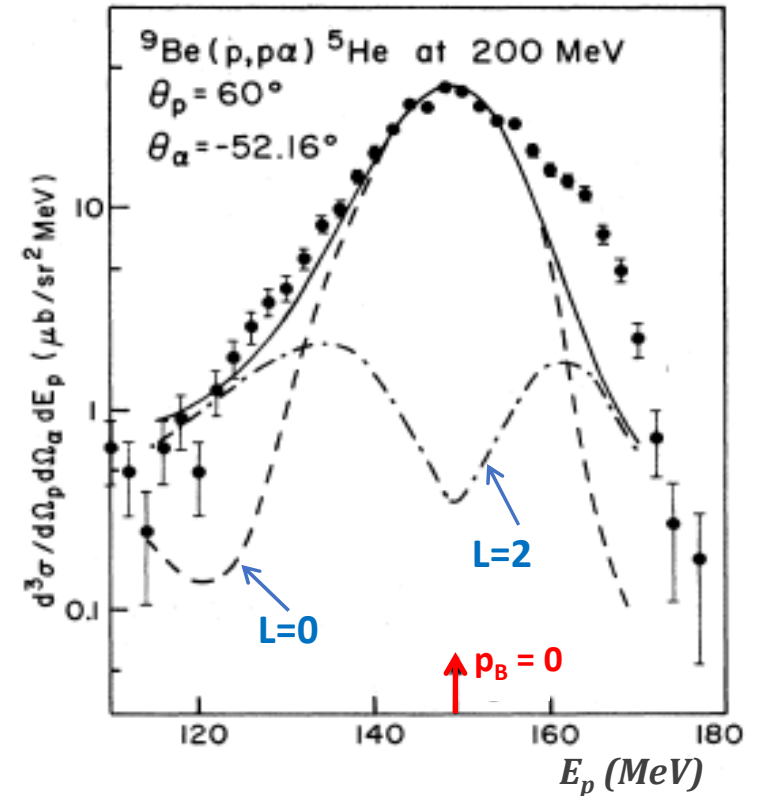
- **Triple differential cross-section**

$$\frac{d^3\sigma}{dE_1 d\Omega_1 d\Omega_2}$$

Energy and solid angle of particle 1 solid angle of particle 2

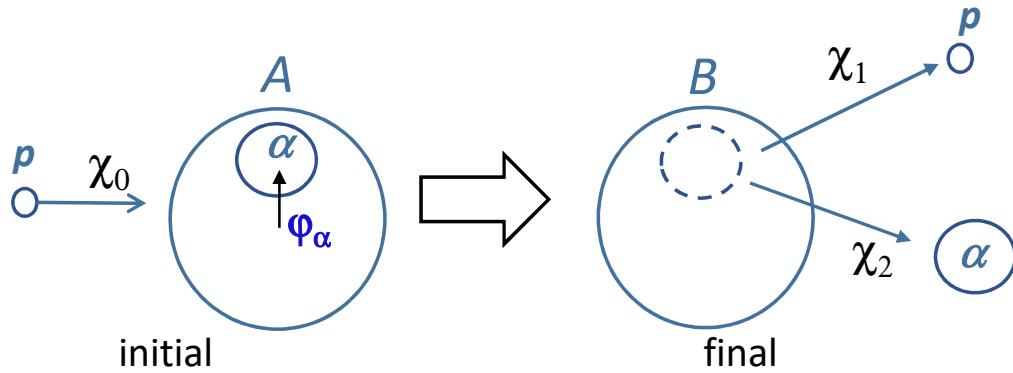
Measured around recoil-less conditions $\vec{p}_B = \vec{0}$ (quasifree)

${}^9\text{Be}(p,p\alpha)$ at 200 MeV



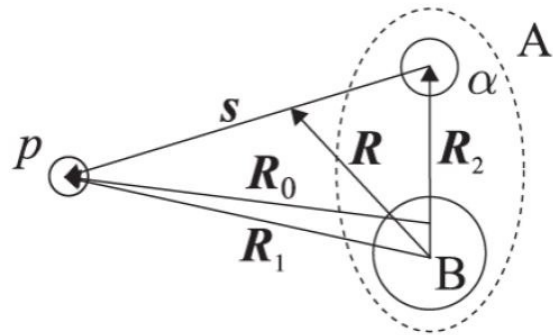
Nadasen *et al.*, PRC(1989)

Amplitude and cross-section in Distorted Wave Impulse Approximation (DWIA)



$$\frac{d^3 \sigma^{DWIA}}{dE_1^L d\Omega_1^L d\Omega_2^L} = F_{\text{kin}} C_0 \frac{d\sigma_{p\alpha}}{d\Omega_{p\alpha}}(\theta_{p\alpha}, E_{p\alpha}) |\bar{T}_{P_0 P_1 P_2}|^2$$

Kinematical factor Constant 2-body p- α Xsection Transition amplitude



$$T_{P_0 P_1 P_2} = \left\langle \chi_{1,P_1}^{(-)}(R_1) \chi_{2,P_2}^{(-)}(R_2) | t_{p\alpha}(s) | \chi_{0,P_0}^{(+)}(R_0) \varphi_{\alpha}(R_2) \right\rangle$$

$\chi_{0,P_0}^{(+)}(R_0)$ $\chi_{1,P_1}^{(-)}(R_1)$ $\chi_{2,P_2}^{(-)}(R_2)$ distorted waves for p-A, p-B and α -B
 Obtained from elastic scattering data

$t_{p\alpha}(s)$ Transition interaction

$\varphi_{\alpha}(R_2)$ **Cluster Wave function**

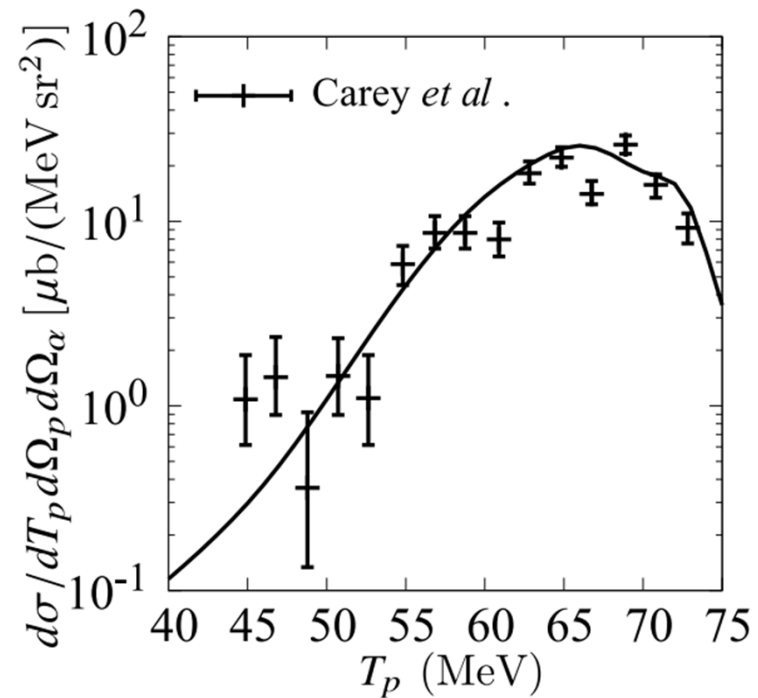
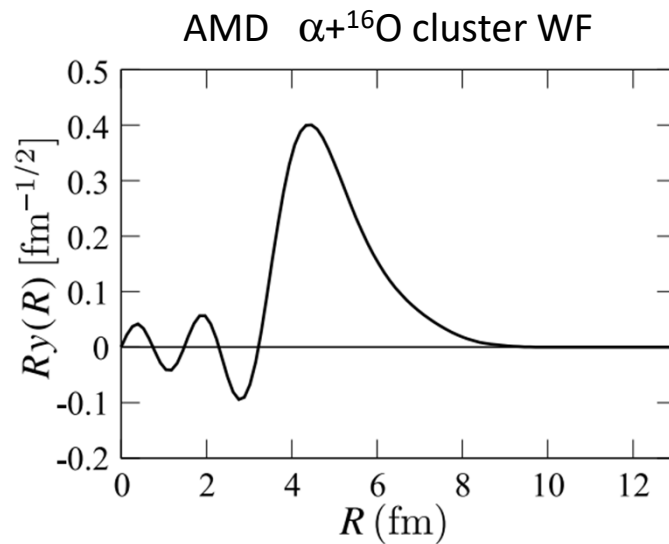
- Phenomenological
- **Microscopic (AMD, ab initio ...)**

Analysis using microscopic cluster WF

“Test” case : reanalysis of $^{20}\text{Ne}(p,p\alpha)^{16}\text{O}$ data at 101.5 MeV/u

K.Yoshida et al., PRC 99, 064610 (2019)

- AMD cluster WF
- Reliable $\alpha+^{16}\text{O}$ optical potential



Data reproduced without any normalization

$(p,p\alpha)$ represents a quantitative probe for α -clustering

THSR-based calculations for $^{10}\text{Be}(p,p\alpha)^6\text{He}(\text{GS})$ at 250 MeV/u

M.Lyu et al., PRC 97 (2018)

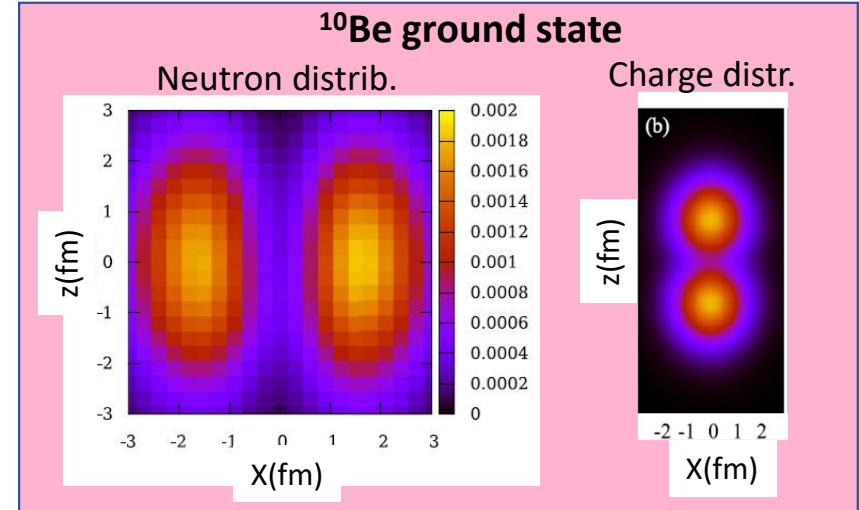
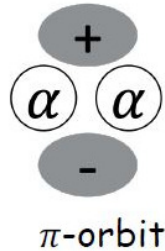
Tohsaki, Horiuchi, Schuck, Röpke (THSR) wave-function
Well adapted to discuss cluster states in light nuclei

- Cluster wave-function overlap of ^{10}Be and ^6He
- Optical potentials folding of calculated density

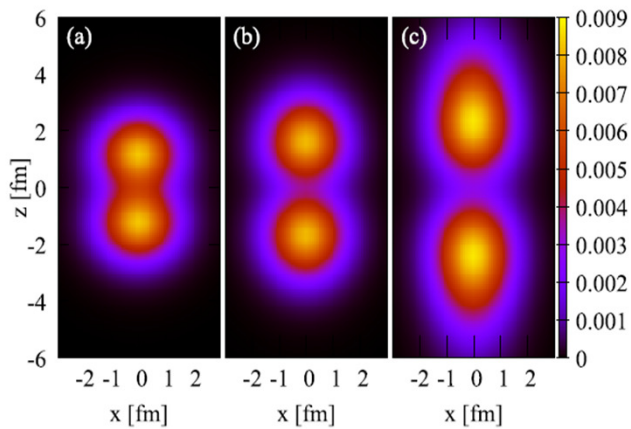
Good reproduction of :

- ^{10}Be GS energy
- Charge radius 2.31fm (exp=2.36fm)

$$^{10}\text{Be}: 2\alpha + 2n(\pi)$$



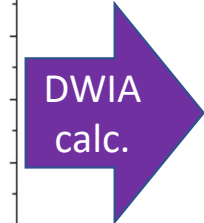
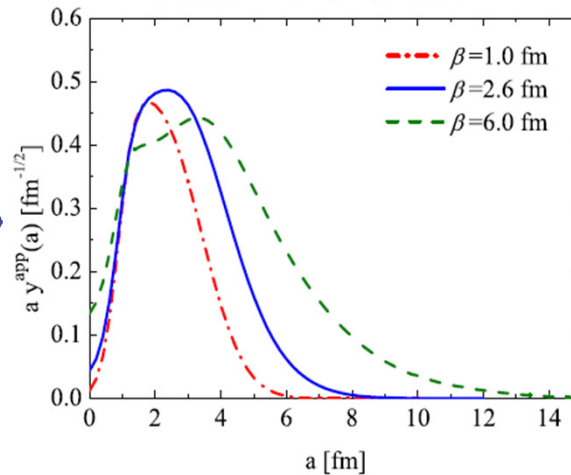
^{10}Be charge distribution



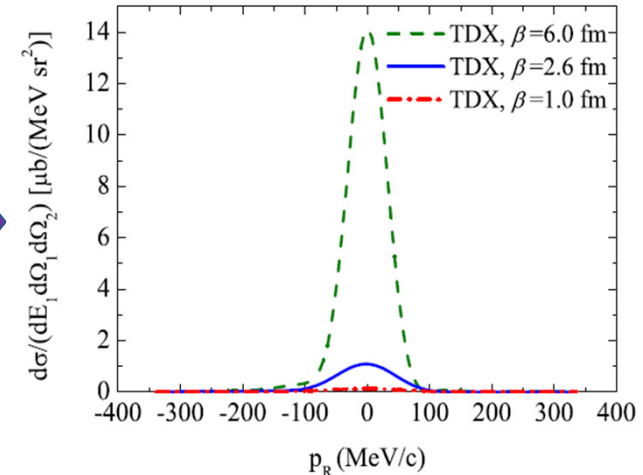
↑ Variational result



Cluster wave-function



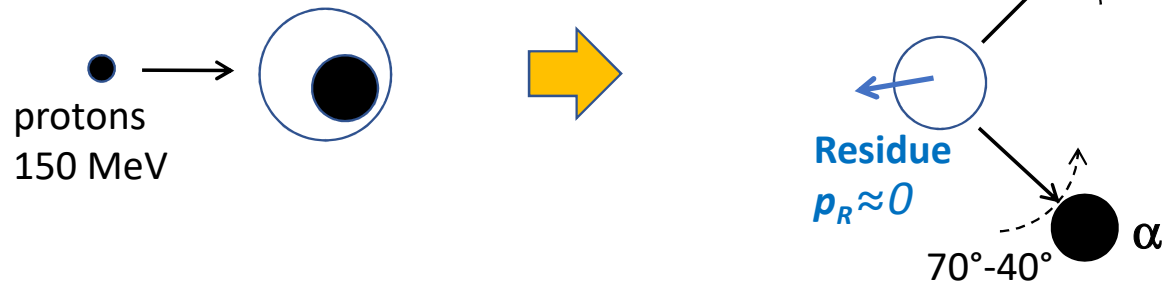
$^{10}\text{Be}(p,p\alpha)$ cross-section



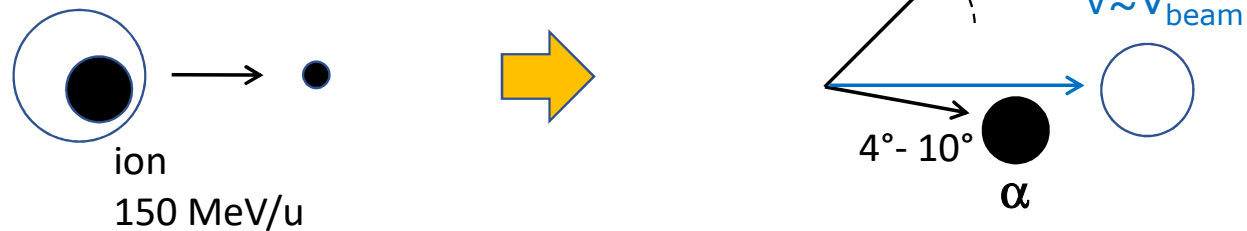
Kinematics for alpha quasifree knockout reactions

Direct vs inverse kinematics

DIRECT



INVERSE



Proton

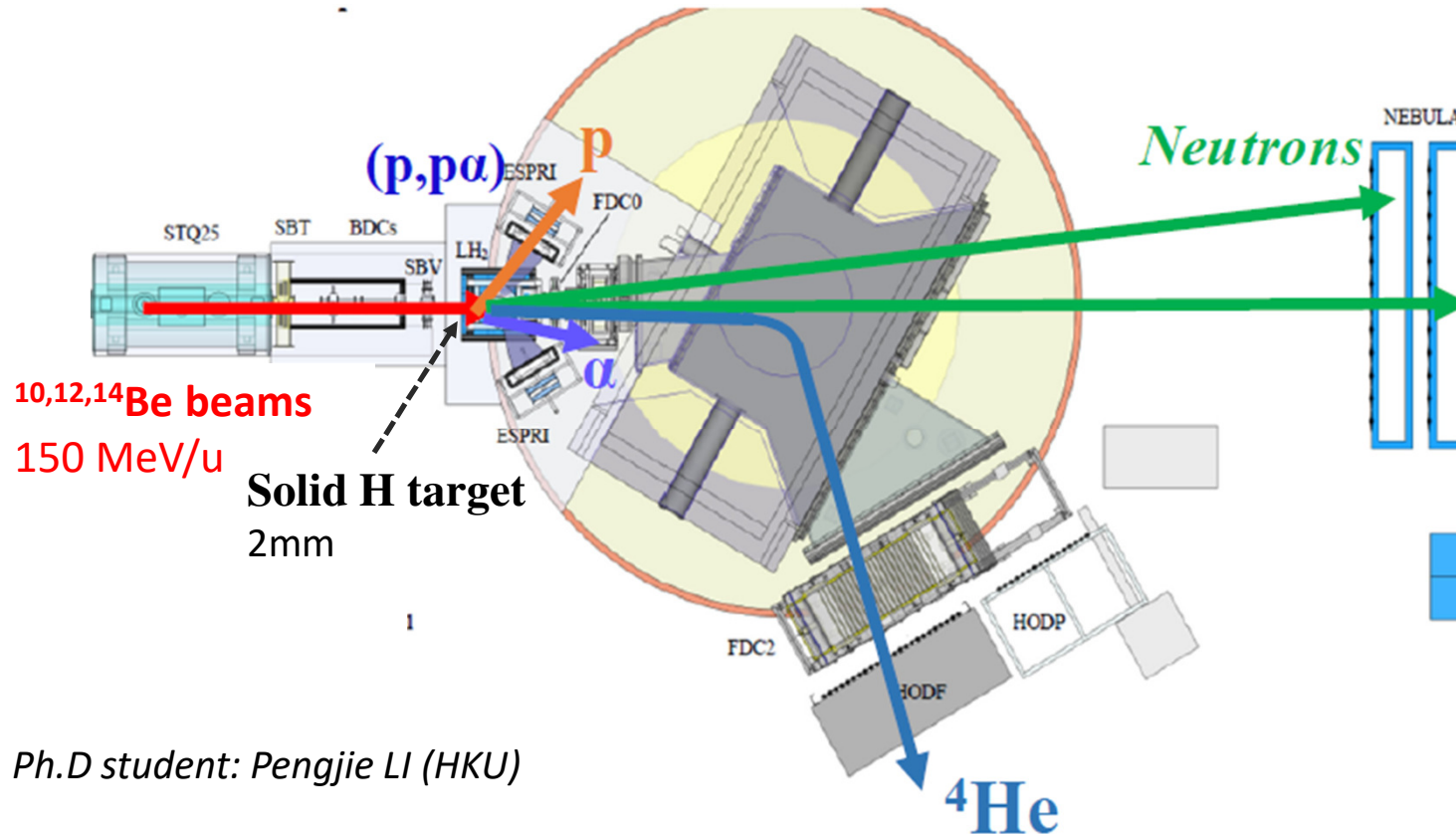
- $50^\circ - 70^\circ$
- $20 \sim 150 \text{ MeV}$

Alpha

- $4 - 10^\circ$
- $v \approx v_{\text{beam}}$

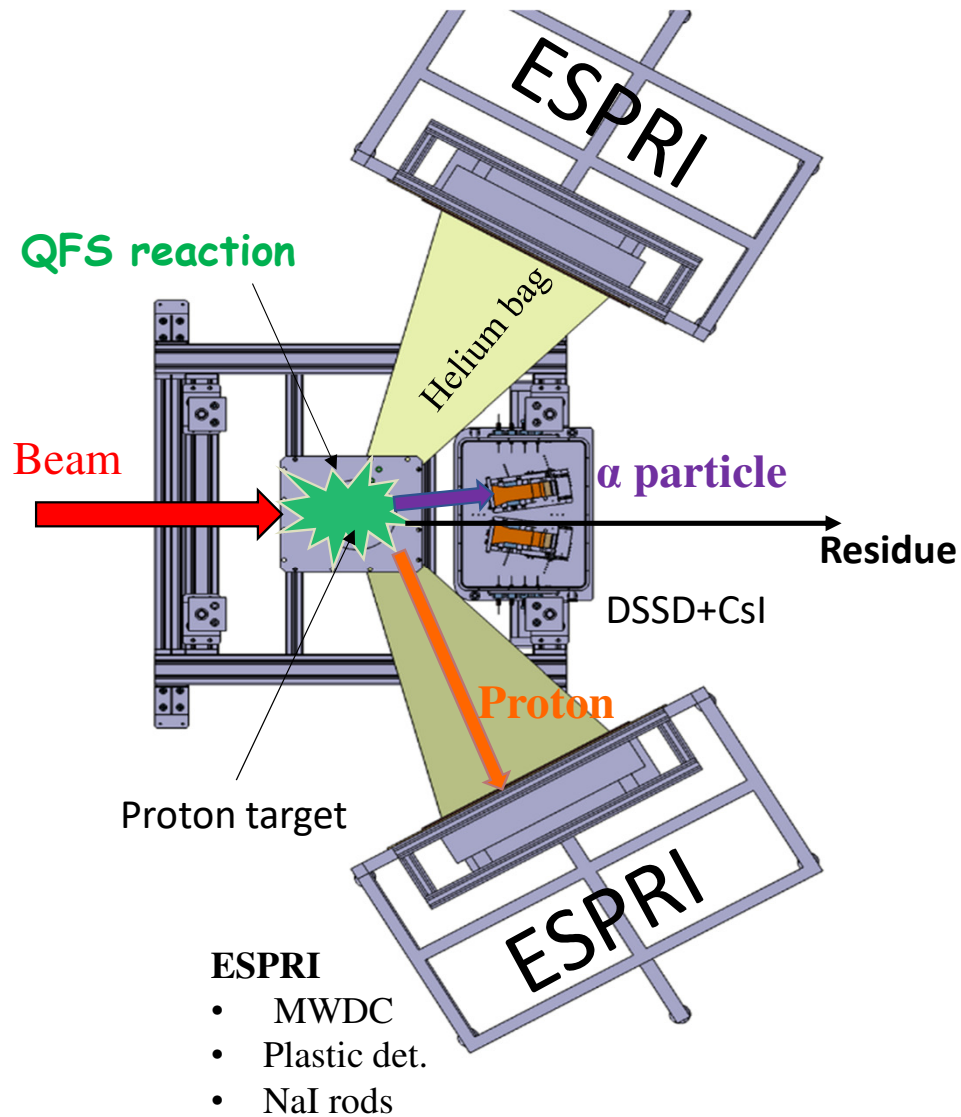
Study $^{10,12,14}\text{Be}(p,p\alpha)$ at 150 MeV/u

- Clustering in n-rich Be
- First spectrum for the 6n system
- Missing-mass measurement
- measure: $\text{GS} \rightarrow \text{GS}$ and $\text{GS} \rightarrow 2^+$ transitions



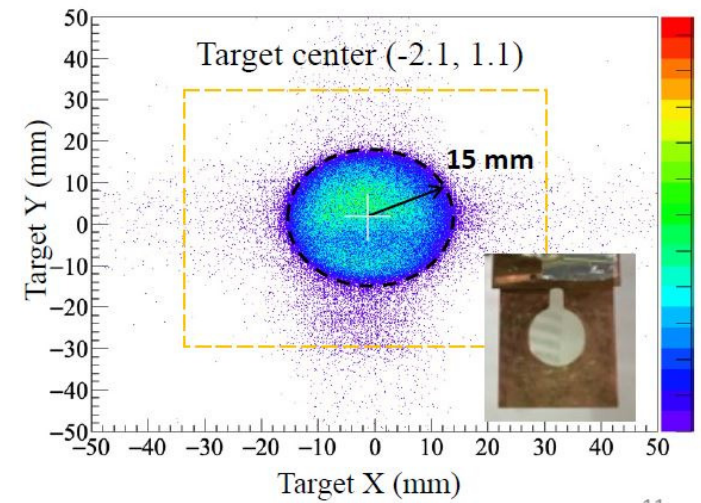
Collaboration: IJCLab, Hong Kong U., RIKEN, TI Tech, LPC Caen, Tohoku U., RCNP Osaka, CEA Saclay, Kyoto U., TU Darmstadt, NIPNE Bucharest, Kyushu U.

Setup around target



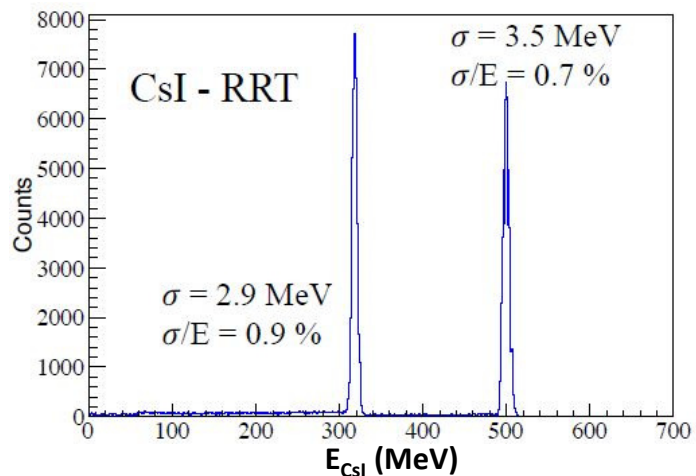
Target : 2mm-thick solid H

Y.Matsuda et al., NIMA 643 (2011)

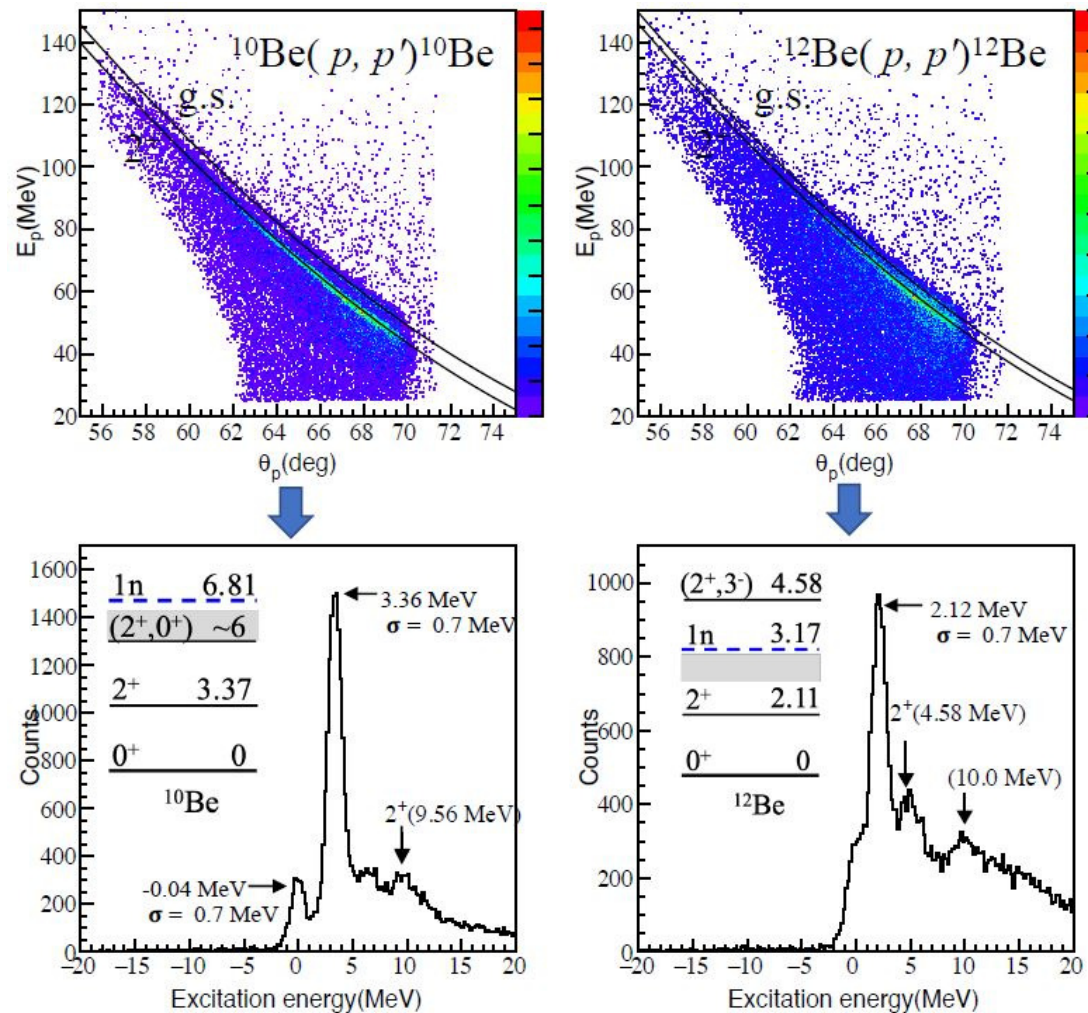


Energy calibrations of Telescopes

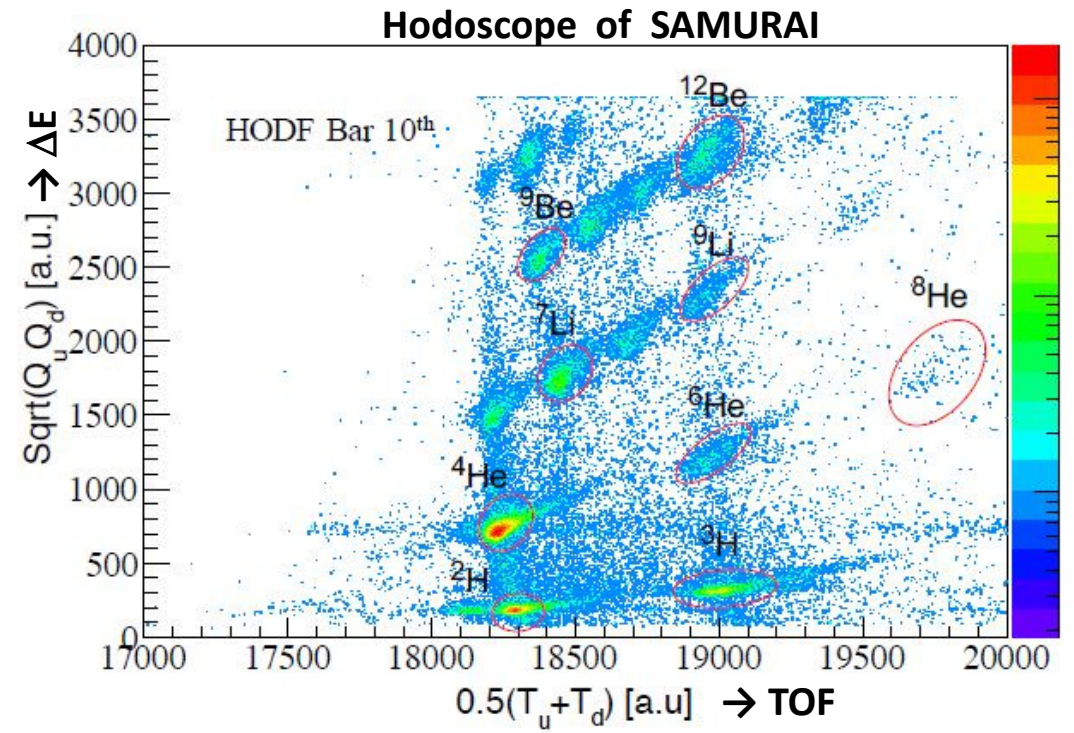
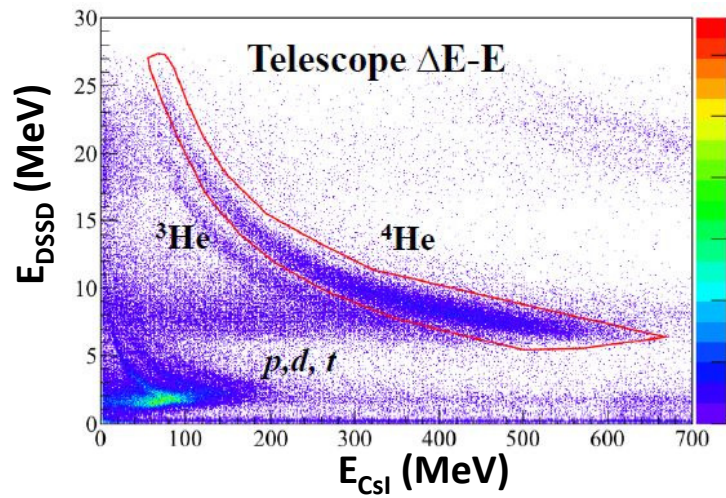
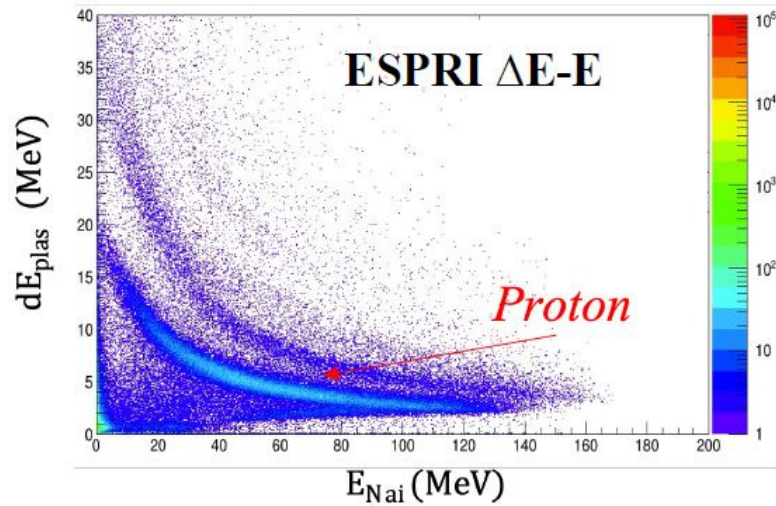
α beams at 120 and 150 MeV/u



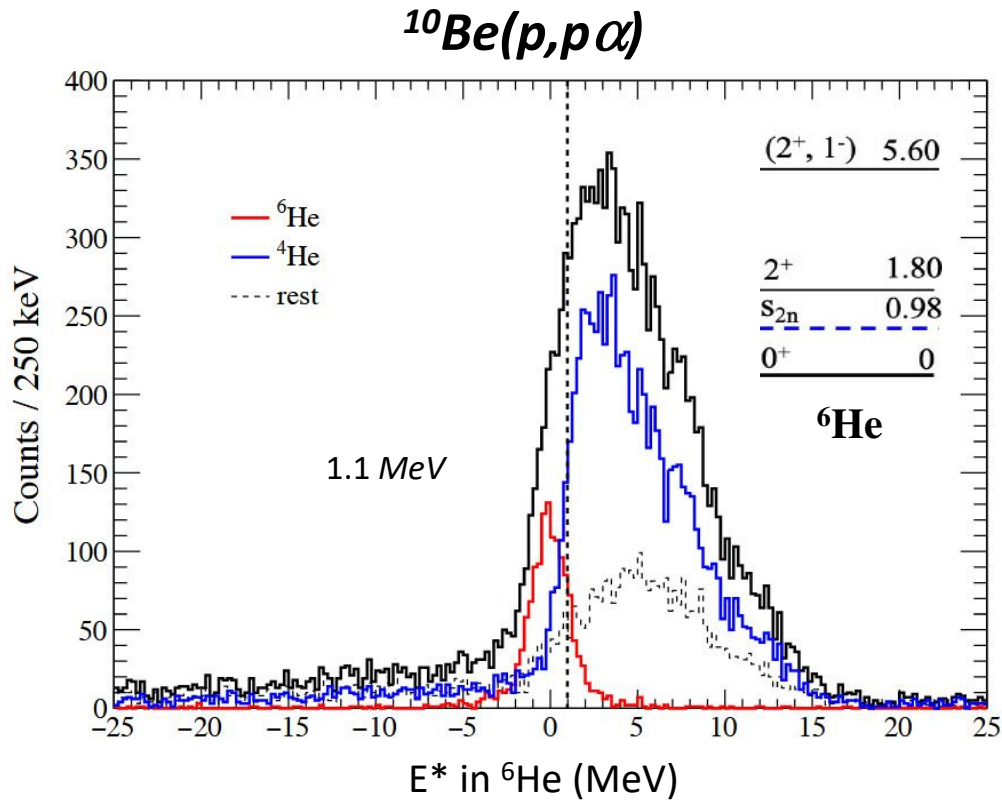
Energy calibrations of ESPRI



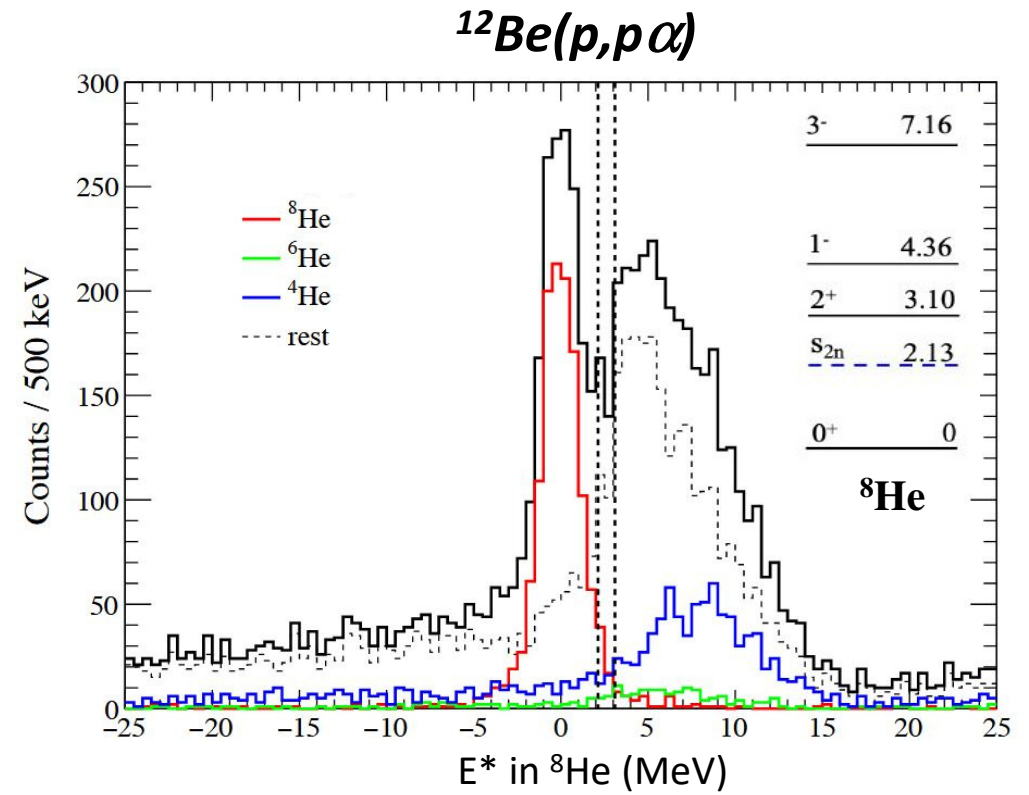
Particle identification – channel selection



Excitation energy spectra



$$\sigma(^{6}\text{He}^{\text{GS}}) = 1.1 \text{ MeV}$$



$$\sigma(^{8}\text{He}^{\text{GS}}) = 1.1 \text{ MeV}$$

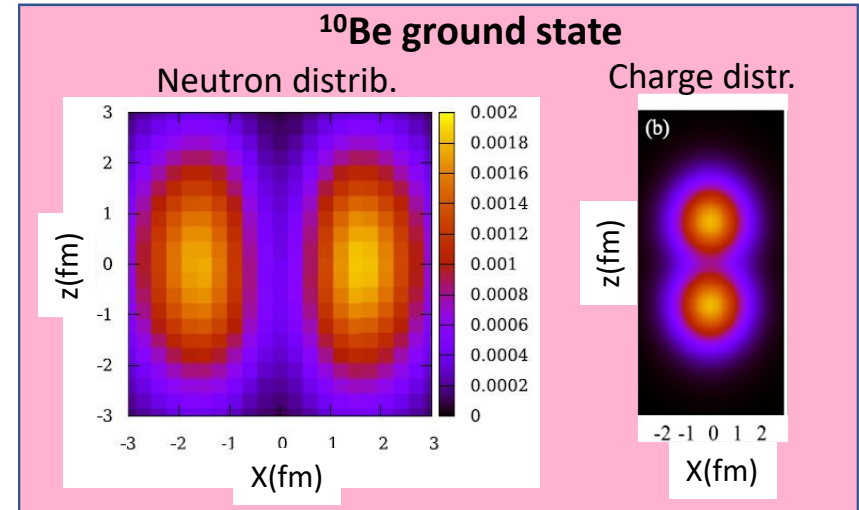
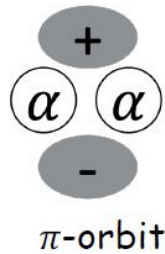
Calculations for $^{10}\text{Be}(p,p\alpha) ^6\text{He}^{(GS)}$ at 150 MeV/u

➤ Tohsaki, Horiuchi, Schuck, Röpke (THSR) wave-function
Well adapted to discuss cluster states in light nuclei

Good reproduction of :

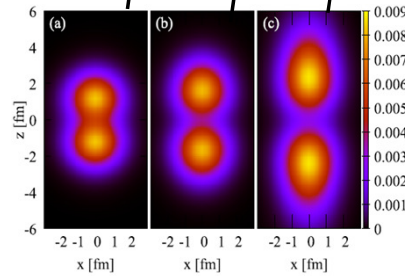
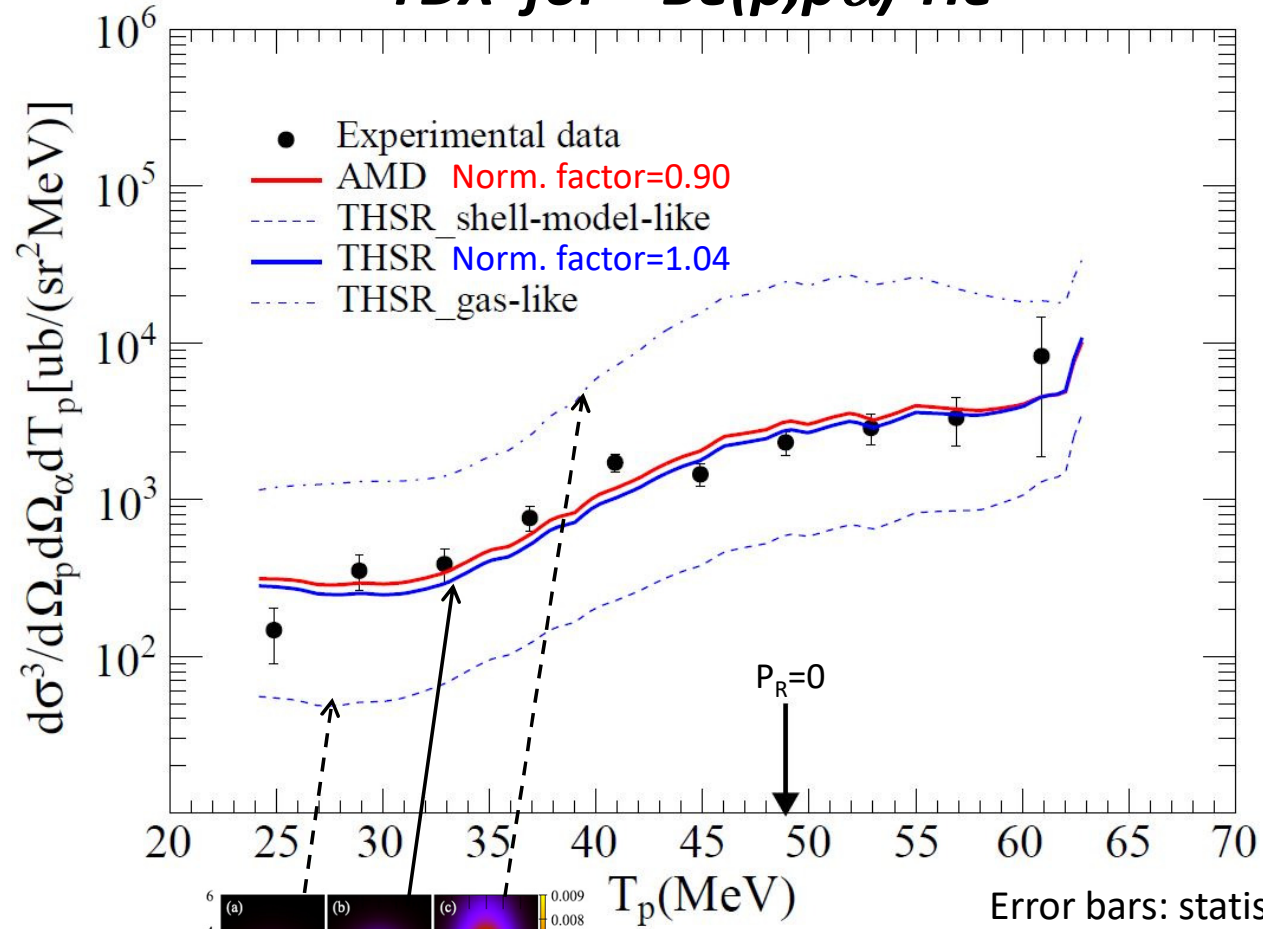
- ^{10}Be GS energy
- Charge radius 2.31fm (exp=2.36fm)

$^{10}\text{Be}: 2\alpha + 2n(\pi)$



➤ AMD cluster WF

TDX for $^{10}\text{Be}(p,p\alpha)^6\text{He}(\text{GS})$

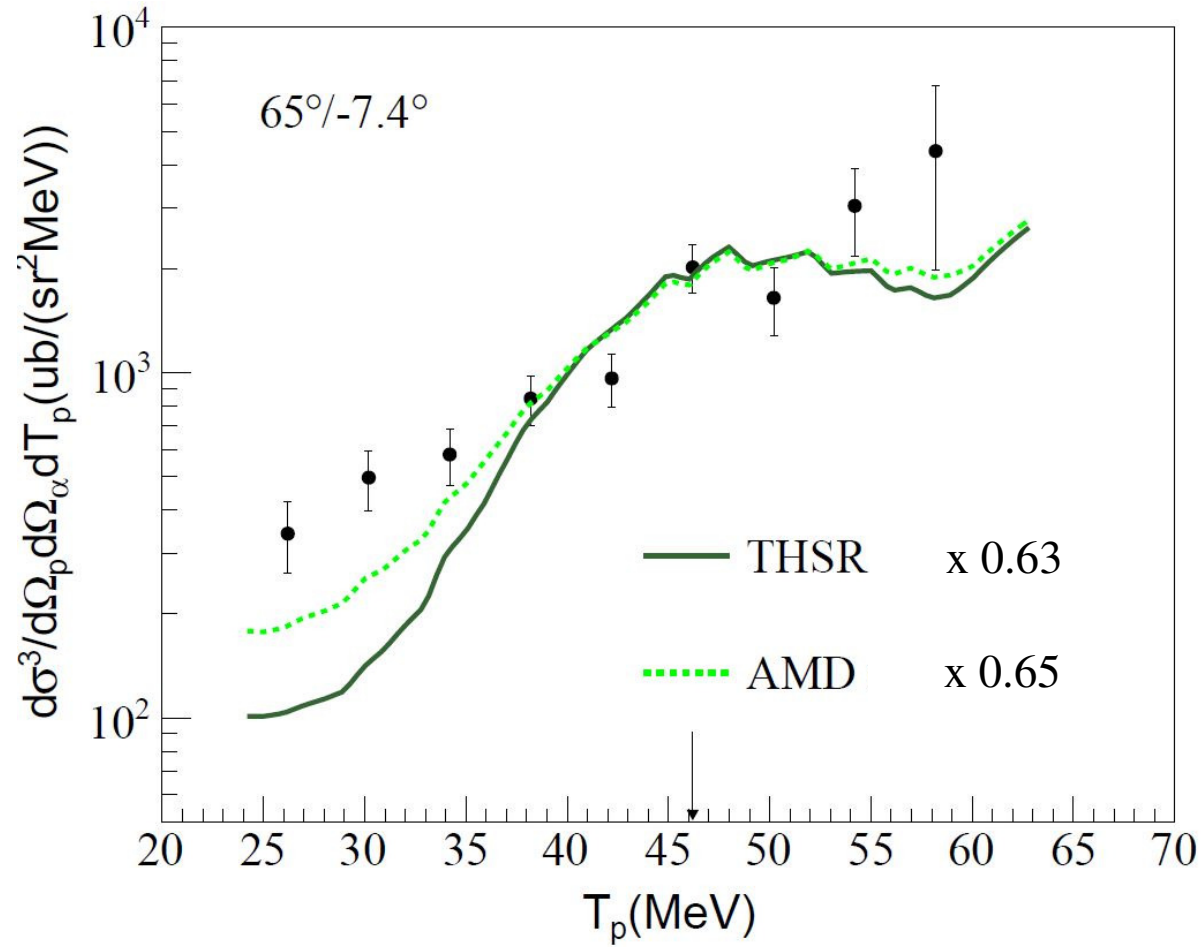


Error bars: statistical + error on PV
 Optical potentials : from Dirac phenomenology

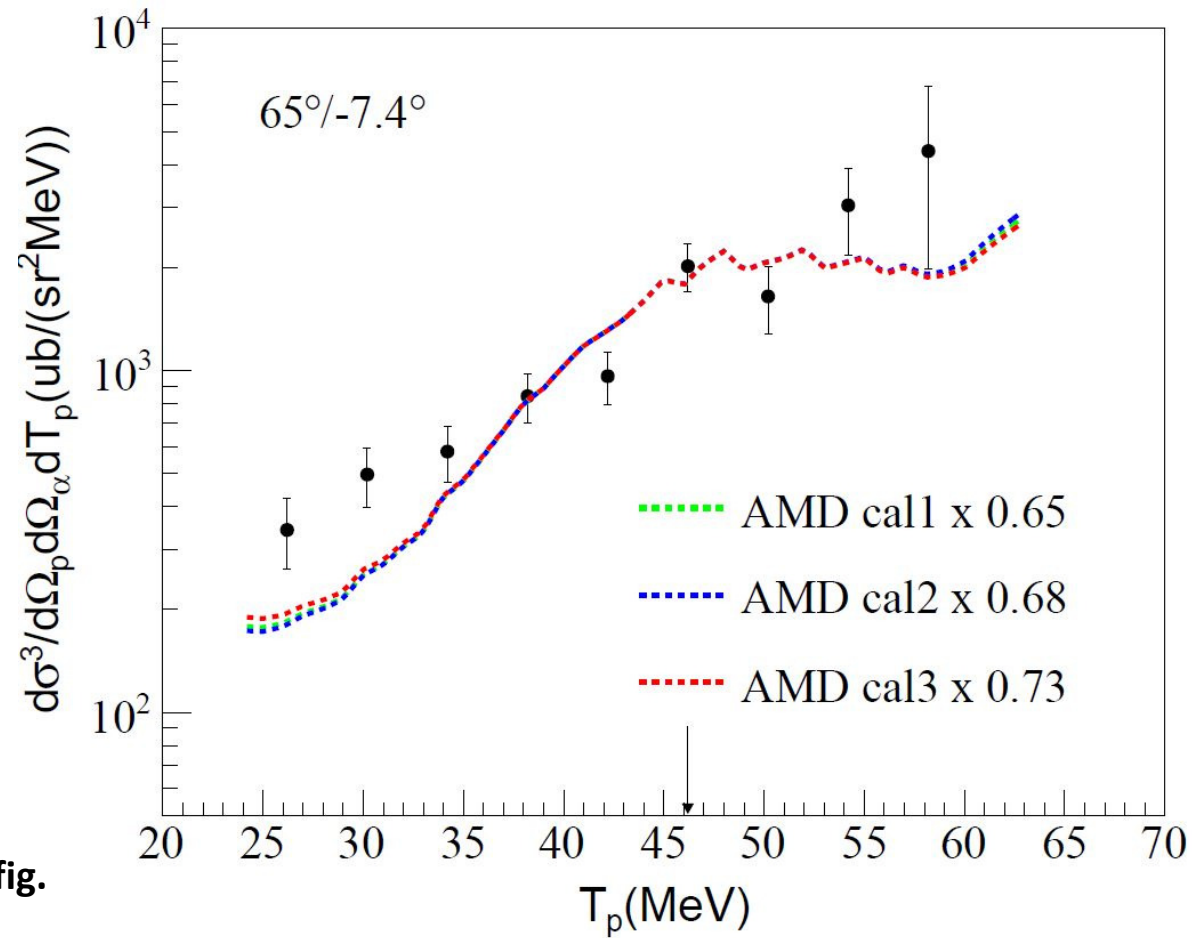
Molecular structure of the ^{10}Be GS is validated

Submitted for publication

TDX for $^{12}\text{Be}(p,p\alpha)^8\text{He}(\text{GS})$



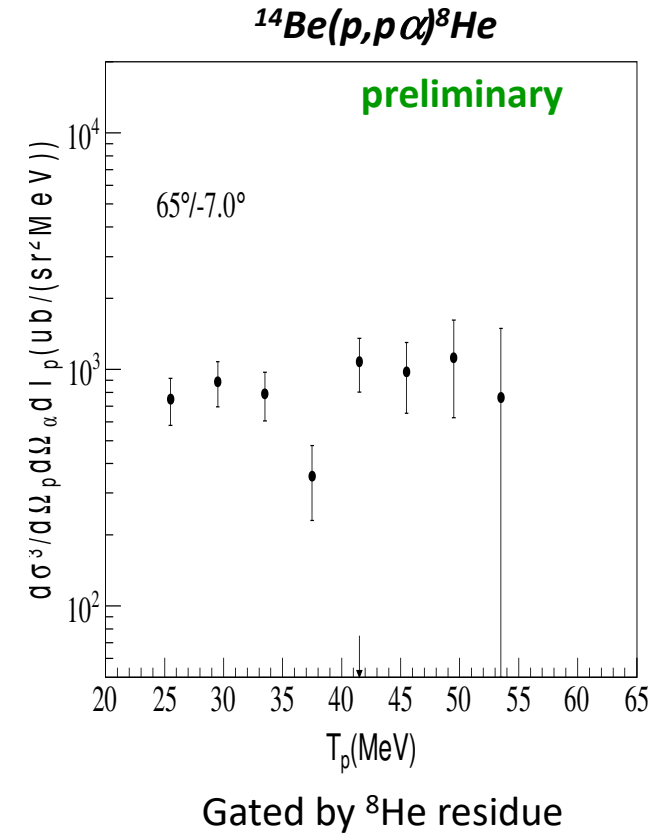
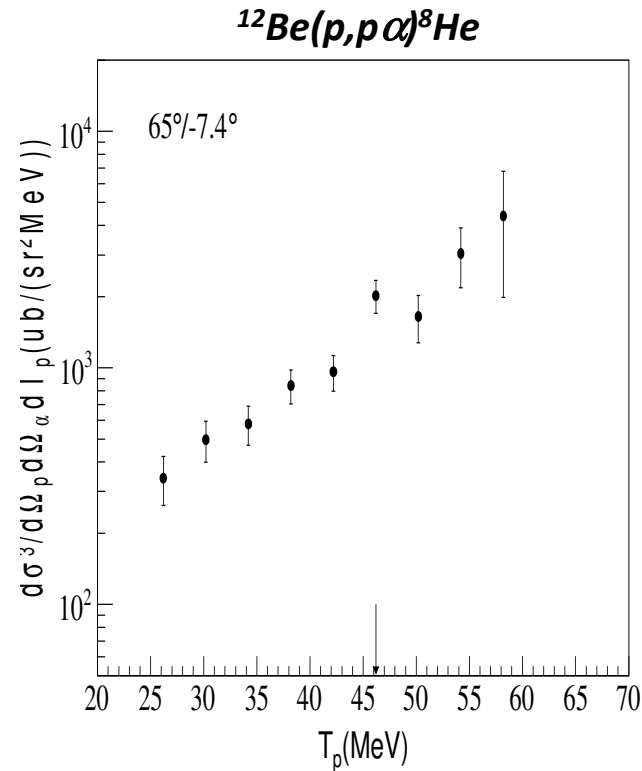
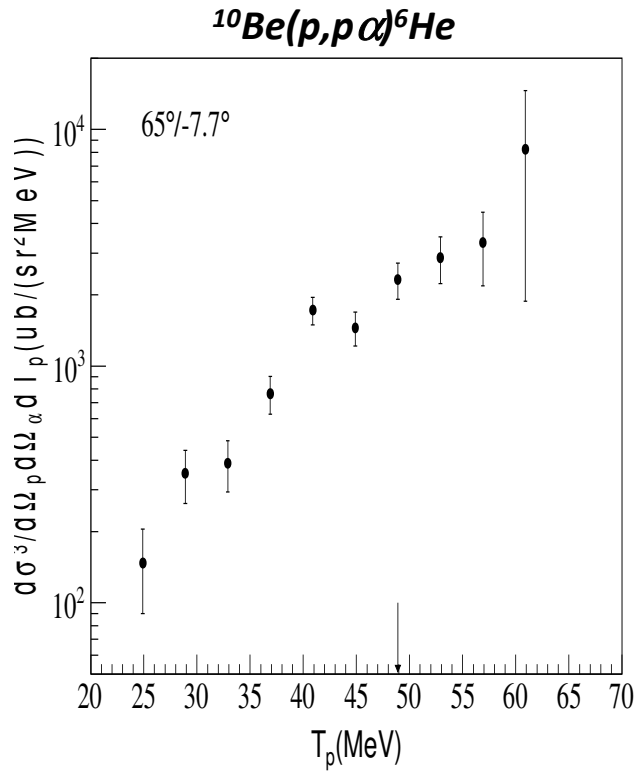
TDX for $^{12}\text{Be}(p,p\alpha)^8\text{He}(\text{GS})$



Sensitivity to intruder config.

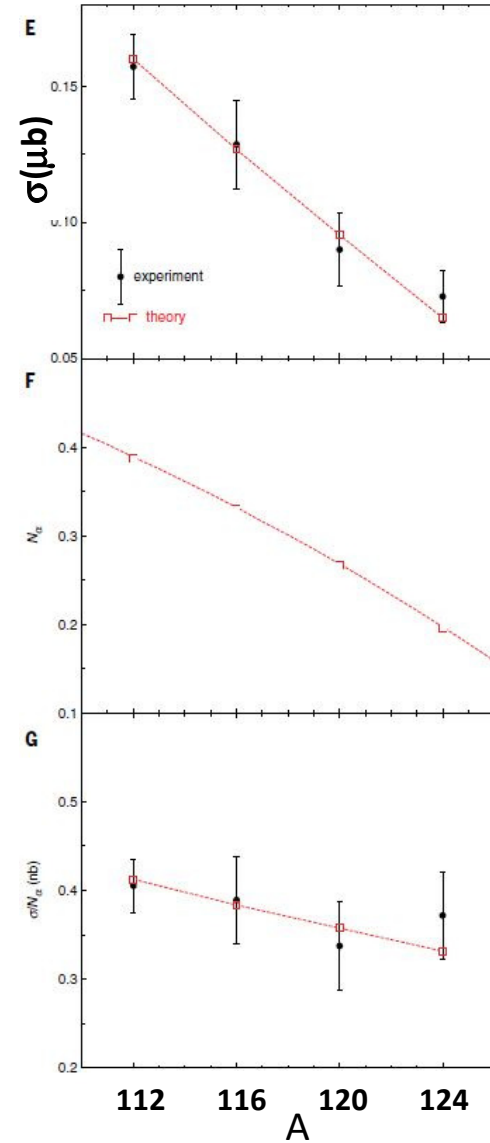
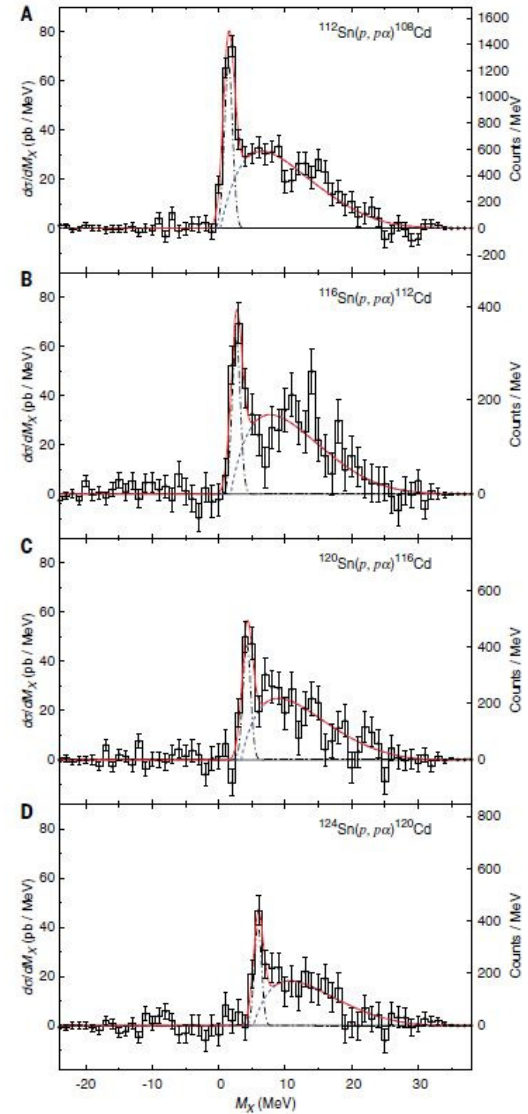
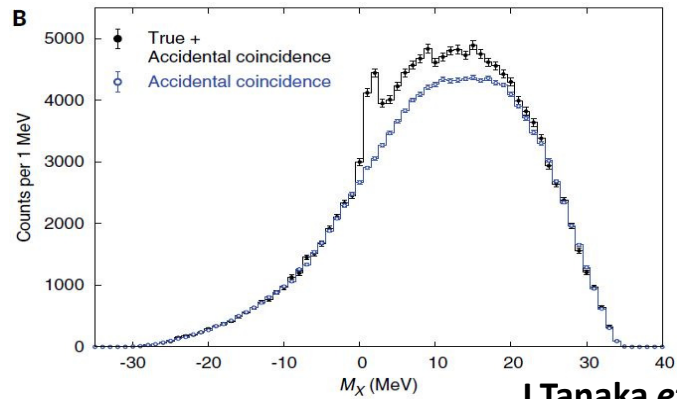
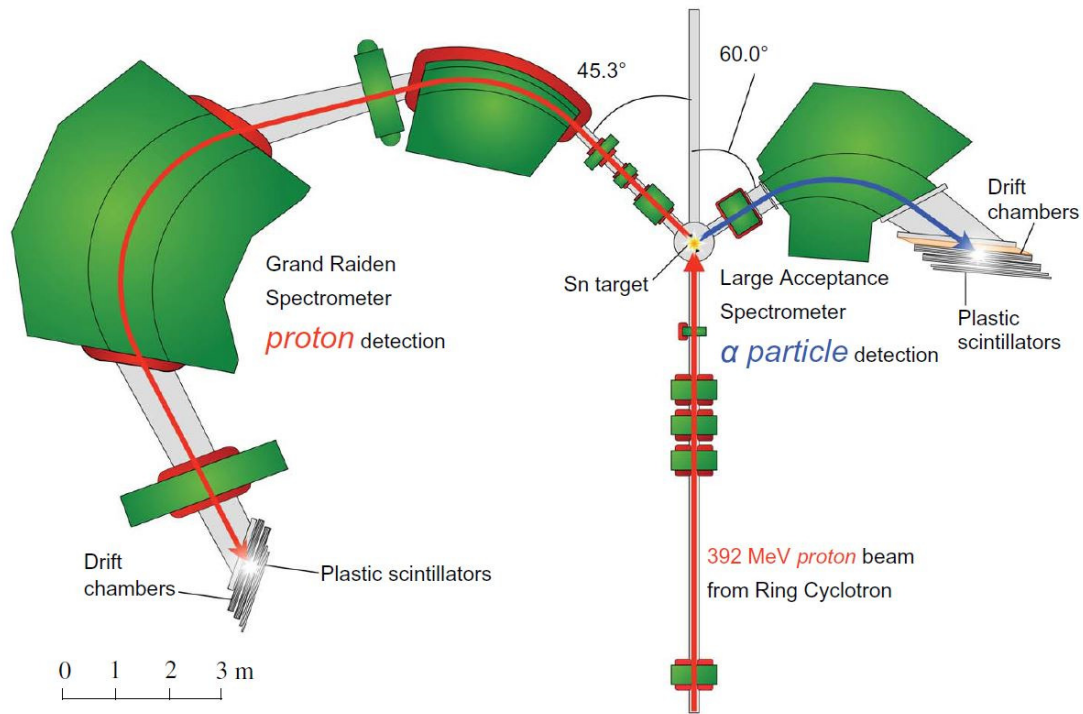
- CAL1: default LS parameter
- CAL2 : weaker LS parameter
- CAL3: pure $2h\omega$

Experimental TDX for $^{10-14}\text{Be}(p,p\alpha)$



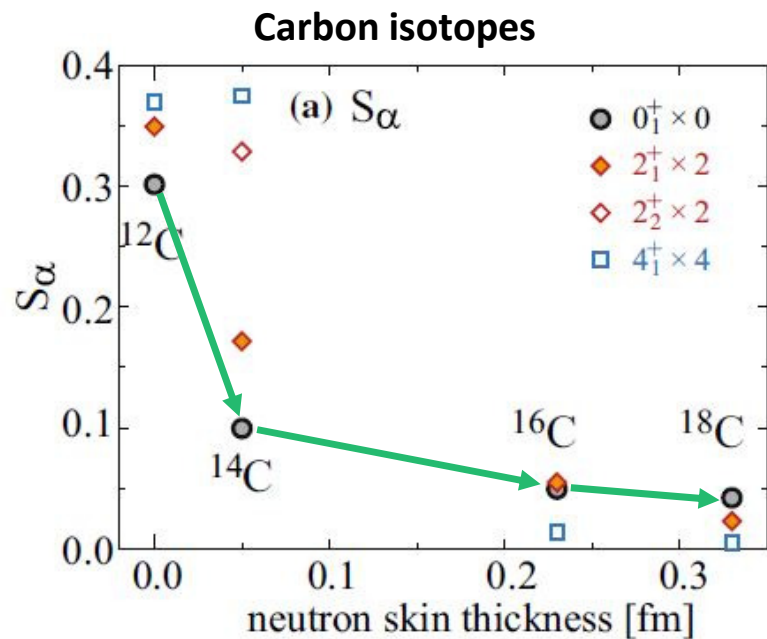
Clustering evolution with N

Study of surface α -clustering in $^{112,116,120,124}\text{Sn}(p,p\alpha)$



J.Tanaka *et al.*, Science 371, 260 (2021)

Clustering evolution towards the dripline

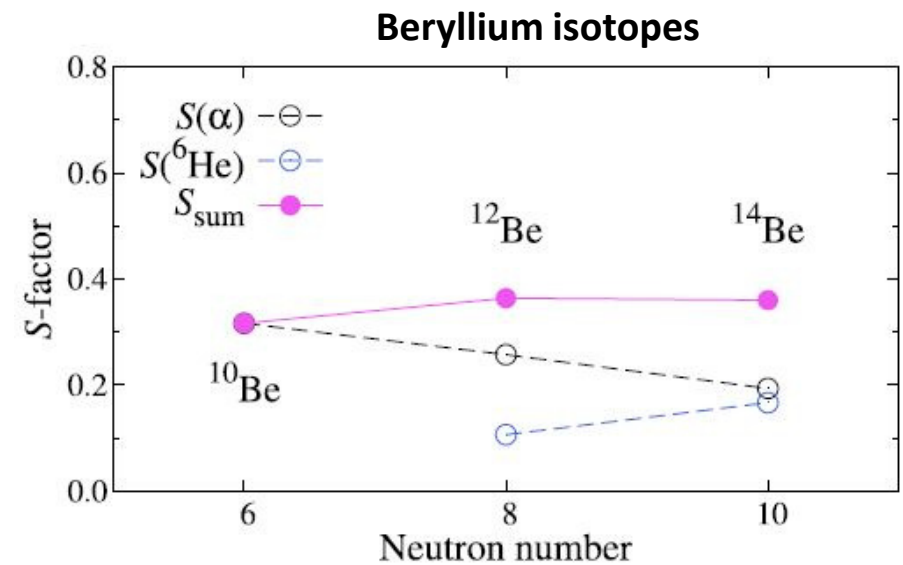


Q. Zhao, Y. Suzuki, J. He, B. Zhou, M. Kimura, EPJA 157 (2021)
AMD calculations using Gogny D1S functional

Hindrance effect due to neutron skin ?

Alternative interpretations

- Neutron single-particle configurations
- Relationship between α -clustering and α -threshold



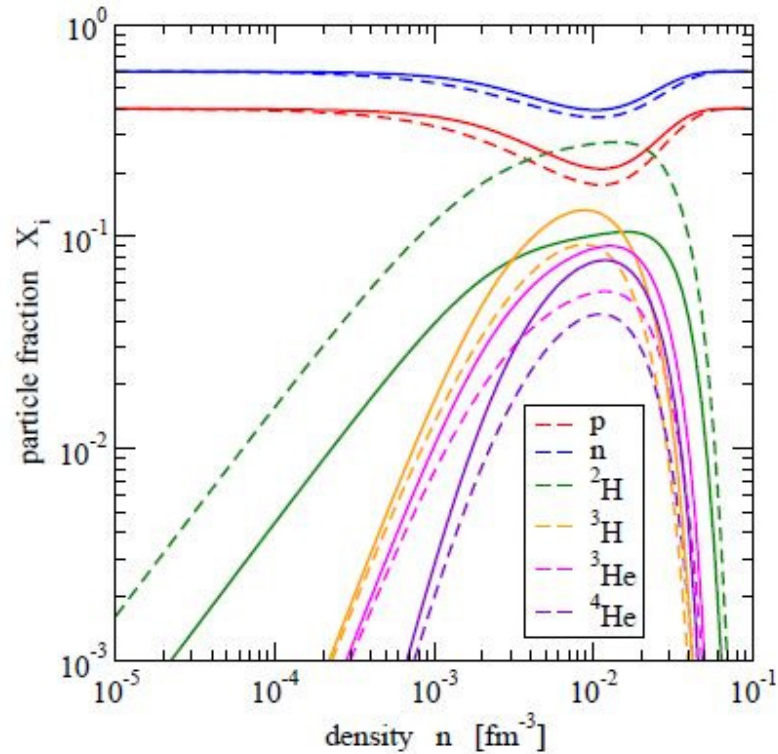
H.Motoki, Y.Suzuki, T.Kawai, M. Kimura, PTEP (2022)113D01
AMD calculations using Gogny D1S

- Hindrance of α clustering
- Development of ^6He clustering

Formation of clusters in infinite nuclear matter

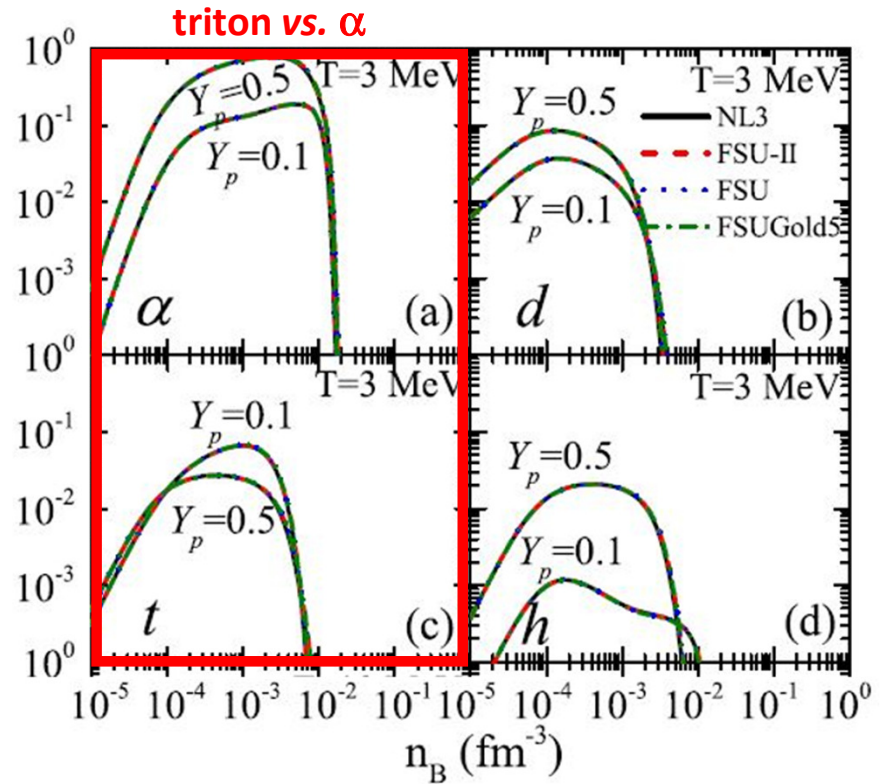
Generalized DFT calculations

All kind of clusters should be formed at low density



S.Typel, J.Phys.Conf.Ser.420,012078(2013)

Neutron-rich clusters might well be predominant in neutron-rich nuclei



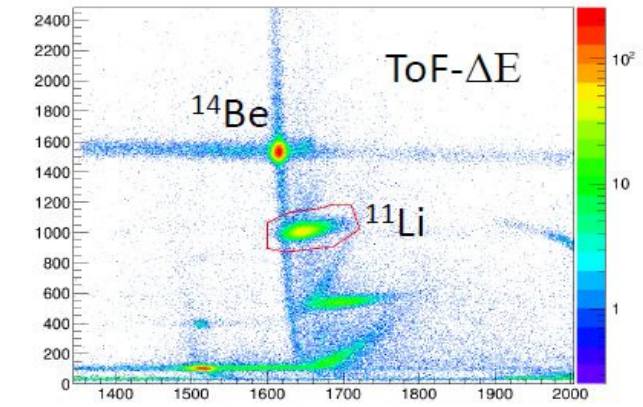
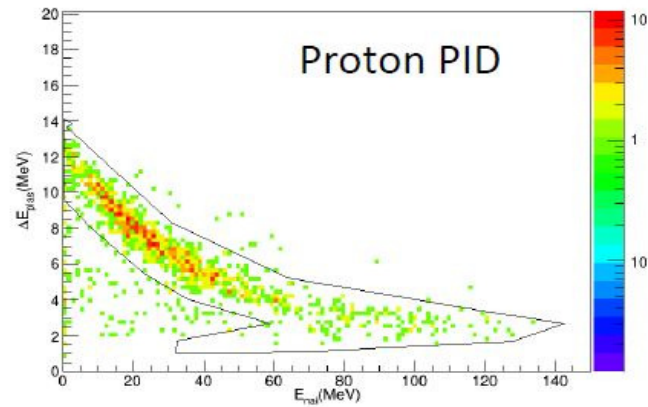
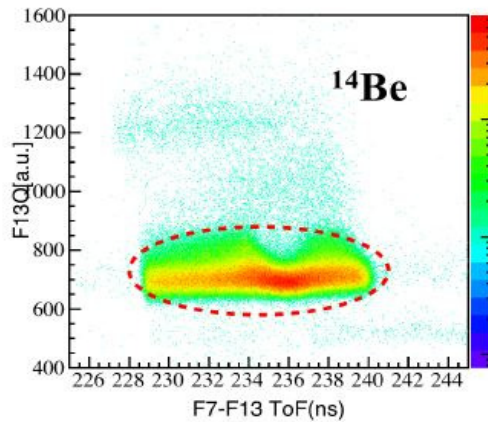
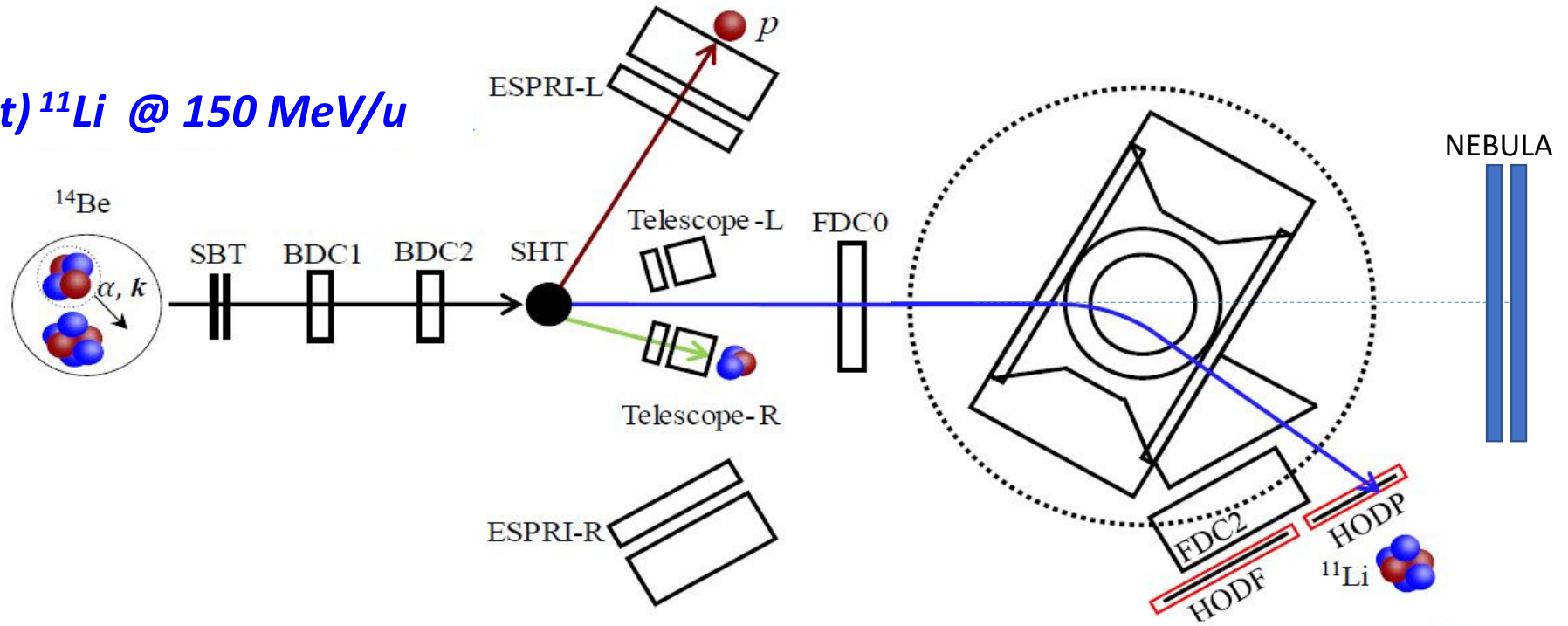
Z.-W. Zhang and L.-W. Chen, Phys. Rev. C 95, 064330 (2017)



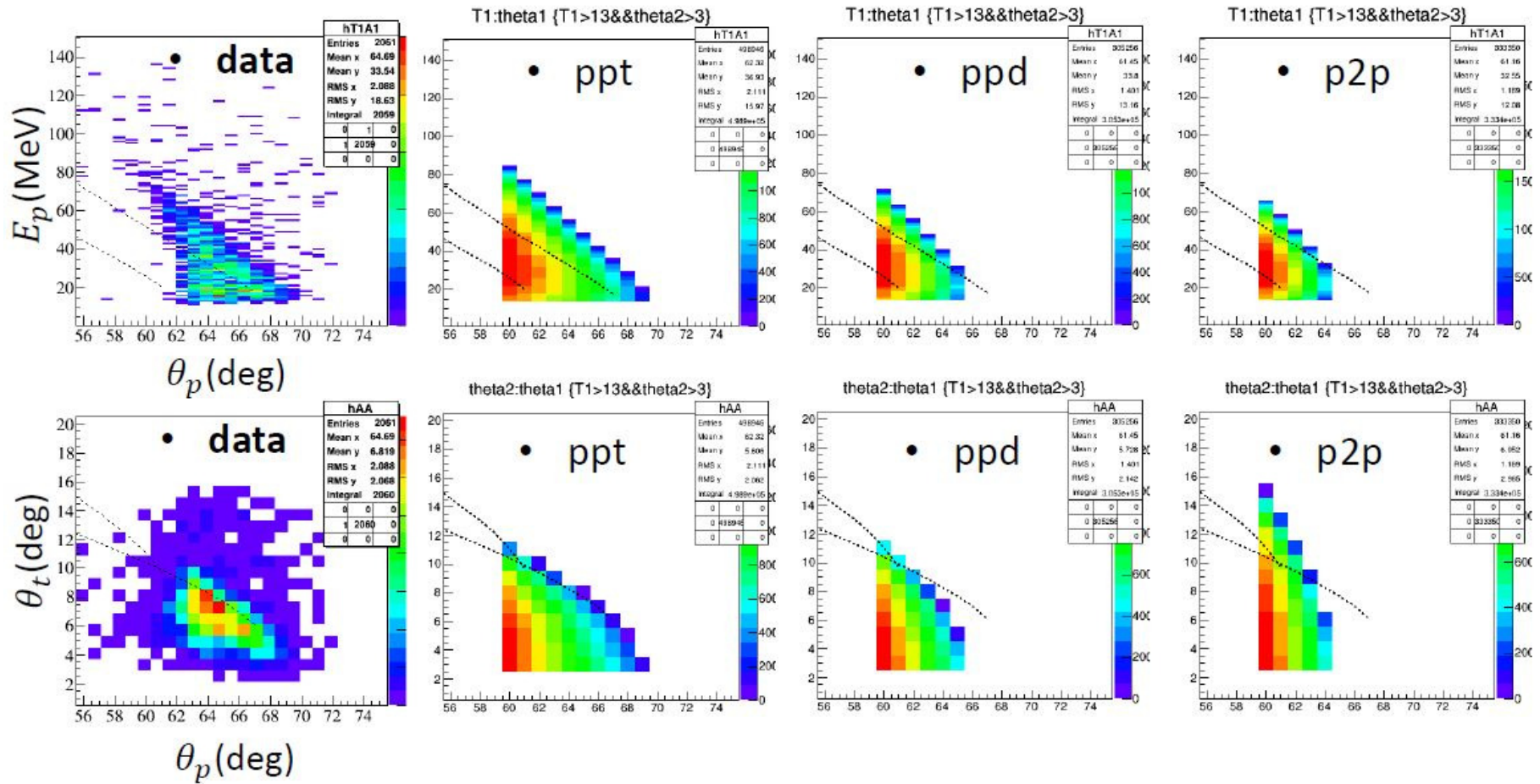
Seek for triton clustering in light n-rich isotopes

Search for triton formation at the surface of ^{14}Be

$^{14}\text{Be}(p,pt)^{11}\text{Li}$ @ 150 MeV/u

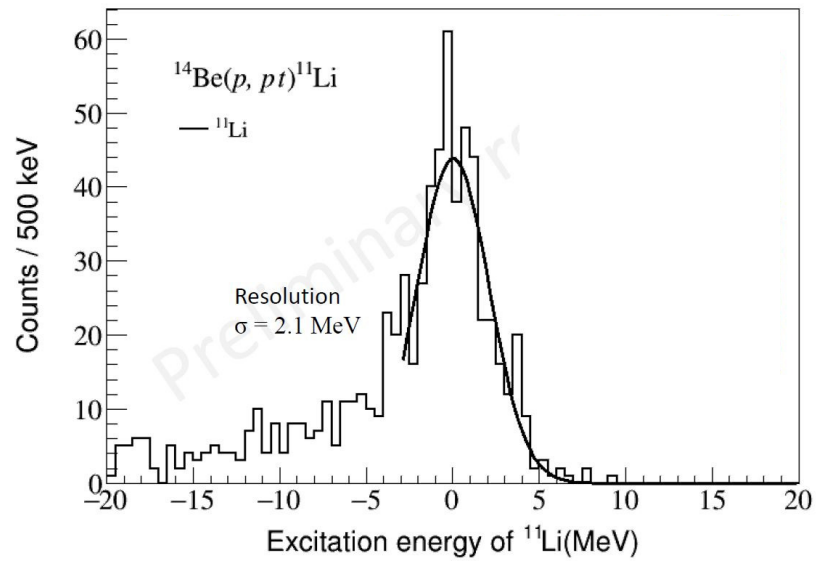


Kinematical correlations

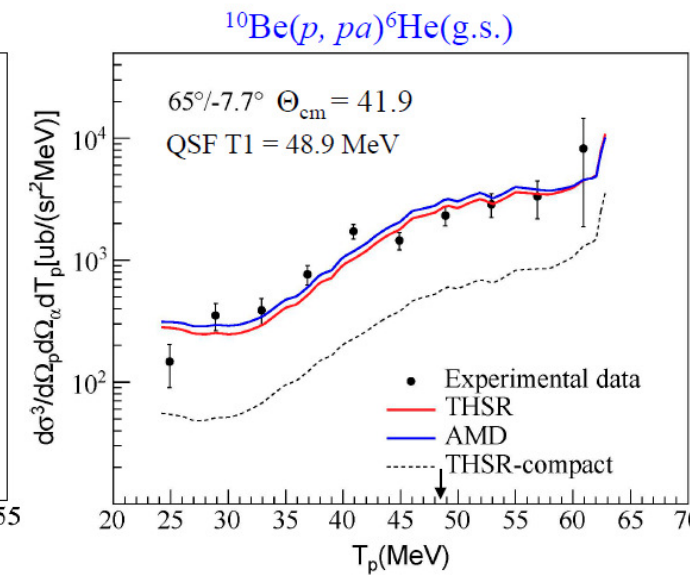
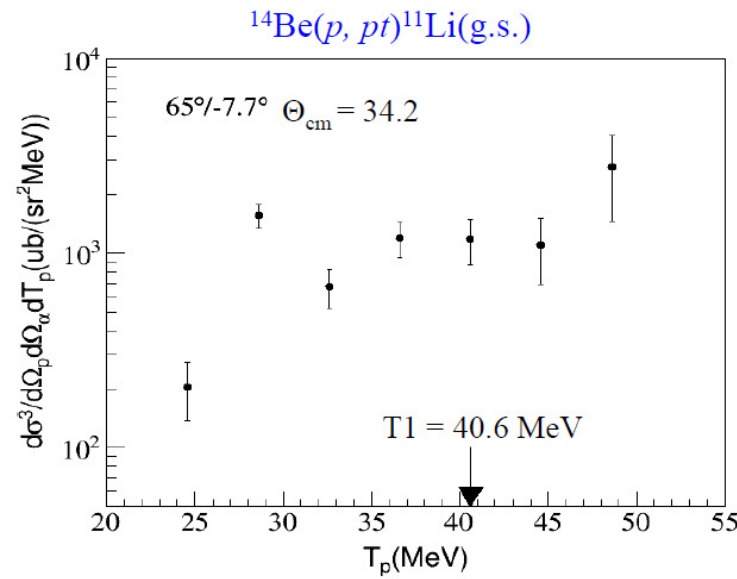


Preliminary results for triton knockout from ^{14}Be

E_x spectrum in ^{11}Li residue



Triple differential cross-section



Comparable magnitude !

Sizeable amount of triton clusters at the surface of the ^{14}Be halo nucleus

Conclusions/Prospects (clustering)

- First measurement of $(p,p\alpha)$ in inverse kinematics with RIB with proper kinematical conditions
→ direct evidence of the Molecular structure of the ^{10}Be GS
- First steps to quantitatively probe cluster evolution in GS towards the dripline
Preliminary results show large amount of tritons at the surface of the halo nucleus ^{14}Be

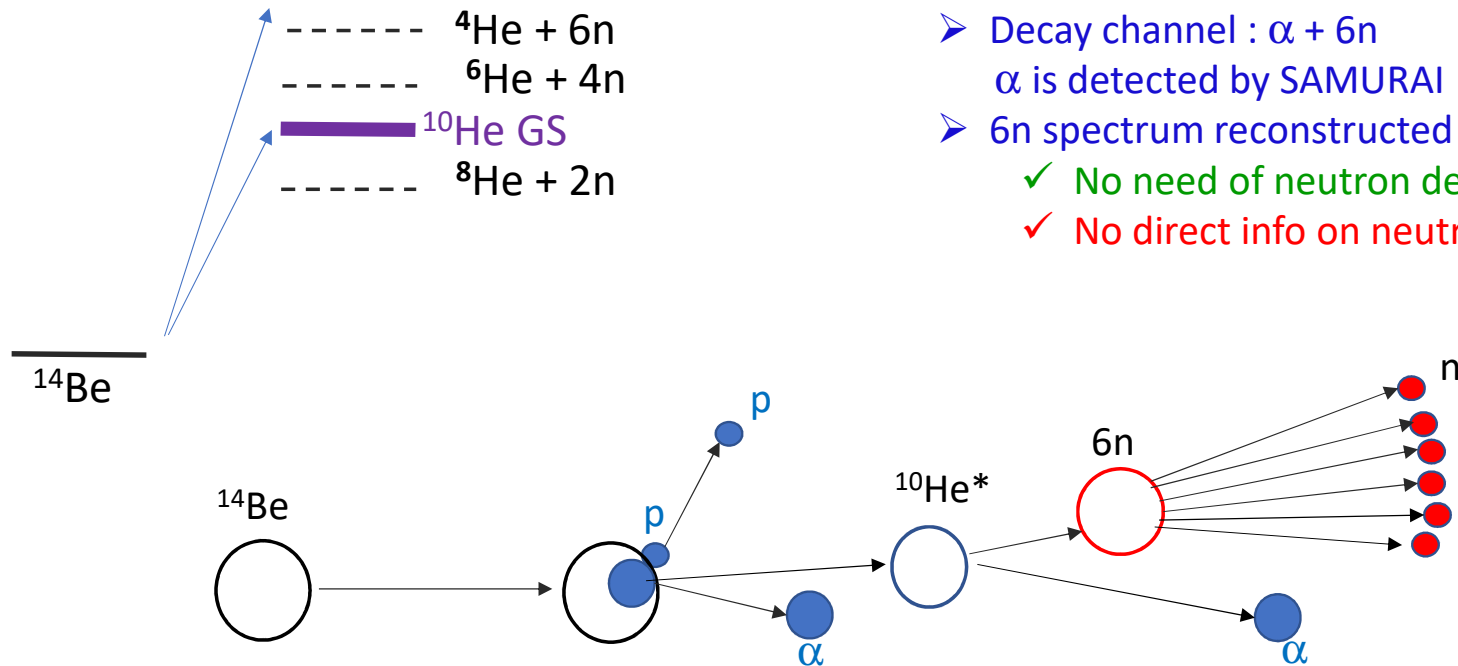
Complementary program using transfer reaction at LISE/GANIL with the MUGAST array
E870 experiment accepted at last GANIL PAC meeting
 (p,α) and $(d,^6\text{Li})$ pickup reactions in inverse kinematics
- Planned study of $(p,p\alpha)$ on n-rich Carbon isotopes at RIKEN/Samurai (accepted expt)
(spokesperson: Zaihong Yang)
- The “ONOKORO” research project (T.Uesaka, J.Zenihiro)
study of $(p,p\alpha)$, (p,pt) , $(p,^3\text{He})$, (p,pd) ... in stable and unstable medium-mass and heavy nuclei
TOGAXSI device under construction

First *exp^{al}* determination of the 6-neutron spectrum

$^{14}\text{Be}(p,p\alpha)$ reaction

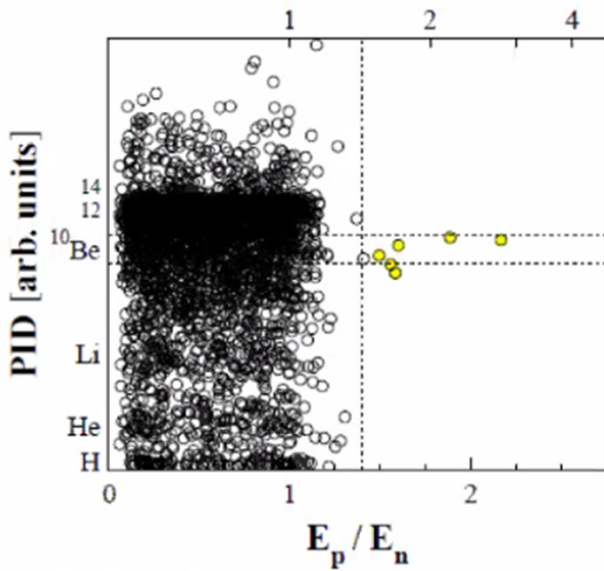
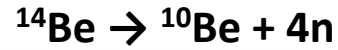
- $^4\text{He} + 6n$
- $^6\text{He} + 4n$
- ^{10}He GS
- $^8\text{He} + 2n$

- $^{10}\text{He}^*$ populated by $^{14}\text{Be}(p,p\alpha)$
- High ^{14}Be rate at RIBF
- Decay channel : $\alpha + 6n$
 α is detected by SAMURAI
- $6n$ spectrum reconstructed by missing mass
 - ✓ No need of neutron detection
 - ✓ No direct info on neutron correlations

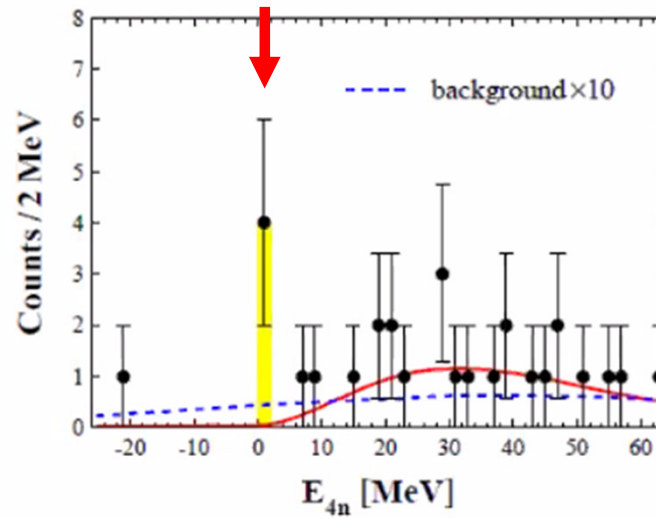
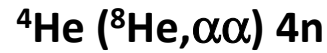


Theory: no realistic calculation for the $6n$ system

Recent (XXI century) signals on tetra neutron

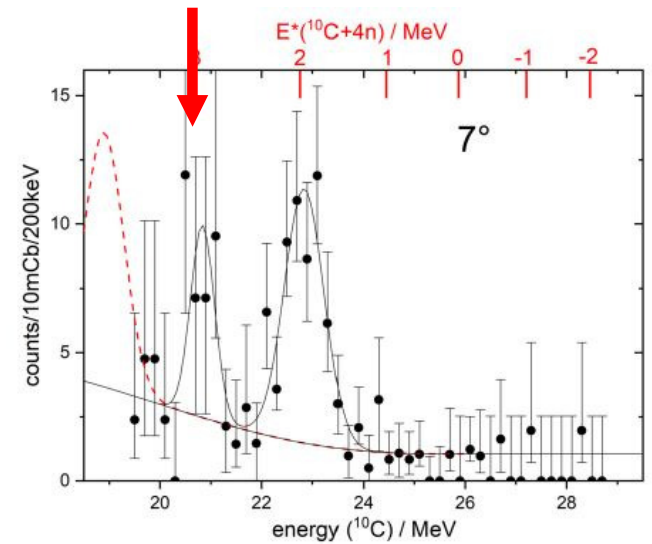
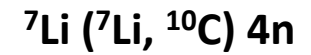


M.Marques et al., PRC65, 044006 (2002)



K.Kisamori et al., PRL 116, 052501 (2016)

$E = 0.83 \pm 0.65 \text{ (stat)} \pm 1.25 \text{ (syst) MeV}$



T.Faestermann et al. Phys.Lett. B 824 (2022)

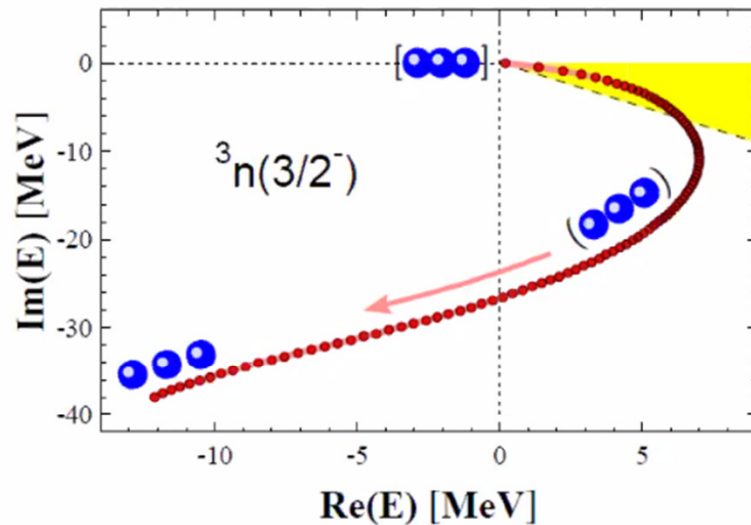
$E = 0.42 \pm 0.16 \text{ MeV}$

Theory : another hard & interesting quest



► 'Exact' calculations are categorical!

- Glöckle, PRC 18 (1978) 564 : $V_{nn} \times 4.2$
- Offermann, NPA 318 (1979) 138 : $V_{nn} \times 3.7$ (+P-waves)
- Witała, PRC 60 (1999) 024002 : avoid 2n with $V_{nn}({}^1S_0) \times 1$
- Hemmdan, PRC 66 (2002) 054001 :

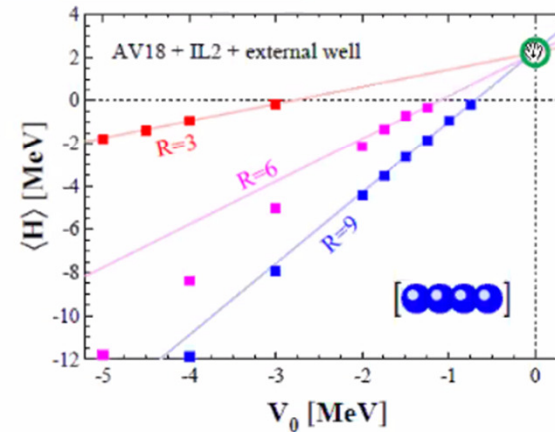


"3n resonances close to the physical region will not exist"

- (3n) Lazauskas, PRC 71 (2005) 044004 : 3NF ✗
- (4n) Lazauskas, PRC 72 (2005) 034003 : 4NF ✗
- (3,4n) Hiyama, PRC 93 (2016) 044004 : 3NF($T=3/2$) ✗!

► Many-body approximations, not so much ...

- Pieper, PRL 90 (2003), 252501 :



"the resonance, if it exists at all, must be very broad"

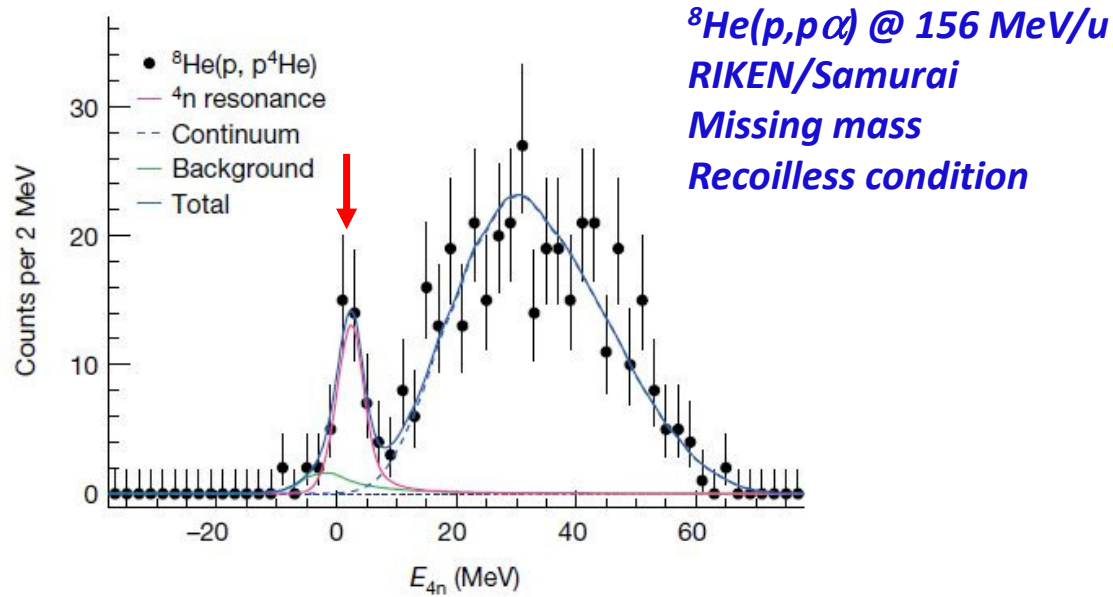
- Shirokov, PRL 117 (2016) 182502
 - Gandolfi, PRL 118 (2017) 232501
 - Fossezi, PRL 119 (2017) 032501
 - Li, PRC 100 (2019) 054313
- } 3n/4n ✓?

Courtesy from F.M.Marques

Observation of a correlated free four-neutron system

M. Duer et al., Nature (London) 606, 678 (2022)

<https://doi.org/10.1038/s41586-022-04827-6> M. Duer¹, T. Aumann^{1,2,3}, R. Gernhäuser⁴, V. Panin^{2,5}, S. Paschalis^{1,6}, D. M. Rossi¹,



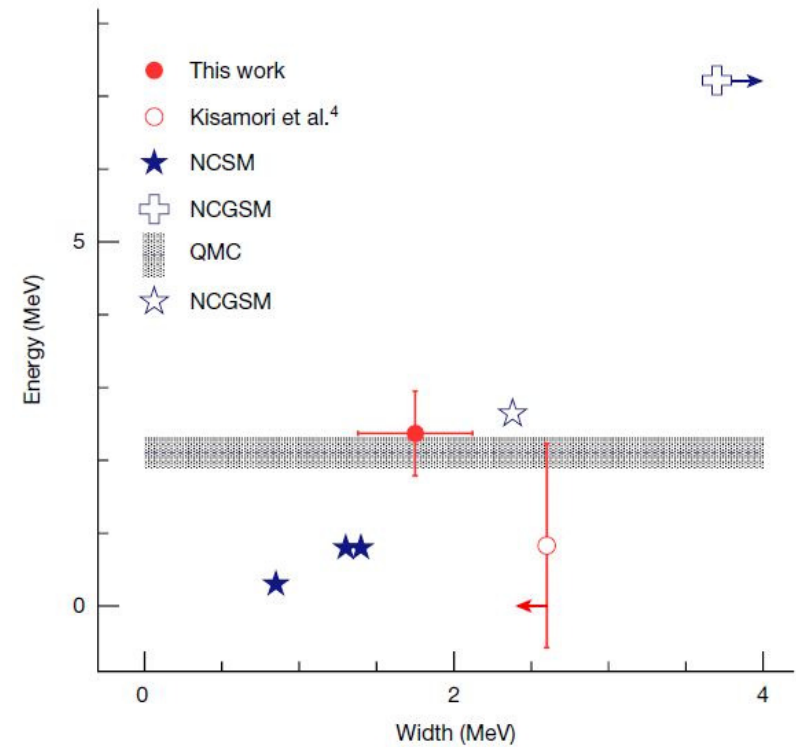
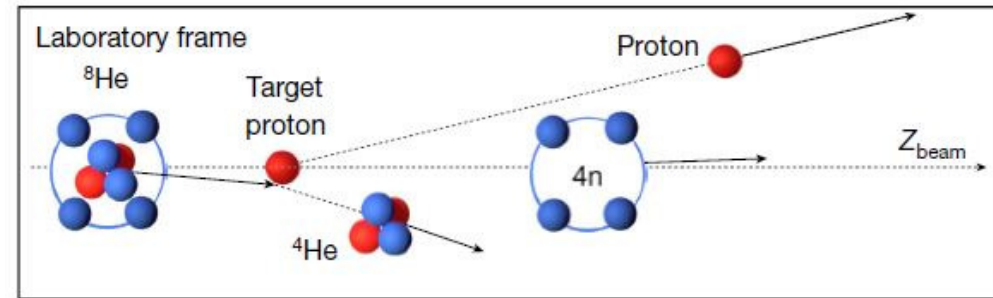
➤ **Low energy peak**

$$E = 2.37 \pm 0.38(\text{stat.}) \pm 0.44(\text{sys.}) \text{ MeV}$$

$$\Gamma = 1.7 \pm 0.22(\text{stat.}) \pm 0.30(\text{sys.}) \text{ MeV}$$

➤ **Broad bump**

well described by non-resonant continuum calculations



Interpretation by Lazauskas, Hiyama, Carbonell

Phys. Rev. Lett. 130, 102501 (2023)

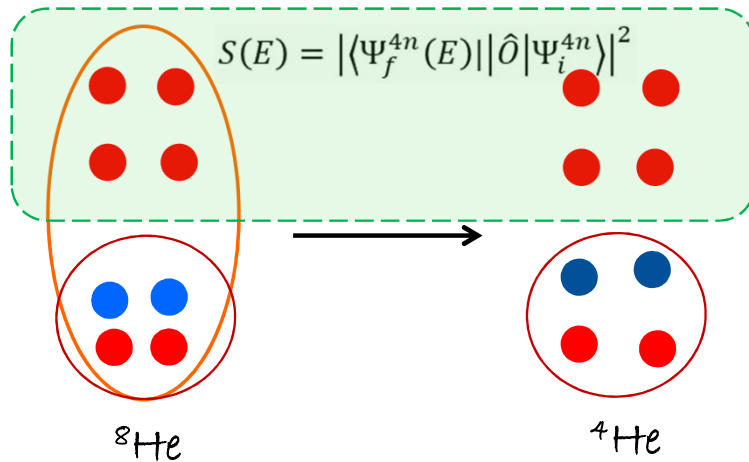
$$H_i = H_0 + \lambda \sum_{i=1}^N |\psi_\alpha(r_i)\rangle \langle \psi_\alpha(r_i)| + \sum_{i<j=1}^N V_{nn}(r_{ij})$$

$$+ \sum_{i=1}^N V(r_{iG}) + \sum_{i<j=1}^N W_{ij}(\rho, r_{ijG}).$$

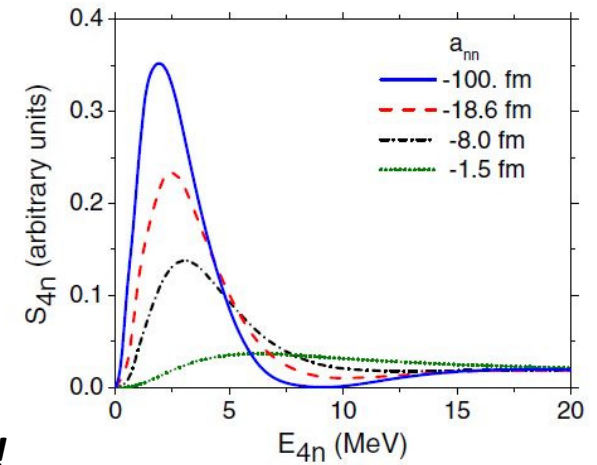
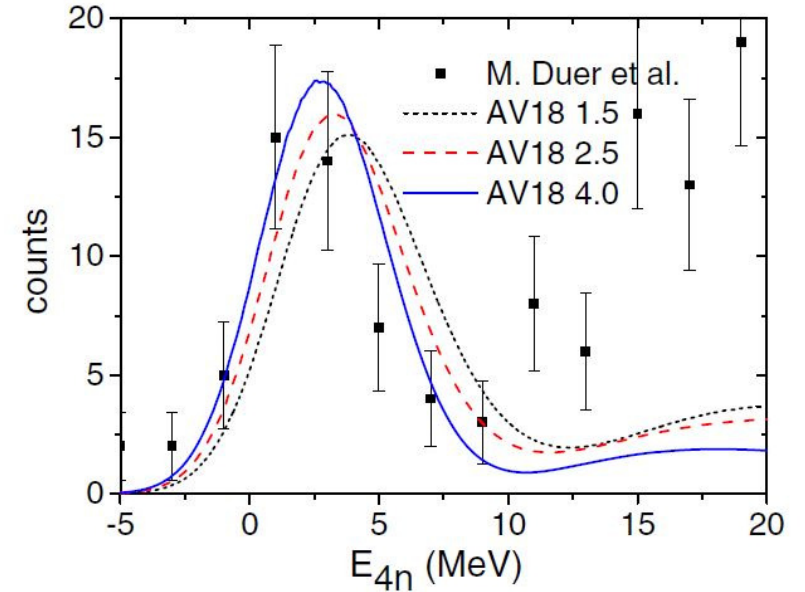
$$\begin{cases} H_i |\Psi_i\rangle = E_i |\Psi_i\rangle. \\ H_f |\Psi_f\rangle = E_{4n} |\Psi_f\rangle. \end{cases}$$

Action of the ^4He mean field on valence n 's adjusted to ^6He and ^8He GS binding

$$H_f = H_0 + \sum_{i<j=1}^4 V_{nn}(r_{ij}).$$



dineutron-dineutron correlations !



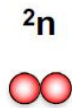
Conclusions/Prospects

3n and 4n system

- Data for ${}^8\text{He} (p,2p) \{{}^3\text{H}+4n\}$ (RIKEN/Samurai) under analysis (LPC Caen)
- $t (t, {}^3\text{He})3n$ (RIKEN/SHARAQ) under analysis (T.Miki)

6n system

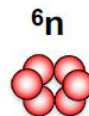
- ${}^{14}\text{Be}(p,pa){}^{10}\text{He}^* \rightarrow 6n + \alpha$ - Data from SAMURAI12 under analysis (O.Nasr, IJCLab)
- ${}^{11}\text{Li}(p,2p){}^{10}\text{He}^* \rightarrow 6n + \alpha$ - SAMURAI47 (Sp. T.Nakamura) to be run in June 2023
- ${}^{6,8}\text{He}(p,3p)$ accepted at RIKEN



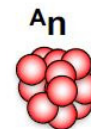
dineutron
 $\tau \sim 10^{-22}\text{s}$
Unbound,
No resonance
 $a_s = -18.9(4)\text{fm}$
Can exist in nuclei



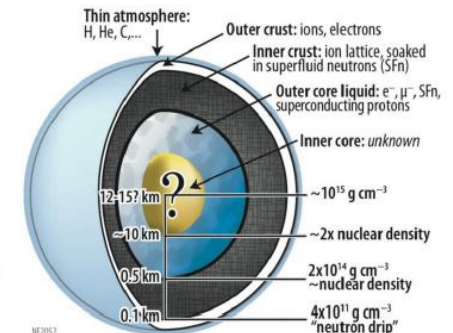
Tetra-neutron
 $\tau \sim \text{a few } 100 \text{ s?}$
or } 10^{-21} \text{ s?}
Studied since 1960s
Only recently, a few positive results have come out



Hexa-neutron
Never measured
Semi-magic?
More stable?



A_n -nuclei
Island of Stability?
Magic number?



Neutron Star
Still Lots of mystery
Uncertain R_{NS}
Uncertain Max M_{NS}
Uncertain Internal Structure

Sketch from T.Nakamura