



# Recent Belle II results related to B anomalies

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On behalf of the Belle II Collaboration

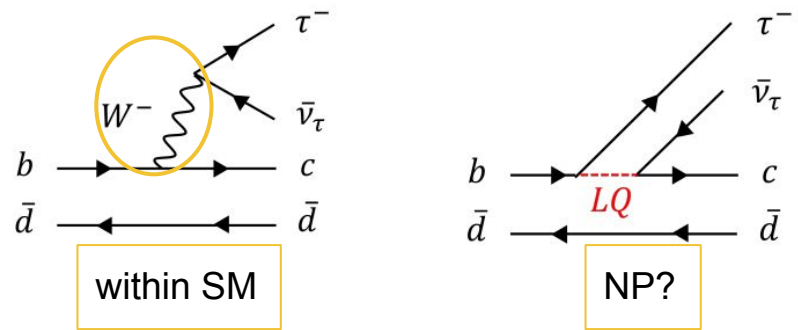
Beauty 2023 @ Clermont-Ferrand  
July 4th, 2023

- **Introduction**
  - **Lepton Flavour Universality**
  - **Belle II experiment**
- **Measurement of  $R(X_{e/\mu})$  at Belle II**
- **Measurement of angular asymmetry in  $B^0 \rightarrow D^* l \nu$**

# Lepton Flavour Universality

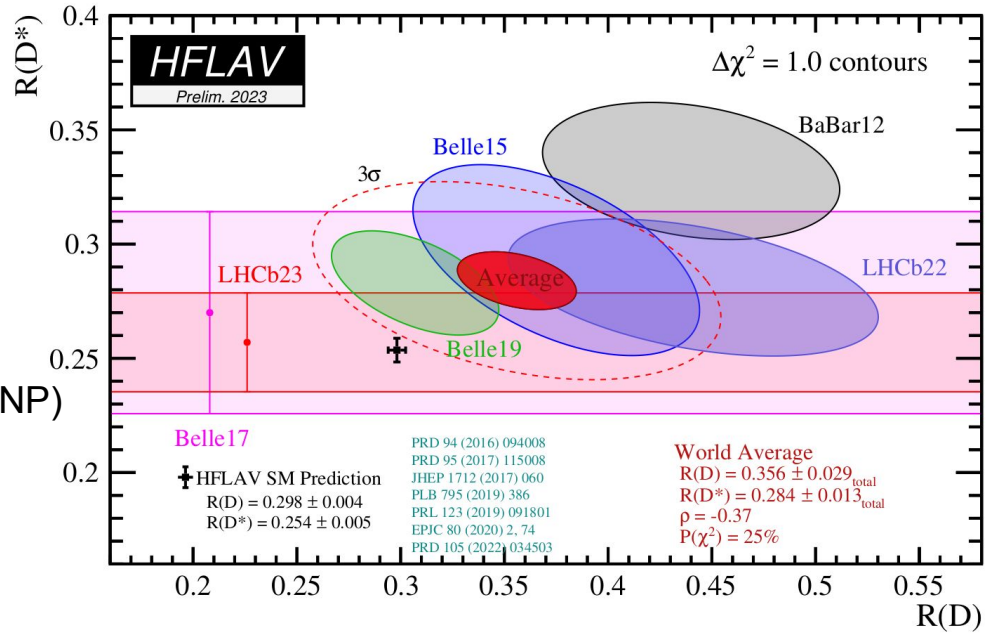
In SM, all charged leptons share the same electroweak coupling — Lepton Flavour Universality (LFU)

- Semileptonic  $B$ -meson decay involving the quark transition, e.g.  $b \rightarrow c/s \ell \nu$ ,  $b \rightarrow c/s \ell \ell$ , ... are sensitive to probe (violation of) LFU



Tension in  $R(D^*)$  could hint a possible new physics(NP)

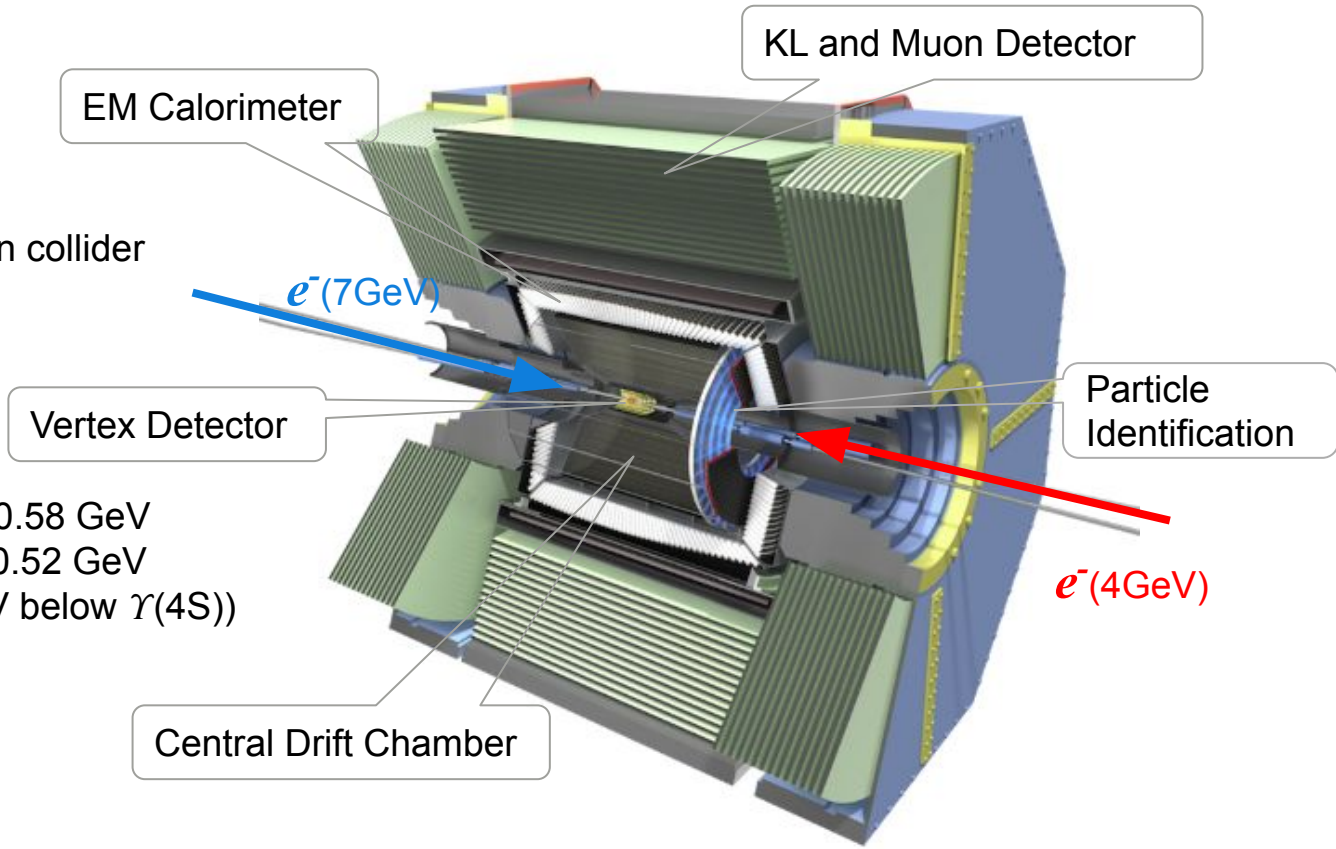
$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)}$$



# SuperKEKB and Belle II Experiment

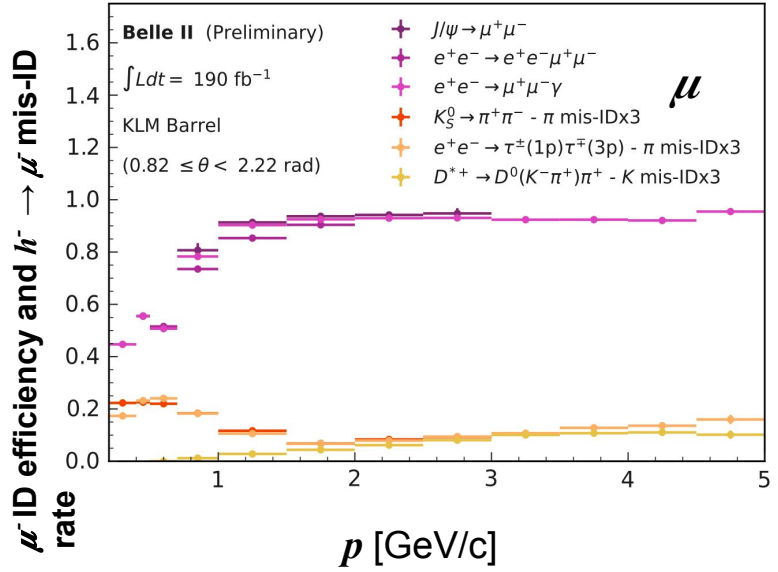
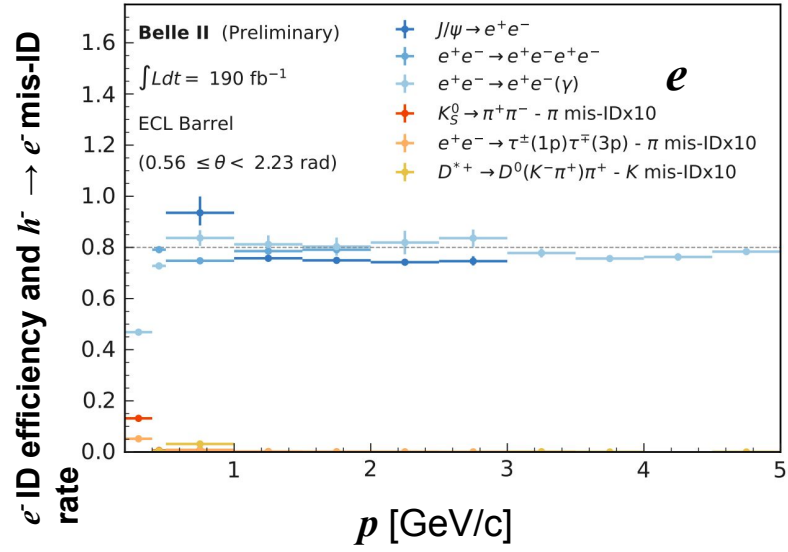
- B-factory : electron-positron collider running @  $\Upsilon(4S)$  producing with  $B\bar{B}$

- Data collected so far: (2019-2022 summer)  
 $\int \mathcal{L} dt = 362 \text{ fb}^{-1}$  @  $\sqrt{s} = 10.58 \text{ GeV}$   
 $\int \mathcal{L} dt = 42 \text{ fb}^{-1}$  @  $\sqrt{s} = 10.52 \text{ GeV}$  (60 MeV below  $\Upsilon(4S)$ )



$\sim 4\pi$  Acceptance

Leptons can be reconstructed with high efficiency and low fake-rate



Similar performance at high momentum for  $e$  and  $\mu$

# $R(X_{e/\mu})$ Measurement in $B \rightarrow X e/\mu \nu$

$$R(X_{e/\mu}) = \frac{B(B \rightarrow X e \nu)}{B(B \rightarrow X \mu \nu)}$$

Preparation for measuring inclusive  $R(X_{\tau/l})$

2301.08266v2 (accepted by PRL)

$X$ : generic hadronic final state of semi-leptonic decay with  $b \rightarrow c/ulv$

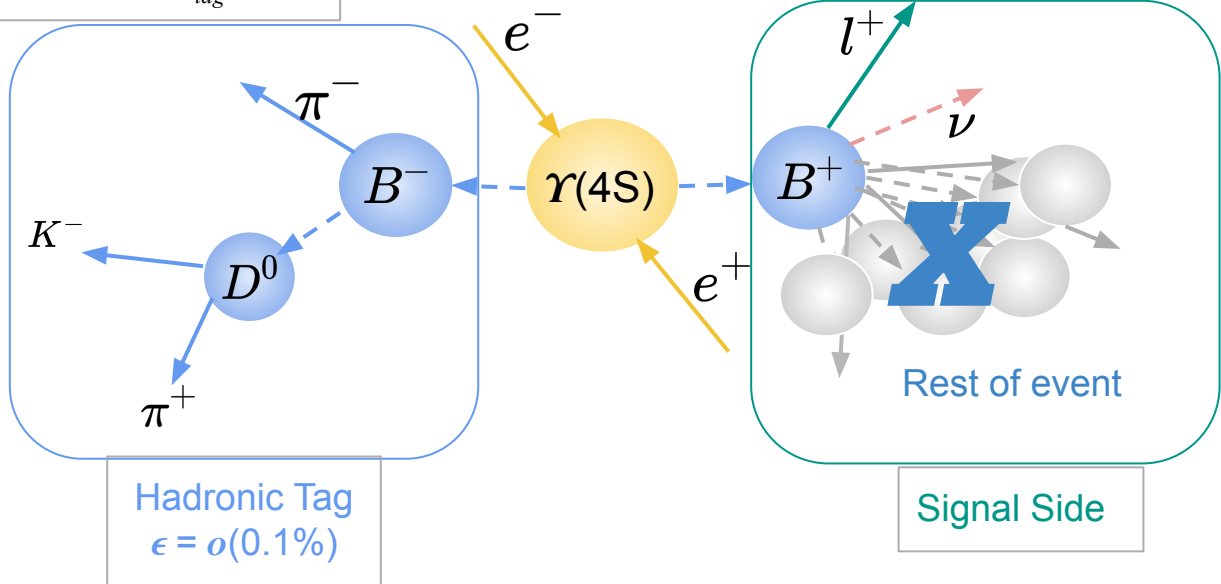
- Belle II data (2019-2021): **189 fb<sup>-1</sup> @  $\sqrt{s} = 10.58\text{GeV}$**   
+ 18 fb<sup>-1</sup> @  $\sqrt{s} = 10.52\text{GeV}$   
(off-resonance data ~ 60 MeV below  $\gamma(4S)$ )

Using Hadronic Full Event Interpretation (FEI) to reconstruct a  $B$ -meson :  $B_{tag}$

Lepton momentum in signal B rest-frame:  
 $p_l^B > 1.3 \text{ GeV}/c$

- Reject most of  $B \rightarrow X \tau \nu$  events
- Reduce fakes and secondaries

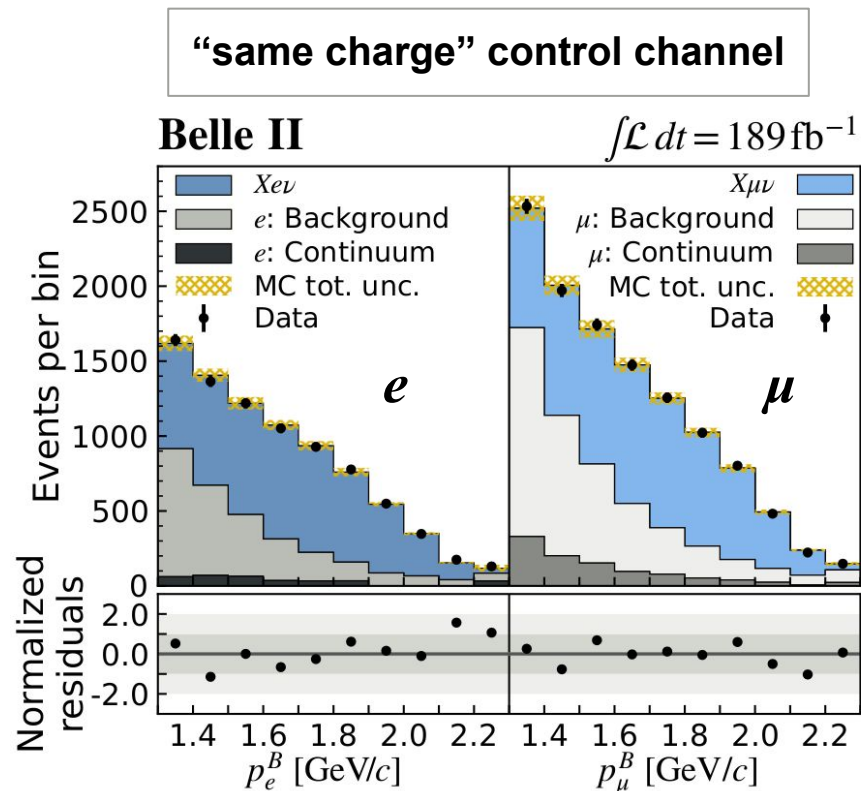
Opposite charge compared with  $B_{tag}$   
Select lepton with **highest lepton-ID probability**



Hadronic Tag  
 $\epsilon = o(0.1\%)$

Signal Side

- Fit  $e$  and  $\mu$  channels simultaneously in 10  $p_i^B$  bins with binned maximum likelihood fit
- 3 templates for each channel:
  - “Continuum”  
(scaled to ‘off-resonance data’)
  - + “Background”  
(fakes + secondaries +...)  
(constraint yields from same charge control channel)
  - +  $X e/\mu \nu$
- Systematics included as nuisance parameters





Extracting signal yields  $N_l^{means}$  in each channel

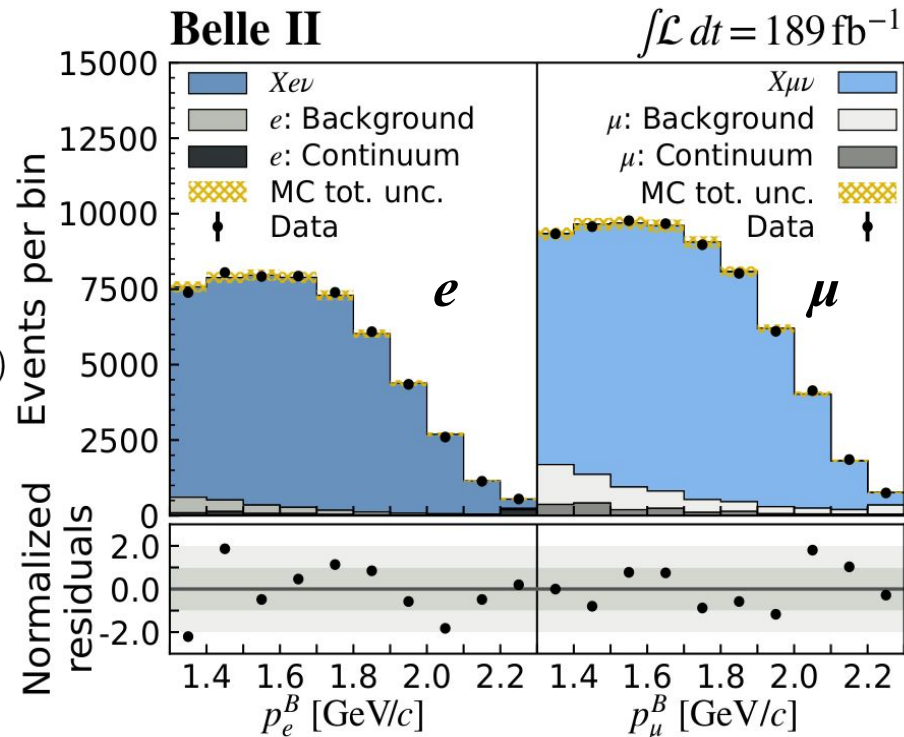
$$R(X_{e/\mu}) = \frac{N_e^{meas}/\epsilon_e}{N_\mu^{meas}/\epsilon_\mu}$$

$$R(X_{e/\mu}) = 1.007 \pm 0.009(stat.) \pm 0.019(syst.)$$

$$R(X_{e/\mu}, p_l^B > 1.3 GeV) = 1.005 \pm 0.009(stat.) \pm 0.019(syst.)$$

- Compatible with Belle measurements in  $B \rightarrow D^* l \nu$  [Phys. Rev. D 100, 052007], [2301.07529v1]
- Most precise branching fraction based lepton universality test with semileptonic  $B$  decays
- **Good agreement with SM prediction of** [JHEP11(2022)007]

$$R(X_{e/\mu}) = 1.006 \pm 0.001$$



# Angular Asymmetries of

$$B^0 \rightarrow D^* l \nu$$

Tests of light-lepton universality

preliminary results

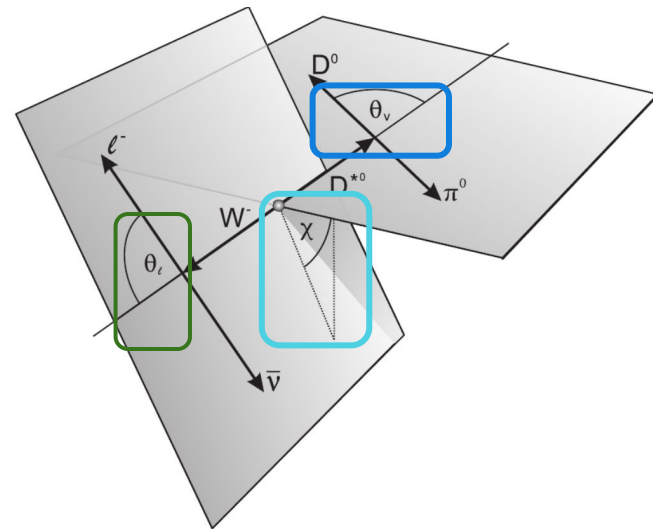
- 4 parameters to fully describe  $B^0 \rightarrow D^* l \nu$  decay:

squared invariant mass of  $l \nu$  system:  $q^2 = (p_B - p_{D^*})^2$   
 + 3 helicity angles  $\theta_l$ ,  $\theta_\nu$  and  $\chi$

- Properties of  $V-A$  coupling are encoded in angular distribution
- Tension in differences of  $A_{FB}$  between  $e$  and  $\mu$  is reported in a re-interpretation of Belle data

[Phys. Rev. D 100, 052007 (2019)] in [Eur. Phys. J. C 81, 984 (2021)]

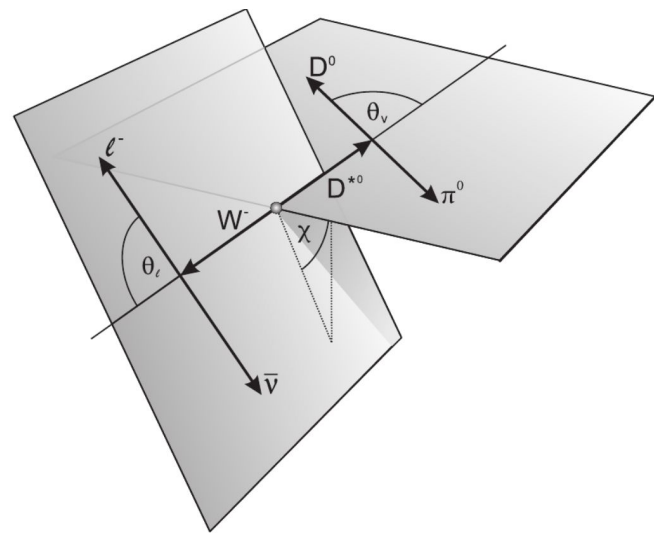
$$A_{FB}(q^2) = \left( \frac{d\Gamma}{dq^2} \right)^{-1} \left[ \int_0^1 - \int_{-1}^0 \right] d \cos \theta_\ell \frac{d^2\Gamma}{d \cos \theta_\ell dq^2}$$



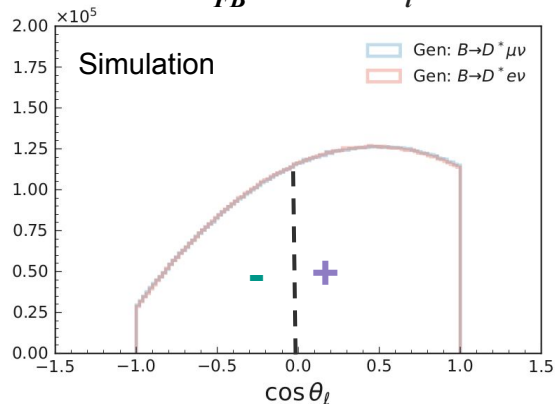
# Asymmetry Observables | Angular Analysis of $B^0 \rightarrow D^* l \nu$

$$A_x = \frac{\int_0^1 \frac{d\Gamma}{dx} dx - \int_{-1}^0 \frac{d\Gamma}{dx} dx}{\Gamma}$$

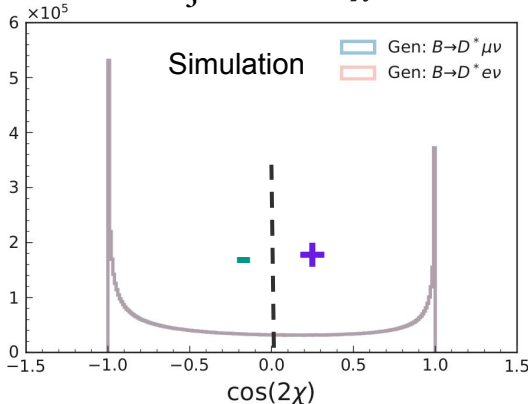
Define a set of 5 asymmetries for observables x



$$A_{FB}: x = \cos \theta_l$$



$$S_3: x = \cos 2\chi$$



$$A_x = \frac{N_x(x > 0) - N_x(x < 0)}{N_x(x > 0) + N_x(x < 0)}$$

$$S_5: x = \cos \chi \cos \theta_\nu$$

$$S_7: x = \sin \chi \cos \theta_\nu$$

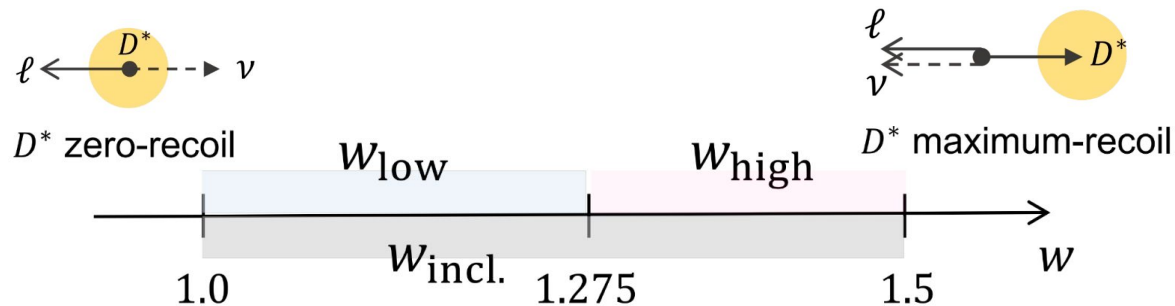
$$S_9: x = \sin 2\chi$$

$S_3, S_9$ : propensity in the alignment of  $l\nu$  and  $D^*$  system

Test  $e/\mu$  universality through the asymmetry difference  
 $\Delta A = A(B \rightarrow D^* \mu \nu) - A(B \rightarrow D^* e \nu)$

$D^*$  recoiling parameter  $w = \frac{m_B^2 + m_{D^*}^2 + q^2 c^2}{2m_B m_{D^*}}$

- $w_{\text{low}} < 1.275$
- $w_{\text{high}} > 1.275$
- $w_{\text{incl.}}$  : full phase-space



For each  $e$  and  $\mu$  channel, measure asymmetry for each angular observable **versus**  $w$

$$A_x(w) = \frac{N_x^+(w) - N_x^-(w)}{N_x^+(w) + N_x^-(w)}$$

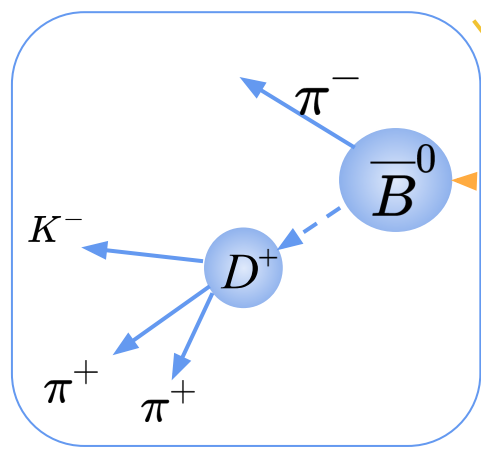
$$\Delta A_x(w) = A_x^\mu(w) - A_x^e(w)$$

# Event Reconstruction | Angular Analysis of $B^0 \rightarrow D^* l \nu$

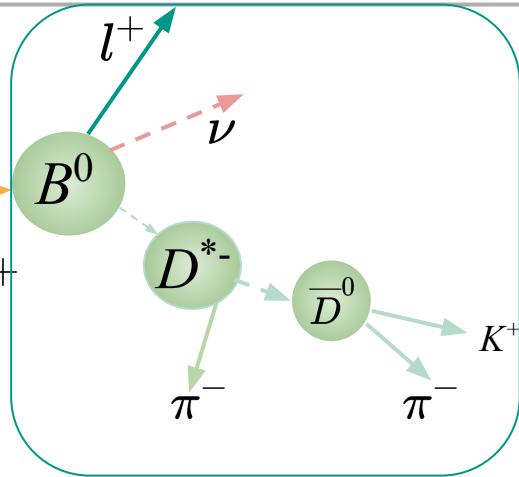
Belle II data (2019-2021):  $189 \text{ fb}^{-1} @ \sqrt{s} = 10.58 \text{ GeV}$

Using Hadronic FEI to reconstruct a  $B$ -meson :  $B_{tag}$

Hadronic Tag  
 $\epsilon = o(0.1\%)$



- Reconstruct a lepton with Lab frame momentum:  $p_l > 1 \text{ GeV}/c$
- Reconstruct a  $D$ -meson with clean and abundant decay modes
- Reconstruct a  $D^*$  by combining a  $D$  and a slow  $\pi$



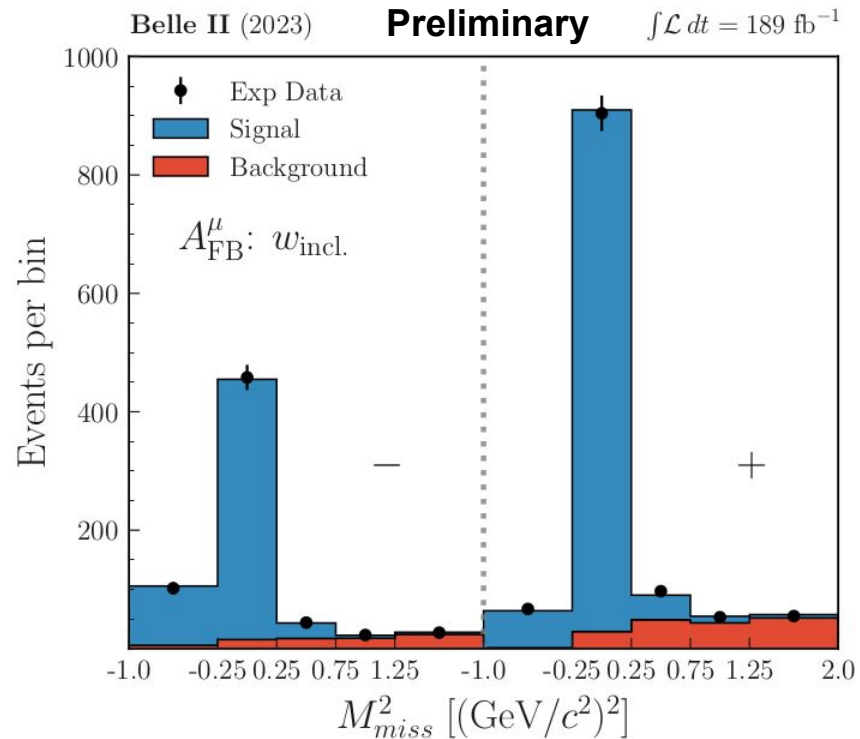
Signal Side  
Reconstruct exclusively by  $B^0 \rightarrow D^* l \nu$

Extract signal yields:

- Binned maximum likelihood fit to  $M_{miss}^2$

$$M_{miss}^2 = p_{miss}^2 = (p_{\gamma(4S)} - p_{B_{tag}} - p_{D^*} - p_l)^2$$

- Main background:  $B^0 \rightarrow D^{**} l \nu$
- Signal is peaked at zero in  $M_{miss}^2$



# Results | Angular Analysis of $B^0 \rightarrow D^* l \nu$

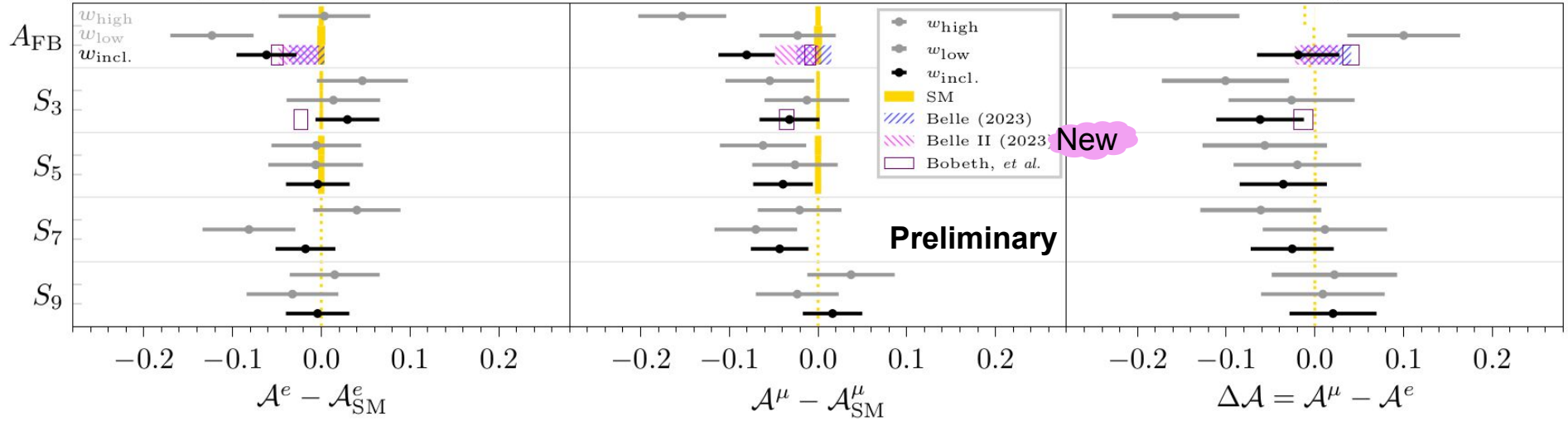
$e$  channel

$\mu$  channel

difference of  $e$  and  $\mu$  channels

Belle II (2023)

$\int \mathcal{L} dt = 189 \text{ fb}^{-1}$



- Statistics dominated
- **All results agree well with SM expectation**

[2301.07529v1](#) (Belle)  
[Eur. Phys. J. C 81, 984 \(2021\)](#)



The Belle II experiment perform two light-lepton universality tests recently

- Inclusive measurement of  $R(X_{e/\mu})$

**Preparation for measuring inclusive  $R(X_{\tau/l})$**

Compatible with **exclusive** Belle measurements

**Good agreement with SM prediction**

- Preliminary result on testing of LFU in angular asymmetry in  $B^0 \rightarrow D^* l \nu$

**Comprehensive LFU test in angular distributions** of semileptonic B decays

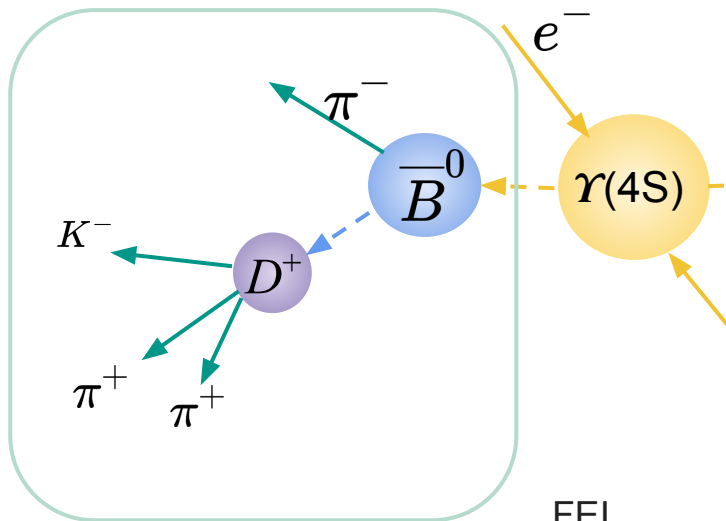
**Good consistency with SM prediction**

**backup**

B-meson pair is produced with opposite flavours

BDT-based algorithm with a hierarchical approach :

- Reconstruct tracks + clusters
- Reconstruct intermediate particles
- Reconstruct a B-meson



FEI

	$B^\pm$ (%)	$B^0$ (%)
Hadronic		
FEI with FR channels	0.53	0.33
FEI	0.76	0.46
FR	0.28	0.18
SER	0.4	0.2
Semileptonic		
FEI	1.80	2.04
FR	0.31	0.34
SER	0.3	0.6

$$R(X_{e/\mu}) = \frac{N_e^{\text{meas}}}{N_\mu^{\text{meas}}} \cdot \frac{N_\mu^{\text{sel}}}{N_e^{\text{sel}}} \cdot \frac{N_e^{\text{gen}}}{N_\mu^{\text{gen}}}$$

$$\epsilon_{Xlv} = \frac{N_{\text{sel}} \times \epsilon_{B_{\text{tag}}}^{\text{Data/MC}}}{2 \times N_{B\bar{B}} \times BR(B \rightarrow Xlv)}$$

$$\epsilon_{Xlv} = \frac{N_{\text{sel}} \times \epsilon_{B_{\text{tag}}}^{\text{Data/MC}}}{2 \times N_{B\bar{B}} \times BR(B \rightarrow Xlv, p_l^B > 1.3 \text{ GeV})}$$

$$R(X_{e/\mu})_{\text{indep}} = R(X_{e/\mu}) \times \frac{F_e^{p_l^B > 1.3 \text{ GeV}}}{F_\mu^{p_l^B > 1.3 \text{ GeV}}}$$

$$R(X_{e/\mu}, p_l^B > 1.3 \text{ GeV}) = 1.005 \pm 0.009(\text{stat.}) \pm 0.019(\text{sys.})$$

Main Sources	sample size	lepton identification	$B \rightarrow X l \nu$ branching fraction	$B \rightarrow X_c l \nu$ form factors	total
Uncertainties(%)	0.9	1.9	0.2	0.1	2.1

Error source	Combination			
	Relative ratio of final uncertainty / %			
	Offres	Fakes, Other	$X l \nu$	$R(X_{e/\mu})$
Total rel. Error	6.8	6.2	0.5	2.1
Statistical	96.0	69.9	79.3	22.0
“Fit”	2.1	19.3	12.4	2.4
PID	1.5	7.1	5.6	75.0
Track efficiency	0.0	0.0	0.0	0.0

completely correlated

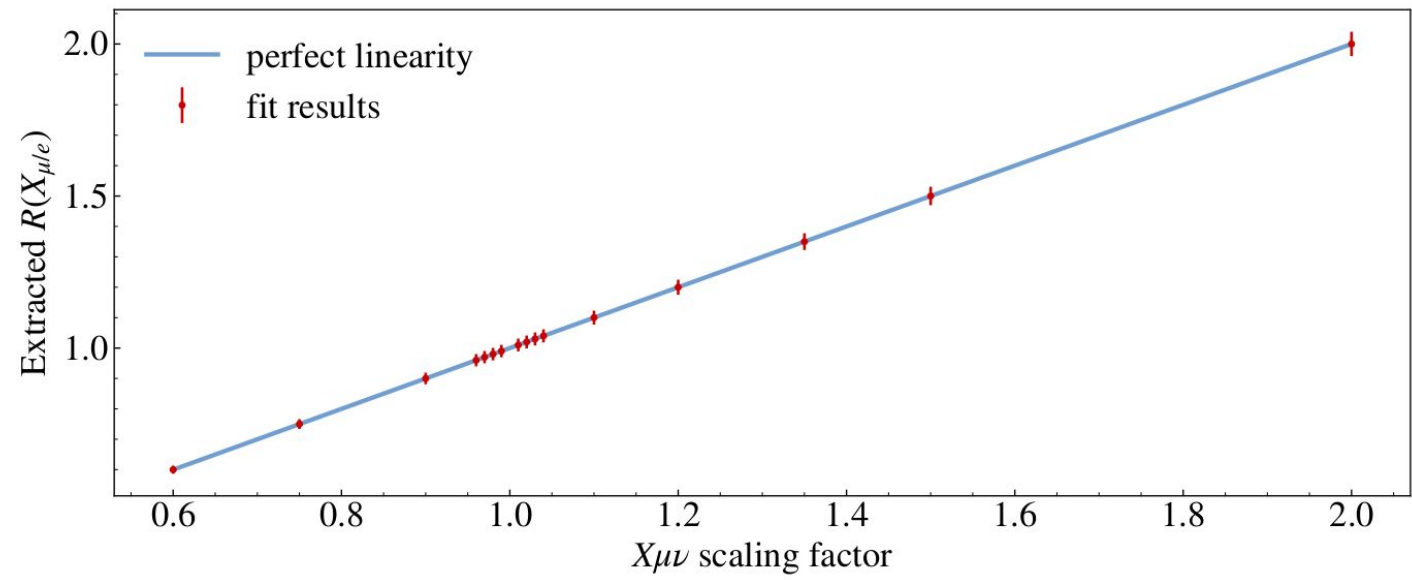
completely uncorrelated

Validated by toy study

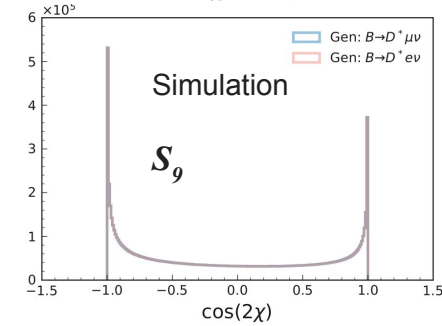
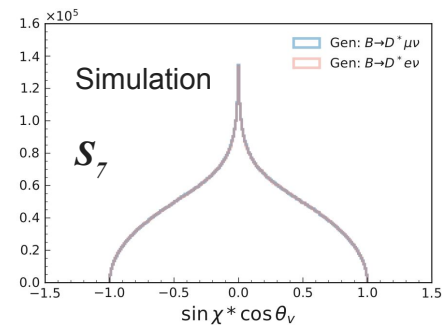
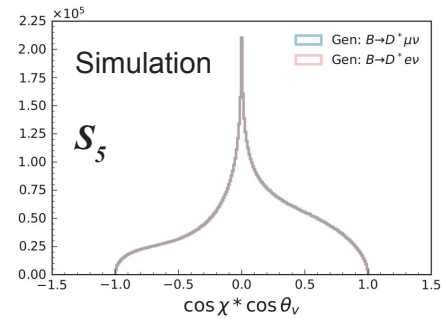
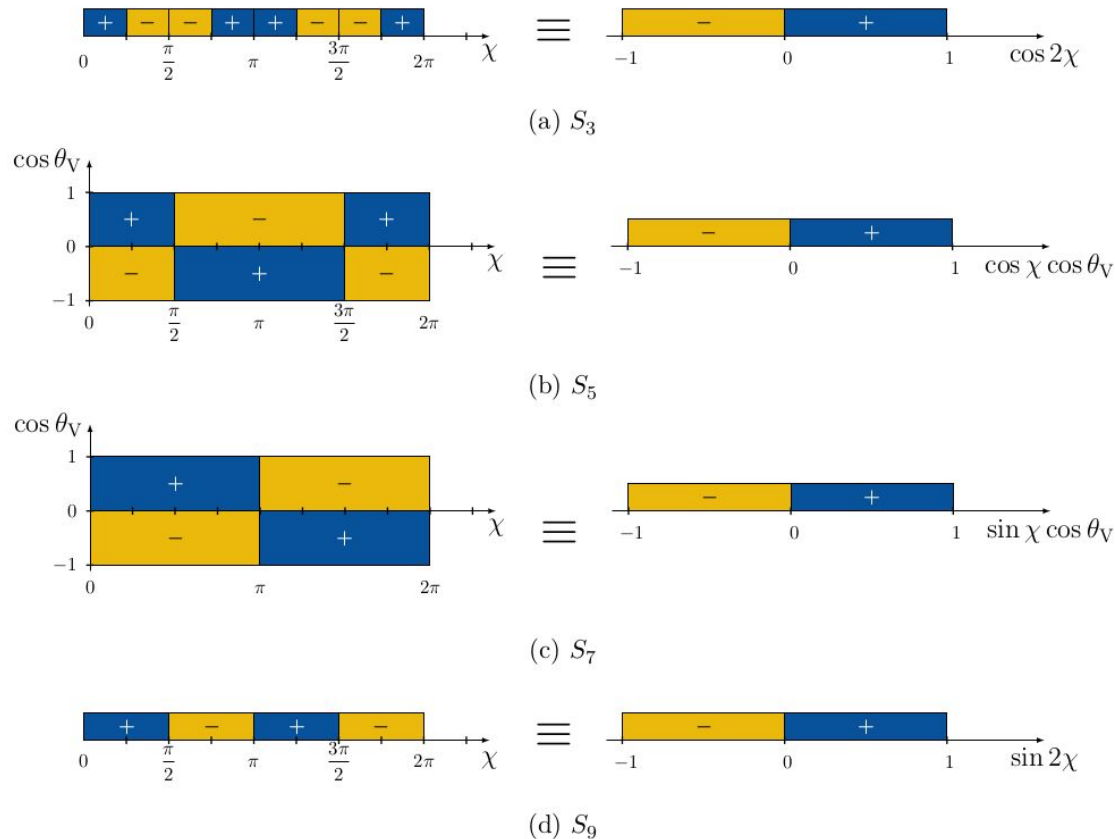
FF $D l \nu$	0.0	0.0	0.0	0.0
FF $D^* l \nu$	0.3	1.2	1.0	0.1
FF $D^{**} l \nu$	0.7	4.5	3.5	0.6
FF $GAP l \nu$	1.0	5.0	4.0	0.2
FF $X_c l \nu$ corr.	-0.9	-4.3	-3.5	-0.1
FF $X_c \tau \nu$ total	0.0	0.0	0.0	0.0
FF $D \tau \nu$	0.0	0.0	0.0	0.0
FF $D^* \tau \nu$	0.0	0.0	0.0	0.0
FF $GAP \tau \nu$	0.0	0.0	0.0	0.0
FF $X_c \tau \nu$ corr.	-0.0	-0.0	-0.0	-0.0

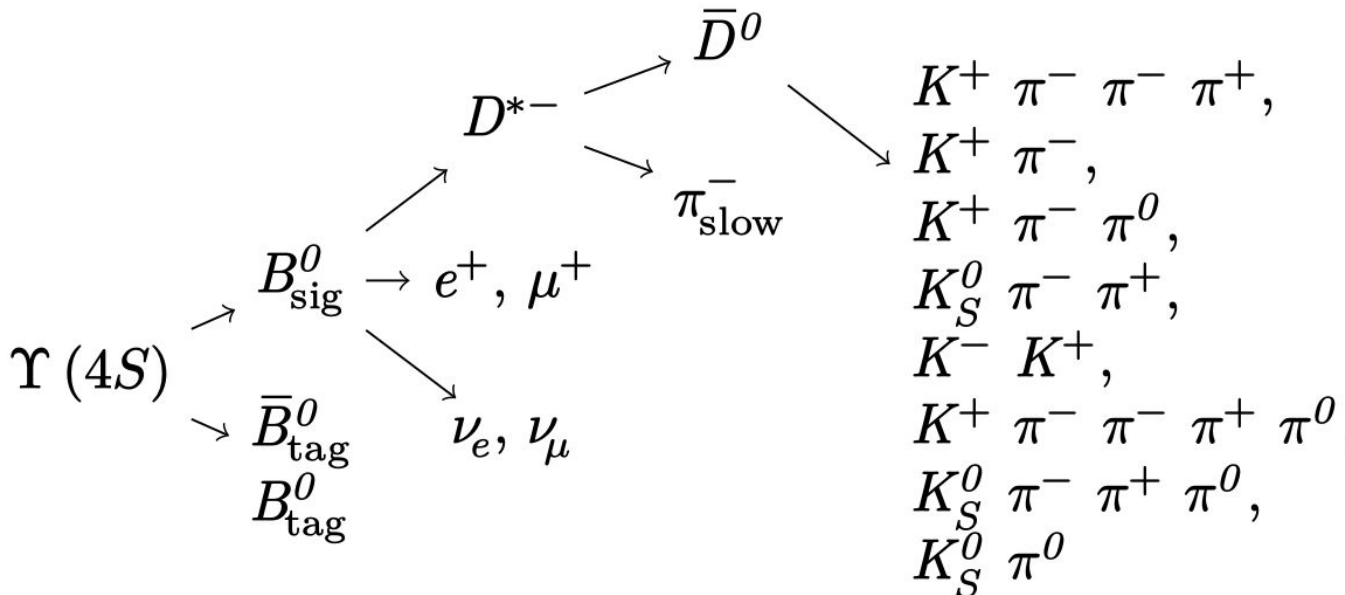
$\mathcal{B}(X_c l \nu)$ tot.	1.4	7.6	5.9	0.2
$\mathcal{B}(D l \nu)$	0.0	0.1	0.1	0.0
$\mathcal{B}(D^* l \nu)$	0.2	1.4	1.0	0.0
$\mathcal{B}(D^{**} l \nu)$	0.3	1.3	1.1	0.0
$\mathcal{B}(D^{(*)} \pi \pi l \nu)$	0.2	0.5	0.4	0.0
$\mathcal{B}(D^{(*)} \eta l \nu)$	1.4	6.4	5.2	0.2
$\mathcal{B}(D_s K l \nu)$	0.0	0.0	0.0	0.0
$\mathcal{B}(X_c l \nu)$ corr.	-0.7	-2.2	-1.9	-0.0
$\mathcal{B}(X_c \tau \nu)$ tot.	0.0	0.0	0.0	0.0
$\mathcal{B}(D \tau \nu)$	0.0	0.0	0.0	0.0
$\mathcal{B}(D^* \tau \nu)$	0.0	0.0	0.0	0.0
$\mathcal{B}(D^{**} \tau \nu)$	0.0	0.0	0.0	0.0
$\mathcal{B}(D^{(*)} \pi \pi \tau \nu)$	0.0	0.0	0.0	0.0
$\mathcal{B}(D^{(*)} \eta \tau \nu)$	0.0	0.0	0.0	0.0
$\mathcal{B}(X_c \tau \nu)$ corr.	-0.0	-0.0	-0.0	-0.0

Fit sensitivity test



the extracted  $R(X_{e/\mu})$  values perfectly follow the expected line





Visualization of the reconstructed  $\Upsilon(4S)$  decay chain, only reconstructed final states are shown explicitly



# Results | Angular Analysis of $B^0 \rightarrow D^* l \nu$

Obs.	$w$ bin	Measurement	SM $\times 10^5$
$\Delta A_{\text{FB}}$	$w_{\text{low}}$	$0.099 \pm 0.064$	$-104 \pm 2$
	$w_{\text{high}}$	$-0.168 \pm 0.072$	$-1133 \pm 9$
	$w_{\text{incl.}}$	$-0.024 \pm 0.046$	$-566 \pm 7$
$\Delta S_3$	$w_{\text{low}}$	$-0.026 \pm 0.071$	$28 \pm 0.2$
	$w_{\text{high}}$	$-0.101 \pm 0.072$	$23 \pm 1$
	$w_{\text{incl.}}$	$-0.062 \pm 0.049$	$18 \pm 1$
$\Delta S_5$	$w_{\text{low}}$	$-0.019 \pm 0.072$	$27 \pm 0.3$
	$w_{\text{high}}$	$-0.055 \pm 0.07$	$107 \pm 4$
	$w_{\text{incl.}}$	$-0.035 \pm 0.049$	$49 \pm 2$
$\Delta S_7$	$w_{\text{low}}$	$0.011 \pm 0.07$	$0 \pm 0$
	$w_{\text{high}}$	$-0.061 \pm 0.068$	$0 \pm 0$
	$w_{\text{incl.}}$	$-0.026 \pm 0.047$	$0 \pm 0$
$\Delta S_9$	$w_{\text{low}}$	$0.009 \pm 0.07$	$0 \pm 0$
	$w_{\text{high}}$	$0.022 \pm 0.071$	$0 \pm 0$
	$w_{\text{incl.}}$	$0.02 \pm 0.049$	$0 \pm 0$

$w$ -Integrated	Central Exp	Stat MC	shape	Unf. & eff.	Lep. ID	$\pi_{\text{slow}}$ eff.	$\mathcal{B}(D^{**})$	$K_S^0$ eff.	form factors	SM
$A_{\text{FB}}^\mu$	0.159	0.030	0.003	0.007	0.0017	0.0002	0.0000	0.0001	$3.03 \times 10^{-6}$	0.0037
$A_{\text{FB}}^e$	0.183	0.032	0.004	0.007	0.0032	0.0002	0.0000	0.0001	$3.52 \times 10^{-7}$	0.0037
$\Delta A_{\text{FB}}$	0.024	0.044	0.005	0.010	0.0036	0.0002	0.0000	0.0003	$4.95 \times 10^{-7}$	0.0000
$S_3^\mu$	0.142	0.032	0.003	0.008	0.0005	0.0002	0.0000	0.0001	$5.48 \times 10^{-6}$	0.0020
$S_3^e$	0.080	0.034	0.004	0.008	0.0004	0.0002	0.0000	0.0001	$5.27 \times 10^{-6}$	0.0020
$\Delta S_3$	0.062	0.046	0.005	0.011	0.0006	0.0004	0.0000	0.0001	$2.10 \times 10^{-7}$	0.0000
$S_5^\mu$	0.155	0.032	0.003	0.008	0.0003	0.0003	0.0000	0.0001	$4.20 \times 10^{-6}$	0.0035
$S_5^e$	0.190	0.034	0.004	0.008	0.0009	0.0008	0.0000	0.0001	$5.50 \times 10^{-6}$	0.0036
$\Delta S_5$	0.035	0.046	0.005	0.011	0.0010	0.0005	0.0000	0.0002	$1.30 \times 10^{-6}$	0.0000
$S_7^\mu$	0.043	0.031	0.003	0.008	0.0001	0.0001	0.0000	0.0001	$4.69 \times 10^{-7}$	0.0000
$S_7^e$	0.018	0.032	0.004	0.008	0.0002	0.0001	0.0000	0.0001	$1.02 \times 10^{-7}$	0.0000
$\Delta S_7$	0.026	0.044	0.005	0.011	0.0003	0.0001	0.0000	0.0001	$3.68 \times 10^{-8}$	0.0000
$S_9^\mu$	0.016	0.032	0.004	0.008	0.0001	0.0002	0.0000	0.0001	$2.12 \times 10^{-7}$	0.0000
$S_9^e$	0.004	0.034	0.003	0.008	0.0002	0.0001	0.0000	0.0001	$3.39 \times 10^{-7}$	0.0000
$\Delta S_9$	0.020	0.046	0.005	0.011	0.0003	0.0002	0.0000	0.0002	$1.28 \times 10^{-7}$	0.0000