

The experimental study I am presenting today was inspired by discussions I had with Peter about ten years ago

# Temperature and density conditions for alpha clustering in alpha-conjugate nuclei

## $^{40}\text{Ca}+^{12}\text{C}$ , 25 AMeV with CHIMERA multidetector (LNS Catania)

B. Borderie<sup>a</sup>, Ad. R. Raduta<sup>a,b</sup>, G. Ademard<sup>a</sup>, M. F. Rivet<sup>a</sup>, E. De Filippo<sup>c</sup>,  
E. Geraci<sup>c,d,e</sup>, N. Le Neindre<sup>a,f</sup>, R. Alba<sup>g</sup>, F. Amorini<sup>g</sup>, G. Cardella<sup>c</sup>, M.  
Chatterjee<sup>h</sup>, D. Guinet<sup>i</sup>, P. Lantesse<sup>i</sup>, E. La Guidara<sup>c,j</sup>, G. Lanzalone<sup>g,k</sup>, G.  
Lanzano<sup>c,l</sup>, I. Lombardo<sup>g,d</sup>, O. Lopez<sup>f</sup>, C. Maiolino<sup>g</sup>, A. Pagano<sup>c</sup>, S.  
Pirrone<sup>c</sup>, G. Politi<sup>c,d</sup>, F. Porto<sup>g,d</sup>, F. Rizzo<sup>g,d</sup>, P. Russotto<sup>g,d</sup>, J.P. Wieleczko<sup>l</sup>

<sup>a</sup>*Institut de Physique Nucléaire, CNRS/IN2P3, Université Paris-Sud 11, Orsay, France*

<sup>b</sup>*National Institute for Physics and Nuclear Engineering, Bucharest-Magurele, Romania*

<sup>c</sup>*INFN, Sezione di Catania, Italy*

<sup>d</sup>*Dipartimento di Fisica e Astronomia, Università di Catania, Italy*

<sup>e</sup>*INFN, Sezione di Bologna and Dipartimento di Fisica, Università di Bologna, Italy*

<sup>f</sup>*LPC, CNRS/IN2P3, Ensicaen, Université de Caen, Caen, France*

<sup>g</sup>*INFN, Laboratori Nazionali del Sud, Catania, Italy*

<sup>h</sup>*Saha Institute of Nuclear Physics, Kolkata, India*

<sup>i</sup>*Institut de Physique Nucléaire, CNRS/IN2P3, Université Claude Bernard Lyon 1,  
Villeurbanne, France*

<sup>j</sup>*CSFNSM, Catania, Italy*

<sup>k</sup>*Università di Enna "Kore", Enna, Italy*

<sup>l</sup>*GANIL, (DSM-CEA/CNRS/IN2P3), Caen, France*

# Outline of the talk

Motivations: theoretical calculations which predict that at low density alpha-conjugate nuclei spontaneously cluster into alpha-particles

Experimental strategy and experiment - How to isolate alpha-conjugate sources with selections

Results

- i) comparisons to simulations (seq. versus simul. emission) to sign a clustering
- ii) extract T and density conditions

Conclusion

# Constrained Hartree-Fock-Bogoliubov approach using Gogny D1S int. $^{16}\text{O}$ , $^{20}\text{Ne}$ ... Constrained self-consistent relativistic Hartree-Bogoliubov (RHB) model based on DD-ME2 effective interaction both by imposing radial deformation

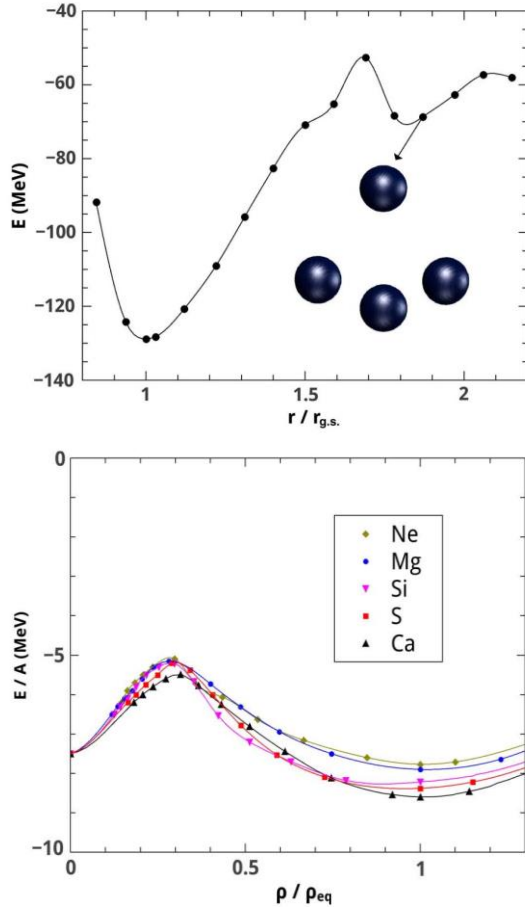


FIG. 5 (color online). Equation of state for a choice of self-conjugate nuclei (EOS-A) as a function of average density scaled by the one at equilibrium; see text for detailed definition.

M. Girod and P. Schuck, PRL 111 (2013) 132503 J.-P. Ebran, E. Khan et al., PRC 89 031303(R) 2014

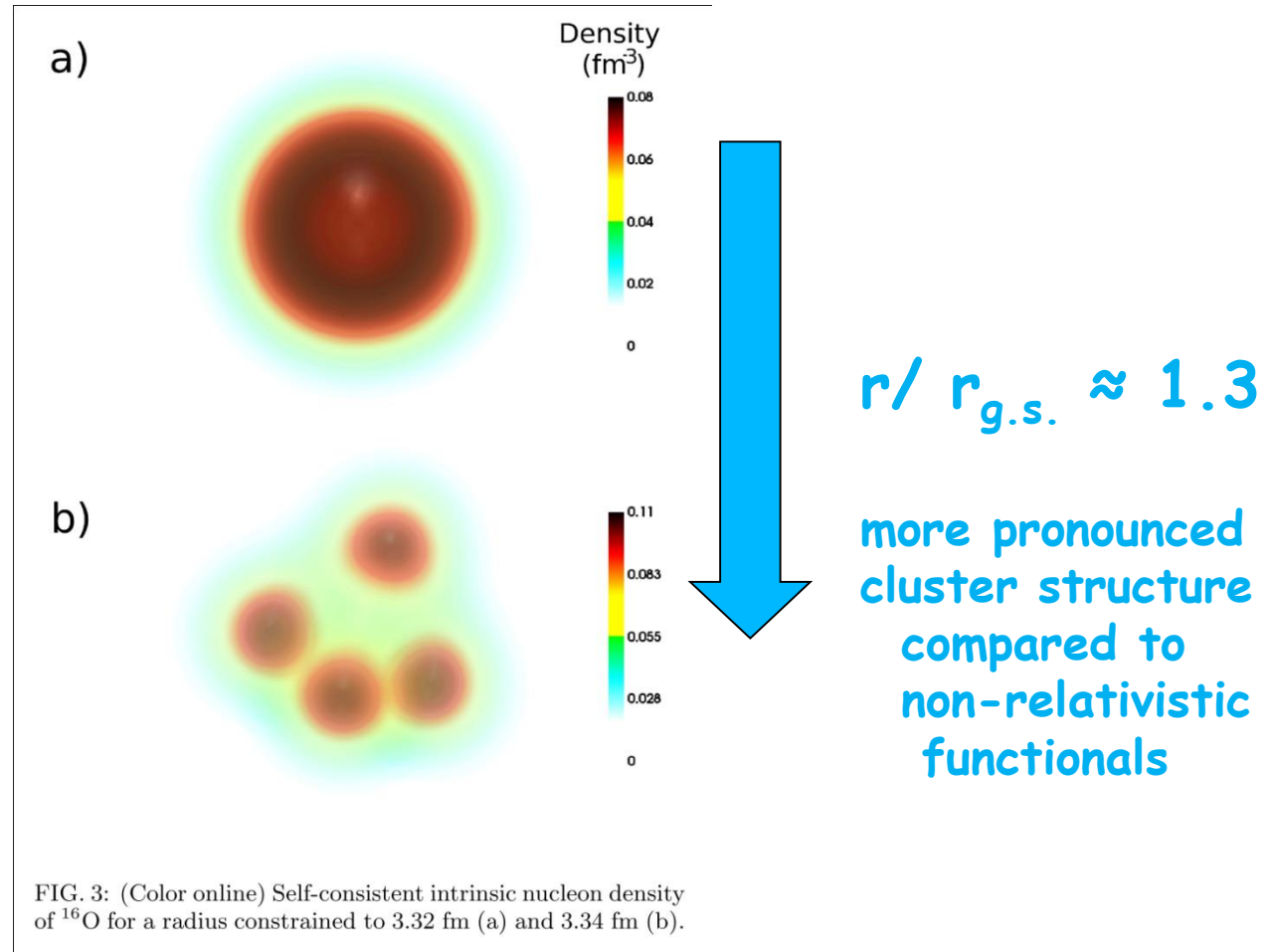


FIG. 3: (Color online) Self-consistent intrinsic nucleon density of  $^{16}\text{O}$  for a radius constrained to 3.32 fm (a) and 3.34 fm (b).

# Experimental strategy

We search for a possible simultaneous emission of alpha-particles from excited expanding alpha-conjugate nuclei

intermediate energy HI reactions to possibly produce some hot expanding projectile fragmentation products

→  $^{40}\text{Ca} + ^{12}\text{C}$  at 25 MeV per nucleon

associated with high detection granularity (CHIMERA) to precisely reconstruct velocity vectors

Well known that around 25-30 AMeV incident energy fragmentation of  $^{20}\text{Ne}$  projectiles is dominated by alpha-conjugate fragmentation products  $^{16}\text{O}$ ,  $^{12}\text{C}$ ...

M. Morjean et al., NPA 438 1985 547

# CHIMERA experiment

1192 telescopes 94% of  $4\pi$

Si  $\approx$  200-300  $\mu\text{m}$

CsI(Tl) from 12 to 3 cm

beam intensity:  $10^7$  ions/s

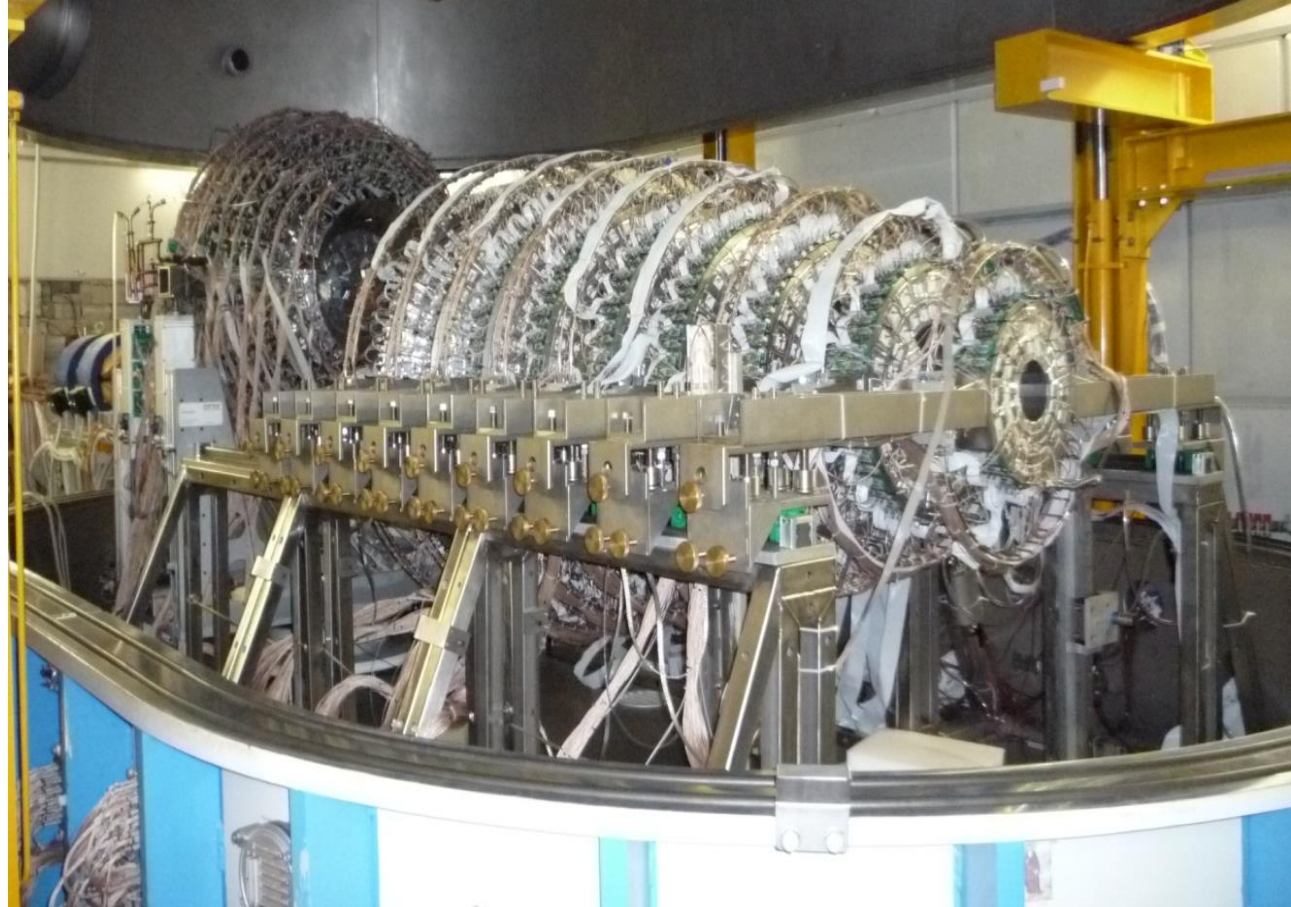
thin target  $320\mu\text{g}/\text{cm}^2$

to avoid random coinc.

angular range used:  $\Theta=1-62^\circ$

=> 816 telescopes

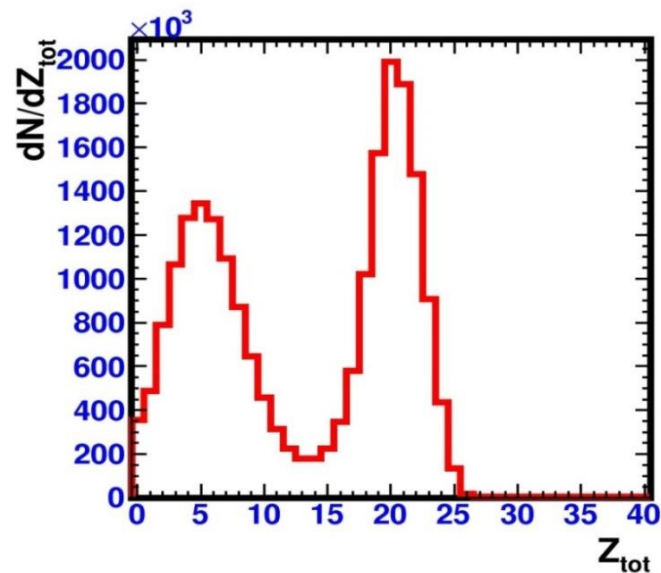
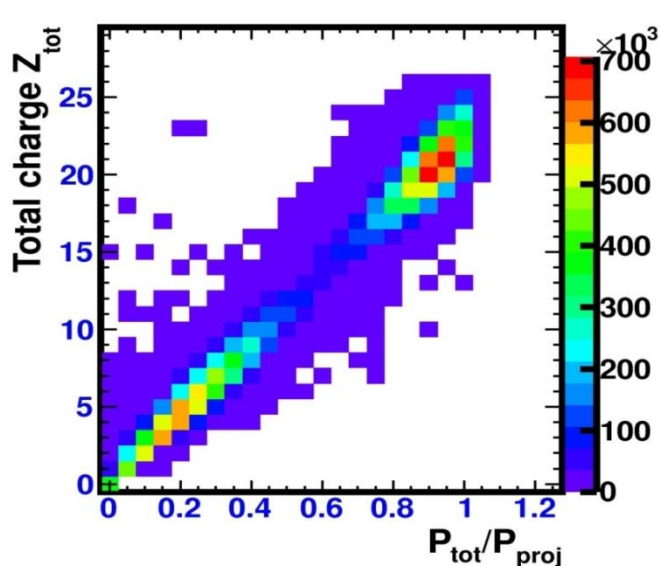
Identification in  $Z$  and  $A$   
for the energy range and  
reaction products of interest



alpha-particles of interest lose the major part of their energy in CsI(Tl):  
dedicated energy calib. from time of flight - energy resolution 1-2.5%

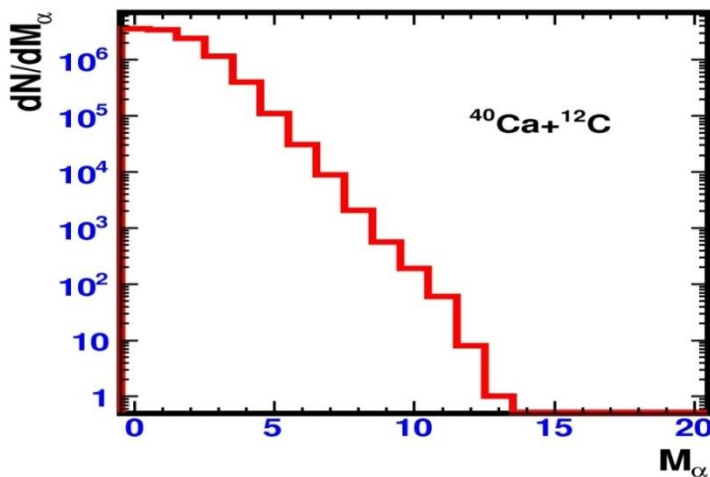
# Overview of event reconstruction/identification

grazing angle =  $1.11^\circ$  - ring 1I ( $1.0^\circ - 1.8^\circ$ ) suppressed to eliminate elas./ quasi elas.



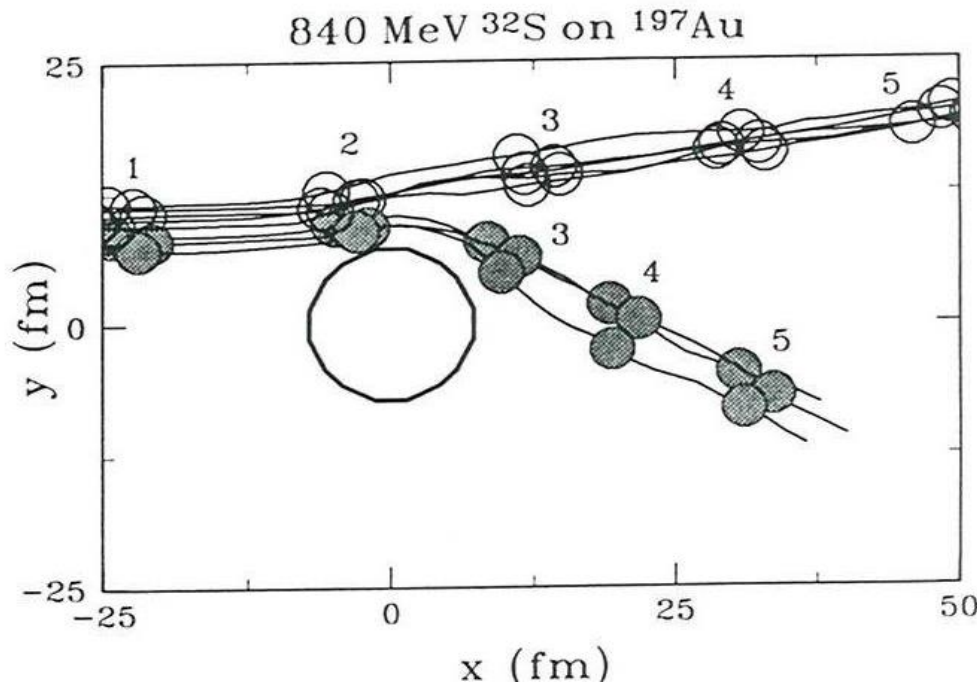
from geometrical efficiency  
well measured events

$$\Rightarrow Z_{tot} \geq 19$$



# Selected mechanism: Proj. Frag. (PF) => $Z_{\text{tot}}=20$ Selected events?

$^{32}\text{S} \approx 26 \text{ AMeV}$  - surface friction model + alpha substructure of the projectile + random force ( elastic  $\alpha - \alpha$  scattering cross section)  
H. Fuchs and K. Mohring, Rep. on Prog. in Physics 57 (1994) n°3



$^{20}\text{Ne}$   
(weakly excited)  
quasi elastic traj.

$^{12}\text{C}^*$   
much more excited  
significantly slowed down  
deflec. to negative angles

For  $^{40}\text{Ca} \Rightarrow 1$  excit. PF which deexcites into alphas ( $M_\alpha=4,5,6,7$ )  
+ a single weakly excited frag. ( $Z_{\text{frag}}=20-2 \times M_\alpha$ )

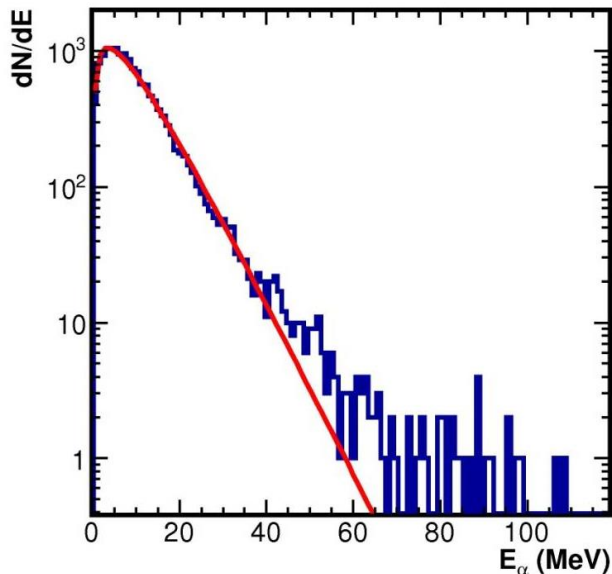


# Selected mechanism - Proj. Frag. (PF) $Z_{\text{tot}}=20$

Selected events: ( $M_{\alpha}=4,5,6,7$ ) + one frag. ( $Z_{\text{frag}}=20-2\times M_{\alpha}$ )

Alpha energy spectrum in the Na c.m.  $M_{\alpha}=5$

Maxwellian distribution  
Presence of preequil.



The question is: does  $M_{\alpha}$  come exclusively from a single set of excited  $\alpha$ -conjugate nuclei? called also Na sources in what follows

## Additional selections

Some  $\alpha$ -particles from preequil.

Some  $\alpha$ -particles from  $^{12}\text{C}^*$ ,  $^{16}\text{O}^*$  (unbound states) either fragments or emitted from Na systems

=> about 10% of events removed

see B.B. et al., PLB 755 (2016) 475,

J. Phys. Conf. Ser. 863 (2017) 012054

=> After selections the answer is yes

Different  $M_{\alpha}$  come exclusively from sets of excited  $\alpha$ -conjugate nuclei

Next step: deexcitation mode ?

$\langle E^* \rangle$  ? T? density ?

# Deexcitation mode

Are  $\alpha$ -particles emitted sequentially or simultaneously from Na sources ?

Answer by comparing to simulations

Simulations with exp.velocity dist., exp.  $E^*$  dist., and ang.moment. dist. as inputs

Results of simulations

filtered by the multidetector replica including detection and identification details - detection efficiency (46.7 to 27.2% when  $Ma$  varies from 4 to 7)

# Are $\alpha$ -particles emitted sequentially or simultaneously from Na sources ?

Sequential emission: GEMINI++ code

Hauser-Feschbach formalism for evap. of particles ( $Z < 5$ )

$n$ ,  $p$ ,  $t$ ,  ${}^3\text{He}$ ,  $\alpha$ -particle,  ${}^6\text{He}$ ,  ${}^{6-8}\text{Li}$  and  ${}^{7-10}\text{Be}$

Transition state formalism for fragments ( $Z > 4$ )

Best agreement with data is obtained with gaussian distributions ( $\text{RMS} = 1.5\hbar$ ) for spin inputs

Simultaneous emission (clustering) mimics a situation in which  $\alpha$  clusters are early formed when the Na system is expanding (theoretical predictions) due to thermal pressure.

i) Na systems split into  $N$   $\alpha$

ii) the remaining available energy ( $E^* + Q$ ) is randomly shared among the  $N$   $\alpha$ -particles such as to conserve energy and linear momentum

J.A. Lopez and J. Randrup, NPA 491 (1989) 477

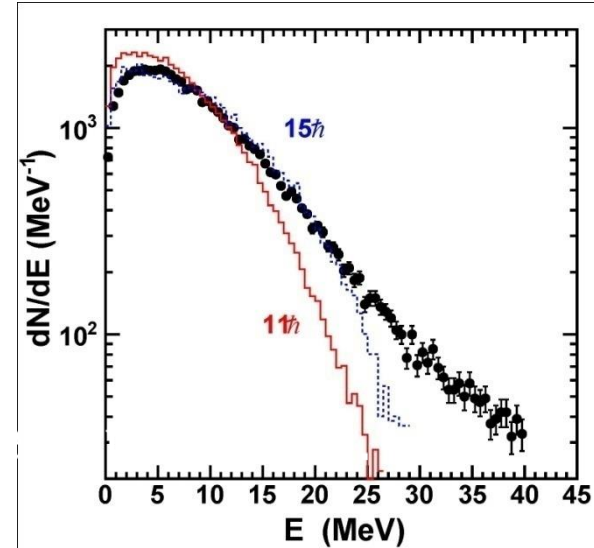
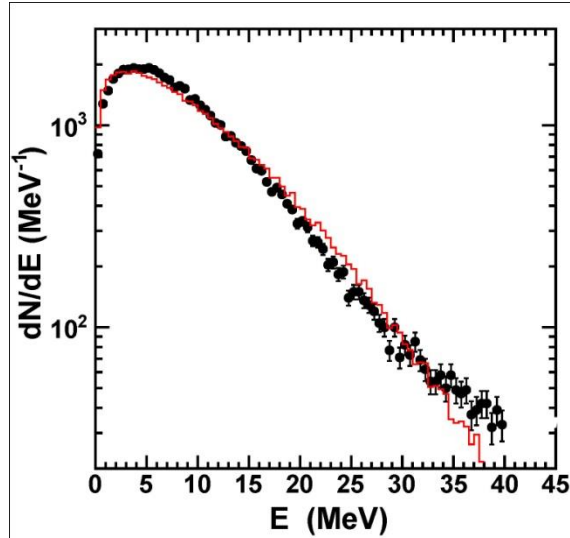
Similar calculated energy spectra are obtained with simulations containing an intermediate freeze-out volume step where  $\alpha$  are formed and then propagated in their mutual Coulomb field => density information

# Na systems ( $^{16}\text{O}^*$ , $^{24}\text{Mg}^*$ ) - energy spectra

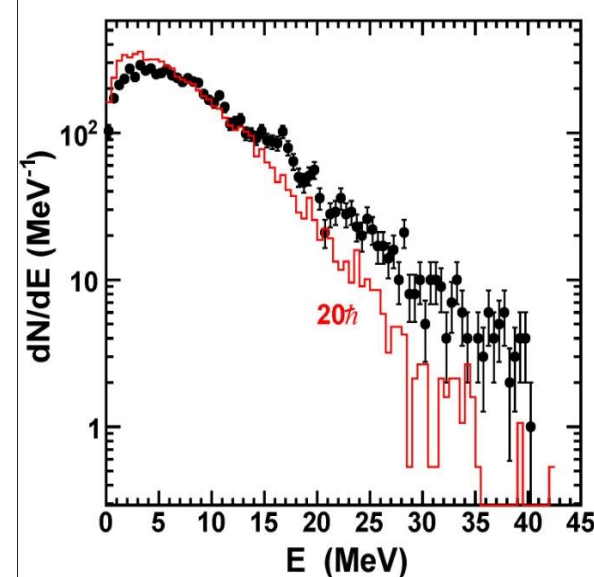
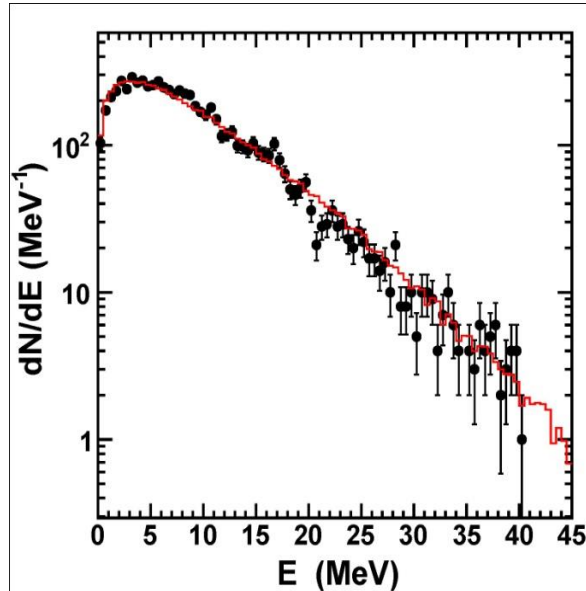
## Simultaneous emission

## GEMINI

Na=4  
 $^{16}\text{O}^* \rightarrow 4\alpha$



Na=6  
 $^{24}\text{Mg}^* \rightarrow 6\alpha$



# T and density from energy spectra

**Information** deduced from Maxwellian fit with volume/breakup pre-exponential factor

A. Goldhaber, PRC 17,2243 (1978)

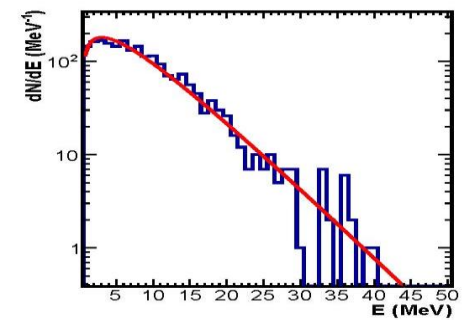
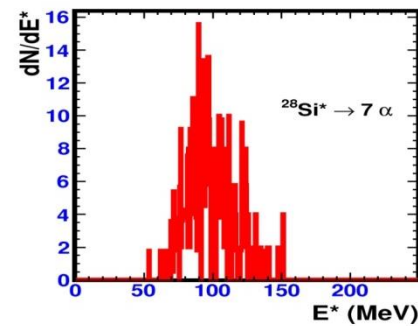
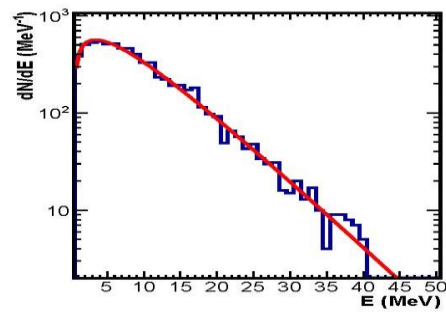
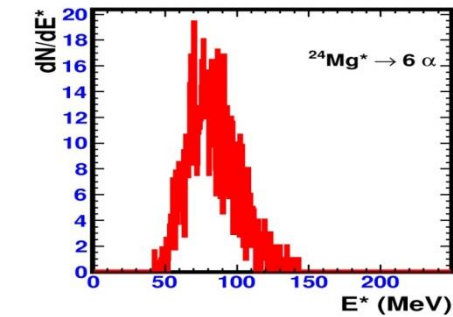
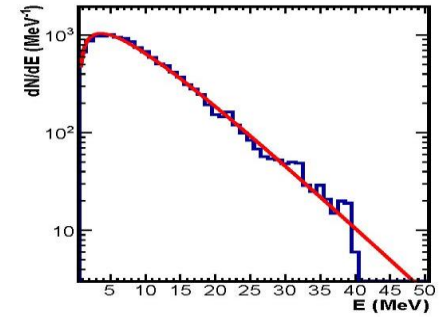
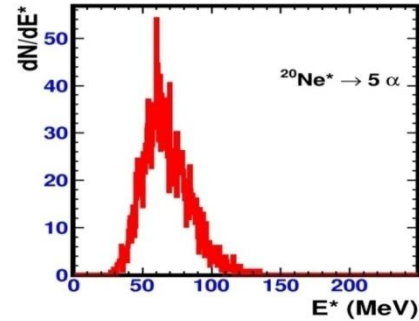
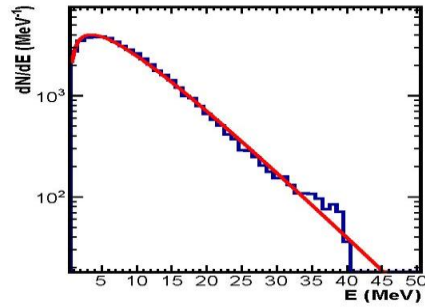
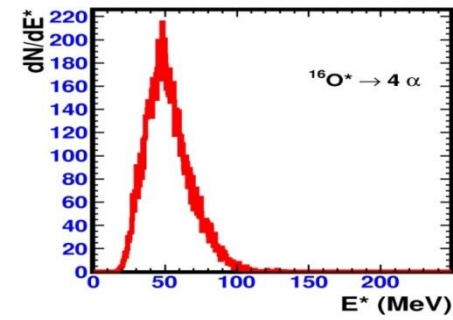
$$\Rightarrow \quad dN/dE = N_0 (E - C_c)^{1/2} \exp[-(E - C_c)/T]$$

Coulomb correction  $C_c$

Most probable value of  $dN/dE = T/2 + C_c$

Comparison with simultaneous simulation with Freeze-Out step to derive F.O. volume values and consequently density

# Excitation energy and Energy spectra



B.B. et al., Symmetry 13, 1562 (2021)

QMBC 2023

# T and density from energy spectra

Na	$\langle E^* \rangle$ (MeV)	T (MeV)	Cc (MeV)	$\rho/\rho_0$
$^{16}\text{O}^*$	52.4	6.15 (0.03)	0.33 (0.03)	0.37 (0.04)
$^{20}\text{Ne}^*$	67.3	6.22 (0.05)	0.45 (0.05)	0.36 (0.04)
$^{24}\text{Mg}^*$	83.5	5.92 (0.07)	0.40 (0.07)	0.34 (0.06)
$^{28}\text{Si}^*$	98.5	5.40 (0.12)	0.37 (0.16)	0.34 (0.11)

$\Rightarrow \langle E^* \rangle \approx 3.3-3.5 \text{ A MeV}$      $T \approx 5.5-6.0 \text{ MeV}$     density  $\approx 1/3 \rho_0$

B.B. et al. Symmetry 13, 1562 (2021)

# Conclusion

The reaction  $^{40}\text{Ca}+^{12}\text{C}$  at 25 MeV/nucleon was used to produce and carefully select specific classes of events from which **excited alpha-conjugate nuclei (Na sources) can be unambiguously identified.**

When compared with simulations (sequential decay and simultaneous decay) **evidence in favour of simultaneous emission (alpha-particle clustering) from expanding alpha-conjugate nuclei is deduced**

**Their  $E^*$  distributions are derived with mean values around 3.5 MeV per nucleon.**

**T around 5.5-6.0 MeV and density around 1/3 saturation density were extracted from energy spectra. Density is in qualitative agreement with self-consistent mean field calculations at zero temperatures.**

**Finite temperature calculations would be welcome for a more valid comparison with the data**



$N_{\alpha}$  sources - excitation energy versus temperature  
from surface/sequential emission

$$dN/dE = N_0 (E - B_c)/T \exp[-(E - B_c)/T]$$

Na	T (MeV)	Bc (MeV)
4	5.18 (0.03)	-1.19 (0.06)
5	5.14 (0.05)	-0.92 (0.11)
6	4.94 (0.07)	-1.05 (0.16)
7	4.57 (0.11)	-1.12 (0.30)

$B_c$  is negative => no physical meaning

# Multi-particle correlation function

R. Charity et al., PRC 52 (1995) 3126

to identify and select nuclei/excited states

N alphas => determination of the alpha emitter  
reference frame =>  $E_{\text{tot}} = \sum E_k^i$

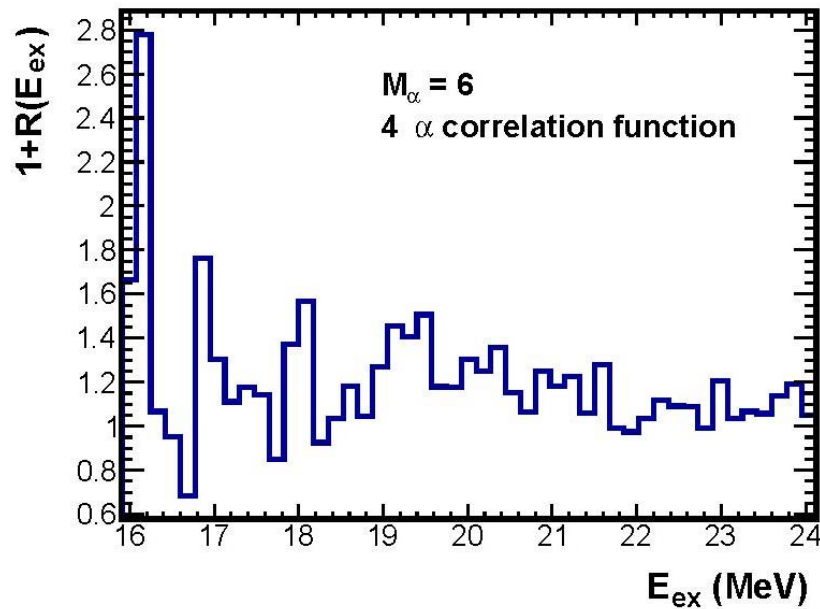
Correlation function:

$$1 + R(E_{\text{tot}}) = Y_{\text{corr}}(E_{\text{tot}}) / Y_{\text{uncorr}}(E_{\text{tot}})$$

$Y_{\text{uncorr}}(E_{\text{tot}})$ : product of single particle yields or mixing particles  
from different events

M. A. Lisa et al., PRC 44 (1991) 2865

% of events removed containing  $^{12}\text{C}^*$ ,  $^{16}\text{O}^*$  and  $^{20}\text{Ne}^*$  fragments which deexcite into  $\alpha$ -particles or Na sources which deexcite via  $^{12}\text{C}^*$ ,  $^{16}\text{O}^*$  and  $^{20}\text{Ne}^*$



Statistically significant peaks are located in the  $E_{ex}$  range 16.7-22.0 MeV

16.84 + 17.20, 17.72 + 18.09, 19.26 + 19.54, 20.05 + 20.41, 21.05 and 21.65 MeV (0+ to 6+)  
Known as 100% alpha emitters

multi-particle CF: for events « participating » to an unbound state a percentage is kept (from 1 to 95%) which corresponds to CF background under the peak  $1 - [(CF-1)/CF] = (1/CF)$

$M_{\alpha}$	% supp. evts	final N of selected evts
4	1.6 (0.1)	12780
5	3.1 (0.3)	2623
6	3.6 (0.5)	1129
7	3.9 (1.1)	291

# Constrained Hartree-Fock-Bogoliubov approach

## $^{16}\text{O}$ , $^{20}\text{Ne}$ ...

When  $A$  increases no more potential well at low density

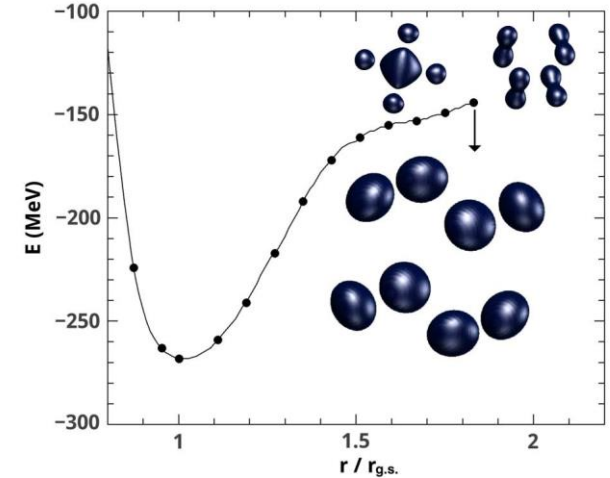
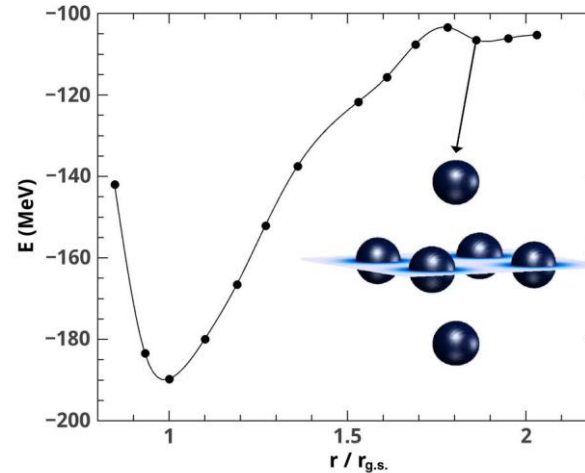
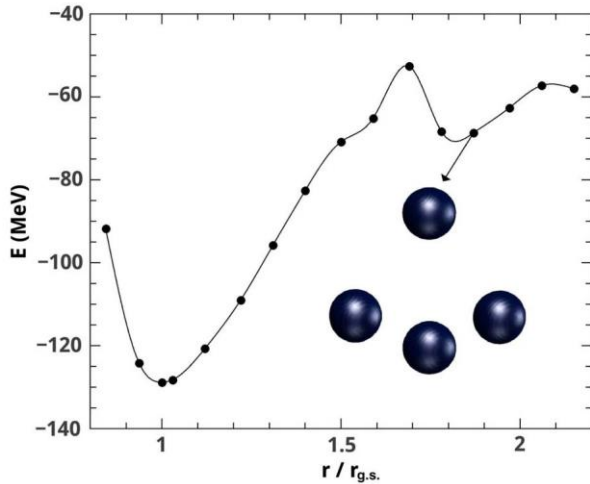


FIG. 1 (color online). Total energy of  $^{16}\text{O}$  as a function of the radius scaled with respect to the one of the ground state  $r_{g.s.}$ . At  $r/r_{g.s.} = \sim 1.8$ , we see that a tetrahedron of four  $\alpha$  particles is formed. No c.m. correction for individual  $\alpha$ 's is applied here. The arrow indicates to which  $r/r_{g.s.}$  value the  $\alpha$  configuration corresponds.

FIG. 2 (color online). Same as Fig. 1 but for  $^{24}\text{Mg}$  with six  $\alpha$ 's. The shaded area only serves to show the three dimensionality of the  $\alpha$  arrangement.

FIG. 3 (color online). Same as Fig. 1 but for  $^{32}\text{S}$  with eight  $\alpha$ 's. Also, configurations with four  $^8\text{Be}$  and a  $^{16}\text{O}$  surrounded by four  $\alpha$ 's are shown.

M. Girod and P. Schuck, PRL 111 (2013) 132503

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# Quality of energy calibration ?

## Two-alpha correlation function

${}^8\text{Be}$

$E_{\text{tot}} = 92 \text{ keV}$  ( $\Gamma = 5.6 \text{ eV}$ )

Exp: 78 keV

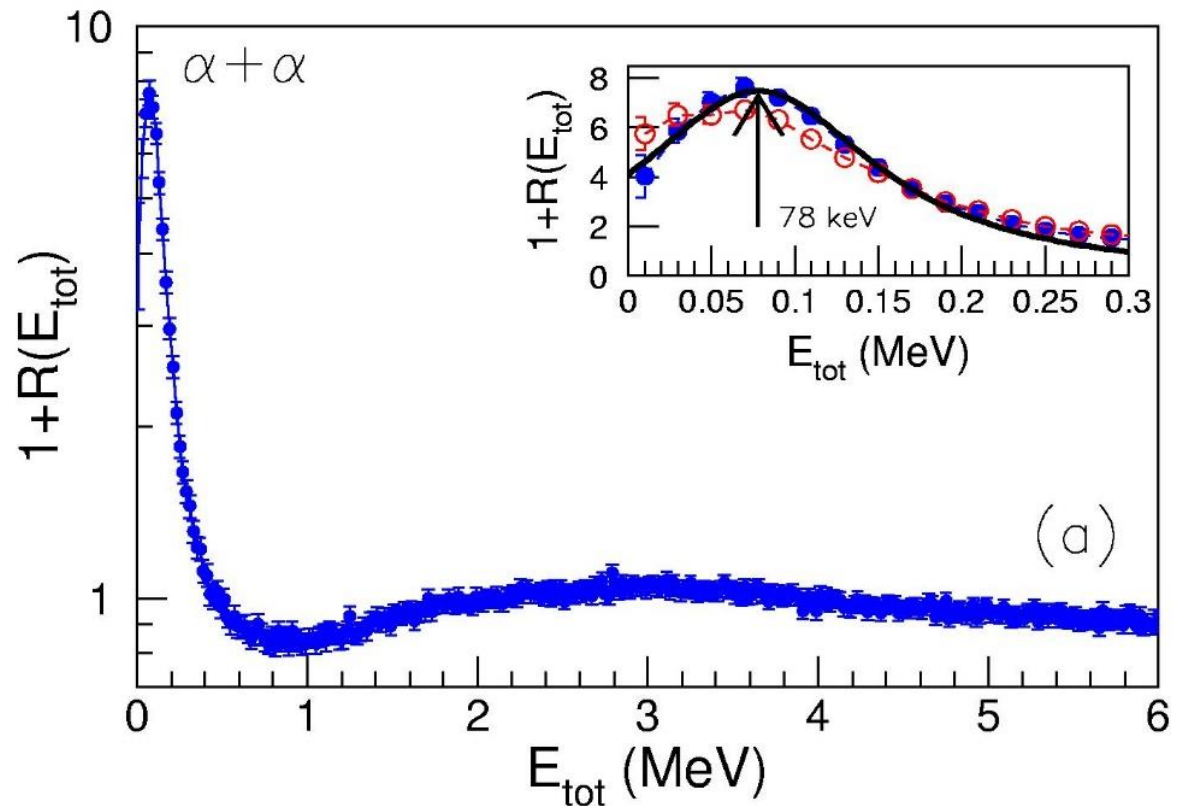
Angle under which particle is emitted (finite granularity)

Dir. of velocity vector:

geometrical center of the module

random angle in the geometrical extension of the module

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# Quality of energy calibration ?

## d-alpha correlations

$${}^6\text{Li}^*$$
$$E_{\text{ex}} = E_{\text{tot}} - Q$$
$$E_{\text{ex}} = 2.186 \text{ MeV}$$

Exp: 2.21 MeV

