

# Fission properties of $r$ -process nuclei predicted with the BCPM EDF

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Conference on Quantum-Many-Body Correlations  
In memory of Peter Schuck

21 – 23 March, 2023

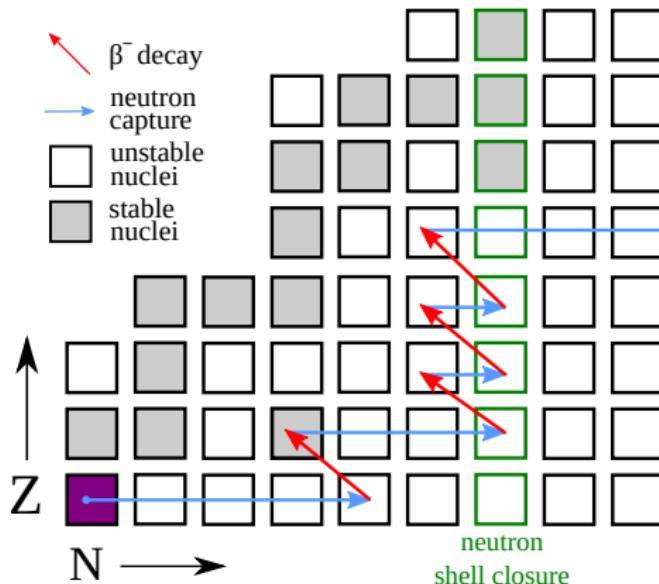
IJCLab, Orsay (FR)



# The $r$ process

B<sup>2</sup>FH, Rev. Mod. Phys. 29, 547 (1957) ; A. Cameron, Report CRL-41 (1957)

$r$ (apid neutron capture) process:  $\tau_{(n,\gamma)} \ll \tau_{\beta^-}$

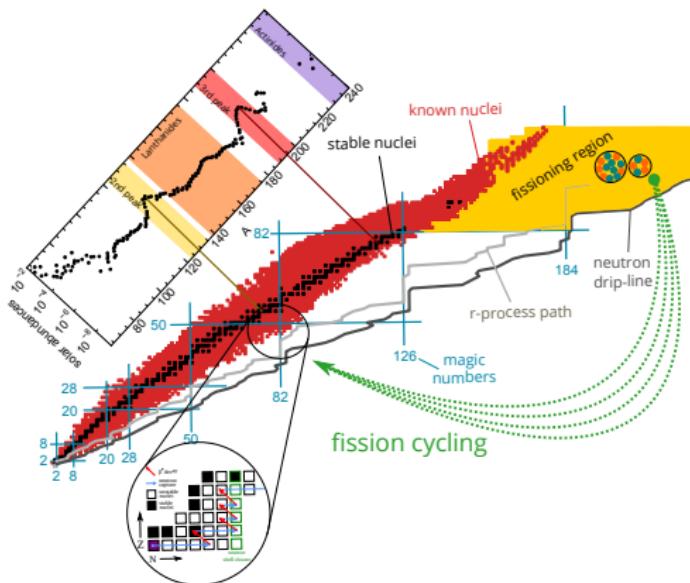


- The **neutron-to-seed ratio** determine how far the  $r$ -process can proceed.
- Astrophysical site with **high neutron fluxes** (e.g., **neutron star mergers**).

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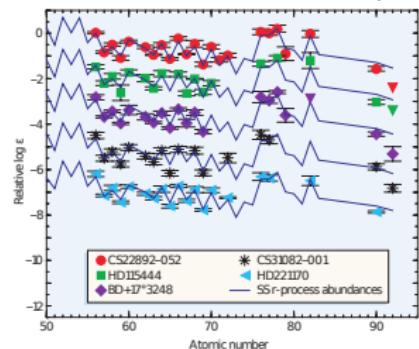
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# Fission and $r$ process

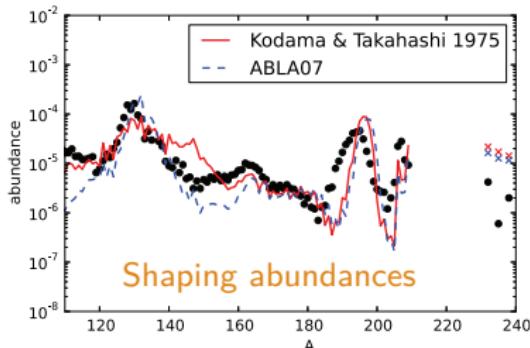
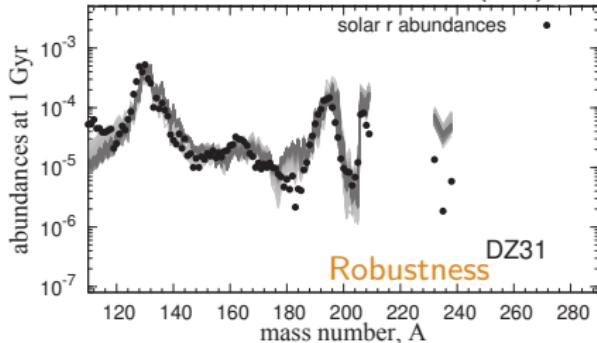
Thielemann+(1983), Panov+(2005), Martinez-Pinedo+(2007), Beun+(2008), ...

Petermann+(2012), Eichler+(2015), Goriely(2015), Mumpower+(2018), Zhu+(2019), Wu+2019, Vassh+(2019), ...

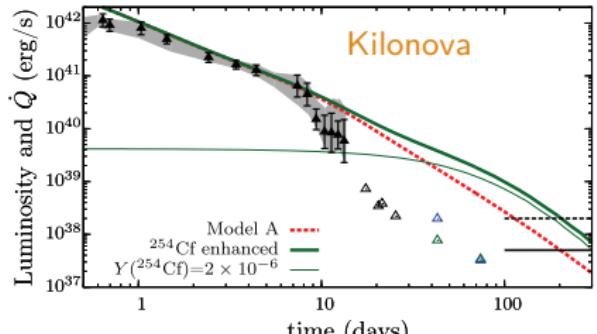
Cowan and Sneden, Nature 440 1151 (2006)



J. Mendoza-Temis *et al.*, PRC 95, 055805 (2015)

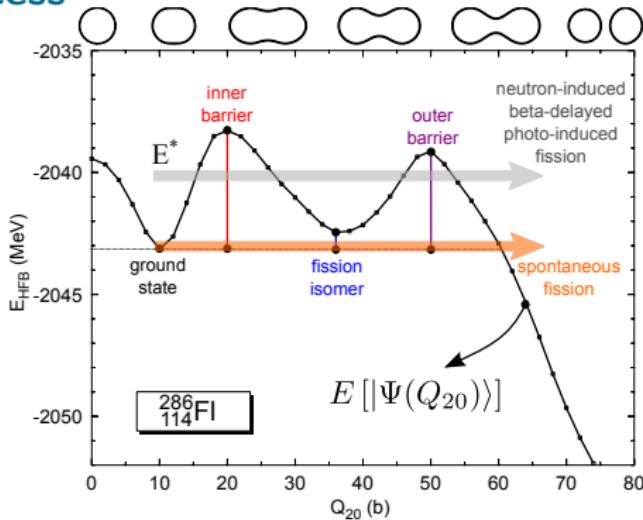


M. Eichler *et al.*, Astrophys. J. 808, 30 (2015)



M.-R. Wu *et al.*, Phys. Rev. Lett. 122, 062701 (2019).

# The fission process



## Potential Energy Surface $\mathcal{V}$

Energy evolution from the initial state to the scission point.

## Collective inertias $\mathcal{M}$

Resistance of the nucleus against the deformation forces.

$$P_{\text{fiss}} = \left(1 + \exp(-2S[L])\right)^{-1} \rightarrow S[L(Q_{20})] = \int_a^b dQ_{20} \sqrt{\mathcal{M}(Q_{20})[\mathcal{V}(Q_{20}) - E_0]}$$

## The Hartree-Fock-Bogolyubov (HFB) formalism

The ground-state wavefunction is obtained by minimizing the total energy:

$$\delta E[|\Psi\rangle] = 0 \quad \text{with} \quad |\Psi\rangle = \prod_{\mu} \beta_{\mu} |0\rangle \Rightarrow \beta_{\mu} |\Psi\rangle = 0 \quad \forall \mu.$$

The energy landscape is constructed by constraining the deformation of the nucleus  $\langle \Psi(q) | \hat{Q} | \Psi(q) \rangle = q$ :

$$E[|\Psi(q)\rangle] = \langle \Psi(q) | \hat{\mathcal{H}} - \lambda_q \hat{Q} | \Psi(q) \rangle.$$

To assess the systematic uncertainties on theoretical fission properties, 4 different EDFs are employed:

- Barcelona-Catania-Paris-Madrid (**BCPM**) Baldo, Robledo, **Schuck**, Viñas PRC(2013).

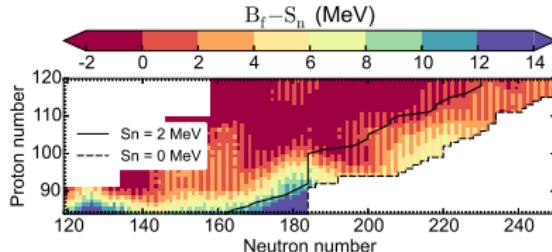
$$E = T_0 + E_{int}^{\infty} + E_{int}^{FR} + E^{s.o.} + E_C + E_{pair};$$

$$E_{int}^{\infty}[\rho_p, \rho_n] = \int d\vec{r} [P_s(\rho)(1 - \beta^2) + P_n(\rho)\beta^2] \rho,$$

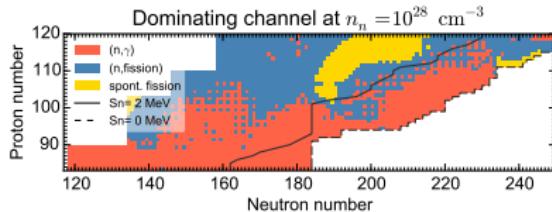
with  $P_s$  and  $P_n$  polynomial fits of microscopic EoS in nuclear matter.

- D1S, D1N, and D1M **Gogny parametrizations**.

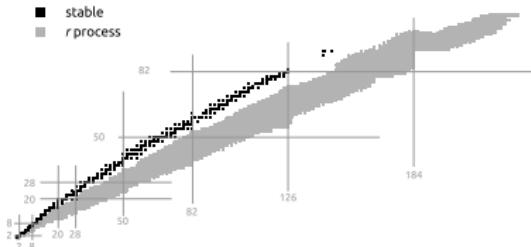
- 1) Compute fission properties and binding energies using EDF.



- 2) Calculate stellar reaction rates from Hauser-Feshbach theory.

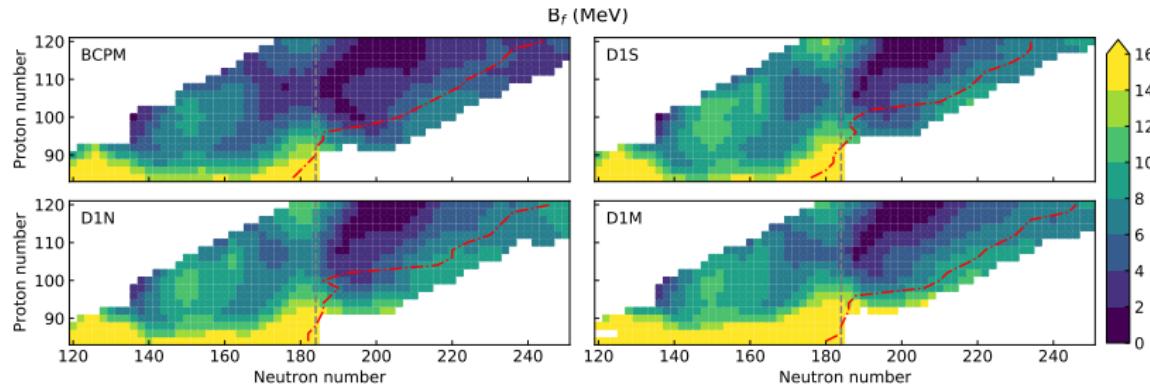


- 3) Obtain  $r$ -process abundances using network calculations.



## Systematic of fission barriers $B_f$

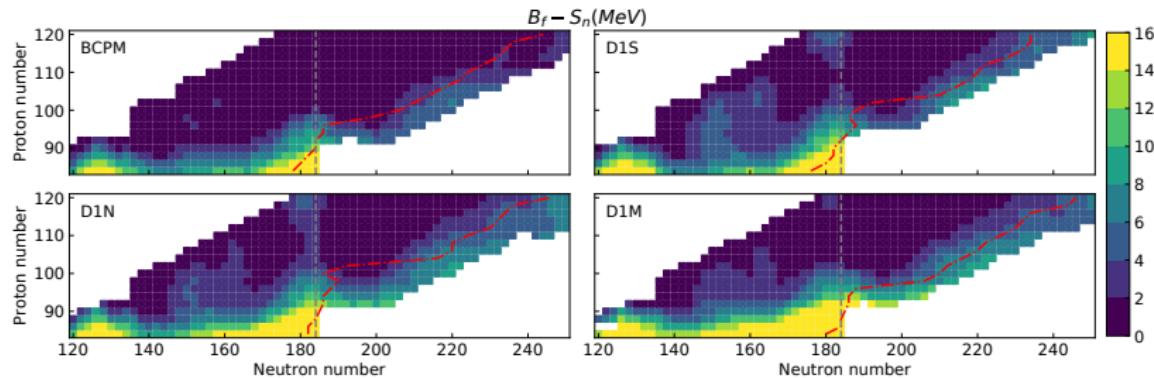
- $B_f \rightarrow$  stability against fission.



- $B_f$  trends qualitatively similar across different D1 interactions:
  - $Z > 94$ : systematic deviations  $\sim 1\text{--}2$  MeV  $\rightarrow m^*/m \sim 0.7 - 0.75$ .
  - $Z \leq 94$ : deviations up to 10 MeV (but very high  $B_f$ ).
- BCMP  $B_f$  up to 5 MeV smaller for  $Z > 94$  ( $m^*/m = 1$ ).
- Location of the  $r$  process differ above  $N = 184$ .

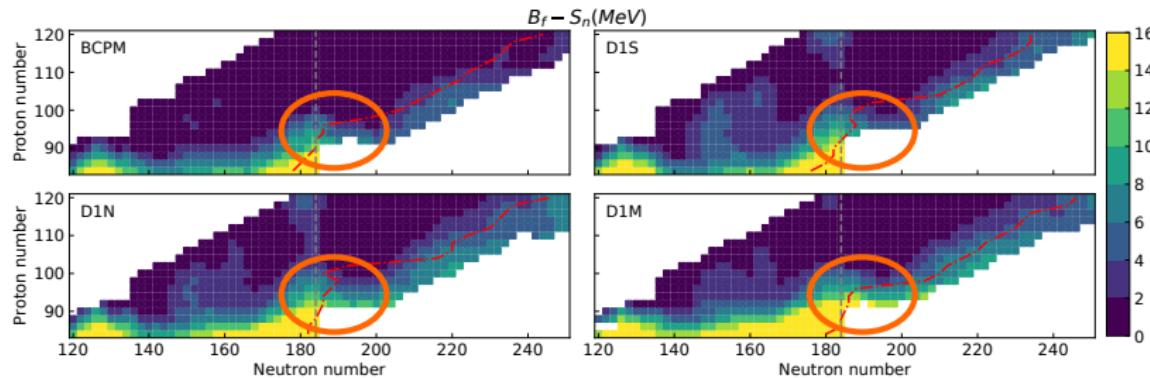
## Systematic of $B_f - S_n$

- For  $B_f - S_n \lesssim 2$  MeV ( $n, \text{fis}$ ) dominates over ( $n, \gamma$ ).



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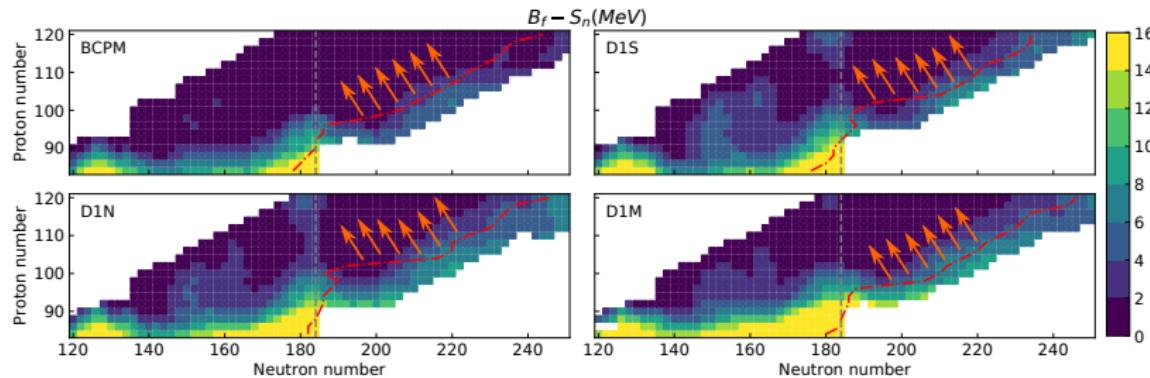
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- Production of (super)heavy nuclei requires the **overcoming of neutron shell closure** at  $N = 184$ .
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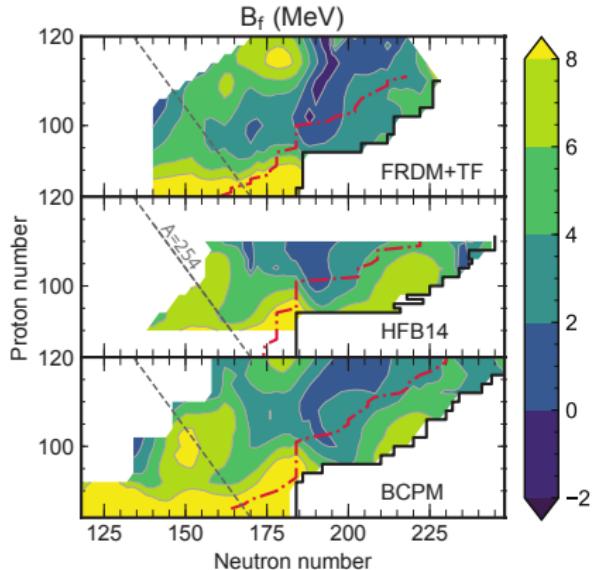


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- Production of superheavy nuclei more favored with D1M ( $r$ -process path proceeds towards lower  $Z$ ).
- Path towards stability interrupted by region of low fission barriers.

# Impact of fission on the $r$ -process

SAG *et al.*, Phys. Rev. C 102, 045804 (2020)

- **Dynamical ejecta:**  $Y_e \lesssim 0.05$ ;  $n/s \approx 600$
- **Accretion disk:**  $Y_e \lesssim 0.15$ ;  $n/s \approx 120$

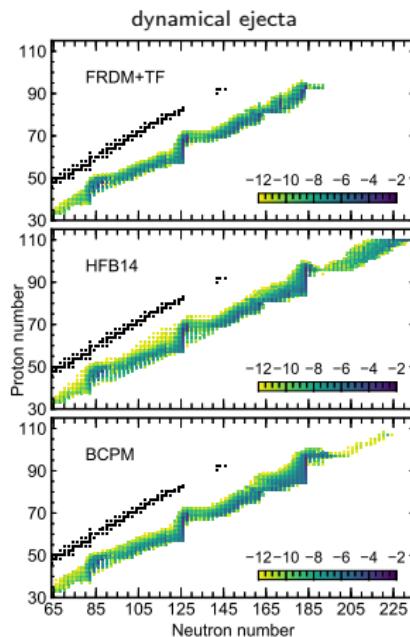
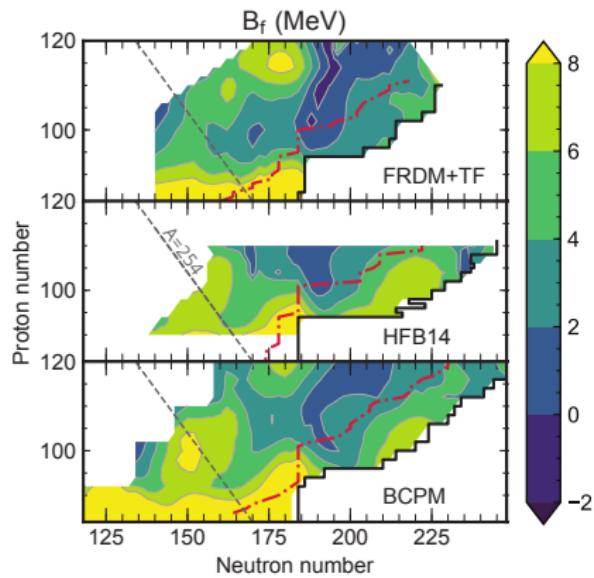


**BCPM:** Giuliani *et al.* (2018); **FRDM+TF:** Panov *et al.* (2010); **HFB14:** Goriely *et al.* (2009).

# Impact of fission on the $\gamma$ -process

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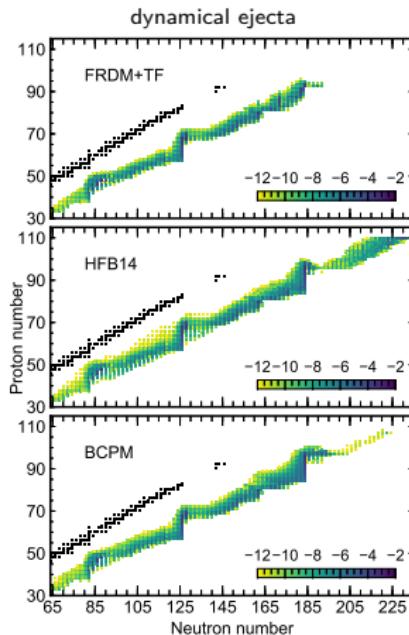
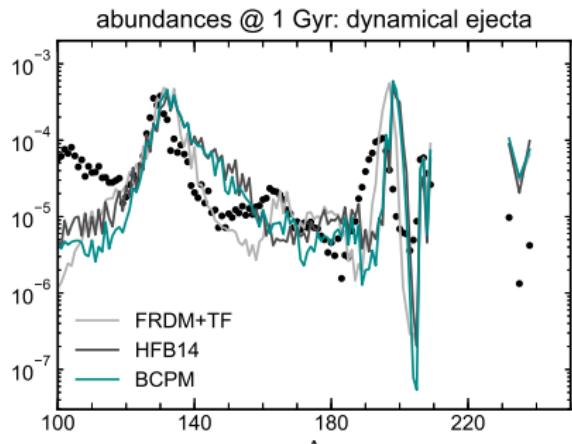


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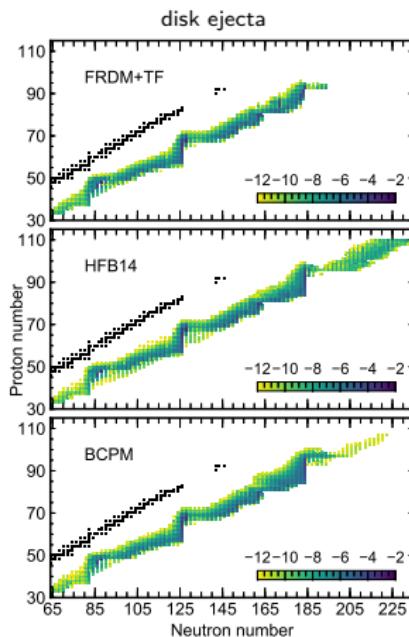
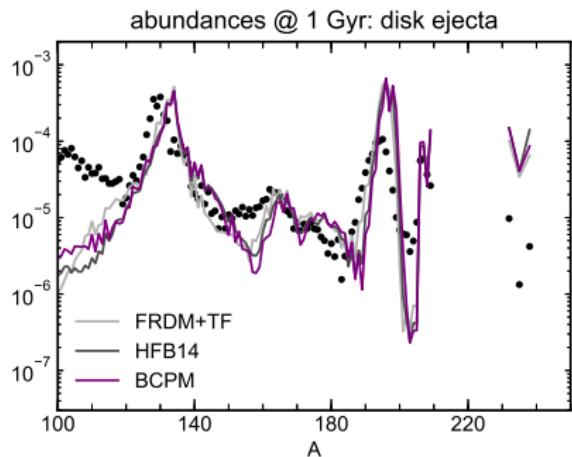


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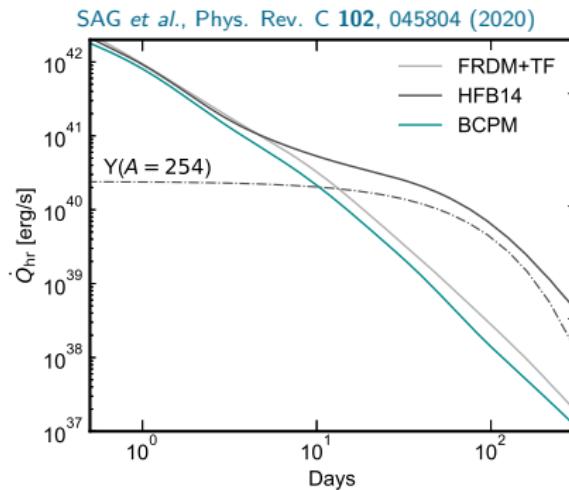


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## Kilonova: BCPM vs FRDM+TF vs HFB14

**Kilonova:** EM transient produced by the decay of  $r$ -process nuclei.

- HFB14:
  - Large accumulation of  $^{254}\text{Cf}$  due to high fission barriers.
- FRDM+TF:
  - $^{254}\text{Cf}$  progenitors destroyed by  $\beta$ -delayed fission.
- BCPM:
  - $^{254}\text{Cf}$  progenitors destroyed by neutrons from fission.

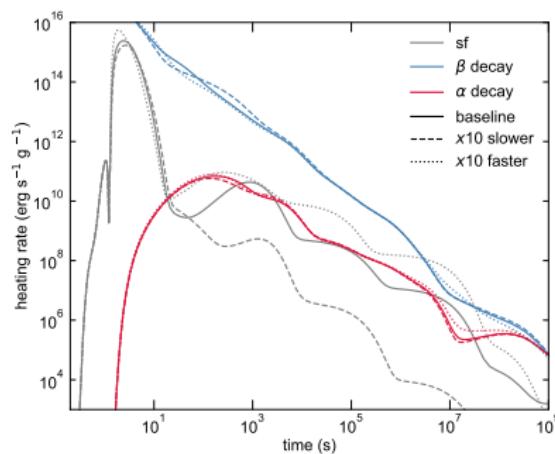
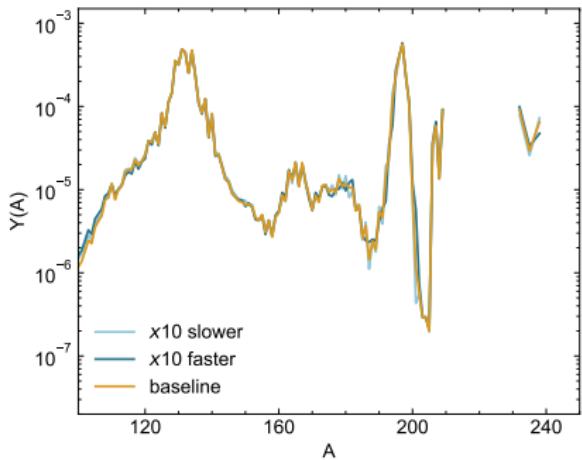


Kilonova light curves sensitive to nuclear properties at  
 $N = 184$  and  $A = 254$

$(n, \gamma)$  vs  $(n, fis)$   
 $\beta$ -delayed and spontaneous fission rates

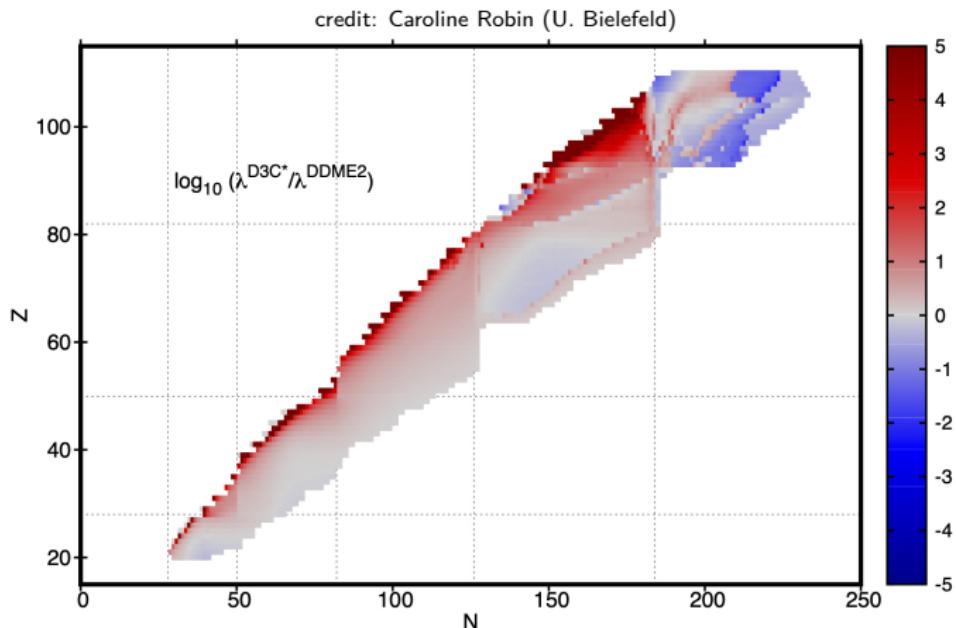
## Impact of $\beta$ -decay rates on fission

- Impact of  $\beta$ -decay half-lives varies with the observable.
- We modified  $t_{1/2}^\beta \geq 3$  s and study the impact on abundances and heating rates.



Fission heating rate sensitive to “slow”  $\beta$ -decay rates  
( $\tau_\beta \gtrsim$  few seconds)

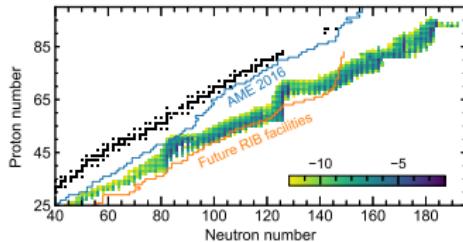
## Systematic of $\beta$ -decay rates



- $\beta$ -decay rates closer to stability show larger uncertainties → more systematic studies are required (see also E. M. Ney *et al.*, Phys. Rev. C **102**, 034326 (2020)).

## Conclusions

- For neutron-rich ejecta, fission plays a crucial role during  $r$ -process.
- Global calculations of neutron-rich nuclei show **large variations** in the predicted fission properties → (consistent) sensitivity studies are required.
- $r$ -process abundances and kilonova light curve are strongly affected by **fission properties** at  $N = 184$  → KN window to exotic region?



- Heating rates sensitive to competition between **fission** and  $\beta$ -decay at  $t \gtrsim$  s.
- Future work/needs:
  - Sensibility studies exploring the impact of **fission rates** on nucleosynthesis calculations.
  - Systematic studies of  $\beta$ -decays half-lives and strengths crucial for assessing uncertainties.

## Collaborators

MSU & NSCL/FRIB (East Lansing)



E. Flynn  
R. Jain  
D. Lay  
W. Nazarewicz  
L. Neufcourt

GSI & TUD (Darmstadt)



G. Martínez Pinedo

Universität Bielefeld

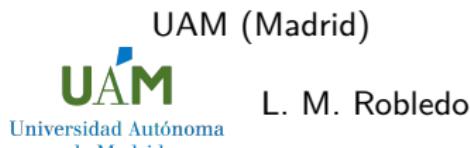


C. Robin

## Funding



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L. M. Robledo

VECC (Kolkata)



J. Sadhukhan

Sinica Institute (Taiwan)

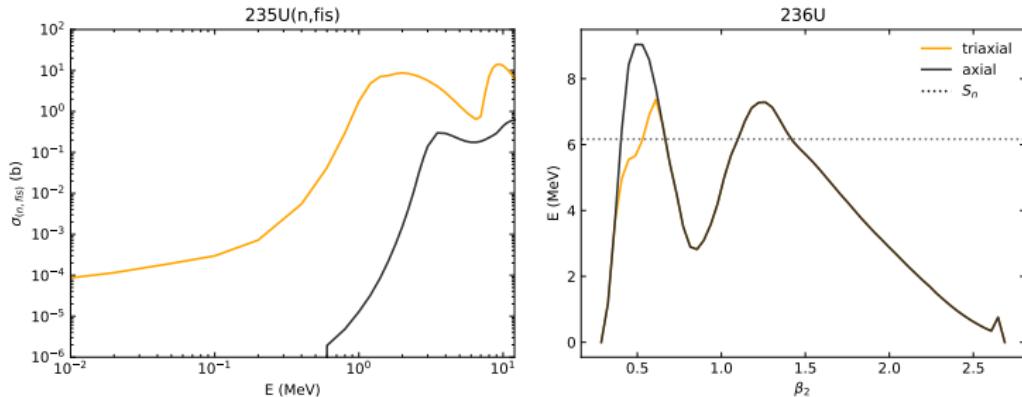


M.-R. Wu

# Backup

## Global calculation of fission nuclear properties

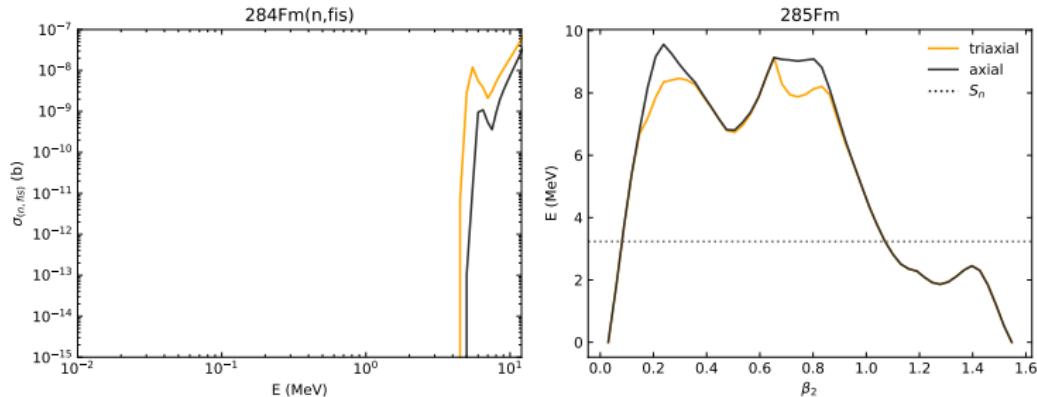
- Model assumptions → systematic uncertainties → impact on nucleosynthesis?
- Relevant physics close to stability ≠ relevant physics in exotic nuclei.



- Systematic deviations close to stability could be compensated in exotic nuclei (and vice versa) → global calculations from different models are required.

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